

第一届强相互作用自旋物理会议

The 1st Conference on Strong-Interaction Spin Physics

Qingdao, China

28 July, 2026

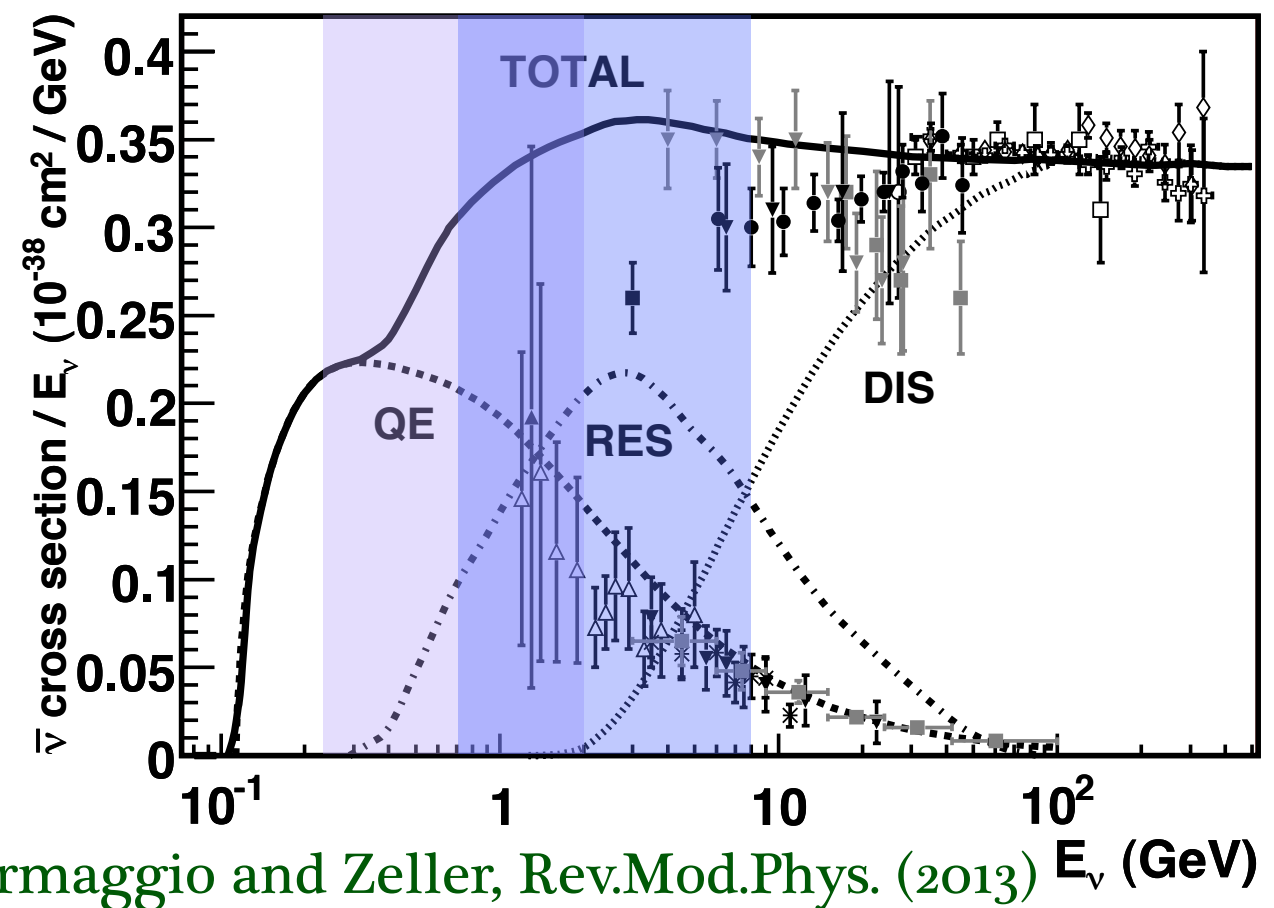
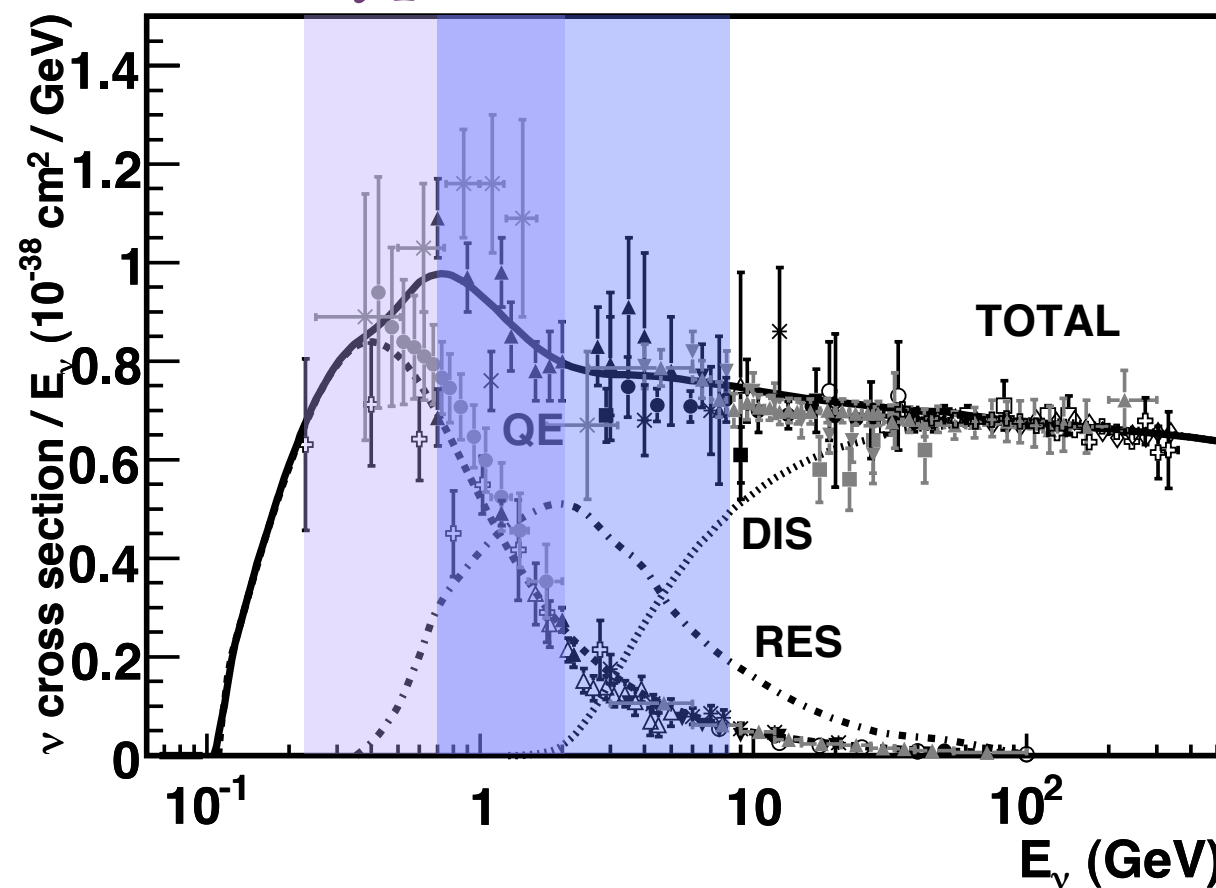
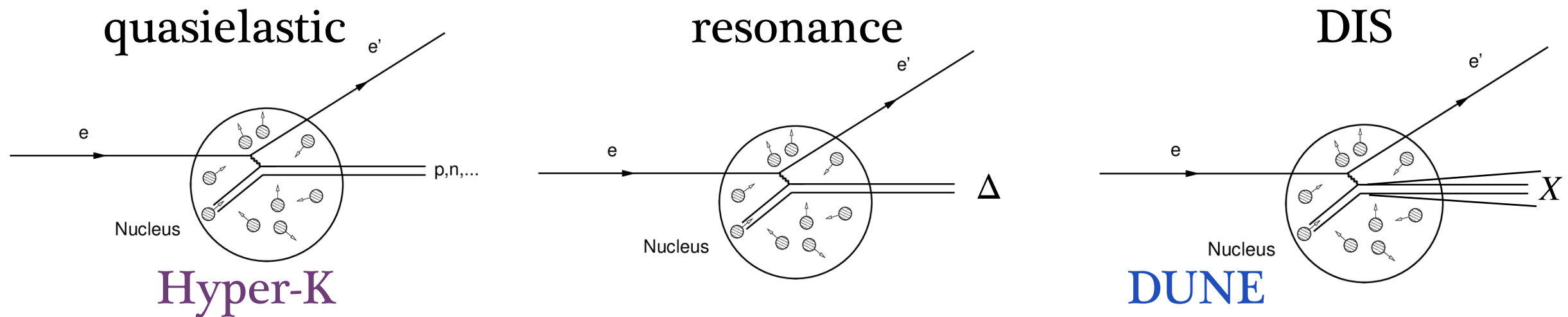
Radiative corrections in (anti)neutrino-nucleon scattering and nucleon structure



托马拉克

Sasha Tomalak

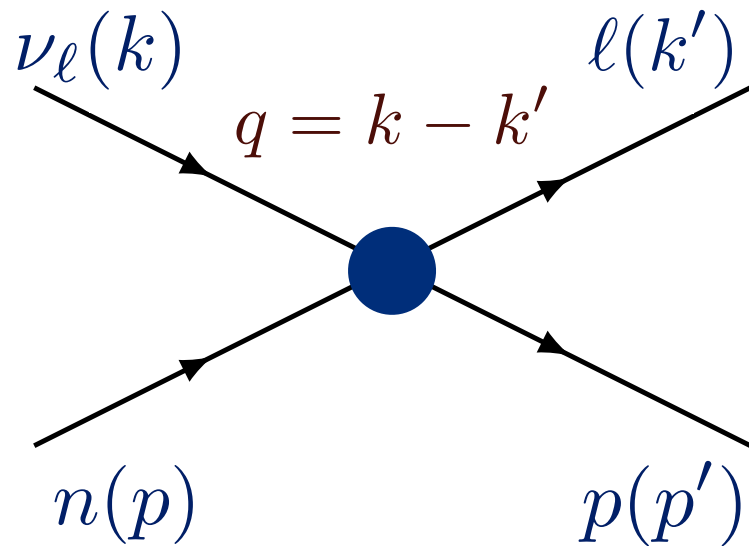
Interaction mechanisms



Formaggio and Zeller, Rev.Mod.Phys. (2013)

- significant overlap with prior and modern JLab energy range
- DUNE experimental program requires 3-5 % precise cross sections

Elastic scattering on free nucleon



neutrino energy

$$E_\nu$$

momentum transfer

$$Q^2 = -q^2$$

contact interaction at GeV energies

- assuming isospin symmetry, nucleon current:

$$\Gamma^\mu(Q^2) = \langle p | \bar{u} (\gamma^\mu - \gamma^\mu \gamma_5) d | n \rangle$$

$$\Gamma^\mu(Q^2) = \gamma^\mu F_D^V(Q^2) + \frac{i\sigma^{\mu\nu} q_\nu}{2M} F_P^V(Q^2) + \gamma^\mu \gamma_5 F_A(Q^2) + \frac{q^\mu}{M} \gamma_5 F_P(Q^2)$$

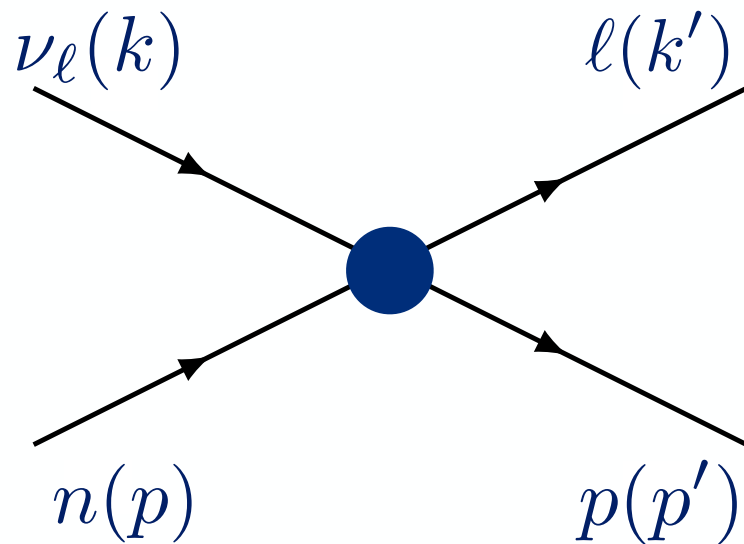
form factors: isovector Dirac and Pauli axial and pseudoscalar

$$F_{D,P}^V = F_{D,P}^p - F_{D,P}^n$$

tree-level amplitude

$$T = \frac{G_F V_{ud}}{\sqrt{2}} (\bar{\ell}(k') \gamma_\mu (1 - \gamma_5) \nu_\ell(k)) (\bar{p}(p') \Gamma^\mu(Q^2) n(p))$$

Elastic scattering on free nucleon



$$\nu = E_\nu/M - \tau - r^2$$

$$r = \frac{m_\ell}{2M} \quad \tau = \frac{Q^2}{4M^2}$$

unpolarized cross section

$$\frac{d\sigma}{dQ^2} \sim \frac{M^2}{E_\nu^2} \left((\tau + r^2) A(Q^2) - \nu B(Q^2) + \frac{\nu^2}{1 + \tau} C(Q^2) \right)$$

Llewellyn Smith (1972)

- structure-dependent functions

$$A = \tau (G_M^V)^2 - (G_E^V)^2 + (1 + \tau) F_A^2 - \underbrace{r^2 \left((G_M^V)^2 + F_A^2 - 4\tau F_P^2 + 4F_A F_P \right)}$$

$$B = \pm 4\tau F_A G_M^V$$

$$C = \tau (G_M^V)^2 + (G_E^V)^2 + (1 + \tau) F_A^2$$

- **pseudoscalar** form factor contribution is suppressed by lepton mass
- cross section is sensitive to both **vector** and **axial** contributions

Elastic scattering on free nucleon

- only 3 experiments performed with deuterium bubble chamber
- direct access to form-factor shape

ANL 1982: 1737 events

BNL 1981: 1138 events

FNAL 1983: 362 events

world data: ~3200 events

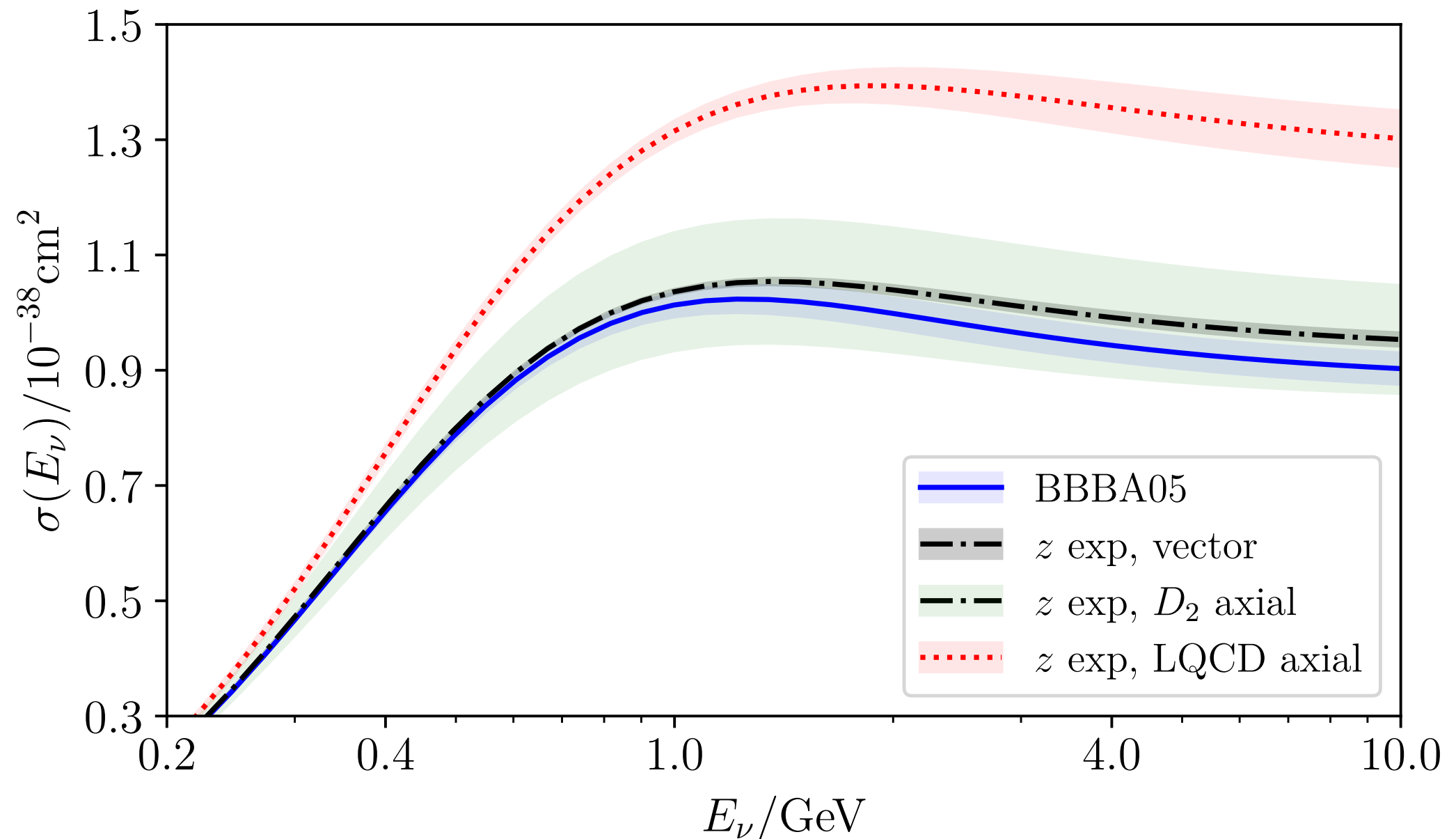


Fermilab bubble chamber, Richard Drew

- axial form factor extracted based on electromagnetic structure

A.S. Meyer, M. Betancourt, R. Gran and R.J. Hill, PRD (2016)

