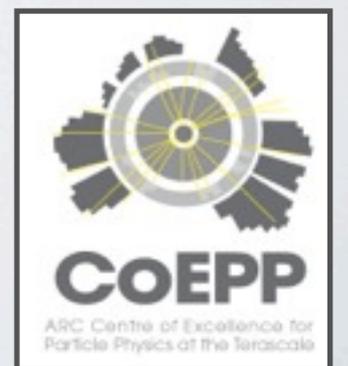


Charge symmetry violation in moments of the nucleon PDFs

Ross D. Young
CSSM & CoEPP, University of Adelaide

The Seventh International Symposium on
Chiral Symmetry in Hadrons & Nuclei
Beijing, China, 27–30 October, 2013



Outline

Charge symmetry violation in nucleon structure

Warm-up: neutron–proton mass splitting

CSV in moments of parton distributions

Use hyperon moments from lattice QCD to determine CSV

Chiral extrapolation of octet baryon matrix elements

Implications for the NuTeV Standard Model test

CSV in nucleon structure

Proton–neutron symmetry. Exact if:

up–down quark masses degenerate $m_u = m_d$

quark electromagnetic charges equal $Q_u = Q_d$

In reality:

$$\frac{M_n - M_p}{M_p} \sim 0.14\%$$

Quark masses

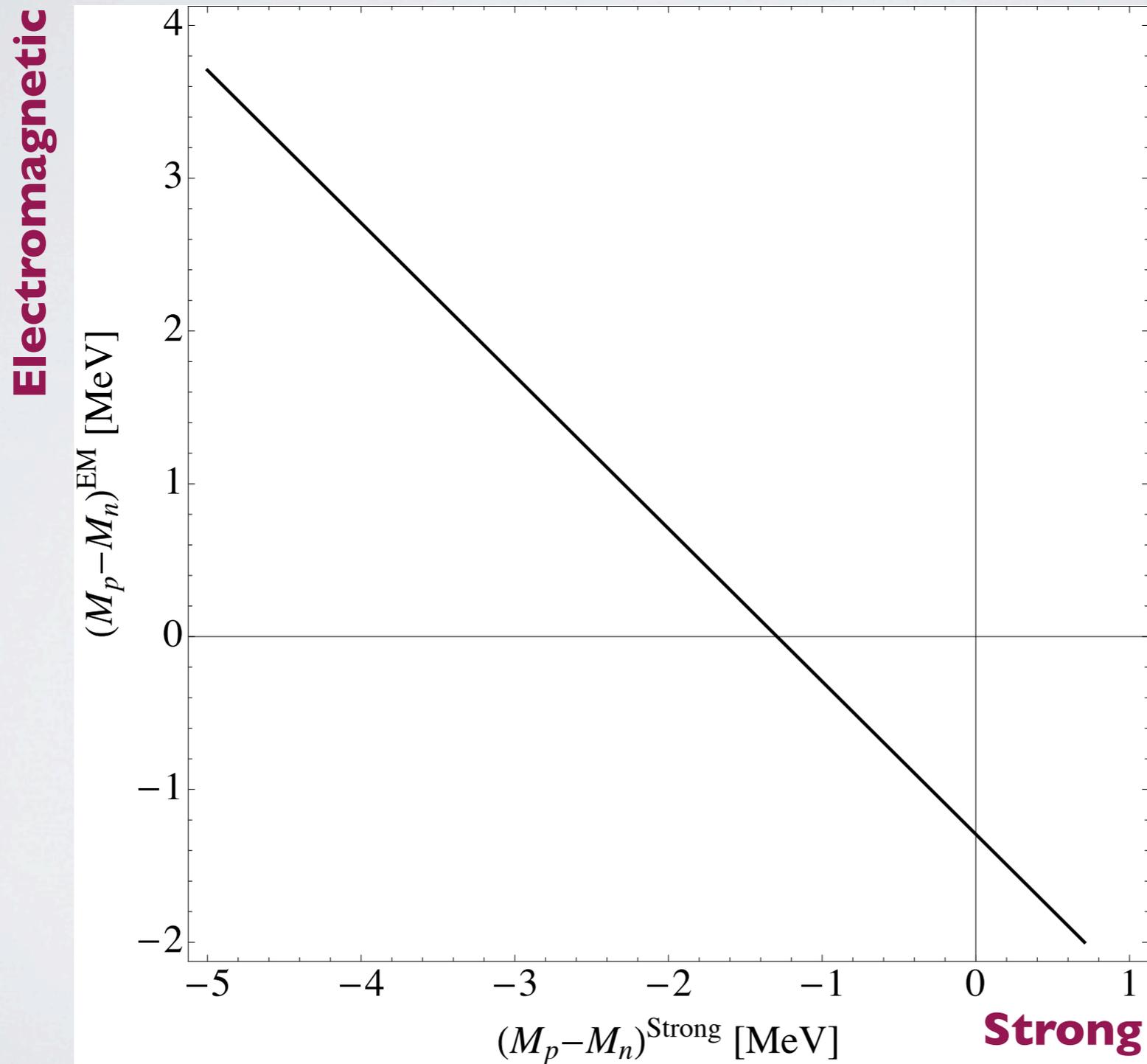
$$\frac{m_d - m_u}{M_p} \sim 0.5\%$$

Electromagnetic corrections $Q_u \neq Q_d$

$$\mathcal{O}(\alpha) \sim 1\%$$

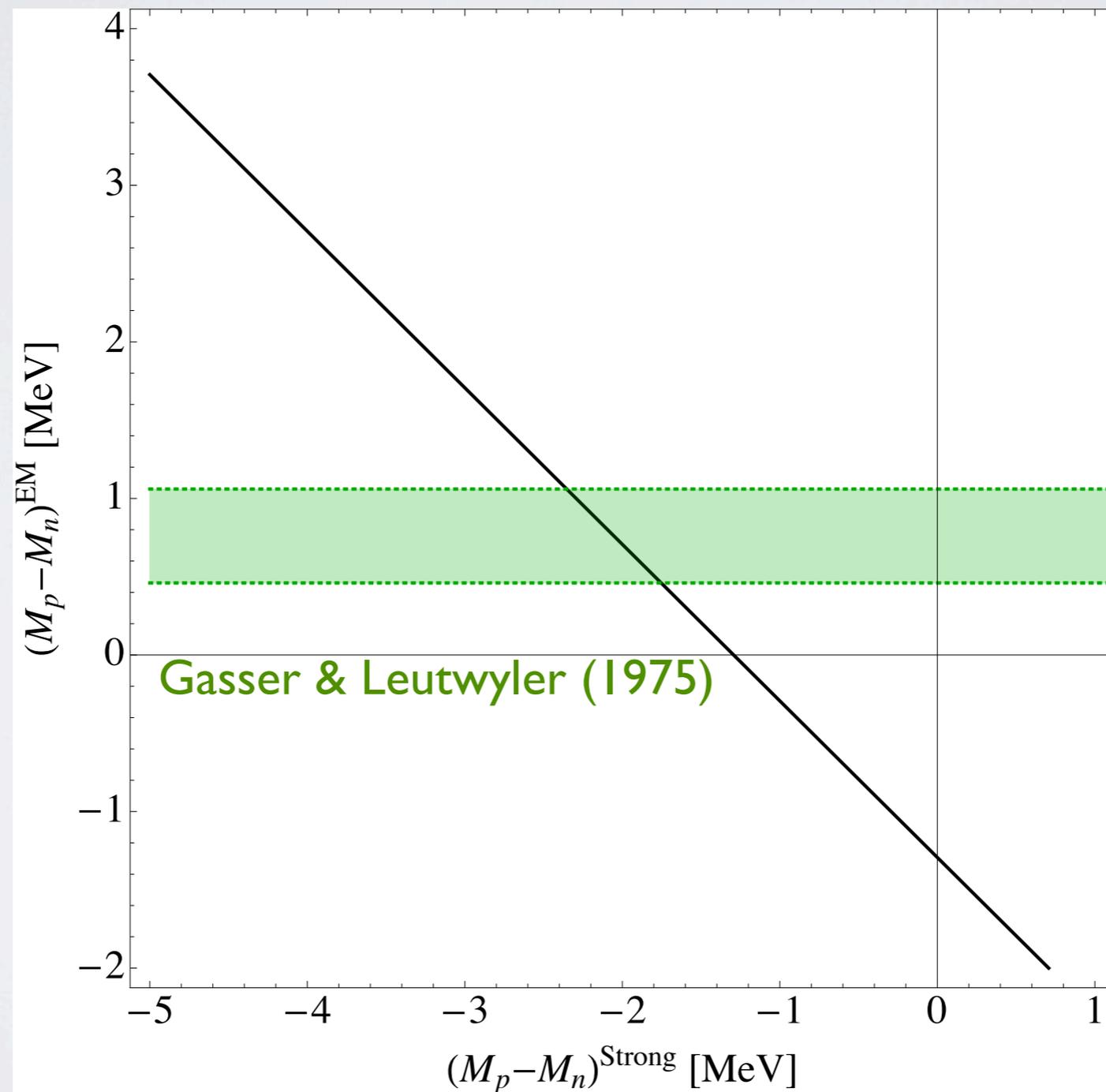
Experimental Constraint

Experiment: $M_p - M_n = -1.2933322(4) \text{ MeV}$



Cottingham Formula

Dispersion relation: electromagnetic self-energy written in terms of electron scattering observables



Subtracted Dispersion Relation

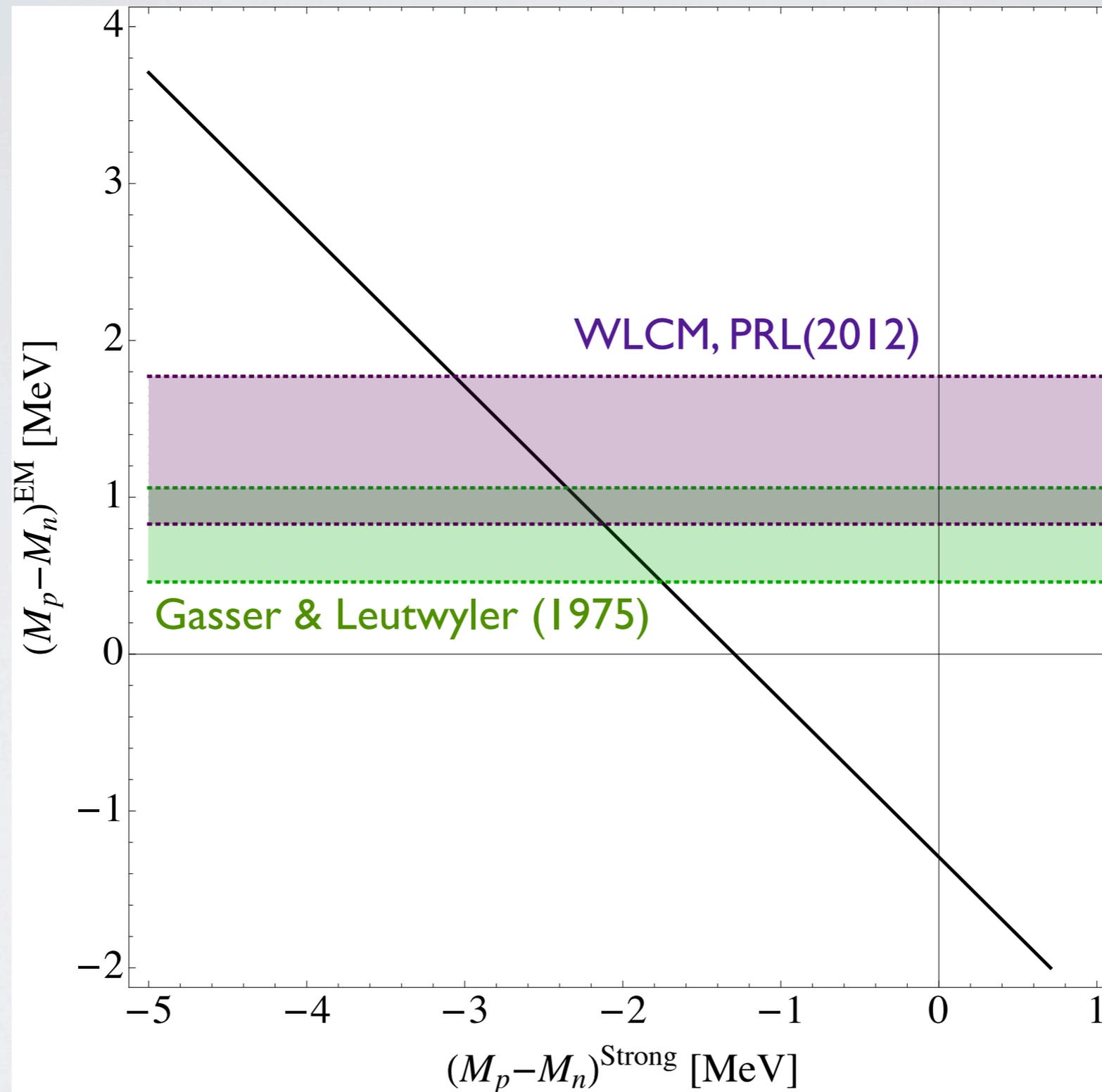
Walker-Loud, Carlson & Miller (WLCM), PRL(2012)

