

Neutrino Physics at Colliders

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Special thanks to Dr. Ji-Yuan Liu for collaboration and help

Outline

- 1 Basics about neutrinos
- 2 Conventional seesaws and tests
- 3 Going beyond conventional seesaws
- 4 Summary and outlook

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- 1 Basics about neutrinos
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What we experimentally know about ν

■ Precision data

3 active, almost massless neutrinos

interact as assigned in standard model (SM)

■ Oscillation data

neutrinos have nondegenerate masses $m_{1,2,3}$

leptons mix in CC weak interactions θ_{ij}

$$V = U \cdot \text{Diag}\{e^{i\rho}, e^{i\sigma}, 1\},$$

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13} \\ -c_{12}s_{23}s_{13} - s_{12}c_{23}e^{-i\delta} & -s_{12}s_{23}s_{13} + c_{12}c_{23}e^{-i\delta} & s_{23}c_{13} \\ -c_{12}c_{23}s_{13} + s_{12}s_{23}e^{-i\delta} & -s_{12}c_{23}s_{13} - c_{12}s_{23}e^{-i\delta} & c_{23}c_{13} \end{pmatrix},$$

$$s_{ij} = \sin \theta_{ij}, c_{ij} = \cos \theta_{ij}, ij = 12, 23, 13$$

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What we experimentally know about ν

- Global 3ν oscillation analysis for NH Fogli *et al.*, 2012

Parameter	Best fit	1σ range	2σ range	3σ range
$\delta m^2/10^{-5} \text{ eV}^2$	7.54	[7.32, 7.80]	[7.15, 8.00]	[6.99, 8.18]
$\Delta m^2/10^{-3} \text{ eV}^2$	2.43	[2.33, 2.49]	[2.27, 2.55]	[2.19, 2.62]
θ_{12}	33.6°	$[32.6^\circ, 34.8^\circ]$	$[31.6^\circ, 35.8^\circ]$	$[30.6^\circ, 36.8^\circ]$
θ_{23}	38.4°	$[37.2^\circ, 40.0^\circ]$	$[36.2^\circ, 42.0^\circ]$	$[35.1^\circ, 53.0^\circ]$
θ_{13}	8.9°	$[8.5^\circ, 9.4^\circ]$	$[8.0^\circ, 9.8^\circ]$	$[7.5^\circ, 10.2^\circ]$

$$\delta m^2 \equiv m_2^2 - m_1^2 \text{ and } \Delta m^2 \equiv m_3^2 - (m_1^2 + m_2^2)/2.$$

- Almost no knowledge on CP phases; neither on mass hierarchy:
 either $m_1 < m_2 < m_3$ – normal hierarchy (NH)
 or $m_3 < m_1 < m_2$ – inverted hierarchy (IH)

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What we experimentally know about ν

Constraints on absolute neutrino mass

- nuclear β decays: $m_\beta \equiv \sqrt{\sum |V_{ei}|^2 m_i^2}$
 $m_\beta < 2.1 \text{ eV}$ @ 95% C.L. Troitsk Collaboration 2011
 $\Rightarrow m_\beta \sim 0.2 \text{ eV}$ (90% C.L.) KATRIN
- lepton-number violating $0\nu\beta\beta$ decays: $m_{\beta\beta} \equiv |\sum V_{ei}^2 m_i|$
 $m_{\beta\beta} \lesssim 0.4 \text{ eV}$ W. Rodejohann 2012
 $\Rightarrow m_{\beta\beta} \sim 0.02 \text{ eV}$
- cosmological and astrophysical considerations: $\Sigma \equiv \sum m_i$
 $\Sigma < 0.44 \text{ eV}$ @ 95% C.L. 9-year WMAP 2012
 $\Sigma < 0.23 \text{ eV}$ @ 95% C.L. Planck 2013
 $\Rightarrow \Sigma \sim 0.05 \text{ eV}$

What we experimentally know about ν 's relatives

ν and ℓ share CC weak interactions

\Rightarrow gain info from lepton-flavor violating (LFV) transitions

■ μ decays

$BR(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$ @ 90% C.L. MEG 2013

$BR(\mu \rightarrow 3e) < 1.0 \times 10^{-12}$ @ 90% C.L. SINDRUM 1988

■ $\mu - e$ conversion in nuclei

$BR(\mu^- \text{Ti} \rightarrow e^- \text{Ti}) < 4.3 \times 10^{-12}$ @ 90% C.L. SINDRUM II 1993

$BR(\mu^- \text{Au} \rightarrow e^- \text{Au}) < 7 \times 10^{-13}$ @ 90% C.L. SINDRUM II 2006

$\Rightarrow 10^{-16} \sim 10^{-18}$ COMET, PRISM/PRIME, Mu2e, Project-X

■ LFV decays of τ and of B mesons

less restrictive: BRs $\sim 10^{-8}$ BaBar, Belle, CDF

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What we suppose ν to be

SM

assumes only left-handed (LH) neutrinos ν_L

– Only Majorana ν mass could be possible

– But gauge symmetries do *not* allow it!

