

Review of crosstalk between beam-beam interaction and lattice nonlinearity in e^+e^- colliders

ZHANG Yuan(IHEP), ZHOU Demin(KEK)

Outline

- DAFNE
- DAFNE upgrade
- KEKB
- Super-KEKB
- BEPCII

- DAFNE

DAFNE: Cubic lattice nonlinearity

Only one IP

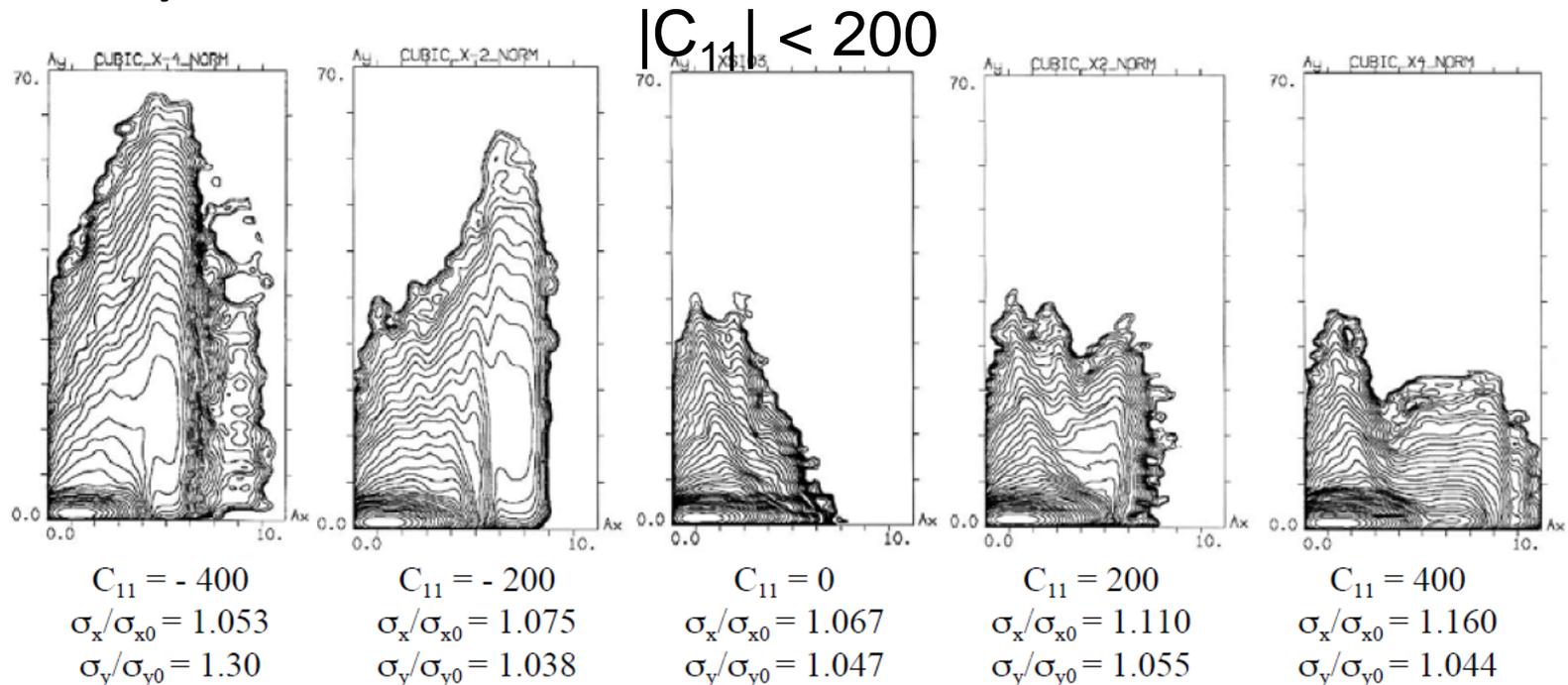


Figure 3. Beam-beam blow up and tail growth as a function of the cubic lattice nonlinearity (numerical simulations). Equilibrium density contour plots in the space of normalised betatron amplitudes are shown.

$$\Delta v_x = 2c_{11}J_x$$

DAFNE: Cubic lattice nonlinearity

One IP + 2 nearest PC

$$c_{11} = -350$$

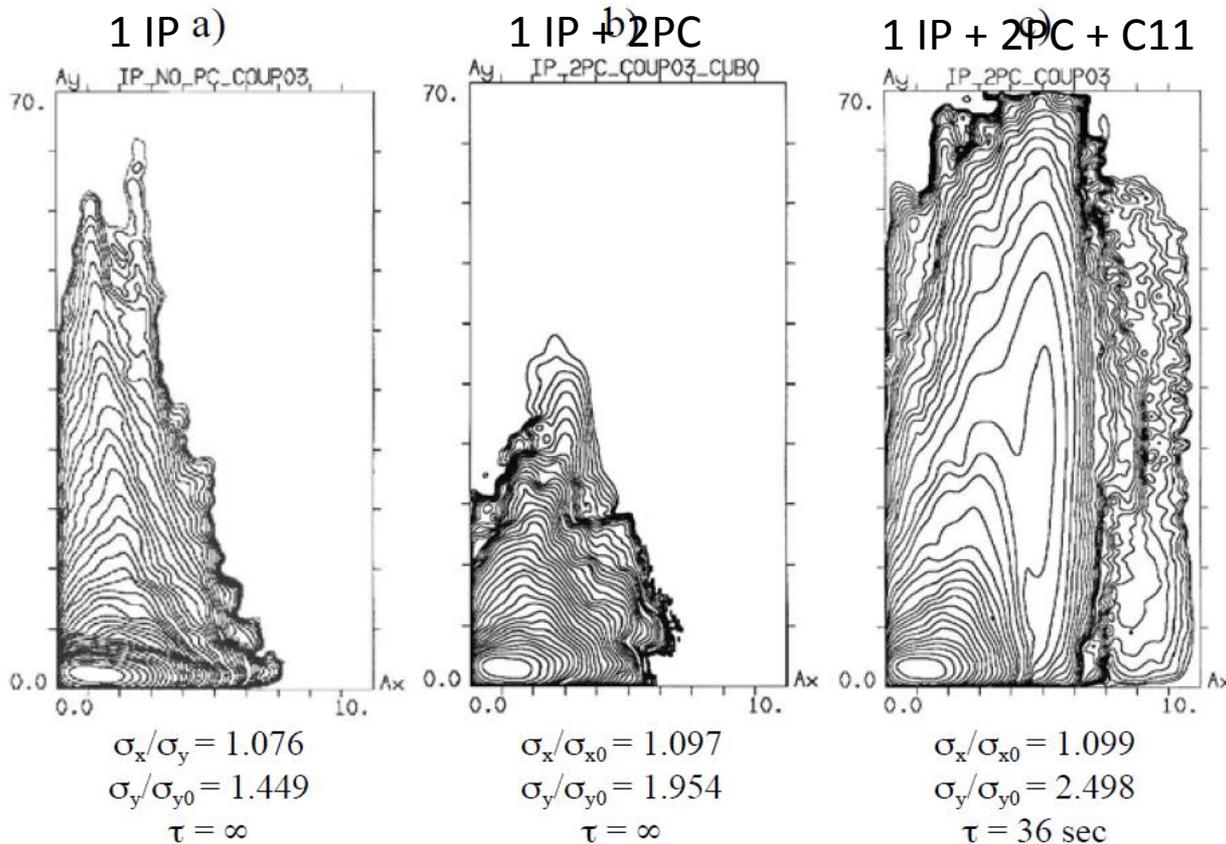
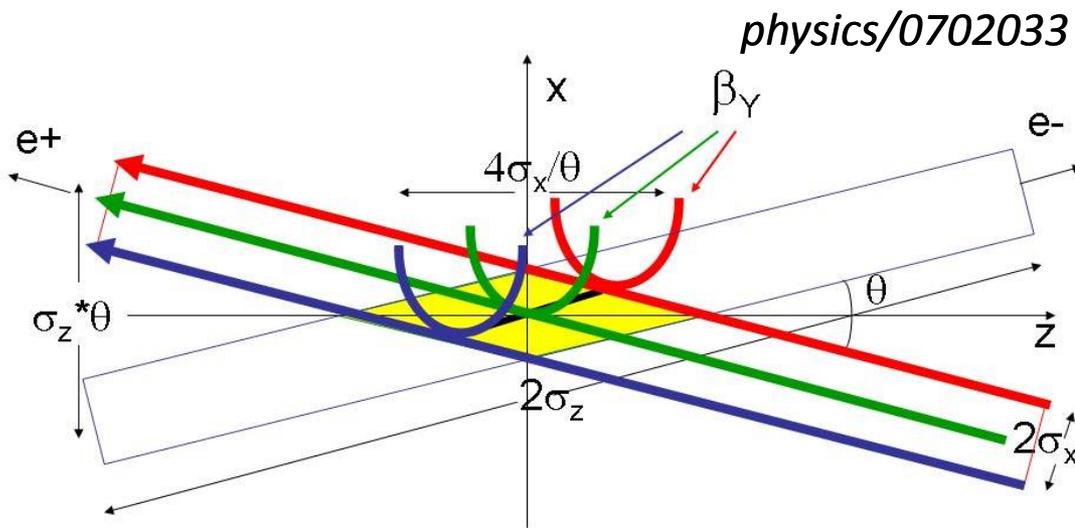


Figure 4. Equilibrium density contour plots taking into account 2 Parasitic Crossings and lattice nonlinearities.

- DAFNE-Upgrade

Crab Waist in 3 Steps

1. Large Piwinski's angle $\Phi = \text{tg}(\theta/2)\sigma_z/\sigma_x$
2. Vertical beta comparable with overlap area $\beta_y \approx 2\sigma_x/\theta$
3. Crab waist transformation $y = xy'/\theta$



1. P.Raimondi, 2° SuperB Workshop, March 2006

2. P.Raimondi, D.Shatilov, M.Zobov, physics/0702033



Crabbed Waist Advantages

1. Large Piwinski's angle

$$\Phi = \text{tg}(\theta/2)\sigma_z/\sigma_x$$

- a) Luminosity gain with N
- b) Very low horizontal tune shift
- c) Vertical tune shift decreases with oscillation amplitude

2. Vertical beta comparable with overlap area

$$\beta_y \approx 2\sigma_x/\theta$$

- a) Geometric luminosity gain
- b) Lower vertical tune shift
- c) Suppression of vertical synchro-betatron resonances

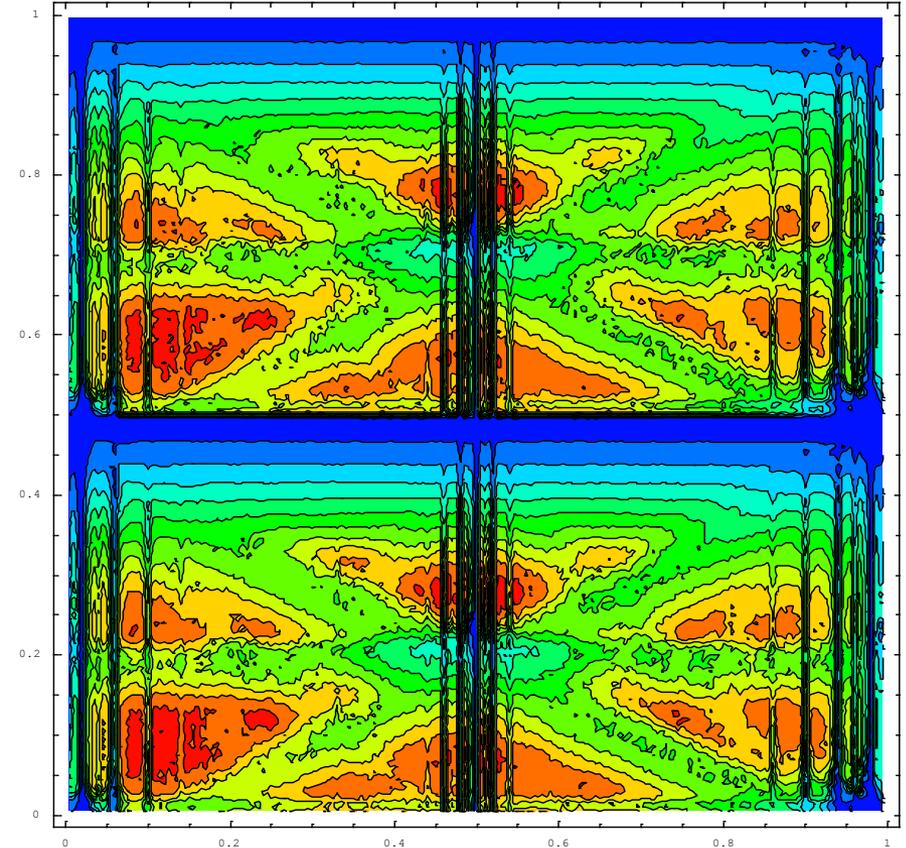
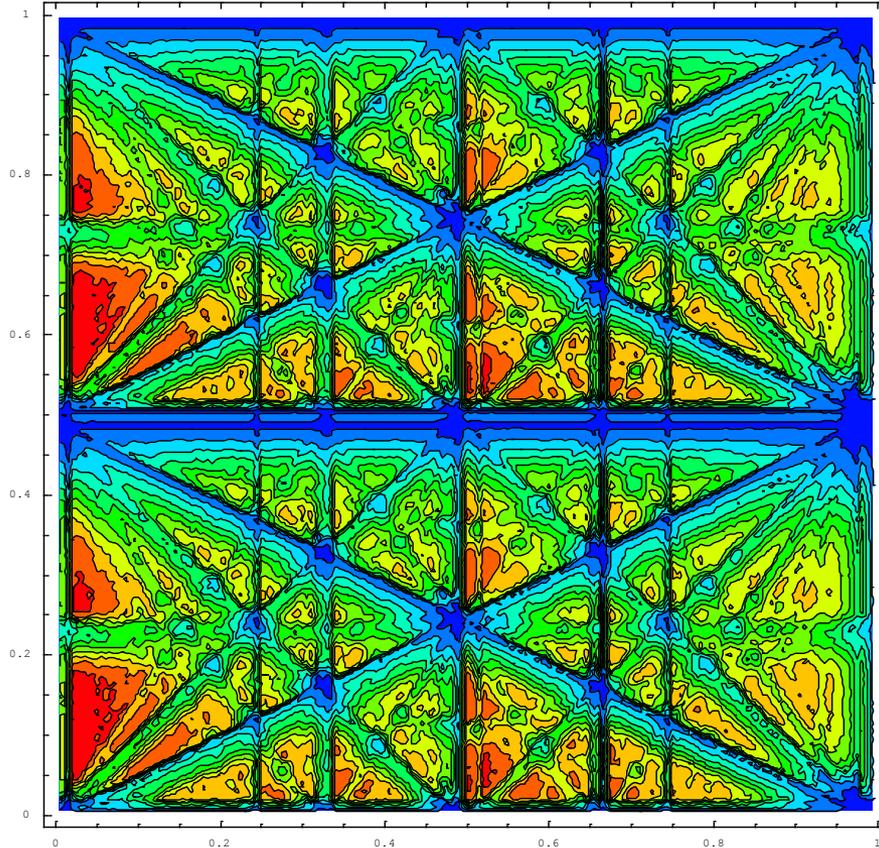
3. Crabbed waist transformation

$$y = xy'/\theta$$

- a) Geometric luminosity gain
- b) **Suppression of X-Y betatron and synchro-betatron resonances**

X-Y Resonance Suppression

Much higher luminosity!



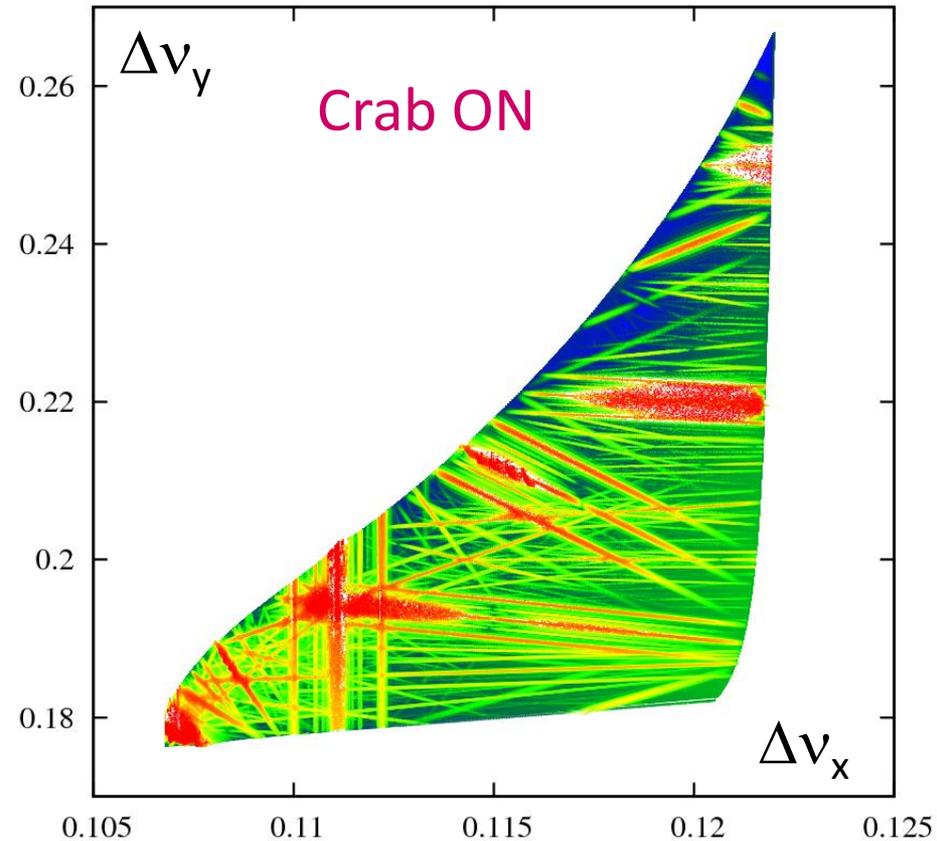
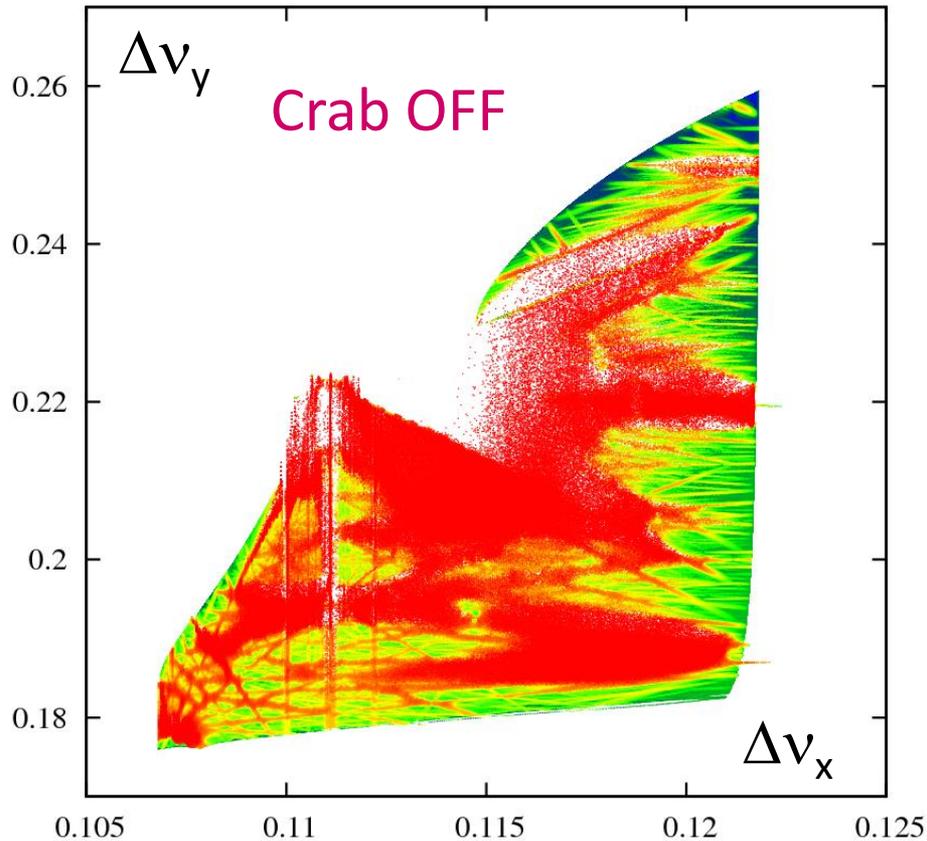
Typical case (KEKB, DAΦNE etc.):

