

## BESIII 实验上粲介子含轻衰变研究进展

潘祥  
东南大学

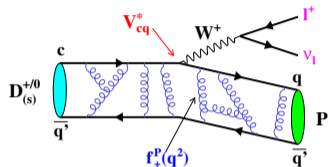
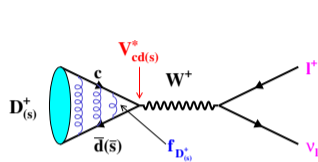
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重庆大学  
2026 年 4 月 24 日至 28 日

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## Introduction

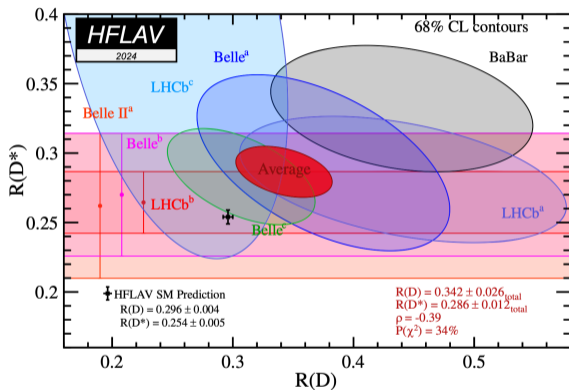
$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



$$V^\dagger V = 1 \quad \Gamma = \frac{G_F^2}{8\pi} |V_{cq}|^2 |f_{D_s^+}|^2 m_\ell^2 m_{D_s^+} (1 - m_\ell^2/m_{D_s^+}^2)^2 \quad \frac{d\Gamma}{dq^2} = \chi \frac{G_F^2 |\vec{p}_P|^3}{24\pi^3} |V_{cq}|^2 |f_+(q^2)|^2$$

- Uncertainties of  $V_{\text{CKM}} \Rightarrow$  mainly contributed by  $|V_{cs}|$  ( $\sigma = 0.6\%$ ) and  $|V_{cd}|$  ( $\sigma = 1.8\%$ )
- Latest LQCD:  $f_{D_s^+} = 249.9(05)$  MeV ( $\sigma = 0.2\%$ );  $f_{D^+} = 212.1(07)$  MeV ( $\sigma = 0.3\%$ );  
 $f_+^{D \rightarrow \bar{K}}(0) = 0.7452(31)$  ( $\sigma = 0.4\%$ );  $f_+^{D \rightarrow \pi}(0) = 0.6300(51)$  ( $\sigma = 0.8\%$ )
- Decay constant  $f_{D_s^+}$  and FF  $f_+(0)$  measurements  $\Rightarrow$  Calibrate LQCD calculations
- $|V_{cq}|$  measurement  $\Rightarrow$  Test CKM matrix unitarity

## Introduction



- Evidence ( $3.14\sigma$ ) of LFU violation in  $B \rightarrow D^{(*)} \ell^+ \nu_\ell$

- Precision test of LFU in charm sector
- Leptonic decay

$$\mathcal{R}_{D^+:\tau/\mu}^{\text{SM}} = \frac{m_\tau^2 (1 - m_\tau^2/m_{D^+}^2)^2}{m_\mu^2 (1 - m_\mu^2/m_{D^+}^2)^2} = 2.66 \pm 0.01$$

$$\mathcal{R}_{D_s^+:\tau/\mu}^{\text{SM}} = \frac{m_\tau^2 (1 - m_\tau^2/m_{D_s^+}^2)^2}{m_\mu^2 (1 - m_\mu^2/m_{D_s^+}^2)^2} = 9.75 \pm 0.01$$

- Semileptonic decay [PRD107(2023)094516]

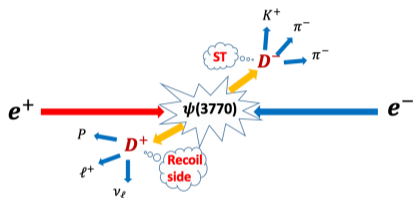
$$\mathcal{R}_{D \rightarrow \bar{K}:\mu/e}^{\text{SM}} = 0.97606(16)^{\text{QED}} [500]^{\text{QED}}$$

$$\mathcal{R}_{D \rightarrow \pi:\mu/e}^{\text{SM}} = 0.98671(17)^{\text{QED}} [500]^{\text{QED}}$$

$$\mathcal{R}_{D_s \rightarrow K^0:\mu/e}^{\text{SM}} = 0.98099(10)^{\text{QCD}} [500]^{\text{QED}}$$

- Other  $D \rightarrow P \ell^+ \nu_\ell$ :  $\mathcal{R}_{\mu/e} \in (0.95 - 0.99)$  based on different quark models

