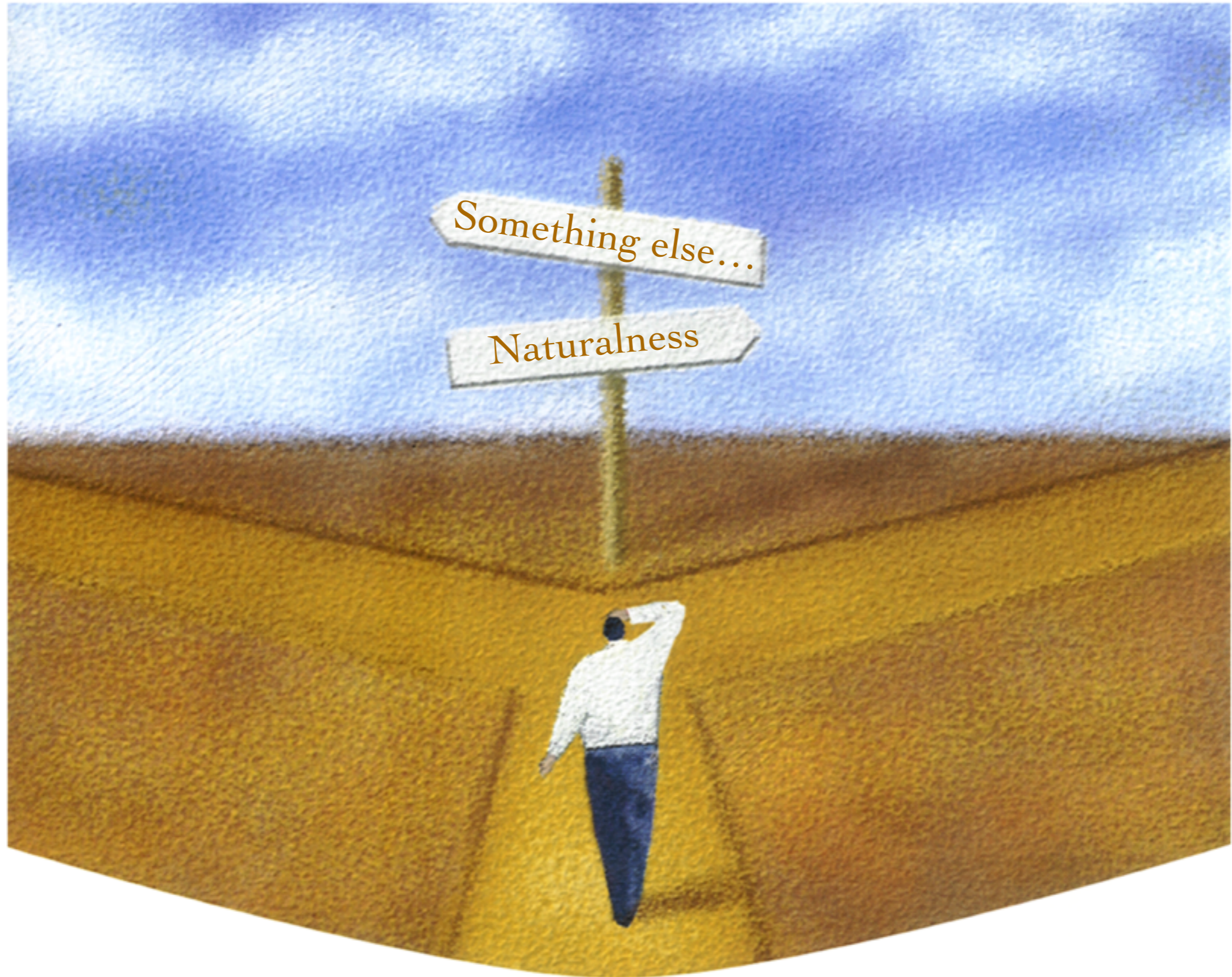


**SMALL NUMBERS
AND
LARGE MACHINES**

Savas Dimopoulos
Stanford University

The Origin of Small Numbers



Small Numbers and Coincidences

Naturalness - Dynamics

Problem

Hydrogen Binding Energy

Deuteron Binding Energy

Nuclear Binding Energy

π^+ - π^0 mass difference

$K - \bar{K}$ mixing

QCD scale

Electron Mass

Solution

$$E_b = \frac{1}{2} \frac{e^4}{(4\pi)^2} m_e$$

$$E_b \approx \frac{1}{2} \frac{1}{(4\pi)^2} \frac{m_N}{2}$$

Symmetry/Dynamics

Flavor Symmetry

Dimensional Transmutation

Chiral Symmetry

Small Numbers and Coincidences

Something else...

Problem

Earth-Sun Distance

Cosmological Constant

7 eV line of ^{229}Th nucleus

Solar Eclipse

Solution

Environmental Selection 10^{22} suns

Environmental Selection? 10^{500} universes!

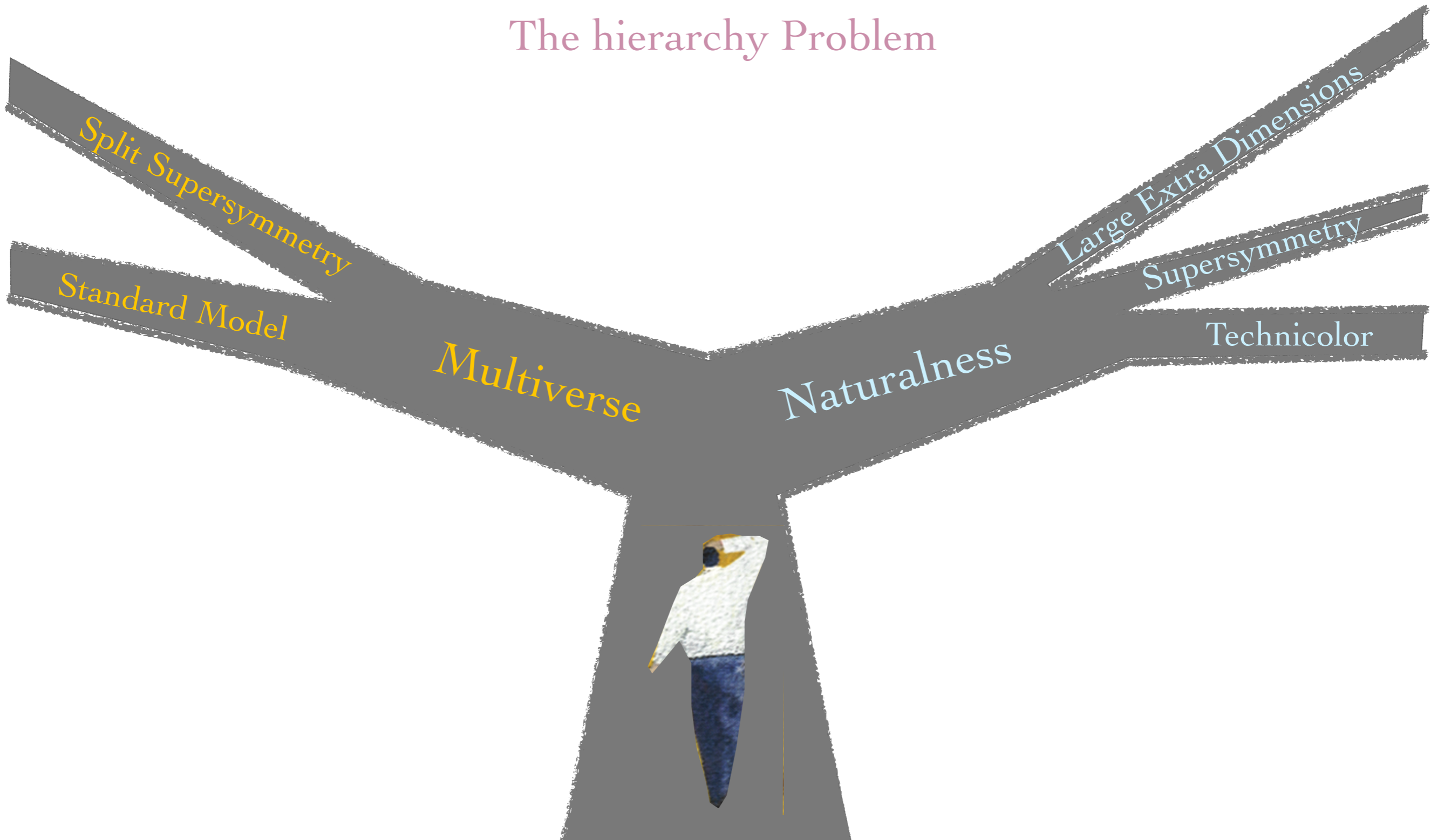
“Look-elsewhere” effect

Plain Luck!

Small Numbers and Coincidences

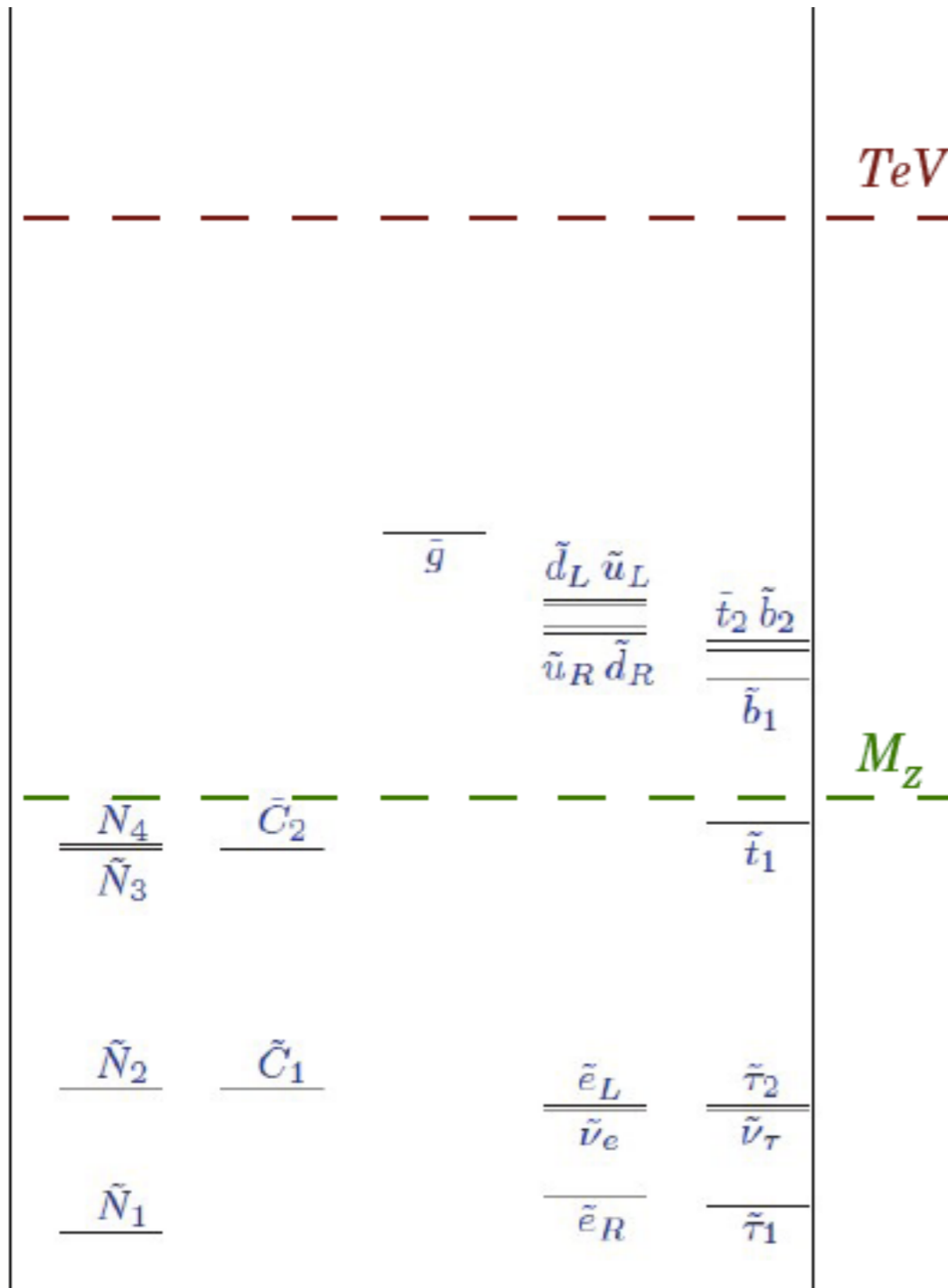
What about the Electroweak Scale?

The hierarchy Problem

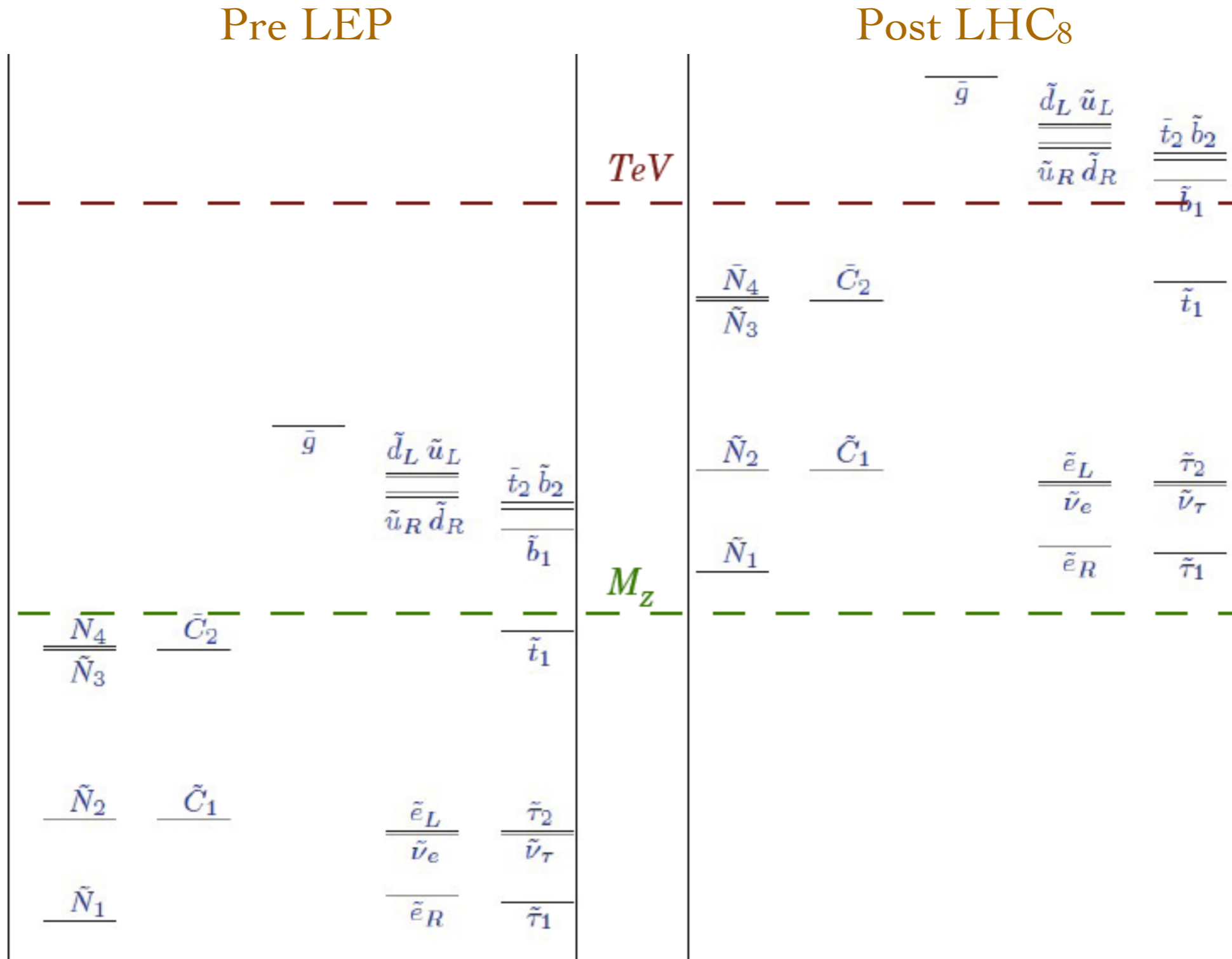


The Hard Facts

Pre LEP

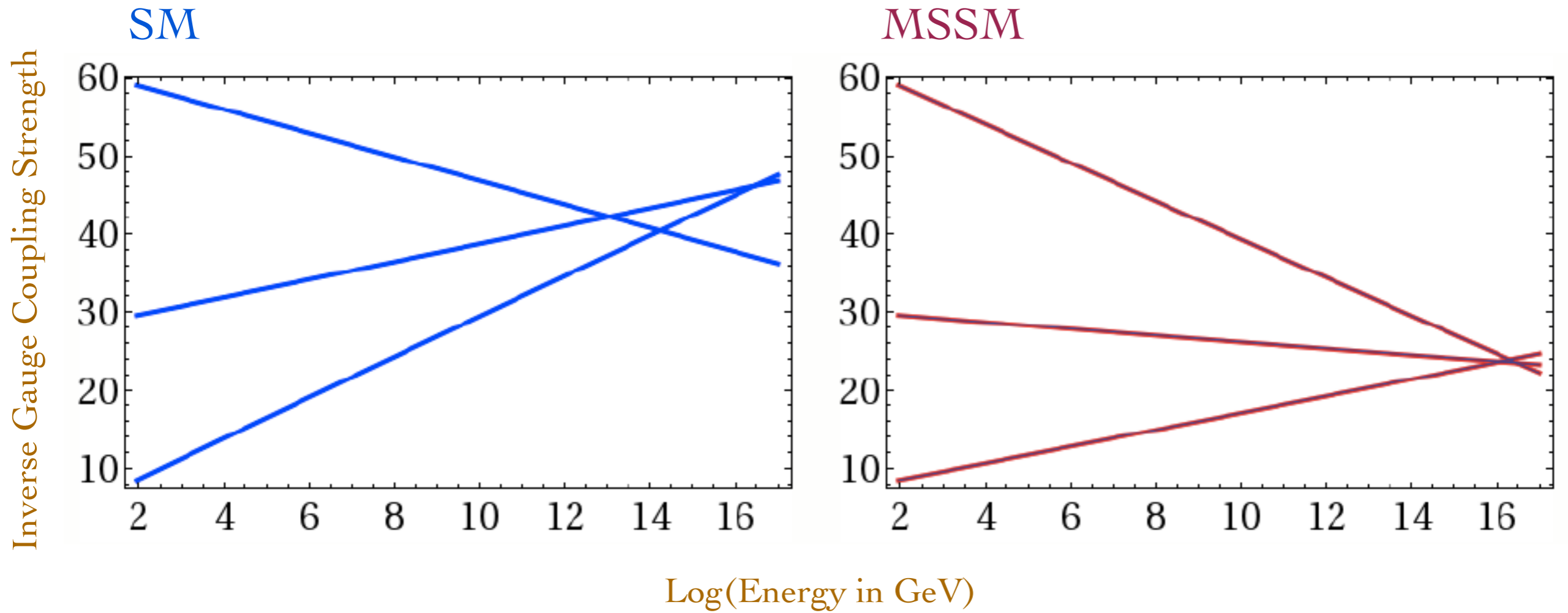


The Hard Facts



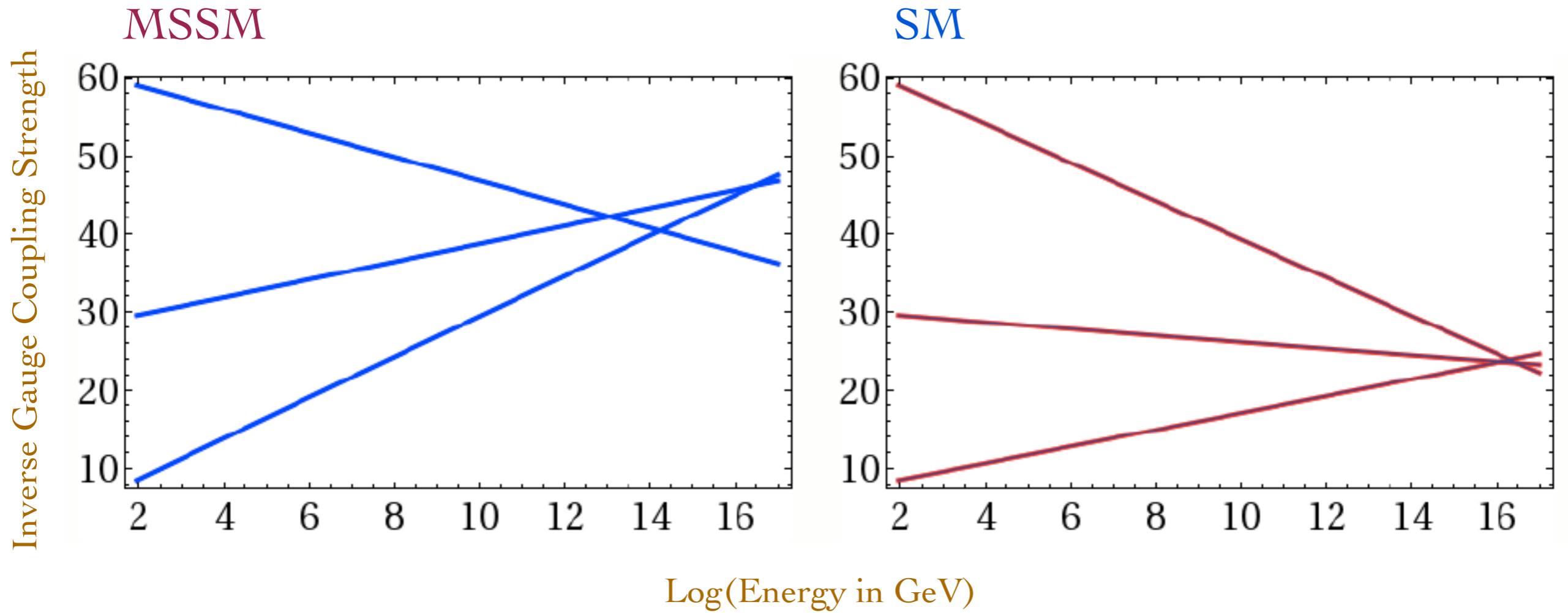
The connection with the hierarchy problem is diminished

Why Supersymmetry?



