

Incoherent pion production in neutrino-nucleus scattering

E.Hernández¹, J. Nieves², M.J. Vicente Vacas³

¹ Universidad de Salamanca, Spain

² IFIC, Valencia, Spain

³ Universidad de Valencia, Spain

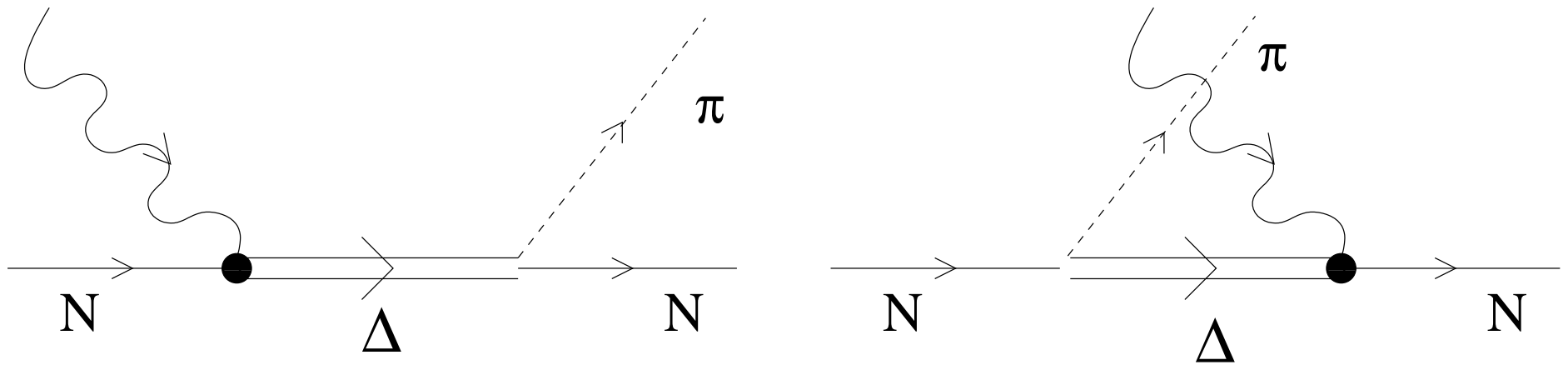
E. Hernández, J. Nieves and M.J. Vicente-Vacas, Physical Review D 87, 113009 (2013)

Outline of the talk

- Pion production model at the nucleon level
- Incoherent pion production
 - Pion production inside the nucleus
 - Medium modifications
 - Pion FSI
 - Results

Delta Pole Term for weak pion production off the nucleon

The dominant contribution for weak pion production at intermediate energies is given by the Δ pole mechanism



$N \rightarrow \Delta$ weak current I

$$\langle \Delta^+; p_\Delta = p + q | j_{cc^+}^\mu(0) | n; p \rangle = \cos \theta_C \bar{u}_\alpha(\vec{p}_\Delta) \Gamma^{\alpha\mu}(p, q) u(\vec{p})$$

$$\begin{aligned} & \Gamma^{\alpha\mu}(p, q) \\ &= \left[\frac{C_3^V}{M} (g^{\alpha\mu} \not{q} - q^\alpha \gamma^\mu) + \frac{C_4^V}{M^2} (g^{\alpha\mu} q \cdot p_\Delta - q^\alpha p_\Delta^\mu) + \frac{C_5^V}{M^2} (g^{\alpha\mu} q \cdot p - q^\alpha p^\mu) + C_6^V g^{\mu\alpha} \right] \gamma_5 \\ &+ \left[\frac{C_3^A}{M} (g^{\alpha\mu} \not{q} - q^\alpha \gamma^\mu) + \frac{C_4^A}{M^2} (g^{\alpha\mu} q \cdot p_\Delta - q^\alpha p_\Delta^\mu) + C_5^A g^{\alpha\mu} + \frac{C_6^A}{M^2} q^\mu q^\alpha \right] \end{aligned}$$

$N \rightarrow \Delta$ weak current II

- Vector form factors: determined from the analysis of photo and electroproduction

[O. Lalakulich *et al.*, Phys. Rev. D74, 014009 (2006)]

$$C_3^V = \frac{2.13}{(1 - q^2/M_V^2)^2} \cdot \frac{1}{1 - \frac{q^2}{4M_V^2}}, \quad C_4^V = \frac{-1.51}{(1 - q^2/M_V^2)^2} \cdot \frac{1}{1 - \frac{q^2}{4M_V^2}},$$

$$C_5^V = \frac{0.48}{(1 - q^2/M_V^2)^2} \cdot \frac{1}{1 - \frac{q^2}{0.776M_V^2}}, \quad C_6^V = 0 \text{ (CVC)}, \quad M_V = 0.84 \text{ GeV}$$

- Axial form factors:

Use Adler's model $C_4^A(q^2) = -\frac{C_5^A(q^2)}{4}, \quad C_3^A(q^2) = 0$

and PCAC $C_6^A(q^2) = C_5^A(q^2) \frac{M^2}{m_\pi^2 - q^2}$

and take (E.A. Paschos *et al.*, Phys. Rev. D69, 014013 (2004))