# BESIII dataset and double-tag method

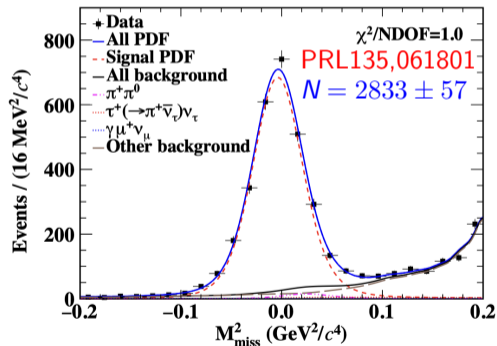


- $e^+e^-$  annihilations data near threshold  
 $\Rightarrow$  Double-tag method & Clean environment
- Undetectable neutrinos  $\Rightarrow$  extract the leptonic signals  
 $U_{\text{miss}} = E_{\text{miss}} - |\vec{p}_{\text{miss}}|$ ,  $M_{\text{miss}}^2 = E_{\text{miss}}^2 - |\vec{p}_{\text{miss}}|^2$
- BF with double-tag method:  $\mathcal{B} = \frac{N_{\text{DT}}}{N_{\text{ST}} \epsilon_{\text{DT}} / \epsilon_{\text{ST}}}$   
 $\Rightarrow$  Systematic uncertainties on the ST mostly canceled

Data sample	$E_{\text{cm}}$ (GeV)	$\mathcal{L}_{\text{int}}$ ( $\text{fb}^{-1}$ )	Single tag yields ( $\times 10^6$ )
$e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$	3.773	20.3	$\bar{D}^0 \sim 16.9$ ; $D^- \sim 11.0$
$e^+e^- \rightarrow D_s^\pm D_s^{*\mp}$	4.128-4.226	7.33	$D_s^- \sim 0.8$
$e^+e^- \rightarrow D_s^{*+} D_s^{*-}$	4.237-4.669	10.64	$D_s^- \sim 0.12$

Precision measurement of the branching fraction of  $D^+ \rightarrow \mu^+ \nu_\mu$ 

Reference	$\mathcal{L}$ (fb $^{-1}$ )	BF( $\times 10^{-4}$ )	$f_{D^+}$ (MeV)	$ V_{cd} $	Precision (%)
CLEO, PRD78,052003	0.818	3.82(32)(09)	207.1(87)(24)(08)	0.2195(92)(26)(09)	4.4
BESIII, PRD89,051104	2.93	3.71(19)(06)	204.1(52)(17)(08)	0.2164(55)(17)(09)	2.7
<b>BESIII, PRL135,061801</b>	<b>20.3</b>	<b>4.034(80)(40)</b>	<b>213.5(21)(11)(08)</b>	<b>0.2265(23)(11)(09)</b>	<b>1.2 ★</b>



$$\Gamma_{D^+ \rightarrow \ell^+ \nu_\ell} = \Gamma_{D^+ \rightarrow \ell^+ \nu_\ell}^{(0)} \left[ 1 + \frac{\alpha}{\pi} C_p \right]$$

$$= \frac{G_F^2 f_{D^+}^2 m_{D^+}^3}{8\pi} |V_{cd}|^2 \mu_\ell^2 (1 - \mu_\ell^2)^2 \left[ 1 + \frac{\alpha}{\pi} C_p \right]$$

- the radiative correction term [1]:  $\left[ 1 + \frac{\alpha}{\pi} C_p \right]$
- Structure-dependent bremsstrahlung [2,3]  $\implies$  Subtracted in the fit
- Short-distance (+1.8%) [4,5] and Long-distance (-2.5%) [6] electroweak correction

1 D. Silverman and H. Yao, Phys. Rev. D 38, 214 (1988).

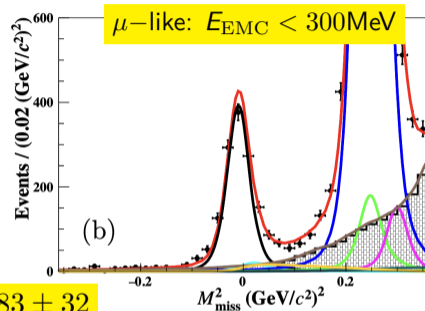
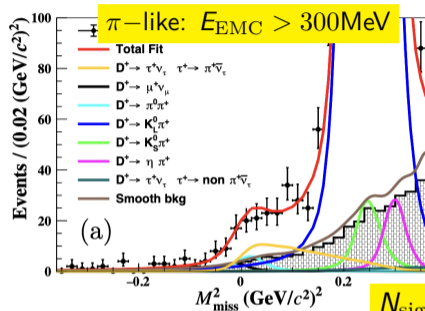
2 G. Burdman, J.T. Goldman, and D. Wyler, Phys. Rev. D 51, 111 (1995).