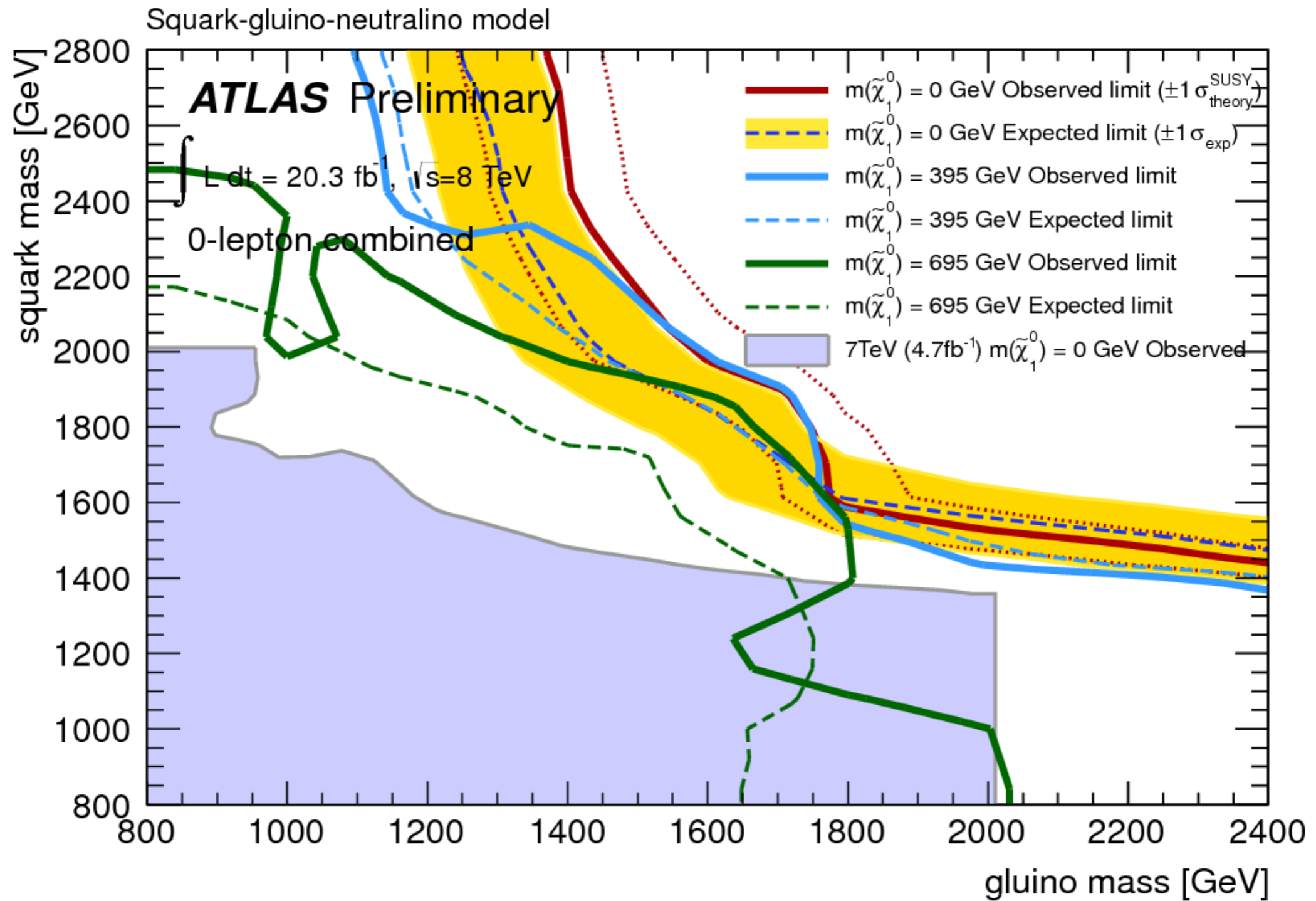
Gauge Coupling running at two loops

Why Supersymmetry?



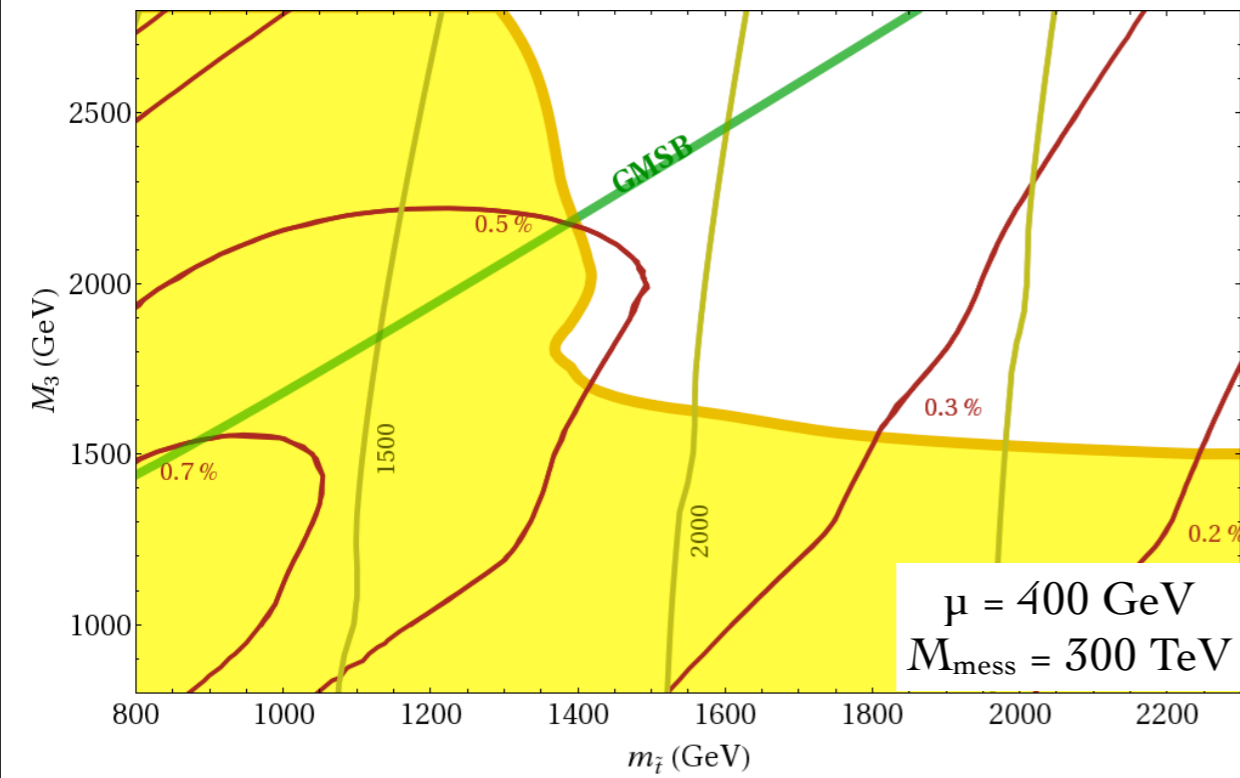
Gauge Coupling running at two loops

The Missing Superpartner Problem



The Status of Naturalness in SUSY

MSSM with A-terms

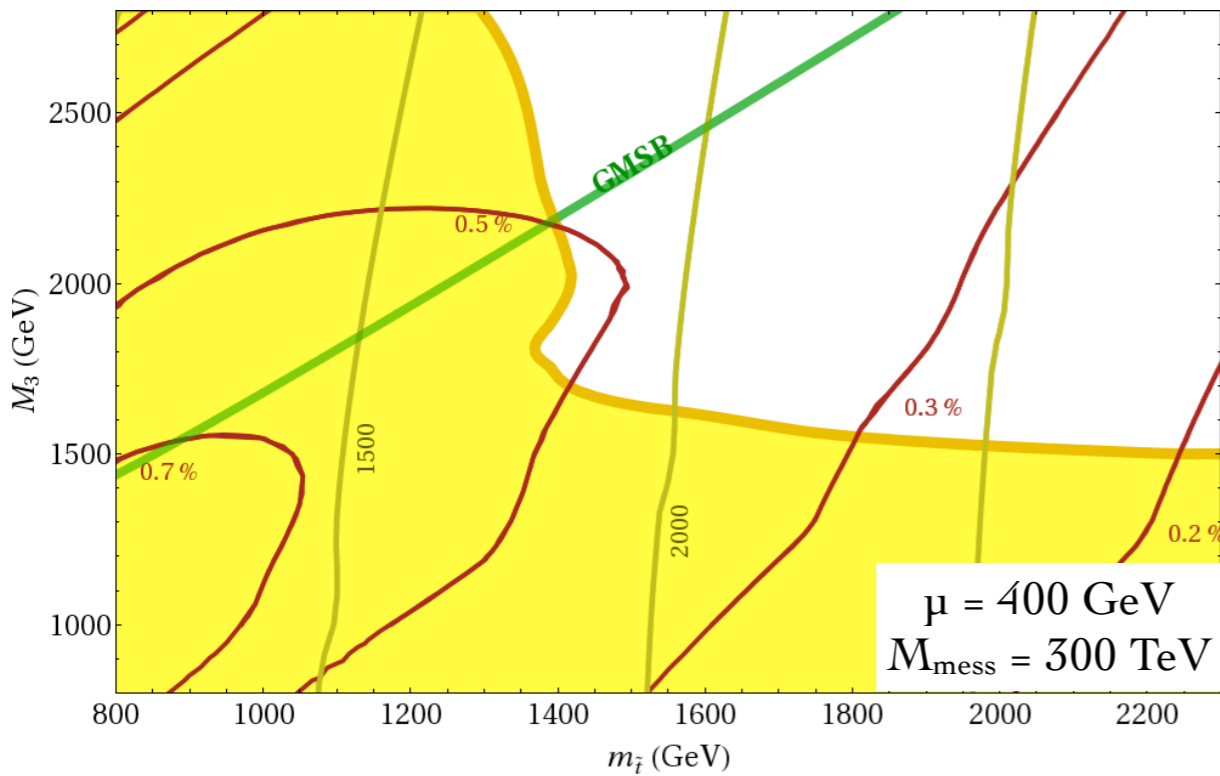


Arvanitaki et. al. (2013)

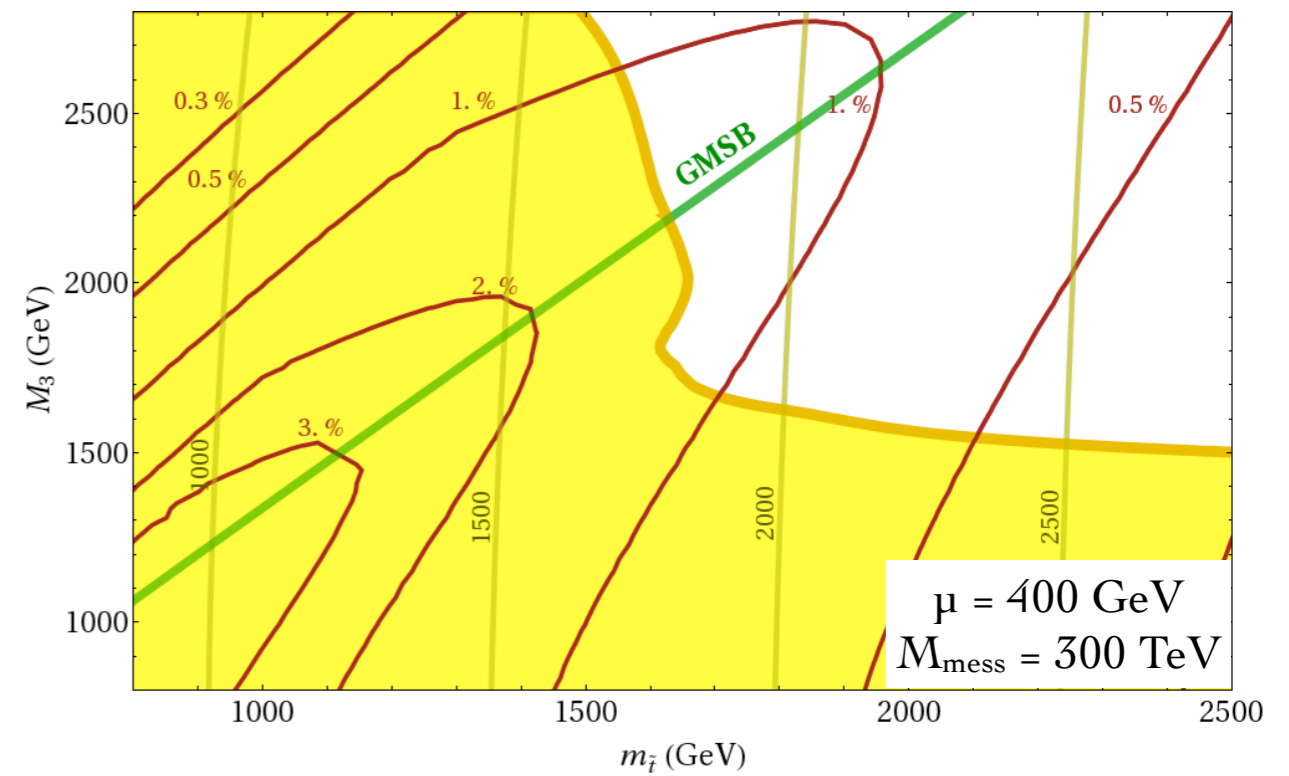
- **In the MSSM:** Tuning dominated by the Higgs Mass

The Status of Naturalness in SUSY

MSSM with A-terms



NMSSM
or any model that “fixes” the Higgs mass

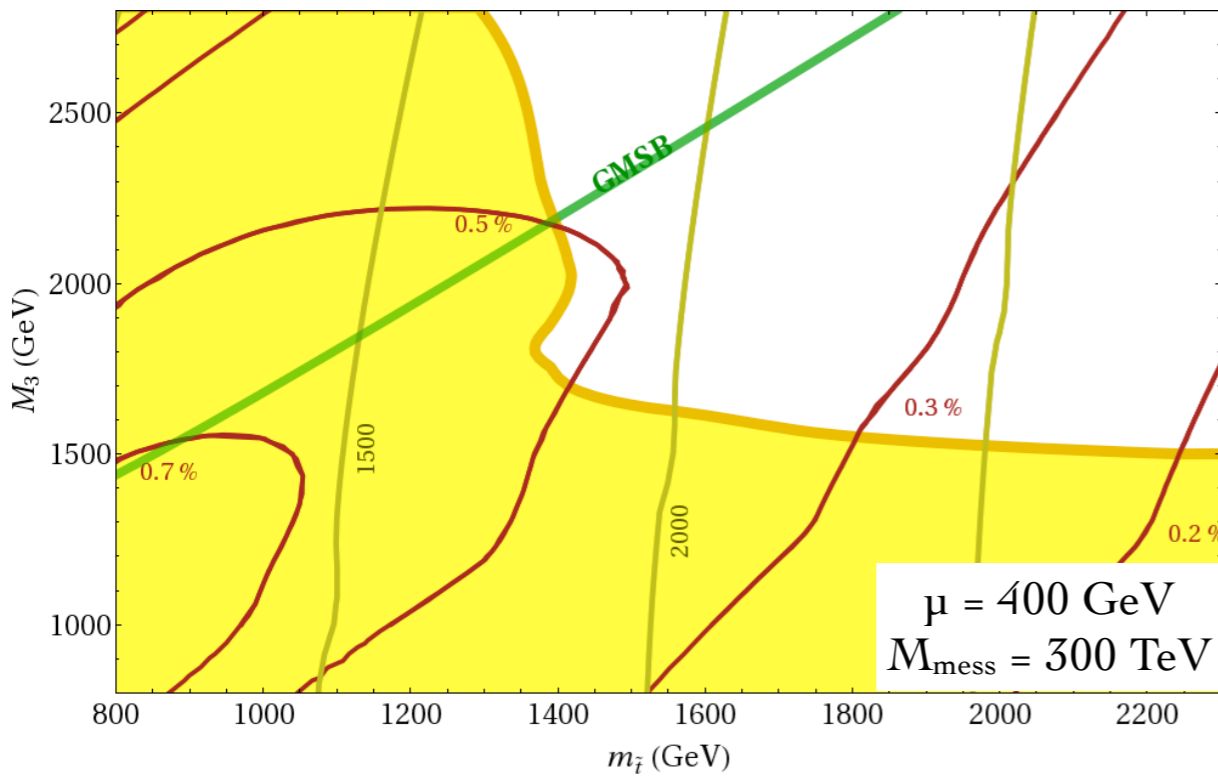


Arvanitaki et. al. (2013)

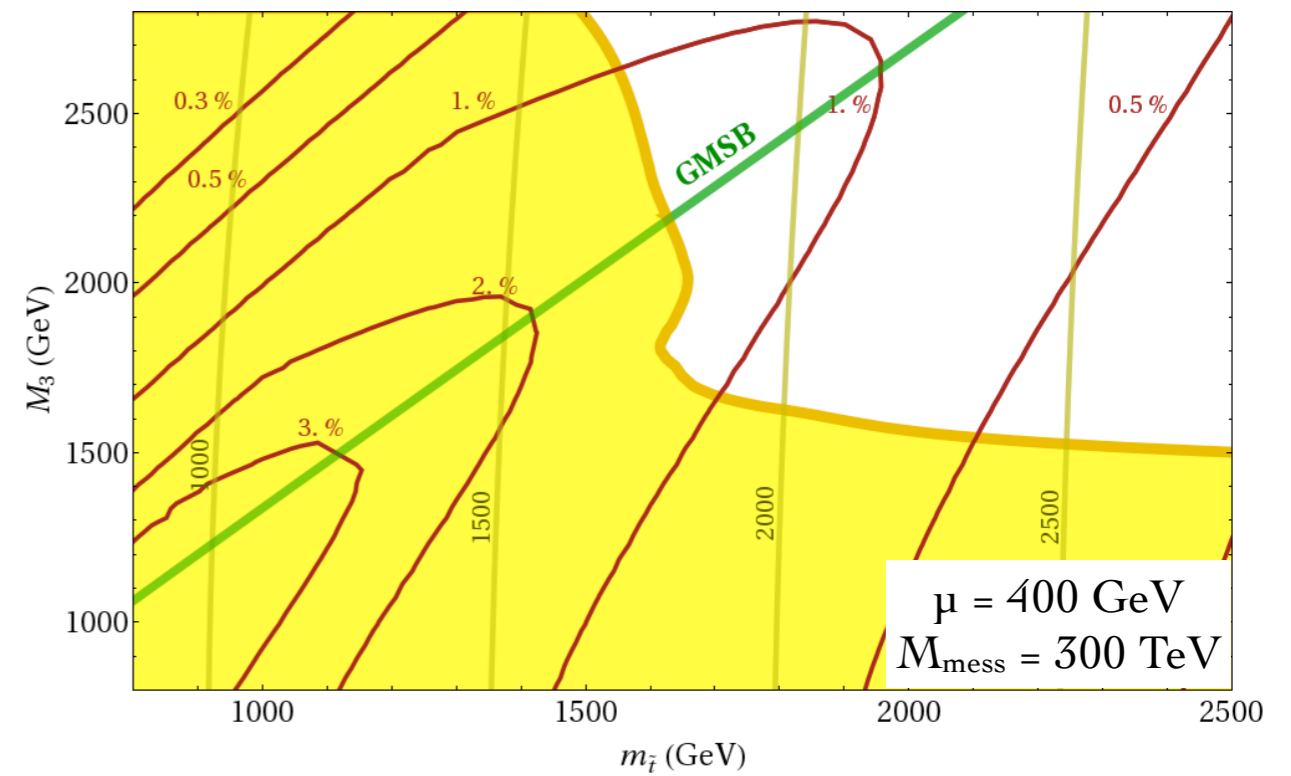
- **In the MSSM:** Tuning dominated by the Higgs Mass
- **In any model that fixes the Higgs mass:** Tuning dominated by LHC bounds