Neutrino-nucleon scattering (CC)



A.S. Meyer, A. Walker-Loud, C. Wilkinson, Ann. Rev. of 72, 010622-120608 (2022)

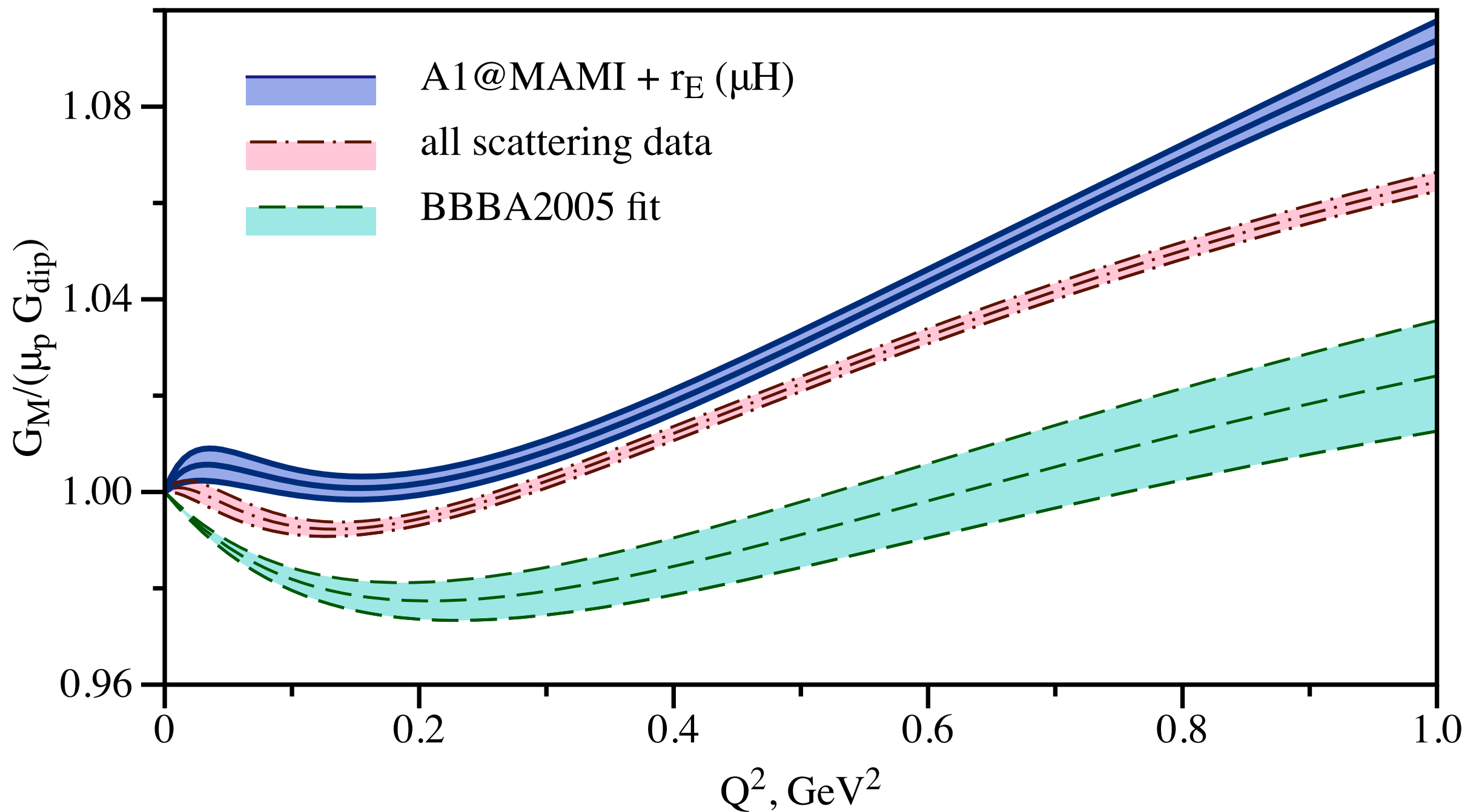
A.S. Meyer, M. Betancourt, R. Gran, and R.J. Hill, PRD (2016)

Kaushik Borah, Gabriel Lee, Richard J. Hill, and O.T. , PRD (2021)

- acknowledged discrepancy: lattice QCD $\leftrightarrow$ experimental data

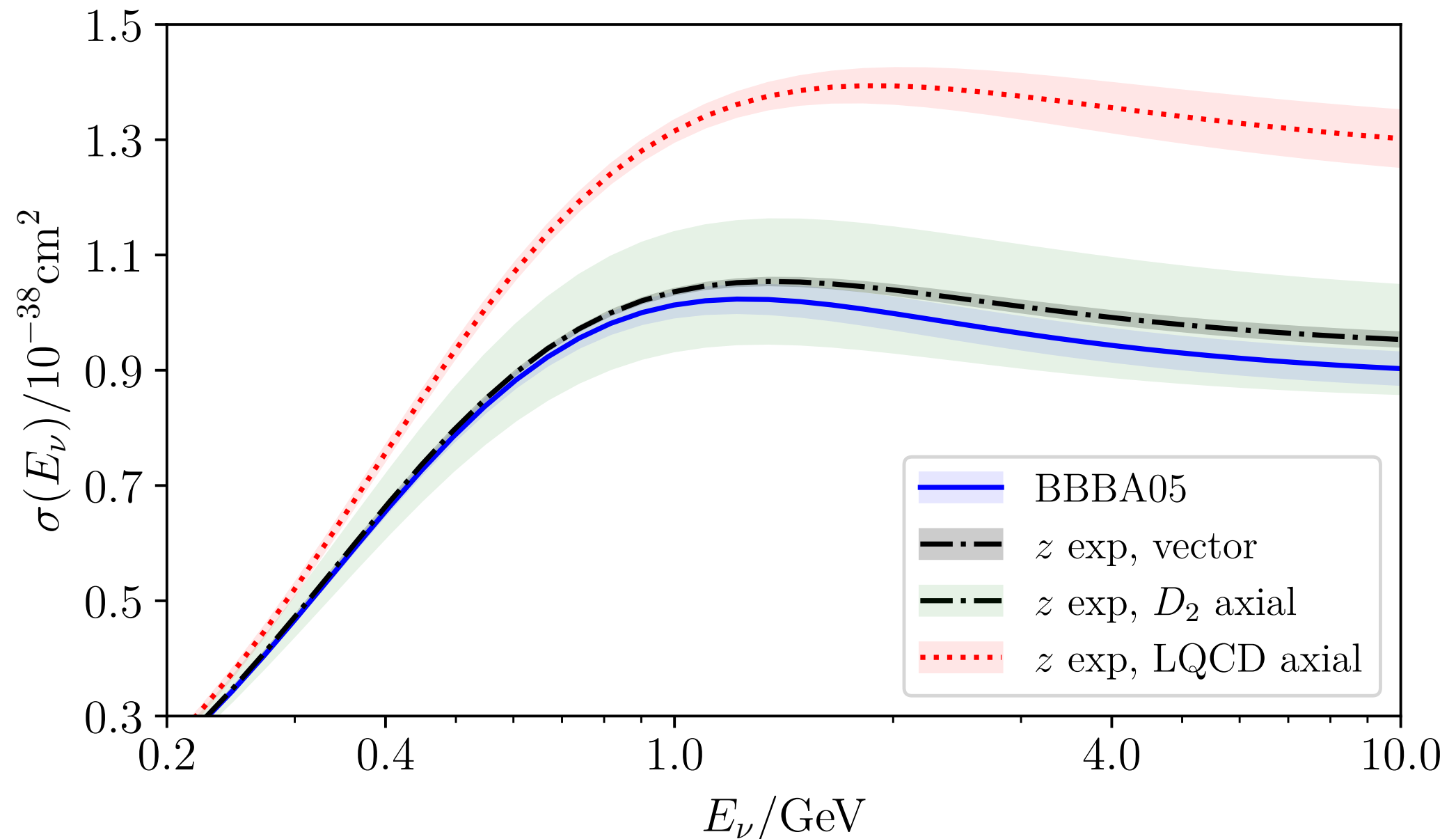
Origin of difference

- fits of proton magnetic form factor:



- proton magnetic form factor has to be precisely measured again

Neutrino-nucleon scattering (CC)



A.S. Meyer, A. Walker-Loud, C. Wilkinson, Ann. Rev. of 72, 010622-120608 (2022)

A.S. Meyer, M. Betancourt, R. Gran, and R.J. Hill, PRD (2016)

Kaushik Borah, Gabriel Lee, Richard J. Hill, and O.T. , PRD (2021)

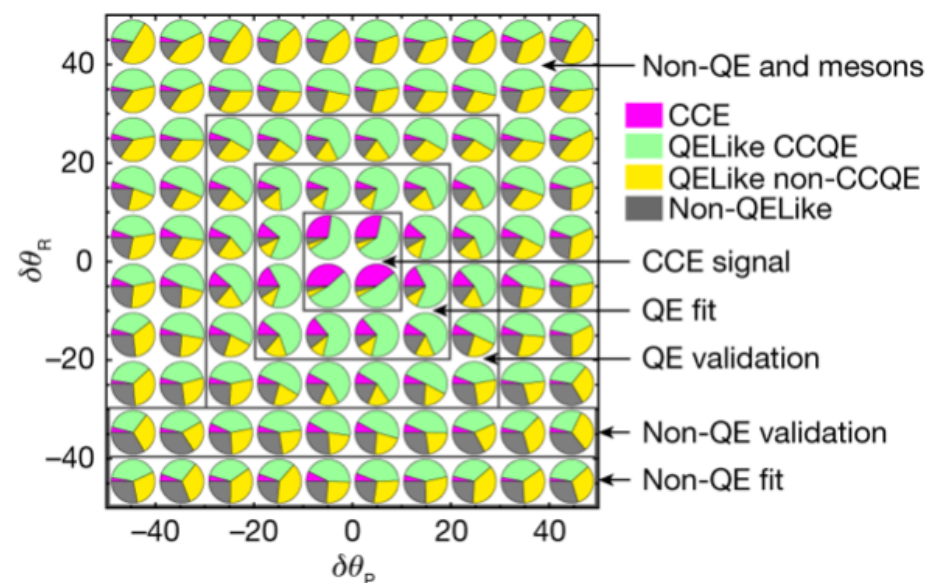
- acknowledged discrepancy: lattice QCD $\leftrightarrow$ experimental data

MINERvA result with free protons

- idea of scattering on molecular hydrogen realized !!!

$$\bar{\nu}_\mu p \rightarrow \mu^+ n$$

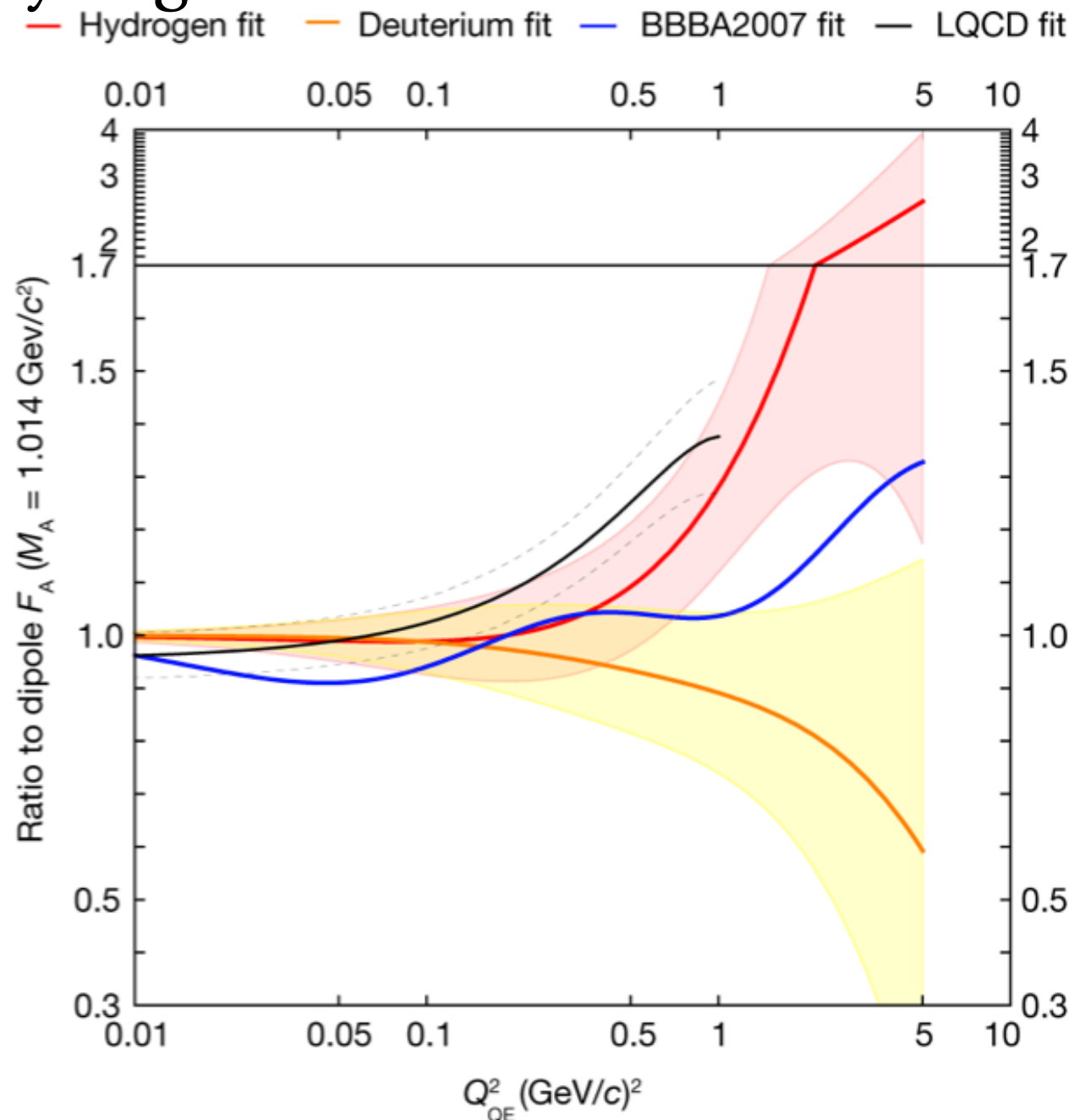
kinematic selection



5580 events over
12500 background

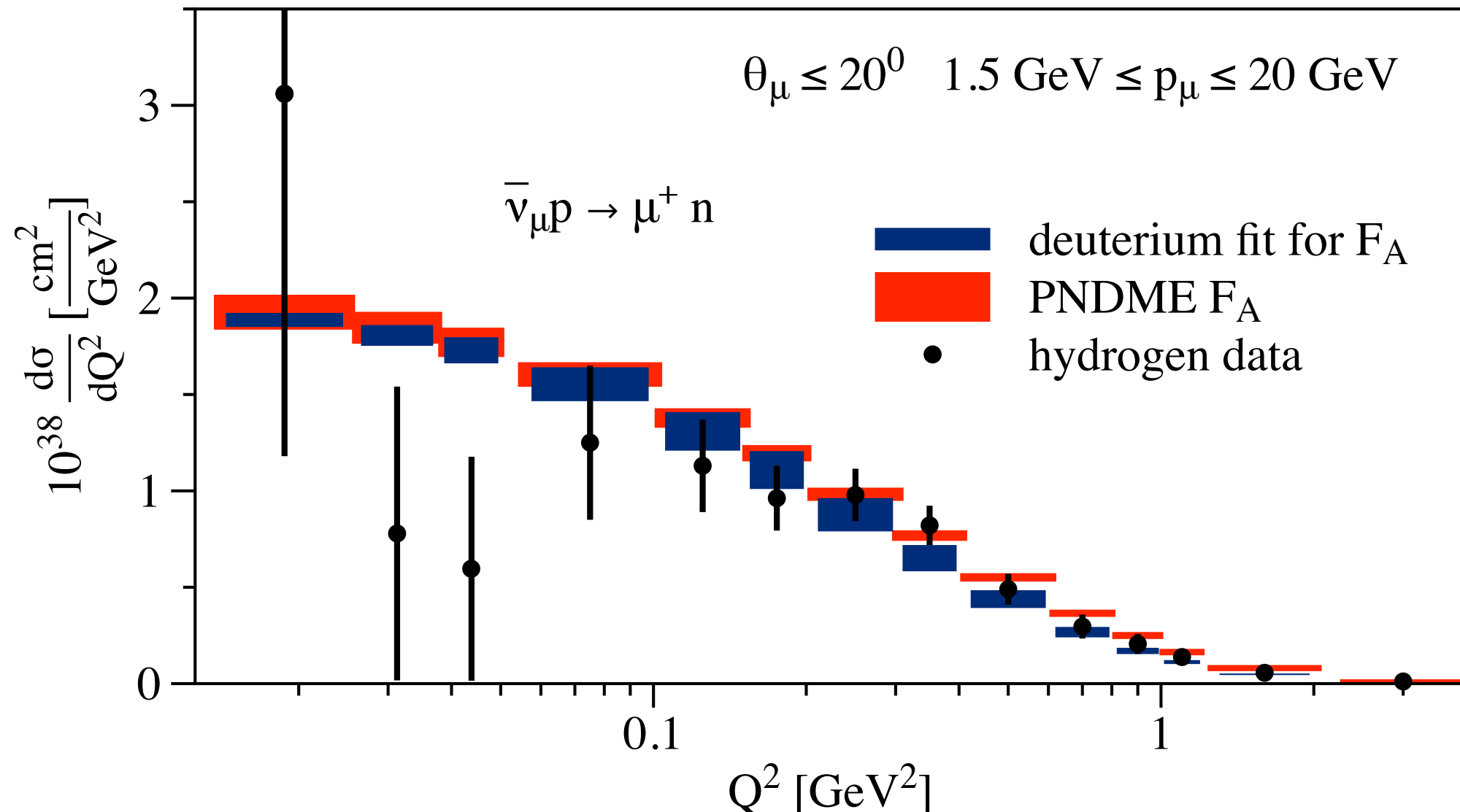
background nuclear events
constrained by scattering of ν

