

# Studies of $1^{-+}$ states at BESIII

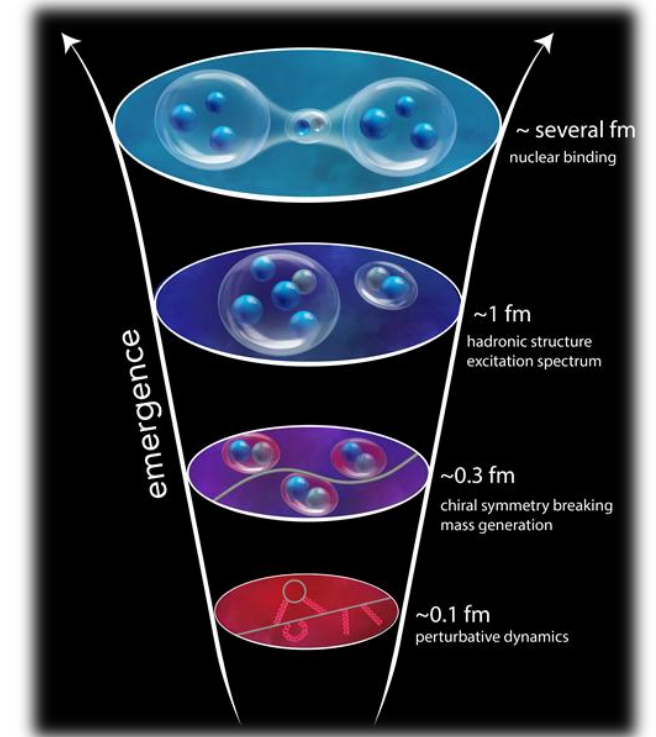
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2026 轻强子专题研讨会 2026.05.14-18, 商丘

# Mysterious gluons

- How does QCD give rise to hadrons?
  - What is the origin of confinement?
  - How is the mass generated in QCD?
- Role of gluons in hadrons
  - How to access soft gluon dynamics
- Key thing to search for: hadrons explicitly manifest the **gluonic degrees of freedom**
  - Gluonic excitations: **Glueballs and hybrids**, which provide critical information on the strong force and QCD vacuum



Eur.Phys.J.A 60 (2024) , 173

# Light hadrons with exotic quantum numbers

- Finding unambiguous signature for exotics

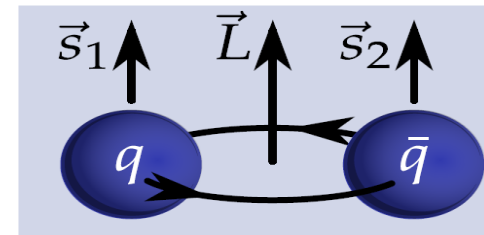
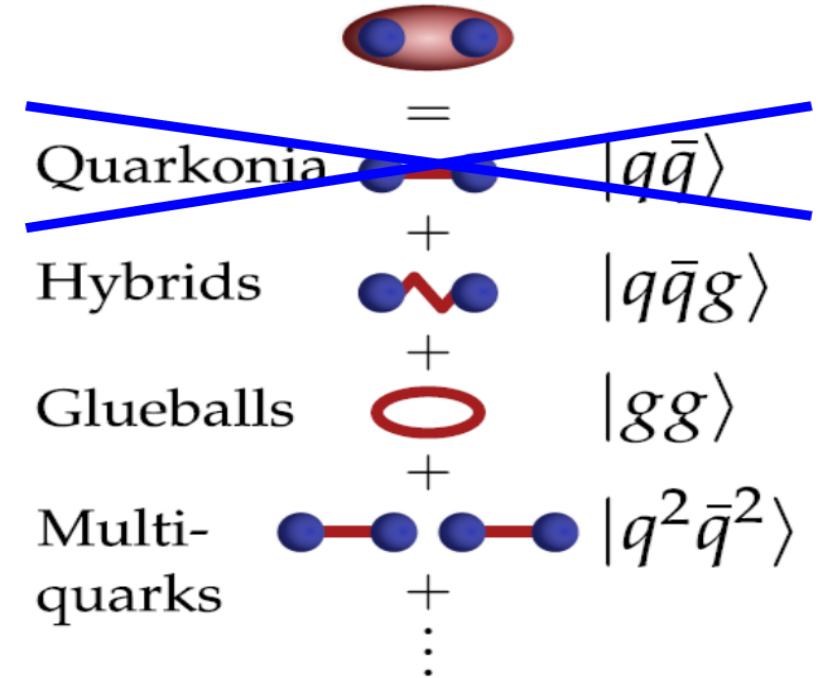
- **Efforts concentrate on Spin-exotic**

- **Forbidden for  $q\bar{q}$ :**

$$J^{PC} = 0^{--}, \text{even}^{+-}, \text{odd}^{-+}$$

## Experiments:

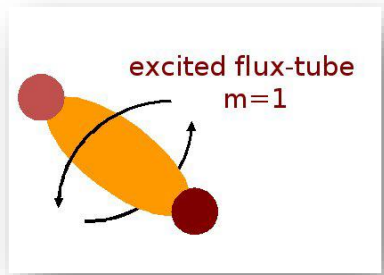
- **Hadroproduction:** GAMS, VES, E852, COMPASS, [AMBER](#)
- **$p\bar{p}$  annihilation:** Crystal Barrel, OBELIX, [PANDA](#)
- **Photoproduction:** [GlueX\(2017-\)](#), CLAS



$$\vec{J} = \vec{L} + \vec{S} \quad \mathbf{P} = (-1)^{L+1} \quad \mathbf{C} = (-1)^{L+S}$$

Allowed  $J^{PC}$ :  $0^{-+}, 0^{++}, 1^{--}, 1^{+-}, 2^{++}, \dots$

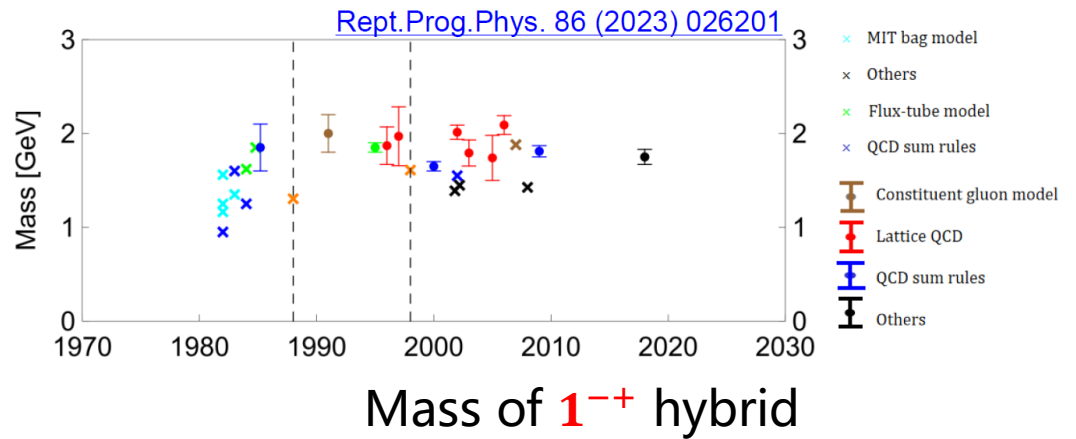
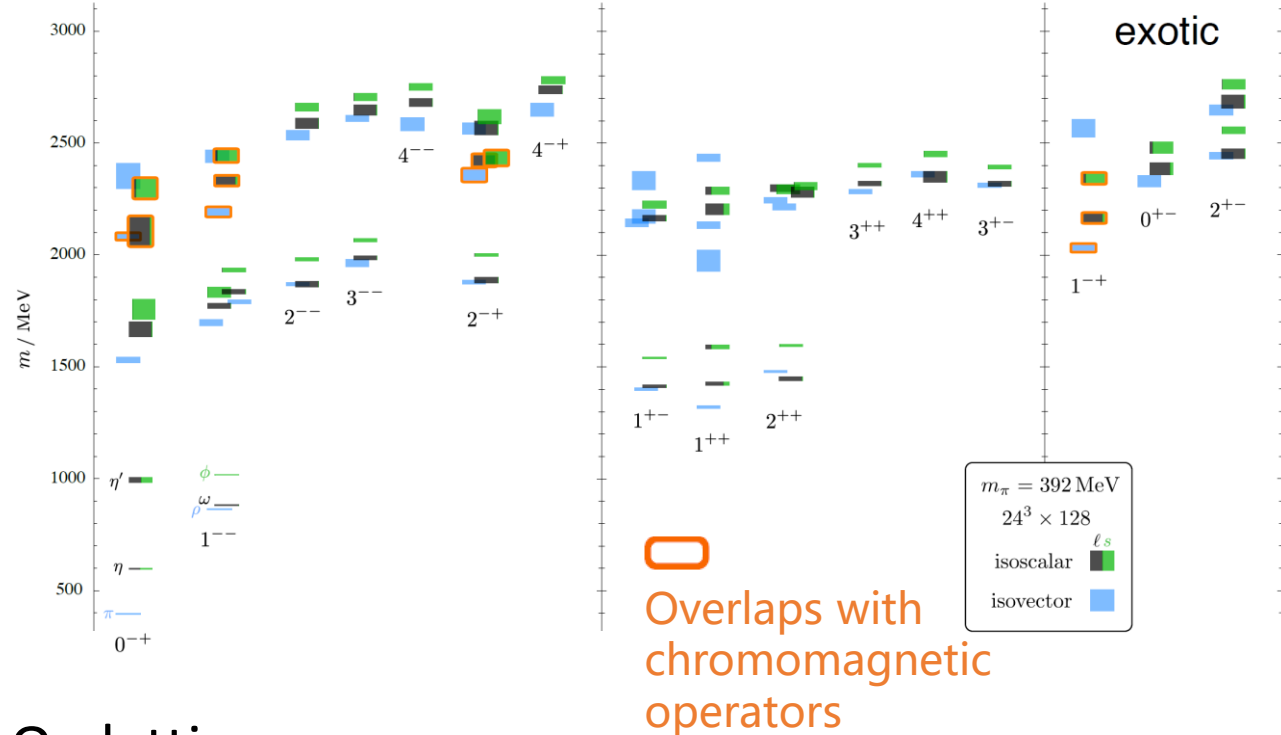
# Predictions