The Status of Naturalness in SUSY

MSSM with A-terms



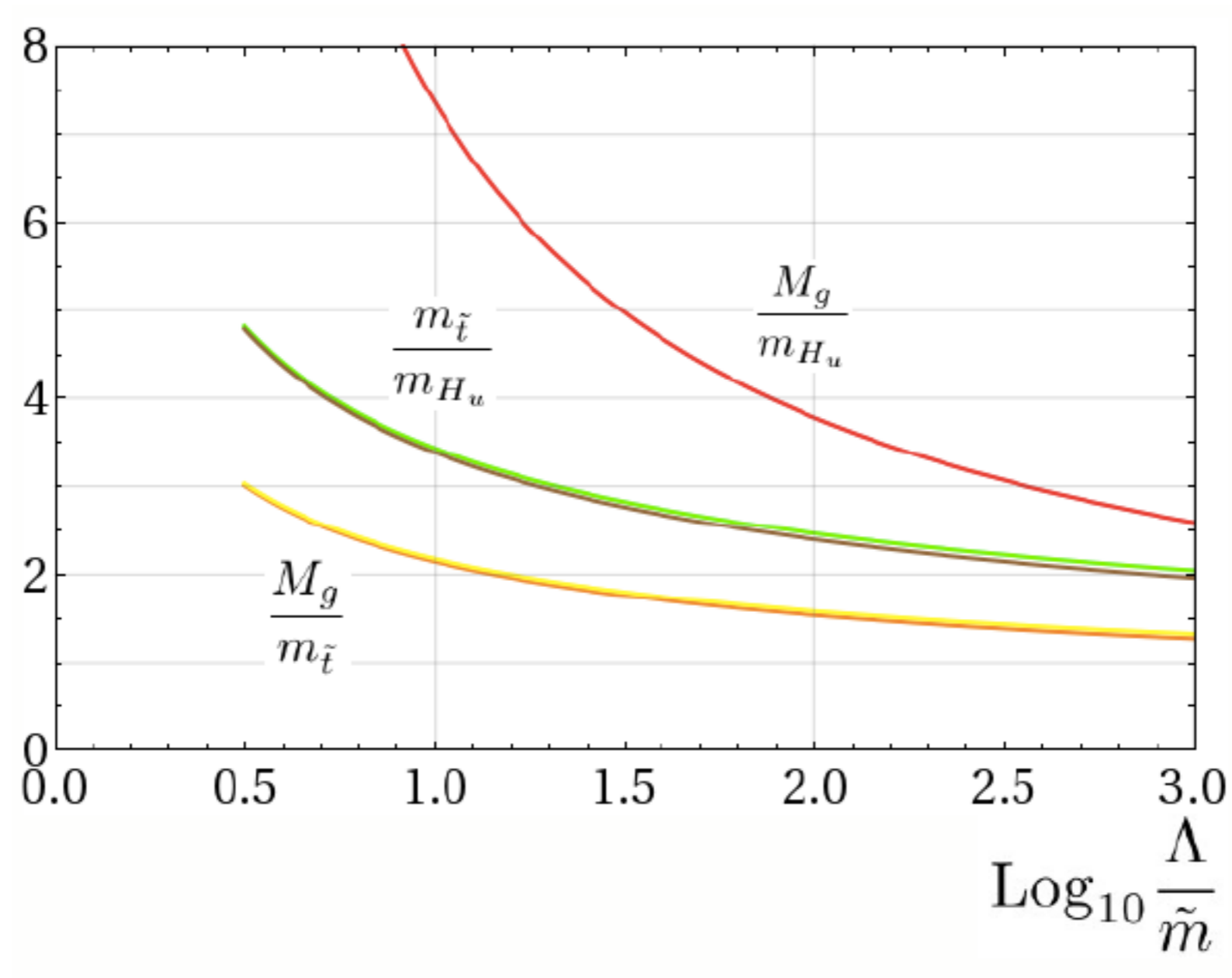
NMSSM
or any model that "fixes" the Higgs mass



Arvanitaki et. al. (2013)

- In the MSSM: Tuning dominated by the Higgs Mass
- In any model that fixes the Higgs mass: Tuning dominated by LHC bounds
- LHC pushes the bounds on Naturalness
- Natural SUSY and RPV: Gluino bounds above a TeV imply significant tuning

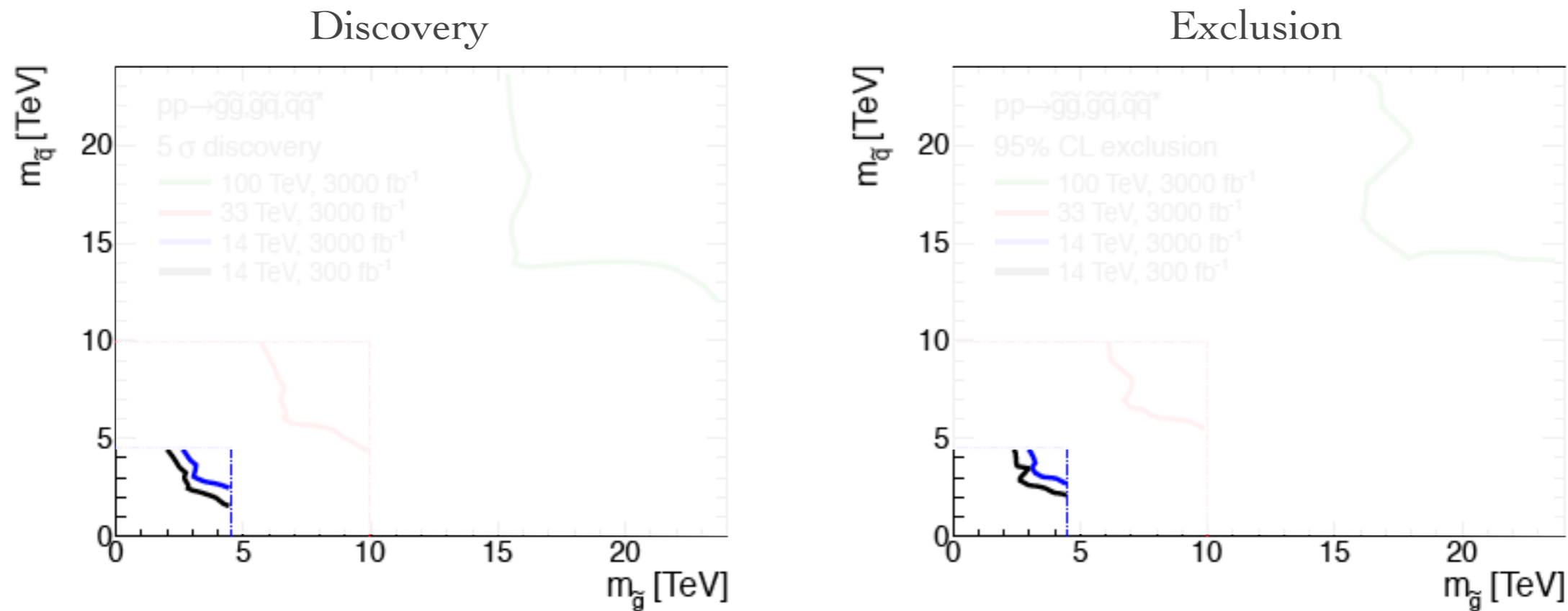
The Gluino Sucks



Gluino Bounds constrain all Low Energy Supersymmetry scenarios

Reach of 100 TeV

Squark-Gluino Reach



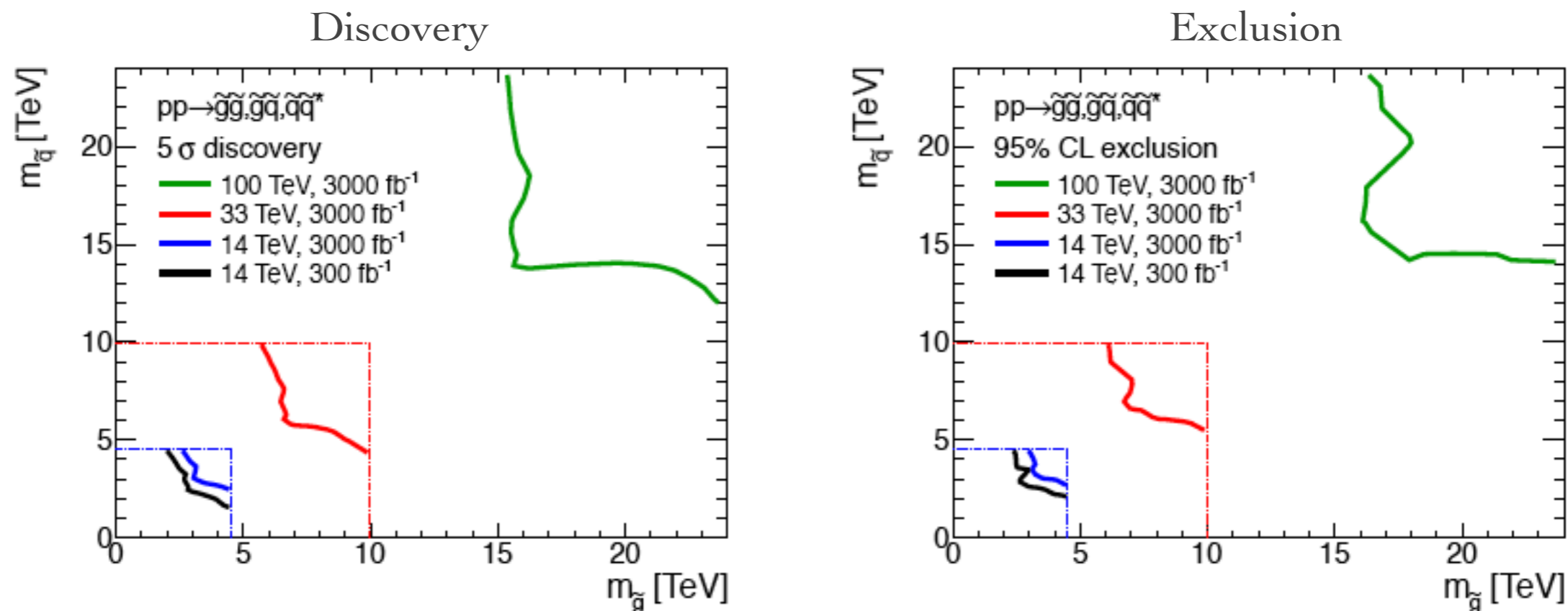
Cohen et. al. (2013)

LHC 14:

Probing theories worse than 1% tuned

Reach of 100 TeV

Squark-Gluino Reach



Cohen et. al. (2013)

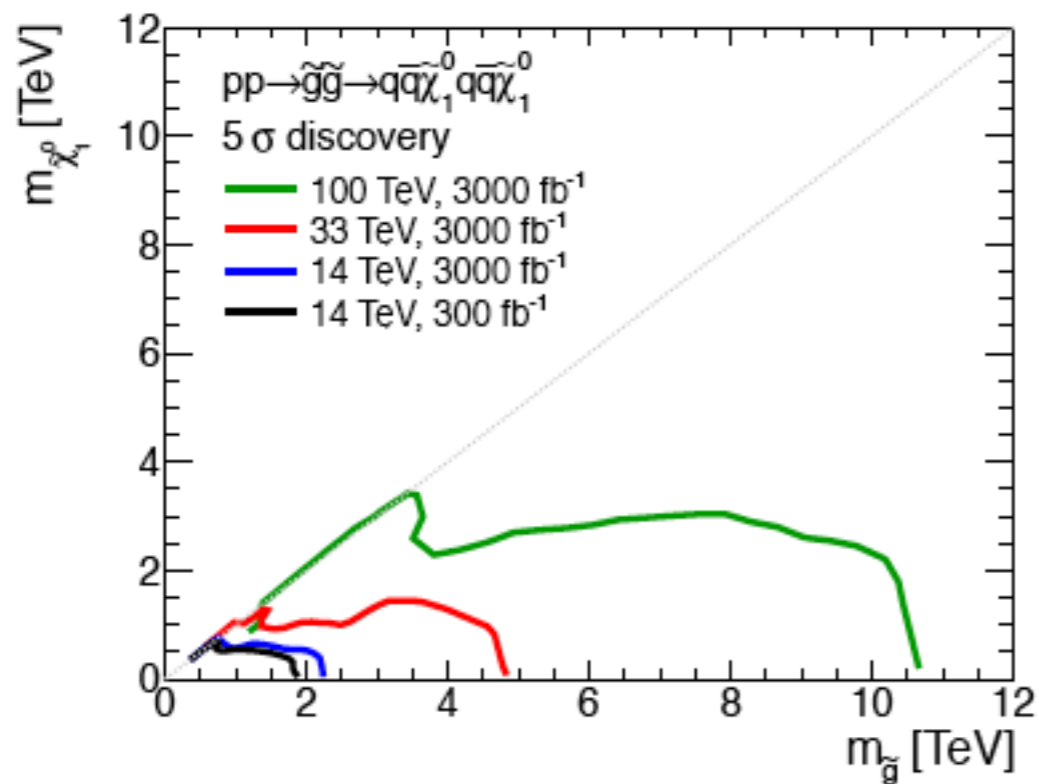
LHC 14: Probing theories worse than 1% tuned

100 TeV Collider: Probes Naturalness at the 0.01% level

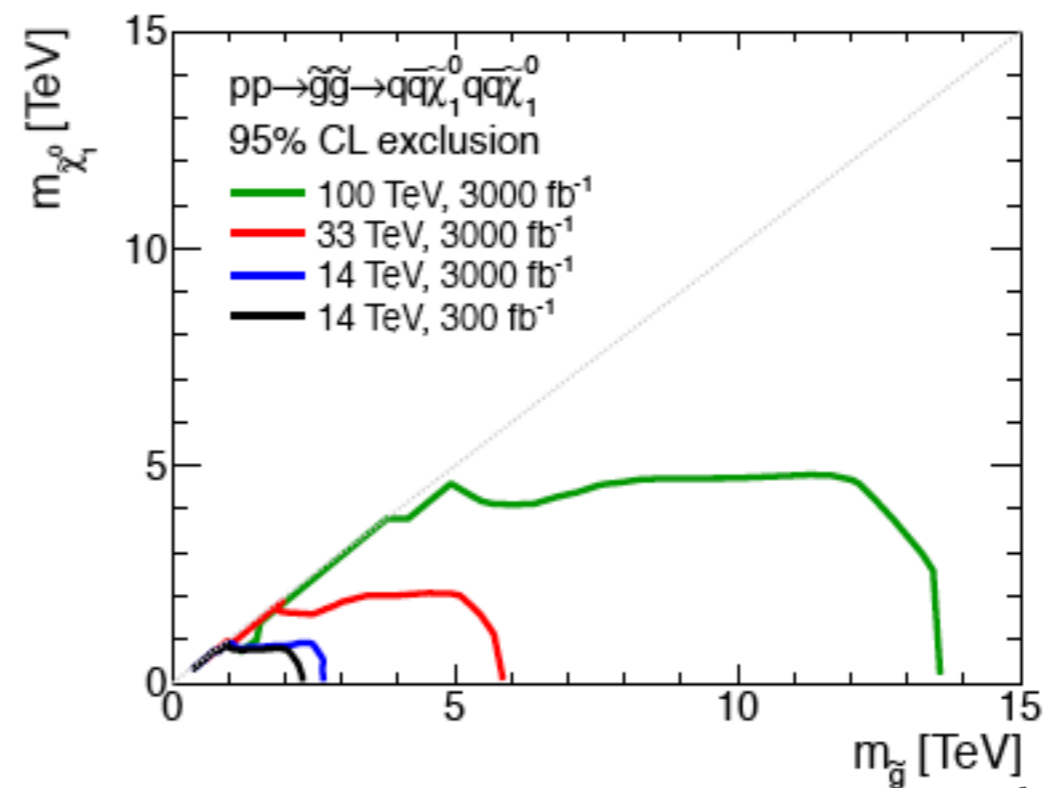
Reach of 100 TeV

Glino Reach

Discovery



Exclusion

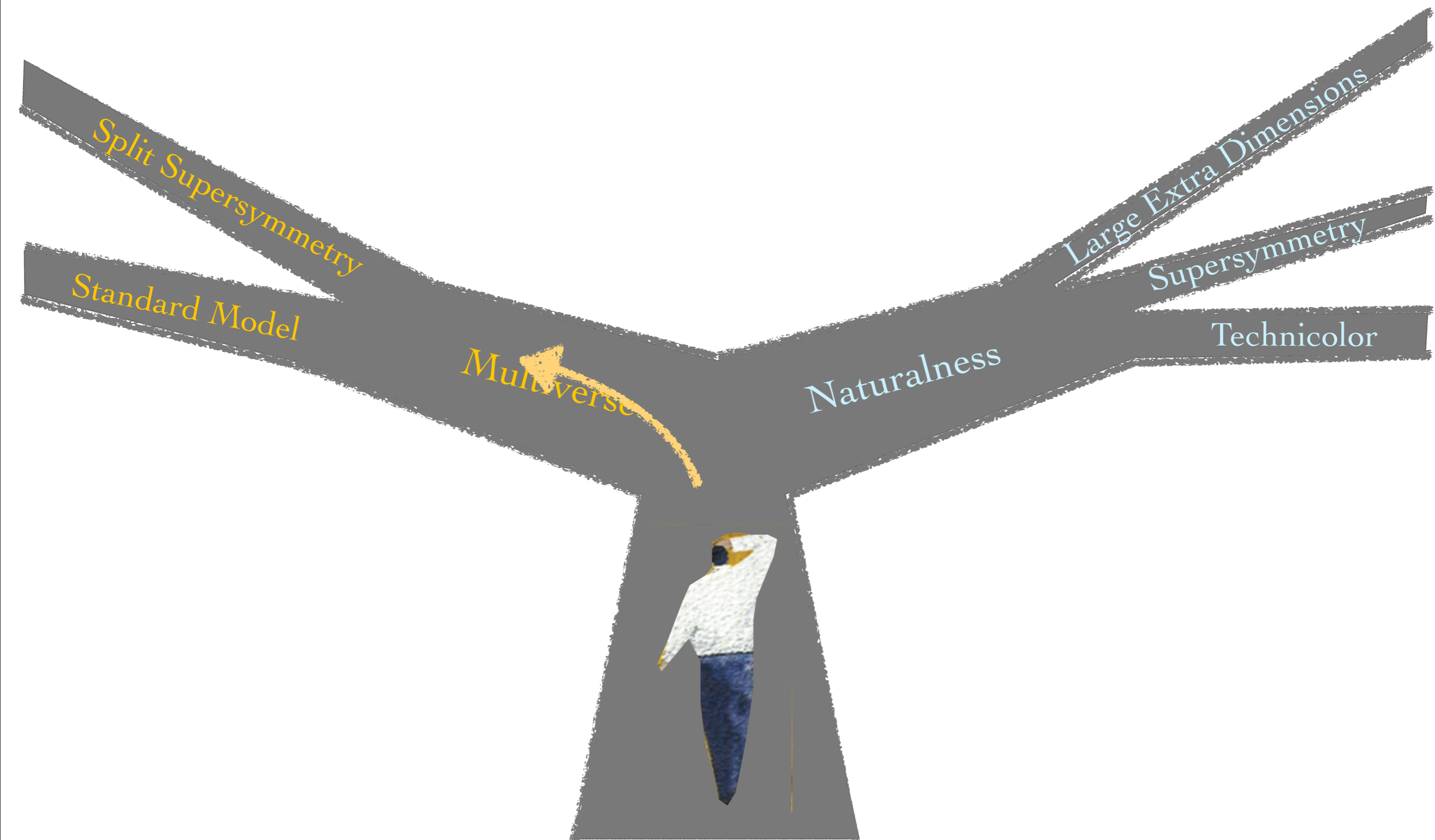


Cohen et. al. (2013)

LHC 14: Probing theories worse than 1% tuned

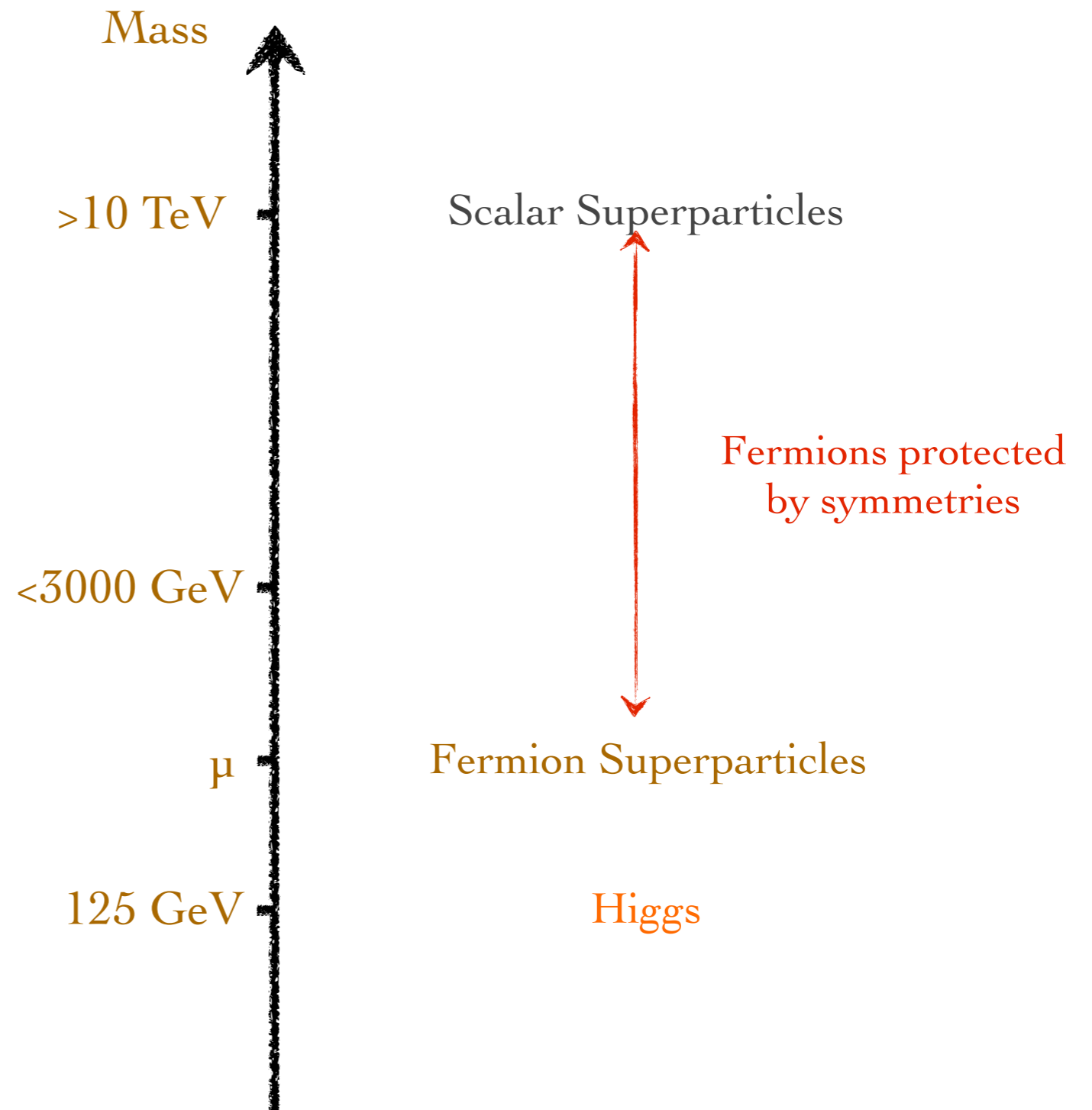
100 TeV Collider: Probes Naturalness at the 0.01% level

At the Crossroads



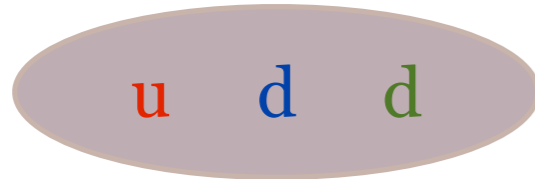
Split Supersymmetry

- Preserves successes of Dark Matter and gauge coupling unification
- Atomic Principle: One tuned light higgs

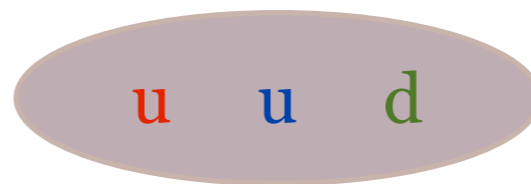


What if we now vary the weak scale?

