

Charged-Current Coherent ρ Production in Neutrino-nucleus Interactions

Xinchun Tian
for the NOMAD Collaboration

Department of Physics and Astronomy



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Outline

Coh ρ production in neutrino-nucleus

Motivation

The NOMAD Experiment

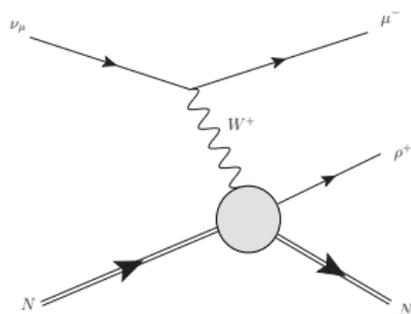
The Analysis

Coherent Meson Production Study at LBNE

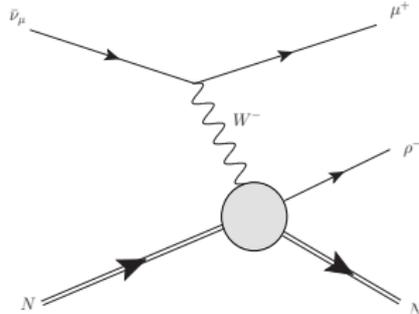
Conclusion

Vector Meson Dominance Model

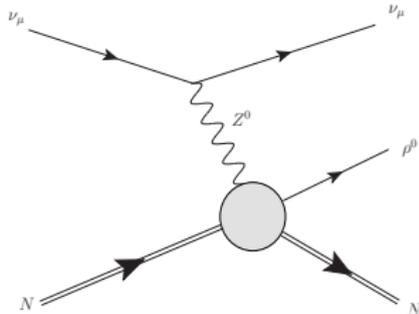
$$\nu_\mu A \rightarrow \mu^- A \rho^+$$



$$\bar{\nu}_\mu A \rightarrow \mu^+ A \rho^-$$



$$\nu_\mu A \rightarrow \nu_\mu A \rho^0$$



Conservation of Vector Current

$$\frac{d^3\sigma(\nu_\mu A \rightarrow \mu^- \rho^+ A)}{dQ^2 d\nu dt} = \frac{G_F^2}{4\pi^2} \frac{f_\rho^2}{1 - \epsilon} \frac{|q|}{E_\nu^2} \left[\frac{Q}{Q^2 + m_\rho^2} \right]^2 (1 + \epsilon R) \left[\frac{d\sigma^T(\rho^+ A \rightarrow \rho^+ A)}{dt} \right]$$

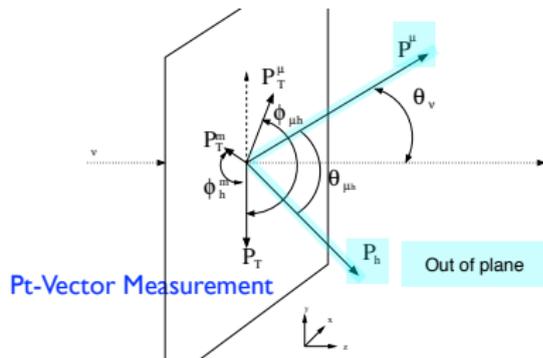
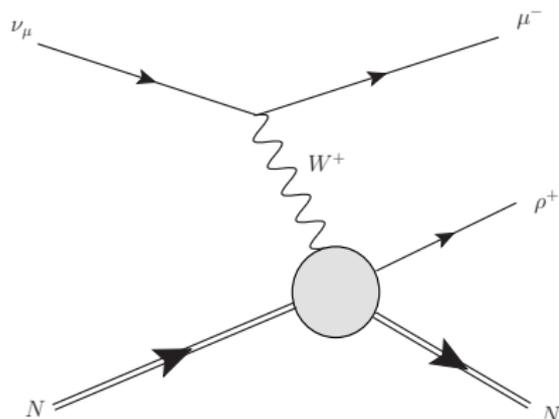
In simple Rein Sehgal meson absorption model

$$\frac{d\sigma^T(\rho^+ A \rightarrow \rho^+ A)}{dt} = \frac{\mathcal{A}^2}{16\pi} \sigma^2(h\nu) \exp(-b|t|) F_{abs}$$

