



Possible hidden-bottom pentaquarks from P-wave $\Lambda_b B^{(*)} / \Sigma_b^{(*)} B^{(*)}$ interactions

arXiv: 2607.14913

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Outline

I. Background and motivation: Similar hadronic molecular states exist in the bottom quark sector;

II. Theoretical framework;

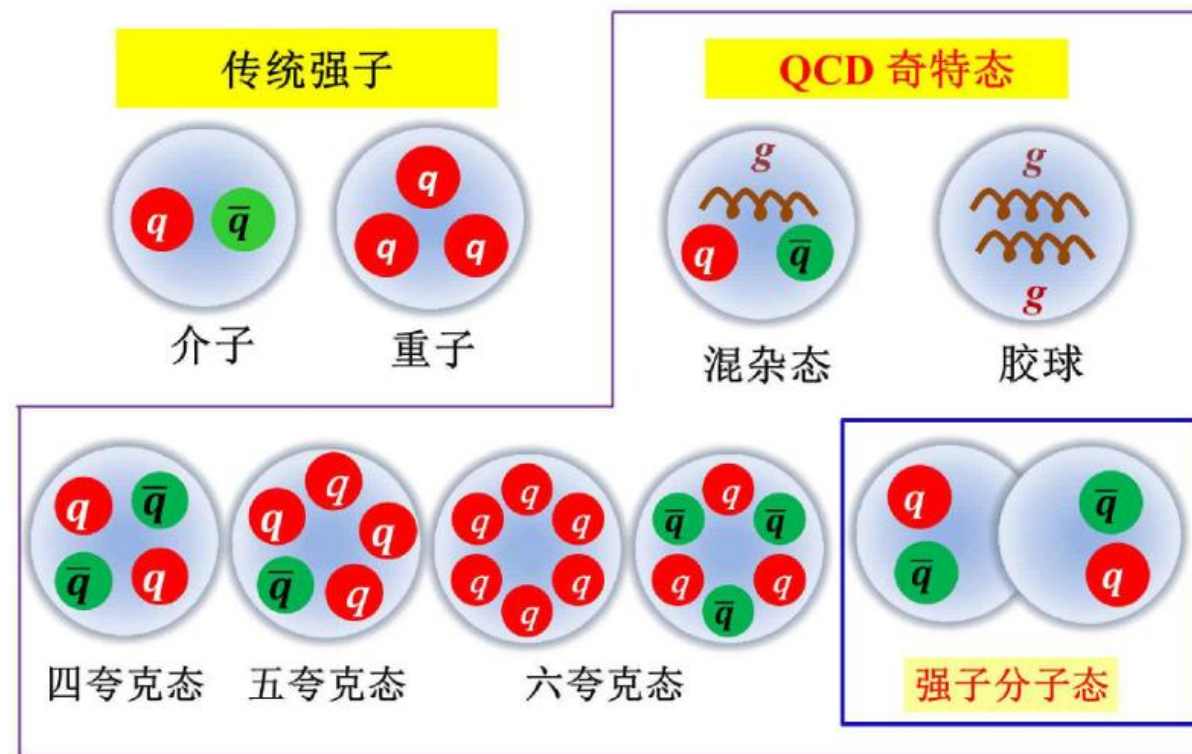
III. Numerical results: single-channel and coupled-channel analysis;

IV. Summary

1.1 Hadronic molecular state

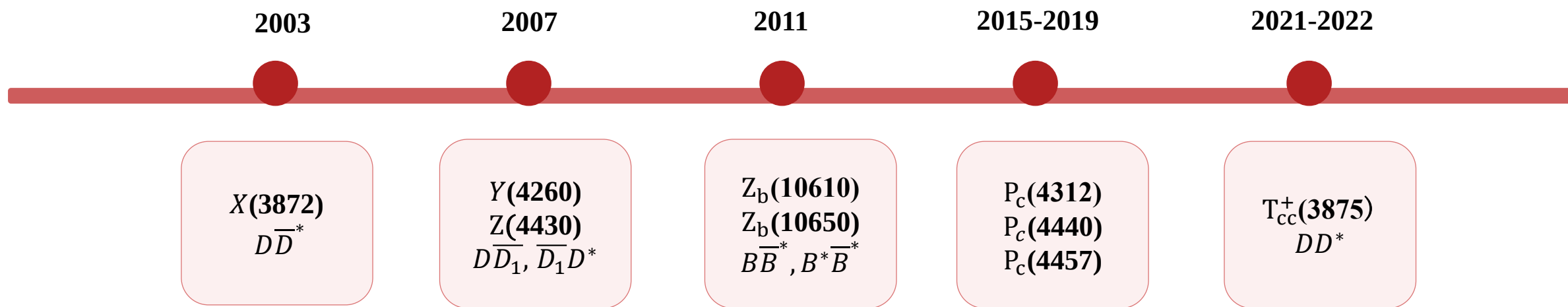
- The **hadronic molecular state** consists of two or more hadrons, which form weak binding via strong interactions.

1. Chin. Sci. Bull.59, 3815-3830 (2014).
2. PTEP 2016 no.6, 062C01 (2016).
3. Phys. Rept. 639, 1-121 (2016).
4. FewBody Syst. 57 no.12, 1185-1212 (2016).
5. Prog. Part. Nucl. Phys. 93, 143-194 (2017).
6. Rev.Mod. Phys. 90 no.1, 015003 (2018).
7. Rev. Mod. Phys. 90 no.1,015004 (2018).
8. Prog. Part. Nucl. Phys. 107,237-320 (2019).
9. Phys. Rept. 873, 1-154 (2020).
10. Phys. Rept. 1019, 1-149 (2023).
11. Rept. Prog. Phys. 86no.2, 026201 (2023).
12. Rev. Mod. Phys.98 (2026) no.2, 021001 (2026).
13. arXiv:2602.19887.