1. low Piwinski angle $\Phi < 1$
2. β_y comparable with σ_z

Crab Waist On:

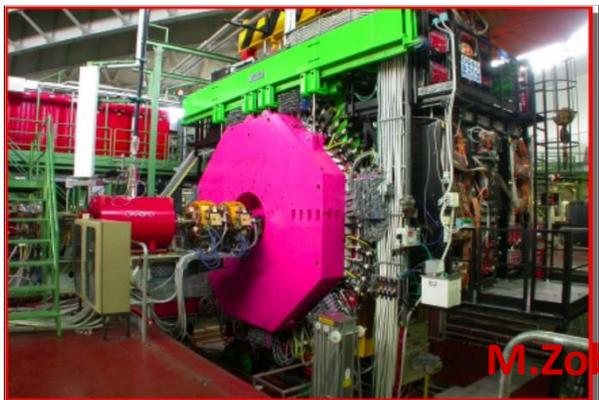
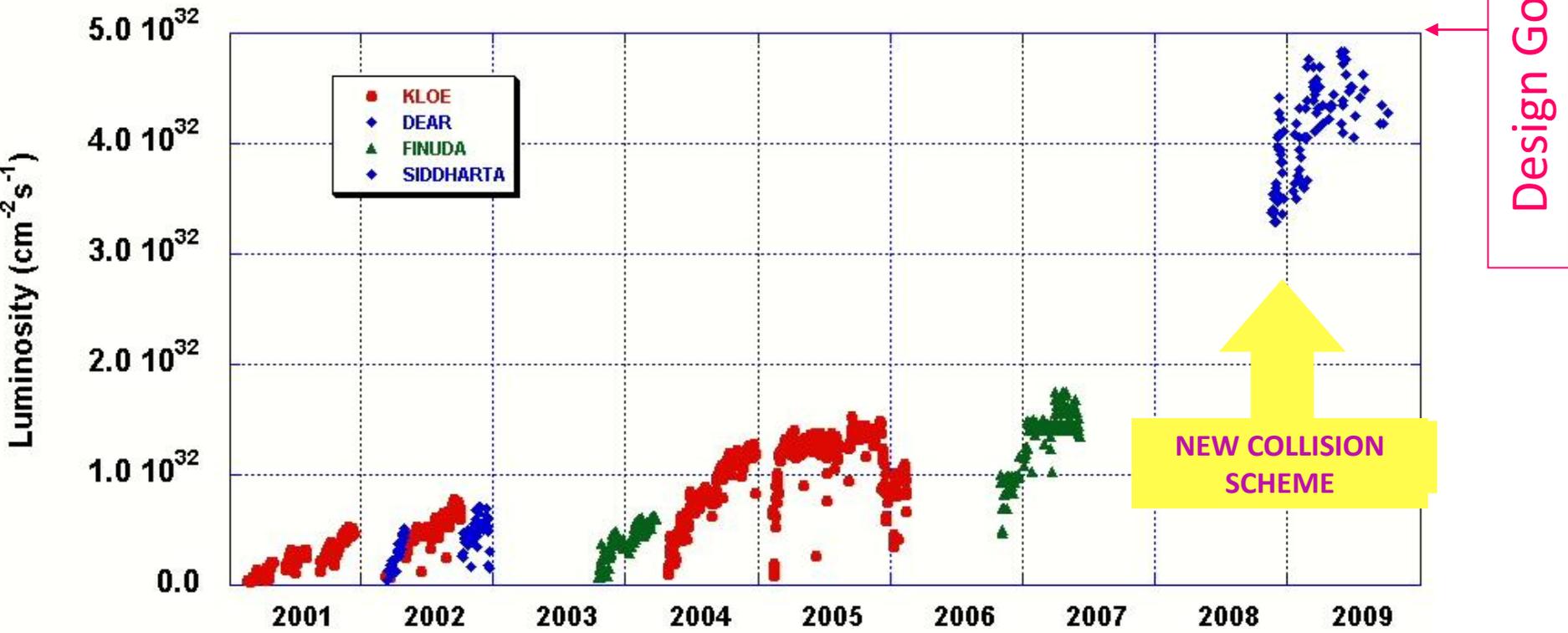
1. large Piwinski angle $\Phi \gg 1$
2. β_y comparable with σ_x/θ

Frequency Map Analysis of Beam-Beam Interaction

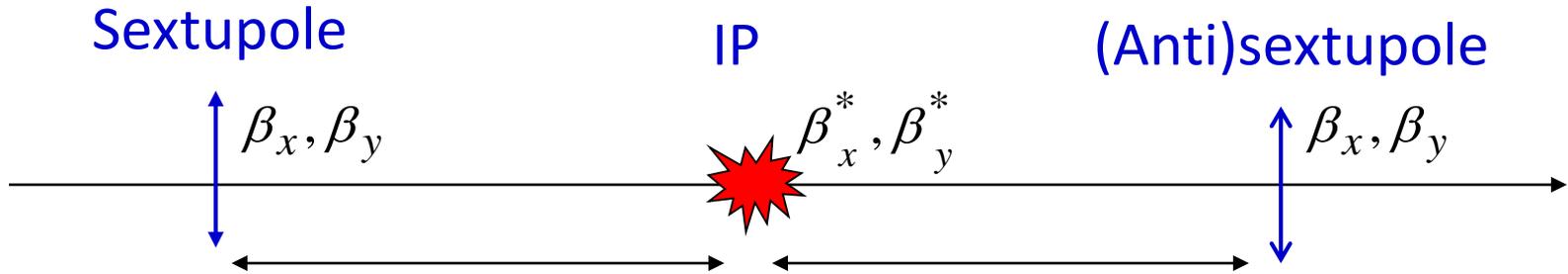


D.Shatilov, E.Levichev, E.Simonov and M.Zobov
Phys.Rev.ST Accel.Beams 14 (2011) 014001

DAΦNE Peak Luminosity



Crabbed Waist Scheme



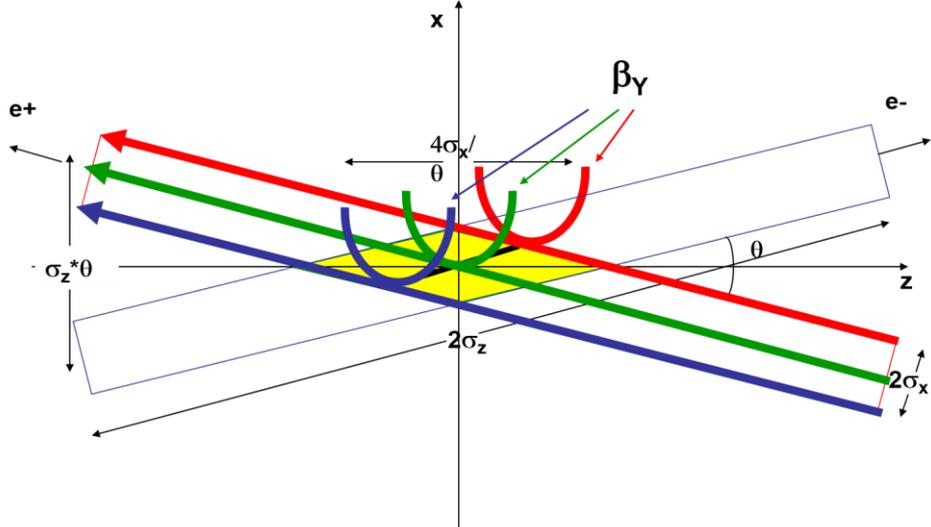
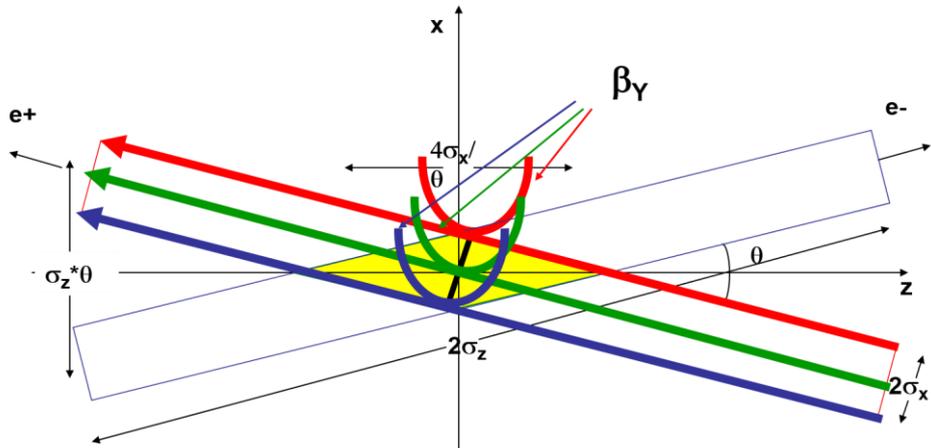
Sextupole strength

$$K = \frac{1}{2\theta} \frac{1}{\beta_y^* \beta_y} \sqrt{\frac{\beta_x^*}{\beta_x}}$$

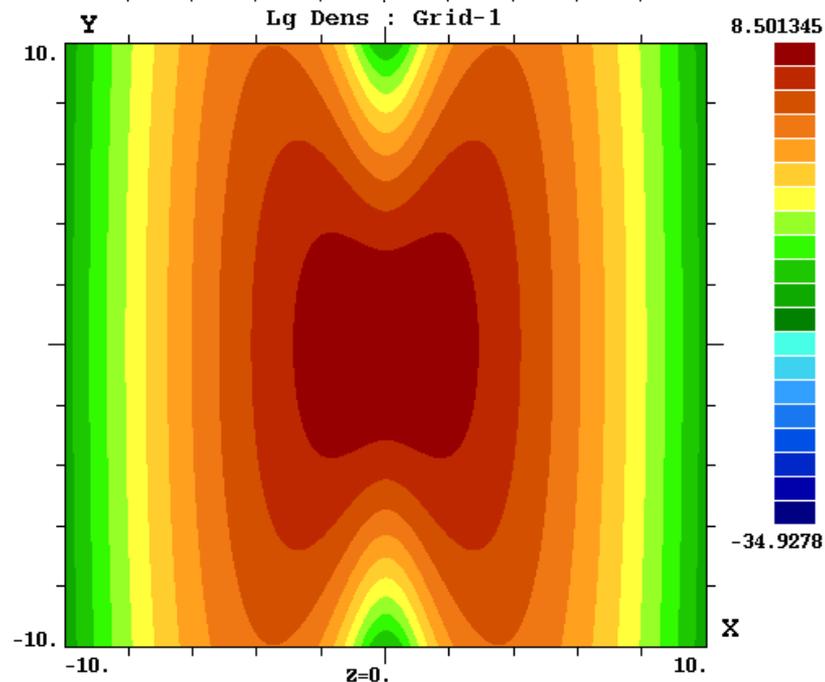
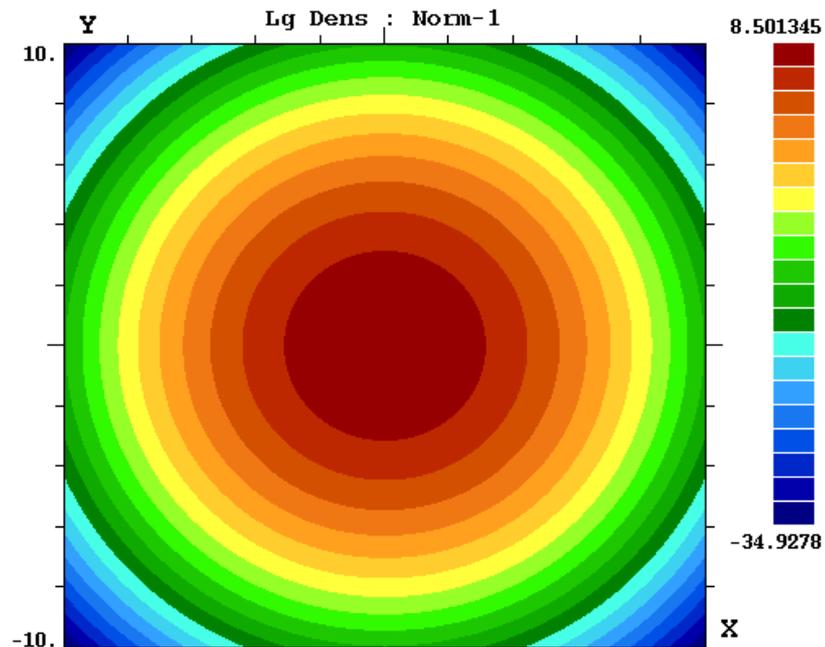
Equivalent Hamiltonian

$$H = H_0 + \frac{1}{2\theta} xp_y^2$$

$$\beta_y = \beta_y^* + \frac{(s - x/\theta)^2}{\beta_y^*}$$



Logarithm of the bunch density at IP ($z=0$).
The scales are ± 10 sigma for X and Y.



Normal form analysis of crabed- wasit transformtaion

- One-turn map with beam-beam

$$\exp(: -axp_y^2 :) \exp(: H_{bb} :) \exp(: axp_y^2 :) \exp(: H_{arc} :)$$

- One-turn map without beam-beam at IP

$$\exp(: axp_y^2 :) \exp(: H_{arc} :) \exp(: -axp_y^2 :)$$

$$\exp: f_2(X) : \exp: f_3(X) : \exp: f_4(X) :$$

$$f_3 = \exp: -f_2(X) : bxp_y^2 - bxp_y^2$$

$$= b(\cos \mu_x x - \sin \mu_x p_x)(\sin \mu_y y + \cos \mu_y p_y)^2 - bxp_y^2$$

$$f_4 = -\frac{1}{2} : \exp: -f_2(X) : bxp_y^2 : bxp_y^2$$

There only exist 3rd order generating function:

$$\begin{aligned} F_3 = & (-235.7 + 3.200564813177209 \times 10^{-15}i)e^{-i\phi_x} \sqrt{A_x A_y} \\ & - (235.7 + 3.200564813177209 \times 10^{-15}i)e^{i\phi_x} \sqrt{A_x A_y} \\ & + (117.85 + 4.947431353485854 \times 10^{-15}i)e^{-i\phi_x - 2i\phi_y} \sqrt{A_x A_y} \\ & + (117.85 + 2.779027008514845 \times 10^{-15}i)e^{i\phi_x - 2i\phi_y} \sqrt{A_x A_y} \\ & + (117.85 - 2.779027008514845 \times 10^{-15}i)e^{-i\phi_x + 2i\phi_y} \sqrt{A_x A_y} \\ & + (117.85 - 4.947431353485854 \times 10^{-15}i)e^{i\phi_x + 2i\phi_y} \sqrt{A_x A_y} \end{aligned}$$

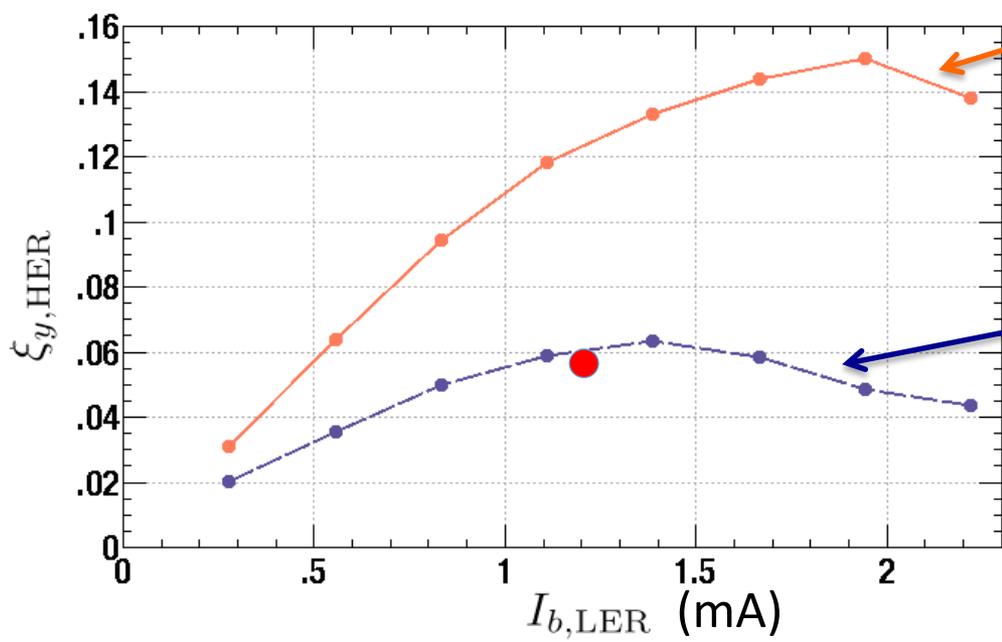
以工作点 $Q_x/Q_y = 0.51/0.58$, $\beta_x/\beta_y = 1.0/0.015$, $a = 10$ 为例,

- KEKB

Motivation of crab cavity at KEKB

Y. Funakoshi, Beam-Beam Workshop, CERN, 2013

- Crab Crossing can boost the beam-beam parameter higher than 0.15 ! (K. Ohmi)



