

# Optimization of dynamic aperture for the ESRF upgrade

Andrea Franchi  
on behalf of the  
ASD Beam Dynamics Group

Workshop on Accelerator R&D for Ultimate Storage Rings  
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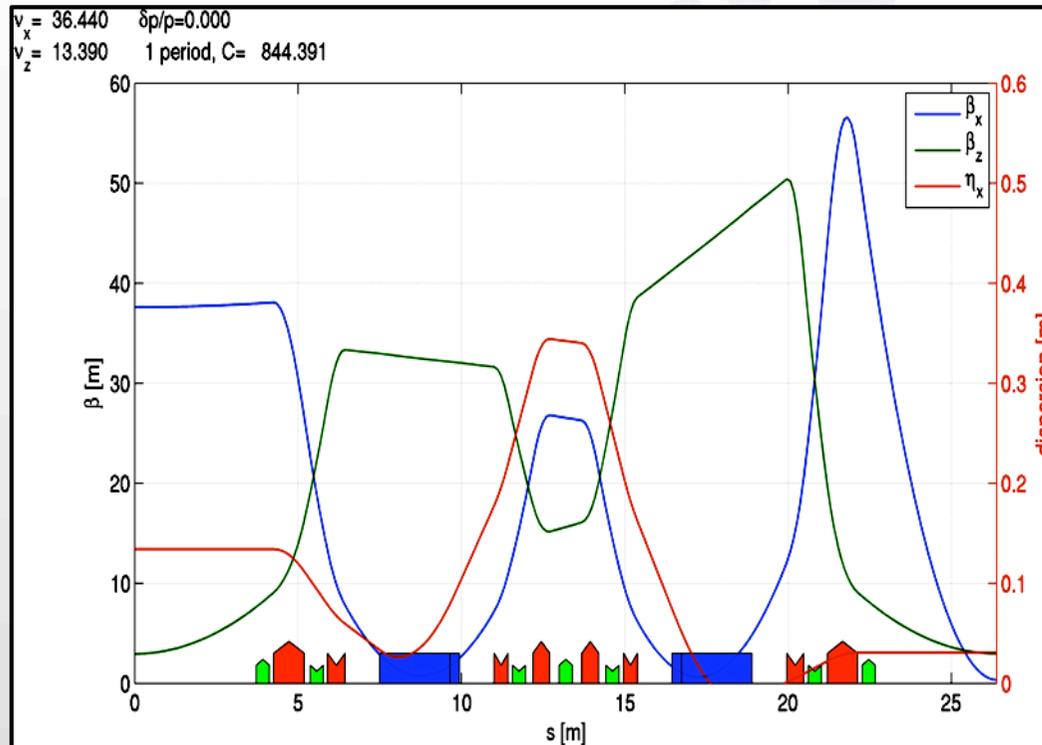
## Outlines

- The Hybrid Multi-Bend (HMB) lattice
- Nonlinear optics: existing ESR SR Vs HMB lattice
- Optimizing dynamic aperture

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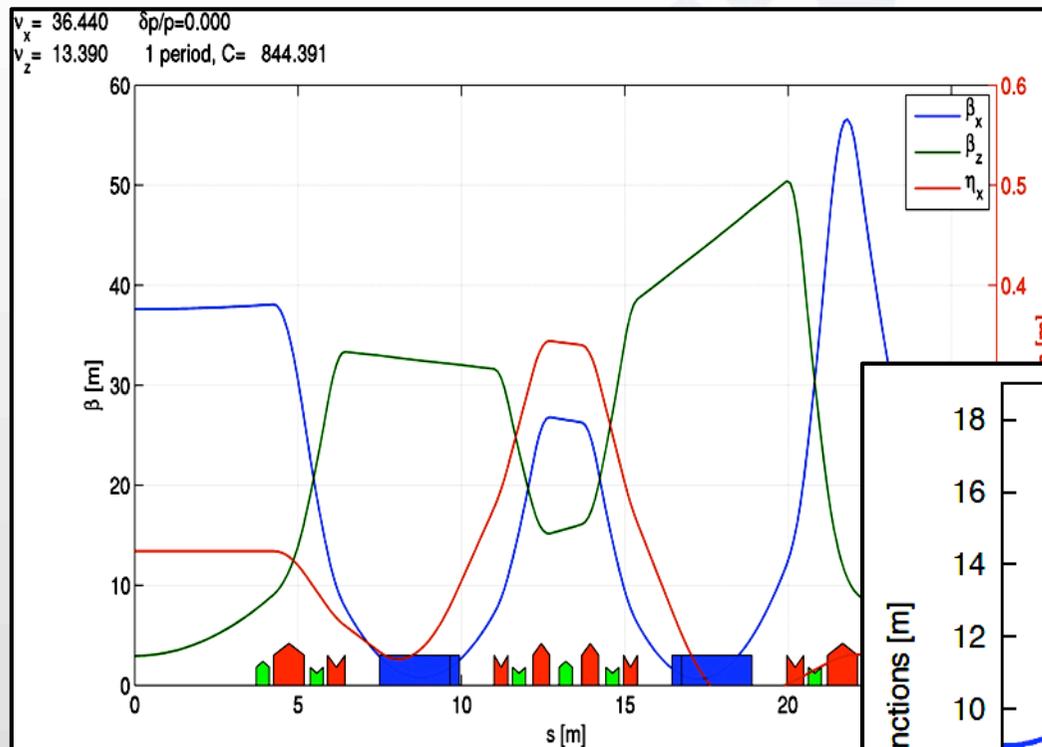
# The Hybrid Multi-Bend (HMB) lattice



## Double-Bend Achromat (DBA)

- Many 3<sup>rd</sup> gen. SR sources
- Local dispersion bump (originally closed) for chromaticity correction

# The Hybrid Multi-Bend (HMB) lattice

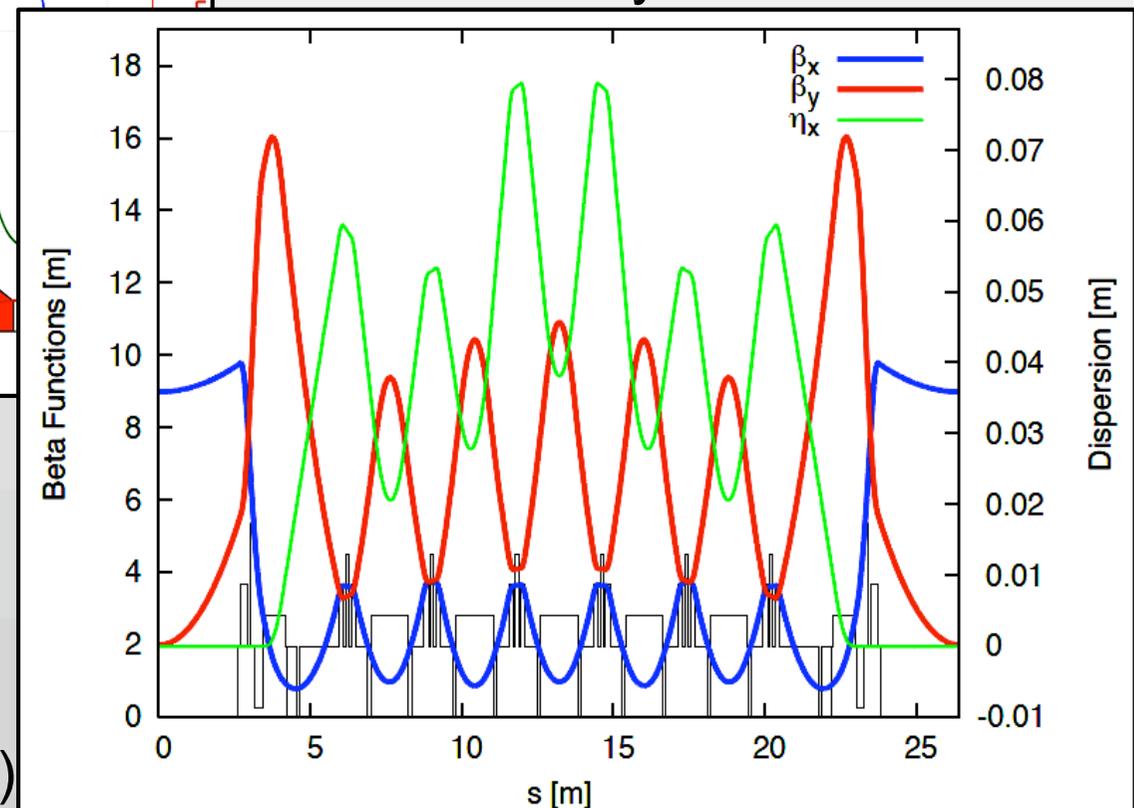


## Double-Bend Achromat (DBA)

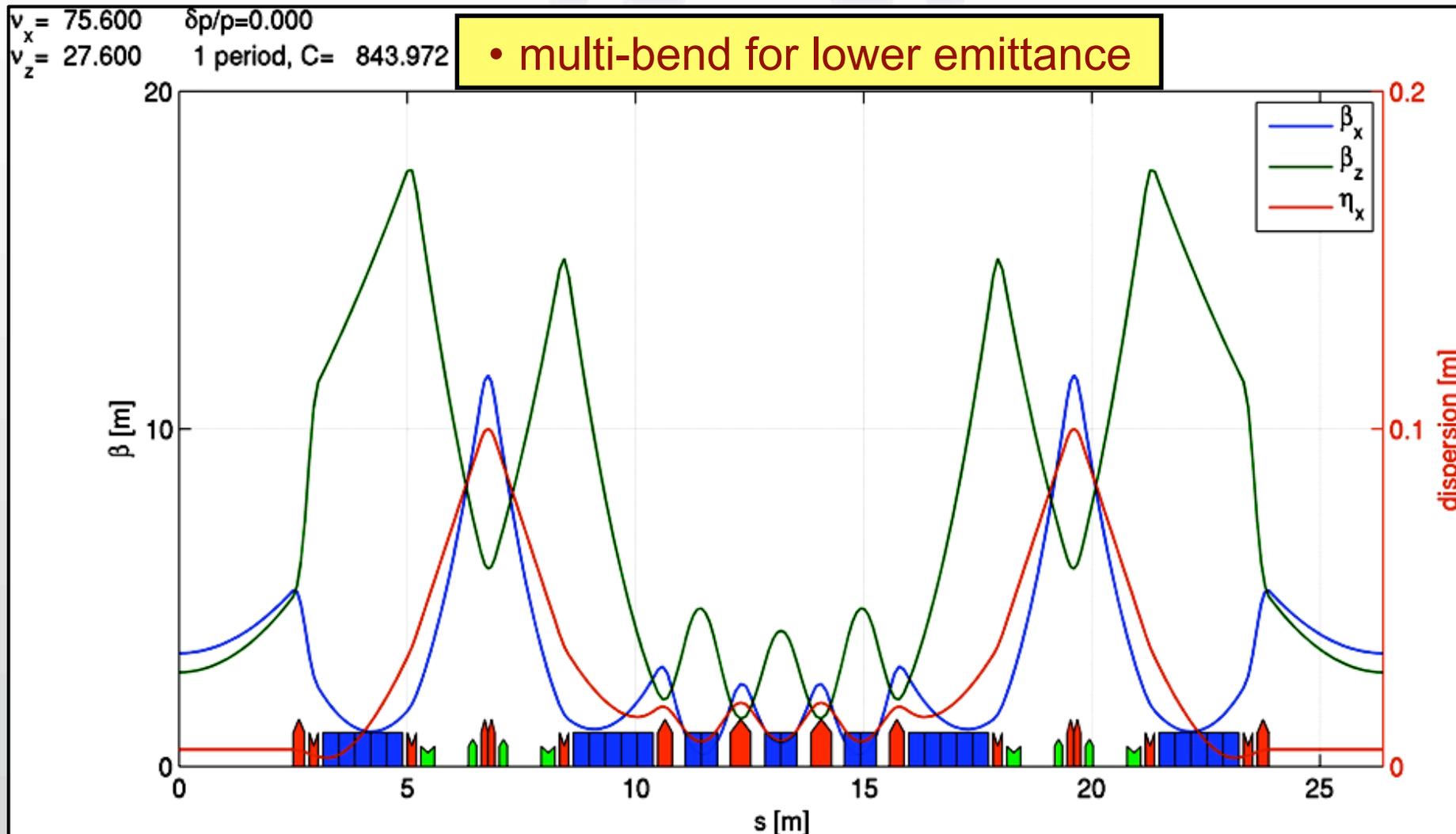
- Many 3<sup>rd</sup> gen. SR sources
- Local dispersion bump (originally closed) for chromaticity correction

## Multi-Bend Achromat (MBA)

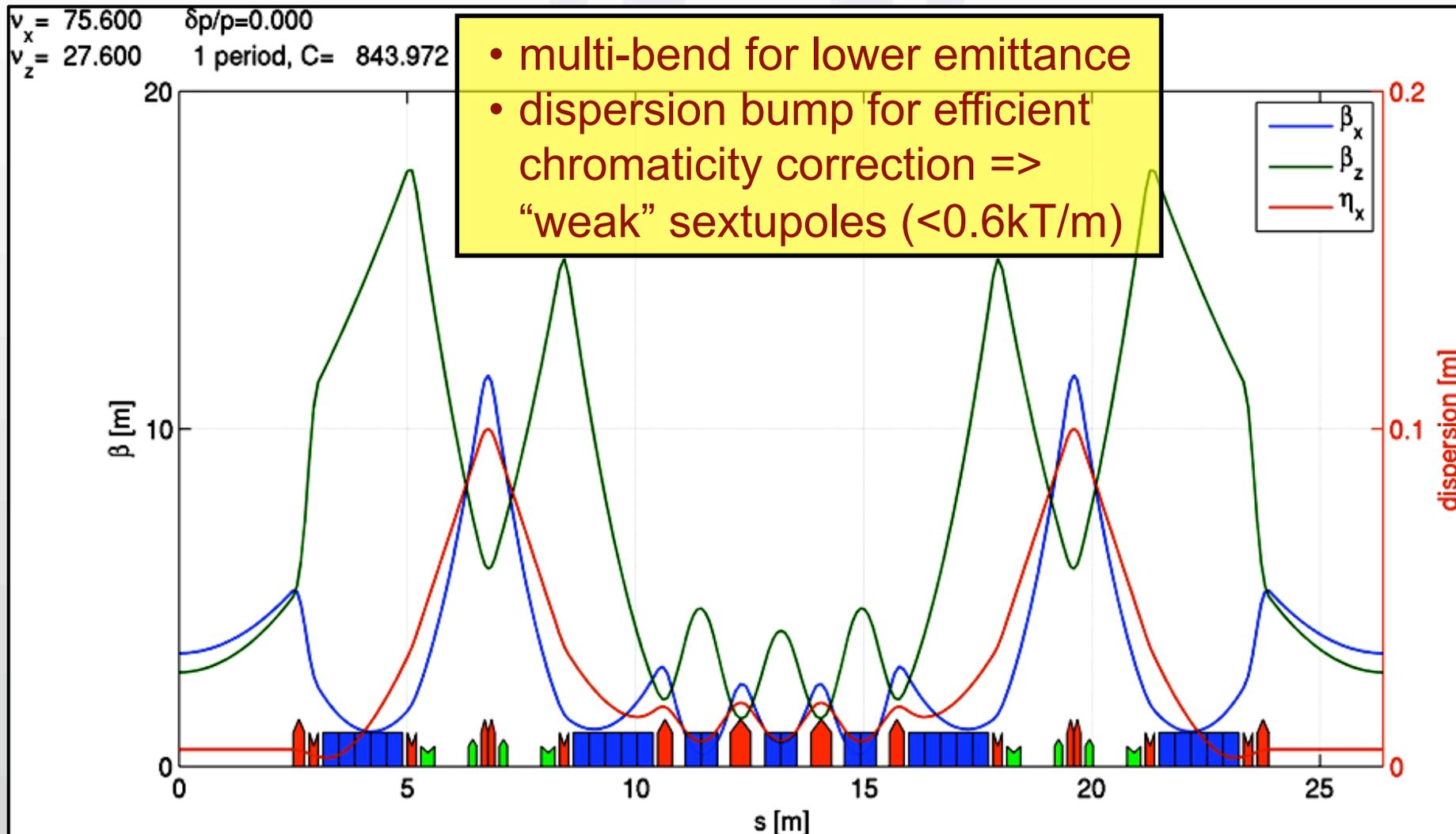
- MAX IV and other USRs
- No dispersion bump, its value is a trade-off between emittance and sextupoles (DA)



