

Simulation-based inference for precision neutrino physics through neural Monte Carlo tuning

Credits: JUNO

Arsenii Gavrikov^{1,a}

based on [Commun Phys](#) **9**, 63 (2026)

¹Tsung-Dao Lee Institute and School of Physics and Astronomy,
Shanghai Jiao Tong University

^aarsenii.gavrikov@sjtu.edu.cn



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Simulation-based inference: bypassing intractable likelihoods

- ❖ In physics (and beyond) we employ mechanistic models (that act as forward models):

- from fundamental particle interactions to cosmological evolution
- **known forward process but unknown inverse**

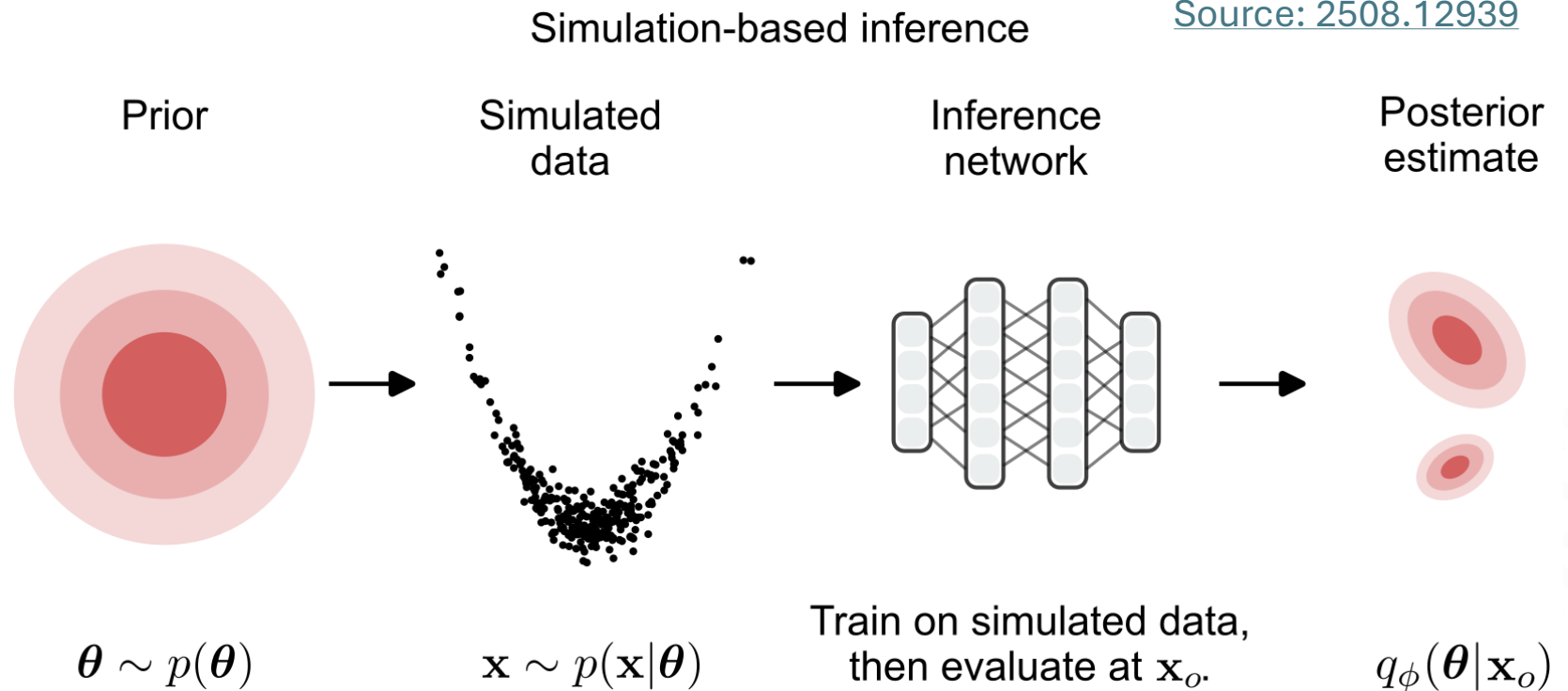
- ❖ We **rely on high-fidelity**

simulators (like Geant4 or GENIE) that encode fundamental theory to generate synthetic data: $p(\mathbf{x} | \boldsymbol{\theta})$

- ❖ $p(\mathbf{x} | \boldsymbol{\theta})$ is **not explicitly available**: the likelihood intractability problem

- ❖ To infer the parameters $\boldsymbol{\theta}$, we **have to estimate** $p(\boldsymbol{\theta} | \mathbf{x})$

- ❖ ML can help here too!



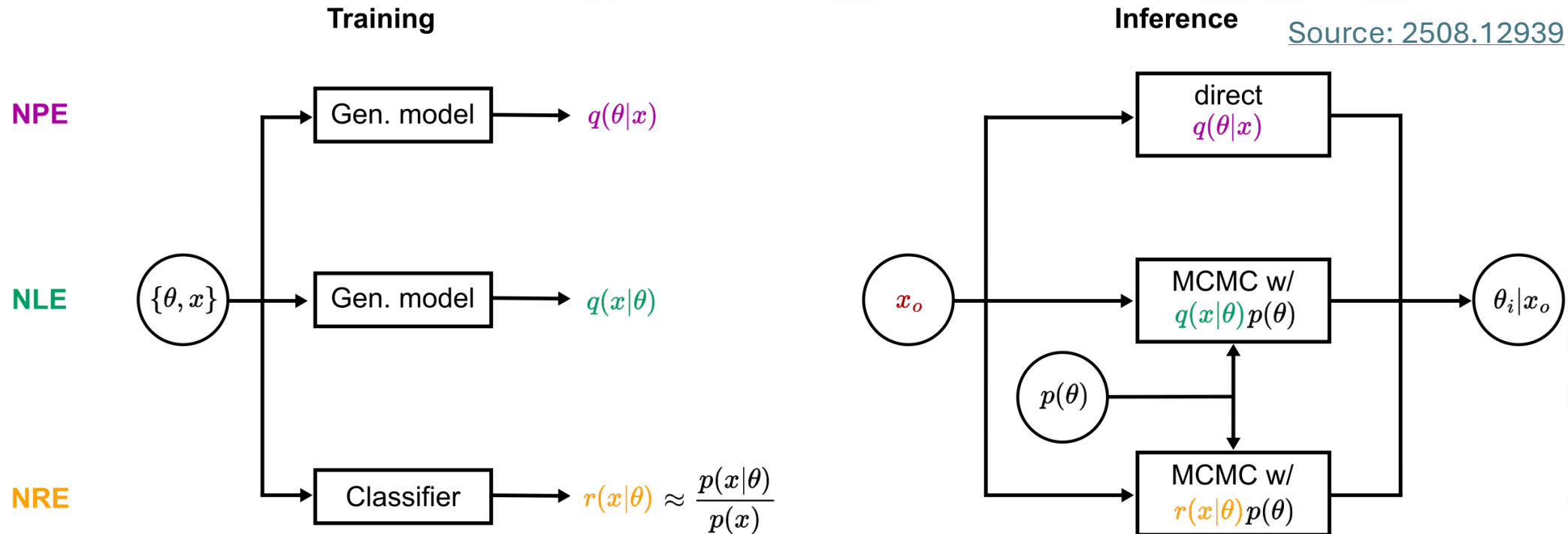
[1] [2010.06439v2](#)

[2] [PNAS 117 \(48\) 30055-30062](#)

[3] [2508.12939](#)

Simulation-based inference: bypassing intractable likelihoods

- ❖ The ML approach: learning the inference quantity from simulator outputs
- ❖ Three complementary strategies:
 - Neural Posterior Estimation (**NPE**): directly learns the **posterior** $p(\theta | x)$
 - Neural Likelihood Estimation (**NLE**): learns the **likelihood** $p(x | \theta)$, the posterior is then evaluated with e.g. MCMC
 - Neural Ratio Estimation (**NRE**): trains a binary classifier to approximate the **likelihood ratio** $r(x | \theta) = p(x|\theta)/p(x)$



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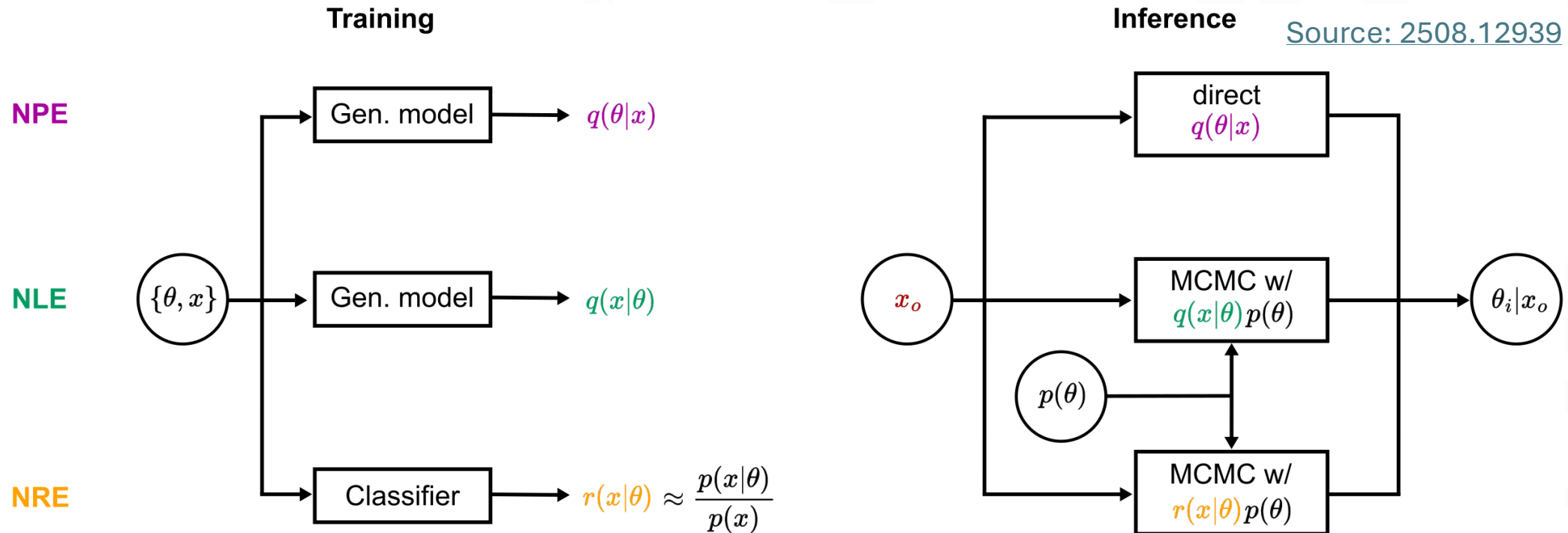
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I) Fast inference

II) Probabilistic reconstruction



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[Source: 2508.12939](#)

Criterion	NPE	NLE	NRE
Inference speed	++ (ms)	– (sec-min)	– (sec-min)
Simulation efficiency for i.i.d. data	—	++	++
Embedding network compatibility	++	—	++
Training computational cost	Medium	Medium	Low
Invalid simulation handling	++	—	—
Hyperparameter tuning complexity	Low	High	High

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The JUNO experiment

Credits: JUNO

The JUNO experiment



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Jiangmen Underground Neutrino Observatory (**JUNO**):

- **multi-purpose** neutrino experiment
- located in **China**
- largest **liquid scintillator (LS) detector** ever built



Data-taking is ongoing since August 2025 and [first physics results are already out!](#)

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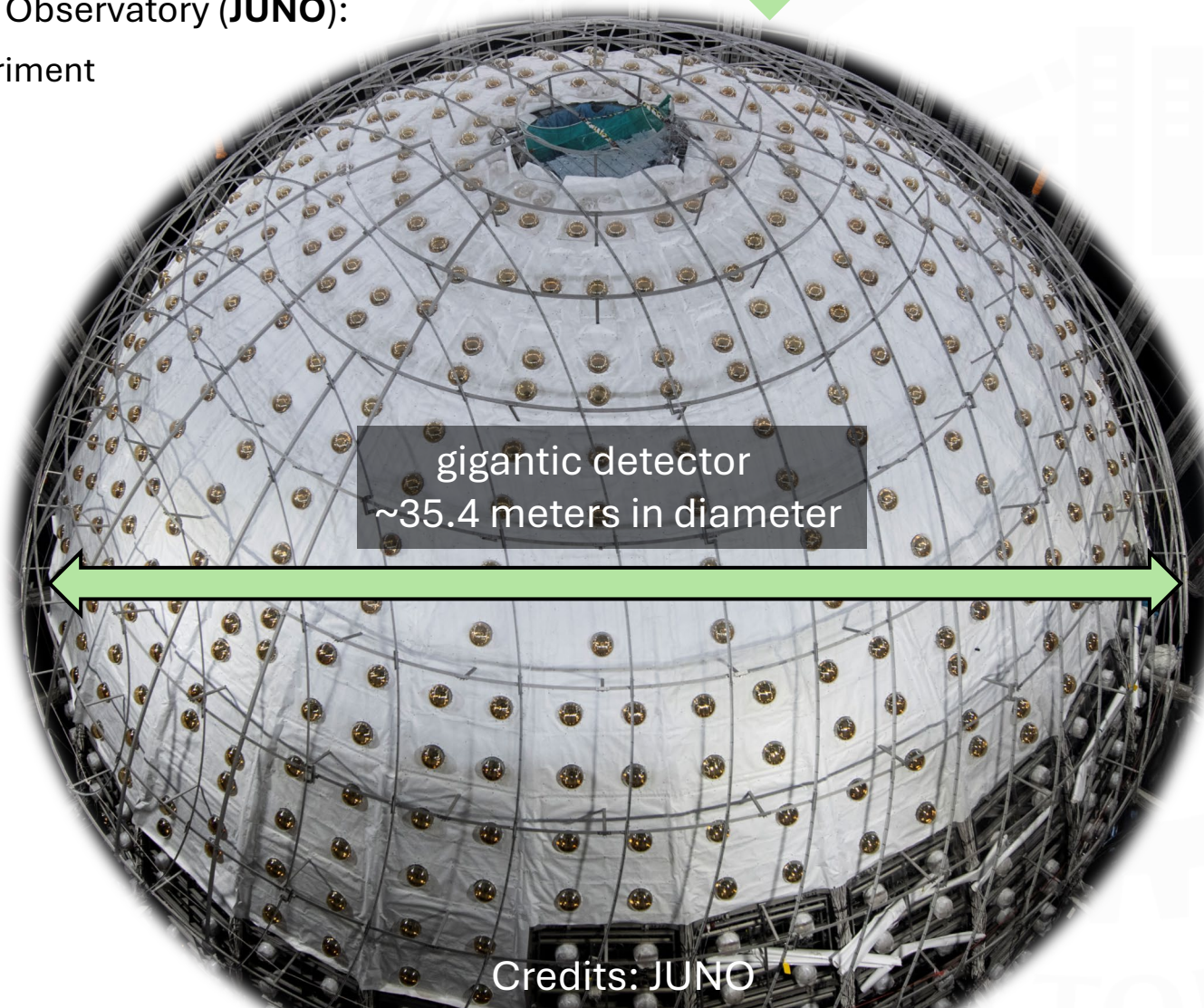


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~650 meters deep
underground

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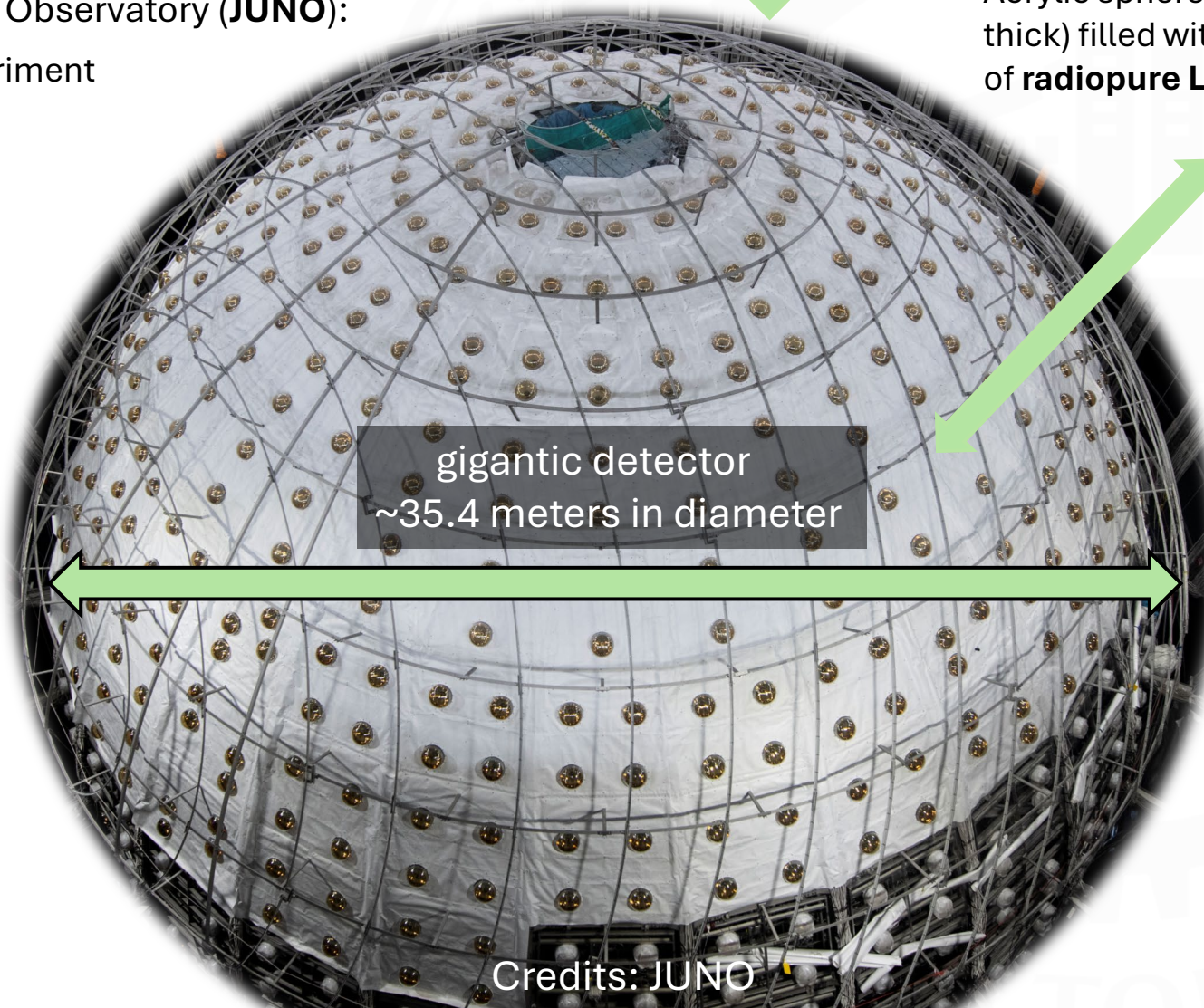
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Acrylic sphere (12 cm
thick) filled with **20 kton**
of **radiopure LS**

LS of JUNO is organic:
LAB + 2.5 g/L PPO + 3
mg/L bis-MSB



gigantic detector
~35.4 meters in diameter

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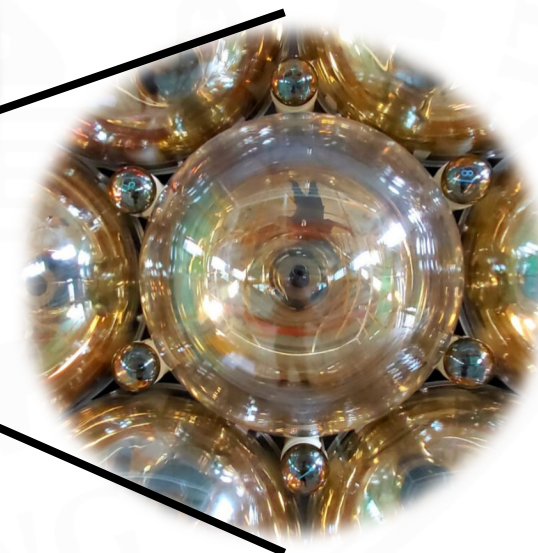
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~78% **photo-coverage** by
photo-multiplier tubes (PMTs):

- 17596 Large 20" PMTs
- 25587 small 3" PMTs

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The JUNO experiment



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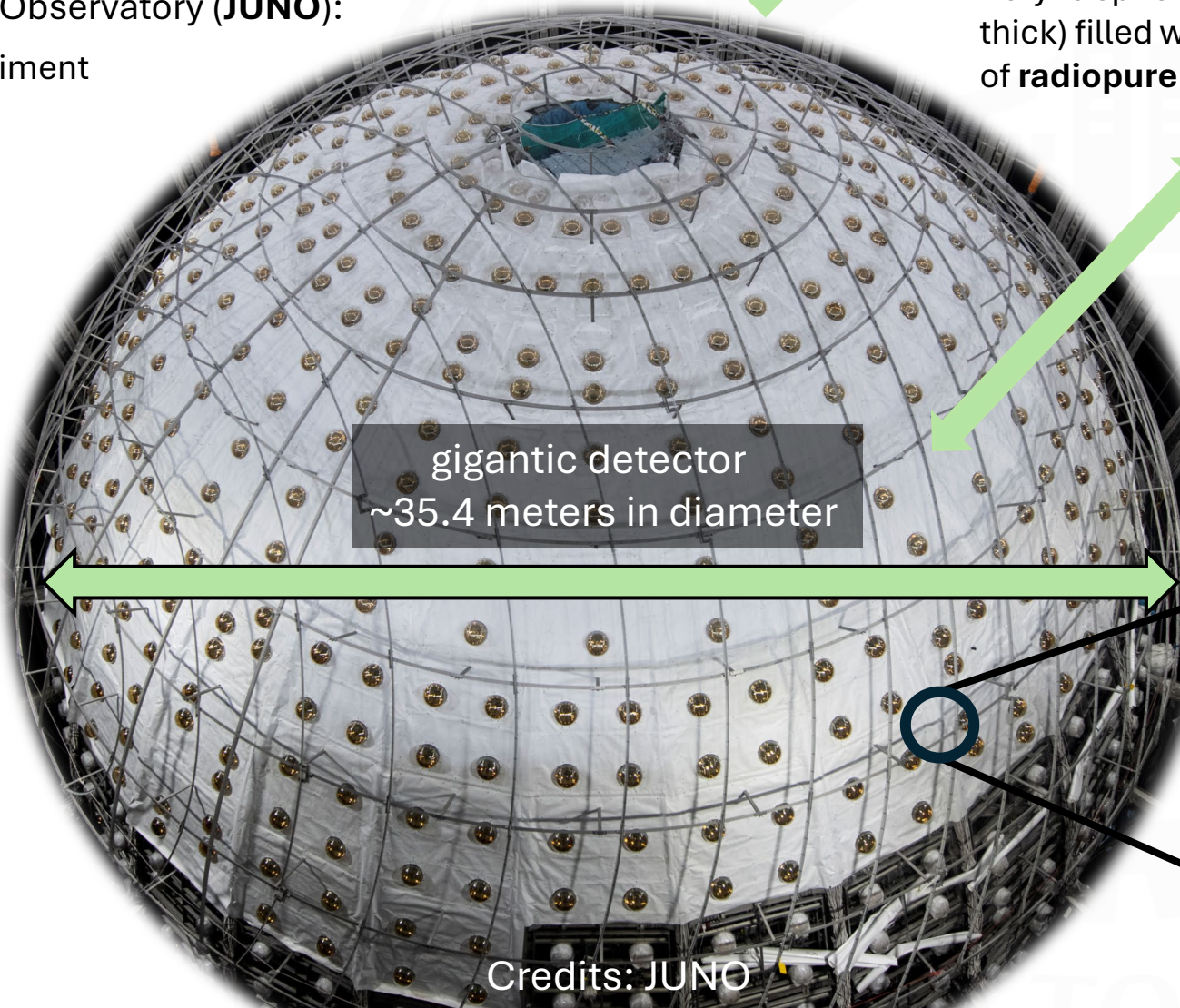
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The main goals of JUNO:

