

# 核子电磁与引力形状因子的 夸克-双夸克描述

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Based on:  
[arXiv:2507.13484](https://arxiv.org/abs/2507.13484)

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商丘, 2026.05.17

- ◆ Motivation
- ◆ Dyson-Schwinger Equations
- ◆ EMFFs of Nucleon
- ◆ GFFs of Nucleon [*Preliminary*]
- ◆ Summary and Outlook

# Motivations

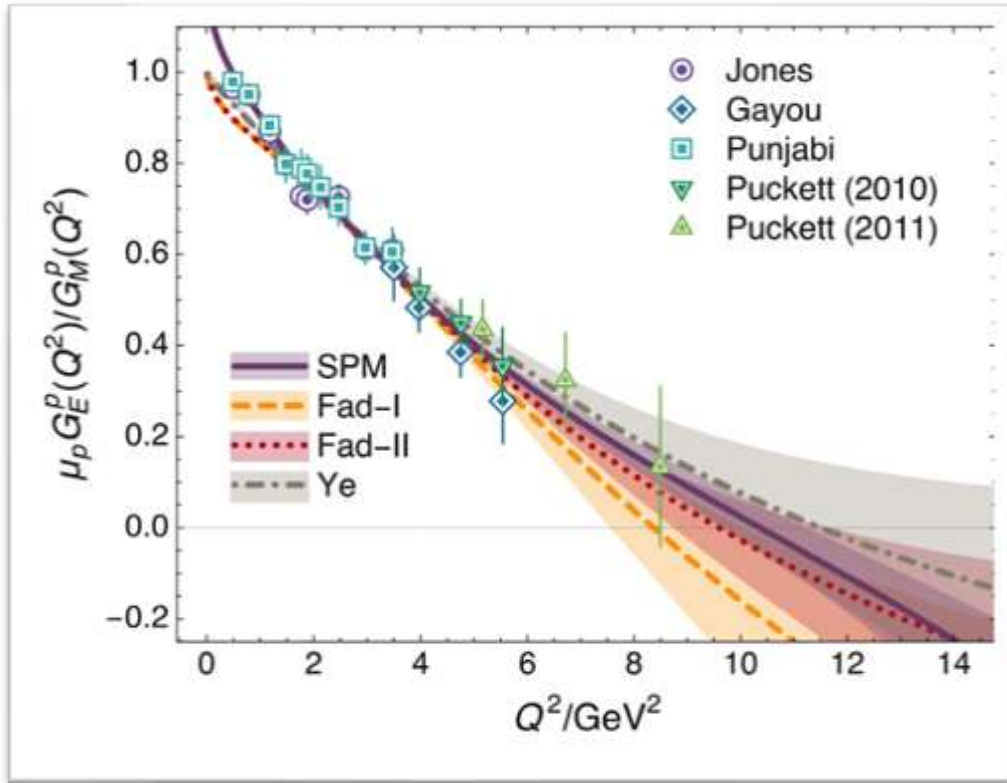
## ➤ Nucleon structure

- The nucleon magnetic moment was measured to be about  $\mu_p \approx 2.5\mu_N$  (Frisch and Stern, 1933) and  $\mu_n \approx -1.5\mu_N$  (Alvarez and Bloch, 1940);
- The first determination of the proton charge radius  $0.74 \pm 0.24$  fm was brought by studies of elastic electron-proton scattering ( McAllister and Hofstadter, 1956);
- The structure of the nucleon in DIS is described in terms of **parton model** (Feynman, 1969); The development of the parton model were key to establishing **quantum chromodynamics**.
- Nowadays: Origin of proton mass? Spin puzzle? PDFs (GPDs, TMDs)? D-term(the less well-known)? .....

## ➤ Form factors

- ✓ The electromagnetic form factors (EMFFs) are important quantities for the understanding of **hadron's electromagnetic structure**:  
charge radius, magnetic momentum, charge and magnetisation densities
- ✓ The gravitational form factors (GFFs) contains fundamental information on **hadron's mechanical properties**:  
mass, spin, D term, the distributions of energy and internal forces
- ✓ The evolution behavior of the FFs with  $Q^2$  can reveal the scale dependence of **effective degrees of freedom**.  
meson-baryon, dressed quark, current quark

# Motivations



D. Binosi, C. D. Roberts, Z.-Q.Yao, arXiv: 2503.05984

$$T_a^{\mu\nu}(\vec{r}) = \int \frac{d^3\Delta}{(2\pi)^3 2E} e^{-i\vec{\Delta}\cdot\vec{r}} \langle p' | T_a^{\mu\nu} | p \rangle$$

In order to obtain a more reliable distribution of mechanical properties, it is necessary to obtain the results of the form factor over a wider range of momentum  $Q^2$ .

As a continuous non-perturbative method, DSEs is a good choice!

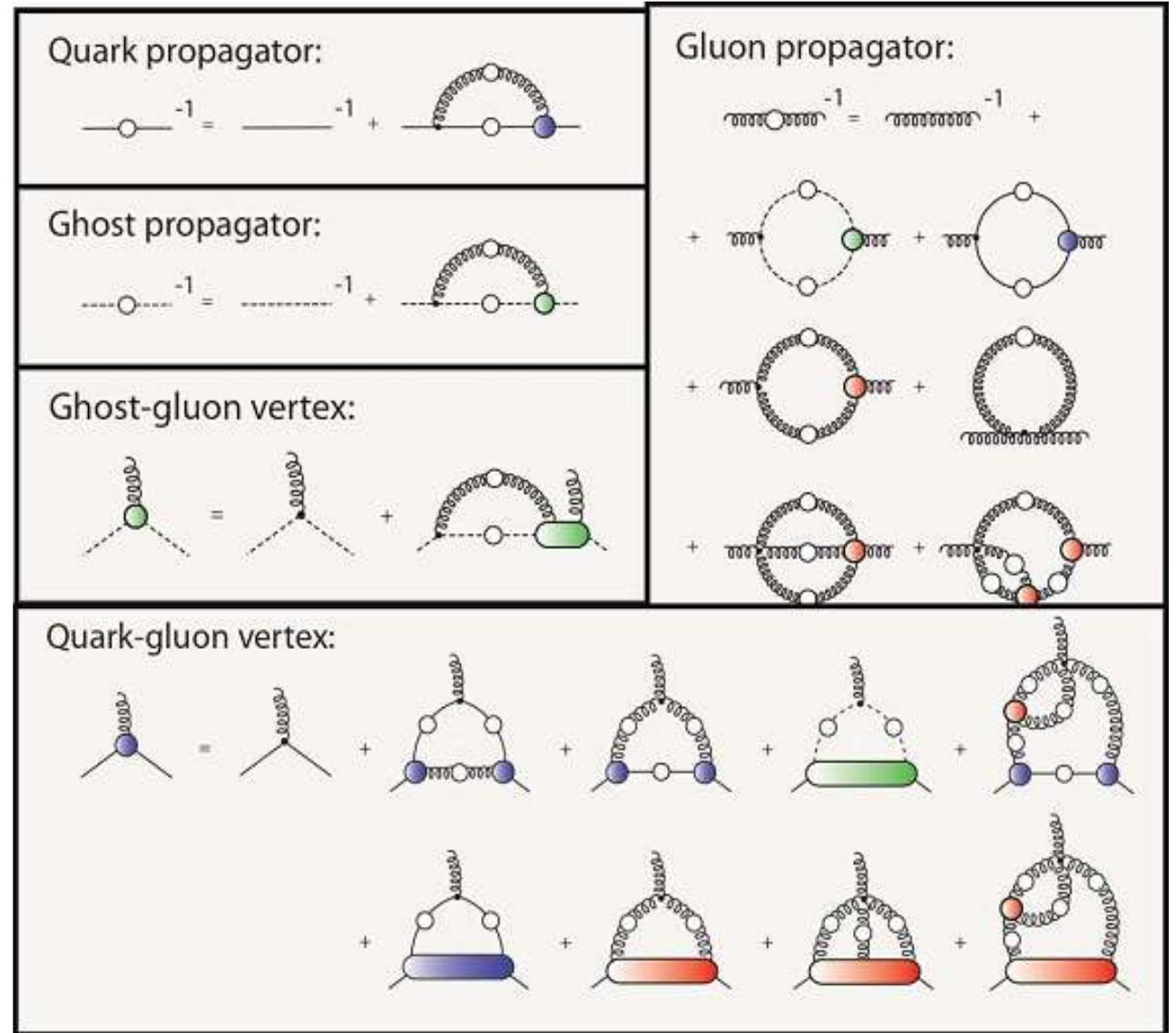
# Dyson-Schwinger Equations(DSEs)

