

# Exotic dibaryons with a heavy antiquark

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in collaboration with

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Hadrons and Nuclei (Chiral2013)

# Outline

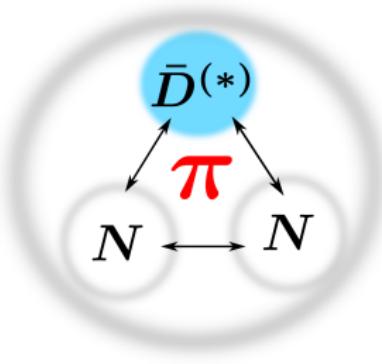
## ① Introduction

- Heavy Quark Spin Symmetry
- $\pi$  exchange potential between heavy meson and nucleon.

## ② Results of $\bar{D}^{(*)} NN$ and $B^{(*)} NN$

## ③ Results of $P^{(*)} NN$ in $m_Q \rightarrow \infty$

## ④ Summary



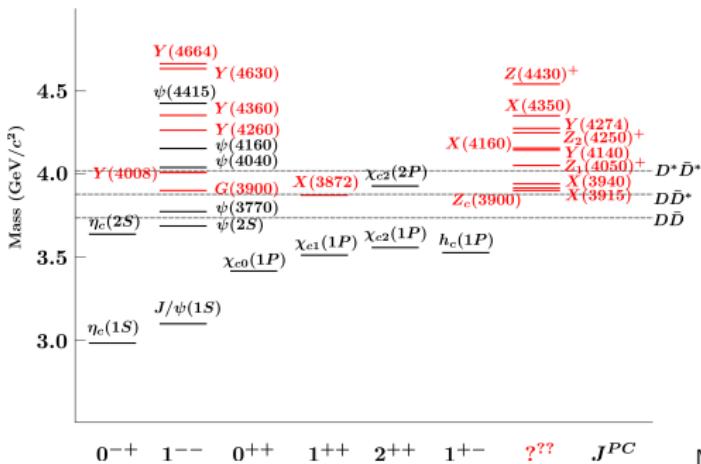
3-body system

# Exotic hadrons in the heavy quark region

## Introduction

- New particles ( $XZY$ ) with heavy quarks: Belle, BaBar...
- These states cannot be explained by **a simple quark model** (Baryons  $qqq$ , Meson  $q\bar{q}$ ). → Exotic hadrons

In charm sector,



Charmonium  $c\bar{c}$   
and  
**Exotic hadrons**

Fig.: Charmonium spectroscopy.

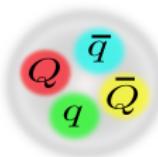
N. Brambilla, et al. Eur.Phys.J.C 71(2011)1534  
S. Godfrey and N. Isgur, PRD 32(1985)189

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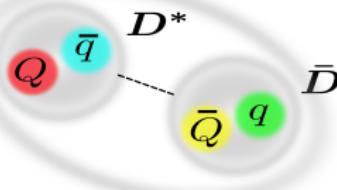
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### Structures of exotic hadrons. (Meson)



Tetraquark  
(Compact)



Hadronic molecule



$Q\bar{Q}g$  hybrid

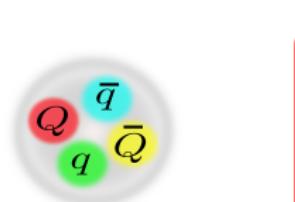
$Q$ : Heavy quark ( $c, b$ )    $q$ : Light quark ( $u, d$ )

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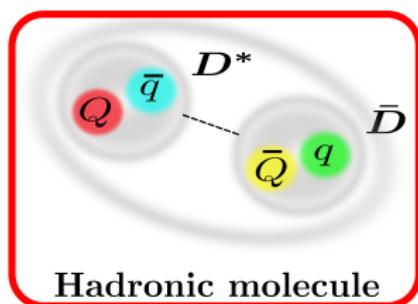
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$Q$ : Heavy quark ( $c, b$ )    $q$ : Light quark ( $u, d$ )

- Hadron molecules: Loosely bound state or resonance of two hadrons. Candidates?  $X(3872)$ ,  $Z_b$ ...