- **neutrino mass ordering** at 3σ after ~6-7 years
- sub-percent measurements of the **oscillation parameters**:
 $\Delta m_{21}^2, \Delta m_{31}^2, \sin^2 \theta_{12}$
- using reactor $\bar{\nu}_e$

Overall physics potential and program is broader

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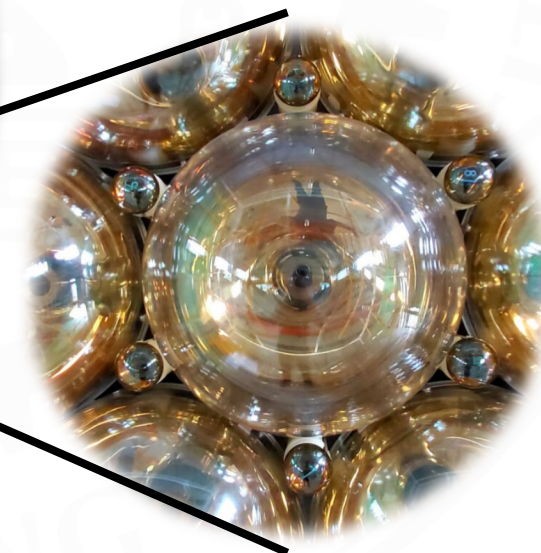
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The core challenge:

- **Energy resolution:** 3% at 1 MeV
- **<1% control over energy scale** systematic uncertainty

need for **highly accurate and well-tuned Monte Carlo (MC)** simulations

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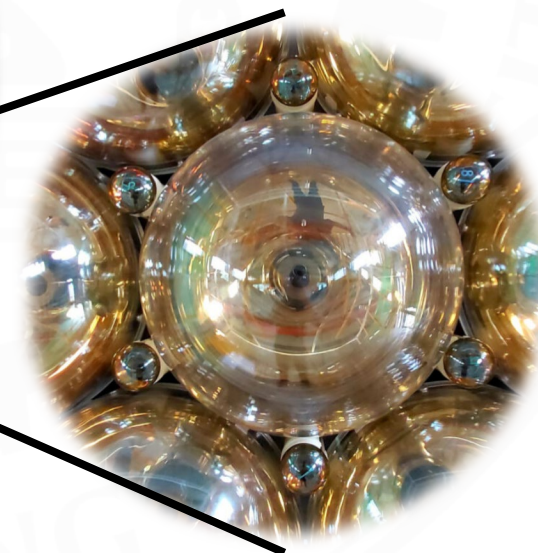
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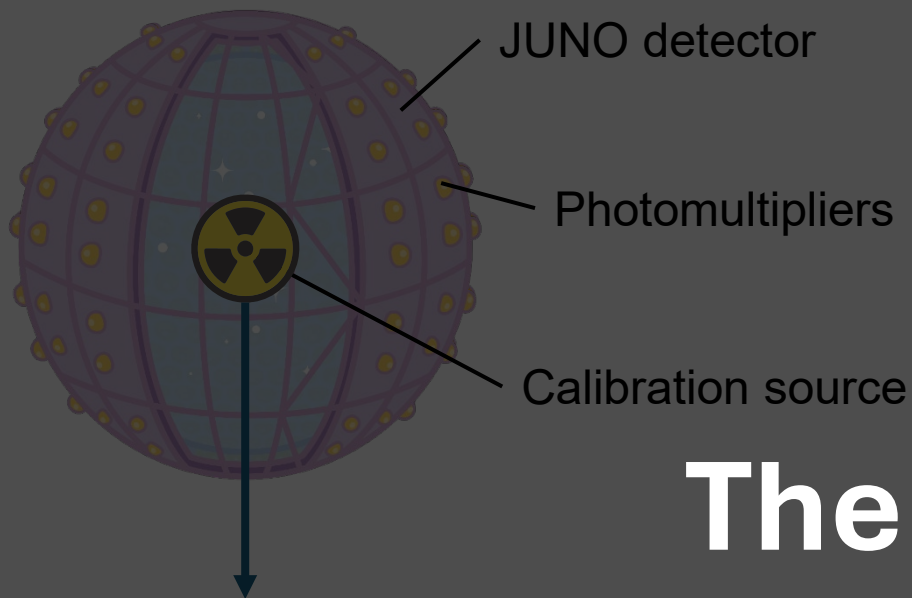
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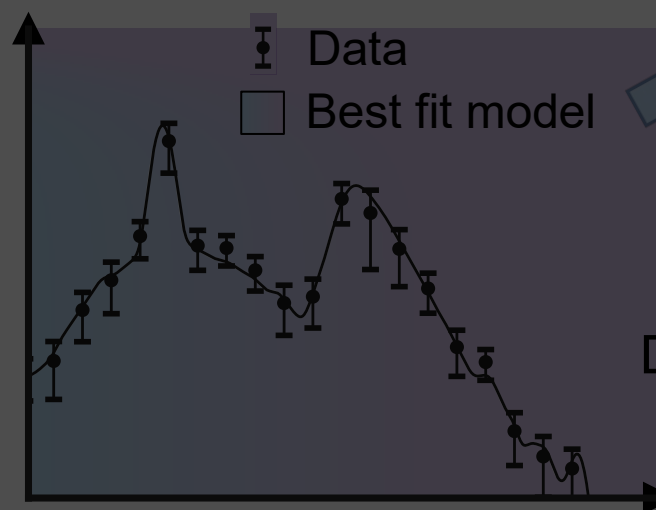


Credits: JUNO

JUNO calibration data



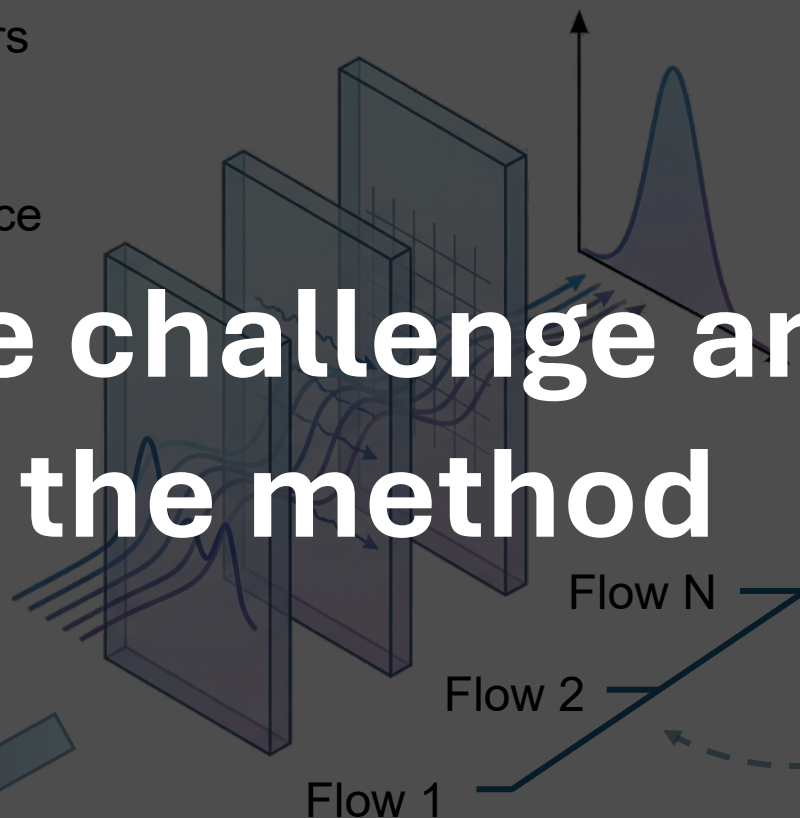
Complex energy spectrum



Data simulated by tuned Monte Carlo describing calibration data

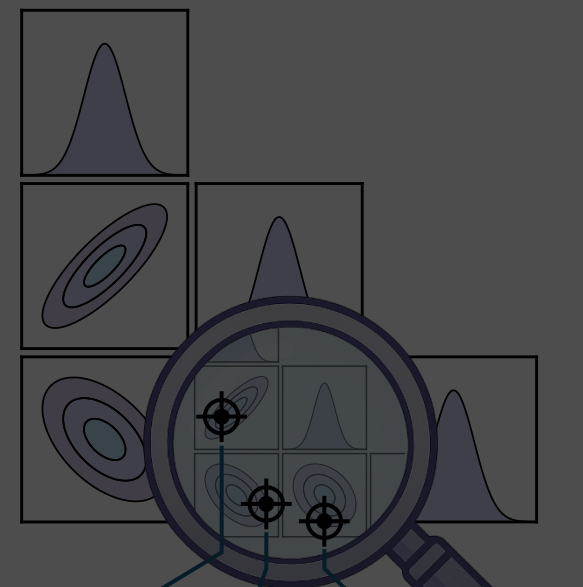
Normalizing flows

Turning the spectrum to a normal distribution



Parameter estimation

Bayesian inference with Nested Sampling



k_B Birks' constant

f_C Cherenkov factor

Y Light yield

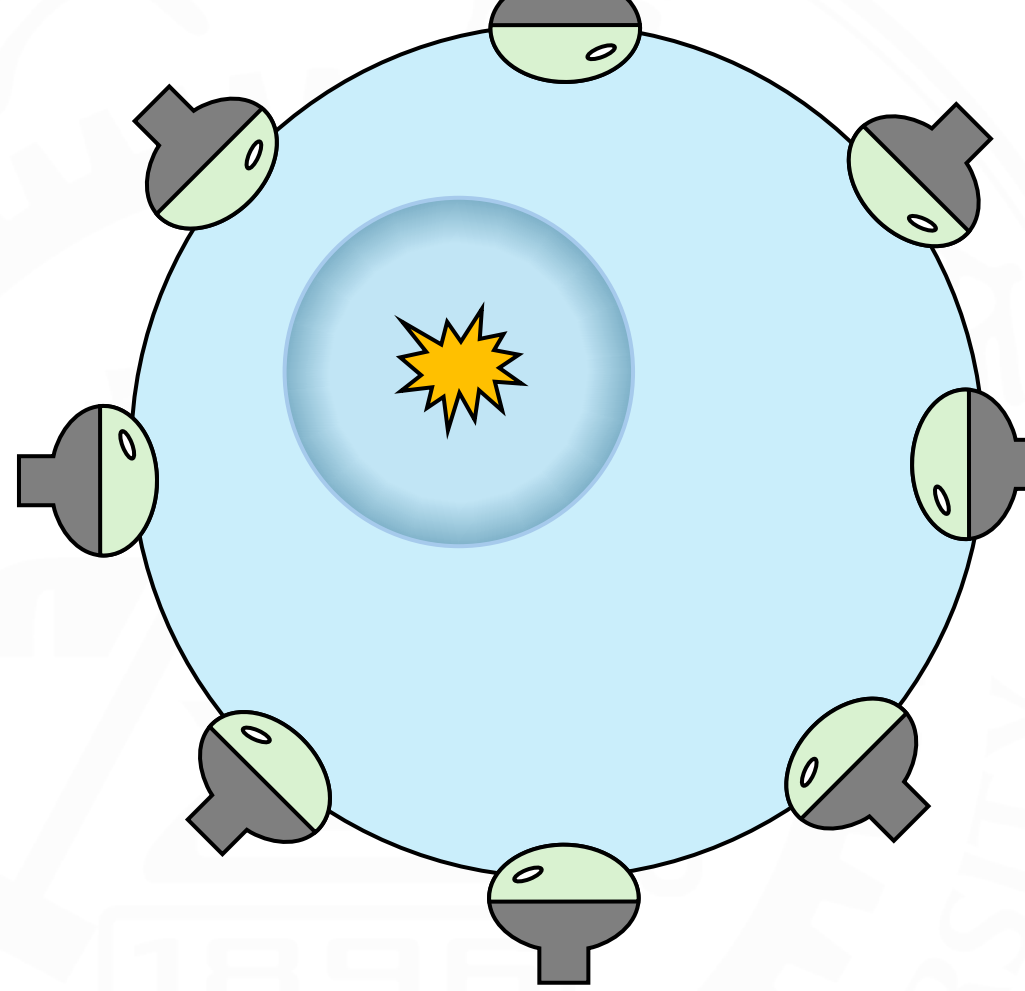
Best fit parameters

Tuned configuration better matching calibration data

Physics challenge

❖ Detection principle of JUNO:

- JUNO is a **calorimeter**: a particle deposits energy in the scintillator.
- The scintillator emits **light collected by PMTs** and measured as a total **number of photo-electrons (NPE)** → our proxy for the visible energy



Physics challenge

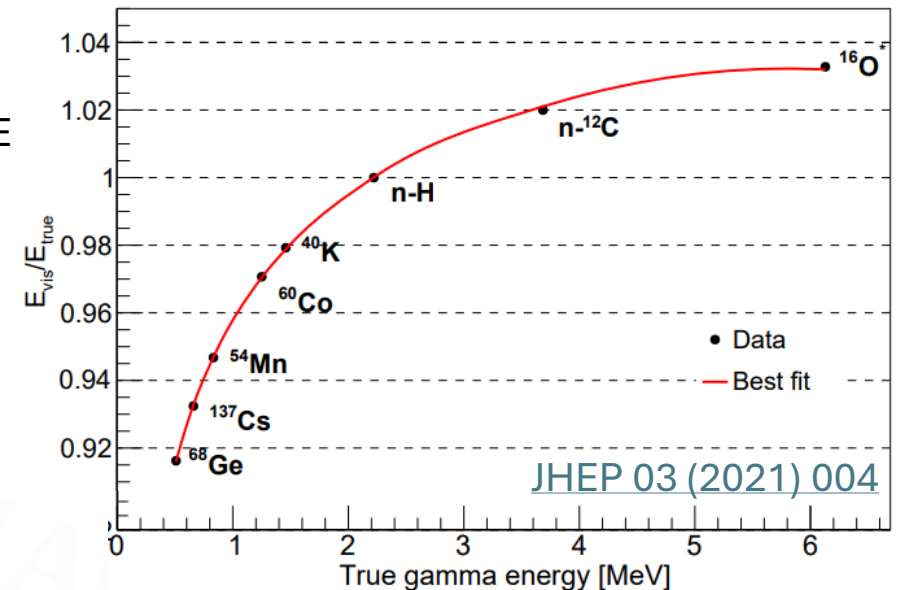
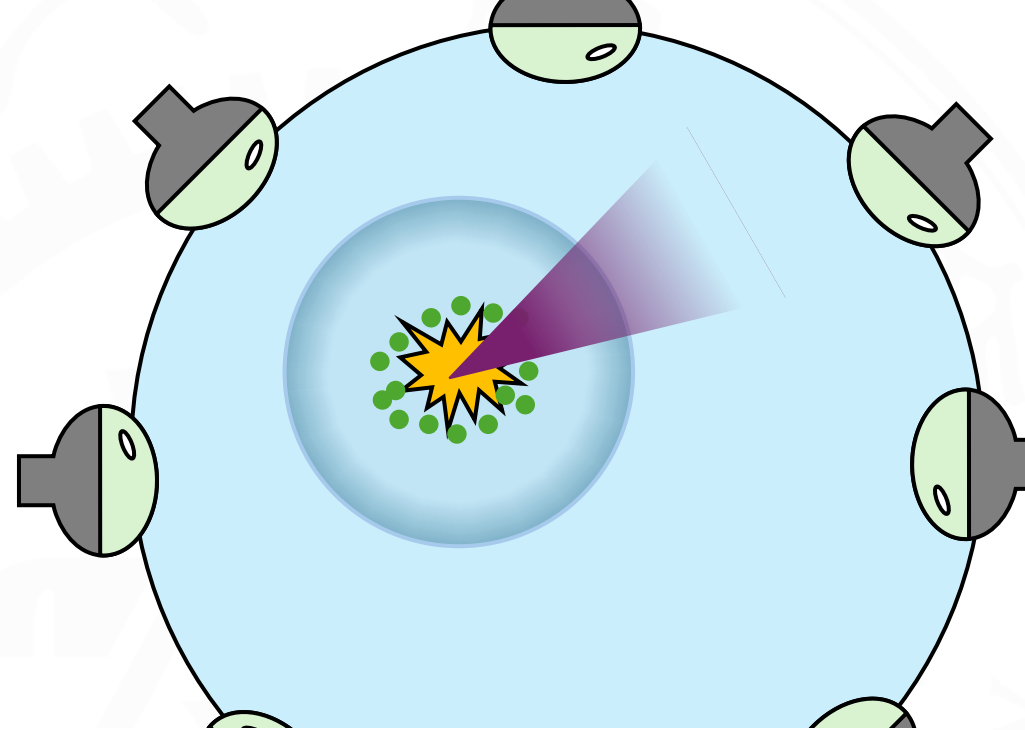
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❖ Challenge:

- The relationship between true deposited energy and NPE is **not linear**
- In simulation, we model this non-linear relationship with **3 parameters**:
 - **Birks' constant** (k_B) ↓: models quenching, which reduces visible NPE
 - **Cherenkov factor** (f_C) ↑: model the contribution of Cherenkov light
 - **Light yield** (Y) ↑: models the overall scaling factor (after quenching)

calibration sources



Physics challenge

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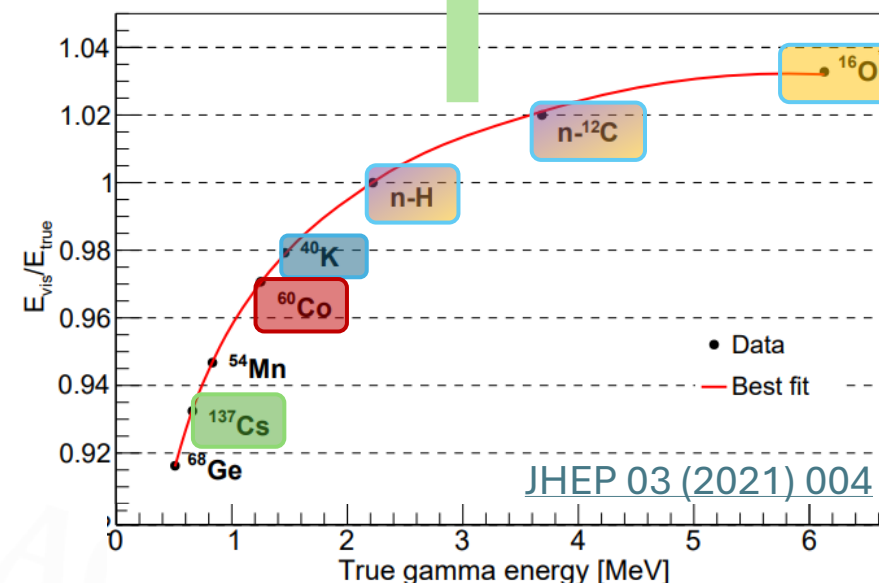
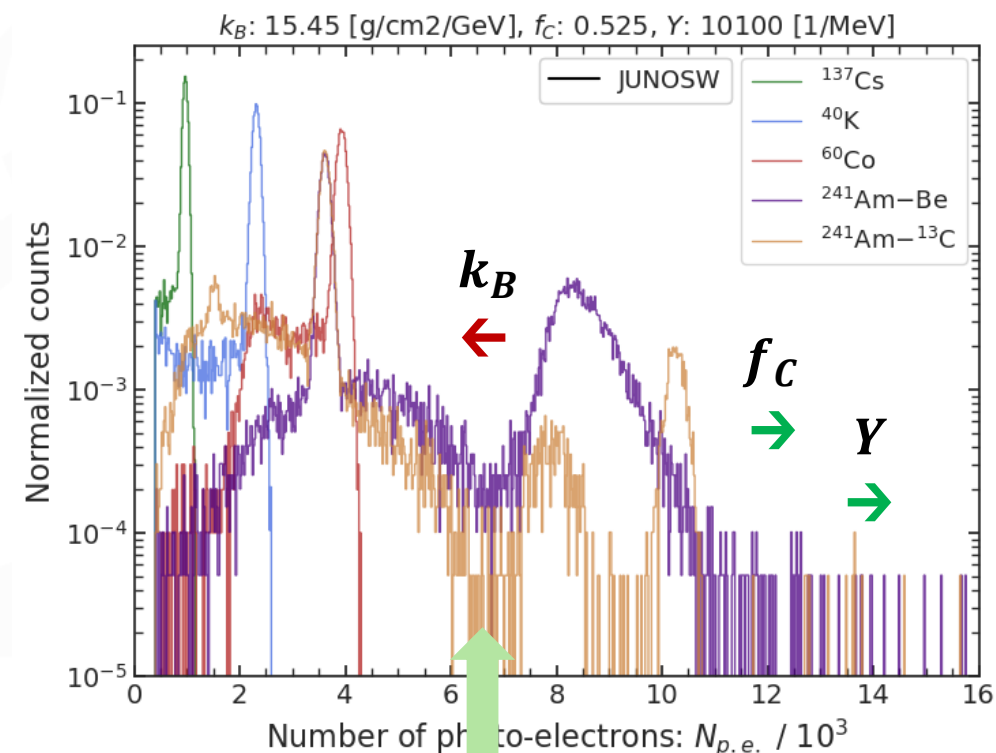
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Task: tune (k_B , f_C , Y) so that our MC matches real calibration data