1.2 Experimental status

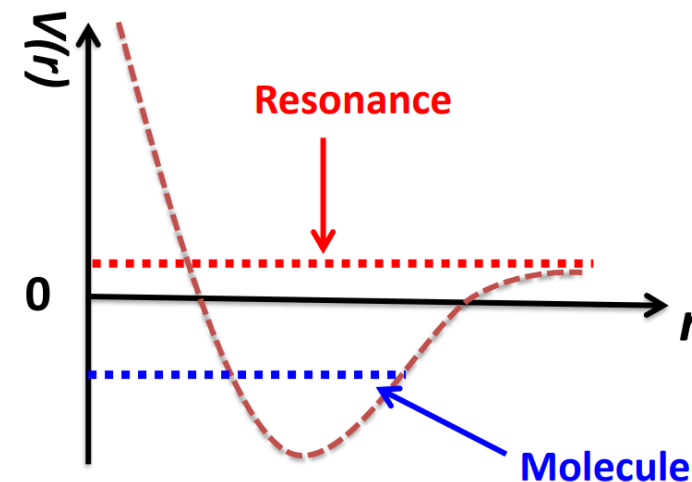
- Current studies have largely focused on meson-meson and meson-baryon systems in the charm sector:



- Compared to charmed hadronic molecules, research on their bottom counterparts has lagged, partly due to their **higher production thresholds** and **limited experimental data** in earlier years.

1.3 P-wave interactions

- The centrifugal barrier can suppress shallow **bound states**, while it can also sustain **resonances**.
- For a P-wave molecule, the orbital excitation flips the overall parity, leading to quantum numbers distinct from those of the S-wave systems.



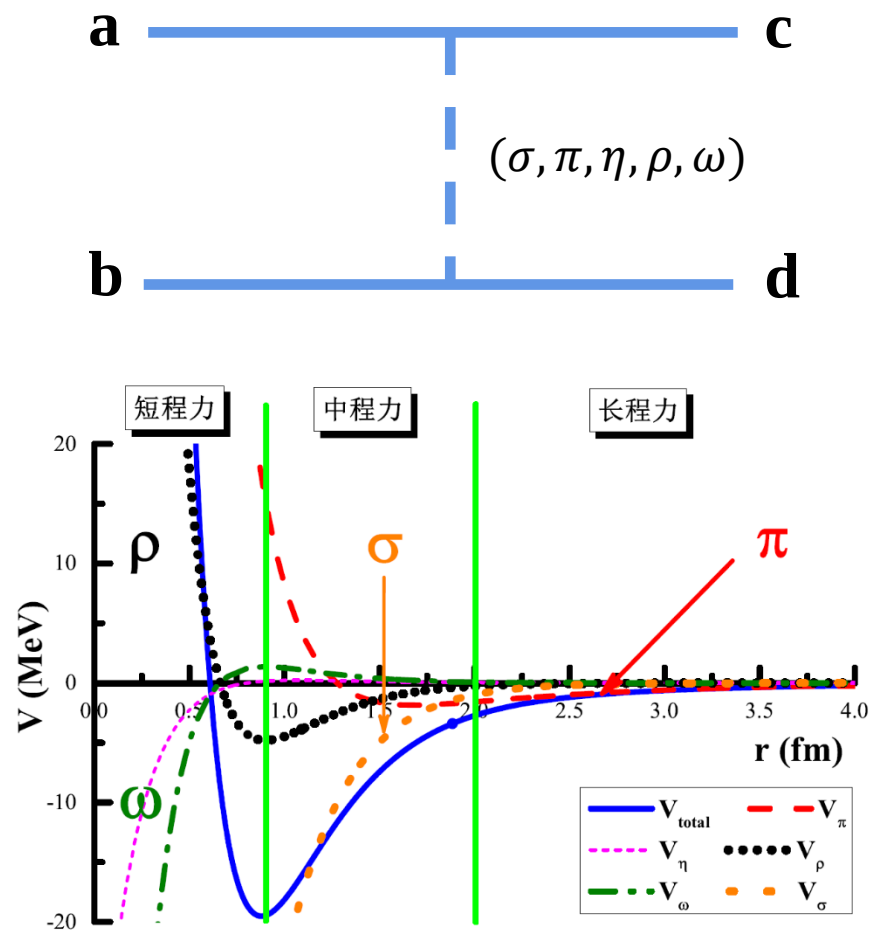
$$V_{\text{eff}}(r) = V(r) + \boxed{\frac{\hbar^2 l(l+1)}{2\mu r^2}} \longrightarrow \text{P-wave centrifugal barrier : } \frac{\hbar^2}{\mu r^2}$$

- Our results offer key theoretical insights into the interaction mechanisms of the **heavy-flavor baryon-meson** systems.
- May also help to clarify the internal structures of the observed **P_c** states.