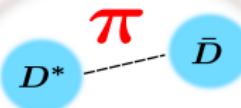
S.K.Choi *et al.*, PRL91 (2003) 262001, A.Bondar, *et al.*, PRL108(2012)122001

# Hadronic molecule and $\pi$ exchange potential

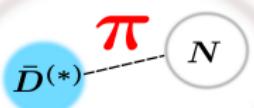
## Introduction

### Hadronic molecules

Meson-Meson



Meson-Baryon



- Driving force to form molecules:  **$\pi$  exchange potential ?**
- In the heavy quark region,

# Hadronic molecule and $\pi$ exchange potential

## Introduction

### Hadronic molecules

Meson-Meson

Meson-Baryon



### Heavy Quark Spin Symmetry

- Driving force to form molecules:  **$\pi$  exchange potential ?**
- In the heavy quark region,  $\pi$  exchange potential is enhanced by **the Heavy Quark Spin Symmetry**.
- Meson-Meson molecules: The importance of **the tensor force** in “Deuson” N. A. Törnqvist, Z. Phys. C **61** (1994) 525
- $\bar{D}N$  and  $BN$  ( $\bar{Q}qqqq$ ) → **Genuinely Exotics!**

T. D. Cohen, et al., PRD**72**(2005)074010, S. Yasui and K. Sudoh, PRD**80**(2009)034008

Y.Y., S.Ohkoda, S.Yasui and A.Hosaka, PRD**84**(2011)014032 and PRD**85**(2012)054003

⇒ **KN ( $\bar{s}qqqq$ ) doesn't exist due to a repulsive force.**

# Heavy Quark Spin Symmetry and Heavy meson

## Introduction

### Heavy Quark Spin Symmetry

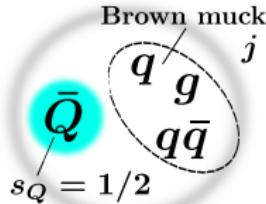
N.Isgur, M.B.Wise, PRL **66**, 1130

- In the heavy quark limit ( $m_Q \rightarrow \infty$ ),

$$\vec{J} = \vec{s}_Q + \vec{j}$$

$s_Q$ : Heavy quark spin,  $j$ : the total angular momentum of the **brown muck**

(**Brown muck**: Everything other than the heavy quark in the hadron)



▷  $s_Q = 1/2$  and  $j$  are decoupled

⇒ **Degenerate states**  $\left\{ \begin{array}{l} (j + 1/2)^P \\ (j - 1/2)^P \end{array} \right. \quad (j \neq 0)$

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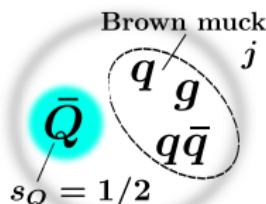
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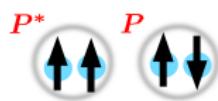
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$\triangleright s_Q = 1/2$  and  $j$  are decoupled

$\Rightarrow$  **Degenerate states**  $\left\{ \begin{array}{l} (j+1/2)^P \\ (j-1/2)^P \end{array} \right.$  ( $j \neq 0$ )

↓ Heavy meson



$\left\{ \begin{array}{l} \text{Heavy pseudoscalar meson } \mathbf{P}(0^-) \text{ and} \\ \text{Heavy vector meson } \mathbf{P}^*(1^-) \text{ are degenerate.} \end{array} \right.$

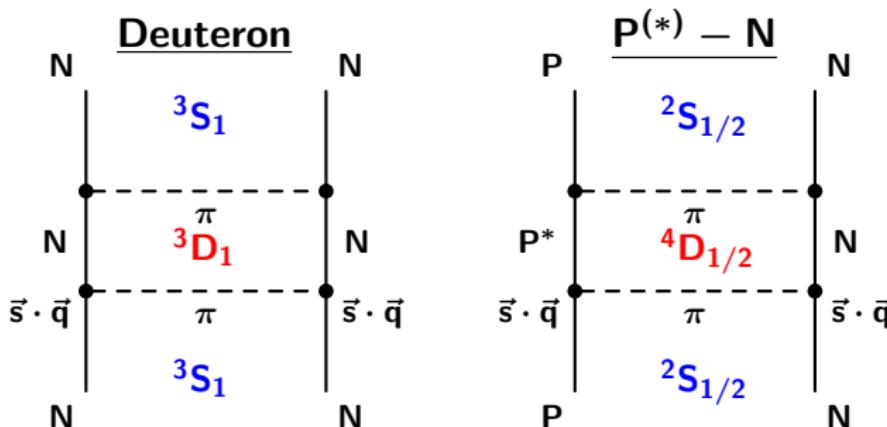
Indeed, mass splitting between  $P$  and  $P^*$  is small.