- Continuum Schwinger function methods
- ✓ nonperturbative
- ✓ symmetry-preserving
- Owing to the infinite coupling feature, it is necessary to truncate the DSEs at a certain level for practical calculations.

C. D. Roberts and A. G. Williams, *Prog. Part. Nucl. Phys.* 33 (1994) 477-575.

C. D. Roberts and S. M. Schmidt, *Prog. Part. Nucl. Phys.* 45 (2000) S1-S103.

P. Maris and C. D. Roberts, *Int. J. Mod. Phys. E* 12 (2003) 297-365.



# Dyson-Schwinger Equations(DSEs)

- 2n-point Green function  $G^n$  obeys Dyson's equation:

$$G^n = G_0^n + G_0^n K G^n$$

$K$  is the n-quark scattering kernel,  $G_0^n$  is the disconnected n-quark propagator.

- A bound state of mass  $M$  with wave function  $\psi$  show up as a pole in the 2n-point function, i.e. in the vicinity of the pole,  $G^n$  becomes(  $P$  is the total momentum):

$$G^n \sim \frac{\psi(k_1, k_2, \dots, k_n) \bar{\psi}(p_1, p_2, \dots, p_n)}{P^2 + M^2}$$

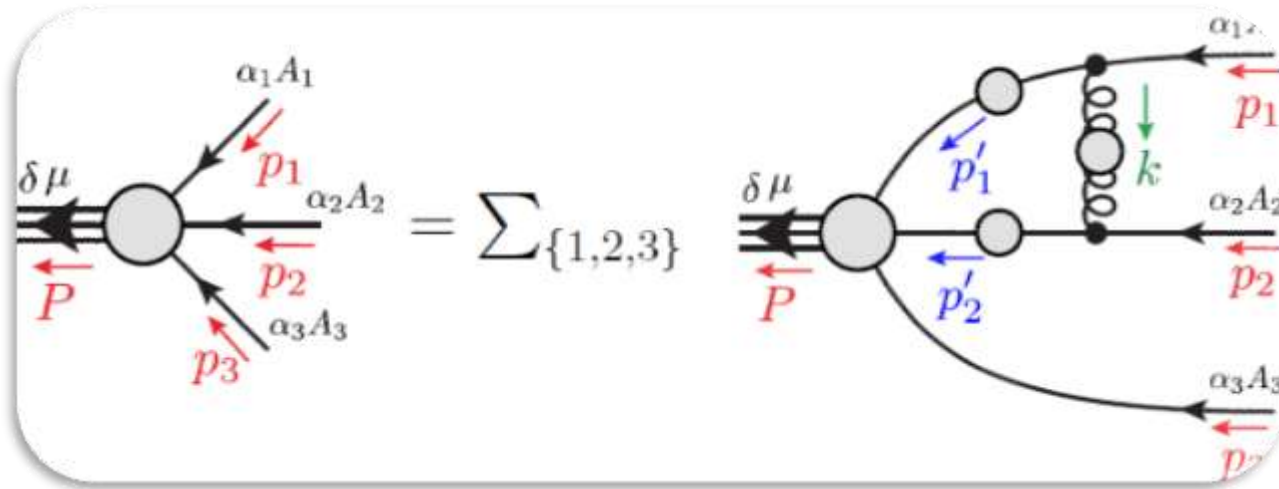
- Comparing residues, one finds the homogeneous bound state equation:

$$\psi = G_0 K \psi$$

- For the Faddeev equation of three quark system, the kernel consists of three terms:

$$K = K_1 + K_2 + K_3$$

# Dyson-Schwinger Equations(DSEs)



- ✓ Nucleon mass from a covariant three-quark Faddeev equation,  
G. Eichmann et al., Phys. Rev. Lett. 104 (2010) 201601
- ✓ Poincaré-covariant analysis of heavy-quark baryons,  
S.-X. Qin (秦思学) et al., Phys.Rev. D 97 (2018) 114017/1-13
- ✓ Nucleon Gravitational Form Factors,  
Z.-Q. Yao (姚照干) et al., Eur. Phys. J. A 61 (2025) 92/1-13

- Baryons appear as poles in the six-point Schwinger function, and their amplitude satisfy a homogeneous integral equation-Faddeev equation.
- Direct solution of Faddeev equation using rainbow-ladder truncation is now possible, but remains **challenging problem – algorithms and numerical analysis.**

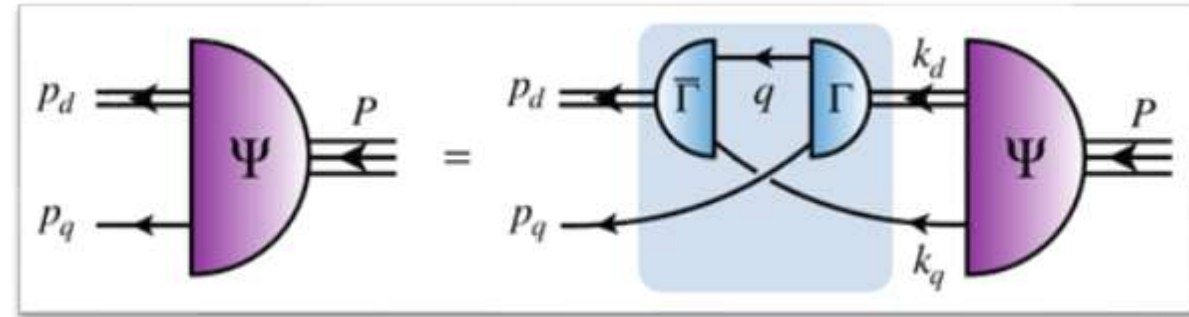
# Dyson-Shwinger Equations(DSEs)

## ➤ Faddeev Equation(Quark+Diquark Framework)

- For many applications, diquark approximation to quark+quark scattering kernel is used
- **Prediction:** Owing to DCSB, *diquark correlations may exist within baryons*

Diquark correlations in hadron physics: Origin, impact and evidence

M.Yu.Barabanov, Craig D.Roberts et al. Prog.Part.Nucl.Phys. 116 (2021) 103835



## ➤ Diquark correlation

- $(I=0, J^P=0^+)$ : isoscalar-scalar diquark
- $(I=1, J^P=1^+)$ : isovector-axialvector diquark
- $(I=0, J^P=0^-)$ : isoscalar-pseudoscalar diquark
- $(I=0, J^P=1^-)$ : isoscalar-vector diquark
- $(I=1, J^P=1^-)$ : isovector-vector diquark