Coh ρ^0 is about 15% of Coh ρ^+ related by weak mixing angle

$$\frac{d^3\sigma(\nu_\mu A \rightarrow \nu_\mu \rho^0 A)}{dQ^2 d\nu dt} = \frac{1}{2} (1 - 2 \sin^2 \theta_W)^2 \frac{d^3\sigma(\nu_\mu A \rightarrow \mu^- \rho^+ A)}{dQ^2 d\nu dt}$$

Kinematic Variables



$$\nu, Q^2, x, y, W^2$$

$$t = [\sum_i (E_i - p_{i,L})]^2 + [\sum_i (p_{i,T})]^2$$

$$z = E(1 - \cos \theta)$$

Motivation

Physics

- Structure of Weak-Current and its Hadronic-Content
 - $\text{Coh}\pi$: Partially Conserved Axial Current (PCAC) and Adler's theorem at high energy ($E_\nu > 2 \text{ GeV}$) and Microscopic model at low energy ($E_\nu < 1.5 \text{ GeV}$)
 - $\text{Coh}\rho$: Conserved Vector Current (CVC) and Vector Meson Dominance (VMD)

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Utility

- $\text{Coh}\pi^+/\text{Coh}\pi^-$: Identical final state ($\mu^\mp\pi^\pm$) to constraint the $\bar{\nu}/\nu$ energy scale
- Neutrino $\text{Coh}\rho$ measurements ($\pm, 0$) in conjunction with the photoproduction data on $\text{Coh}\rho^0$ will provide a constraint on neutrino flux
- A background in $\text{Coh}\pi^\pm$ measurements

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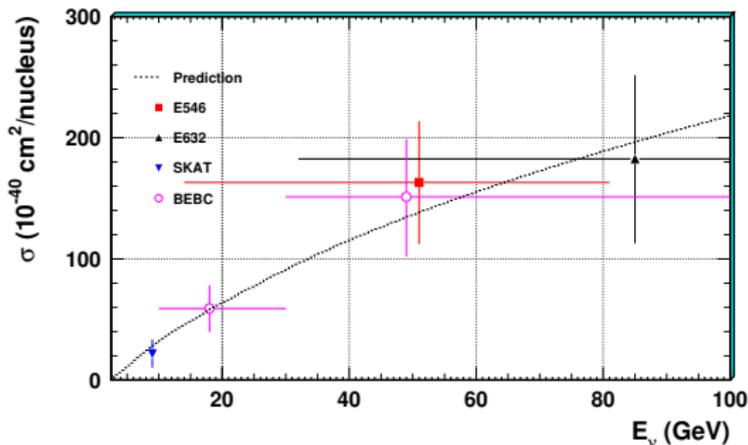
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A matrix of 6 coherent-meson measurements leads to much better modeling of low- Q^2 processes and provides constraints on flux that are independent of the usual methods.

Coh ρ^\pm Measurements Overview



Experiment	$\nu/\bar{\nu}$	Channel	Target	$\langle E_\nu \rangle$ (GeV)	σ (10^{-40} cm ² /nucleus)
E546	ν	ρ^+	Neon (A=20)	51	189.7 ± 59
BEBC WA59	$\bar{\nu}$	ρ^-	Neon (A=20)	18	73 ± 23
E632	$\nu + \bar{\nu}$	ρ^\pm	Neon (A=20)	86	210 ± 80
SKAT	ν	ρ^+	Freon (A=30)	10	29 ± 16