$$\left\{ \begin{array}{l} m_{B^*} - m_B \sim 45 \text{ MeV} \\ m_{D^*} - m_D \sim 140 \text{ MeV} \end{array} \right. \Leftrightarrow \left\{ \begin{array}{l} m_{K^*} - m_K \sim 400 \text{ MeV} \\ m_{\rho} - m_{\pi} \sim 600 \text{ MeV} \end{array} \right.$$

# The one pion exchange potential in $P^{(*)}N$ system.

## Introduction

- The  $\pi$  exchange potential (OPEP) appears through  $PP^*\pi$  and  $P^*P^*\pi$  vertices. ( $PP\pi$  is forbidden.)  
→ The OPEP is enhanced when  $P$  and  $P^*$  are degenerate.
- The OPEP is important in the heavy meson system.
- The OPEP(**Tensor force**) generates a **strong attraction** in Analogy with Deuteron.

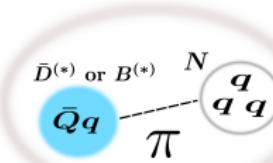


Tensor force  $\Rightarrow {}^3S_1 - {}^3D_1$

$PN({}^2S_{1/2}) - P^*N({}^4D_{1/2})$

# $P(^*)N$ molecule (2-body system)

(previous works)



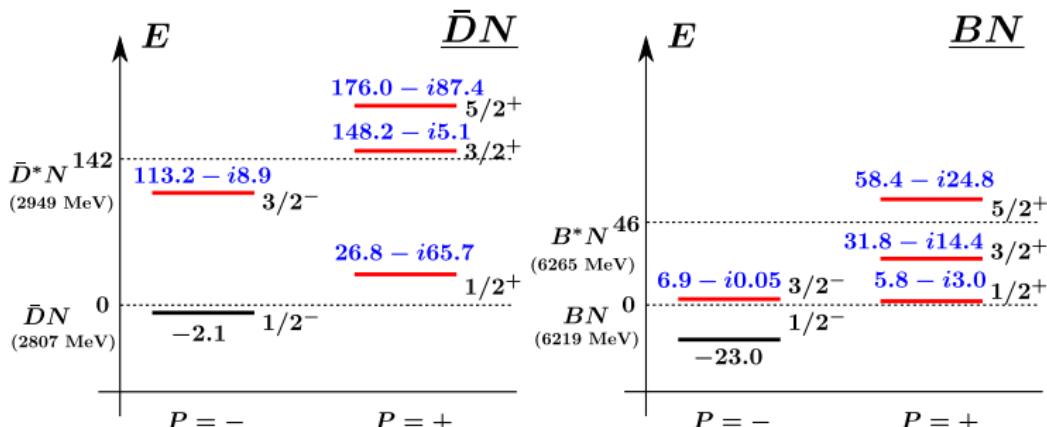
▷ Bound and resonant states were obtained.

S. Yasui and K. Sudoh, PRD **80**(2009)034008

Y.Y., S.Ohkoda, S.Yasui and A.Hosaka, PRD **84**(2011)014032, PRD **85**(2012)054003

Exotic baryons!

▷ The tensor force of OPEP plays an important role.



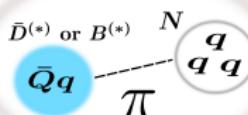
— : Bound state

— : Resonance ( $E_{re} - i\Gamma/2$ ) Unit: MeV

Y.Y., S.Ohkoda, S.Yasui and A.Hosaka, PRD **84** 014032 (2011) and PRD **85** 054003 (2012)