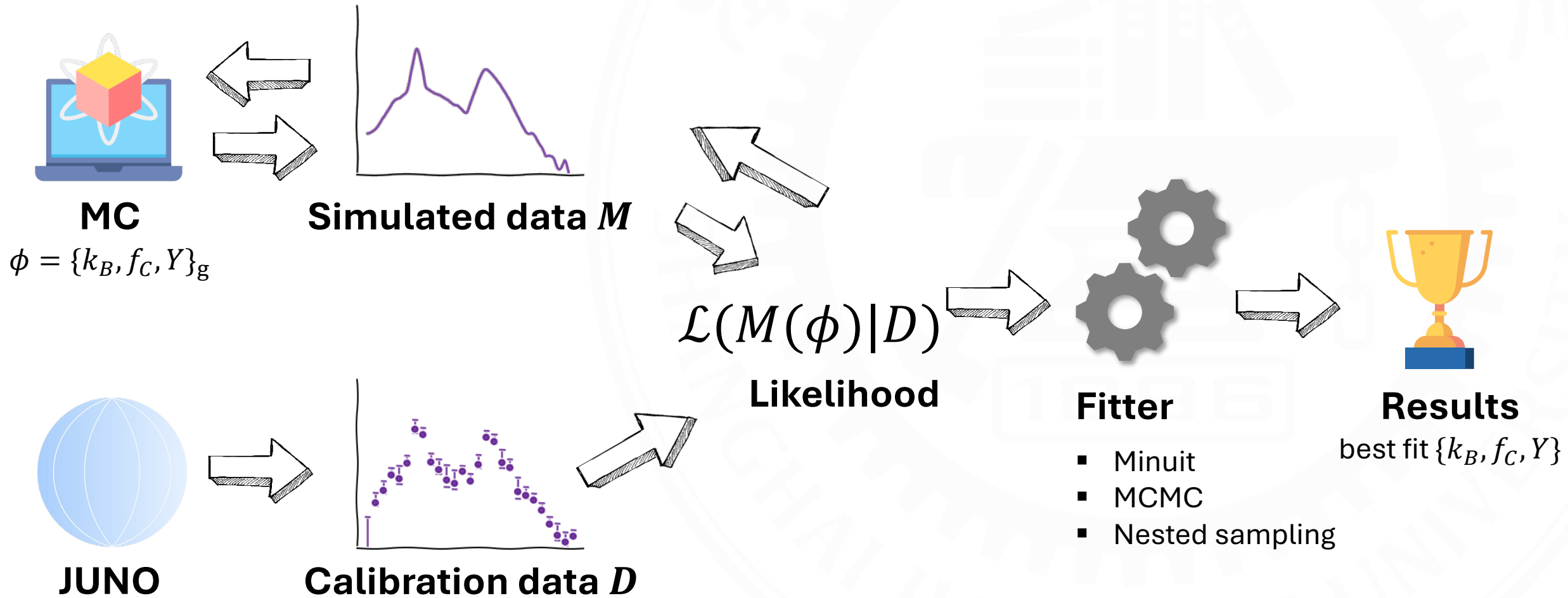
➡ **pivotal to control systematic uncertainties**



Monte Carlo tuning strategy



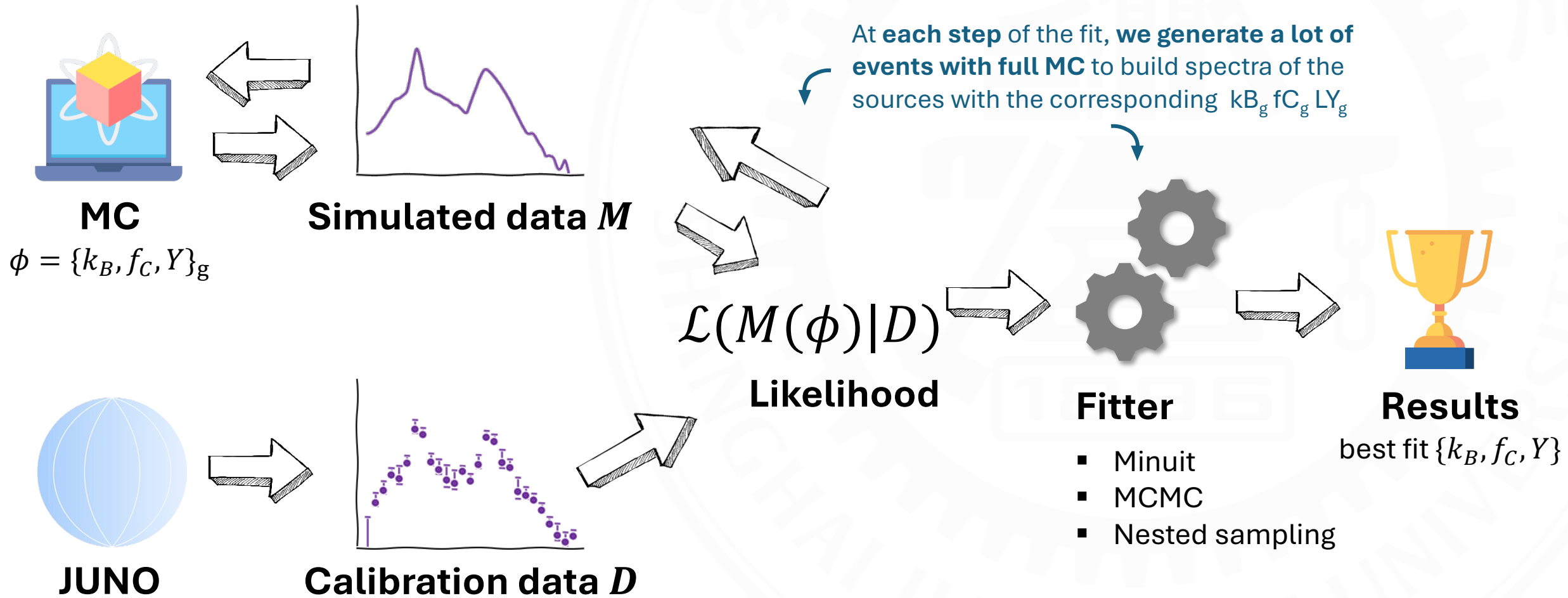
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Monte Carlo tuning strategy



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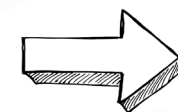


Monte Carlo tuning strategy

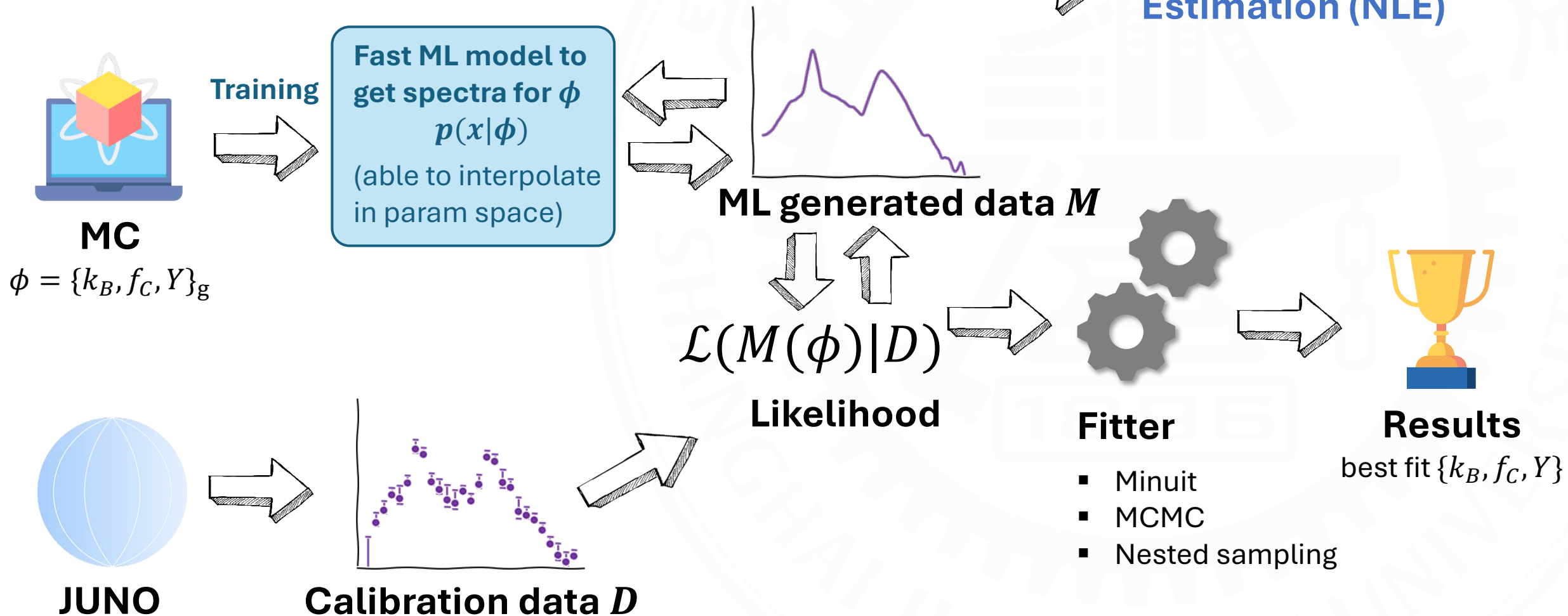


The most straightforward approach would be...

too impractical and slow! Can we replace it with a surrogate model?



Neural Likelihood
Estimation (NLE)



Two Neural Likelihood Estimators



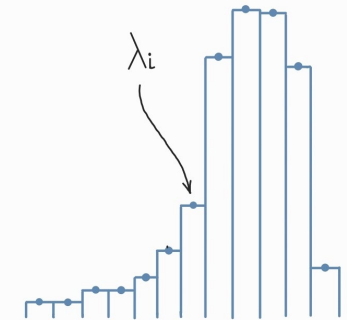
- + *straight and reliable model*
- *requires pre-defined binning*

Multi-output regressor

Aims to directly learn a **mapping** from the parameters and a source type to the histogram representing the **spectra PDF**

Provides **PDF estimation** by outputting a histogram

TEDE



Conditions:
k_B, f_C, Y + source type **S**

We use a **Transformer encoder-based** model as the density estimator (**TEDE**)

- + *exact probability density function*
- + *no pre-defined binning*
- + *opens a possibility of an unbinned fit*

Normalizing Flow-based model

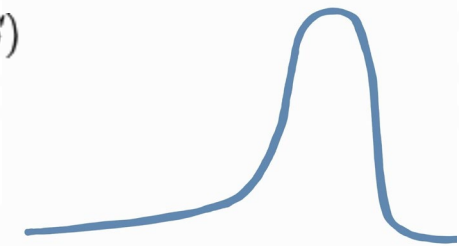
Aims to learn the exact **conditional probability** of the energies* for a given set of parameters and a source type:

$$P(E | k_B, f_C, L_Y, S)$$

Provides the **exact conditional PDF** for any energy value:

$$P(E | k_B, f_C, L_Y, S)$$

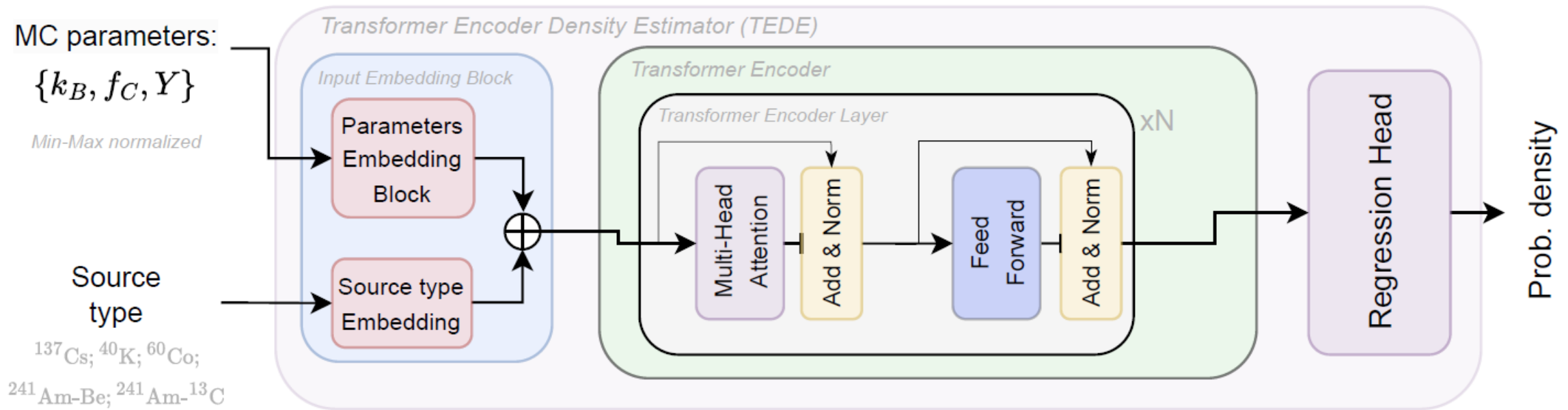
NFDE



*represented by amount of light collected

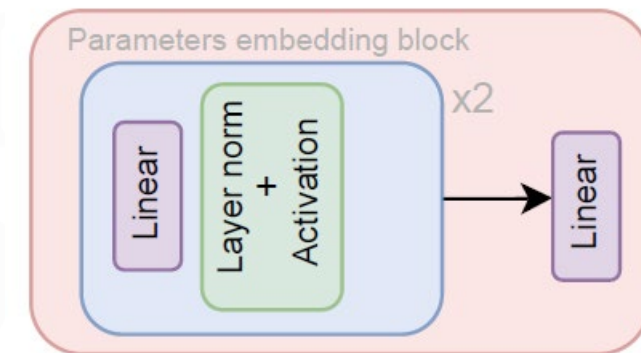
We use **Normalizing Flows**-based model (NFDE) to evaluate the exact conditional probability for the events and build the PDF

Transformer Encoder Density Estimator (TEDE)



Multi-output regressor is based on the **Transformer's encoder** :

- A powerful architecture, well known for NLP and CV applications
- Each condition (MC parameter or source type) is treated as a token
- Regressor Head block to convert outputs to the spectra PDF with pre-defined binning (**bin size of 20 PEs**)

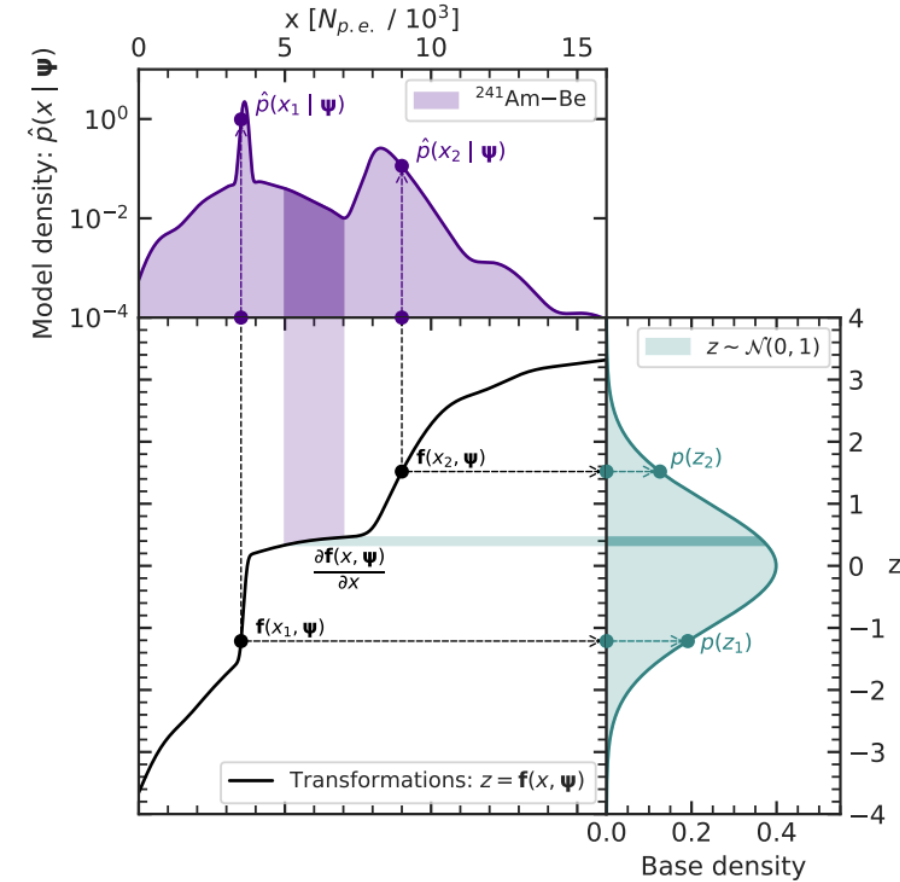
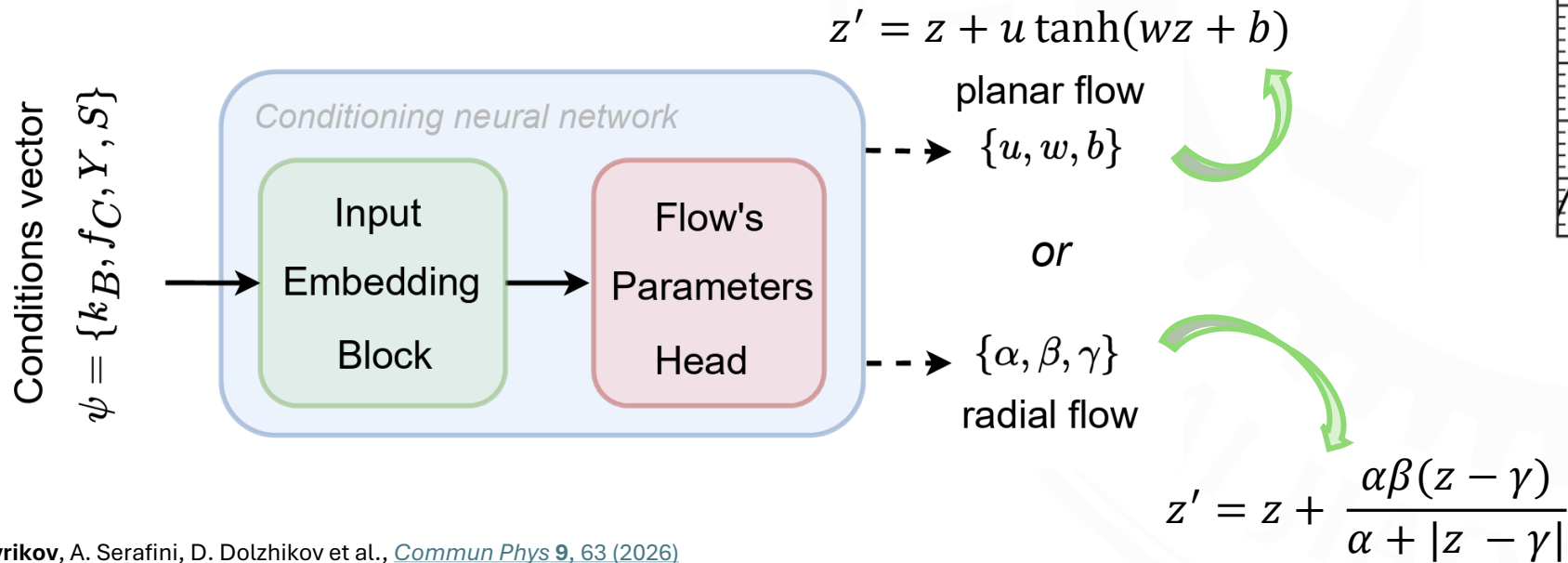


Normalizing Flows Density Estimator (NFDE)



Normalizing flows:

- **generative** ML model aimed to **explicitly model a density estimation**
- generalizable for modeling a **conditional density estimation** as well (via a dedicated **conditioning neural network**)
- based on an **idea of transforming a simple known distribution** (e.g. *standard Gaussian*) **to the complex, desired distribution** by applying multiple learnable (*using data*) and invertible transformations called **flows**.