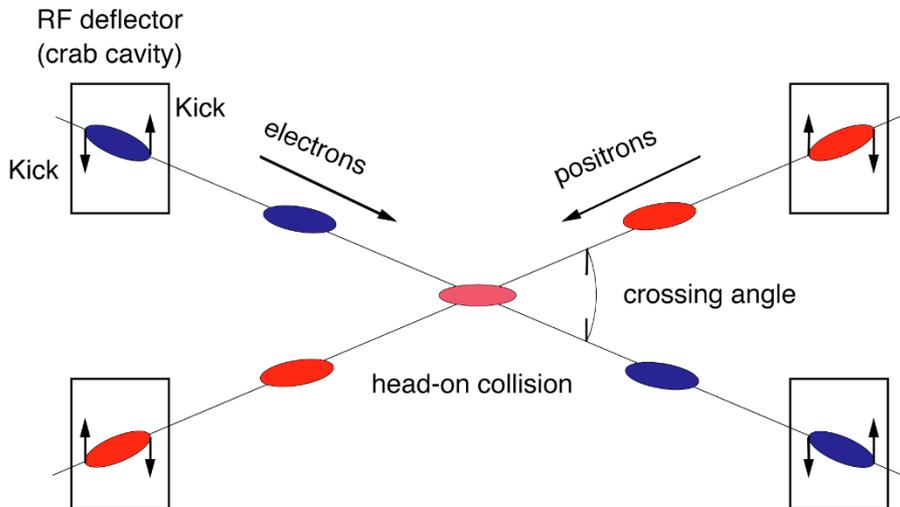
Head-on (crab)

Strong-strong beam-beam simulation

22mrad crossing angle

Head-on } $\rightarrow \xi_{y,HER} \sim 0.15$

$v_x = .508$

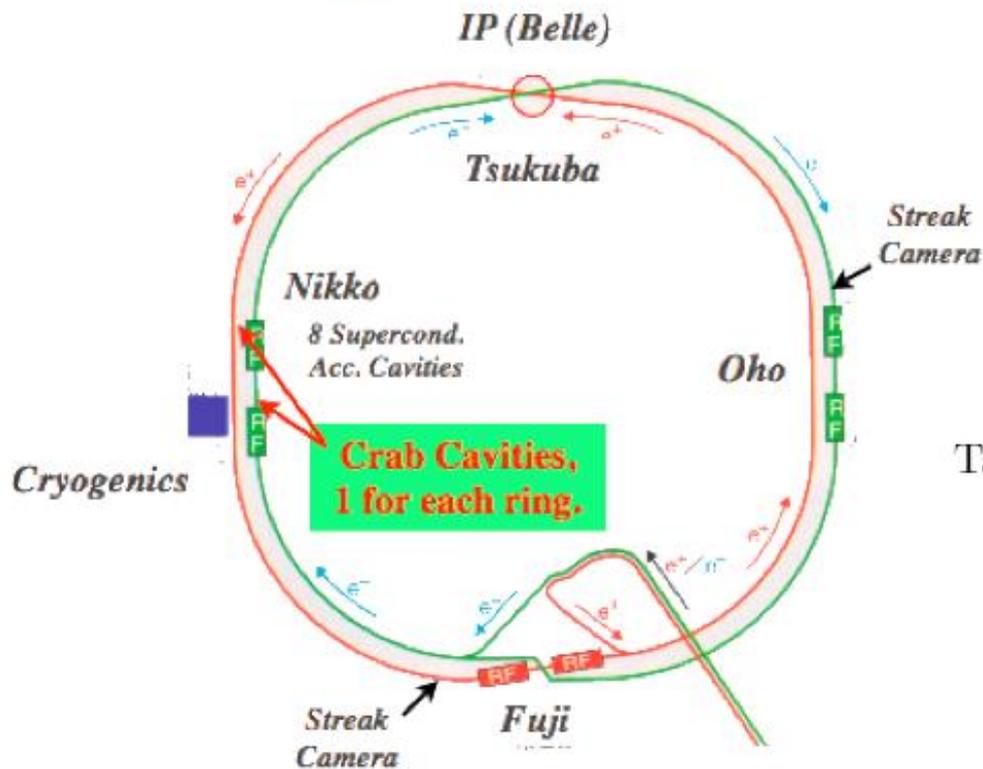


First proposed by R. B. Palmer in 1988 for linear colliders.

Luminosity would be doubled with crab cavities!!!

- After this simulation appeared, the development of crab cavities was revitalized.

Single Crab Cavity Scheme



Beam tilts all around the ring.
 z-dependent horizontal closed orbit.
 tilt at the IP:

$$\frac{\theta_x}{2} = \frac{\sqrt{\beta_x^C \beta_x^*} \cos(\psi_x^C - \mu_x/2) V_C \omega_{rf}}{2 \sin(\mu_x/2) E_c}$$

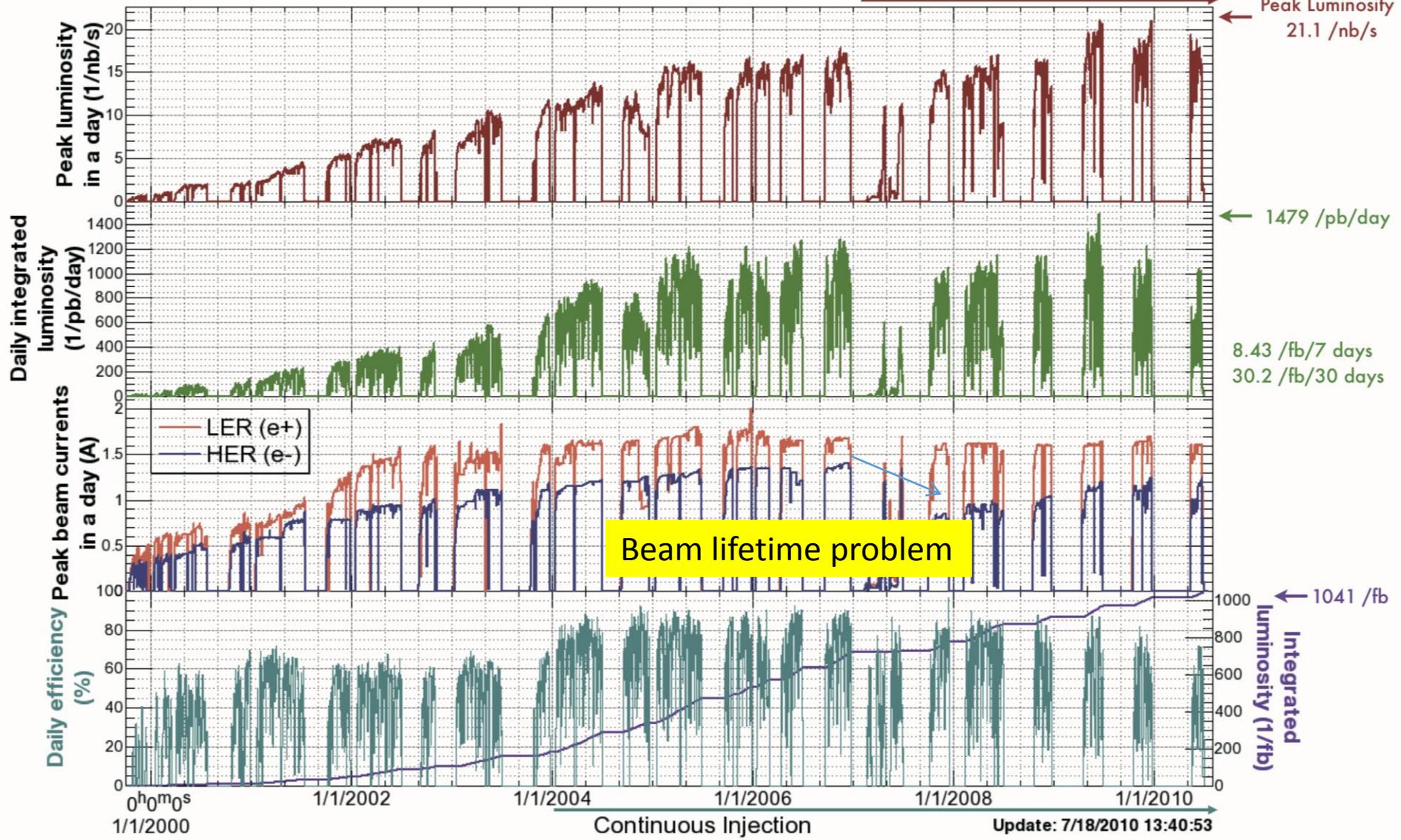
Table 1: Typical parameters for the crab crossing.

Ring	LER	HER	
θ_x	22		mrad
β_x^*	80	80	cm
β_x^C	73	162	m
$\mu_x/2\pi$	0.505	0.511	
$\psi_x^C/2\pi$	~ 0.25	~ 0.25	
V_C	0.95	1.45	V
$\omega_{rf}/2\pi$	509		MHz

- * 1 crab cavity per ring.
- * saves the cost of the cavity and cryogenics.
- * avoids synchrotron radiation hitting the cavity.

Skew-sextupoles

Luminosity of KEKB Oct. 1999 - June 2010



General Chromaticity

The chromaticities of Twiss parameters and X-Y couplings

$$\alpha_u(\delta) = \sum_{i=0}^{\infty} \alpha_{ui} \delta^i \quad \beta_u(\delta) = \sum_{i=0}^{\infty} \beta_{ui} \delta^i$$

$$\nu_u(\delta) = \sum_{i=0}^{\infty} \nu_{ui} \delta^i \quad r_j(\delta) = \sum_{i=0}^{\infty} r_{ji} \delta^i$$

$$u = x, y \quad \text{and} \quad j = 1, 2, 3, 4,$$

The δ -dependent transverse matrix can be split into the product of two matrices. All the chromatic dependences are lumped into $M_H(\delta)$

$$M(\delta) = M(0)M_H(\delta)$$

Generating function F_2 is used to represent the transformation of $M_H(\delta)$. The generating function guarantees the 6D symplectic condition. Hamiltonian which expresses generalized chromaticity is given by

$$F_2(q_i, \bar{p}_i, z, \bar{\delta}) = x\bar{p}_x + y\bar{p}_y + z\bar{\delta} + H_I(x, \bar{p}_x, y, \bar{p}_y, \bar{\delta})$$

$$H_I(x, \bar{p}_x, y, \bar{p}_y, \bar{\delta}) \quad (1)$$

$$= \sum_{n=1}^{\infty} (a_n x^2 + 2b_n x \bar{p}_x + c_n \bar{p}_x^2 + 2d_n x y + 2e_n x \bar{p}_y + 2f_n y \bar{p}_x + 2g_n \bar{p}_x \bar{p}_y + u_n y^2 + 2v_n y \bar{p}_y + w_n \bar{p}_y^2) \bar{\delta}^n / 2.$$

Alternative way is the direct map for the betatron variables $\mathbf{x} = (x, p_x, y, p_y)^T$ and z as

$$\mathbf{x}(s+L) = M_4(\delta)\mathbf{x}(s).$$

$$z(s+L) = z(s) + \mathbf{x}^t M_4^t(\delta) S_4 \partial_\delta M_4(\delta) \mathbf{x} / 2$$

Measurement of chromatic coupling

HER

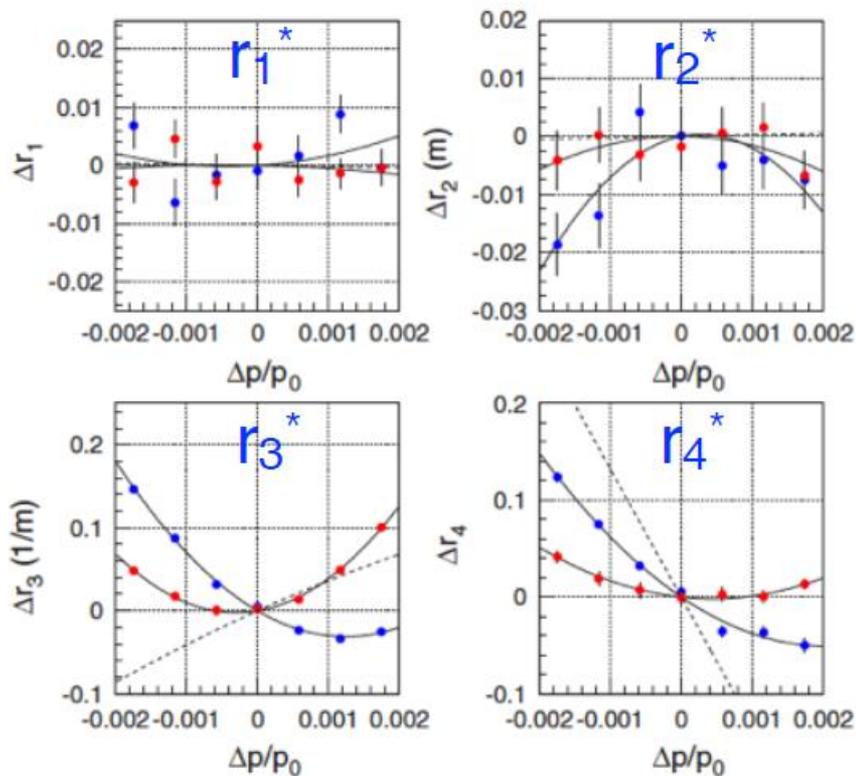


FIG. 3. (Color) Measured chromatic X-Y coupling at IP in HER. The blue plots indicate those before and the red plots indicate those after the skew sextupole correction. The dashed line indicates the natural chromatic X-Y coupling estimated using the model lattice by SAD.

LER

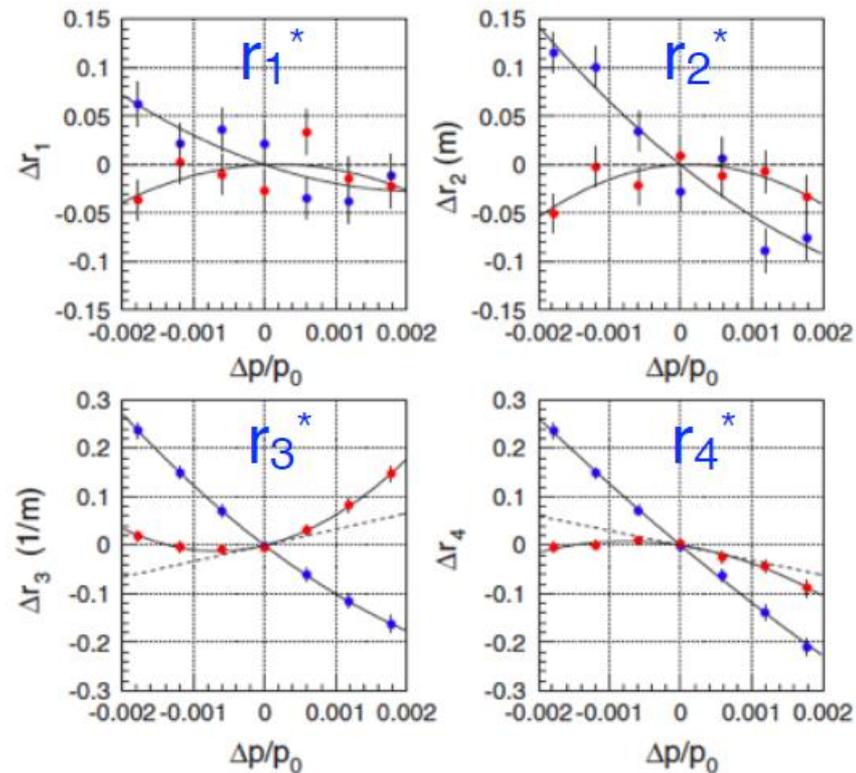
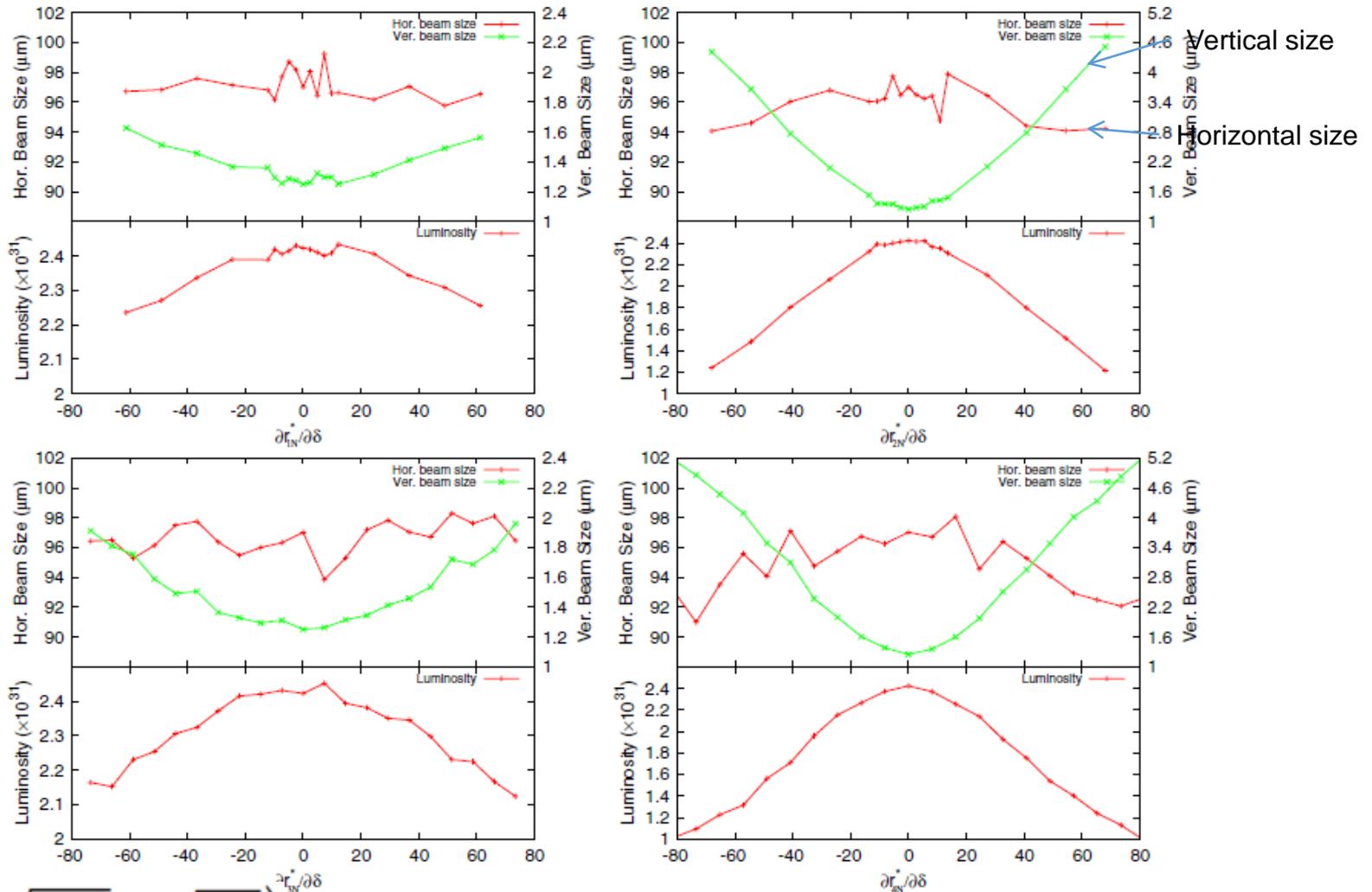


FIG. 4. (Color) Measured chromatic X-Y coupling at IP in LER. The blue plots indicate those before and the red plots indicate those after the skew sextupole correction. The dashed line indicates the natural chromatic X-Y coupling estimated using the model lattice by SAD.