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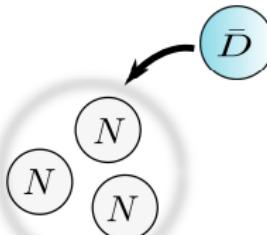
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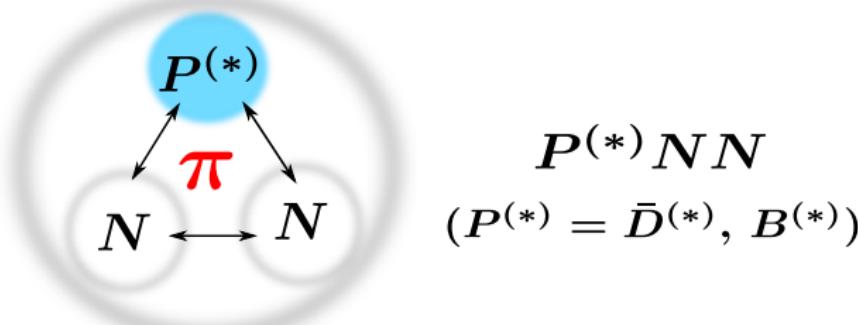
# $P^{(*)}$ nuclei (Few body or many body)?



- $P^{(*)}$  nuclei ( $P^{(*)} = \bar{D}^{(*)}, B^{(*)}$ ) → Exotics!
  - Impurity effects e.g. glue-like effect.
  - Heavy meson-nucleon interaction.
- several works for  $\bar{D}(B)$  meson in nuclear matter and in  $^{12}\text{C}$ ,  $^{208}\text{Pb}$ ...  
e.g. C. Garcia-Recio, et al., PRC**85** (2012)025203.  
S. Yasui and K. Sudoh, PRC**87**(2013)015202.
- However, there is **no study for few-body  $\bar{D}(B)$  nuclei** in the literature so far.

## Main Subject

- Exotic dibaryons with a heavy antiquark,  $\bar{D}^{(*)}NN$  and  $B^{(*)}NN$  (3-body system).



- $P = \bar{D}(\bar{c}q), B(\bar{b}q) \rightarrow \text{Genuinely exotic states!}$   
 $\Leftrightarrow \text{KNN doesn't exist.}$  ( $KN$  interaction is repulsive force.)
- We study **bound and resonant states** by solving the coupled-channel Schrödinger equations for **PNN and  $P^*NN$  channels**.
- We employ only OPEP.  $(\rho, \omega \dots \rightarrow \text{Future Work})$

# Lagrangian( $P^{(*)} - N$ ) and Form factor

## ▷ Lagrangian

### • Heavy-light chiral Lagrangian

R.Casalbuoni *et al.* PhysRept.281(1997)145

$$\mathcal{L}_{\pi HH} = ig_\pi \text{Tr} [H_b \gamma_\mu \gamma_5 A_{ba}^\mu \bar{H}_a], \quad g_\pi = 0.59 \text{ for } \bar{D} \text{ and } B$$

From  $D^* \rightarrow D\pi$  decay

$$H_a = \frac{1+\not{v}}{2} [\mathbf{P}_a^* \gamma^\mu - \mathbf{P}_a \gamma^5], \quad \bar{H}_a = \gamma^0 H_a \gamma^0$$

vector    pseudoscalar

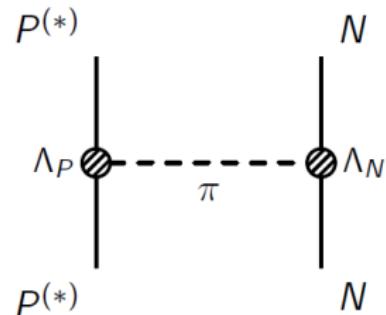
### • Bonn model

R.Machleidt *et al.* Phys Rept.149(1987)1

$$\mathcal{L}_{\pi NN} = ig_{\pi NN} \bar{N}_b \gamma^5 N_a \hat{\pi}_{ba}, \quad g_{\pi NN}^2 / 4\pi = 13.6$$

From NN data

## ▷ Form factor ( $P^{(*)}N$ )



# Lagrangian( $P^{(*)} - N$ ) and Form factor

## ▷ Lagrangian

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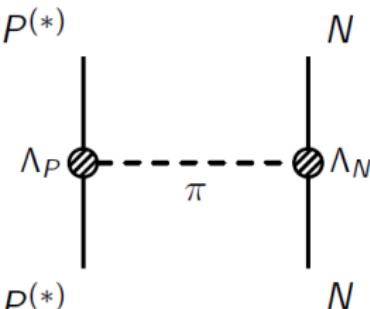
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## ▷ Form factor ( $P^{(*)}N$ )

$$F(\vec{q}) = \frac{\Lambda_N^2 - m_\pi^2}{\Lambda_N^2 + |\vec{q}|^2} \frac{\Lambda_P^2 - m_\pi^2}{\Lambda_P^2 + |\vec{q}|^2}$$