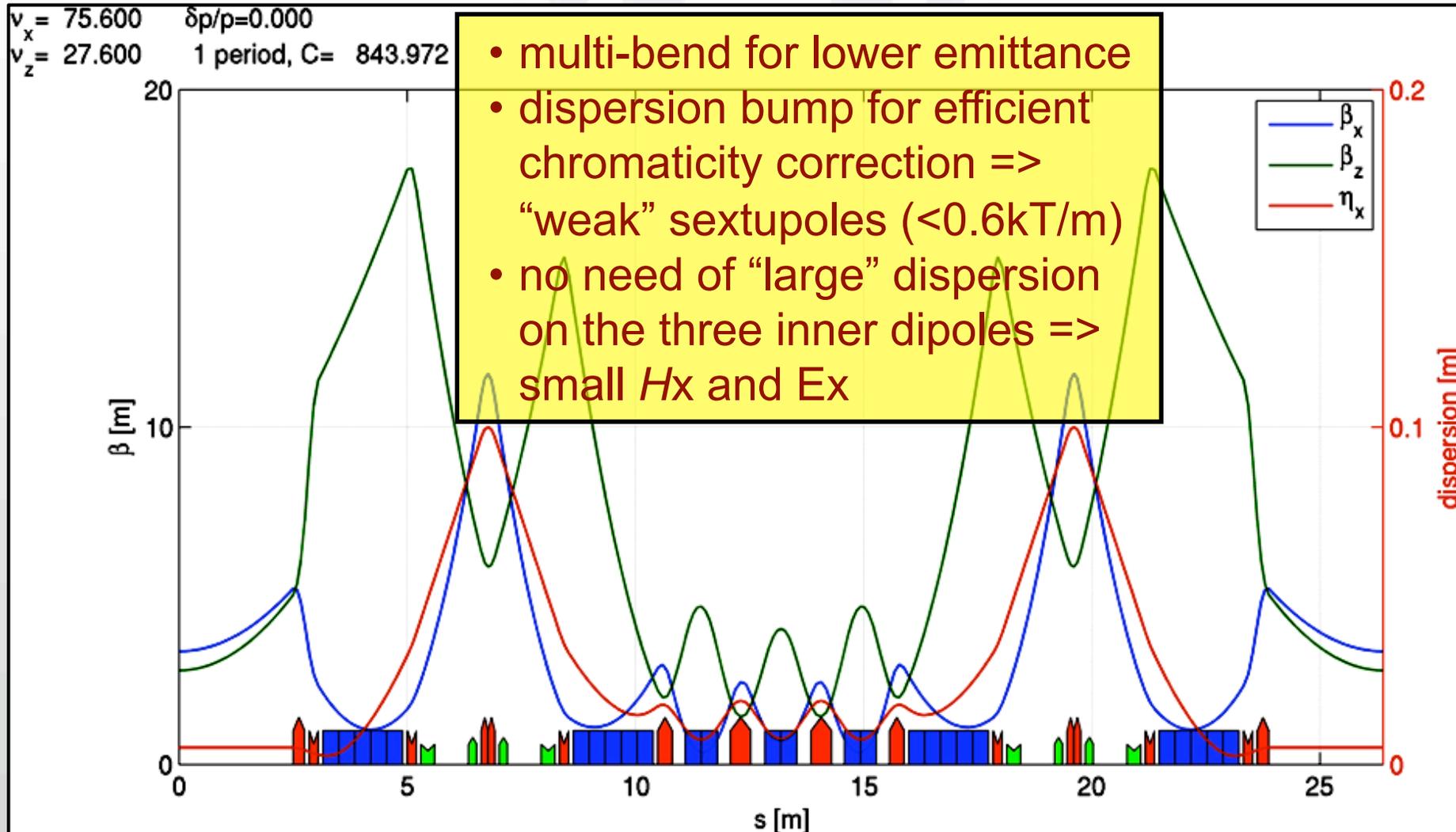
# The Hybrid Multi-Bend (HMB) lattice



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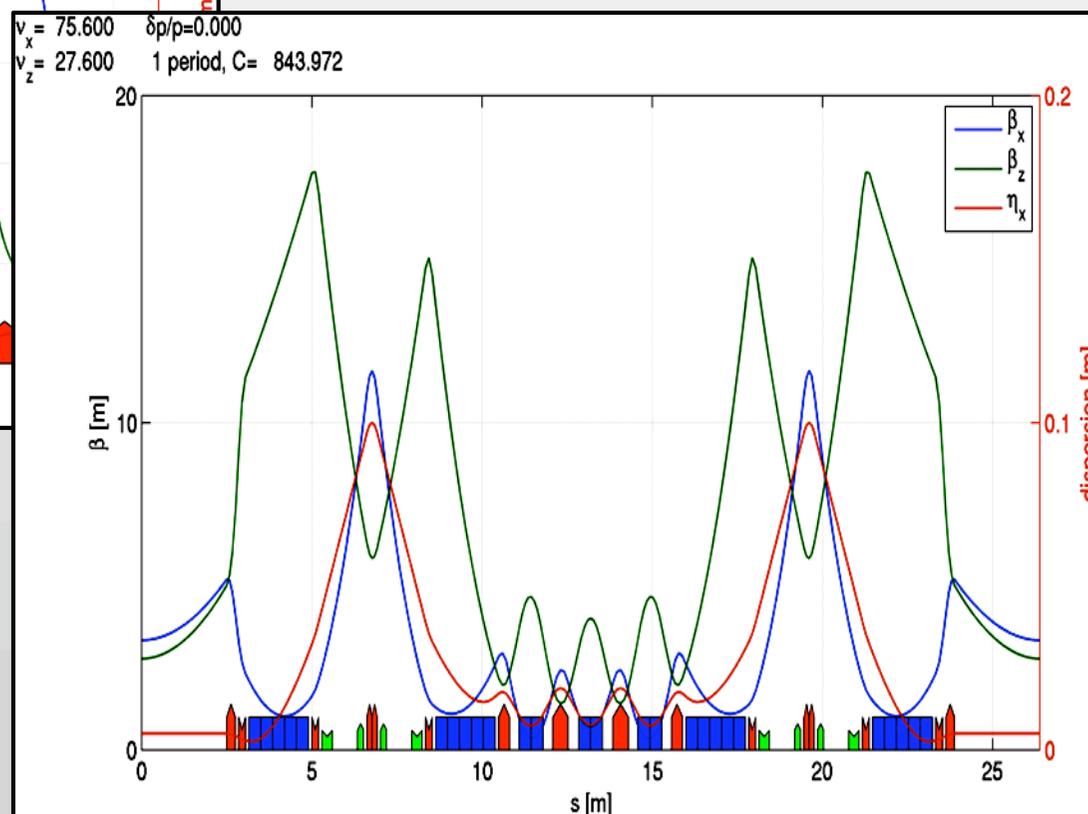
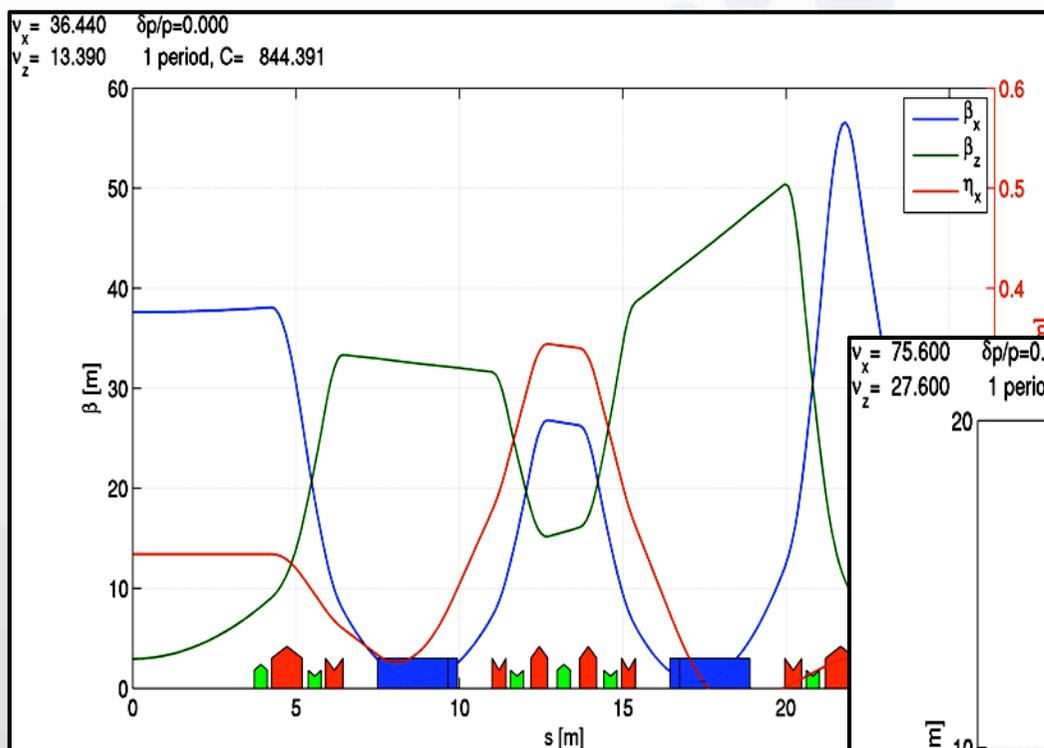
# The Hybrid Multi-Bend (HMB) lattice



# The Hybrid Multi-Bend (HMB) lattice

## ESRF existing (DBA) cell

- $Ex = 4 \text{ nm}\cdot\text{rad}$
- tunes (36.44, 13.39)
- nat. chromaticity (-130, -58)



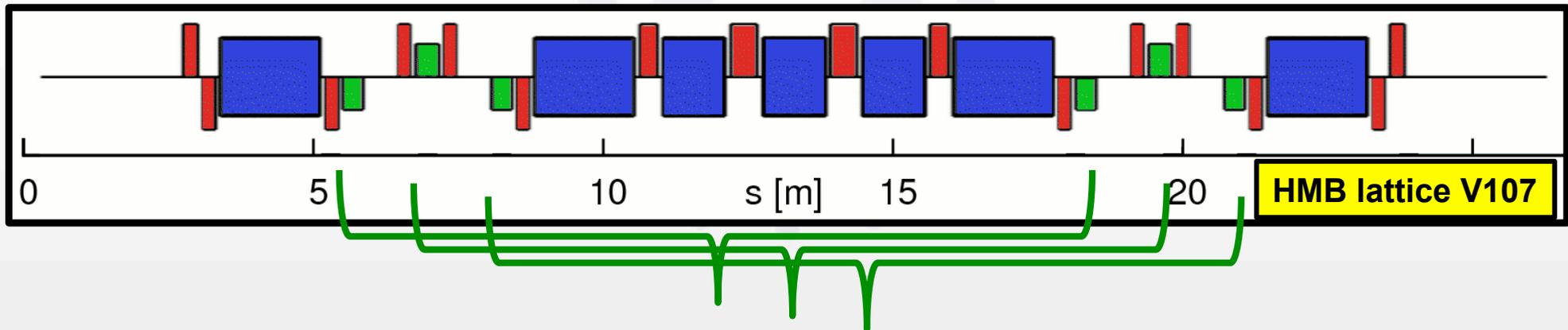
## Proposed HMB cell

- $Ex = 160 \text{ pm}\cdot\text{rad}$
- tunes (75.60, 27.60)
- nat. chromaticity (-97, -79)

## Outlines

- The Hybrid Multi-Bend (HMB) lattice
- **Nonlinear optics: existing ESR SR Vs HMB lattice**
- Optimizing dynamic aperture

# Nonlinear optics: the HMB lattice

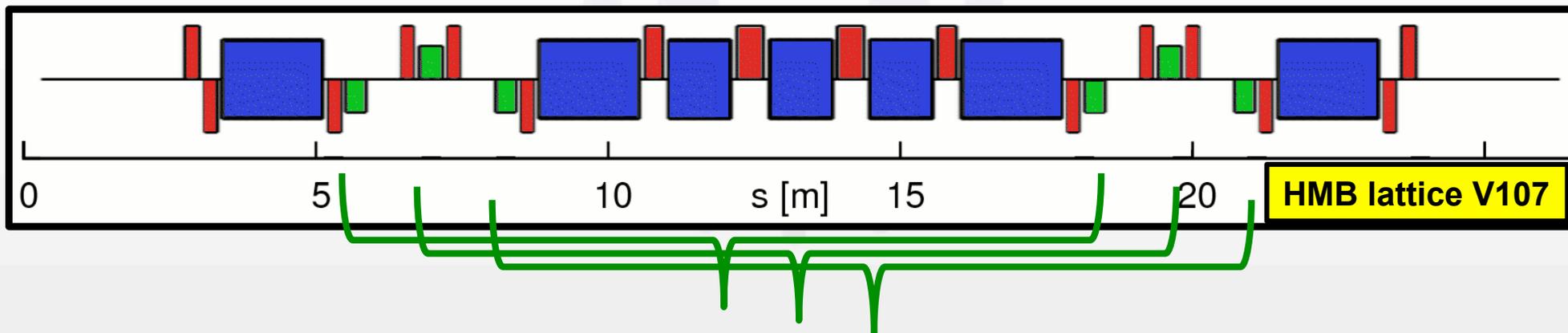


phase advance between pairs of (chrom.) sextupoles:

$$\Delta\varphi_x=(2n+1)\pi \quad \Delta\varphi_y=n\pi$$

$\Delta\varphi_x=(2n+1)\pi$  to minimize at the cell ends the Resonance Driving Terms from  $x^3$  ( $f_{3000}$  and  $f_{1200} \approx 0$ )  $\Rightarrow$  elliptical horizontal phase space

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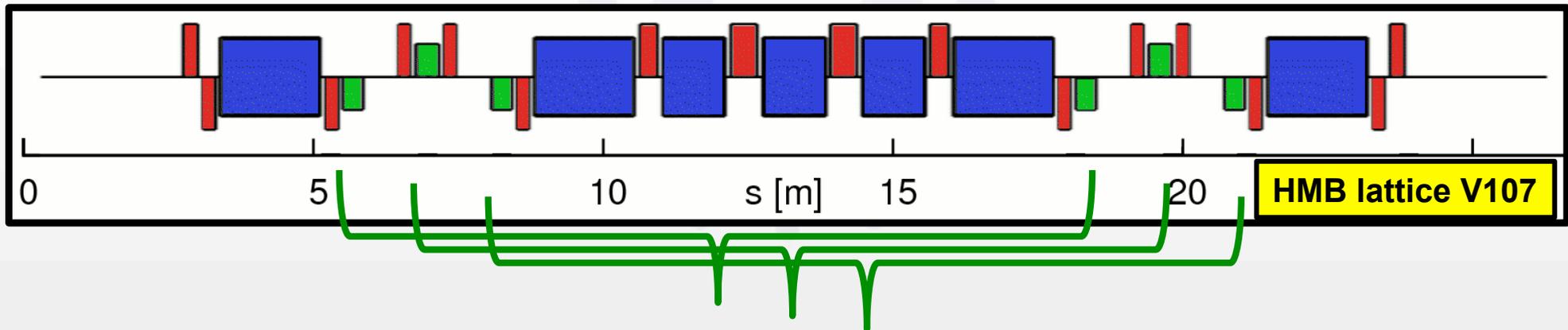
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+

$\Delta\varphi_y = n\pi$  minimize those from  $xy^2$  ( $f_{1020}$  and  $f_{0120} \approx 0$ ) rendering vertical phase space elliptical too [ $f_{0111} \approx 0$  from  $\Delta\varphi_x = \pi$ ] ...