- ✓ G. Eichmann, H. Sanchis-Alepuz, R. Williams, R. Alkofer, C. S. Fischer, Prog.Part.Nucl.Phys. 91 (2016) 1- 100
- ✓ ChenChen, B. El-Bennich, C. D. Roberts, S. M. Schmidt, J. Segovia, S-L. Wan, Phys.Rev. D97 (2018) no.3, 034016

# EMFFs of Nucleon

- The nucleon electromagnetic interaction current:

$$\begin{aligned}
 J_\mu(P_f, P_i) &= ie \Lambda_+(P_f) \Lambda_\mu(Q, P) \Lambda_+(P_i), \\
 &= ie \Lambda_+(P_f) \left[ \gamma_\mu F_1(Q^2) \right. \\
 &\quad \left. + \frac{1}{2m_N} \sigma_{\mu\nu} Q_\nu F_2(Q^2) \right] \Lambda_+(P_i),
 \end{aligned}$$

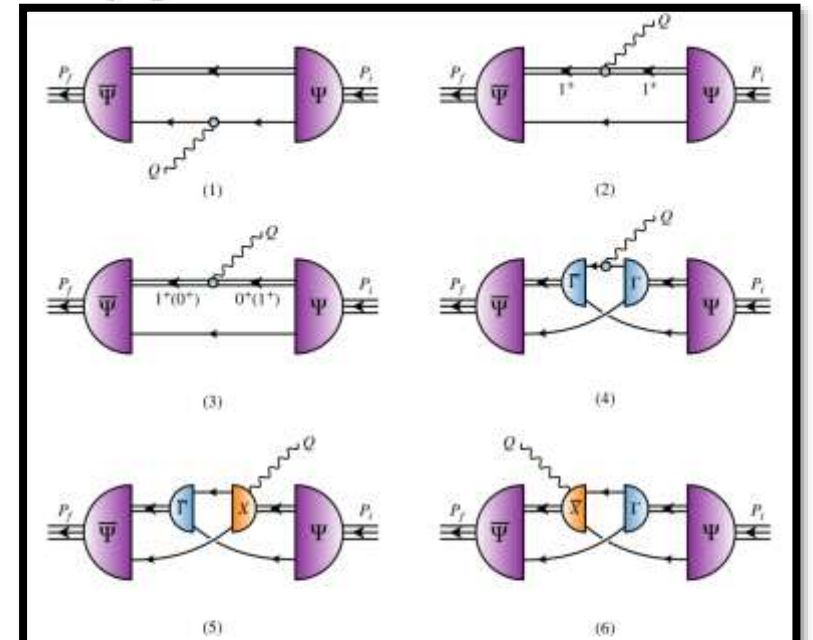
where  $Q = P_f - P_i$  is the transferred photon momentum.  $\Lambda_+$  is the projection operator of a positive energy nucleon,  $F_{1,2}$  are the Dirac and Pauli form factors.

- The nucleon charge and magnetization distributions ( $\tau = Q^2/[4m_N^2]$ ):

$$\begin{aligned}
 G_E(Q^2) &= F_1(Q^2) - \tau F_2(Q^2), \\
 G_M(Q^2) &= F_1(Q^2) + F_2(Q^2).
 \end{aligned}$$

The  $SU(2)_F$  isospin limit is used:  $m_u = m_d$ .

$$\begin{aligned}
 J_\mu(P_f, P_i) &= \int \frac{d^4p}{(2\pi)^4} \frac{d^4k}{(2\pi)^4} \\
 &\sum_{i=1}^6 \bar{\Psi}(p, -P_f) \Lambda_\mu^i(p, P_f; k, P_i) \Psi(k; P_i)
 \end{aligned}$$



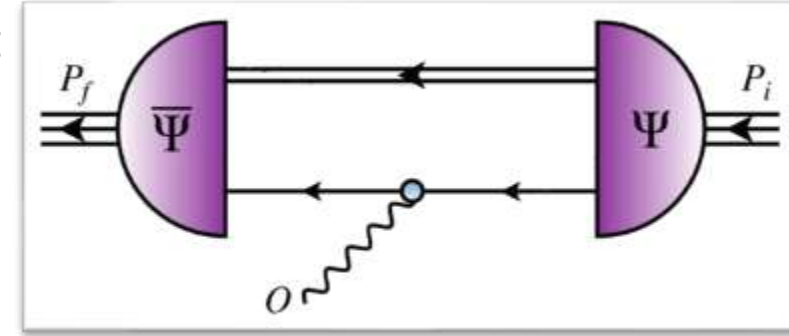
**Fig. 2** The collection of electromagnetic interaction diagrams that ensures a conserved current for on-shell nucleons described by the Faddeev amplitude,  $\Psi$ , calculated as described in Sect. 2. Legend. *single line*, dressed-quark propagator; *undulating line*, electromagnetic probe;  $\Gamma$ , diquark correlation amplitude; *double line*, diquark propagator; and  $\chi$ , seagull terms.

# EMFFs of Nucleon

➤ The unamputated photon-quark vertex satisfy Ward identity:

$$i(\ell_1 - \ell_2)_\mu \chi_\mu(\ell_1, \ell_2) = S(\ell_2) - S(\ell_1)$$

the following Ansatz for the vertex, expressed in terms of quantities already specified in dress quark propagator:



$$\begin{aligned} \chi_\mu(\ell_1, \ell_2) = & \gamma_\mu \Sigma_{\sigma V} + 2\ell_\mu [\gamma \cdot \ell \Delta_{\sigma V} + i\Delta_{\sigma S}] \\ & + \frac{1}{2} [s_1 - \bar{s}_1] [\gamma \cdot Q \gamma_\mu \gamma \cdot \ell - \gamma \cdot \ell \gamma_\mu \gamma \cdot Q] \Delta_{\sigma V} \\ & - [s_2 - \bar{s}_2] \sigma_{\mu\nu} Q_\nu \Delta_{\sigma S} + \frac{i}{2} [1 + s_3] \gamma \cdot Q \sigma_{\mu\nu} Q_\nu \Delta_{\sigma V} \end{aligned}$$

$$\Sigma_F = \frac{1}{2} [F(\ell_1^2) + F(\ell_2^2)]$$

$$\Delta_F = [F(\ell_1^2) - F(\ell_2^2)] / [\ell_1^2 - \ell_2^2]$$

$$s_i = a_i + b_i \exp\left[-\frac{1}{4} \mathcal{E}(Q^2) / M_q^E\right],$$

$$\bar{s}_{1,2} = 1 - s_{1,2}$$

$$\mathcal{E}(Q^2) / M_q^E = \left(1 + Q^2 / [2M_q^E]^2\right)^{1/2} - 1.$$

where  $\ell = [\ell_1 + \ell_2] / 2$  and  $Q = \ell_1 - \ell_2$ .