Standard Cottingham formula

Two Lorentz equivalent decompositions of the $\gamma N \rightarrow \gamma N$
Compton amplitude produce inequivalent self-energies

WLCM: Use a subtracted dispersion relation to remove this ambiguity

New dispersive result



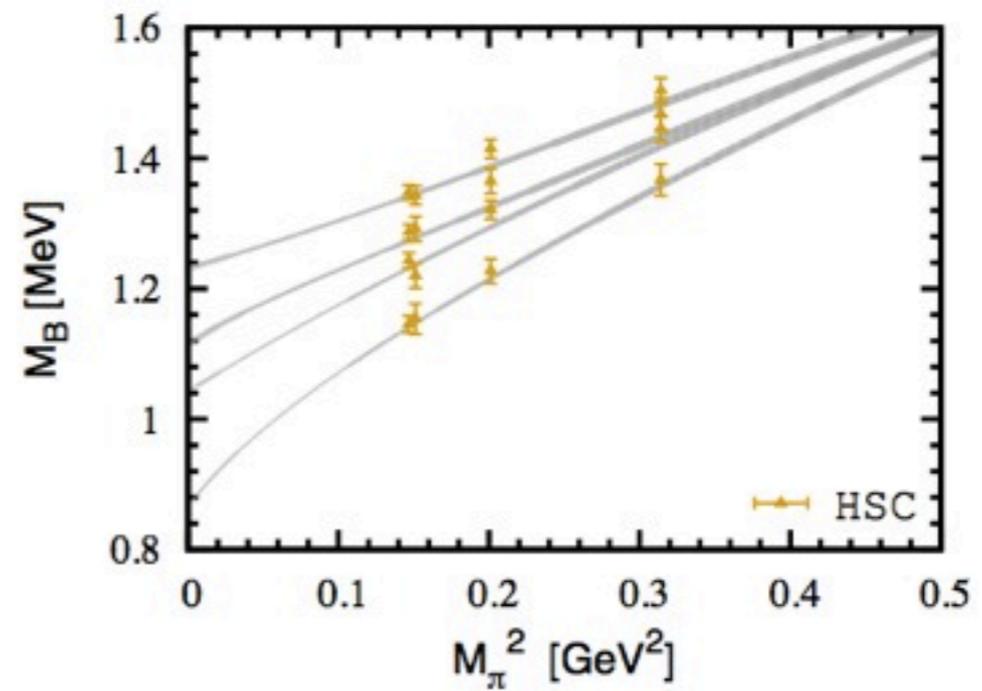
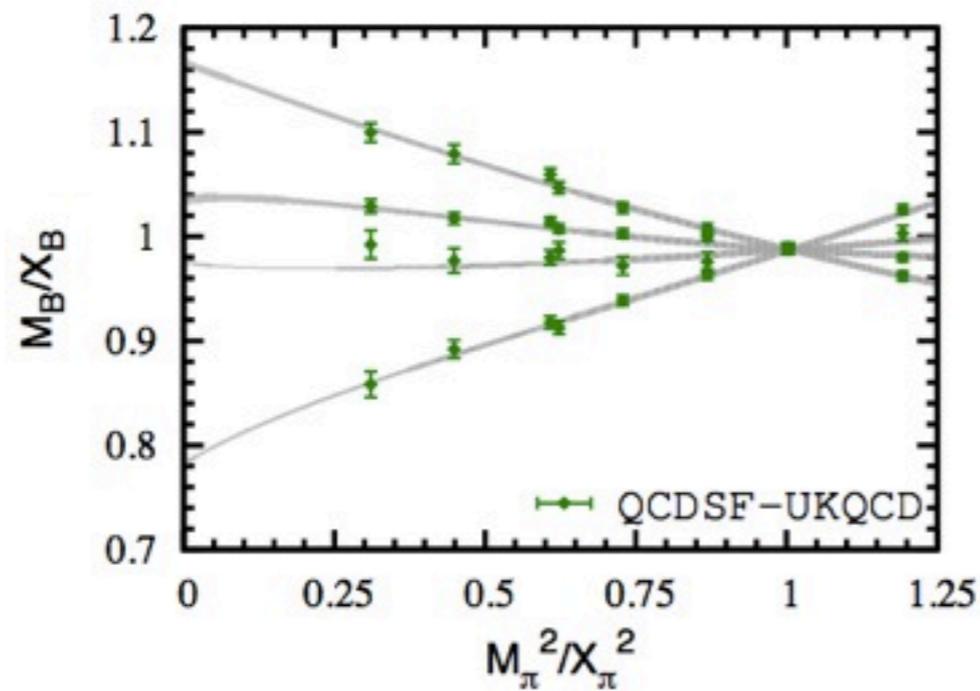
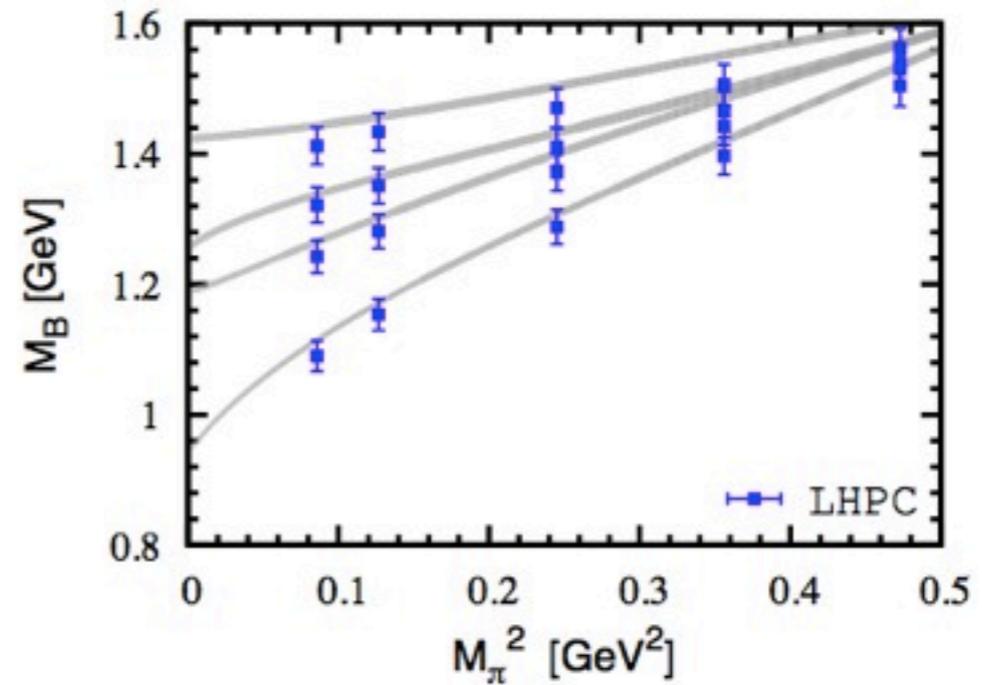
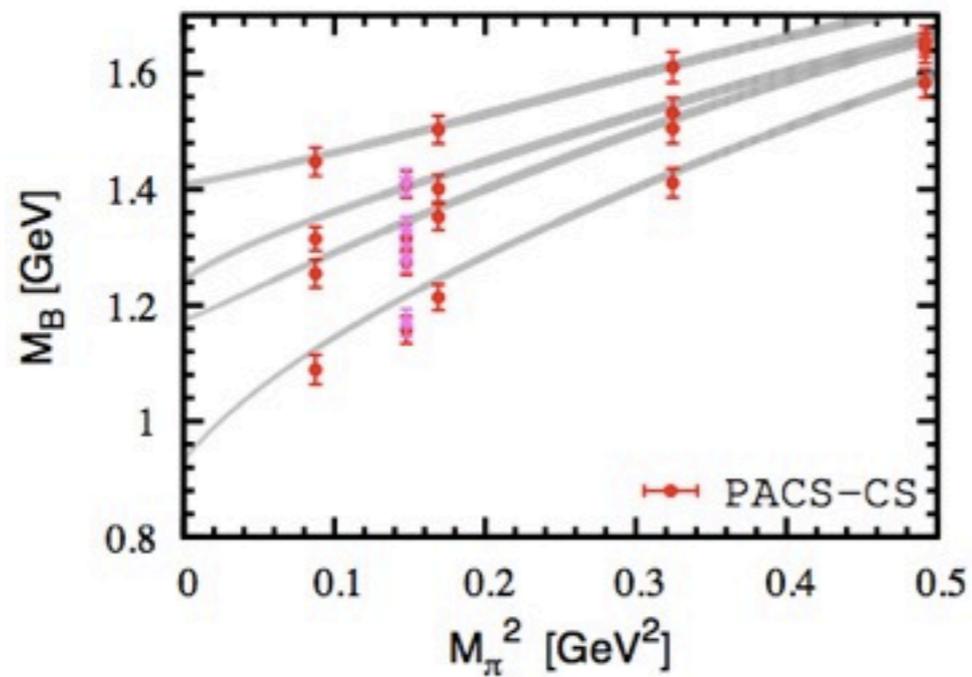
Precision limited by knowledge of real part of forward Compton amplitude

Lattice: “Strong”

Lattice QCD has a long history of describing quark mass dependence of observables

Lattice: "Strong"

Lattice
dependence



Octet baryon masses: NNNLO ChPT

X.-L. Ren et al., JHEP 12 (2012) 073

Lattice: “Strong”

Lattice QCD has a long history of describing quark mass dependence of observables