Neutron



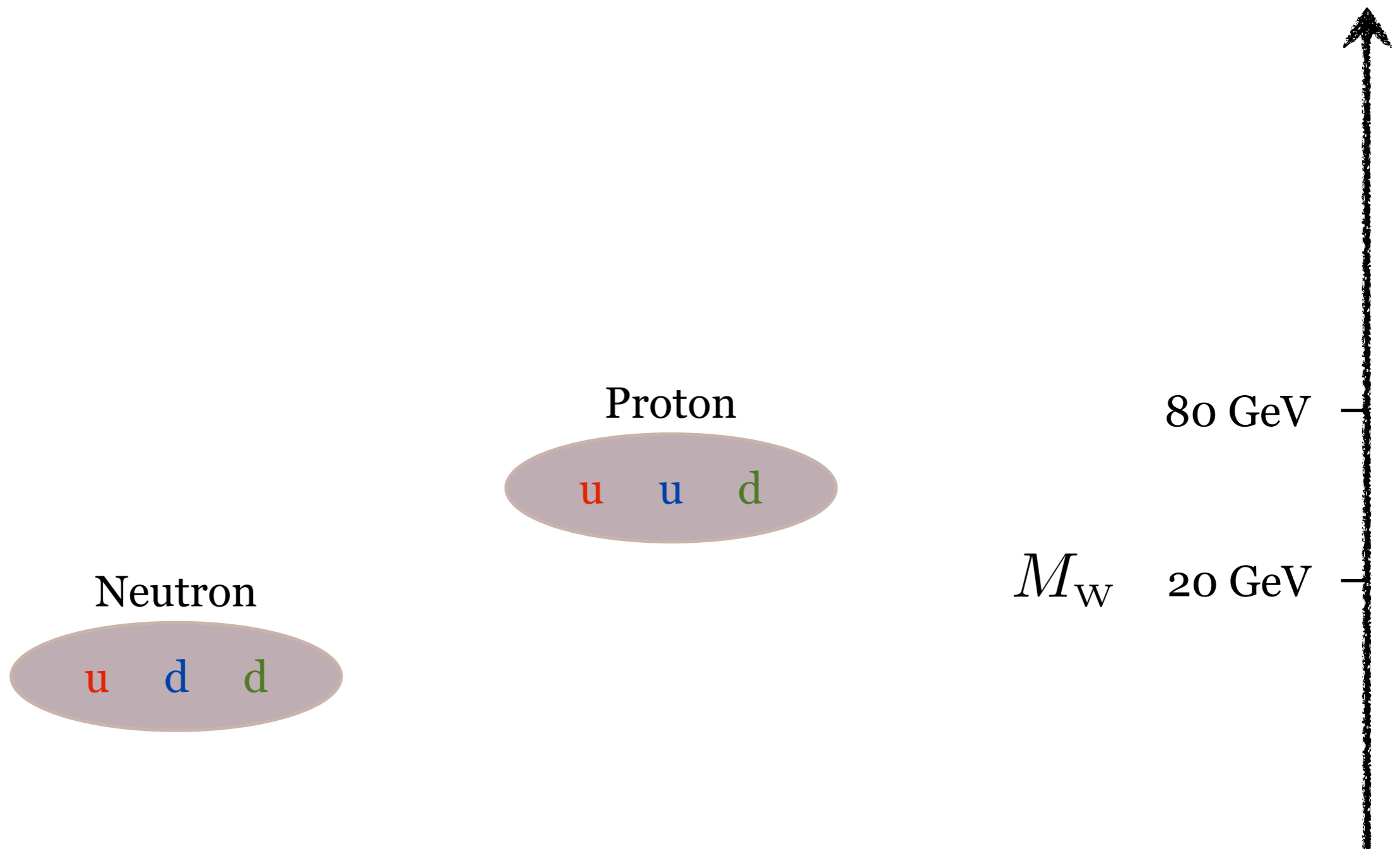
Proton



M_W 80 GeV



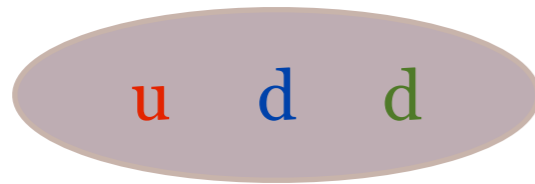
What if we now vary the weak scale?



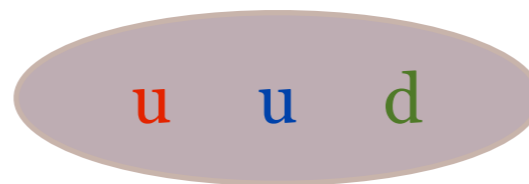
Protons decay to neutrons inside nuclei:
No Hydrogen

What if we now vary the weak scale?

Neutron



Proton



M_W 400 GeV

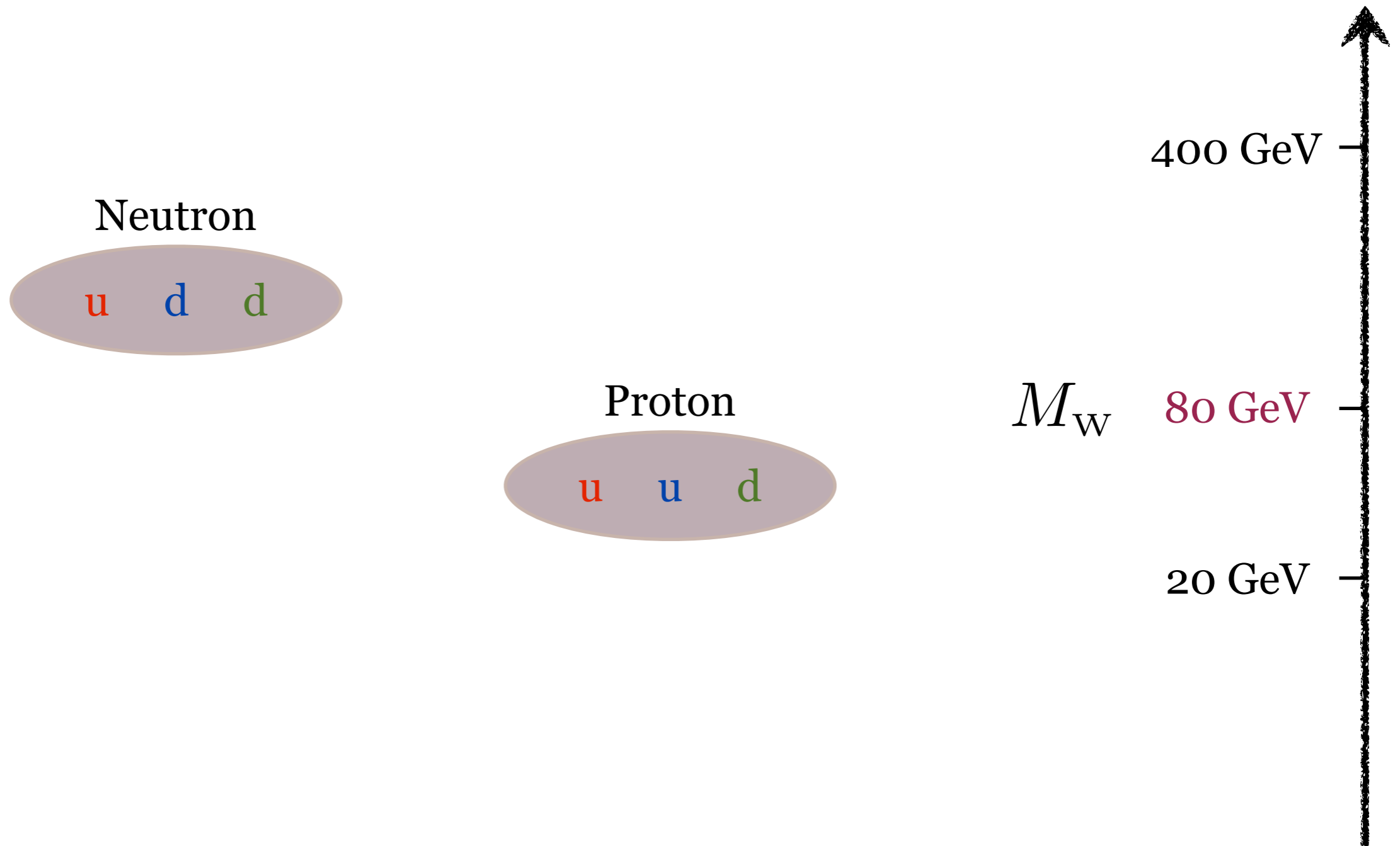
80 GeV

20 GeV



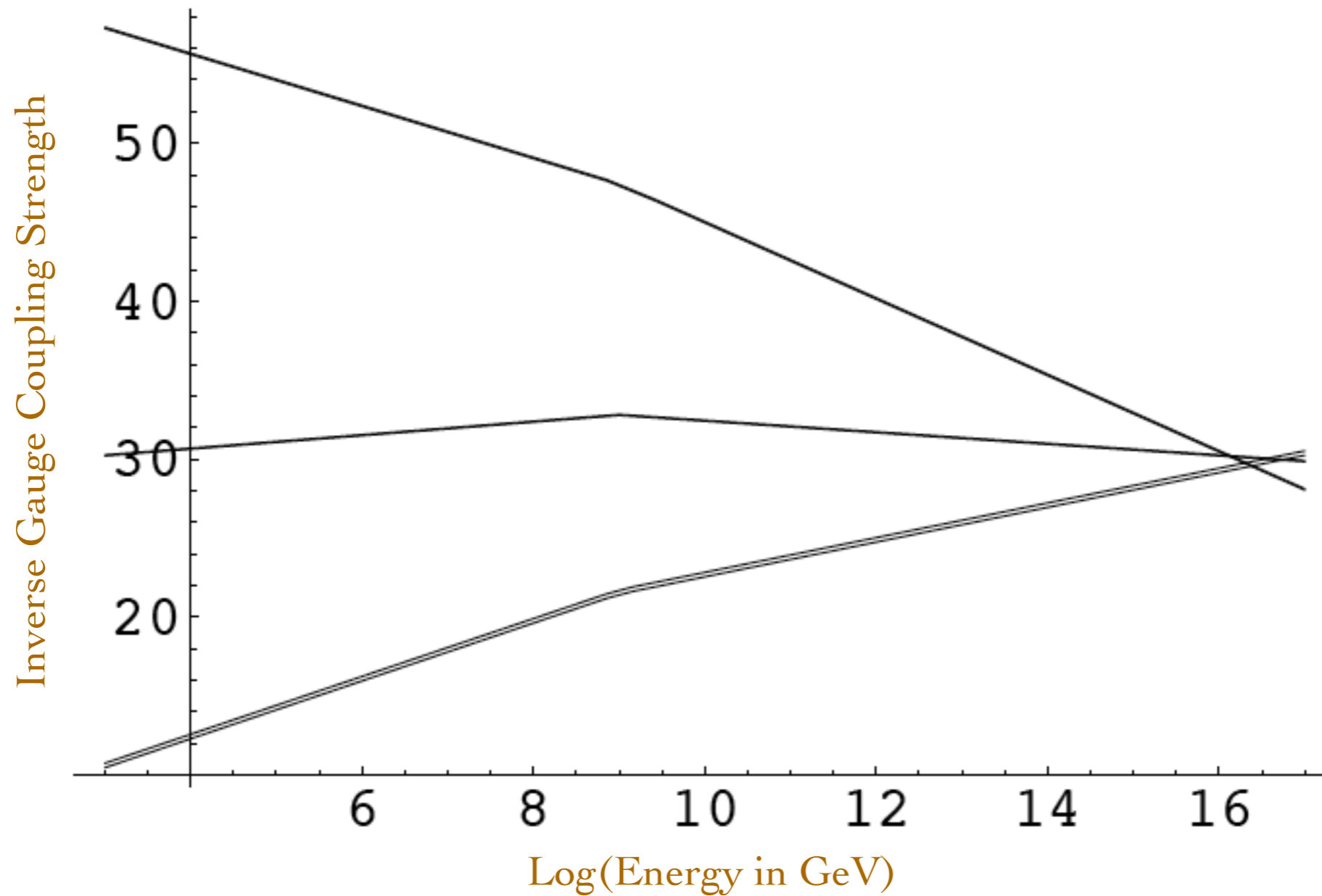
Neutrons decay inside nuclei:
Only Hydrogen

What if we now vary the weak scale?



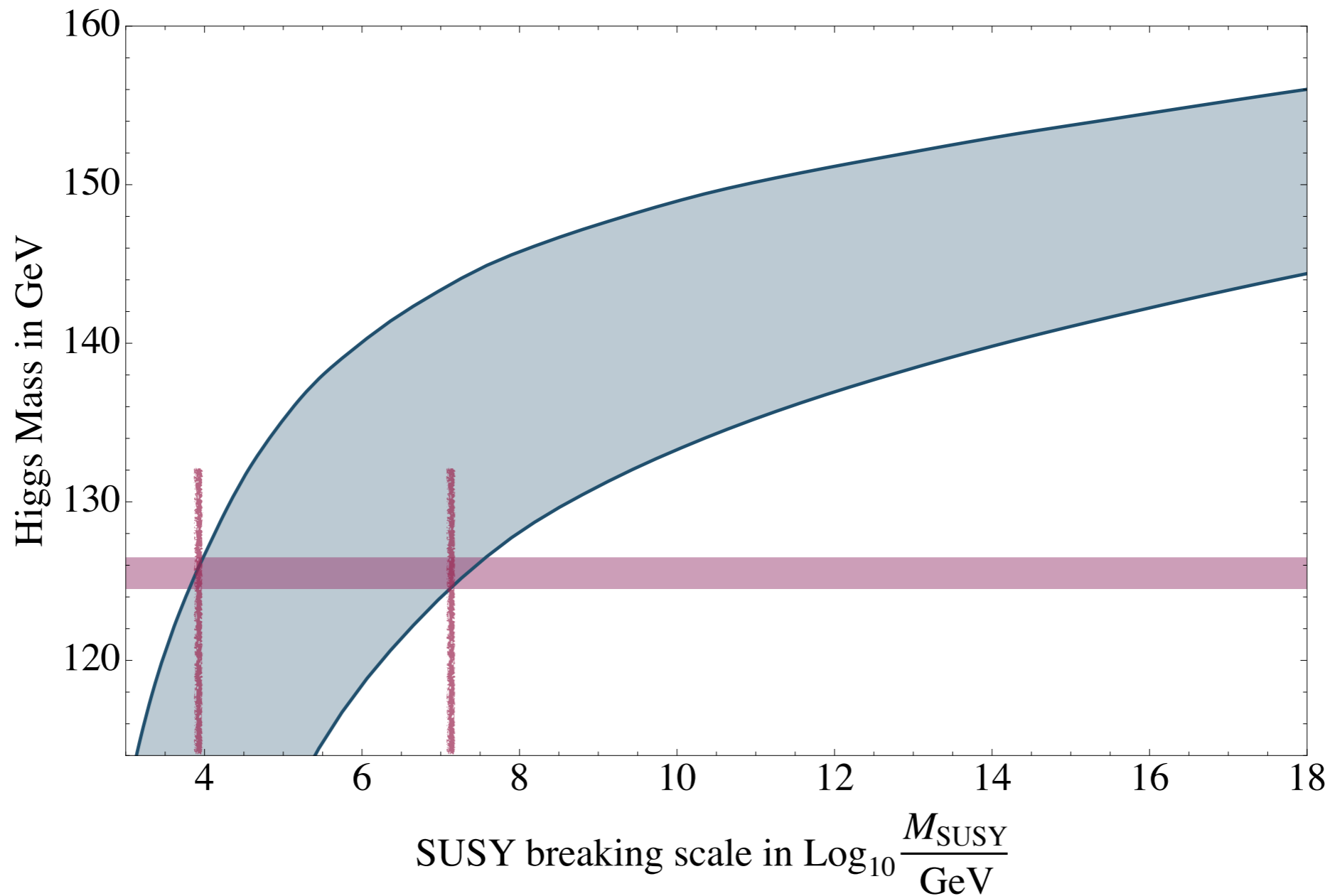
The weak scale at ~ 100 GeV is essential for the existence of atoms:
'Atomic principle'