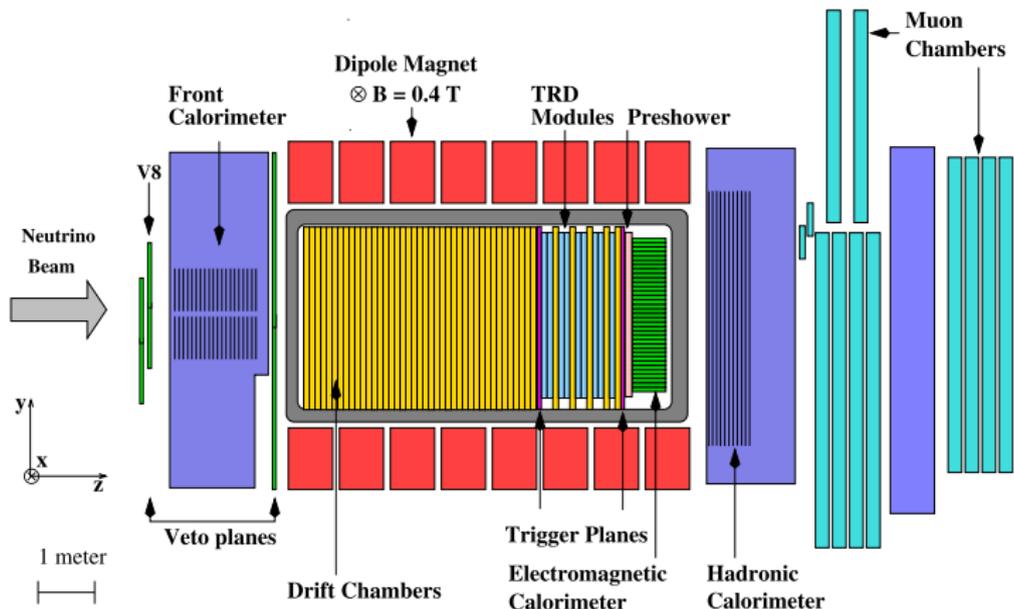
Table: The Coh ρ^\pm measurements have very large errors and the first measurement of Coh ρ^0 in NC was reported by H. Duyang at this conference, no measurement at low energy.

The NOMAD (Neutrino Oscillation MAgnetic Detector) Experiment Elements

The NOMAD experiment was designed to search for $\nu_\mu \rightarrow \nu_\tau$ oscillations at $\Delta m^2 \geq 5 \text{ eV}^2$ at CERN SPS.

- **Beam** 450 GeV protons from CERN Super Proton Synchrotron (SPS) incident on a beryllium target producing the neutrino beam (0-300 GeV, average E_ν is ~ 25 GeV)
- **Detector** Active target (2.7 tons, mostly “Carbon” with low density $\sim 0.1 \text{ g/cm}^3$) composed of Drift Chamber Tracker embedded in a 0.4 T B-field
- **Data** High precision data with 1.4 M ν_μ -CC

The NOMAD Detector



sub-detectors		performance
Drift Chambers (2.7 tons)	Target & tracking	$\delta r < 200 \mu\text{m}$ $\delta p \sim 3.5\% @ p < 10 \text{ GeV}/c$
Transition Radiation Detector (TRD)	e^\pm identification	90% e^\pm eff. with π rejection @ 10^3
Muon Chambers	Muon identification	$\epsilon \sim 97\% @ p_\mu > 5 \text{ GeV}/c$
Electromagnetic Calorimeter (ECL)	Lead glass	$\frac{\sigma(E)}{E} = (1.04 \pm 0.01)\% + \frac{3.22 \pm 0.07}{\%} E(\text{GeV})$
Hadronic Calorimeter (HCAL)	neutron and K_L^0 veto	

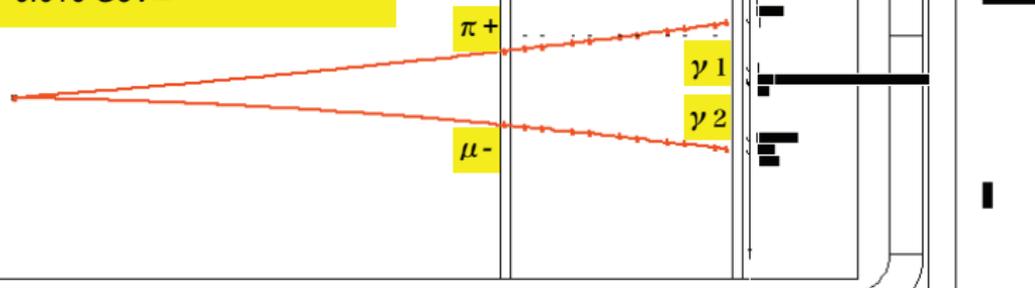
What we are looking for - $\mu^- \pi^+ + 2$ clusters