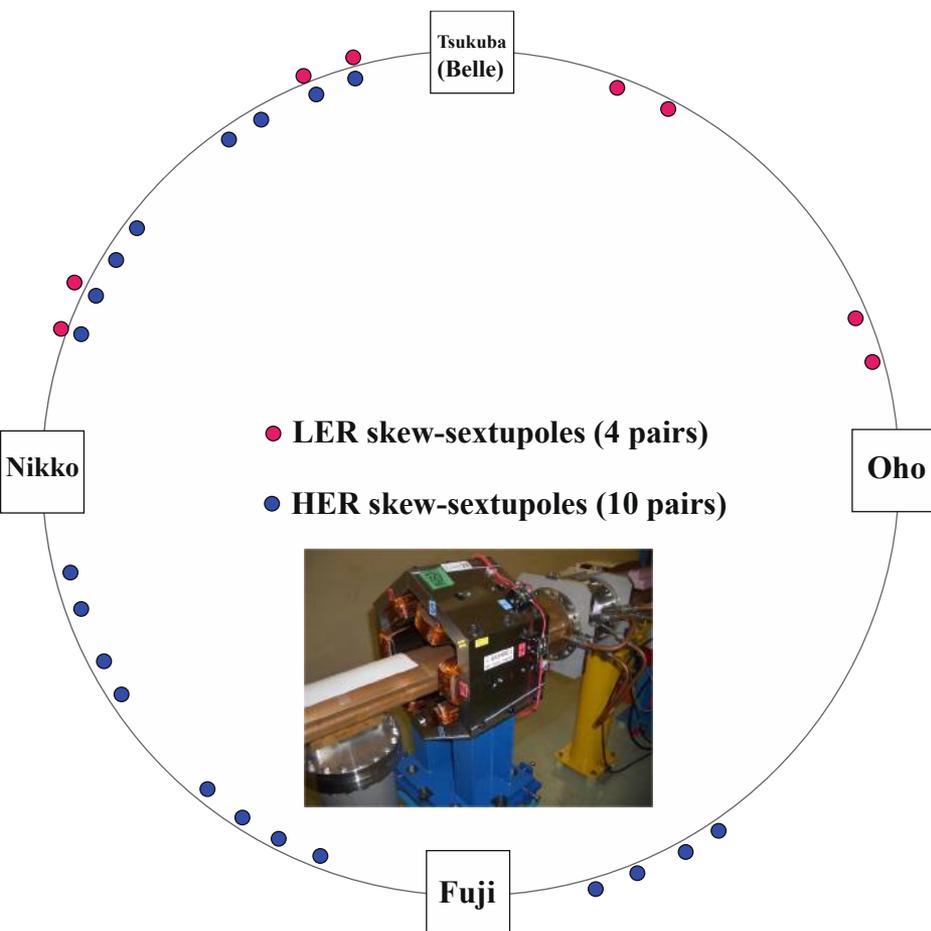
Scan of first-order chromatic coupling (WS, Crab on)

D. Zhou, et al., PRST--AB 13, 021001 (2010).



$$\begin{pmatrix} r_{1N}^* & r_{2N}^* \\ r_{3N}^* & r_{4N}^* \end{pmatrix} = \begin{pmatrix} r_1^* \sqrt{\beta_x^*/\beta_y^*} & r_2^*/\sqrt{\beta_x^*\beta_y^*} \\ r_3^* \sqrt{\beta_x^*\beta_y^*} & r_4^* \sqrt{\beta_y^*/\beta_x^*} \end{pmatrix} \quad \text{G. 8. (Color) Scan of first-order chromaticity of X-Y couplings at the IP.}$$

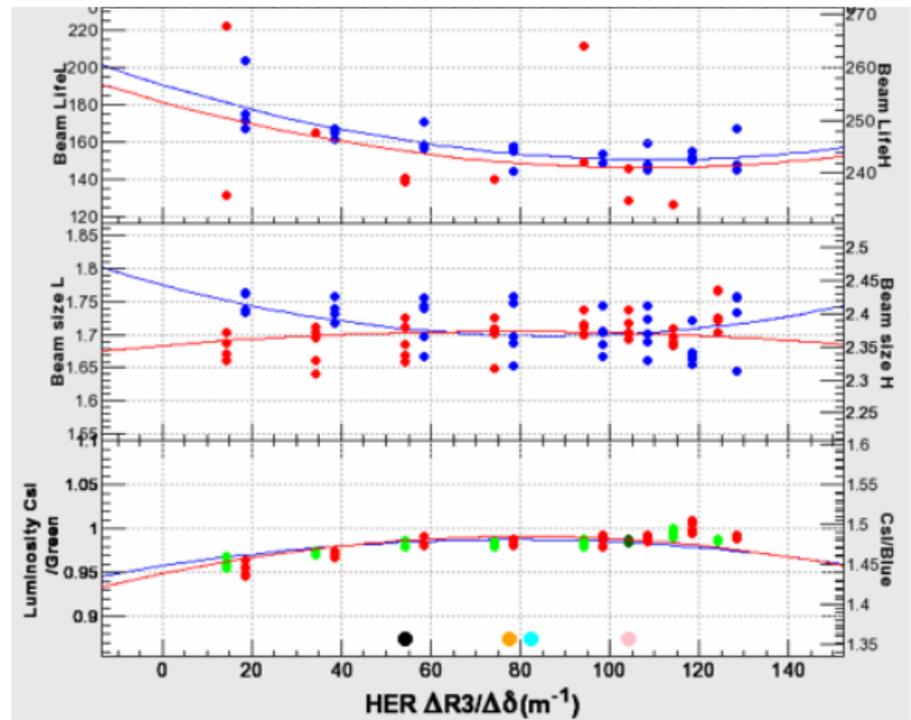
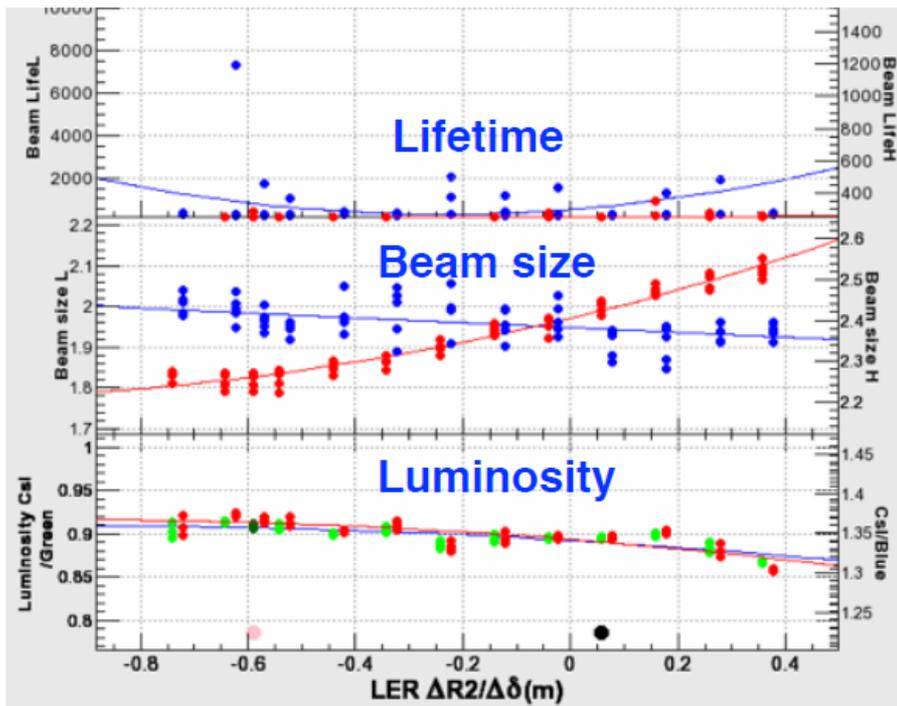
Chromaticity of x-y coupling at IP



- Ohmi et al. showed that the linear chromaticity of x-y coupling parameters at IP could degrade the luminosity, if the residual values, which depend on machine errors, are large.
- To control the chromaticity, skew sextupole magnets were installed during winter shutdown 2009.
- The skew sextuples are very effective to increase the luminosity at KEKB.
- The gain of the luminosity by these magnets is ~15%.

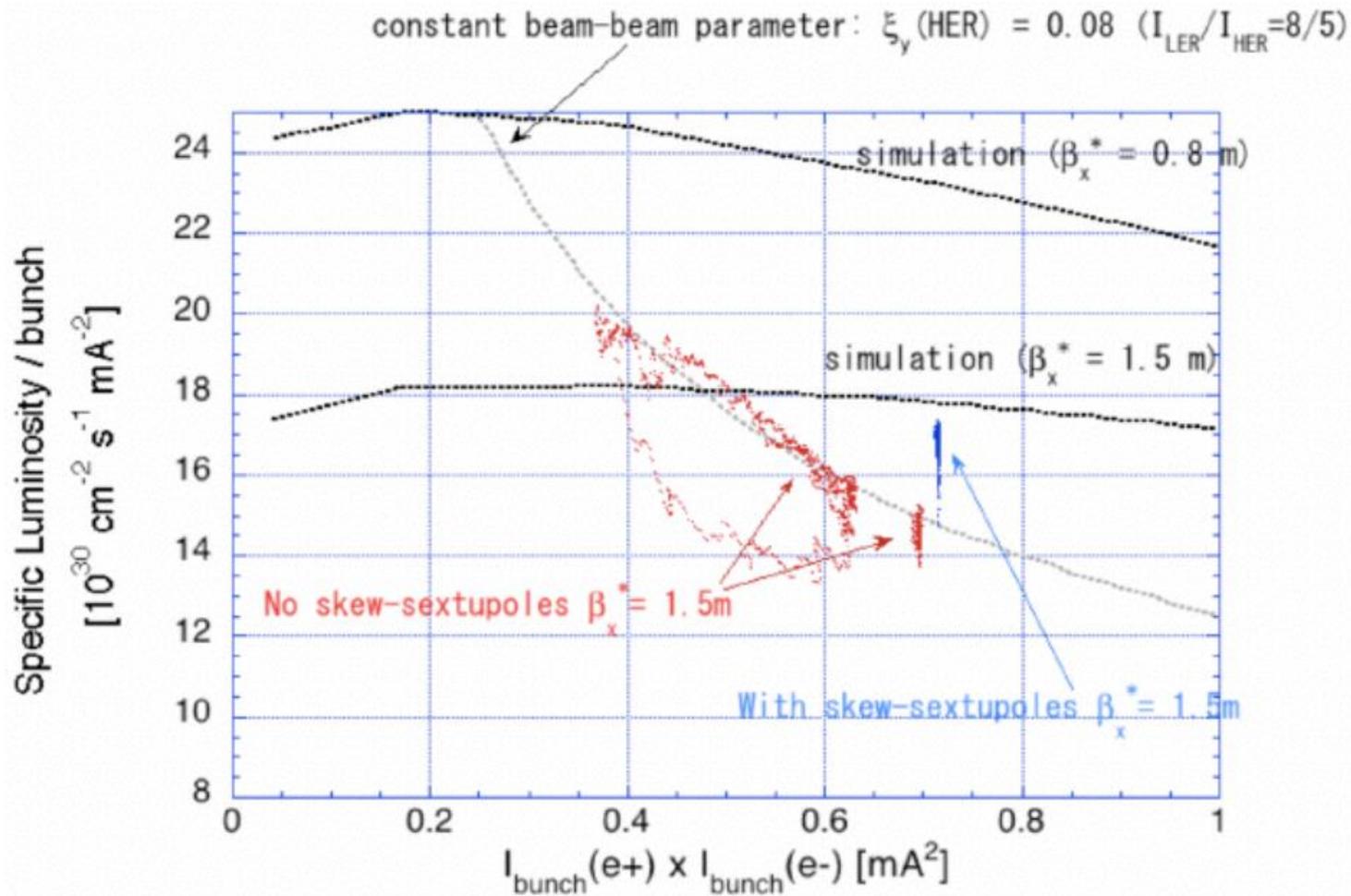
Experimental observations

The first scans of chromatic coupling at IP during the KEKB operation:



Experimental observations (cont'd)

Skew-sextupole tuning was very effective w/ crab on ...

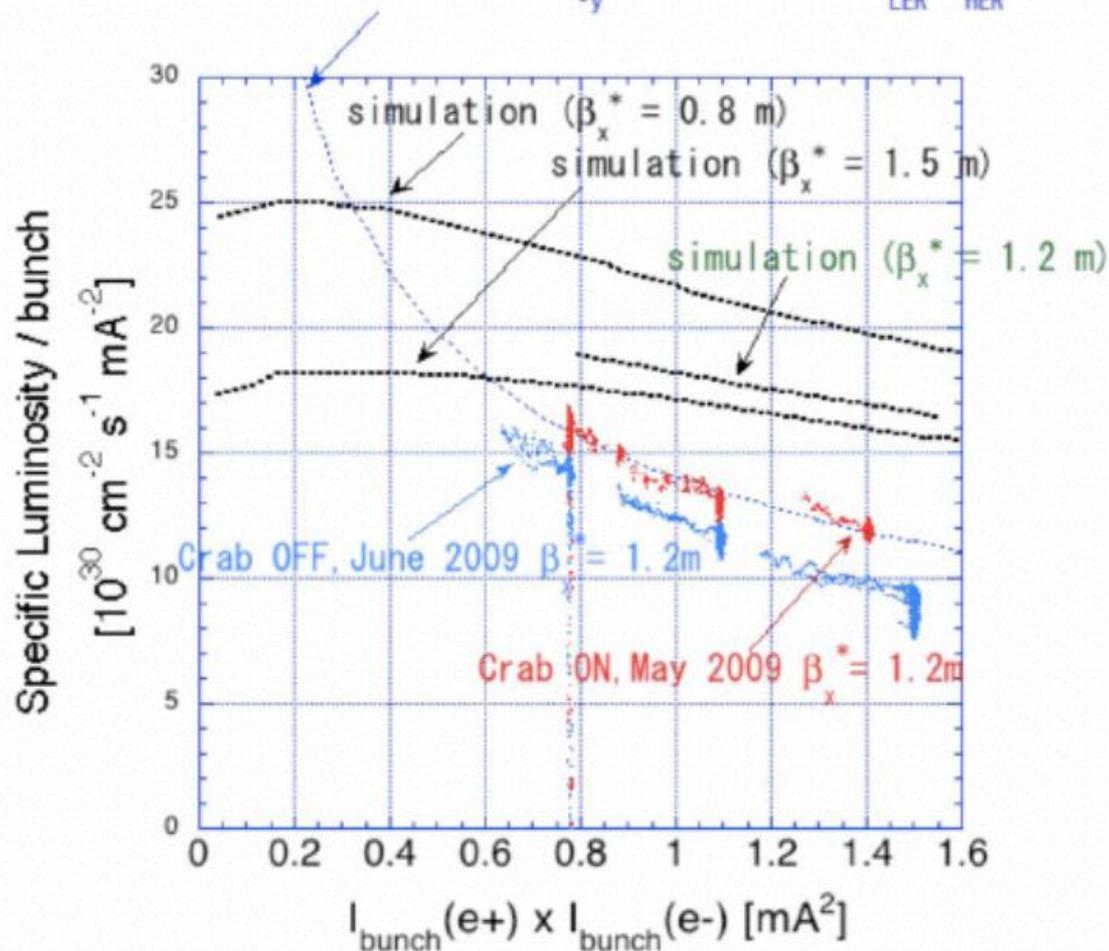


Experimental observations (cont'd)

Specific lum. w/ crab on and w/ skew-sext. tuning optimized

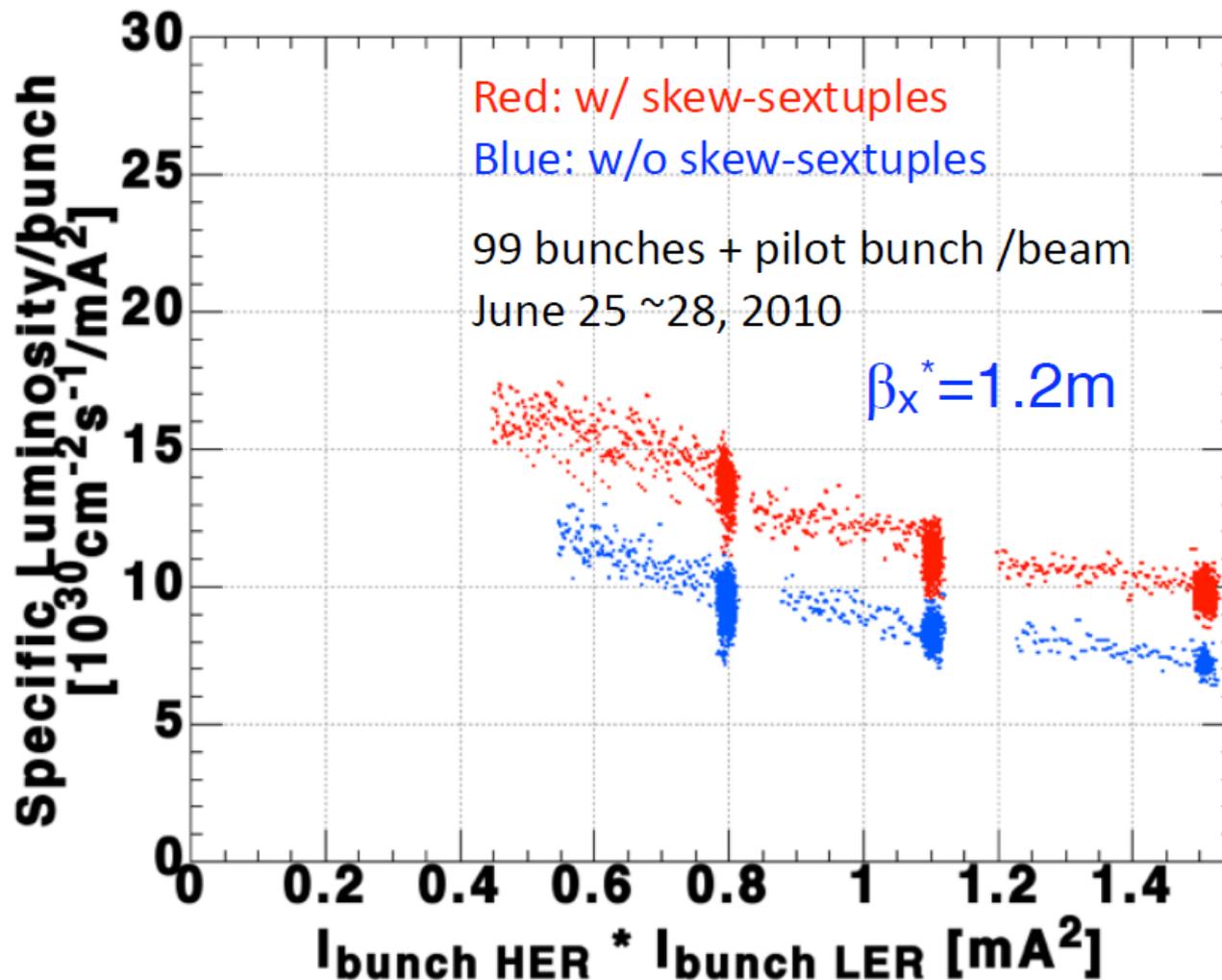
Lum. gain from crab cavities: ~20%, Lum. gain from skew-sext.: ~15%

constant beam-beam parameter: $\xi_y(\text{HER}) = 0.09$ ($I_{\text{LER}}/I_{\text{HER}}=8/5$)