3 A. Bazavov *et al.*, Phys. Rev. D 98, 074512 (2018).

4 J. C. Yang and M.Z. Yang, Nucl. Phys. B914, 301 (2017).

5 A. Sirlin, Nucl. Phys. B196, 83 (1982).

6 T. Kinoshita, Phys. Rev. Lett. 2, 477 (1959).

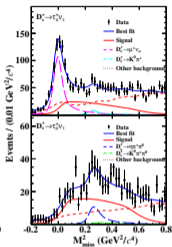
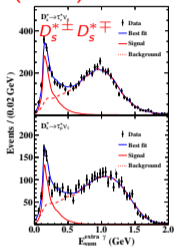
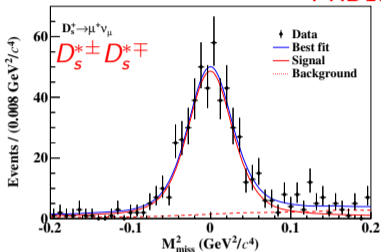
Measurement of the branching fraction of  $D^+ \rightarrow \tau^+ \nu_\tau$  via  $\tau^+ \rightarrow \pi^+ \bar{\nu}_\tau$ 

- $7.93 \text{ fb}^{-1} @ 3.773 \text{ GeV}$  [JHEP01(2025)89]
- Precision of BF is improved by  $1.8\times$ :  $\mathcal{B}(D^+ \rightarrow \tau^+ \nu_\tau) = (9.9 \pm 1.1 \pm 0.5) \times 10^{-4}$
- $f_{D^+} = (204.6 \pm 11.4 \pm 5.2) \text{ MeV}$  ( $\sim 5.9\%$ )  $|V_{cd}| = 0.217 \pm 0.012 \pm 0.006$  ( $\sim 6.2\%$ )
- LFU test:  $\mathcal{R}_{\tau/\mu} = \frac{\Gamma_{D^+ \rightarrow \tau^+ \nu_\tau}}{\Gamma_{D^+ \rightarrow \mu^+ \nu_\mu}} = 2.45 \pm 0.31$ , consistent with  $\mathcal{R}_{\tau/\mu}^{\text{SM}} = 2.66 \pm 0.01$

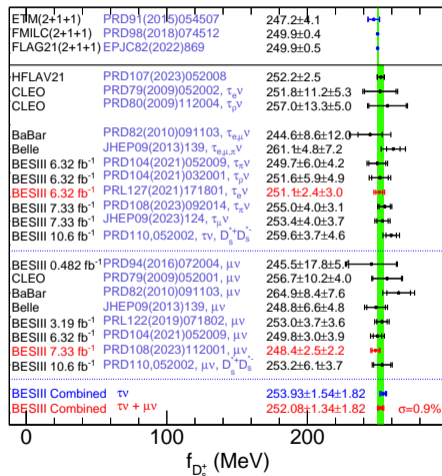
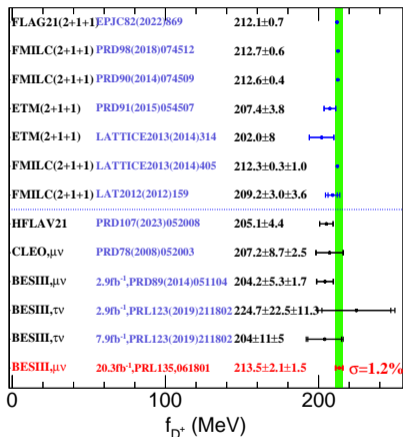
Measurement of  $D_s^+ \rightarrow \ell^+ \nu_\ell$ 

PRD110(2024)052002

$$\tau^+ \rightarrow \begin{cases} e^+ \nu_e \bar{\nu}_\tau \\ \mu^+ \nu_\mu \bar{\nu}_\tau \\ \pi^+ \bar{\nu}_\tau \\ \pi^+ \pi^0 \bar{\nu}_\tau \end{cases}$$