⇒ $m_\nu \neq 0$ calls for phys beyond SM

Trivial extension

add right-handed (RH) ν_R to form massive Dirac ν as we do for ℓ

must tolerate tiny Yukawa coupling of order or less than 10^{-11}

Why isn't it exactly zero at all?!

We need an understanding of tiny m_ν !

What we suppose ν to be

We are *apt to believe* a tiny number like m_ν is a remnant of some high-scale phys

We are not certain about what it is

but we can parameterize our ignorance systematically –
regard SM as a low-energy EFT

$\Rightarrow m_\nu$ may arise from an effective higher-dim interaction Weinberg 1980

$$\mathcal{L}_{\text{int}} = \frac{\lambda}{\Lambda} \bar{\theta}_5 + \text{h.c.}, \quad \bar{\theta}_5 = (\overline{F_L^c} \varepsilon H) (H^T \varepsilon F_L), \quad H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}, \quad F_L = \begin{pmatrix} \nu_L \\ \ell_L \end{pmatrix}$$

$$\Rightarrow \frac{\lambda}{\Lambda} \frac{v^2}{2} \overline{\nu_L^c} \nu_L + \text{h.c.}, \quad \text{via } \langle H^0 \rangle = \frac{v}{\sqrt{2}} \quad \text{Majorana mass}$$

Very roughly, for $\nu \sim 250$ GeV, $\lambda \sim 1$, $m_\nu \sim 0.1$ eV requires

$$\Lambda \sim 10^{15} \text{ GeV}$$

Main questions to address

What's the origin of such a tiny mass? Seesaw models?

Of Majorana nature as most seesaws assume?

Possible to test? At colliders?

Dilemma:

m_ν tends to demand extremely **large Λ** , while

accessibility to new phys responsible for m_ν relies on a **not-too-high Λ**

What to do with this tension?

Even higher-dim interactions?

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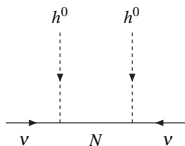
Weinberg operator and its tree level realizations

Weinberg operator \mathcal{O}_5 for m_ν is **unique** Weinberg 1980

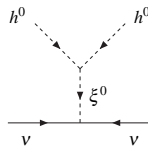
Group theor. analysis shows that it has **3 and only 3 apparently different** realizations of \mathcal{O}_5 at tree level Ma 1998

They hint at **3 different origins** from an underlying theory

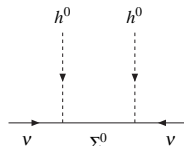
– 3 types of conventional seesaws



(a) Type I



(b) Type II



(c) Type III

Type I seesaw

New particles: n_s sterile neutrinos N_R ; lepton # violated by 2 units

$$\dots + \overline{N}_R i \not{\partial} N_R - \left[\overline{F}_L Y_N \tilde{H} N_R + \frac{1}{2} \overline{N}_R^c M_R N_R + \text{h.c.} \right]$$

Mass matrix for $n_s + 3$ neutral particles:

$$M_\nu = \begin{pmatrix} 0 & M_D \\ M_D & M_R \end{pmatrix}, \quad M_D = Y_N v / \sqrt{2}$$

Seesaw limit: $|M_D| \ll |M_R|$; generally 3 light and n_s heavy:

$$M_{\text{light}} \simeq -M_D M_R^{-1} M_D^T, \quad M_{\text{heavy}} \simeq M_R$$

$n_s \geq 2$ to gain at least 2 massive light ν 's

Heavy neutrinos interact with SM particles only through Yukawa coupling Y_N and mixing with light neutrinos

\Rightarrow very hard to test a genuine type I seesaw!

Collider test of *effective type I* seesaw

- Most works study *effective type I* seesaw; assuming
 - essentially one sterile neutrino at work
 - masses, mixing and couplings as free parameters, not restricted by theoretical relations as in genuine type I seesaw, but by various data: precision electroweak data, LFV processes, $0\nu\beta\beta$ decay, etc.
- Main signal: $pp \rightarrow W^\pm \rightarrow \ell^\pm N \rightarrow \ell^\pm \ell^\pm jj$ like-sign dilepton events
- Works differ mainly in background analysis.
- I show a few typical results.