Experimental observations (cont'd)

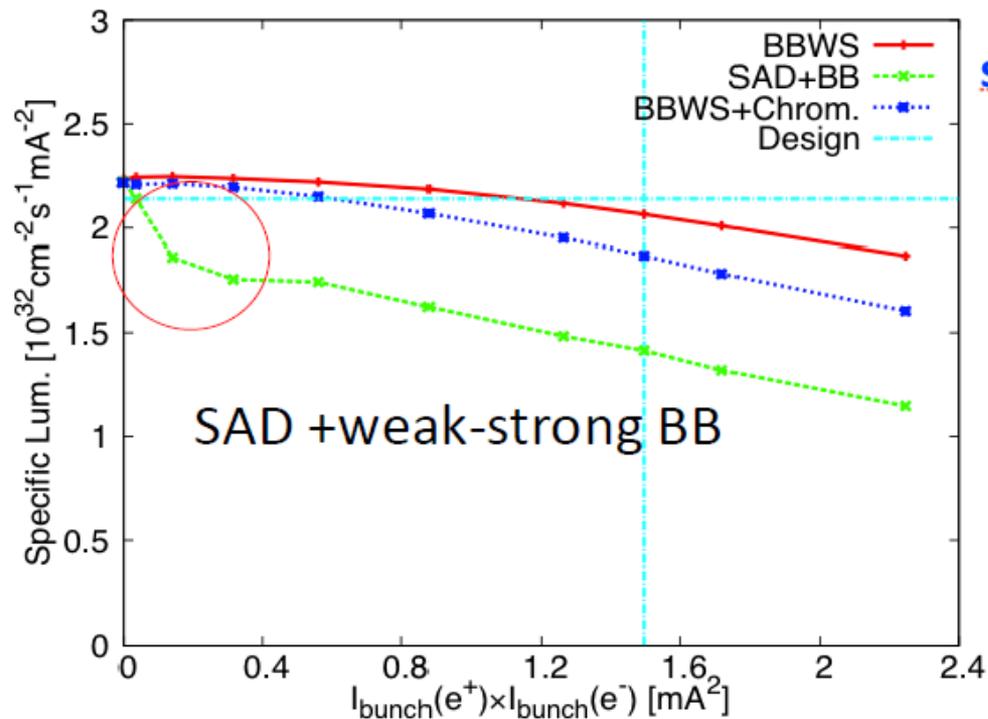
Skew-sextupole tuning was very effective even w/ crab off.
This was a surprise...



- Super-KEKB

Weak-strong Simulation for LER lattice

- Even low current, luminosity loss $\sim 20\%$ is seen.
- 30% loss at the design current.
- Chromatic effect can not explain the lum. Loss.

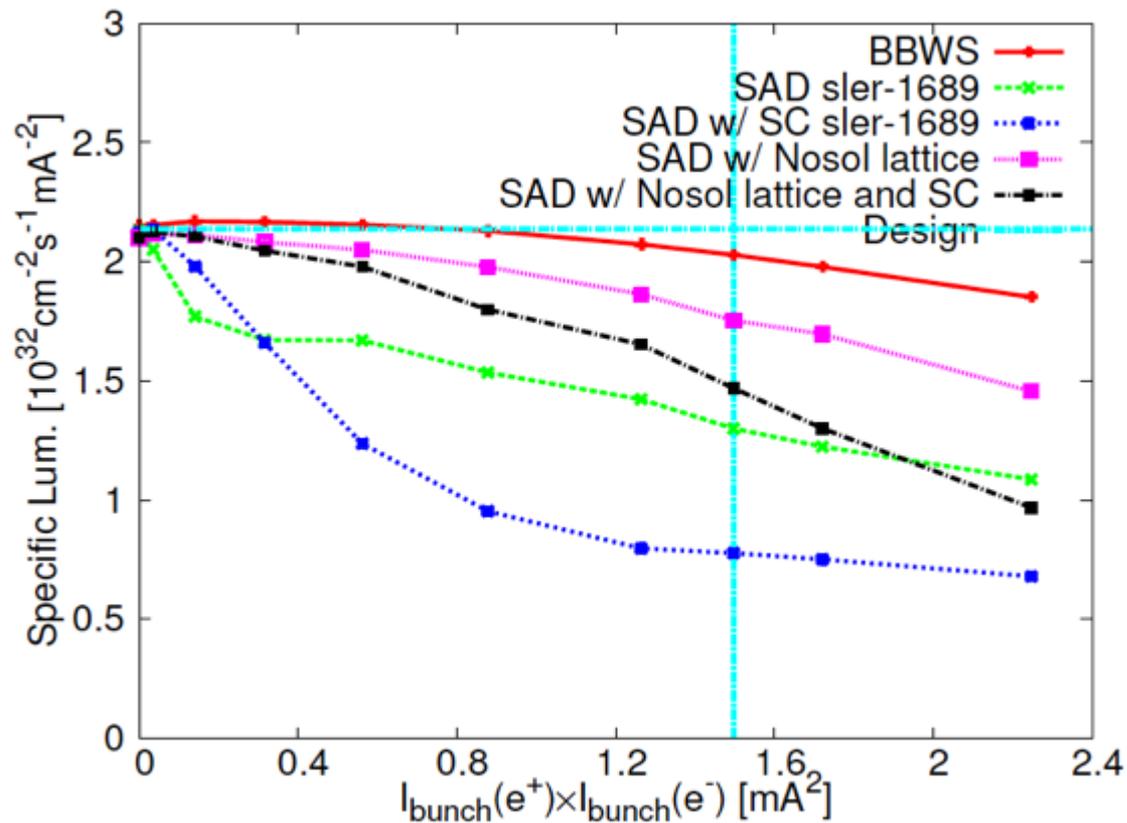


sler_1684

K. Ohmi, D. Zhou
SuperKEKB MAC2014, Mar 3-4, 2014

LER: Simplified IR

- Simplified lattice by H. Sugimoto
- Sler_simple001.sad: no solenoid but preserve main optics parameters
- No significant luminosity degradation at low current
- Solenoid is the main source of lattice nonlinearity?

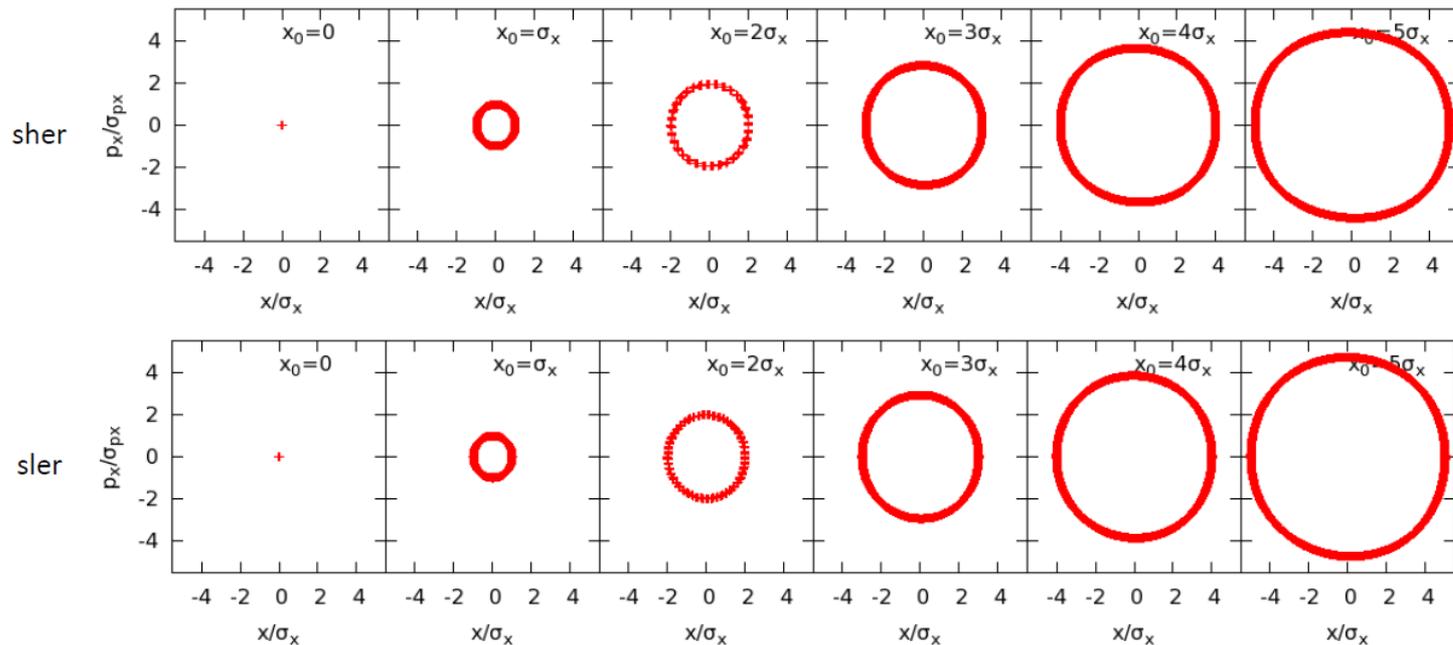


D. Zhou and Y. Zhang(IHEP),
SuperKEKB optics meeting,
Apr.17, 2014

Lattice nonlinearity from turn-by-turn data

- Initial coordinates $(x_0, 0, 0, 0, 0, 0)$;
- x_0 changes from 0 to $5\sigma_x$
- Watch point is at IP, beam-beam is off

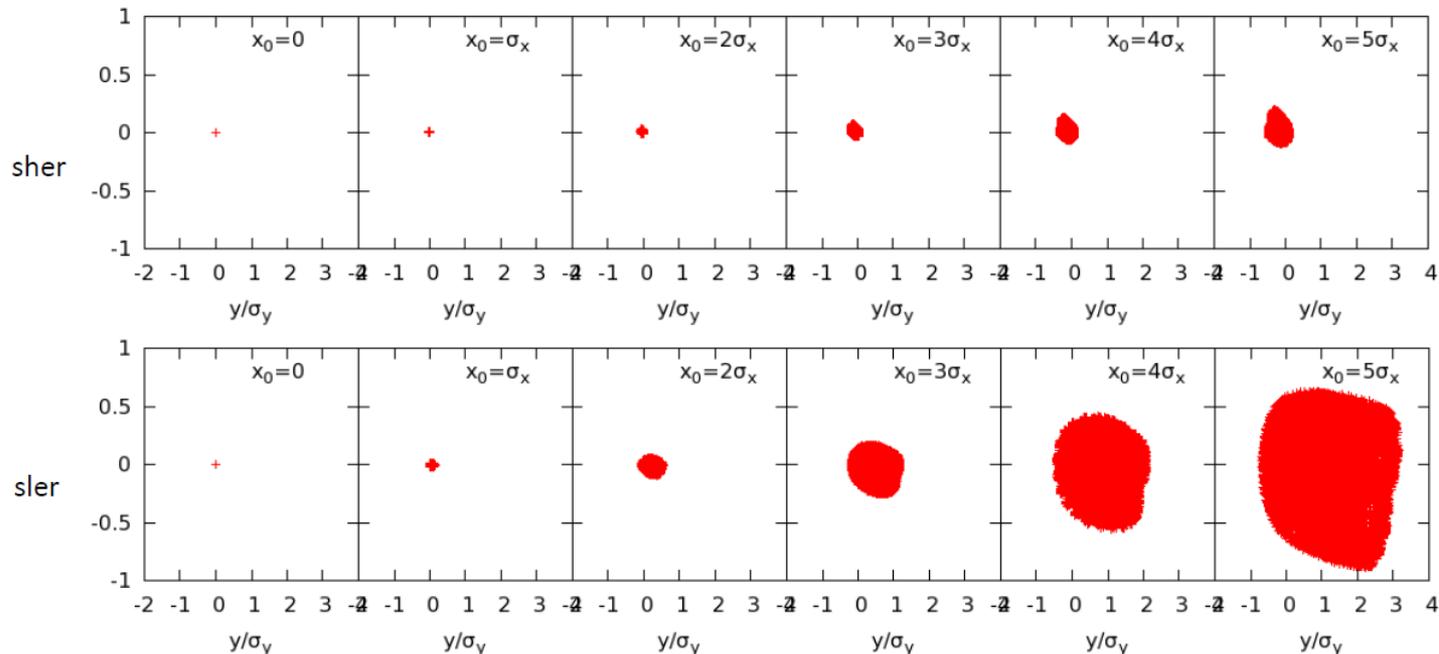
sher-5767 vs ler-1689 in X direction



Lattice nonlinearity from turn-by-turn data (Cont.)

- Evidence of nonlinear X-Y coupling
- COD in Y direction as function of X offset

sher-5767 vs ler-1689 in Y direction



Frequency Analysis

- Linear Normalized Coordinate

$$\hat{x} = \frac{x}{\sqrt{\beta_x}}, \hat{p}_x = p_x * \sqrt{\beta_x}$$

$$\hat{y} = \frac{y}{\sqrt{\beta_y}}, \hat{p}_y = p_y * \sqrt{\beta_y},$$

- Turn-by-Turn data could be represented by (with first order approximation)

$$\begin{aligned} \hat{x}(m) - i\hat{p}_x(m) &= \sqrt{2A_x} e^{i(m\mu_x + \phi_{x,0})} \\ &\quad - \sum_{abcd} 2iaf_{abcd}^{(3)} (2A_x)^{\frac{a+b-1}{2}} (2A_y)^{\frac{c+d}{2}} e^{i(b-a+1)(m\mu_x + \phi_{x,0})} e^{i(d-c)(m\mu_y + \phi_{y,0})} \end{aligned}$$

$$\begin{aligned} \hat{y}(m) - i\hat{p}_y(m) &= \sqrt{2A_y} e^{i(m\mu_y + \phi_{y,0})} \\ &\quad - \sum_{abcd} 2icf_{abcd}^{(3)} (2A_x)^{\frac{a+b}{2}} (2A_y)^{\frac{c+d-1}{2}} e^{i(b-a)(m\mu_x + \phi_{x,0})} e^{i(d-c+1)(m\mu_y + \phi_{y,0})} \end{aligned}$$

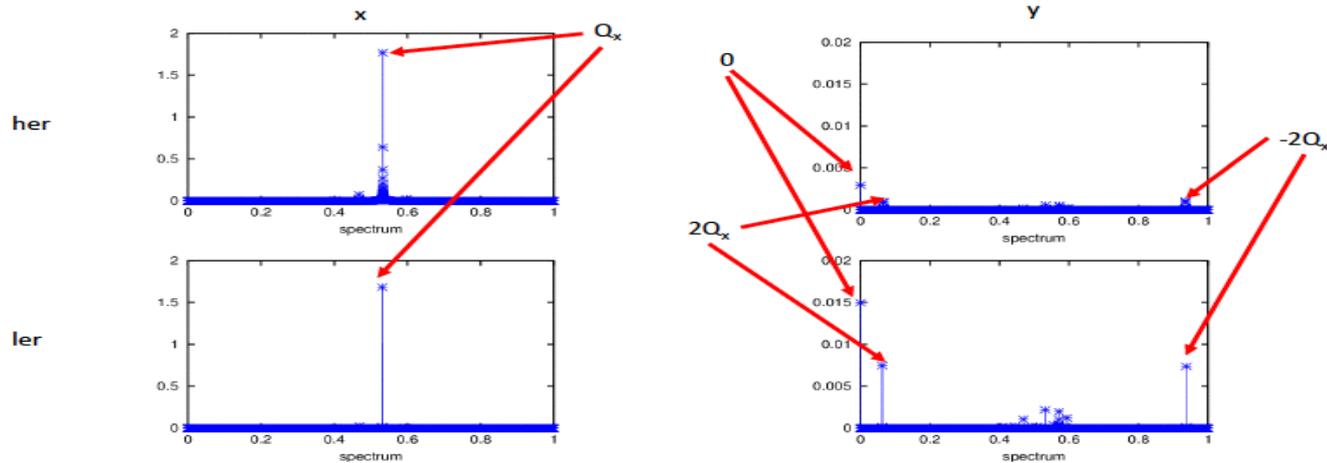
- FFT with

$$\hat{x} - i\hat{p}_x \text{ in x direction}$$

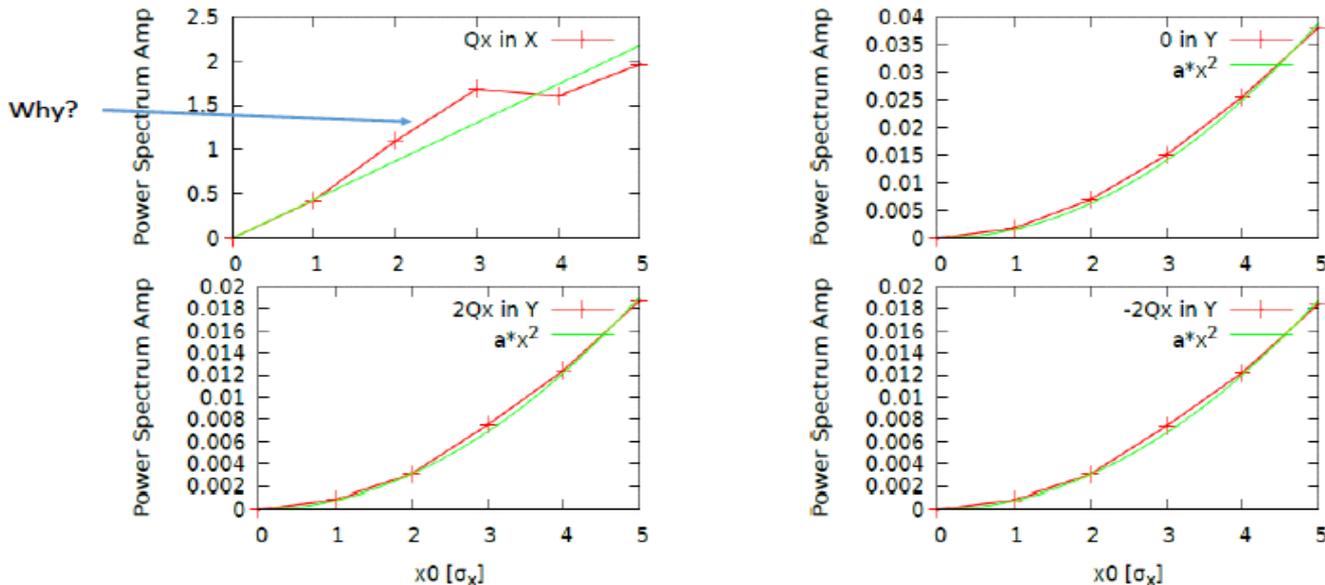
$$\hat{y} - i\hat{p}_y \text{ in y direction}$$

Frequency Analysis (cont.)