# Nonlinear optics: the HMB lattice



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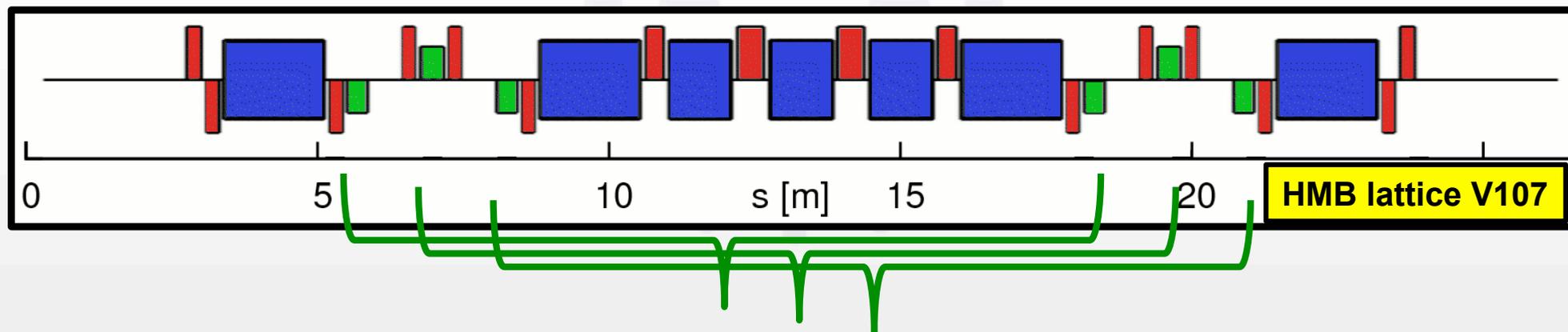
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... provided that second-order (octupolar-like) RDTs are kept low

no harmonic sextupoles

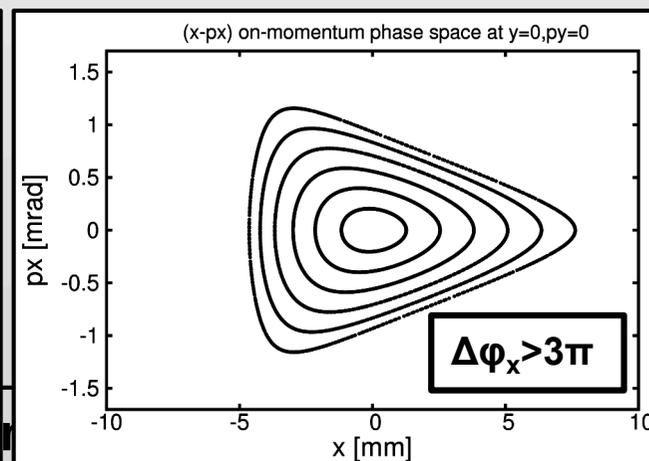
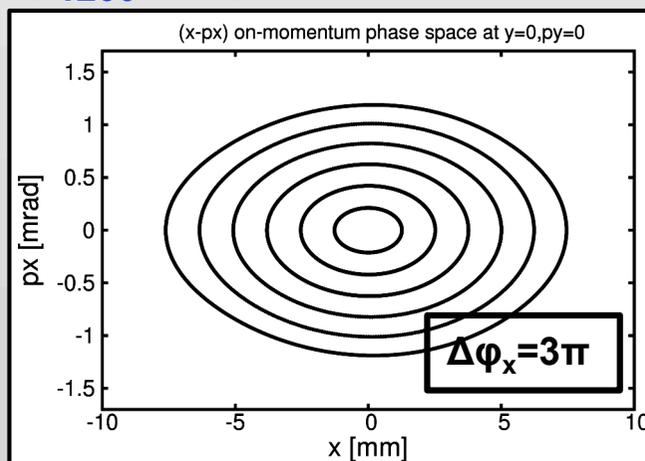
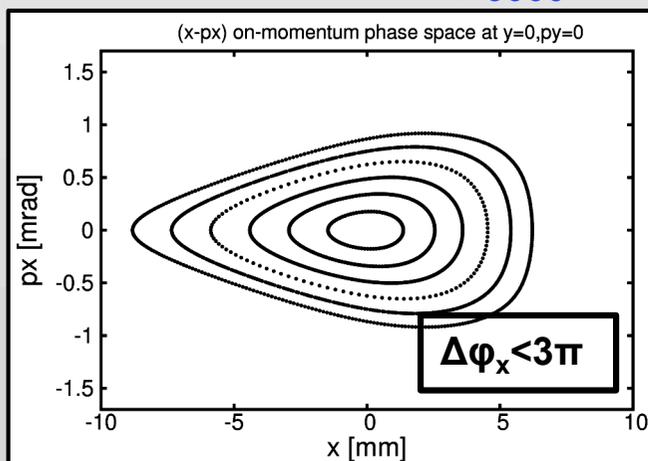
# Nonlinear optics: the HMB lattice



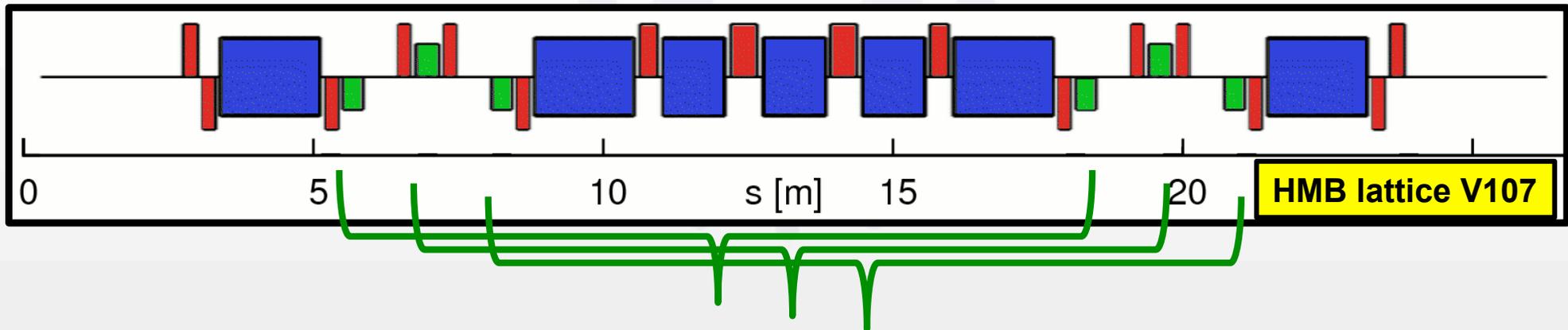
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# Nonlinear optics: the HMB lattice



phase advance between pairs of (chrom.) sextupoles:

$$\Delta\varphi_x = (2n+1)\pi \quad \Delta\varphi_y = n\pi$$

This constraint does not help minimize **amplitude-dependent detuning** generated by second-order cross-products of sextupolar terms within the cell [ $\propto \cos(\Delta\varphi_x), \sin(3\Delta\varphi_y), \dots$ ] and across other cells.

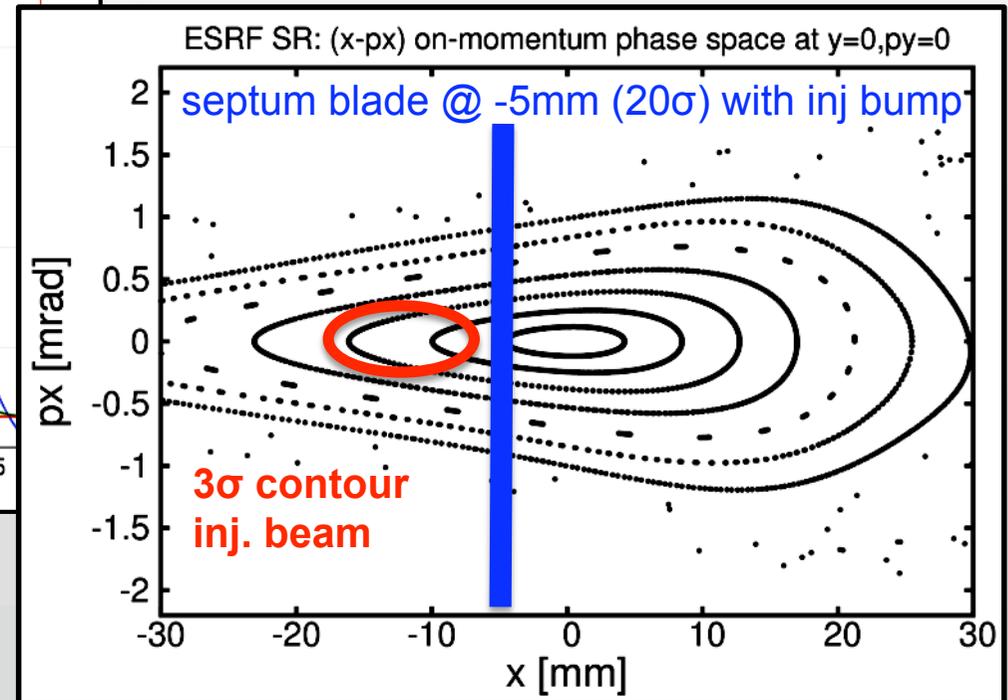
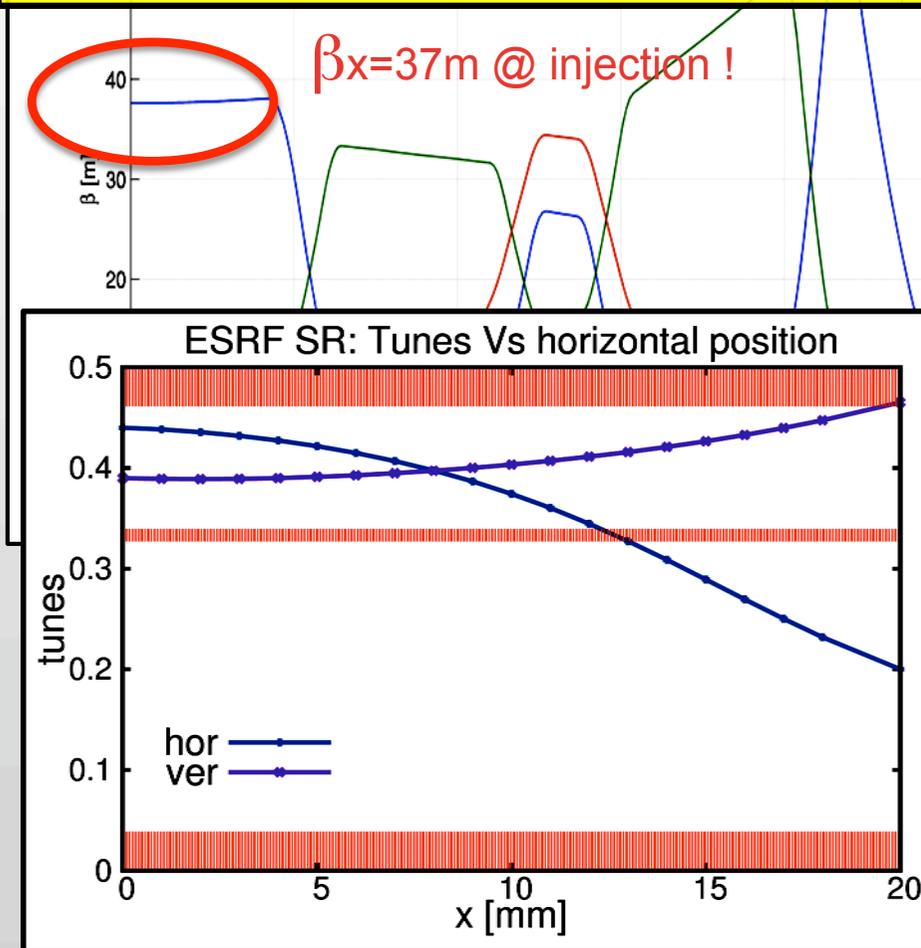
no harmonic sextupoles

# Nonlinear optics: existing ESR SR Vs HMB lattice

$$\begin{aligned}
 dQ_x/dJ_x &= -15 \times 10^3 & d^2Q_x/dJ_x^2 &= 0.3 \times 10^9 \\
 dQ_y/dJ_x &= -11 \times 10^3 & d^2Q_y/dJ_x^2 &= 0.2 \times 10^9 \\
 dQ_y/dJ_y &= 12 \times 10^3 & d^2Q_y/dJ_y^2 &= 0.2 \times 10^9
 \end{aligned}$$