M. Ding, K. Raya, A. Bashir, D. Binosi, L. Chang, M. Chen, C.D. Roberts, Phys. Rev. D 99, 014014 (2019).

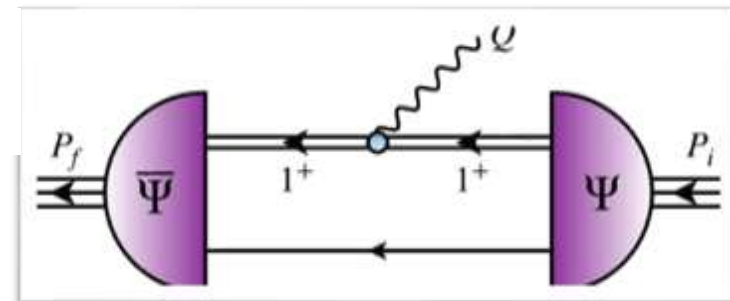
# EMFFs of Nucleon

➤ The photon-diquark vertex satisfy a Ward identity:

$$Q_\mu \chi_\mu^{0+}(l_1, l_2) = \left[ \Delta^{0+}(l_2^2) - \Delta^{0+}(l_1^2) \right] F_{sc}(Q^2) \quad F_{sc}(Q^2) = \frac{1}{1 + \frac{1}{6} r_{sc}^2 Q^2}$$

➤ The photon- scalar diquark vertex:

$$\chi_\mu^{0+}(l_1, l_2) = -2k_\mu \Delta_{\Delta^{0+}}(l_1^2, l_2^2) F_{sc}(Q^2)$$

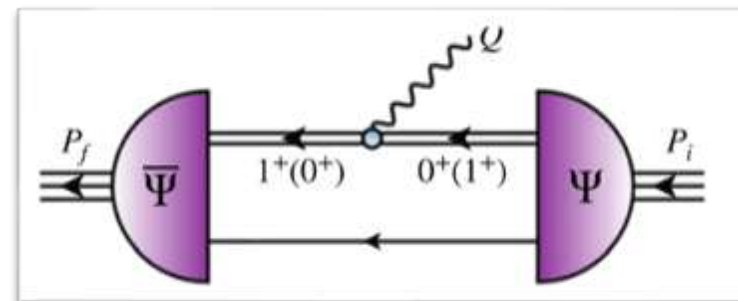


➤ The photon- axialvector diquark vertex:

$$\begin{aligned} \chi_{\mu\alpha\beta}^{1+}(l_1, l_2) = & - \left[ 2\delta_{\alpha\beta} l_\mu \Delta_{\Delta^1}(l_1^2, l_2^2) + \frac{1}{m_{1+}^2} (\delta_{\mu\alpha} l_{1\beta} \Delta^1(l_1^2) + \delta_{\mu\beta} l_{2\alpha} \Delta^1(l_2^2)) \right. \\ & \left. + \frac{2}{m_{1+}^2} l_{2\alpha} l_{1\beta} l_\mu \Delta_{\Delta^1}(l_1^2, l_2^2) \right] F_{av}(Q^2) + \kappa (Q_\beta \delta_{\mu\alpha} - Q_\alpha \delta_{\mu\beta}) \Delta_{\Delta^1}(l_1^2, l_2^2) \end{aligned}$$

➤ The photon-scalar-axialvector diquark vertex:

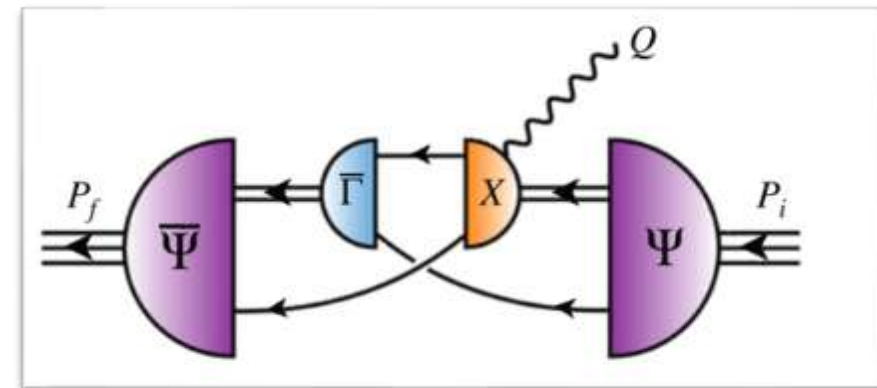
$$\Gamma_{SA}^{\gamma\alpha}(l_1, l_2) = -\Gamma_{AS}^{\gamma\alpha}(l_1, l_2) = \frac{i}{M_N} \kappa_{sa} F_{sa}(Q^2) \varepsilon_{\gamma\alpha\rho\lambda} l_{1\rho} l_{2\lambda}$$



# EMFFs of Nucleon

➤ The coupling of photon to diquark amplitude:

$$\begin{aligned}
 X_{\mu}^{JP}(k, Q) &= e_{\text{by}} \frac{4k_{\mu} - Q_{\mu}}{4k \cdot Q - Q^2} \left[ \Gamma^{JP}(k - Q/2) - \Gamma^{JP}(k) \right] \\
 &+ e_{\text{ex}} \frac{4k_{\mu} + Q_{\mu}}{4k \cdot Q + Q^2} \left[ \Gamma^{JP}(k + Q/2) - \Gamma^{JP}(k) \right]
 \end{aligned}$$



M. Oettel, M. Pichowsky and L. von Smekal, Eur. Phys. J. A 8, 251-281 (2000)

➤ The parameters are chosen by reproducing selected results from 3-body analyses of nucleon elastic electromagnetic form factors:

$a_1$	$a_2$	$a_3$	$b_1$	$b_2$	$b_3$
0.17	1.47	-0.93	1.03	-0.17	1.61
$r_{\text{sc}}/\text{fm}$	$r_{\text{av}}/\text{fm}$				
0.31	1.05				

Z.-Q. Yao, D. Binosi, Z.-F. Cui, C. D. Roberts, arXiv:2403.08088

# EMFFs of Nucleon

**Table 2** Calculated results for  $Q^2 \simeq 0$  (static) properties of nucleon electromagnetic form factors. Also listed, for comparison, results obtained using the *ab initio* three-body approach [25] and experiment [74, PDG].

		$r_E^2/\text{fm}^2$	$r_E^2 M^2$	$r_M^2/\text{fm}^2$	$r_M^2 M^2$	$\mu$
herein	$p$	$0.67^2$	$4.02^2$	$0.67^2$	$4.02^2$	2.80
	$n$	$-0.29^2$	$-1.73^2$	$0.72^2$	$4.30^2$	-1.86
[25]	$p$	$0.89^2$	$4.23^2$	$0.82^2$	$3.91^2$	2.23
	$n$	$-0.25^2$	$-1.19^2$	$0.81^2$	$3.87^2$	-1.33
[74, PDG]	$p$	$0.84^2$	$4.00^2$	$0.85^2$	$4.05^2$	2.79
	$n$	$-0.34^2$	$-1.62^2$	$0.86^2$	$4.11^2$	-1.91