## “Constituent gluon”

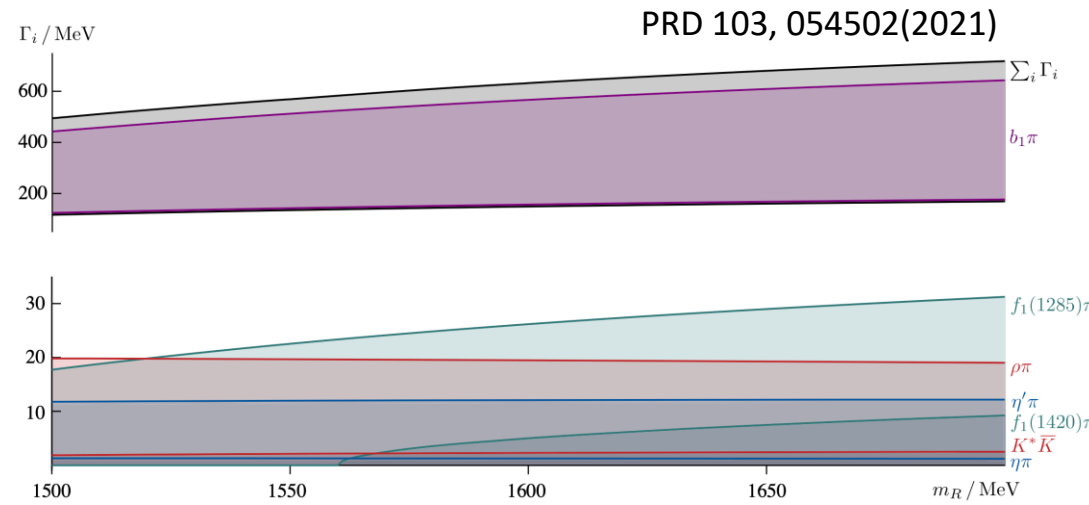
- $(J^{PC})_g = 1^{+-}$
- $M_g \sim 1.3 \text{ GeV}$

PRD 88 094505(2013)



On lattice,

- Meson excitations similar to quark model
- Hybrid supermultiplet:  $0^{-+}$ ,  $1^{--}$ ,  $2^{-+}$ ,  $1^{-+}$
- Lightest spin-exotic state in LQCD:  $1^{-+}$  hybrid

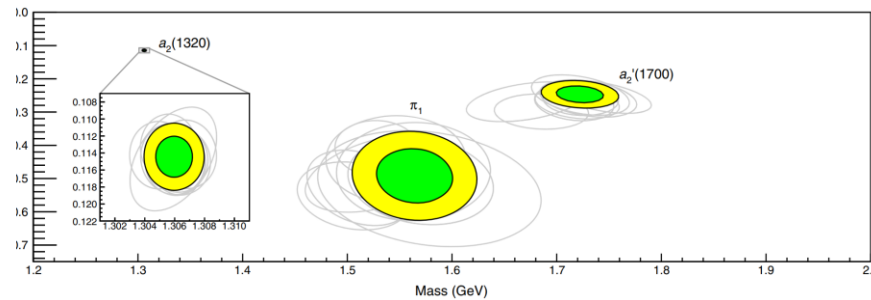
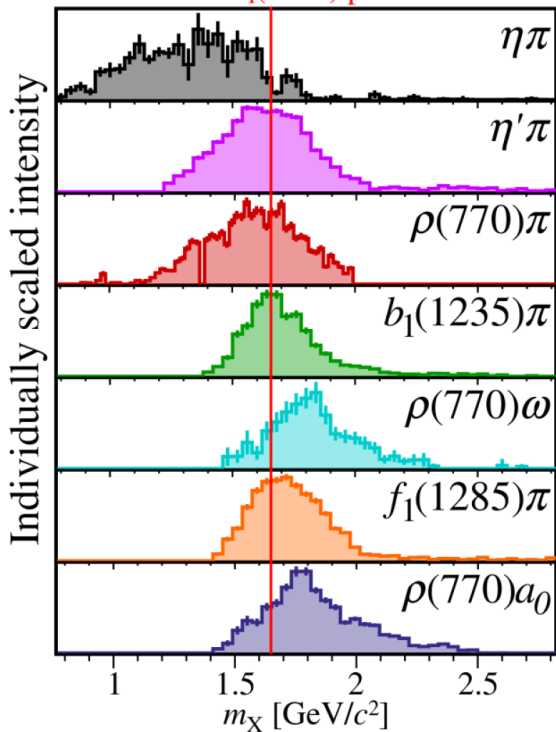


# Spin-exotic mesons

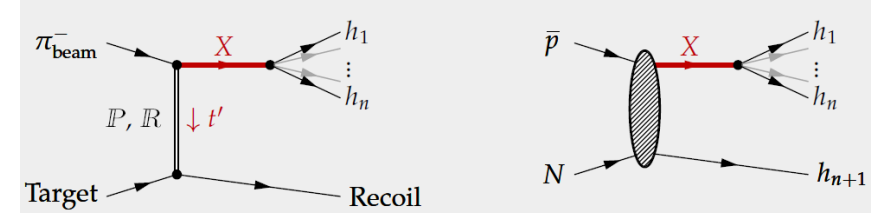
- Candidates over 3 decades
  - $\pi_1(1400)$ ,  $\pi_1(1600)$ ,  $\pi_1(2015)$  (needs confirmation), all isovectors

Spin-exotic  $J^{PC}=1^{-+}$  waves at COMPASS preliminary

Nominal  $\pi_1(1600)$  position



[PRL 122, 042002 (2019), EPJ C 81, 1056 (2021)]



Review: PRC 82, 025208 (2010), PPNP 82, 21 (2015), EPJC 83 (2023) 1125

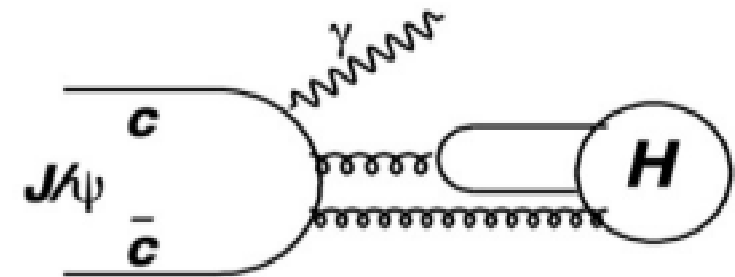
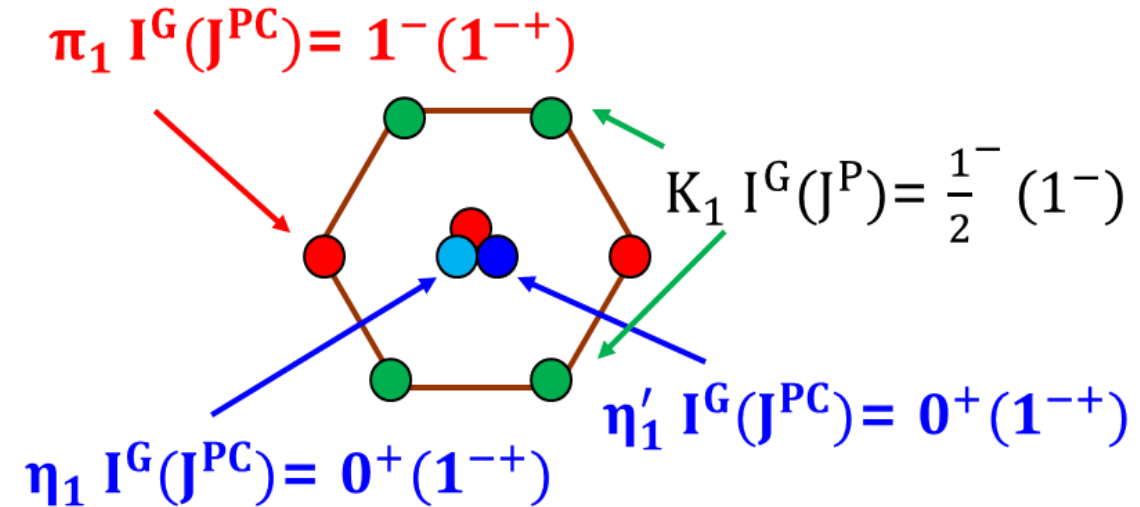
|               | Decay mode | Reaction   | Experiment                                  |
|---------------|------------|--|---|
| $\pi_1(1400)$ | $\eta\pi$  | $\pi^-p \rightarrow \pi^-\eta p$<br>$\pi^-p \rightarrow \pi^0\eta n$<br>$\pi^-p \rightarrow \pi^-\eta p$<br>$\pi^-p \rightarrow \pi^0\eta n$<br>$\bar{p}n \rightarrow \pi^-\pi^0\eta$<br>$\bar{p}p \rightarrow \pi^0\pi^0\eta$ | GAMS<br>KEK<br>E852<br>E852<br>CBAR<br>CBAR |
|               | $\rho\pi$  | $\bar{p}p \rightarrow 2\pi^+2\pi^-$  | Obelix                                      |
| $\pi_1(1600)$ | $\eta'\pi$ | $\pi^-Be \rightarrow \eta'\pi^-\pi^0Be$<br>$\pi^-p \rightarrow \pi^-\eta'p$  | VES<br>E852                                 |
|               | $b_1\pi$   | $\pi^-Be \rightarrow \omega\pi^-\pi^0Be$<br>$\bar{p}p \rightarrow \omega\pi^+\pi^-\pi^0$<br>$\pi^-p \rightarrow \omega\pi^-\pi^0p$   | VES<br>CBAR<br>E852                         |
|               | $\rho\pi$  | $\pi^-Pb \rightarrow \pi^+\pi^-\pi^-X$<br>$\pi^-p \rightarrow \pi^+\pi^-\pi^-p$  | COMPASS<br>E852                             |
|               | $f_1\pi$   | $\pi^-p \rightarrow \rho\eta\pi^+\pi^-\pi^-$<br>$\pi^-A \rightarrow \eta\pi^+\pi^-\pi^-A$  | E852<br>VES                                 |
| $\pi_1(2015)$ | $f_1\pi$   | $\pi^-p \rightarrow \omega\pi^-\pi^0p$   | E852  |
|               | $b_1\pi$   | $\pi^-p \rightarrow \rho\eta\pi^+\pi^-\pi^-$   |   |