Coherent- p^+ Candidate Event

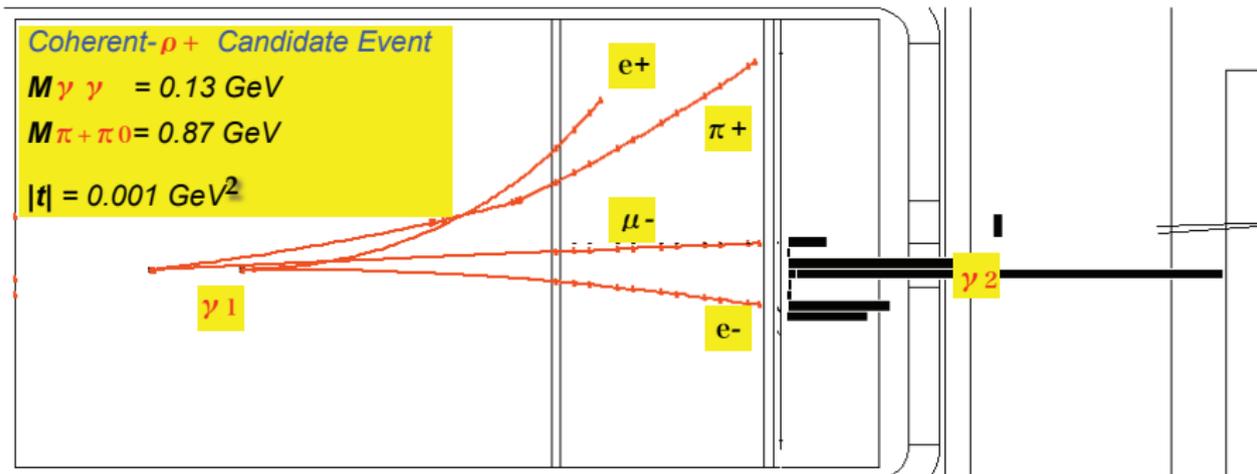
$$M_{\gamma\gamma} = 0.135 \text{ GeV}$$

$$M_{\pi^+\pi^0} = 0.711 \text{ GeV}$$

$$|t| = 0.016 \text{ GeV}^2$$



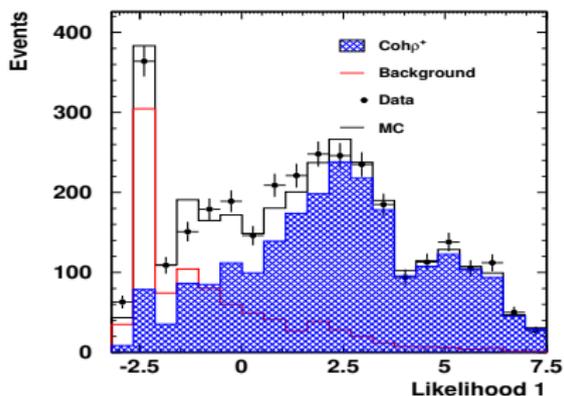
What we are looking for - $\mu^- \pi^+ + 1 \text{ cluster} + 1 V_0$



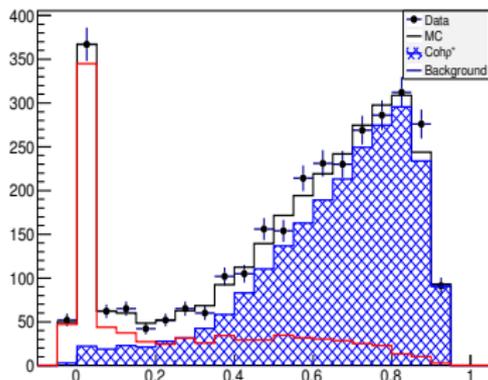
The analysis essentials

- The events passing the preselection were subjected to multi-variant analysis
- The background is constrained using the control (background) region
- Mockdata tests validate the whole analysis chain
- Two independent, Likelihood and Neural-Network analysis yield very consistent results