**Magnetic moments:**

$$\mu_N = G_M^N(Q^2 = 0).$$

**Radii:**

$$\langle r_{E,M}^2 \rangle^N = -6 \left. \frac{d \ln G_{E,M}^N(Q^2)}{dQ^2} \right|_{Q^2=0}$$

$$\langle r_E^2 \rangle^n = -6 G_E^{n'}(Q^2)|_{Q^2=0}$$

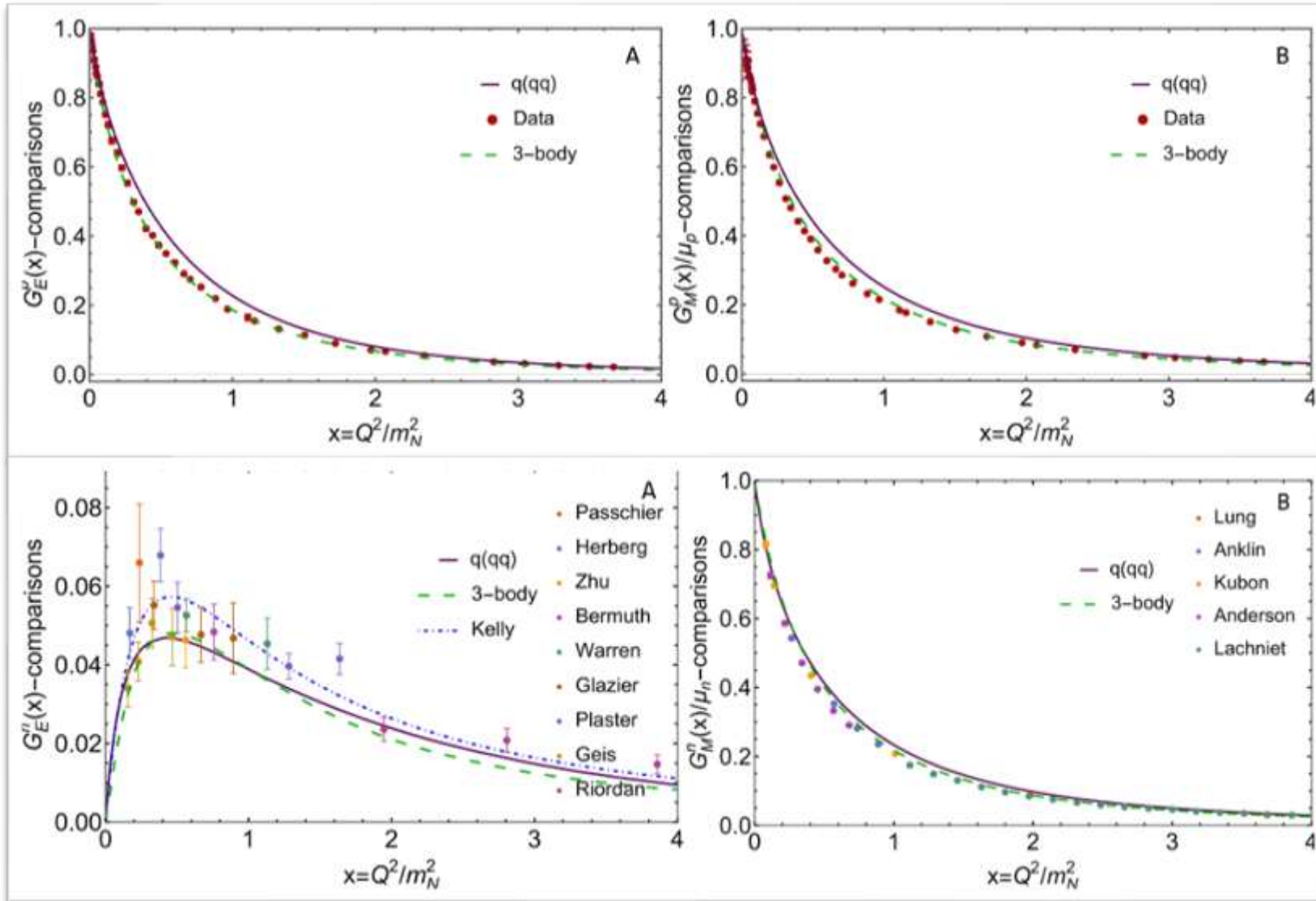
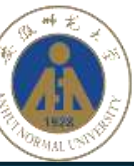
$$r_E^P \approx r_M^P$$

[25] Z.-Q. Yao, D. Binosi, Z.-F. Cui, C. D. Roberts, arXiv: 2403. 08088.

[74] S. Navas, et al., Review of particle physics, Phys. Rev. D 110 (3) (2024) 030001.

P. Cheng, et al., arXiv: [2507.13484](https://arxiv.org/abs/2507.13484)

# EMFFs of Nucleon

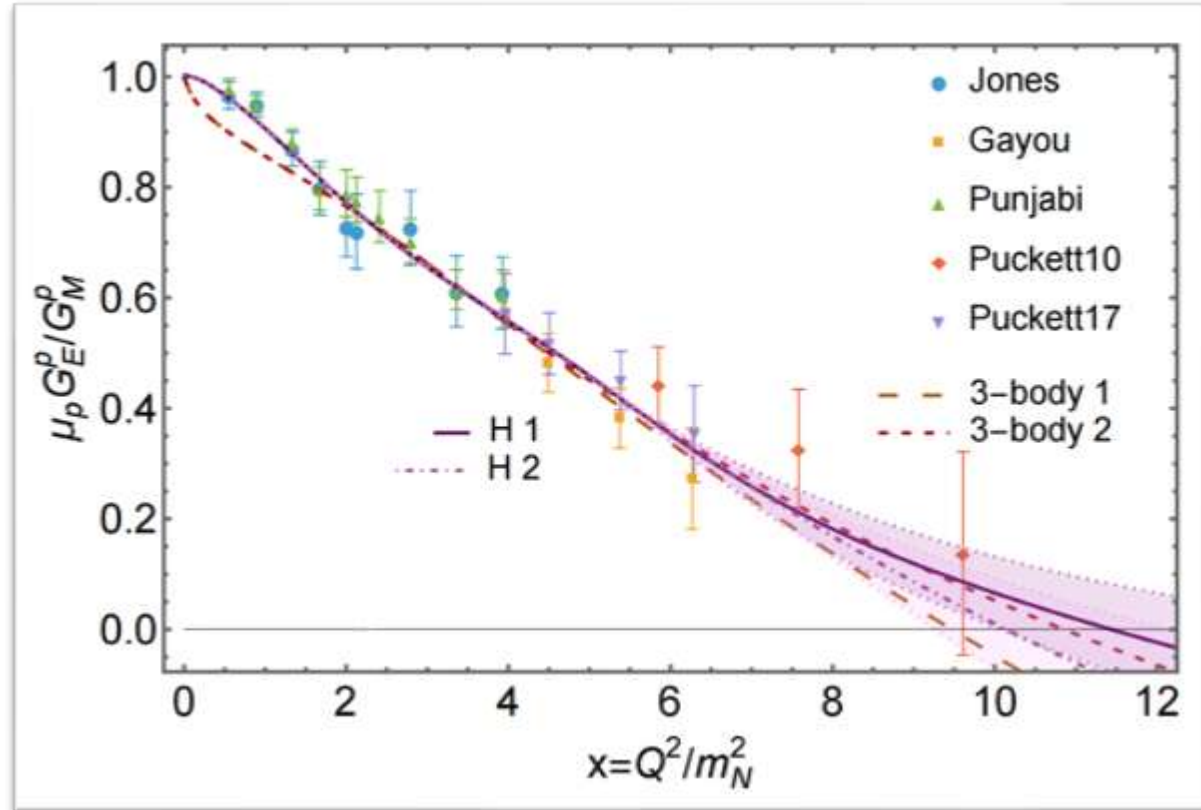
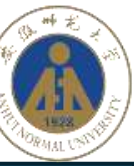


✓ The agreement is good for  $x > 2$ .

✓ For  $x < 2$ , the differences may stem from the contribution of the meson cloud.

