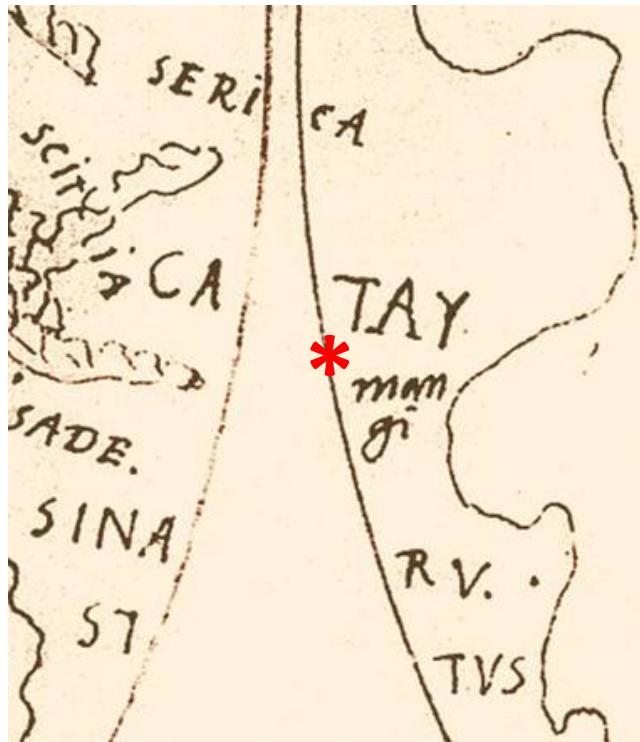


# Neutrino Physics – Theory and Phenomenology



Serica (*Land of Silk*)

Catay (*Northern China*)

Mangi (*Southern China*)

Sinaru[m] Situs (*Chinese Land*)

\* We are here

Elvio Lisi  
INFN, Bari, Italy

# Prologue: 500 years ago (A.D. ~ 1514)



Northern hemisphere

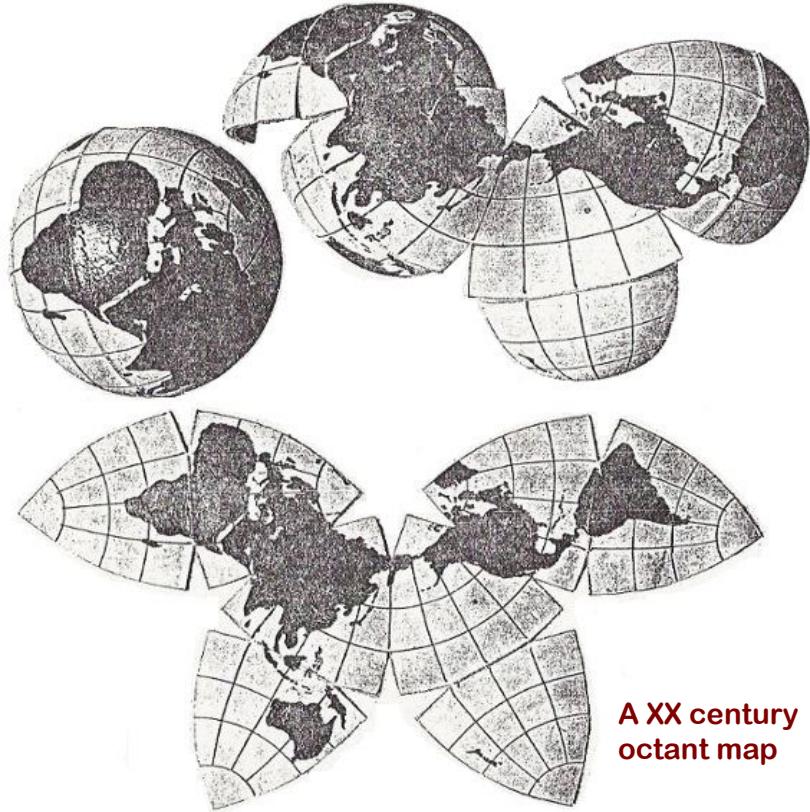
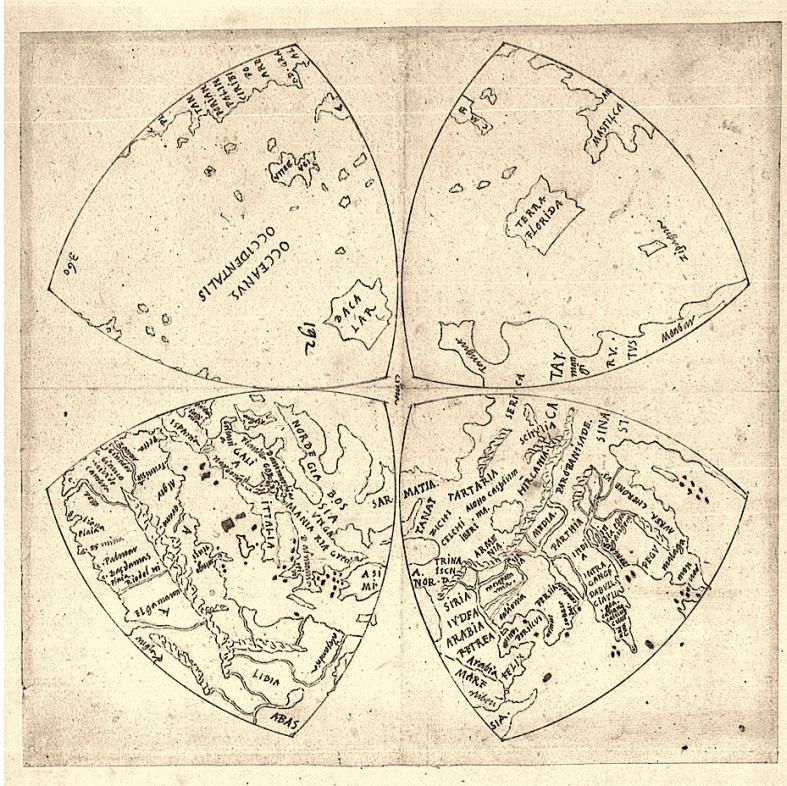


Southern hemisphere

A remarkable world map by Leonardo da Vinci...

[Royal Library, Windsor Collection. Executed by one of Leonardo's workshop assistants.]

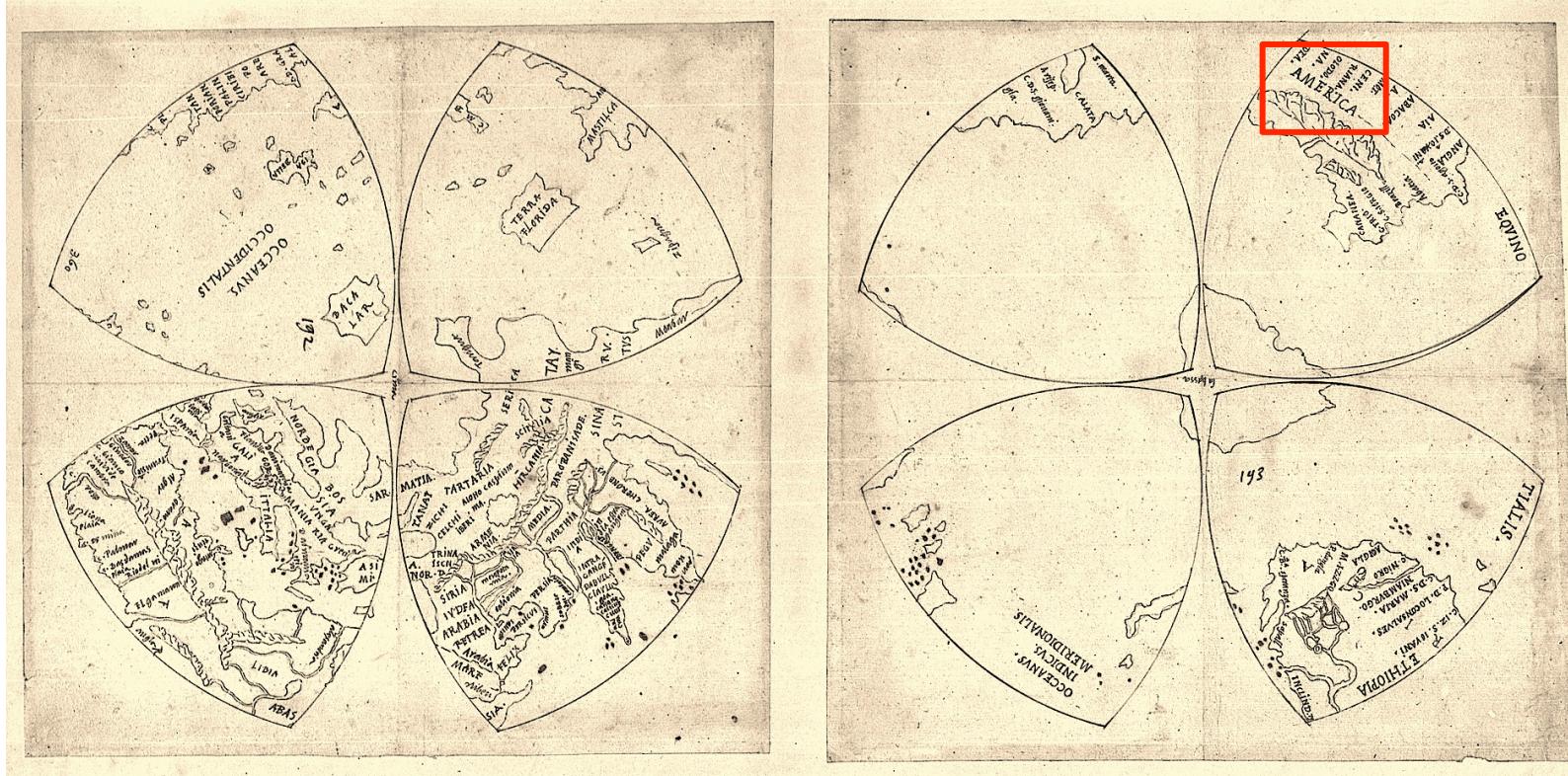
# Earliest known world map ...



A XX century  
octant map

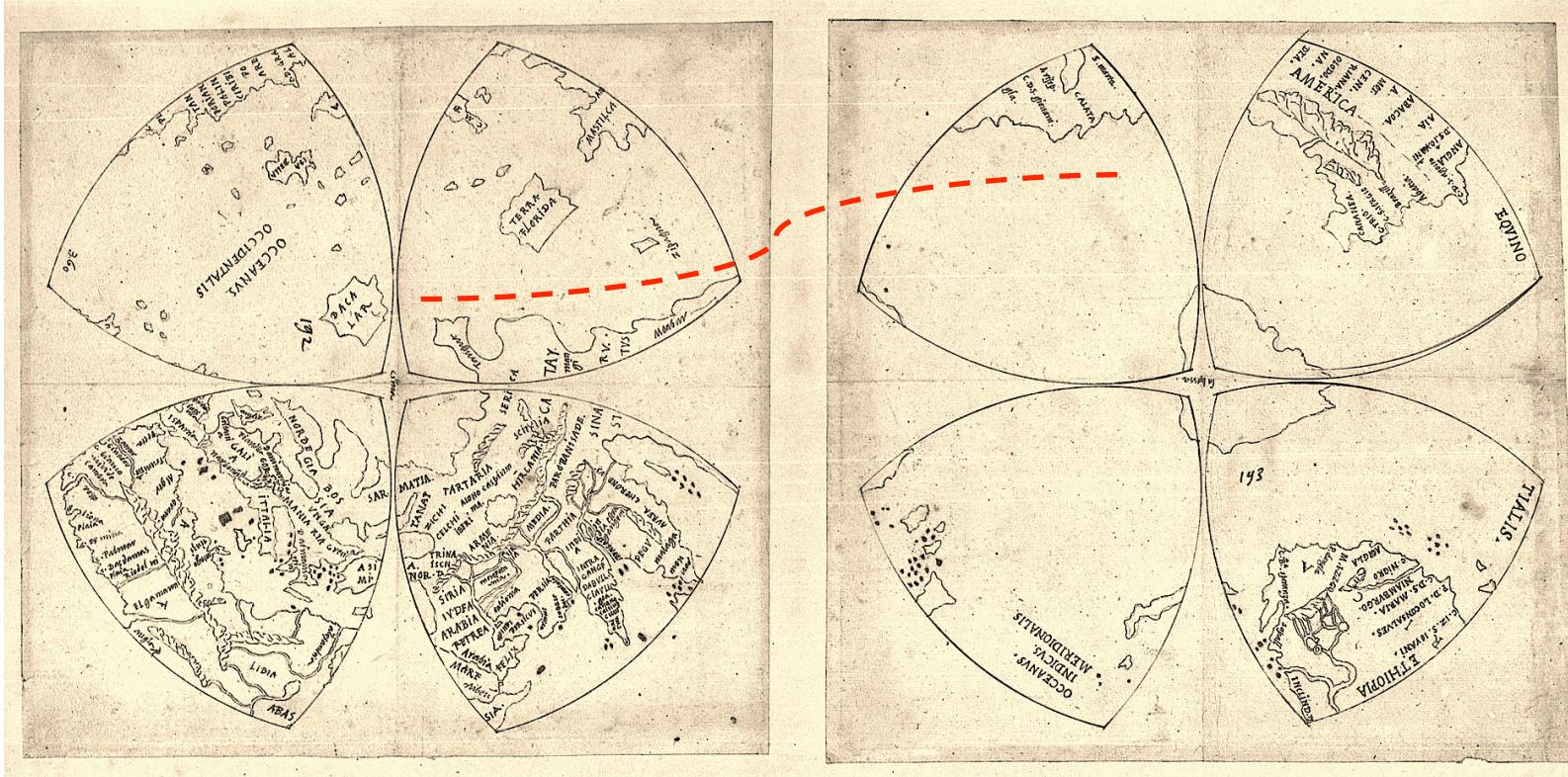
... made with octant projections

# Earliest known world map ...



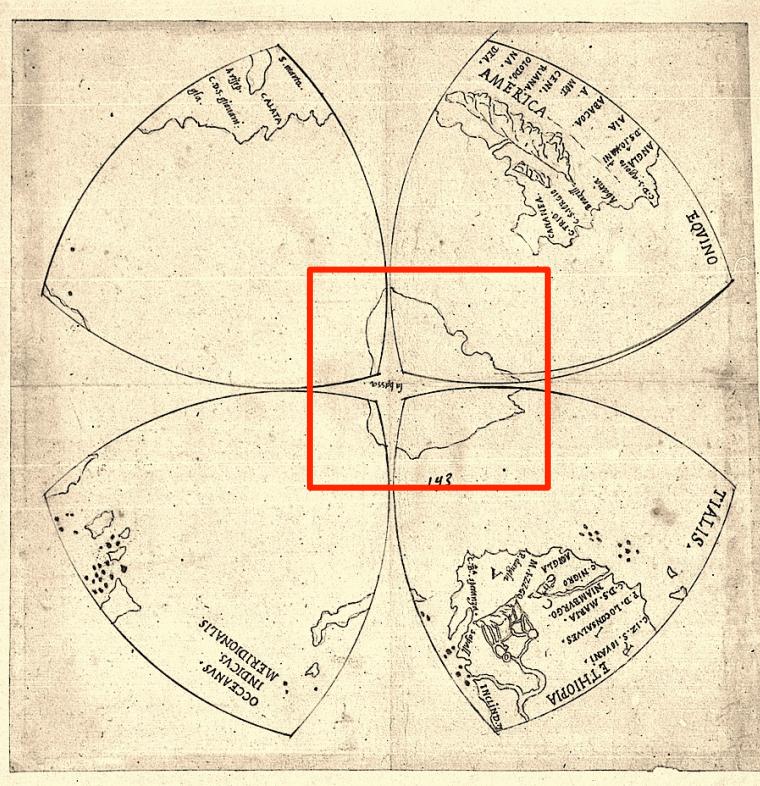
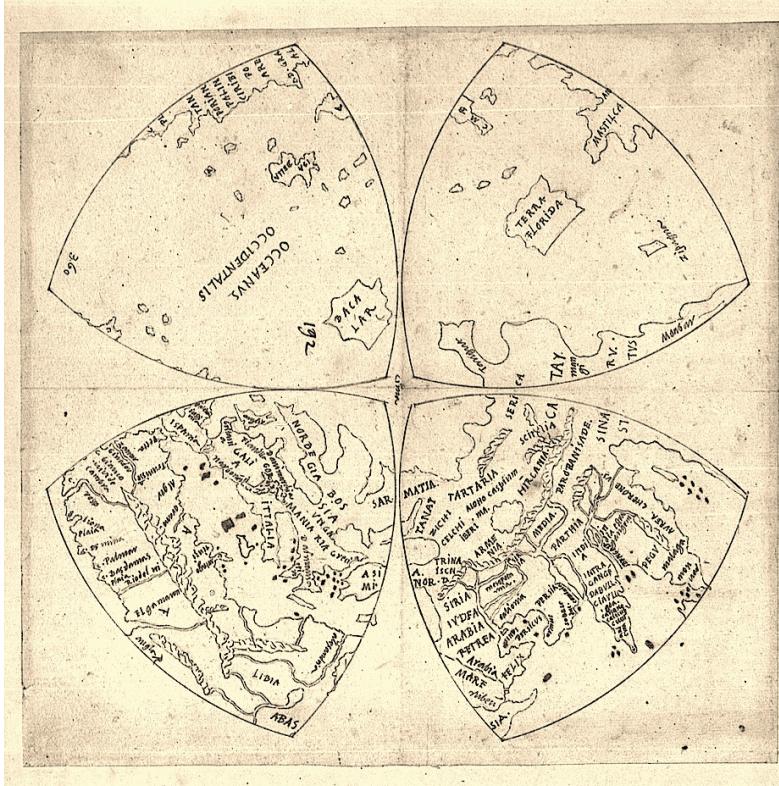
... made with octant projections  
... showing the name “America”