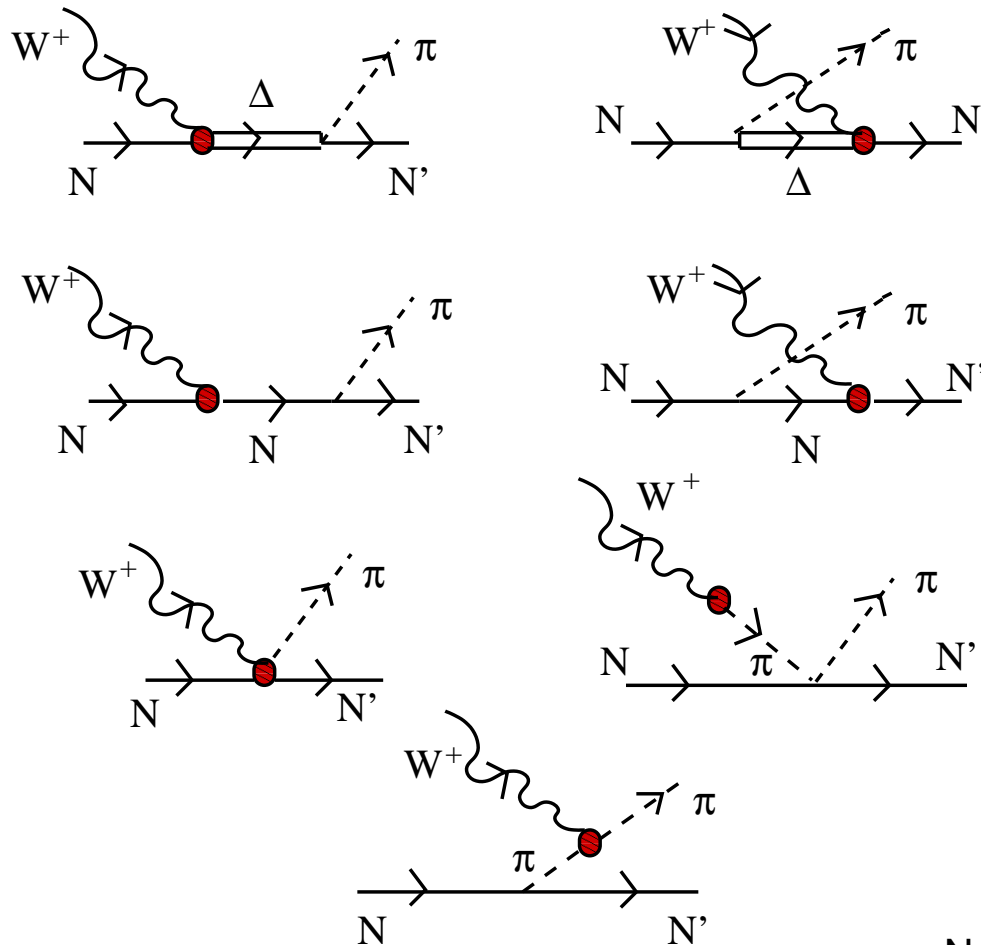
$$C_5^A(q^2) = \frac{C_5^A(0)}{(1 - q^2/M_{A\Delta}^2)^2} \cdot \frac{1}{1 - \frac{q^2}{3M_{A\Delta}^2}}$$

with $C_5^A(0) = 1.2$ (as given by the off-diagonal GTR) and $M_{A\Delta} = 1.05 \text{ GeV}$.

Background Terms

Our model in Phys. Rev. D 76, 033005 (2007) includes background terms required by chiral symmetry. To that purpose we use a SU(2) non-linear σ model Lagrangian.

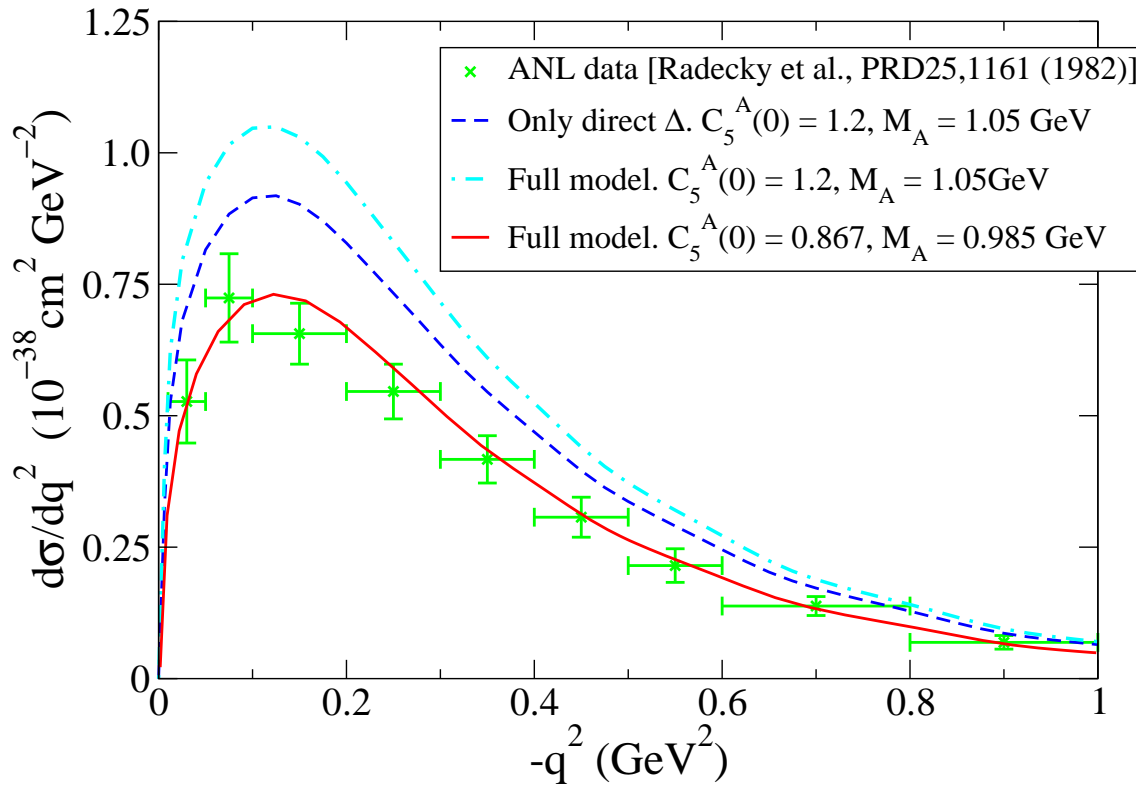
- No freedom in coupling constants
- We supplement it with well known form factors



$\nu_\mu p \rightarrow \mu^- p \pi^+$ reaction I

Flux averaged q^2 -differential $\nu_\mu p \rightarrow \mu^- p \pi^+$ cross section $\int_{M+m_\pi}^{1.4 \text{ GeV}} dW \frac{d\bar{\sigma}_{\nu\mu\mu^-}}{dq^2 dW}$

$\nu_\mu p \rightarrow \mu^- p \pi^+$ averaged over the ANL flux, $W < 1.4 \text{ GeV}$



$$C_5^A(q^2) = \frac{C_5^A(0)}{(1 - q^2/M_{A\Delta}^2)^2} \cdot \frac{1}{1 - \frac{q^2}{3M_{A\Delta}^2}}$$