2.1 OBE model

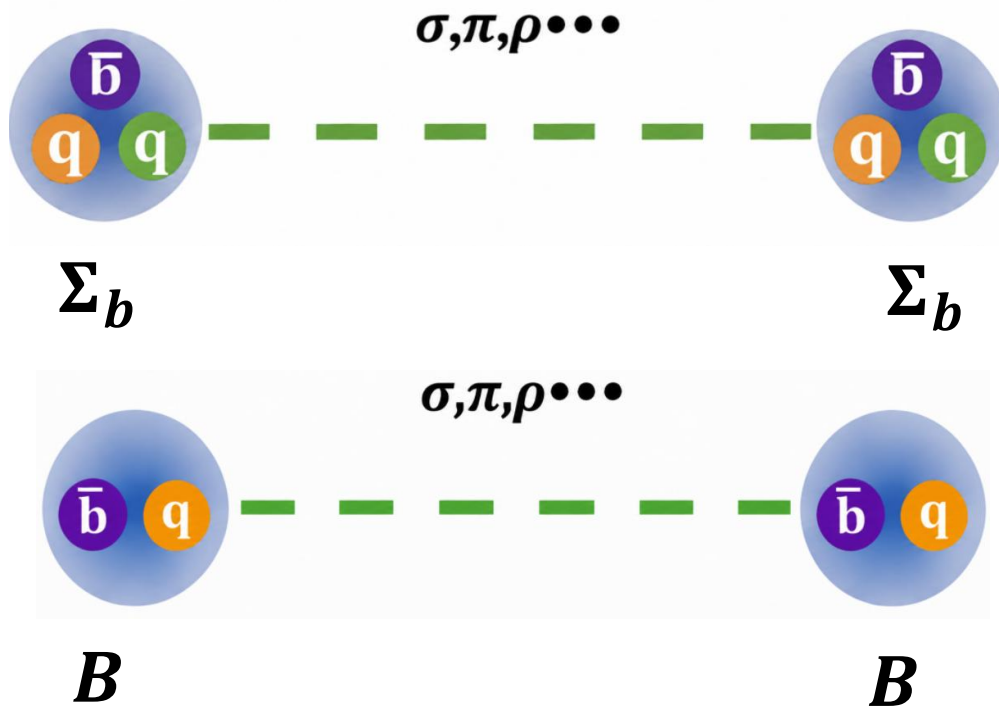
- 1935, Yukawa: **pion-exchange** and nucleon-nucleon interaction.
- In the OBE model, the interaction between two hadrons is mediated by the exchange of light mesons.
- Nijmegen potential and Bonn potential:
- ρ/σ exchange $\sim$ **two π** exchange;
- ω exchange $\sim$ **multi- π** exchange

Yukawa, Proc. Phys. Math. Soc. Japan 17, 48 (1935)



2 Theoretical framework

2.1 Effective Lagrangians



$g_s = 0.76$	$g = 0.59$	$\beta = 0.9$
$l_s = 6.2$	$g_1 = 0.94$	$\beta_s = -1.74$
$\lambda = 0.56 \text{ GeV}^{-1}$	$\lambda_s = -3.31 \text{ GeV}^{-1}$	$g_V = 5.8$

heavy quark symmetry and chiral symmetry;

$$\begin{aligned} \mathcal{L}_H = & g_s \langle \bar{H}_a^{(\bar{Q})} \sigma H_b^{(\bar{Q})} \rangle + i g \langle \bar{H}_a^{(\bar{Q})} \gamma_\mu \mathcal{A}_{ab}^\mu \gamma_5 H_b^{(\bar{Q})} \rangle \\ & - i \beta \langle \bar{H}_a^{(\bar{Q})} v_\mu (\mathcal{V}^\mu - \rho^\mu)_{ab} H_b^{(\bar{Q})} \rangle \\ & + i \lambda \langle \bar{H}_a^{(\bar{Q})} \sigma_{\mu\nu} F^{\mu\nu}(\rho) H_b^{(\bar{Q})} \rangle, \end{aligned}$$

$$\mathcal{L}_{\mathcal{B}_3} = l_B \langle \bar{\mathcal{B}}_3 \sigma \mathcal{B}_3 \rangle + i \beta_B \langle \bar{\mathcal{B}}_3 v^\mu (\mathcal{V}_\mu - \rho_\mu) \mathcal{B}_3 \rangle,$$

$$\begin{aligned} \mathcal{L}_{\mathcal{B}_6^{(\ell,*)}} = & l_S \langle \bar{S}_\mu \sigma S^\mu \rangle - \frac{3}{2} g_1 \epsilon^{\mu\nu\lambda\kappa} v_\kappa \langle \bar{S}_\mu \mathcal{A}_\nu S_\lambda \rangle \\ & + i \beta_S \langle \bar{S}_\mu v_\alpha (\mathcal{V}^\alpha - \rho^\alpha) S^\mu \rangle \\ & + \lambda_S \langle \bar{S}_\mu F^{\mu\nu}(\rho) S_\nu \rangle, \end{aligned}$$

$$\mathcal{L}_{\mathcal{B}_3 \mathcal{B}_6^{(\ell,*)}} = i g_4 \langle \bar{S}^\mu \mathcal{A}_\mu \mathcal{B}_3 \rangle + i \lambda_l \epsilon^{\mu\nu\lambda\kappa} v_\mu \langle \bar{S}_\nu F_{\lambda\kappa} \mathcal{B}_3 \rangle + \text{h.c.}$$

1. Chin. Phys. C 36, 6-13 (2012).
2. Phys. Rep. 281, 145 (1997).
3. Phys. Lett. B 292, 119(1992).
4. Phys. Rev.D 85, 014015 (2012).



2.1 OBE model

- Amplitude $M(a + b \rightarrow c + d)$
- Breit approximation $V(\vec{q}) = -M(a + b \rightarrow c + d) / \sqrt{2m_a 2m_b 2m_c 2m_d}$
- Fourier transform $V(r) = \int \frac{d^3 q}{(2\pi)^3} e^{i\vec{q} \cdot \vec{r}} V(\vec{q}) F^2(q^2, m_E^2)$
- Form factor $F(q^2, m_E^2) = \frac{\Lambda^2 - m^2}{\Lambda^2 - q^2}$

Form factor $F(q^2, m_E^2)$ (One free parameter $< 2\text{GeV}$), m and q are the cutoff, mass and four-momentum of the exchanged meson, respectively.