# Earliest known world map ...



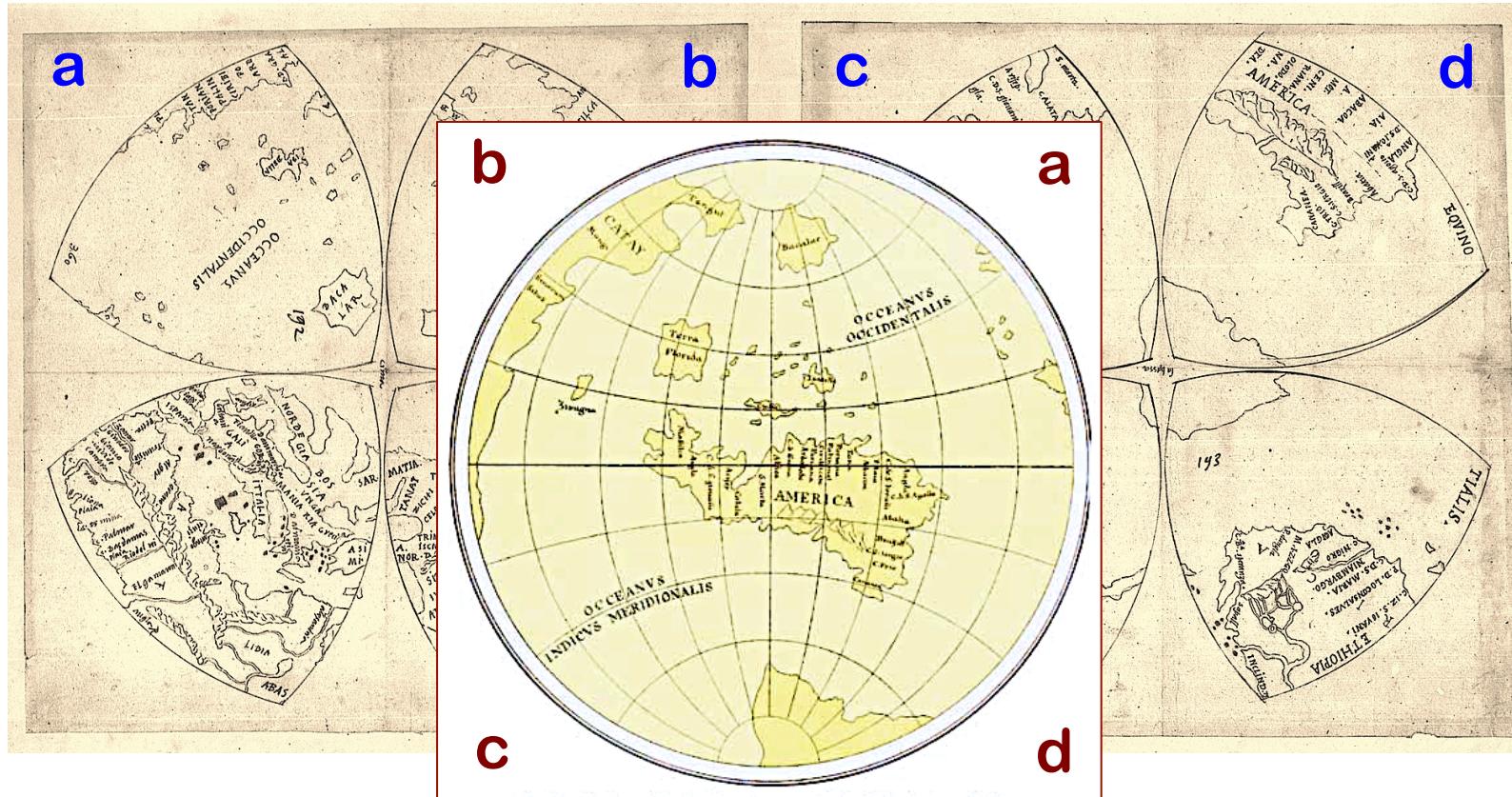
... made with octant projections  
... showing the name “America”  
... with America’s west coast disconnected from Asia

# Earliest known world map ...



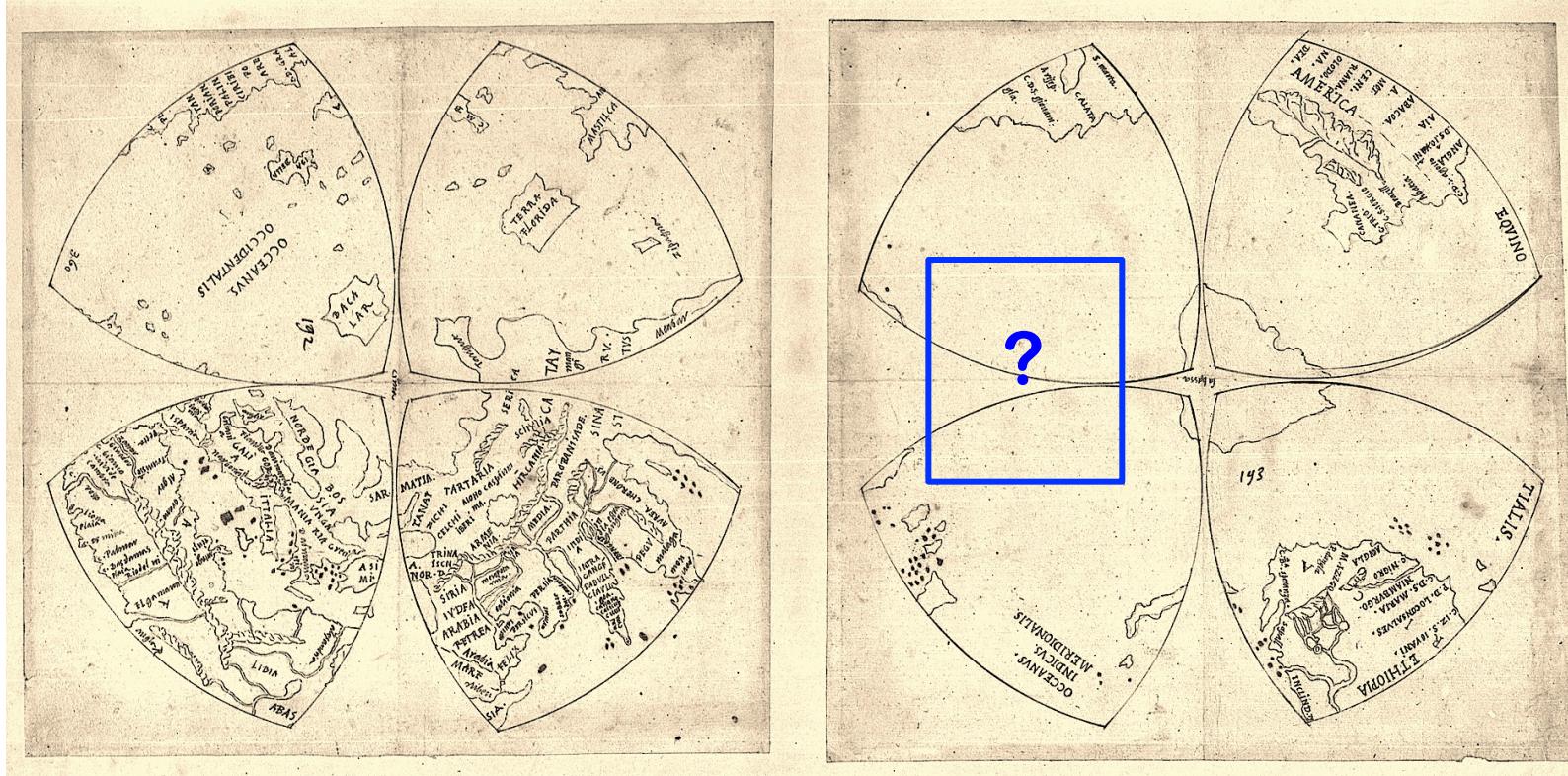
... made with octant projections  
... showing the name “America”  
... with America’s west coast disconnected from Asia  
... indicating a large Southern continent

# But, A.D. 1514 too early to...



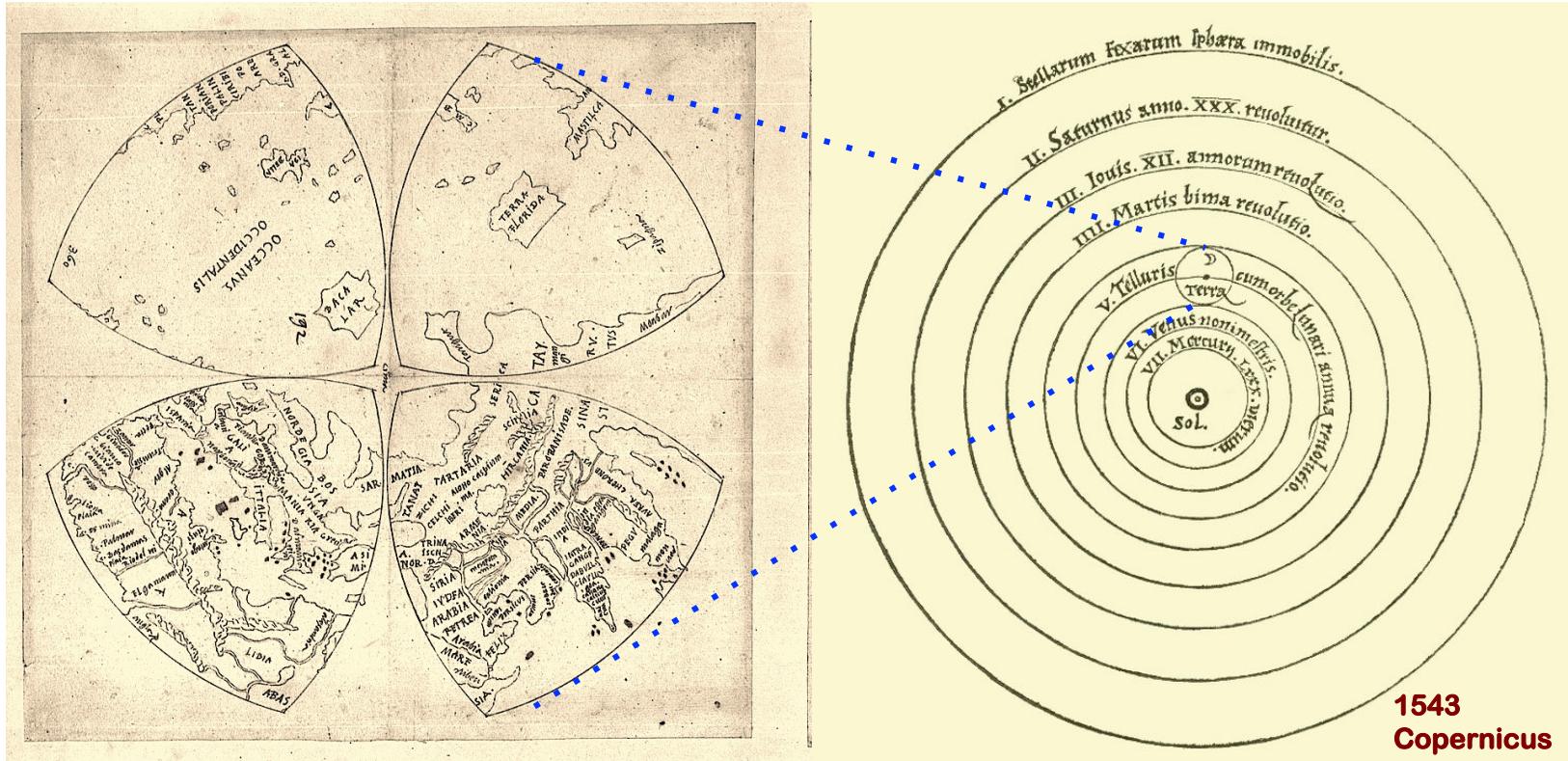
... avoid strong mapping distortions and biases

# But, A.D. 1514 too early to...



... avoid strong mapping distortions and biases  
... know about Australian continent (~ 90 years later)

# But, A.D. 1514 too early to...



1543  
Copernicus

- ... avoid strong mapping distortions and biases
- ... know about Australian continent (~ 90 years later)
- ... know about a larger world picture (~ 30 years later)

500 years later...

...we are in a similar situation in neutrino  
(and particle) physics:

- being excited by recent discoveries
- mapping (quasi)known lands (with biases?)
- planning expeditions to unknown lands
- trying to find a larger “world picture”

Theory may give some guidance in this  
(probably) long and difficult enterprise,  
largely driven by new experiments.

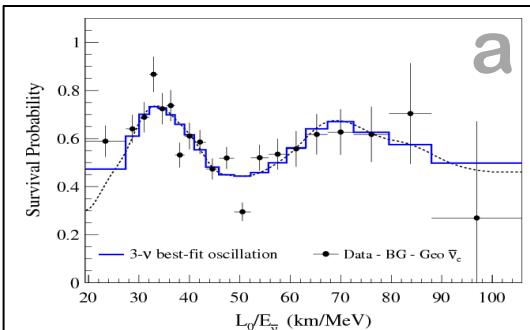
## TALK OUTLINE:

- being excited by recent discoveries
- mapping (quasi)known lands (with biases?)
- planning expeditions to unknown lands
- trying to find a larger “world picture”

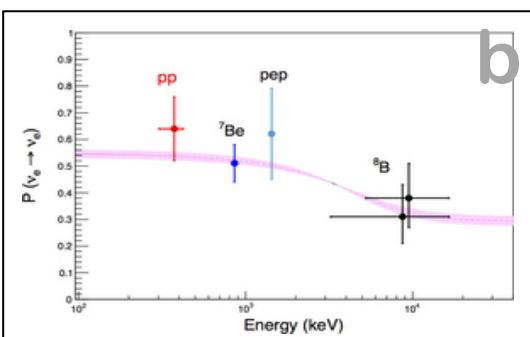
...charting the neutrino world...

# Recent discoveries: $\alpha \rightarrow \beta$ oscillations in vacuum and matter

$e \rightarrow e$



$e \rightarrow e$

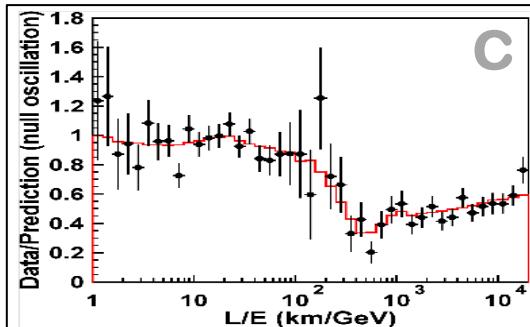


Data from various types of neutrino experiments: (a) solar, (b) long-baseline reactor, (c) atmospheric, (d) long-baseline accelerator, (e) short-baseline reactor, (f,g) long baseline accelerator (and, in part, atmospheric).