# $1^{-+}$ Hybrids

- **Isoscalar  $1^{-+}$**  is critical to establish the hybrid nonet
  - Can be produced in the gluon-rich charmonium decays
  - Can decay to  $\eta\eta'$  in P-wave

PRD 83,014021 (2011), PRD 83,014006 (2011), EPJ P135, 945(2020)

→ Search for  $\eta_1 (1^{-+})$  in  $J/\psi \rightarrow \gamma\eta\eta'$



$$\Gamma(J/\psi \rightarrow \gamma H) \sim O(\alpha\alpha_s^3)$$

# Observation of An Exotic $1^{-+}$ Isoscalar State $\eta_1(1855)$

PRL 129 192002(2022) , PRD 106 072012(2022)

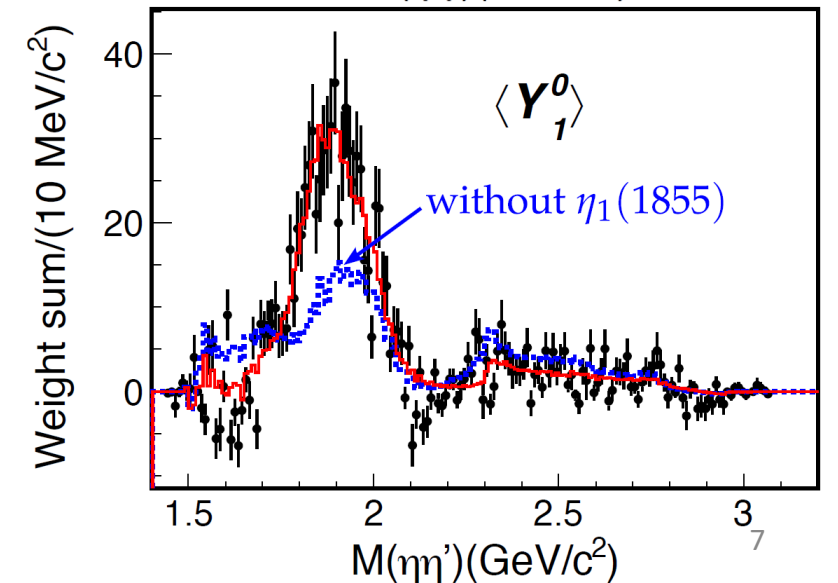
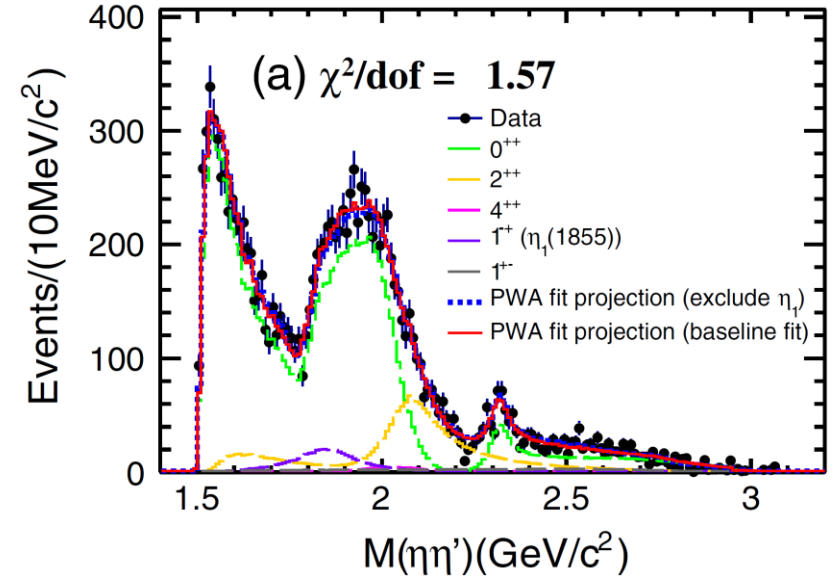
- An isoscalar  $1^{-+}$  ,  $\eta_1(1855)$ , has been observed in  $J/\psi \rightarrow \gamma\eta\eta'$  ( $>19\sigma$ )

$$M = (1855 \pm 9_{-1}^{+6}) \text{ MeV}/c^2, \Gamma = (188 \pm 18_{-8}^{+3}) \text{ MeV}/c^2$$

$$B(J/\psi \rightarrow \gamma\eta_1(1855) \rightarrow \gamma\eta\eta') = (2.70 \pm 0.41_{-0.35}^{+0.16}) \times 10^{-6}$$

- Mass consistent with hybrid on LQCD

- $\eta\eta'$  in P-waves uniquely indicates  $1^{-+}$  exotic quantum numbers



# Observation of An Exotic $1^-+$ Isoscalar State $\eta_1(1855)$

PRL 129 192002(2022) , PRD 106 072012(2022)

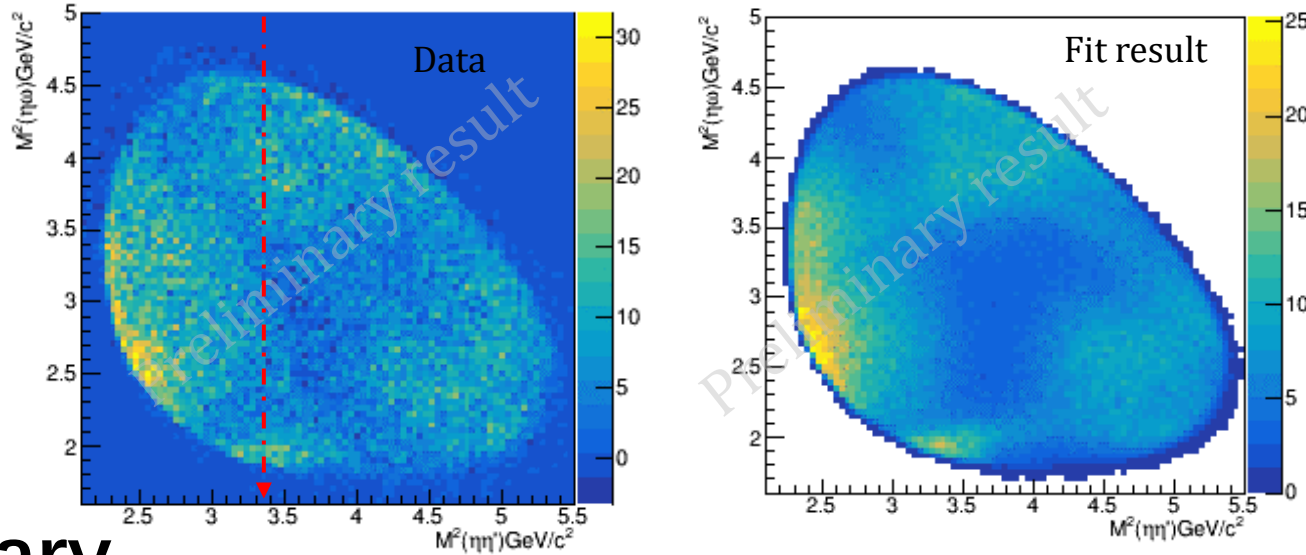
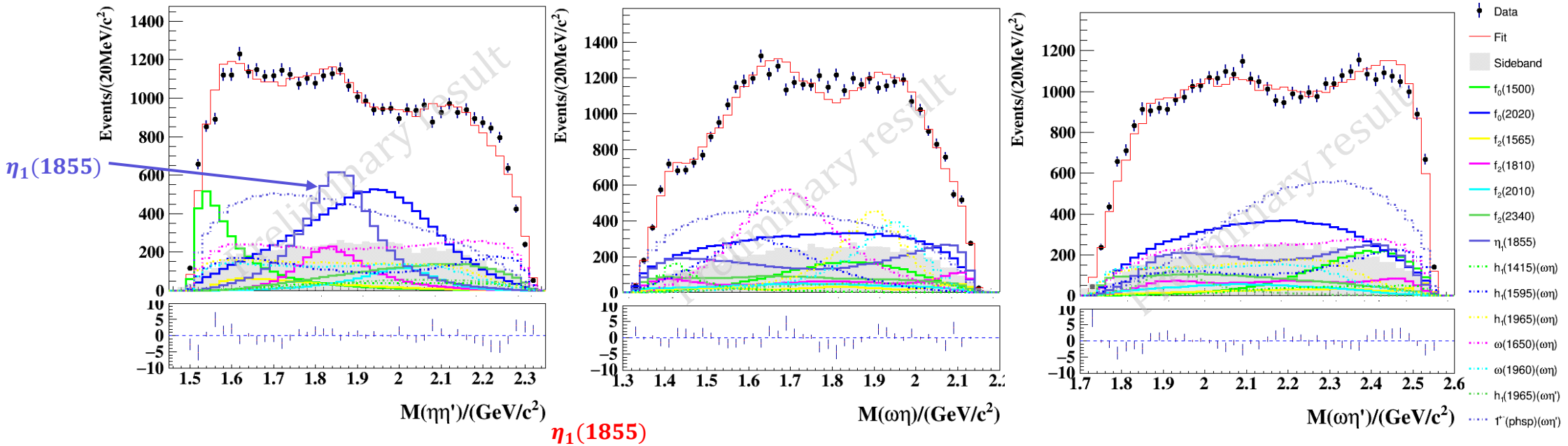
- Inspired many interpretations:  
Hybrid/ $K\bar{K}_1$  Molecule/Tetraquark?