Unification in Split Supersymmetry



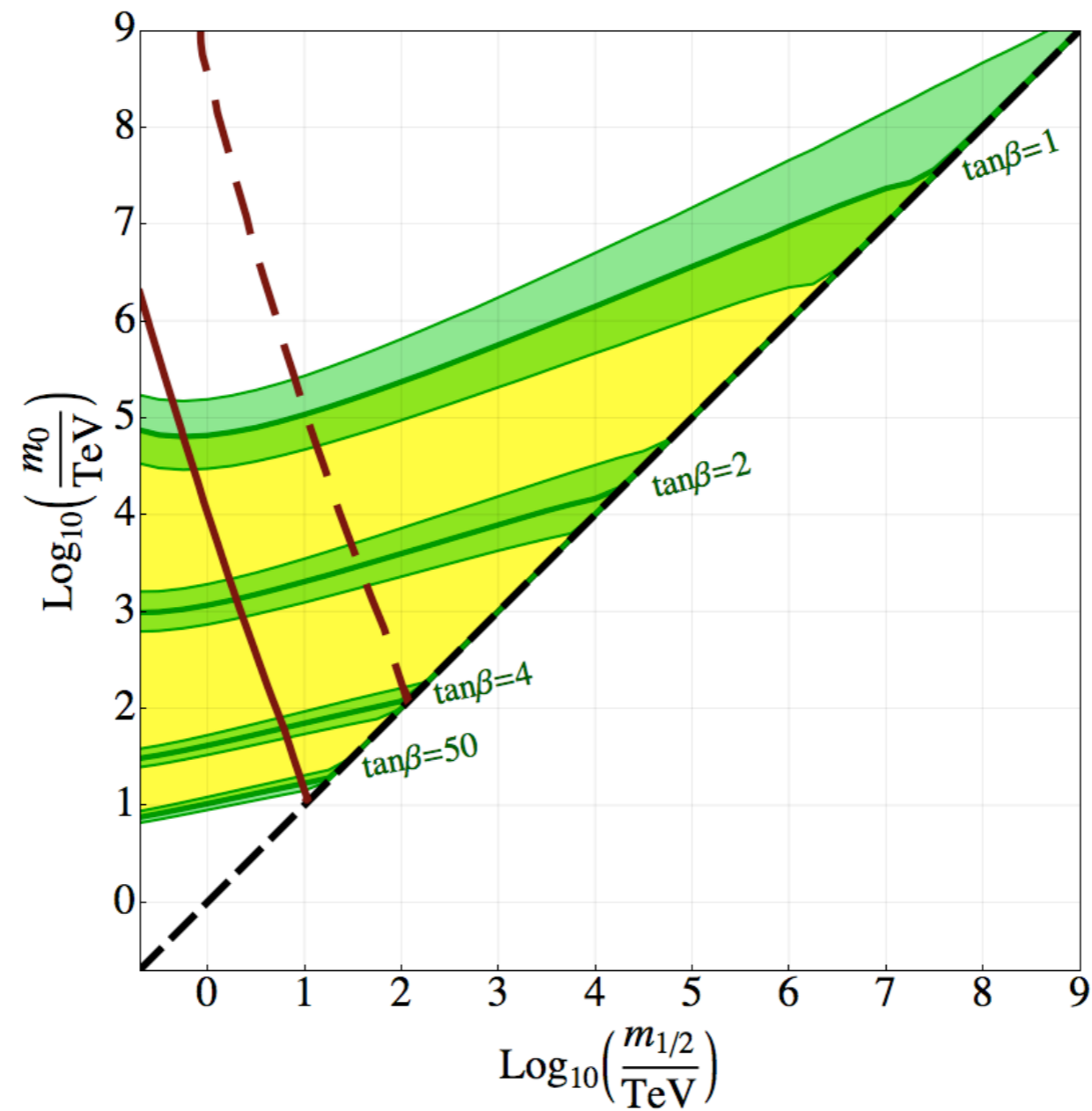
Works as well as ordinary Supersymmetry

125 GeV Higgs in Split Supersymmetry



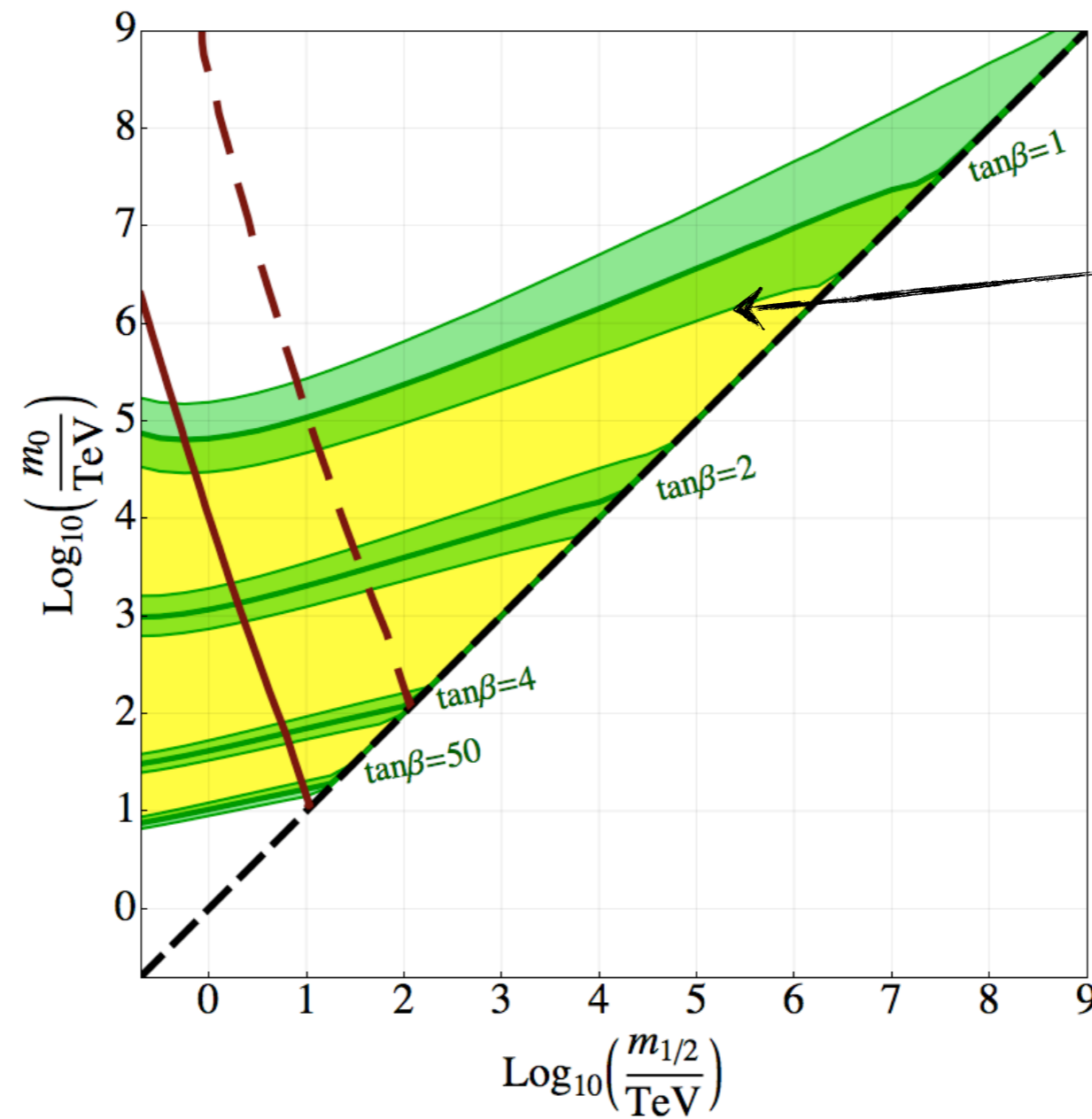
- Favors scalars between 10 - 10^4 TeV: **Mini-Split**

The 125 GeV Higgs and Unification in Mini-Split



w/ Arvanitaki, Craig, Villadoro

The 125 GeV Higgs and Unification in Mini-Split

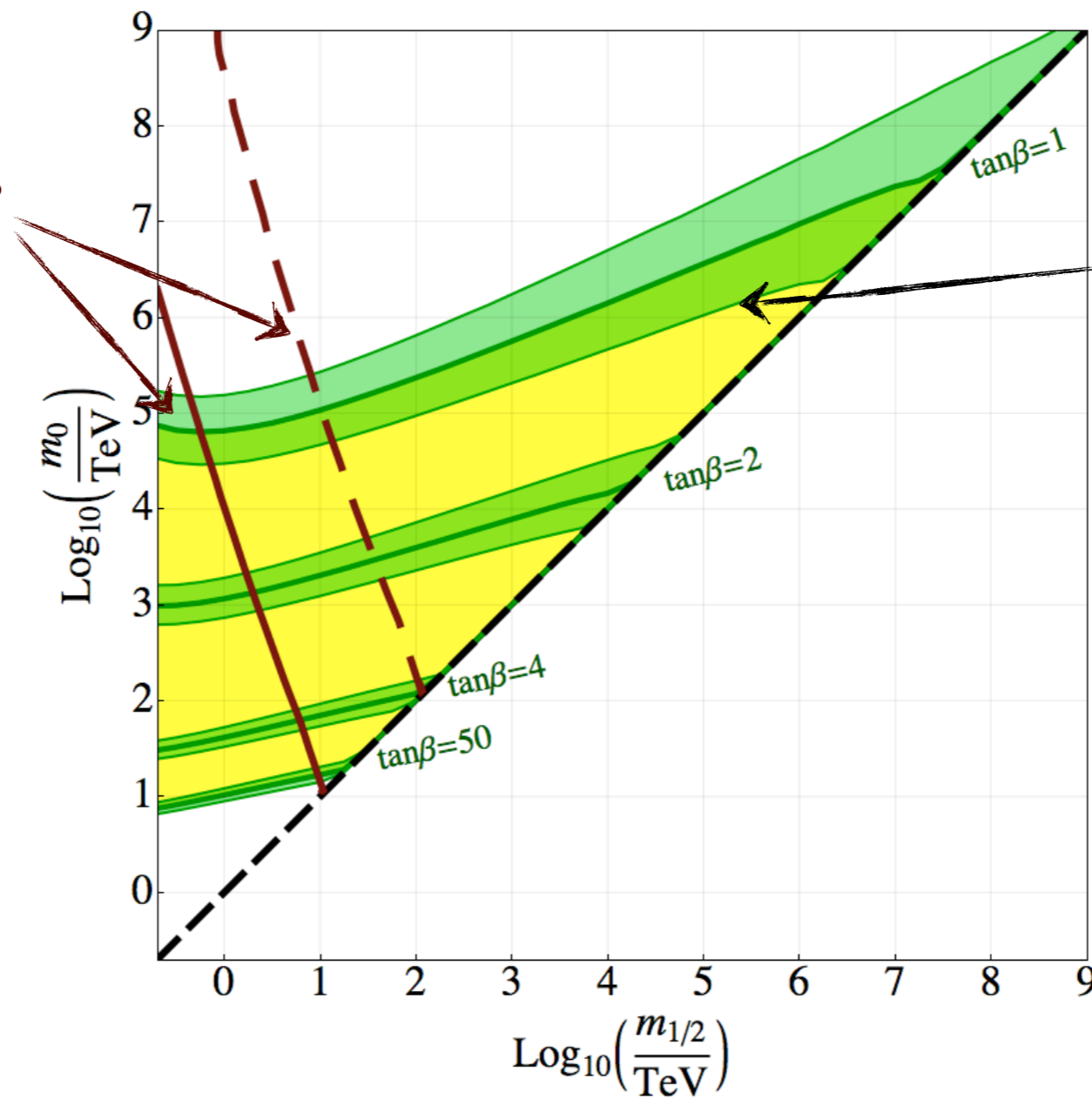


Parameter space
for 125 GeV Higgs

w/ Arvanitaki, Craig, Villadoro

The 125 GeV Higgs and Unification in Mini-Split

1σ and 2σ contours
for unification

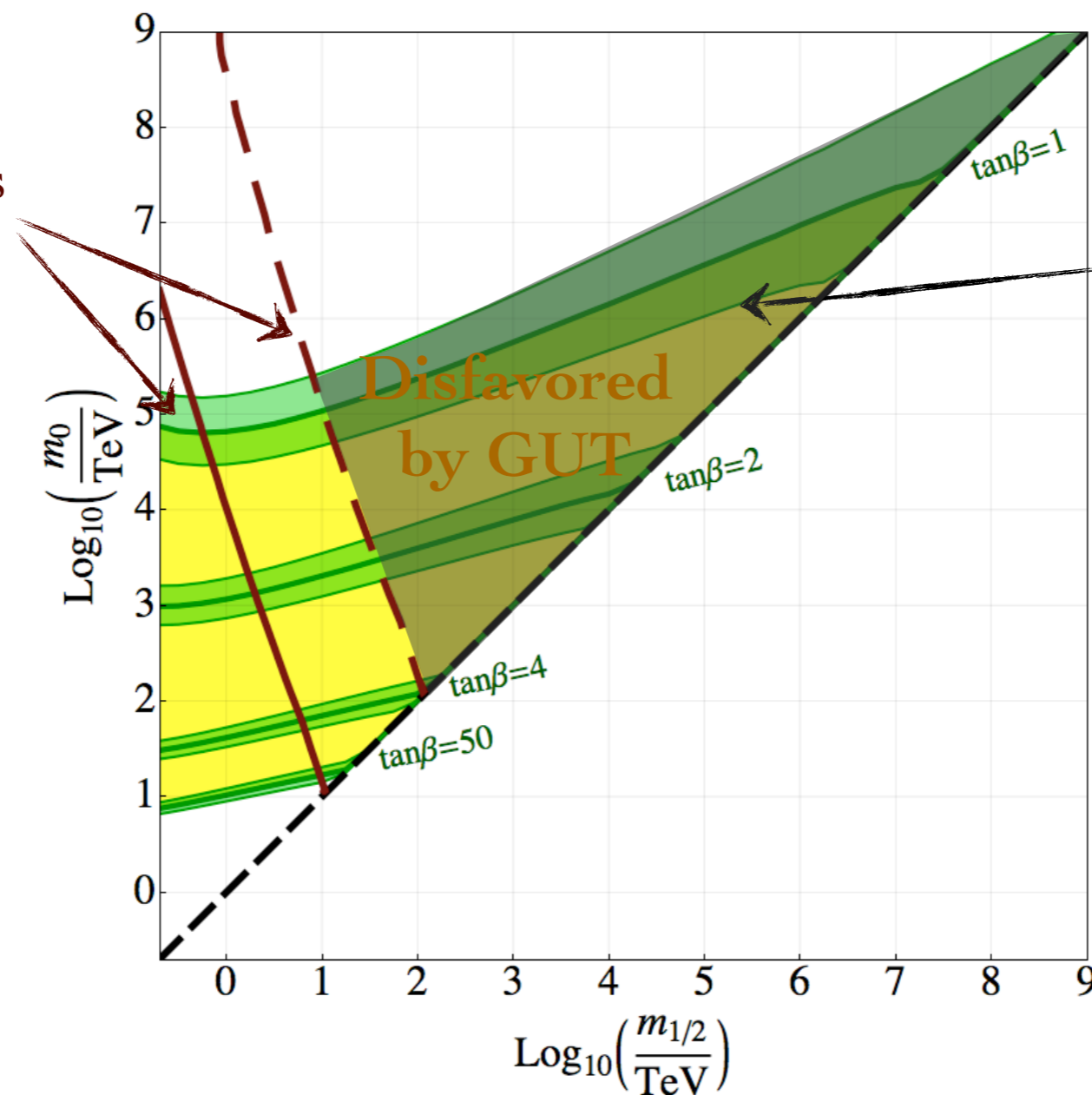


Parameter space
for 125 GeV Higgs

w/ Arvanitaki, Craig, Villadoro

The 125 GeV Higgs and Unification in Mini-Split

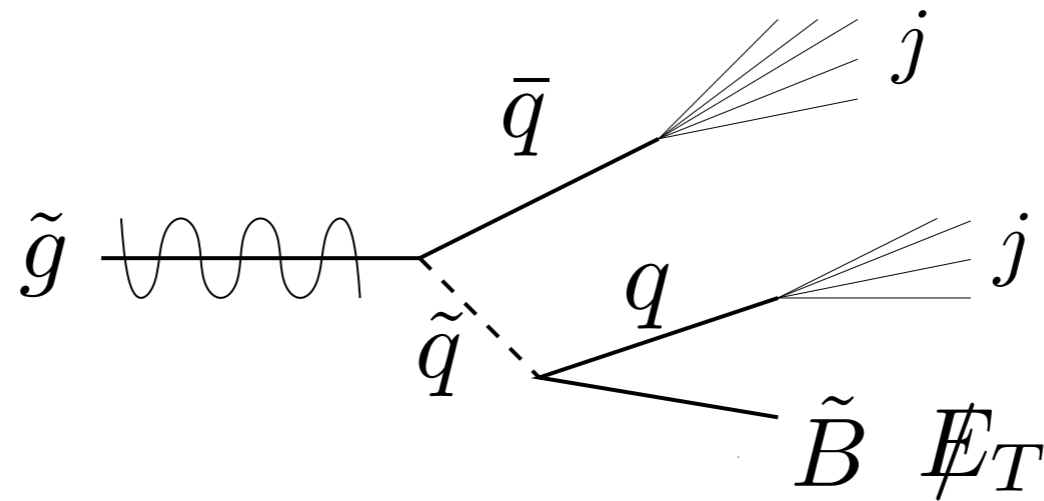
1σ and 2σ contours
for unification



- Higgsinos have to be lighter than 100 TeV for Unification
- Scalars below 100 TeV when $\tan\beta > \text{few}$
- Unification: Further motivates 100 TeV collider

Long-lived Gluinos

Gluino decay through the heavy scalars



Signature:

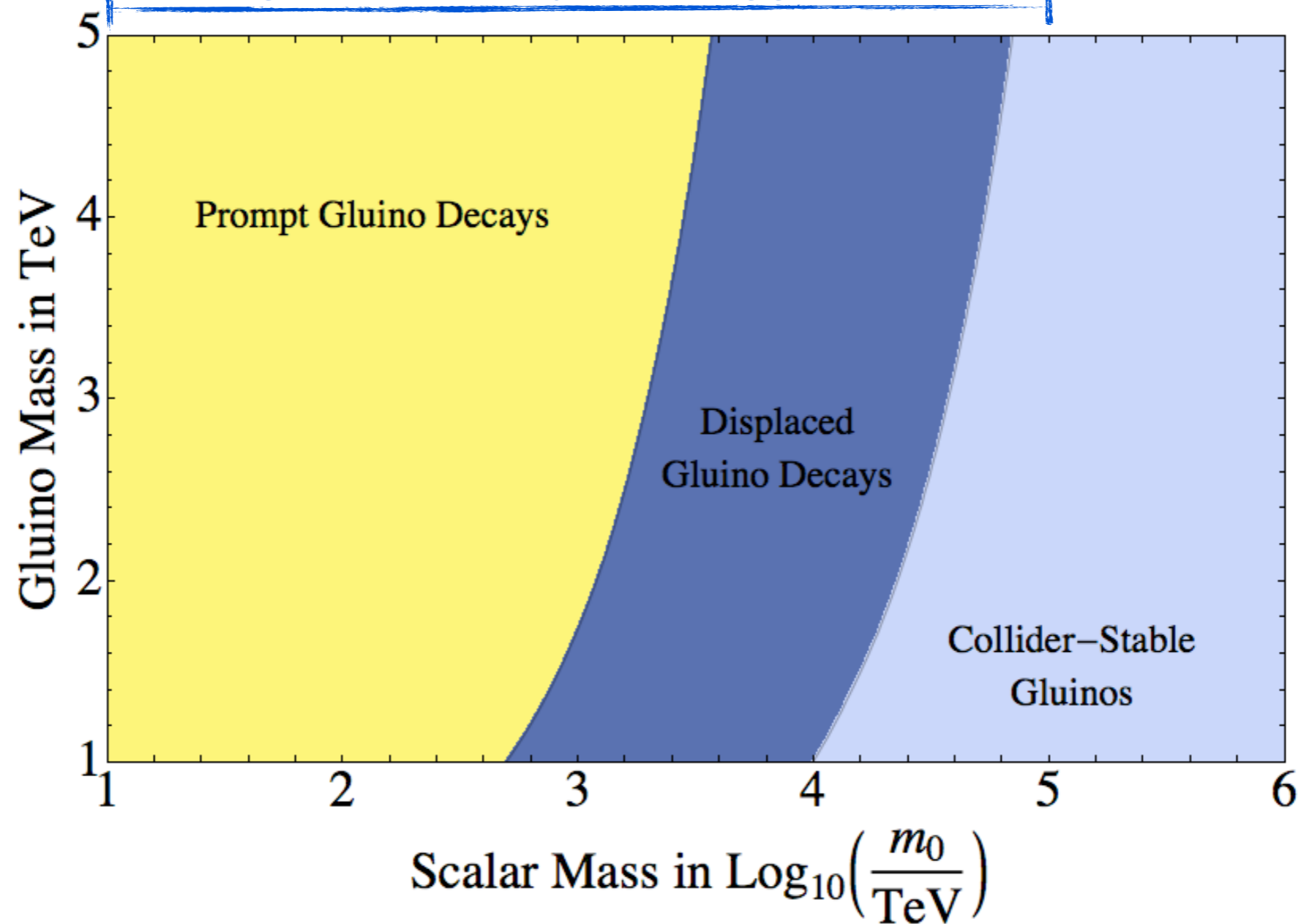
2 jets and missing energy

Lifetime:

$$c\tau_{\tilde{g}} \simeq 3 \times 10^{-2} \text{ m} \left(\frac{1 \text{ TeV}}{m_{\tilde{g}}} \right)^5 \left(\frac{M_{\text{Susy}}}{10^4 \text{ TeV}} \right)^4$$