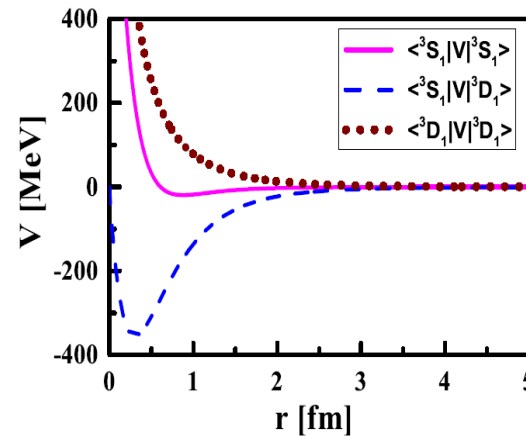
3.1 Molecule

- In judging the reasonableness of the loosely bound state, we adhere to the criterion based on:
- $\Lambda \sim 1 \text{ GeV}$
- E to be of the order of a few to several tens of MeV
- $r_{\text{RMS}} \sim 1 \text{ fm}$.

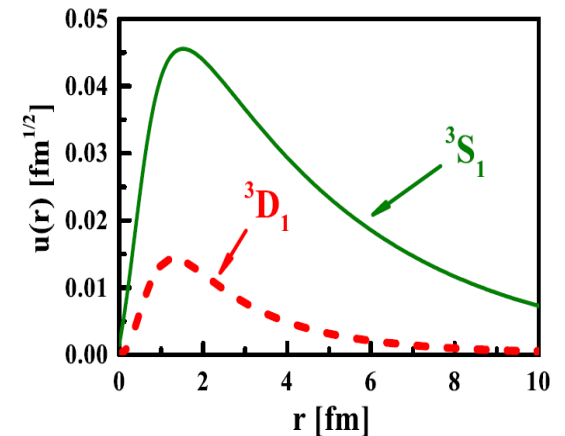
The cutoff parameter Λ , binding energy E , mass M , and radius r_{RMS} are given in units of GeV , MeV , MeV , and fm

Deuteron

loosely bound molecular state,
composed by a proton and a neutron



Effective potentials



Wave functions

$$I(J^P) = 0(1^+), \quad E = -2.225 \text{ MeV}, \quad R = 4.318 \text{ fm}$$

3.2 Resonances

Resonances {
 Shape-type
 Feshbach-type

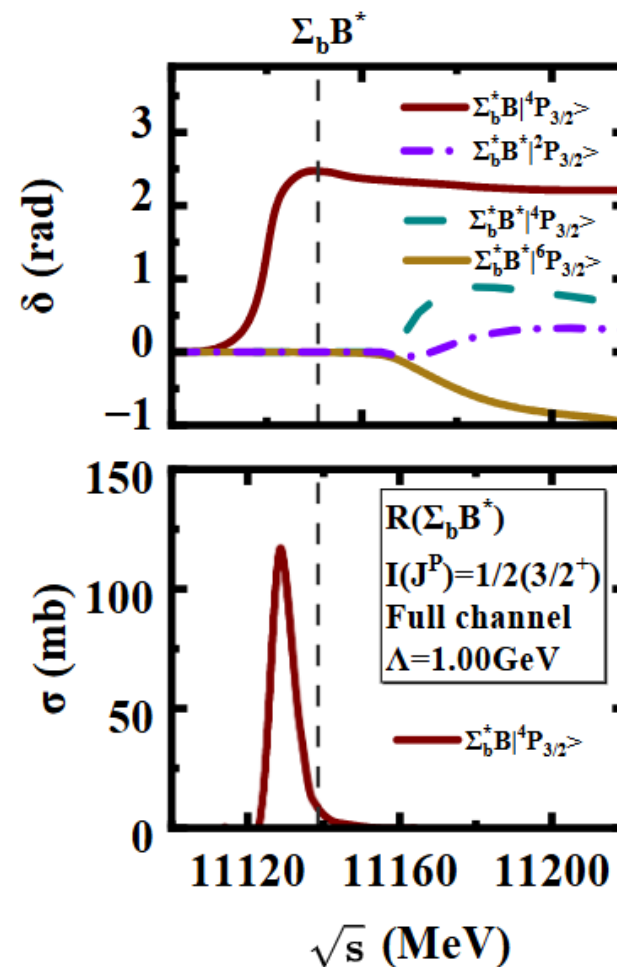
- Scattering cross section

$$\sigma_t = \frac{4\pi}{2\mu E} \sum_{l=0}^{\infty} (2l+1) \sin^2 \delta_l(E)$$

$$\delta_l(E_r) = (n + 1/2)\pi, \quad n = 0, 1, 2 \dots$$

$$\Gamma_r = 2 / \left(\frac{d\delta}{dE} \right)_{E_r}$$

- Mass: $M = M_{\Sigma_b^*} + M_B + E$



3.3 $\frac{1}{2}(\frac{1}{2}^+)$ system

$$\Lambda_b B / \Lambda_b B^* / \Sigma_b B / \Sigma_b^* B / \Sigma_b B^* / \Sigma_b^* B^*$$