Mockdata Exercise



Neural Network - Data vs MC

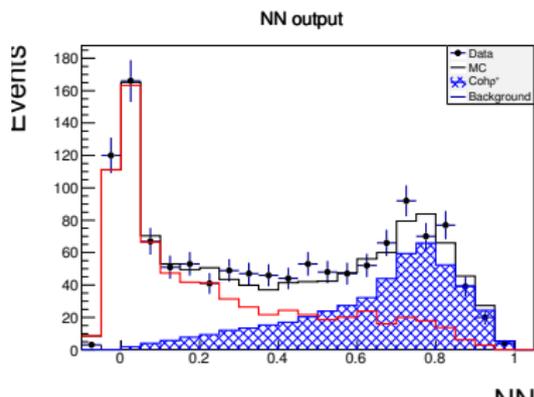
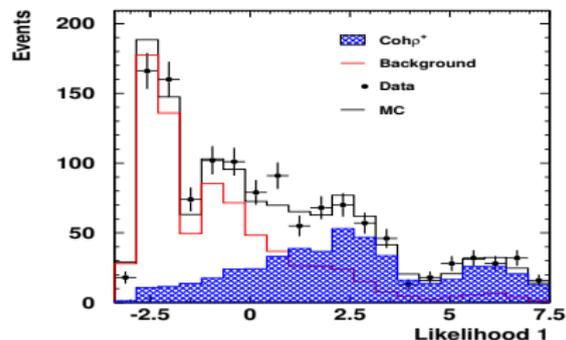


Input	Output
20,363	20144.2 ± 613.5

Input	Output
20,363	$20,396 \pm 613.8$

Mockdata test also shows that the acceptance and resolution smearing correction work.

Actual Data Analysis - LH/NN distribution



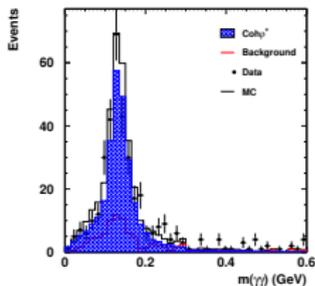
Algorithm	Background	Data	Efficiency	Coh ρ^+ Signal
LH	86.1	363	0.064	4318.8 ± 307.4
NN	76.1	356	0.065	4332.0 ± 319.4

Note: We do not apply a cut on $M_{\gamma\gamma}$ or $M_{\pi^+\gamma\gamma}$

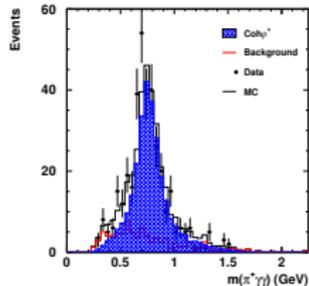
Kinematics in the signal region - MC agrees with Data reasonably well and consistent with $\text{Coh}\rho^+$

A Coherent Rho+ signal must pass four tests

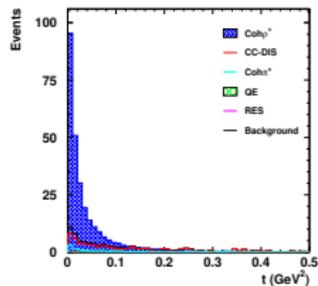
$M_{\gamma\gamma}$ should show π^0 structure



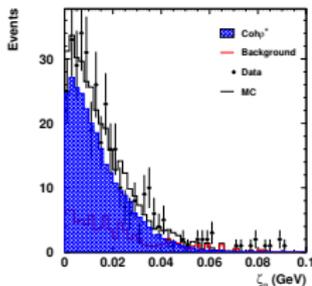
$M_{\pi^+\gamma\gamma}$ should show ρ^+ structure



t should show "coherence"