Datasets: training/validation strategy

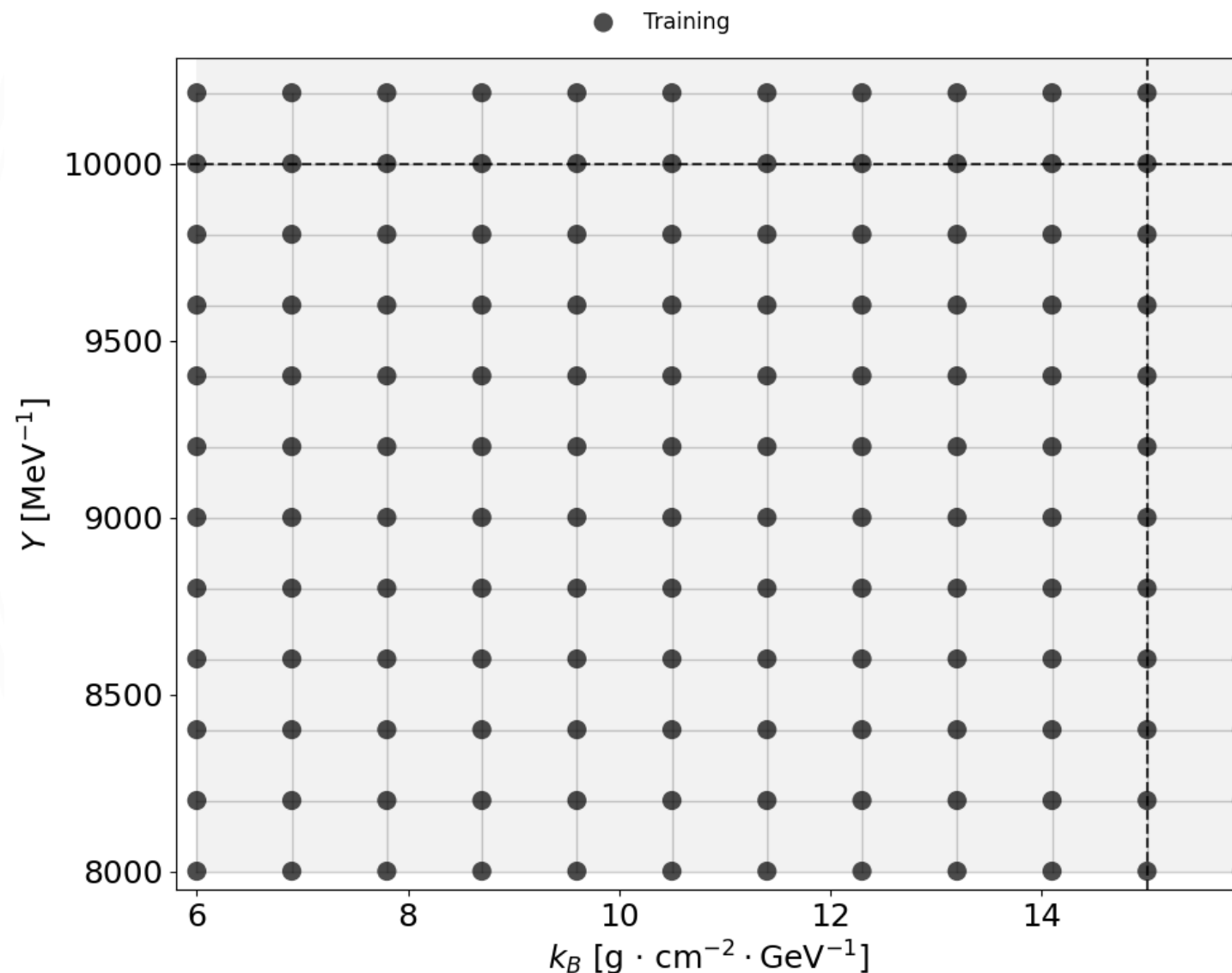


Always in the center of the detector

Y and k_B example

Training data

- 21 points per param (21^3 combs)
- 10k events x 5 sources per point (~500M events)



Datasets: training/validation strategy

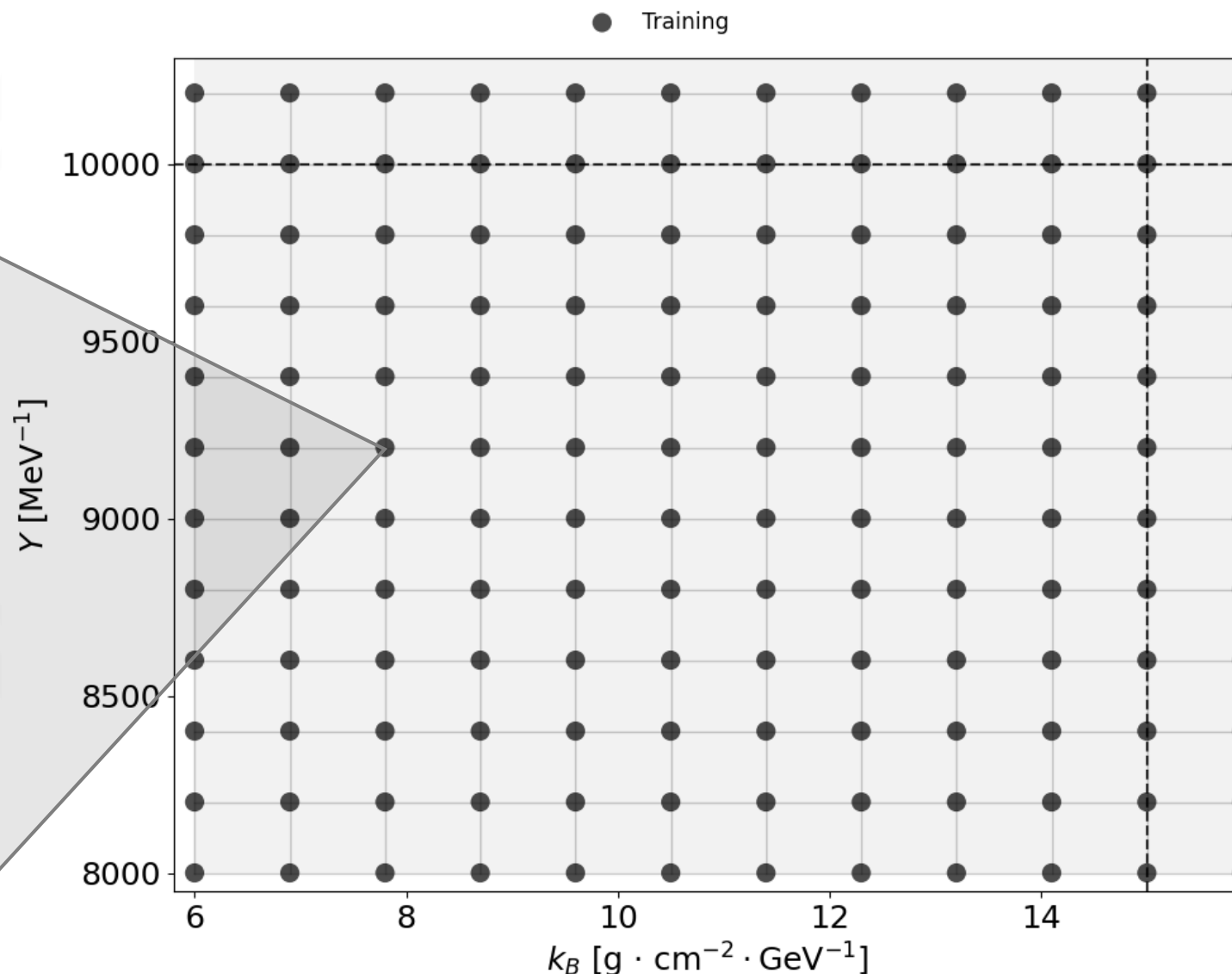
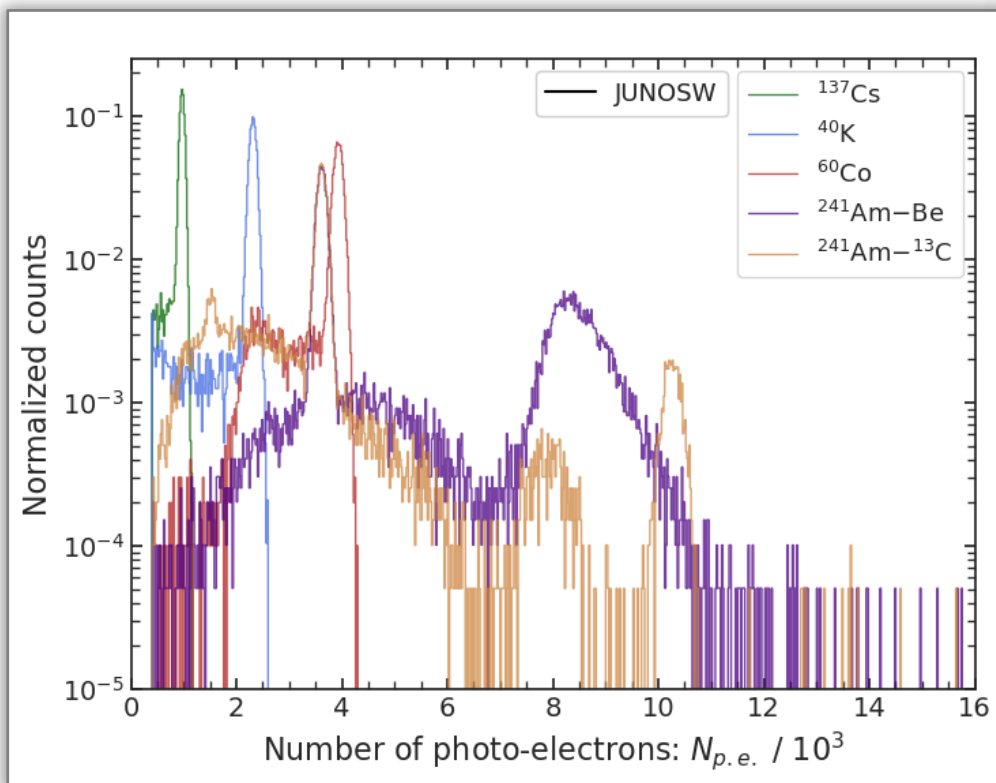


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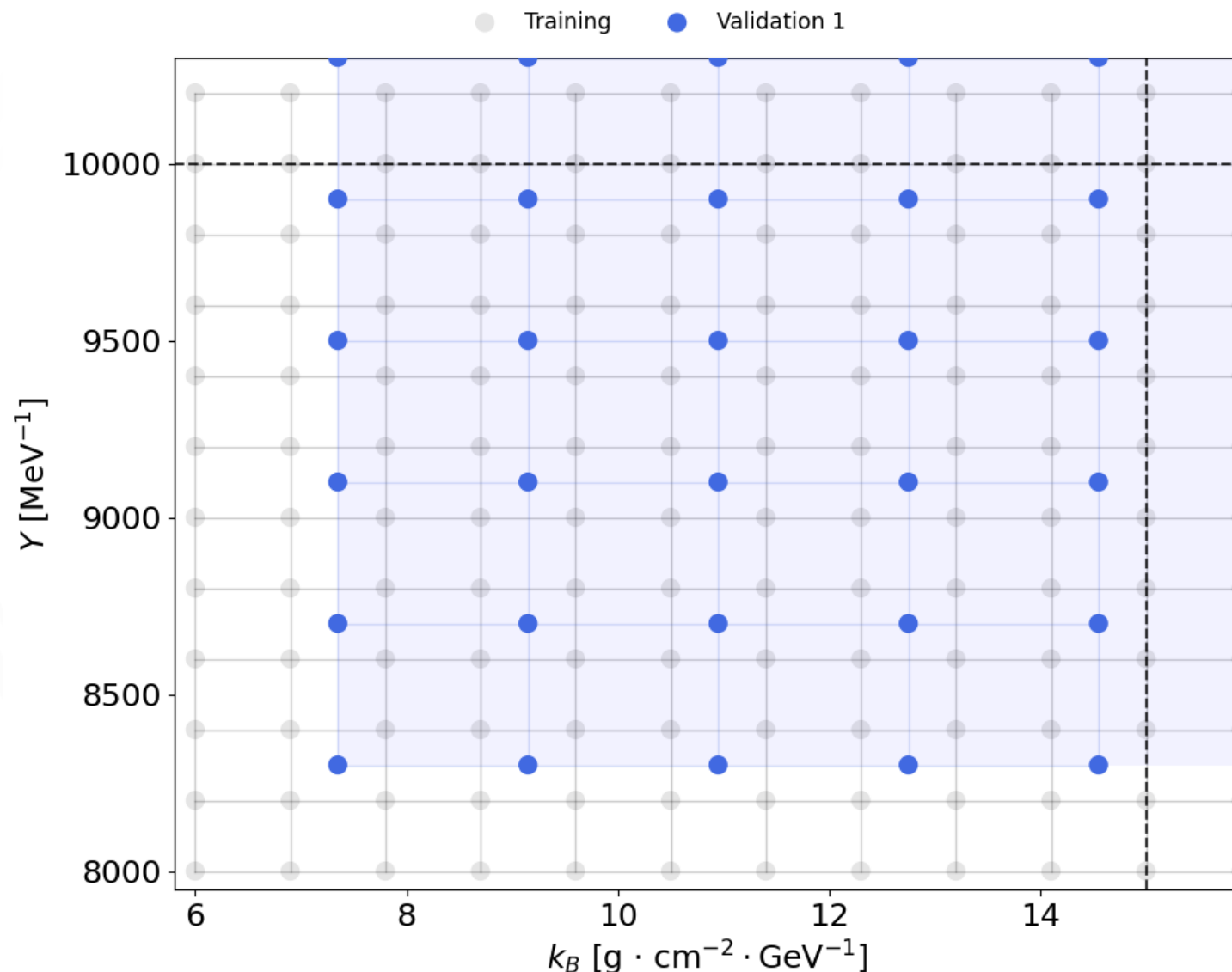
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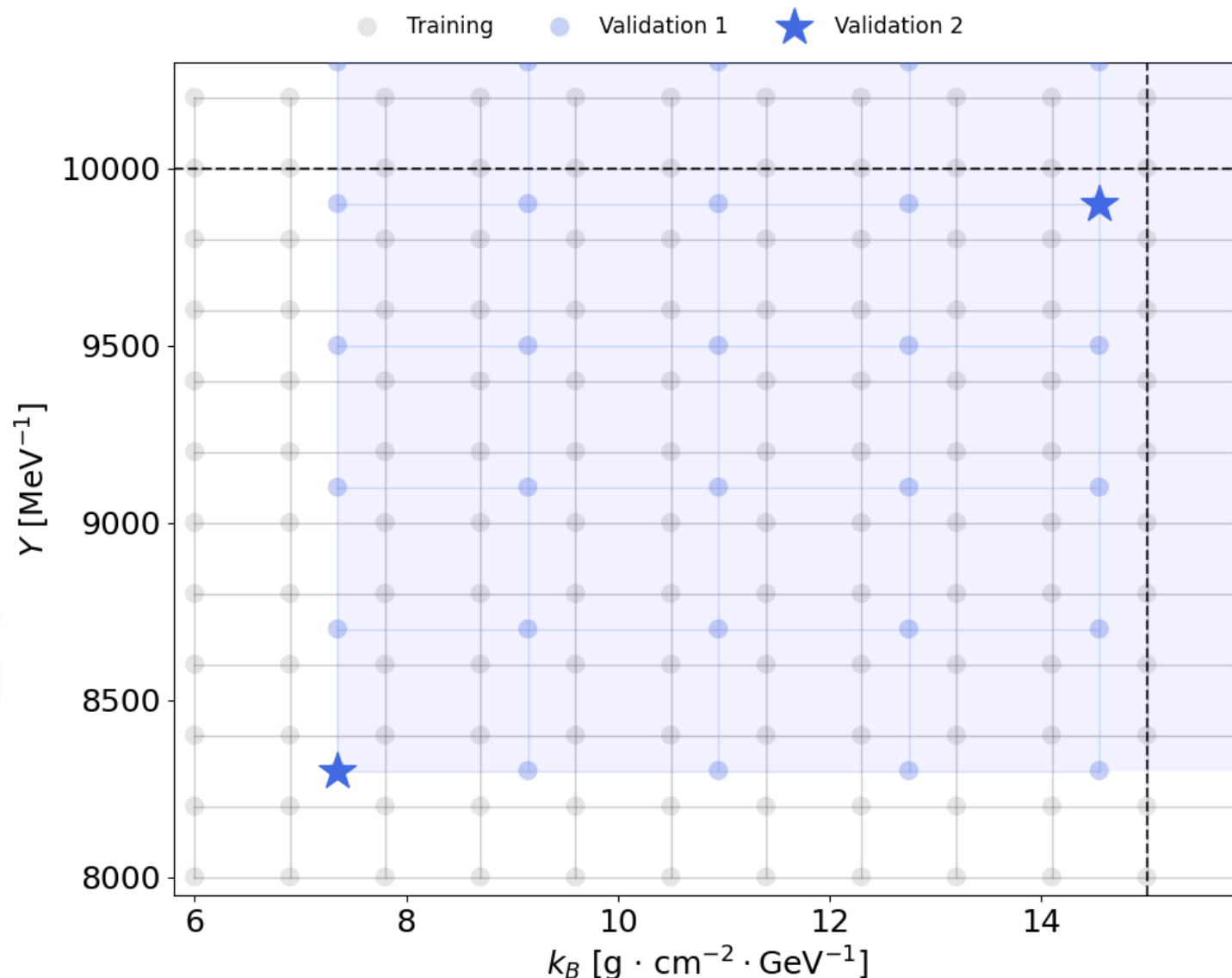
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Validation data #2

- 3 points in total
- 10M x 5 events per point (150M events)
- anchor PDF to high-stat spectra



Datasets: training/validation strategy



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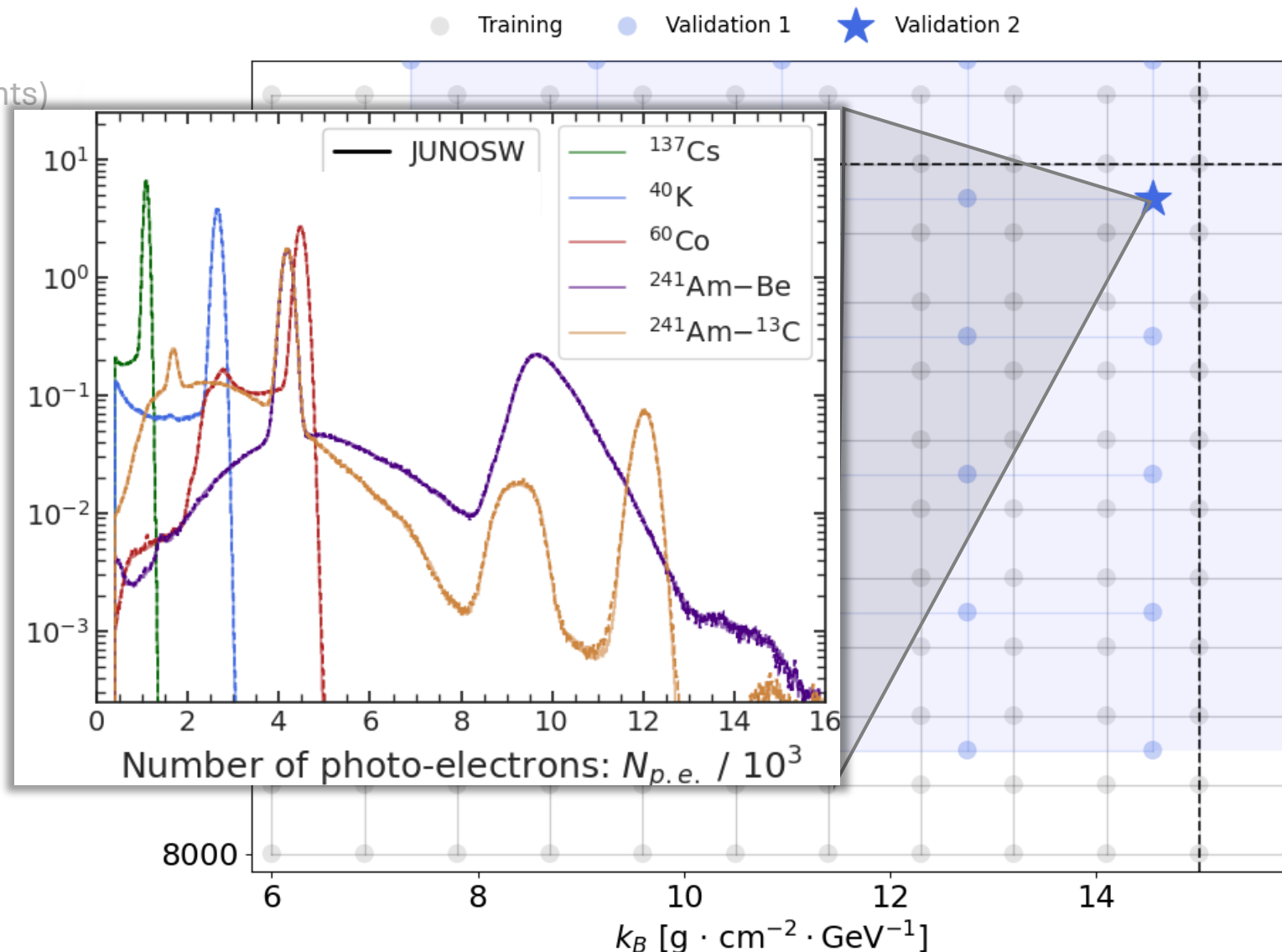
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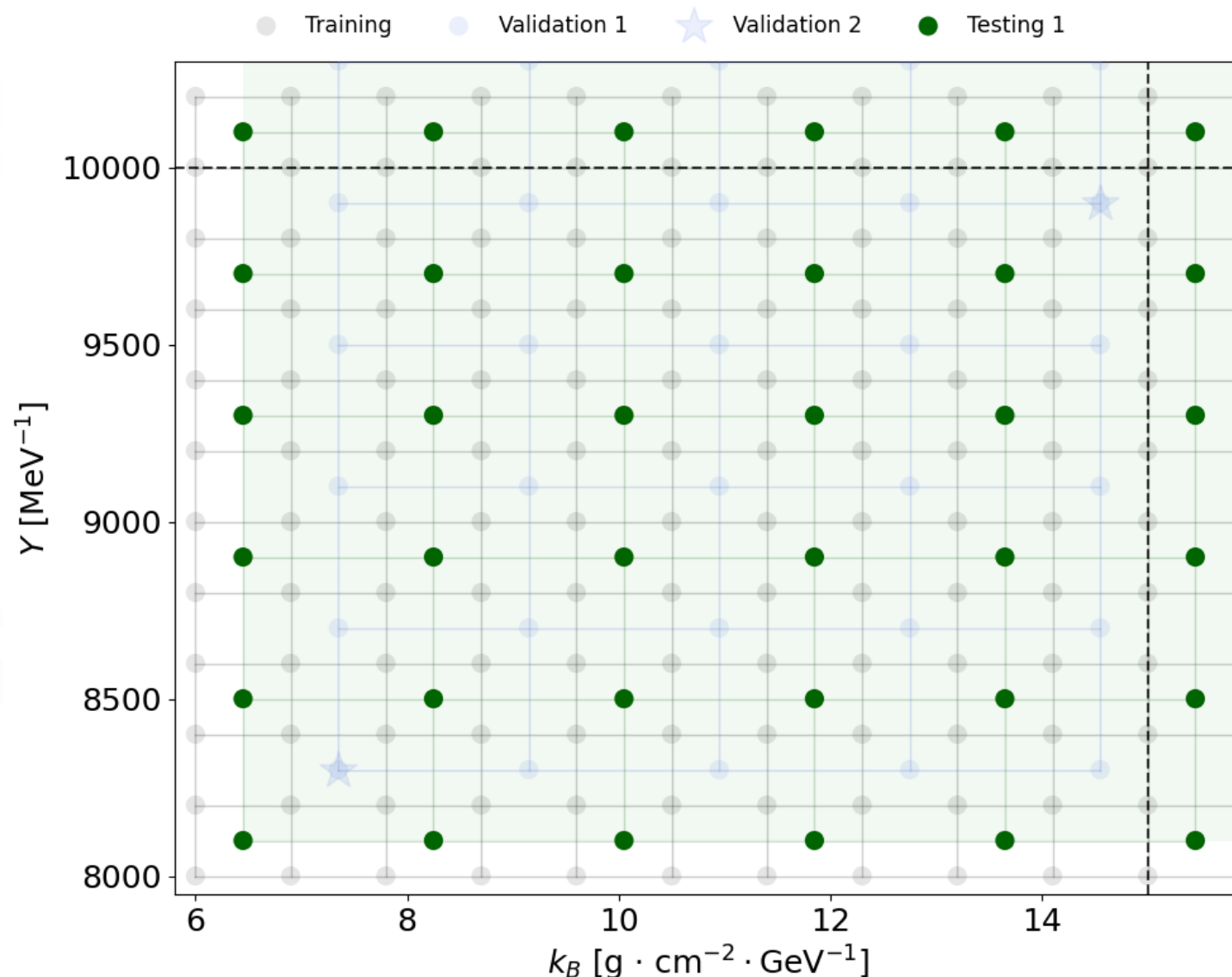
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Y and k_B example



