

First CFHEP Symposium on Circular Collider Physics

Standard Model Tests

Qing-Hong Cao

Peking University

On behalf of the SM Working Group

Chong Sheng Li, Zhao Li, Li Lin Yang

Some recent theoretical progress in Higgs boson and top quark physics at hadron colliders

arXiv: 1401.1101

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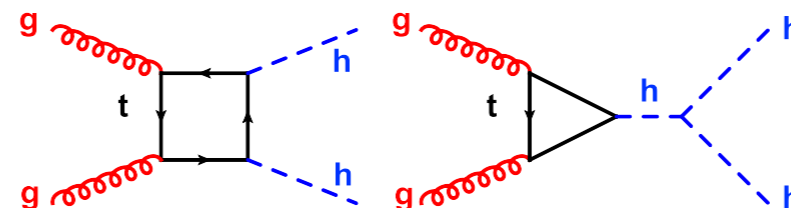
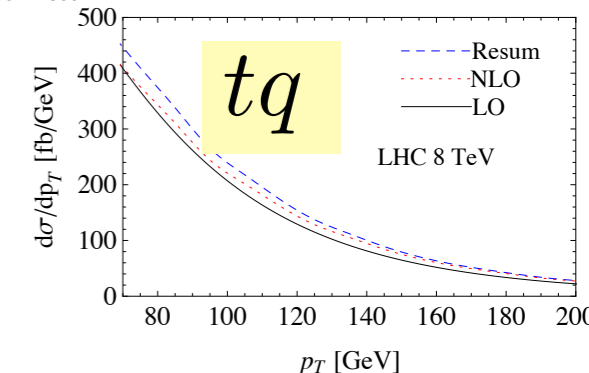
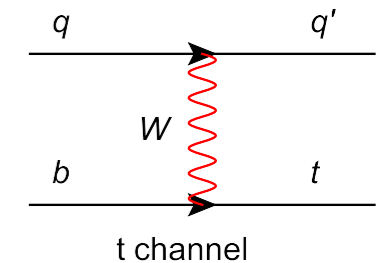
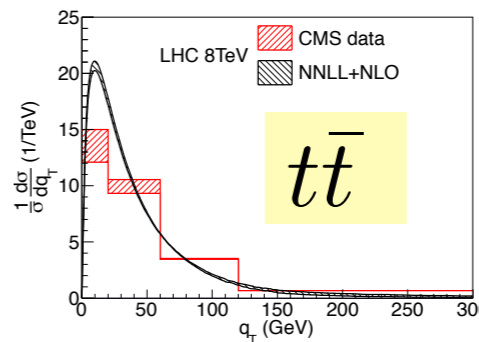
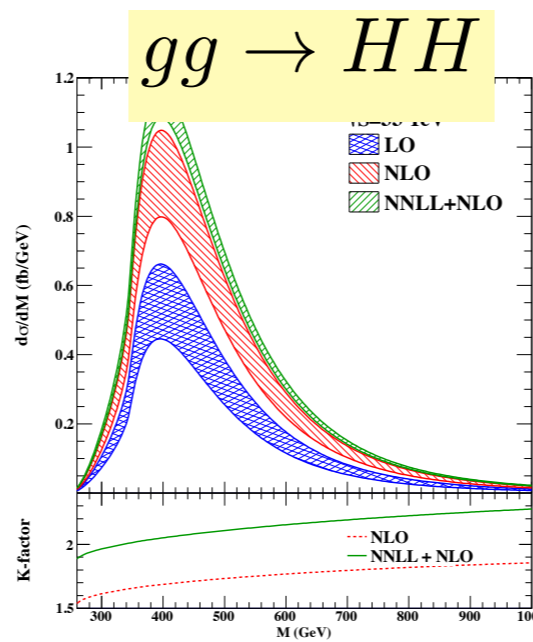
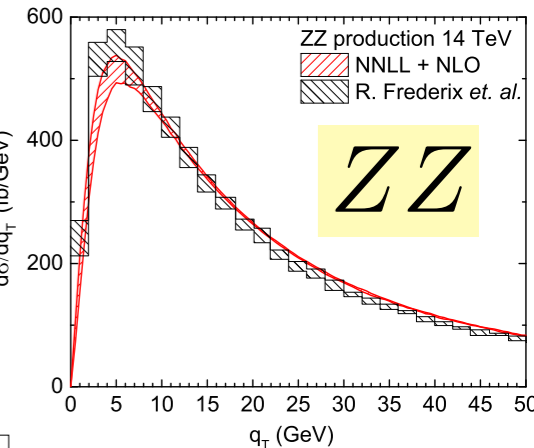
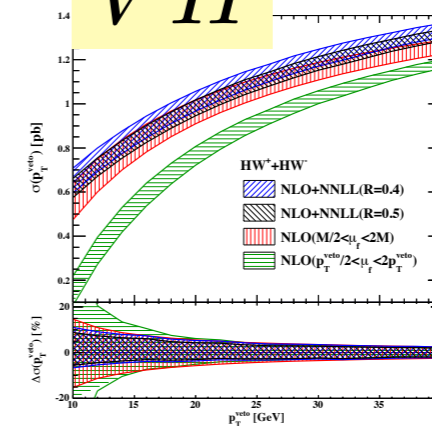
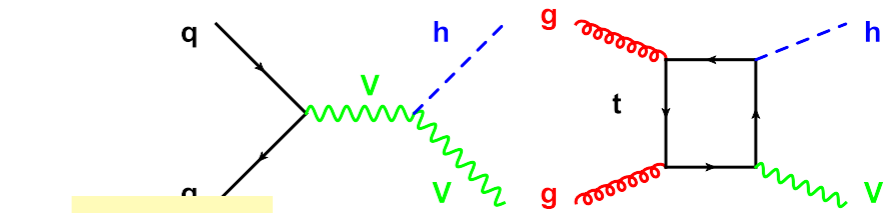
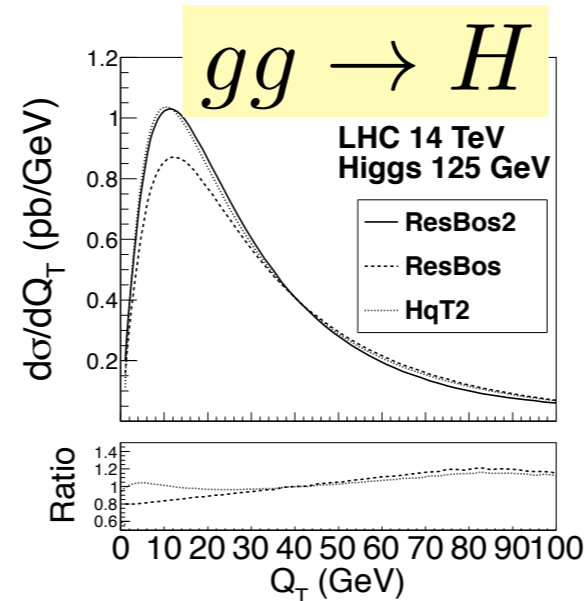
²*Center for High Energy Physics, Peking University, Beijing 100871, China*

(Dated: January 9, 2014)

In this review we briefly summarize some recent theoretical progress in Higgs boson and top quark physics, especially the fixed-order and resummation predictions in QCD at both the Tevatron and the LHC.

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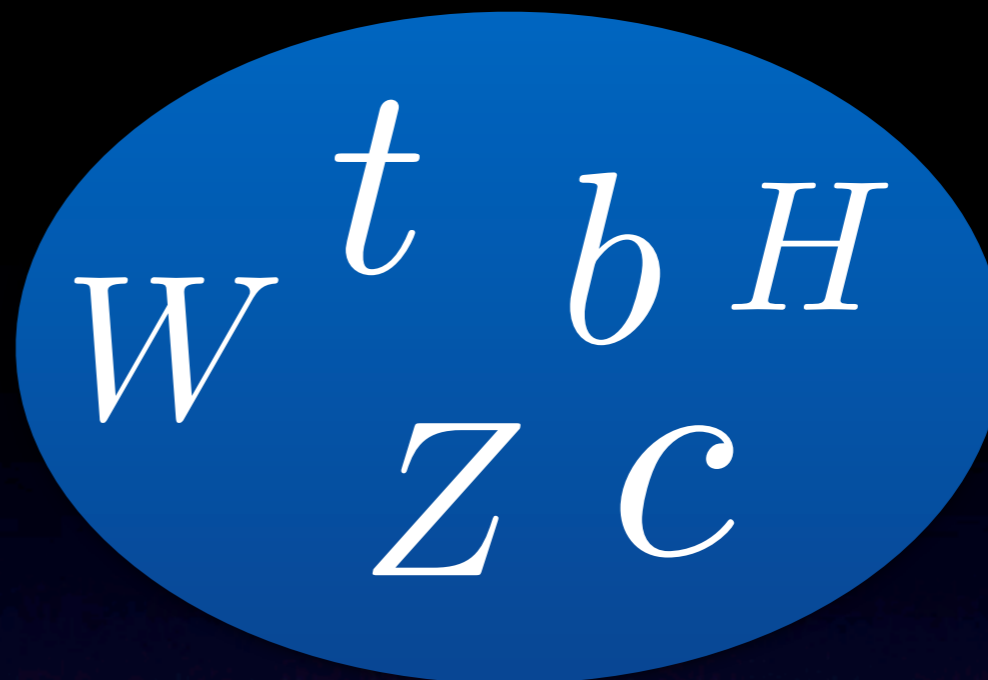
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ILC, TLEP, CEPC

Precision

Mass
Width
Spin
Coupling



Unknowns
of the SM ??

Heavy
Resonance

Energy Frontier

VHLC, SpC

SM Physics Precision

Precision measurements

Mass: W-boson, Top-quark, Higgs-boson

Width: W-boson, Top-quark, Higgs-boson

Spin: Higgs-boson, Top-quark spin correlation

CP: Higgs-boson

see Z. G. Si's talk

Indirect searches

Anomalous couplings and rare decay

(Effective field theory)

Untested Aspects of the SM

Higgs electroweak couplings

See Higgs Working-Group's report

Higgs boson self-coupling

Boosted object techniques

Triple-gauge-coupling / Quartic-gauge-coupling

Dim-6 and Dim-8 operators in linear realization

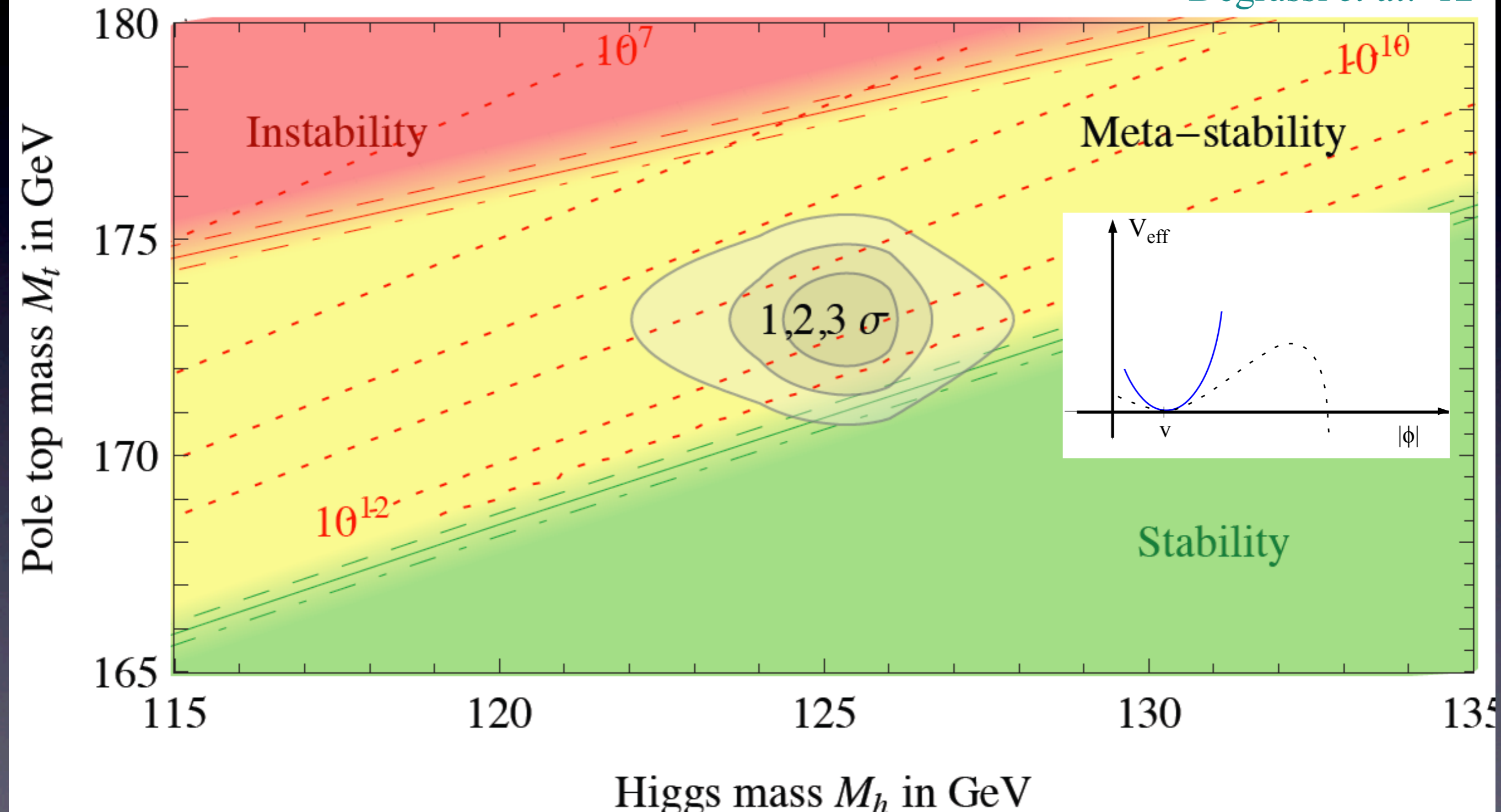
Weak interaction of the 3rd generation quarks

Fully understanding top- and bottom-quark
chirality structure of couplings, $V_{tb}=1?$...

Mass Precision

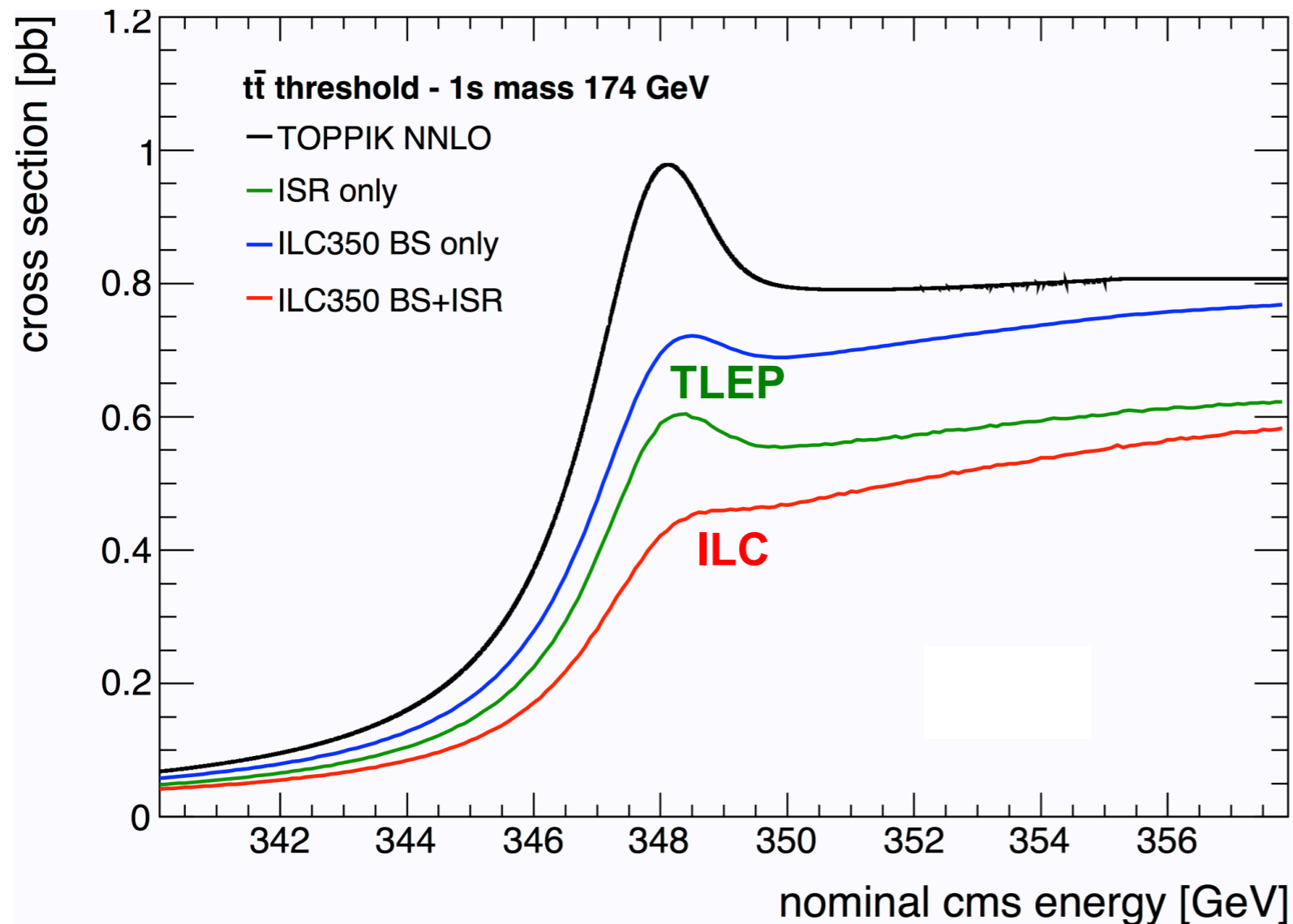
Top-Quark Mass vs Higgs-Boson Mass

Degrassi *et al.* '12



Top-Quark Mass at ILC and TLEP

Collider	TLEP 350	ILC 350
Total Integrated Luminosity (ab^{-1})	2.6	0.35
Number of $t\bar{t}$ pairs	1,000,000	100,000