Results suggested a refit of C_5^A

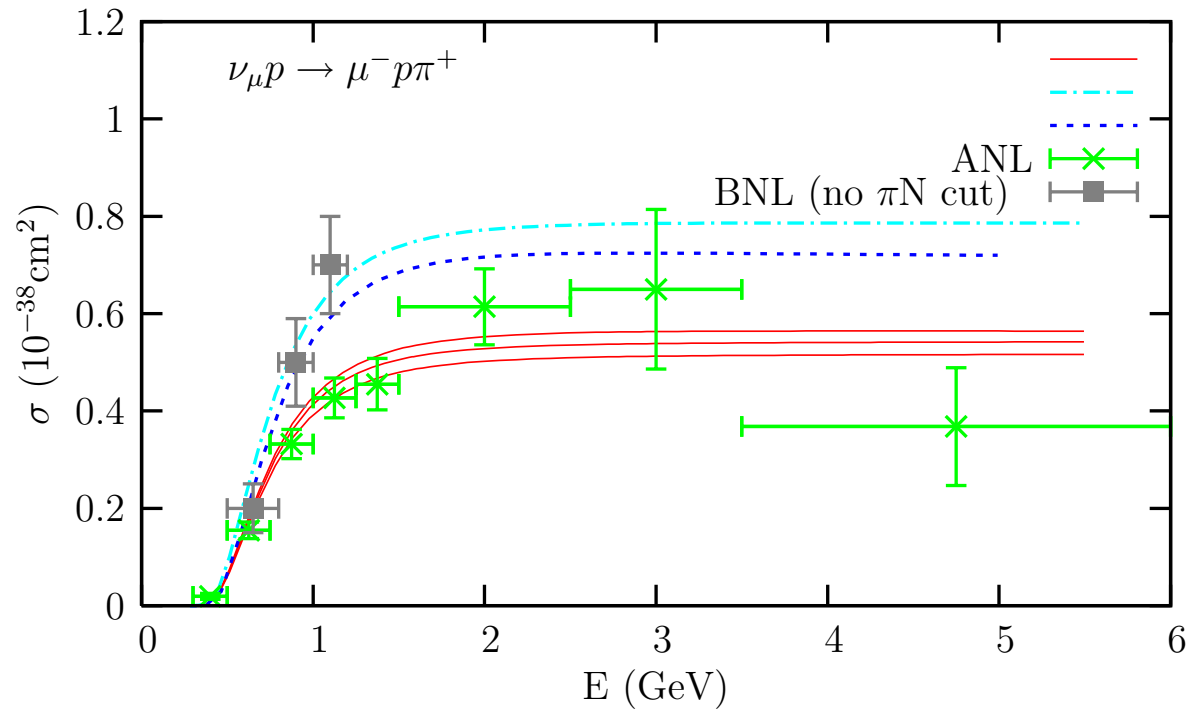
$$C_5^A(0) = 0.867 \pm 0.075$$

$$M_{A\Delta} = 0.985 \pm 0.082 \text{ GeV}$$

[Phys. Rev. D 76, 033005 (2007)]

ANL data seems to prefer $C_5^A(0)$ values smaller than the one provided by the off-diagonal GTR

$\nu_\mu p \rightarrow \mu^- p \pi^+$ reaction II



BNL data [T. Kitagaki et al., Phys. Rev. D34, 2554 (1986)]

Note BNL data prefers $C_5^A(0) = 1.2$

How to reconcile ANL & BNL data and still have $C_5^A(0) \approx 1.2$

K.M. Graczyk et al. [Phys. Rev. D 80, 093001 (2009)]

- ANL and BNL data were measured in deuterium
 - Deuteron effects were estimated by L. Alvarez-Ruso et al [Phys. Rev. C 59, 3386 (1999)] to reduce the cross section by 5-10% .
- Large uncertainties in the neutrino flux normalization, 10% for BNL data and 20% for ANL data.

They made a combined fit to both ANL&BNL data, assuming that only the Δ mechanism contributed, including deuteron effects, and treating flux uncertainties as systematic errors. They found

$$C_5^A(0) = 1.19 \pm 0.08, \quad M_{A\Delta} = 0.94 \pm 0.03 \text{ GeV}$$

for a pure dipole parameterization for $C_5^A(q^2)$.

A very good agreement with the off-diagonal GTR is found!

No background terms included

Background terms included

In our work in Phys. Rev. D 81, 085046 (2010) we included background terms in a combined fit to ANL & BNL data that took into account deuteron effects and flux normalization uncertainties.