- 1st measurement of axial form factor on “free” protons $\bar{\nu}_\mu p \rightarrow \mu^+ n$



Lattice QCD vs MINERvA

- PNDME 2023 axial-vector form factor as representative of lattice QCD



- $\lesssim 1\sigma$ agreement for each bin besides two at small Q^2

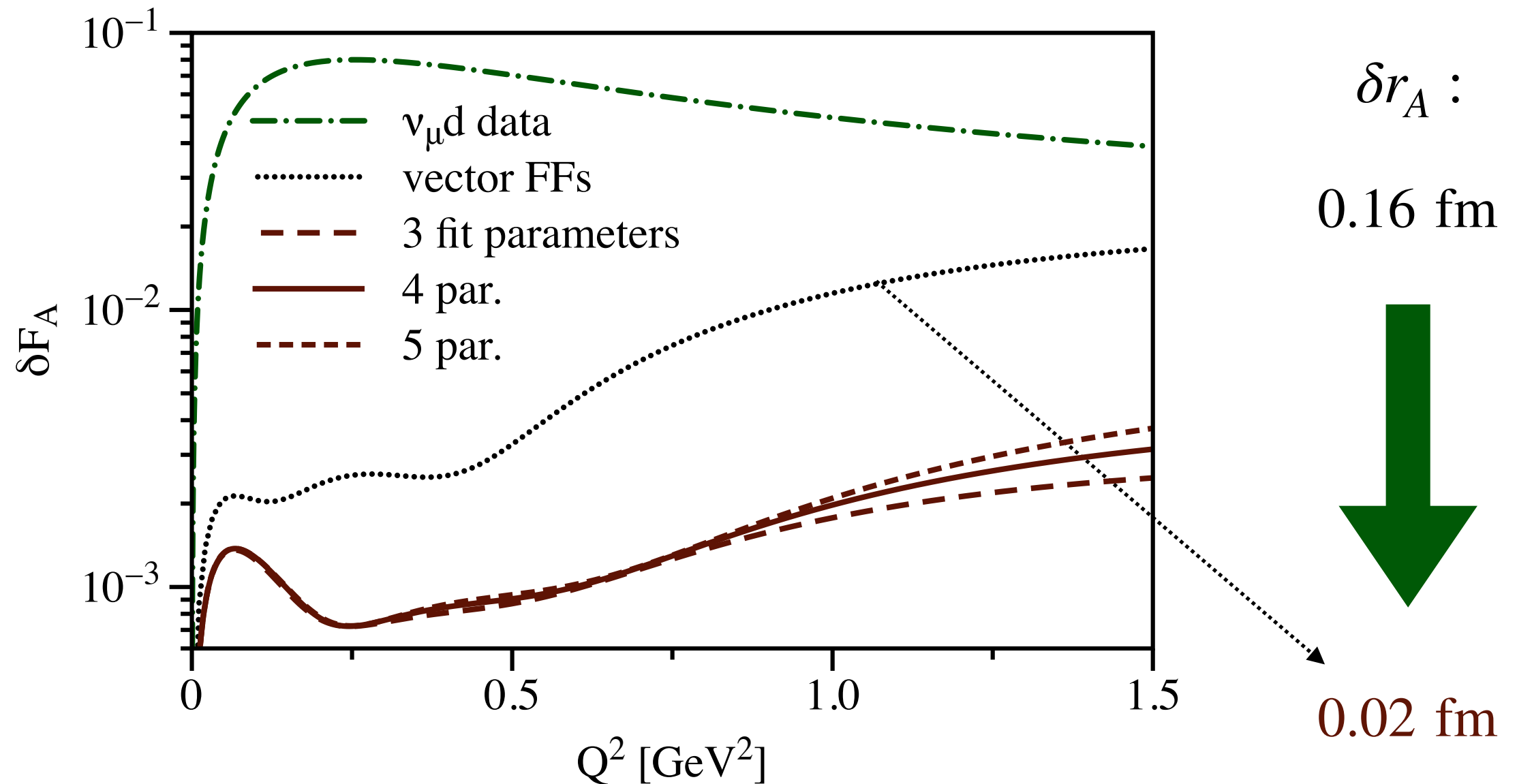
- 2-3 σ tension between lattice QCD and deuterium data
- MINERvA hydrogen data consistent with LQCD and deuterium

O.T, Rajan Gupta, and Tanmoy Bhattacharya, PRD (2023)

DUNE projections

- estimates for 700 kg of H in Straw Tube Tracker at near detector

H. Duyang, B. Guo, S. R. Mishra, and R. Petti, PLB (2019)



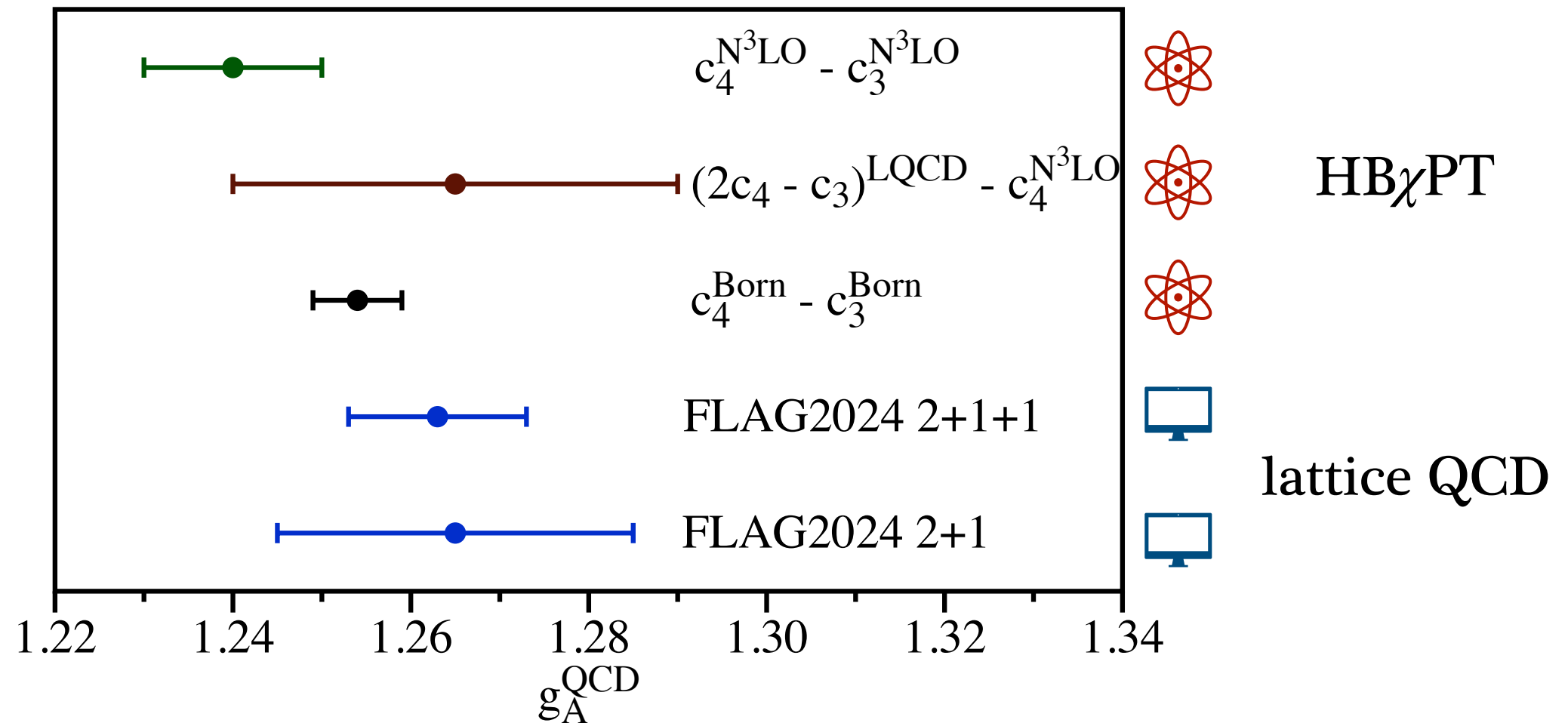
- order of magnitude improvement in axial form factor and radius
- DUNE will probe vector form factors and isospin symmetry

Roberto Petti, O.T., and Richard J. Hill, letter in PRD (2024)

Nucleon axial-vector charge

- effective field theory approach to low-energy charged currents

Standard Model $\rightarrow$ LEFT $\rightarrow$ HB χ PT $\rightarrow$ π EFT



O.T. and Yi-Bo Yang, Universe (2026)

Vincenzo Cirigliano, Wouter Dekens, Emanuele Mereghetti, and O.T., PRD (2024) and PRD (2025)

V. Cirigliano, J. de Vries, L. Hayen, E. Mereghetti, and A. Walker-Loud, PRL (2022)

- first consistent at 0.1%-level QED radiative corrections

factorization for radiative corrections with model for hard function

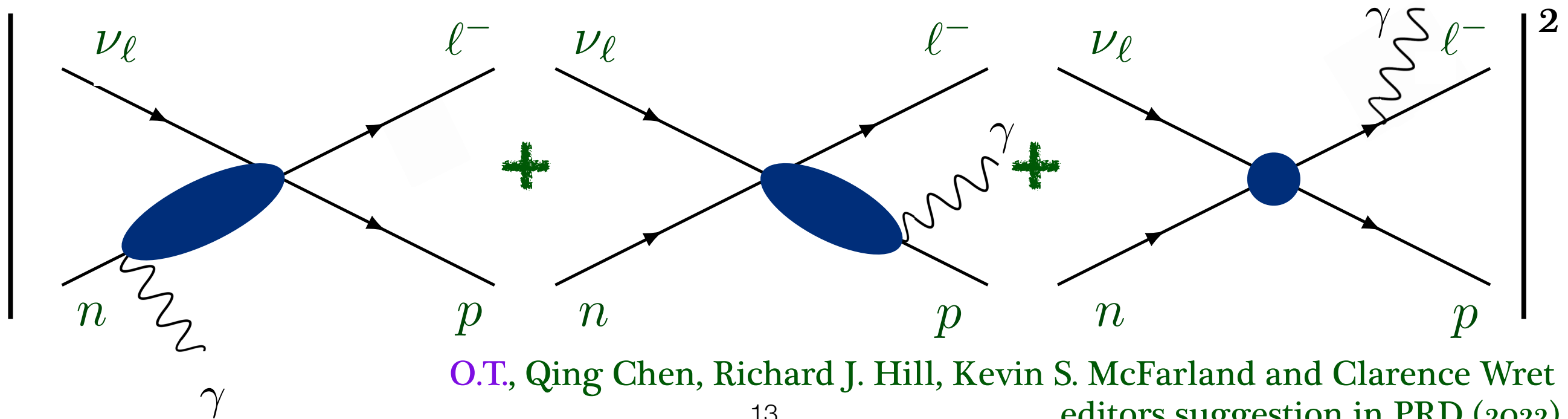


Charged-current elastic scattering on nucleons

O.T., Qing Chen, Richard J. Hill and Kevin S. McFarland, Nature Commun. (2022)

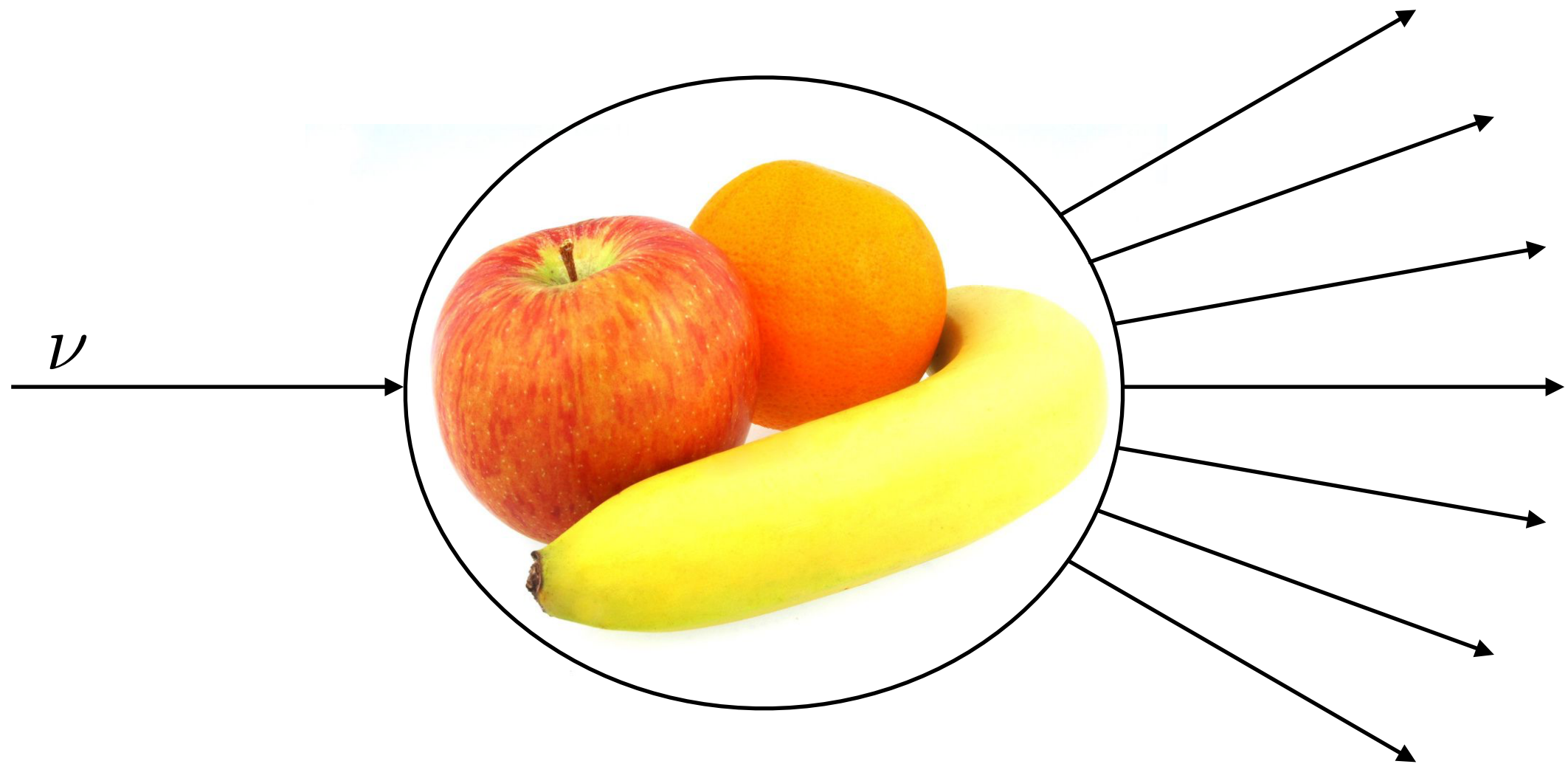
precise predictions for flavor ratios and radiative corrections

in exclusive and inclusive observables with GeV neutrino beams

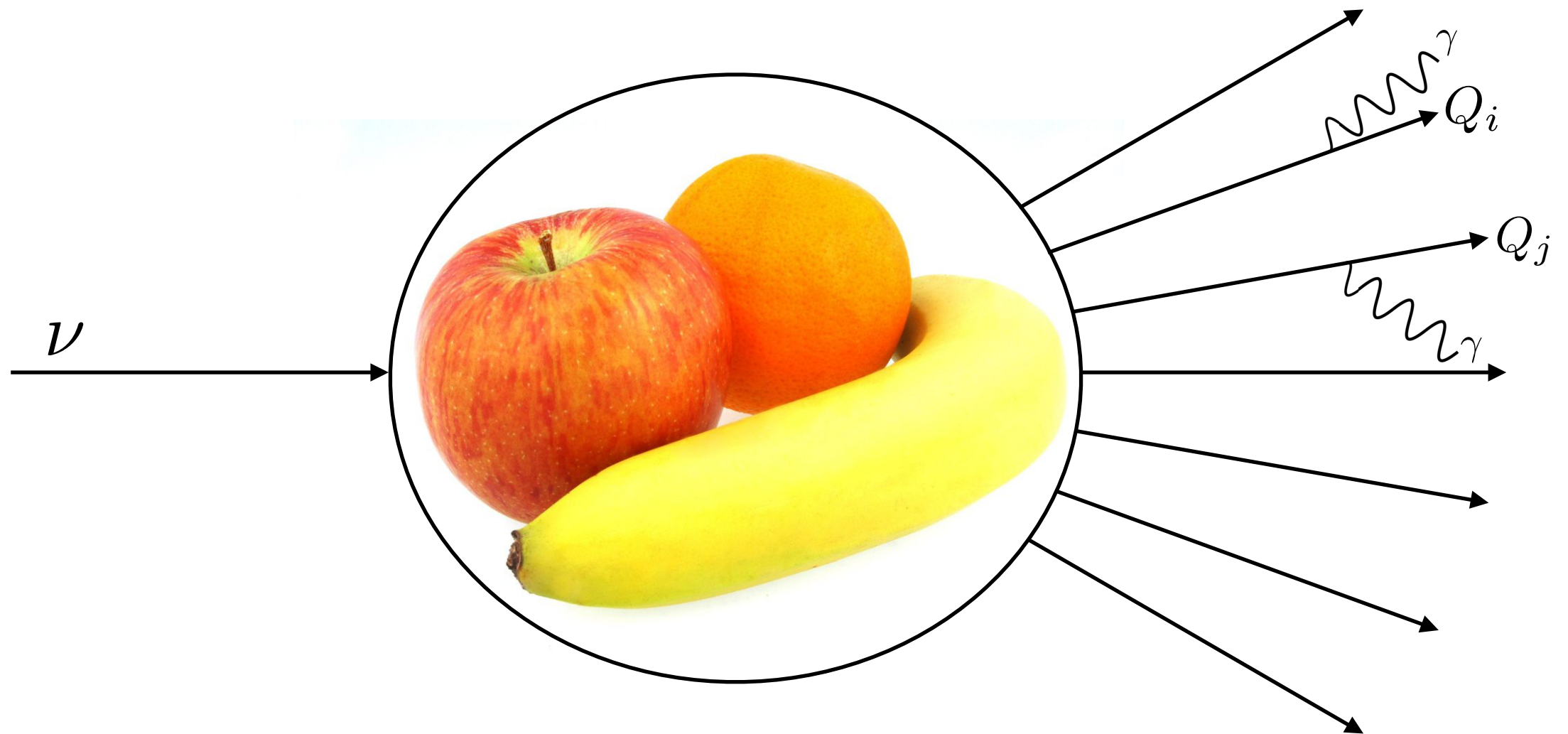


O.T., Qing Chen, Richard J. Hill, Kevin S. McFarland and Clarence Wret
editors suggestion in PRD (2022)