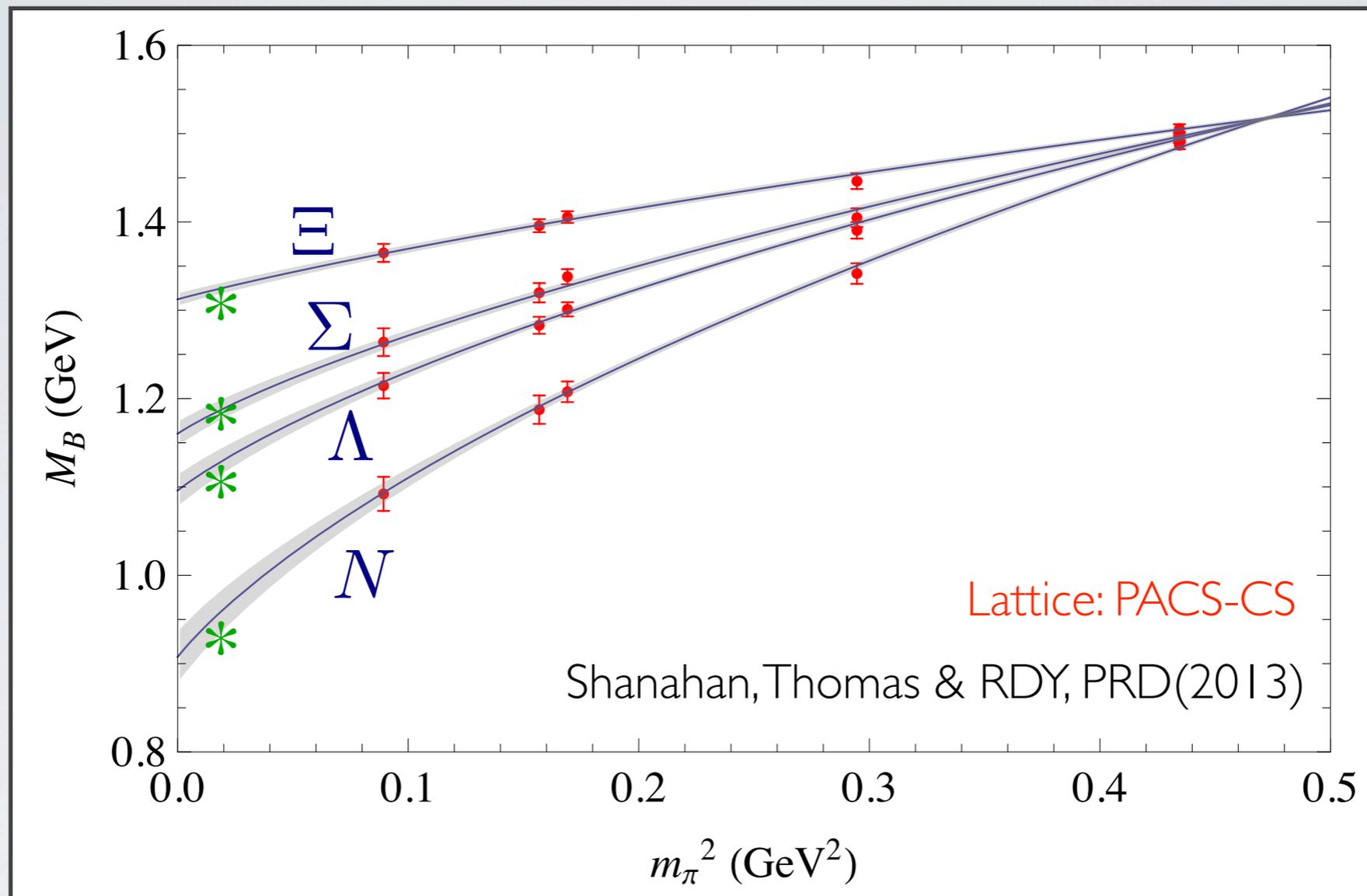
Just require splitting of up and down quark masses;

But, all dynamical lattice simulations have $m_u = m_d$

Study mass variation with partially-quenched valence quarks

Use SU(3) symmetry in relation to hyperon masses

SU(3) Finite-Range Regularisation

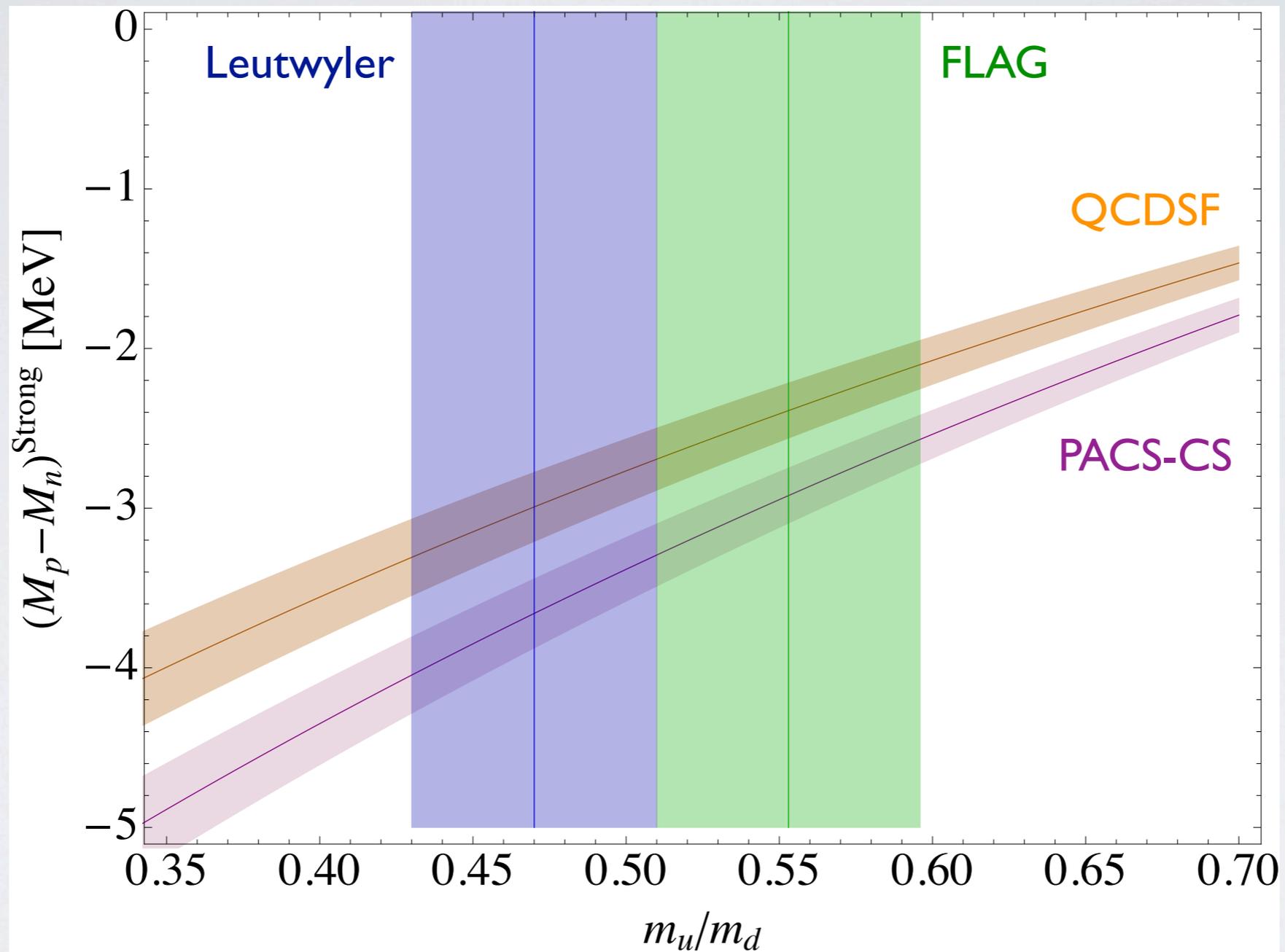


SU(2) symmetric simulation:

No new parameters in EFT to break SU(2)

Strong mass splitting

Sensitive to quark mass ratio



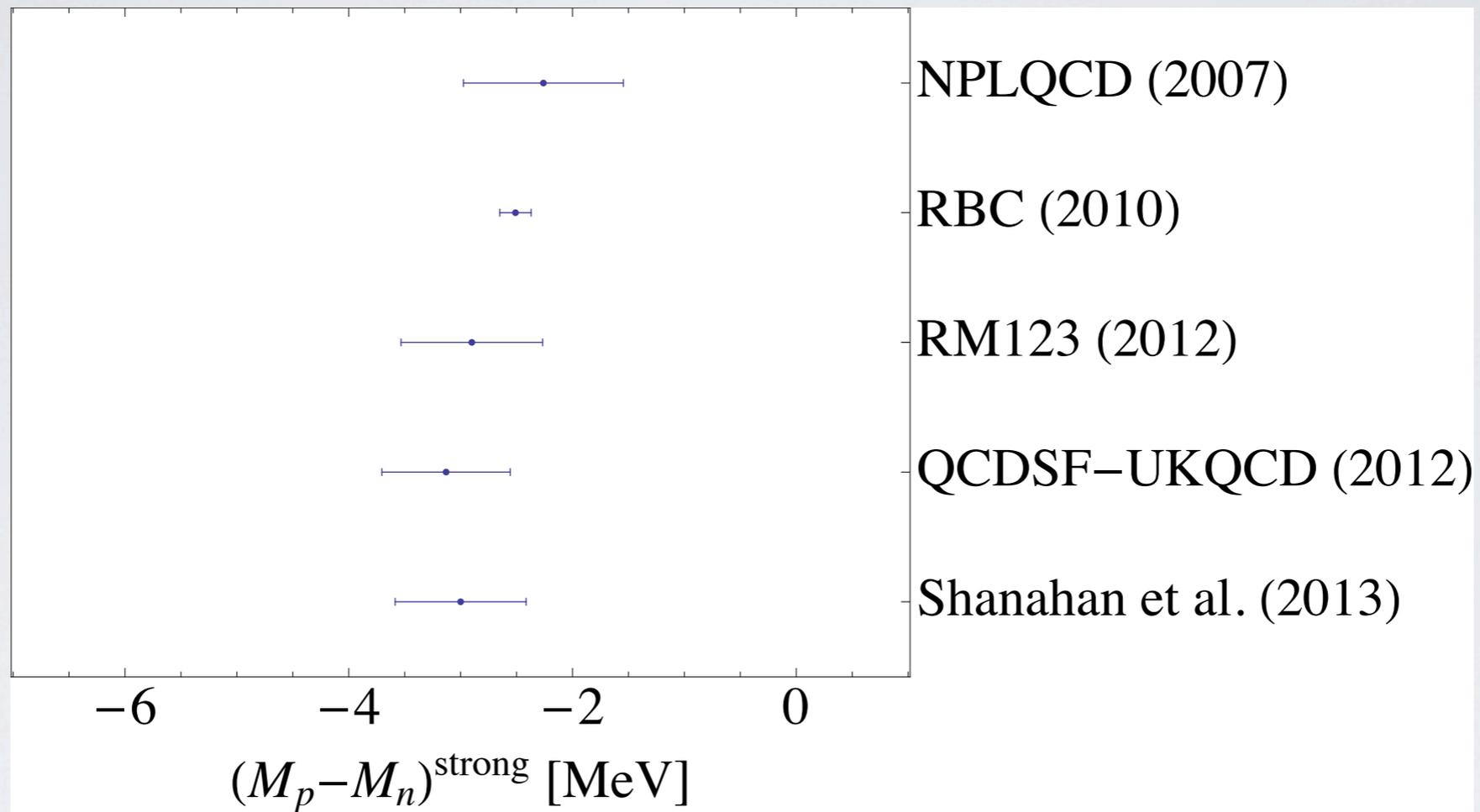
Our result

$$(M_p - M_n)^{\text{strong}} = -3.0 \pm 0.6 \text{ MeV}$$

Shanahan, Thomas & RDY, PLB(2013)