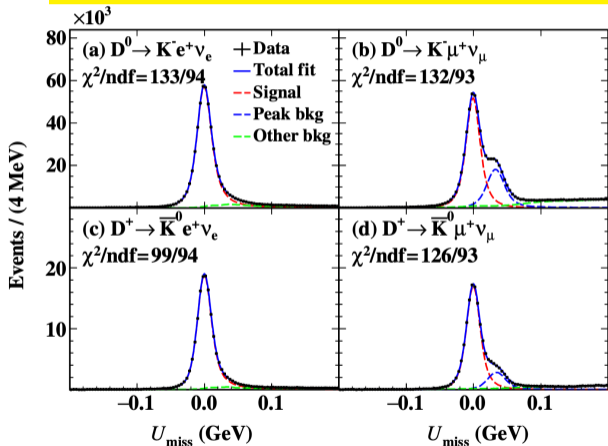


Reference	Data set (fb <sup>-1</sup> )	$B(\%)$	$f_{D_s^+}$ $D_s^+ \rightarrow \mu^+ \nu_\mu$	$ V_{cs} $	Stat
PRD 108, 112001(2023)	7.33 $D_s^\pm D_s^\mp$	$0.5294 \pm 0.0108 \pm 0.0085$	$248.4 \pm 2.5 \pm 2.2(\sigma = 1.4\%)$	$0.968 \pm 0.010 \pm 0.009(\sigma = 1.4\%)$	
PRD 110, 052002 (2024)	10.64 $D_s^{*\pm} D_s^\mp$	$0.547 \pm 0.026 \pm 0.016$	$246.5 \pm 5.9 \pm 3.6(\sigma = 2.8\%)$	$0.986 \pm 0.023 \pm 0.014(\sigma = 2.8\%)$	
			$D_s^+ \rightarrow \tau^+ \nu_\tau$		
PRL 127, 171801 (2021)	6.32 $D_s^\pm D_s^\mp$	$5.27 \pm 0.10 \pm 0.12$	$251.1 \pm 2.4 \pm 3.0(\sigma = 1.5\%)$	$0.978 \pm 0.009 \pm 0.012(\sigma = 1.5\%)$	$\tau^+ \rightarrow e^+ \nu_e \bar{\nu}_\tau$
PRD 104, 052009 (2021)	6.32 $D_s^\pm D_s^\mp$	$5.21 \pm 0.25 \pm 0.17$	$249.7 \pm 6.0 \pm 4.2(\sigma = 2.9\%)$	$0.972 \pm 0.023 \pm 0.016(\sigma = 2.9\%)$	$\tau^+ \rightarrow \pi^+ \bar{\nu}_\tau$
PRD 104, 032001 (2021)	6.32 $D_s^\pm D_s^\mp$	$5.29 \pm 0.25 \pm 0.20$	$251.6 \pm 5.9 \pm 4.9(\sigma = 3.0\%)$	$0.980 \pm 0.023 \pm 0.019(\sigma = 3.0\%)$	Simultaneous fit at various energy points
JHEP 09, 124 (2023)	7.33 $D_s^\pm D_s^\mp$	$5.37 \pm 0.17 \pm 0.15$	$253.4 \pm 4.0 \pm 3.7(\sigma = 2.2\%)$	$0.987 \pm 0.016 \pm 0.014(\sigma = 2.2\%)$	$\tau^+ \rightarrow \pi^+ \pi^0 \bar{\nu}_\tau$
PRD 108, 092014 (2023)	7.33 $D_s^\pm D_s^\mp$	$5.44 \pm 0.17 \pm 0.13$	$255.0 \pm 4.0 \pm 3.4(\sigma = 2.1\%)$	$0.993 \pm 0.015 \pm 0.013(\sigma = 2.1\%)$	$\tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau$
PRD 110, 052002 (2024)	10.64 $D_s^{*\pm} D_s^\mp$	$5.60 \pm 0.16 \pm 0.20$	$252.7 \pm 3.6 \pm 4.5(\sigma = 2.3\%)$	$1.011 \pm 0.014 \pm 0.018(\sigma = 2.3\%)$	$\tau^+ \rightarrow \mu^+ \bar{\nu}_\tau$ with BDT constrain the same BF $\tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau, e^+ \nu_e \bar{\nu}_\tau, \pi^+ \bar{\nu}_\tau, \pi^+ \pi^0 \bar{\nu}_\tau$

Comparison of  $f_{D^+}$  and  $f_{D_s^+}$ 

Precise measurements of  $D^0 \rightarrow K^- \ell^+ \nu_\ell$  and  $D^+ \rightarrow \bar{K}^0 \ell^+ \nu_\ell$ 

arXiv:2601.21196, 2601.21185, submitted to PRL



- Data:  $20.3 \text{ fb}^{-1} @ 3.773 \text{ GeV}$

- Improved measurement of BFs

$$\mathcal{B}(D^0 \rightarrow K^- e^+ \nu_e) = (3.527 \pm 0.005 \pm 0.016)\%$$

$$\mathcal{B}(D^0 \rightarrow K^- \mu^+ \nu_\mu) = (3.429 \pm 0.007 \pm 0.017)\%$$

$$\mathcal{B}(D^+ \rightarrow \bar{K}^0 e^+ \nu_e) = (8.918 \pm 0.025 \pm 0.050)\%$$

$$\mathcal{B}(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu) = (8.763 \pm 0.029 \pm 0.052)\%$$

- Most precision LFU test: Consistent with

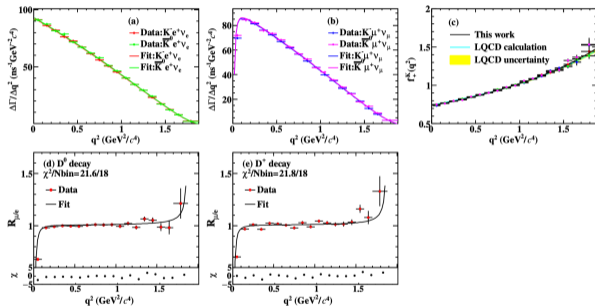
$$\mathcal{R}_{\text{SM}} = 0.975 \pm 0.001$$

$$\frac{\mathcal{B}(D^0 \rightarrow K^- \mu^+ \nu_\mu)}{\mathcal{B}(D^0 \rightarrow K^- e^+ \nu_e)} = 0.972 \pm 0.003 \pm 0.004$$

$$\frac{\mathcal{B}(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu)}{\mathcal{B}(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)} = 0.982 \pm 0.004 \pm 0.002$$

Precise measurements of  $D^0 \rightarrow K^- \ell^+ \nu_\ell$  and  $D^+ \rightarrow \bar{K}^0 \ell^+ \nu_\ell$ 

$$\frac{d\Gamma^\ell}{dq^2} = \frac{G_F^2 |V_{cs}|^2 |q| q^2}{96\pi^3 m_D^2} \left( \frac{q^2 - m_\ell^2}{q^2} \right)^2 \left[ \left( \frac{2q^2 + m_\ell^2}{2q^2} \right) |h_0(q^2)|^2 + \frac{3m_\ell^2}{2q^2} |h_t(q^2)|^2 \right], h_0(q^2) = \frac{2m_D |q|}{\sqrt{q^2}} f_+(q^2), h_t(q^2) = \frac{m_D^2 - m_K^2}{\sqrt{q^2}} f_0(q^2)$$