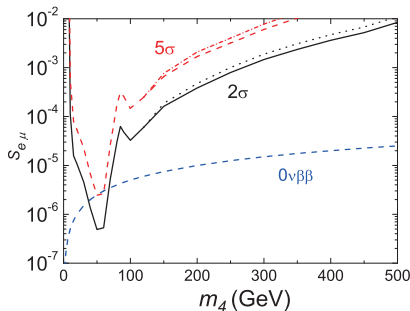
Collider test of *effective type I* seesaw

$$\sigma(pp \rightarrow \ell_1^\pm \ell_2^\pm W^\mp) \approx (2 - \delta_{\ell_1 \ell_2}) S_{\ell_1 \ell_2} \sigma_0 \quad \text{Han and Zhang 2006}$$

$$S_{\ell_1 \ell_2} = \frac{|V_{\ell_1 N} V_{\ell_2 N}|^2}{\sum_l |V_{\ell N}|^2}, \quad \sigma_0: \text{largely indept of mixing parameters}$$

Sensitivity at 14 TeV LHC with 100 fb^{-1} Atre et al 2009

$$m_N \sim 375 \text{ (250) GeV} \quad \text{or} \quad S_{e\mu} \sim 7 \times 10^{-7} \text{ (} 3 \times 10^{-6} \text{)} \quad \text{for } 2\sigma \text{ (} 5\sigma \text{)}$$



Less optimistic due to large background from $b\bar{b}$ decays

of $\ell^\pm\ell^\pm jj$ events at LHC for 30 fb^{-1} : Aguilera et al 2007

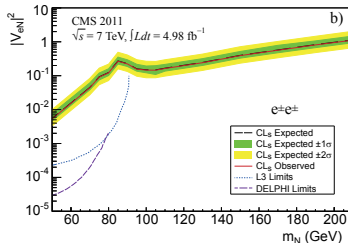
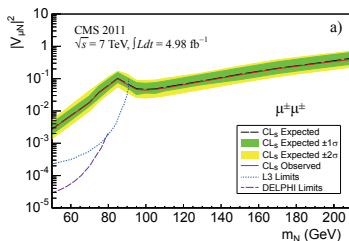
$m_N = 150\text{ GeV}$. (a) $V_{\mu N} = 0.098$; (b) $V_{eN} = 0.073$; (c) both

	Pre-selection			Selection		
	$\mu^\pm\mu^\pm$	$e^\pm e^\pm$	$\mu^\pm e^\pm$	$\mu^\pm\mu^\pm$	$e^\pm e^\pm$	$\mu^\pm e^\pm$
N (a)	113.6	0	0	59.1	0	0
N (b)	0	72.0	0	0	17.6	0
N (c)	78.4	25.5	82.6	41.6	4.7	22.4
$b\bar{b}nj$	14800	52000	82000	0	0	0
$c\bar{c}nj$	(11)	300	200	(0)	0	0
$t\bar{t}nj$	1162.1	8133.0	15625.3	2.4	8.3	7.7
tj	60.8	176.5	461.5	0.0	0.0	0.1
$Wb\bar{b}nj$	124.9	346.7	927.3	0.4	0.6	0.3
$Wt\bar{t}nj$	75.7	87.2	166.9	0.3	0.0	0.0
$Zb\bar{b}nj$	12.2	68.9	117.0	0.0	0.2	0.0
$WWnj$	82.8	89.0	174.8	0.5	0.1	0.7
$WZnj$	162.4	252.0	409.2	4.8	1.8	2.3
$ZZnj$	3.8	13.3	12.9	0.0	0.6	0.1
$WWWnj$	31.9	30.1	64.8	0.9	0.1	0.0

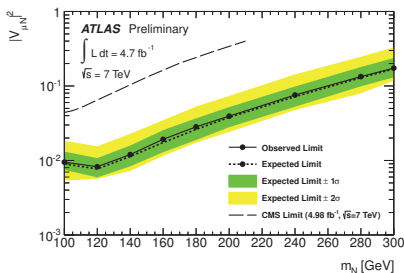
5σ sensitivity for m_N up to **200 GeV** with $V_{\mu N} = 0.098$

5σ sensitivity for m_N up to **145 GeV** with $V_{eN} = 0.073$

Collider test of *effective type I* seesaw: LHC data



1207.6079



ATLAS-CONF-2012-139



Type II seesaw

New particles: **scalar triplet Δ** of $Y = +2$
doubly-charged, singly-charged, and neutral

$$\begin{aligned}\mathcal{L} &\supset \frac{1}{2} \text{Tr}(D^\mu \Delta)^\dagger (D_\mu \Delta) - \left[f_{ij} \overline{F_{Li}^C} (i\sigma_2) \Delta F_{Lj} + \text{h.c.} \right] \\ V &\supset -m_H^2 H^\dagger H + m_\Delta^2 \text{Tr}(\Delta^\dagger \Delta) + [\mu (H^\dagger \Delta \tilde{H}) + \text{h.c.}] \\ &\quad + \frac{1}{2} \lambda_1 (H^\dagger H)^2 + \lambda_4 (H^\dagger H) \text{Tr}(\Delta^\dagger \Delta) + \lambda_6 (H^\dagger \Delta \Delta^\dagger H)\end{aligned}$$

vev's and Majorana ν mass:

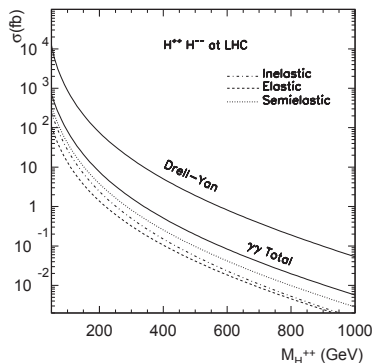
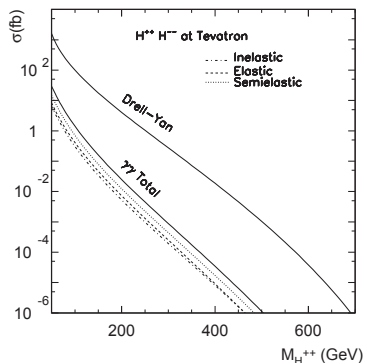
$$\begin{aligned}\langle H \rangle = v &\simeq \sqrt{\frac{m_H^2}{\lambda_1}}, \quad \langle \Delta \rangle = v_\Delta \simeq \frac{-\mu v^2}{m_\Delta^2 + (\lambda_4 + \lambda_6) v^2} \\ m_\nu &= f v_\Delta\end{aligned}$$

enjoy electroweak interactions

\Rightarrow rich phenomenology expected, details depending on v_Δ .

Collider test of type II seesaw

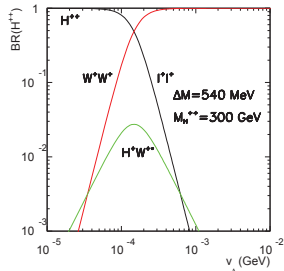
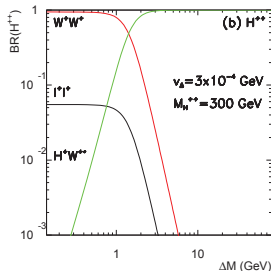
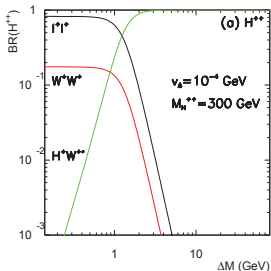
$\sigma(pp(\bar{p}) \rightarrow H^{\pm\pm}H^{\pm\pm})$ by Drell-Yan and $\gamma\gamma$ fusion



Han, Mukhopadhyaya, Si and Wang, PRD76, 2007

Collider test of type II seesaw

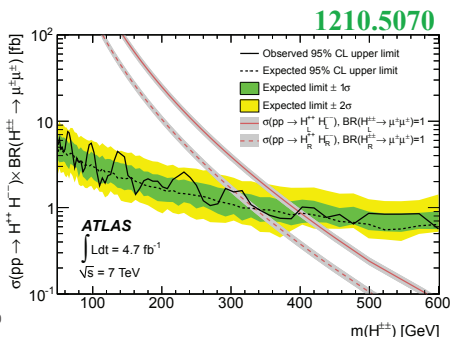
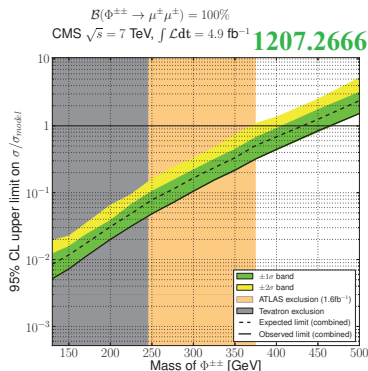
$\text{Br}(H^{\pm\pm})$ vs mass splitting $\Delta M \equiv M_{H^{++}} - M_{H^+}$ and v_Δ



Fileviez Perez, Han, Huang, Li and Wang 2008

For $v_\Delta < 10^{-4} \text{ GeV}$, $l^\pm l^\pm$ signals at LHC with 300 fb^{-1} should be observable up to $M_{H^{++}} \sim 1 \text{ TeV}$.