Neutrino interactions

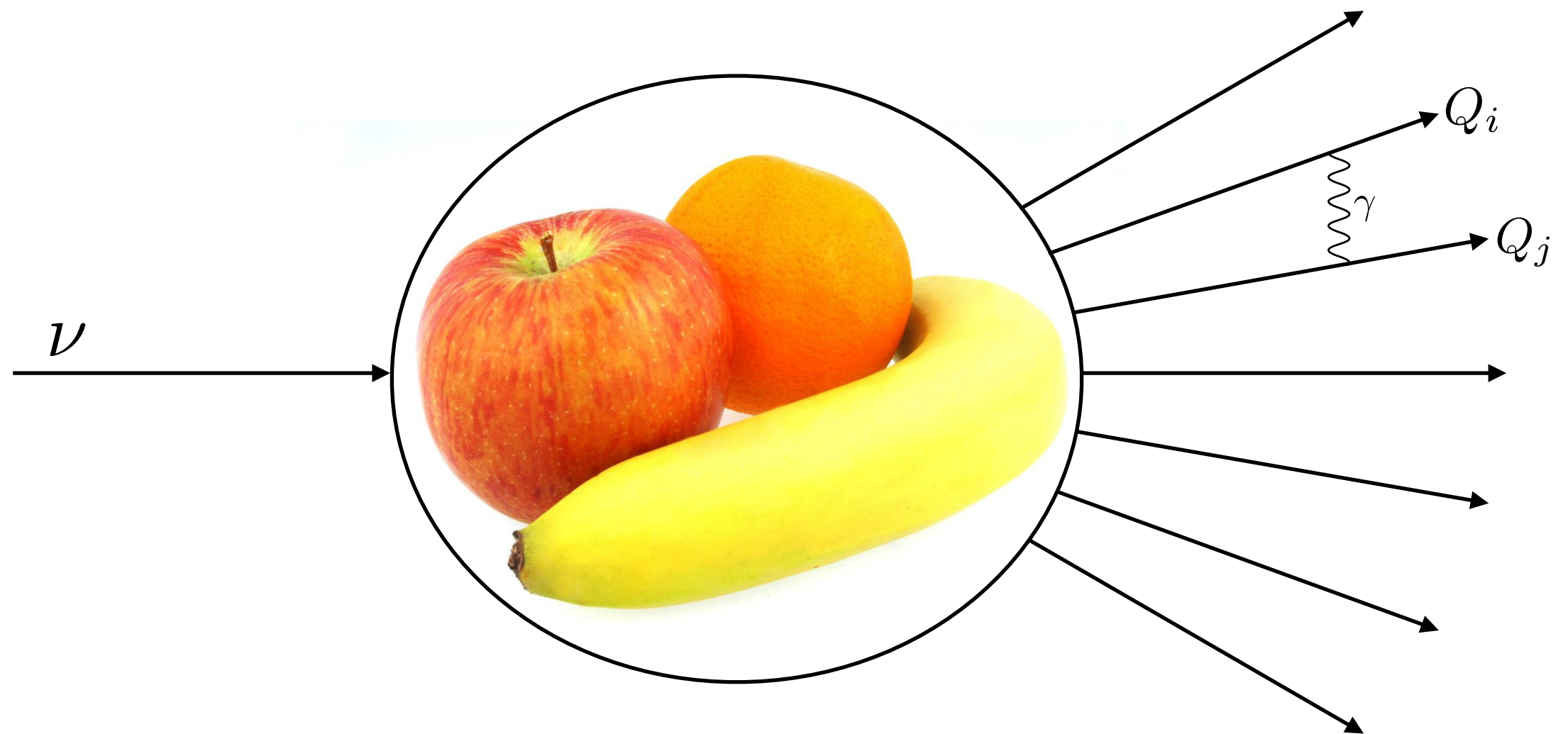


QED corrections



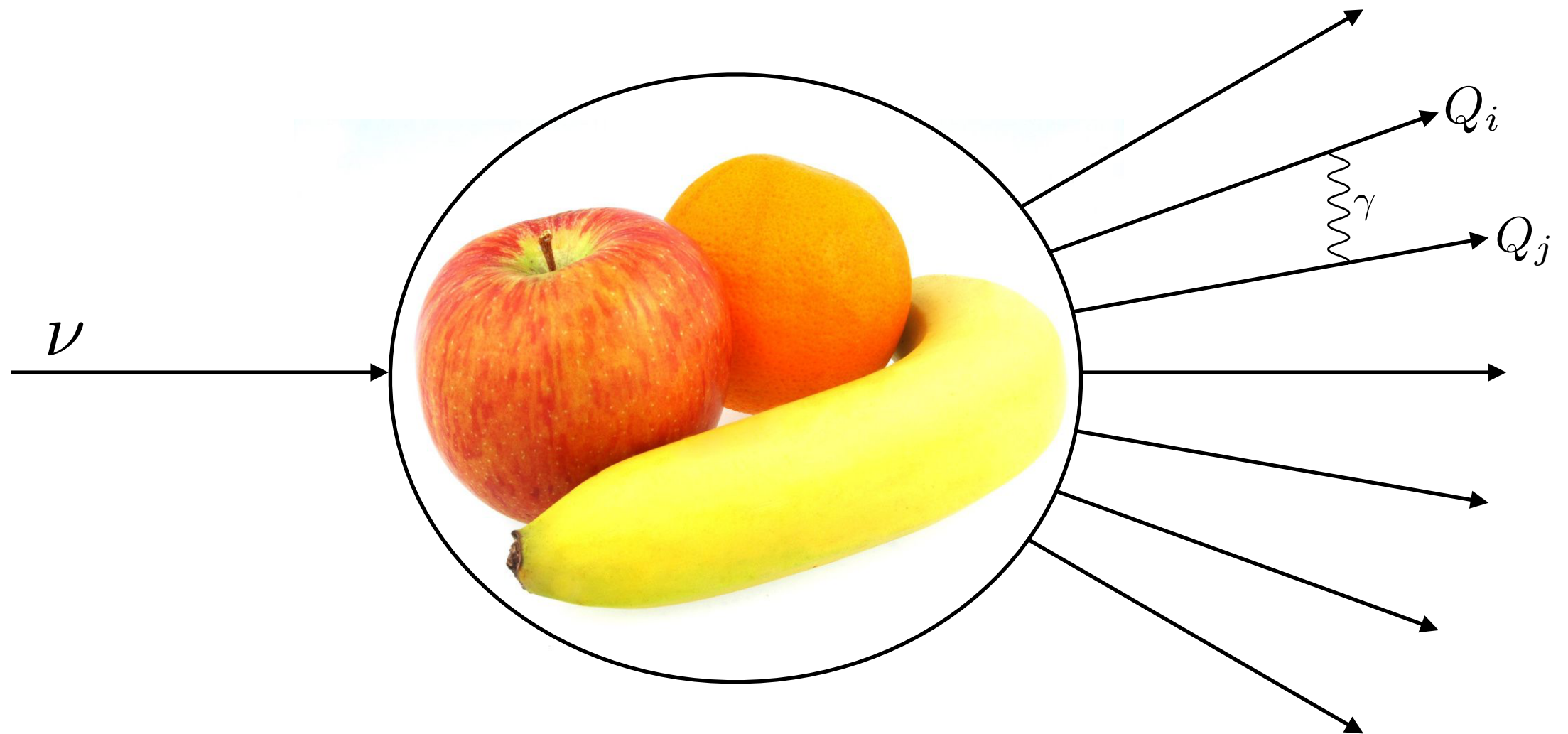
- all charged particles couple to real and virtual photons

QED corrections



- all charged particles couple to real and virtual photons

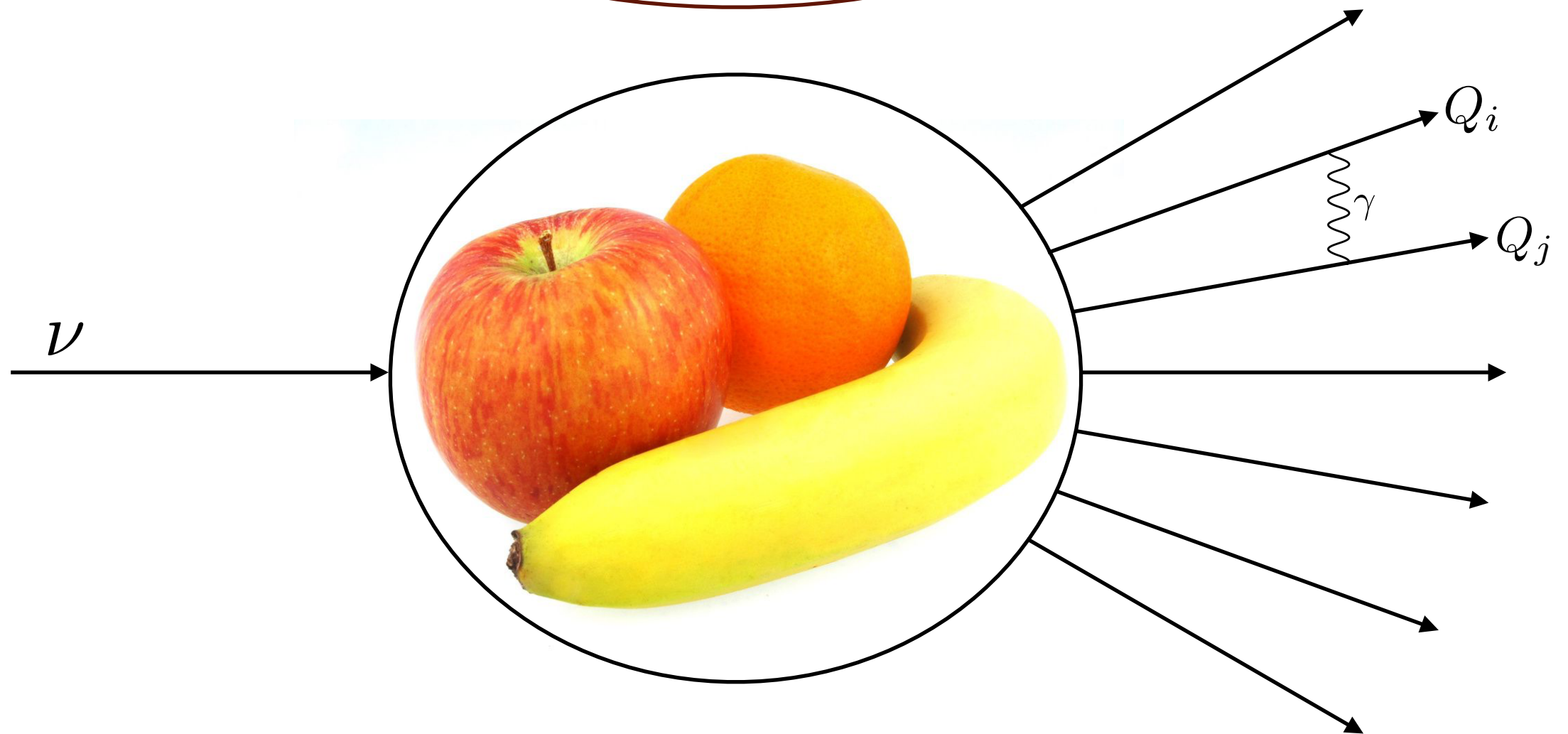
QED corrections



- $\frac{\alpha}{\pi} \sim 0.2 \%$ suppression by electromagnetic coupling constant

QED corrections

$$m_e \ll m_\mu \ll E_\nu$$

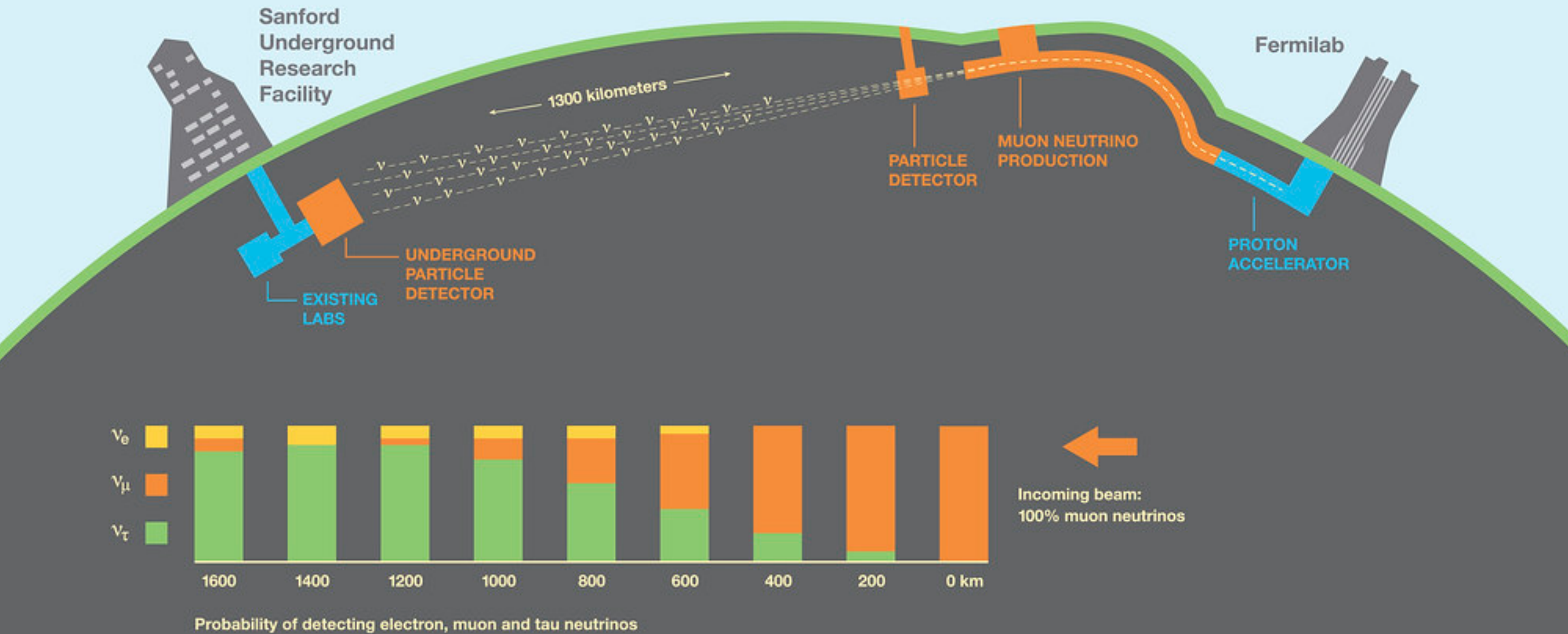


$$\frac{\alpha}{\pi} \sim 0.2 \% \text{ multiplied by } \ln \frac{E_\nu}{m_e} \sim 6 - 10 \text{ or } \ln^2 \frac{E_\nu}{m_e} \sim 36 - 100$$

- scale separation introduces large flavor-dependent QED logarithms

Neutrino experiments

Deep Underground Neutrino Experiment



$$N_\nu \sim \int dE_\nu \Phi_\nu(E_\nu) \times \sigma(E_\nu) \times R(E_\nu, E_\nu^{\text{rec}})$$

- precise neutrino physics: need in cross sections

Factorization approach

- cross section is given by **factorization formula**

$$d\sigma \sim S \left(\frac{\Delta E}{\mu} \right) J \left(\frac{m_\ell}{\mu} \right) H \left(\frac{M}{\mu} \right)$$

- determine **hard function** at hard scale by matching experiment or hadronic model to the theory with heavy nucleon