P. Cheng, et al., arXiv: [2507.13484](https://arxiv.org/abs/2507.13484)

# EMFFs of Nucleon



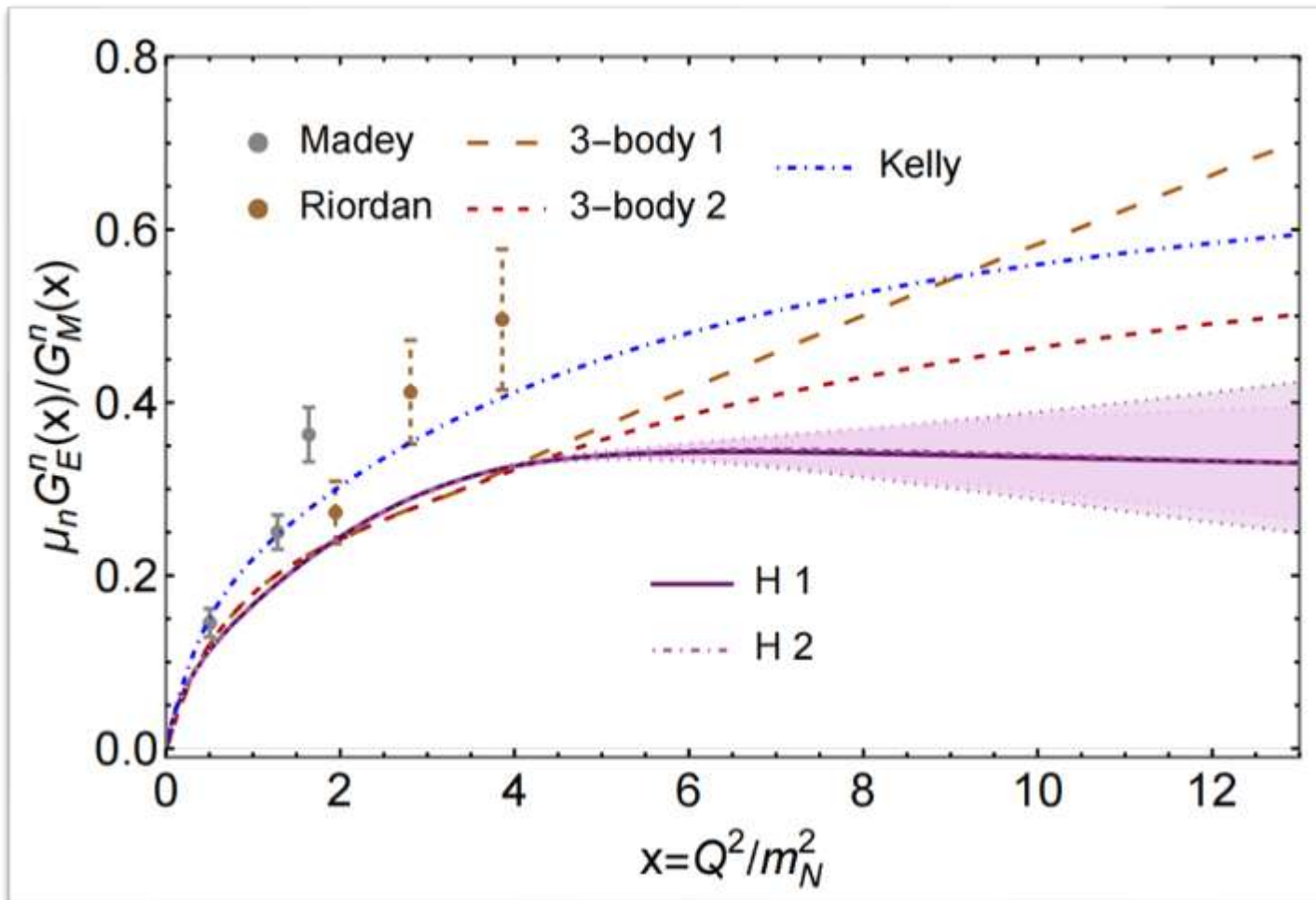
✓ A zero in  $G_E^p$ :

$q(qq)$  herein 3 – body

SPM 1  $11.44^{+3.35}_{-1.37}$   $9.47^{+1.90}_{-0.92}$

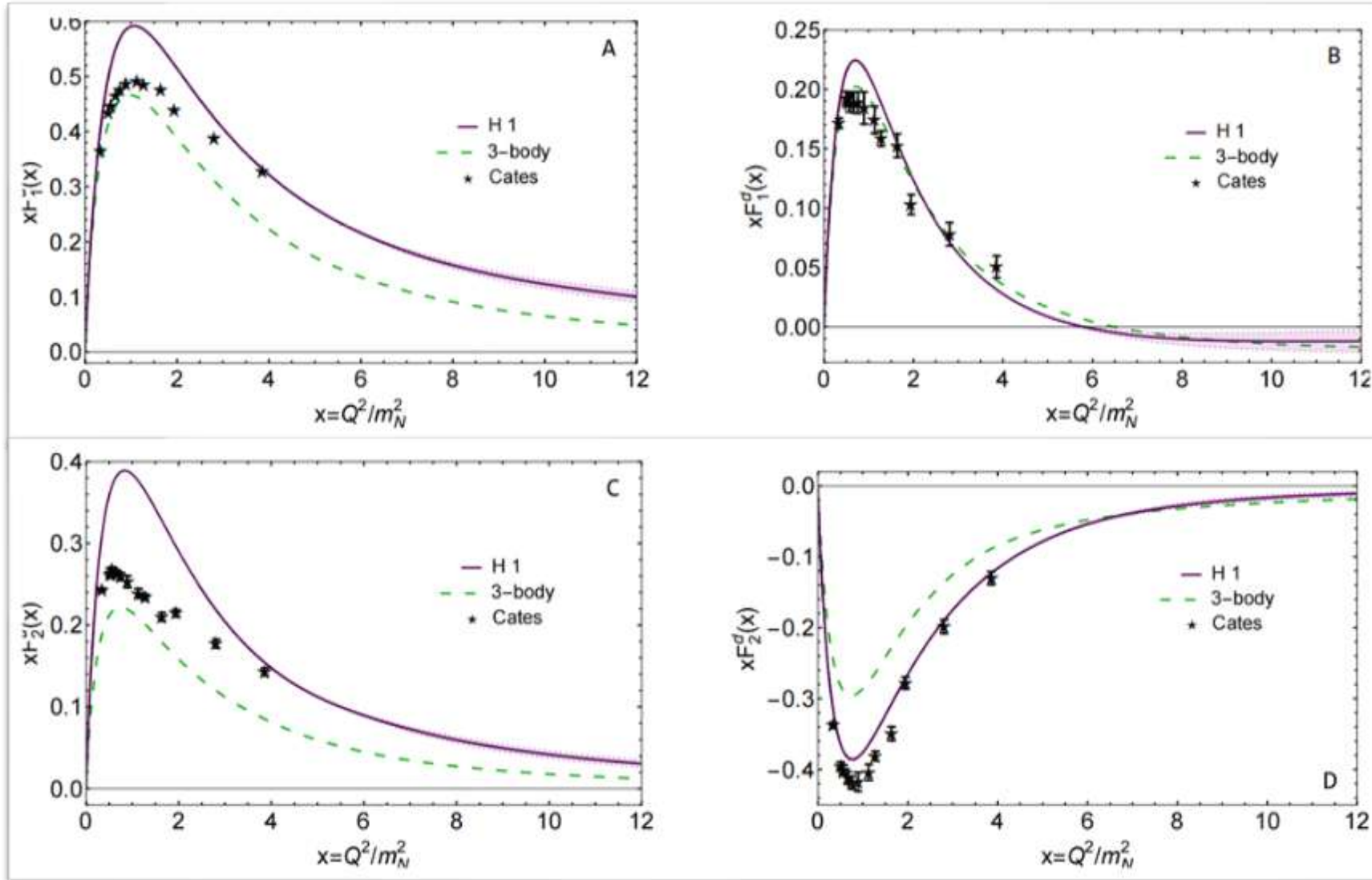
SPM 2  $10.14^{+1.99}_{-0.88}$   $10.85^{+2.37}_{-0.96}$

P. Cheng, et al., arXiv: [2507.13484](https://arxiv.org/abs/2507.13484)



- ✓ The results are consistent with the trend of the experimental data.
- ✓ Regarding comparison with the 3-body analyses, deviations become evident on  $x \gtrsim 5$ .
- ✓ Finding no zero crossing in  $G_E^n$  on  $x \lesssim 15$ .