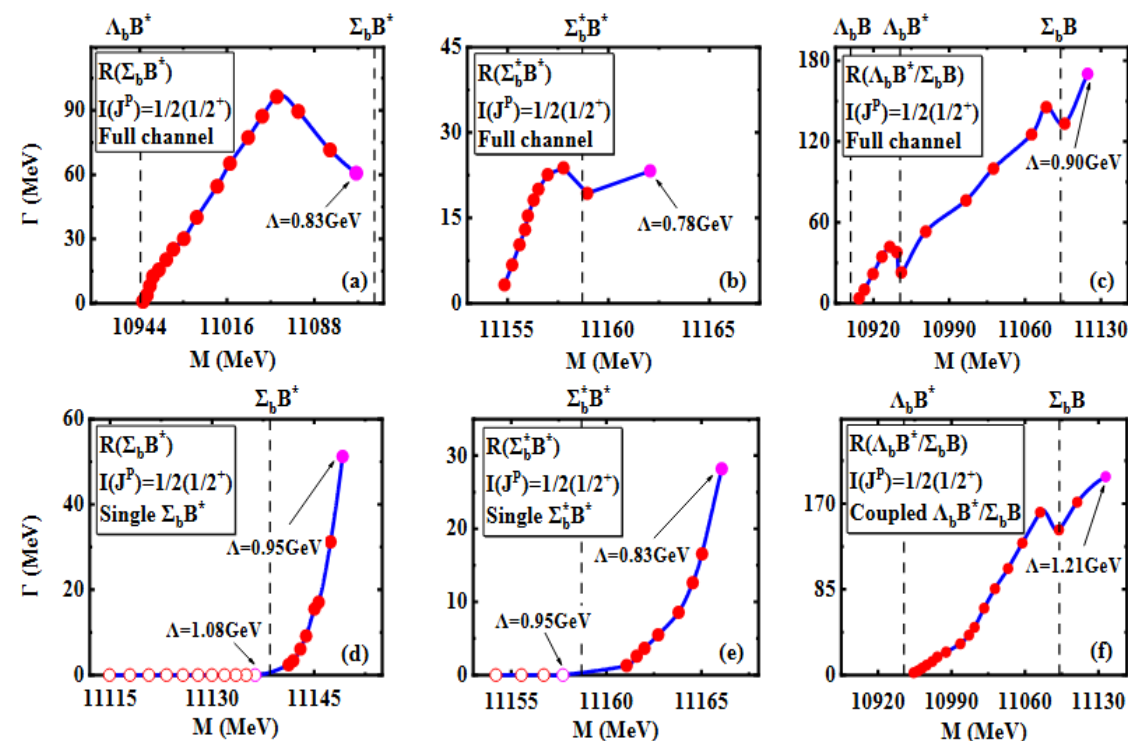
Bound states

Couple channel	Λ	E	r_{RMS}	$\Lambda_b B(^2P_{1/2})$	$\Lambda_b B^*(^2P_{1/2}/^4P_{1/2})$	$\Sigma_b B(^2P_{1/2})$	$\Sigma_b B^*(^2P_{1/2})$	$\Sigma_b B^*(^2P_{1/2}/^4P_{1/2})$	$\Sigma_b^* B(^2P_{1/2}/^4P_{1/2})$
	1.04	-0.97	0.90	42.26	19.25/0.17	5.42	1.01	3.36/4.96	22.33/1.24
	1.05	-10.05	0.52	29.42	23.09/0.24	5.81	1.62	5.50/4.97	27.44/1.91
	1.06	-20.99	0.45	23.49	24.28/0.46	5.72	2.03	7.13/4.62	29.92/2.35

Single channel

Λ	E	r_{RMS}	$\Sigma_b B^*(^2P_{1/2}/^4P_{1/2})$
1.08	-2.18	1.22	88.13/11.87
1.10	-5.00	0.98	89.70/10.30
1.12	-8.53	0.84	90.89/9.11
Λ	E	r_{RMS}	$\Sigma_b^* B^*(^2P_{1/2}/^4P_{1/2})$
0.95	-0.98	1.58	79.53/20.47
0.99	-6.02	0.99	82.40/17.60
1.03	-13.86	0.78	84.49/15.51

Resonances



$$I(J^P) = \frac{1}{2}(\frac{1}{2}^+)$$

$$\Sigma_b B^*, \Sigma_b^* B^*$$

$$\Lambda_b B^* / \Sigma_b B$$



good molecular candidates



Feshbach-type Resonance

3.4 $\frac{1}{2}(\frac{3}{2}^+)$ system

$$\Lambda_b B / \Lambda_b B^* / \Sigma_b B / \Sigma_b^* B / \Sigma_b B^* / \Sigma_b^* B^*$$