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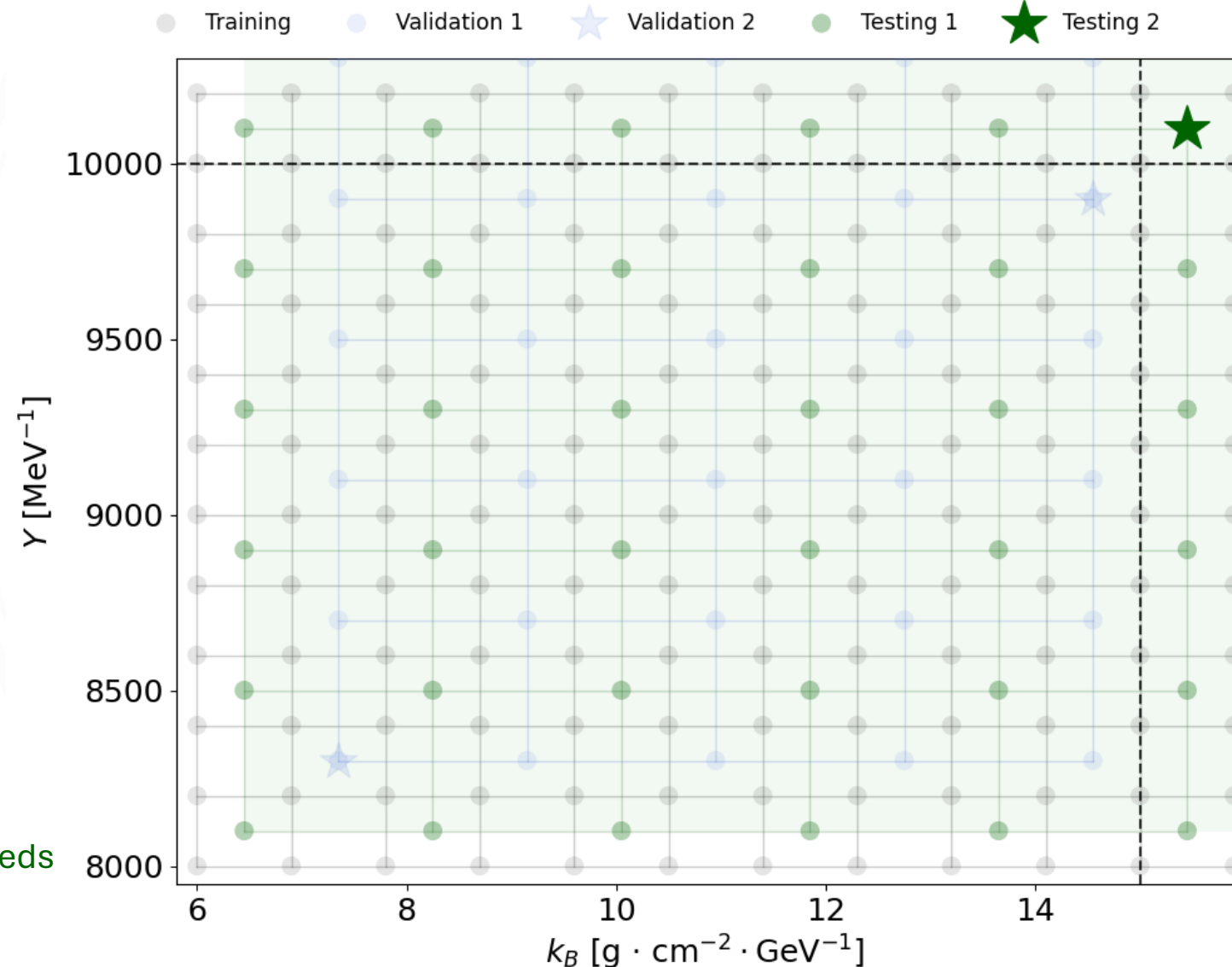
Testing data #1

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Testing data #2

- 1 point
- 1000 x [1k; 2k; 5k; 10k; 25k] events x 5 with diff. seeds
- Analysis of **systematic uncertainty** of the model

Y and k_B example



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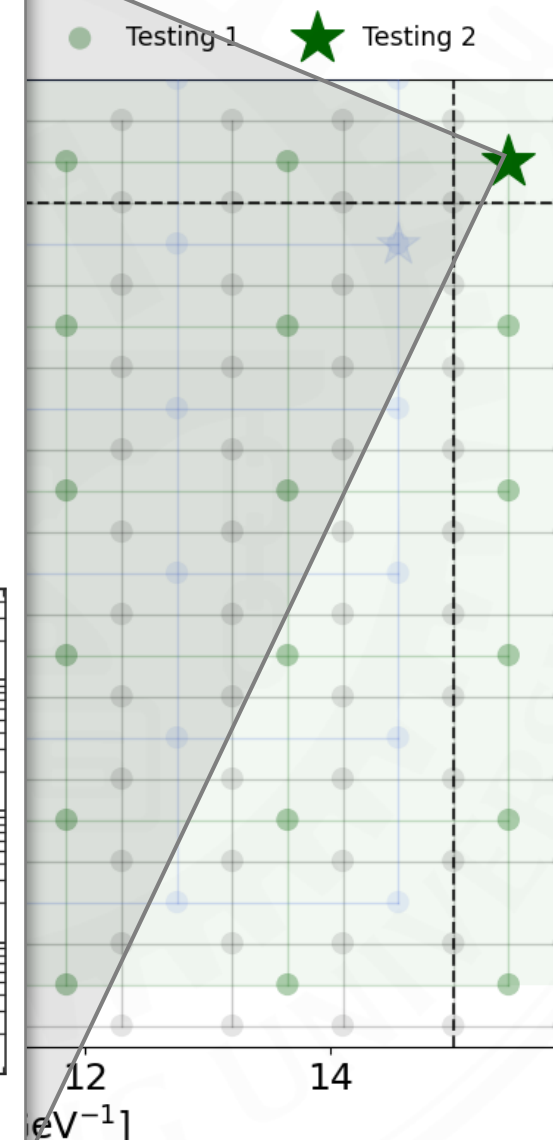
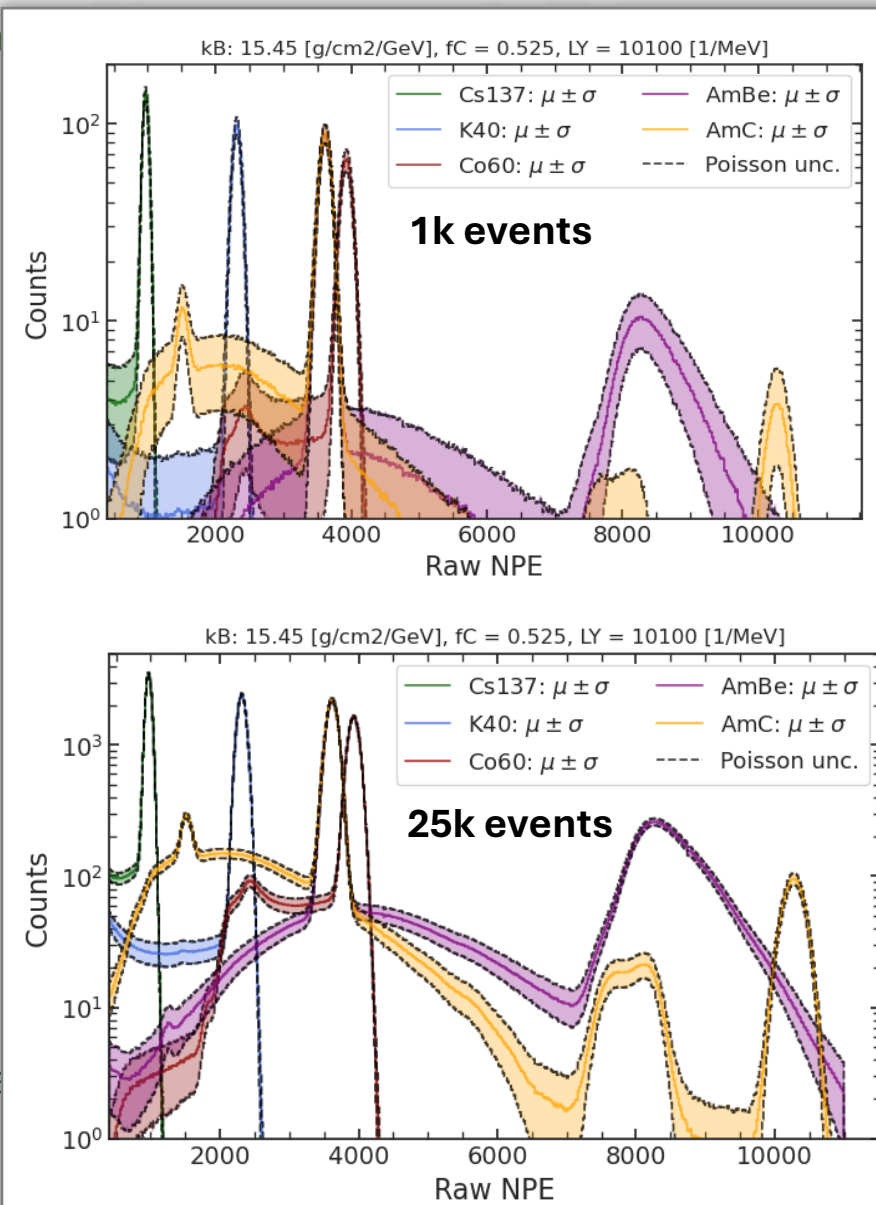
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- 10 points per param (10^3 combs)
- 10k x 5 events per point (50M events)
- check possible **biases over parameter space**

Testing data #2

- 1 point
- 1000 x [1k; 2k; 5k; 10k; 25k] events x 5 with diff. see
- Analysis of **systematic uncertainty** of the model



Datasets: training/validation strategy



Always in the center of the detector

Training data

- 21 points per param (21^3 combs)
- 10k events x 5 sources per point (~500M events)

Validation data #1

- 10 points per param (10^3 combs)
- 10k x 5 events per point (50M events)
- cover most of parameter space

Validation data #2

- 3 points in total
- 10M x 5 events per point (150M events)
- anchor PDF to high-stat spectra

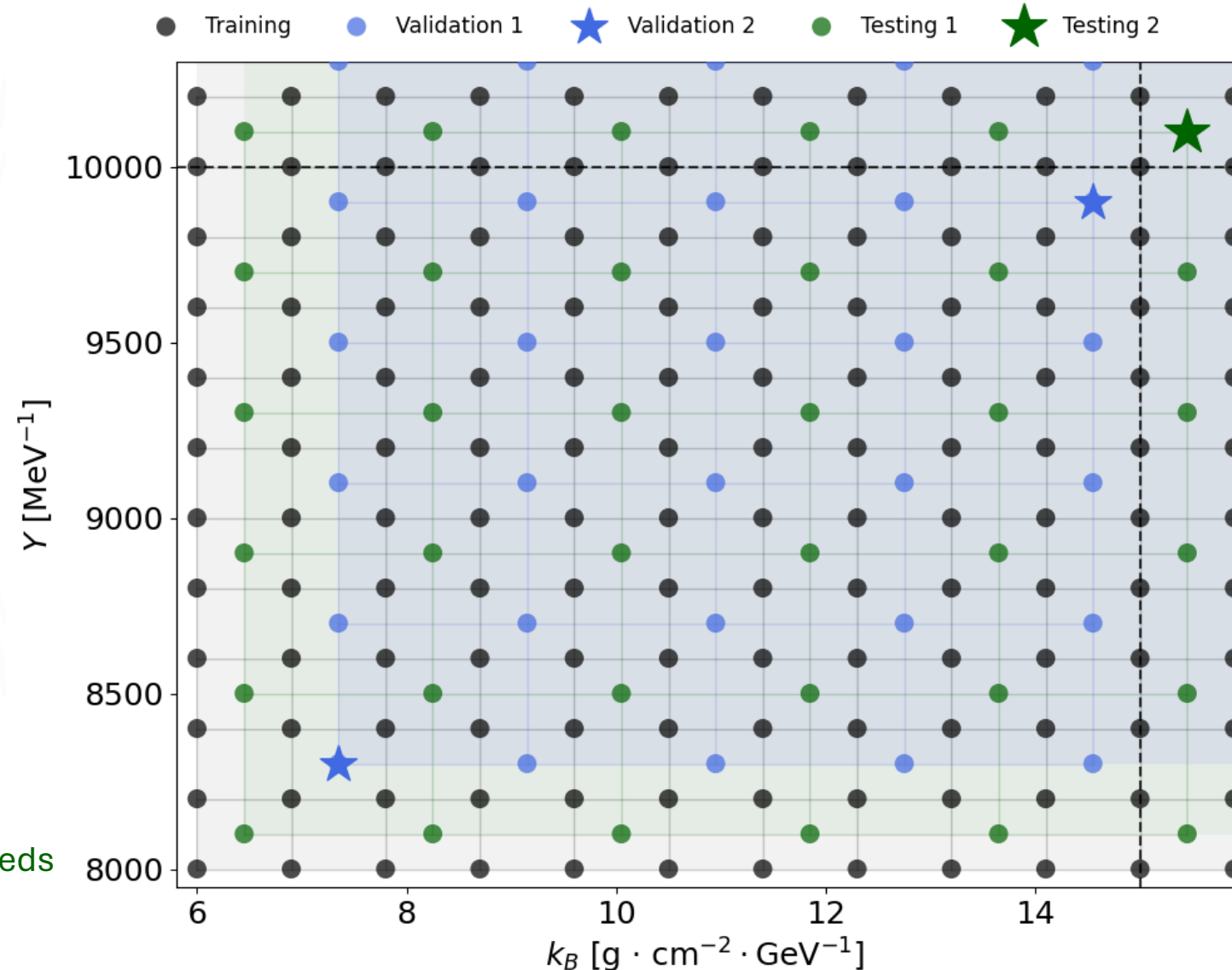
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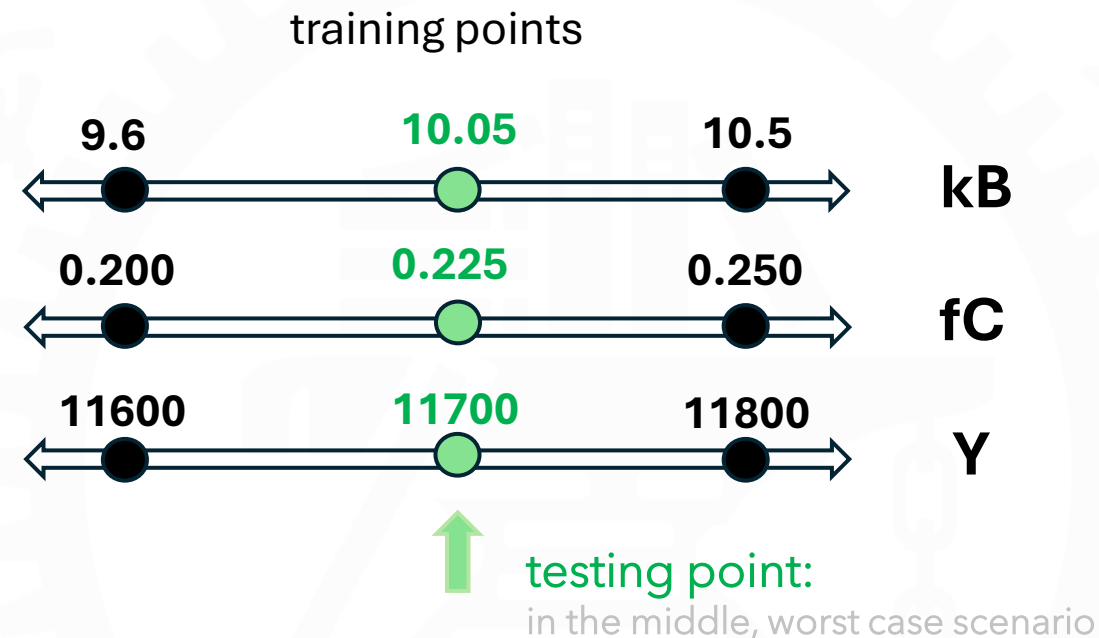
Y and k_B example



Some results: spectra modelling



Example with NFDE:



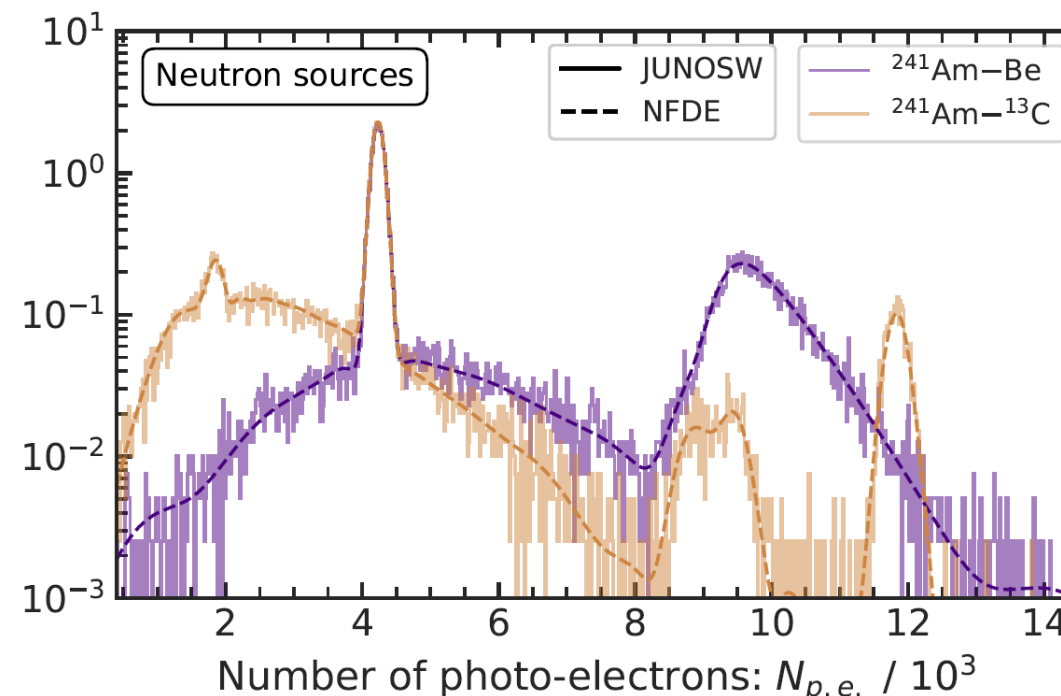
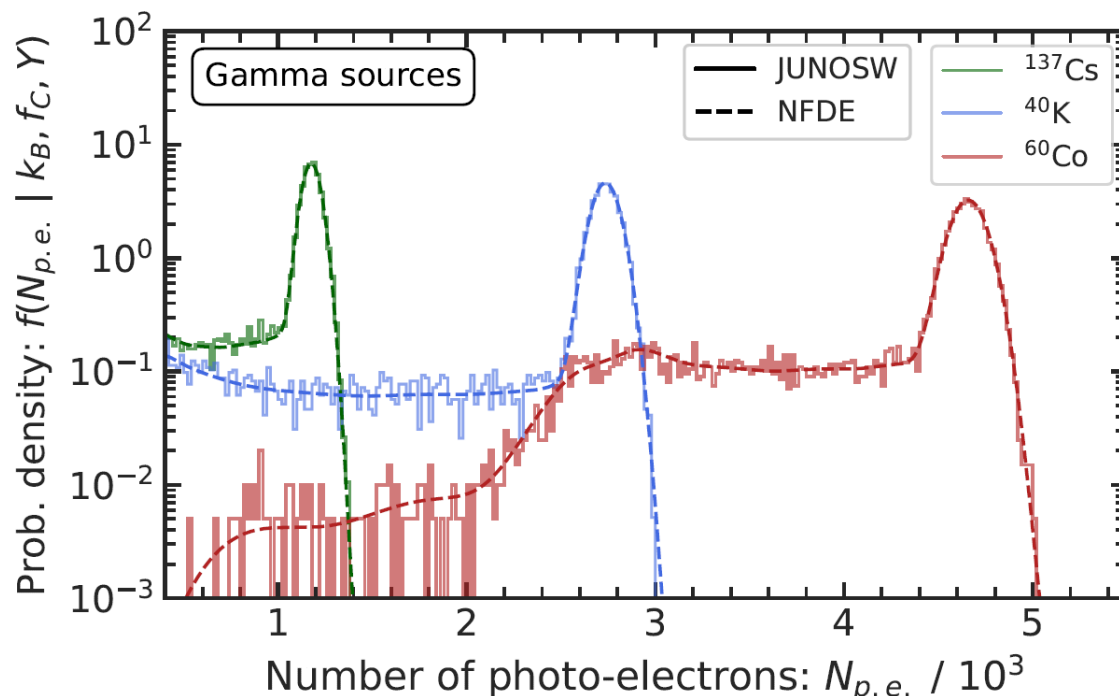
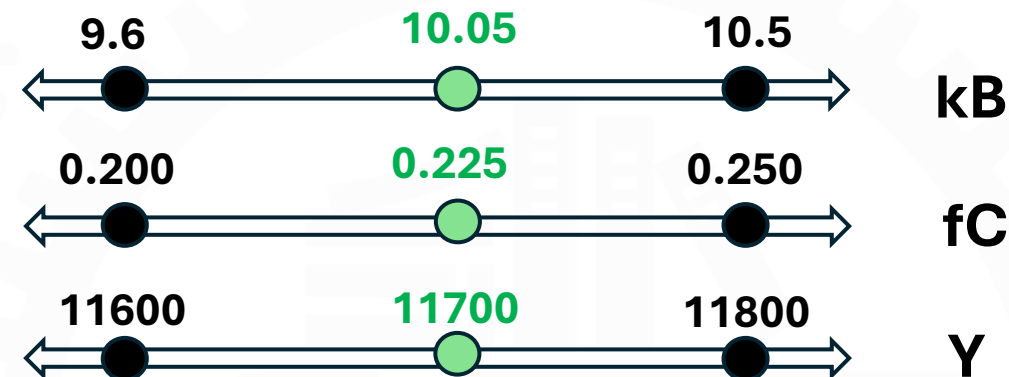
Some results: spectra modelling



Example with NFDE:

Model provides spectra estimates for *any continuous* values of the parameters

Accurate interpolation. Model's outputs are smooth and denoised



Some results: parameter estimation



Example with NFDE:

- **Combined fit** on all sources together
- **Cost function:** Extended unbinned likelihood (NFDE)
- **Optimizer:** Nested Sampling (ultranest)*
- Estimate the **k_B , f_C , Y best parameters**
- Explores full phase space, **provides full posterior**
- **Shows correlations** between the parameters