HFLAV23	PRD113(2026)012008	$0.7376 \pm 0.0034 \pm 0.0001$	
FLAG24	PRD113(2026)014508	$0.7430 \pm 0.0027$	
ETM	PRD96(2017)054514	$0.765 \pm 0.031$	
HPQCD	PRD107(2023)014510	$0.7441 \pm 0.0040$	
Fermilab and MILC	PRD107(2023)094516	$0.7452 \pm 0.0031$	
BaBar	$D^0 \rightarrow K^- e^+ \nu_e$ PRD76(2007)052005	$0.7263 \pm 0.0072 \pm 0.0092$	
Belle	$D \rightarrow \bar{K} e^+ \nu_e$ PRL97(2006)061804	$0.6944 \pm 0.0072 \pm 0.0216$	
CLEO-c	$D \rightarrow \bar{K} e^+ \nu_e$ PRD80(2009)032005	$0.7365 \pm 0.0041 \pm 0.0041$	
BESIII	$D \rightarrow K_L^0 e^+ \nu_e$ PRD92(2015)112008	$0.7478 \pm 0.0062 \pm 0.0113$	
BESIII	$D \rightarrow \bar{K}^0 \ell^+ \nu_\ell$ arXiv:2601.21196	$0.7355 \pm 0.0007 \pm 0.0014$	
Average		$0.7342 \pm 0.0007 \pm 0.0008$	

- $f_+^K(0) = 0.7355 \pm 0.0007_{\text{stat}} \pm 0.0014_{\text{syst}}; |V_{cs}| = 0.9608 \pm 0.0009_{\text{stat}} \pm 0.0019_{\text{syst}} \pm 0.0040_{\text{LQCD}}$
- Experimental uncertainties of  $f_+^K(0)$  and  $|V_{cs}|$ : 0.22%
- Additional uncertainty of the input  $f_+^K(0)$  calculated by LQCD: 0.42%

# Precise measurements of $D^0 \rightarrow K^- \ell^+ \nu_\ell$ and $D^+ \rightarrow \bar{K}^0 \ell^+ \nu_\ell$

- $\theta_W$  is the angle between the lepton momentum and the direction opposite to the  $D$ -meson momentum in the  $\ell \nu_\ell$  rest frame
- Forward-backward asymmetry:  $A_{\text{FB}}(q^2) = \frac{d\Gamma^\ell(\cos\theta_W > 0) - d\Gamma^\ell(\cos\theta_W < 0)}{d\Gamma^\ell(\cos\theta_W > 0) + d\Gamma^\ell(\cos\theta_W < 0)}$

- Theoretical expression:

$$A_{\text{FB}}(q^2) = \frac{3\mathcal{N}(q^2)}{2} \frac{1}{d\Gamma^\ell/dq^2} \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \frac{m_\ell^2}{q^2} \text{Re}(h_0(q^2)h_t(q^2))$$

- Overall forward-backward asymmetry

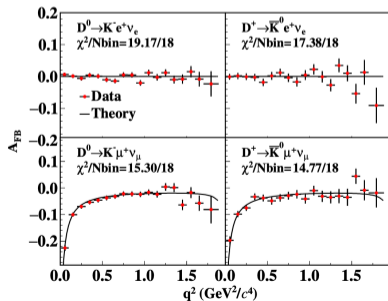
$$\langle A_{\text{FB}}^{K^- e^+ \nu_e} \rangle = (+0.3 \pm 1.7 \pm 1.7) \times 10^{-3}$$

$$\langle A_{\text{FB}}^{K^- \mu^+ \nu_\mu} \rangle = (-58.8 \pm 2.2 \pm 2.1) \times 10^{-3}$$

$$\langle A_{\text{FB}}^{\bar{K}^0 e^+ \nu_e} \rangle = (-0.9 \pm 2.9 \pm 1.8) \times 10^{-3}$$

$$\langle A_{\text{FB}}^{\bar{K}^0 \mu^+ \nu_\mu} \rangle = (-54.4 \pm 3.6 \pm 0.7) \times 10^{-3}$$

- Agree with  $\langle A_{\text{FB}}^e \rangle = 0$  and  $\langle A_{\text{FB}}^\mu \rangle = -0.055 \pm 0.002$



First Experimental Constraint on the Scalar Current in the  $D^{0(+)} \rightarrow \bar{K}\ell^+\nu_\ell$  Transition

- Corresponding effective Lagrangian:  $\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{cs}^* \sum_{\ell=e,\mu,\tau} \sum_i c_i^\ell \mathcal{O}_i^\ell + \text{H.C.}$