We used a simpler dipole parameterization for $C_5^A(q^2)$

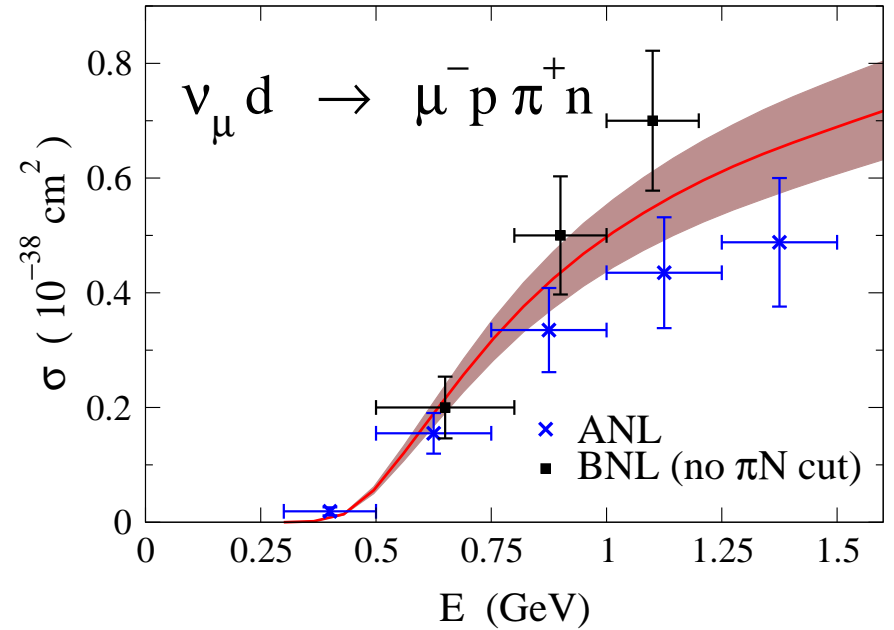
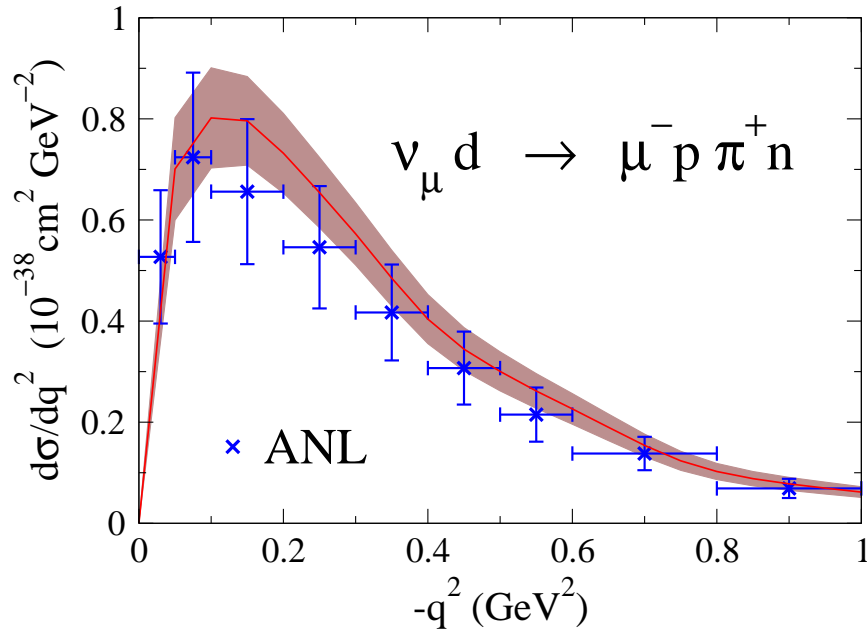
$$C_5^A(q^2) = \frac{C_5^A(0)}{(1 - q^2/M_{A\Delta}^2)^2}$$

Using Adler's constraints we got

$$C_5^A(0) = 1.00 \pm 0.11, \quad M_{A\Delta} = 0.93 \pm 0.07 \text{ GeV}$$

$C_5^A(0)$ compatible with its GTR value at the 2σ level.

Comparison with ANL & BNL data

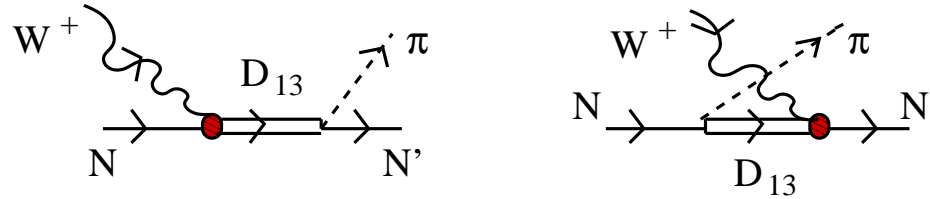


68% confidence level bands are shown.

The total experimental errors shown contain flux uncertainties that are considered as systematic errors and have been added in quadratures to the statistical ones.

Other resonances

In order to go to higher neutrino energies, we include in our model the $D_{13}(1520)$ resonance (isospin 1/2, spin 3/2) that, apart from the Δ , it gives the most important resonant contribution [T. Leitner et al., Phys. Rev. C 79, 034601 (2009)]



We adjust the πNN^* coupling to the $N^* \rightarrow N\pi$ width and get $g_D = 20 \text{ GeV}^{-1}$. GTR then fixes the value $C_5^A(0) = -2.1$ for the $W^+ n \rightarrow N^{*+}$ transition.

For the axial form factors we take [O. Lalakulich *et al.*, Phys. Rev. D74, 014009 (2006)]

$$C_3^A = C_4^A = 0, \quad C_5^A = \frac{-2.1}{(1 - q^2/M_A^2)^2} \frac{1}{1 - q^2/(3M_A^2)}, \quad C_6^A(q^2) = C_5^A(q^2) \frac{M^2}{m_\pi^2 - q^2}, \quad M_A = 1 \text{ GeV}$$

while for vectors we fit the form factor results in T. Leitner's thesis to get

$$C_3^V = \frac{-2.98}{[1 - q^2/(1.4M_V^2)]^2}, \quad C_4^V = \frac{4.21/D_V}{1 - q^2/(3.7M_V^2)}, \quad C_5^V = \frac{-3.13/D_V}{1 - q^2/(0.42M_V^2)}, \quad C_6^V = 0$$

with $M_V = 0.84 \text{ GeV}$ and $D_V = (1 - q^2/M_V^2)^2$

The inclusion of the $D_{13}(1520)$ does not affect the initial fit of the Δ form factors

● Having $I = 1/2$, it does not contribute to the $\nu_\mu p \rightarrow \mu^- p \pi^+$ channel

Incoherent pion production in nuclei.

Our starting point is the differential cross section at the nucleon level. For instance for CC processes and massless neutrinos we have

$$\frac{d\sigma(\nu N \rightarrow l^- N' \pi)}{d \cos \theta_\pi dE_\pi} = 2\pi \frac{G_F^2}{4\pi^2} \frac{|\vec{k}_\pi|}{|\vec{k}|} \frac{1}{4M} \frac{1}{(2\pi)^3} \int d\Omega' dE' |\vec{k}'| \frac{1}{2E_{N'}} \delta(E_N + q^0 - E_\pi - E_{N'}) \mathcal{L}_{\mu\sigma} \mathcal{W}^{\mu\sigma}$$

with

$$q = k - k', \quad E_{N'} = \sqrt{M^2 + (\vec{p}_N + \vec{q} - \vec{k}_\pi)^2}$$

$$\mathcal{L}_{\mu\sigma} = k_\mu k'_\sigma + k_\sigma k'_\mu - k \cdot k' g_{\mu\sigma} + i\epsilon_{\mu\sigma\alpha\beta} k'^\alpha k^\beta$$

$$\mathcal{W}^{\mu\sigma}(p_N, q, k_\pi) = \overline{\sum_{\text{spins}}} \langle N' \pi | j_{CC}^\mu(0) | N \rangle \langle N' \pi | j_{CC}^\sigma(0) | N \rangle^*$$

For incoherent production on a nucleus we have to sum over all nucleons in the nucleus.