- **soft and collinear functions** are evaluated **perturbatively**

SCET power expansion parameter

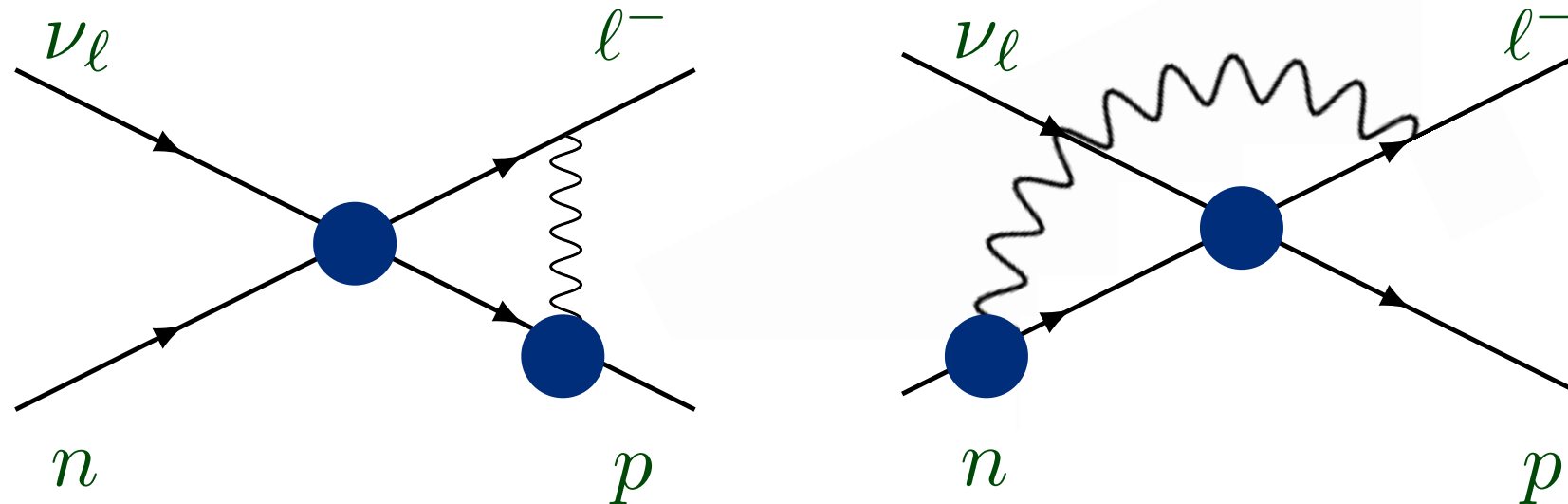
$$\lambda \sim \frac{m_\mu^2}{E_\nu^2} \sim (\Delta\theta)^2 \sim \frac{\Delta E}{E_\nu}$$

$\ln \lambda$ enhancements

O.T, Qing Chen, Richard J. Hill and Kevin S. McFarland, Nature Commun. (2022)

O.T, Qing Chen, Richard J. Hill, Kevin S. McFarland and Clarence Wret
editors suggestion in PRD (2022)

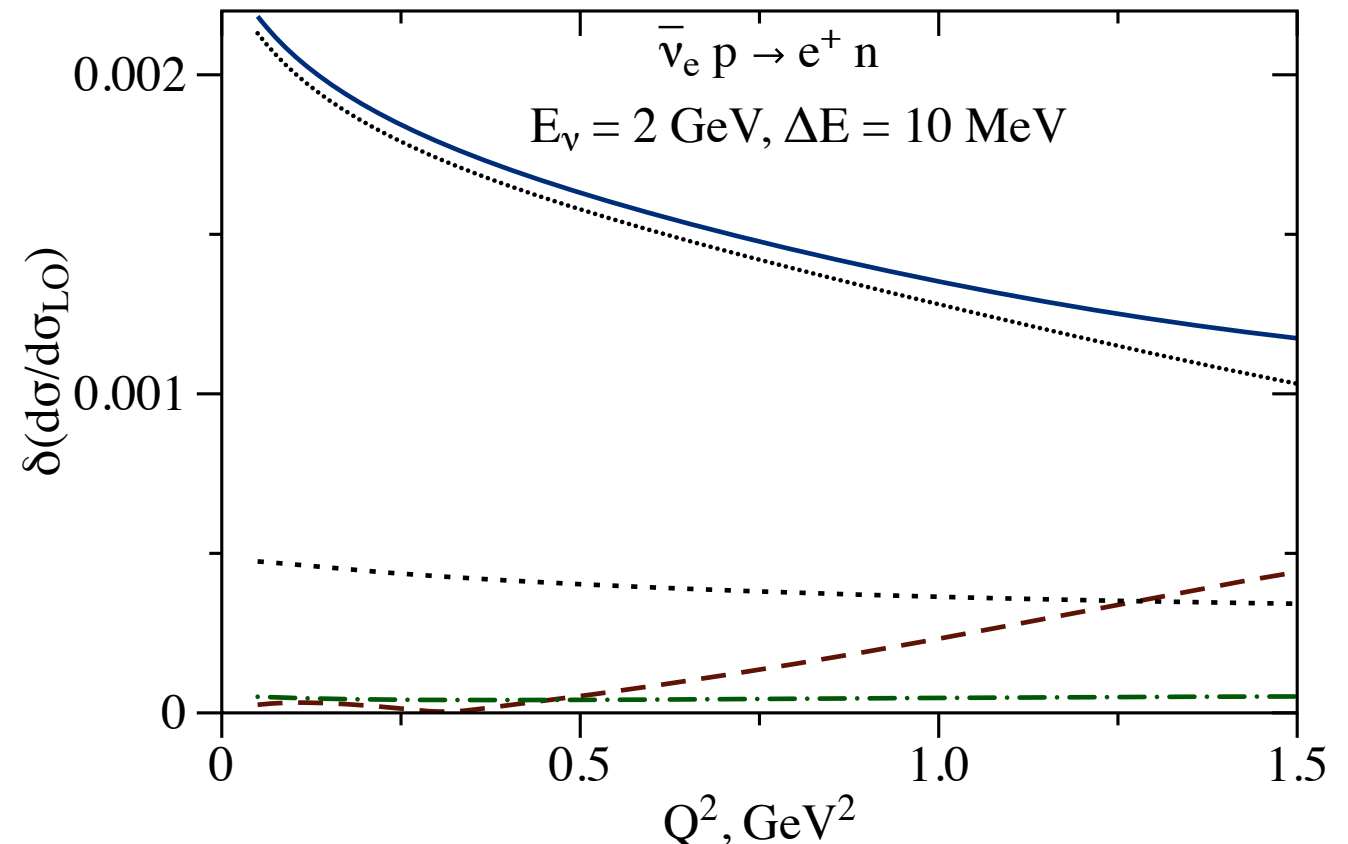
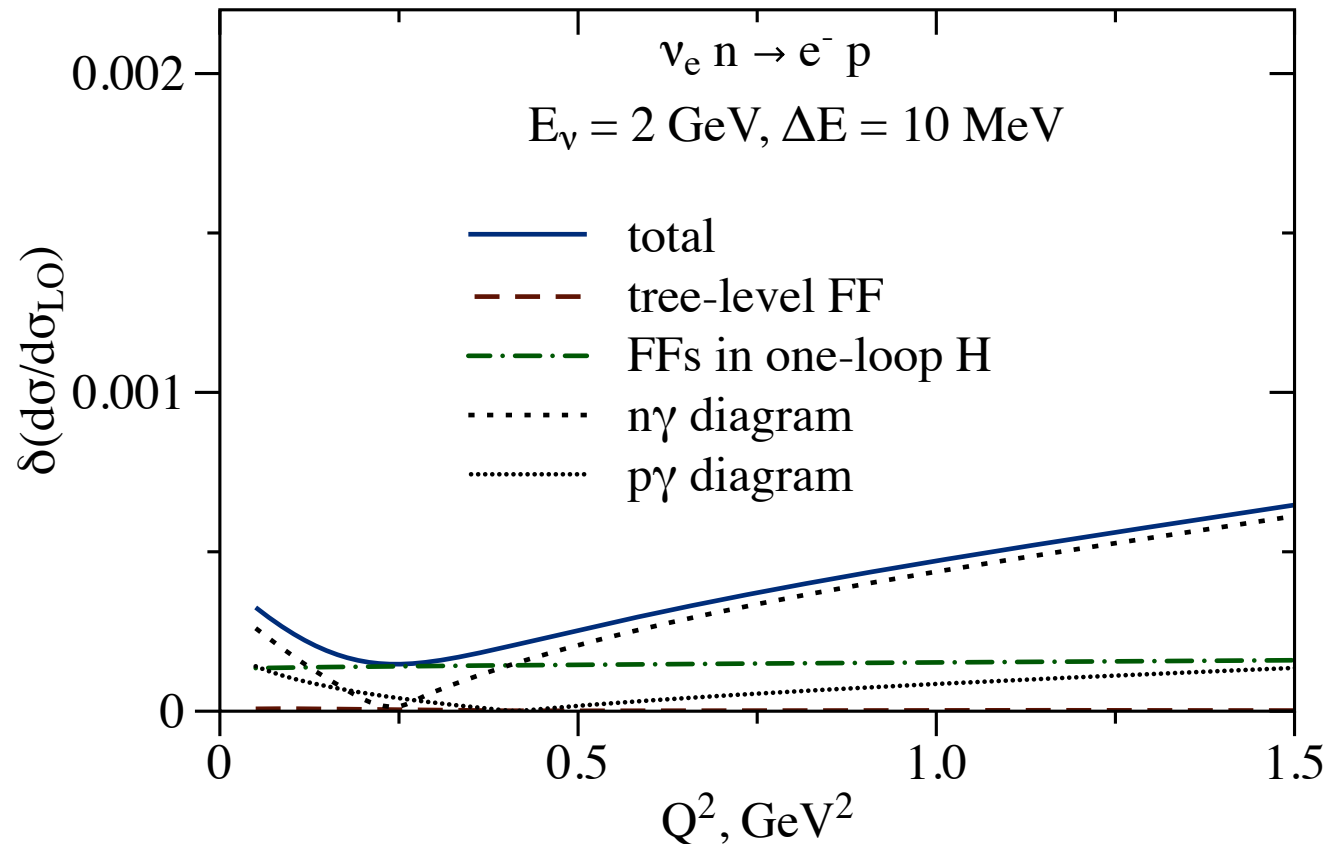
Hadronic model at GeV scale



- exchange of photon between the charged lepton and nucleons
 - assume **onshell form** for each interaction with dipole form factors
discussed for neutrino-nucleon scattering: Graczyk, PLB (2013)
 - add **self energy** for charged particles
 - reproduce soft and collinear regions of SCET
- best determination of hard function

Error budget

- uncertainties from hard function

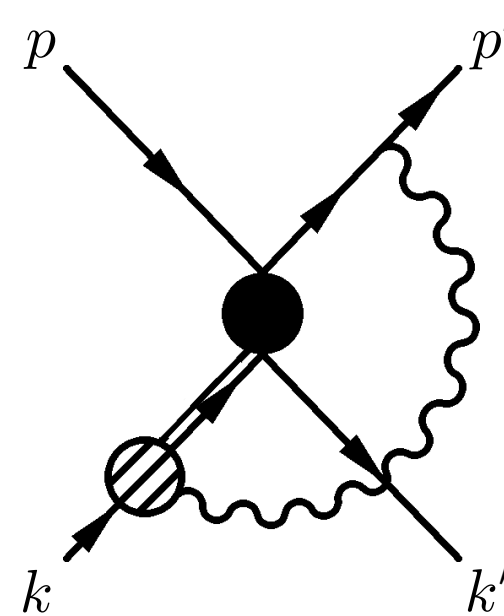
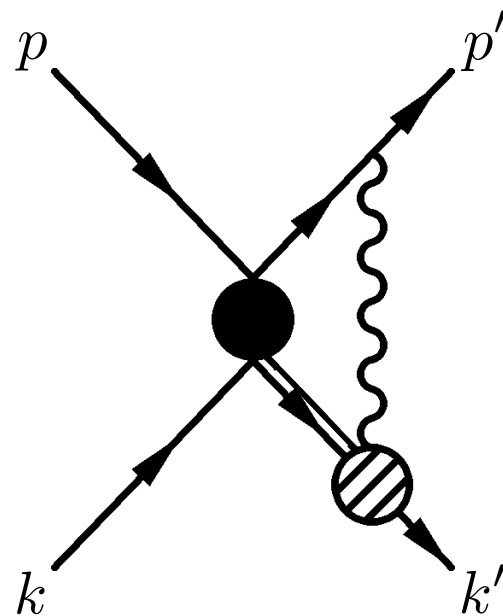


- nucleon form factors Meyer, Betancourt, Gran and Hill, PRD (2016)
Kaushik Borah, Gabriel Lee, Richard J. Hill and O.T., PRD (2020)
- add perturbative uncertainty by variation of scale

- uncertainty of permille level for the ratio to LO result

Δ resonance contribution

- vector part with **magnetic transition** only; **pQCD** for axial-vector



$$C_5^A(Q^2) \lesssim \frac{\ln Q^2}{Q^6}$$

- **free from soft singularities** $\longrightarrow$ **flavor-independent**

- **expected collinear limit**

$$g_M, g_E, f_A, f_{A3} \sim \text{const}$$

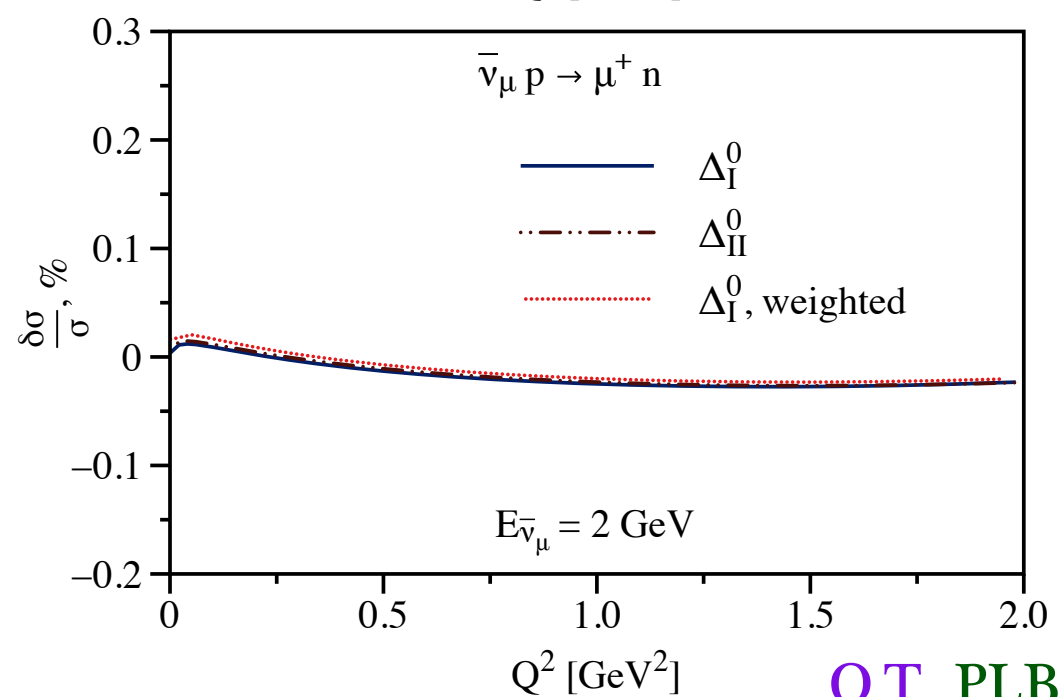
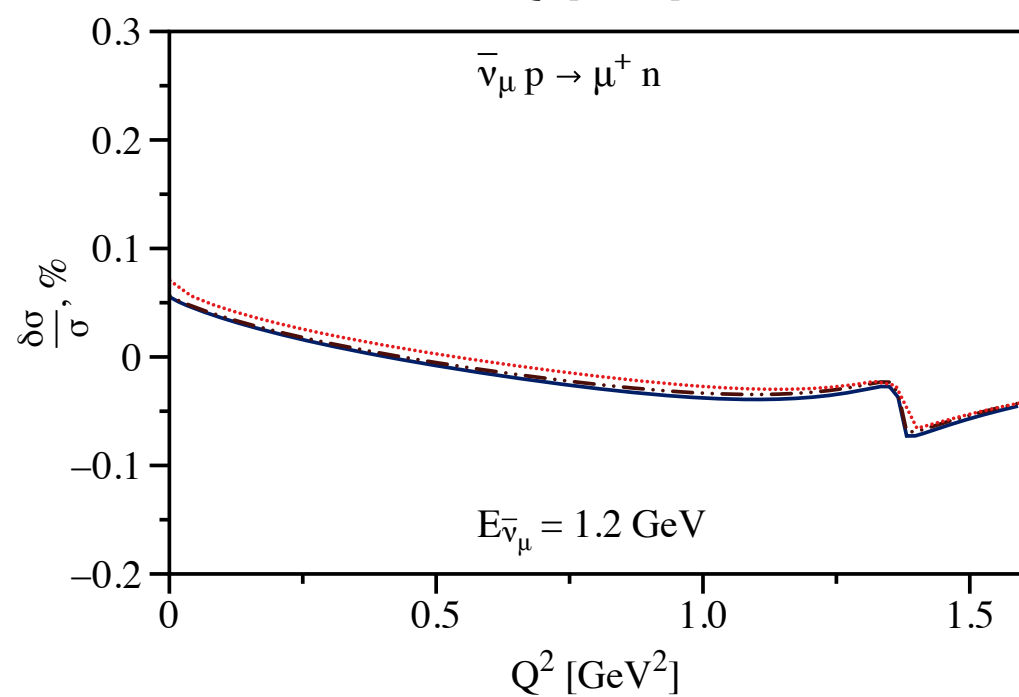
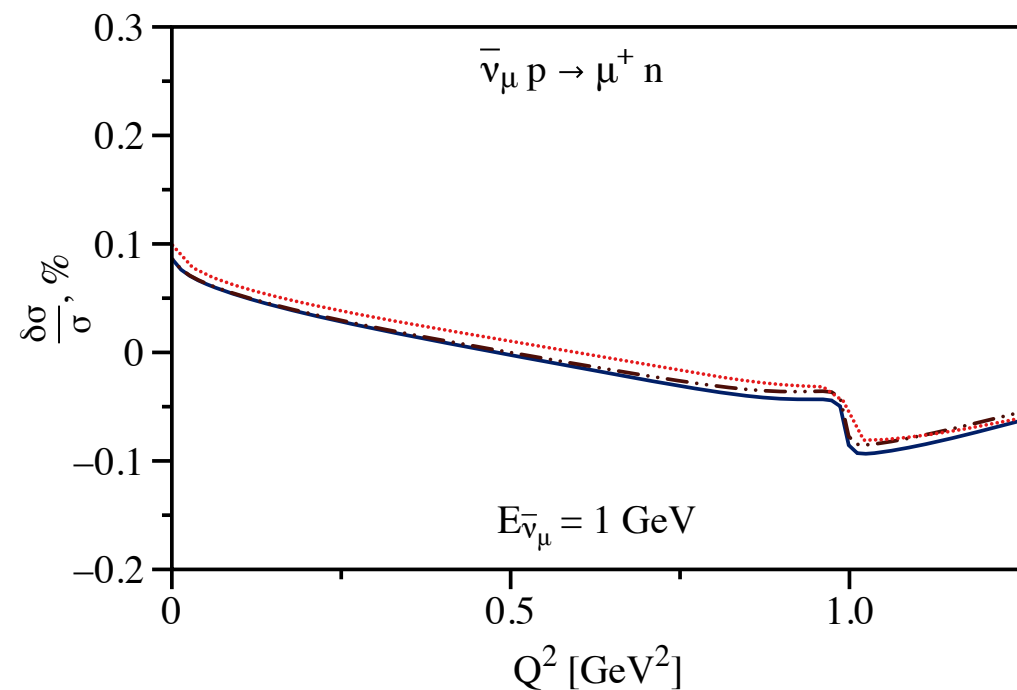
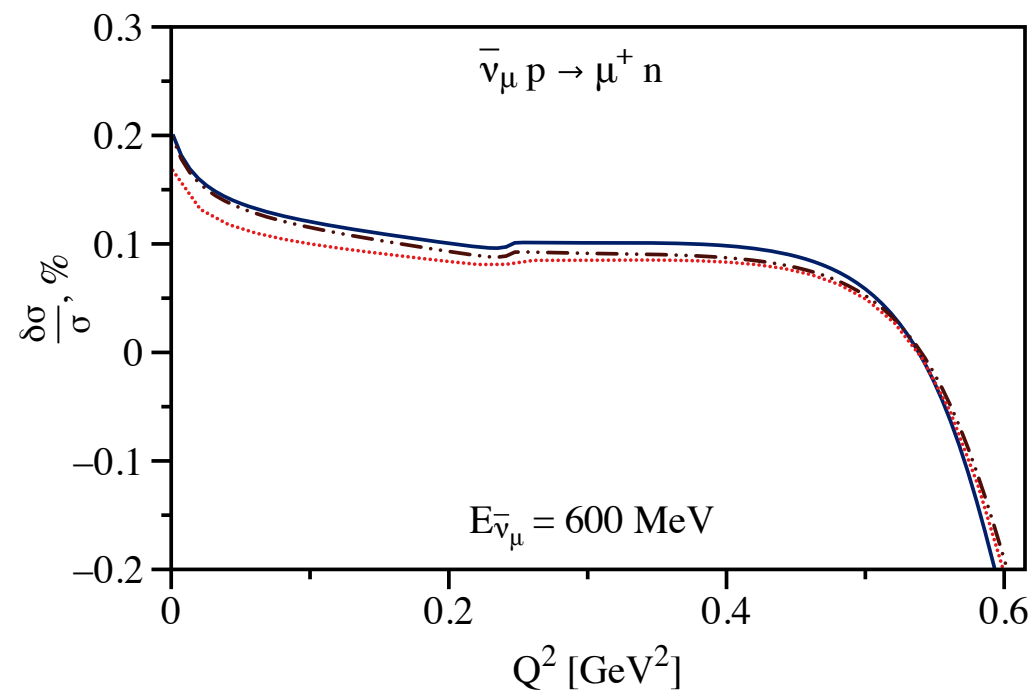
$$f_P, f_3, f_R, f_T \sim \ln m$$