NPA 1047 122874(2024); Rept.Prog.Phys. 86 (2023) 026201;  
PRD 107 (2023) 7, 074028; SCPMA 65 (2022) 6, 261011;  
CPC 46 , 051001(2022); CPL 39, 051201 (2022);  
PLB 834, 137478(2022); PRD 106 , 074003(2022); PRD 106,  
036005(2022) ;...

- **Opens a new direction** to completing the picture of spin-exotics
  - As a “**recent achievements and highlights**” in hadron spectroscopy in the NuPECC LRP
  - 50 years of QCD: Exotic mesons, “observation of an  $\eta_1(1855)$  state could be **a breakthrough**” [EPJ.C 83 (2023) 1125]



# PWA results of $J/\psi \rightarrow \omega\eta\eta'$



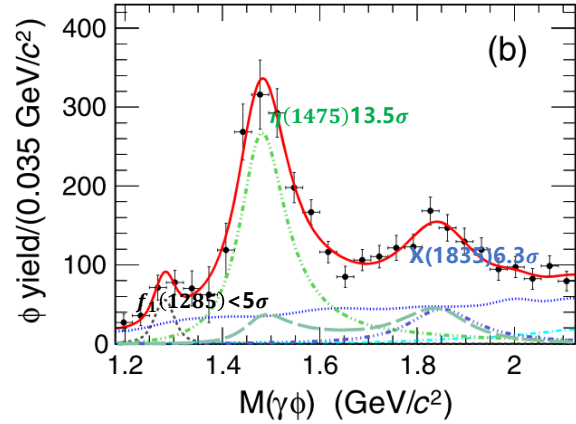
# PWA results of $J/\psi \rightarrow \omega\eta\eta'$

| Resonance      | $J^{PC}$ | Decay mode    | Sig.( $\sigma$ ) | Br   |
|----------------|----------|---------------|------------------|--|
| $f_0(1500)$    | $0^{++}$ | $\eta\eta'$   | 14.5             | $(4.40 \pm 0.08_{-2.21}^{+2.89}) \times 10^{-5}$                   |
| $f_0(2020)$    | $0^{++}$ | $\eta\eta'$   | 21.4             | $(2.01 \pm 0.02_{-1.07}^{+0.47}) \times 10^{-4}$                   |
| $f_2(1565)$    | $2^{++}$ | $\eta\eta'$   | 8.6              | $(1.71 \pm 0.05_{-0.77}^{+0.90}) \times 10^{-5}$                   |
| $f_2(1810)$    | $2^{++}$ | $\eta\eta'$   | 12.4             | $(4.03 \pm 0.08_{-0.96}^{+3.84}) \times 10^{-5}$                   |
| $f_2(2010)$    | $2^{++}$ | $\eta\eta'$   | 6.1              | $(2.34 \pm 0.06_{-1.33}^{+3.69}) \times 10^{-5}$                   |
| $f_2(2340)$    | $2^{++}$ | $\eta\eta'$   | 8.4              | $(5.32 \pm 0.10_{-2.98}^{+2.20}) \times 10^{-5}$                   |
| $\eta_1(1855)$ | $1^{-+}$ | $\eta\eta'$   | <b>23.7</b>      | <b><math>(1.15 \pm 0.01_{-0.45}^{+0.10}) \times 10^{-4}</math></b> |
| $h_1(1415)$    | $1^{+-}$ | $\omega\eta$  | 16.7             | $(2.09 \pm 0.06_{-0.72}^{+0.60}) \times 10^{-5}$                   |
| $h_1(1595)$    | $1^{+-}$ | $\omega\eta$  | 16.3             | $(7.28 \pm 0.10_{-3.16}^{+5.93}) \times 10^{-5}$                   |
| $h_1(1965)$    | $1^{+-}$ | $\omega\eta$  | 19.7             | $(7.43 \pm 0.10_{-3.13}^{+1.52}) \times 10^{-5}$                   |
| $\omega(1650)$ | $1^{--}$ | $\omega\eta$  | 18.8             | $(1.59 \pm 0.02_{-0.27}^{+0.34}) \times 10^{-4}$                   |
| $\omega(1960)$ | $1^{--}$ | $\omega\eta$  | 20.0             | $(7.48 \pm 0.11_{-2.78}^{+1.43}) \times 10^{-5}$                   |
| $h_1(1965)$    | $1^{+-}$ | $\omega\eta'$ | 14.6             | $(2.27 \pm 0.06_{-0.37}^{+1.04}) \times 10^{-5}$                   |
| $1^{+-}(phsp)$ | $1^{+-}$ | $\omega\eta'$ | 16.6             | $(2.15 \pm 0.02_{-0.82}^{+0.35}) \times 10^{-4}$                   |

# $J/\psi \rightarrow \gamma\gamma\phi$ , a $s\bar{s}$ flavor filter

BESIII PhysRevD.111.052011(2025)

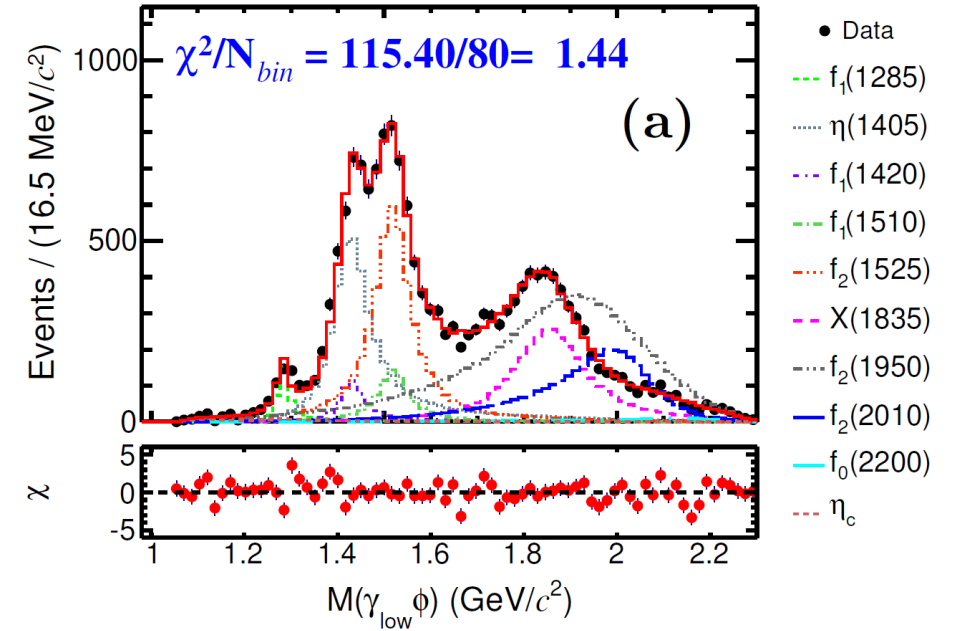
PR D97 051101 (2018)