Incoherent pion production in nuclei.

We assume the nucleus can be described by its density and we shall use the local density approximation

The cross section at the nucleus level for initial pion production (prior to any FSI) is then

$$\frac{d\sigma}{d \cos \theta_\pi dE_\pi} = \int d^3 r \sum_{N=n,p} 2 \int \frac{d^3 p_N}{(2\pi)^3} \theta(E_F^N(r) - E_N) \theta(E_N + q^0 - E_\pi - E_F^{N'}(r)) \frac{d\sigma(\nu N \rightarrow l^- N' \pi)}{d \cos \theta_\pi dE_\pi}$$

To compare with experiment, we have to convolute it with the neutrino flux $\Phi(|\vec{k}|)$

$$\begin{aligned} \frac{d\sigma}{d \cos \theta_\pi dE_\pi} &= \int d|\vec{k}| \Phi(|\vec{k}|) 4\pi \int dr r^2 \sum_{N=n,p} 2 \int \frac{d^3 p_N}{(2\pi)^3} \theta(E_F^N(r) - E_N) \theta(E_N + q^0 - E_\pi - E_F^{N'}(r)) \\ &\quad \times \frac{d\sigma(\nu N \rightarrow l^- N' \pi)}{d \cos \theta_\pi dE_\pi} \end{aligned}$$

From there we obtain

$$\frac{d\sigma}{d|\vec{k}| 4\pi r^2 dr d \cos \theta_\pi dE_\pi} = \Phi(|\vec{k}|) \sum_{N=n,p} 2 \int \frac{d^3 p_N}{(2\pi)^3} \theta(E_F^N(r) - E_N) \theta(E_N + q^0 - E_\pi - E_F^{N'}(r)) \frac{d\sigma(\nu N \rightarrow l^- N' \pi)}{d \cos \theta_\pi dE_\pi}$$

What else is left to do?

- Medium effects in the production process.
- Final state interaction of the outgoing pion.

Incoherent pion production in nuclei.

Prior to that, there is an approximation in the evaluation of $\frac{d\sigma}{d|\vec{k}| 4\pi dr d\cos\theta_\pi dE_\pi}$.

Doing the d^3p_N integral first we have (We define $Q = q - k_\pi$ and refer the nucleon polar angles to the \vec{Q} axis)

$$\begin{aligned} & \int_{-1}^1 d\cos\theta_N \int_0^{2\pi} d\varphi_N \int_M^\infty |\vec{p}_N| E_N dE_N \theta(E_F^N - E_N) \theta(E_N + Q^0 - E_F^{N'}) \\ & \times \frac{1}{E_N E_{N'}} \delta(E_N + Q^0 - E_{N'}) \mathcal{W}^{\mu\sigma}(p_N, q, k_\pi) \\ & = \frac{\theta(-Q^2)\theta(Q^0)\theta(E_F^N - \mathcal{E})}{|\vec{Q}|} \int_0^{2\pi} d\varphi_N \int_{\mathcal{E}}^{E_F^N} dE_N \mathcal{W}^{\mu\sigma}(p_N, q, k_\pi)|_{\cos\theta_N^0} \end{aligned}$$

where

$$\cos\theta_N^0 = \frac{Q^2 + 2E_N Q^0}{2|\vec{p}_N||\vec{Q}|}, \quad E' = \frac{-Q^0 + |\vec{Q}|\sqrt{1 - 4M^2/Q^2}}{2}, \quad \mathcal{E} = \max\{M, E_F^{N'} - Q^0, E'\}$$

Taking an average $\tilde{\varphi}_N$, \tilde{E}_N and the corresponding value for $\cos\theta_N^0$ in $\mathcal{W}^{\mu\sigma}(p_N, q, k_\pi)$ we have

$$\approx 2\pi \frac{(E_F^N - \mathcal{E})\mathcal{W}^{\mu\sigma}(\tilde{p}_N, q, k_\pi)}{|\vec{Q}|} \theta(-Q^2)\theta(Q^0)\theta(E_F^N - \mathcal{E})$$

Incoherent pion production in nuclei. Medium corrections

Δ properties are strongly modified in the nuclear medium.

Its imaginary part is modified due

- Pauli blocking of the final nucleon affects the free width.
- In medium modification of the pionic decay width others than Pauli blocking
- Absorption processes $\Delta N \rightarrow NN$ and $\Delta NN \rightarrow NNN$.

We thus modify the Δ propagator of the direct Δ contribution approximating

$$\frac{1}{p_{\Delta}^2 - M_{\Delta}^2 + iM_{\Delta}\Gamma_{\Delta}} \approx \frac{1}{\sqrt{p_{\Delta}^2 + M_{\Delta}}} \frac{1}{\sqrt{p_{\Delta}^2 - M_{\Delta} + i\Gamma_{\Delta}/2}}$$

and substituting

$$\frac{\Gamma_{\Delta}}{2} \rightarrow \frac{\Gamma_{\Delta}^{\text{Pauli}}}{2} - \text{Im} \Sigma_{\Delta}$$

while keeping M_{Δ} in the particle propagator unchanged.

Incoherent pion production in nuclei. Medium corrections

The evaluation of $\text{Im } \Sigma_{\Delta}$ was done by E. Oset and L.L. Salcedo [Nucl. Phys. A 468, 631 (1987)].

The imaginary part can be parameterized as

$$-\text{Im } \Sigma_{\Delta} = C_Q \left(\frac{\rho}{\rho_0} \right)^{\alpha} + C_{A2} \left(\frac{\rho}{\rho_0} \right)^{\beta} + C_{A3} \left(\frac{\rho}{\rho_0} \right)^{\gamma}$$

- The C_Q term corrects the pion production in the medium.
- The C_{A2} term gives rise to W absorption by two nucleons $W^*NN \rightarrow NN$.
- The C_{A3} term gives rise to W absorption by three nucleons $W^*NNN \rightarrow NNN$.