- ①  $\Lambda_N$  is fixed to reproduce the Deuteron. ( $NN$  system)
- ②  $\Lambda_P$ ; We assume  $\Lambda_P/\Lambda_N = r_N/r_P$ .

$$\begin{cases} \Lambda_D = 1.35\Lambda_N \\ \Lambda_B = 1.29\Lambda_N \end{cases} \Rightarrow \begin{array}{l} \Lambda_N = 830 \text{ MeV} \\ \Lambda_D = 1121 \text{ MeV} \\ \Lambda_B = 1070 \text{ MeV} \end{array}$$

S.Yasui and K.Sudoh PRD80(2009)034008

# $P^{(*)}N$ ( $P^{(*)} = \bar{D}^{(*)}, B^{(*)}$ ) and NN interactions

- $\pi$  exchange potential between  $P^{(*)} (= \bar{D}^{(*)}, B^{(*)})$  and  $N$

$$V_{PN-P^*N} = -\frac{g_\pi g_{\pi NN}}{\sqrt{2}m_N f_\pi} \frac{1}{3} \left[ \vec{\varepsilon}^\dagger \cdot \vec{\sigma} C(r) + S_\varepsilon T(r) \right] \vec{\tau}_P \cdot \vec{\tau}_N$$

$$V_{P^*N-P^*N} = \frac{g_\pi g_{\pi NN}}{\sqrt{2}m_N f_\pi} \frac{1}{3} \left[ \vec{T} \cdot \vec{\sigma} C(r) + S_T T(r) \right] \vec{\tau}_P \cdot \vec{\tau}_N$$

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$C(r)$  : Central force,  $T(r)$  : Tensor force

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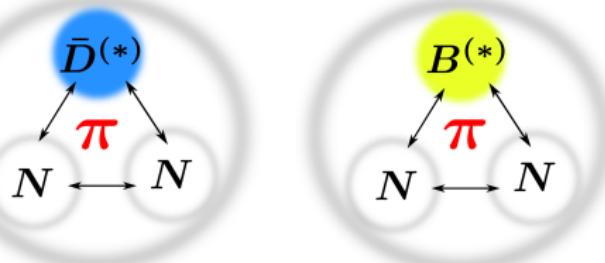
- $NN$  int.: AV8' potential B. S. Pudliner,*et.al.* ,PRC**56**(1997)1720

$$v'_8(r) = \sum_{p=1,8} v'_p(r) \mathcal{O}^p$$

$$\mathcal{O}^{p=1-8} = \begin{cases} \text{Central} & [1, \vec{\sigma}_1 \cdot \vec{\sigma}_2] \otimes [1, \vec{\tau}_1 \cdot \vec{\tau}_2] \quad (4 \text{ operators}) \\ \text{Tensor} & S_{12} \otimes [1, \vec{\tau}_1 \cdot \vec{\tau}_2] \quad (2) \\ \text{LS} & \vec{L} \cdot \vec{S} \otimes [1, \vec{\tau}_1 \cdot \vec{\tau}_2] \quad (2) \end{cases}$$

# Results of $P^{(*)}\bar{N}N$ states (3-body)

Exotic dibaryon states:  $\bar{D}^{(*)}\bar{N}N$ ,  $B^{(*)}\bar{N}N$



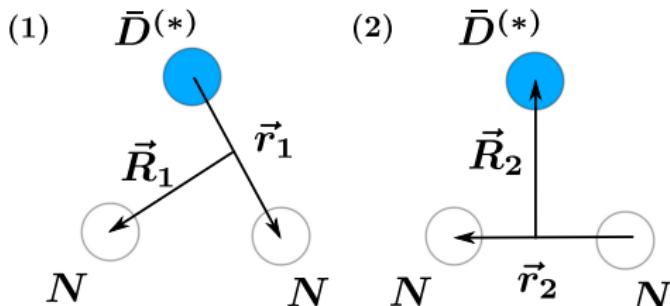
with  $J^P = 0^-, 1^-$  and  $I = 1/2$

## Bound state and Resonance

- Wave functions are expressed by the Gaussian expansion method. E. Hiyama, et al., Prog.Part.Nucl.Phys.51(2003)223
- Resonances → Complex scaling method S.Aoyama,et.al.,PTP116,1(2006)