Collider test of type II seesaw: LHC data



CMS: $m_{\Phi^{++}} \geq (204 - 459) \text{ GeV}$ assuming $\text{BR}(\Phi^{++} \rightarrow \ell^+ \ell^+) \sim 100\%$

(383 – 408) GeV at 4 benchmark points

ATLAS: $m_{\Phi^{++}} \lesssim 409 (e^{\pm} e^{\pm})$, $398 (\mu^{\pm} \mu^{\pm})$, $375 \text{ GeV} (e^{\pm} \mu^{\pm})$ excl. at 95% CL

Type III seesaw

New particles: **fermion triplet** of $Y = 0$:

$$\Sigma_R = \begin{pmatrix} \Sigma_R^0/\sqrt{2} & \Sigma_R^+ \\ \Sigma_R^- & -\Sigma_R^0/\sqrt{2} \end{pmatrix}$$

$$\mathcal{L} \supset \text{Tr} \overline{\Sigma}_R i \not{D} \Sigma_R - \left[\frac{1}{2} \text{Tr} \left(\overline{\Sigma}_R M_\Sigma \Sigma_R^C \right) + \overline{F}_L Y_\Sigma \tilde{H} \Sigma_R + \text{h.c.} \right]$$

Mass matrix of neutral particles:

$$M_\nu = \begin{pmatrix} 0 & M_D \\ M_D & M_\Sigma \end{pmatrix}, \quad \text{where } M_D = Y_\Sigma v/\sqrt{2}$$

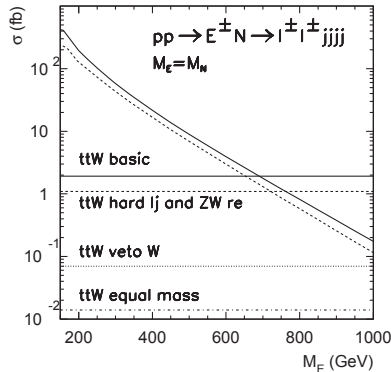
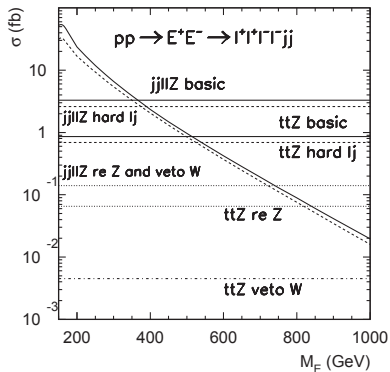
can be diagonalized as in type I seesaw

Differences to type I:

electroweak interactions; charged heavy-light mixing

Relatively less extensively studied

Collider test of type III seesaw

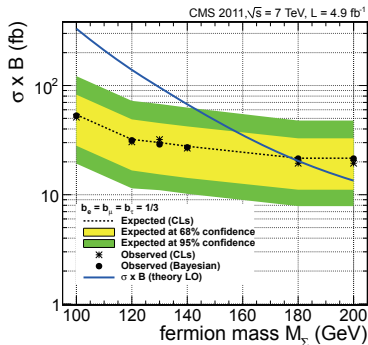


Li and He 2009

A **displaced vertex** of heavy triplet leptons could be visible at LHC.

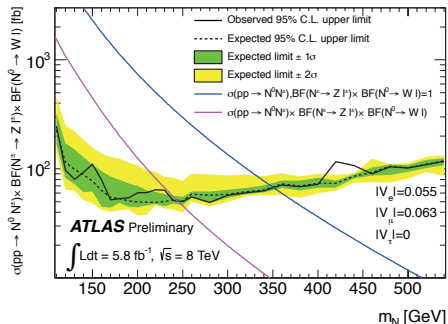
Possible to detect them up to 1 TeV.

Collider test of type III seesaw: LHC data



CMS 1210.1797

$M_{\Sigma} > 180 - 210 \text{ GeV}$ at 95% CL



ATLAS-CONF-2013-019

$M_{\Sigma} > 245 \text{ GeV}$ at 95% CL

A partial list of other papers on conventional seesaws

Type I seesaw at various colliders (ILC, CLIC, etc) [Aguila et al 2005, 2006](#)
(see backup pages)

Comparative study on 3 seesaws and importance of tri-lepton channel $\ell^\pm \ell^\pm \ell^\mp$ for discovery [Aguila et al 2009](#) (see backup pages)

Variants of 3 seesaws:

Type I+II: [Chao, Si, Xing and Zhou 2008](#)

Type I+III from $SU(5)$: [Bajc et al 2007](#); [Arhrib et al 2010](#)

Type I + ℓNH^+ interaction [Bar-Shalom, Eilam, Han and Soni 2008](#)

Type I + $U(1)_{B-L}$ symmetry [Fileviez Perez, Han and Li 2009](#)

Type I + W' [Han, Lewis, Ruiz and Si 2013](#)

Type II + **scalar multiplets** [Aguila and Chala 2013](#)

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Why going beyond conventional seesaws

Tension between **tiny m_ν** and **accessibility of new phys**
(large mass of new particles or/and small couplings)

can be relaxed in two basic approaches

- m_ν induced **radiatively**:

one loop (Zee '80),

two loops (Zee '85, Babu '88),

three loops (Krauss et al '03), ...