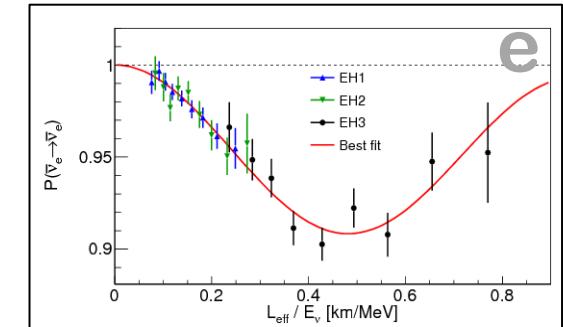
(a) KamLAND [plot]; (b) Borexino [plot], Homestake, Super-K, SAGE, GALLEX/GNO, SNO; (c) Super-K atmosph. [plot], MACRO, MINOS etc.; (d) T2K (plot), MINOS, K2K; (e) Daya Bay [plot], RENO, Double Chooz; (f) T2K [plot], MINOS; (g) OPERA [plot], Super-K atmospheric.

See next talks by Jung, Shiozawa, Cao

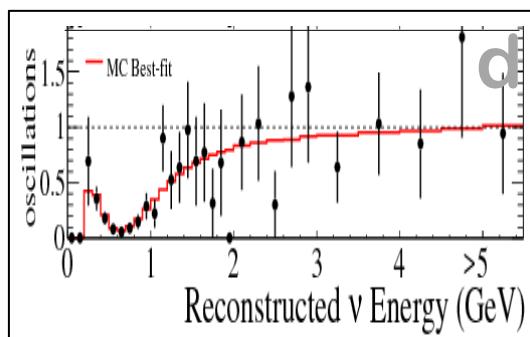
$\mu \rightarrow \mu$



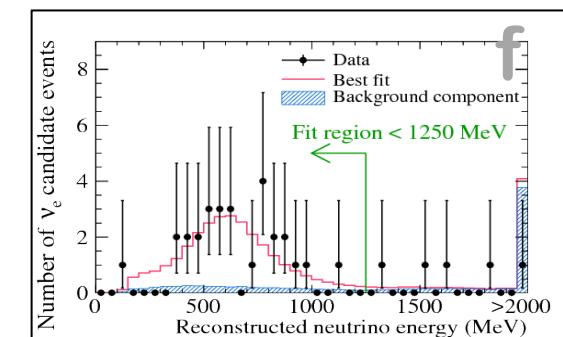
$e \rightarrow e$



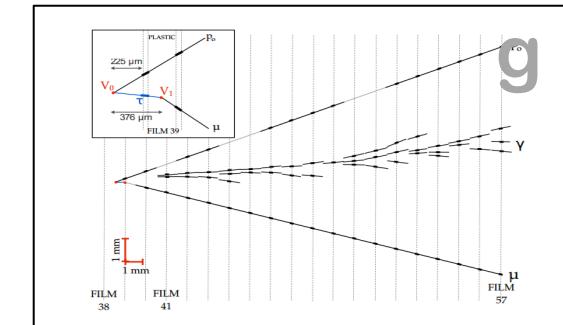
$\mu \rightarrow \mu$



$\mu \rightarrow e$

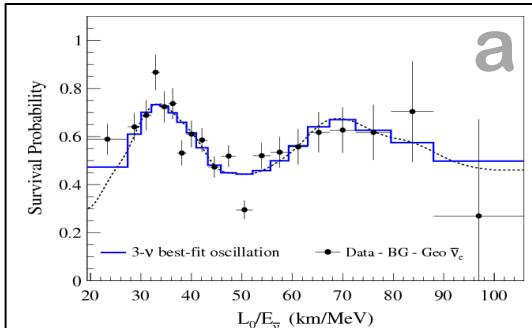


$\mu \rightarrow \tau$

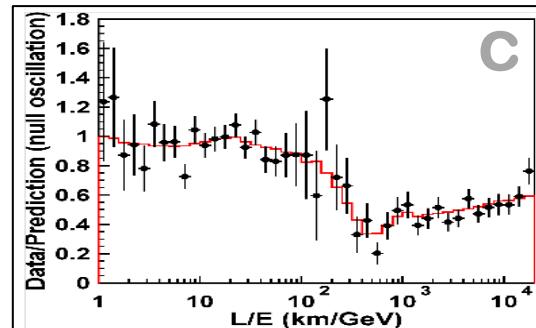


# Can be charted in a simple 3ν theoretical framework

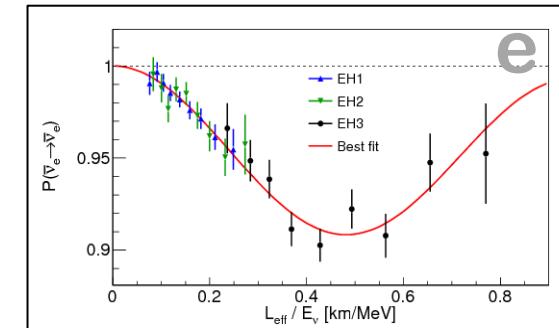
$e \rightarrow e$  ( $\delta m^2$ ,  $\theta_{12}$ )



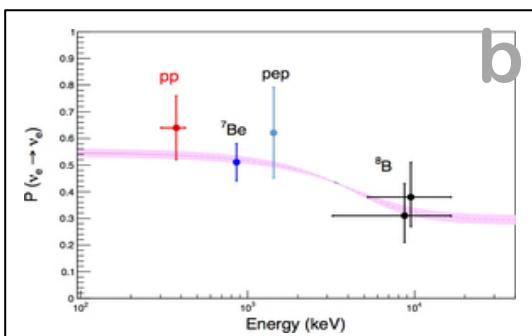
$\mu \rightarrow \mu$  ( $\Delta m^2$ ,  $\theta_{23}$ )



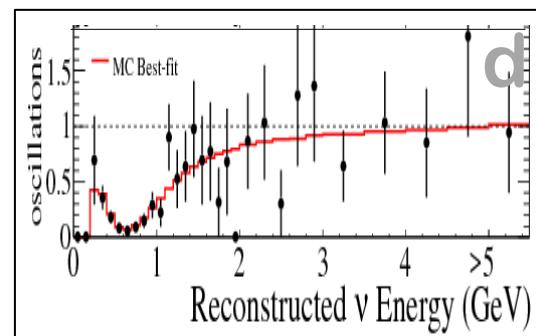
$e \rightarrow e$  ( $\Delta m^2$ ,  $\theta_{13}$ )



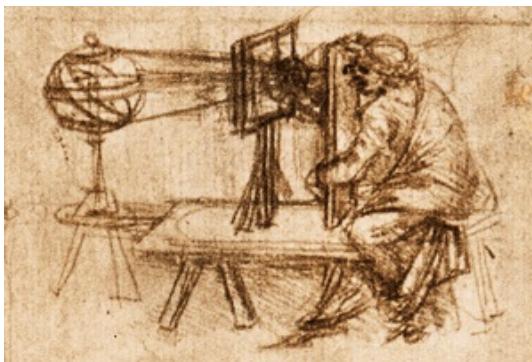
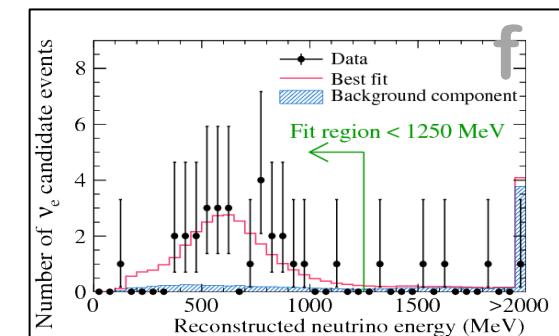
$e \rightarrow e$  ( $\delta m^2$ ,  $\theta_{12}$ )



$\mu \rightarrow \mu$  ( $\Delta m^2$ ,  $\theta_{23}$ )



$\mu \rightarrow e$  ( $\Delta m^2$ ,  $\theta_{13}$ ,  $\theta_{23}$ )

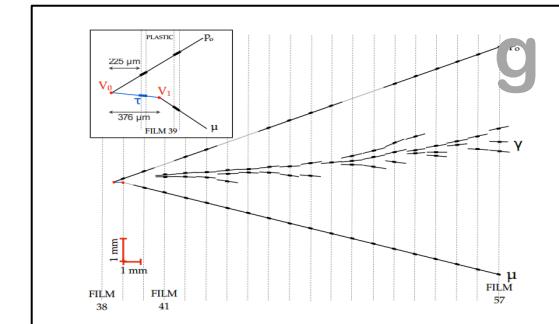


*Terra cognita:*

$$\delta m^2 \quad |\Delta m^2|$$

$$\theta_{12} \quad \theta_{23} \quad \theta_{13}$$

$\mu \rightarrow \tau$  ( $\Delta m^2$ ,  $\theta_{23}$ )



# Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix

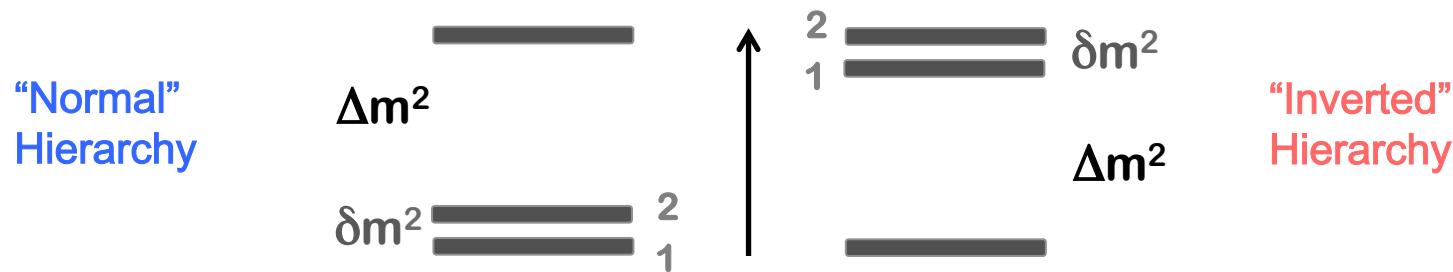
$$U_{\alpha i} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha/2} & 0 \\ 0 & 0 & e^{i\beta/2} \end{bmatrix}$$

[ only if Majorana ]

Mixing angles  $\theta_{23}$ ,  $\theta_{13}$ ,  $\theta_{12}$ : known ✓

CP-violat. phase(s)  $\delta$  ( $\alpha$ ,  $\beta$ ) : unknown ✗

## Mass-squared spectrum (up to absolute scale)



[ + contribution in matter  $\sim G_F \cdot E \cdot \text{density}$  ]

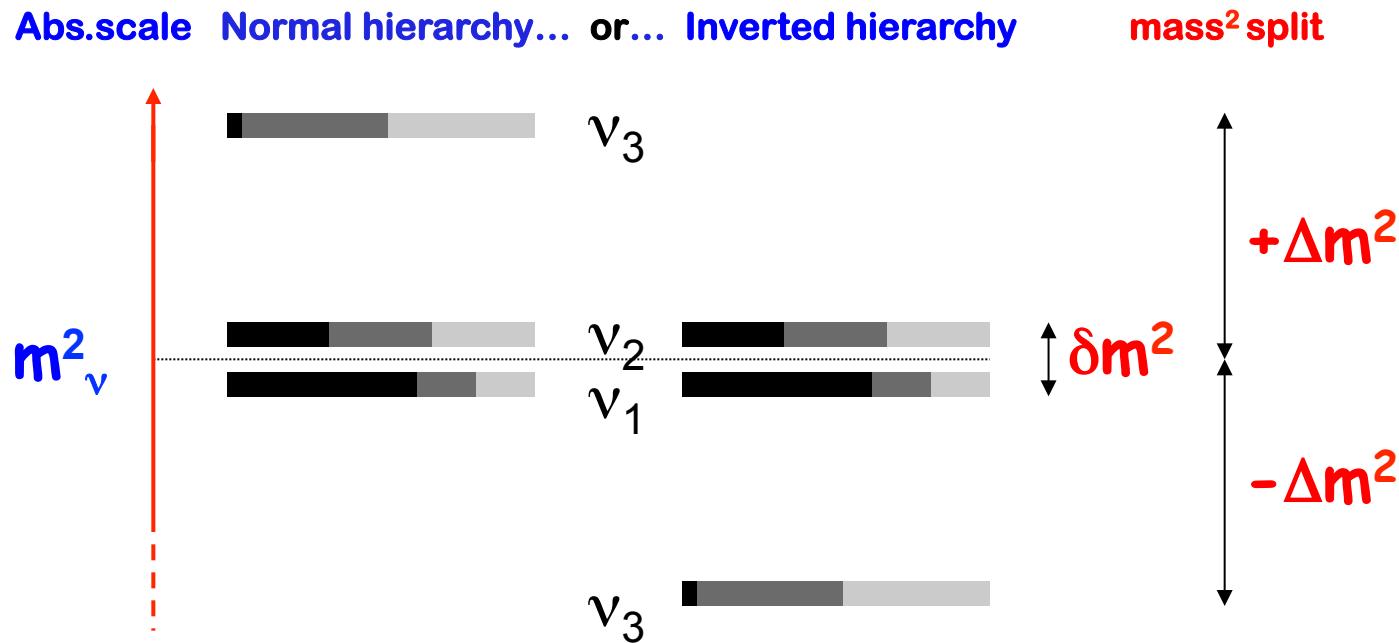
$\delta m^2$ ,  $\Delta m^2$ : known ✓

Matter effects (solar  $\nu$ ): ✓

Hierarchy : unknown ✗

# Current 3 $\nu$ picture in just one slide (with 1-digit accuracy)

Flavors = e  $\mu$   $\tau$



*Terra Cognita:*

$$\begin{aligned}\delta m^2 &\sim 8 \times 10^{-5} \text{ eV}^2 \\ \Delta m^2 &\sim 2 \times 10^{-3} \text{ eV}^2 \\ \sin^2 \theta_{12} &\sim 0.3 \\ \sin^2 \theta_{23} &\sim 0.5 \\ \sin^2 \theta_{13} &\sim 0.02\end{aligned}$$

*Terra Incognita:*

$$\begin{aligned}&\delta \text{ (CP)} \\ &\text{sign}(\Delta m^2) \\ &\text{octant}(\theta_{23}) \\ &\text{absolute mass scale} \\ &\text{Dirac/Majorana nature}\end{aligned}$$

**Old but still strong theoretical argument for Majorana  $\nu$ 's as messengers of new physics scale (see-saw + Weinberg):**

- Effects of high-energy physics as effective operators added to the standard model

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \dots$$

- can be classified systematically

$$\mathcal{L}_5 = (LH)(LH) \rightarrow \frac{1}{\Lambda} (L\langle H \rangle)(L\langle H \rangle) = m_\nu \nu \nu$$

$$\begin{aligned} \mathcal{L}_6 = & QQQL, \bar{L}\sigma^{\mu\nu}W_{\mu\nu}Hl, \epsilon_{abc}W_\nu^{a\mu}W_\lambda^{b\nu}W_\mu^{c\lambda}, \\ & (H^\dagger D_\mu H)(H^\dagger D^\mu H), B_{\mu\nu}H^\dagger W^{\mu\nu}H, \dots \end{aligned}$$

(H. Murayama at ICFA Seminar 2011, CERN)

**Old but still unique experimental probe of Majorana  $\nu$ 's nature via  $\Delta L=2$  process: neutrinoless double beta decay.  
See next talk by Schoenert**

## Charting 3ν param. with more digits: global analysis →

Analysis includes increasingly rich oscill. data sets:

LBL Acc + Solar + KL

LBL Acc + Solar + KL + SBL Reactor

LBL Acc + Solar + KL + SBL Reactor + SK Atm.