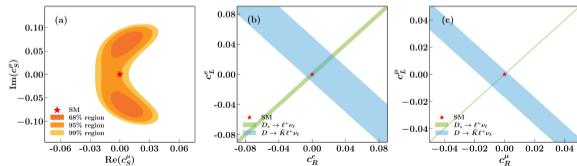
SM:  $\mathcal{O}_{\text{SM}}^\ell = (\bar{s}\gamma_\mu P_L c)(\bar{\nu}_\ell \gamma^\mu P_L \ell)$  with coefficient  $c_{\text{SM}}^\ell = 1$

NP: Potential right(left)-handed scalar current  $\mathcal{O}_{R(L)}^\ell = (\bar{s}P_{R(L)}c)(\bar{\nu}_\ell P_{R(L)}\ell)$  with complex Wilson coefficient  $c_{R(L)}^\ell$

- Simultaneous fit to the measured partial decay rates and forward-backward asymmetries to constraints on the right- and left-handed components of the scalar current with input the BF of  $D_s^+ \rightarrow \ell^+\nu_\ell$

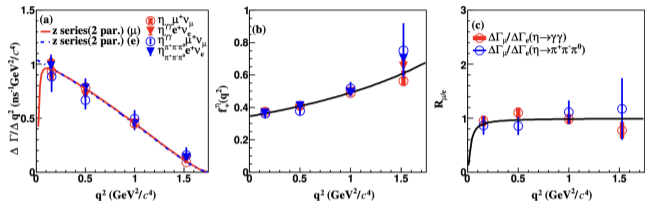
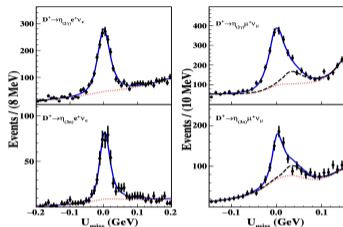
- $h_t(q^2) = \left(1 + c_S^\ell \frac{q^2}{m_\ell(m_s - m_c)}\right) \frac{m_D^2 - m_K^2}{\sqrt{q^2}} f_0(q^2)$  and

$$\mathcal{B}(D_s^+ \rightarrow \ell^+\nu_\ell) = \tau_{D_s} \frac{m_{D_s}}{8\pi} f_{D_s}^2 \left(1 - \frac{m_\ell^2}{m_{D_s}^2}\right)^2 G_F^2 \times |V_{cs}|^2 m_\ell^2 \left|1 - c_P^\ell \frac{m_{D_s}^2}{(m_c + m_s)m_\ell}\right|^2$$



Variable	With SC	Without SC
$f_+(0) V_{cs} $	$0.7167 \pm 0.008 \pm 0.014$	$0.7160 \pm 0.007 \pm 0.014$
$r_1$	$-2.28 \pm 0.04 \pm 0.02$	$-2.32 \pm 0.02 \pm 0.02$
$ c_S^e $	$0.02 \pm 0.02 \pm 0.02$	—
$\text{Re}(c_S^\mu)$	$0.007 \pm 0.008 \pm 0.006$	—
$\text{Im}(c_S^\mu)$	$\pm 0.070 \pm 0.013 \pm 0.010$	—
$\chi^2/\text{ndf}$	132.9/139	138.5/142

$$D^+ \rightarrow \eta \ell^+ \nu_\ell$$



CLFQM	EPJCM6(2026)363	$0.558^{+0.019}_{-0.025}$	
RQM	PRD101(2020)013004	0.547	
CCQM <sup>1</sup>	Front.Phys.14(2019)64401	$0.36 \pm 0.05$	
CCQM <sup>2</sup>	PRD98(2018)114031	$0.67 \pm 0.10$	
LCSR <sup>1</sup>	PRD112(2025)076001	$0.336^{+0.038}_{-0.039}$	
LCSR <sup>2</sup>	PRD88(2013)034023	$0.552 \pm 0.051$	
LCSR <sup>3</sup>	JHEP11(2015)138	$0.429^{+0.165}_{-0.141}$	
LCSR <sup>4</sup>	JHEP10(2025)025	$0.38 \pm 0.13$	
LCSR <sup>5</sup>	PRD113(2026)053005	$0.370^{+0.031}_{-0.024}$	
LCSR <sup>6</sup>	EPJCM4(2024)15	$0.329^{+0.021}_{-0.015}$	
LFQM	J.Phys.G.39(2012)025005	0.71	
Average		$0.343 \pm 0.013$	
CLEO-c	PRD84(2011)032001	$0.382 \pm 0.027 \pm 0.005$	
BESIII	arXiv:2506.02521	$0.347 \pm 0.009 \pm 0.005$	
Average		$0.351 \pm 0.009 \pm 0.005$	