Usually amounts to **higher-dim operators** with additional small factors

Global symmetries or new quantum numbers usually required to
forbid lower-loop contri.

Why going beyond conventional seesaws

- m_ν induced at tree level from higher-dim operators

Fields live in higher-dim reps so that seesaw operates in several steps to avoid lower-dim operators

Global symmetries not necessary

Unique operator at each dim $\mathcal{O}_{5+2n} = \mathcal{O}_5(H^\dagger H)^n$ Liao 2010

I show one example for each approach

Radiatively induced m_ν : color-octet model

New particles:

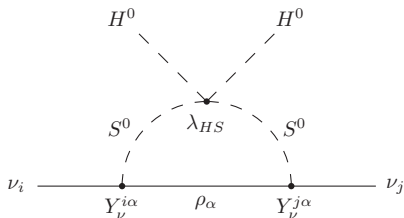
Fileviez Perez and Wise 2009

one scalar $S \sim (8, 2, 1)$ and two fermions $\rho_\alpha \sim (8, 1, 0)$

$$\mathcal{L} \supset -Y_\nu^{i\alpha} \bar{F}_{Li} \tilde{S} \rho_\alpha + \text{h.c.},$$

$$V \supset \frac{1}{2} \lambda_{HS} (S^\dagger H)^2 + \text{h.c.}$$

m_ν induced by

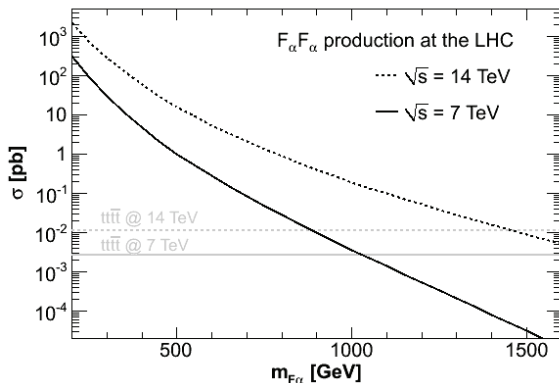


Radiatively induced m_V : color-octet model at LHC

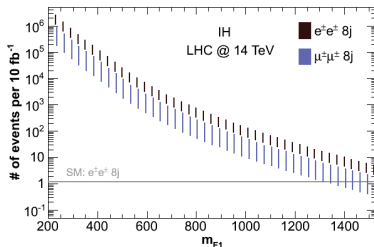
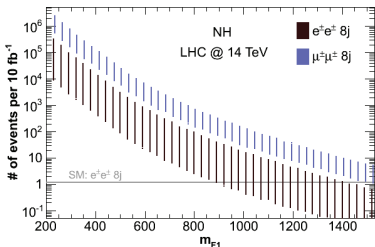
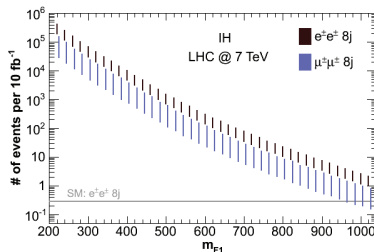
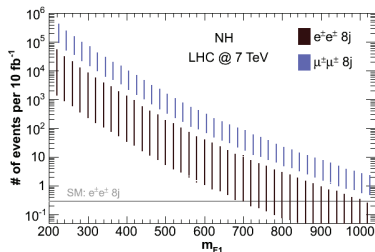
Fileviez Perez, Han, Spinner and Trenkel 2010

Signal: like-sign dileptons via $F_\alpha F_\alpha$ production with $F_\alpha \rightarrow \ell tb \rightarrow \ell 4j$

Pair production cross section of octet fermions: $F_\alpha \equiv (\rho_{R\alpha}^C, \rho_{R\alpha})$



of like-sign dileptons per 10/fb exceeds bkg up to $m_{F_1} \approx m_{F_2} \sim 1$ TeV
 $m_S = 2$ TeV, vertical line: scanning over parameters



New fields in higher-dim reps: higher seesaws at tree

Too many, arbitrary possibilities. Use as our **criteria**: Liao 2010

- For a given set of fields, lowest-dim operator \mathcal{O}_{5+2n} dominates m_ν
- For a given \mathcal{O}_{5+2n} , use as few new fields as possible.
- No symmetry other than SM gauge symmetry imposed.