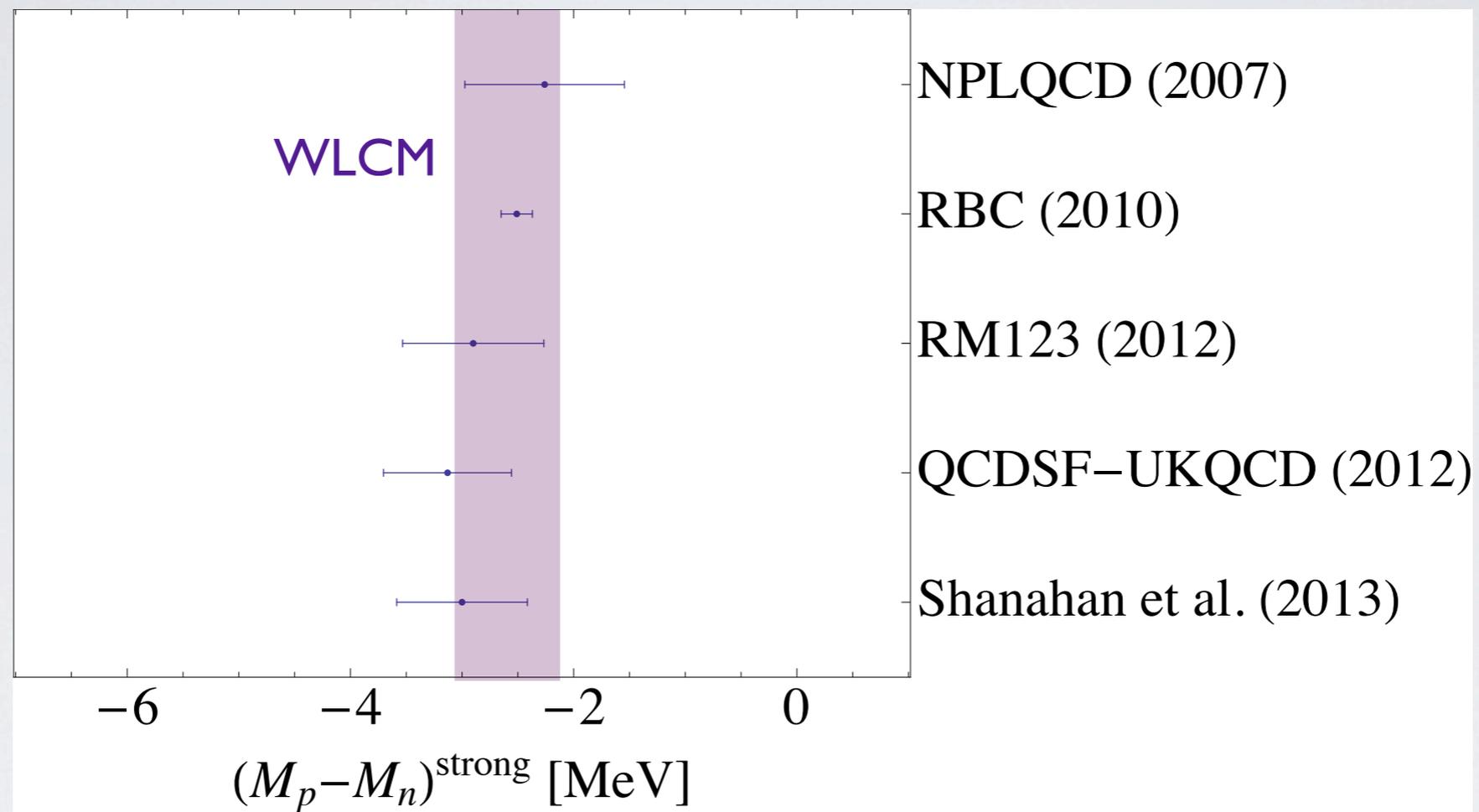
Lattice Summary

Lattice estimates of “strong” part of mass splitting



Lattice Summary

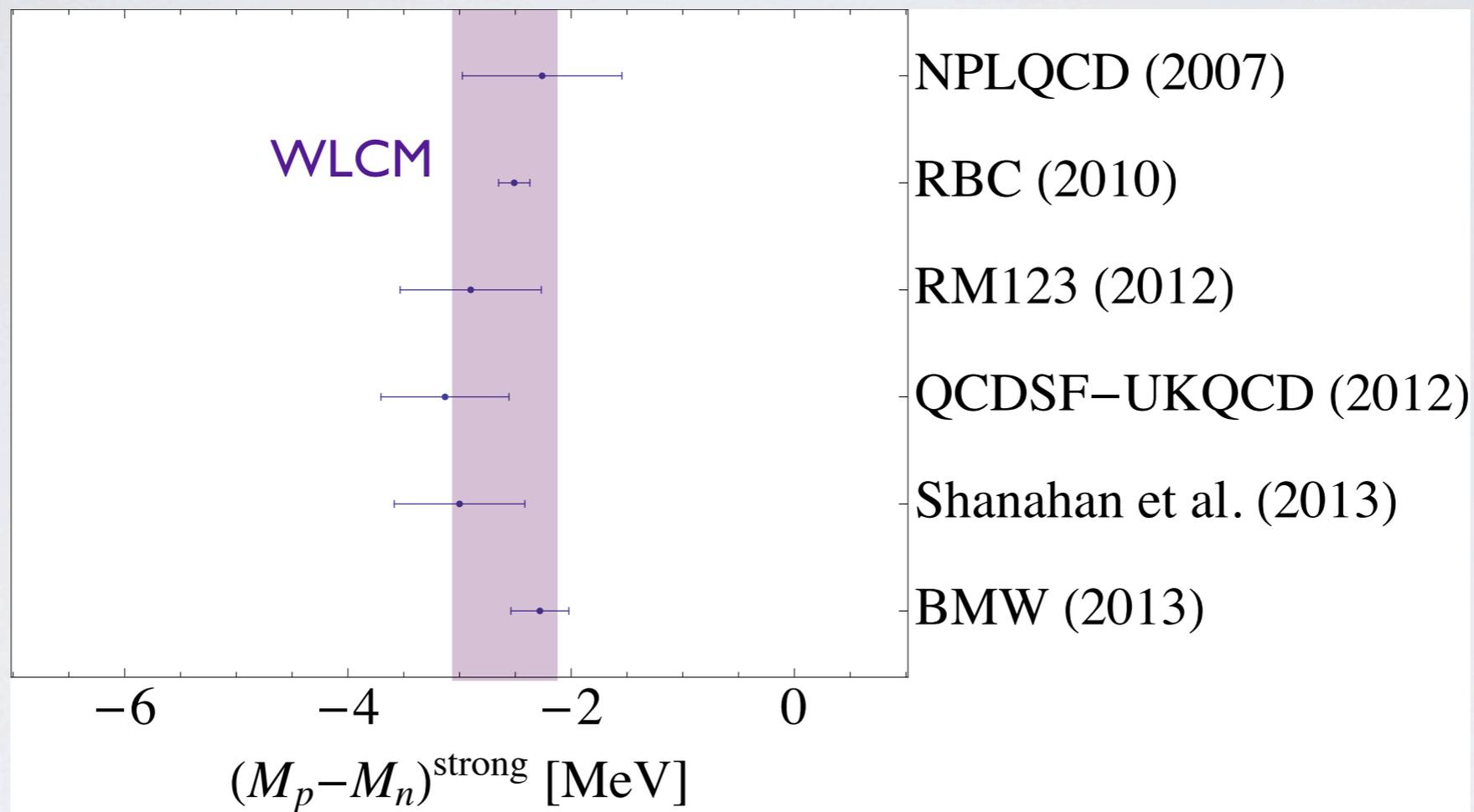
Lattice estimates of “strong” part of mass splitting