## ESR (DBA) Storage Ring

- 3 chromatic and 4 harmonic sextupoles

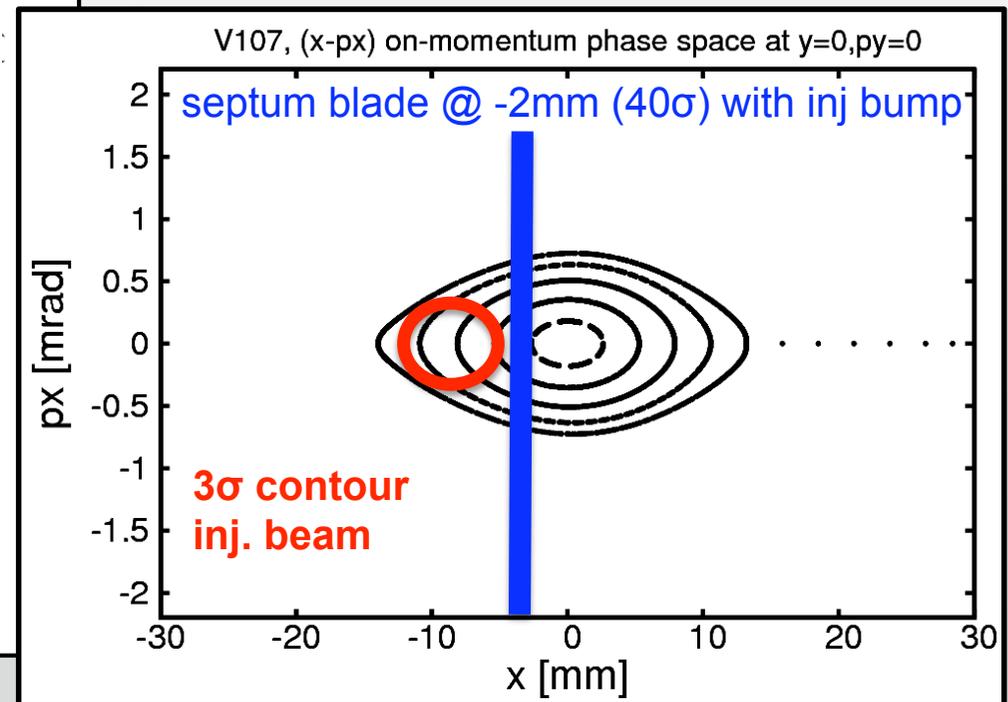
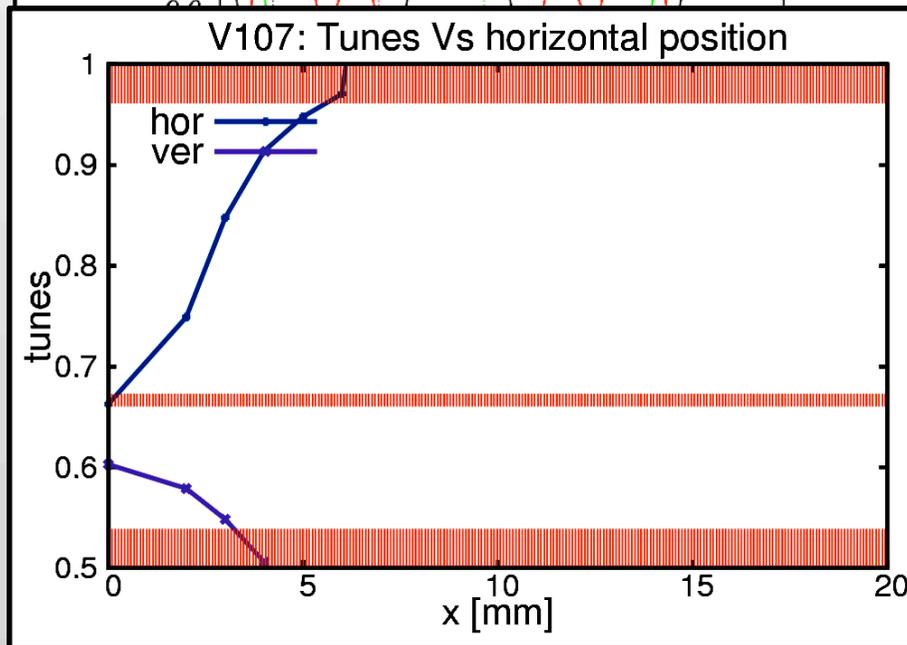
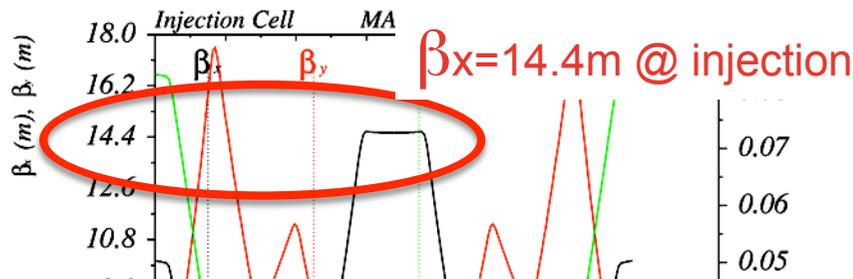


# Nonlinear optics: existing ESR SR Vs HMB lattice

$$\begin{aligned}
 dQ_x/dJ_x &= 100 \times 10^3 & d^2Q_x/dJ_x^2 &= 5.9 \times 10^9 \\
 dQ_y/dJ_x &= -80 \times 10^3 & d^2Q_y/dJ_x^2 &= 29.3 \times 10^9 \\
 dQ_y/dJ_y &= 40 \times 10^3 & d^2Q_y/dJ_y^2 &= 0.9 \times 10^9
 \end{aligned}$$

## HMB lattice (V107)

2+4 chromatic sextupoles, no harmonic sextupoles

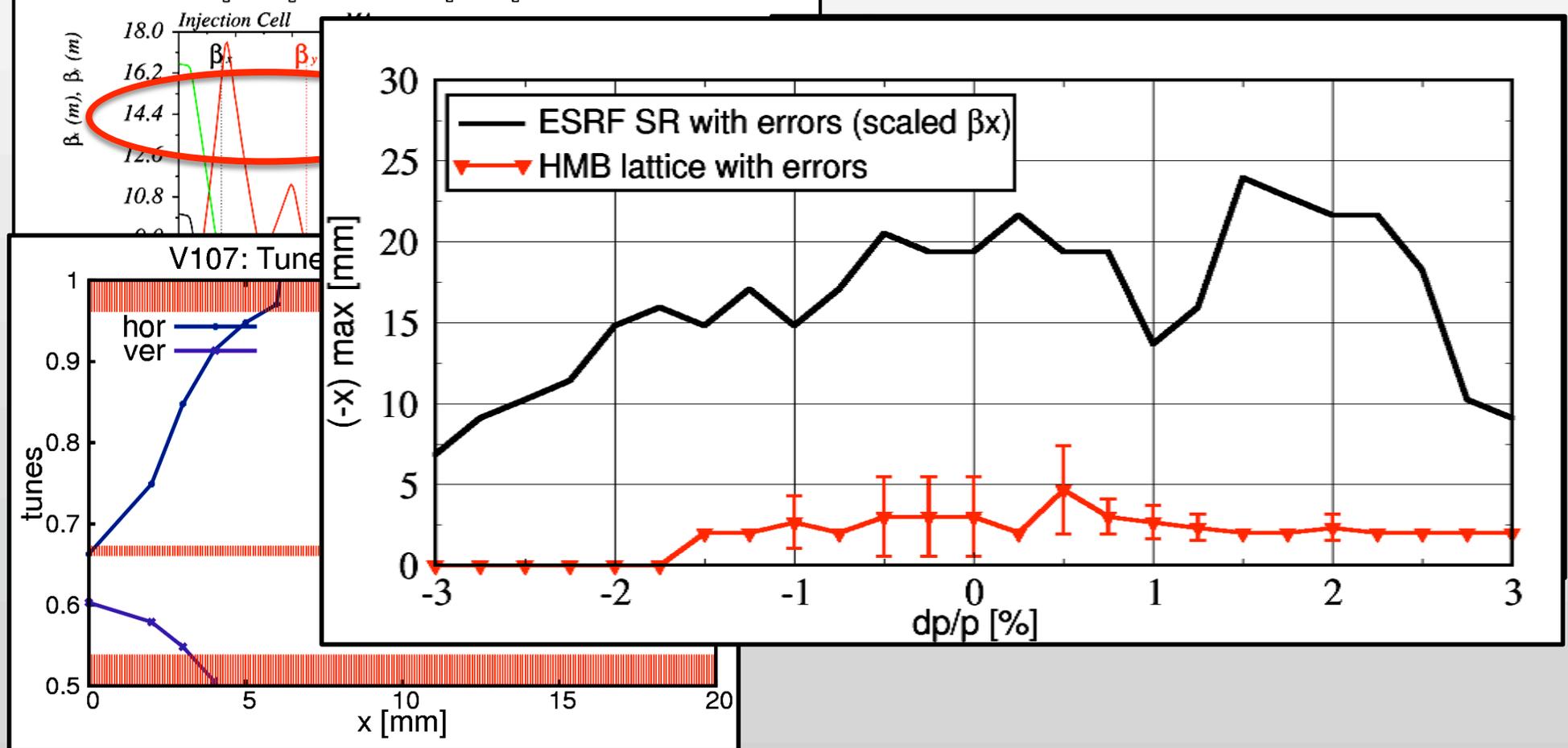


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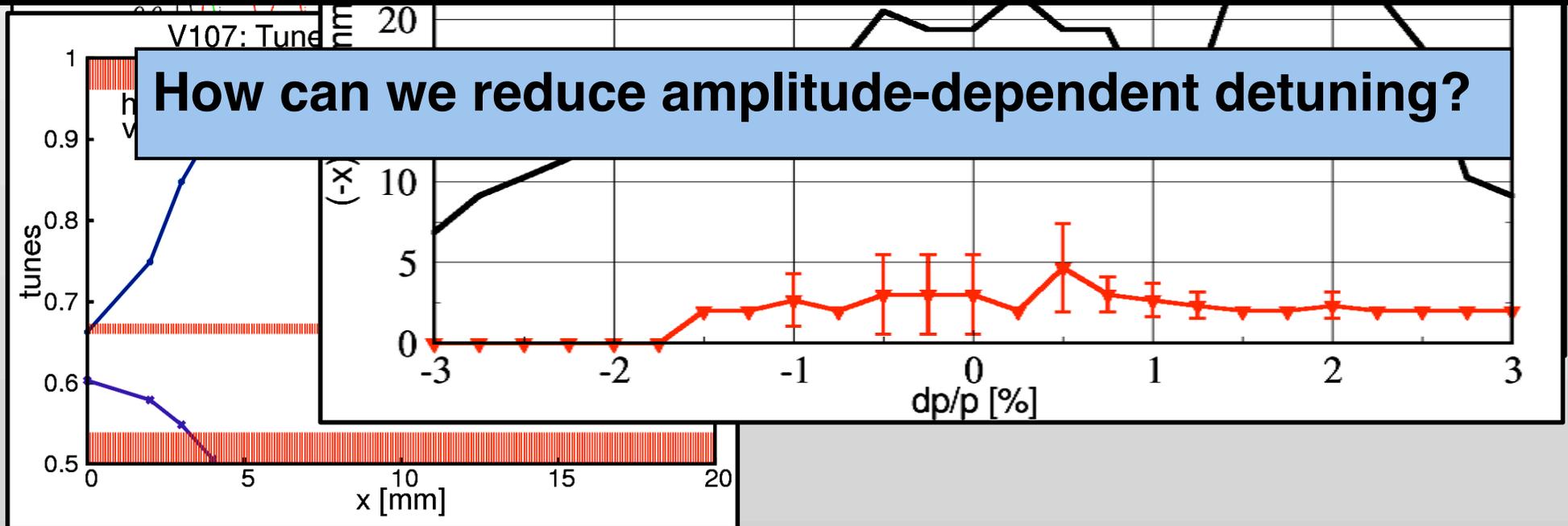
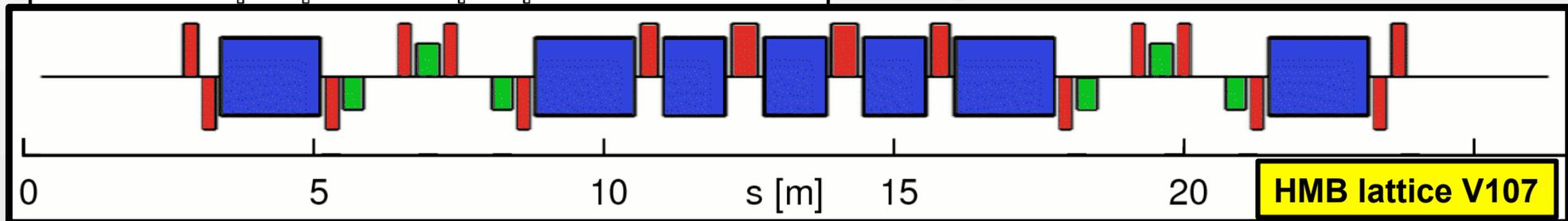


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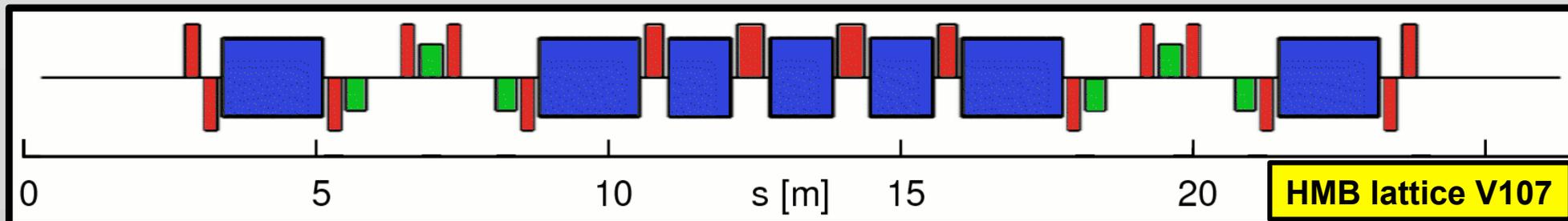
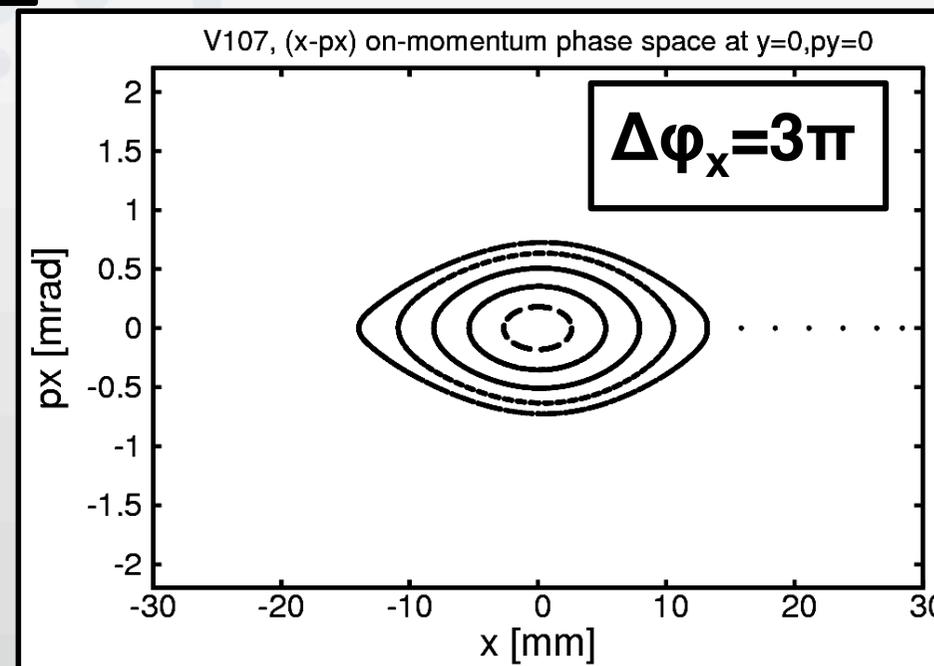
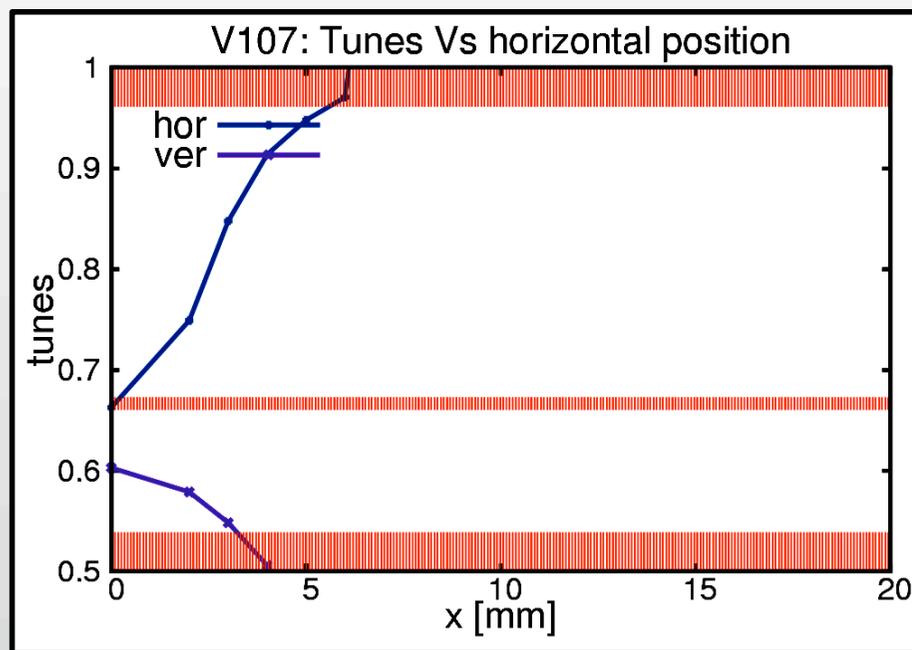
very preliminary, focused on horizontal DA only,  
not yet optimized in vertical plane and energy  
deviation.