Consequences:

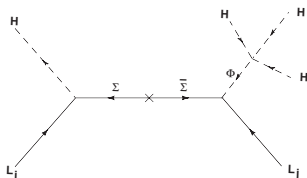
- New **scalars** ϕ and **fermions** Σ are both required to go beyond conventional seesaws.
- Can be classified according to *whether SM H can Yukawa couple to Σ*

New fields in higher-dim reps: (H, Σ) coupled $\Rightarrow \theta_7$

Unique option: one fermion $\Sigma = (1, 2)$ plus one scalar $\Phi = (3/2, 3)$

This is the model proposed in Babu et al 2009

θ_7 from



LHC pheno briefly analysed:

pair-production of multiply charged $\Phi^{\pm\pm\pm}$, $\Phi^{\pm\pm} \rightarrow$ multiple ℓ^\pm , W^\pm

testability yet to be studied

New fields in higher-dim reps: (H, Σ) *not coupled* $\Rightarrow \mathcal{O}_{5+4n}$

General case: *cascade seesaw*

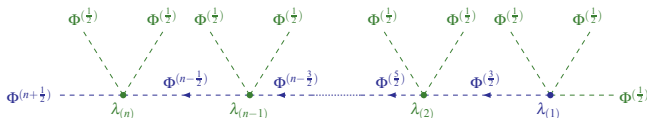
Liao 2010

one fermion $\Sigma = (n+1, 0)$ with integral $n \geq 1$

A sequence of scalars $\Phi^{(m+\frac{1}{2})} = (m+1/2, 1)$ with $m = 1, 2, \dots, n$

Consequences:

- Only $\Phi^{(n+\frac{1}{2})}$ can Yukawa couple to (Σ, F_L)
- Only $\Phi^{(\frac{3}{2})}$ can *directly* develop a naturally small vev, while others develop smaller and smaller vev's by a *cascading process*:

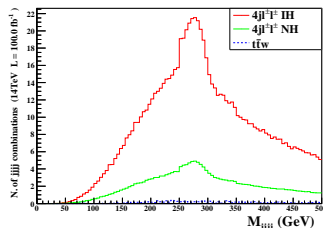
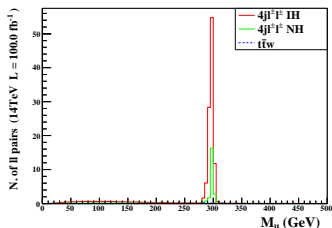


- m_V from \mathcal{O}_{5+4n} without imposing a global sym

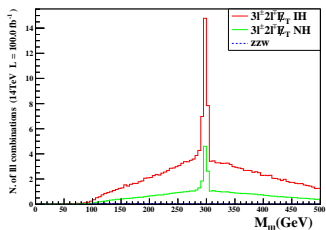


New fields in higher-dim reps: LHC pheno with \mathcal{O}_9

of events of $pp \rightarrow \Phi^{++}\Phi^+ \rightarrow 4i2\ell$ for $M_{\Phi^{++}\Phi^+} = 300$ GeV at 14 TeV



of events of $pp \rightarrow \Sigma^\pm \Sigma^0 \rightarrow 3\ell^\pm 2\ell^\mp + E_T$ for $M_\Sigma = 300$ GeV at 14 TeV



Ding et al 1403.xxxx

see also Chen and Zheng 1312.7207

Outline

- 1 Basics about neutrinos
- 2 Conventional seesaws and tests
- 3 Going beyond conventional seesaws
- 4 Summary and outlook**

Summary and outlook

- Great progress in measurements on **neutrino parameters**, including the oscillation data, cosmological observations, and other low-energy experiments, **is very helpful** for us to do **realistic collider phenomenology**.
- **Conventional seesaw models** have been fully studied in the literature except for **type III**. **Type I** has been done for *effective case*.
- There are a variety of models **beyond conventional seesaws**, some of which have been studied and some are being considered. An open but challenging task is how to distinguish them at colliders.
- Neutrino phys **at lepton colliders** has been less intensively studied because of limited achievable energy for heavy particles, while study at **very high energy colliders** has just started.