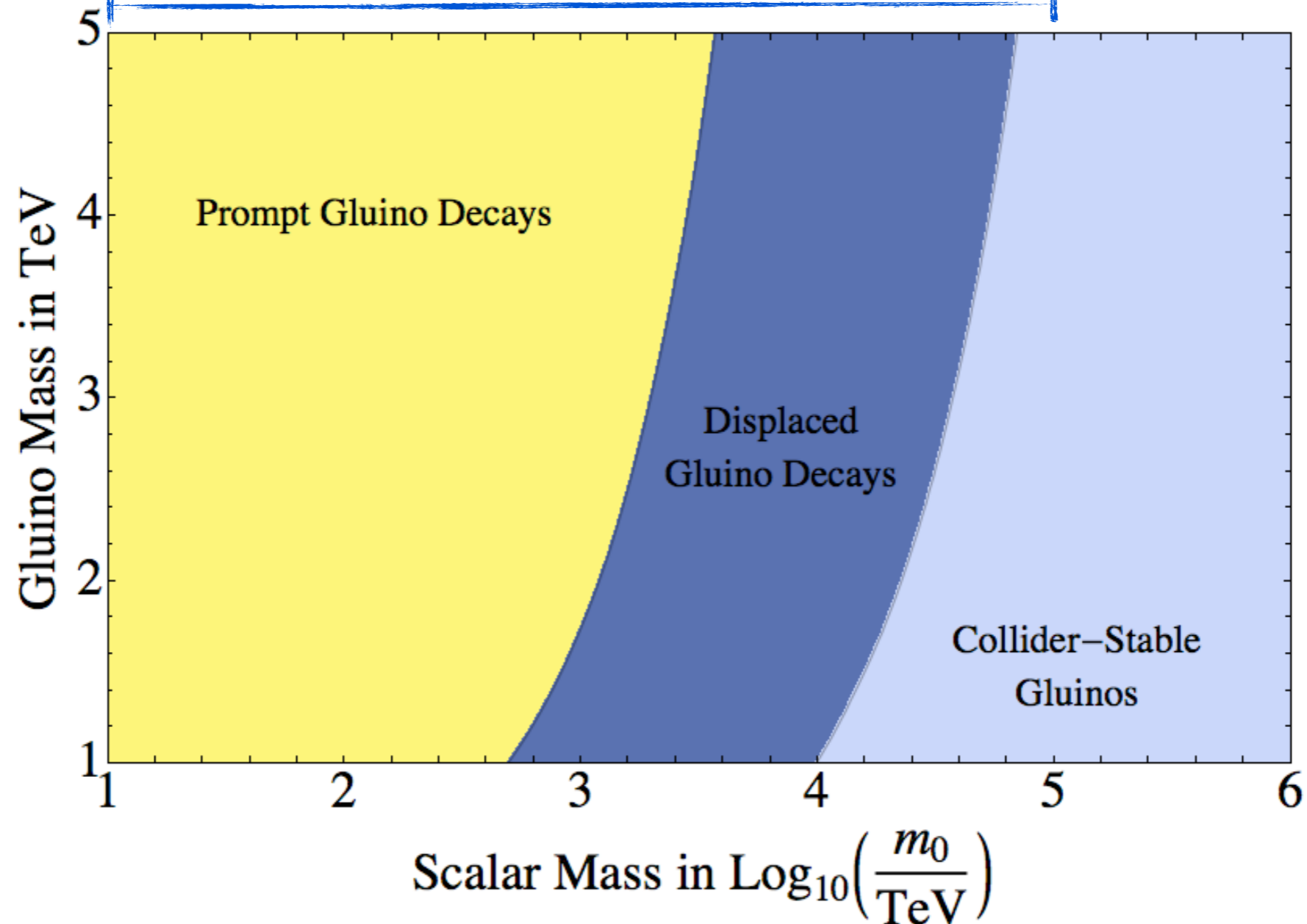
Long-lived Gluinos at the LHC

Range Favored by the Higgs Mass



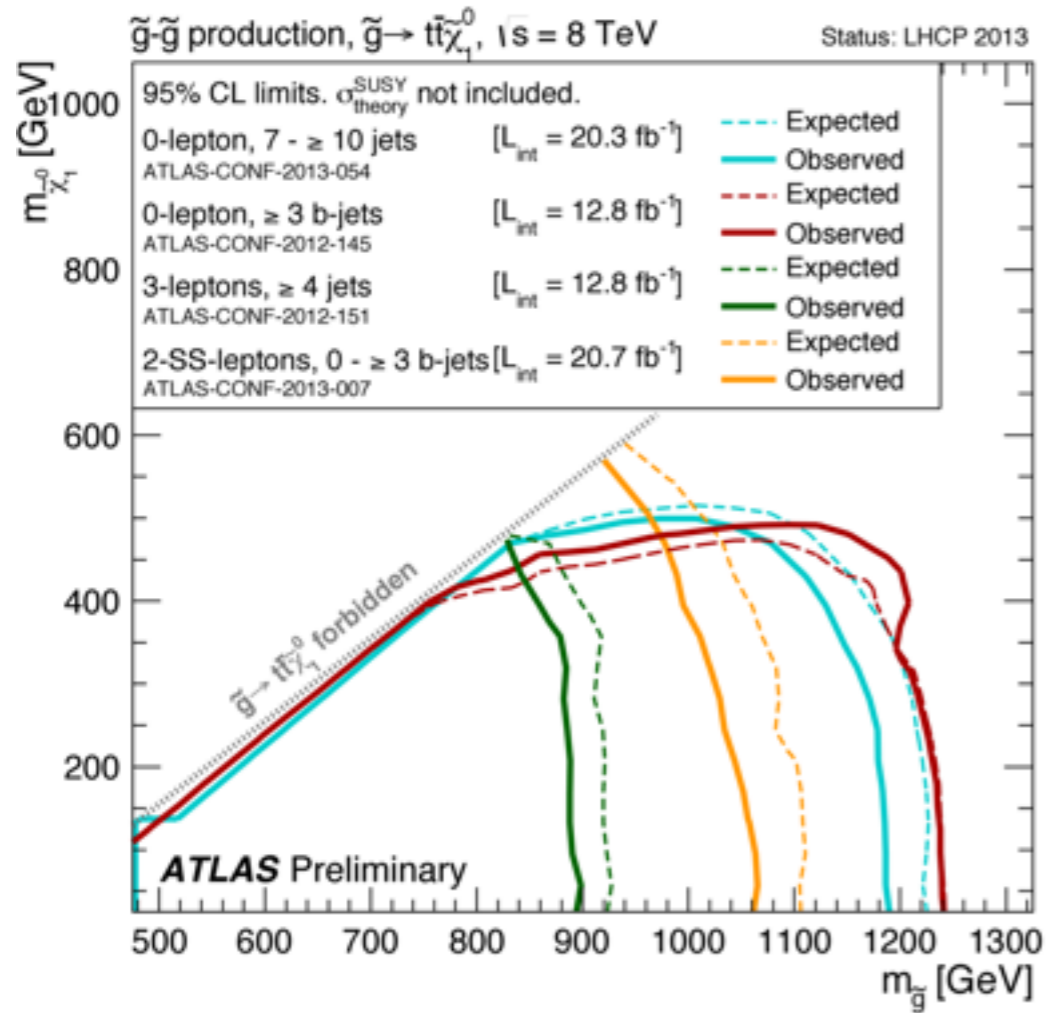
Long-lived Gluinos at the LHC

Range Favored by the Higgs Mass

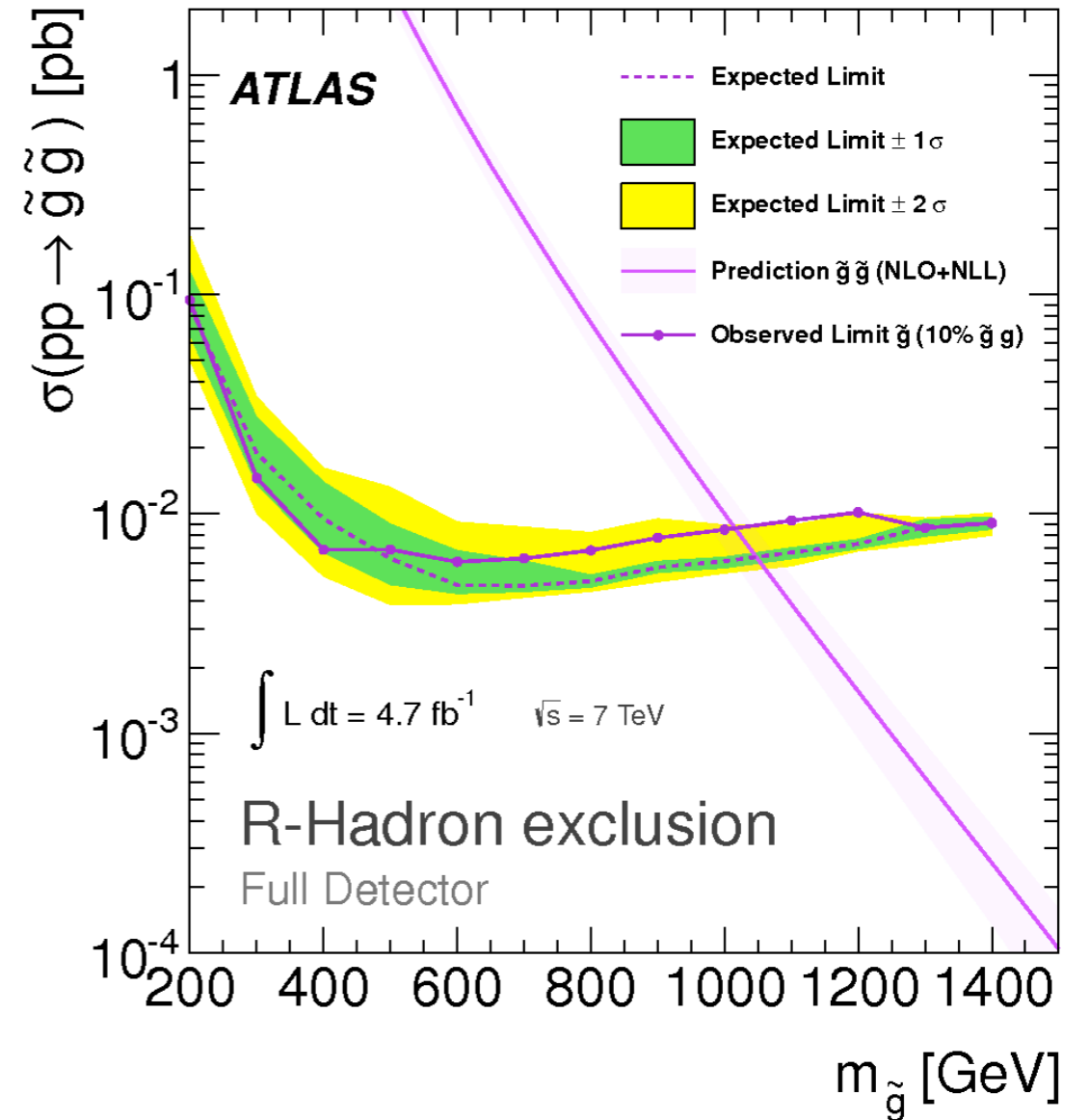


Stops as the lightest scalar sparticle:
Tops and bottoms in the final state of the decay

Gluino Bounds from the LHC



For prompt or slightly displaced gluinos



For collider "stable" gluinos

$M_{\text{gluino}} > 1 \text{ TeV}$ for split gluino

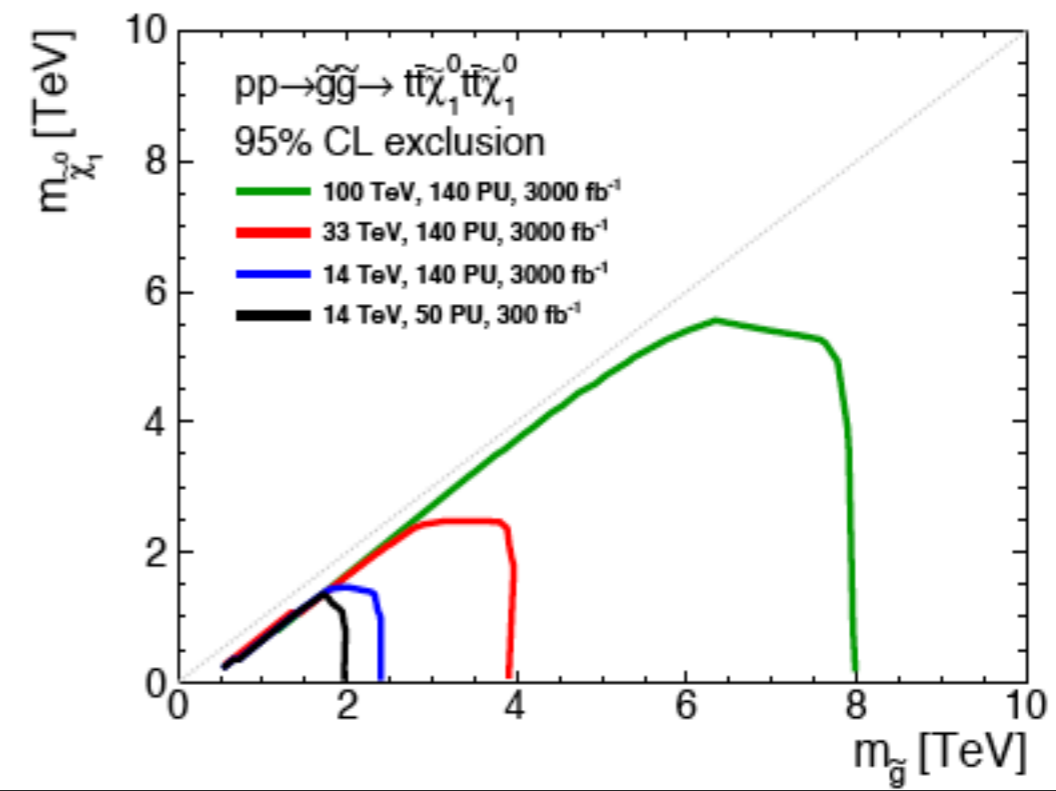
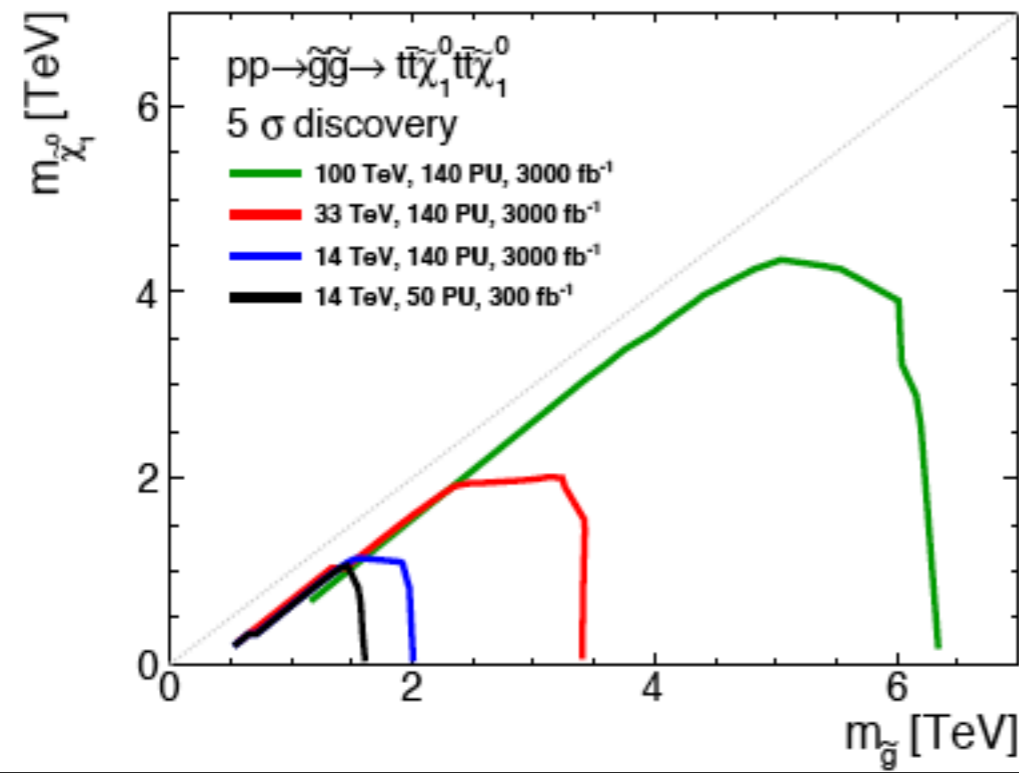
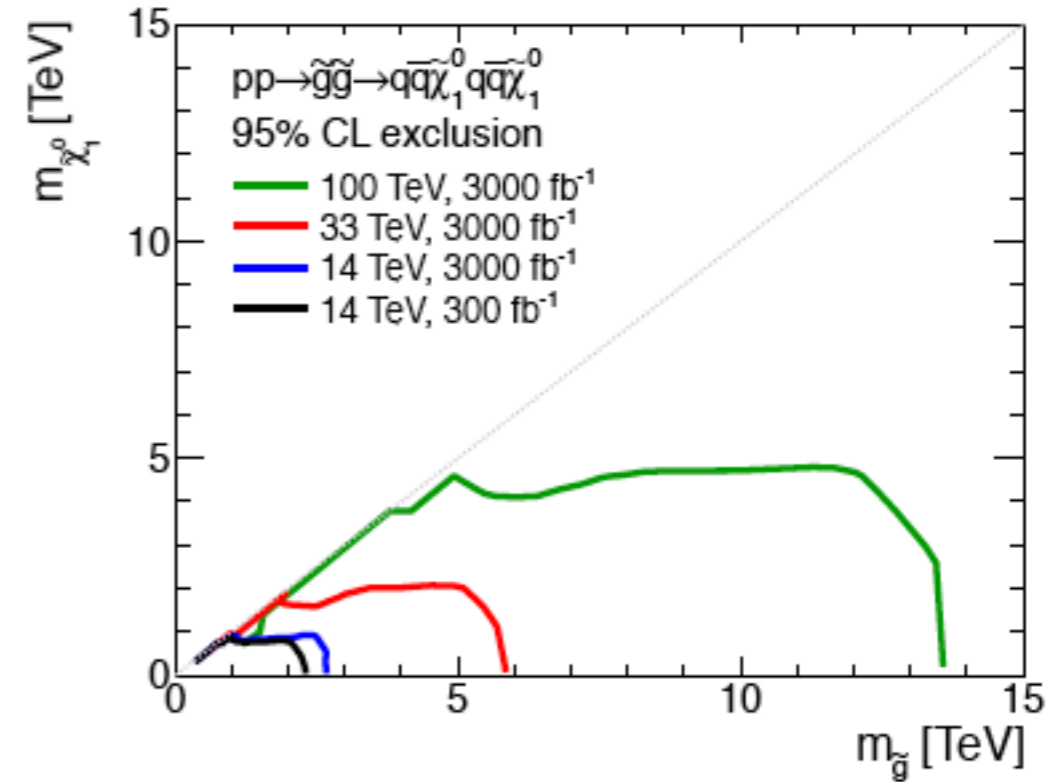
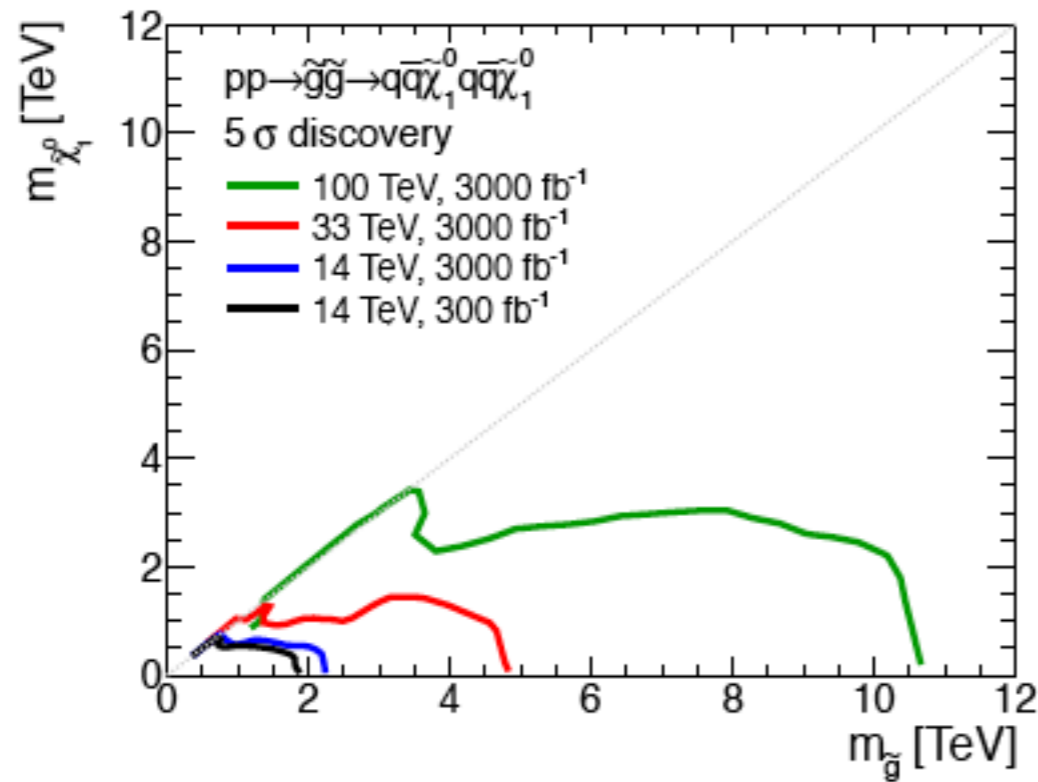
Small window for 10 cm - 1 m lifetimes?

Glauino Reach with 100 TeV

Cohen et. al. (2013)

Discovery

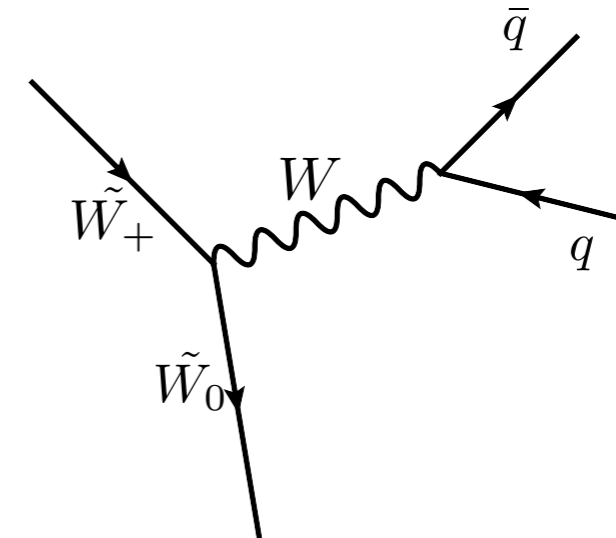
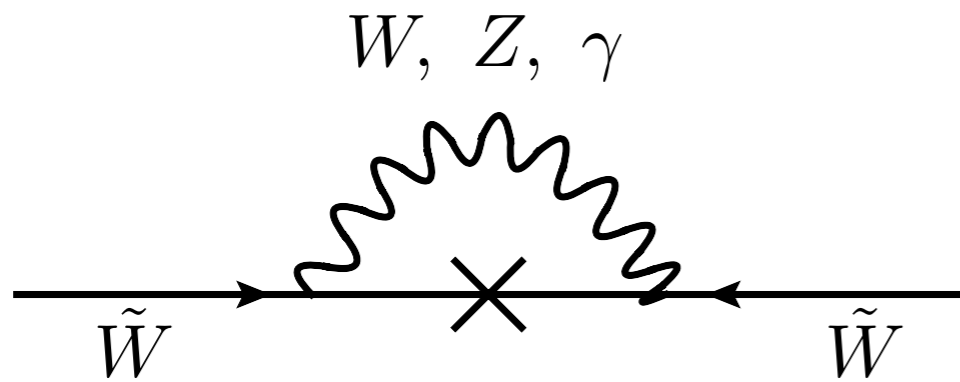
Exclusion



Split Signatures beyond the Gluino: Electroweakinos and Higgsinos

- Light Winos
 - Minimal Dark Matter Candidate $M_{\text{DM}} \sim 2.5 \text{ TeV}$
 - Displaced Wino decays
- Light Higgsinos
 - Minimal Dark Matter Candidate $M_{\text{DM}} \sim 1 \text{ TeV}$
 - Displaced Higgsino decays
- Both Winos and Higgsinos light
 - Electroweakino and Higgsino Yukawa Coupling Unification