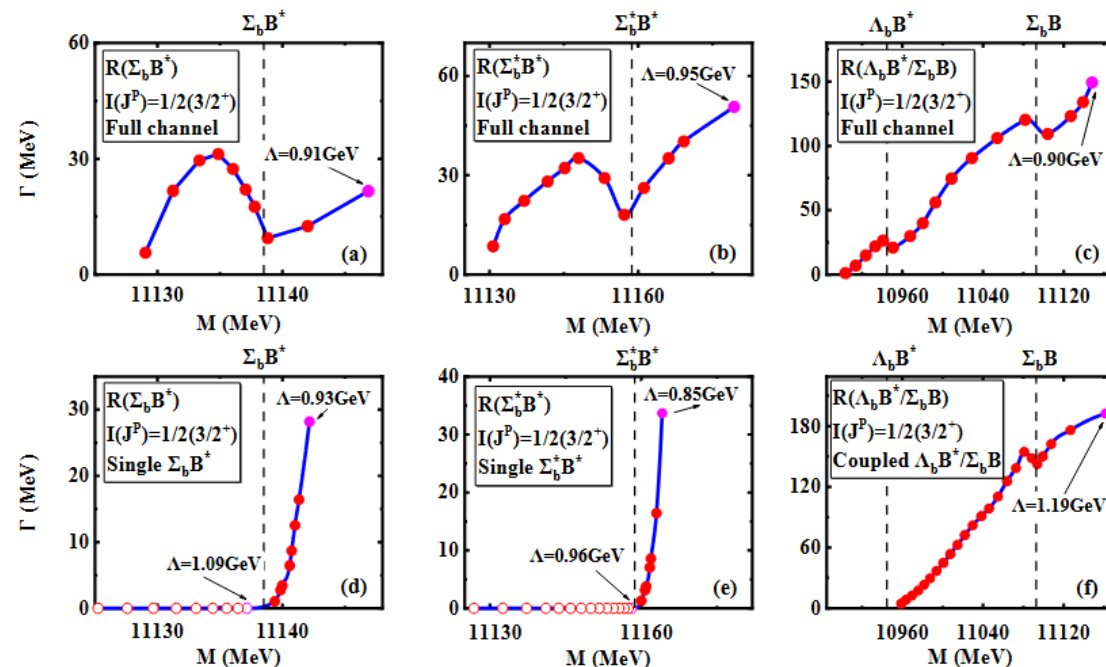
Bound states

Couple channel	Λ	E	r_{RMS}	$\Lambda_b B(^2P_{3/2})$	$\Lambda_b B^*(^2P_{3/2}/^4P_{3/2})$	$\Sigma_b B(^2P_{3/2})$	$\Sigma_b B^*(^4P_{3/2})$	$\Sigma_b B^*(^2P_{3/2}/^4P_{3/2})$	$\Sigma_b^* B(^2P_{3/2}/^4P_{3/2}/^6P_{3/2})$
1.07	-5.5	0.49	23.33		<u>26.14/0.97</u>	4.80	0.14	<u>6.44/1.02</u>	<u>35.90/1.19/0.07</u>
1.08	-18.14	0.40	17.70		<u>27.50/0.87</u>	4.93	0.16	<u>7.98/0.93</u>	<u>38.69/1.21/0.03</u>
1.09	-32.23	0.37	14.94		<u>27.72/0.77</u>	4.91	0.17	<u>9.15/0.84</u>	<u>40.30/1.18/0.02</u>

Single channel

Λ	E	r_{RMS}	$\Sigma_b B^*(^2P_{3/2}/^4P_{3/2})$
1.11	-2.96	1.35	<u>54.30/45.70</u>
1.13	-5.41	1.07	<u>67.98/32.02</u>
1.15	-8.83	0.88	<u>74.41/21.59</u>
Λ	E	r_{RMS}	$\Sigma_b^* B^*(^2P_{3/2}/^4P_{3/2}/^6P_{3/2})$
0.96	-0.63	1.98	<u>36.13/63.47/0.40</u>
0.99	-3.10	1.27	<u>49.36/49.83/0.81</u>
1.02	-7.03	0.98	<u>61.49/37.33/1.18</u>

Resonances



$$I(J^P) = \frac{1}{2}(\frac{3}{2}^+)$$

$$\Sigma_b B^*, \Sigma_b^* B^*$$

$$\Lambda_b B^* / \Sigma_b B$$

→ good molecular candidates

→ Feshbach-type Resonance

3.5 $\frac{1}{2}(\frac{5}{2}^+)$ system

$$\Lambda_b B^* / \Sigma_b^* B / \Sigma_b B^* / \Sigma_b^* B^*$$

Bound states

Couple channel	Λ	E	r_{RMS}	$\Lambda_b B^*(^4P_{\frac{5}{2}})$	$\Sigma_b^* B(^4P_{\frac{5}{2}})$	$\Sigma_b B^*(^4P_{\frac{5}{2}})$	$\Sigma_b^* B^*(^4P_{\frac{5}{2}}/^6P_{\frac{5}{2}})$
	1.10	-2.38	0.69	56.88	<u>15.39</u>	0.41	<u>27.27/0.05</u>
	1.11	-10.20	0.50	50.81	<u>17.47</u>	0.41	<u>31.28/0.03</u>
	1.12	-19.12	0.44	47.09	<u>18.66</u>	0.40	<u>33.83/0.02</u>

Single channel	Λ	E	r_{RMS}	$\Sigma_b^* B^*(^4P_{\frac{3}{2}}/^6P_{\frac{3}{2}})$
	1.10	-0.25	3.05	1.81/ 98.19
	1.30	-4.50	1.49	4.49/ 95.50
	1.50	-12.51	1.07	12.85/ 87.15

$$I(J^P) = \frac{1}{2}(\frac{3}{2}^+)$$

$$\begin{array}{c} \Sigma_b^* B^* \\ \Lambda_b B^* / \Sigma_b^* B / \Sigma_b B^* \end{array}$$