Spectrum ($x_0 = 3\sigma_x$)



Power spectrum analysis (LER)



- There exist very strong 'oscillation' at 0, 2Qx, -2Qx for LER
- It is suspected the cause is
 - f1110 -> 0 in vertical direction, the amplitude is proportional to $(2A_x)$
 - f0210 -> 2Qx in vertical direction, the amplitude is proportional to $(2A_x)$
 - f2010 -> -2Qx in vertical direction, the amplitude is proportional to $(2A_x)$

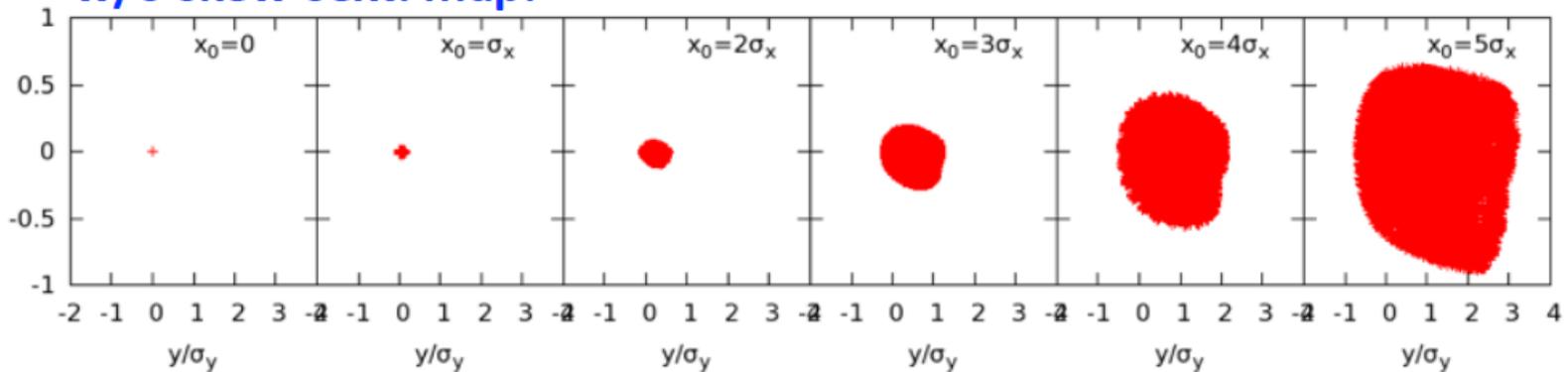
All these terms may come from a skew sextupole like magnet.

$$H \sim 3x^2y - y^3$$

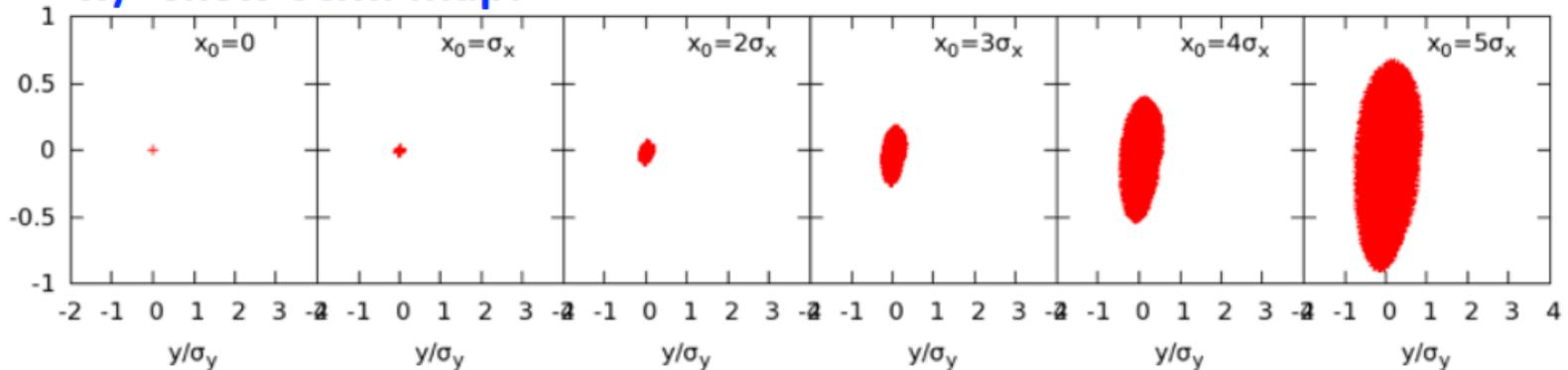
Compensation with a skew-sext map

- Test by inserting a map of $H=K*x^2y$ into the LER lattice
- COD and oscillation amplitude in y are well suppressed as expected

w/o skew-sext. map:



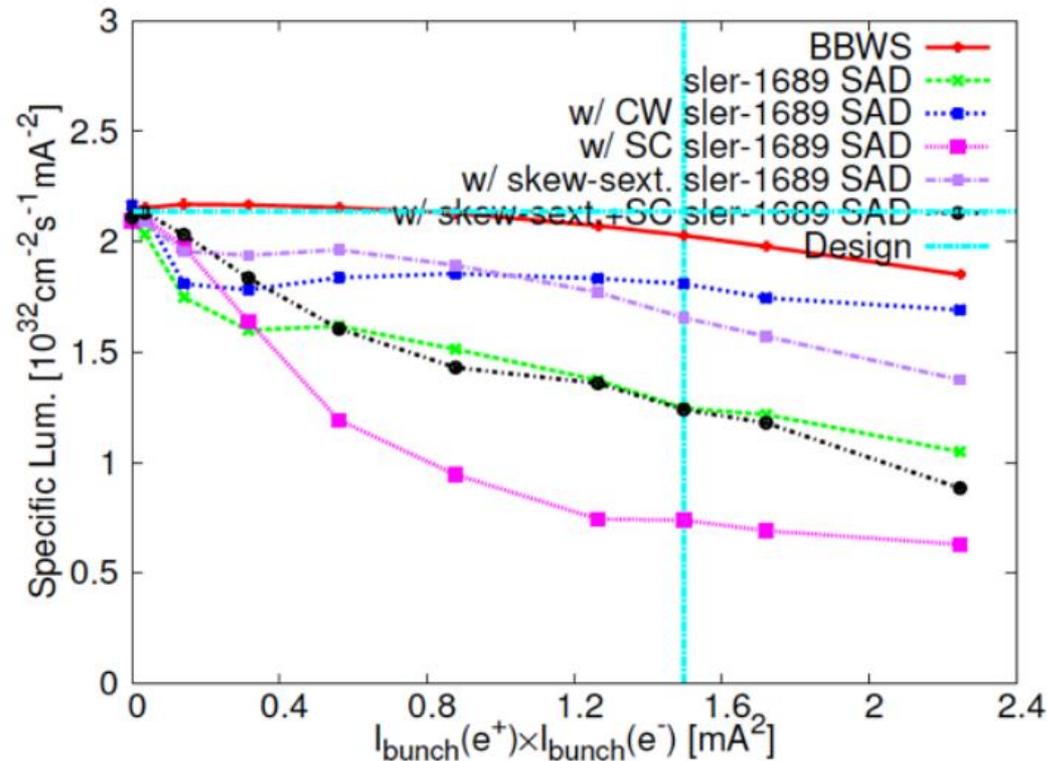
w/ skew-sext. map:



Compensation with a skew-sext map (Cont.)

► Skew-sext. map:

- to cancel the nonlinear term from solenoid
- work well at both low and high currents
- interplay of SC and lattice nonlin. also mitigated partially



Compensation with a skew-sext map (Cont.)

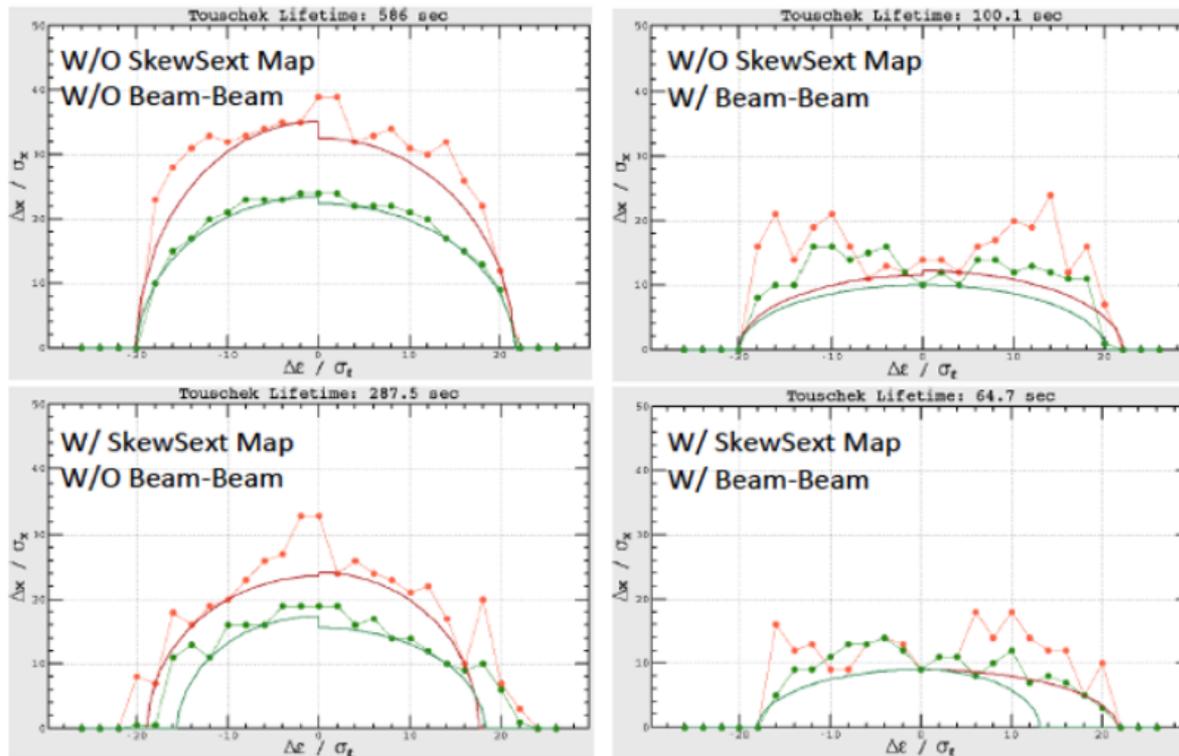
➤ Skew-sext. map:

- cause loss in DA and lifetime (to be understood)

sler_1689

DA and Lifetime

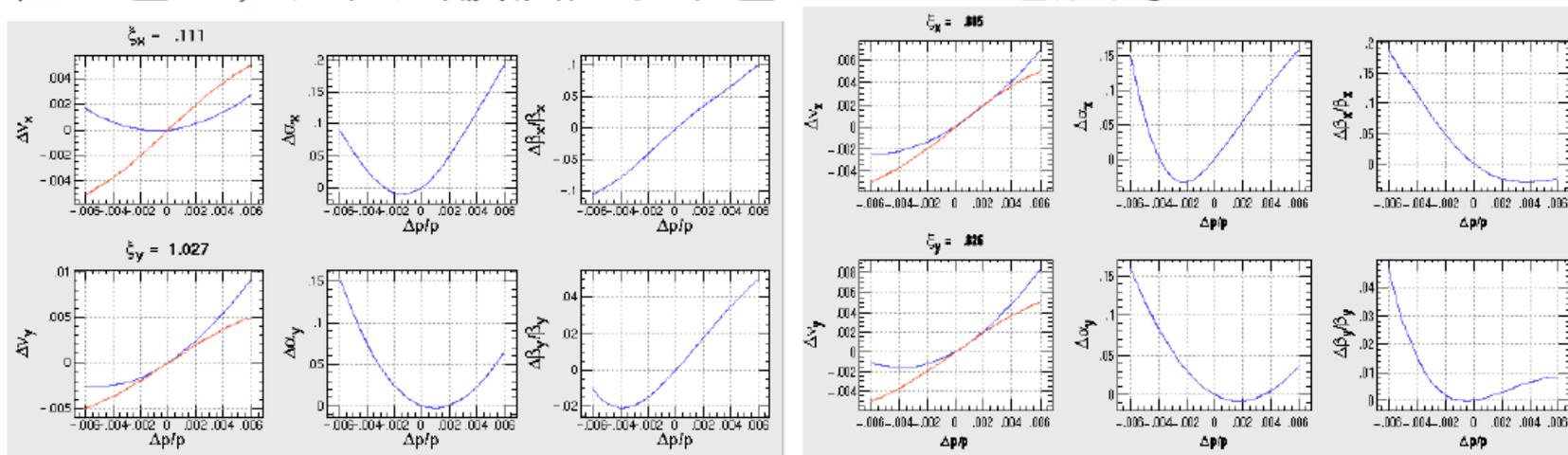
From H. Sugimoto



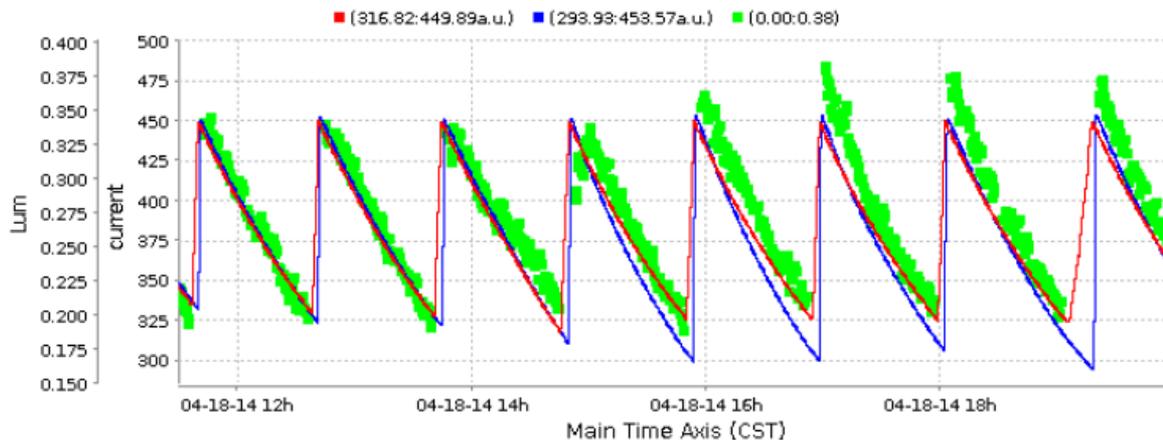
- BEPCII

1W1 兼用模式

- 2014 上半年，开始投入使用 1W1。Q 铁强度重新匹配，但六极铁保持不变。经过连续几个班的优化，亮度仍然偏低 ($3.4e32@430mA$)
- 检查色品；优化六极铁，水平色品由 0.1 增加到 0.8



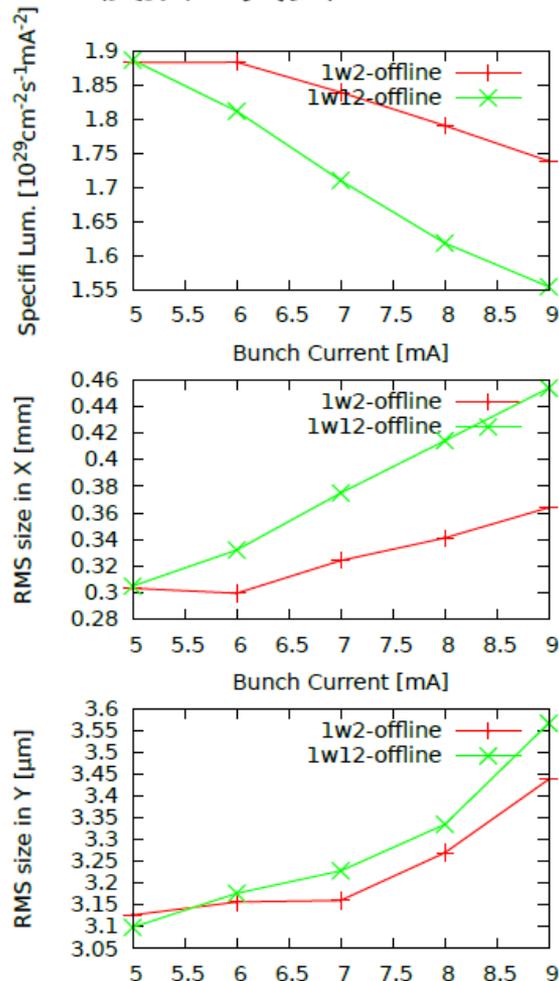
- 经过几个 run 的优化，亮度迅速提高至 $3.8e32$ ，亮度提升超 10%。