$$m_t = 174 \text{ GeV}$$

Peak $\sim 346 \text{ GeV}$

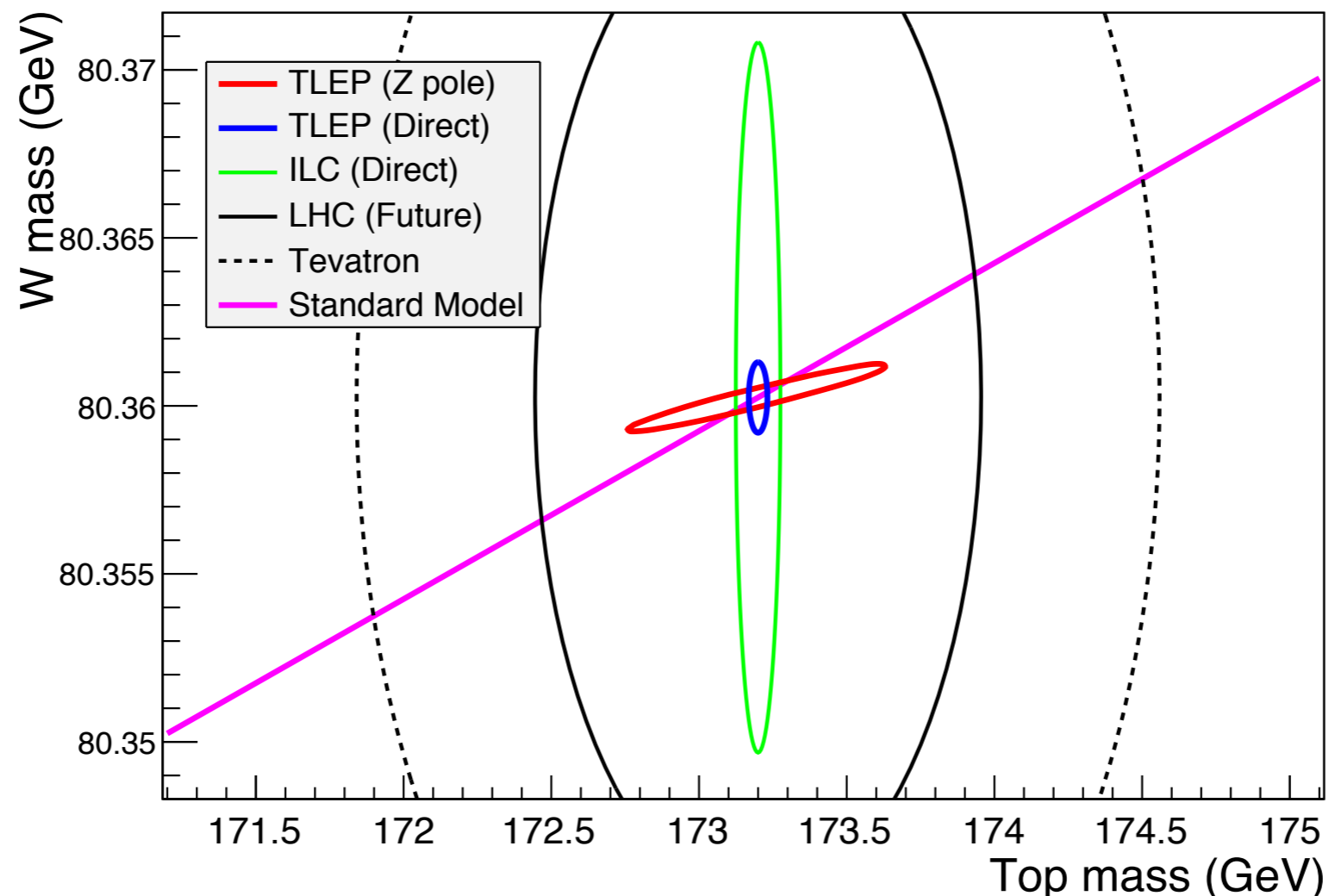
$$m_t = 173 \text{ GeV}$$

Peak $\sim 348 \text{ GeV}$

Top Precision at ILC and TLEP

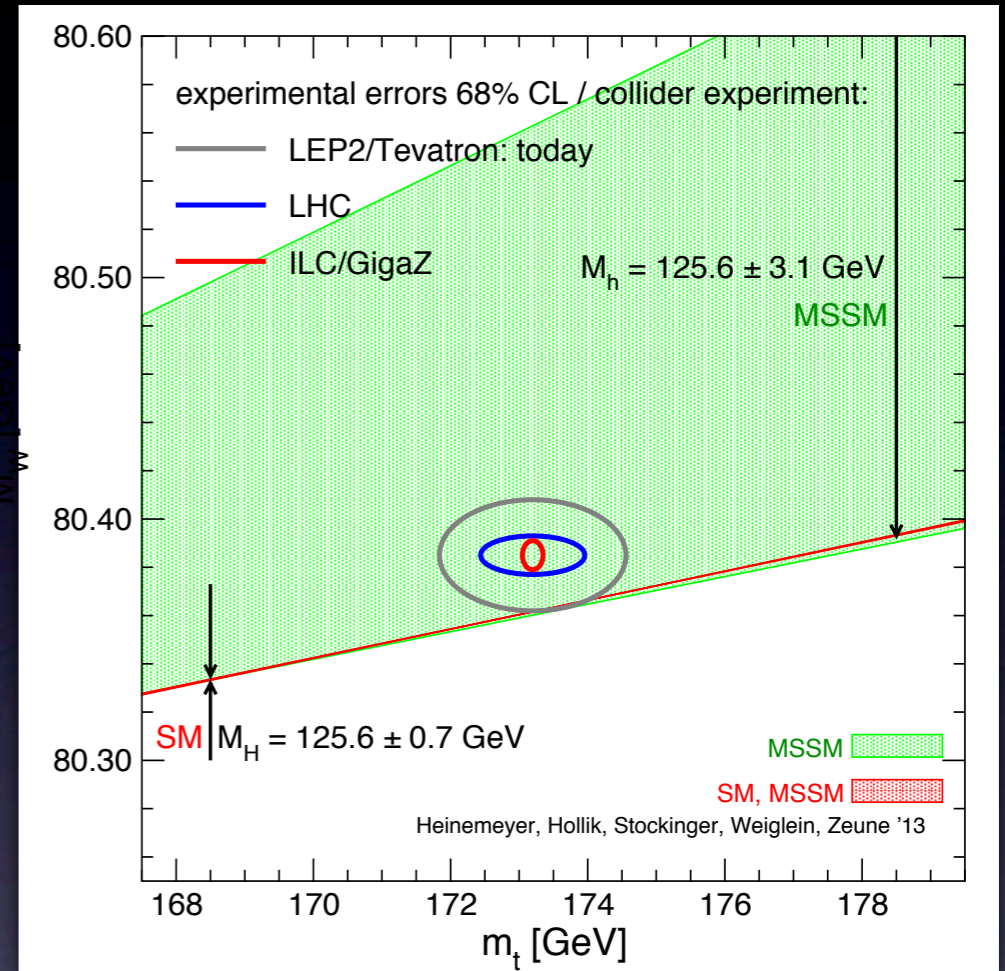
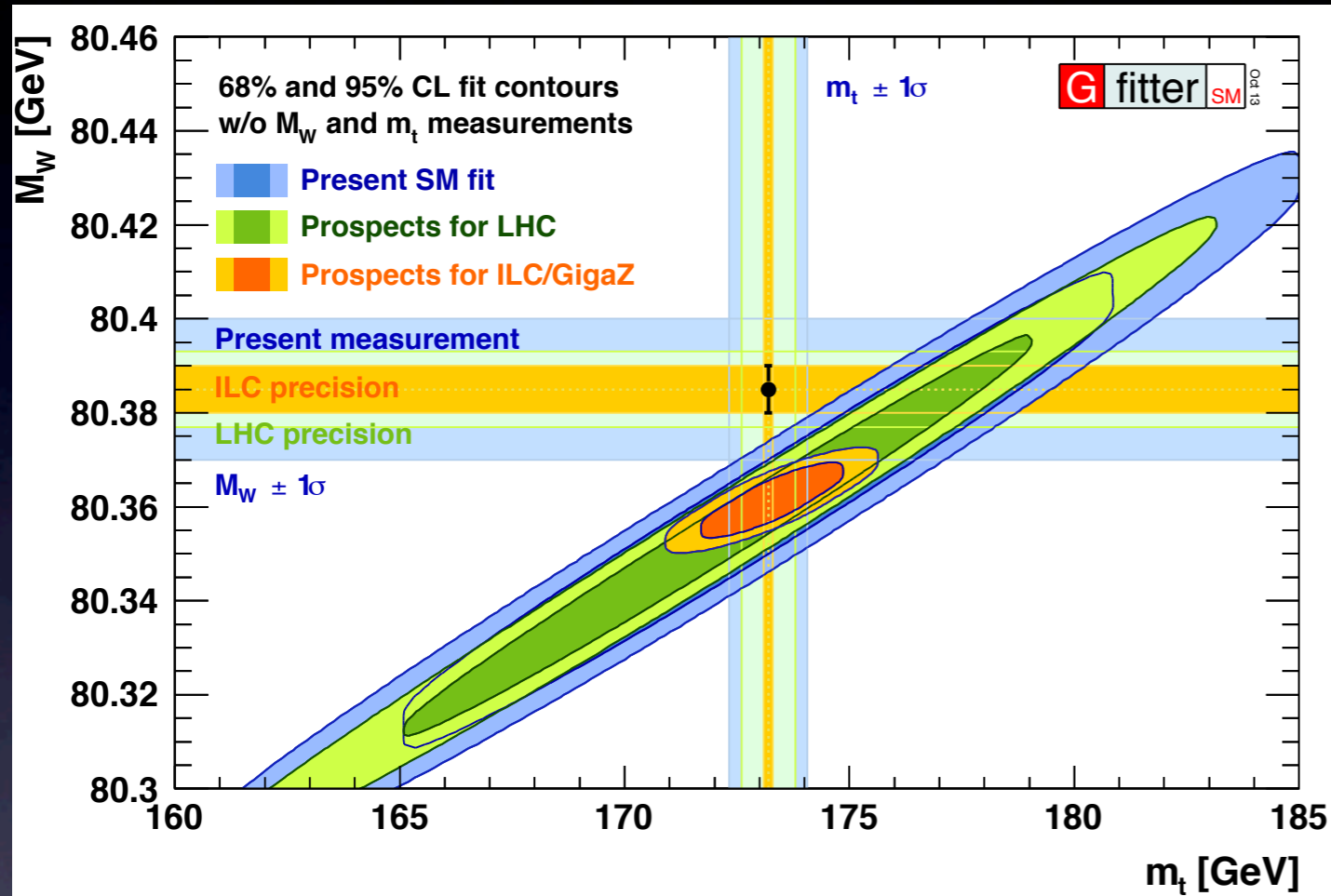
5 years scan

Parameter	m_{top}	Γ_{top}	λ_{top}
TLEP	10 MeV/c²	11 MeV	±13%
ILC	31 MeV/c ²	34 MeV	±40%



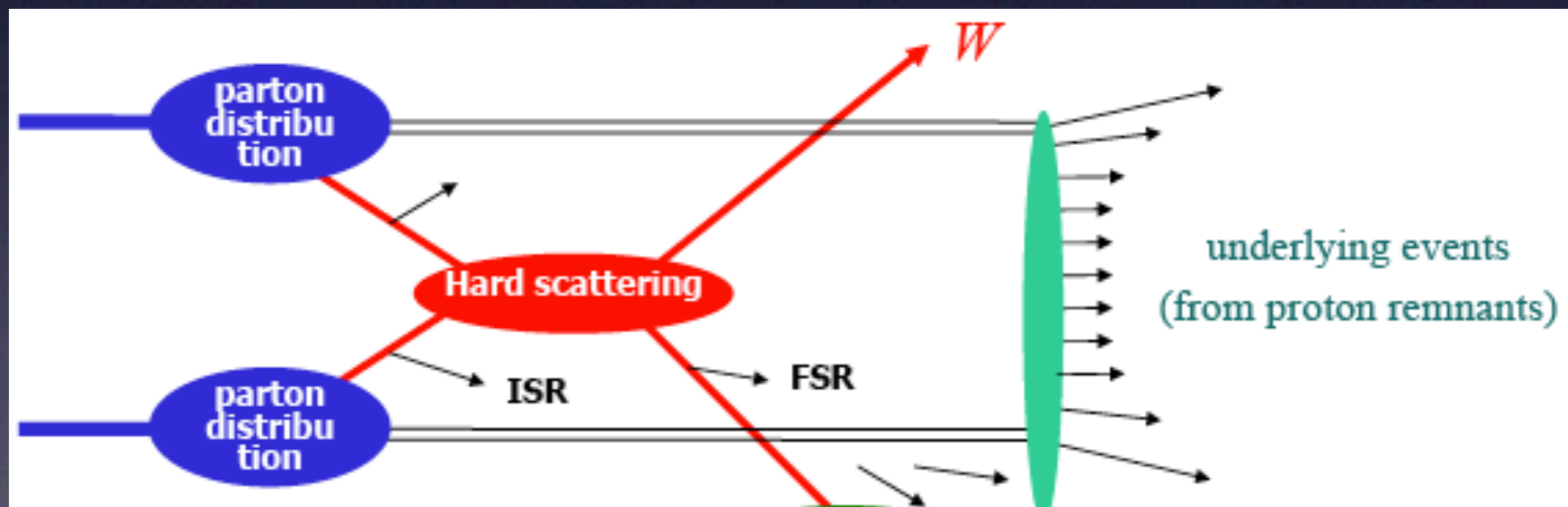
Mass Precision

Top-quark, W-boson and Higgs boson



	LHC	LHC	ILC/GigaZ	ILC	ILC	ILC	TLEP	SM prediction
\sqrt{s} [TeV]	14	14	0.091	0.161	0.161	0.250	0.161	-
\mathcal{L} [fb^{-1}]	300	3000		100	480	500	3000 \times 4	-
ΔM_W [MeV]	8	5	-	4.1-4.5	2.3-2.9	2.8	< 1.2	4.2(3.0)
$\Delta \sin^2 \theta_{\text{eff}}^{\ell}$ [10^{-5}]	36	21	1.3	-	-	-	0.3	3.0(2.6)