O.T., PLB (2026)

- **expected infrared behavior**

Δ resonance contribution

- **width** of Δ resonance included

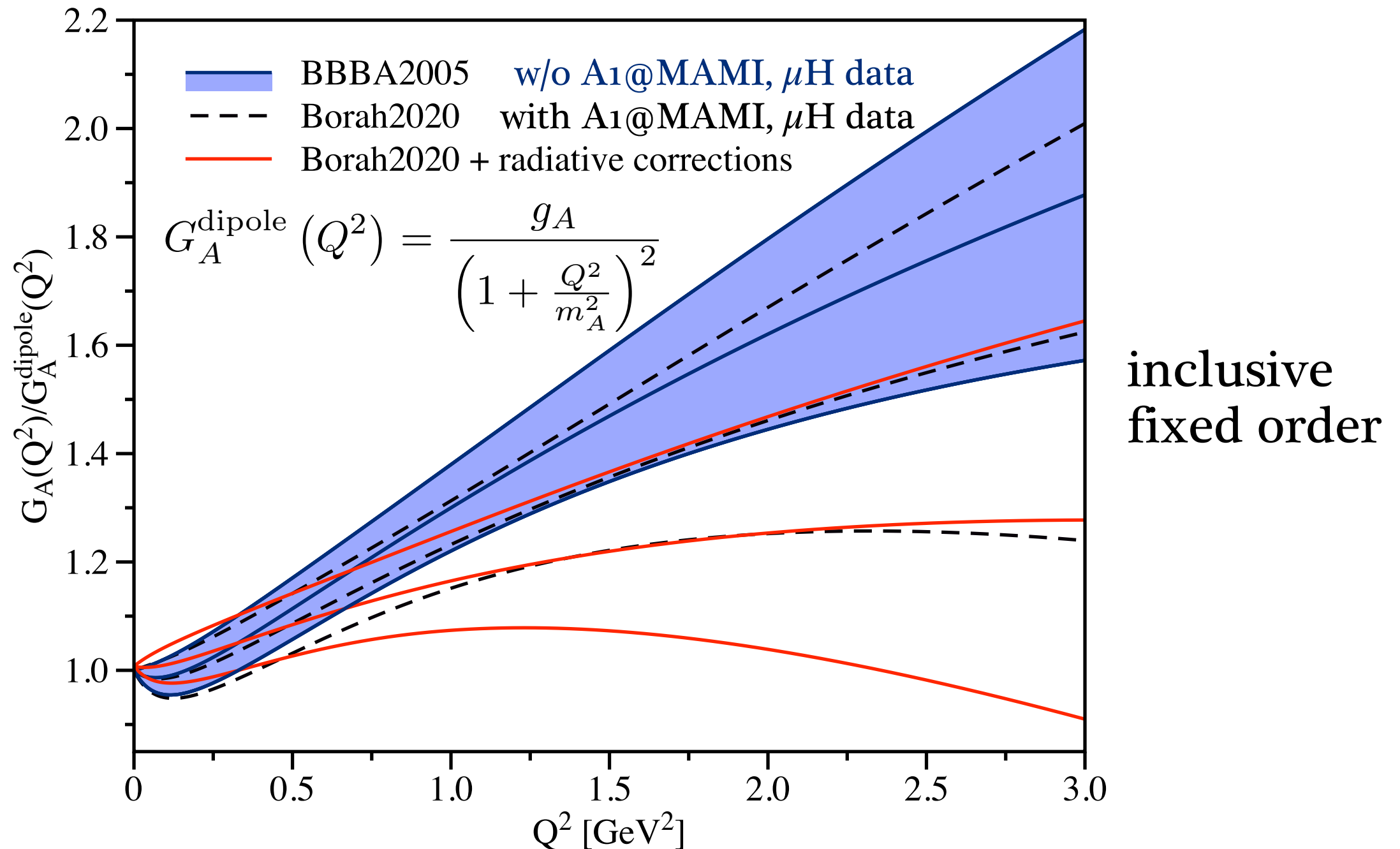


O.T., PLB (2026)

- **in agreement** with conservative error estimates of inelastic states

Nucleon axial-vector form factor

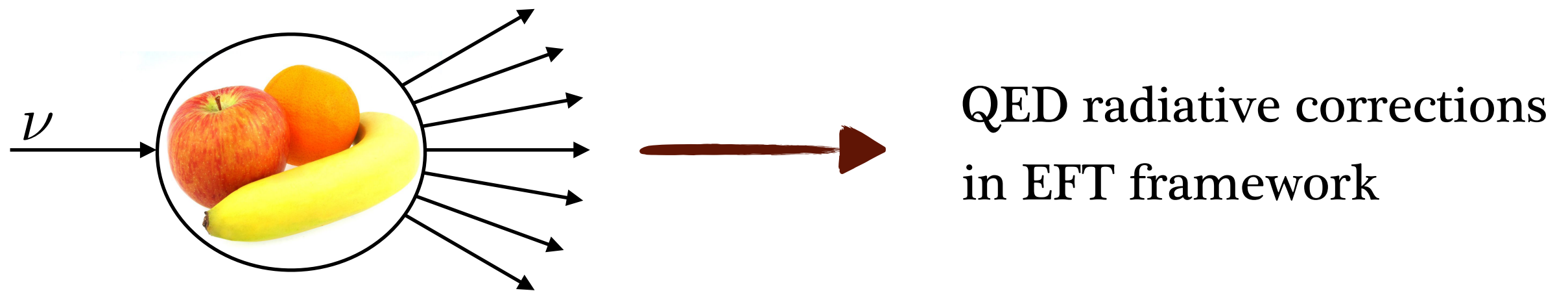
- first extraction of axial-vector form factor with QED



O.T., Aaron S. Meyer, Clarence Wret, Tejin Cai, Richard J. Hill, Kevin S. McFarland, PRD (2026)

- first consistent at 1%-level QED radiative corrections

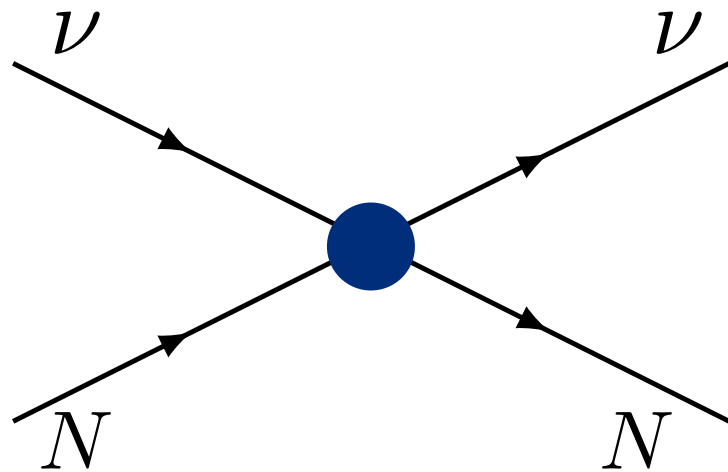
Conclusions



- radiative corrections to (anti)neutrino-nucleon cross sections formulated in factorization framework
- charged-current elastic electron vs muon cross-section ratios evaluated from theory with sub-percent uncertainty
- nucleon axial-vector form factor and radius extracted accounting for radiative corrections

Thanks for your attention !!!

Neutral currents



dominant correction:
large electroweak logarithms

O.T. and Richard J Hill, PRD (2020) and PLB (2020)

hadronic errors improved

O.T., PLB (2026)

low-energy QCD treatment

radiation from protons

Yi Chen, O.T., Bing-Song Zou, arXiv:2607.15050

impact on strangeness in nucleon spin

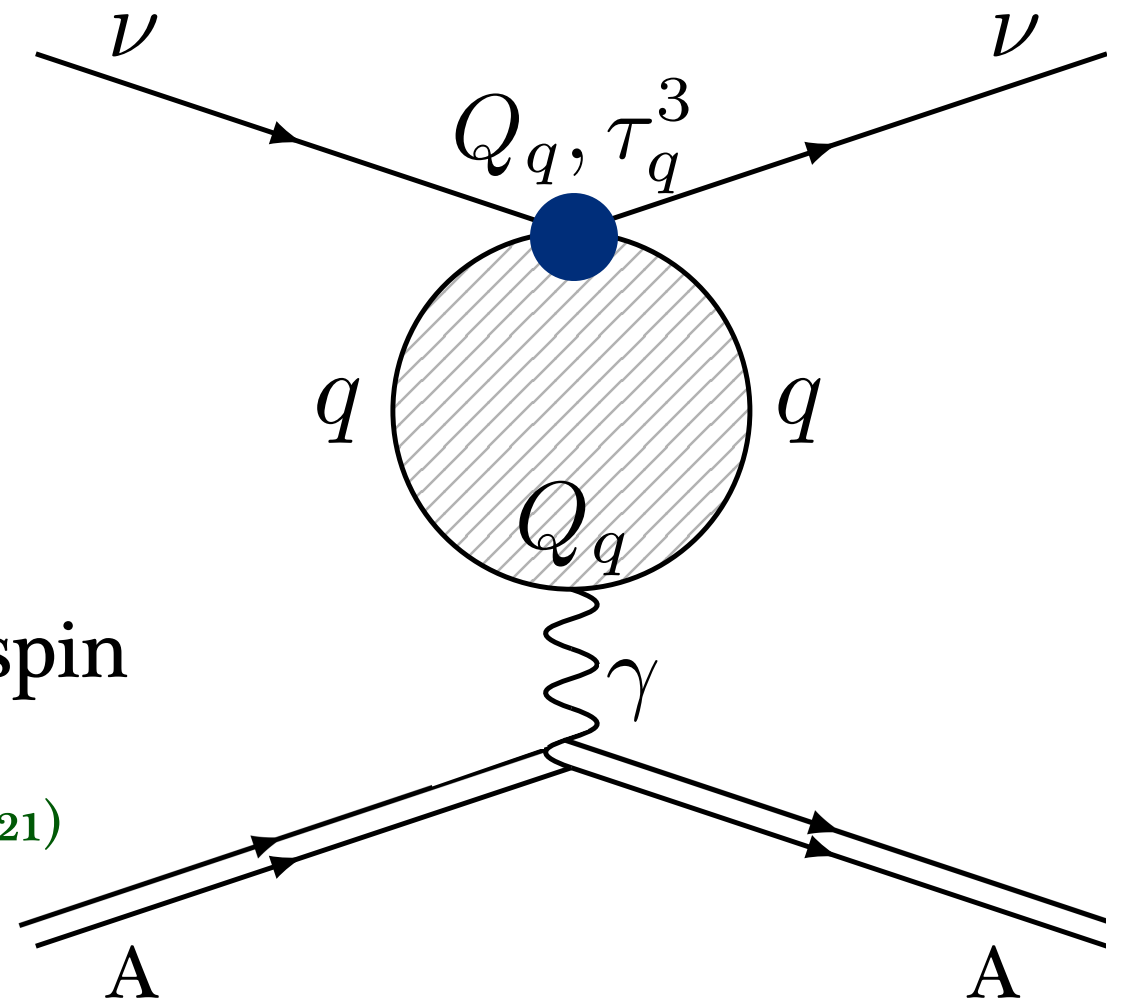
$$G_A^s(0) = \Delta s = -0.044 \pm 0.088$$

Constantia Alexandrou et al., PRD (2021)

analysis w/o radiative corrections

$$p : -0.053$$

$$n : -0.014$$



- radiative corrections ~ strange-quark contributions

Factorization approach

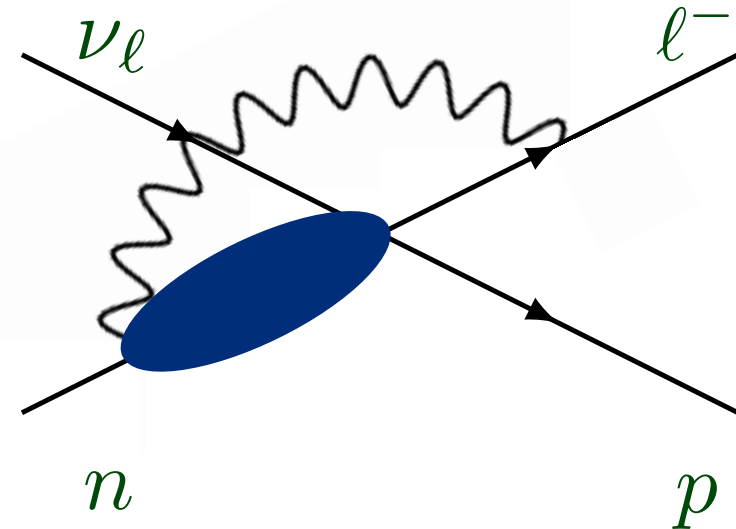
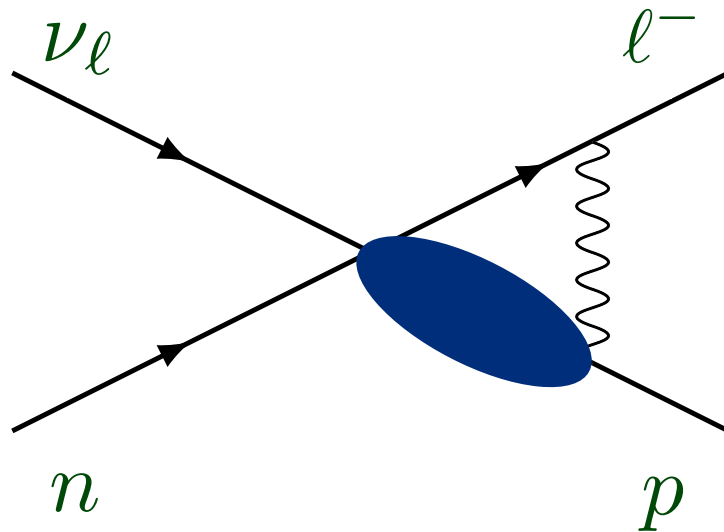
- cross section is given by **factorization formula**

$$d\sigma \sim S \left(\frac{\Delta E}{\mu} \right) J \left(\frac{m_\ell}{\mu} \right) H \left(\frac{M}{\mu} \right)$$