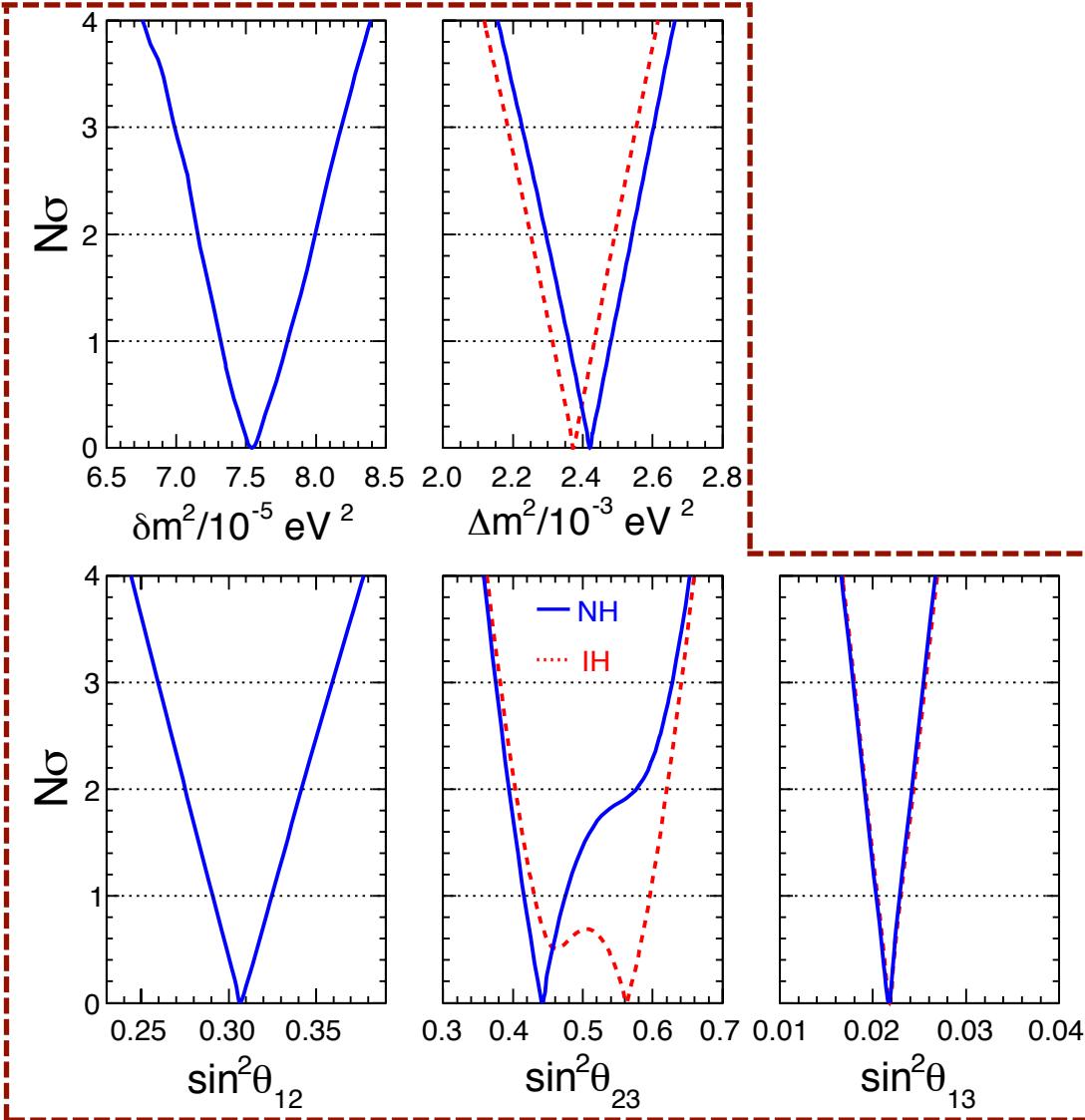
Parameters not shown are marginalized away.

C.L.'s are drawn at  $\Delta\chi^2 = 1, 4, 9 \rightarrow$

$N\sigma = 1, 2, 3$  for projections over single parameters.

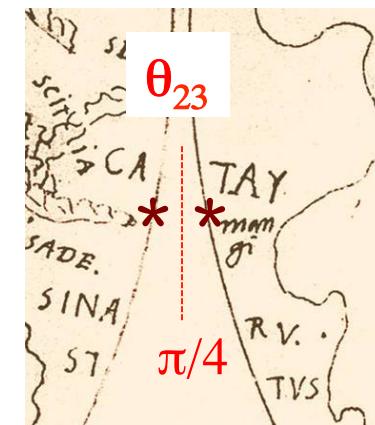
Figures from Capozzi et al., arXiv:1312.2878 (+ Neutrino 2014 updates)  
See also: Gonzalez-Garcia et al., 1409.5439; Forero et al., 1405.7540.

LBL Acc + Solar + KL + SBL Reactors + SK Atm



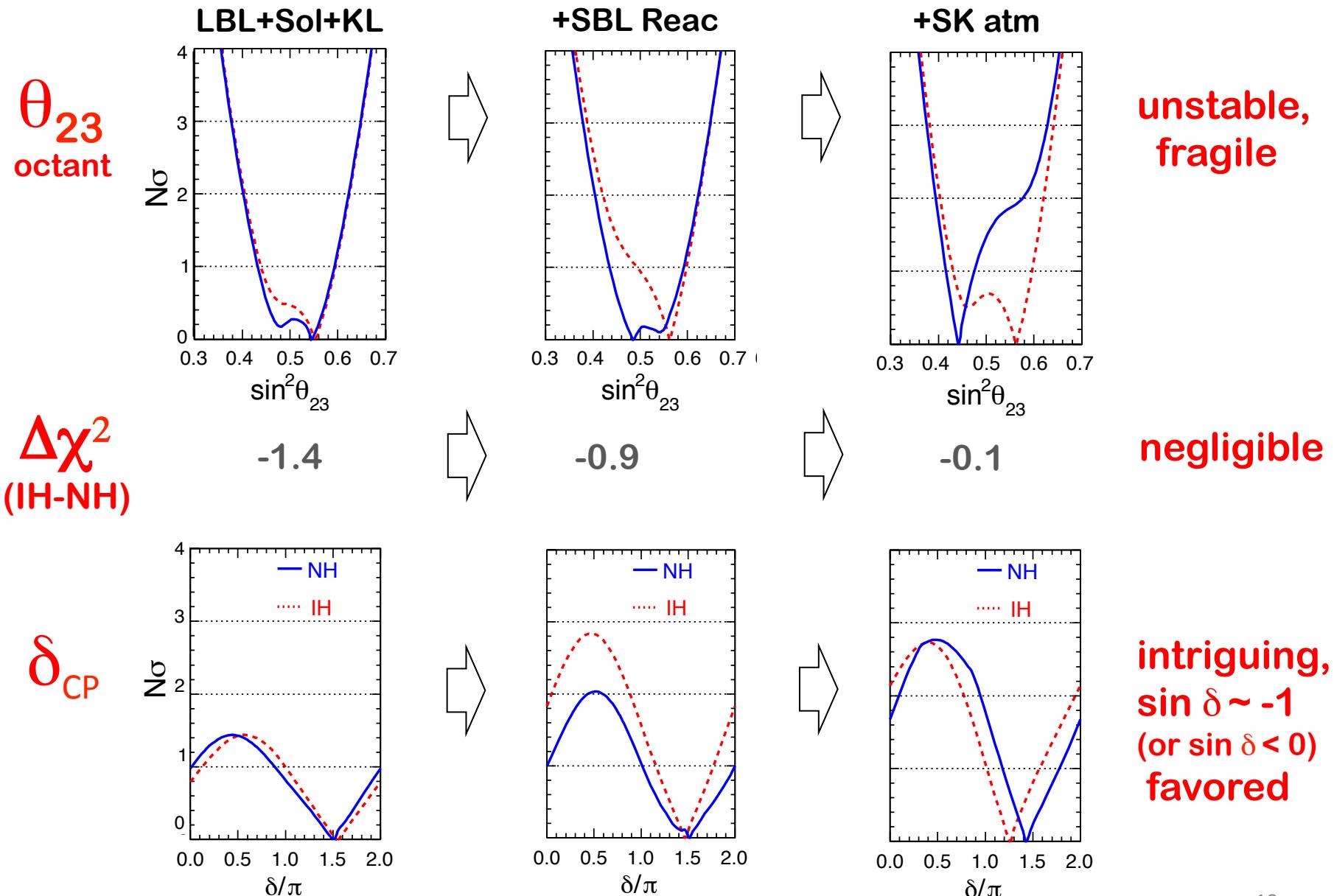
Current accuracy  
in mapping  
Terra Cognita:

$\delta m^2$	2.6 %
$\Delta m^2$	2.6 %
$\sin^2 \theta_{12}$	5.4 %
$\sin^2 \theta_{13}$	8.5 %
$\sin^2 \theta_{23}$	~ 10 % *

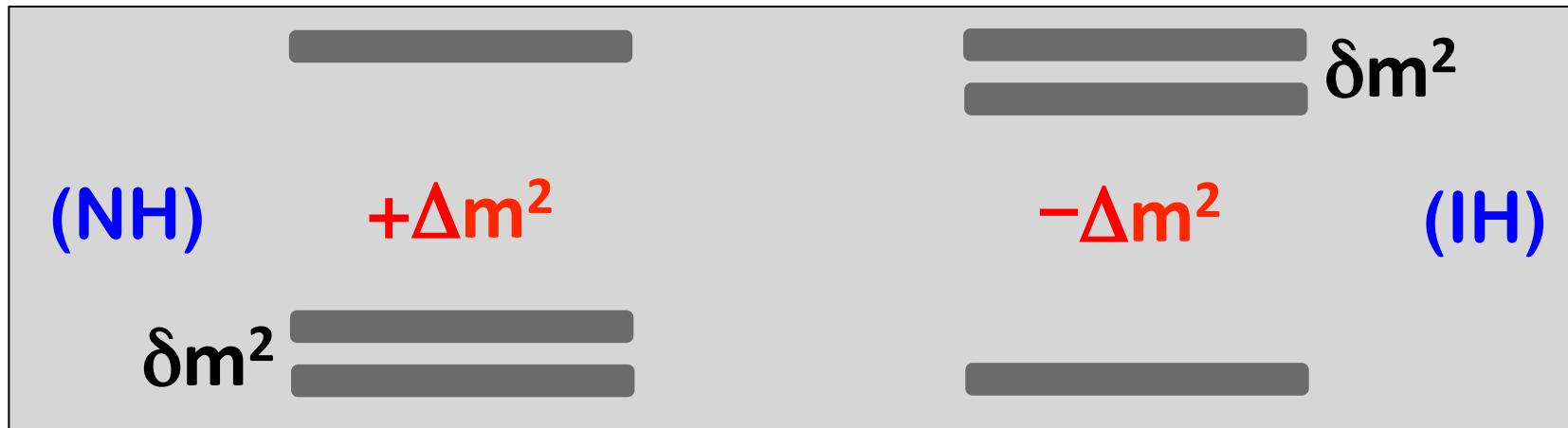


(but... in which octant?)

# Terra Incognita I (oscill. param.): current hints



## Oscillation searches can probe the hierarchy...



... if one can observe **interference** of oscill. driven by  $\pm\Delta m^2$  with oscill. driven by another quantity **Q** with known sign. 3 options:

$$Q = \delta m^2 \quad (\text{medium-baseline reactors})$$

$$Q = 2\sqrt{2} G_F N_e E \quad (\text{matter effects in accel./atmosph. } \nu)$$

$$Q = 2\sqrt{2} G_F N_\nu E \quad (\text{collective effects in SNe})$$

All paths to the hierarchy are being actively investigated from the experimental - theoretical - phenomenological viewpoint.

# The path towards a possible discovery of leptonic CP violation requires 6 steps:

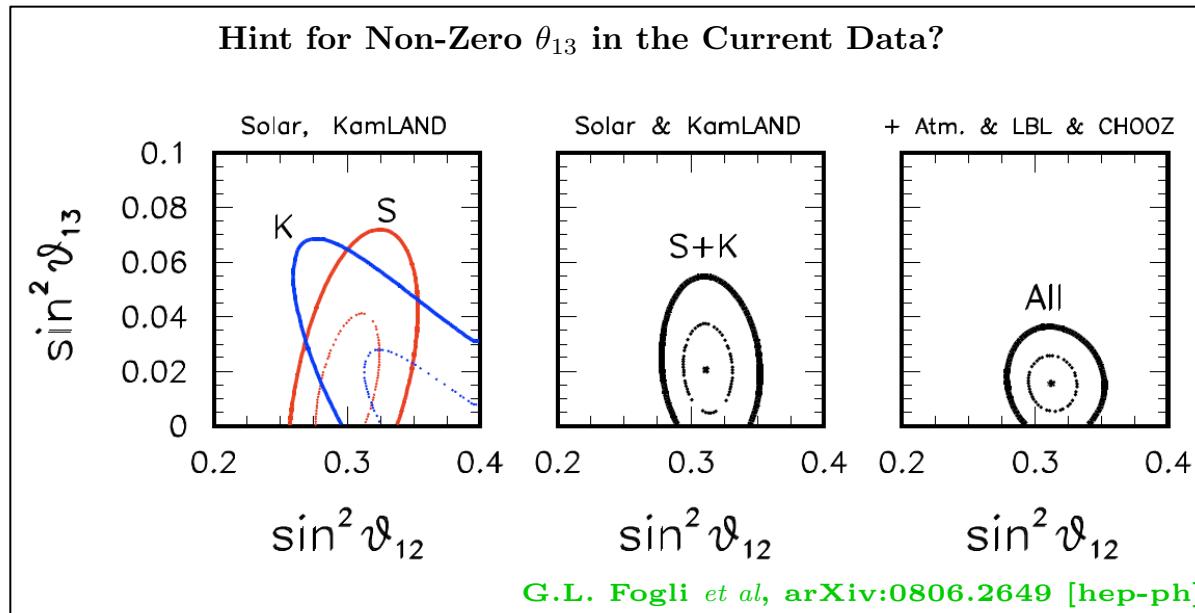
- 3 mixing angles should be nonvanishing ✓
- 2 mass gaps should be nonvanishing ✓
- 1 Dirac phase should be nonvanishing ...

Nature has already allowed us 5 steps in favorable conditions, i.e., at accessible terrestrial scales ...

Current hints suggest that the 6<sup>th</sup> may be at reach...  
...expeditions to neutrino CPV-land are a must!

[and, if neutrinos are Majorana... CPV bonanza with 2 more phases ! ]

Let us hope that history may repeat itself, as for a previous lucky hint...



(A. de Gouvea at ICFA Seminar 2008, SLAC)

so that we may discuss about “nearly maximal leptonic CP violation” at ICFA seminar 20XX!