Parton Distribution Functions



Parton Distribution Functions

Groups providing NNLO PDFs based on non-LHC data

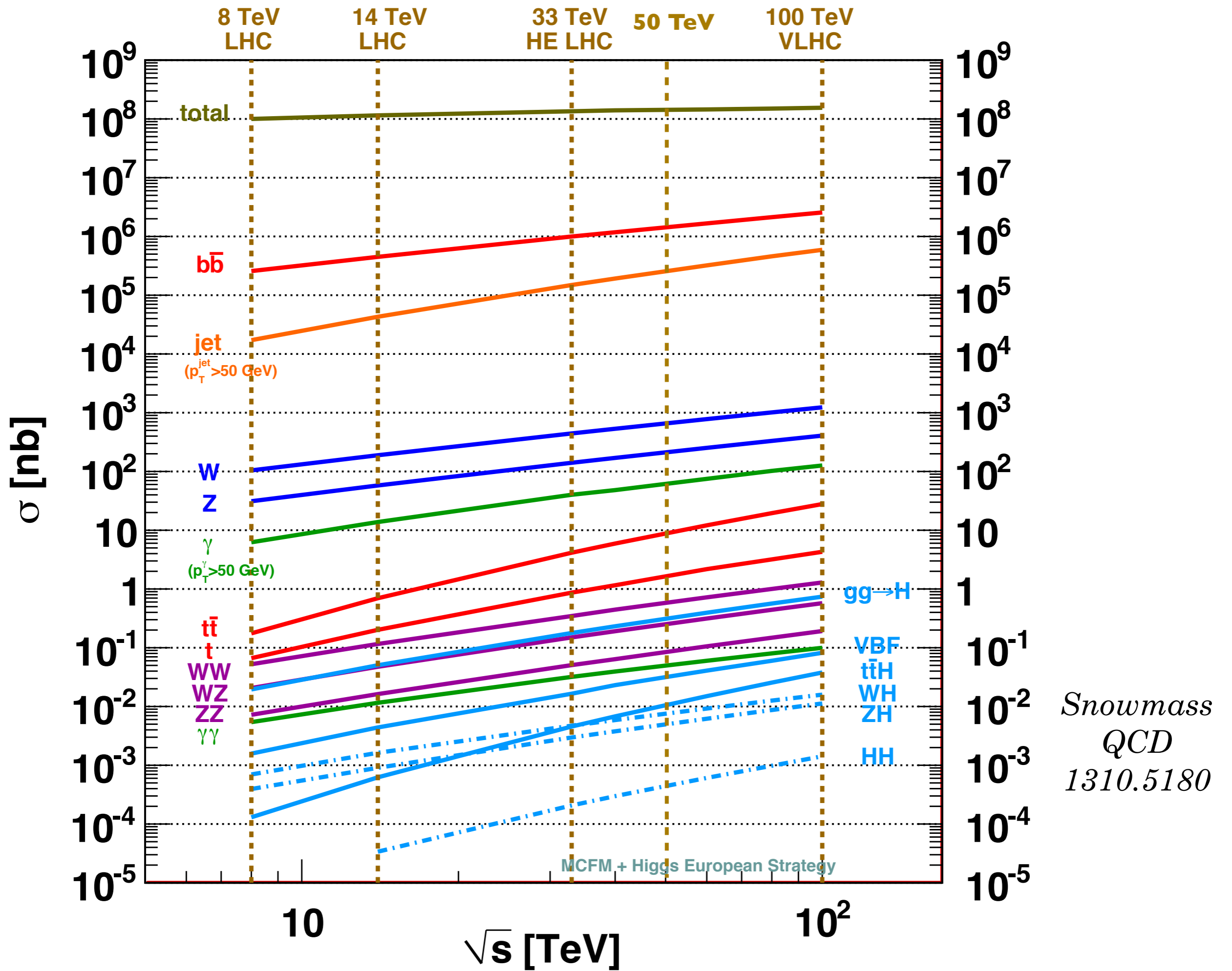
NNLO	CTEQ	MRST/MSTW	NNPDF	ABKM/ABM	HERA	JR
Since	2012	2004	2011	2009	2011	2008
Latest	CT10	MSTW08/CPd	NNPDF2.3	ABM11/12	HERA15	JR09
Error	50	40	100	28	28	26

PDFs at the LHC are aiming at high accuracies and with great diversities
(NNLO in QCD + NLO in EW)

PDF uncertainties

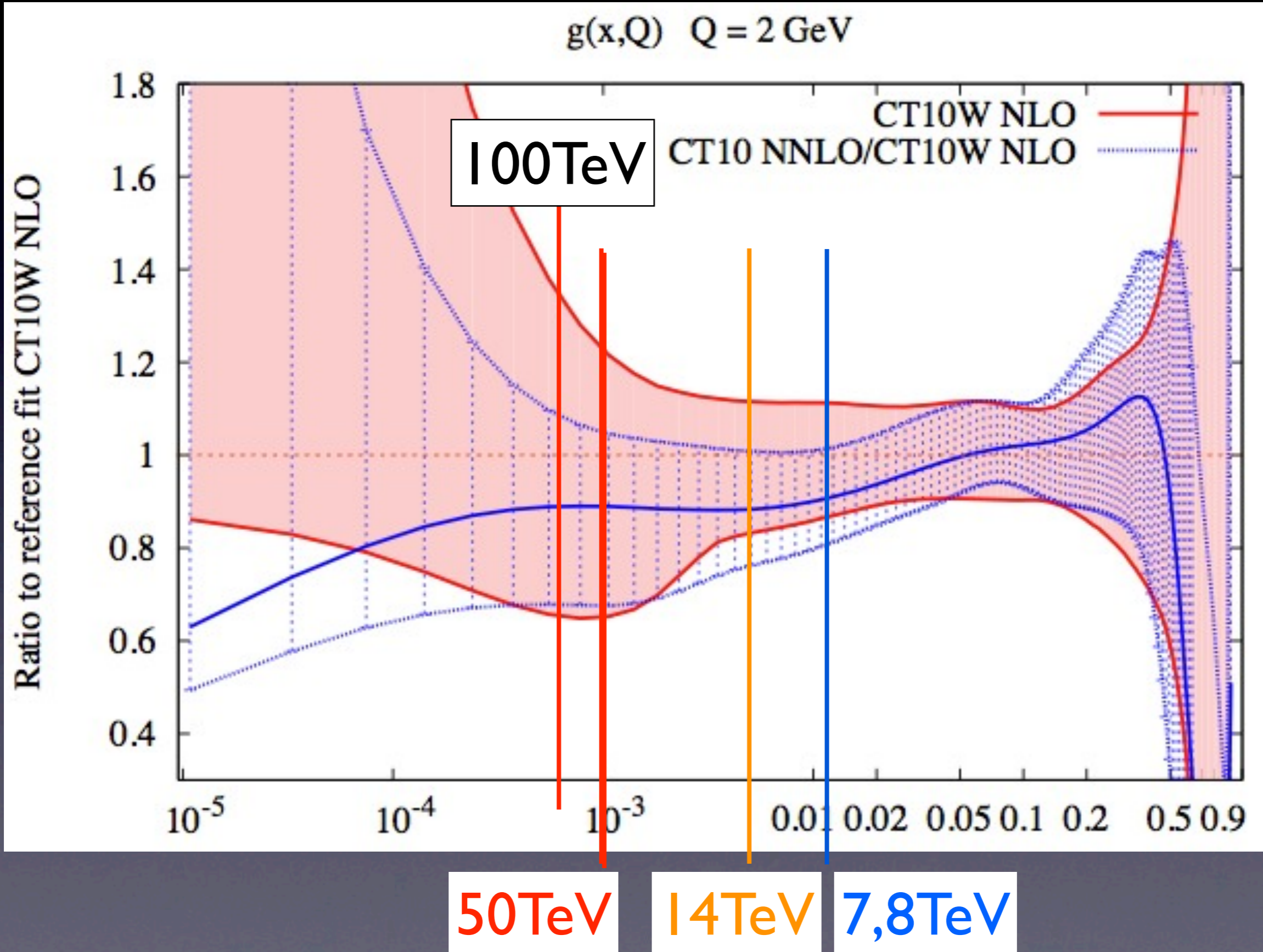
NNLO PDF + EW correction

Variable-Flavor-Number scheme (top-quark PDF?)



Gluon PDFs

$$\langle x \rangle \approx \frac{50 \text{ GeV}}{E_{\text{cm}}}$$



Luminosities and Uncertainties for 14, 100 TeV

Normalized to NNPDF central

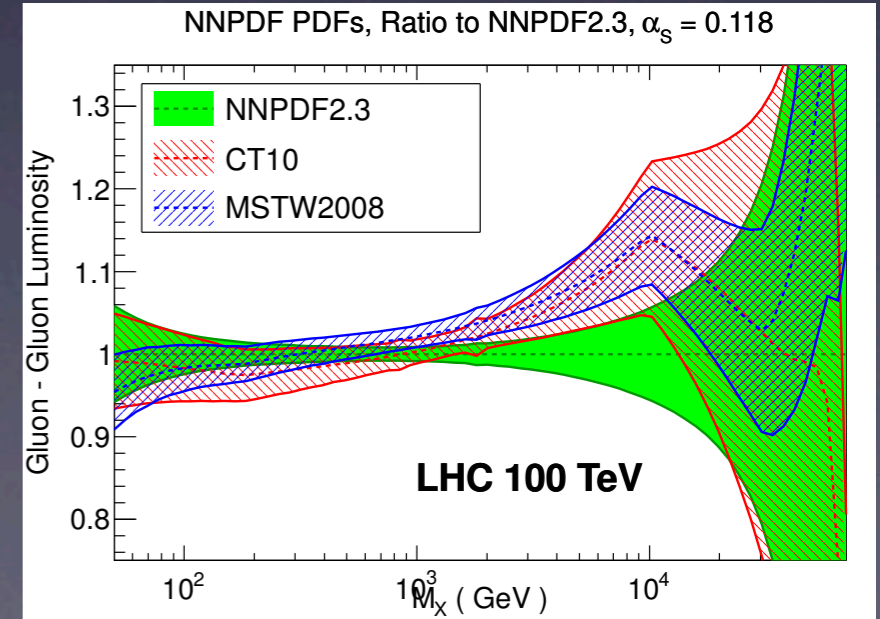
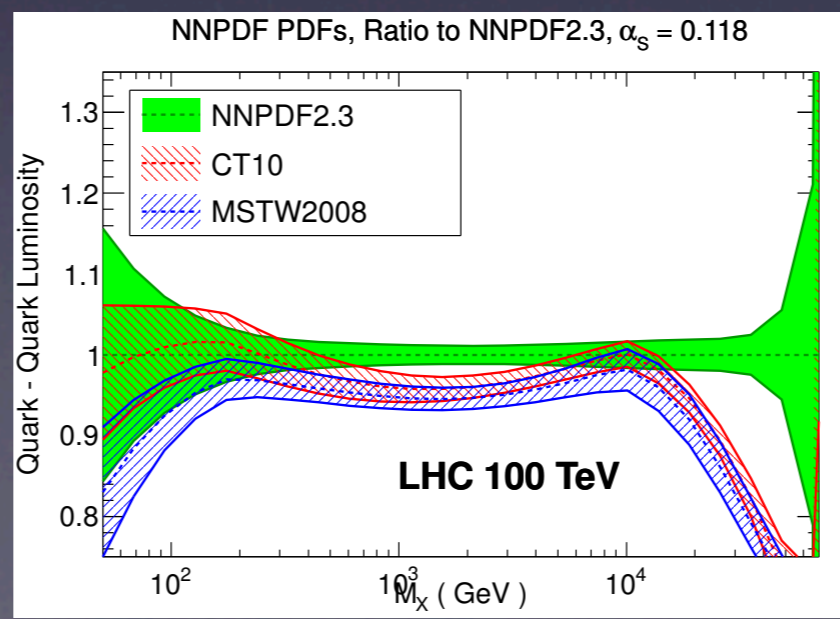
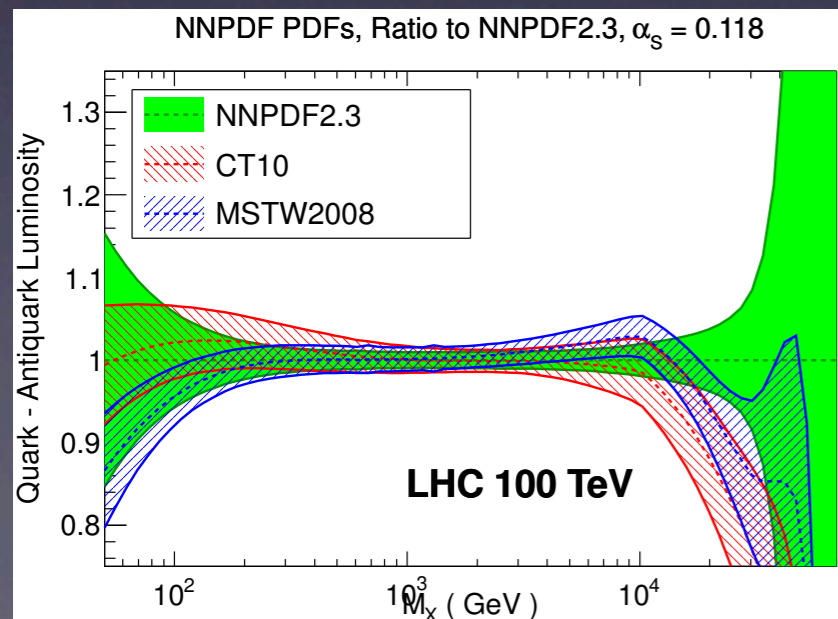
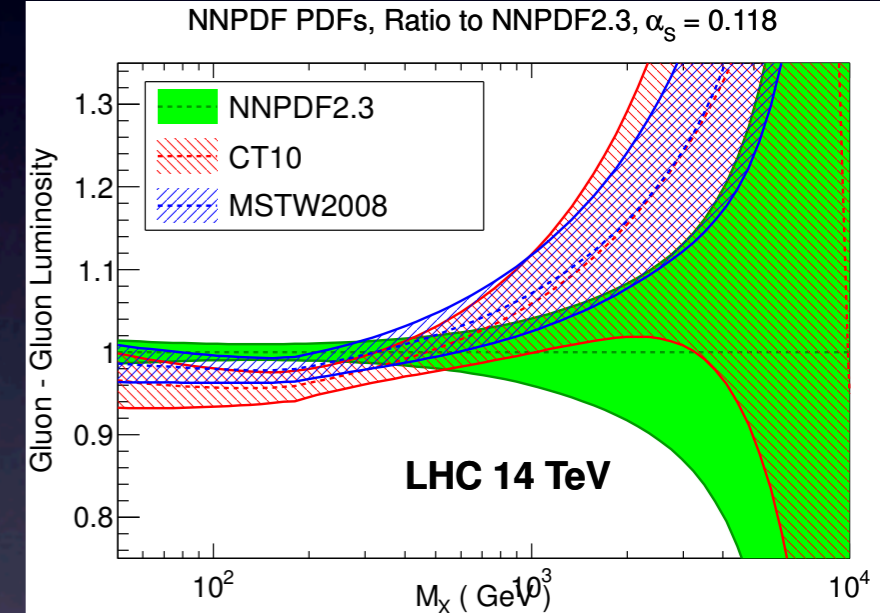
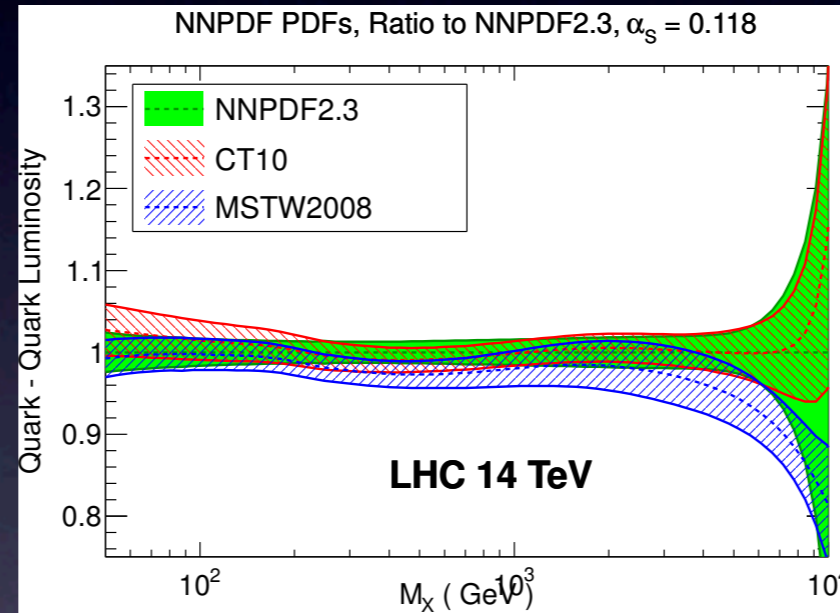
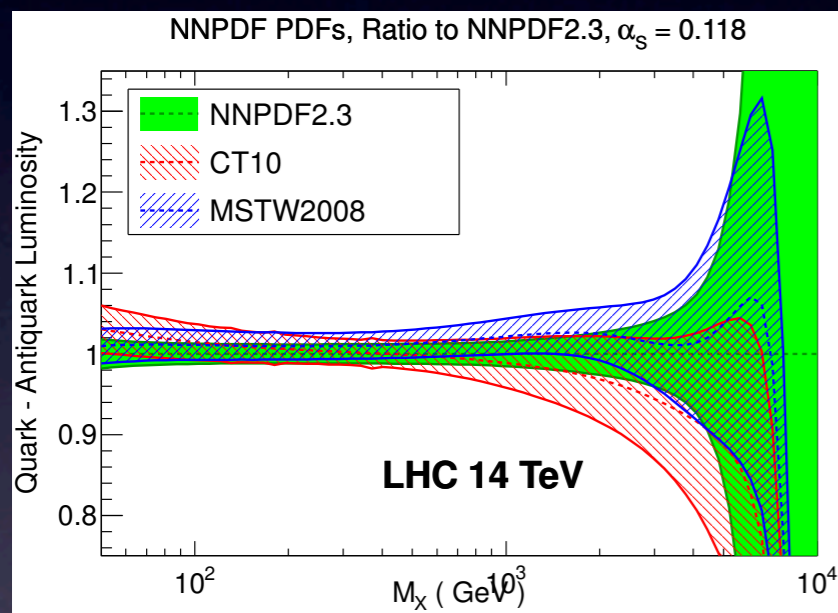
$$\Phi_{ij}(M_X^2) = \frac{1}{s} \int_{\tau}^1 \frac{dx_1}{x_1} f_i(x_1, M_X^2) f_j(\tau/x_1, M_X^2)$$