Lattice errors: focusing errors from H & V ( $6\mu\text{m}$  RMS) displacement of sextupoles generating  $\sim 2\%$  peak beta-beating & 5% coupling, no sext. field errors, orbit corrected.

# Optimizing dynamic aperture

HMB lattice (V107)

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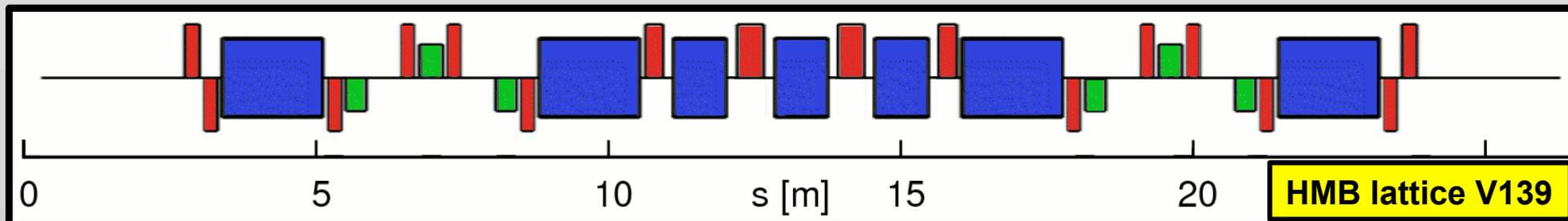
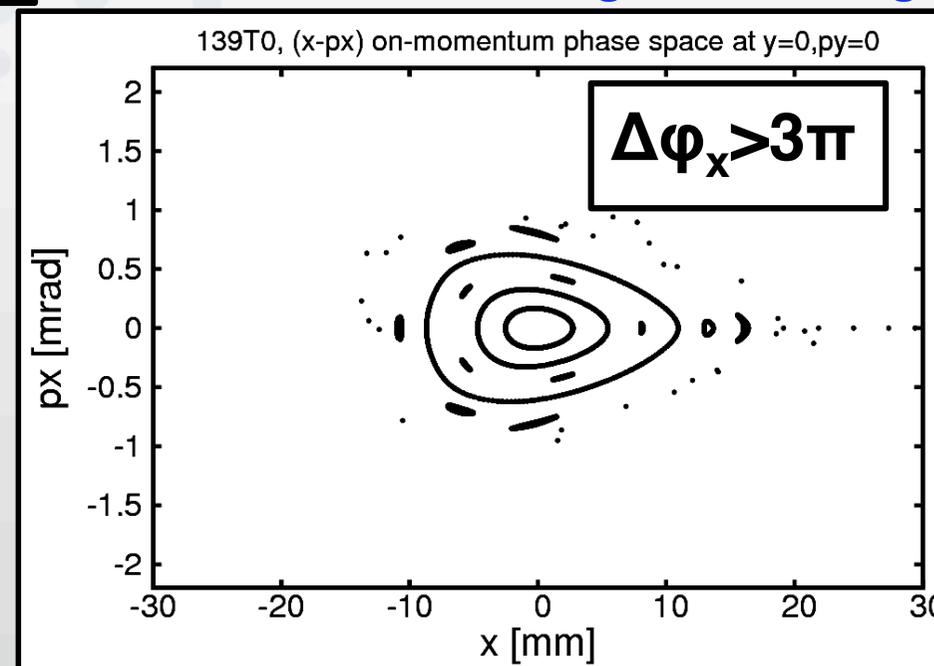
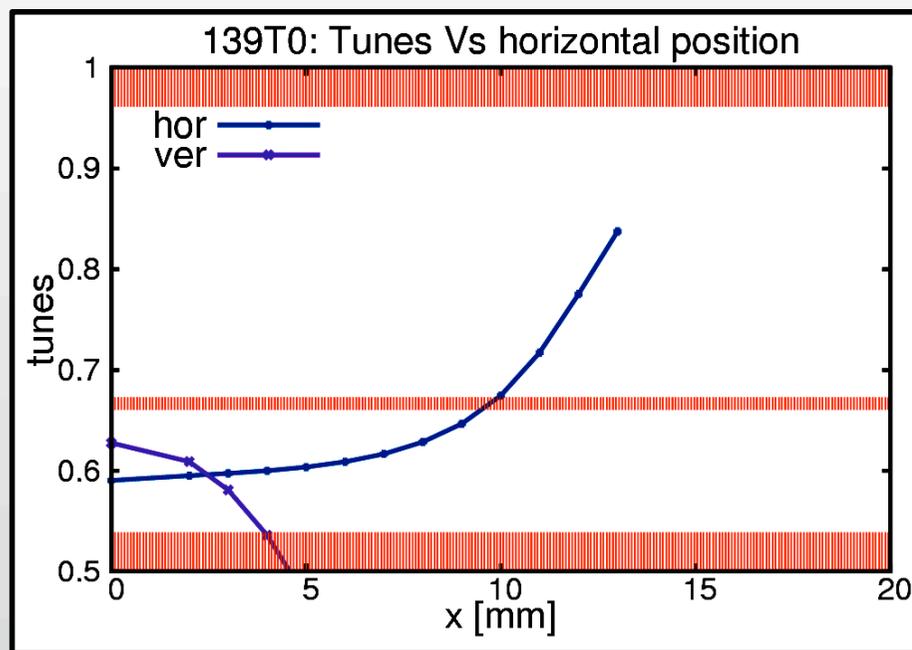


# Optimizing dynamic aperture

$$\begin{aligned}
 dQ_x/dJ_x &= -2 \times 10^3 & d^2Q_x/dJ_x^2 &= 2.7 \times 10^9 \\
 dQ_y/dJ_x &= -82 \times 10^3 & d^2Q_y/dJ_x^2 &= 30.6 \times 10^9 \\
 dQ_y/dJ_y &= -1 \times 10^3 & d^2Q_y/dJ_y^2 &= 0.6 \times 10^9
 \end{aligned}$$

HMB lattice (V139)

- shorter bends for equipment
- lower hor. and ver. detuning
- cross-term detuning still too large

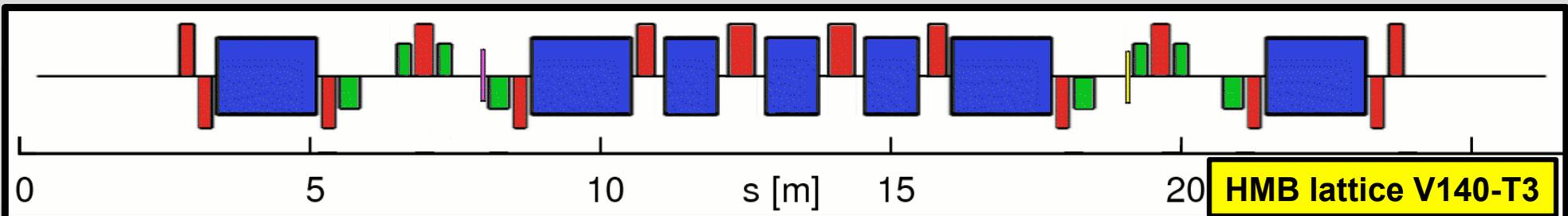
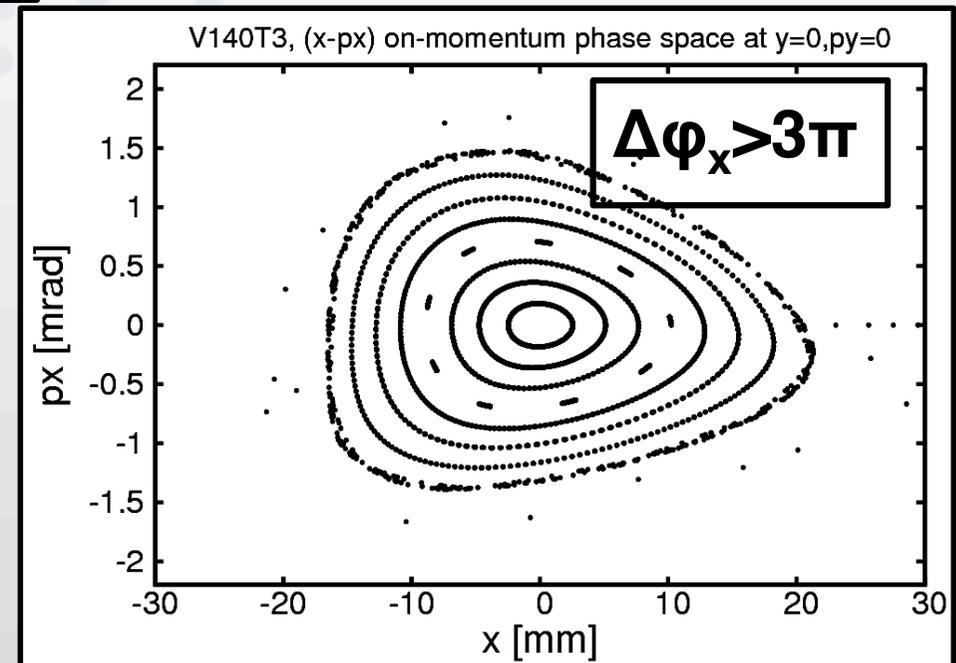
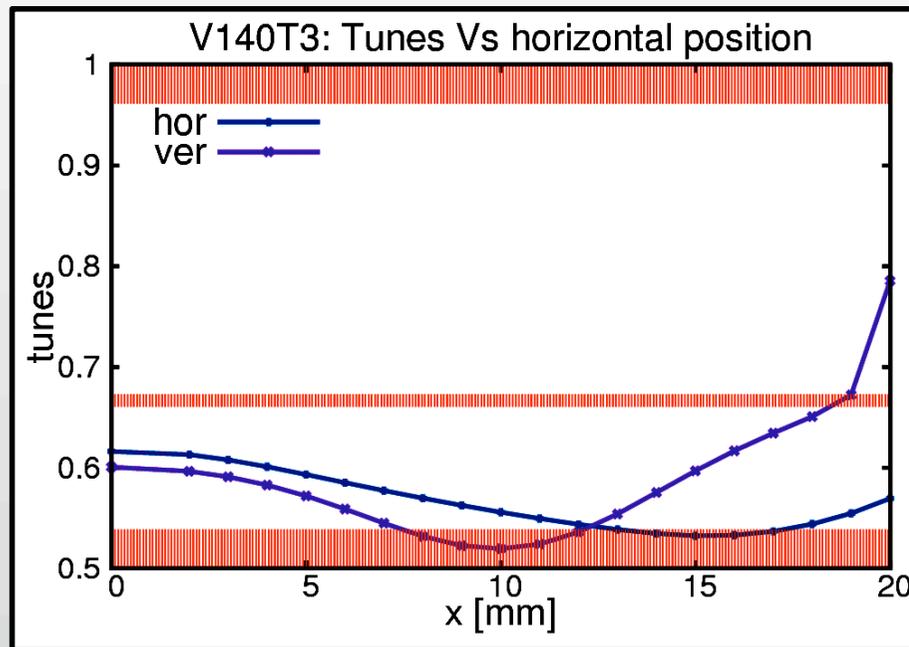


# Optimizing dynamic aperture

## HMB lattice (V140-T3)

- swapped centre quad  $\leftrightarrow$  sext.
- added thin octu- and dodeca-pole
- lower cross-term detuning

$$\begin{aligned}
 dQ_x/dJ_x &= -11 \times 10^3 & d^2Q_x/dJ_x^2 &= 0.6 \times 10^9 \\
 dQ_y/dJ_x &= -15 \times 10^3 & d^2Q_y/dJ_x^2 &= 19.3 \times 10^9 \\
 dQ_y/dJ_y &= -9 \times 10^3 & d^2Q_y/dJ_y^2 &= 4.1 \times 10^9
 \end{aligned}$$

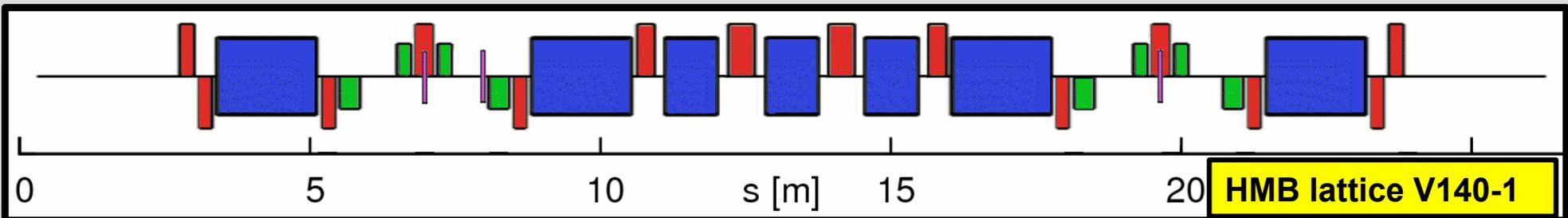
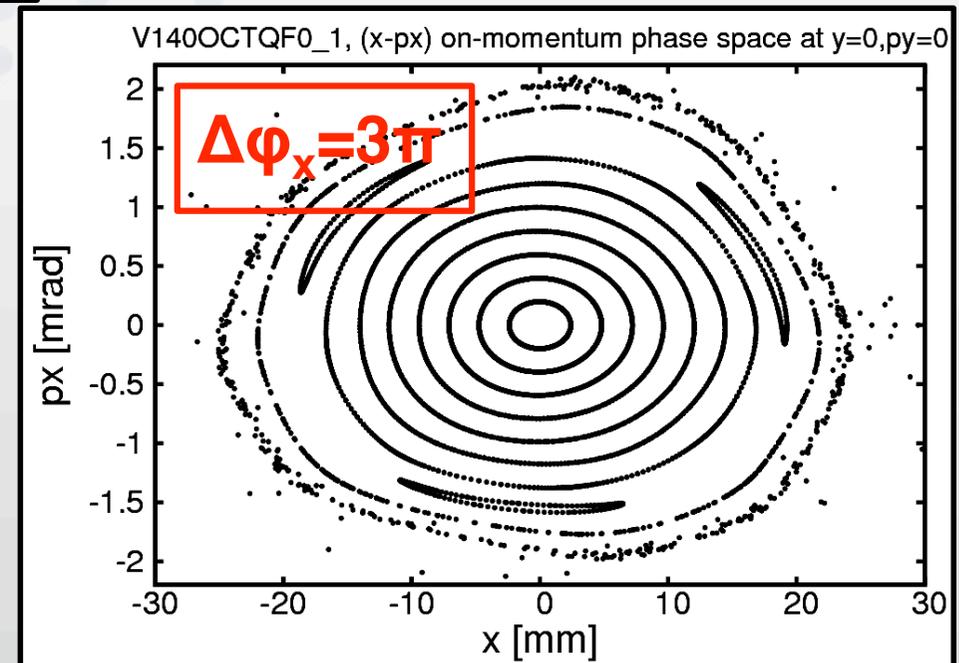
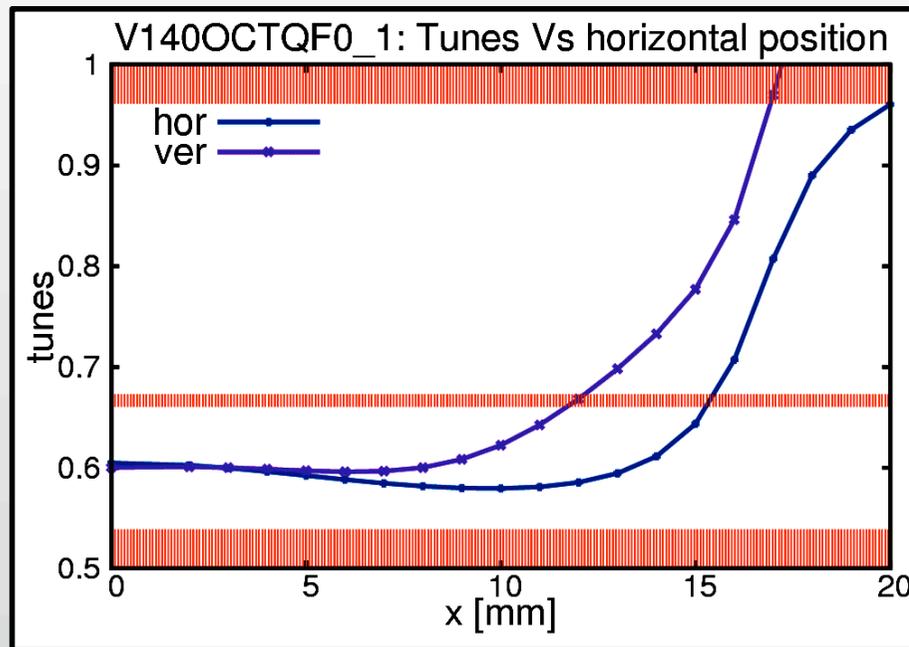