# EMFFs of Nucleon



$$F_i^u = 2F_i^p + F_i^n,$$

$$F_i^d = F_i^p + 2F_i^n,$$

- ✓ The analysis predicts that  $F_1^d$  exhibits a zero:

$$x = 5.80^{+0.20}_{-0.14}$$

close to 3-body's results:

$$x \approx 6.5$$

- ✓ The analysis predicts that  $F_2^d$  doesn't exhibit a zero.

P. Cheng, et al., arXiv: [2507.13484](https://arxiv.org/abs/2507.13484)

# GFFs of Nucleon

- The total GFFs of nucleon are defined as:

$$\begin{aligned} \langle P_f | T_{\mu\nu}^g | P_i \rangle &= \Lambda_{\mu\nu}^{Ng}(P_f, P_i) \\ &= -\Lambda_+(P_f) \left[ P_\mu P_\nu A(Q^2) + iP_{\{\mu\sigma\nu\}\rho} Q_\rho J(Q^2) \right. \\ &\quad \left. + \frac{1}{4}(Q_\mu Q_\nu - \delta_{\mu\nu} Q^2) D(Q^2) \right] \Lambda_+(P_i) / m_N, \end{aligned}$$

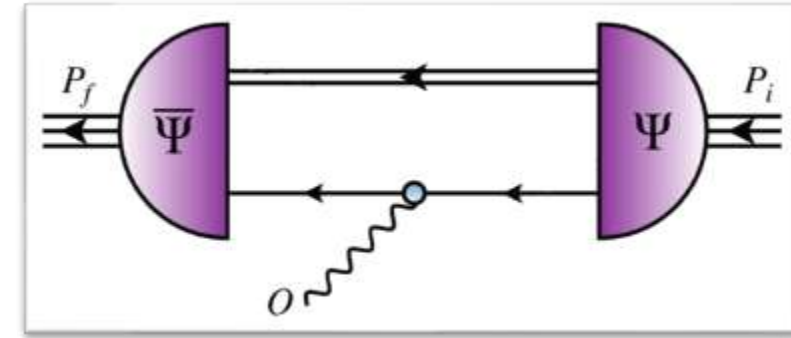
where  $a_{\{\mu b_\nu\}} = (a_\mu b_\nu + a_\nu b_\mu) / 2$ , The GFFs  $A(Q^2)$  is the nucleon mass distribution form factors;  $J(Q^2)$  relates to the nucleon spin distribution;  $D(Q^2)$  provides information on pressure and shear forces inside nucleon.

- The interaction current also has six terms:

$$\Lambda_{\mu\nu}^{Ng}(P_f, P_i) = \int \frac{d^4 p}{(2\pi)^4} \frac{d^4 k}{(2\pi)^4} \sum_{\hat{i}=1}^6 \bar{\Psi}(p, -P_f) J_{\mu\nu}^{\hat{i}}(p, P_f; k, P_i) \Psi(k, P_i).$$

➤ The unamputated graviton-quark vertex:

$$\begin{aligned}
 i\chi_{\mu\nu}^{qq}(\ell_1, \ell_2) = & \ell_\nu [i\gamma_\mu \Sigma_{\sigma\nu} + 2\ell_\mu [i\gamma \cdot \ell \Delta_{\sigma\nu} - \Delta_{\sigma S}]] \\
 & + \frac{i}{2} [s_1 - \bar{s}_1] [\gamma \cdot Q \gamma_\mu \gamma \cdot \ell - \gamma \cdot \ell \gamma_\mu \gamma \cdot Q] \Delta_{\sigma\nu} \\
 & - i[s_2 - \bar{s}_2] \sigma_{\mu\rho} Q_\rho \Delta_{\sigma S} - \frac{1}{2} [1 + s_3] \gamma \cdot Q \sigma_{\mu\rho} Q_\rho \Delta_{\sigma\nu} \\
 & - \frac{\delta_{\mu\nu}}{2} [S(\ell_1) + S(\ell_2)] + i\chi_{\mu\nu}^{qqT}(\ell_1, \ell_2)
 \end{aligned}$$



where  $\chi_{\mu\nu}^{qqT}$  represents all possible other transverse structures. It may be determined by solving the iBSE. In doing so, one sees the emergence of isoscalar scalar mesons in the graviton+quark vertex. Duing to the lightest scalar dominates, the following term is used:

$$\chi_{\mu\nu}^{qqT}(\ell_1, \ell_2) = iS(\ell_1)T_{\mu\nu}(Q)S(\ell_2)P_q^S(Q^2) \quad P_q^S(t) = \frac{-tr_{S_q}}{t + m_{S_q}^2}$$

where the predicted:  $m_{S_q} = 0.55\text{GeV}$  ,  $r_{S_q} = 0.193\text{GeV}$

Y. Z. Xu, M. Ding, K. Raya, C. D. Roberts, J. Rodríguez-Quintero and S. M. Schmidt, Eur. Phys. J. C 84, 191 (2024)

# GFFs of Nucleon

➤ The graviton- scalar diquark vertex:

$$\chi_{\mu\nu}^{g,0^+}(\ell_1, \ell_2) = \left[ -2\ell_\mu \ell_\nu \Delta_{\Delta^{0^+}}(\ell_1^2, \ell_2^2) - \delta_{\mu\nu} \frac{\Delta^{0^+}(\ell_1^2) + \Delta^{0^+}(\ell_2^2)}{2} \right] F_{sc}(Q^2)$$

where the  $r_{sc}$  being a parameter:  $r_{sc} = 0.74 r_{sc}^{em}$ .

Y. Z. Xu, M. Ding, K. Raya, C. D. Roberts, J. Rodríguez-Quintero and S. M. Schmidt, Eur. Phys. J. C 84, 191 (2024)

➤ The graviton- axialvector diquark vertex:

$$\begin{aligned} \chi_{\mu\nu,\alpha\beta}^{g,1^+}(\ell_1, \ell_2) = & \left[ -\ell_\nu \left[ \delta_{\alpha\beta}(\ell_1 + \ell_2)_\mu \Delta_{\Delta^{1^+}}(\ell_1^2, \ell_2^2) + \frac{1}{m_{1^+}^2} \left( \delta_{\mu\alpha} \ell_{1\beta} \Delta^{1^+}(\ell_1^2) + \delta_{\mu\beta} \ell_{2\alpha} \Delta^{1^+}(\ell_2^2) \right) \right. \right. \\ & \left. \left. + \frac{1}{m_{1^+}^2} \ell_{2\alpha} \ell_{1\beta} (\ell_1 + \ell_2)_\mu \Delta_{\Delta^{1^+}}(\ell_1^2, \ell_2^2) \right] - \delta_{\mu\nu} \frac{\Delta_{\alpha\beta}^{1^+}(\ell_1) + \Delta_{\alpha\beta}^{1^+}(\ell_2)}{2} \right] F_{av}(Q^2) \end{aligned}$$

where the  $r_{ax}$  being a parameter:  $r_{ax} = 0.74 r_{ax}^{em}$ .