Snowmass report:
QCD 1310.5180

$q\bar{q}$

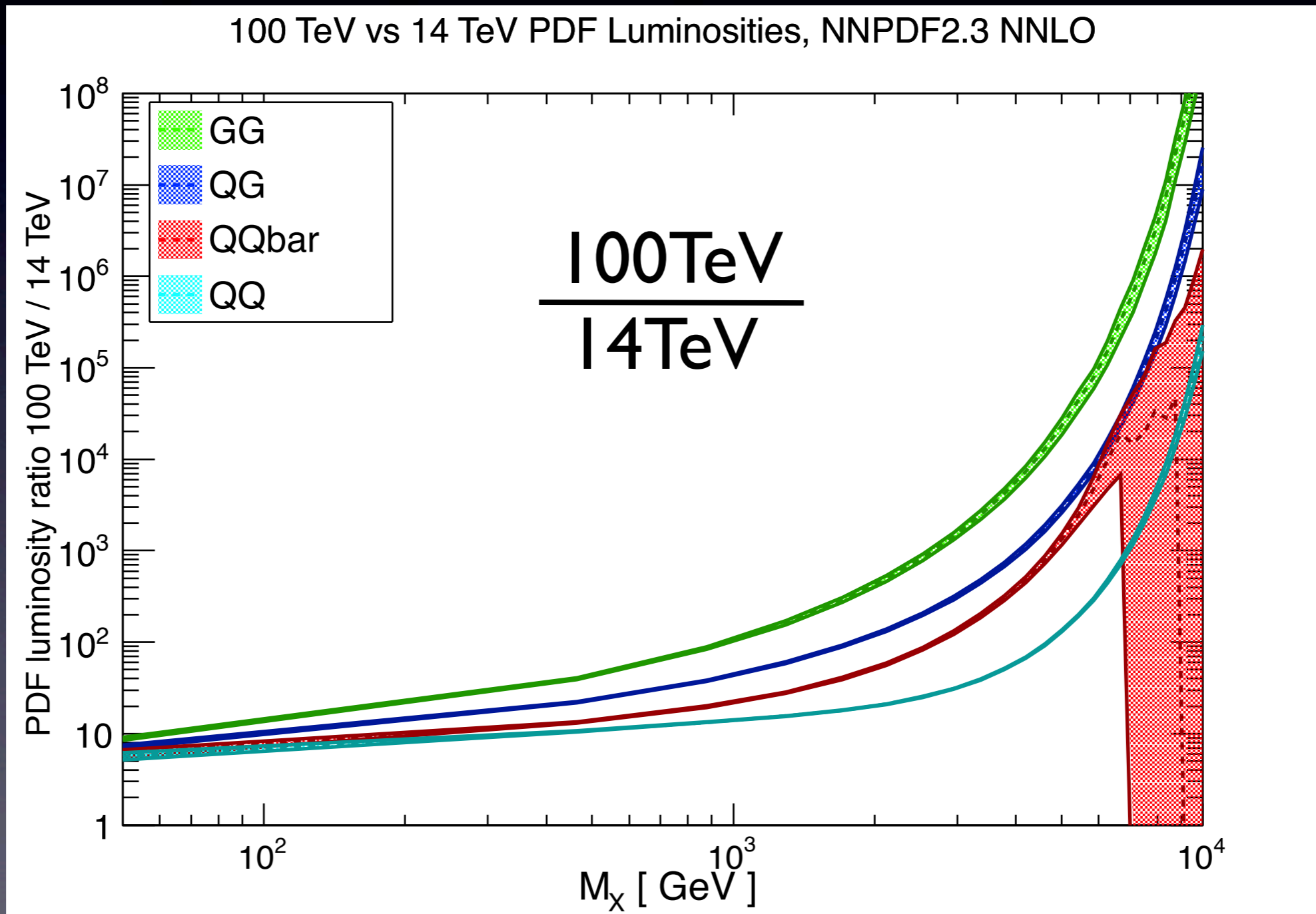
qq

gg



PDF Luminosities

$$\Phi_{ij} (M_X^2) = \frac{1}{s} \int_{\tau}^1 \frac{dx_1}{x_1} f_i (x_1, M_X^2) f_j (\tau/x_1, M_X^2)$$

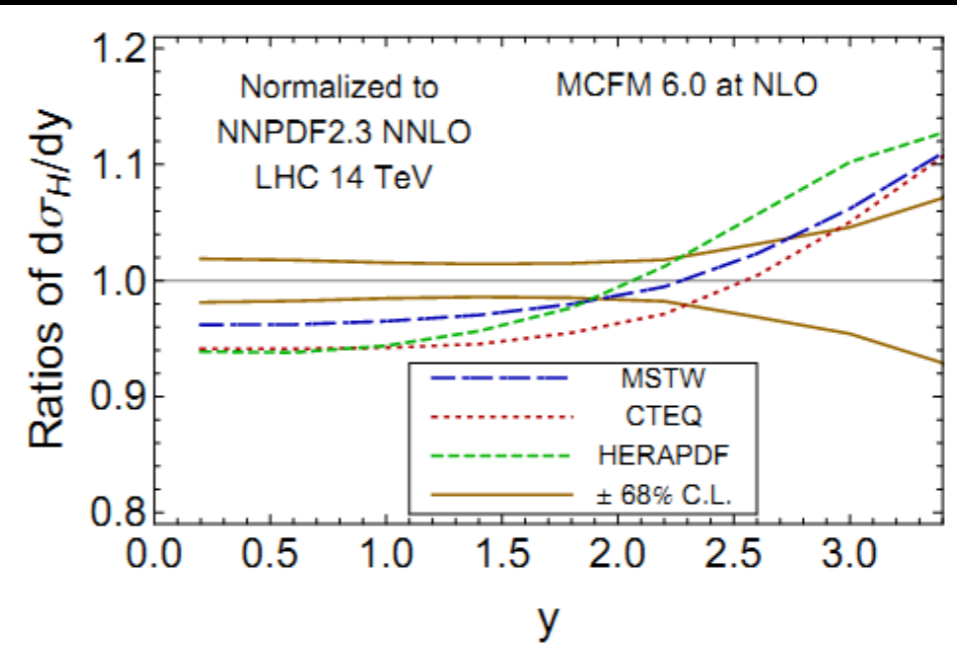
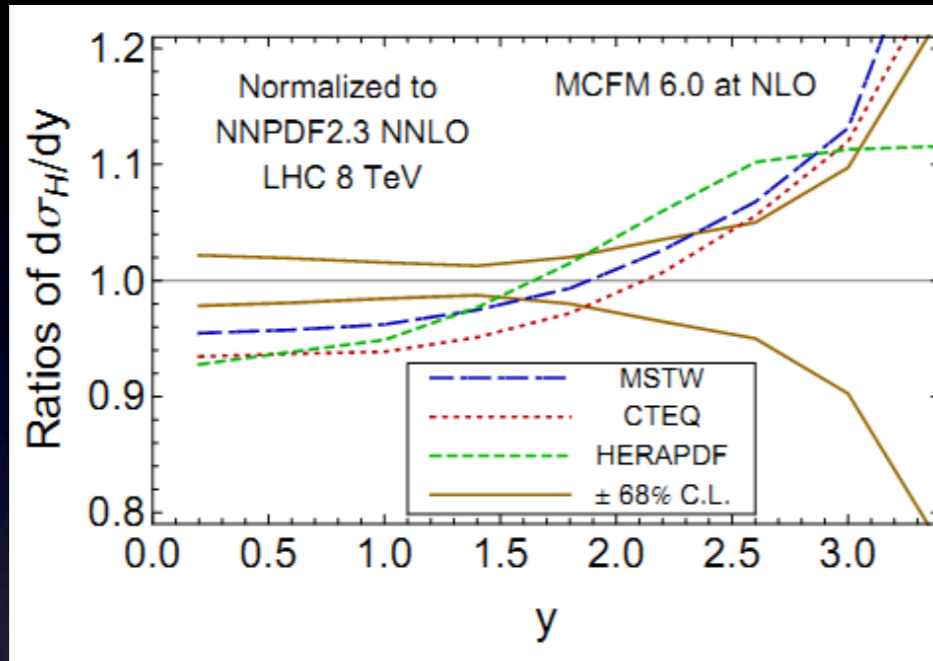


Standard Candle of Gluon PDF

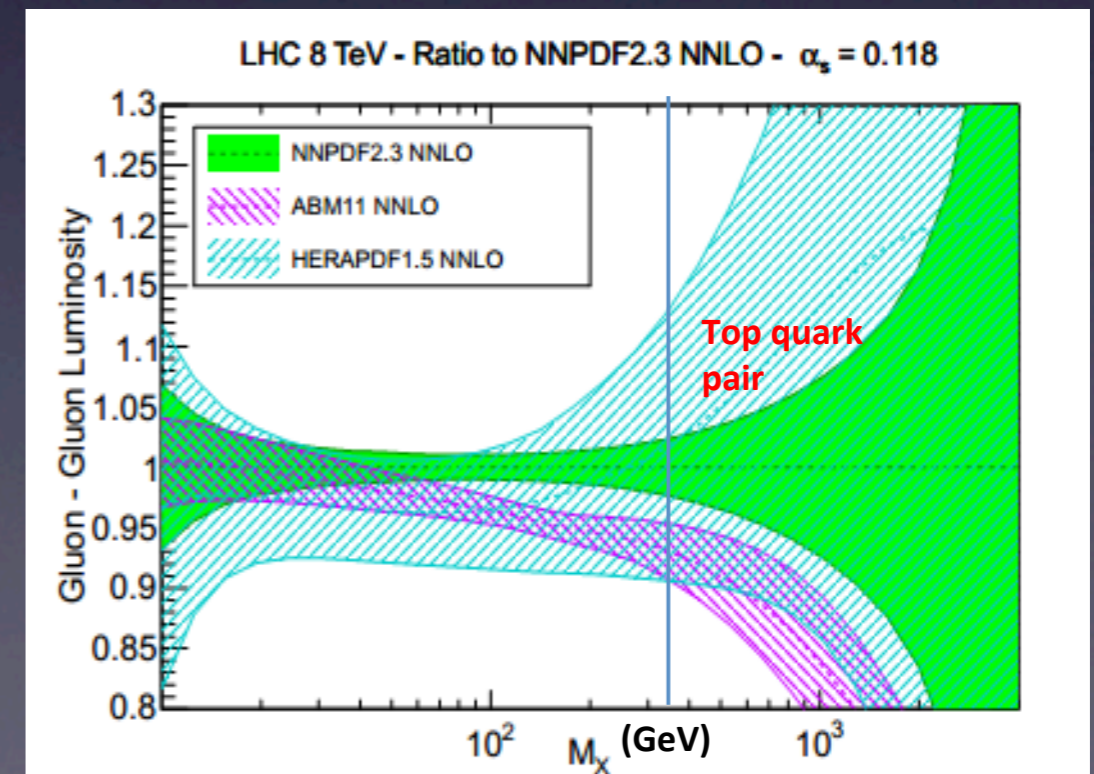
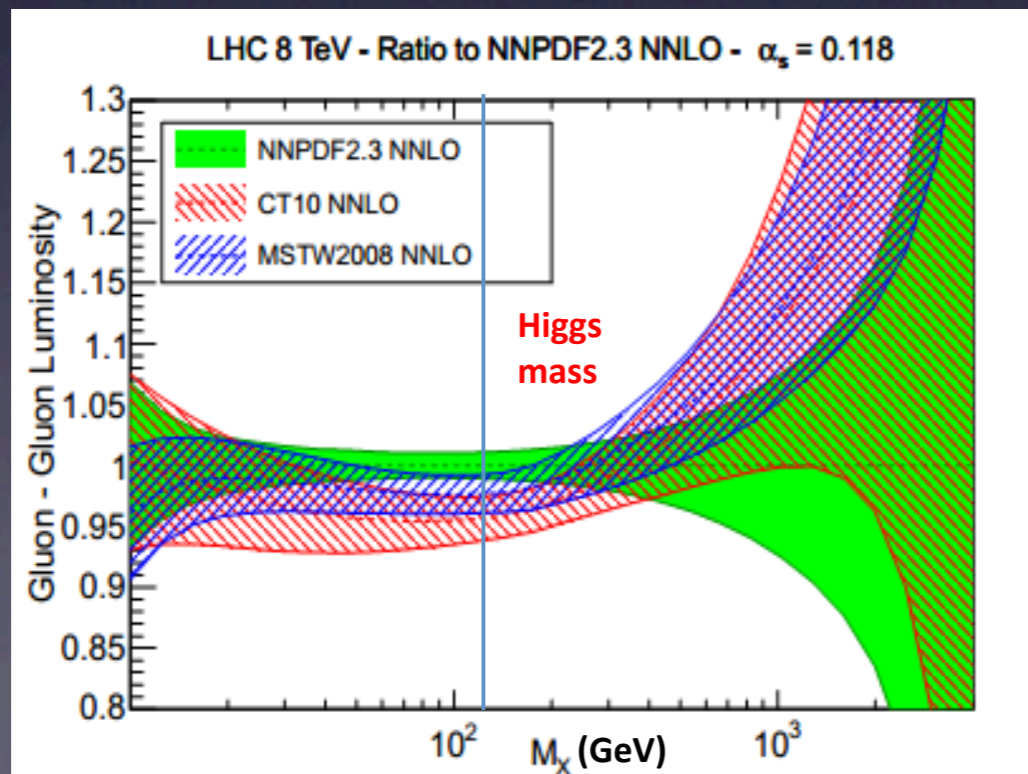
(Higgs production + Top-pair production)