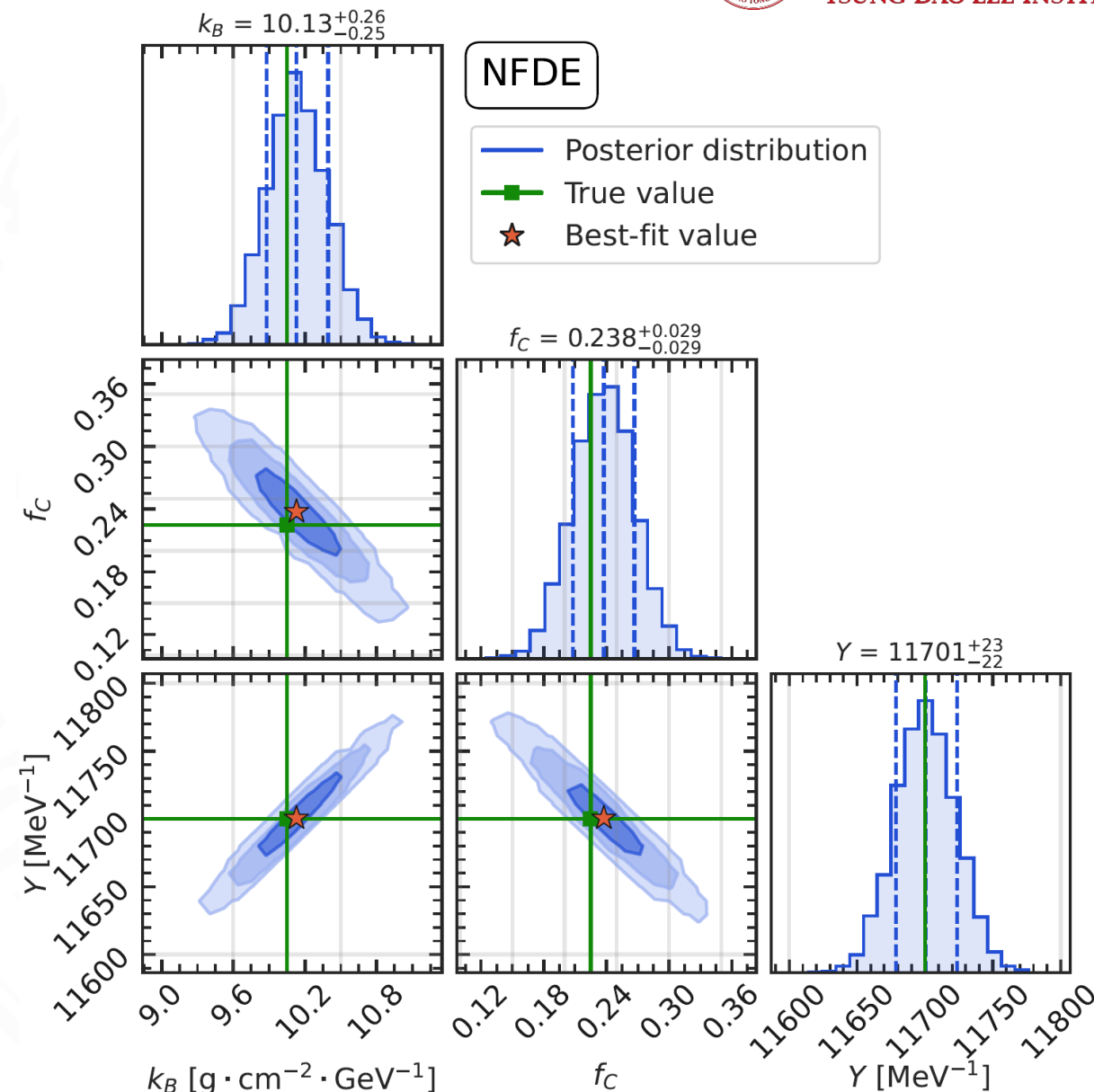
Parameters estimation combined:

- k_B : 10.13 ± 0.26 | 10.05 [$\text{g}/\text{cm}^2/\text{GeV}$]
- f_C : 0.238 ± 0.029 | 0.225
- Y : 11701 ± 23 | 11700 [$1/\text{MeV}$]

→ **well within 1σ** (fluctuations expected for 1 fit)

*all fits performed with Minuit, MCMC, Nested Sampling (ultranest) → consistent results

A. Gavrikov, A. Serafini, D. Dolzhikov et al., *Commun Phys* **9**, 63 (2026)



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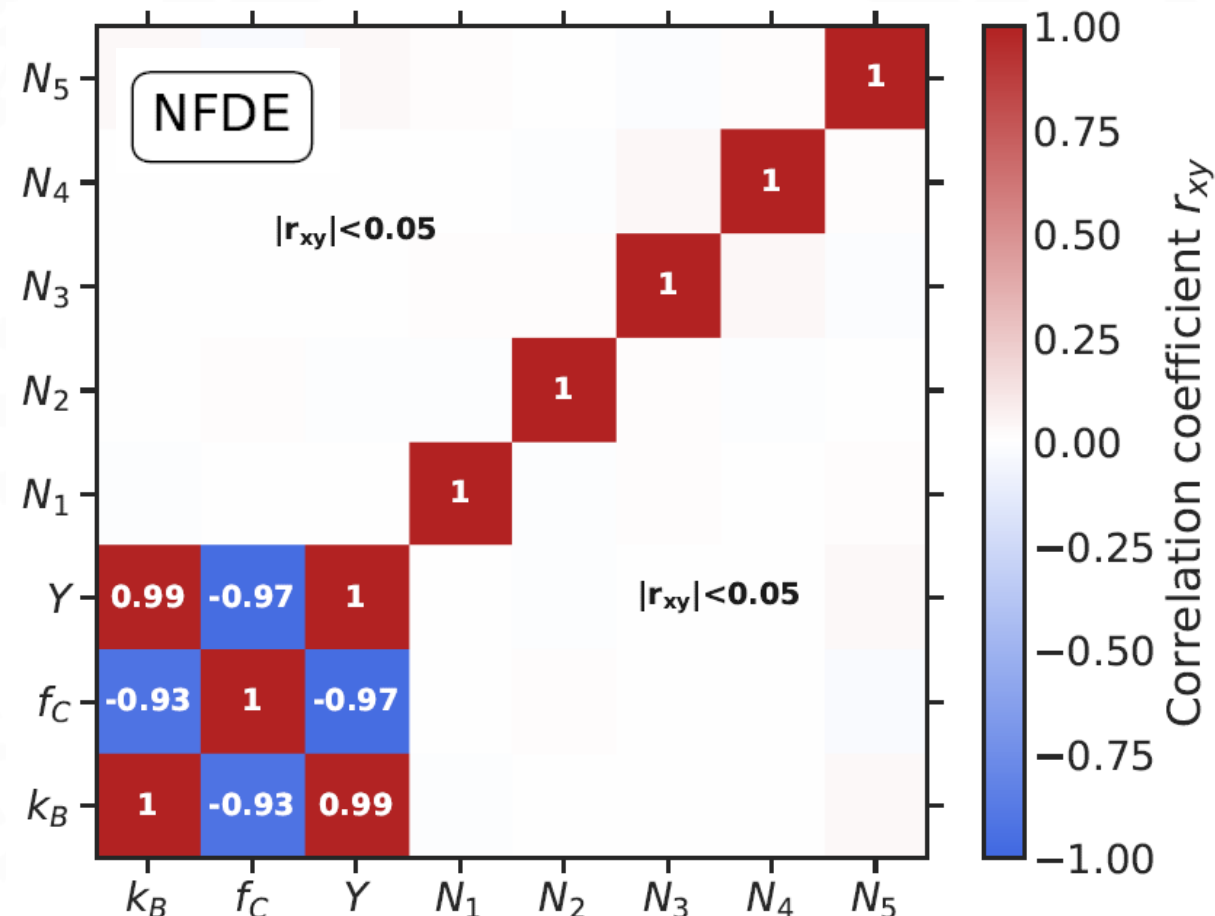
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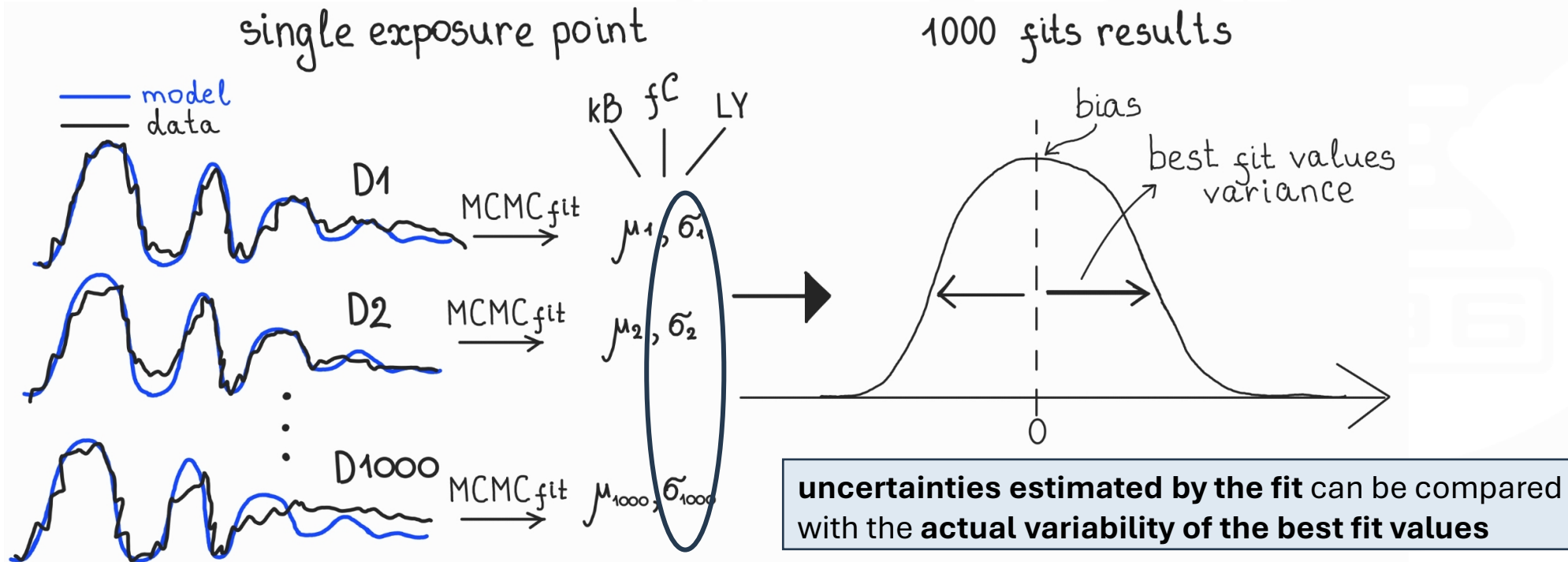


Evaluate ML-driven systematic uncertainty



To perform systematic uncertainty estimation analysis, we use the testing dataset 2:

- **Unseen during training point** in the parameter space: $kB, fC, LY = (15.45, 0.525, 10100)$
- **5 different exposures:** 1k, 2k, 5k, 10k, 25k events
- **1000 datasets with different MC generator seed** per each exposure



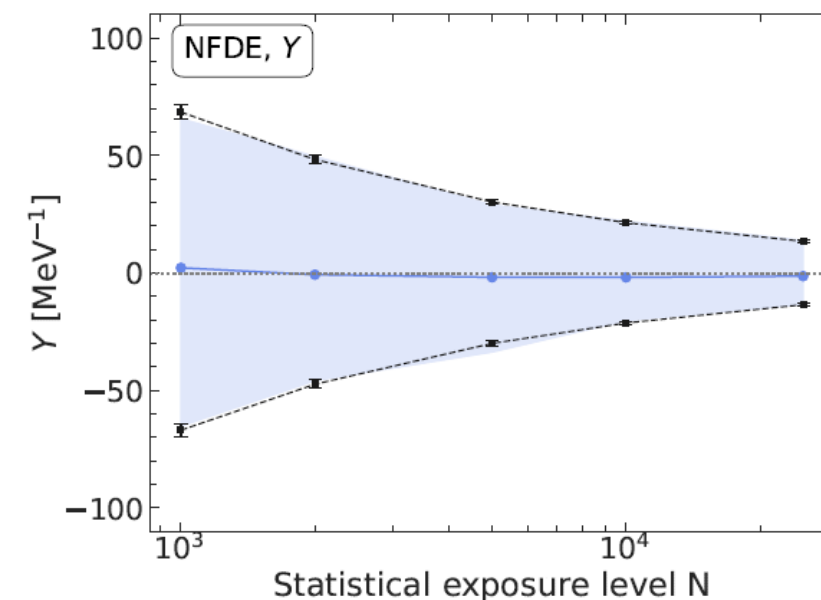
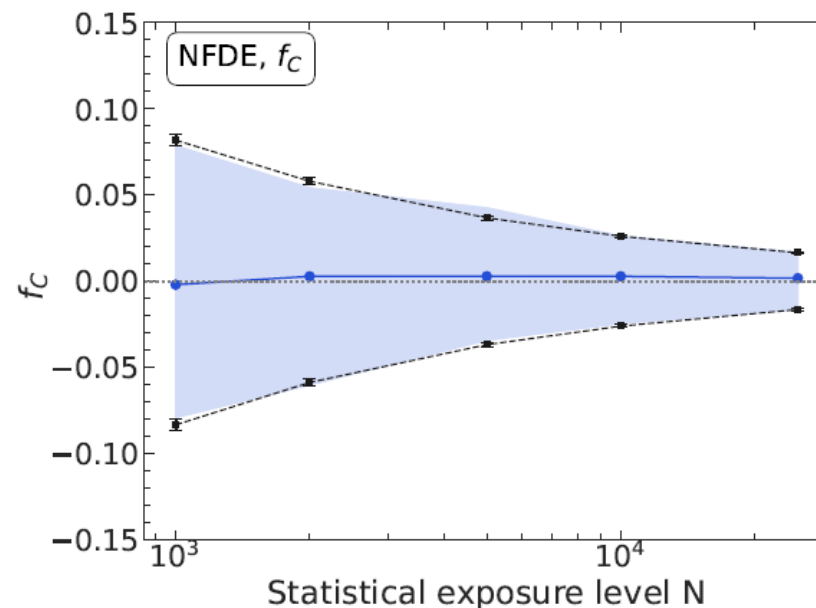
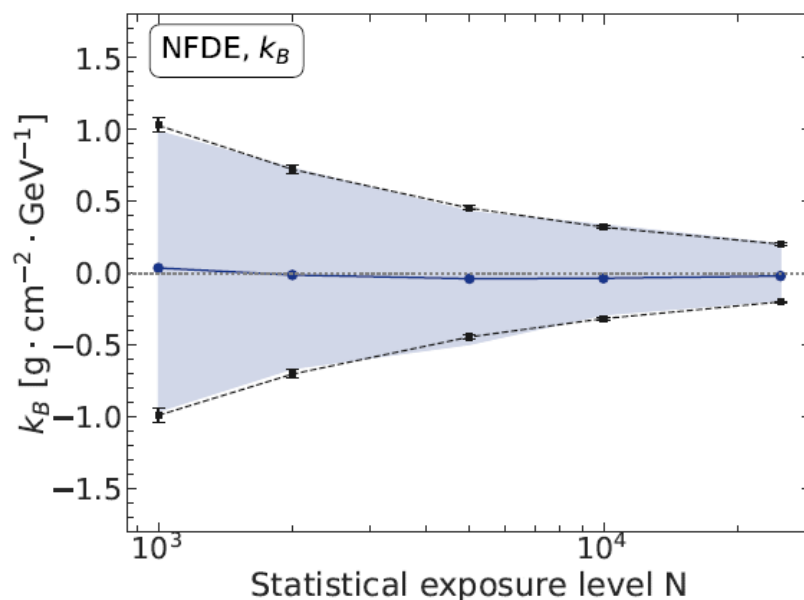
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- ➔ **Estimated uncertainty matches observed variability**

--- ■ --- Estimated Stat. Unc.
■ Observed Std. Dev.

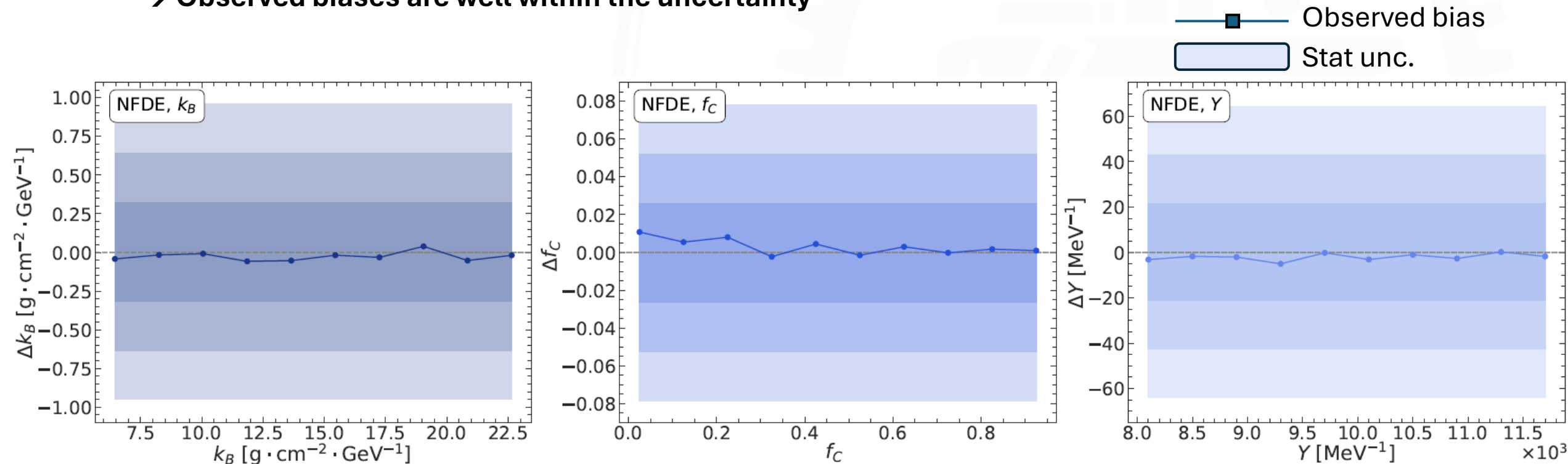


Estimation of ML-driven systematic bias

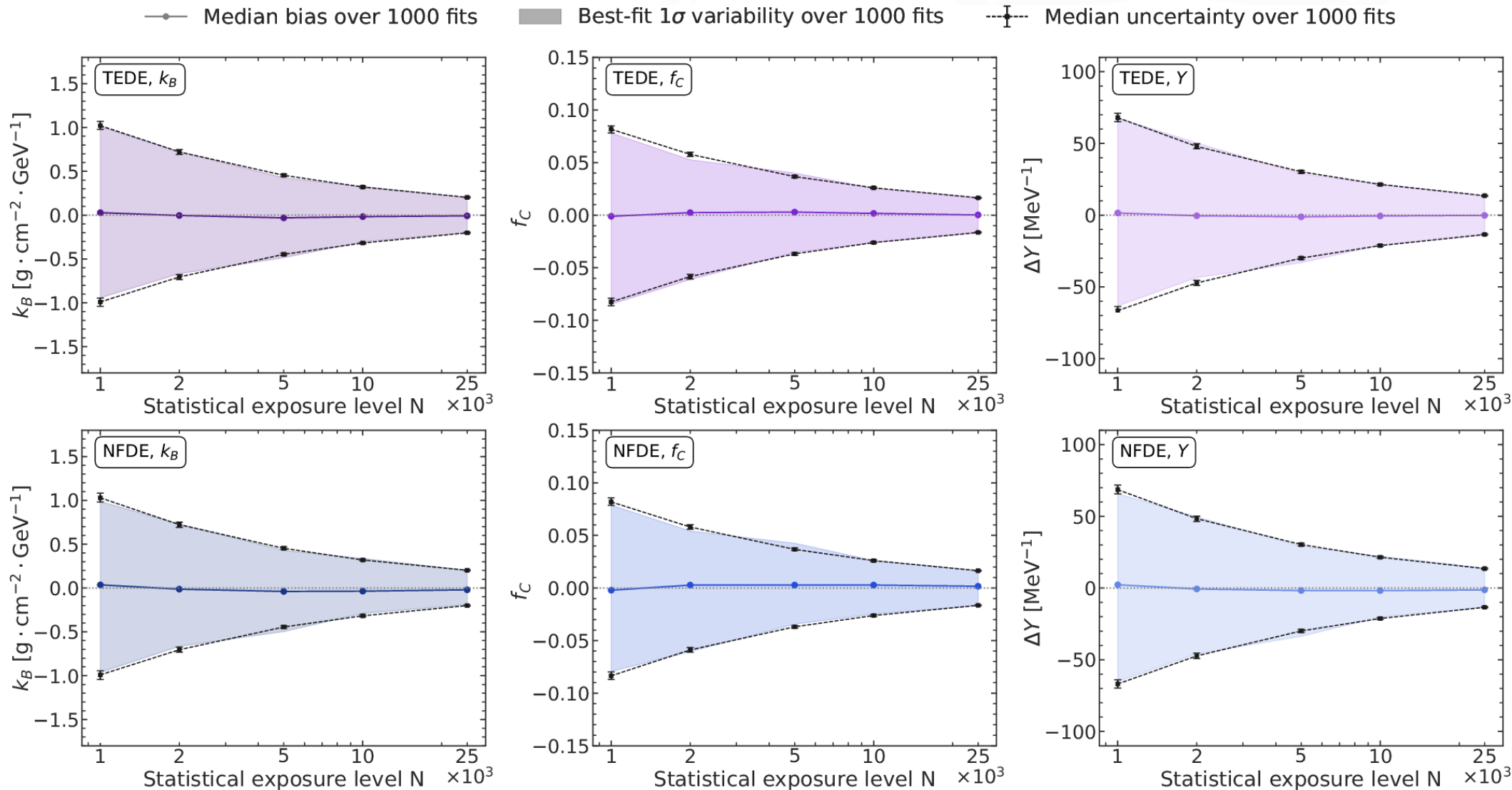


Using the testing dataset 1, one can check the bias across different points:

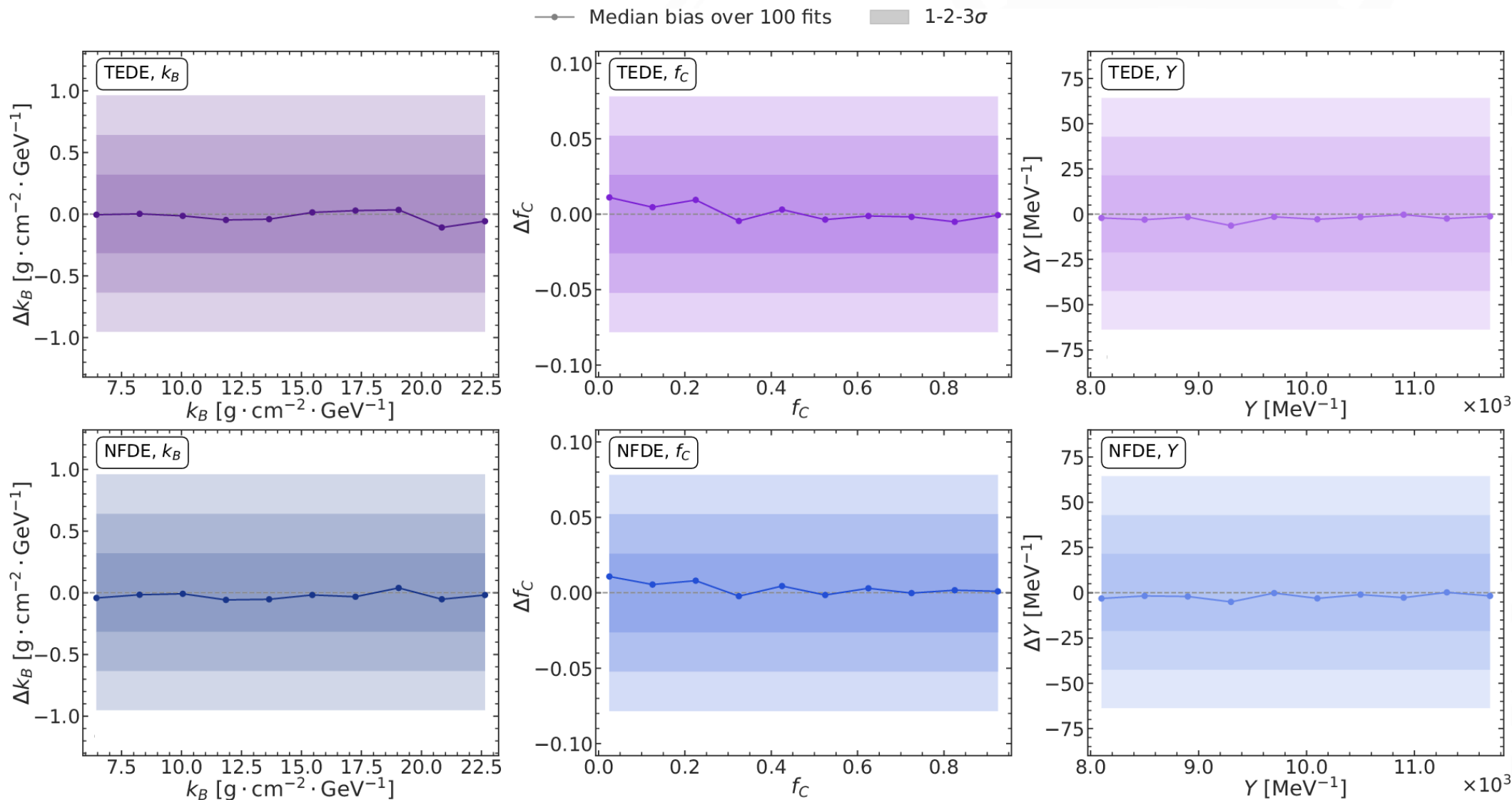
- Run MCMC fits per each testing point of the dataset
 - Compare bias with the uncertainty **obtained by the previous analysis** for the 10k exposure point
- **Observed biases are well within the uncertainty**



TEDE vs. NFDE (uncertainty)



TEDE vs. NFDE (bias)



Summary



Summary



- ❖ **Challenge: systematics investigation** for precision **neutrino physics with JUNO** and accurate energy calibration
→ requires an extremely **well tuned MC**, but the **traditional MC tuning** process is **computationally prohibitive**

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 - requires an extremely **well tuned MC**, but the **traditional MC tuning** process is **computationally prohibitive**
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- ❖ **Key Achievements:**
 - our **models successfully learn** the complex, **non-linear energy response of the JUNO detector MC**, including the strong correlations between k_B , f_C and Y parameters in the MC
 - when integrated with **Bayesian inference**, our method recovers all parameters with **near-zero systematic bias**
 - parameter **uncertainties are limited purely by statistics** and scale correctly as $1/\sqrt{N}$
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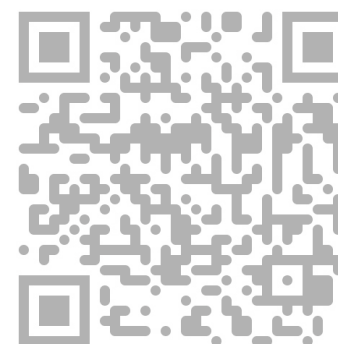
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- ❖ **The approach itself is detector-agnostic** and can be applied in other experiments to solve similar problems
- ❖ **Ongoing work:** neural scaling laws for optimizing the simulation budgets & implementation and validation of the approach within the experiment



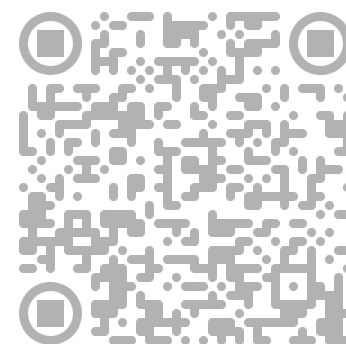
李政道研究所
TSUNG-DAO LEE INSTITUTE

Thank you!

Repo



Paper





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TSUNG-DAO LEE INSTITUTE

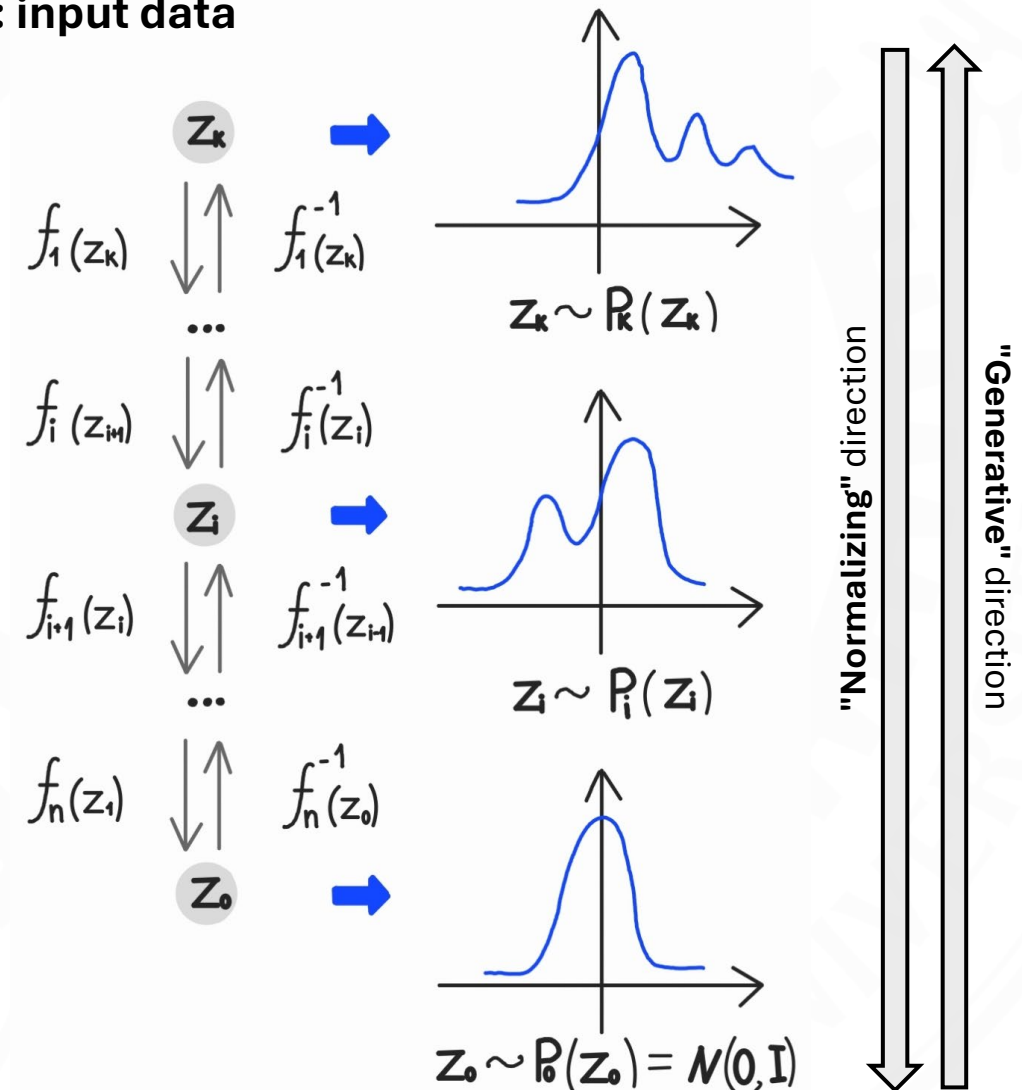
Backup

Normalizing flows-based density estimation

❖ Normalizing flows [1]:

- **Generative** machine learning **model**
- Aims to **explicitly model a density estimation**
- Can be generalized for modeling a **conditional density estimation** as well
- To obtain a value from the target distribution:
 - sample a value from the base distribution and passing it through all the flows

$\mathbf{x}$: input data



[1] R. J. Rezende et al, arxiv: 1505.05770

Normalizing flows-based density estimation

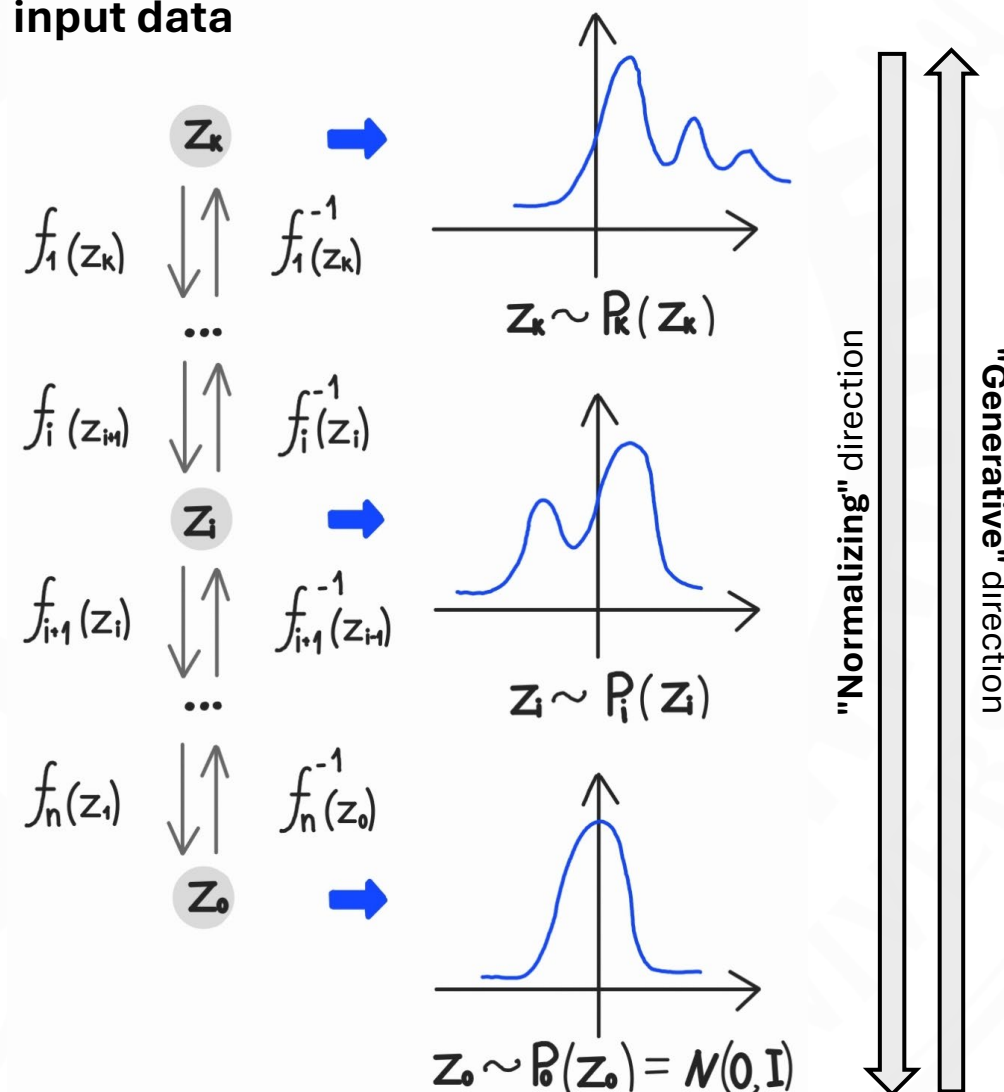
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❖ Normalizing flows are based on an **idea of transforming a simple known distribution** (e.g. *standard Gaussian*) **to the complex, desired distribution** by applying multiple learnable (*using data*) transformations

❖ **Each transformation** is called Flow and **must be invertible**

x: input data



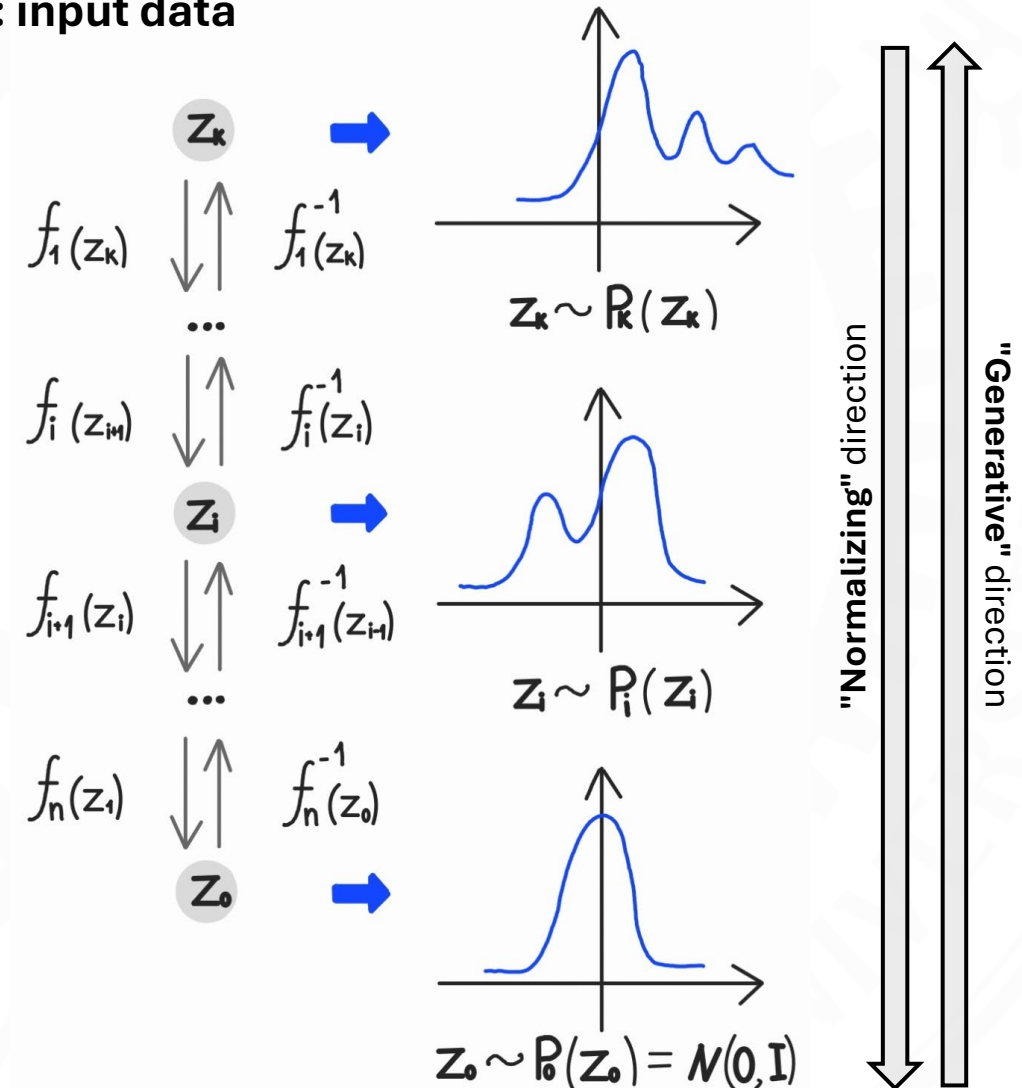
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Normalizing flows-based density estimation

❖ Normalizing flows [1]:

- Transformations can be very diverse as long as they follow **the invertibility condition**
- **Planar flow:**
 - $f_{\theta}(x) = x + u_{\theta} \tanh(xw_{\theta} + b_{\theta})$

x: input data



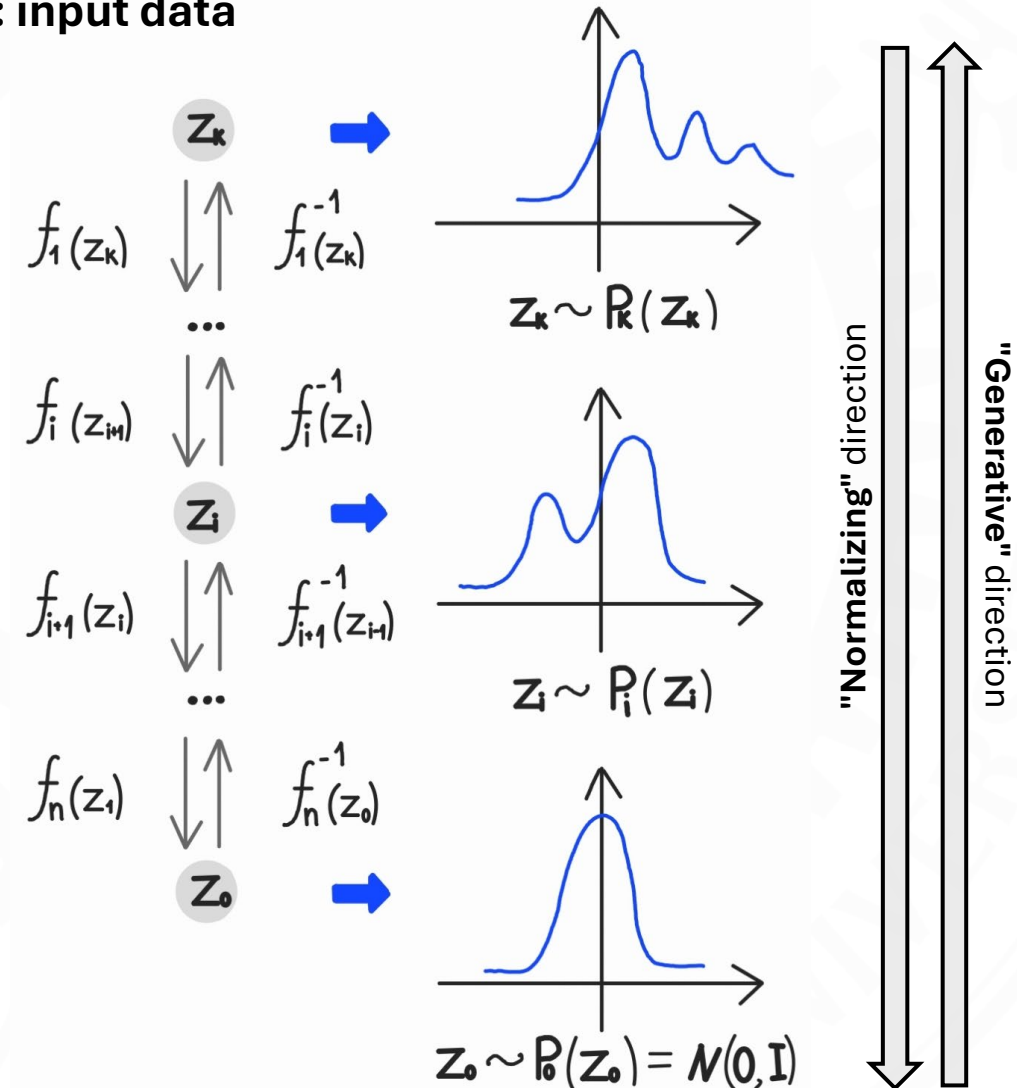
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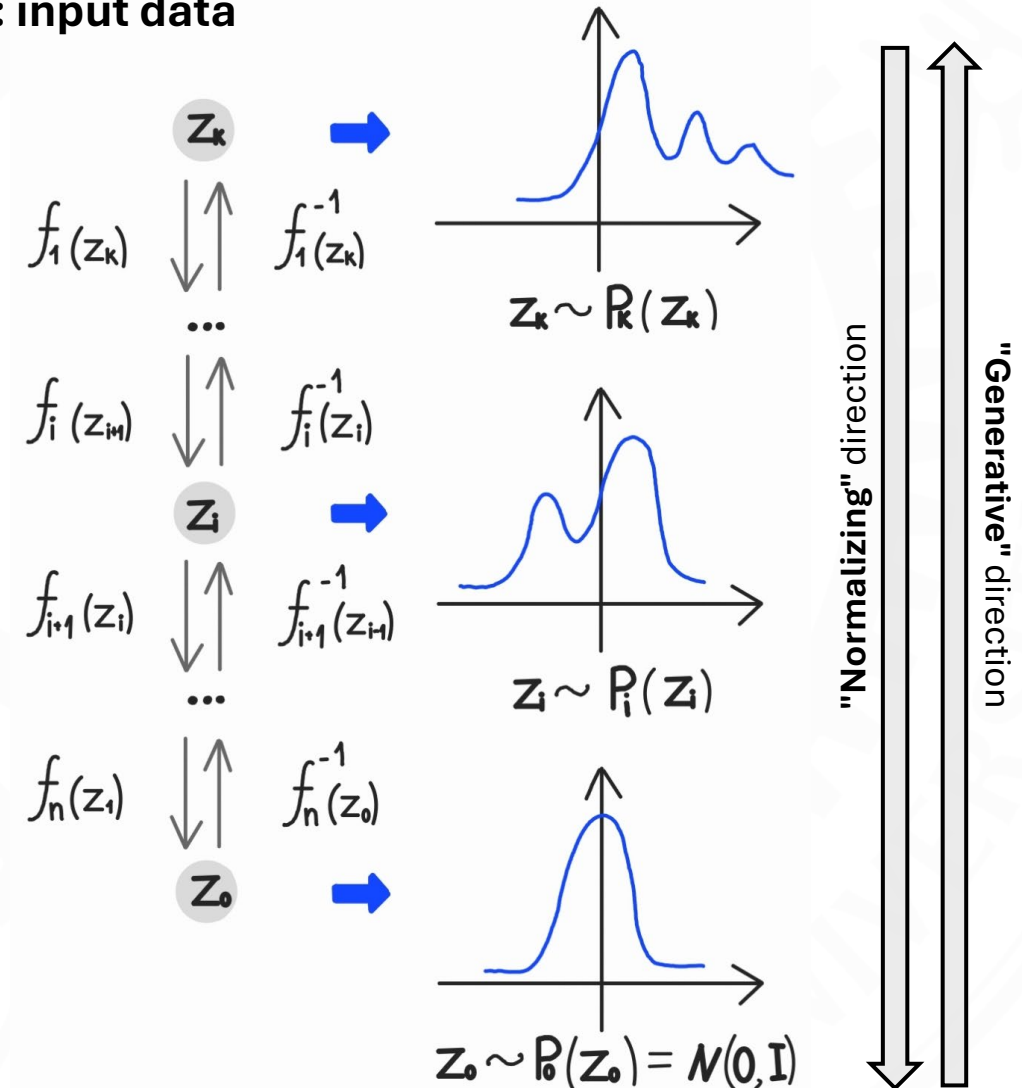
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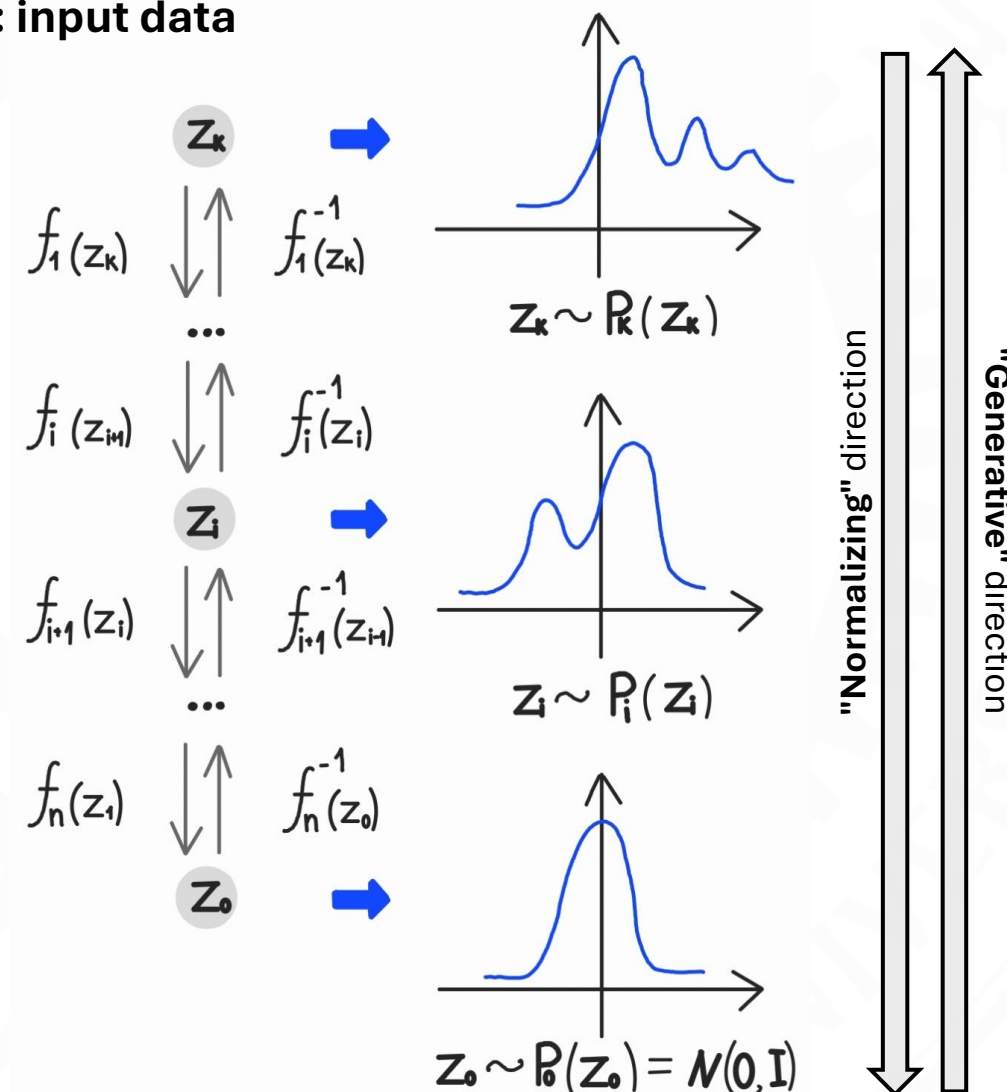
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❖ How to perform the inference with the model?