# Terra Incognita II (absolute mass observables)

## ( $m_\beta$ , $m_{\beta\beta}$ , $\Sigma$ )

In the 3ν framework:

$\beta$  decay, sensitive to the “effective electron neutrino mass”:

$$m_\beta = [c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{\frac{1}{2}}$$

Ov $\beta\beta$  decay: only if Majorana. “Effective Majorana mass”:

$$m_{\beta\beta} = |c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$

Cosmology: Dominantly sensitive to sum of neutrino masses:

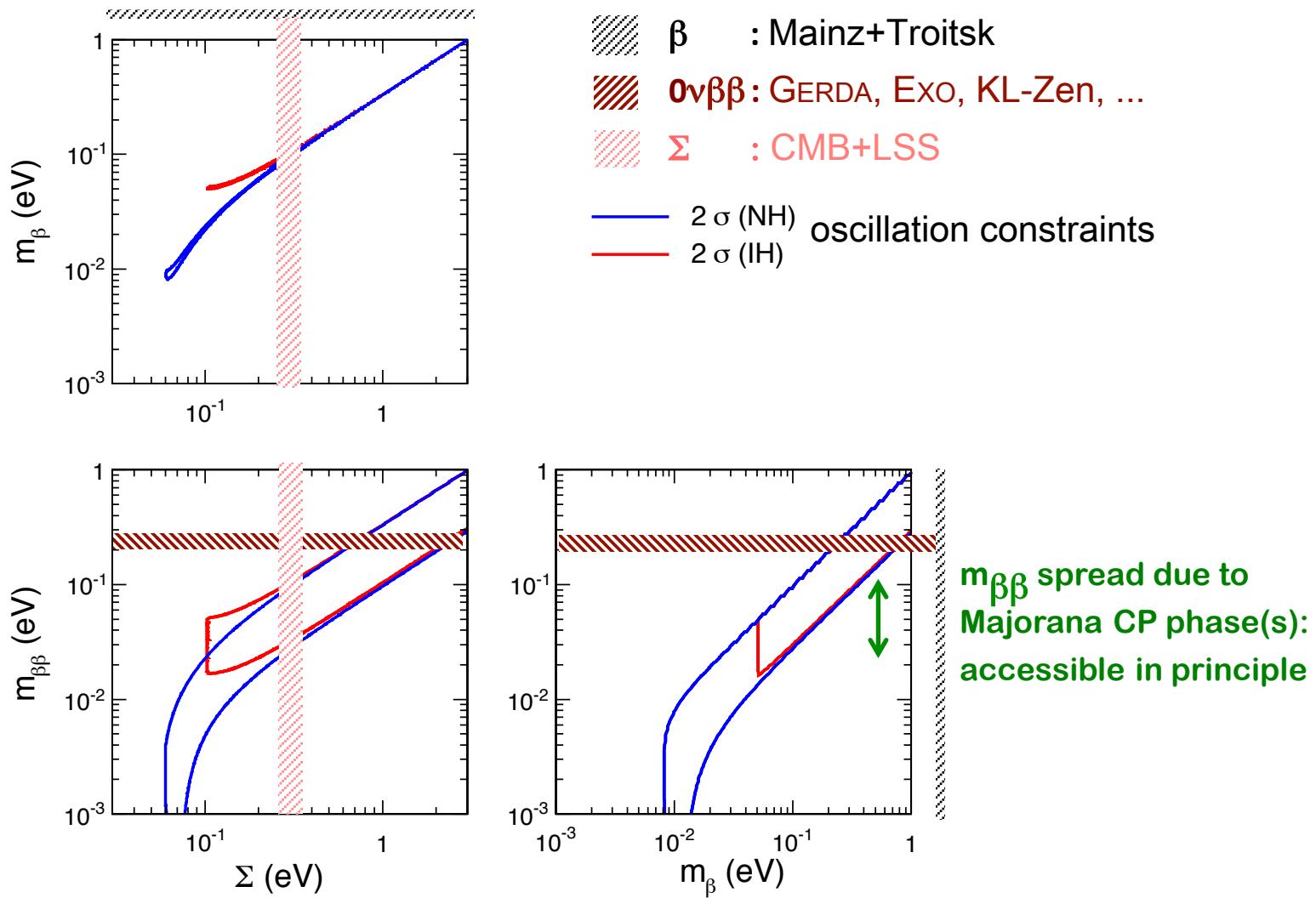
$$\Sigma = m_1 + m_2 + m_3$$

Note 1: These observables may provide handles to distinguish NH/IH.

Note 2: Majorana case gives a new source of CPV (unconstrained)

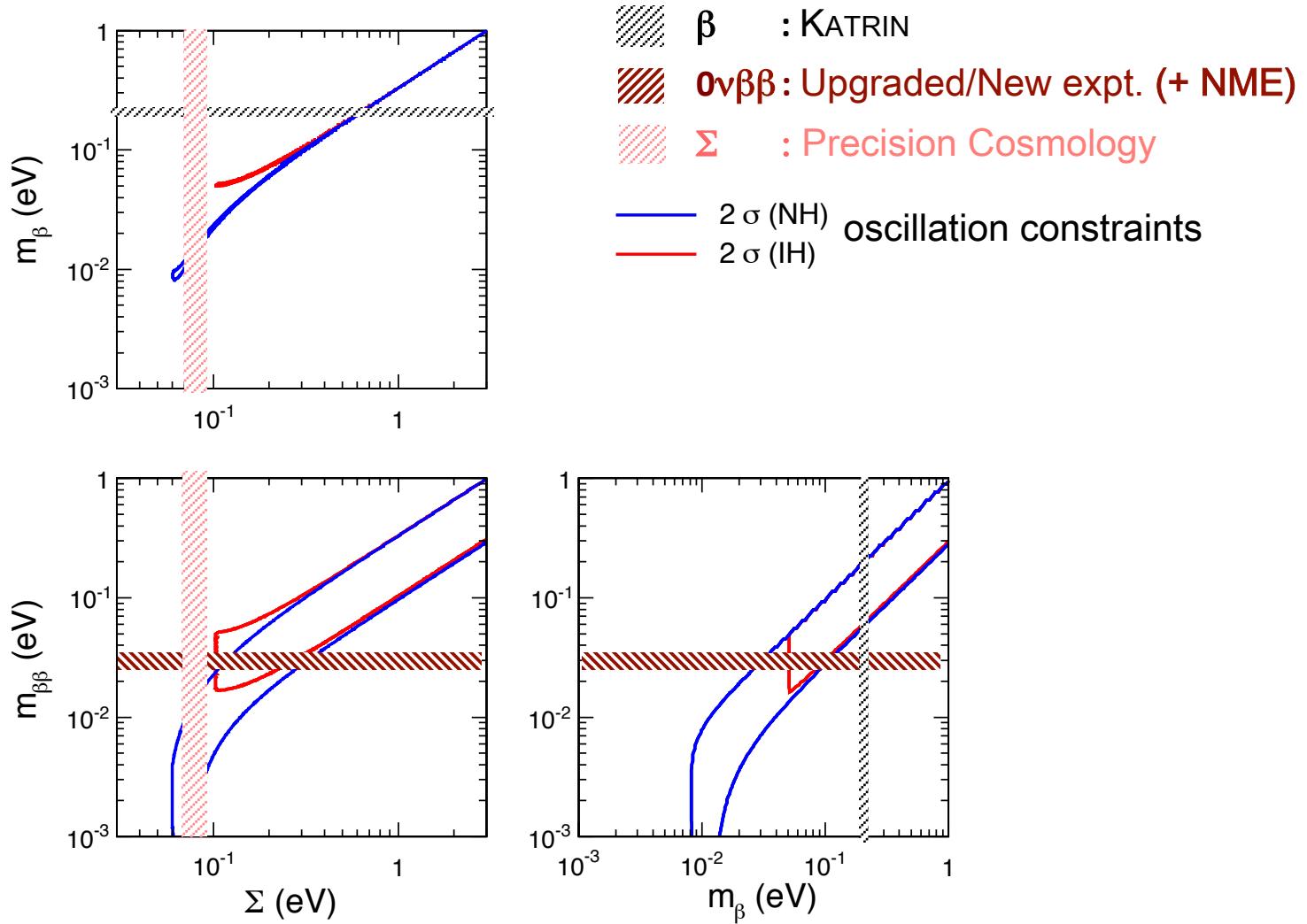
Note 2: The three observables are correlated by oscillation data →

# Upper limits on $m_\beta$ , $m_{\beta\beta}$ , $\Sigma$ (up to some syst.) + osc. constraints



[Clearly, the inverted hierarchy case would make life easier...]

# Upper limits on $m_\beta$ , $m_{\beta\beta}$ , $\Sigma$ in $\sim 10$ years ?

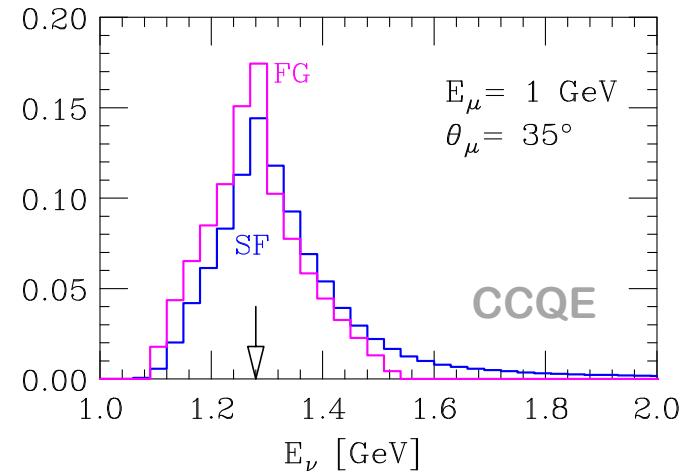


Large phase space for discoveries about  $\nu$  mass and nature.

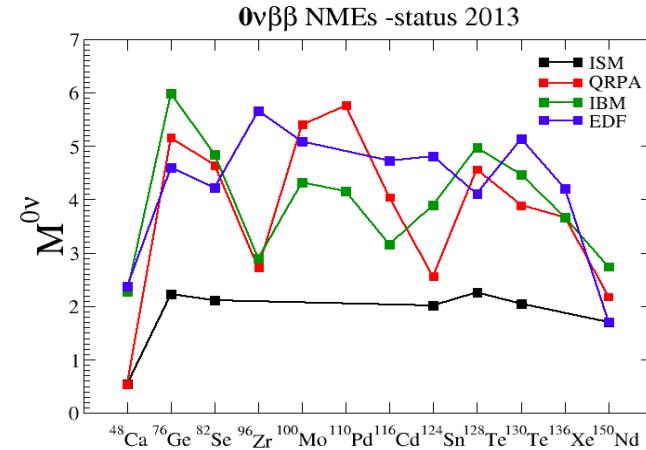
Theory can help in both “mapping” and “discovery” expeditions

Two examples of well-defined, long-term theory programs:

Must improve modeling of  $\nu$ -nucleus cross sections, to understand energy spectra in accelerator and atmospheric searches for CPV and mass hierarchy



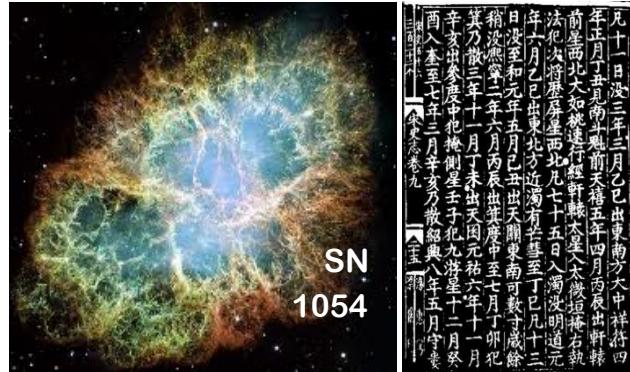
Must improve modeling of nuclear structure, to understand and compare signals or limits on  $0\nu\beta\beta$  decay rates and related weak/strong processes



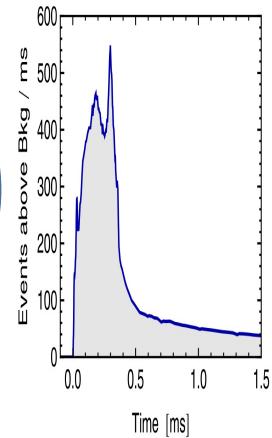
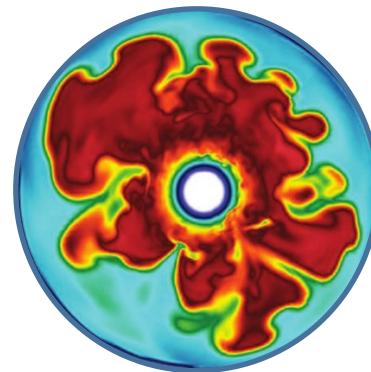
Require joint effort from nuclear and particle phys. communities

# Another long-term theory program for an “unpredictable” event:

Sooner or later (say,  $10 \pm 10$  years ?), another **galactic SN** should explode... Its “autopsy” will keep us busy for decades, and teach us a lot about astrophysics and neutrino physics.



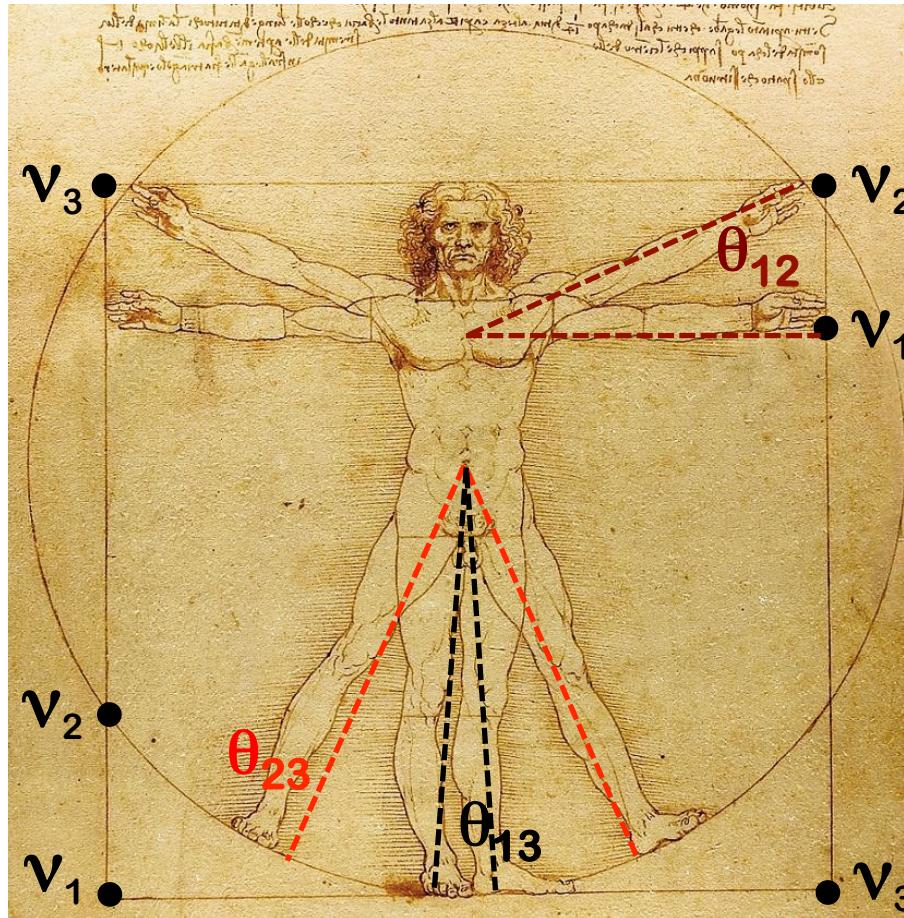
Simulations of SN explosions, **(anti)nu  
fluences** and flavor transitions, which are already very demanding, will need to reach complexity levels comparable -probably- to QCD lattice calculations.



Will spark a truly interdisciplinary program from diverse communities

see also next talk by Halzen

Neutrino flavor theory: is the current picture suggestive of some “simmetry”?  
Or the symmetry is only in our mind, and there is just randomness?  
Are there possible connections with the quark flavor sector?