**HMB lattice V140-T3**

# Optimizing dynamic aperture

$$\begin{aligned}
 dQ_x/dJ_x &= -5 \times 10^3 & d^2Q_x/dJ_x^2 &= 0.6 \times 10^9 \\
 dQ_y/dJ_x &= -3 \times 10^3 & d^2Q_y/dJ_x^2 &= 17.7 \times 10^9 \\
 dQ_y/dJ_y &= -6 \times 10^3 & d^2Q_y/dJ_y^2 &= 3.8 \times 10^9
 \end{aligned}$$

- HMB lattice (V140-1)**
- octupole component in QF0 added
  - dodecapole removed
  - lower cross-term detuning

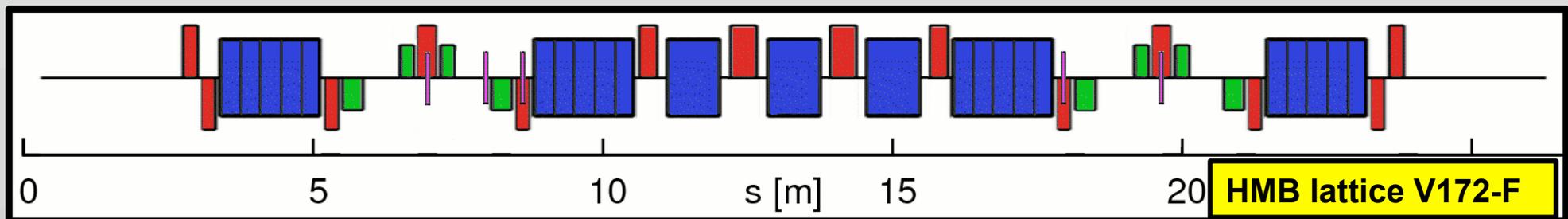
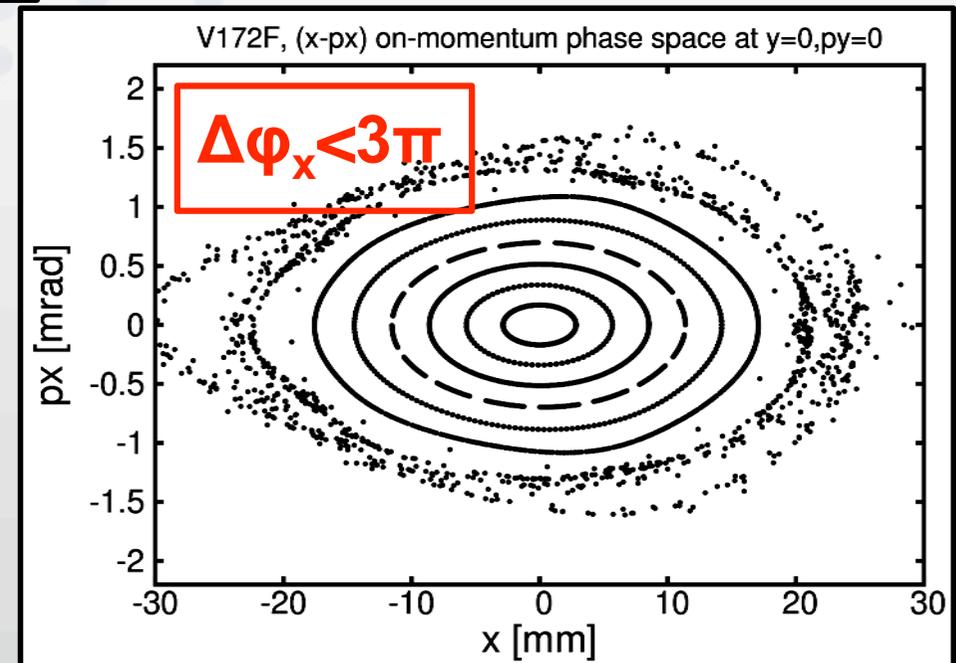
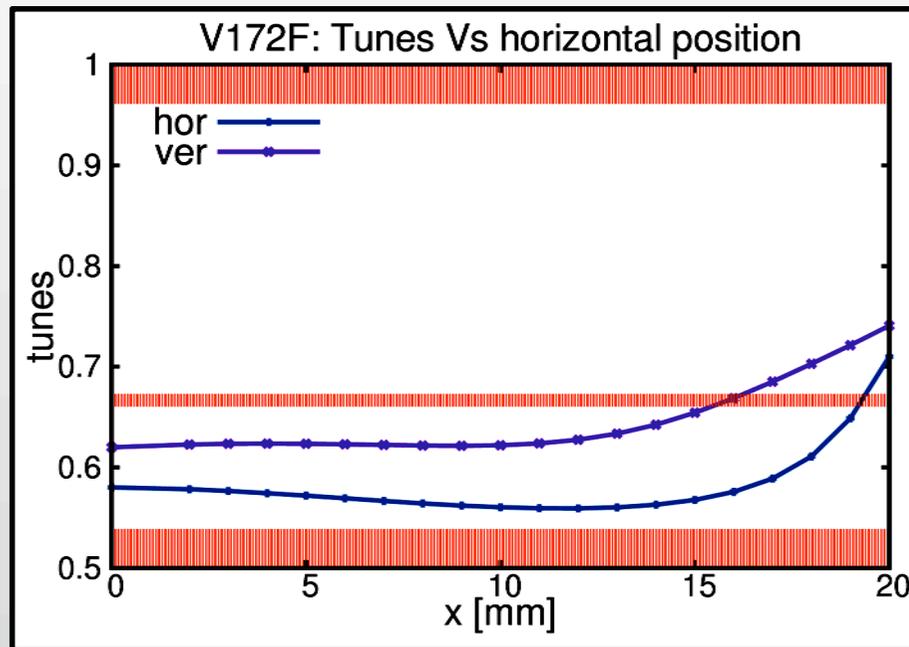


# Optimizing dynamic aperture

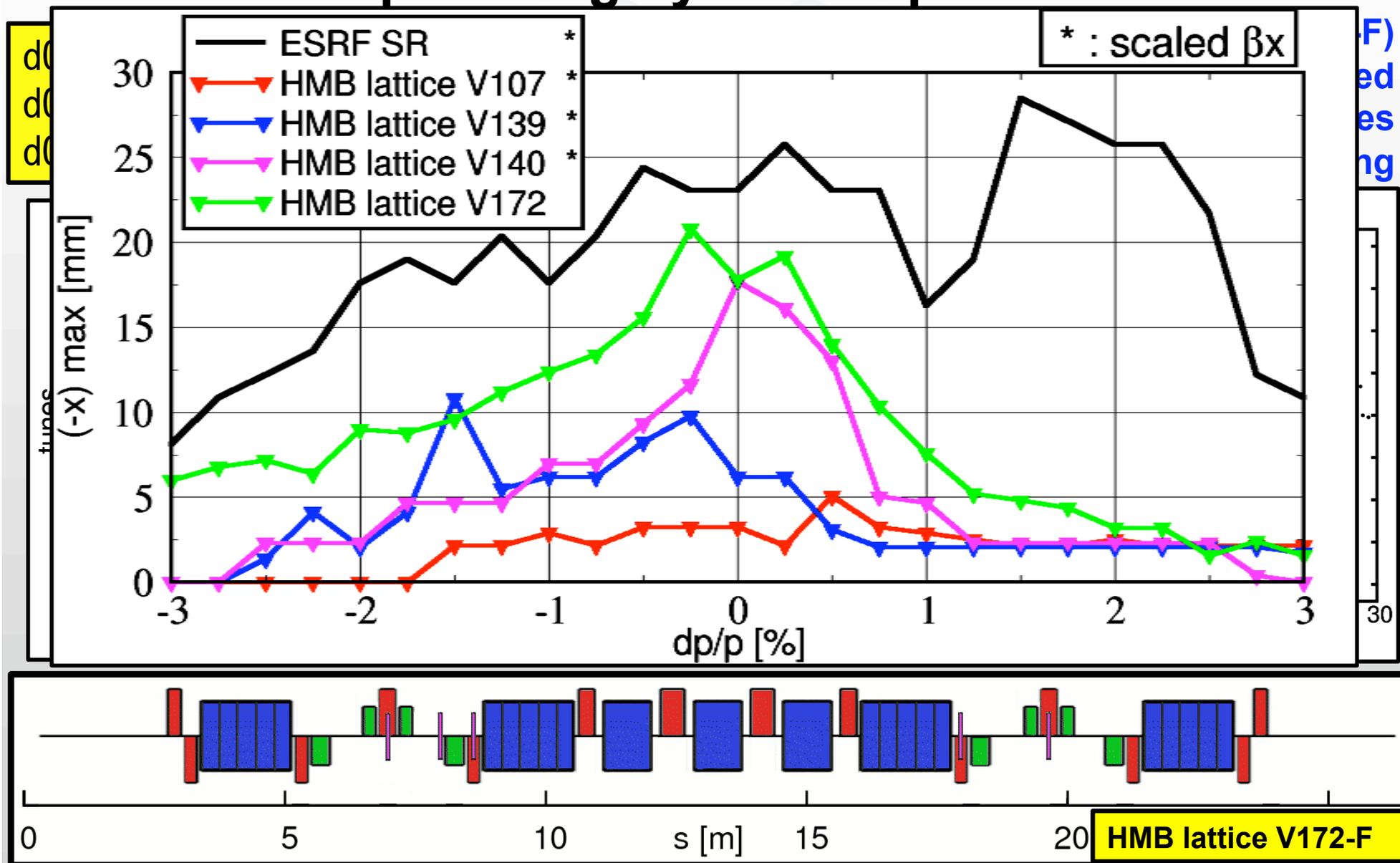
$$\begin{aligned}
 dQ_x/dJ_x &= -4 \times 10^3 & d^2Q_x/dJ_x^2 &= 0.5 \times 10^9 \\
 dQ_y/dJ_x &= -3 \times 10^3 & d^2Q_y/dJ_x^2 &= 0.1 \times 10^9 \\
 dQ_y/dJ_y &= -5 \times 10^3 & d^2Q_y/dJ_y^2 &= 1.0 \times 10^9
 \end{aligned}$$

**HMB lattice (V172-F)**

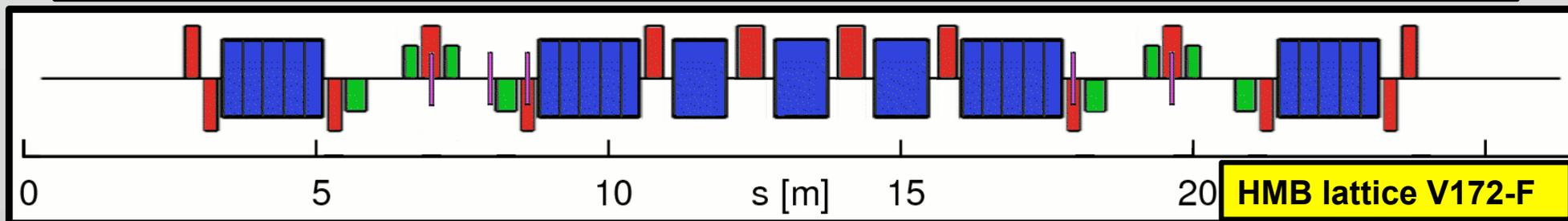
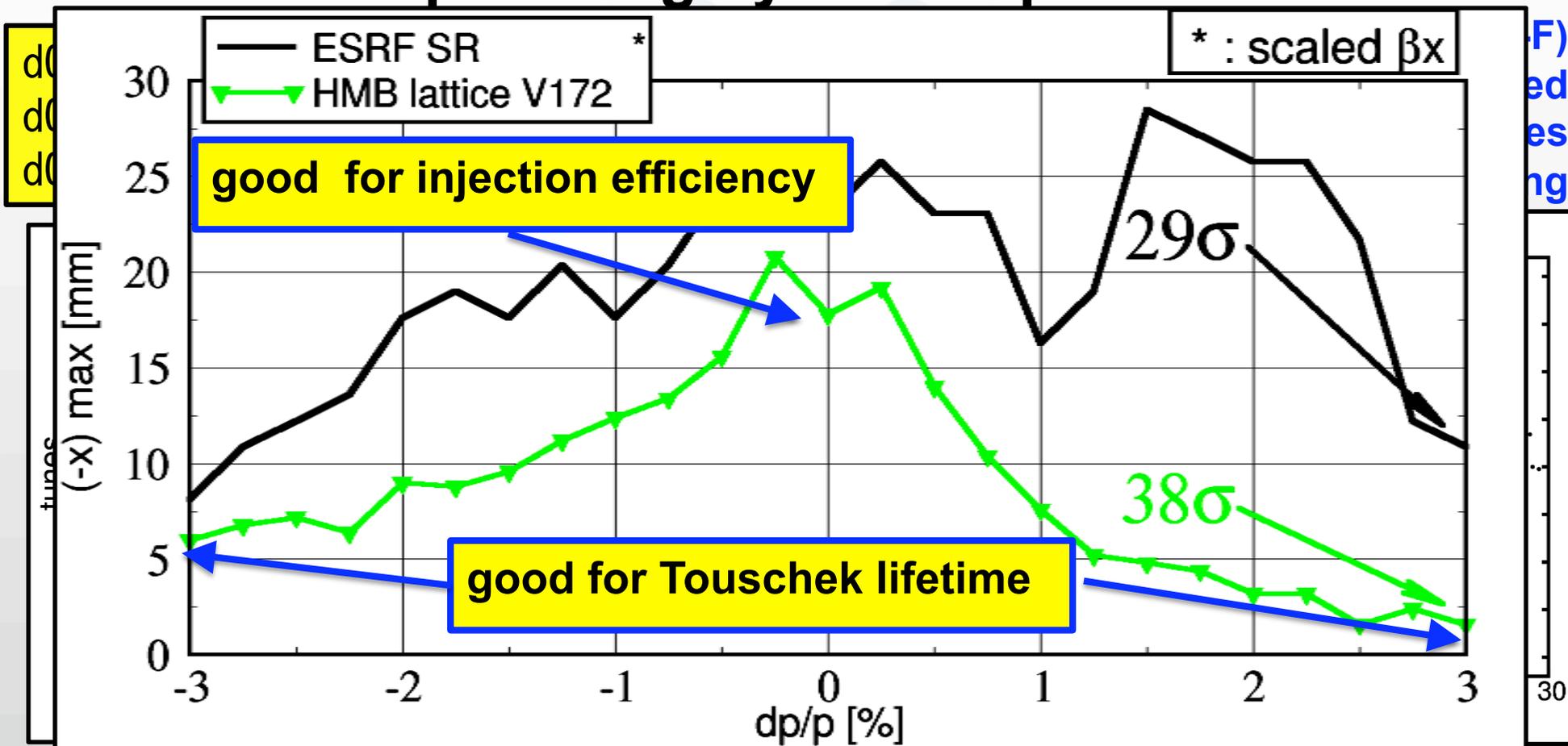
- octupole component in QD0 added
- long. gradient in dipoles
- lower cross-term detuning



# Optimizing dynamic aperture



# Optimizing dynamic aperture



## Conclusion

- lattice design in advanced status of development
- (standard) magnet requirements within reach of existing technology (100 T/m for quads, 2kT/m<sup>2</sup> for sexts)
- dynamic properties already compatible with present injection system
- good energy acceptance
- lattice still evolving to further improve its performances and to match hardware constraints (diagnostic, vacuum, front ends, etc...)