Rapidity distribution

PDF benchmarking, Gao et al, 1211.5142



Gluon-Gluon parton luminosity at 8 TeV

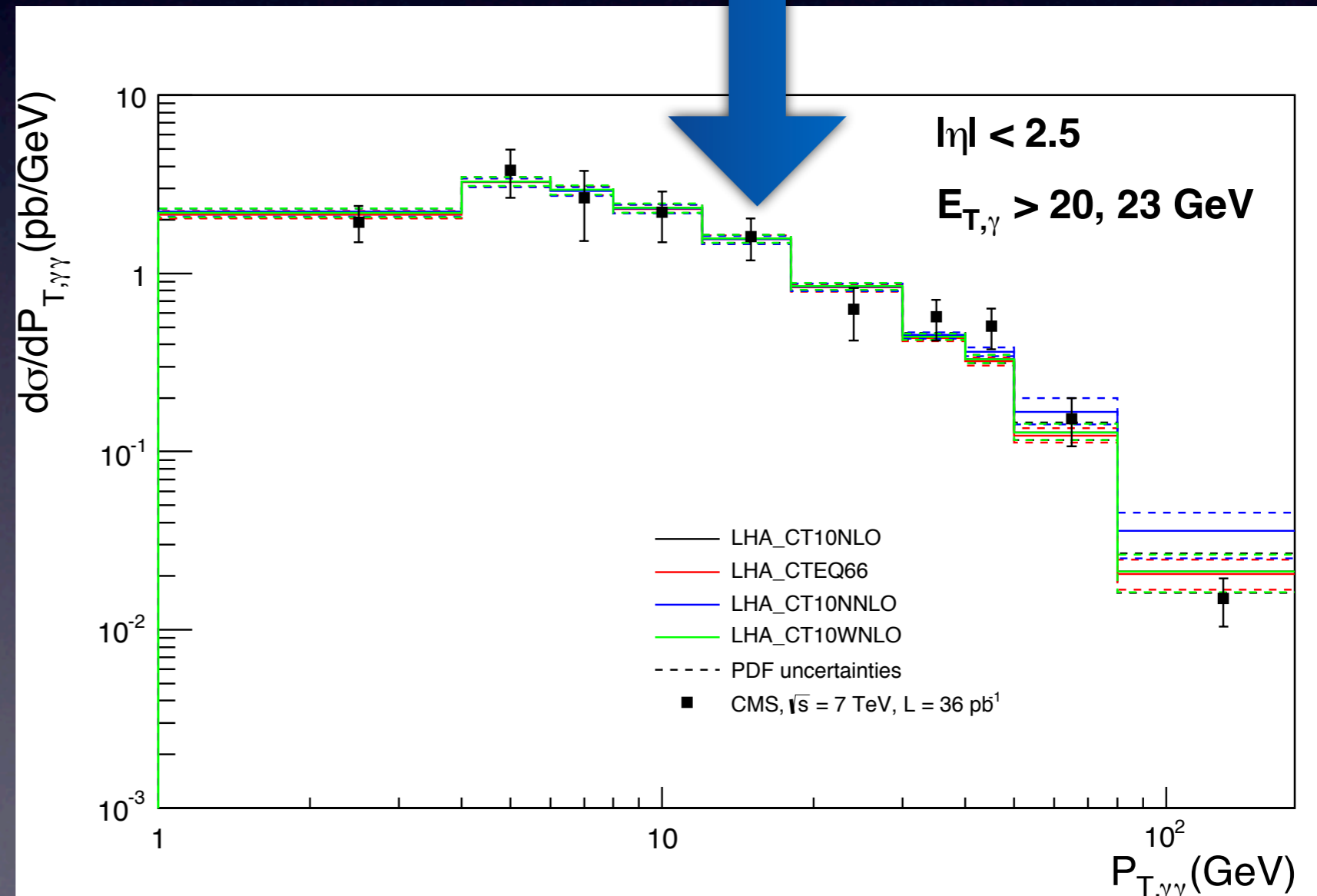
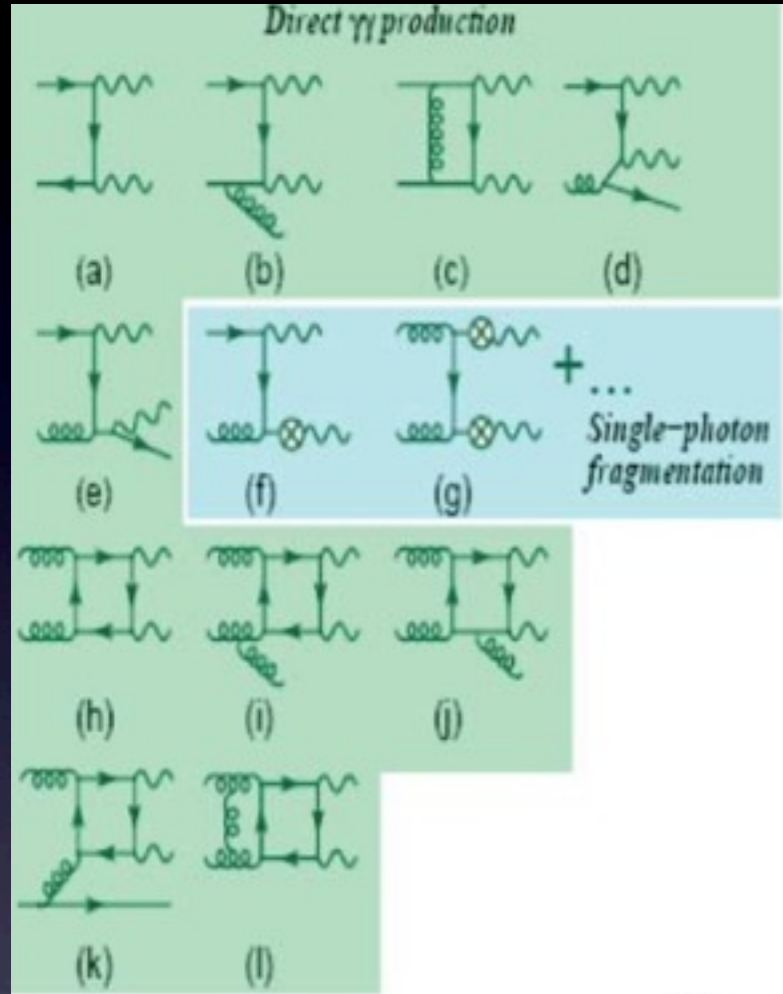