Many interesting ideas, but no obvious answer/guidance so far

# Specific outcomes (a few examples from a vast literature)

No organizing principle  
("anarchy")



Discrete family symmetries  
("geometry")

linear relations between  
 $\theta_{13}\cos\delta$  and  $\theta_{12}, \theta_{23}$

Continuous flavor symmetries  
("dynamics")

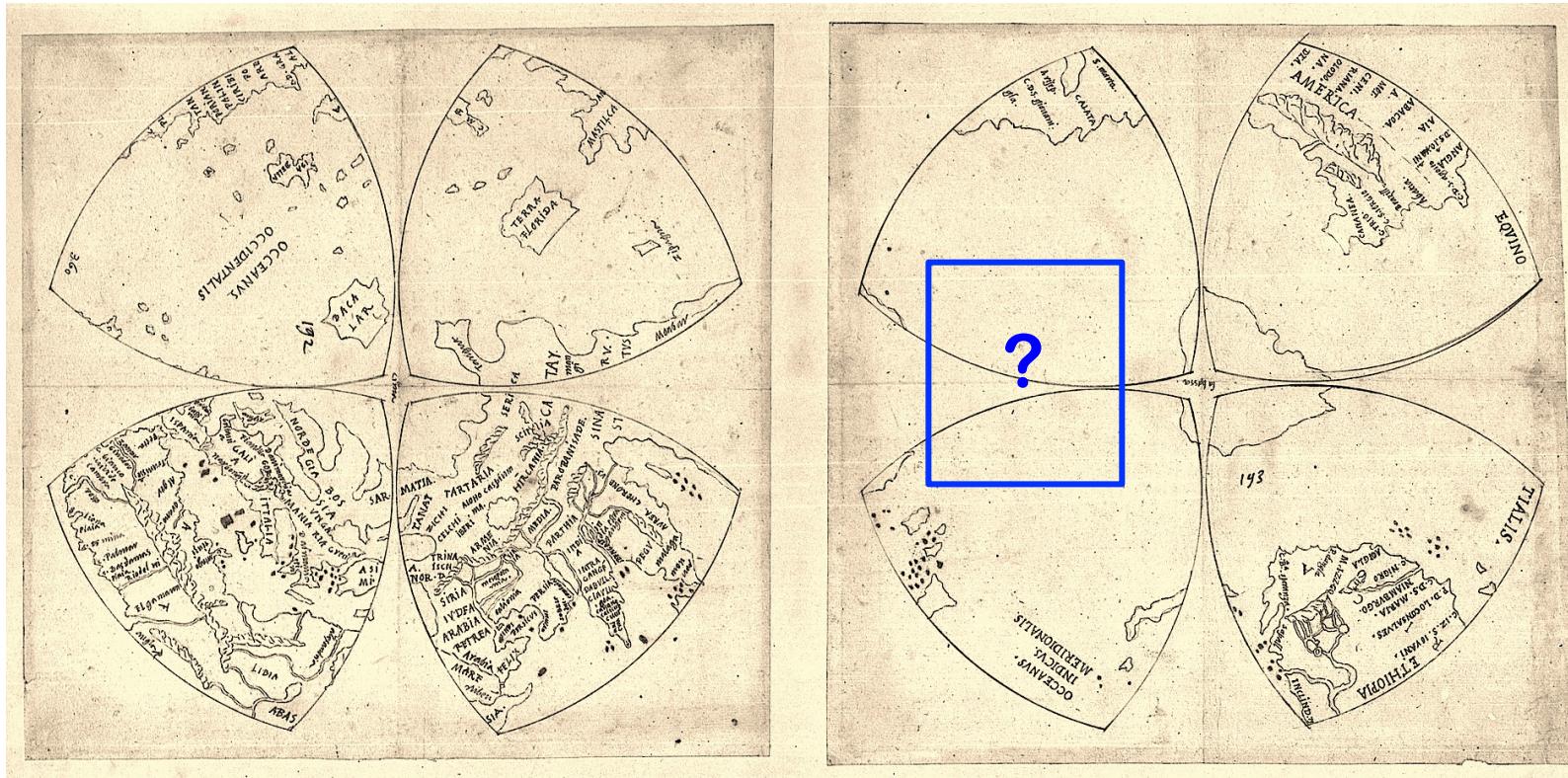
links between neutrino  
spectra/angles/phases

Common quark-lepton features  
("complementarity")

links between  
 $\theta_{13}$  and  $\theta_C$

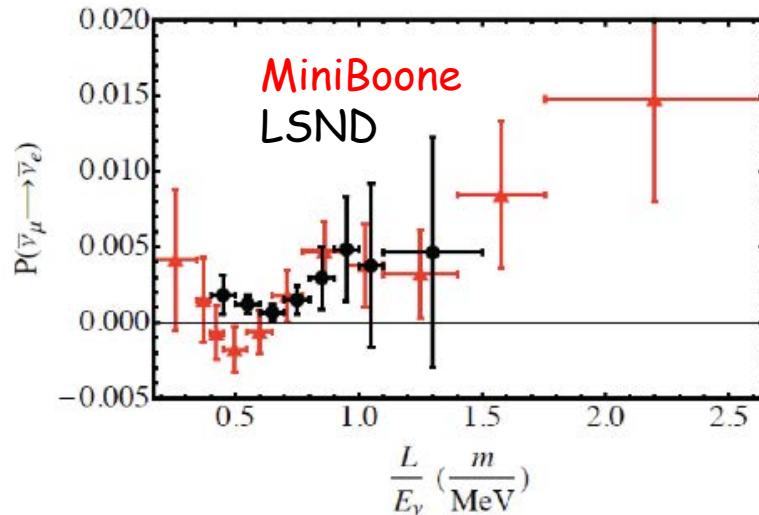
## Model selection will benefit from higher precision

# Beyond the 3ν paradigm



We should not be biased by the success of the 3ν scheme...  
If we sail too close to the 3ν coastline ... we might miss an entire new continent (new neutrino states and interactions)

**Light states: conflicting sightings of  $\nu_s$  with (sub)eV mass from various sailors in the last 20 years... new land or mirage?**



**Available data: intriguing, but not conclusive or convergent.**

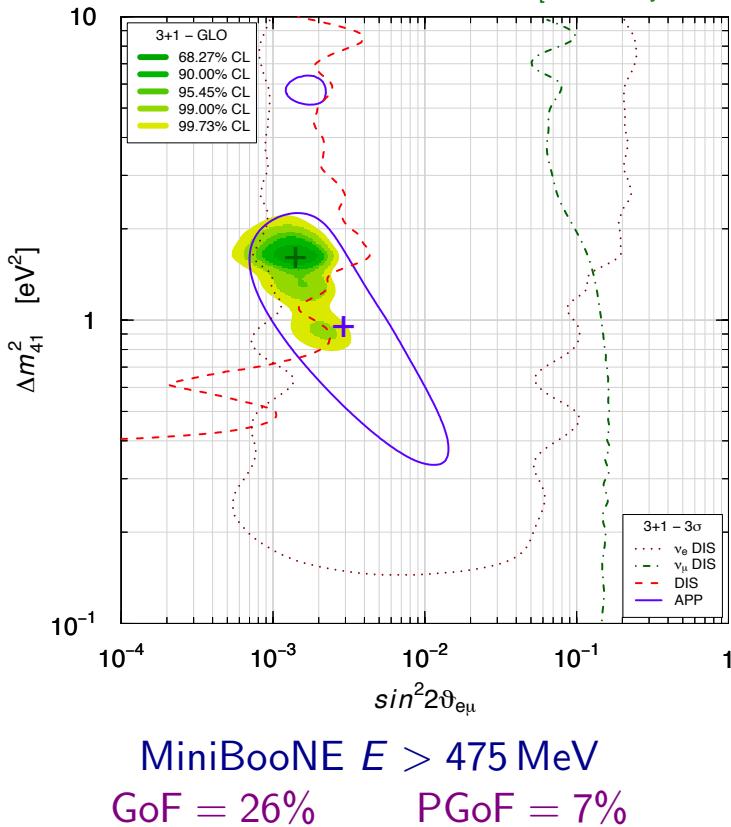
The question raised by the LSND claim is still with us:  
Is there  $\nu_\mu \rightarrow \nu_e$  appearance at a scale  $\sqrt{\Delta M^2} \sim O(0.1-1)$  eV ?

In recent years, further interest in light sterile ν raised by:

- 1) Possible associated  $\nu_e \rightarrow \nu_e$  disappearance signals
- 2) Possible associated extra radiation in cosmology

# 3+1 Global Fit

[Preliminary 2014 Update]



- ▶ APP  $\nu_\mu \rightarrow \nu_e$  &  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ : LSND (Y), MiniBooNE (?), OPERA (N), ICARUS (N), KARMEN (N), NOMAD (N), BNL-E776 (N)
- ▶ DIS  $\nu_e$  &  $\bar{\nu}_e$ : Reactors (Y), Gallium (Y),  $\nu_e C$  (N), Solar (N)
- ▶ DIS  $\nu_\mu$  &  $\bar{\nu}_\mu$ : CDHSW (N), MINOS (N), Atmospheric (N), MiniBooNE/SciBooNE (N)

No Osc. excluded at 6.3 $\sigma$   
 $\Delta\chi^2/NDF = 47.7/3$

[Giunti, Laveder, Y.F. Li, H.W. Long, PRD 88 (2013) 073008]

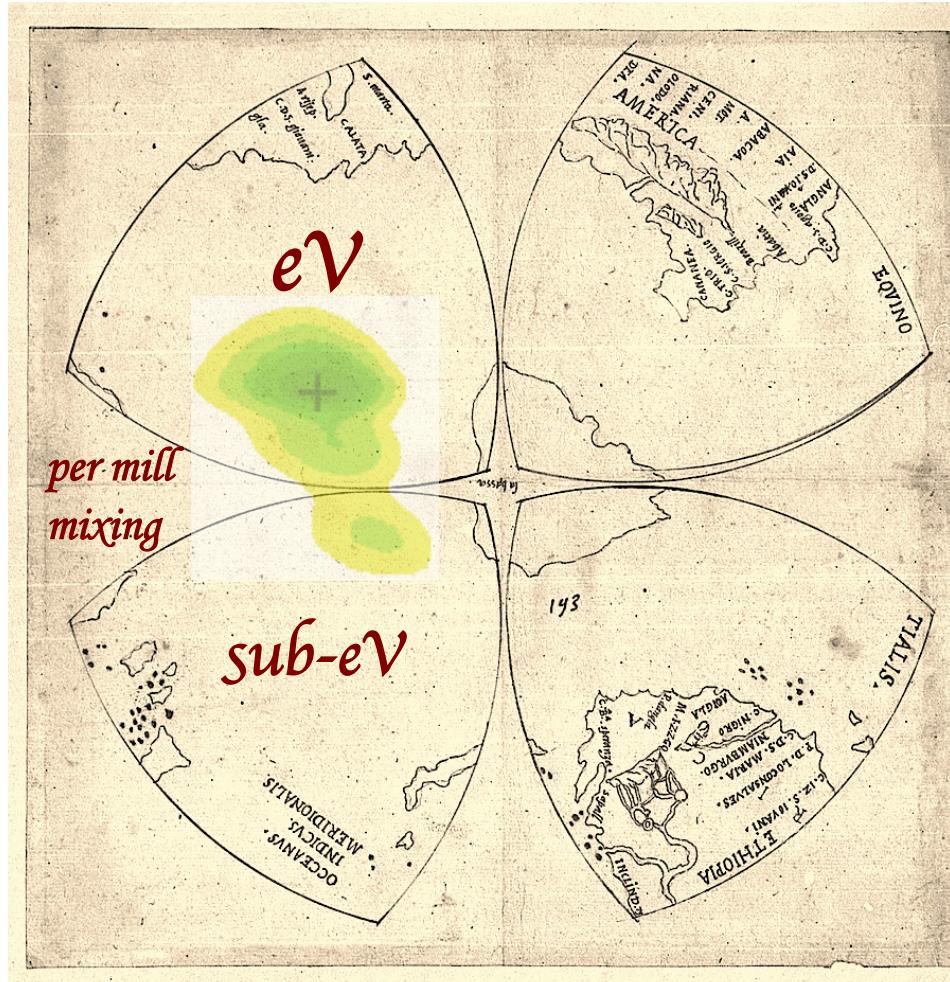
[different approach and conclusions: Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050]

C. Giunti — Phenomenology of Light Sterile Neutrinos — Corfu 2014 — 6 September 2014 — 24

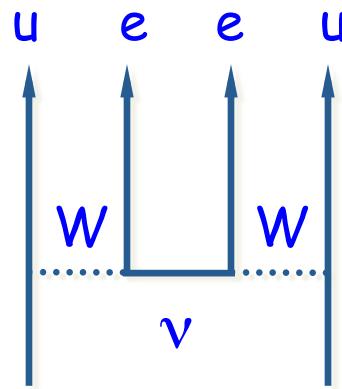
From Giunti et al. 2014. Note: Kopp et al. 2014 find worse GOF.

In general, tension between appearance and disappearance oscillations.  
 Also: some tension between oscillation and cosmology (not included above)

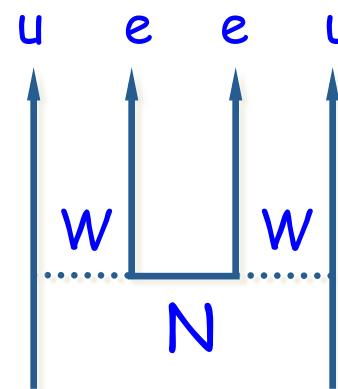
Need a “redundant” oscillation search, exploring a wide mass-mixing range, and cross-checking both appearance and disappearance, in order to discover (or rule out) conclusively light sterile neutrino states.



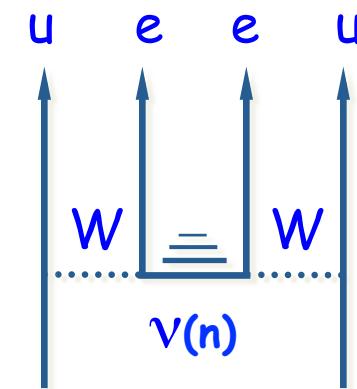
**Nonstandard interactions/processes in neutrino physics: no sightings so far, but they should always be kept in mind; examples in  $0\nu\beta\beta$  decay:**



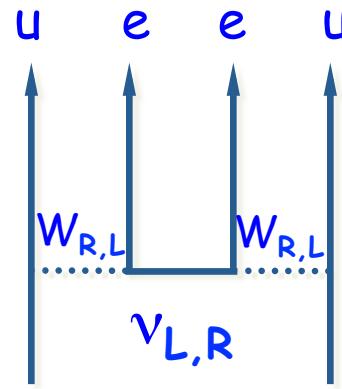
Standard



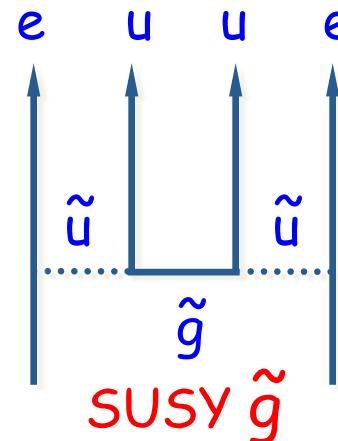
Heavy  $\nu$



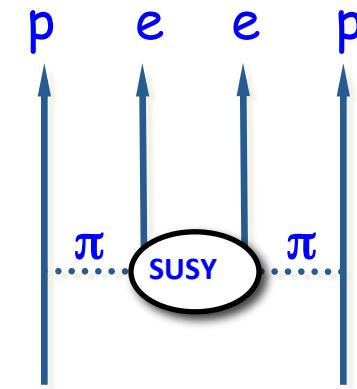
Kaluza-Klein  
(KK $\pm 1$  Brane:  $a = 10^{\pm 1}/\text{GeV}$ )