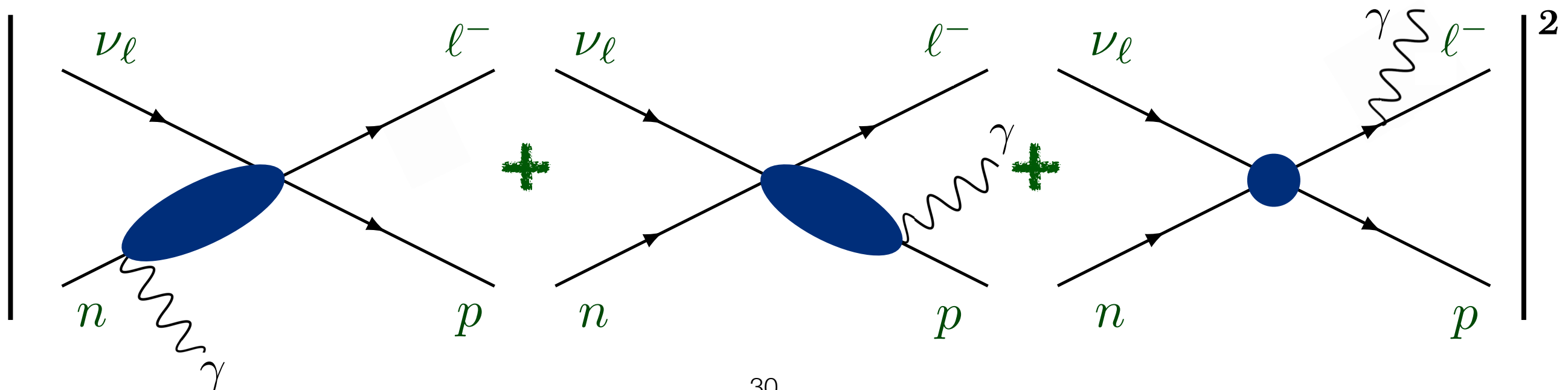
- 
- M determine **hard function** at hard scale by matching experiment or hadronic model to the theory with heavy nucleon
 - m_μ **RGE evolution** of the hard function to scales $\Delta E, m_\ell$
 - ΔE **soft and collinear functions** are evaluated **perturbatively**
 - m_e calculate cross section at low energies accounting for **all large logs**
ep scattering with soft radiation only: Richard J. Hill, PRD (2016)

- **soft and collinear functions** determined **analytically**
- **hard function** describes physics at GeV energies

Inclusive observables

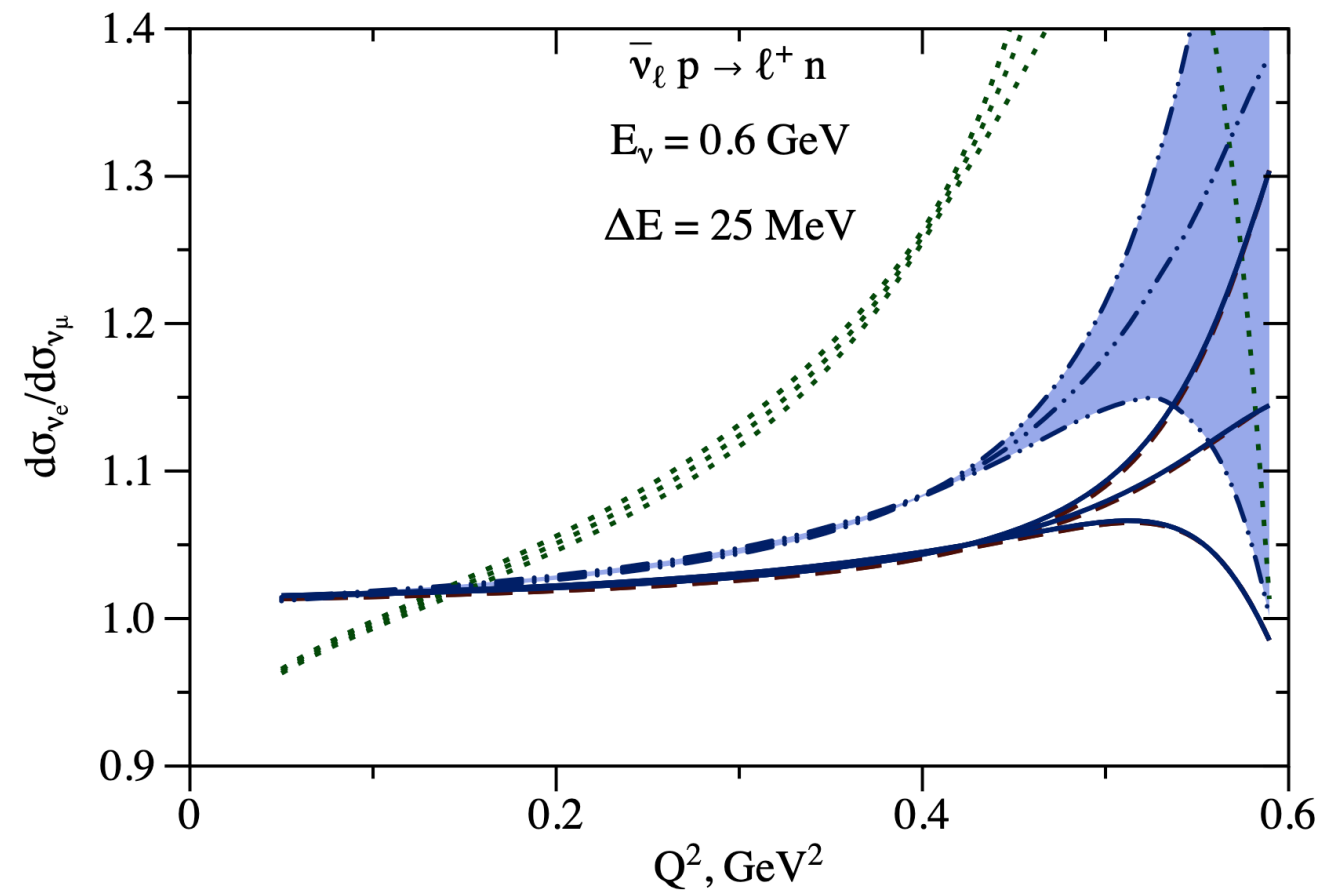
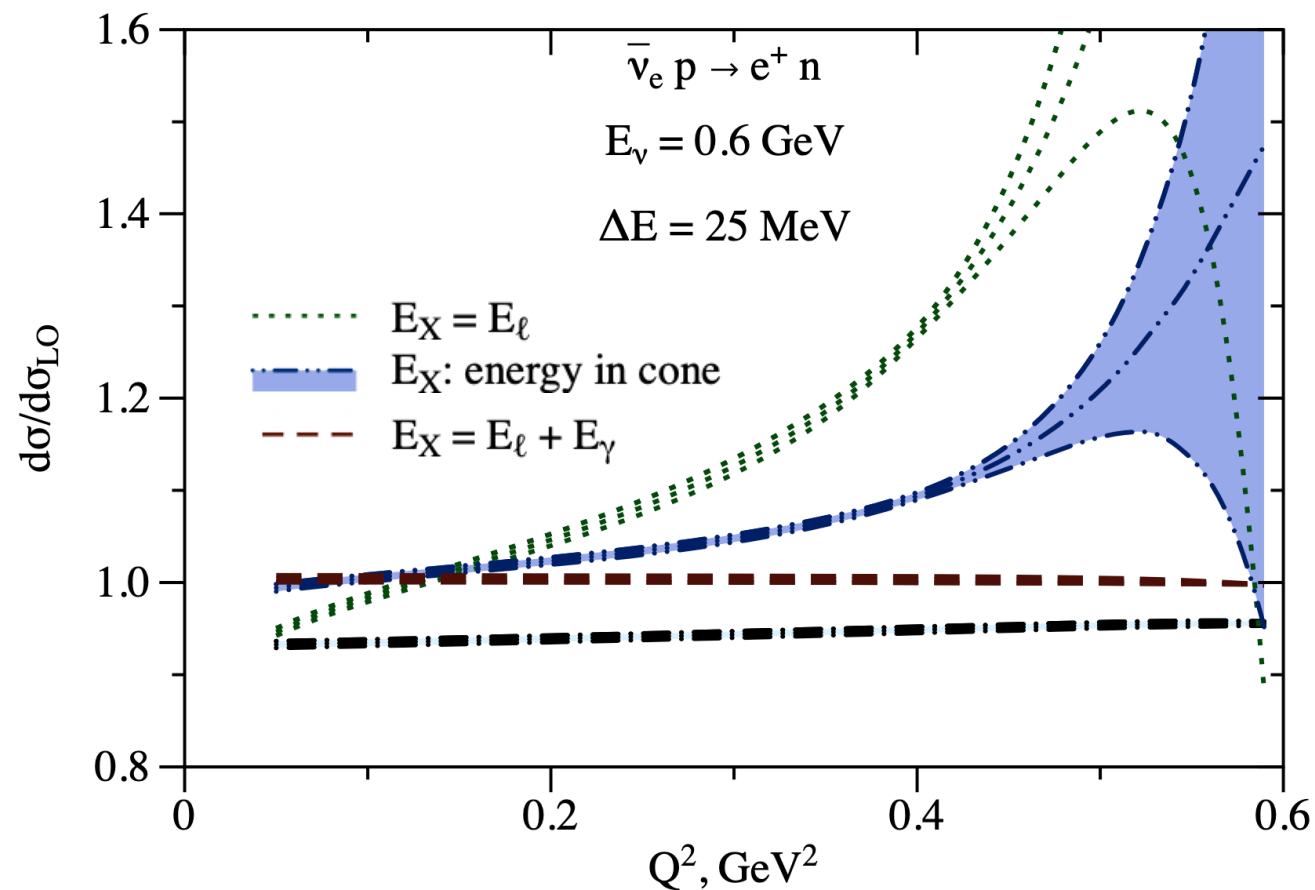


- the same gauge-invariant model for the real radiation
- arbitrary hard photons are part of the observable



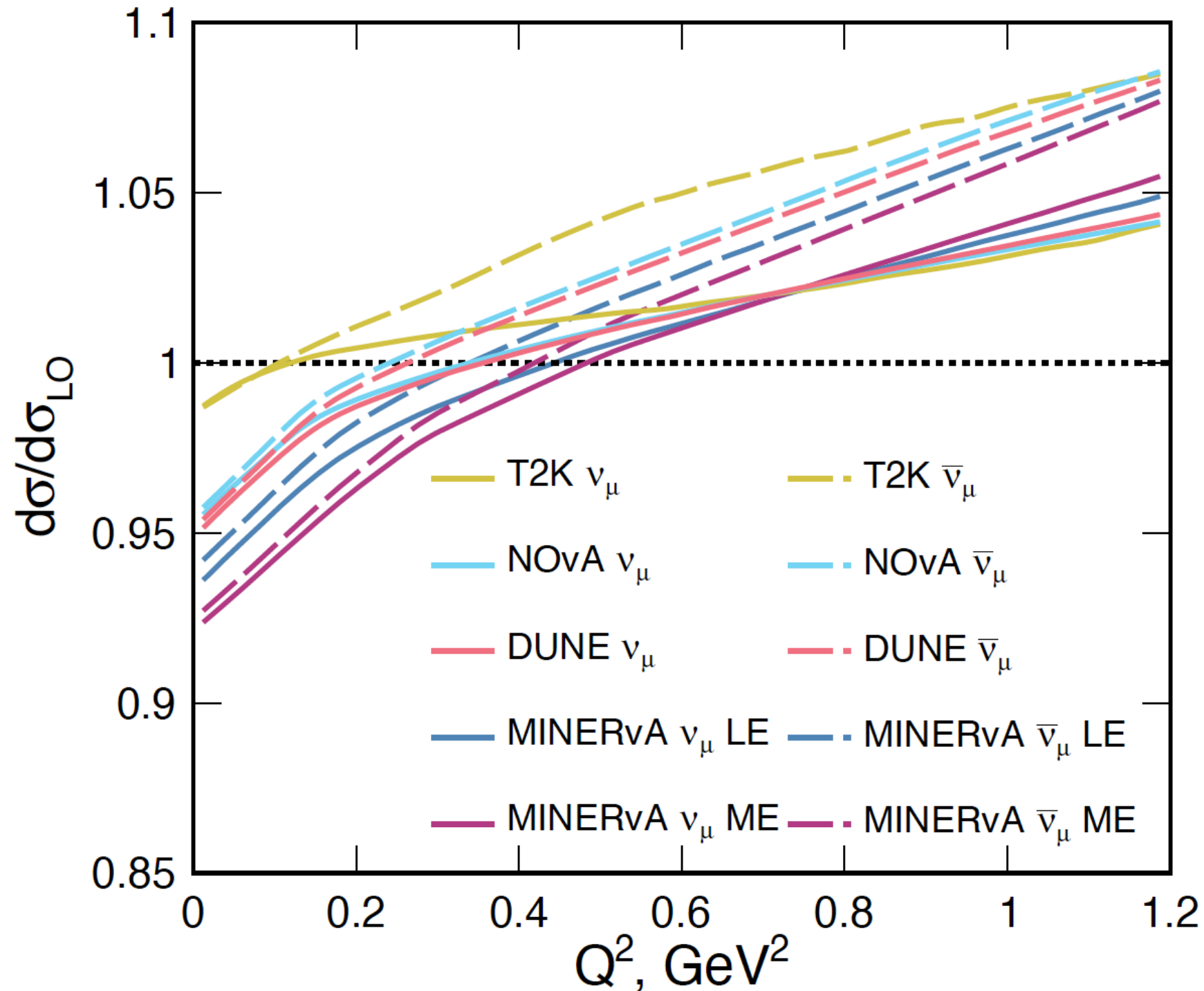
Inclusive observables

- **kinematics** $Q^2 = 2M (E_\nu - E_X)$ is reconstructed with 3 different E_X



- dependence on reconstruction of kinematics and cuts
- precise prediction for ratios $\sigma_{\nu_e}/\sigma_{\nu_\mu}$

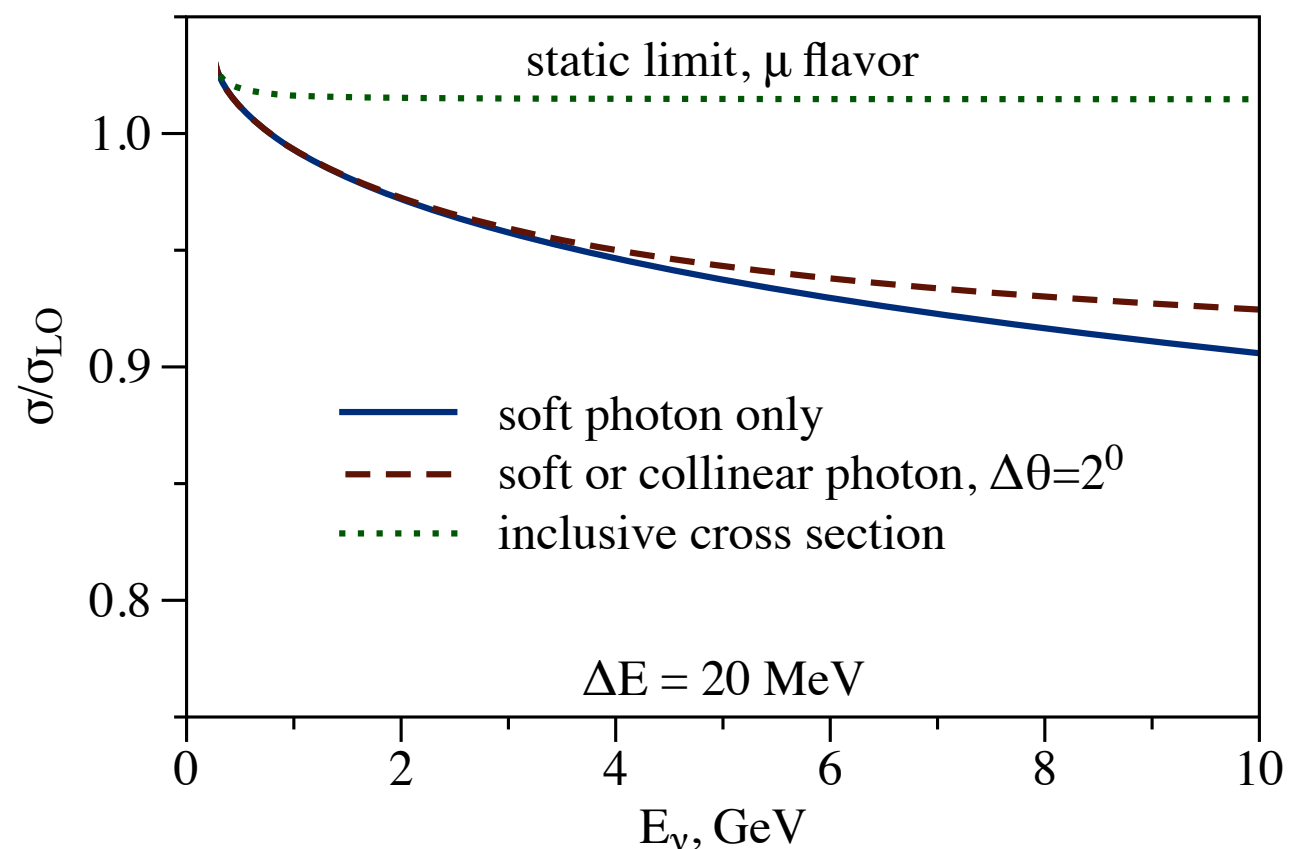
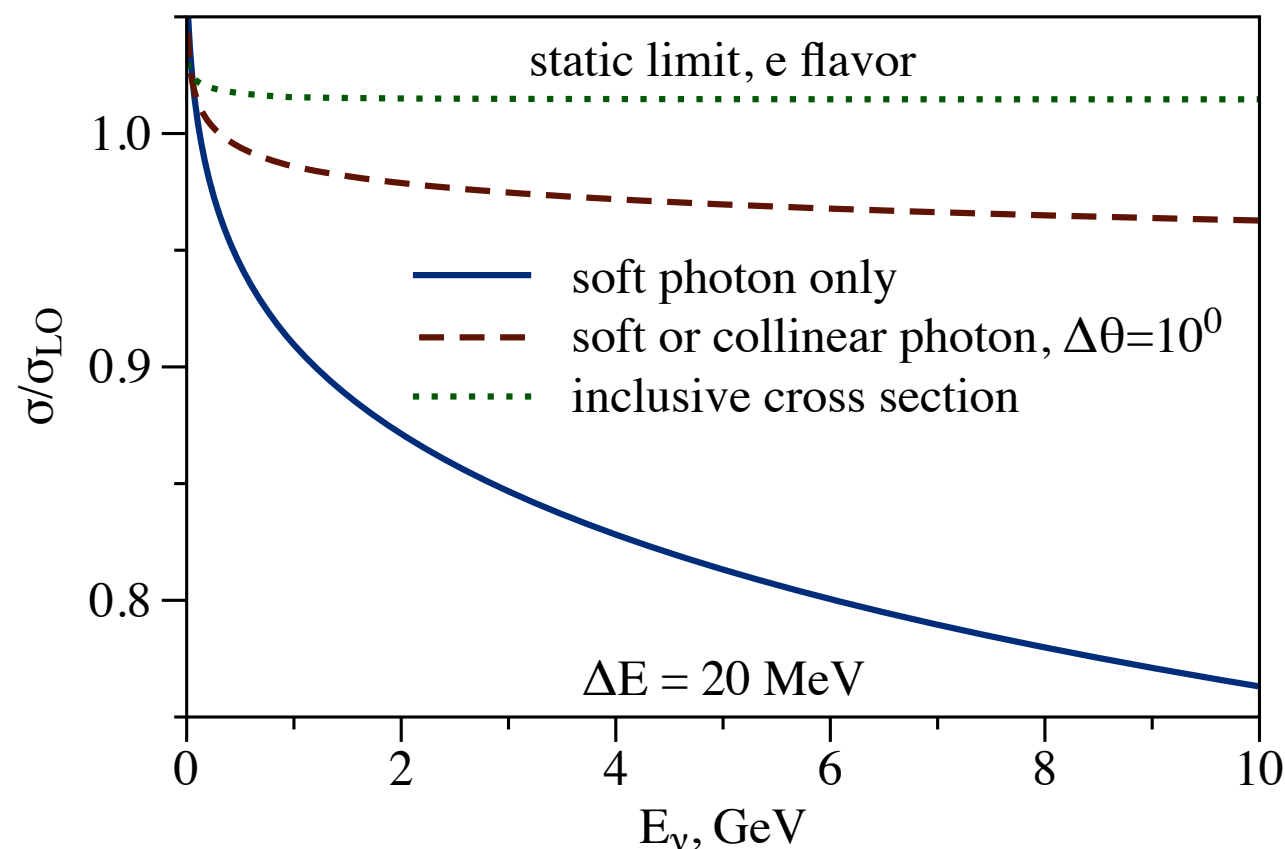
Comparison to data