- arXiv:2506.02521, submitted to JHEP

- Data:  $20.3 \text{ fb}^{-1} @ 3.773 \text{ GeV}$

- **Precisions of BFs and FF are improved by  $\sim 2 \times$**

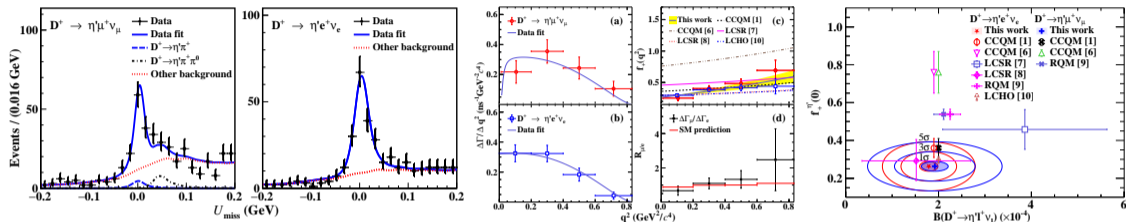
$$\mathcal{B}(D^+ \rightarrow \eta \mu^+ \nu_\mu) = (9.08 \pm 0.35 \pm 0.23) \times 10^{-4}$$

$$\mathcal{B}(D^+ \rightarrow \eta e^+ \nu_e) = (9.75 \pm 0.29 \pm 0.28) \times 10^{-4}$$

$$f_+^\eta(0) = 0.345 \pm 0.008 \pm 0.003$$

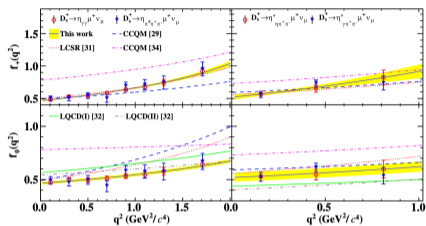
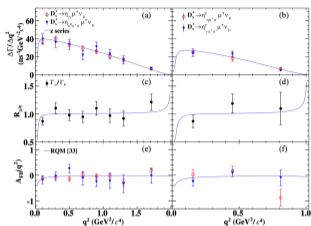
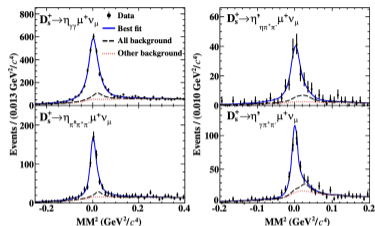
- **LFU test:**  $\mathcal{R}_{\mu/e}^\eta = 0.93 \pm 0.05 \pm 0.02 \implies$  Consistent with SM

# First study of $D^+ \rightarrow \eta' \ell^+ \nu_\ell$ decay dynamics



- Data:  $20.3 \text{ fb}^{-1} @ 3.773 \text{ GeV}$  **PRL134(2025)111801**
- **First observation of  $D^+ \rightarrow \eta' \mu^+ \nu_\mu$  with significance of  $8.6\sigma$**   
 $\mathcal{B}(D^+ \rightarrow \eta' \mu^+ \nu_\mu) = (1.92 \pm 0.28 \pm 0.08) \times 10^{-4}$ ;  $\mathcal{B}(D^+ \rightarrow \eta' e^+ \nu_e) = (1.79 \pm 0.19 \pm 0.07) \times 10^{-4}$
- **First extraction of the FF of  $D^+ \rightarrow \eta' \ell^+ \nu_\ell$ :  $f_+^{\eta'}(0) = 0.263 \pm 0.025 \pm 0.006$**
- **LFU test:  $\mathcal{R}_{\mu/e}^{\eta'} = 1.07 \pm 0.19 \pm 0.03$**
- **$\eta - \eta'$  mixing angle:  $\phi_P = (39.8 \pm 0.8 \pm 0.3)^\circ$  ( $\cot^4 \phi_P = \frac{\Gamma_{D_s^+ \rightarrow \eta' \ell^+ \nu_\ell} / \Gamma_{D_s^+ \rightarrow \eta \ell^+ \nu_\ell}}{\Gamma_{D^+ \rightarrow \eta' \ell^+ \nu_\ell} / \Gamma_{D^+ \rightarrow \eta \ell^+ \nu_\ell}}$ )**

$$D_s^+ \rightarrow \eta^{(\prime)} \mu^+ \nu_\mu$$



• Data:  $7.33 \text{ fb}^{-1}$  @ 4.128-4.226 GeV **PRL132(2024)091802**

• Precision of BFs are improved by a factor of  $\sim 6$

$$\mathcal{B}(D_s^+ \rightarrow \eta \mu^+ \nu_\mu) = (2.235 \pm 0.051 \pm 0.052)\%$$

$$\mathcal{B}(D_s^+ \rightarrow \eta' \mu^+ \nu_\mu) = (0.801 \pm 0.055 \pm 0.028)\%$$

• First extraction of the FFs via semimuonic decays

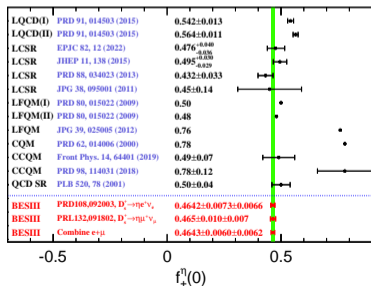
$$f_+^\eta(0) = 0.465 \pm 0.010 \pm 0.007; f_+^{\eta'}(0) = 0.518 \pm 0.038 \pm 0.012$$