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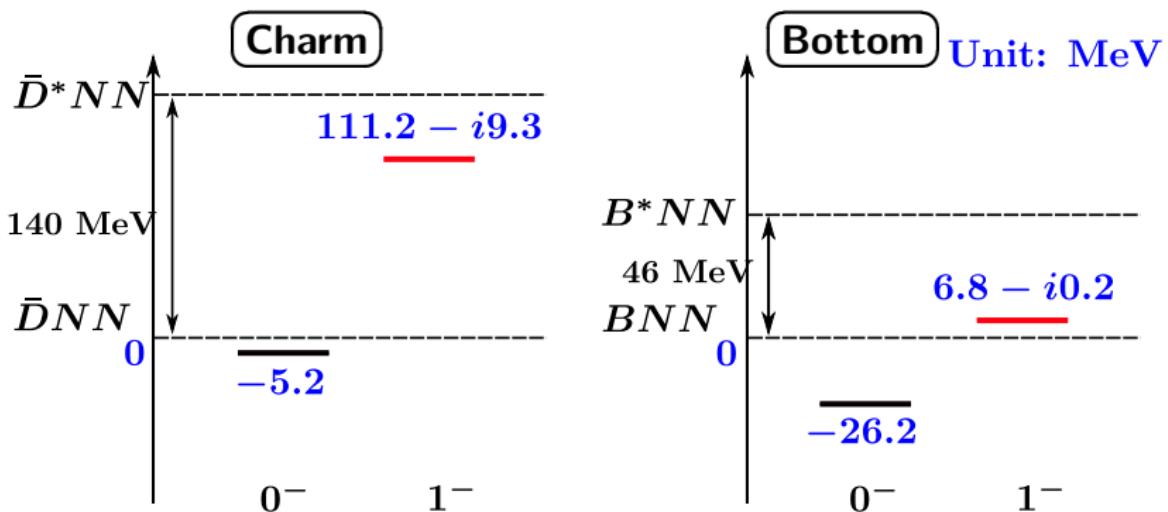


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## Results of $\bar{D}^{(*)}\bar{N}N$ and $B^{(*)}\bar{N}N$ with $I = 1/2$ (Exotic) $\bar{D}NN$ and $BNN$



YY, S. Yasui, and A. Hosaka, arXiv:1309.4324 [nucl-th]

- **Bound states** for  $J^P = 0^-$  and **Resonances** for  $J^P = 1^-$  are found!
  - $BNN > \bar{D}NN$  due to large reduced mass and small  $\Delta m_{BB^*}$ .

# Results of $\bar{D}^{(*)}\text{NN}$ and $B^{(*)}\text{NN}$ with $I = 1/2$ (Exotic) $\bar{D}\text{NN}$ and $B\text{NN}$

- Energy expectation values

The bound state of $\bar{D}NN(0^-)$			
$\bar{D}^{(*)}\text{NN}$	$\langle V_{\bar{D}N-\bar{D}^*N} \rangle$	$\langle V_{\bar{D}^*N-\bar{D}^*N} \rangle$	$\langle V_{NN} \rangle$
Central	-2.3	-0.1	-9.5
Tensor	-47.1	0.7	-0.2
LS	—	—	-0.03

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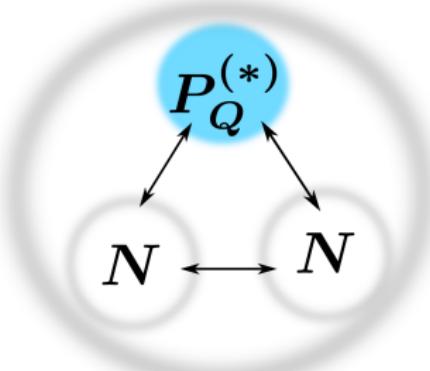
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- Tensor force of  $\bar{D}\text{N} - \bar{D}^*\text{N}$  mixing component generates the strong attraction.
- For  $V_{NN}$ , central force is stronger than tensor force.  
 $\Rightarrow NN(0^+)$  subsystem dominates in the bound state, while  $NN(1^+)$  (=Deuteron) is minor.