Consistent with dispersive estimate by WLCM

Lattice Summary

Lattice estimates of “strong” part of mass splitting

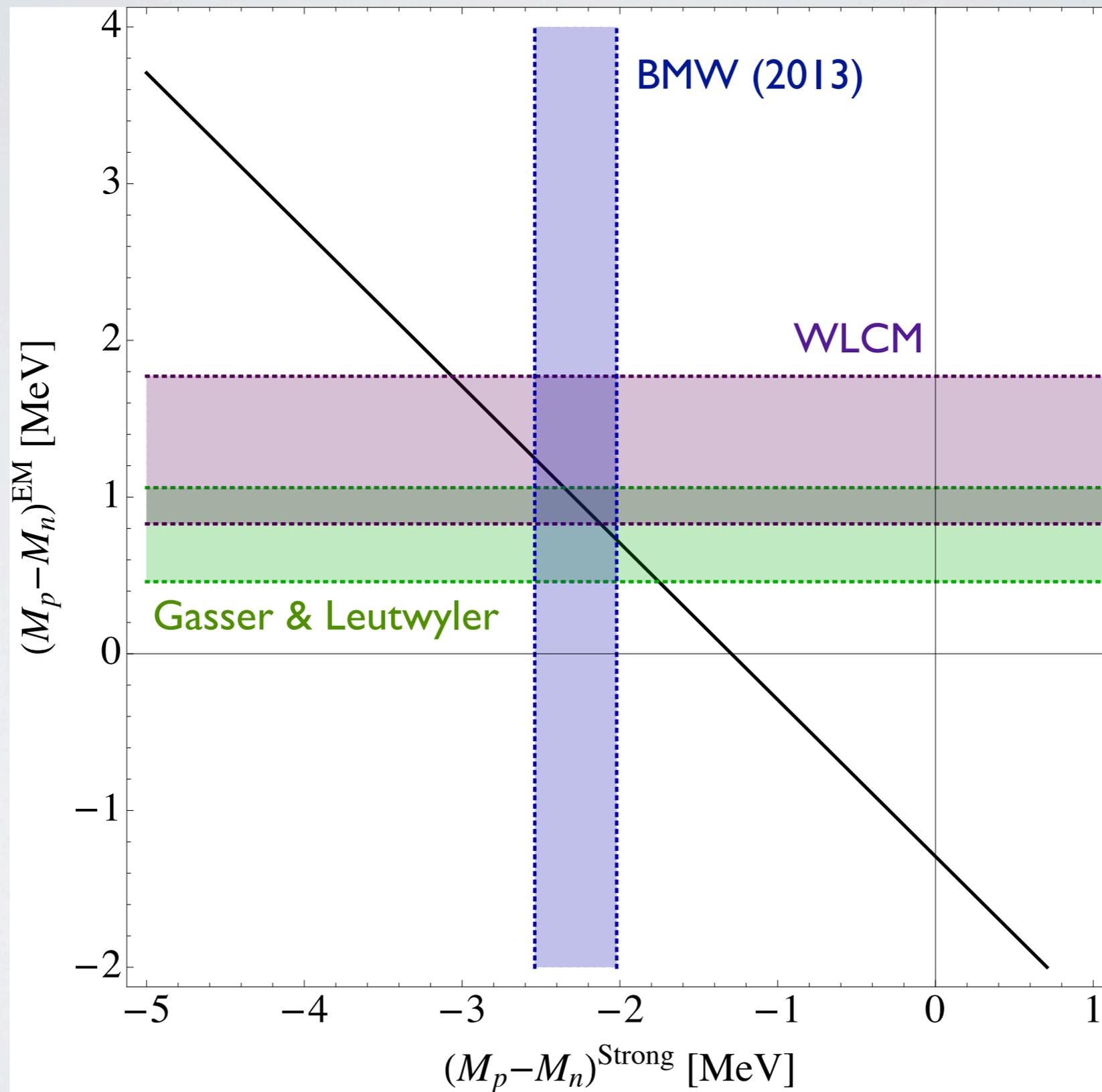


Consistent with dispersive estimate by WLCM

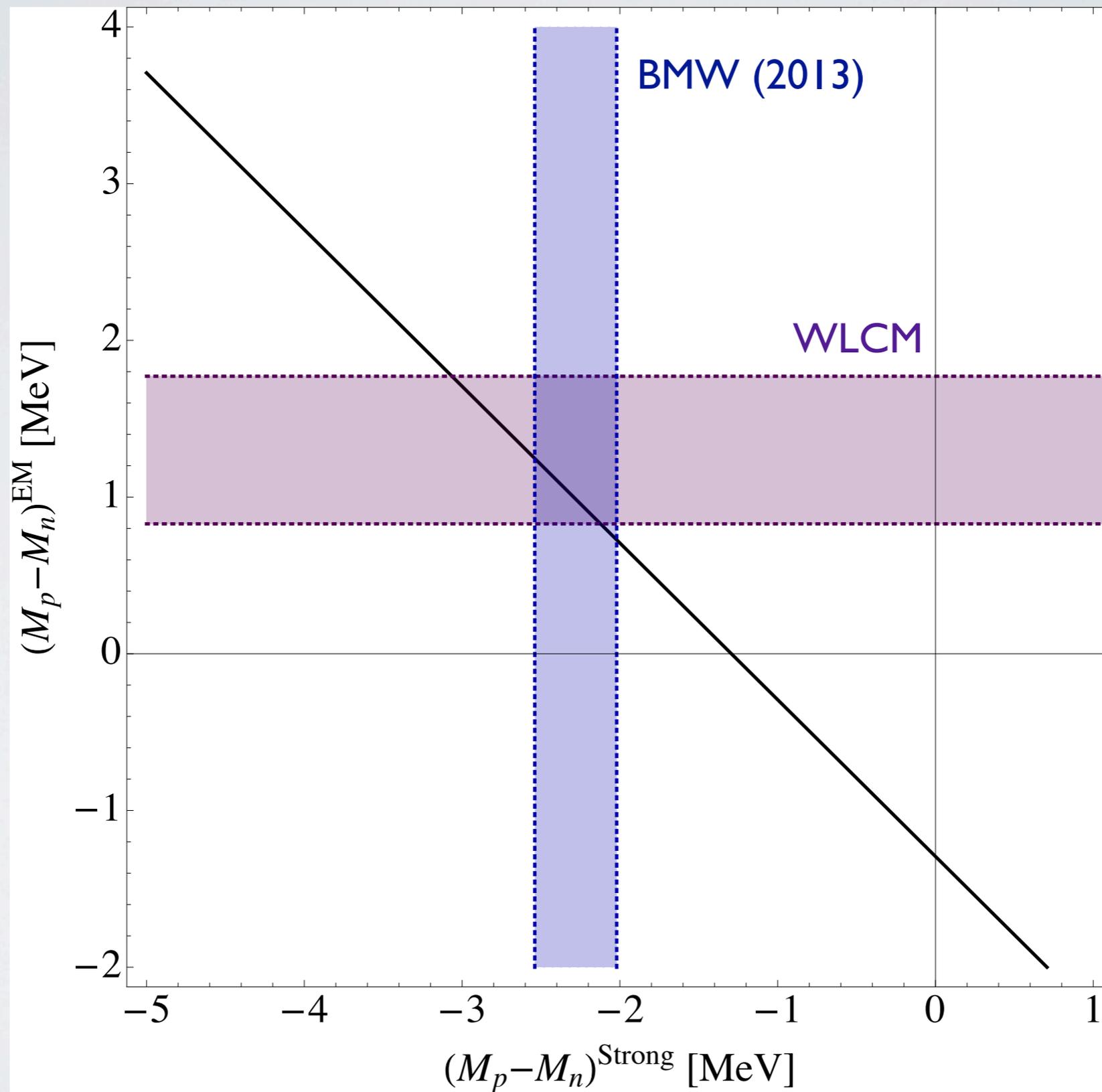
New BMW result

Shanahan et al.: better agreement with FLAG quark mass ratio

Current Status



Current Status



Are charge symmetry violations
relevant to nucleon structure?

NuTeV Experiment

NuTeV Experiment

Paschos-Wolfenstein ratio

$$R_{\text{PW}} = \frac{\sigma_{NC}^{\nu A} - \sigma_{NC}^{\bar{\nu} A}}{\sigma_{CC}^{\nu A} - \sigma_{CC}^{\bar{\nu} A}} \quad \nu - \bar{\nu} \quad \& \quad \frac{\text{neutral current}}{\text{charged current}}$$

NuTeV: indirect measure of this ratio

With

Exact charge symmetry

Vanishing partonic strangeness $s(x) = \bar{s}(x)$

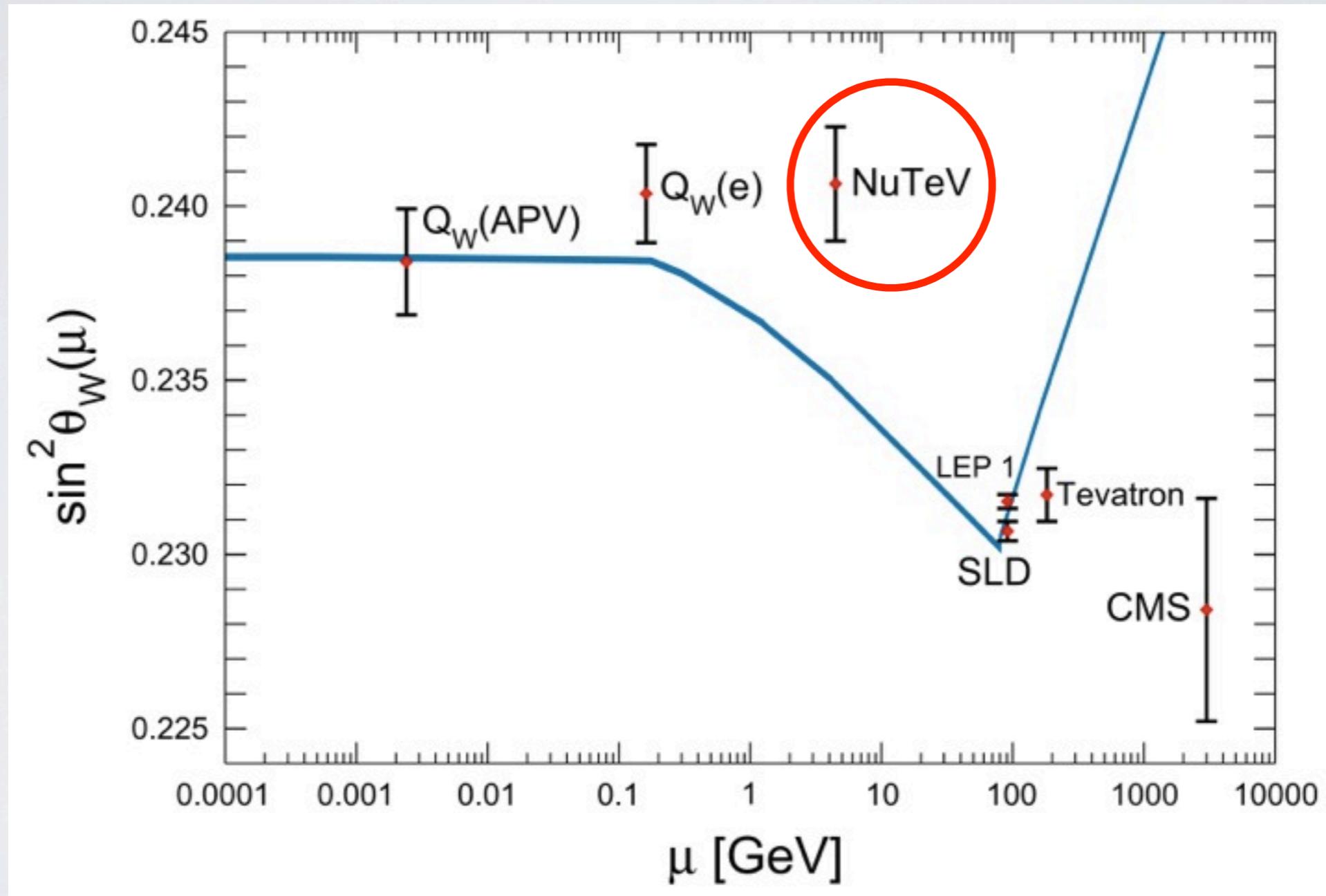
Isoscalar nucleus

\Rightarrow PW ratio direct measure of weak mixing angle

$$R_{\text{PW}} \rightarrow \frac{1}{2} - \sin^2 \theta_W$$

NuTeV & $\sin^2 \theta_W$

NuTeV report a 3-sigma discrepancy from the Standard Model



Relies on assumption that CSV is negligible

Charge symmetry violation in partons

Partonic charge symmetry relations

$$u^p(x) = d^n(x)$$

$$d^p(x) = u^n(x)$$

Charge symmetry violation in partons

Partonic charge symmetry relations

$$u^p(x) = d^n(x)$$

$$d^p(x) = u^n(x)$$

Let's appeal to lattice to determine the breaking

$$\delta u(x) \equiv u^p(x) - d^n(x)$$

$$\delta d(x) \equiv d^p(x) - u^n(x)$$

Charge symmetry violation in partons

Partonic charge symmetry relations

$$u^p(x) = d^n(x)$$

$$d^p(x) = u^n(x)$$

Let's appeal to lattice to determine the breaking

$$\delta u(x) \equiv u^p(x) - d^n(x)$$

$$\delta d(x) \equiv d^p(x) - u^n(x)$$

Lattice can only make contact with moments

$$\langle x^{m-1} \rangle = \int_0^1 dx x^{m-1} [q(x) + (-1)^m \bar{q}(x)]$$

Parton CSV

For small breaking in the u - d quark masses $m_\delta \equiv (m_d - m_u)$

$$\langle x \rangle_{\delta u} \simeq \frac{m_\delta}{2} \left[\left(-\frac{\partial \langle x \rangle_u^p}{\partial m_u} + \frac{\partial \langle x \rangle_u^p}{\partial m_d} \right) - \left(-\frac{\partial \langle x \rangle_d^n}{\partial m_u} + \frac{\partial \langle x \rangle_d^n}{\partial m_d} \right) \right]$$

Parton CSV

For small breaking in the u - d quark masses $m_\delta \equiv (m_d - m_u)$

$$\langle x \rangle_{\delta u} \simeq \frac{m_\delta}{2} \left[\left(-\frac{\partial \langle x \rangle_u^p}{\partial m_u} + \frac{\partial \langle x \rangle_u^p}{\partial m_d} \right) - \left(-\frac{\partial \langle x \rangle_d^n}{\partial m_u} + \frac{\partial \langle x \rangle_d^n}{\partial m_d} \right) \right]$$


Charge symmetry

Parton CSV

For small breaking in the u - d quark masses $m_\delta \equiv (m_d - m_u)$

$$\langle x \rangle_{\delta u} \simeq \frac{m_\delta}{2} \left[\left(-\frac{\partial \langle x \rangle_u^p}{\partial m_u} + \frac{\partial \langle x \rangle_u^p}{\partial m_d} \right) - \left(-\frac{\partial \langle x \rangle_d^n}{\partial m_u} + \frac{\partial \langle x \rangle_d^n}{\partial m_d} \right) \right]$$