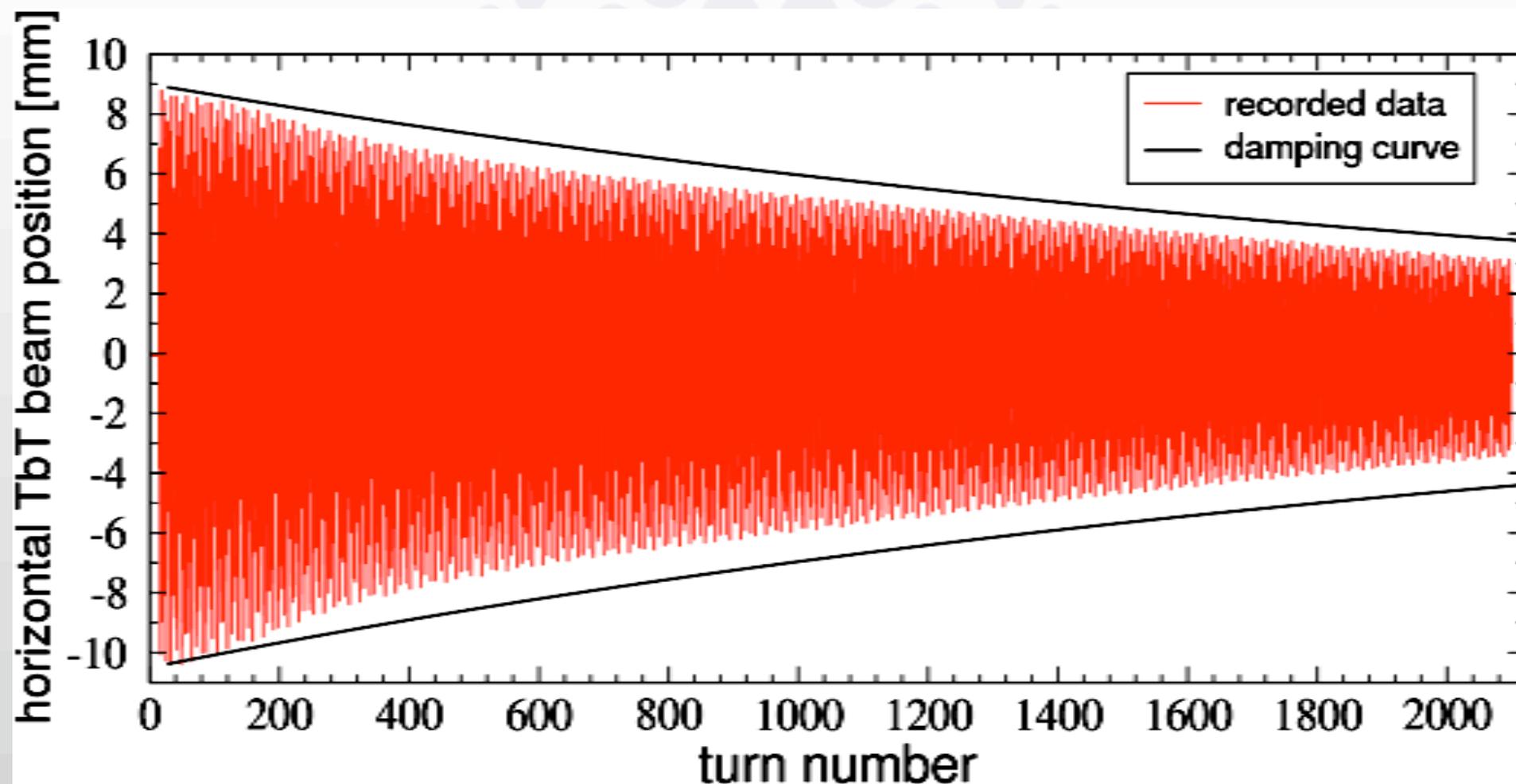
Parameter	Existing Lattice	New Lattice
Energy, $E$ [GeV]	6.03	6.03
Circumference, $C$ [m]	844	844
Tune, $\nu_x, \nu_y, \nu_s$	36.44, 13.39, 0.0054	75.60, 25.60, 0.0034
Emittance, $\epsilon_x, \epsilon_y$ [pm · rad]	4000, 5	160, 5
Bunch length, $\sigma_z$ [ps]	15.6	11
Energy spread, $\sigma_\delta$	$1.06 \cdot 10^{-3}$	$1.06 \cdot 10^{-3}$
Momentum compaction	$17.6 \cdot 10^{-5}$	$8.7 \cdot 10^{-5}$
Damping time, $\tau_x, \tau_y, \tau_s$ [ms]	7, 7, 3.5	7, 11, 7.9
Natural chromaticity, $\xi_{x0}, \xi_{y0}$	-130, -58	-97, -79
Energy loss per turn, $U_0$ [MeV]	4.9	3.05
RF voltage, $V_{RF}$ [MV]	8	6
RF frequency, $f_{RF}$ [MHz]	352	352
Harmonic number	992	992
Beta at ID center, $\beta_x, \beta_y$ [m]	37.6, 3.0 (high $\beta$ ) 0.35, 3.0 (low $\beta$ )	3.35, 2.79
Beam size at ID center, $\sigma_x, \sigma_y$ [ $\mu\text{m}$ ]	413, 3.9 (high $\beta$ ) 50, 3.9 (low $\beta$ )	24, 3.7
Beam div. at ID center, $\sigma_{x'}, \sigma_{y'}$ [ $\mu\text{rad}$ ]	10, 1.3 (high $\beta$ ) 107, 1.3 (low $\beta$ )	6.8, 1.3

# NAME	L	ANGLE	R0	B0	G1	G2	G3L	BETX	BETY	DX
#	[m]	[mrad]	[m]	[T]	[T/m]	[T/m^2]	[T/m^2]	[m]	[m]	[mm]
"QFMA"	0.25				93.71			4.16	7.21	4.3
"QDMA"	0.20				-87.77			2.33	11.39	2.9
"BPI1E"	0.35	9.89	35.38	0.57				1.52	12.67	3.4
"BPI1D"	0.35	6.89	50.76	0.40				1.16	13.73	7.2
"BPI1C"	0.35	5.40	64.86	0.31				1.03	14.85	13.1
"BPI1B"	0.35	4.20	83.40	0.24				1.15	16.03	20.6
"BPI1A"	0.35	3.60	97.30	0.21				1.50	17.27	29.6
"QDID"	0.20				-38.35			2.13	17.04	39.1
"SD1A"	0.30					-1808		3.84	13.44	55.4
"SF1A"	0.18					1885		10.05	6.87	92.9
"QF0"	0.15				55.29			11.59	5.86	100.0
"OCF0"	0.00						-13215	11.59	5.86	100.0
"QF0"	0.15				55.29			10.85	6.16	97.0
"SF1A"	0.18					1885		8.43	7.50	85.7
"OCF"	0.10						-11646	4.30	10.92	61.5
"SD1B"	0.30					-1808		2.17	13.99	43.1
"QD0"	0.20				-57.82			1.39	14.52	33.0
"BPI1A"	0.35	3.60	97.30	0.21				1.11	10.58	24.5
"BPI1B"	0.35	4.20	83.40	0.24				1.16	7.98	19.4
"BPI1C"	0.35	5.40	64.86	0.31				1.42	5.76	15.9
"BPI1D"	0.35	6.89	50.76	0.40				1.91	3.94	14.7
"BPI1E"	0.35	9.89	35.38	0.57				2.61	2.52	16.3
"QF1"	0.32				102.68			2.24	2.33	15.8
"BPI2E1"	0.35	12.74	27.47	0.73	-44.04			0.36	4.68	7.4
"BPI2E2"	0.35	12.74	27.47	0.73	-44.04			0.74	3.40	10.9
"QF2"	0.45				96.52			2.06	1.75	16.7
"BPI2E1"	0.35	12.74	27.47	0.73	-44.04			0.68	4.02	7.5

HMB lattice

# NAME	L	ANGLE	R0	B0	G1	G2	BETX	BETY	DX
#	[m]	[mrad]	[m]	[T]	[T/m]	[T/m <sup>2</sup> ]	[m]	[m]	[mm]
<b>SBEND</b>	2.45	<b>98.00</b>	<b>24.96</b>	<b>0.86</b>			1.77	32.16	79.40
<b>g1.qf2</b>	0.94				<b>7.86</b>		26.48	16.34	111.60
<b>g1.qd3</b>	0.53				<b>-12.14</b>		7.81	33.34	59.54
<b>g1.qd4</b>	0.42				<b>-12.10</b>		10.87	28.24	219.10
<b>g1.qf5</b>	0.52				<b>14.78</b>		26.81	15.17	344.30
<b>g1.qd6</b>	0.52				<b>-16.47</b>		20.53	41.27	9.45
<b>g1.qf7</b>	0.92	<b>ESRF SR</b>			<b>13.71</b>		52.41	9.08	30.79
<b>g2.s04</b>	0.40					<b>124.31</b>	38.00	8.16	134.30
<b>g2.s06</b>	0.40					<b>-165.15</b>	18.85	22.20	93.90
<b>g2.s13</b>	0.40					<b>-88.02</b>	15.39	23.32	260.90
<b>g2.s19</b>	0.40					<b>443.32</b>	26.53	15.61	342.30
<b>g2.s20</b>	0.40					<b>-419.43</b>	14.37	27.19	250.60
<b>g2.s22</b>	0.40					<b>-95.81</b>	30.47	30.16	15.43
<b>g2.s24</b>	0.40					<b>132.33</b>	44.47	8.15	30.80

# Beam response after horizontal kick ...

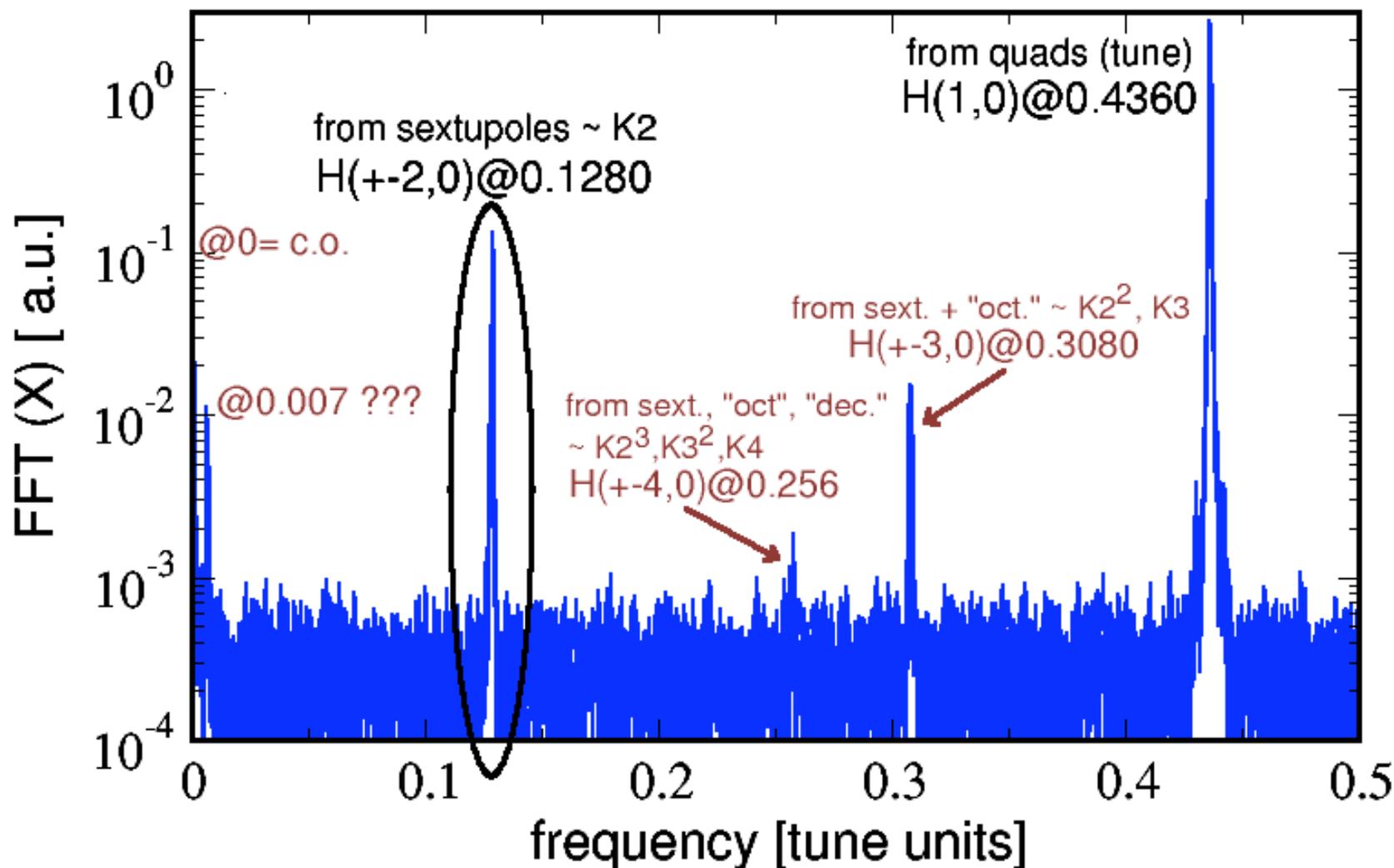


# ... and its spectrum (FFT) *measured*

— K1@700A

## BPM TbT HORIZONTAL SPECTRUM

MDT of Oct. 17th 2010 (MAF, FFT over 2048 turns)