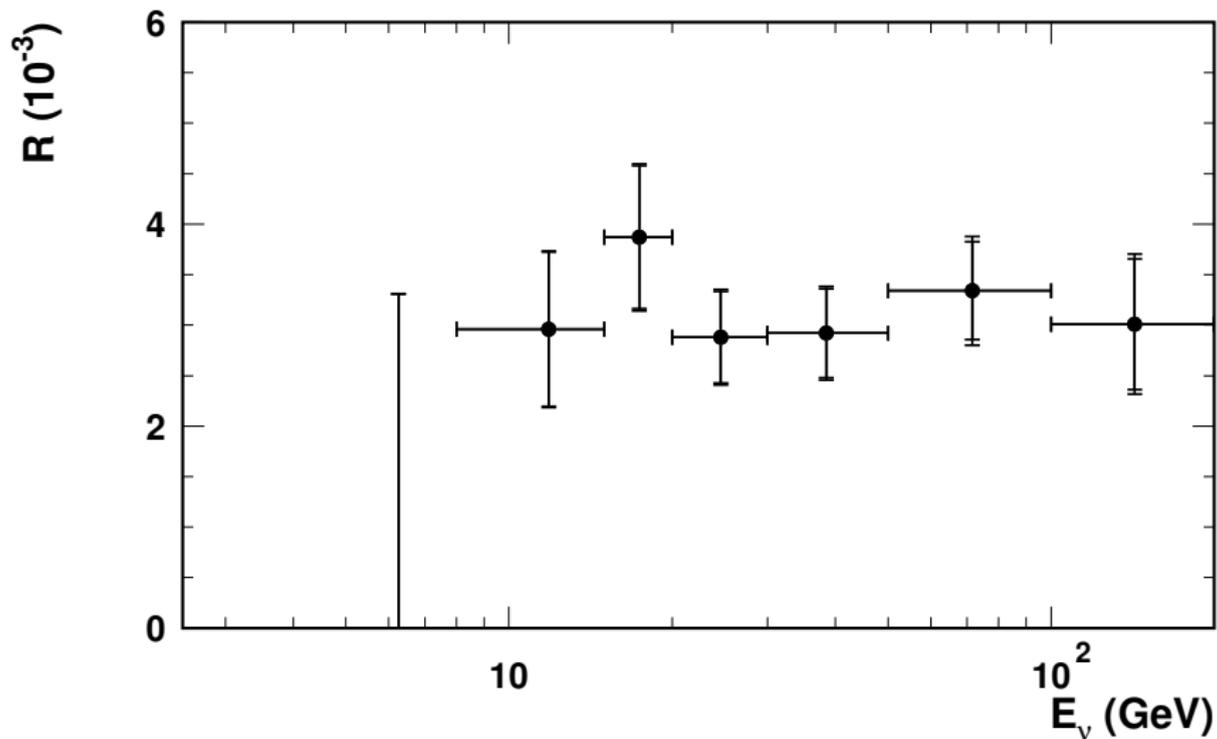
ρ^+ should be collinear with beam direction

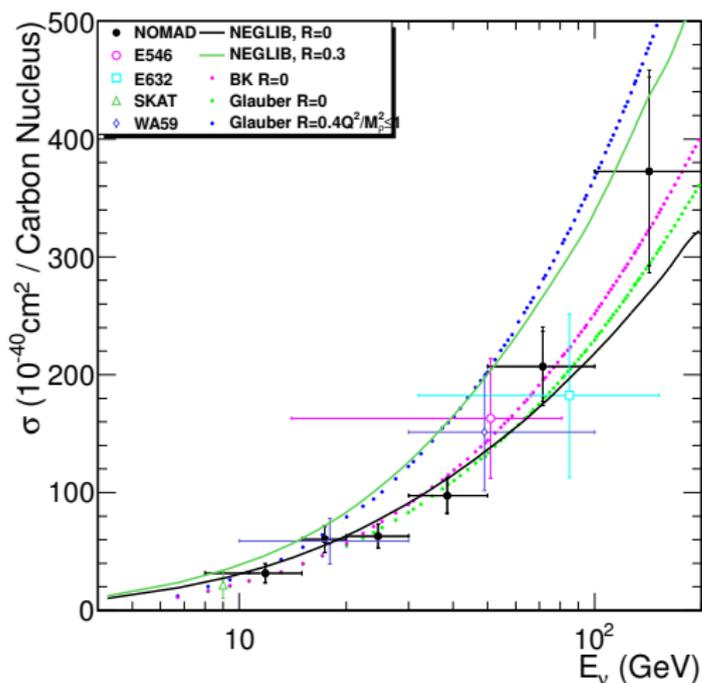


Systematics

Total overall systematic error - $\pm 3.9\%$

- Background normalization - $\pm 1.6\%$
 - Dominated by CC-DIS, use the control region in LH to get a normalization factor and error
- Absolute normalization - $\pm 2.5\%$
 - From inclusive CC cross section measurement
- Efficiency - $\pm 2.5\%$
 - Mockdata study - $< 1\%$
 - Vary LH-cuts, difference in LH .vs. NN - $\pm 1.6\%$
 - Vary the MC-parameters - $\pm 2.5\%$