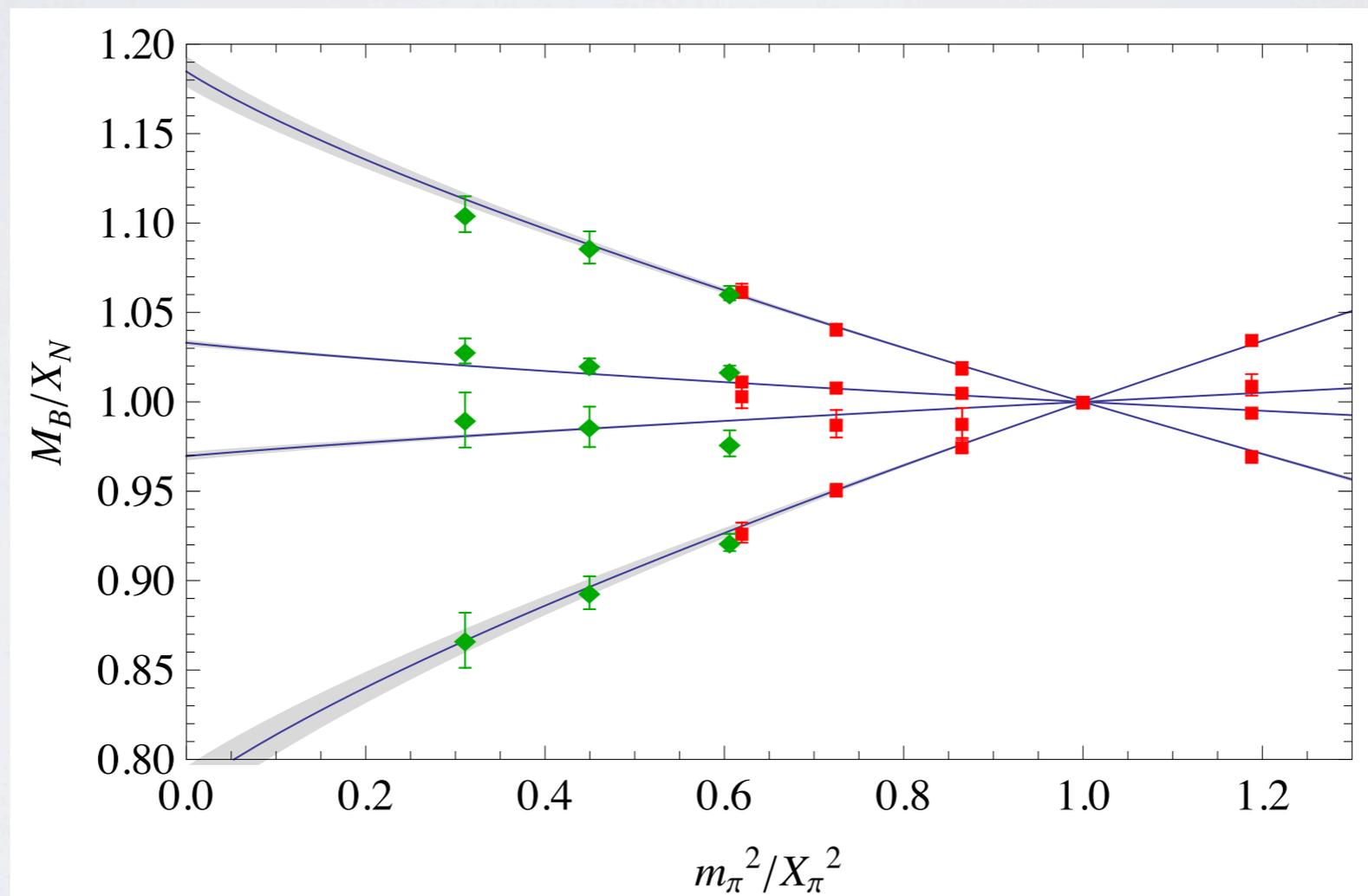

Charge symmetry

$$\langle x \rangle_{\delta u} \simeq m_\delta \left[-\frac{\partial \langle x \rangle_u^p}{\partial m_u} + \frac{\partial \langle x \rangle_u^p}{\partial m_d} \right]$$

QCDSF-UKQCD Lattices

Tune lattice parameters such to have exact SU(3) symmetry at the physical average (light) quark mass

$$\overline{m}_q^{\text{lat}} = (m_u + m_d + m_s)^{\text{phys}} / 3$$



Hold singlet mass fixed on trajectory to physical point

Hyperon PDF moments

Near SU(3) symmetric point

$$\langle x \rangle_u^p \simeq \langle x \rangle_u^{\Sigma^+} \simeq \langle x \rangle_s^{\Xi^0}$$

Hence we can estimate relevant derivatives

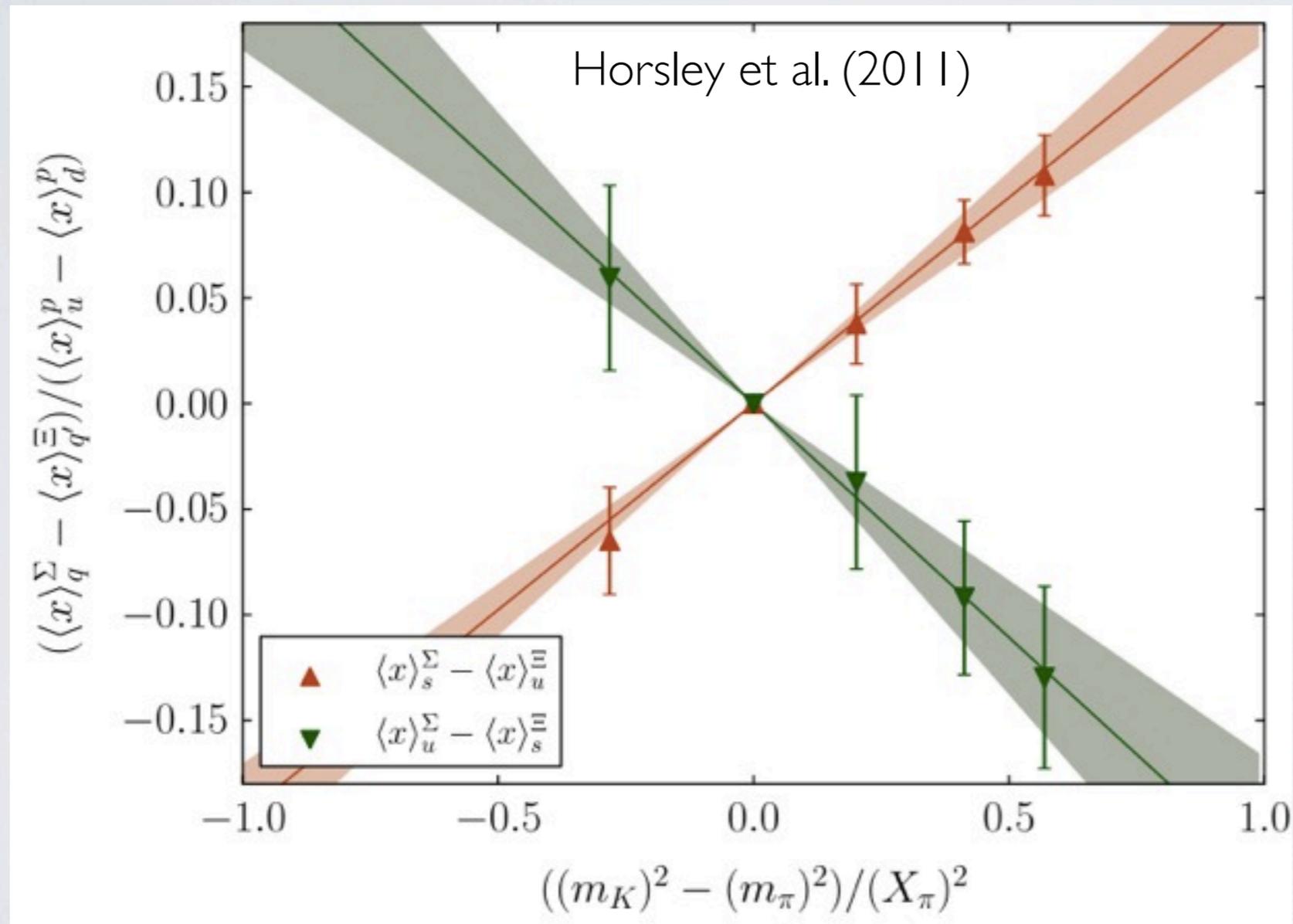
$$\frac{\partial \langle x \rangle_u^p}{\partial m_u} \simeq \frac{\langle x \rangle_s^{\Xi^0} - \langle x \rangle_u^p}{m_s - m_l}, \quad \frac{\partial \langle x \rangle_u^p}{\partial m_d} \simeq \frac{\langle x \rangle_u^{\Sigma^+} - \langle x \rangle_u^p}{m_s - m_l}$$

$$\Rightarrow \langle x \rangle_{\delta u} \simeq m_\delta \left[-\frac{\partial \langle x \rangle_u^p}{\partial m_u} + \frac{\partial \langle x \rangle_u^p}{\partial m_d} \right] \simeq m_\delta \frac{\langle x \rangle_u^{\Sigma^+} - \langle x \rangle_s^{\Xi^0}}{m_s - m_l}$$

Just need to determine hyperon moments about SU(3) symmetric point

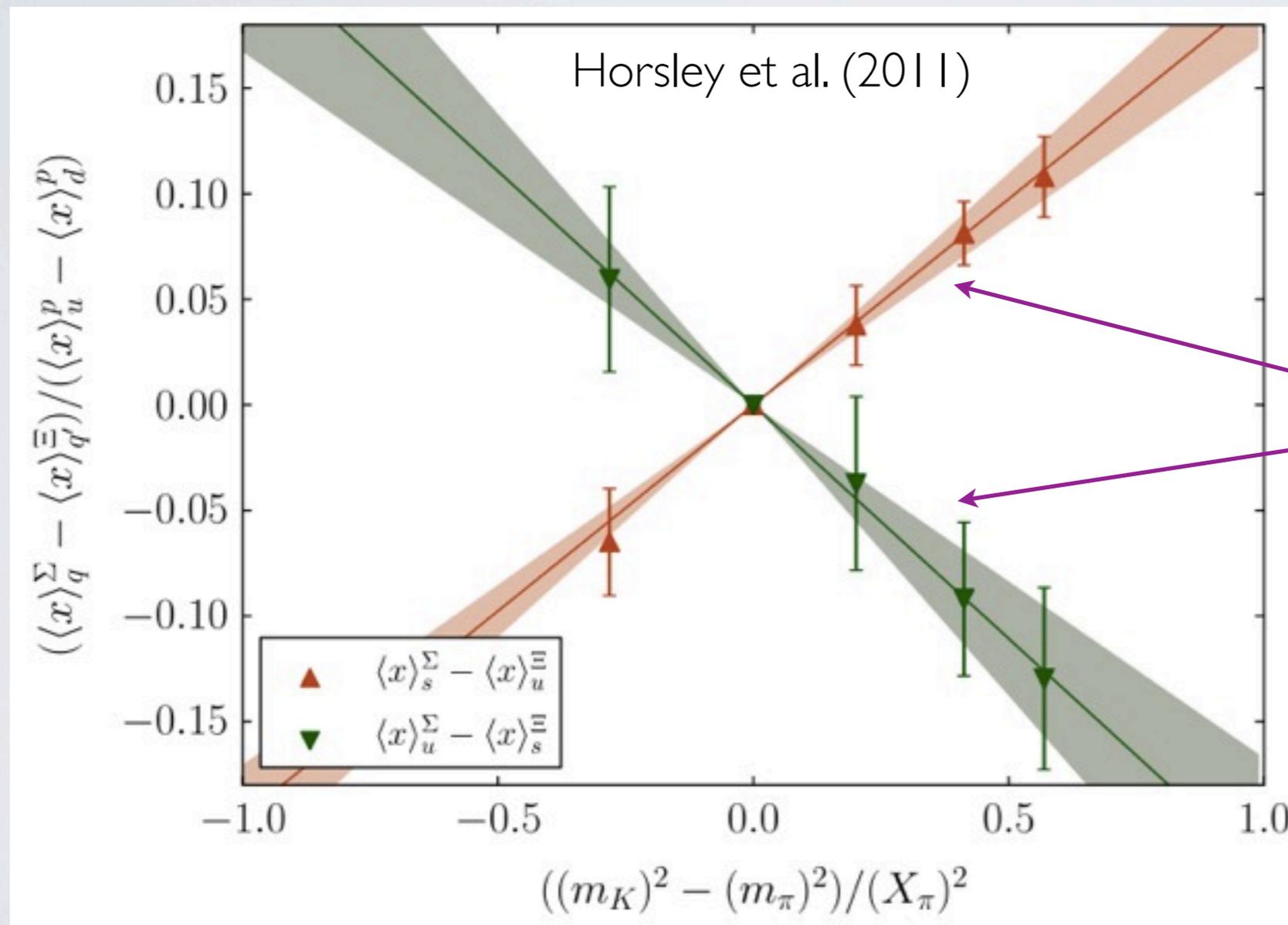
Charge Symmetry Violation

Lattice results for quark-mass dependence of hyperon momentum fractions



Charge Symmetry Violation

Lattice results for quark-mass dependence of hyperon momentum fractions



Slopes determine
CSV at SU(3)
symmetric point

Chiral extrapolation of hyperon moments

Tree-level operators

$$\left[\alpha^{(n)} (\bar{B} B \lambda_q) + \beta^{(n)} (\bar{B} \lambda_q B) + \sigma^{(n)} (\bar{B} B) \text{Tr}(\lambda_q) \right] p^{\{\mu_1 \dots \mu_n\}} - \text{Tr}$$