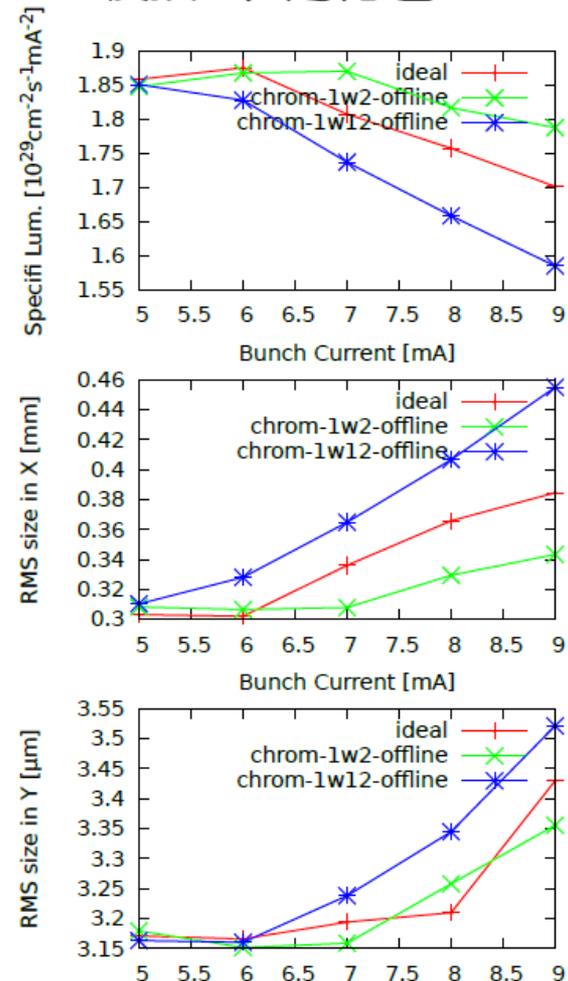
1W1 兼用模式 - Simulation

实际调束，新的六极铁搭配（1w12-offline）亮度高，但模拟结果反而低。不稳定性的贡献？

模拟：真实 lattice



模拟：只考虑色品

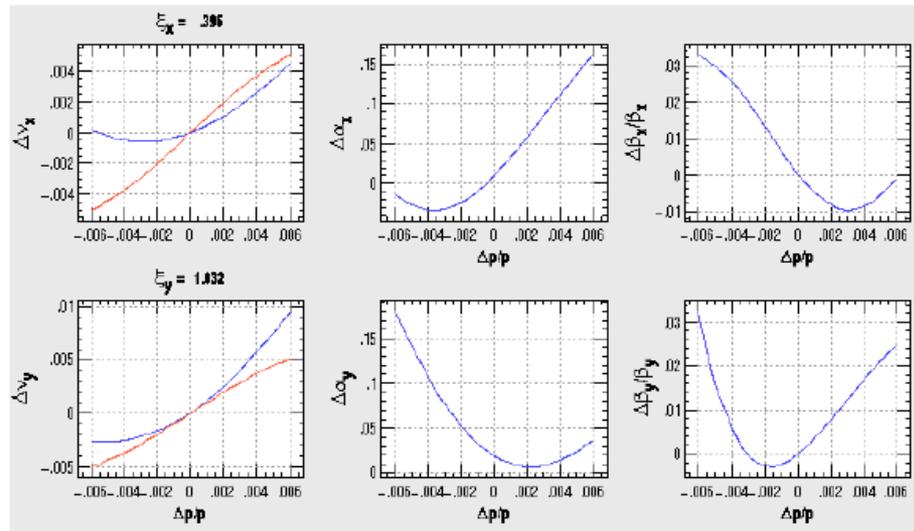
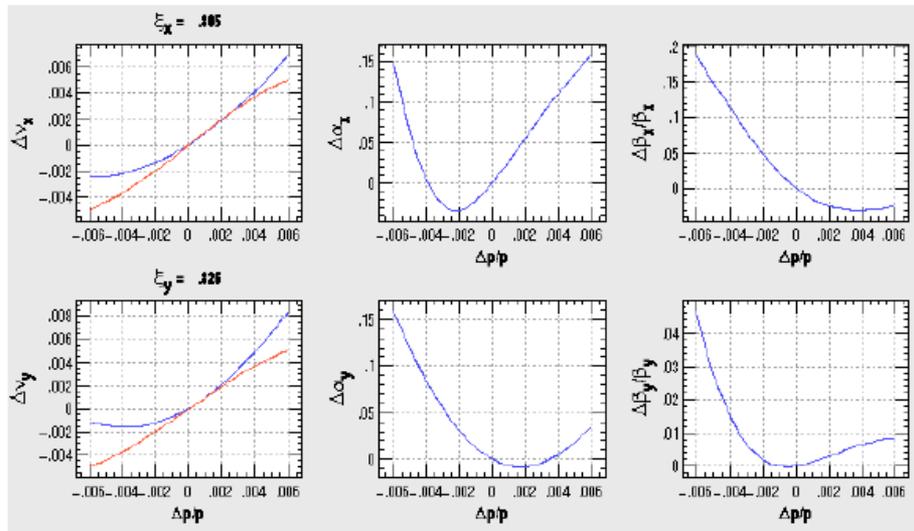


新的亮度在线调节方法 - chromaticity knob

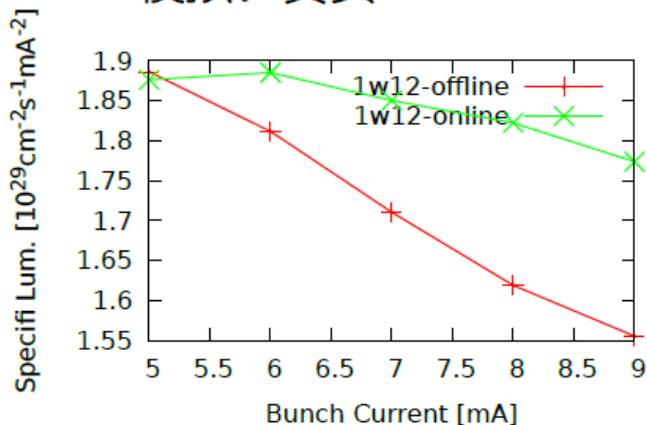
第一次投入使用 @2014-05-09n, **亮度提升超 10%!**

之前: 最高亮度 $4.6e32@450m*450mA$

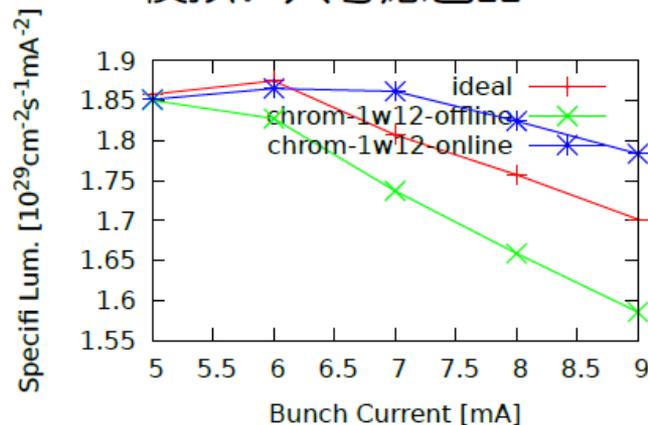
之后: 最高亮度 $5.2e32@450mA*450mA$



模拟: 真实 lattice

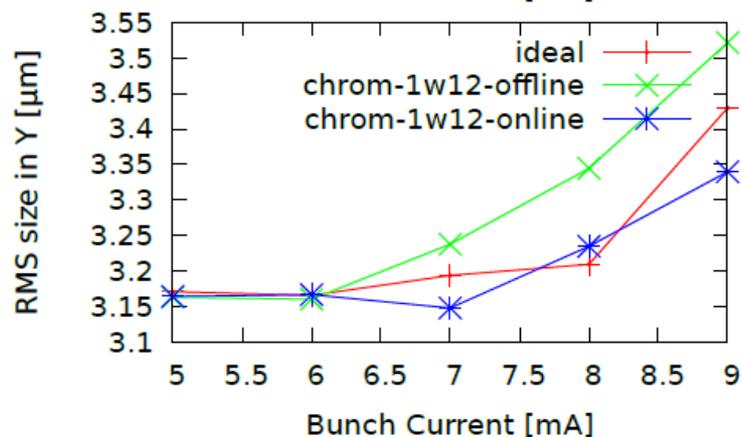
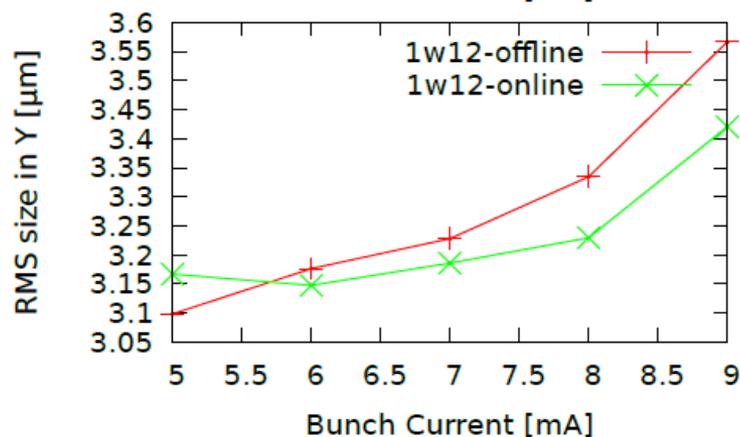
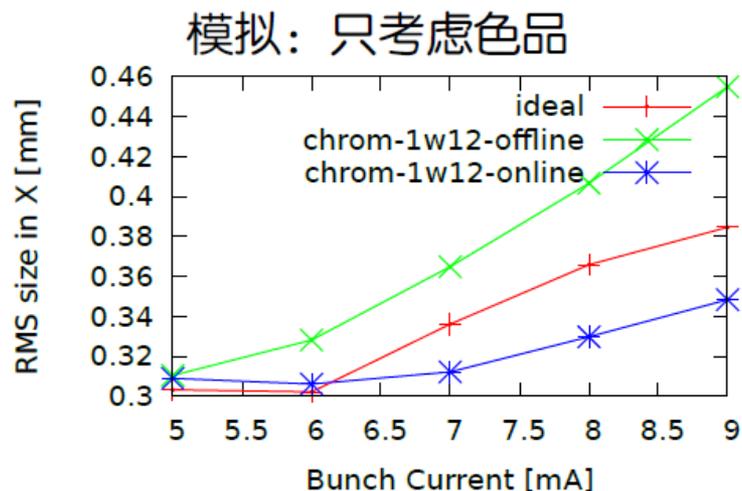
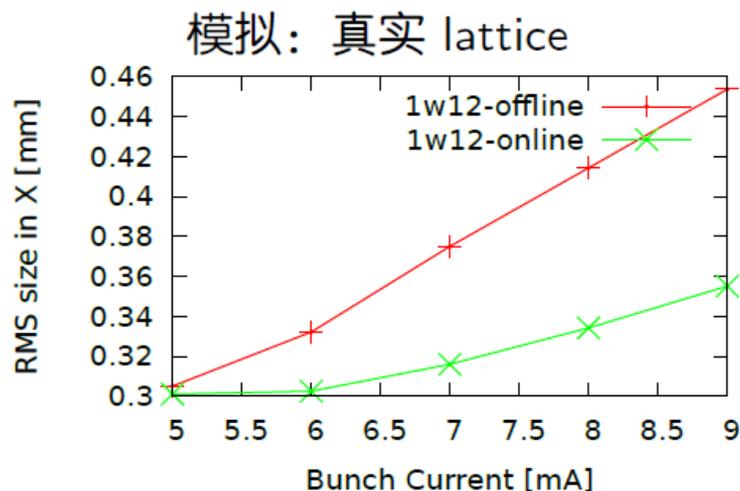


模拟: 只考虑色品

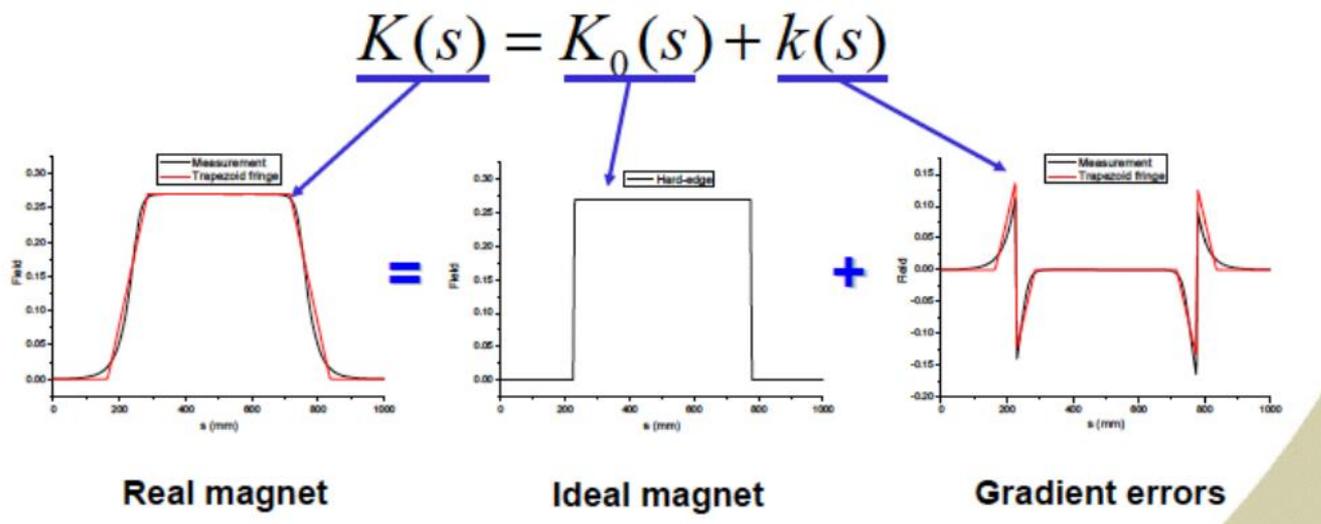


新的亮度在线调节方法 - chromaticity knob (2)

亮度的高低主要来自水平方向的尺寸差别，即水平方向的色品导致了水平和纵向的共振。



Fringe effect in BEPCII (using SAD)



二极铁

原始定义, 例子:

R4IMB02 =(L= 1.414956 ANGLE= 0.154685006 E1= 0.5 E2= 0.5 K1= 0.

修改为:

R4IMB02 =(L= 1.414956 ANGLE= 0.154685006 E1= 0.5 E2= 0.5 K1= 0.
F1=0.177 FRINGE=1)

超导四极铁

原始定义, 例子:

SSCQ01I =(L= 0.025 K1=-0.000370337)

修改为:

SSCQ01I =(L= 0.025 K1=-0.000370337 F1 =.025 FRINGE =3)

四极铁

原始定义, 例子:

R3IQ02 =(L= 0.54800000000000004 K1= -6.1350440677200004E-002)

修改为:

R3IQ02 =(L= 0.54800000000000004 K1= -6.1350440677200004E-002 F1 =.
133 FRINGE =3)

螺线管场

原始定义:

ESOL001 =(BZ= 0)

改为:

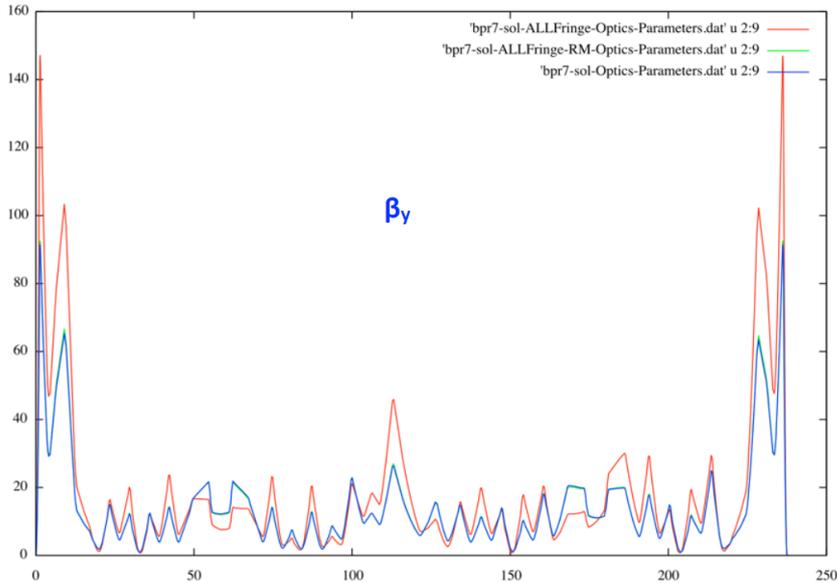
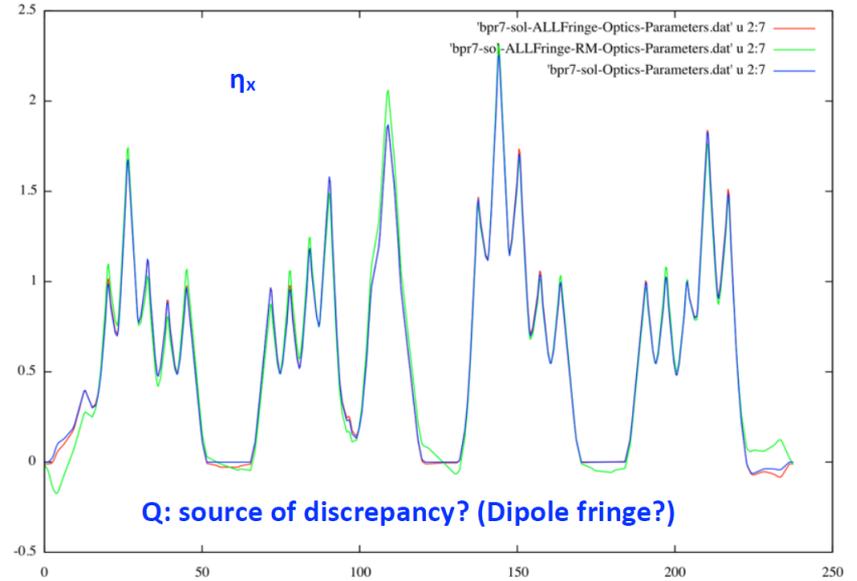
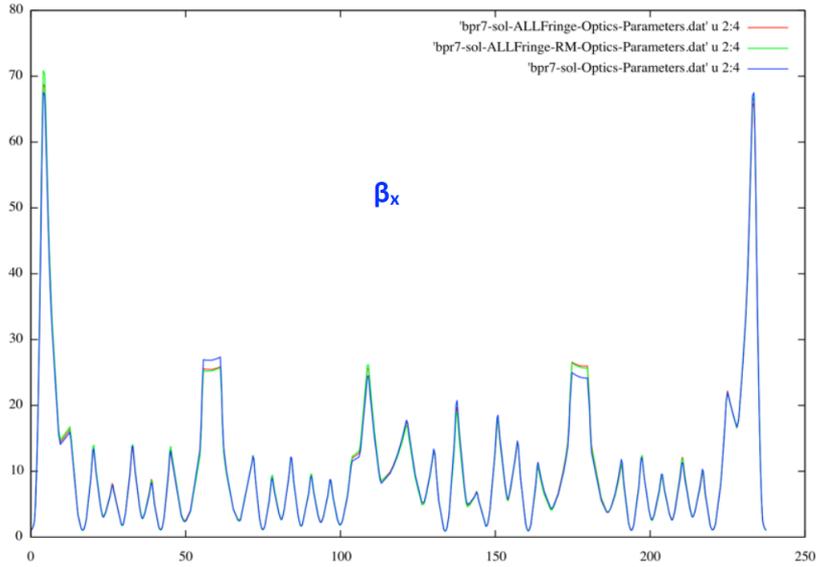
ESOL001 =(BZ= 0 F1=0.02)