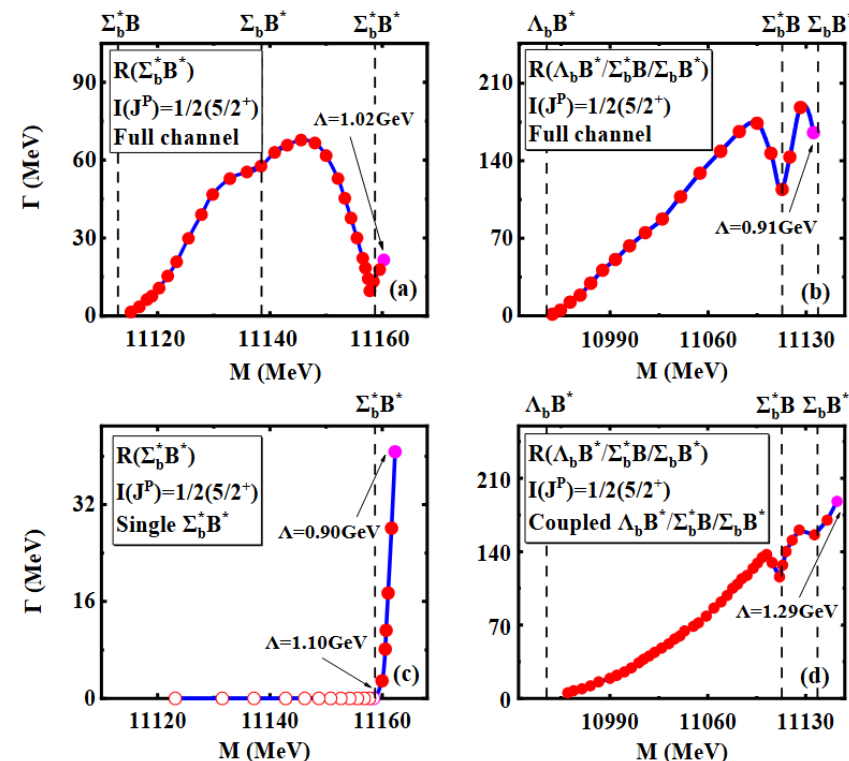


good molecular candidates



Feshbach-type Resonance

Resonances



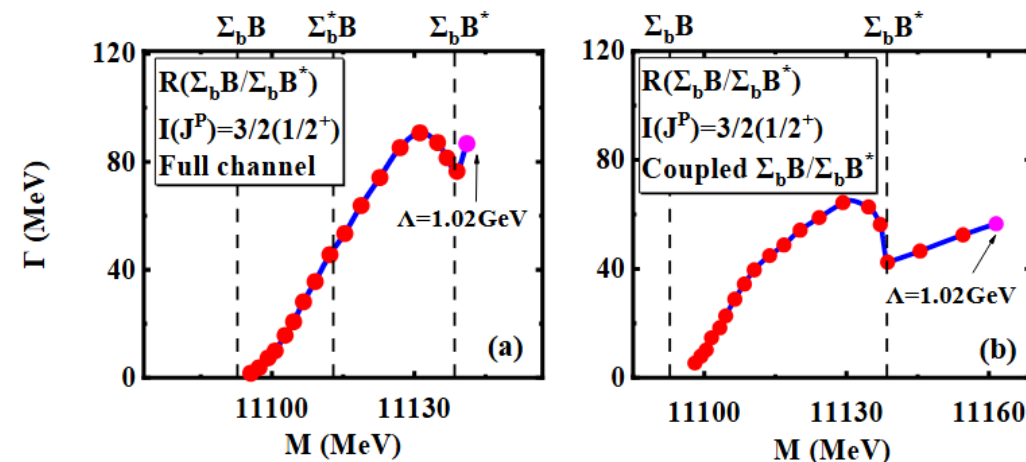
3.6 $\frac{3}{2}(\frac{1}{2}^+)$ system

$$\Sigma_b B / \Sigma_b^* B / \Sigma_b B^* / \Sigma_b^* B^*$$

Bound states

Couple channel	Λ	E	r_{RMS}	$\Sigma_b B(^2P_{\frac{1}{2}})$	$\Sigma_b^* B(^2P_{\frac{1}{2}})$	$\Sigma_b B^*(^2P_{\frac{1}{2}}/^4P_{\frac{1}{2}})$	$\Sigma_b^* B^*(^2P_{\frac{1}{2}}/^4P_{\frac{1}{2}})$
	1.21	-0.11	1.79	61.45	2.72	1.10 / 32.98	$\sim 0 / 1.75$
	1.23	-4.61	0.86	47.14	5.15	1.21 / 43.18	$\sim 0 / 3.32$
	1.25	-11.12	0.69	38.83	7.73	1.04 / 47.34	$\sim 0 / 5.06$

Resonances



- The $I = 3/2$ systems are expected to behave differently from the $I = 1/2$.
- The attractive interaction mediated by exchanged mesons is generally weakened, and larger cut-off values are usually required to obtain the bound states or resonances.

$$\Sigma_b B / \Sigma_b B^*$$



Feshbach-type Resonance

3.7 $\frac{3}{2}(\frac{3}{2}^+)$ system

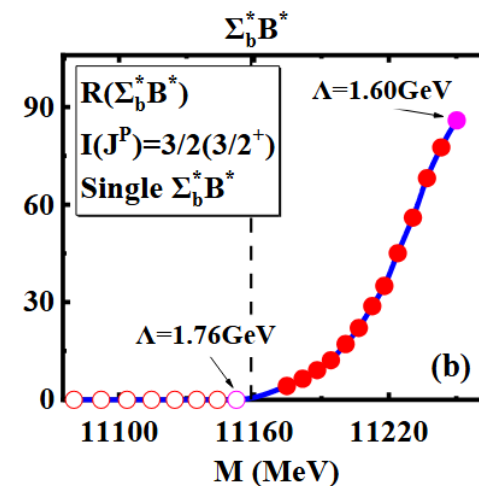
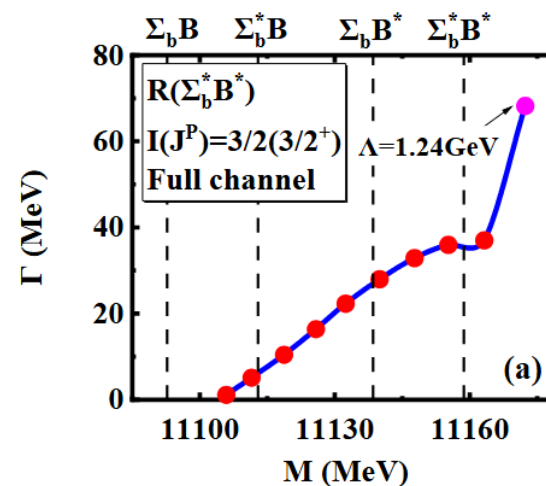
$$\Sigma_b B / \Sigma_b^* B / \Sigma_b B^* / \Sigma_b^* B^*$$