Not only the Δ propagator is modified, but we have a new contribution to pion production, corresponding to the C_Q piece, that have to be added incoherently. We do this in a approximate way taking as amplitude square for this process the one for the ΔP contribution multiplied by

$$\frac{C_Q (\rho/\rho_0)^{\alpha}}{\Gamma_{\Delta}^{\text{free}}/2}$$

Incoherent pion production in nuclei. Final state interaction

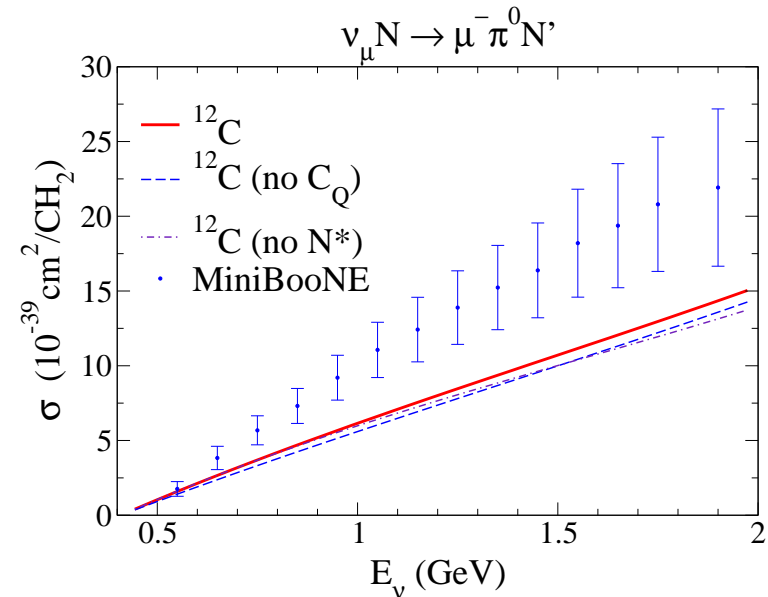
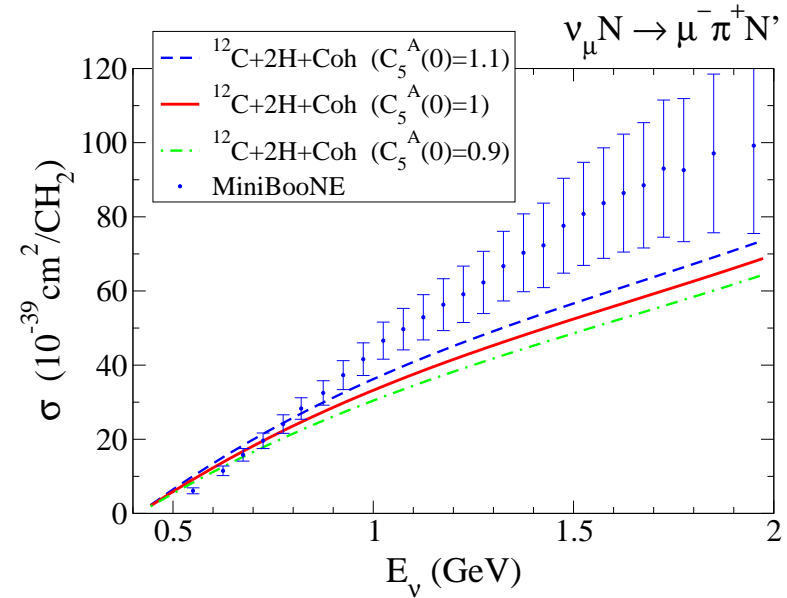
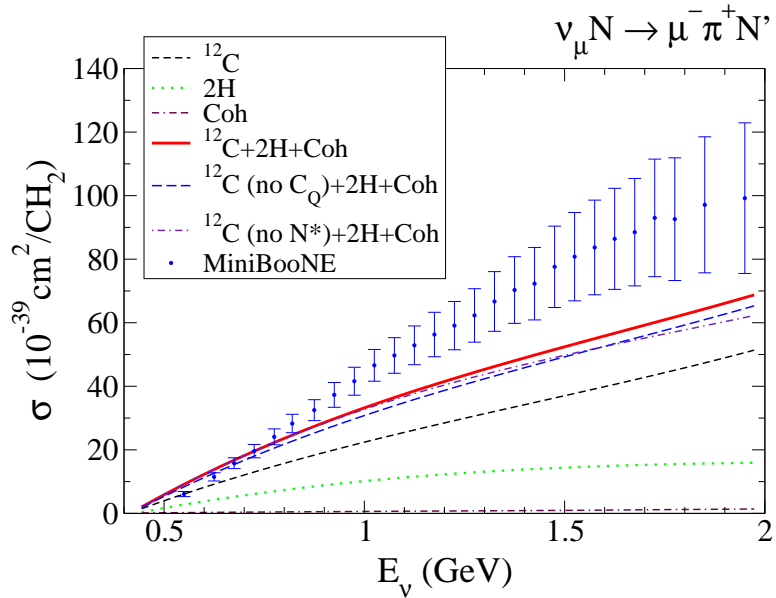
Once the pions are produced, we follow their path on its way out of the nucleus.

We use, with slight modifications, the model of L.L. Salcedo et al. [Nuc. Phys. A484, 557 (1988)]