RHC  $\lambda, \eta$   
 $\lambda = \text{RH had}, \eta = \text{LH had}$

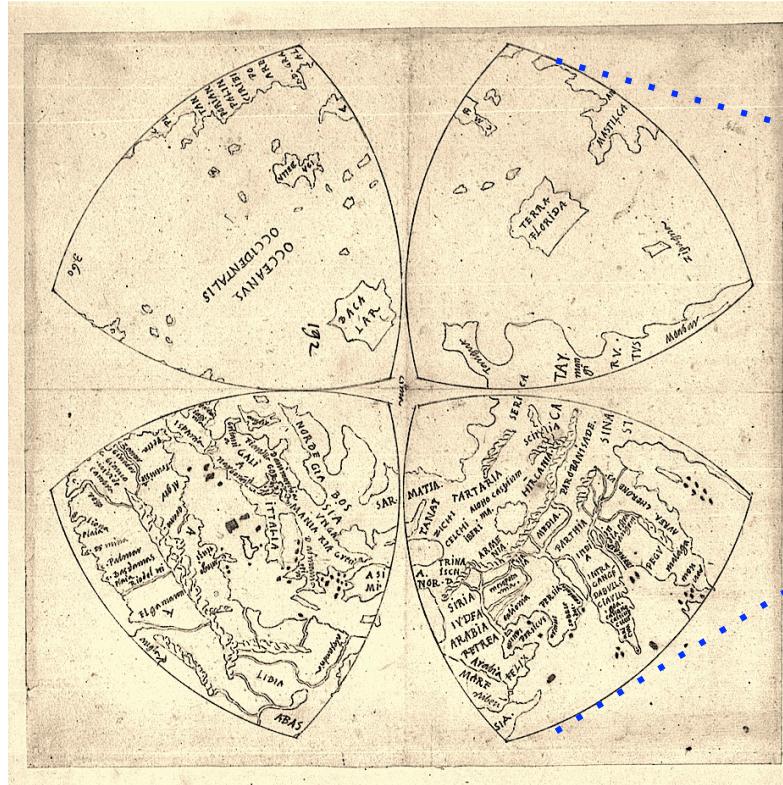


SUSY  $\tilde{g}$

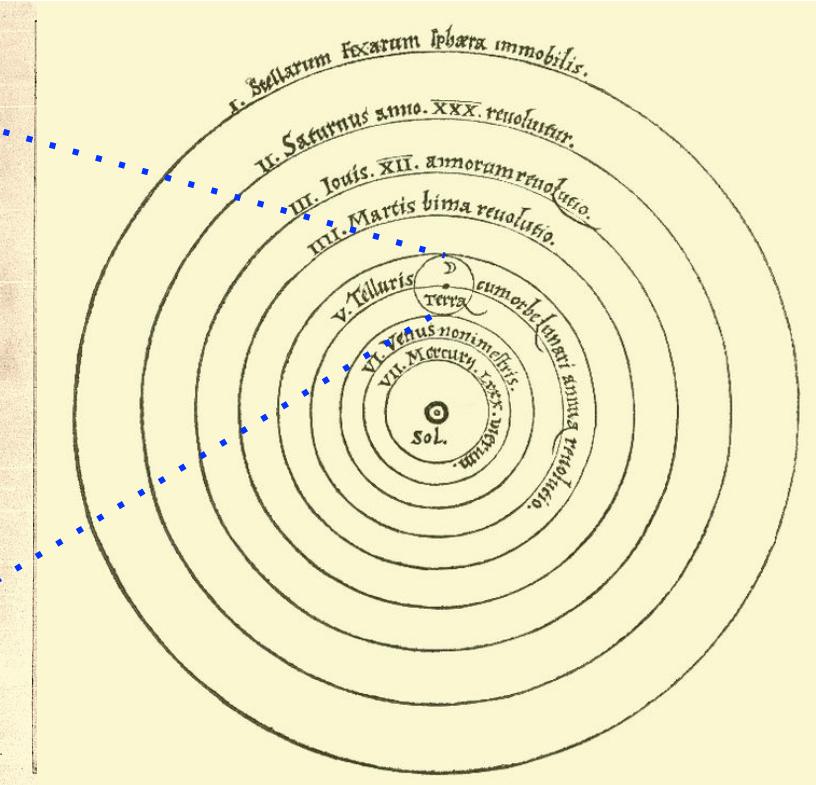


SUSY  $\pi$

# Towards a larger picture and higher scales



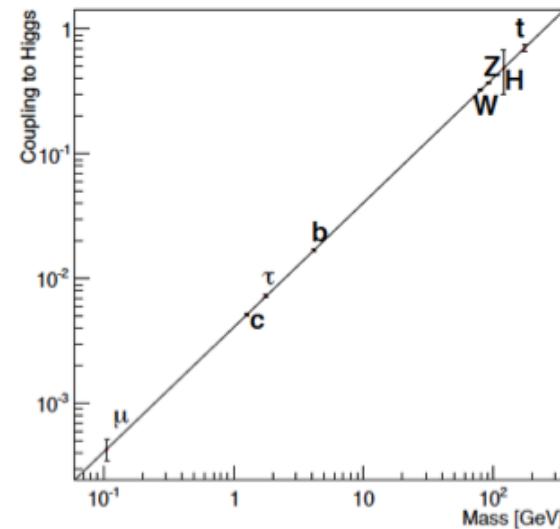
1514 Leonardo



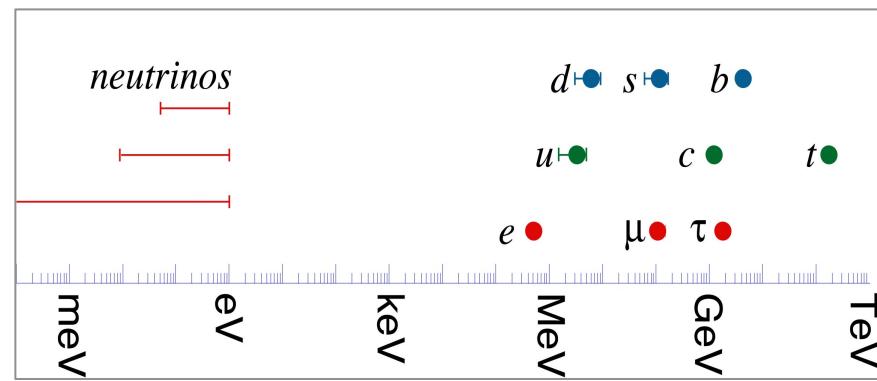
1543 Copernicus

# Linking two fundamental research expeditions:

## 1. Test Higgs sector

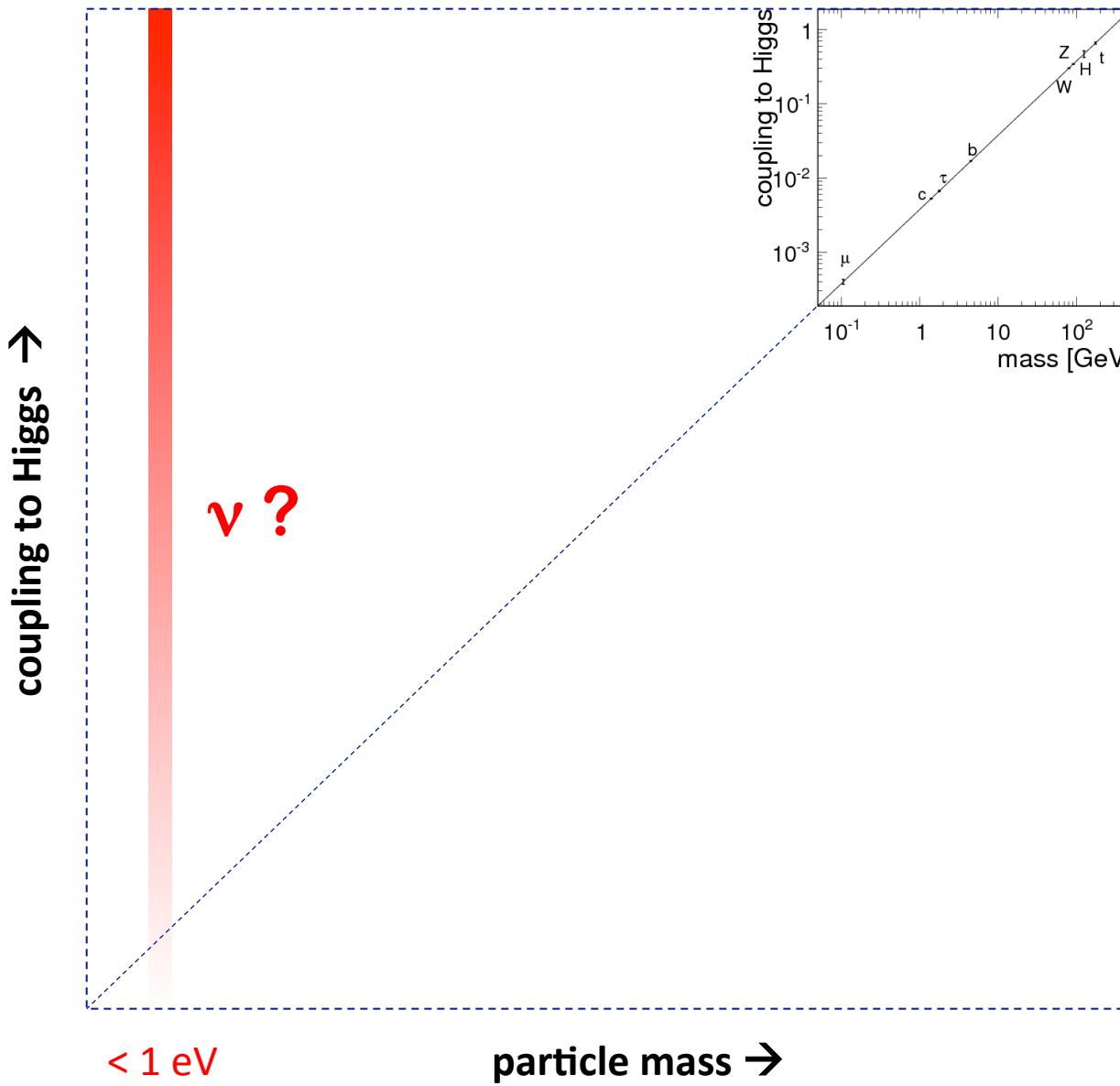


## 2. Find $\nu$ masses



**1 + 2**

Where are the  $\nu$ 's on this plot? Why are they so light?



# Options:

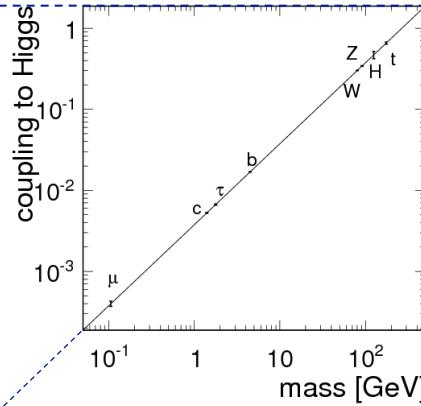
coupling to Higgs →

$\nu$

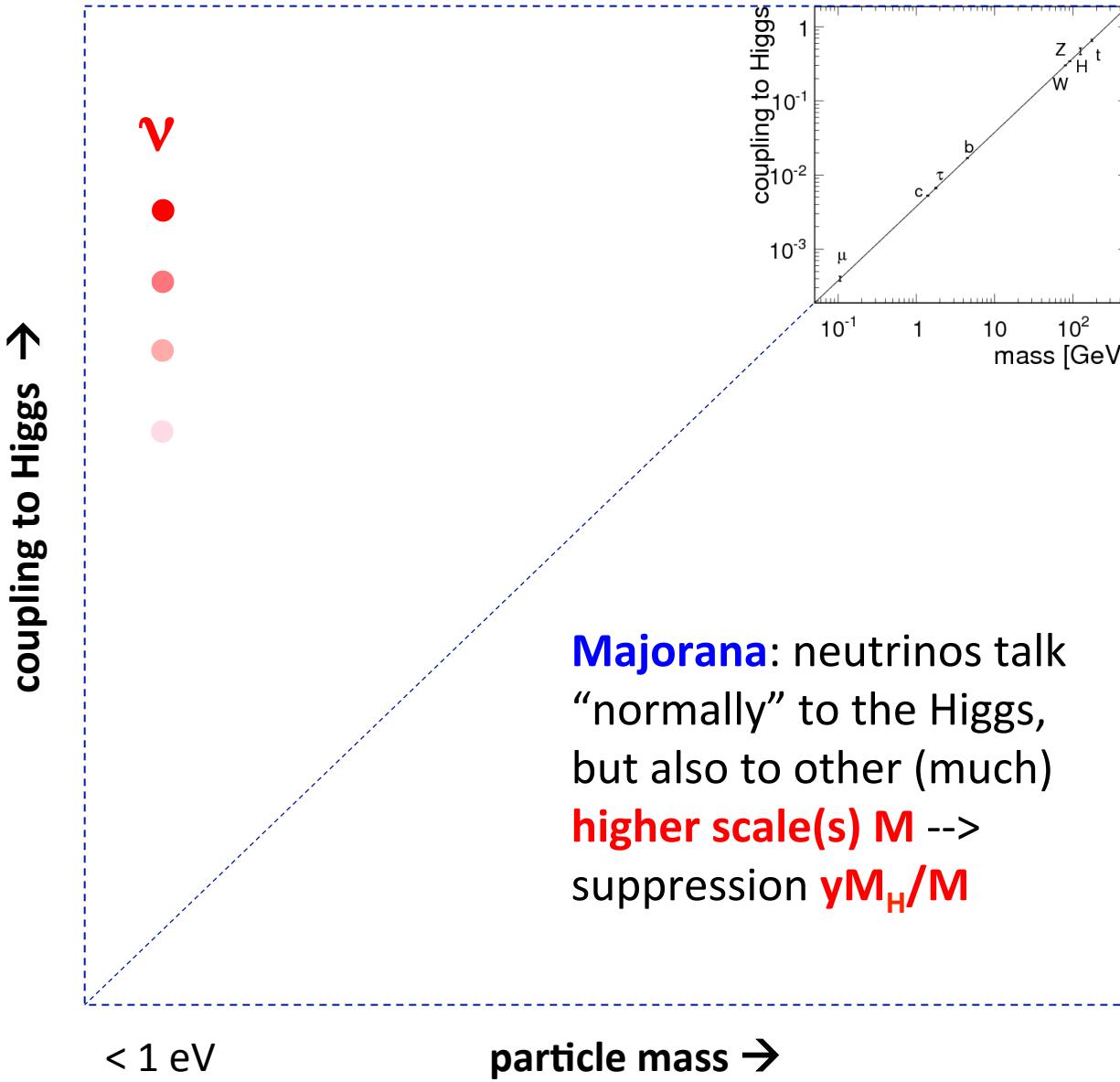
< 1 eV

particle mass →

**Dirac:** neutrinos “talk”  
very weakly to the  
Higgs boson,  $y < 10^{-12}$   
for unknown reasons...

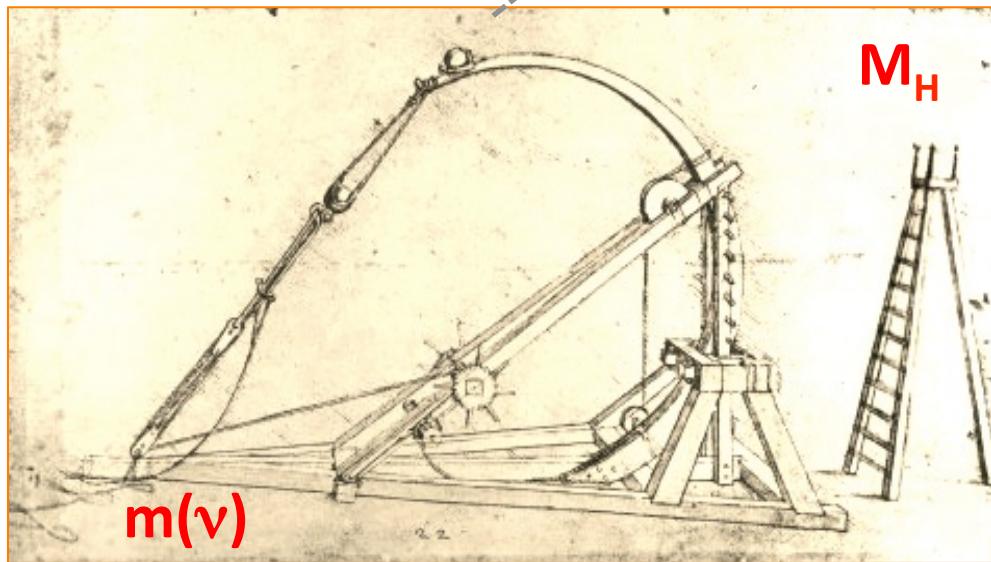


# Options:



**Neutrinos masses** may offer  
a great opportunity to jump  
**beyond the EW framework**  
via see-saw ...

M  
•  
•  
•  
•



... and to address fundamental physics issues, such as:

- new sources of CP violation at low and high energies
- lepton number violation and associated phenomena
- matter-antimatter asymmetry of the universe ...

CP-violating decays of heavy neutrinos at scale  
 $M$  may generate lepton asymmetry (leptogenesis):  
Discovery of leptonic CP violation and of Majorana nature (+ proton decay?) would be important steps towards this scenario.