• Most precision test of lepton flavor universality in  $D_s$  sector

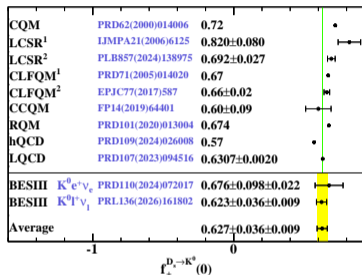
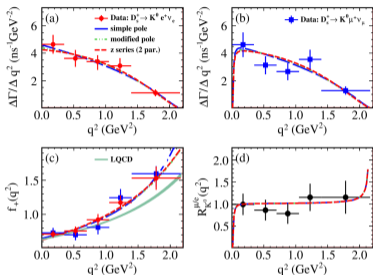
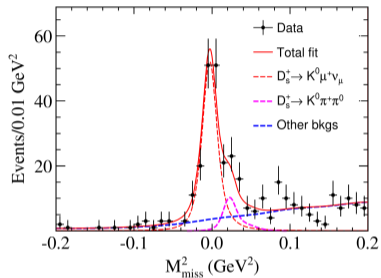
$$\mathcal{R}_{\mu/e}^\eta = 0.991 \pm 0.029 \pm 0.016; \mathcal{R}_{\mu/e}^{\eta'} = 0.988 \pm 0.082 \pm 0.031$$

• First extraction of the forward-backward asymmetry parameters

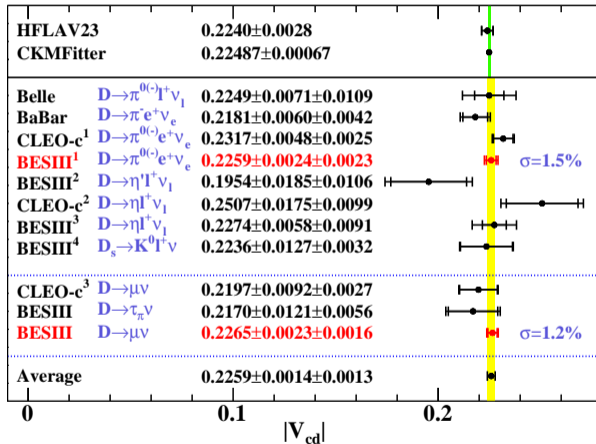
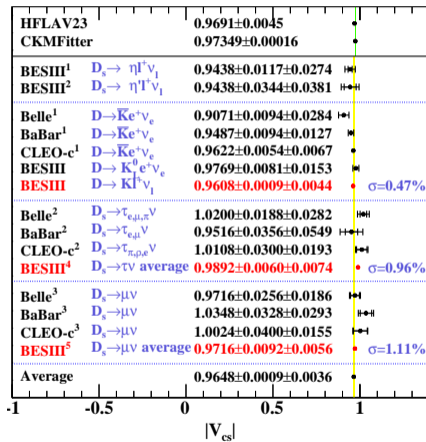
$$\langle A_{\text{FB}}^\eta \rangle = -0.059 \pm 0.031 \pm 0.005; \langle A_{\text{FB}}^{\eta'} \rangle = -0.064 \pm 0.079 \pm 0.006$$



# First Measurement of the $D_s^+ \rightarrow K^0 \mu^+ \nu_\mu$ Decay



- 7.33 fb<sup>-1</sup>@4.128-2.226 GeV **PRL136(2026)161802**
- **First observation of  $D_s^+ \rightarrow K^0 \mu^+ \nu_\mu$** :  $\mathcal{B}(D_s^+ \rightarrow K^0 \mu^+ \nu_\mu) = (2.89 \pm 0.27 \pm 0.12) \times 10^{-3}$
- **Improve measurement of FF combined with  $D_s^+ \rightarrow K^0 \ell^+ \nu_\ell$** :  $f_+^{K^0}(0) = 0.623 \pm 0.036 \pm 0.011$
- **LFU test**:  $\mathcal{R}_{\mu/e}^{K^0} = 0.97 \pm 0.12 \pm 0.04 \implies$  Consistent with  $\mathcal{R}_{\mu/e}^{\text{SM}} = 0.98099(10)(500)$

Comparison of  $|V_{cs}|$  and  $|V_{cd}|$ 

# Summary

- (Semi)leptonic decays of charm mesons are important for determining CKM matrix elements, calibrating LQCD, testing LFU, *et al.*;
  - Precisions of  $|V_{cd}|$  and  $|V_{cs}|$  have been reduced to 1.2% and 0.5%, respectively;
  - Precisions of  $f_{D^+}$ ,  $f_{D_s^+}$  and  $f_+^{D \rightarrow \bar{K}}(0)$  have been reduced to 1.2%, 0.9%, and 0.21%, respectively;
  - No evidence of LFU violation is found in charm decay
- More precision measurements ( $D \rightarrow \pi \ell^+ \nu_\ell \dots$ ) and searching for rare semileptonic decays will be presented
- Additional  $3 \text{ fb}^{-1}$  data @4.178 GeV in future [CPC44(2020)040001] will further improve the precisions in  $D_s$  sector.
- Review of experimental studies of charmed meson decays at BESIII, arXiv:2604.20644

## Thank you