$$\log p(x|y) = \log p(z_0) + \sum_{k=1}^{K-1} \log \frac{df_{k,\theta_k}(z_k)}{dz_k} + \log \frac{df_{K,\theta_K}(x)}{dx}$$

Data	MC parameters + source type	well-known (e.g. standard Gaussian)	Computed based on the learned transformations
------	-----------------------------	-------------------------------------	---

x: input data



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Training and validation of the models



- For both models we use **Kullback–Leibler divergence as the loss function** for training:
- As validation metrics we use p-norm distances between distributions' CDFs:

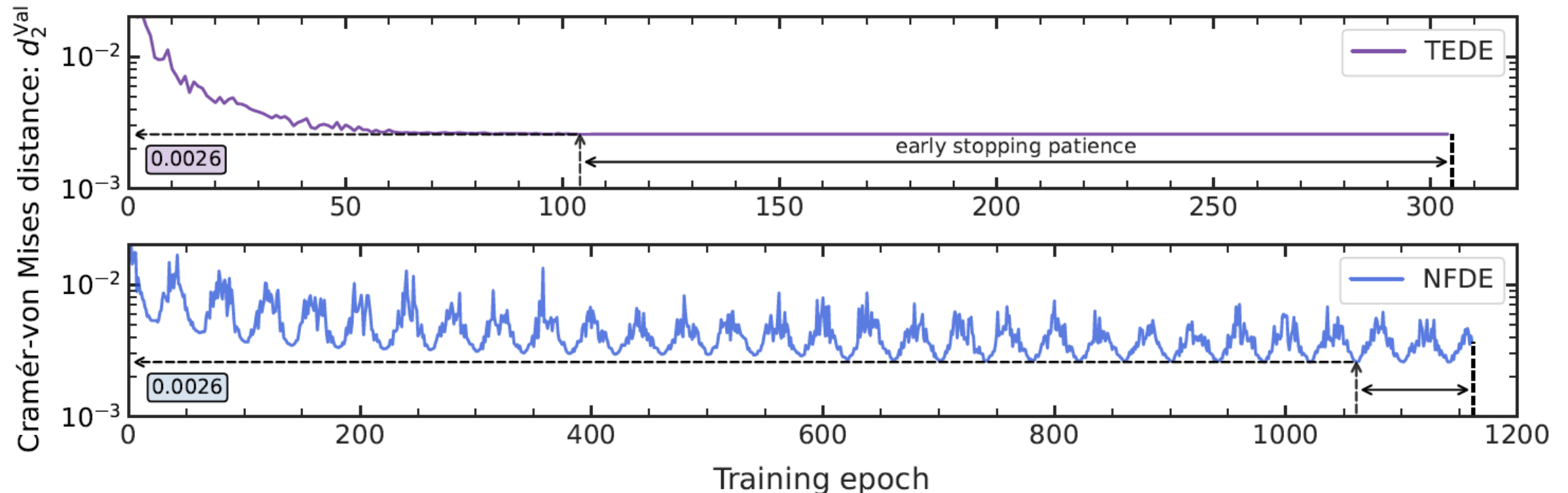
$$d_p(F_u, F_v) = \left(\int_{-\infty}^{+\infty} |F_u(x) - F_v(x)|^p dx \right)^{\frac{1}{p}}$$

as it is applicable for both TEDE and NFDE cases

$p = 1$: Wasserstein distance

$p = 2$: **Cramer von Mises distance**

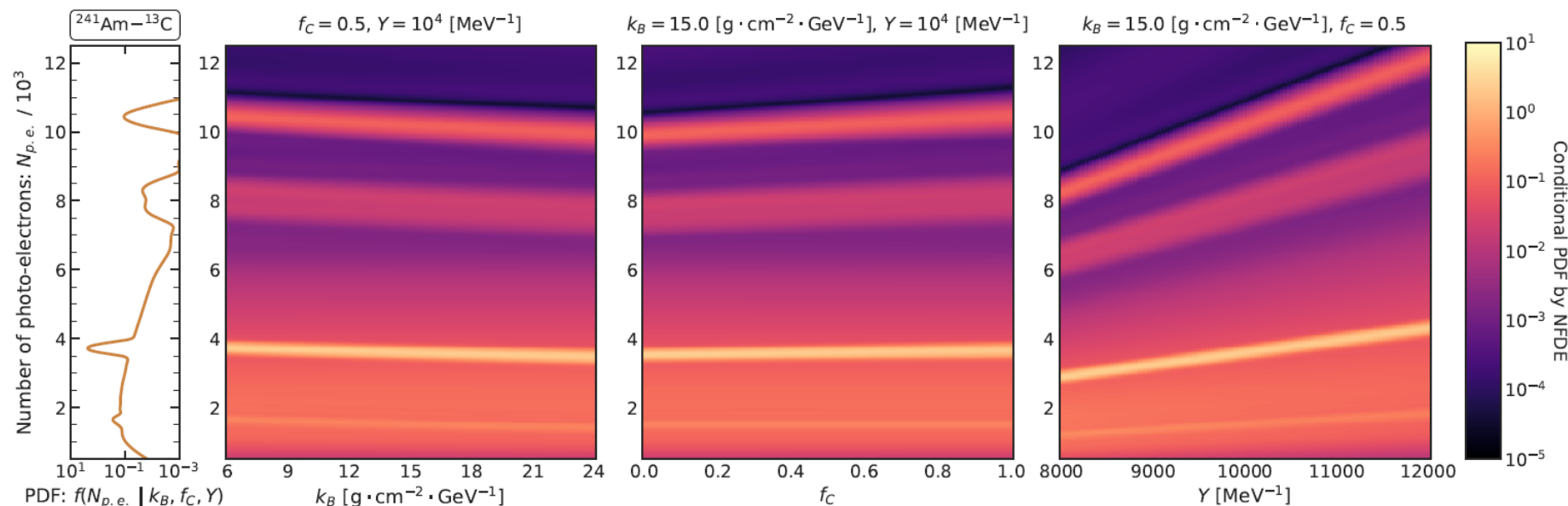
$p \rightarrow \infty$: Kolmogorov-Smirnov distance



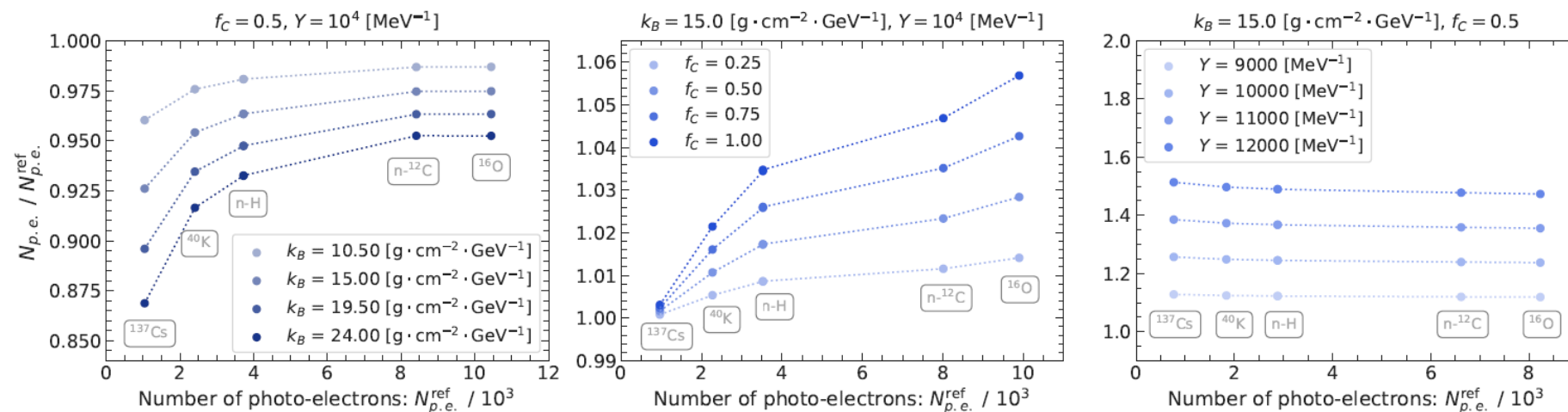
Learned dependences



1) PDF vs. parameter
(almost linear)



2) PDFs vs. energy (NPE)
(energy non-linearity)



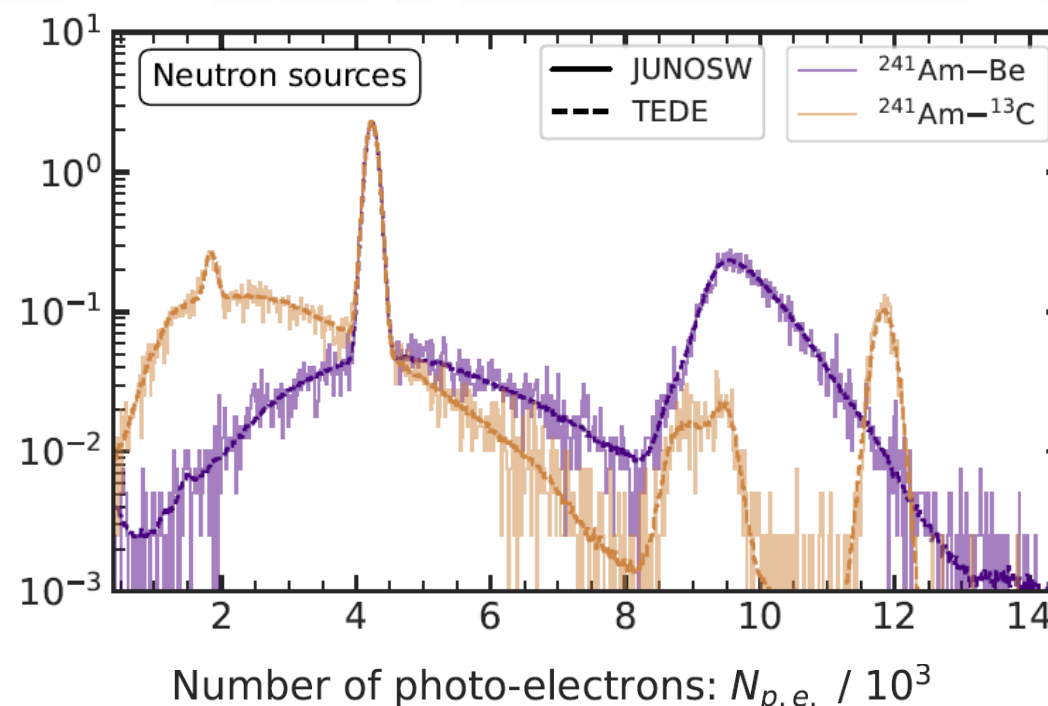
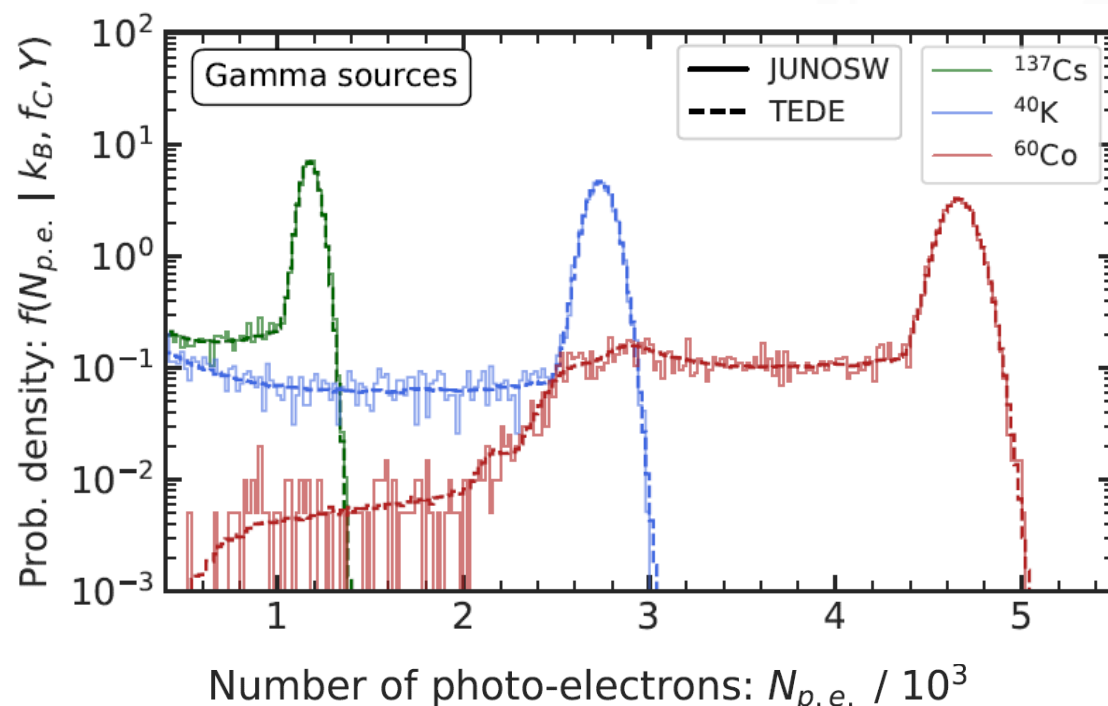
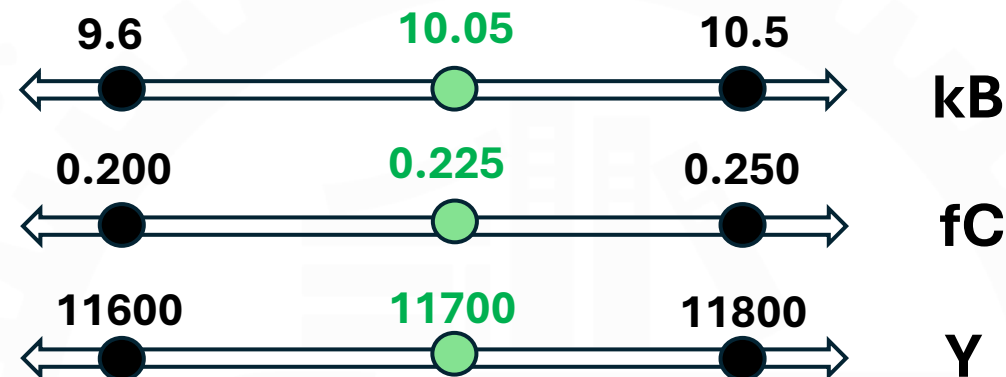
Some results: spectra modelling



Example with TEDE:

Model provides spectra estimates for *any continuous* values of the parameters

Accurate interpolation. Model's outputs are smooth and denoised



Hyperparameter optimization



Hyperparameters	TEDE
<i>Model architecture hyperparameters</i>	
n_{tokens}	$\{k \mid k \in \mathbb{N}, 1 \leq k \leq 5\}$: 1
d_{model}	$\{50k \mid k \in \mathbb{N}, 1 \leq k \leq 10\}$: 100
n_{head}	$\{5, 10, 25\}$: 10
n_{layers}	$\{k \mid k \in \mathbb{N}, 1 \leq k \leq 5\}$: 4
d_{ff}	$\{32k \mid k \in \mathbb{N}, 1 \leq k \leq 15\}$: 384
Dropout rate	$\{p_{\text{drop}} \mid 0.0 \leq p_{\text{drop}} \leq 0.5\}$: 0.0
Activation function [114, 199–201]	ReLU, GeLU
Softmax temperature	$\{T \mid 0.25 \leq T \leq 3.0\}$: 2.03
<i>General training hyperparameters</i>	
Optimizer [115, 202]	AdamW, RMSprop
Learning rate	$\{\eta \mid 10^{-5} \leq \eta \leq 10^{-2}\}$: 1.9×10^{-3}
Scheduler type [203, 204]	Exponential, ReduceOnPlateau, CosineAnnealing, None
Weight decay	$\{\lambda \mid 10^{-6} \leq \lambda \leq 10^{-1}\}$: 8×10^{-5}
Batch size	$\{2^k \mid k \in \mathbb{N}, 4 \leq k \leq 9\}$: 64
<i>Optimizer-specific hyperparameters</i>	
AdamW decay rate β_1	$\{\beta_1 \mid 0.5 \leq \beta_1 \leq 0.95\}$: 0.930
AdamW decay rate β_2	$\{\beta_2 \mid 0.9 \leq \beta_2 \leq 0.999\}$: 0.929
RMSprop parameter α	$\{\alpha \mid 0.9 \leq \alpha \leq 0.999\}$: –
<i>Scheduler-specific hyperparameters</i>	
Cosine annealing period T_{max}	$\{T_{\text{max}} \mid 5 \leq T_{\text{max}} \leq 75\}$: –
Exponential rate τ	$\{\tau \mid 0.8 \leq \tau \leq 0.99\}$: 0.92
Reduce on plateau factor γ	$\{\gamma \mid 0.8 \leq \gamma \leq 0.99\}$: –
<i>Optimization procedure setting</i>	
Number of trials	250
Accelerator	GPU

Hyperparameters	NFDE
<i>Model architecture hyperparameters</i>	
n_{flows}	$\{100 + 5k \mid k \in \mathbb{Z}, 0 \leq k \leq 20\}$: 120
n_{units}	$\{10 + 5k \mid k \in \mathbb{Z}, 0 \leq k \leq 8\}$: 30
Flow type	Planar (fixed)
Activation function [114, 199–201]	ReLU, GeLU, Tanh, SiLU
<i>General training hyperparameters</i>	
Optimizer [115, 202]	AdamW (fixed)
Learning rate	10^{-4} (fixed)
Scheduler type [203, 204]	ReduceOnPlateau, CosineAnnealing
Weight decay	10^{-4} (fixed)
Batch size	50 (fixed, 1 per CPU unit)
<i>Optimizer-specific hyperparameters</i>	
AdamW decay rate β_1	$\{\beta_1 \mid 0.5 \leq \beta_1 \leq 0.95\}$: 0.87
AdamW decay rate β_2	$\{\beta_2 \mid 0.9 \leq \beta_2 \leq 0.999\}$: 0.901
<i>Scheduler-specific hyperparameters</i>	
Cosine annealing period T_{max}	$\{T_{\text{max}} \mid 5 \leq T_{\text{max}} \leq 75\}$: 50
Reduce on plateau factor γ	$\{\gamma \mid 0.8 \leq \gamma \leq 0.99\}$: –
<i>Optimization procedure setting</i>	
Number of trials	25
Accelerator	50 parallel CPUs