- lepton energy spectra with lepton kinematics
- NEUT generator + flux averaging

Static nucleon limit

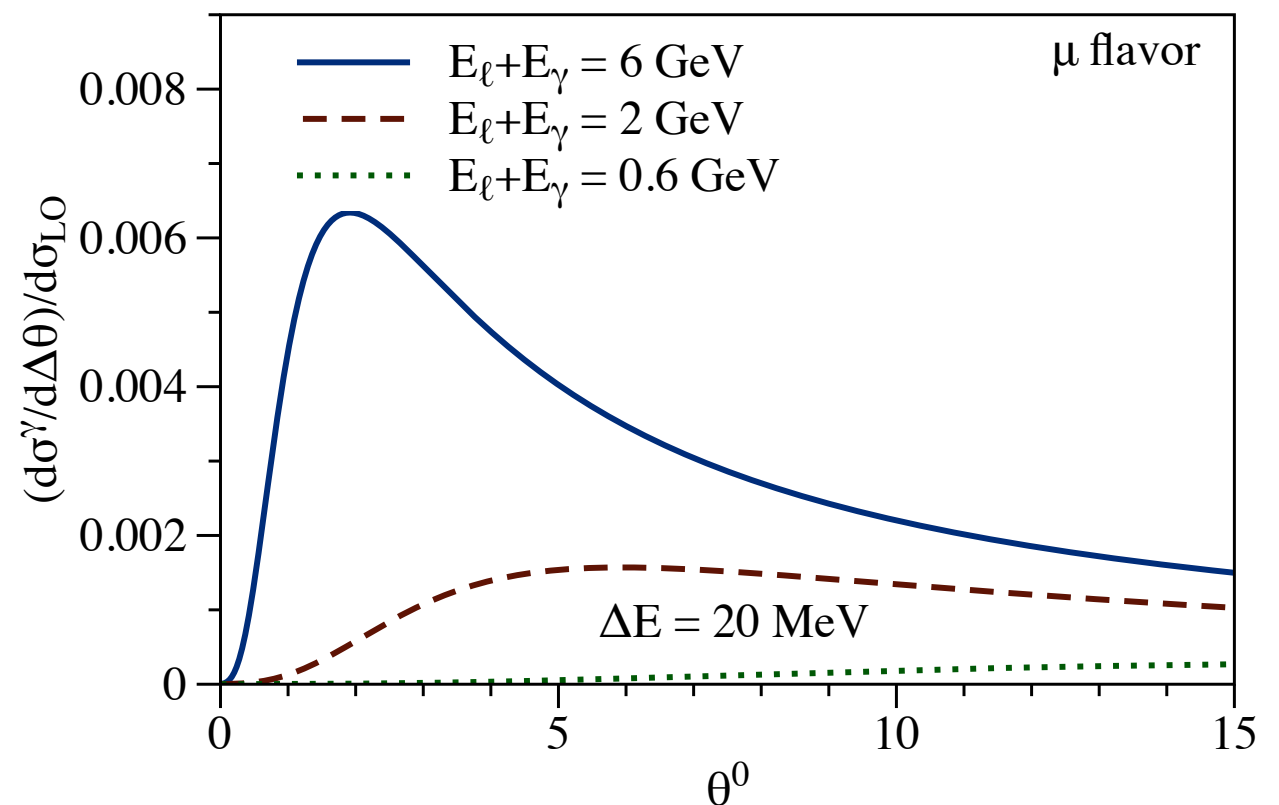
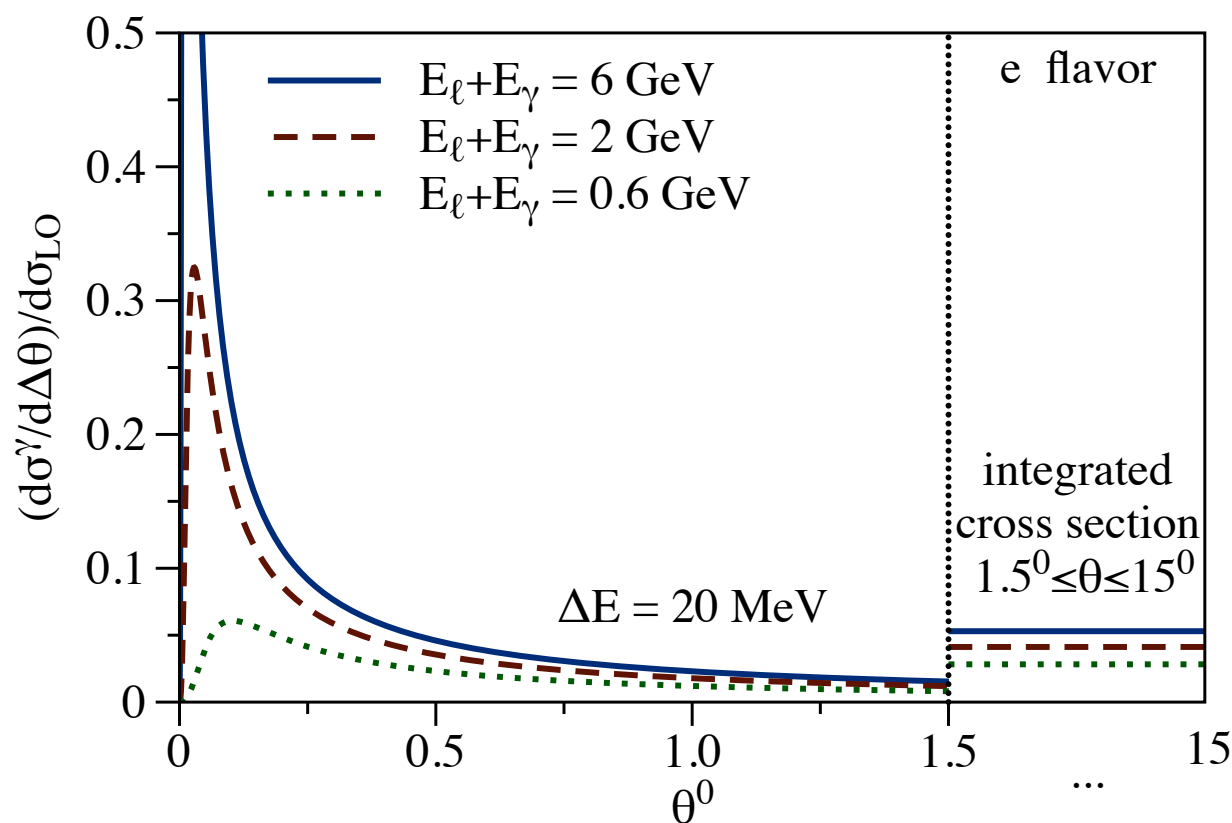
- formal limit of infinitely heavy nucleus $m_\ell \ll E_\ell \ll M$
- provides correct soft and collinear logarithms
- soft-photon energy < 20 MeV, jet size: 10° for electron and 2° for muon



- flavor-dependent effect, same for $\nu_\ell n \rightarrow \ell^- p$ vs $\bar{\nu}_\ell p \rightarrow \ell^+ n$
- collinear observable: cancellation of virtual vs real logs
- inclusive observables ($+\gamma$): few % level, flavor independent

Electron vs muon jets

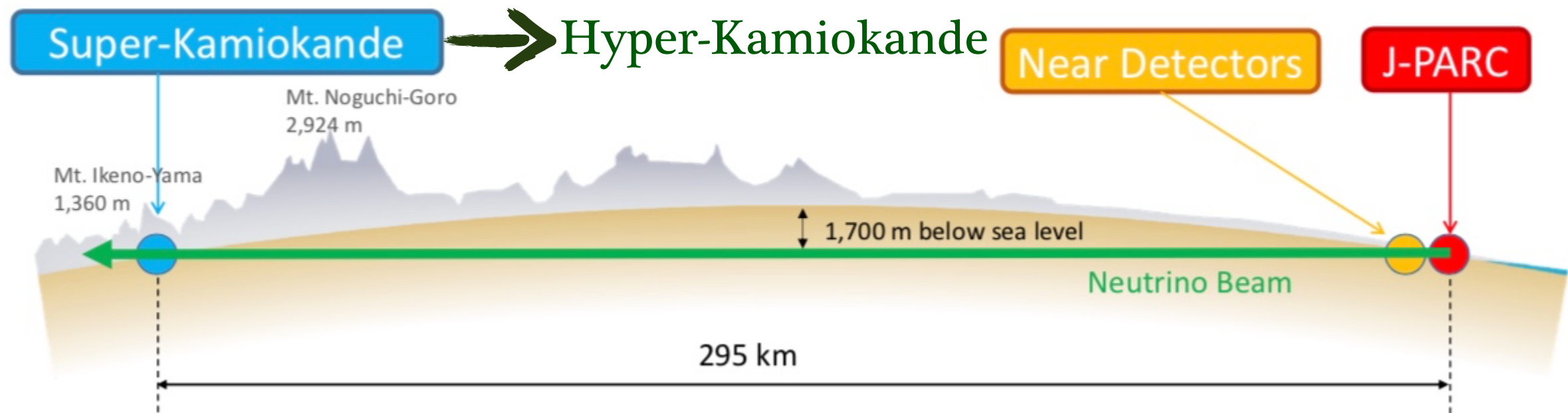
- factorization for radiation of collinear photons
- cone angle is defined to lepton direction
- photons of energy > 20 MeV, fixed energy in the cone



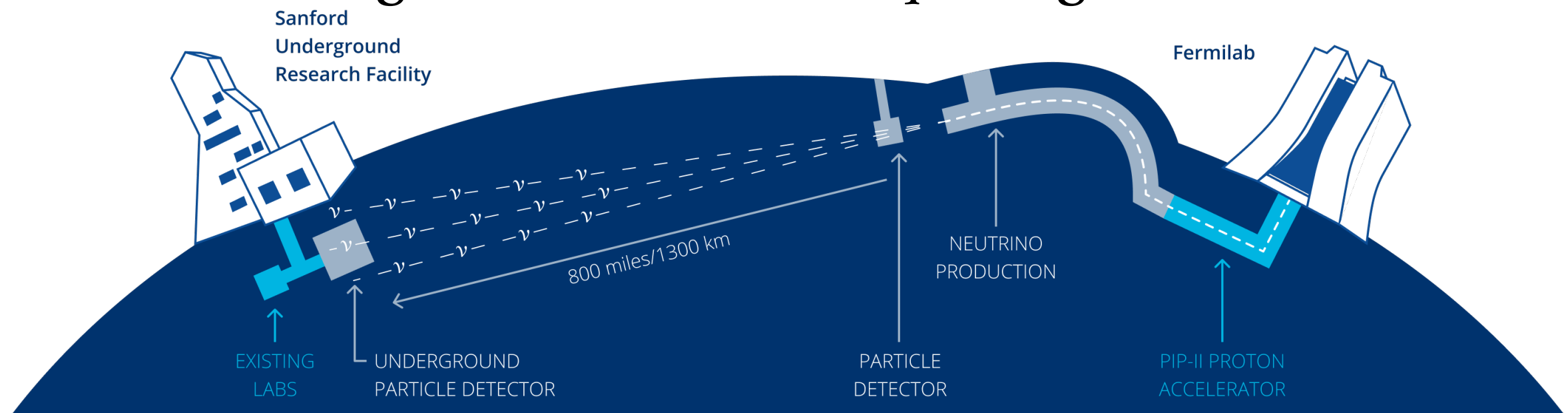
- flavor-dependent effect, same for $\nu_\ell n \rightarrow \ell^- p$ vs $\bar{\nu}_\ell p \rightarrow \ell^+ n$
- forward-peaked radiation for electron flavor
- negligible radiation for muons with shifted peak position

CP violation and mass hierarchy@laboratory

650 m under rocks in mountain, 2600000t of pure water



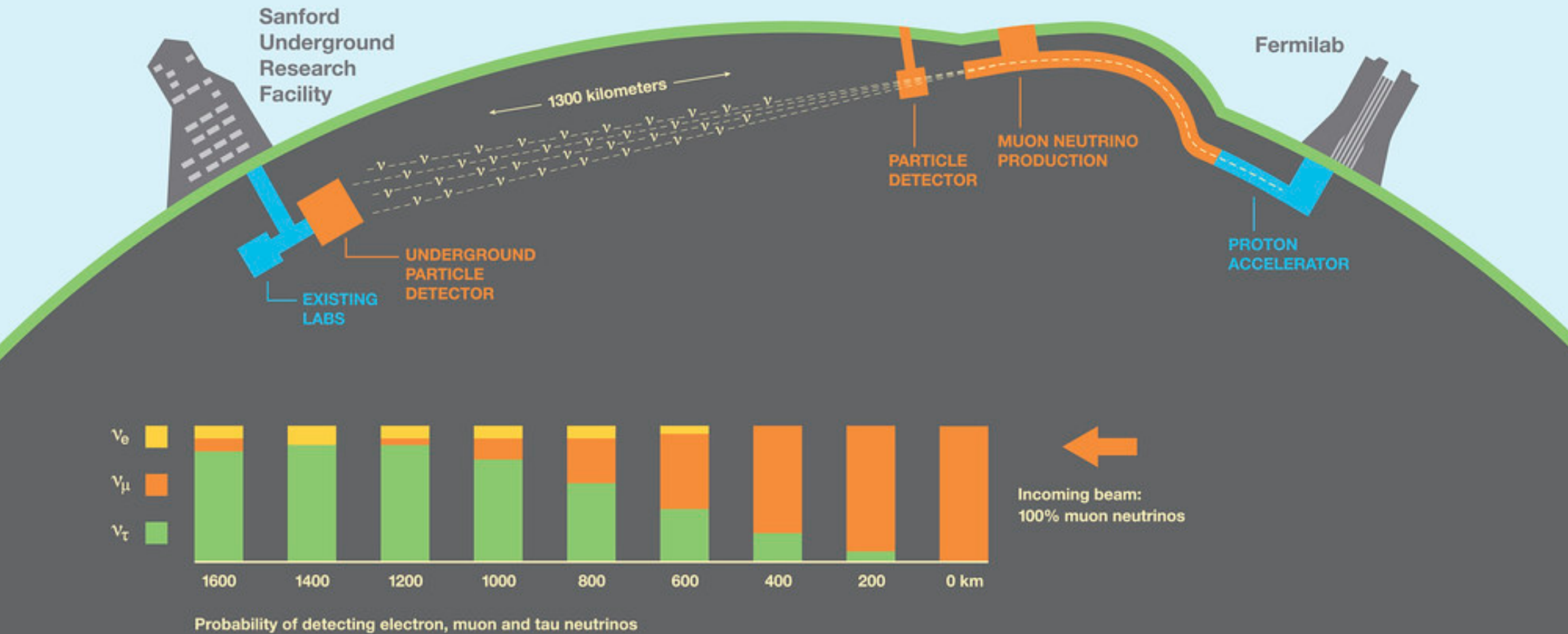
1.5 km underground, 4x700000t of liquid argon



- CP violation in PMNS and mass hierarchy in next 10-20 years !!!

Neutrino experiments

Deep Underground Neutrino Experiment



$$N_\nu \sim \int dE_\nu \Phi_\nu(E_\nu) \times \sigma(E_\nu) \times R(E_\nu, E_\nu^{\text{rec}})$$

- precise neutrino physics: need in cross sections