Linear optics parameters

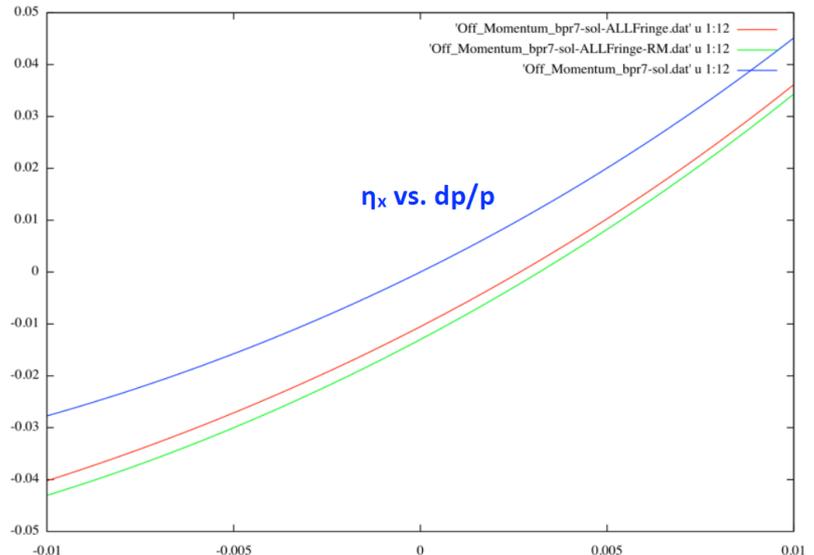
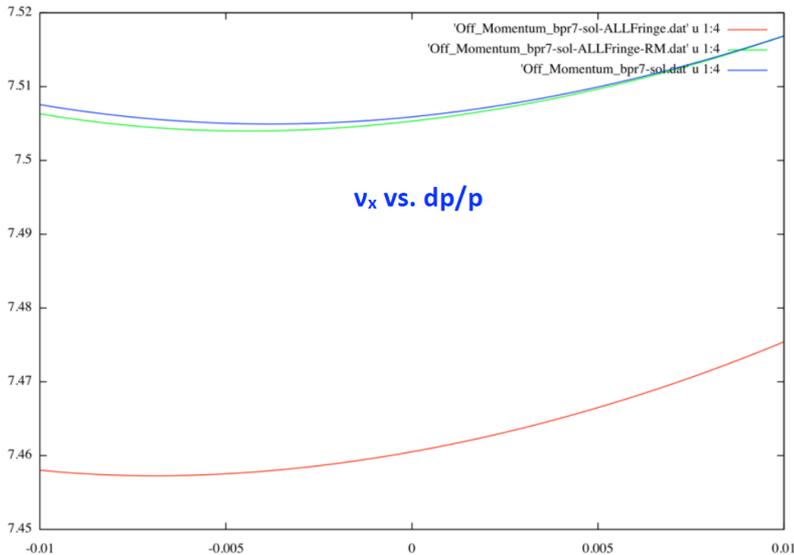
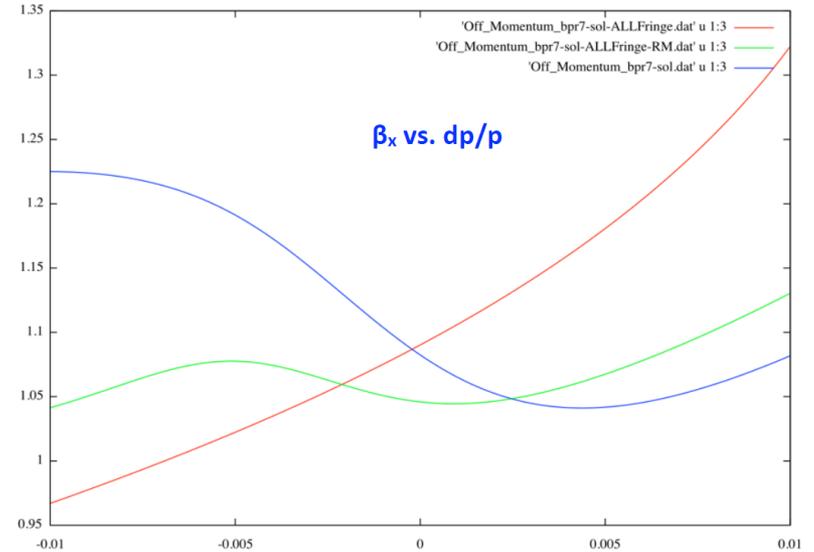
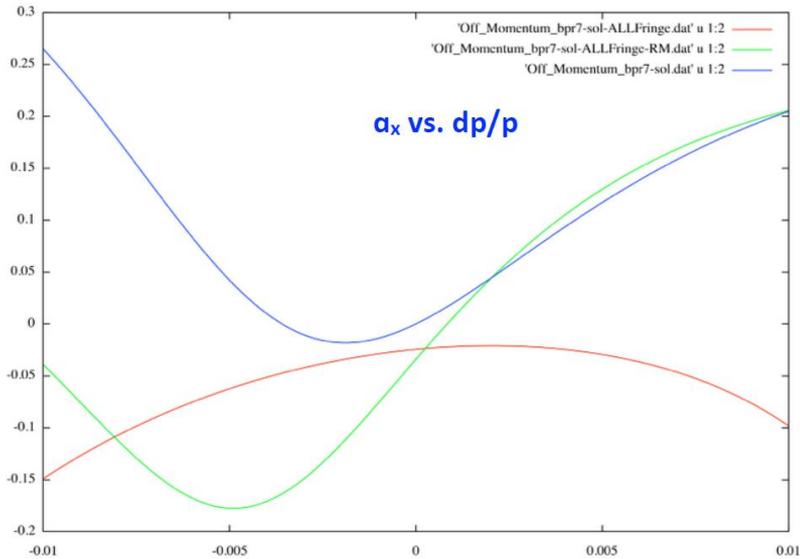
使用 SAD(Ver.1.0.10.5.7a3) 计算 BPR(Ver. bpr7-sol.sad) 的线性 optics 参数 (@IP):

Fringe type	None	B	Q	SCQ	SOL	All
C (m)	237.531	237.531	237.531	237.531	237.531	237.531
β_x (m)	1.082	1.082	1.089	1.078	1.082	1.090
β_y (m)	0.0153	0.01535	0.0135	0.0150	0.0153	0.0095
ν_x	7.506	7.506	7.461	7.506	7.506	7.461
ν_y	5.577	5.558	5.536	5.575	5.577	5.514
α_x	8.32E-5	8.32E-5	-0.0245	8.44E-5	8.32E-5	-0.0244
α_y	4.22E-6	-0.015	0.016	4.31E-6	4.22E-6	-0.0470
α_p	0.017	0.017	0.0172	0.0170	0.0170	0.0172
τ_x (ms)	24.701	25.696	24.700	24.701	24.701	25.696
τ_y (ms)	24.744	25.743	24.744	24.744	24.744	25.743
τ_s (ms)	12.383	12.884	12.384	12.383	12.383	12.884
ϵ_x (nm)	97.645	95.185	97.986	97.619	97.645	95.521
ϵ_z (μm)	5.956	5.836	5.990	5.956	5.956	5.870
σ_p (10^{-4})	5.2075	5.154	5.208	5.2075	5.2075	5.1546
σ_z (cm)	1.144	1.132	1.151	1.144	1.144	1.139

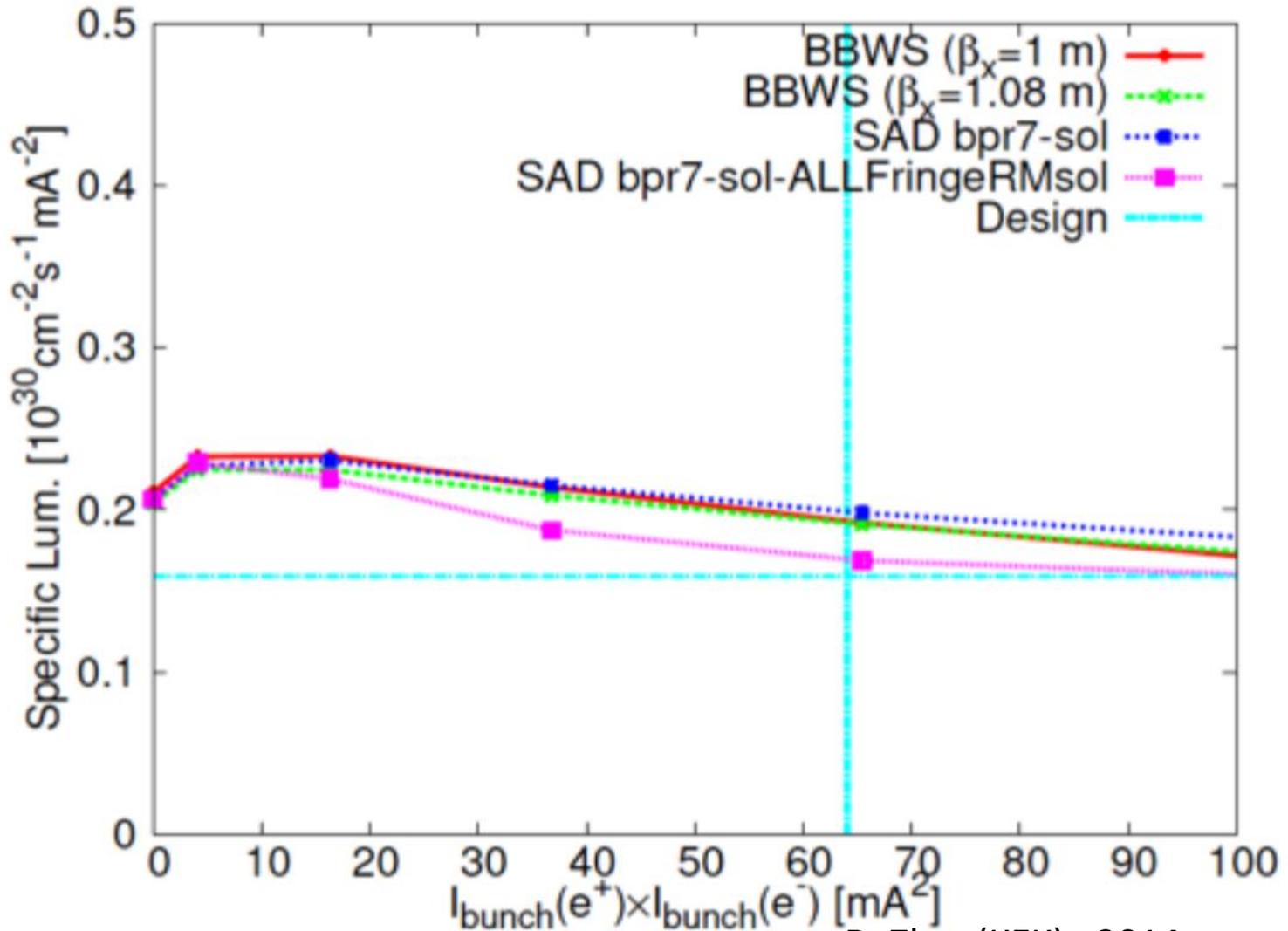
原始模型, +边缘场, +LOCO校正



原始模型, +边缘场, +LOCO校正 (cont.)

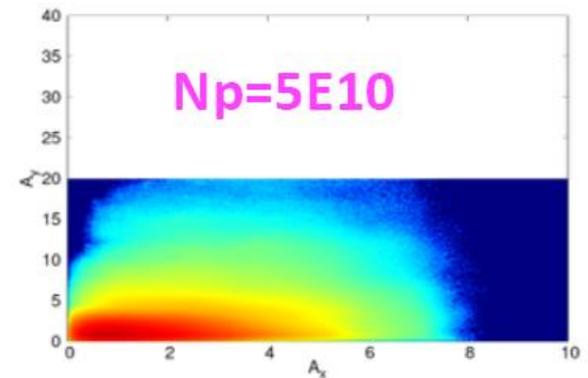
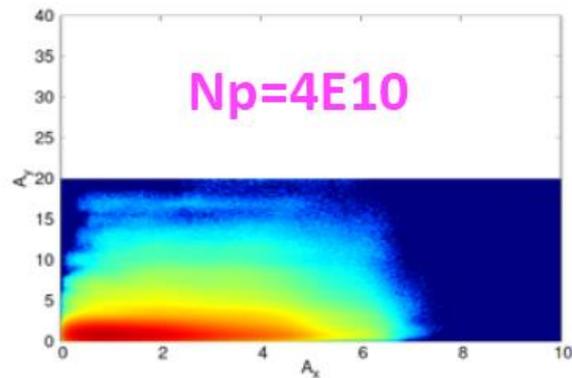
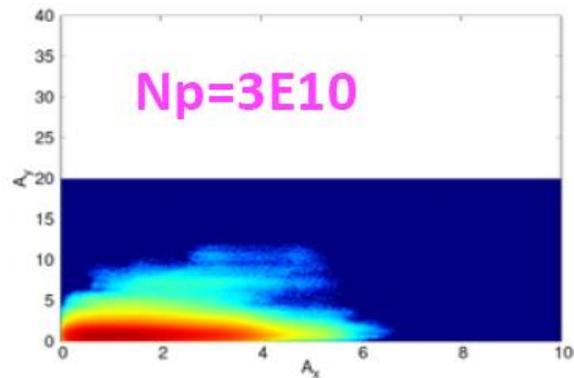
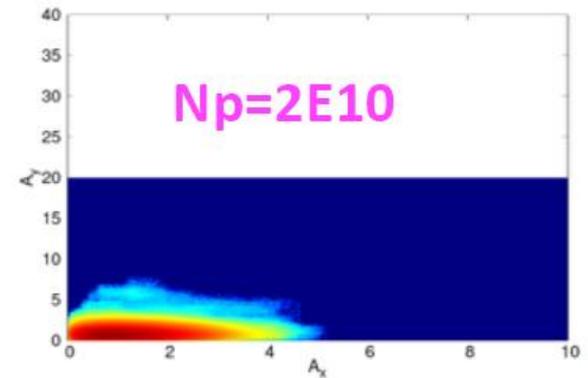
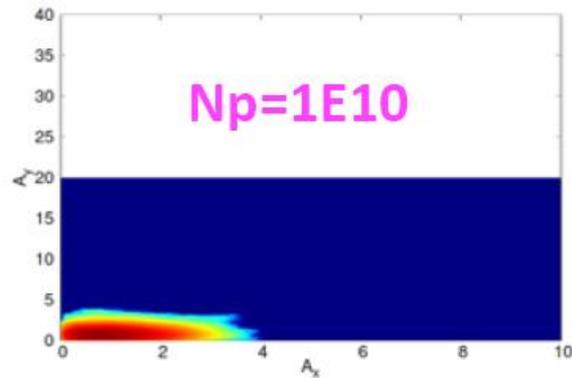
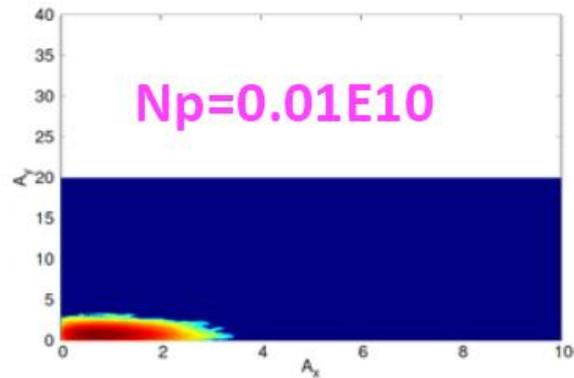


亮度： 原始模型 vs 边缘场+LOCO校正 loss~15%



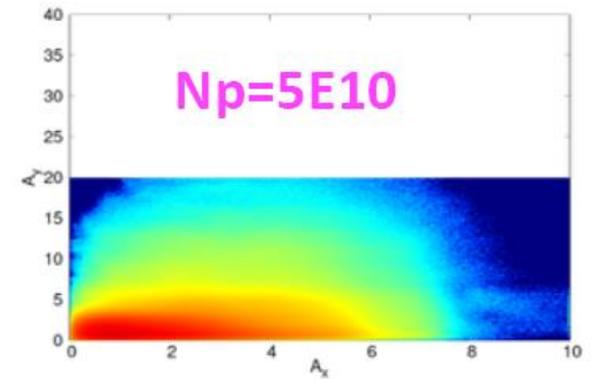
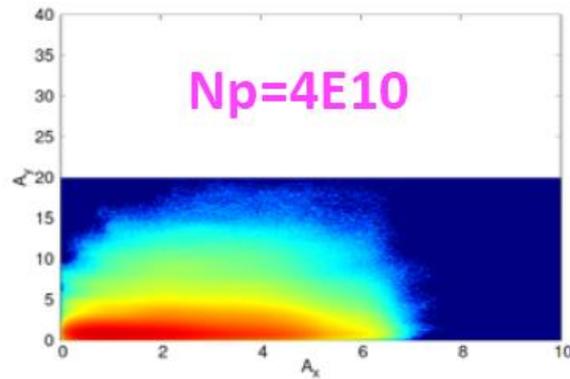
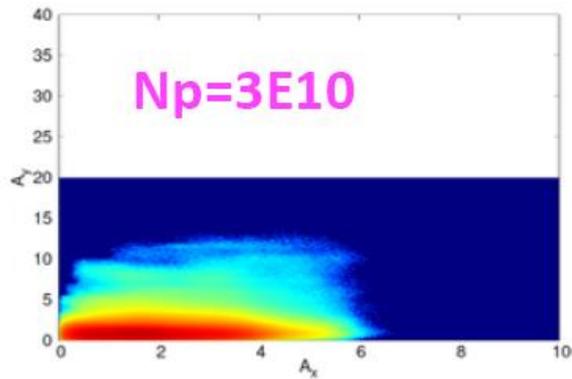
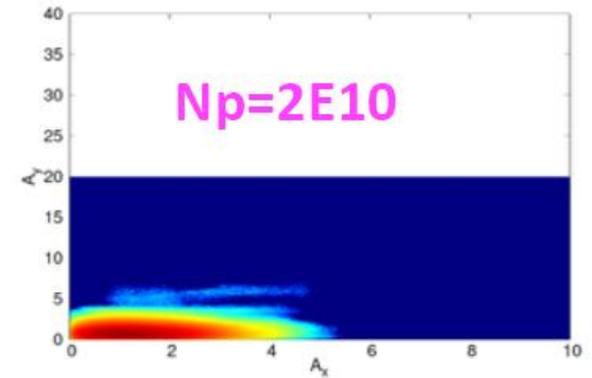
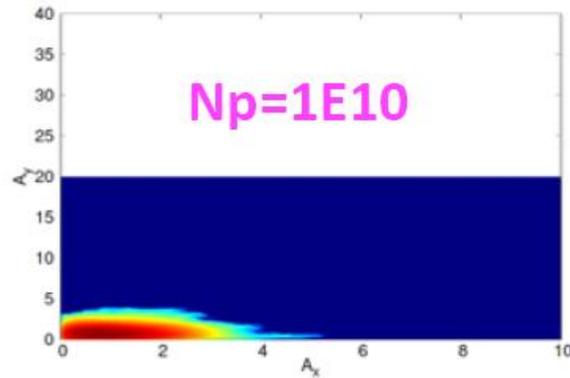
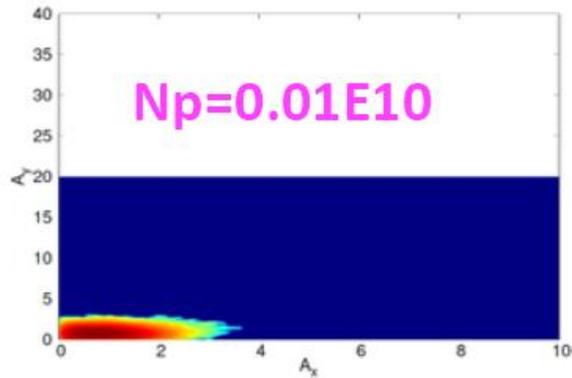
Beam tail

► bpr7-sol:



Beam tail

► bpr7-sol-AllFringeRMsol:



Summary

所有的非线性都已经在“实际”机器中被发现对亮度产生影响：

- Detuning
- Chromaticity (tune/twiss parameters/coupling)
- normal/skew multipole magnet