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**$M \sim \text{low scale}$**

At the other end of the spectrum, low-scale (e.g. EW) see-saw may also generate (at the price of fine-tuning) additional interesting phenomenology: dark matter candidates, di-lepton and heavy lepton events in HEP

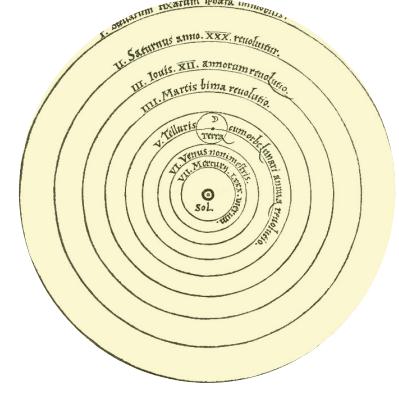
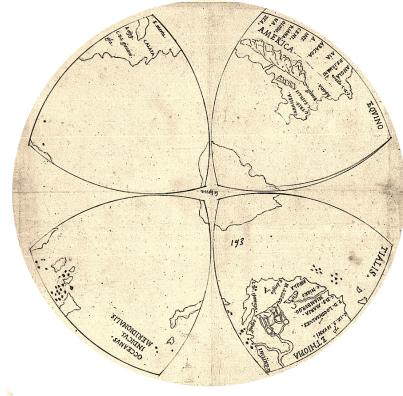
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In principle, several sterile states might even be split  
among widely difference energy scales, and contribute  
to various phenomena in (astro)particle physics.  
**Let us remain open-minded!**

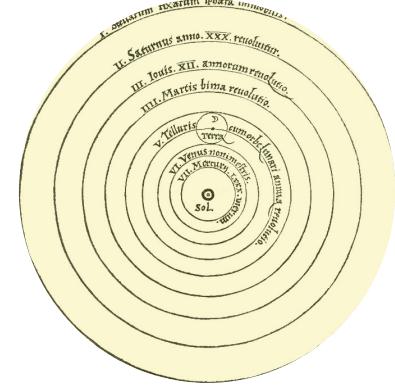
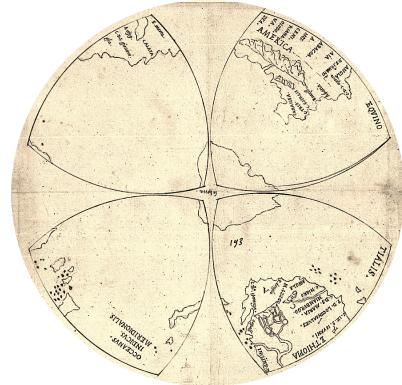
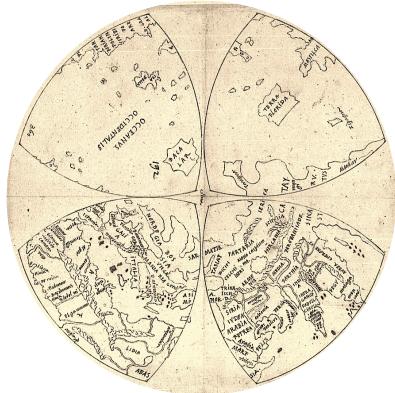
# EPILOGUE



# EPILOGUE

*Terra Cognita...*

$$\begin{aligned}\delta m^2 &\sim 8 \times 10^{-5} \text{ eV}^2 \\ \Delta m^2 &\sim 2 \times 10^{-3} \text{ eV}^2 \\ \sin^2 \theta_{12} &\sim 0.3 \\ \sin^2 \theta_{23} &\sim 0.5 \\ \sin^2 \theta_{13} &\sim 0.02\end{aligned}$$



# EPILOGUE

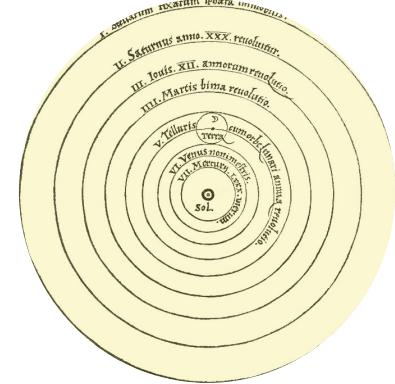
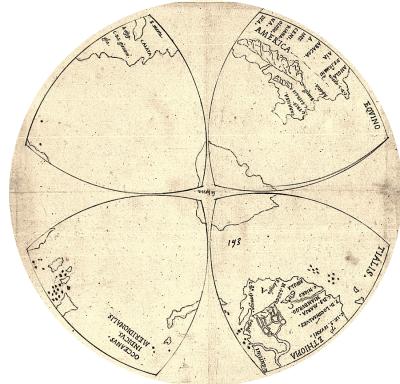
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*Terra Incognita...*

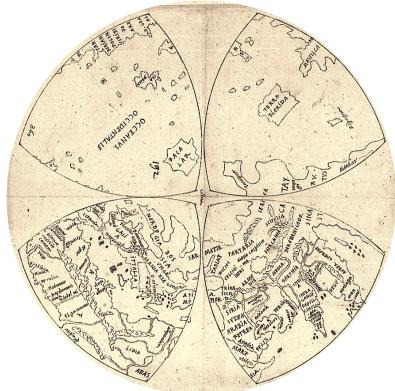
$$\begin{aligned}&\delta \text{ (CP)} \\ &\text{sign}(\Delta m^2) \\ &\text{octant}(\theta_{23}) \\ &\text{absolute masses} \\ &\text{Dirac/Majorana}\end{aligned}$$



# EPILOGUE

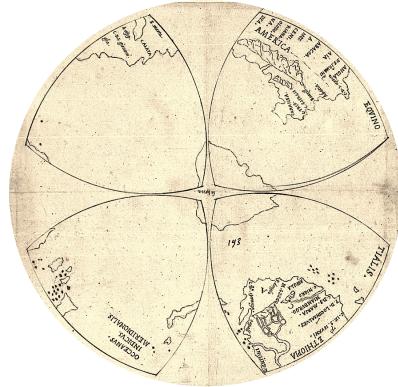
*Terra Cognita...*

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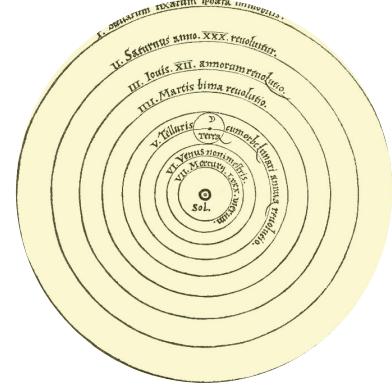
*Terra Incognita...*

$$\begin{aligned}\delta &(\text{CP}) \\ \text{sign}(\Delta m^2) \\ \text{octant}(\theta_{23}) \\ \text{absolute masses} \\ \text{Dirac/Majorana}\end{aligned}$$



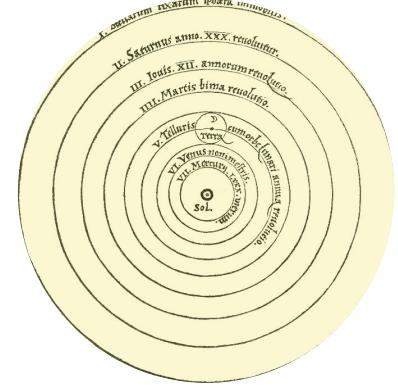
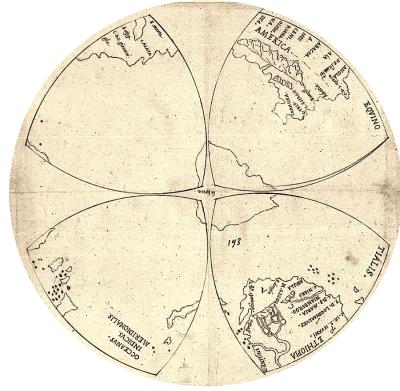
*....and beyond...*

**new light states  
new heavy states  
nonstandard inter.  
flavor structure  
baryon asymmetry**



# EPILOGUE

Further theoretical and experimental explorations will require significant time, resources and ... good fortune!  
So, for neutrino physics, let us wish...



# EPILOGUE

Further theoretical and experimental explorations will require significant time, resources and ... good fortune!  
So, for neutrino physics, let us wish...



Lu  
Luck



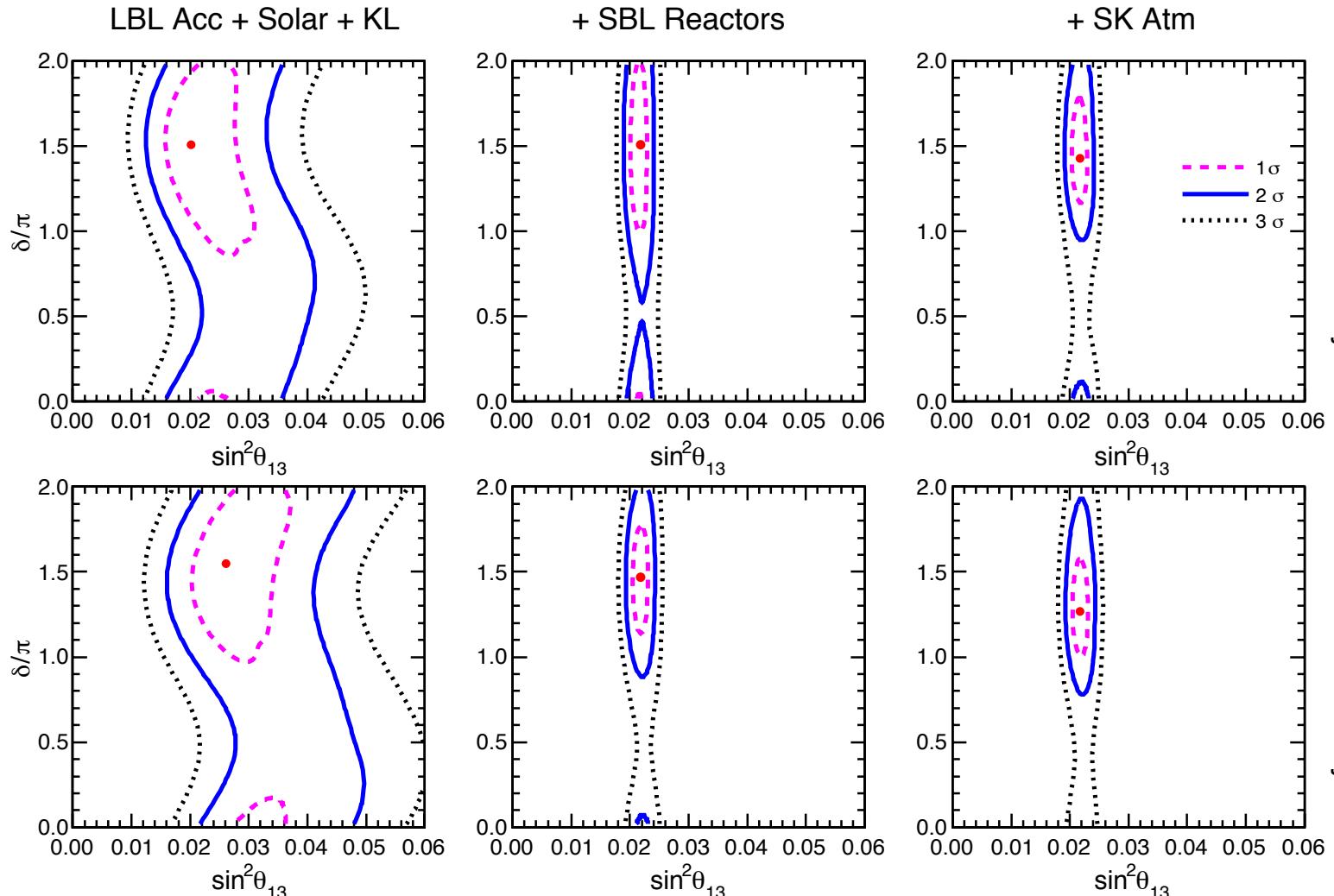
Fu  
Prosperity



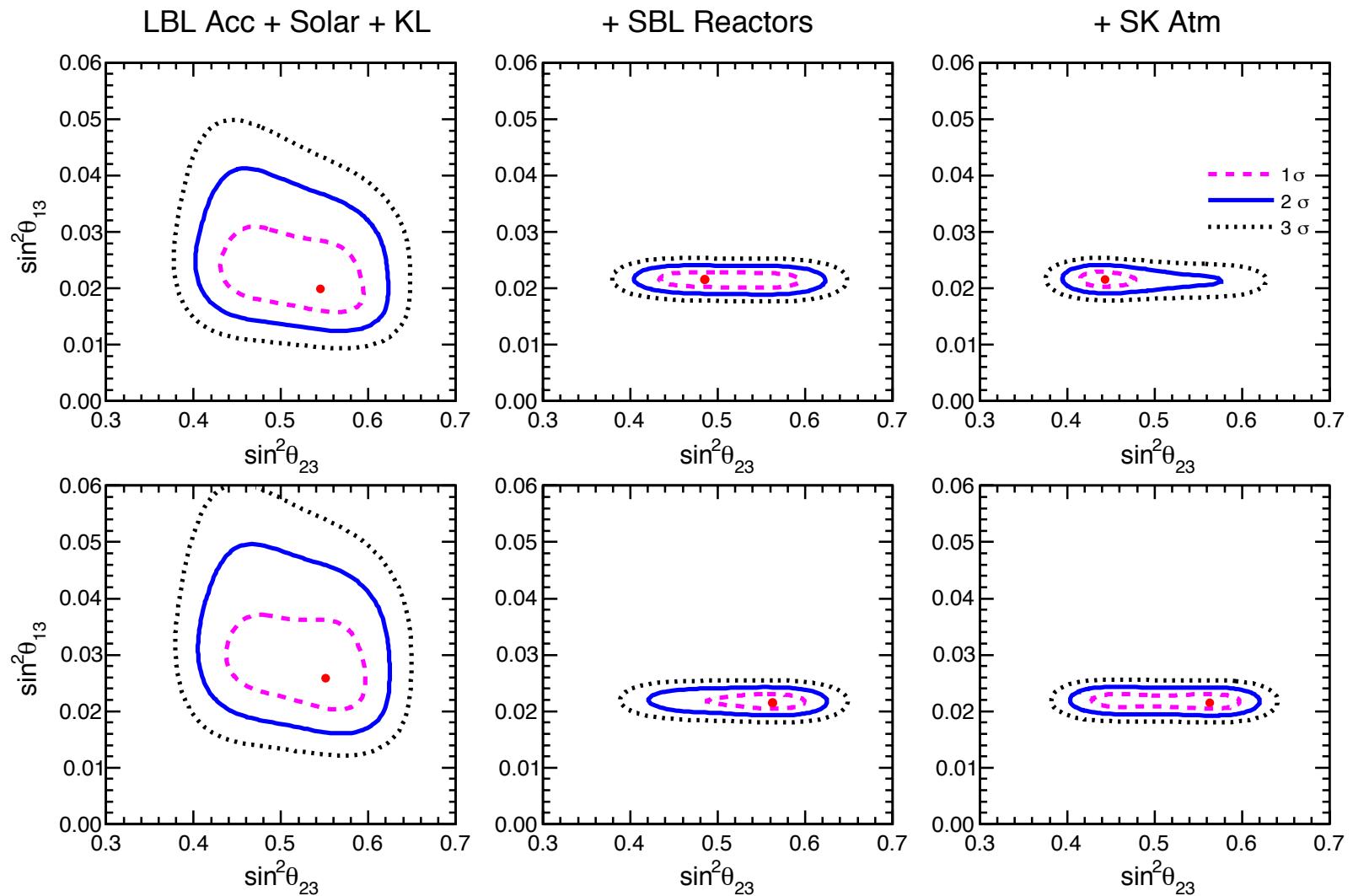
Shou  
Longevity

# **Additional slides**

# $(\theta_{13}, \delta)$ covariance plot



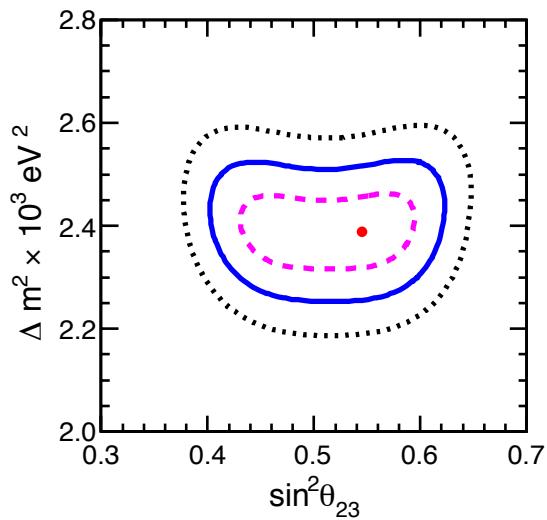
Current CP hint apparently stable for increasingly rich data sets.  
In combination,  $\delta/\pi \sim 1.4$  and  $\sin\delta < 0$  favored in both hierarchies.



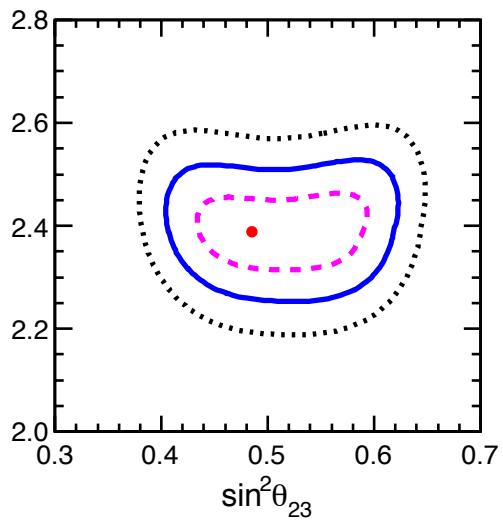
Normal Hierarchy

Inverted Hierarchy

LBL Acc + Solar + KL



+ SBL Reactors



+ SK Atm