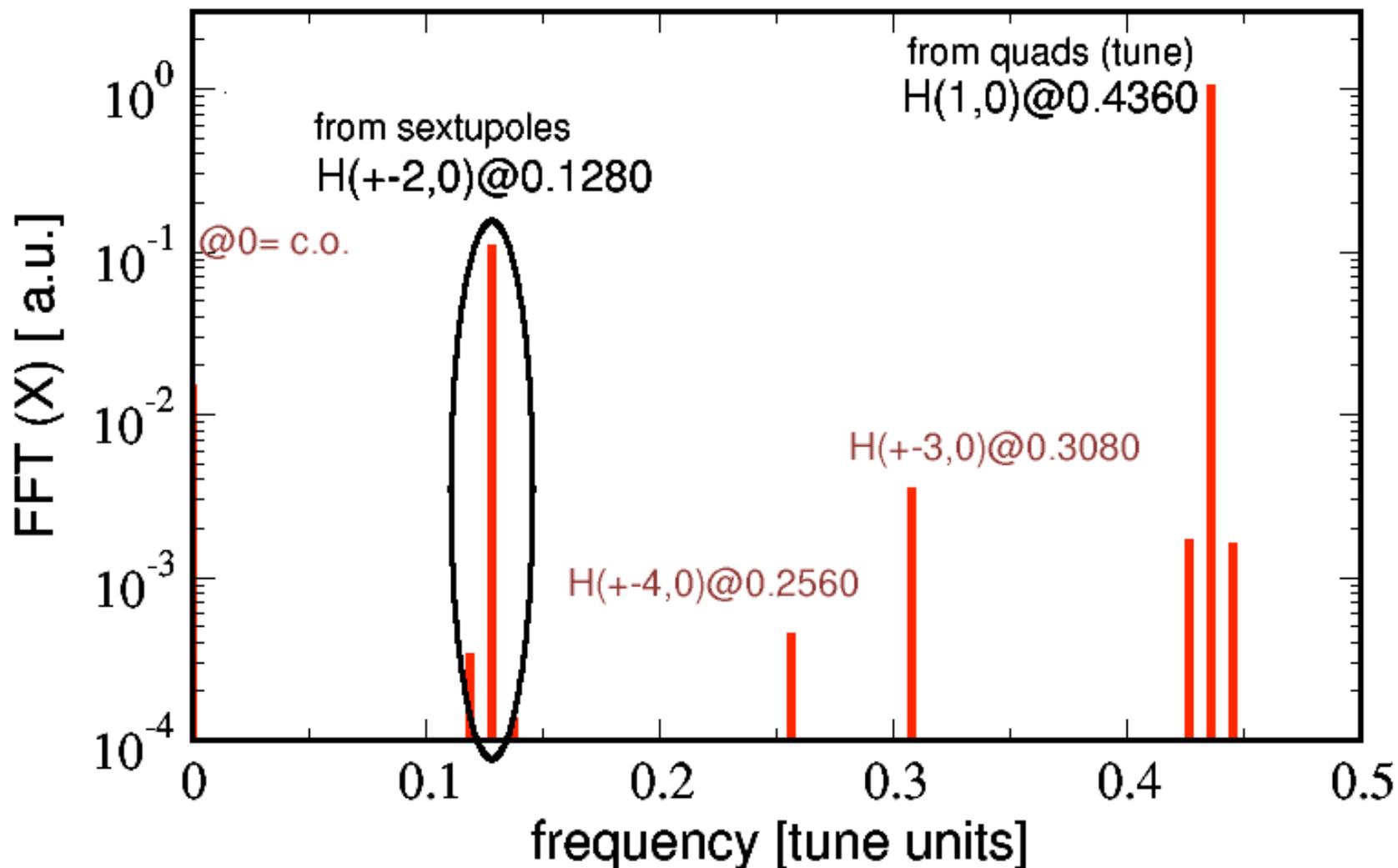


# ... and its spectrum (FFT) *simulated*

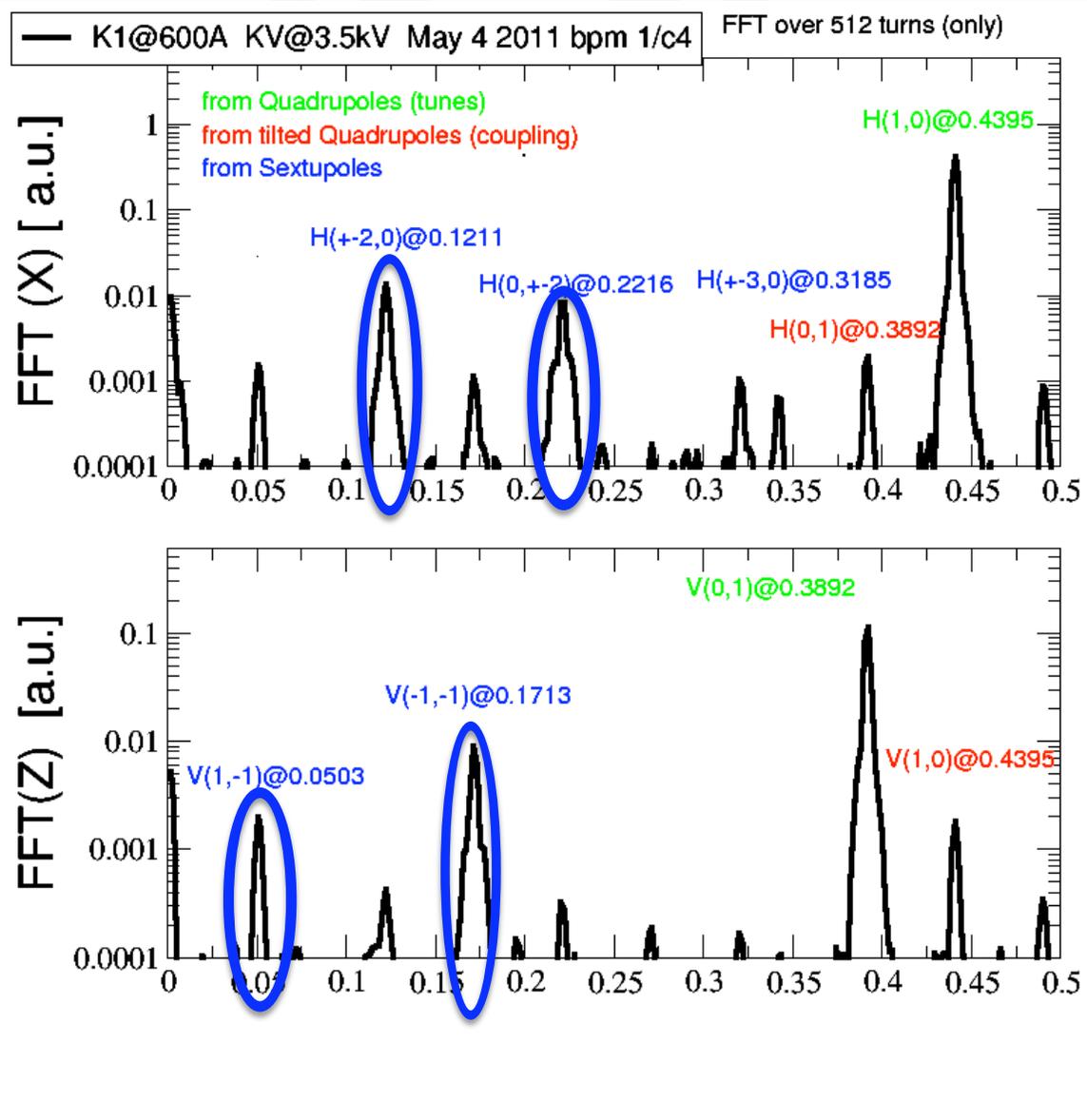
x0=10 mm

## BPM TbT HORIZONTAL SPECTRUM

From tracking simulation with sextupoles only

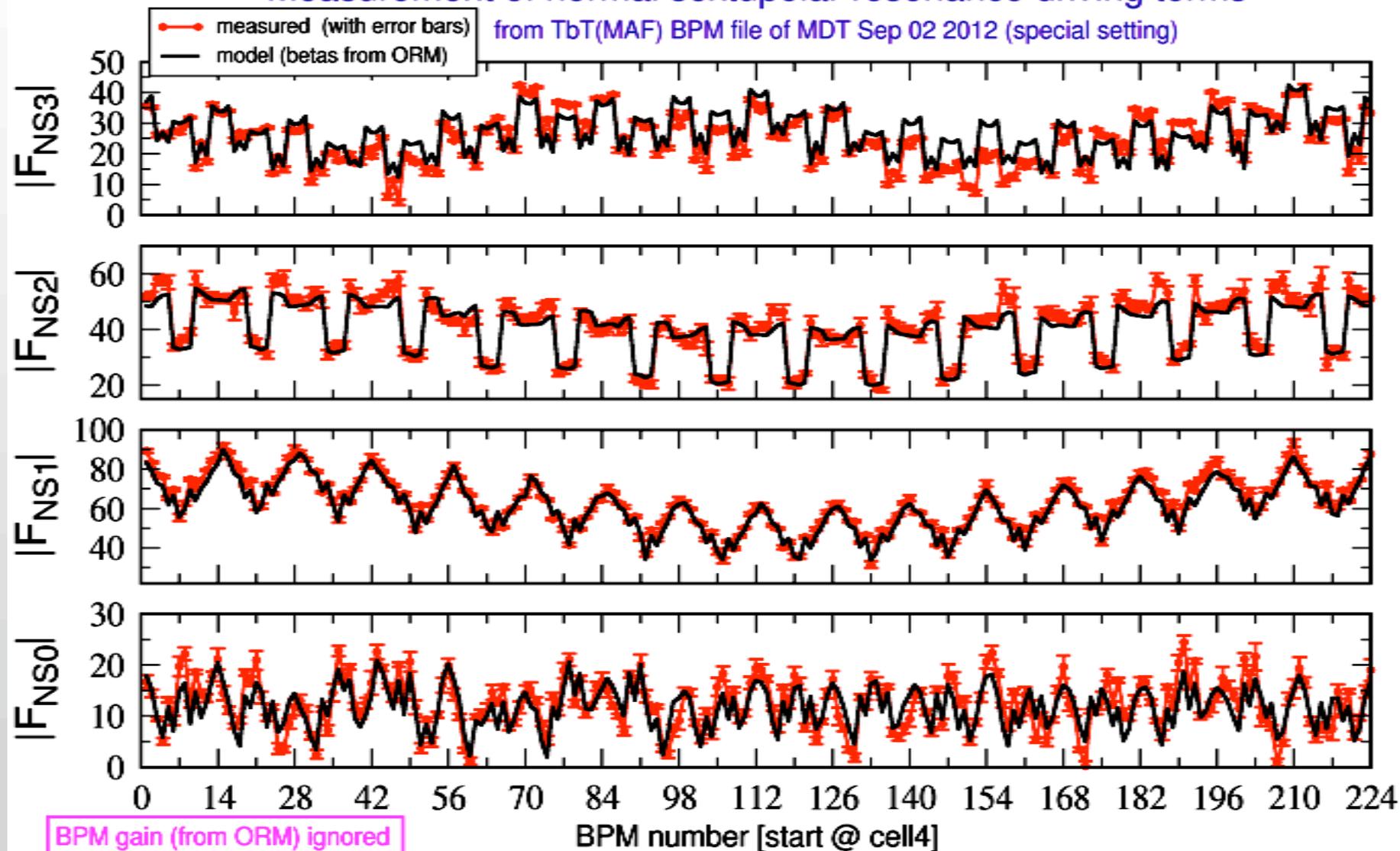


# ... and its spectrum (FFT) *measured*

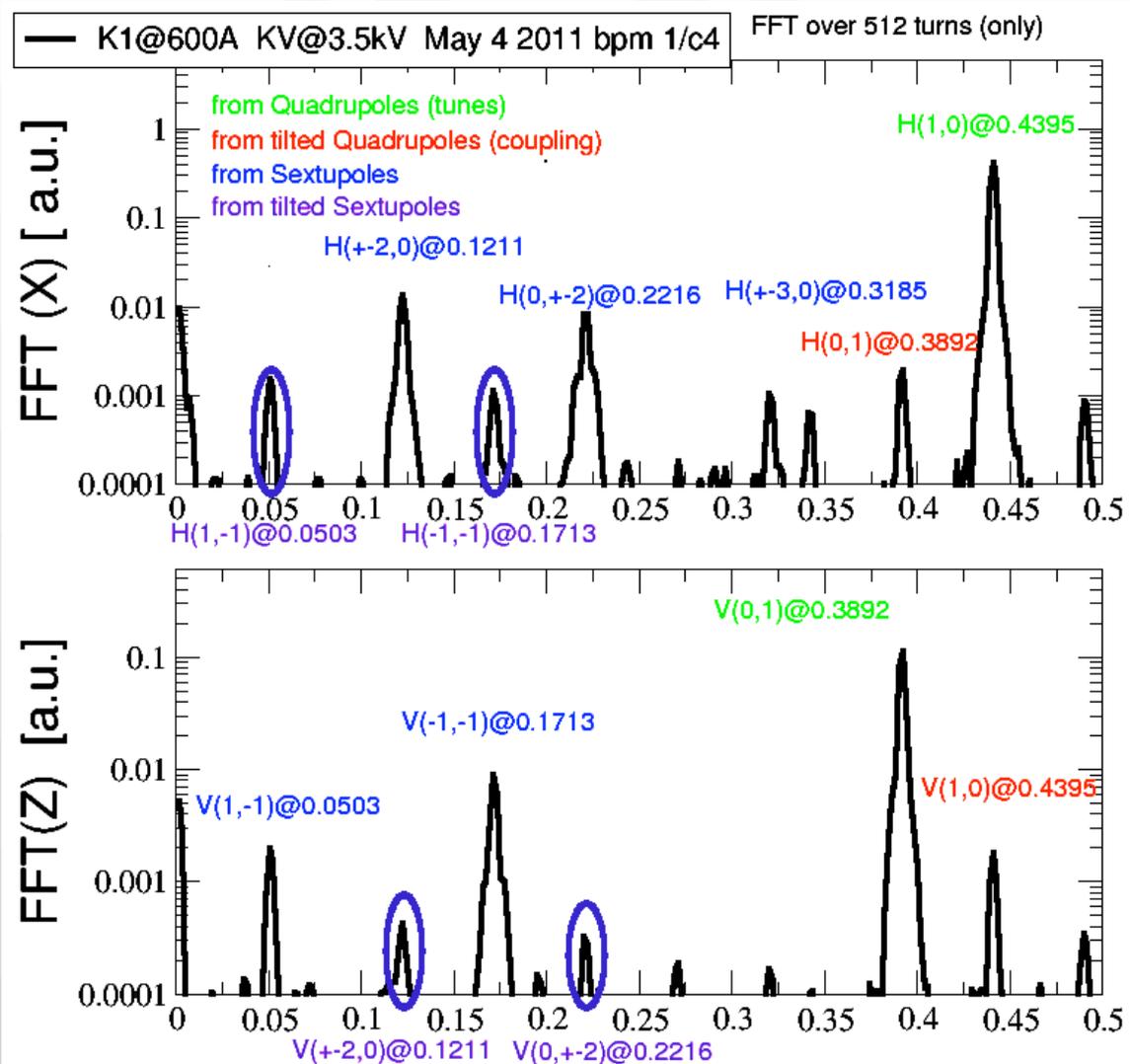


# its normal sextupolar RDTs *measured*

## Measurement of normal sextupolar resonance driving terms



# ... and its spectrum (FFT) *measured*



# its skew sextupolar RDTs *measured*

## Measurement of skew sextupolar resonance driving terms