Di-photon Production and Gluon PDF

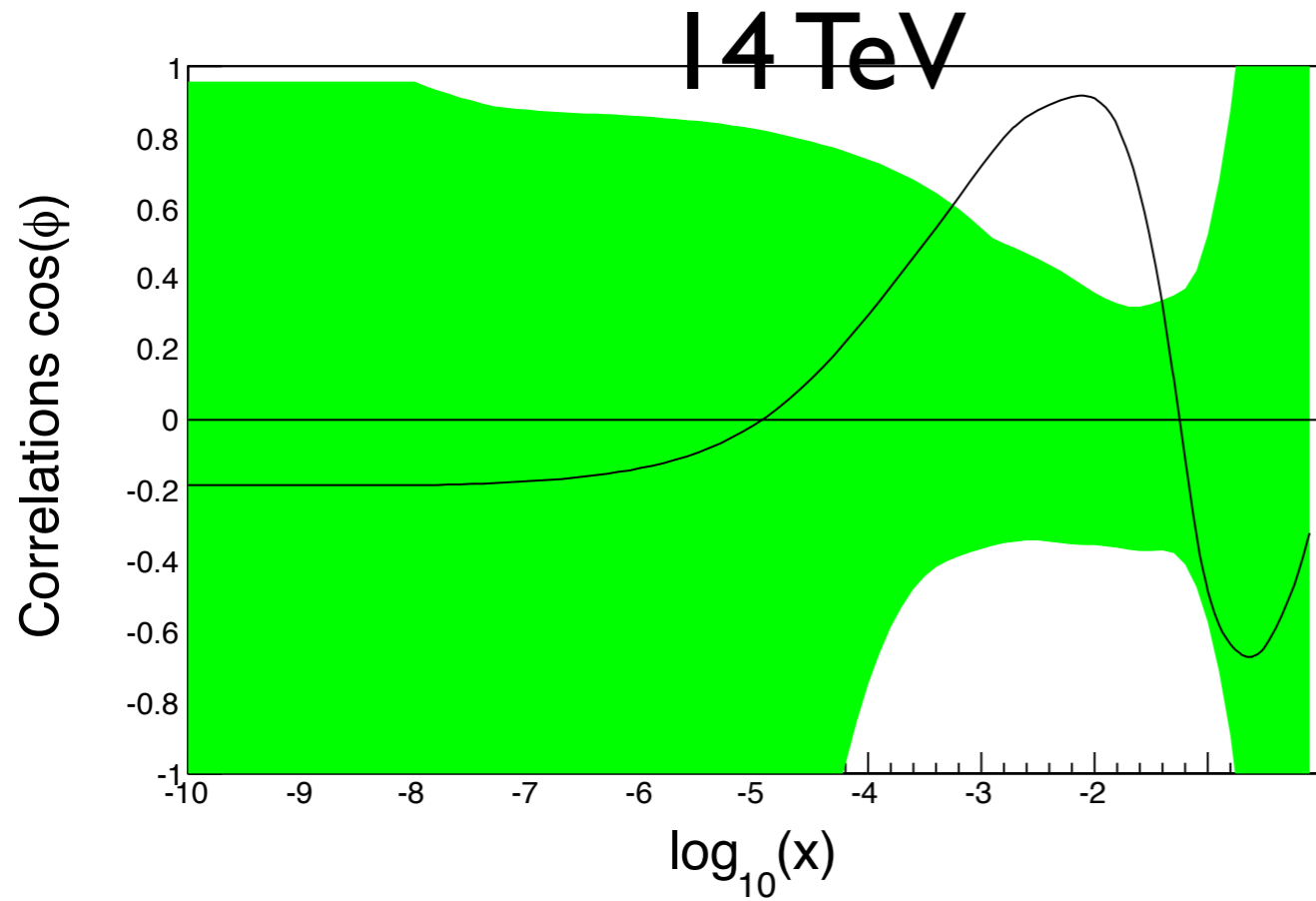
Zhao Li

CSS q_T resummation

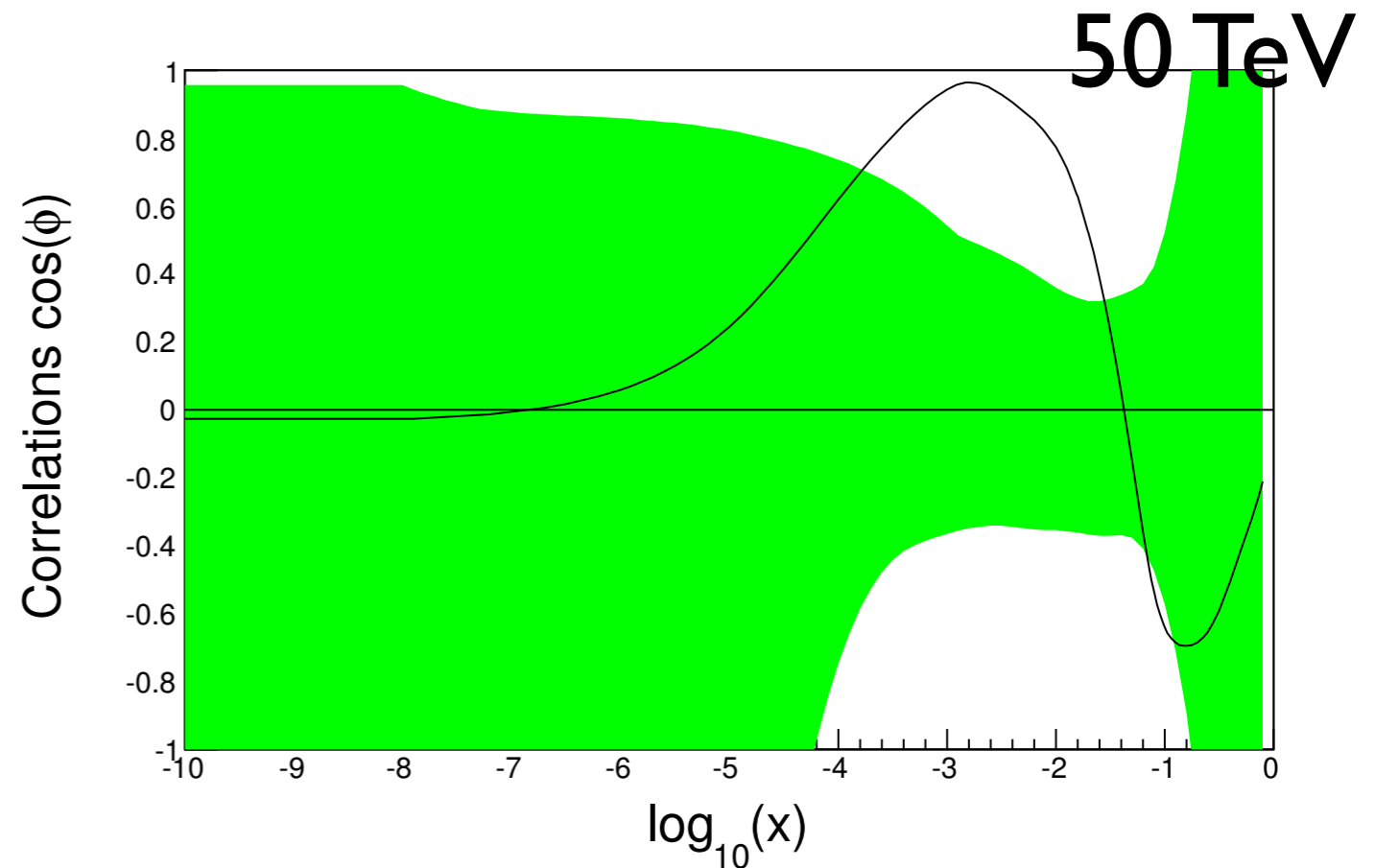
$$p_T(\gamma\gamma) = 15 \text{ GeV}$$



Di-photon Production and Gluon PDF

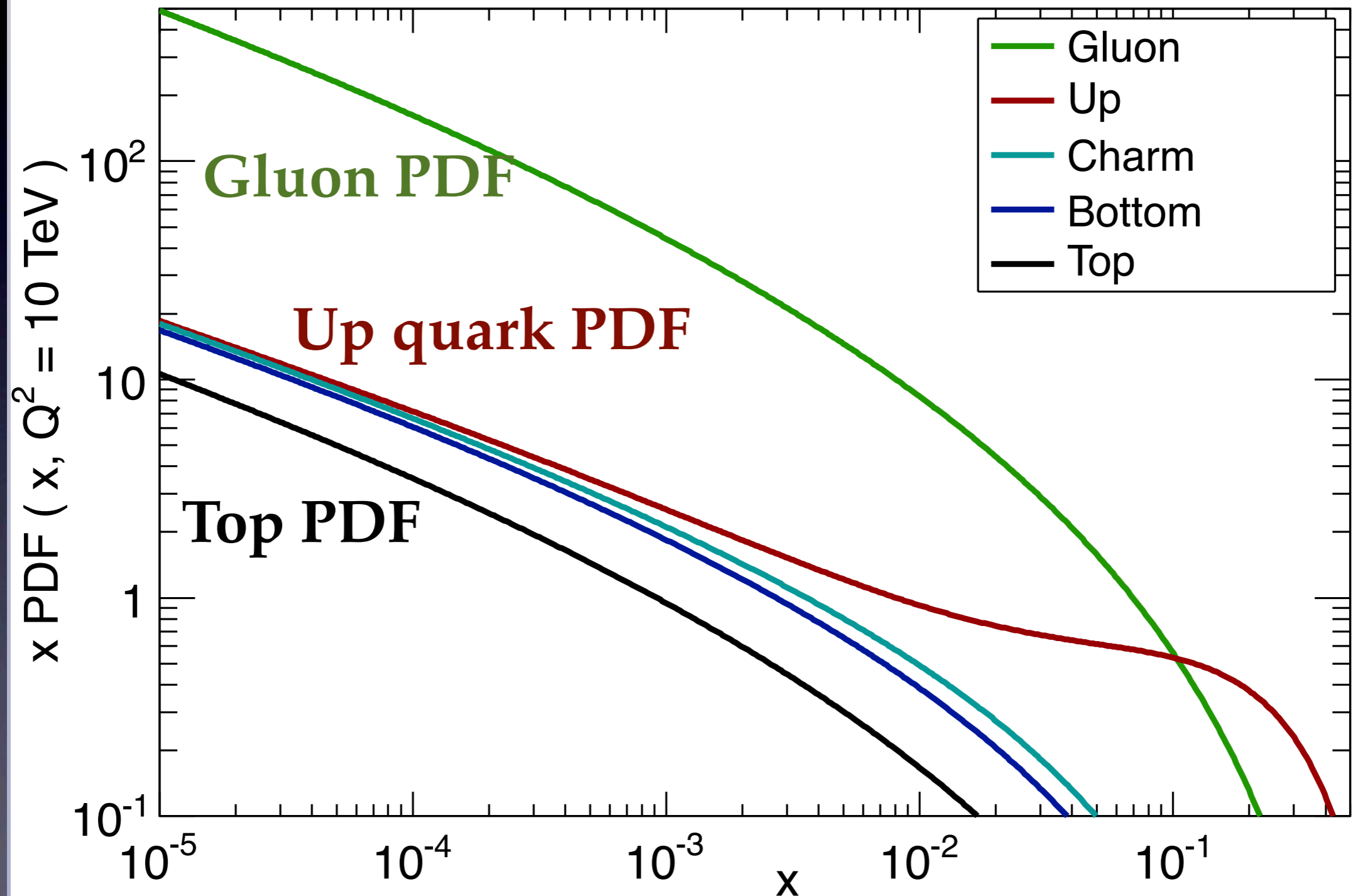


Differential x-section
versus PDF (mainly
gluon) correlation



Top-Quark PDFs

NNPDF2.3 NNLO $N_F = 6$



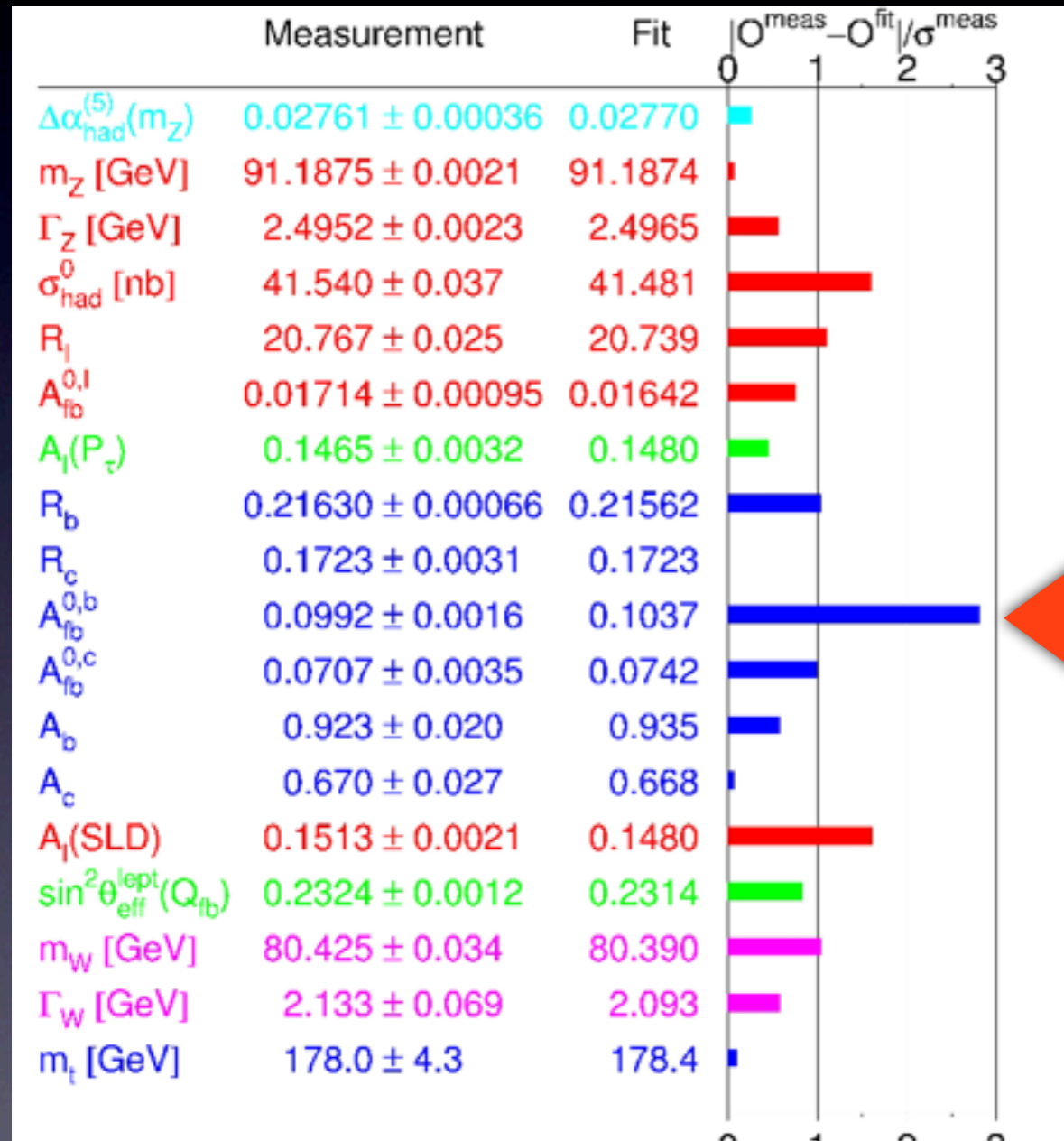
Third Generation Quarks

Weak Couplings of 3rd Generation

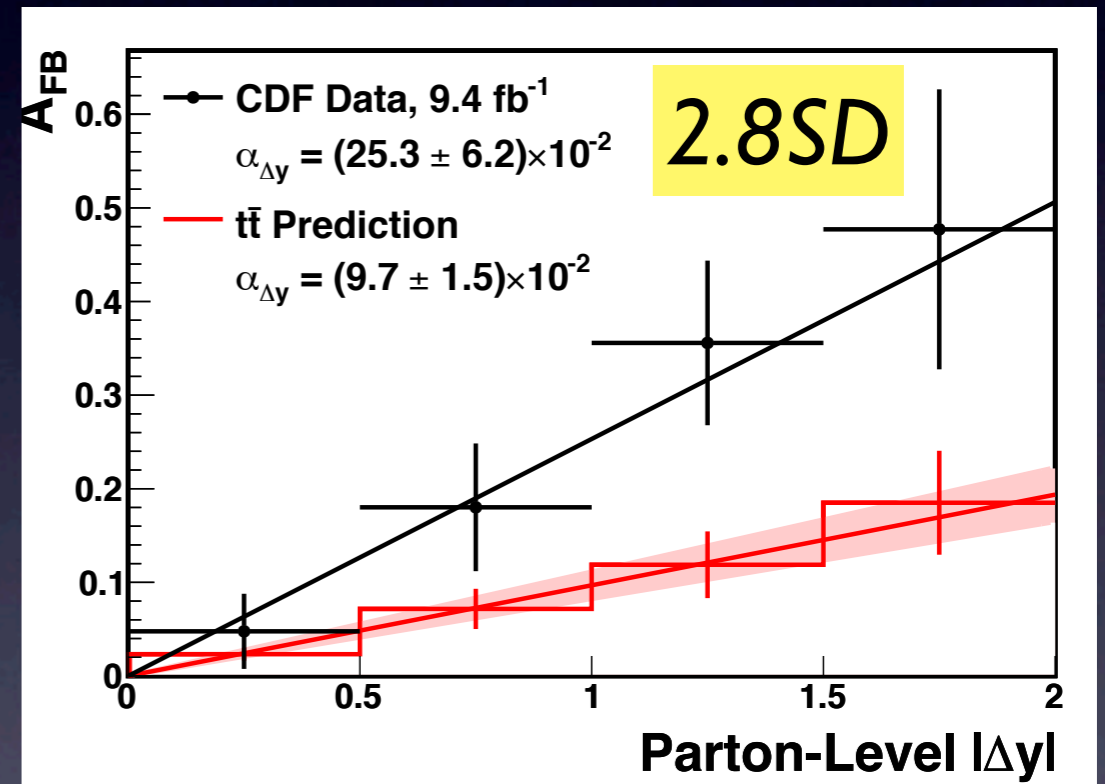
Something is rotten in the 3rd generation quarks

Top charge asymmetry at the Tevatron

see Z. G. Si's talk



AFB(b) at LEP



Measurement	Measured Value, %	Theoretical Expectation [1], %
CDF 9.4 fb^{-1}	16.4 ± 4.7	8.8 ± 0.6
D0 5.4 fb^{-1}	19.6 ± 6.5	

Bernreuther and Z. G. Si, 1205.6580

$A_{FB}(b)$ and $R(b)$

CEPC

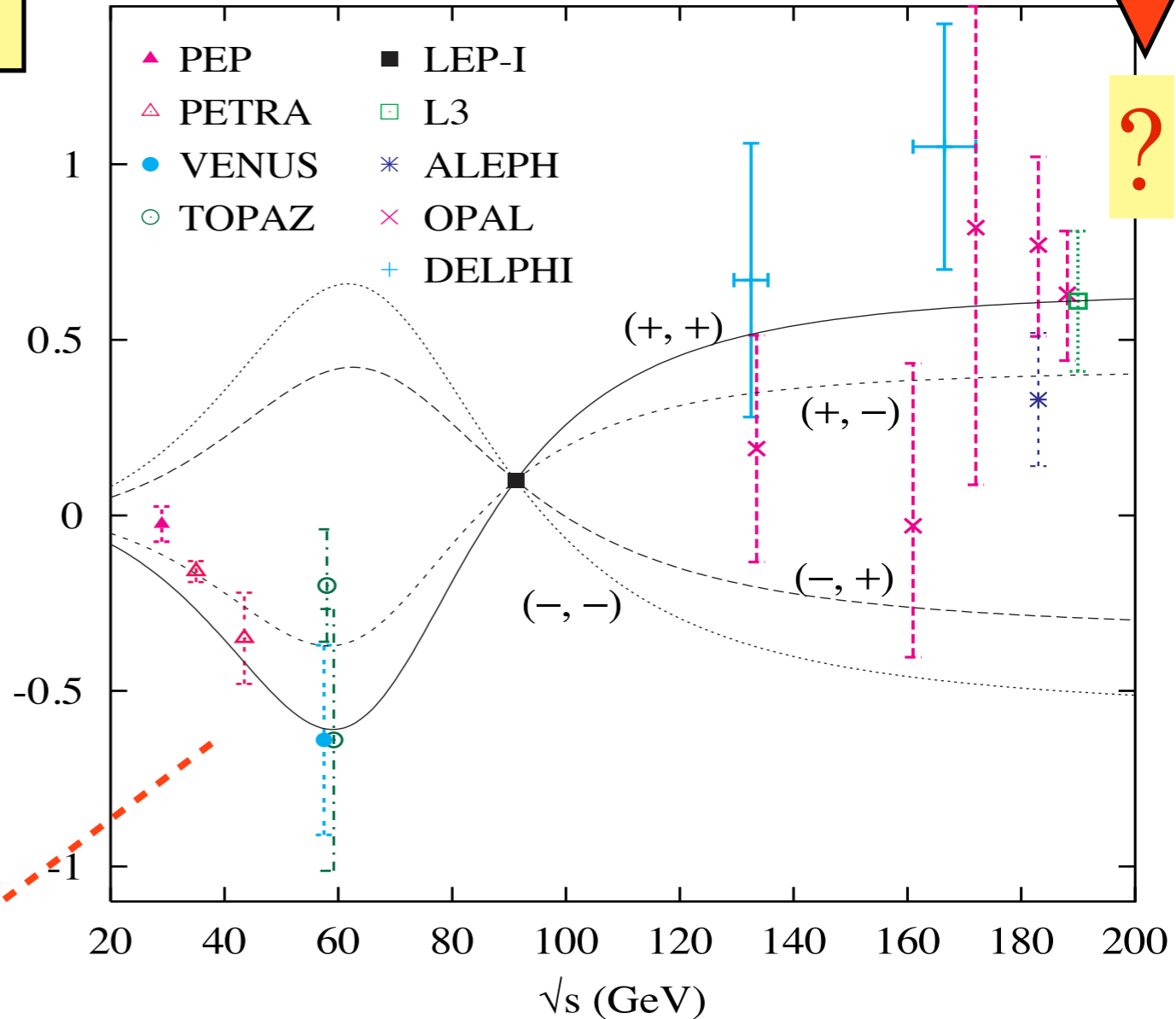
$$\mathcal{L}_{Zb\bar{b}} = \frac{-e}{s_W c_W} Z_\mu \bar{b} \gamma^\mu [\bar{g}_L^b P_L + \bar{g}_R^b P_R] b$$

$$R_b \equiv \frac{\Gamma(Z \rightarrow b\bar{b})}{\Gamma(Z \rightarrow \text{hadrons})} \simeq \frac{(\bar{g}_L^b)^2 + (\bar{g}_R^b)^2}{\sum_q [(\bar{g}_L^q)^2 + (\bar{g}_R^q)^2]}$$

$$A_{FB}^b|_{\sqrt{s} \simeq m_Z} = \frac{3}{4} A_\ell A_b$$

$$A_b \simeq \frac{(\bar{g}_L^b)^2 - (\bar{g}_R^b)^2}{(\bar{g}_L^b)^2 + (\bar{g}_R^b)^2}$$

A_{FB}^b



+

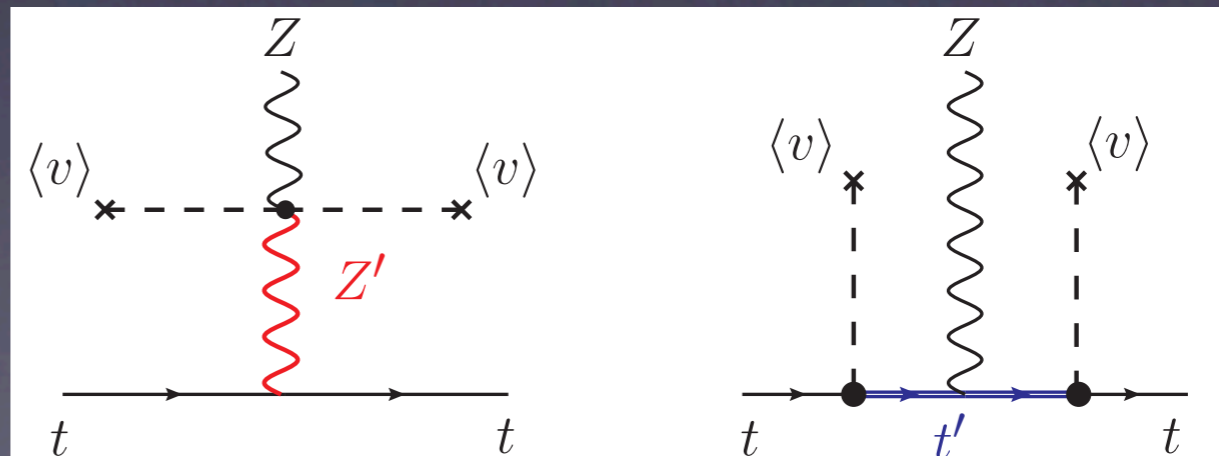
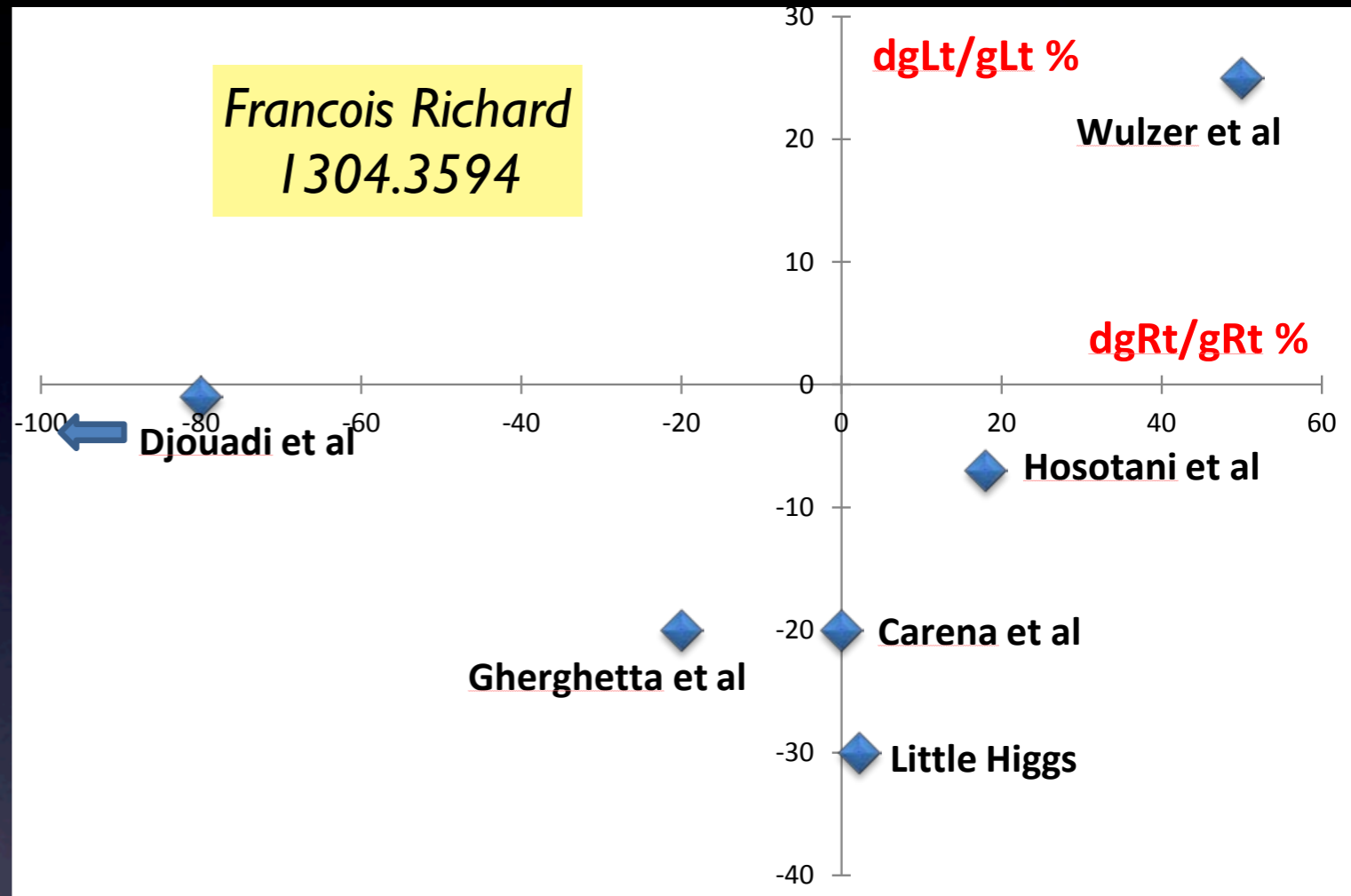
$$(\bar{g}_L^b, \bar{g}_R^b) \approx (\pm 0.992 g_L^b(SM), \pm 1.26 g_R^b(SM))$$