$\mathcal{O}(m_q)$ counterterms

$$\left\{ \begin{aligned} & b_1^{(n)} \text{Tr} [\bar{B} [[\lambda_q, B], M]] + b_2^{(n)} \text{Tr} [\bar{B} \{[\lambda_q, B], M\}] \\ & + b_3^{(n)} \text{Tr} [\bar{B} [\{\lambda_q, B\}, M]] + b_4^{(n)} \text{Tr} [\bar{B} \{\{\lambda_q, B\}, M\}] \\ & + b_5^{(n)} \text{Tr} [\bar{B} B] \text{Tr} [\lambda_q M] + b_6^{(n)} \text{Tr} [\bar{B} B \lambda_q] \text{Tr} [M] \\ & + b_7^{(n)} \text{Tr} [\bar{B} \lambda_q B] \text{Tr} [M] + b_8^{(n)} \text{Tr} [\bar{B} M B] \text{Tr} [\lambda_q] \\ & + b_9^{(n)} \text{Tr} [\bar{B} B M] \text{Tr} [\lambda_q] \\ & + b_{10}^{(n)} \text{Tr} [\bar{B} \lambda_q] \text{Tr} [M B] \end{aligned} \right\} p^{\{\mu_1 \dots \mu_n\}} - \text{Tr}$$

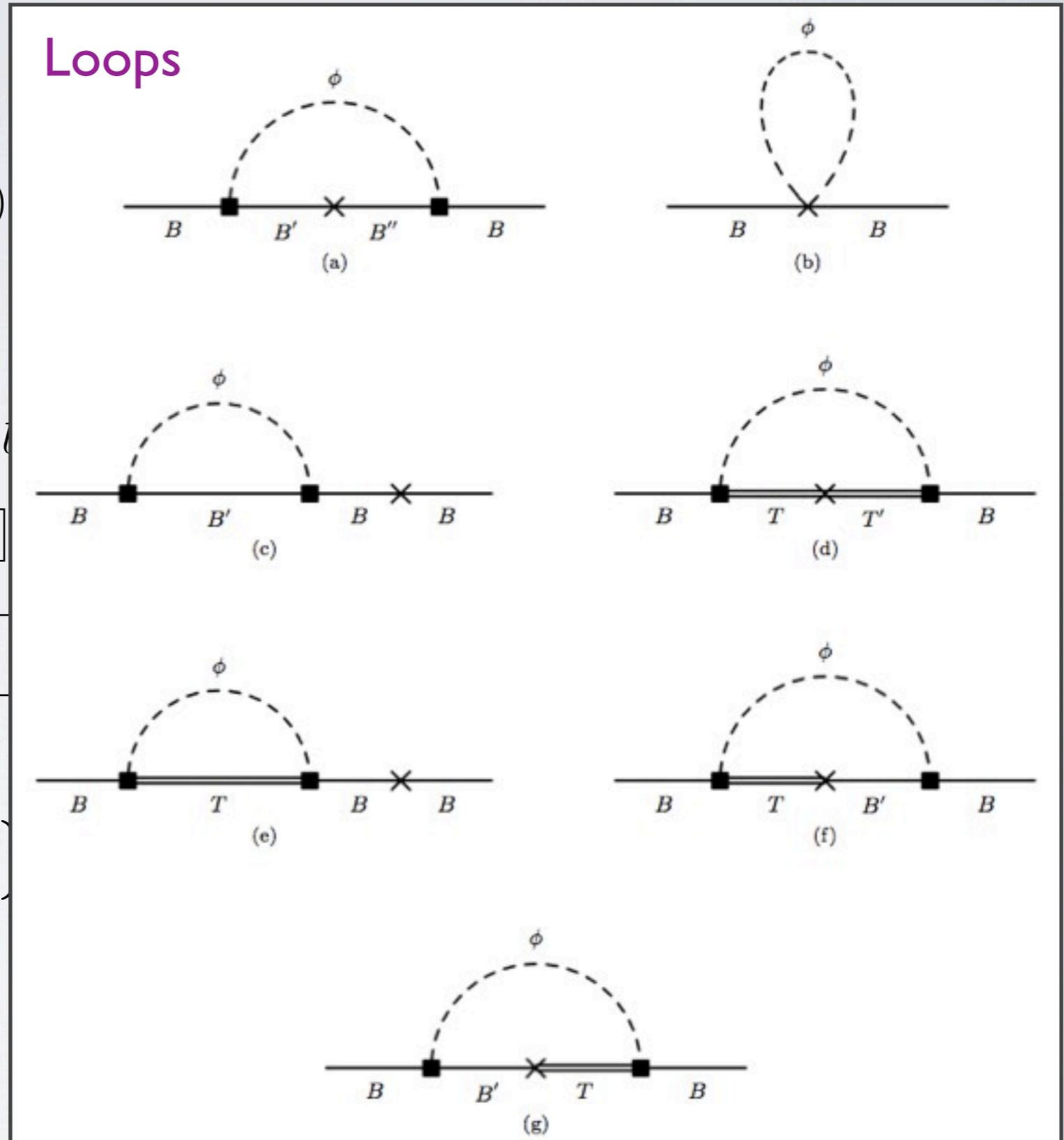
Chiral extrapolation of hyperon moments

Tree-level operators

$$\left[\alpha^{(n)} (\overline{B} B \lambda_q) + \beta^{(n)} (\overline{B} \lambda_q B) \right]$$

$\mathcal{O}(m_q)$ counterterms

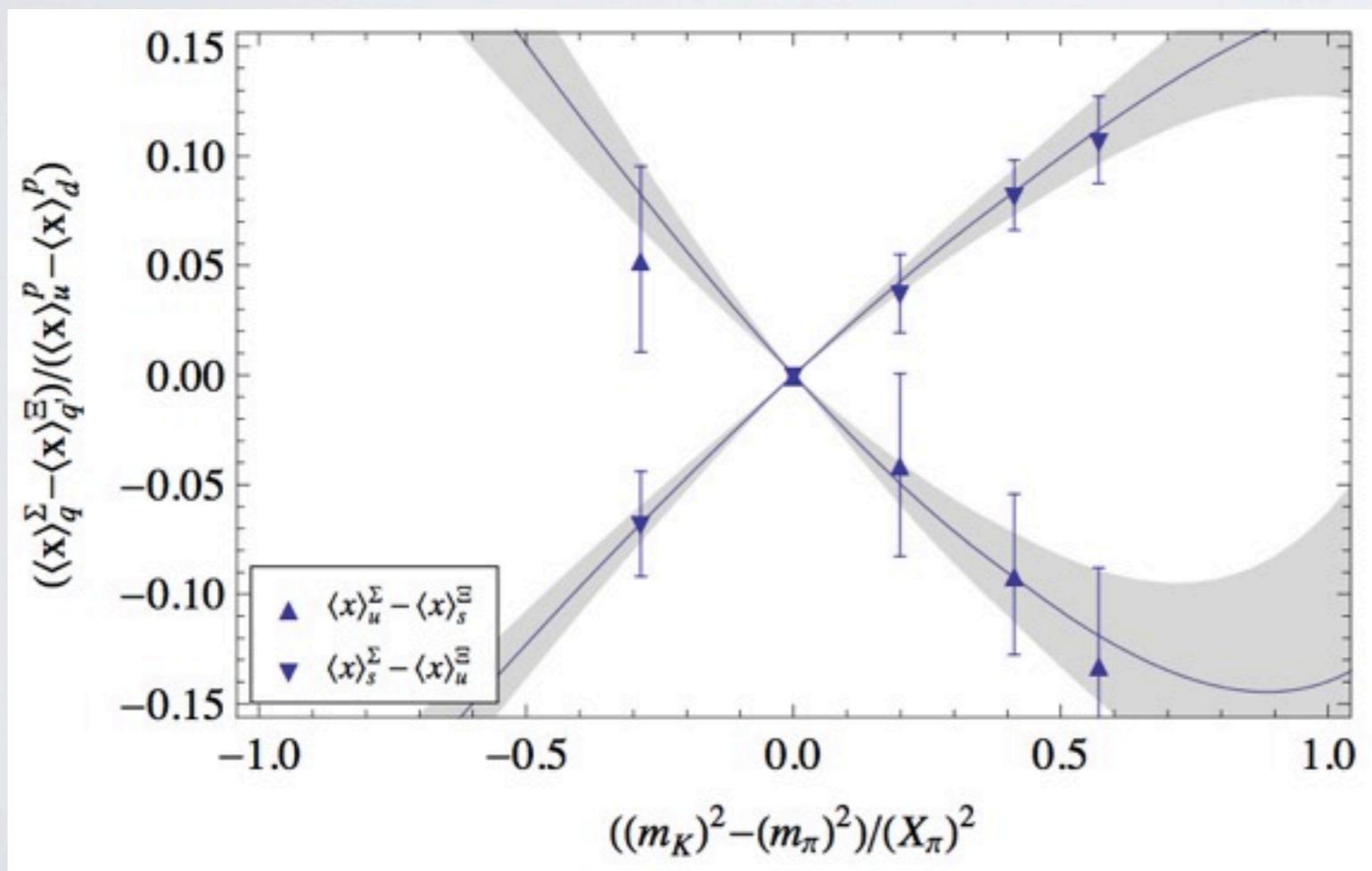
$$\left\{ \begin{aligned} & b_1^{(n)} \text{Tr} [\overline{B} [[\lambda_q, B], M]] + \\ & + b_3^{(n)} \text{Tr} [\overline{B} [\{\lambda_q, B\}, M]] + \\ & + b_5^{(n)} \text{Tr} [\overline{B} B] \text{Tr} [\lambda_q M] + \\ & + b_7^{(n)} \text{Tr} [\overline{B} \lambda_q B] \text{Tr} [M] + \\ & + b_9^{(n)} \text{Tr} [\overline{B} B M] \text{Tr} [\lambda_q] + \\ & + b_{10}^{(n)} \text{Tr} [\overline{B} \lambda_q] \text{Tr} [M B] \end{aligned} \right\}$$



Chiral extrapolation of CSV

Just as for baryon masses, we can fit isospin symmetric lattice results for hyperons

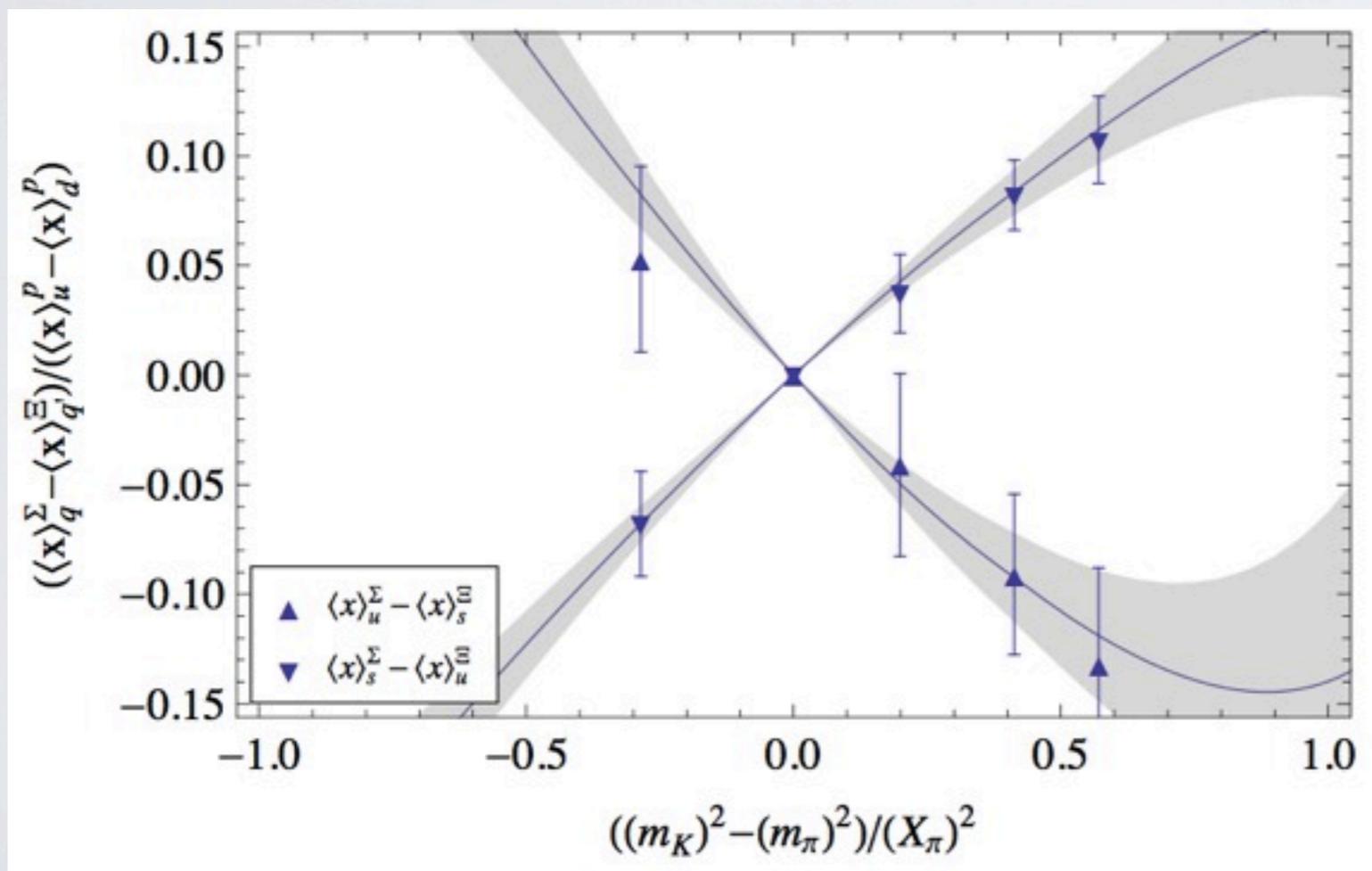
No new parameters in EFT to determine CSV