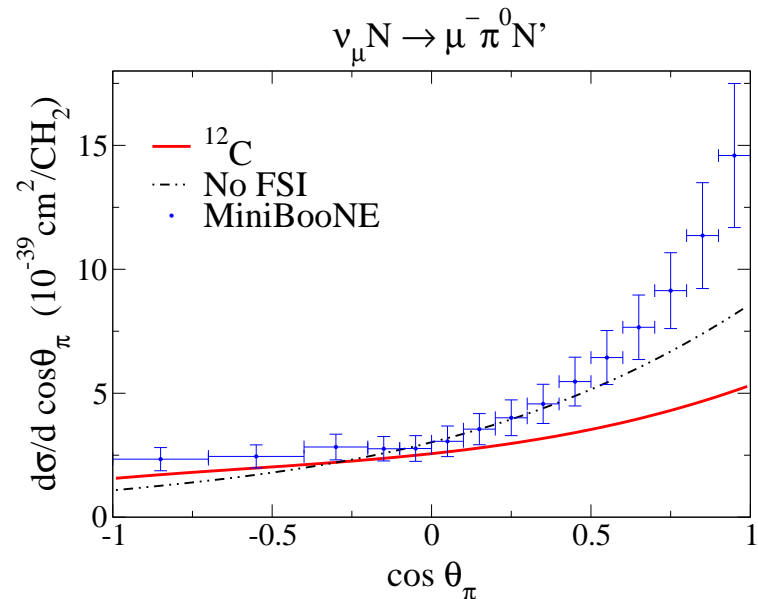
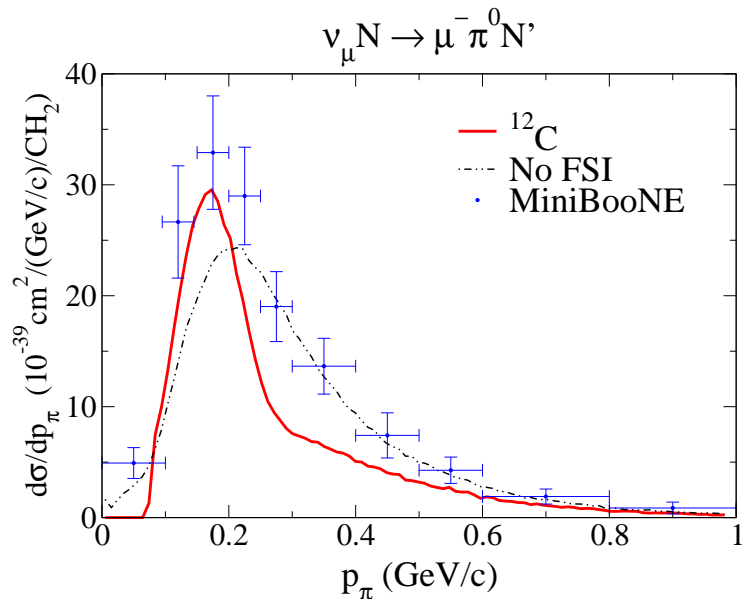
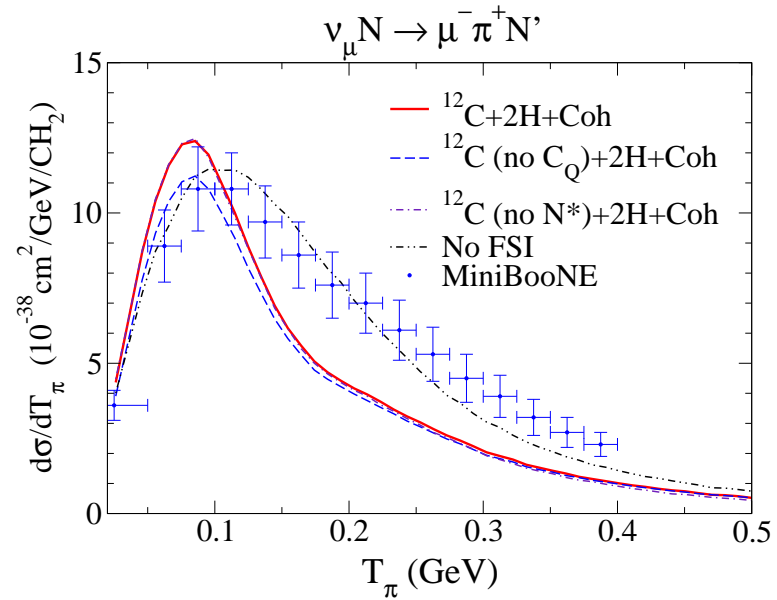
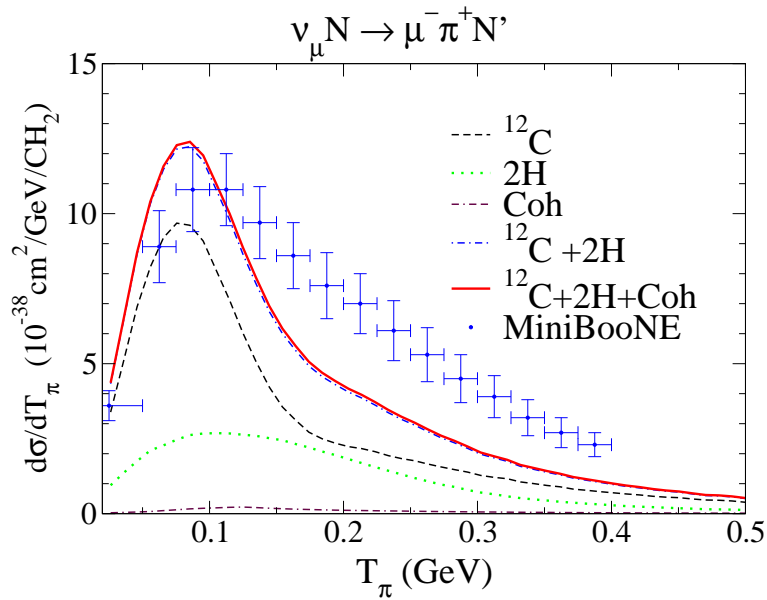
- P-wave and S-wave pion absorption.
- P-wave (mediated by Δ production) quasielastic scattering on a nucleon.
 - Pions change energy and direction.
 - Pions could change charge.
- Pion propagate on straight lines in between collisions.

Besides, coherent production is possible in some channels. For that we use the model in J.E. Amaro et al, Phys. Rev. D 79, 013002 (2009), but with the new form factors described above.