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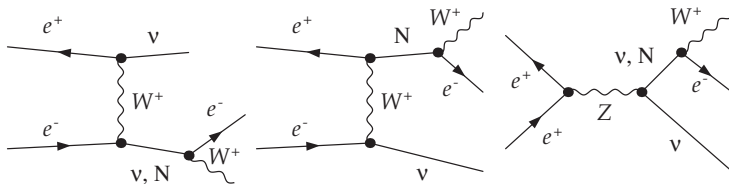
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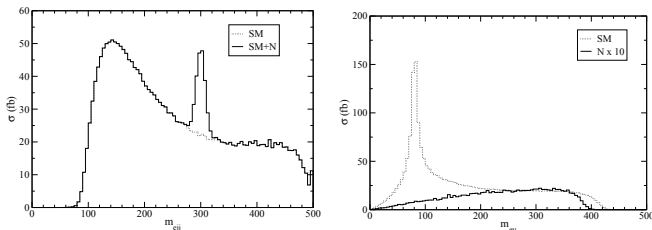
Backup: Simulation on type I seesaw at ILC

- $e^+e^- \rightarrow N\nu \rightarrow \ell W\nu$ at ILC Aguila et. al., PLB613, 2005



s-channel is suppressed compared to the first two

- Kinematical distributions of m_{ejj} (left) and $m_{e\nu}$ (right) for $V_{eN} = 0.073$, $V_{\mu N} = V_{\tau N} = 0$, and $m_N = 300$ GeV.



- Cross sections (in fb) for $e^+ e^- \rightarrow e^\mp W^\pm \nu$

	No cuts	m_{ejj}	$m_{e\nu}$	$m_{ejj}, m_{e\nu}$
SM	2253	89.1	1387	53.6
SM + N	2339	173.7	1489	130.8

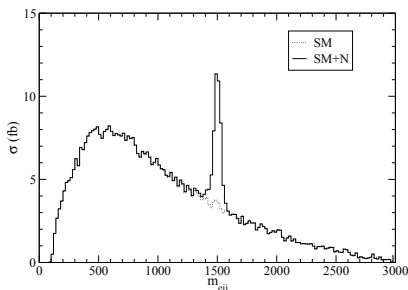
before and after the kinematical cuts:

$$290 \text{ GeV} \leq m_{ejj} \leq 310 \text{ GeV}, \quad m_{e\nu} \leq 40 \text{ GeV} \text{ or } m_{e\nu} \geq 110 \text{ GeV}.$$

Backup: Simulation on type I seesaw at CLIC

- Kinematical distributions for $e^+e^- \rightarrow e^\mp W^\pm \nu$ of m_{eij} with

$V_{eN} = 0.05$, $V_{\mu N} = V_{\tau N} = 0$, and $m_N = 1500$ GeV. Aguila et. al., JHEP0505, 2005



	No cut	With cut
SM	516	14.6
SM + N	548	39.4

Cross sections (in fb) before and after the kinematical cut:
 $1460 \text{ GeV} \leq m_{eij} \leq 1540 \text{ GeV}$.

- Their conclusions: if no signal is found at ILC or CLIC:

- ILC: $V_{eN} \leq 0.007$ for $m_N = 200 - 400$ GeV.
- CLIC: $V_{eN} \leq 0.002 - 0.006$ for $m_N = 1 - 2$ TeV.

Backup: Distinguish 3 conventional seesaws at LHC

Luminosity for discovery in each model Aguila et. al., NPB813, 2009

	Seesaw I $m_N = 100 \text{ GeV}$	Seesaw II $m_\Delta = 300 \text{ GeV}$	Seesaw III $m_\Sigma = 300 \text{ GeV}$
Six leptons	-	-	×
Five leptons	-	-	28 fb^{-1}
$\ell^\pm \ell^\pm \ell^\pm \ell^\mp$	-	-	15 fb^{-1} $m_E \text{ rec}$
$\ell^+ \ell^+ \ell^- \ell^-$	-	$19 / 2.8 \text{ fb}^{-1}$ $m_{\Delta^{++}} \text{ rec}$	7 fb^{-1} $m_E \text{ rec}$
$\ell^\pm \ell^\pm \ell^\pm$	-	-	30 fb^{-1}
$\ell^\pm \ell^\pm \ell^\mp$	$< 180 \text{ fb}^{-1}$	$3.6 / 0.9 \text{ fb}^{-1}$ $m_{\Delta^{++}} \text{ rec}$	2.5 fb^{-1} $m_N \text{ rec}$
$\ell^\pm \ell^\pm$	$< 180 \text{ fb}^{-1}$ $m_N \text{ rec}$	$17.4 / 4.4 \text{ fb}^{-1}$ $m_{\Delta^{++}} \text{ rec}$	1.7 fb^{-1} $m_\Sigma \text{ rec}$
$\ell^+ \ell^-$	×	$15 / 27 \text{ fb}^{-1}$ $m_\Delta \text{ rec}$	80 fb^{-1} $m_\Sigma \text{ rec}$
ℓ^\pm	×	×	