Amplitude analysis with ML techniques for background subtraction



← Fit to mass spectrum

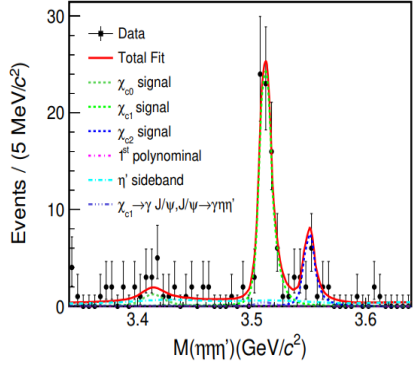


From the amplitude analysis,

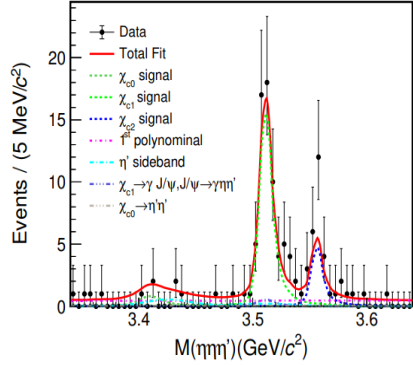
- $\eta(1405)$  is observed, while  $\eta(1475)$  can not be excluded
- $X(1835) \rightarrow \gamma\phi$  suggests its assignment of  $\eta'$  excitation
- $\eta_c \rightarrow \gamma\phi$  are observed. The very first radiative decay mode of  $\eta_c$
- Observation of  $f_2(1950)$  and  $f_0(2200) \rightarrow \gamma\phi$  unfavored their glueball interpretations [PRD 108, 014023, Sci.China Phys.Mech.Astron. 67 (2024) 11, 111012]
- **No evidence of  $X(2370)/\eta_1(1855)$ , well consistent with the predictions for glueball/hybrid** [PRD 107, 114020, NPA 1037, 122683]

# Search for $\eta_1$ in $\chi_{c1} \rightarrow \eta\eta\eta'$

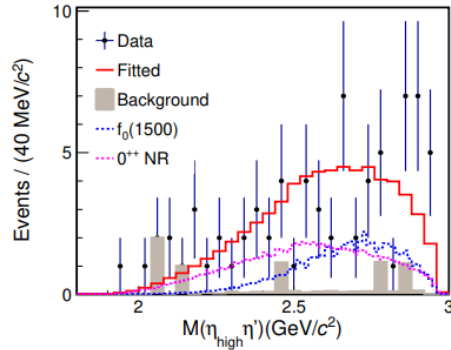
BESIII CPC 49, 10 (2025)



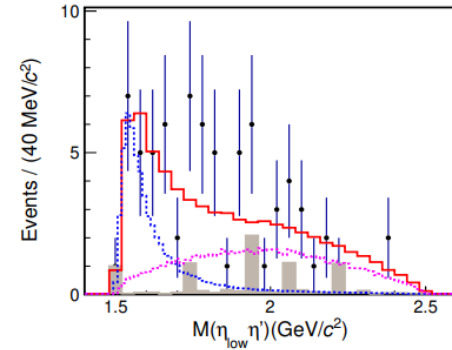
(a)



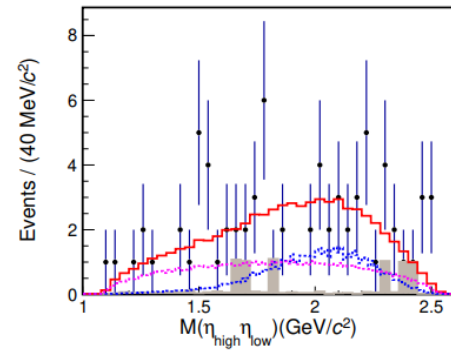
(b)



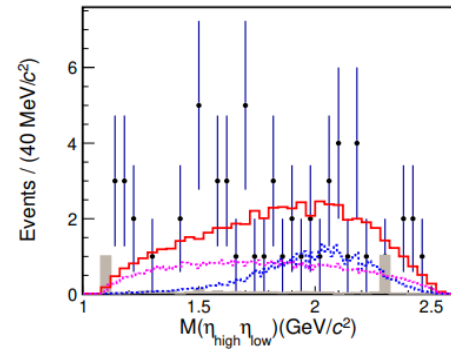
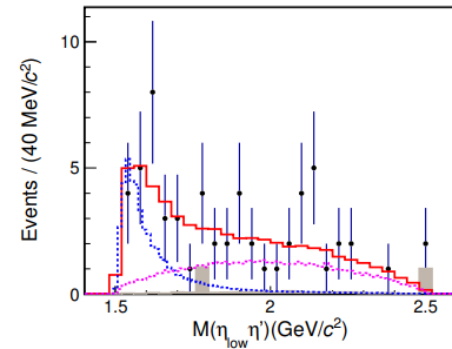
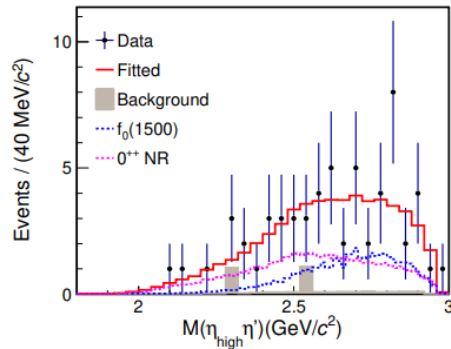
(a)



(b)



(c)



(f)

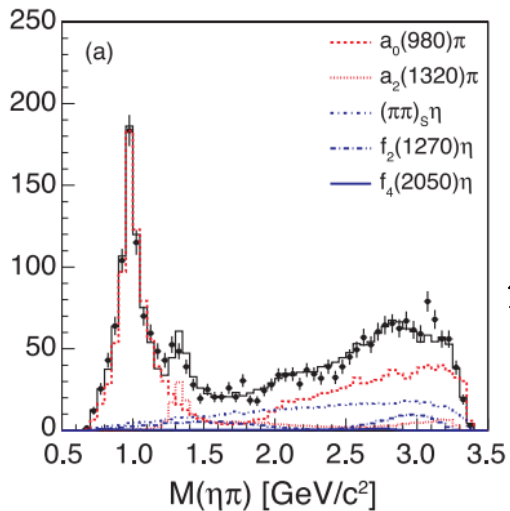
$$\mathcal{B}(\chi_{c1} \rightarrow \eta\eta\eta') = (1.39 \pm 0.13(\text{stat.}) \pm 0.09(\text{sys.})) \times 10^{-4}$$

$$\mathcal{B}(\chi_{c1} \rightarrow \eta_1(1855)\eta) \cdot \mathcal{B}(\eta_1(1855) \rightarrow \eta\eta') < 9.79 \times 10^{-5}$$

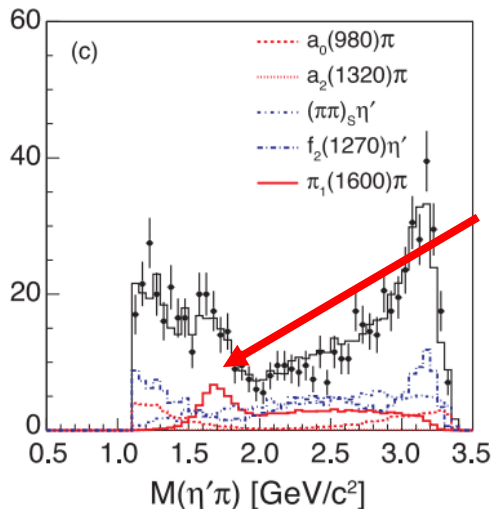
# Studies of $\pi_1$ in $\chi_{c1} \rightarrow \pi^+ \pi^- \eta^{(\prime)}$

PR D84 112009 (2011)

$2.6 \times 10^7$   $\psi(3686)$ @CLEO – c



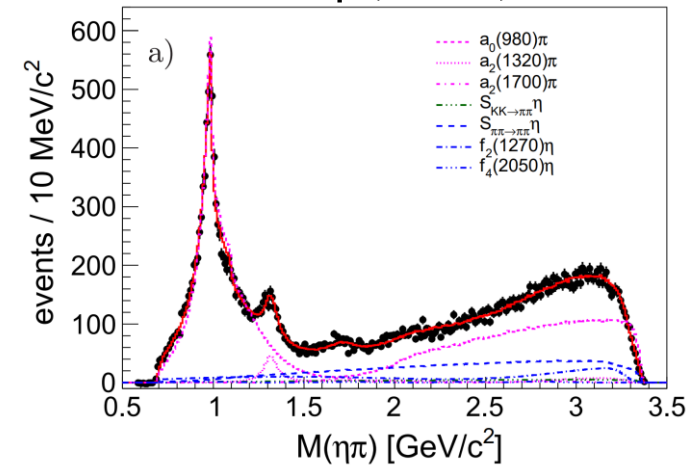
No evidence of  
 $\pi_1 \rightarrow \eta\pi$