Measurement of $N(\text{Coh}\rho^+)/N_{\text{CC}}$ as a function of E_ν 

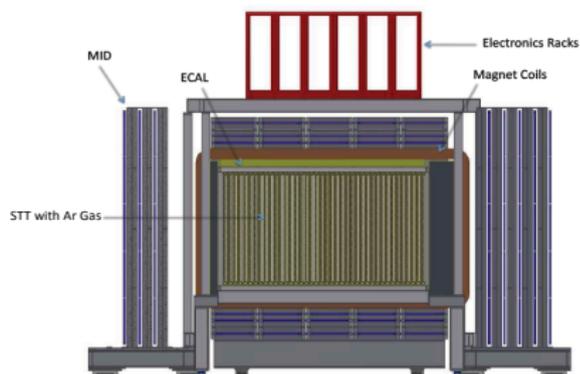
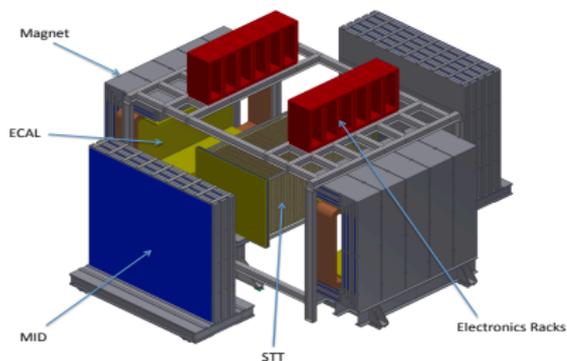
Measurement of $\sigma_{\text{Coh}\rho^+}$ as a function of E_ν 

NOMAD data favor the model with $R = 0$, i.e. there is little longitudinal contribution in $\text{Coh}\rho$ production

Sensitivity Study of Coherent-Meson Production in a Fine Grain Straw Tube Tracker (STT) - the proposed LBNE Near Detector

- The LBNE ND will have a much a higher resolution and statistics ($\times 50$) than NOMAD, but lower energy ($\sim 1/4$)

The proposed LBNE Near Detector - STT (Built on the NOMAD experience)



- Determination of the beam flux at the Near Site and the measurement of ν_e -appearance backgrounds (Primary purpose)
- Precision Standard Model neutrino physics measurements, such as precise measurement of the weak mixing angle

Performance Metric	STT
Tracking Detector Mass	7 tons
Vertex Resolution	0.1 mm
Angular Resolution	2 mrad
E_e Resolution	5%
E_μ Resolution	5%
$\nu_\mu/\bar{\nu}_\mu$ ID	YES
$\nu_e/\bar{\nu}_e$ ID	YES
NC π^0 /CCe Rejection	0.1%
NC γ /CCe Rejection	0.2%
CC μ /CCe Rejection	0.01%

Conclusion

- We have conducted a measurement of Coherent ρ^+ production using NOMAD data - a clear Coherent ρ^+ signal is observed
 - We observe - 4318.8 ± 307.4 (stat.) ± 168.4 (syst.) fully corrected Coherent ρ^+ events
 - The rate with respect to ν_μ -CC events (1.44 M) is $(3.00 \pm 0.24) \times 10^{-3}$
 - $R(\text{Coh}\rho^0/\text{Coh}\rho^+) = (634.5 \pm 146.3) / (4318.8 \pm 350.5) = 0.147 \pm 0.036$
- The observed rate and kinematics are consistent with theory (CVC and VMD)
- The analysis is largely data-driven - the backgrounds are constrained using control samples
- The knowledge from NOMAD analysis of the coherent meson studies is applicable on LBNE ND studies which will have a much a higher resolution and statistics, but lower energy, than NOMAD

Cross Section

$$\frac{d^3\sigma(\nu\mu\mathcal{A} \rightarrow \mu^-\rho^+\mathcal{A})}{dQ^2 d\nu dt} = \frac{G_F^2}{4\pi^2} \frac{f_\rho^2}{1-\epsilon} \frac{|q|}{E_\nu^2} \left[\frac{Q}{Q^2 + m_\rho^2} \right]^2 (1 + \epsilon R) \left[\frac{d\sigma^T(\rho^+\mathcal{A} \rightarrow \rho^+\mathcal{A})}{dt} \right] \quad (1)$$