Weak Couplings of 3rd Generation Quarks

Z-t-t coupling

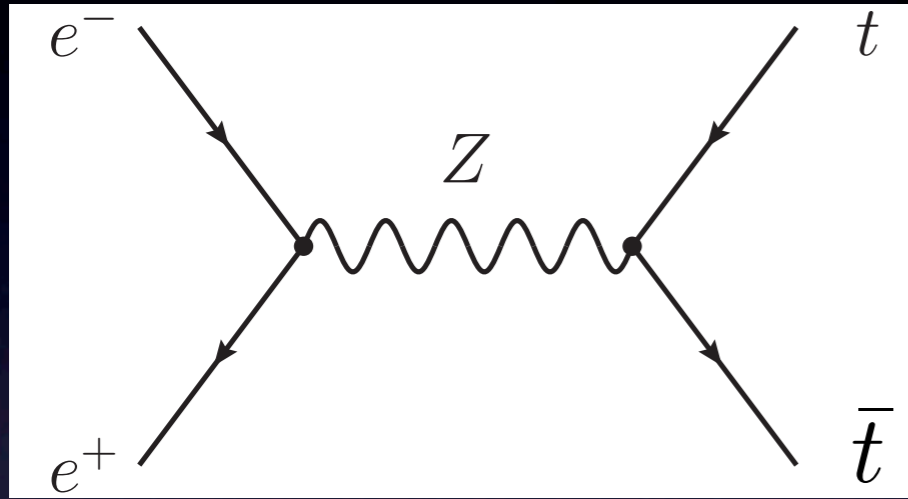
$$\begin{aligned} \mathcal{O}_{\phi q}^{(1)} &= i (\phi^\dagger D_\mu \phi) (\bar{q} \gamma^\mu q), \\ \mathcal{O}_{\phi q}^{(3)} &= i (\phi^\dagger \tau^I D_\mu \phi) (\bar{q} \gamma^\mu \tau^I q), \\ \mathcal{O}_{\phi t} &= i (\phi^\dagger D_\mu \phi) (\bar{t}_R \gamma^\mu t_R), \\ \mathcal{O}_{\phi b} &= i (\phi^\dagger D_\mu \phi) (\bar{b}_R \gamma^\mu b_R), \\ \mathcal{O}_{\phi\phi} &= (\phi^\dagger \epsilon D_\mu \phi) (\bar{t}_R \gamma^\mu b_R), \end{aligned}$$

Berger, QHC, Low,
 Phys.Rev.D80:074020(2009)
 0907.2191



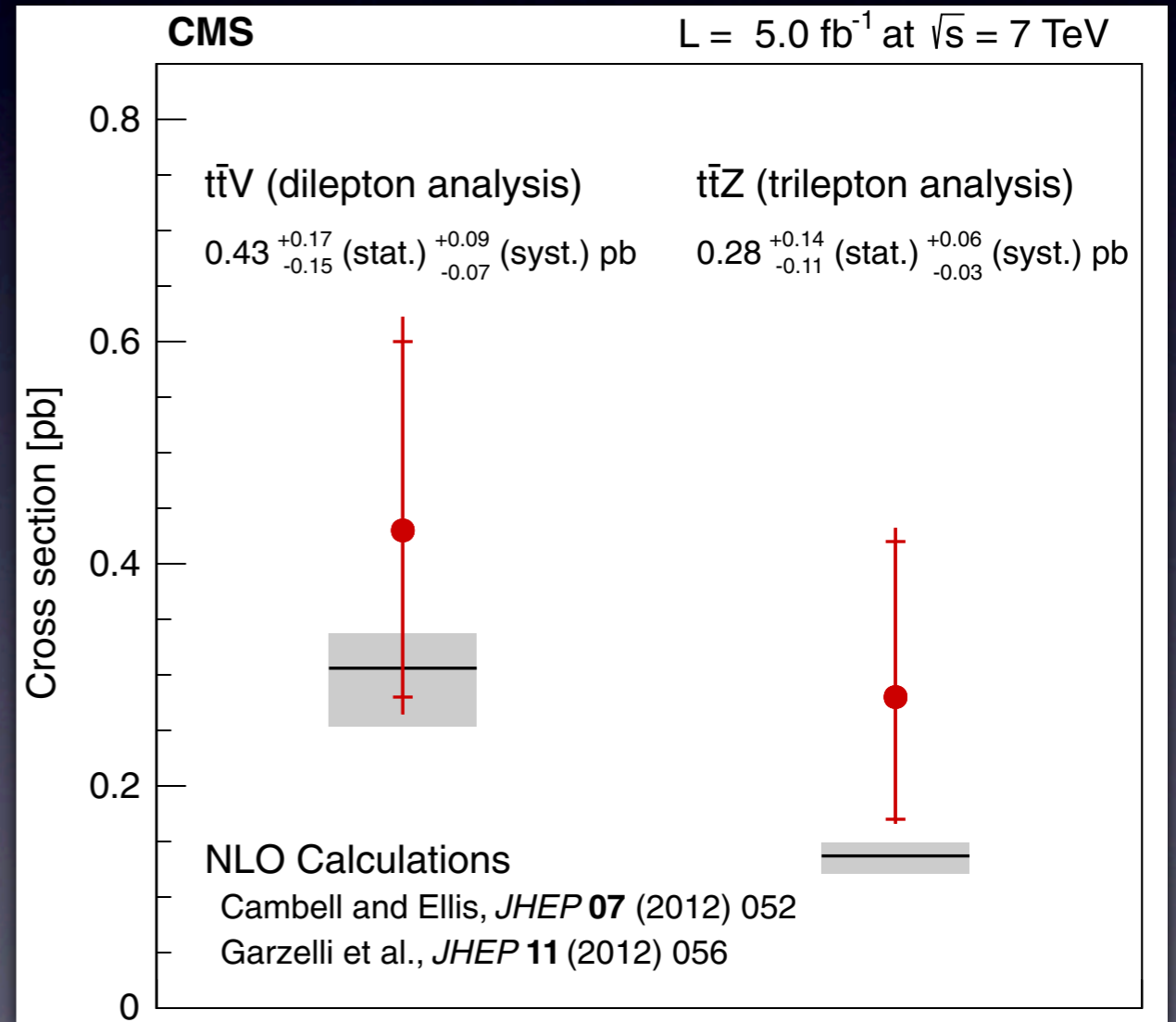
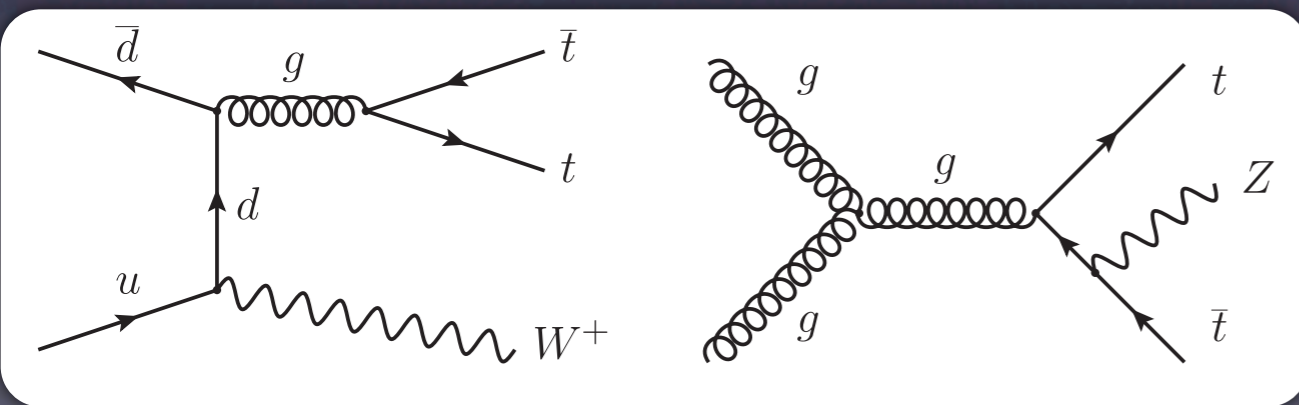
Z-t-t Coupling Measurements

Precision Machine

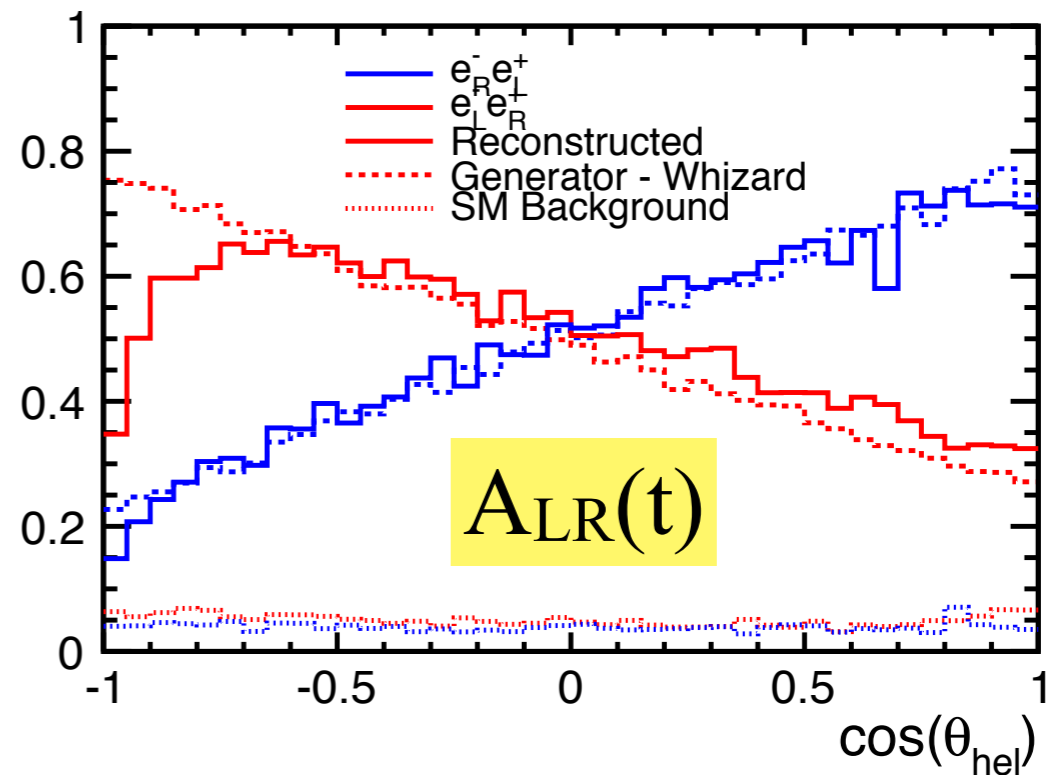
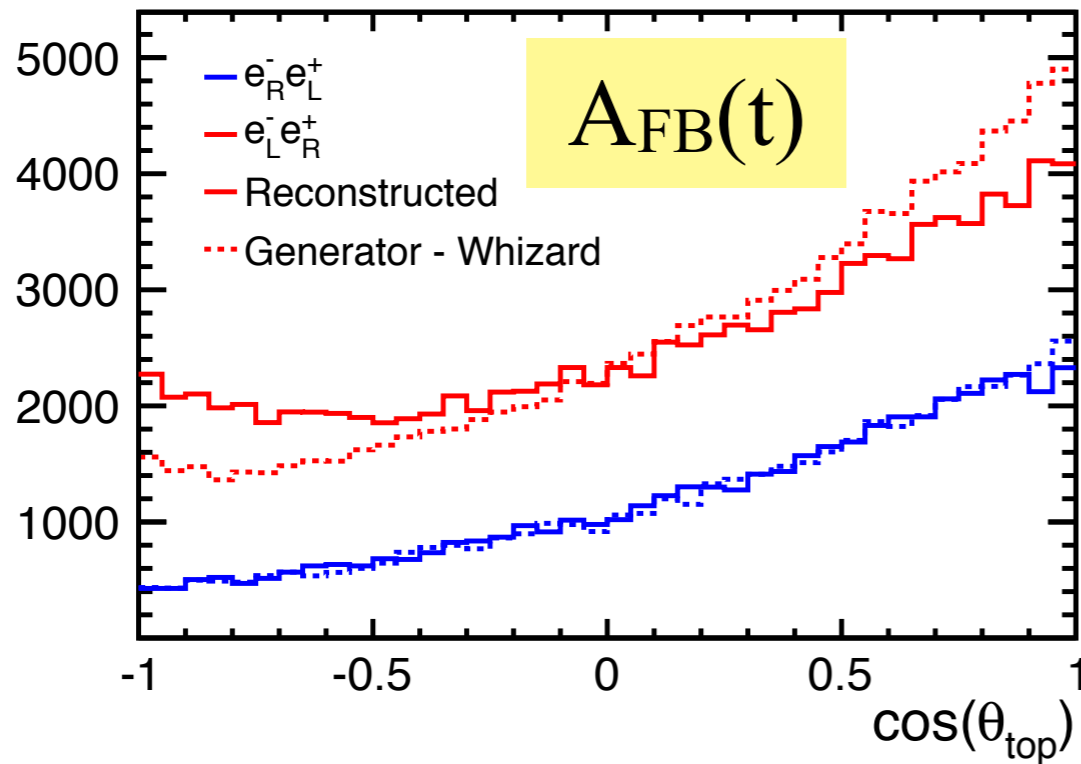


CMS, *PRL* 110, 172002 (2013)