Bound states

Couple channel	Λ	E	r_{RMS}	$\Sigma_b B(^2P_{3/2})$	$\Sigma_b^* B(^4P_{3/2})$	$\Sigma_b B^*(^2P_{3/2}/^4P_{3/2})$	$\Sigma_b^* B^*(^2P_{3/2}/^4P_{3/2}/^6P_{3/2})$
	1.35	-5.69	0.46	7.41	<u>34.14</u>	<u>0.06 / 37.96</u>	<u>0.01 / 17.86 / 2.56</u>
	1.36	-17.16	0.38	4.79	<u>34.62</u>	<u>0.03 / 39.45</u>	<u>0.01 / 19.30 / 1.80</u>
	1.37	-29.79	0.34	3.54	<u>34.67</u>	<u>0.02 / 40.18</u>	<u>0.01 / 20.25 / 1.33</u>

Single channel	Λ	E	r_{RMS}	$\Sigma_b^* B^*(^2P_{3/2}/^4P_{3/2}/^6P_{3/2})$
	1.752	-0.56	1.20	2.34 / 0.68 / 96.98
	1.760	-6.79	0.91	1.52 / 0.28 / 98.02
	1.768	-13.17	0.78	0.68 / 0.03 / 99.29

Resonances



$$\Sigma_b^* B^* \quad I(J^P) = \frac{3}{2}(\frac{3}{2}^+)$$



molecular candidate

3.8 $\frac{3}{2}(\frac{5}{2}^+)$ system

$$\Sigma_b^* B / \Sigma_b B^* / \Sigma_b^* B^*$$

Bound states

Couple channel	Λ	E	r_{RMS}	$\Sigma_b^* B(^4P_{\frac{5}{2}})$	$\Sigma_b B^*(^4P_{\frac{5}{2}})$	$\Sigma_b^* B^*(^4P_{\frac{5}{2}}/^6P_{\frac{5}{2}})$
	1.32	-7.12	0.45	38.59	38.67	<u>22.73/ 0.01</u>
	1.33	-16.24	0.40	37.37	39.37	<u>23.25/0.01</u>
	1.34	-26.22	0.38	36.65	39.76	<u>23.58/ 0.01</u>

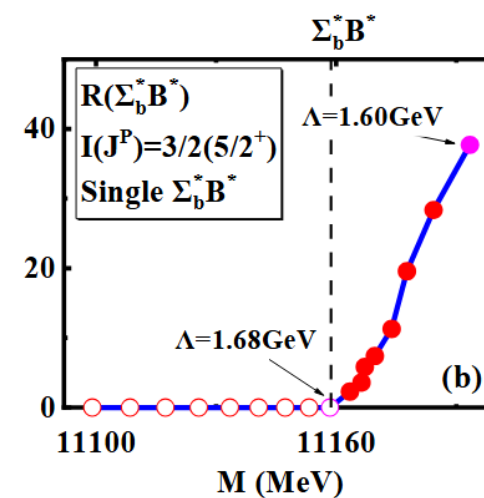
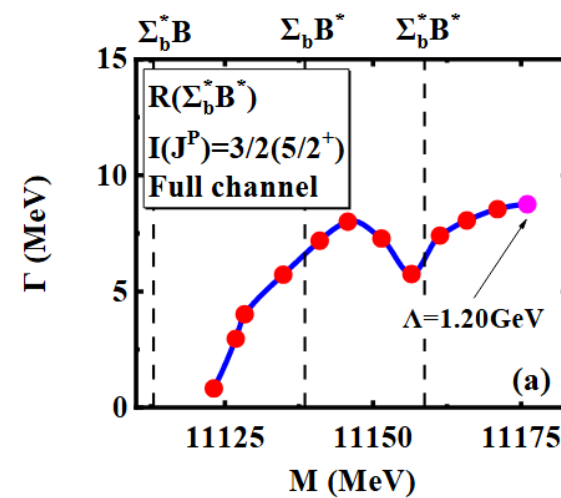
Single channel	Λ	E	r_{RMS}	$\Sigma_b^* B^*(^4P_{\frac{5}{2}}/^6P_{\frac{5}{2}})$
	1.68	-0.25	1.13	2.45/ 97.55
	1.69	-6.47	0.87	1.48/ 98.52
	1.70	-12.45	0.70	0.17/ 99.83

$$\Sigma_b^* B^* \quad I(J^P) = \frac{3}{2}(\frac{5}{2}^+)$$



good molecular candidate

Resonances



- In this work, we have systematically studied the possible hidden-bottom molecular pentaquark states arising from the **P-wave** $\Lambda_b B^{(*)} / \Sigma_b^{(*)} B^{(*)}$ interactions within the **OBE model**.

$I(J^P)$	$\frac{1}{2}(\frac{1}{2}^+)$	$\frac{1}{2}(\frac{3}{2}^+)$	$\frac{1}{2}(\frac{5}{2}^+)$	$\frac{3}{2}(\frac{1}{2}^+)$	$\frac{3}{2}(\frac{3}{2}^+)$	$\frac{3}{2}(\frac{5}{2}^+)$
Molecules	$\Sigma_b B^*$ $\Sigma_b^* B^*$	$\Sigma_b B^*$ $\Sigma_b^* B^*$	$\Sigma_b^* B^*$		$\Sigma_b^* B^*$	$\Sigma_b^* B^*$
Feshbach-type	$\Lambda_b B^* / \Sigma_b B$	$\Lambda_b B^* / \Sigma_b B$	$\Lambda_b B^* / \Sigma_b^* B$ $\Sigma_b B / \Sigma_b B^*$	$\Sigma_b B / \Sigma_b B^*$		

- The identification of such states would offer crucial insights into the nature of exotic hadrons and deepen our understanding of the interaction mechanisms between heavy baryons and heavy mesons.



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Thanks for your attention