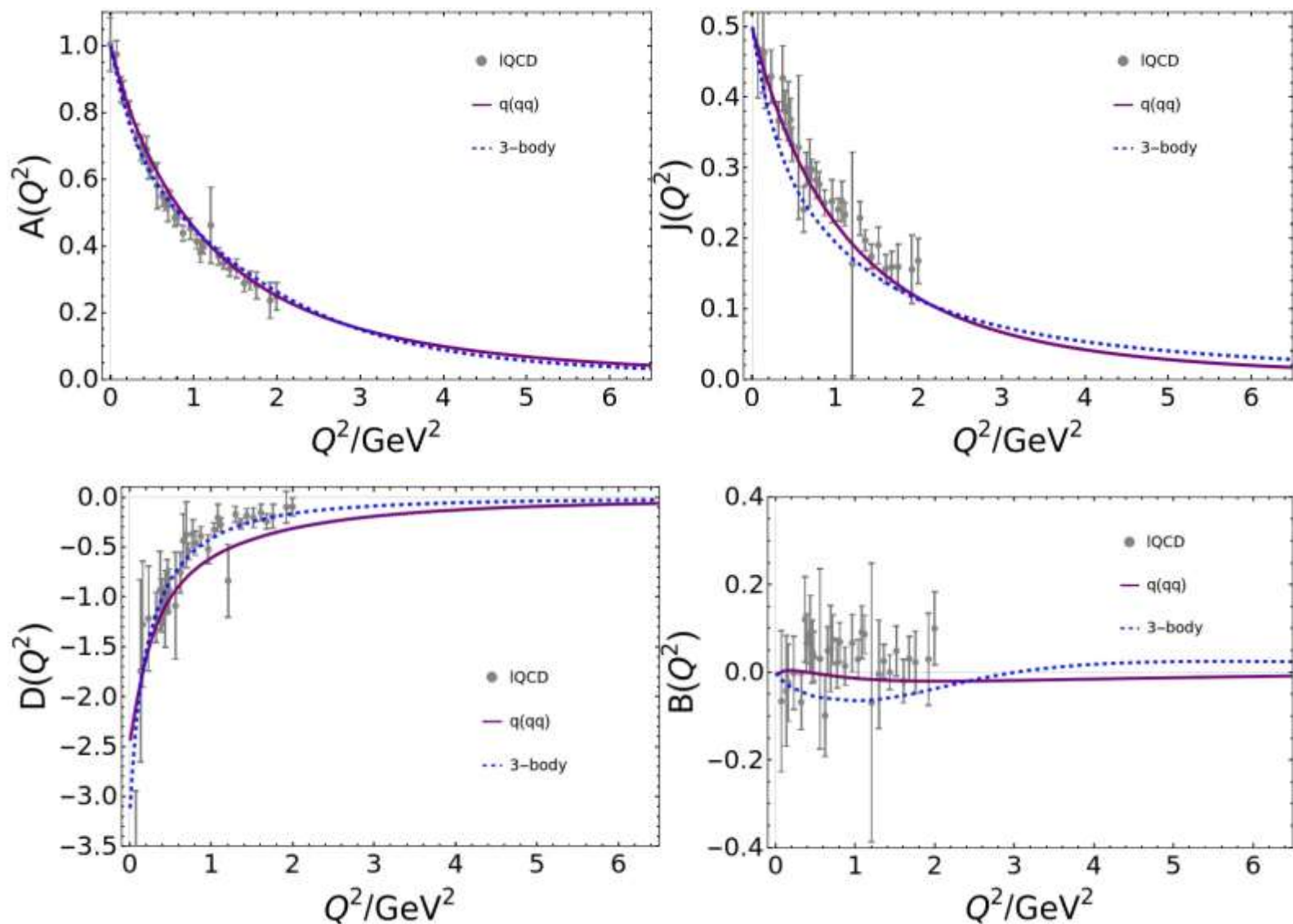
➤ The coupling of graviton to diquark amplitude:

$$\begin{aligned} X_{\mu\nu}^{JP}(\ell; K) = & p_{qv} \frac{4\ell_\mu - Q_\mu}{4\ell \cdot Q - Q^2} \left[ \Gamma^{JP}(\ell - Q/2; K) - \Gamma^{JP}(\ell; K) \right] \\ & + \frac{4\ell_\mu + Q_\mu}{4\ell \cdot Q + Q^2} \left[ \Gamma^{JP}(\ell + Q/2; K) - \Gamma^{JP}(\ell; K) \right] q_\nu + \delta_{\mu\nu} \Gamma(\ell; K), \end{aligned}$$

M. Oettel, M. Pichowsky and L. von Smekal, Eur. Phys. J. A 8, 251-281 (2000)

where  $p_q$ : the bystander quark,  $q$ : the exchange quark.

# GFFs of Nucleon



- ✓ The predictions of  $A(Q^2)$  and  $J(Q^2)$  agree with available IQCD results within mutual uncertainties.
- ✓ The magnitude of D term ( $D(0)$ ) is approximately 50% smaller than the results of 3-body and IQCD.

*Preliminary*

# GFFs of Nucleon

Table 2:  $D$ -term( $D(0)$ ) and radii for the corresponding nucleon GFFs.(The unit of radii are  $fm$ .)

$D$ -term	$q(qq)$	3-body	DR	IQCD(dipole)	IQCD(z-expansion)
	-2.67	-3.11(1)	$-3.38^{+0.34}_{-0.35}$	-3.87(97)	-3.35(58)
$\sqrt{\langle r_{mass}^2 \rangle}$	0.65	0.72(4)	$0.70^{+0.03}_{-0.04}$	-	-
$\sqrt{\langle r_{mech}^2 \rangle}$	0.51	0.64(2)	$0.72^{+0.09}_{-0.08}$	-	-
$\sqrt{\langle r_{\Theta}^2 \rangle}$	0.88	-	$0.97^{+0.03}_{-0.03}$	-	-
$\sqrt{\langle r_J^2 \rangle}$	0.61	-	$0.70^{+0.02}_{-0.02}$	-	-

$$\langle r_{mass}^2 \rangle = \left[ -6 \frac{d}{dt} A(t) \Big|_{t=0} - 3 \frac{D(0)}{2m_N^2} \right] \frac{1}{A(0)}$$

$$\langle r_{mech}^2 \rangle = \frac{6}{\int_0^\infty dt [D(t)/D(0)]}$$

$$\langle r_J^2 \rangle = -20 \frac{d}{dt} J(t) \Big|_{t=0}$$

$$\langle r_{\Theta}^2 \rangle = -6 \frac{d}{dt} \frac{A(t)}{A(0)} \Big|_{t=0} - \frac{9D(0)}{2m_N^2}$$

$$r_E^P \approx r_M^P > r_{mass} > r_{mech}$$

Preliminary

# Summary and Outlook

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- We predict **a zero in  $G_E^p$  at  $x = Q^2/m_N^2 \approx 11$** ; the absence of such a zero in  $G_E^n$ ; **a zero at  $x \approx 5.8$  in the proton's  $d$ -quark Dirac form factor.**
- Within the same framework, the predicted of GFFs  $A(Q^2)$  and  $J(Q^2)$  agree with available IQCD results, and we predict  $r_E^p \approx r_M^p > r_{mass} > r_{mech}$ .
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***Thank you for your attention!***