Wino LSP with Heavy Higgsinos

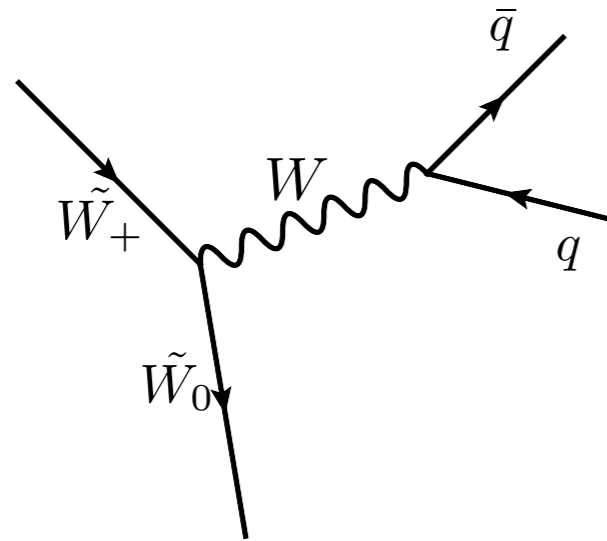


$$\Delta m \sim \frac{\alpha}{4\pi} M_Z \approx 155 - 175 \text{ MeV}$$

$$\Gamma \sim \frac{G_F^2}{4\pi} f_\pi^2 \Delta m^3$$

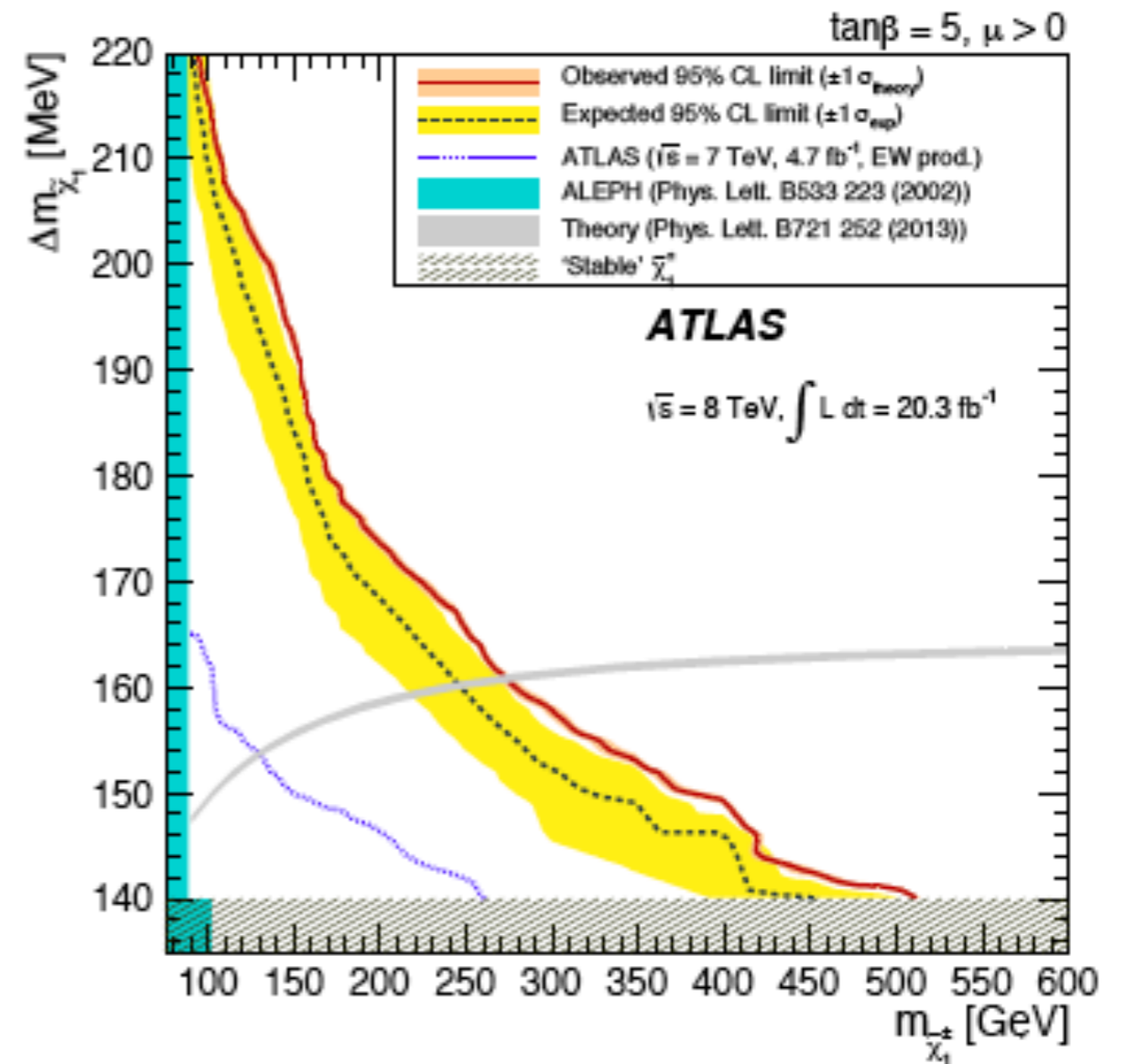
- Charged wino heavier than Neutral Wino
- cm size tracks with soft pions

Wino LSP with Heavy Higgsinos

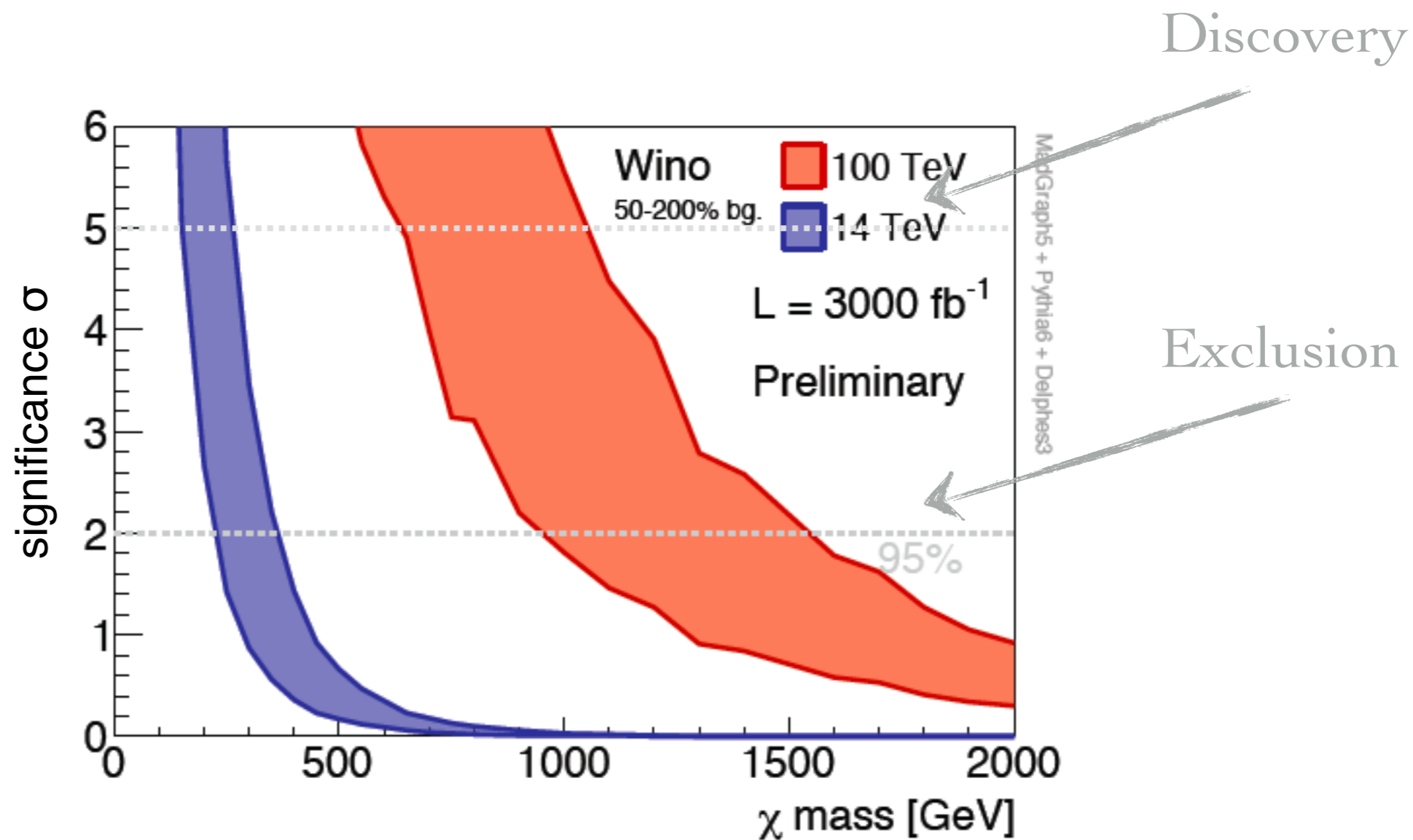


$$\Delta m \approx 155 - 175 \text{ MeV}$$

- ISR mono-jets
- Charged track length of order cm



Wino reach at 100 TeV

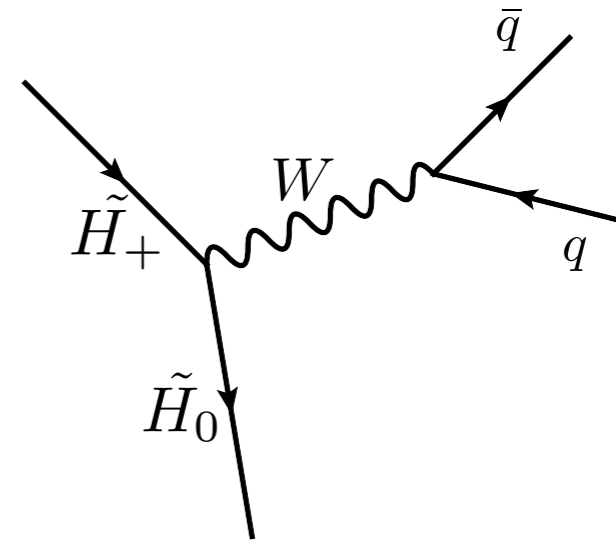


Talk given by Lian-Tao Wang

Factor of few gain compared to the LHC

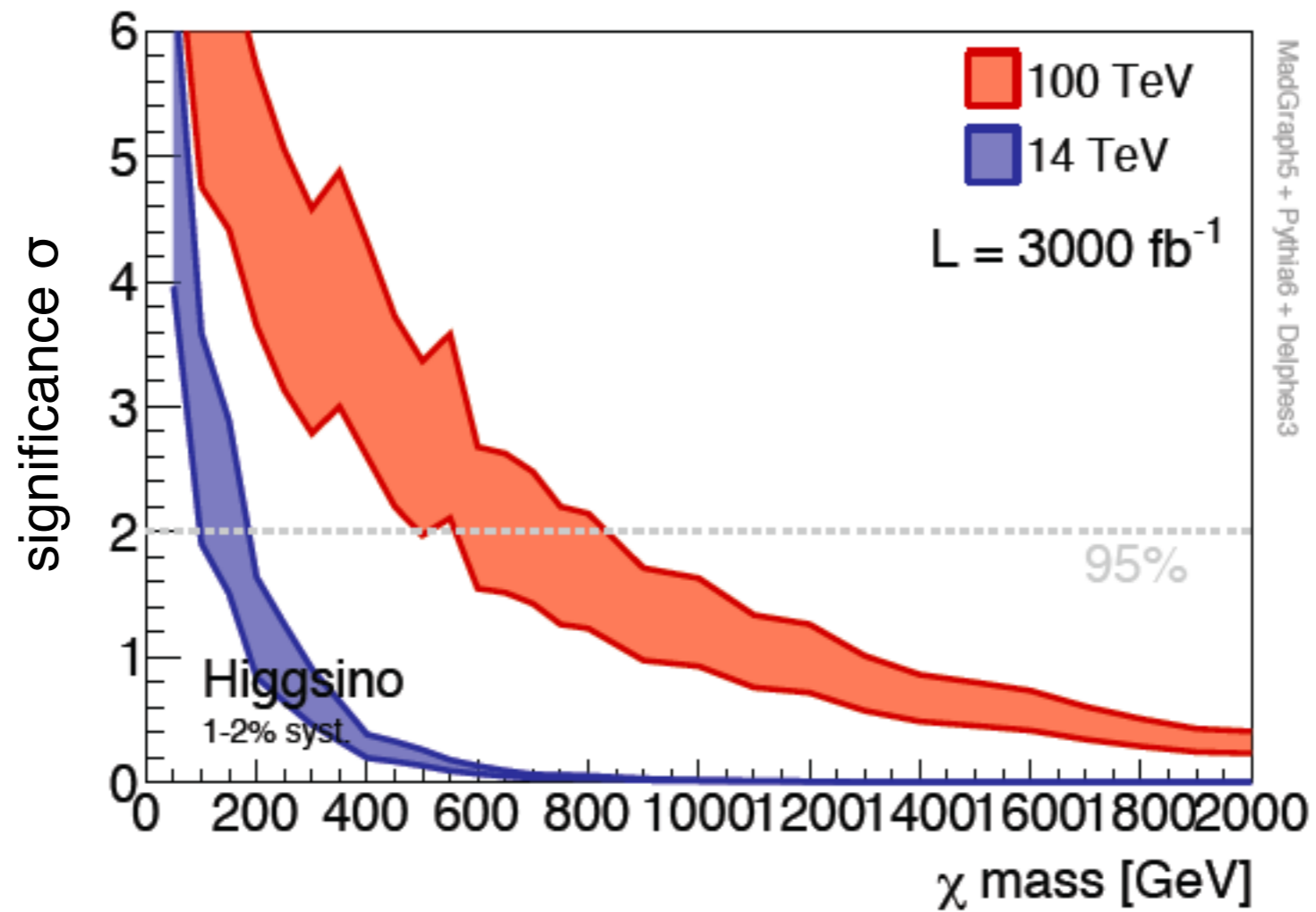
Higgsino LSP: The Minimal Model for Unification

- Only light Higgsinos in the Spectrum
- Mass splitting ~ 355 MeV
- Soft pions with sub-cm charged tracks
- No LHC bounds
 - No working search strategy yet



Higgsino reach at 100 TeV

Monojet Search

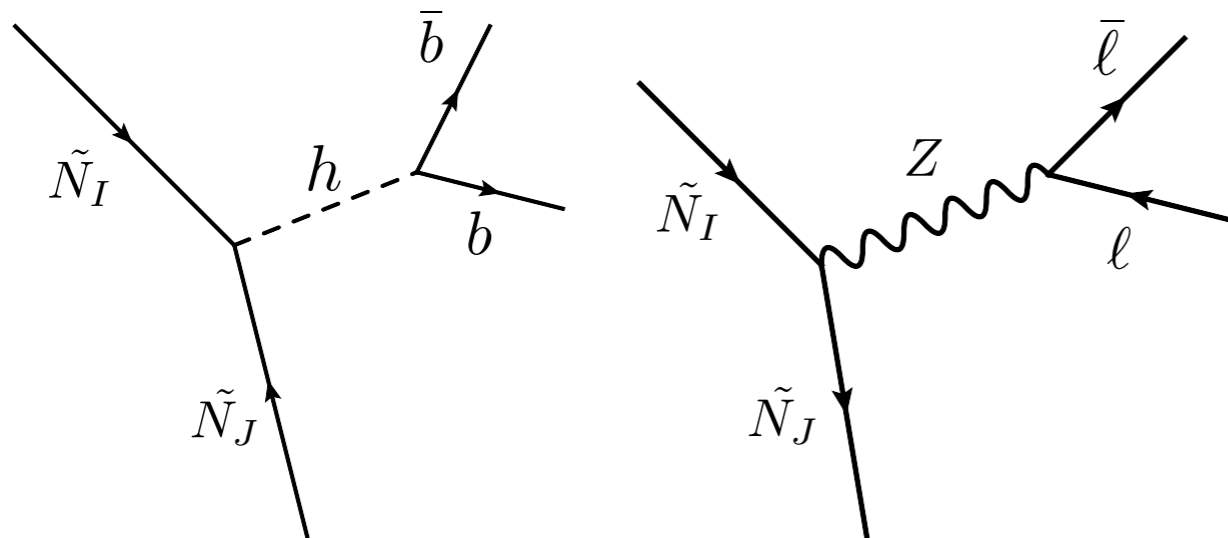


Talk given by Lian-Tao Wang

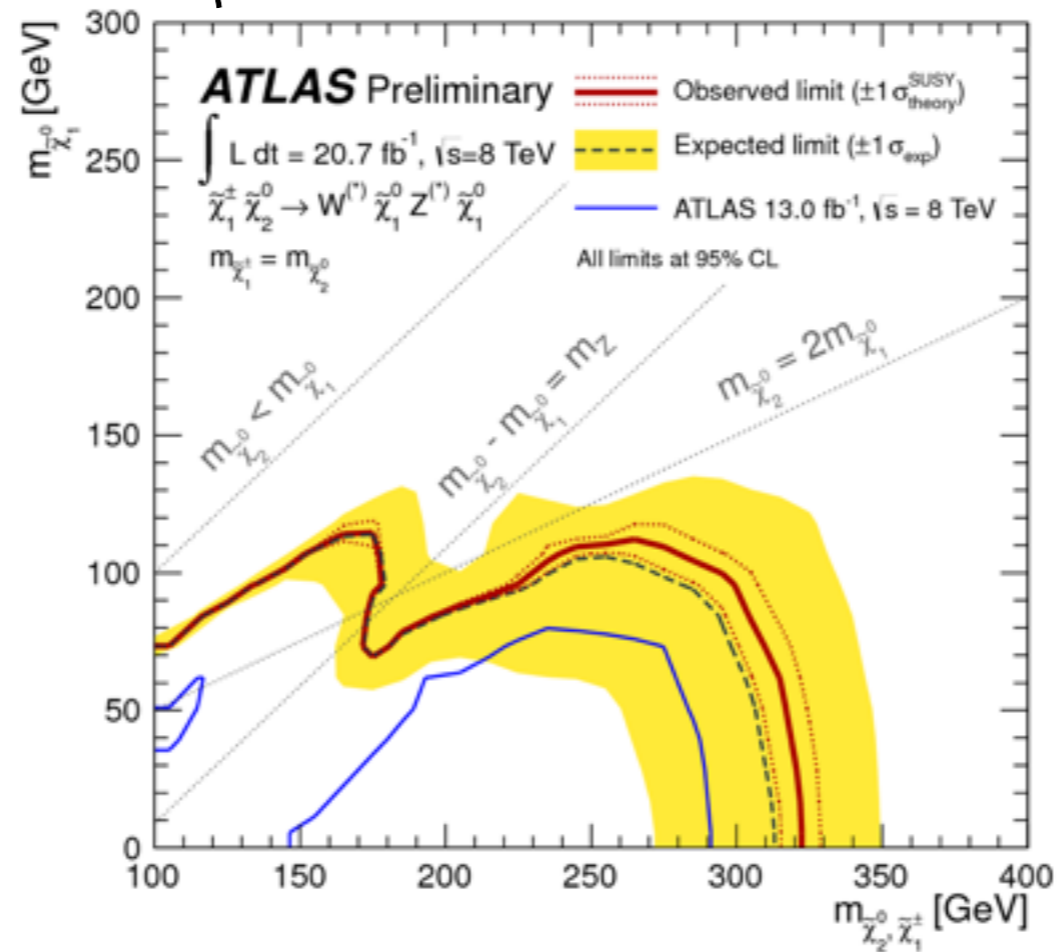
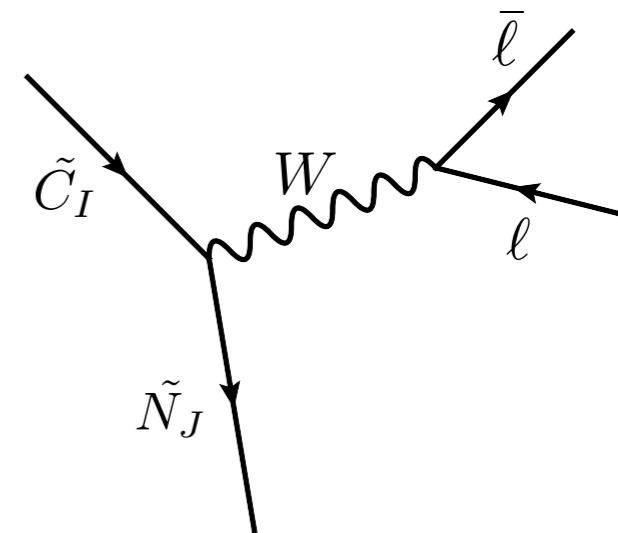
Factor of few gain compared to the LHC