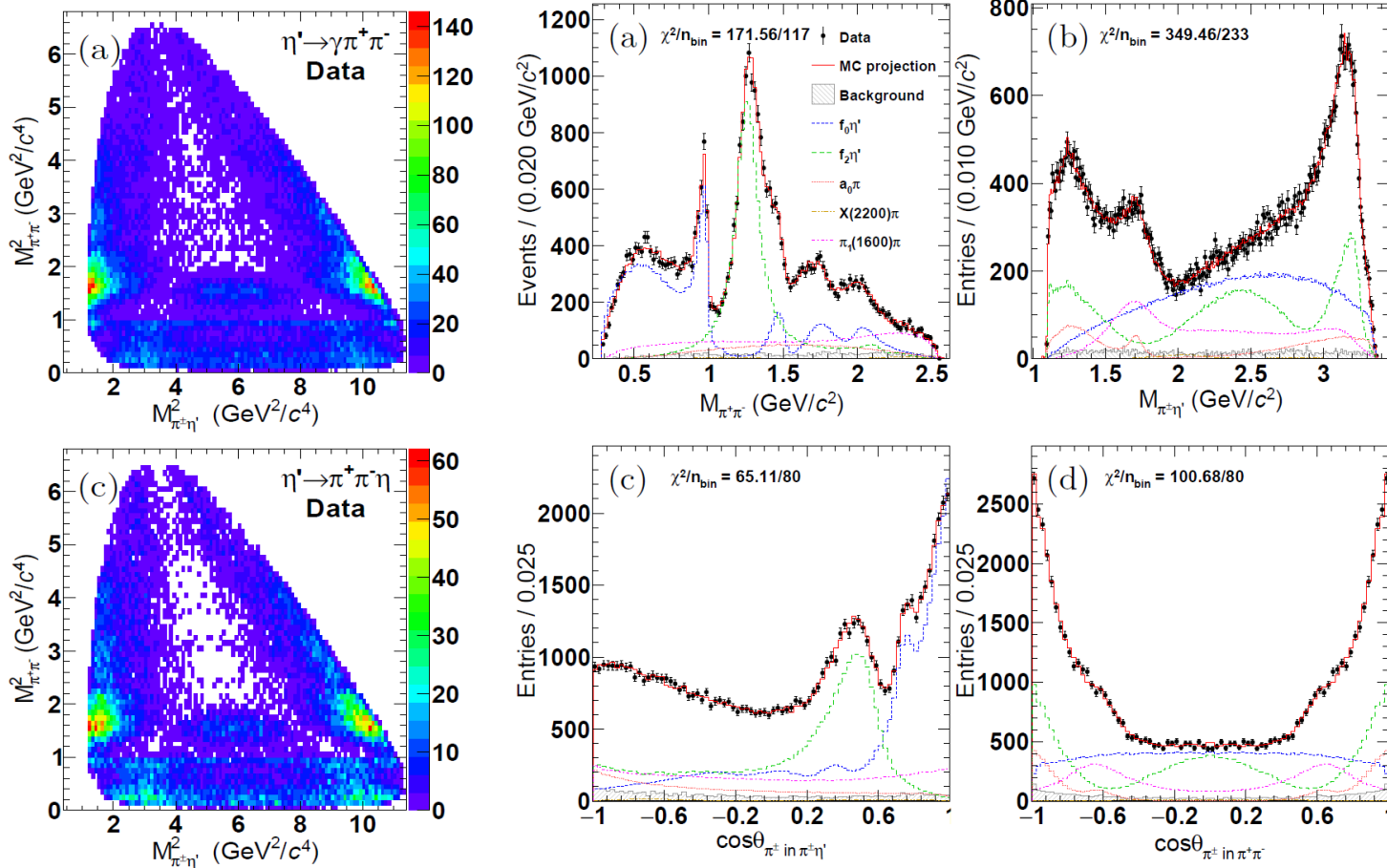
Evidence of  $\pi_1 \rightarrow \eta'\pi$   
(without significant  
BW phase motion)

PR D95 032002(2017)

$44.8 \times 10^7$   $\psi(3686)$ @BESIII



# Observation of $\pi_1$ in $\chi_{c1} \rightarrow \pi^+ \pi^- \eta'$



- $\pi_1(1600)$  observed  $> 21\sigma$
- with a significant BW phase motion  $> 11\sigma$
- $J^{PC} = 1^{-+}$ , better than other assignments  $> 17\sigma$

BW with mass-dependent width

$$M = (1828 \pm 8_{-33}^{+11}) \text{ MeV}/c^2,$$

$$\Gamma = (638 \pm 26_{-86}^{+35}) \text{ MeV}/c^2$$

$$B[\chi_{c1} \rightarrow \pi_1(1600)^\pm \pi^\mp] \\ \times B[\pi_1(1600)^\pm \rightarrow \pi^\pm \eta'] \\ = (4.30 \pm 0.14_{-1.03}^{+1.04}) \times 10^{-4}$$

**pole:  $(1690 \pm 16_{-44}^{+36}) - i(217 \pm 5_{-19}^{+7})\text{MeV}$**

BW with constant width

$$M = (1675 \pm 9_{-32}^{+32}) \text{ MeV}/c^2,$$

$$\Gamma = (443 \pm 15_{-56}^{+18}) \text{ MeV}/c^2$$

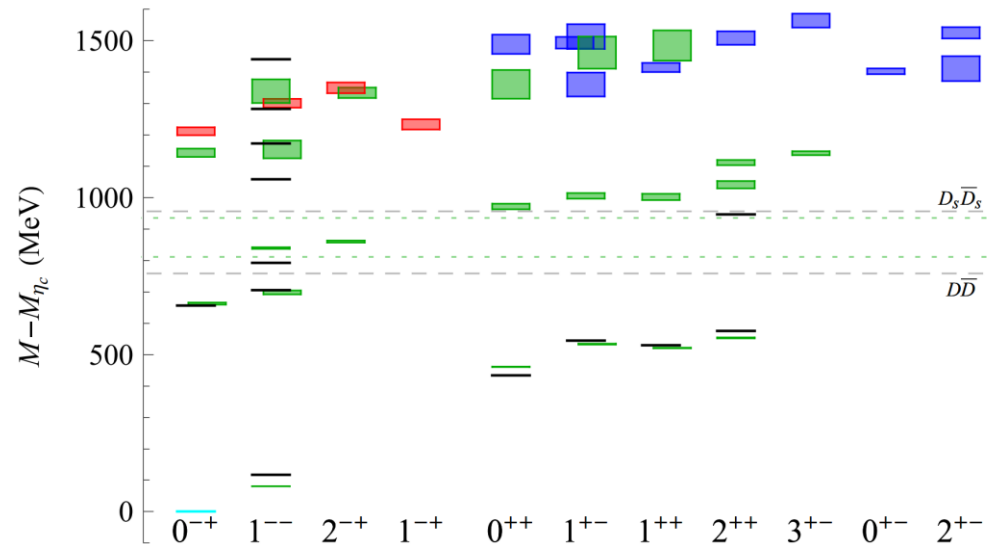
$$B[\chi_{c1} \rightarrow \pi_1(1600)^\pm \pi^\mp] \\ \times B[\pi_1(1600)^\pm \rightarrow \pi^\pm \eta'] \\ = (4.27 \pm 0.14_{-1.32}^{+0.86}) \times 10^{-4}$$

**pole:  $(1689 \pm 10_{-35}^{+33}) - i(220 \pm 7_{-27}^{+9})\text{MeV}$**

- Pole position is consistent with CLEO-c, COMPASS and JPAC <sup>14</sup>

# $\bar{c}c\eta$ hybrids

LQCD predicts similar supermultiplet as light hybrids



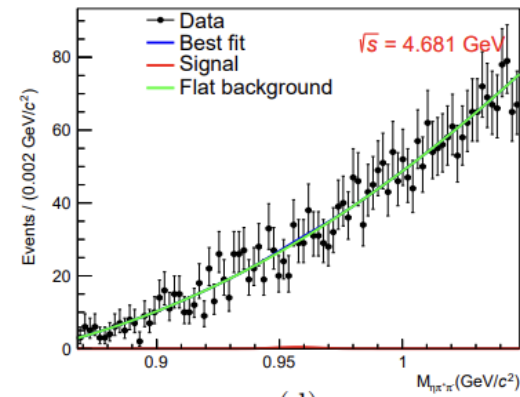
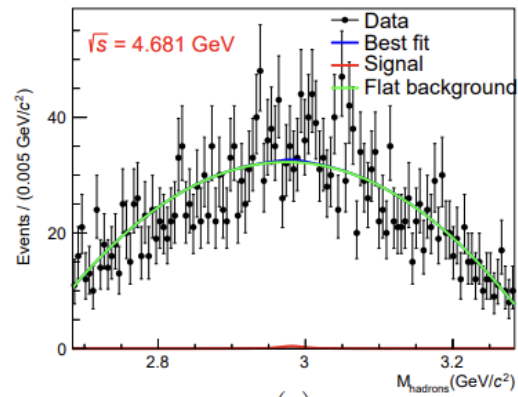
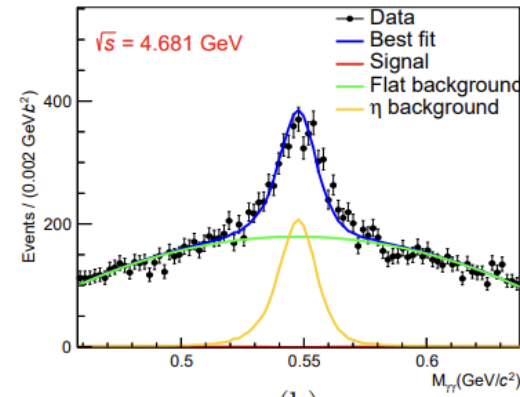
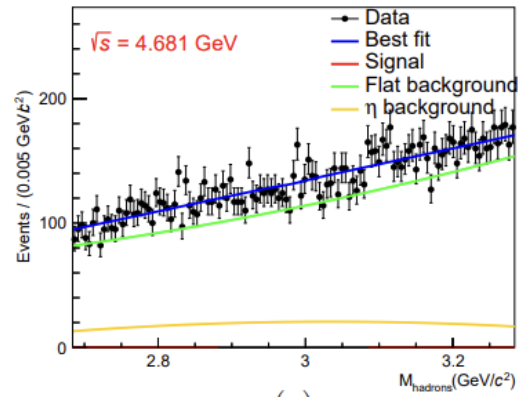
JHEP 07 (2012), 126

- Y(4230)?
  - Seem to be contradicting with the exp. observation:  
 $\sigma(D^*\bar{D} + c.c.) \gg \sigma(D^*D^*)$
- Transitions between  $1^{--}$  and  $\{0, 1, 2\}^{-+}$
- Molecule states of  $1^{-+}$  and  $1^{--}$  ?