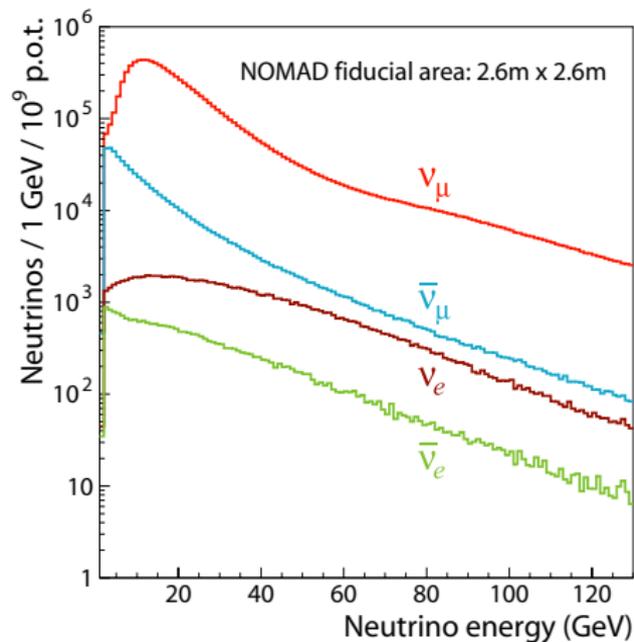
where G_F is the weak coupling constant, $Q^2 = -q^2 = -(k - k')^2$, $t = (p - p')^2$, $\nu = E_\nu - E_\mu$, $x = Q^2/(2\nu M)$, $y = \nu/E_\nu$, g_ρ is related to the ρ form-factor, the polarization parameter $\epsilon = \frac{4E_\nu E_\mu - Q^2}{4E_\nu E_\mu + Q^2 + 2\nu^2}$, and $R = \frac{d\sigma^L/dt}{d\sigma^T/dt}$ with σ^L and σ^T as the longitudinal and transverse ρ -nucleus cross sections. The ρ form factor f_ρ is related to the corresponding factor in charged-lepton scattering, $f_\rho^\pm = f_{\rho^0}^\gamma \sqrt{2} \cos\theta_C$, θ_C is the Cabibbo angle and $f_\rho^\gamma = m_\rho^2/\gamma_\rho$ is the coupling of ρ^0 to photon ($\gamma_\rho^2/4\pi = 2.4 \pm 0.1$).

Following the Rein-Sehgal model of meson-nucleus absorption,

$$\frac{d\sigma^T(\rho^+\mathcal{A} \rightarrow \rho^+\mathcal{A})}{dt} = \frac{\mathcal{A}^2}{16\pi} \sigma^2(hn) \exp(-b|t|) F_{abs} \quad (2)$$

where $\sigma(hn)$ is the 'hadron-nucleon' cross-section with the energy of the hadron $\simeq \nu$, $b = R^2/3$ such that $R = R_0 \mathcal{A}^{1/3}$, with $R_0 = 1.12 fm$ and the absorption factor $F_{abs} = 0.47 \pm 0.03$.

The SPS Beam



ν	ν/ν_μ
ν_μ	1.0
$\bar{\nu}_\mu$	0.025
ν_e	0.015
$\bar{\nu}_e$	0.0015

MC

- Total ν_μ -CC is normalized to 1.44 M
- QE is normalized to 33 k
- Resonance is normalized to 43 k ($\sim 15\%$ error)
- $\text{Coh}\pi^+$ is normalized to 10 k ($\sim 25\%$ error)

MC

- Deep Inelastic Scattering (DIS)
 - Modelled with the help of modified LEPTO 6.1 package
 - Production of all zoo of hadrons is simulated with help of JETSET 7.4
 - Structure functions are calculated for LO GRV 98 pdf according A. Bodek prescriptions
- Quasi-Elastic scattering (QE)
 - Based on the Smith-Moniz approach
 - The vector form-factors F_V and F_M are supposed to be well known (the GKex(05) parametrization)
 - The axial form-factor has the dipole form $F_A(Q^2) = F_A(0)[1 + Q^2/M_A^2]^{-2}$
- Resonance/single pion production
 - Based on ReinSehgal (RS) model
 - Set of 18th baryon resonances with masses below 2 GeV as in RS but with all relevant parameters updated according to the most recent PDG
 - Factors which were estimated in RS numerically are corrected by using the new data and a more accurate integration algorithm
- Coherent pion production
 - Based on Rein-Sehgal (RS) model
- Final state interactions
 - Modelled with the help of DPMJET package, based on the Formation Zone Intranuclear Cascade model