Electroweakinos and Higgsinos at the LHC

Neutralino decays

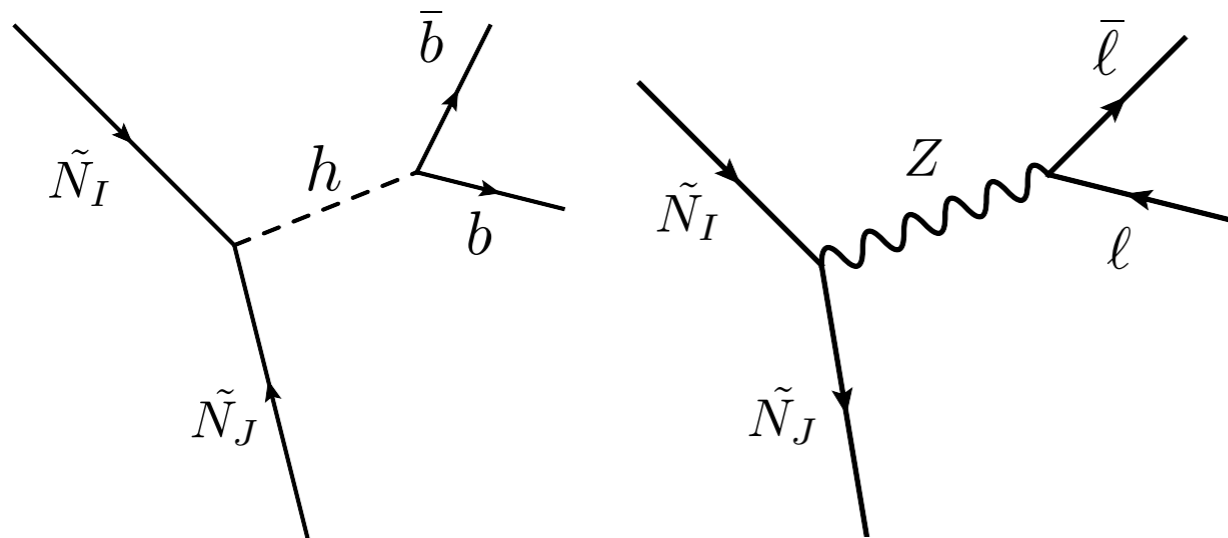


Chargino decays

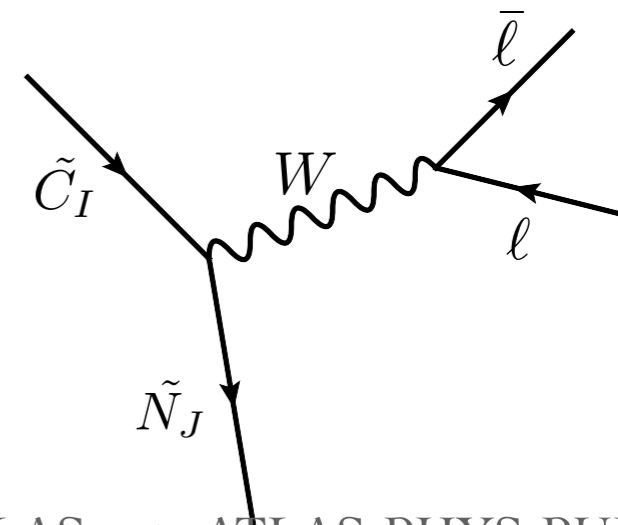


Electroweakinos and Higgsinos at the LHC

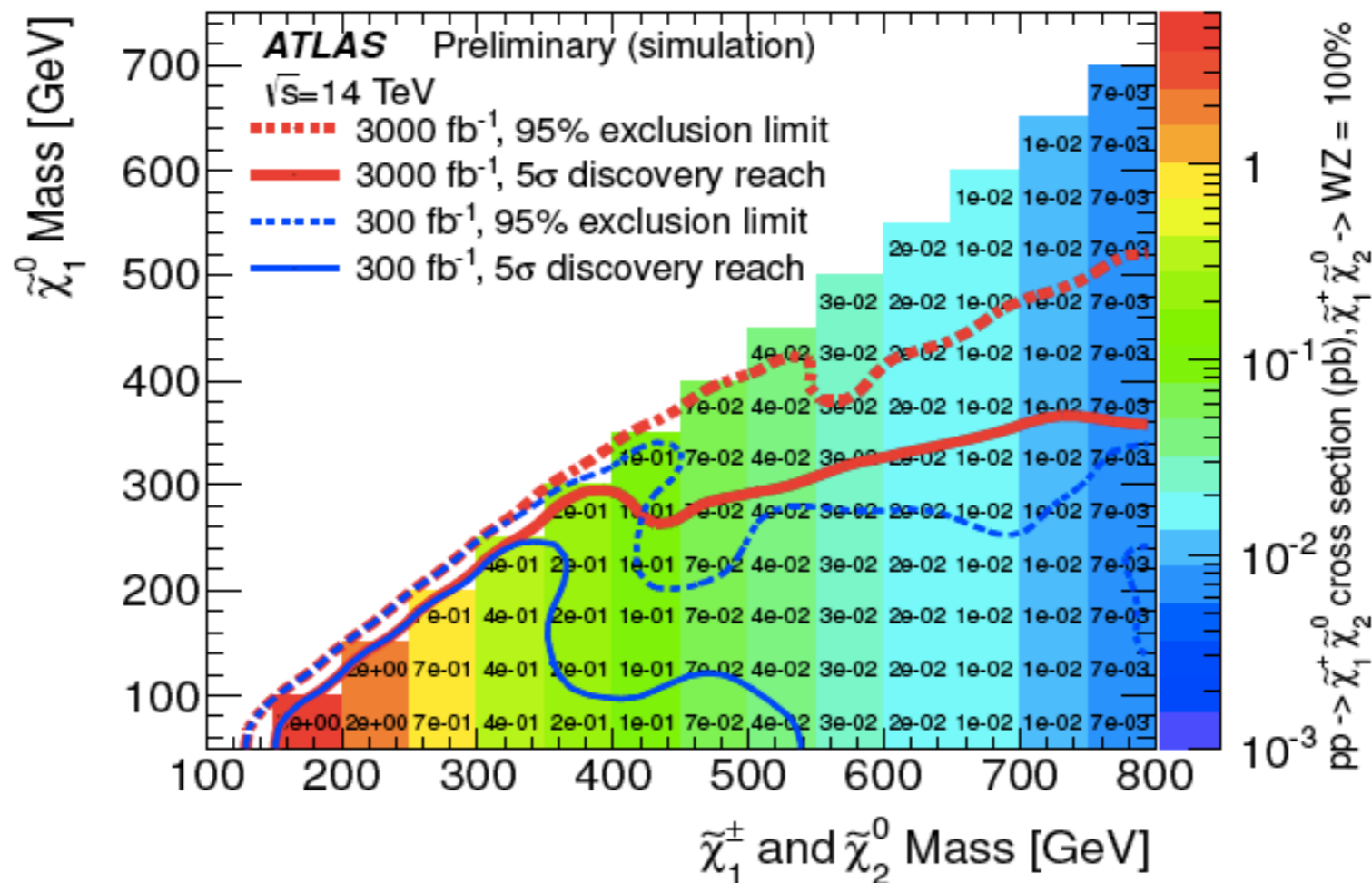
Neutralino decays



Chargino decays

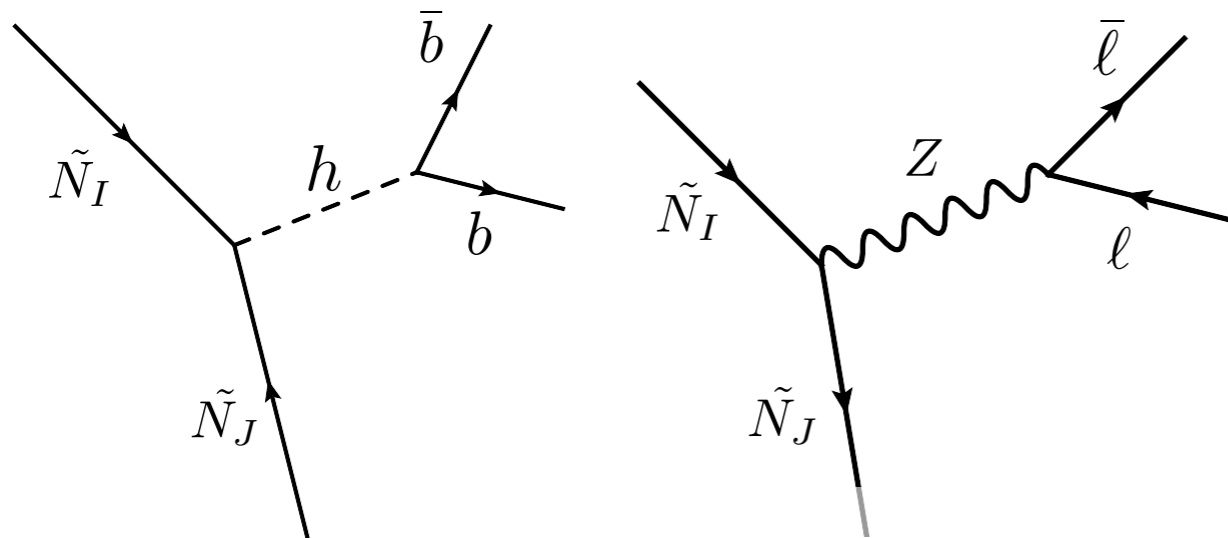


Taken from ATLAS note ATLAS-PHYS-PUB-2013-002

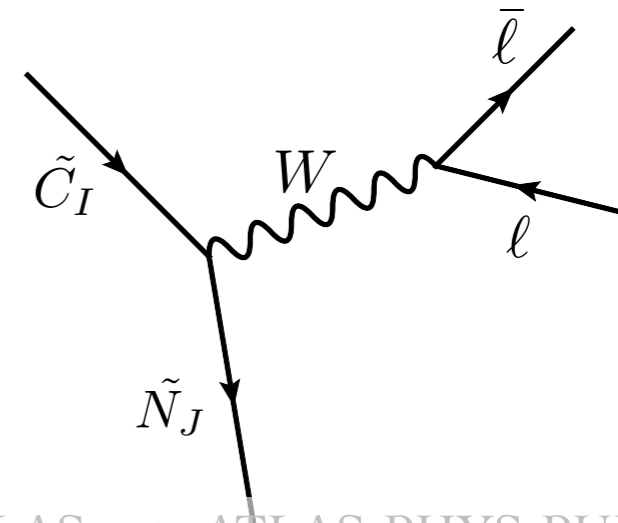


Electroweakinos and Higgsinos at the LHC

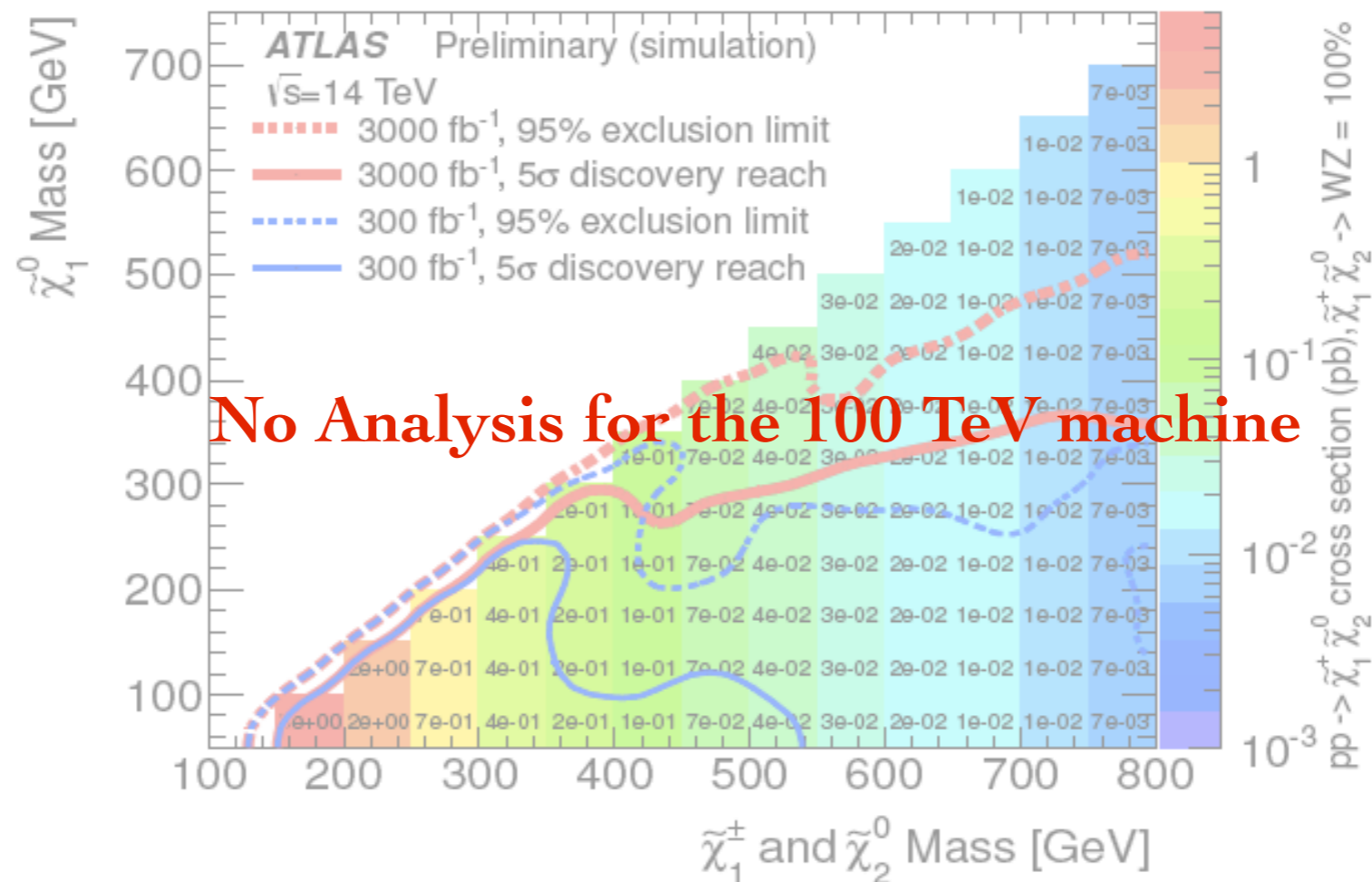
Neutralino decays



Chargino decays

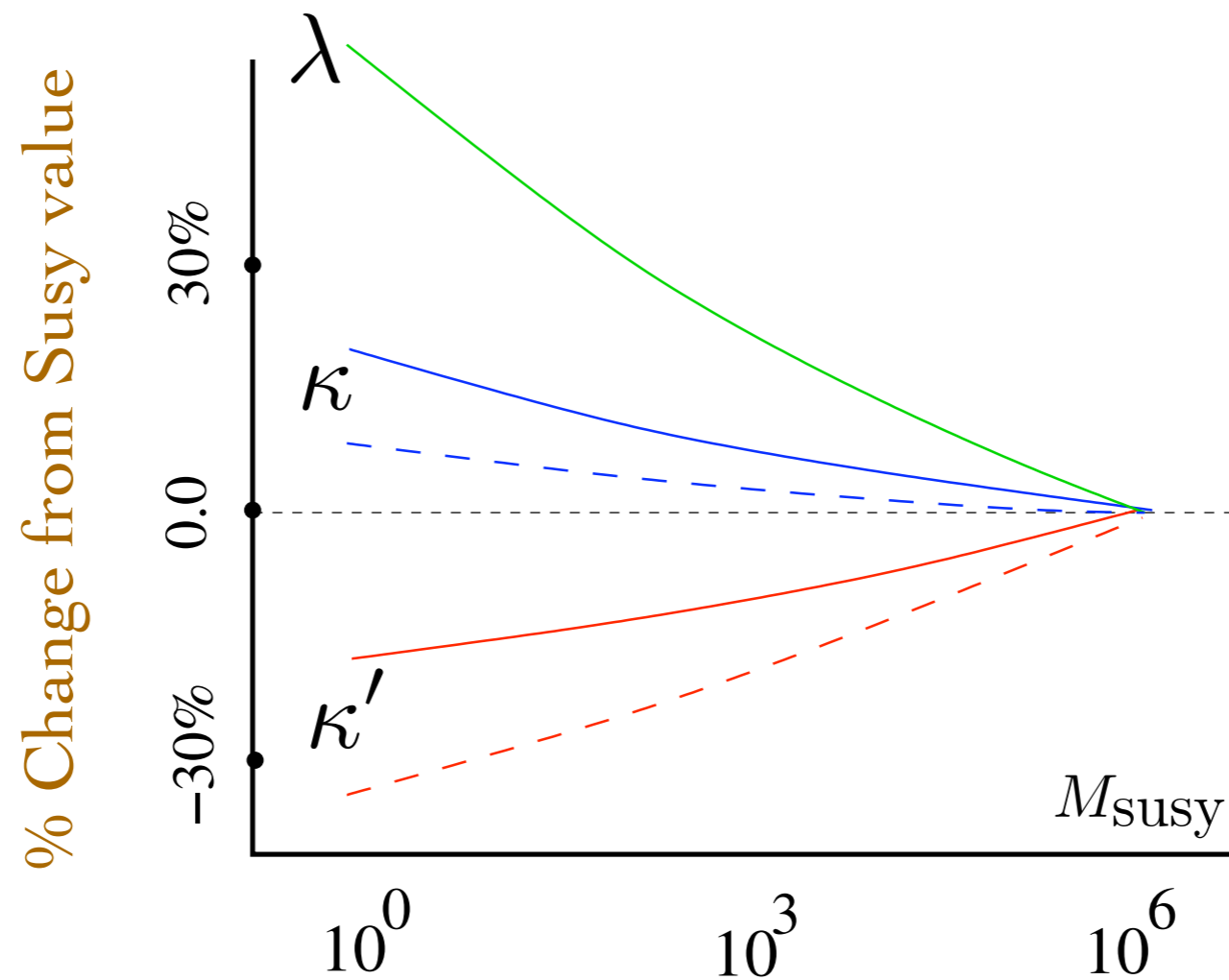


Taken from ATLAS note ATLAS-PHYS-PUB-2013-002



Electroweakinos and Higgsinos at the LHC

Gaugino and Higgsino Yukawa Coupling Unification

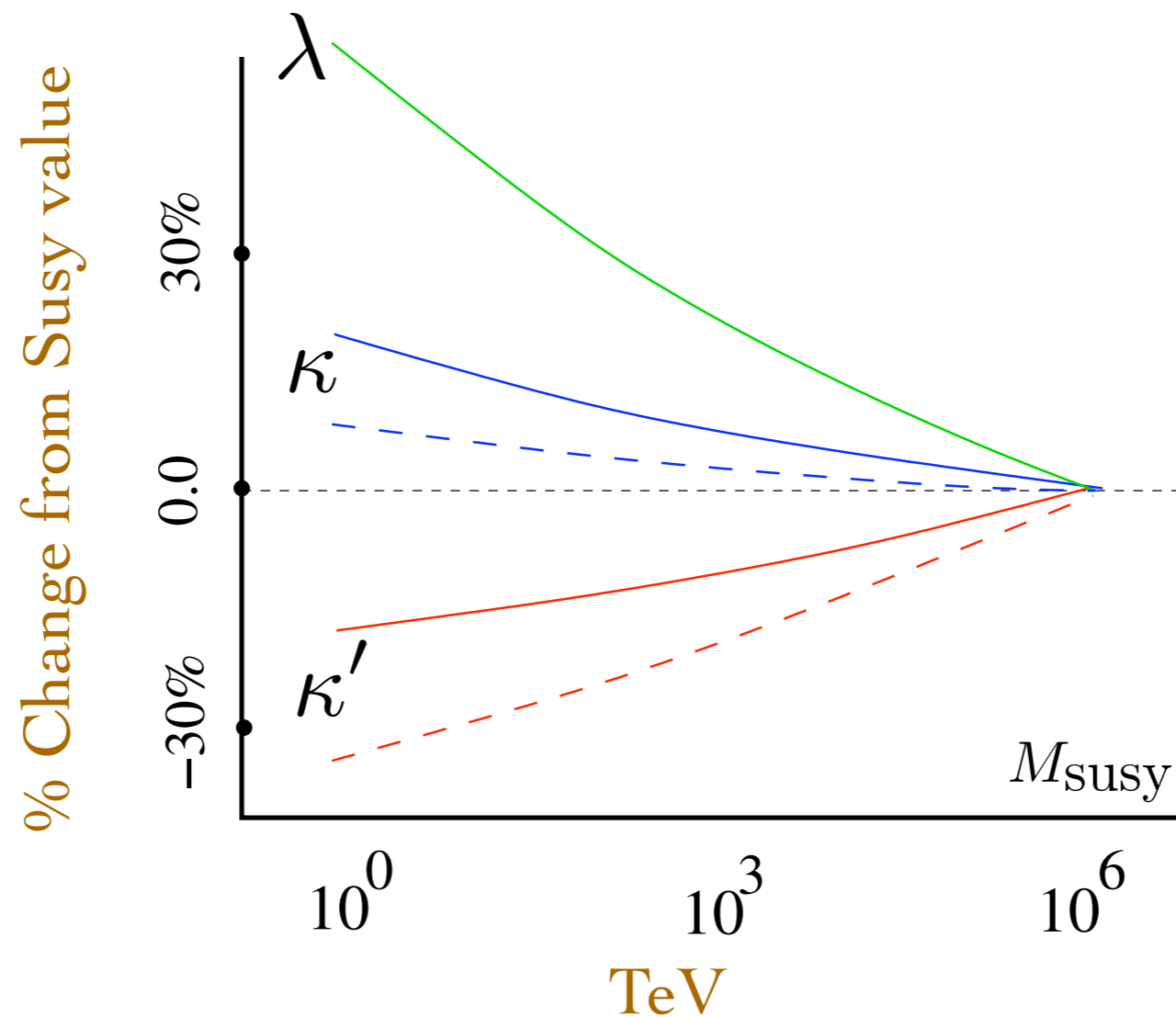


$$\kappa_u H \widetilde{H}_u \widetilde{W} + \kappa_d H^\dagger \widetilde{H}_d \widetilde{W} \quad \kappa'_u H \widetilde{H}_u \widetilde{B} + \kappa'_d H^\dagger \widetilde{H}_d \widetilde{B}$$

λ : Higgs Quartic

Electroweakinos and Higgsinos at the LHC

Gaugino and Higgsino Yukawa Coupling Unification



Combined with gluino lifetime measurement establishes supersymmetric origin of new particles

Mini-Split Phenomenology

- Displaced Gluinos
- Displaced Winos and Higgsinos
- Yukawa Coupling Unification

Model Ranking

Model	Grade
MSSM	D-
NMSSM	D
Natural SUSY	C
R-parity breaking	C
Colorless Top Partners	C
Split SUSY	B

The Mystery of Naturalness



Sherlock: '[I draw your attention] to the curious incident of the dog in the night-time.'

Inspector: 'The dog did nothing in the night-time.'

Sherlock: 'That was the curious incident.'

Sherlock Holmes

-Silver Blaze

The Mystery of Naturalness



Sherlock: '[I draw your attention] to the curious incident of the dog in the night-time.'

Inspector: 'The dog did nothing in the night-time.'

Sherlock: 'That was the curious incident.'

Sherlock Holmes

-Silver Blaze

"Data! Data! Data!" he cried impatiently. "I can't make bricks without clay."

Sherlock Holmes

-The Adventure of the Copper Beeches