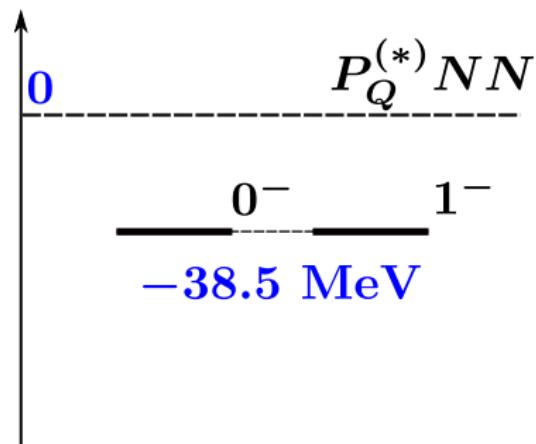
# Results of $P_Q^{(*)}$ NN states ( $m_Q \rightarrow \infty$ )



$P_Q^{(*)}$ NN ( $m_{P_Q^*} - m_{P_Q} = 0$ )

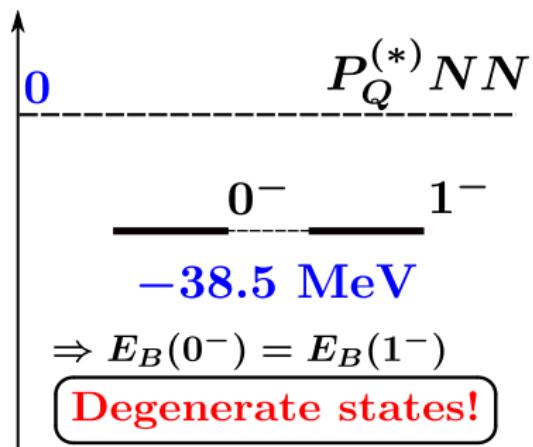
# Results of $P_Q^{(*)}NN$ in $m_Q \rightarrow \infty$ (Exotic)

- We find bound states both for  $J^P = 0^-$  and  $1^-$ !



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- $P^{(*)}NN$ : Degenerate states  $(j - 1/2, j + 1/2)^P = (0, 1)^-$   
→ Brown muck  $[qNN]^P$  has  $j^P = 1/2^+$ .
- $PNN$ :  $E(1^-) - E(0^-) = 0.0$  MeV  
 $BNN$ :  $E(1^-) - E(0^-) = 33.0$  MeV  
 $\bar{D}NN$ :  $E(1^-) - E(0^-) = 116.4$  MeV

# Summary

- We have investigated genuinely exotic dibaryons formed by  $P^{(*)}NN$ .
- The  $\pi$  exchange potential was employed between a heavy meson  $P^{(*)}$  and a nucleon  $N$ .
- For the  $\bar{D}NN$  and  $BNN$  states, we have found the bound states with  $J^P = 0^-$  and resonances with  $J^P = 1^-$  for  $I = 1/2$ .
- **Tensor force of  $\pi$  exchange** plays a crucial role to produce a strong attraction.
- The **PN – P\*N mixing** component is important to yield these states.
- In  $m_Q \rightarrow \infty$ , we have obtained the degenerate states of  $J^P = 0^-$  and  $1^-$ .

# Back up

# Central force and Tensor force

- Central force  $C(r)$  and Tensor force  $T(r)$

$$C(r) = \int \frac{d^3 q}{(2\pi)^3} \frac{m_\pi^2}{\vec{q}^2 + m_\pi^2} e^{i\vec{q}\cdot\vec{r}} F(\Lambda_P, \vec{q}) F(\Lambda_N, \vec{q})$$

$$S_T(\hat{r}) T(r) = \int \frac{d^3 q}{(2\pi)^3} \frac{-\vec{q}^2}{\vec{q}^2 + m_\pi^2} S_T(\hat{q}) e^{i\vec{q}\cdot\vec{r}} F(\Lambda_P, \vec{q}) F(\Lambda_N, \vec{q})$$

$$F(\Lambda, \vec{q}) = \frac{\Lambda^2 - m_\pi^2}{\Lambda^2 + \vec{q}^2}$$