Further studied at  
BESIII and Belle II

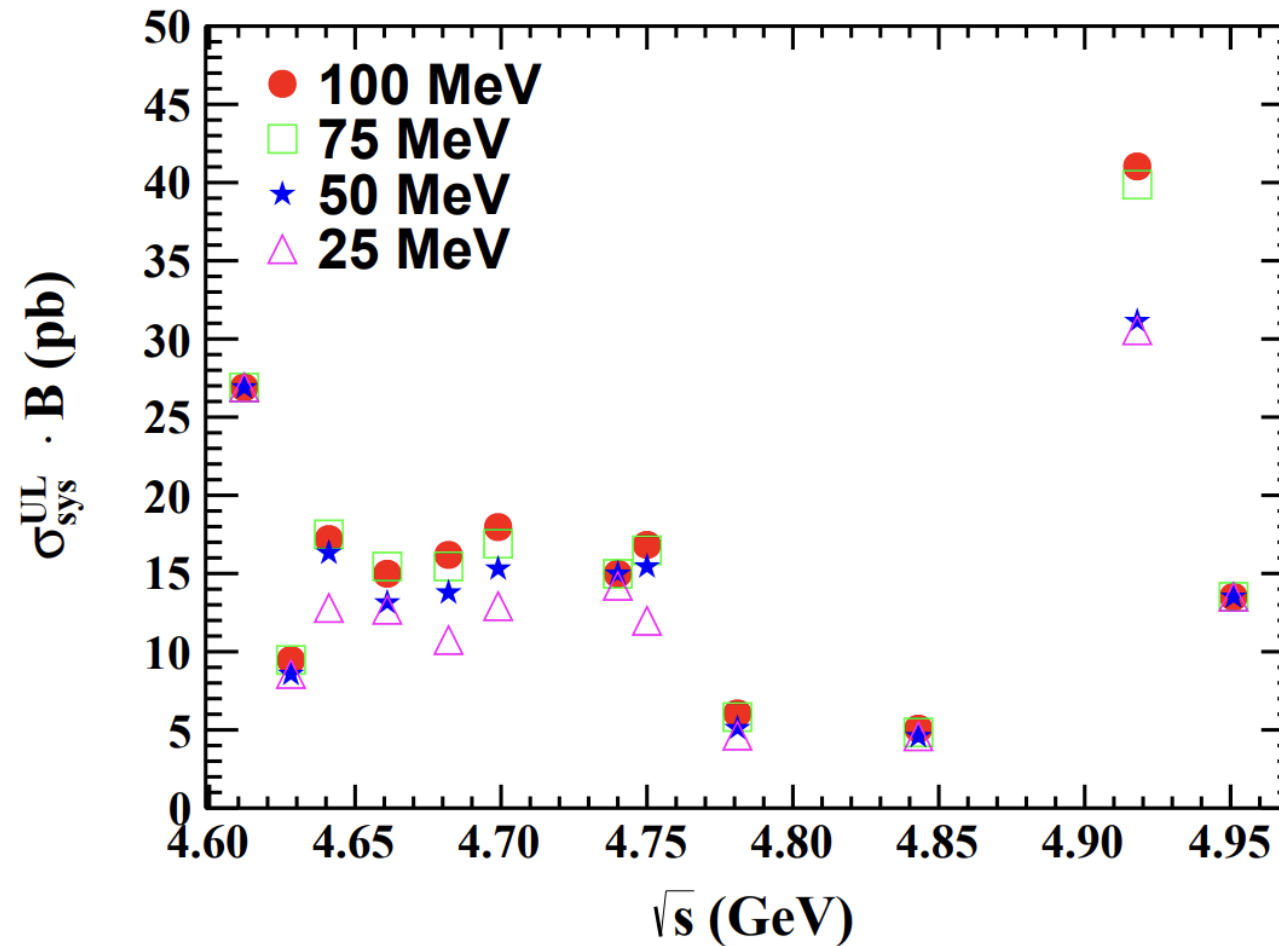
# Search for $1^{-+}$ charmonium-like hybrid via $e^+e^- \rightarrow \gamma\eta^{(\prime)}\eta_c$ at center-of-mass energies between 4.258 and 4.681 GeV

BESIII PR D 111, 112007 (2025)



Search for a  $1^{-+}$  molecular state via  $e^+e^- \rightarrow \gamma D_s^+ D_{s1}^- (2536) + c.c.$

BESIII PRD 112, 032002(2025)

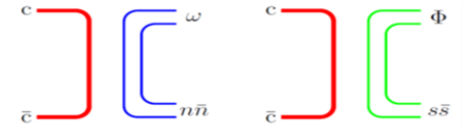


# $1^{-+}$ Hybrids

- How to discriminate hybrid/molecule/tetraquark?

- $\eta_1(1855) \rightarrow f_1\eta, K_1K$  are important
- $\Gamma_{\pi_1 \rightarrow b_1\pi} / \Gamma_{\pi_1 \rightarrow \eta'\pi}$  is not available yet

- Where is the  $\eta_1^{(')}$ ?  $J/\psi \rightarrow \omega\eta\eta', \phi\eta\eta'$  to access quark contents

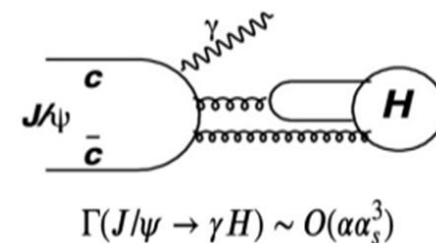
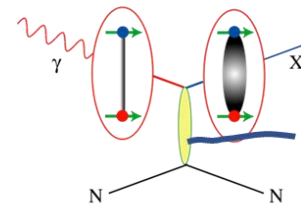
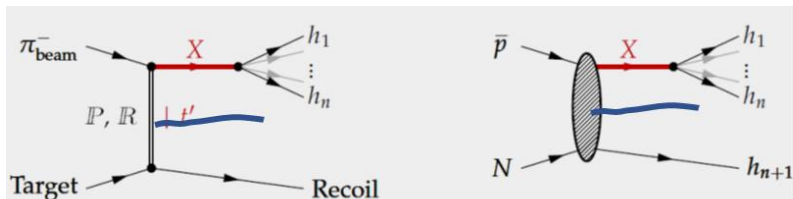


- Why  $\eta'$  is the observation channel for  $\pi_1(1600)$  and  $\eta_1(1855)$ ?  $U_1(A)$  anomaly?

- Does  $K_1$  exist and how to identify it?

- Where are the other  $J^{PC} = (0^{--}, \text{even}^{+-}, \text{odd}^{-+})$  states? Analog in  $\bar{c}c$  exists?

- New results from COMPASS, AMBER, BESIII, GlueX and PANDA are eagerly awaited. **Stay tuned**



Thank you

backup

# Observation of **An Exotic $1^- +$ Isoscalar State $\eta_1(1855)$**

PRL 129 192002(2022) , PRD 106 072012(2022)

- Angular distribution as a function of  $M(\eta\eta')$  expressed **model-independently**

$$\langle Y_l^0 \rangle \equiv \sum_{i=1}^{N_k} W_i Y_l^0(\cos\theta_{\eta}^i)$$

- Related to the spin-0(S), spin-1(P), spin-2(D) amplitudes in  $\eta\eta'$  by:

$$\sqrt{4\pi}\langle Y_0^0 \rangle = S_0^2 + P_0^2 + P_1^2 + D_0^2 + D_1^2 + D_2^2,$$