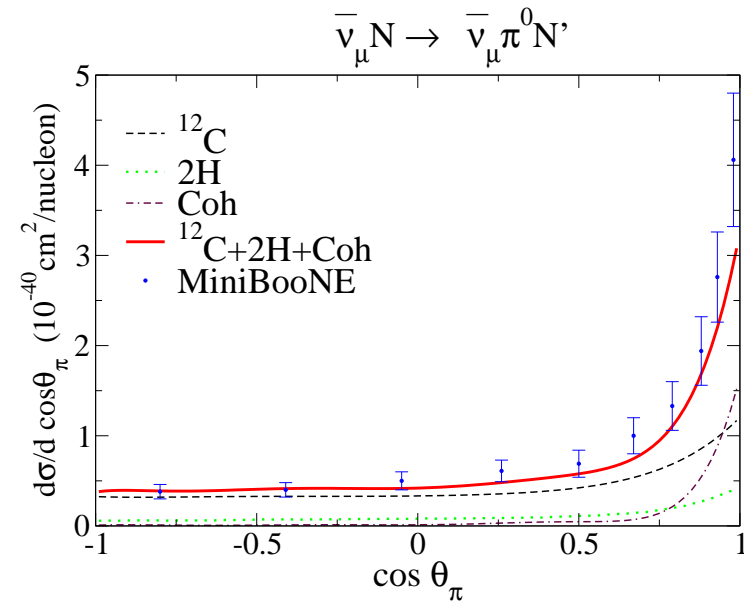
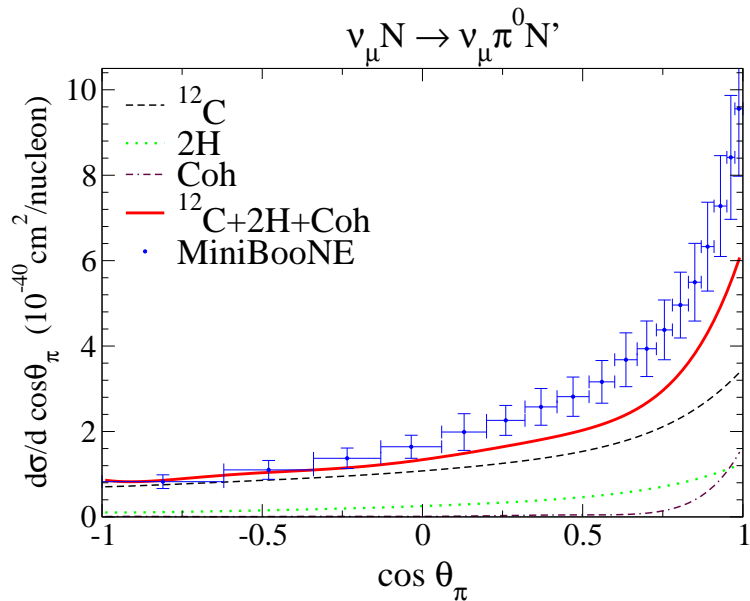
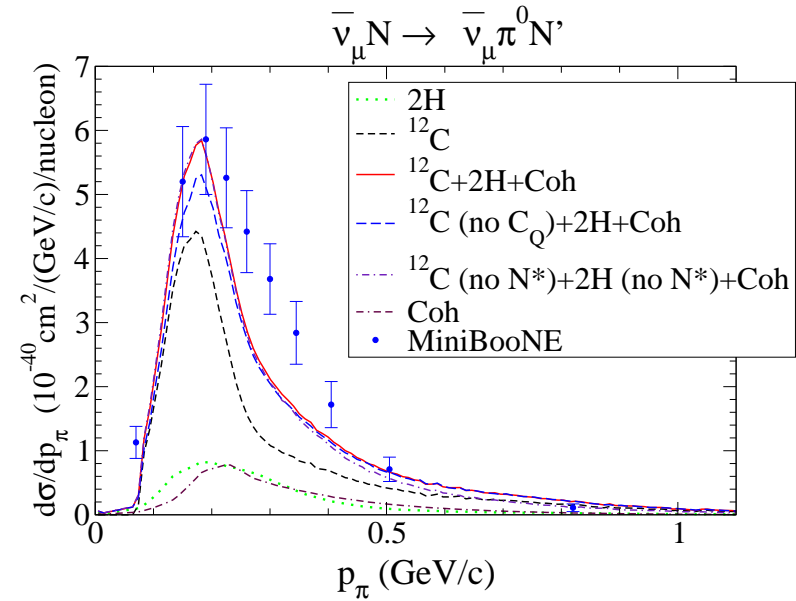
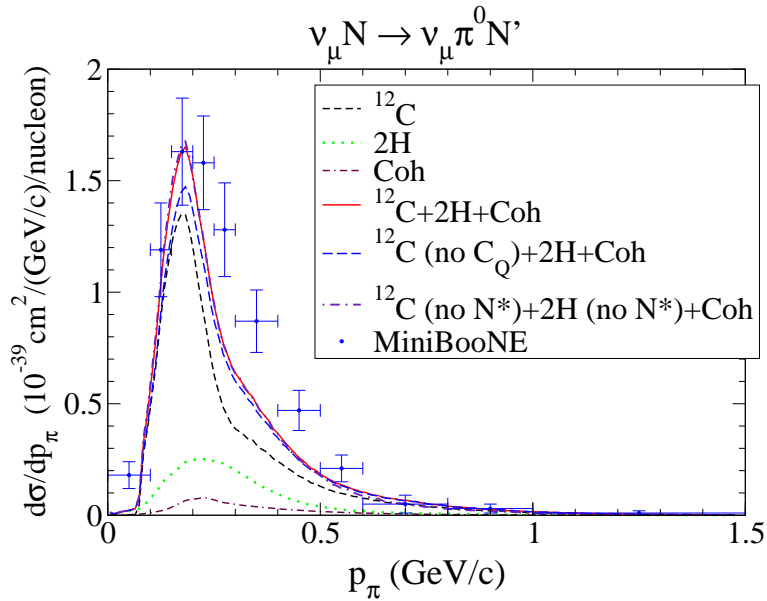
Incoherent pion production in nuclei. CC Results



Incoherent pion production in nuclei. CC Results



Incoherent pion production in nuclei. NC Results



Summary

- I have shown the ingredients of the Monte Carlo program we have developed to describe incoherent pion production in nuclei
 - Microscopic model for pion production on the free nucleon modified by
 - The presence of the nuclear medium
 - Δ propagator is modified inside the medium
 - New net contribution to pion decay due to the in medium modification of the pionic width of the Δ
 - The inclusion of a new resonance contribution with small effects on the cross sections
 - Simulation of the pion's path on its way out of the nucleus
 - Absorption
 - Quasielastic scattering
- Our results show a deficit of high energy forward pions when compared to experiment
- MiniBooNE data seems to prefer $C_5^A(0)$ values close to the PCAC prediction (≈ 1.16)