Chiral extrapolation of CSV

Just as for baryon masses, we can fit isospin symmetric lattice results for hyperons

No new parameters in EFT to determine CSV



Our result

$$\langle x \rangle_{\delta u} = -0.0023(7)$$

$$\langle x \rangle_{\delta d} = 0.0017(4)$$

Back to NuTeV

Correction to the Paschos-Wolfenstein ratio from CSV

$$\Delta R_{\text{PW}}^{\text{CSV}} = \frac{1}{2} \left(1 - \frac{7}{3} \sin^2 \theta_W \right) \frac{\langle x \rangle_{\delta u^-} - \langle x \rangle_{\delta d^-}}{\langle x \rangle_{u^-} + \langle x \rangle_{d^-}}$$

Back to NuTeV

Correction to the Paschos-Wolfenstein ratio from CSV

$$\Delta R_{\text{PW}}^{\text{CSV}} = \frac{1}{2} \left(1 - \frac{7}{3} \sin^2 \theta_W \right) \frac{\langle x \rangle_{\delta u^-} - \langle x \rangle_{\delta d^-}}{\langle x \rangle_{u^-} + \langle x \rangle_{d^-}}$$

Our result + CSV from QED parton evolution

⇒ Reduce NuTeV Standard Model discrepancy by ~ 1 -sigma

Back to NuTeV

Correction to the Paschos-Wolfenstein ratio from CSV

$$\Delta R_{\text{PW}}^{\text{CSV}} = \frac{1}{2} \left(1 - \frac{7}{3} \sin^2 \theta_W \right) \frac{\langle x \rangle_{\delta u^-} - \langle x \rangle_{\delta d^-}}{\langle x \rangle_{u^-} + \langle x \rangle_{d^-}}$$

Our result + CSV from QED parton evolution

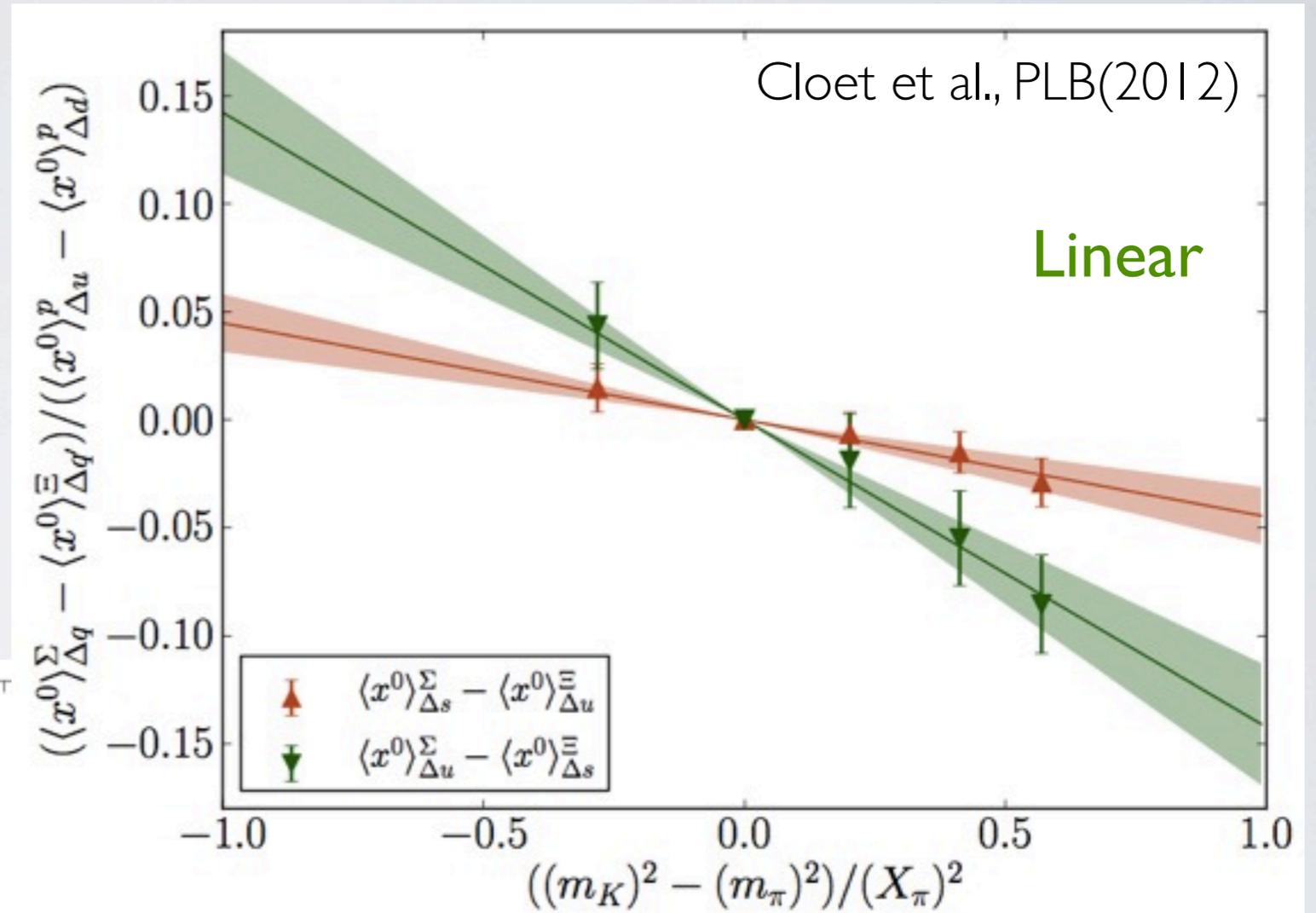
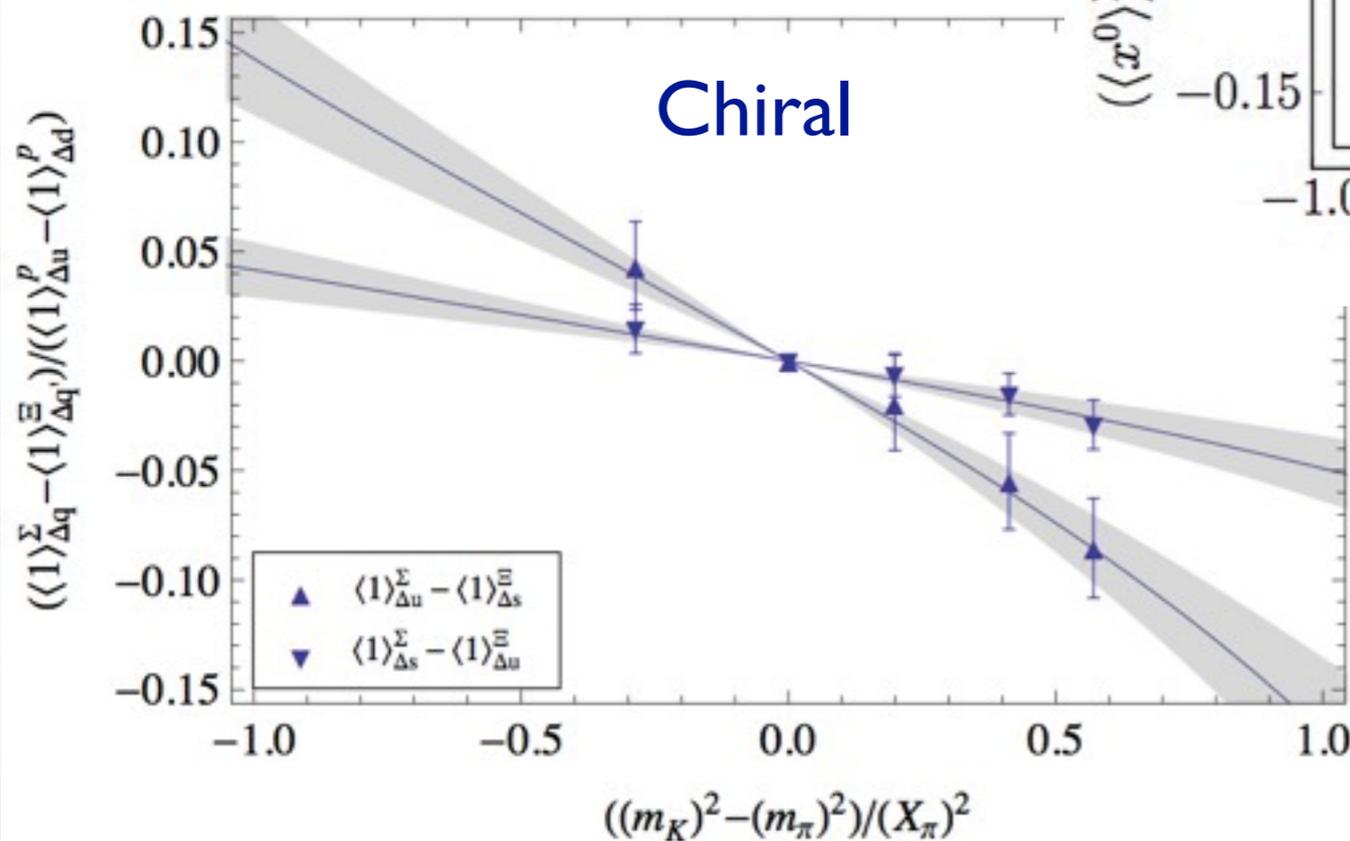
⇒ Reduce NuTeV Standard Model discrepancy by ~ 1 -sigma

Futher corrections: Non-isoscalar nucleus, strangeness

see Bentz, Cloet, Londergan & Thomas PLB(2010)

Spin-dependent CSV

~1% correction to the Bjorken sum rule



Summary

Effects of charge symmetry violation are becoming increasingly significant in precision studies

Improved understanding of the proton-neutron mass splitting

Subtracted Cottingham formula & new lattice results

Unambiguously resolved CSV parton moments in lattice QCD

Reduces the NuTeV anomaly

Could improve sensitivity of future SM tests: eg. PVDIS@JLab

Spin-dependent CSV could be seen at future electron collider

Thanks [see *parallel talk*: P. Shanahan, 9:20am Tuesday]

Phiala Shanahan, Tony Thomas, James Zanotti, QCDSF-UKQCD