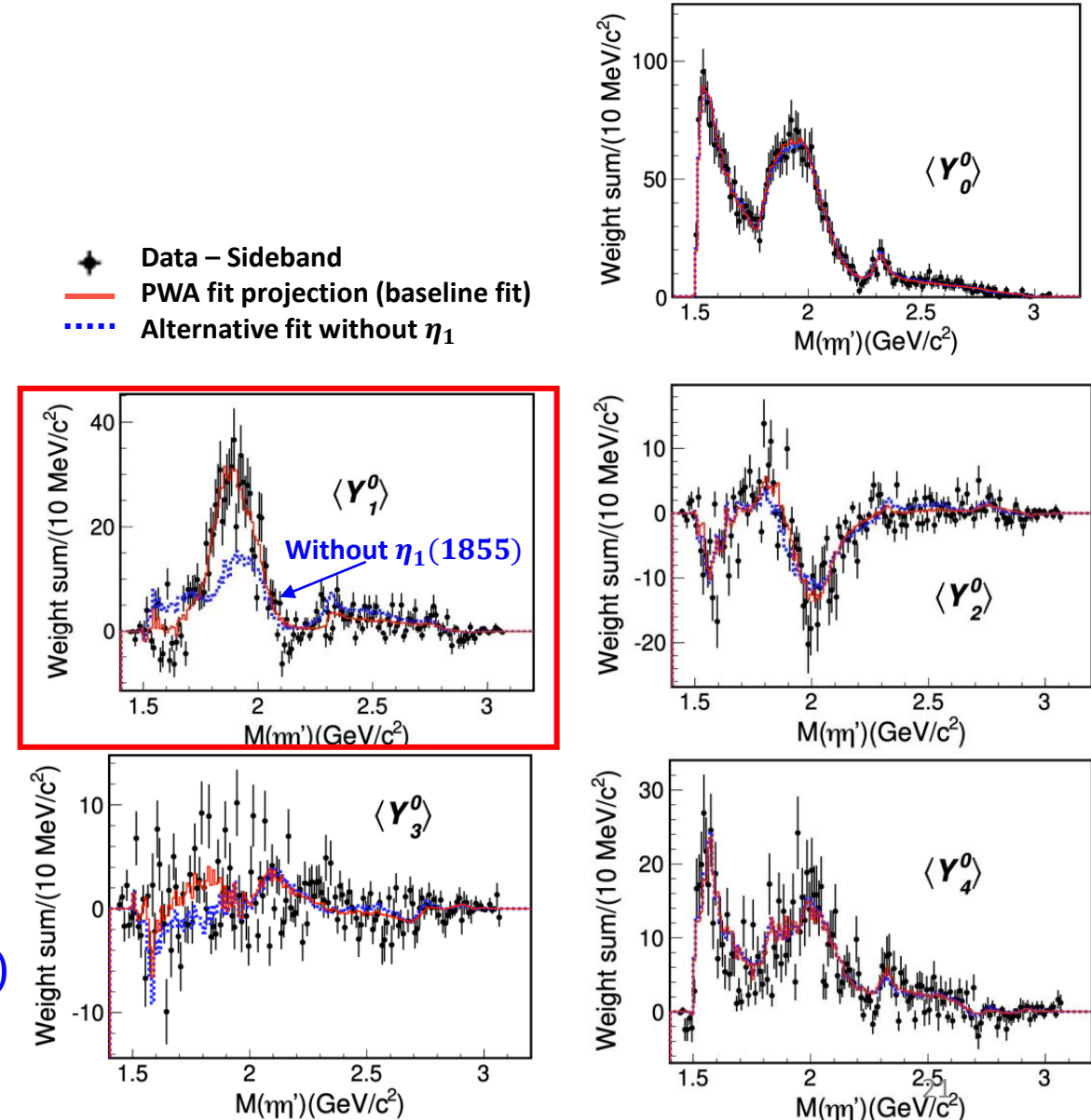
$$\sqrt{4\pi}\langle Y_1^0 \rangle = 2S_0P_0 \cos\phi_{P_0} + \frac{2}{\sqrt{5}}(2P_0D_0 \cos(\phi_{P_0} - \phi_{D_0}) + \sqrt{3}P_1D_1 \cos(\phi_{P_1} - \phi_{D_1})),$$

$$\sqrt{4\pi}\langle Y_2^0 \rangle = \frac{1}{7\sqrt{5}}(14P_0^2 - 7P_1^2 + 10D_0^2 + 5D_1^2 - 10D_2^2) + 2S_0D_0 \cos\phi_{D_0},$$

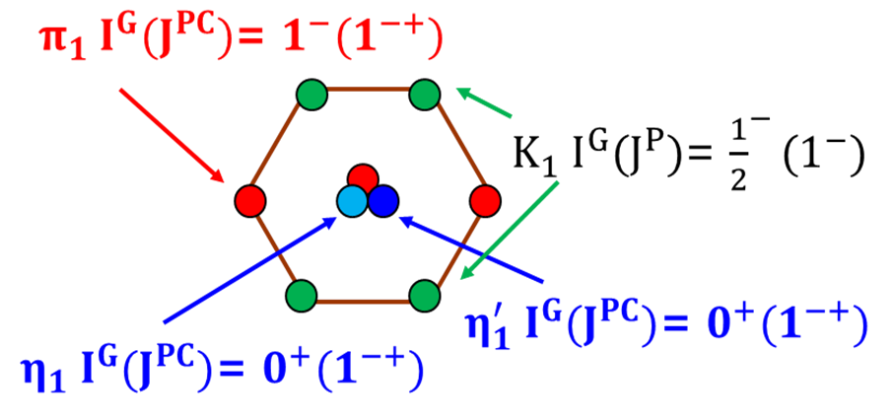
$$\sqrt{4\pi}\langle Y_3^0 \rangle = \frac{6}{\sqrt{35}}(\sqrt{3}P_0D_0 \cos(\phi_{P_0} - \phi_{D_0}) - P_1D_1 \cos(\phi_{P_1} - \phi_{D_1})),$$

$$\sqrt{4\pi}\langle Y_4^0 \rangle = \frac{1}{7}(6D_0^2 - 4D_1^2 + D_2^2).$$

- Narrow structure** in  $\langle Y_1^0 \rangle$ 
  - **Cannot be described by resonances in  $\gamma\eta(\eta')$**
  - **$\eta_1(1855) \rightarrow \eta\eta'$  needed**



# What about $K_1$ ?



Exotic Kaons are difficult to be established, because they do not have exotic quantum numbers

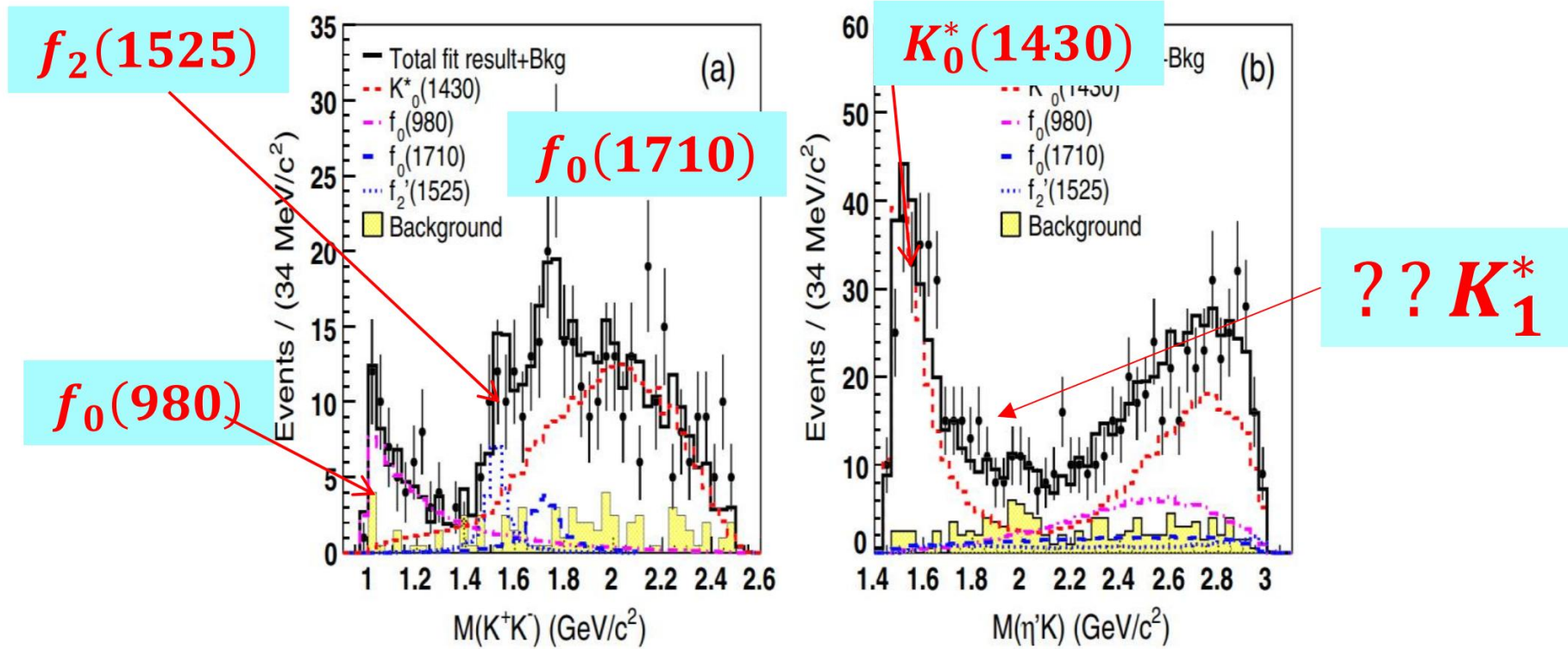
Decay property is the key

- $K_1(1270)$
- $K_1(1400)$
- $K^*(1410)$
- $K_0^*(1430)$
- $K_2^*(1430)$
- $K(1460)$
- $K_2(1580)$
- $K(1630)$
- $K_1(1650)$
- $K^*(1680)$
- $K_2(1770)$
- $K_3^*(1780)$
- $K_2(1820)$
- $K(1830)$
- $K_0^*(1950)$
- $K_2^*(1980)$

$$\chi_{c1} \rightarrow K^+ K^- \eta'$$

PWA with 106 million  $\psi(3686)$

PhysRevD.89.074030



Now, BESIII has 2.7 billion  $\psi(3686)$ . An updated analysis is underworking