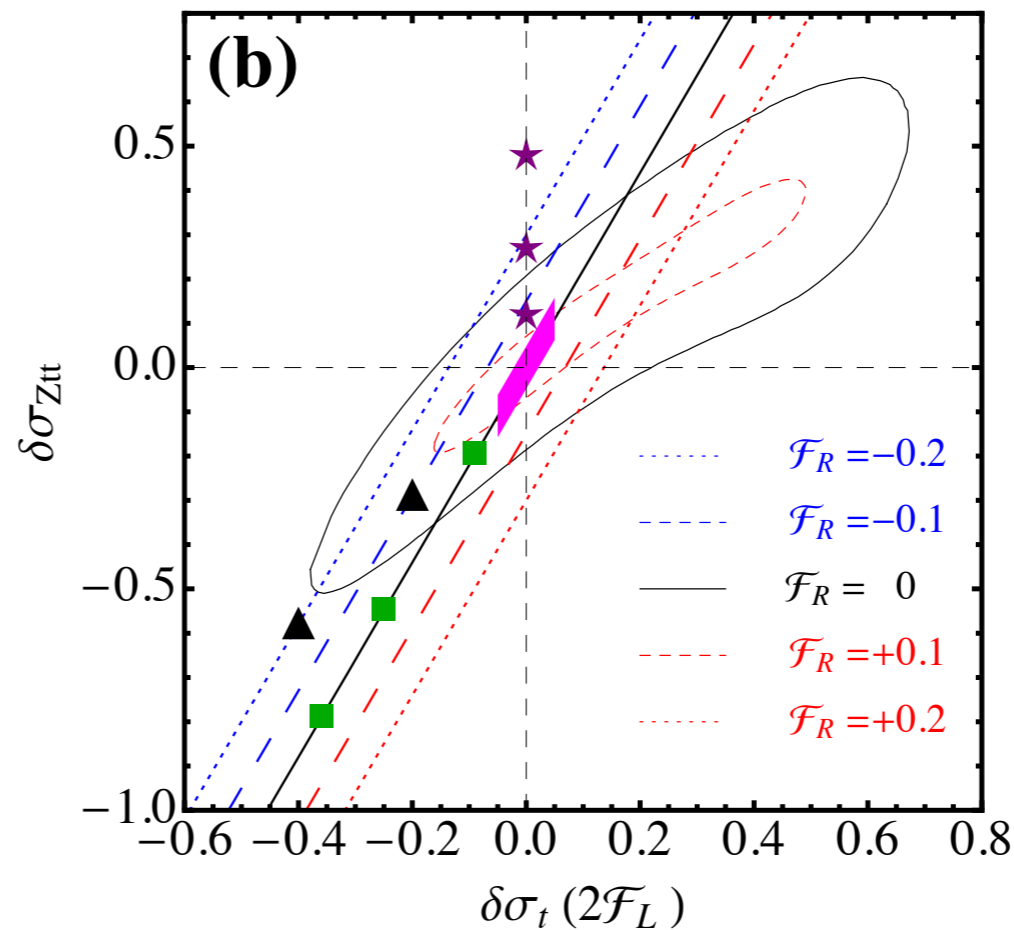
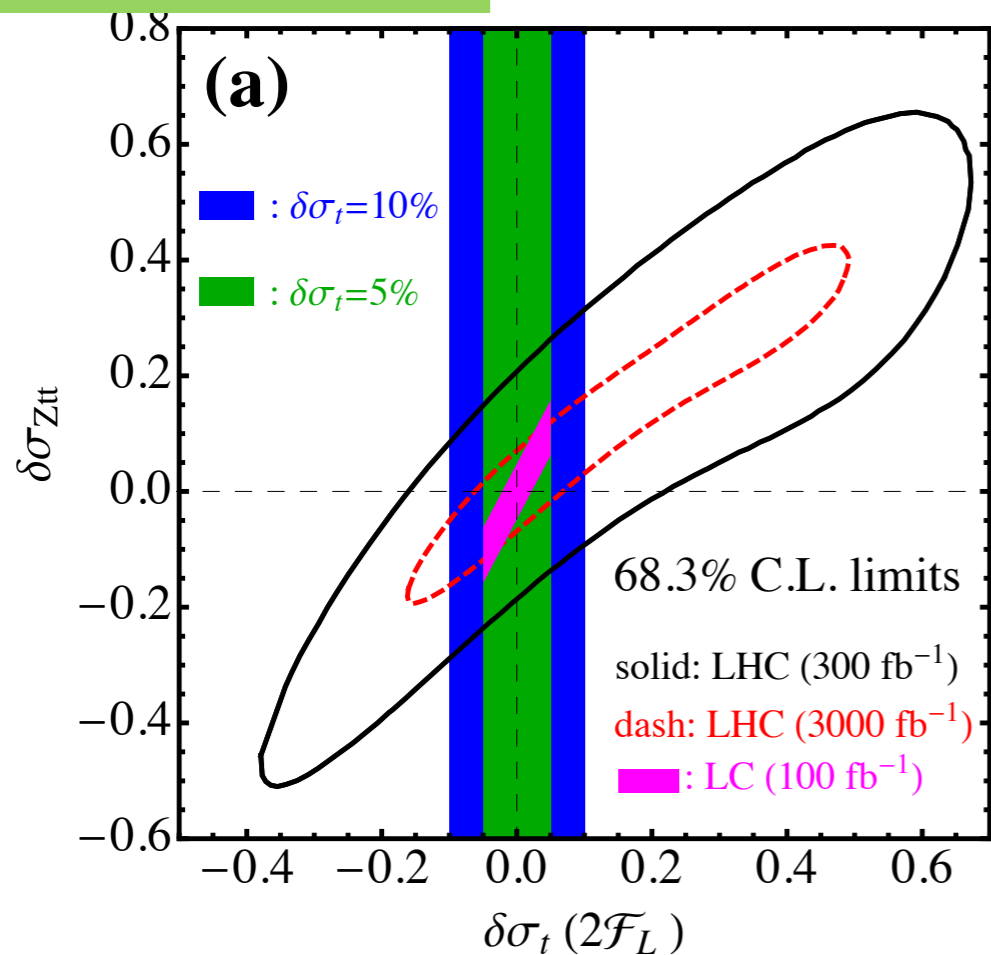
Energy Frontier



500GeV ILC, 250 fb⁻¹



LHC 14TeV

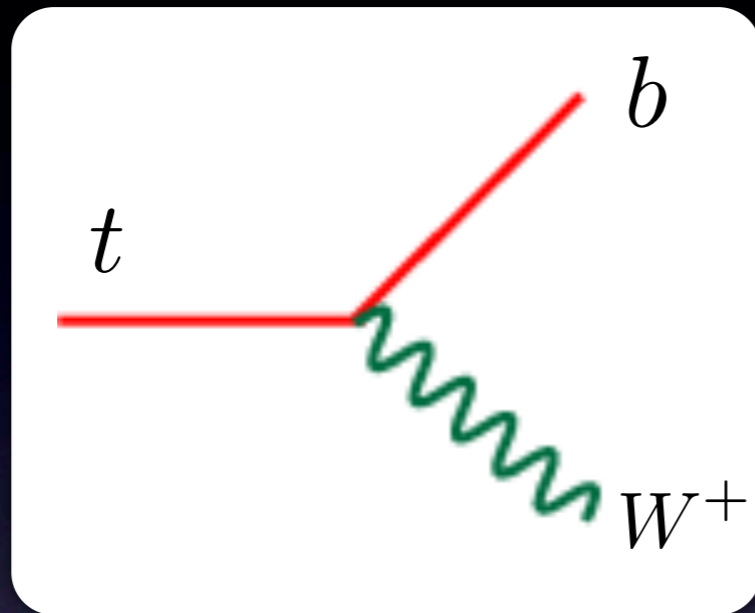


- : left-handed t-prime
- ★ : right-handed t-prime
- ▲ : chiral 4th generation

Berger, QHC, Low, 0907.2191

W-t-b Coupling

Have we measured Wtb coupling already? No!



$$i \frac{g}{\sqrt{2}} V_{tb} \gamma^\mu P_L$$

V_{tb} measurement from Top-quark decay

$$R = \frac{\text{Br}(t \rightarrow Wb)}{\text{Br}(t \rightarrow Wq)} = \frac{|V_{tb}|^2}{\sum_q |V_{tq}|^2} = |V_{tb}|^2$$

Unitarity Assumption

How can one measure V_{tb} without assuming CKM unitarity (three generations) or the SM electroweak coupling?

Boosted Physics

New kinematics at a 100 TeV machine

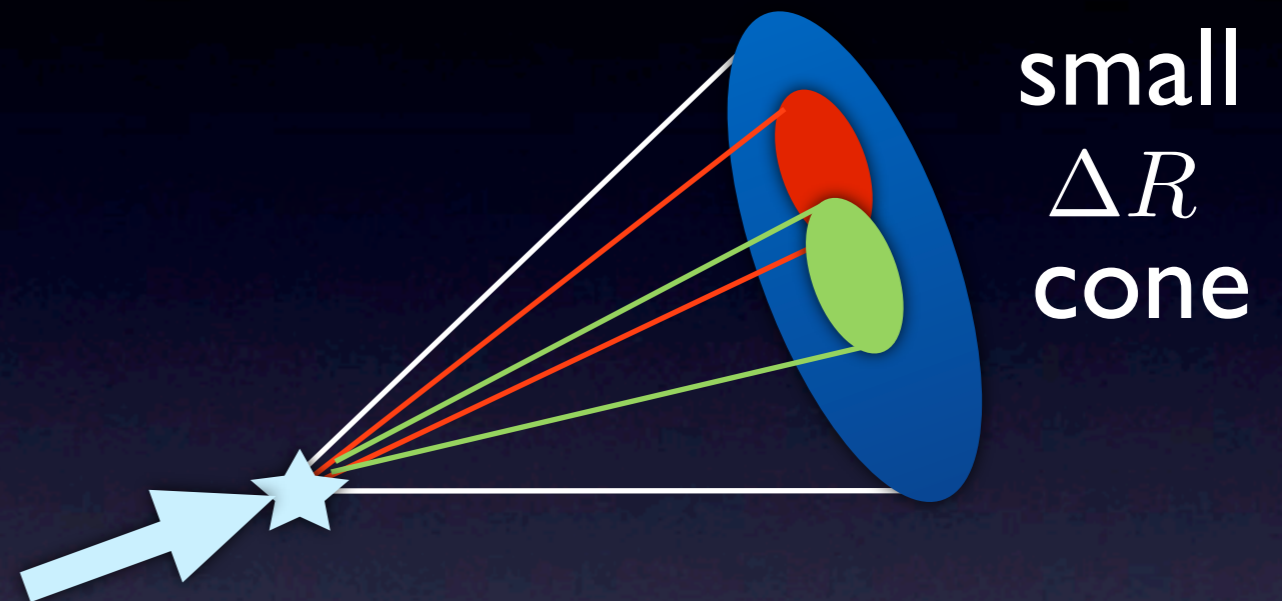
Boosted Physics

New physics often occurs in the tail of high PT region.

T-prime, B-prime

W-prime, Z-prime

Heavy scalar



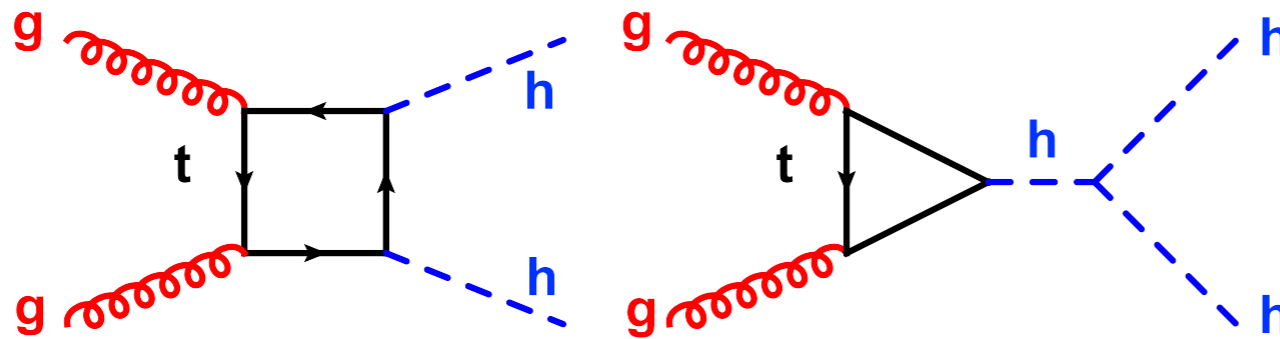
SM processes in large invariant mass range are bootcamp for all boost techniques

Higgs-boson pair production

Vector-boson pair production

Higgs Self-coupling Measurement

$$V(H) = \frac{1}{2}M_H^2 H^2 + \lambda_{HHH}vH^3 + \frac{1}{4}\lambda_{HHHH}H^4$$



Li Lin Yang

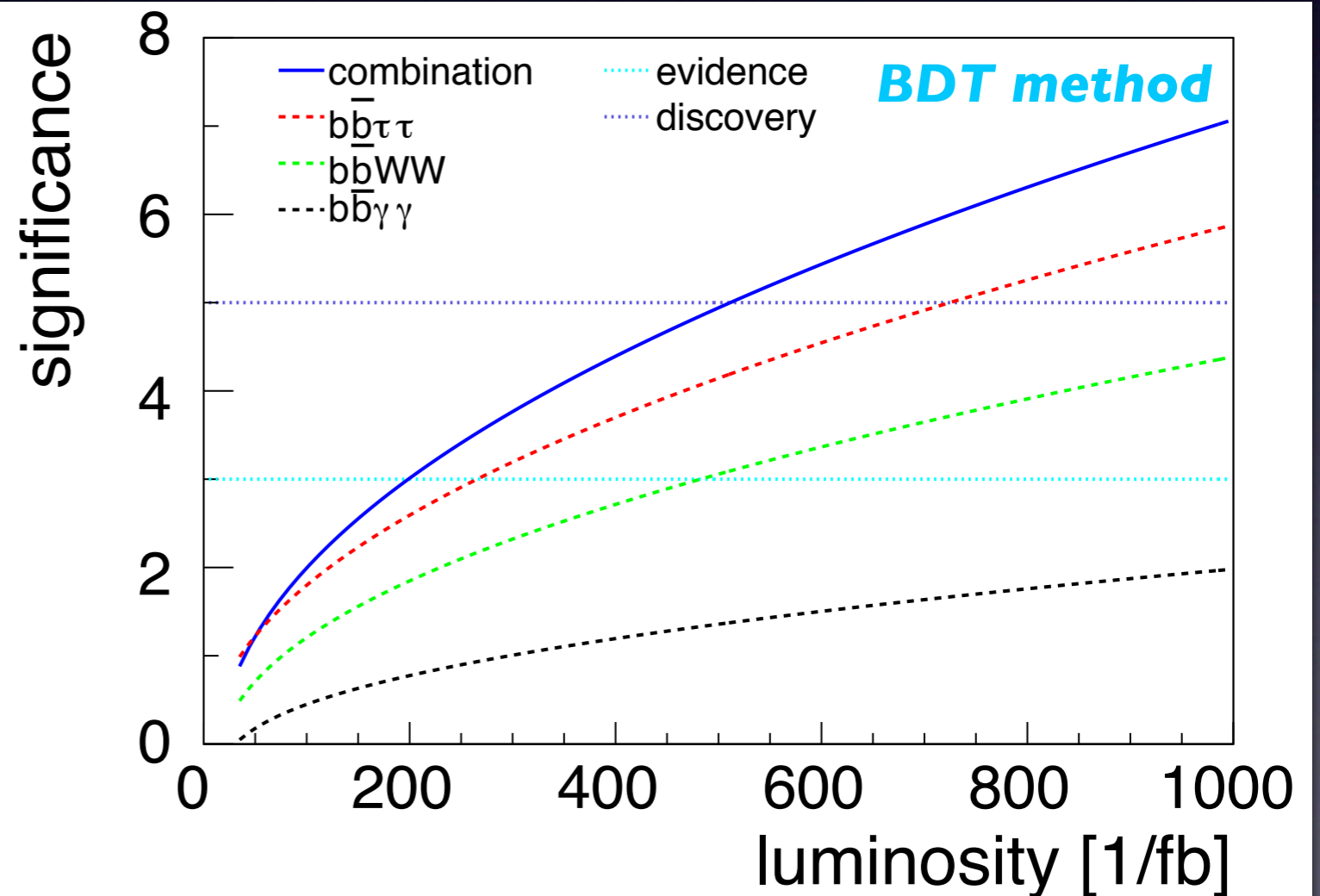
$$p_T^H \geq 200 \text{ GeV}$$

Signal X-section

\sqrt{s} [TeV]	14	33	50	100
σ_{NLO} [fb]	33.9	208	446	1419
σ_{NNLO} [fb]	41.1	249	530	1672

Signal vs Background

14TeV	S (600 fb ⁻¹)	B (600 fb ⁻¹)
$b\bar{b}\tau^+\tau^-$	50	104
$b\bar{b}W^+W^-$	11.2	7.4
$b\bar{b}\gamma\gamma$	6	12.5

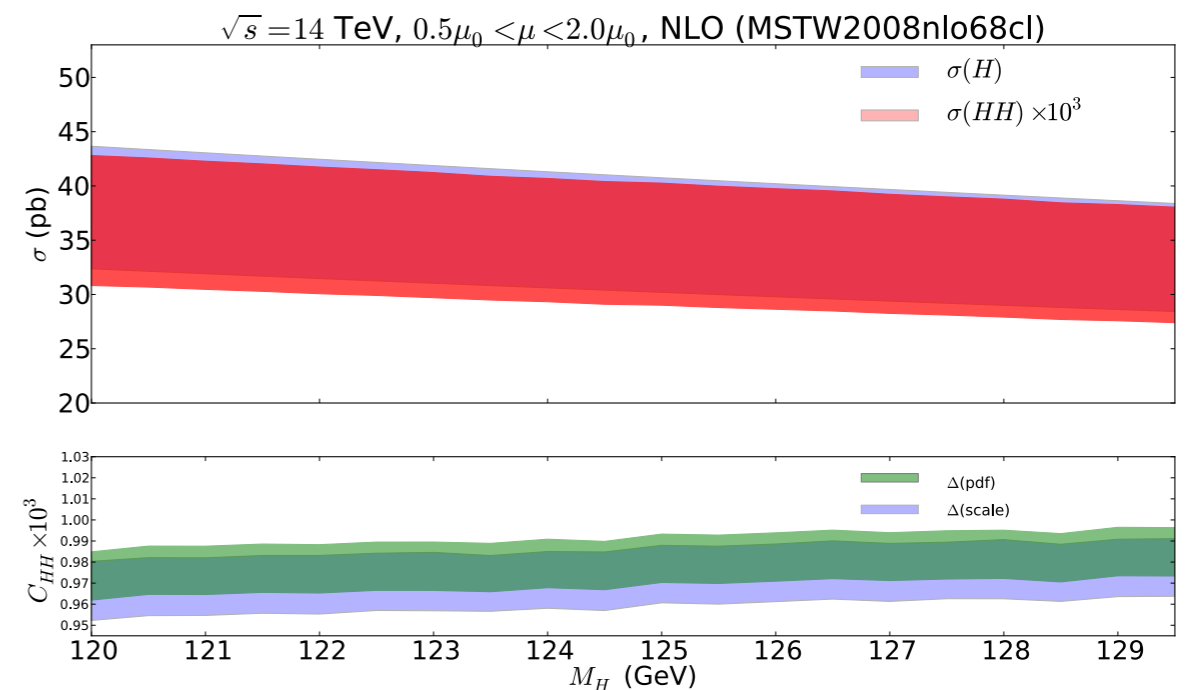
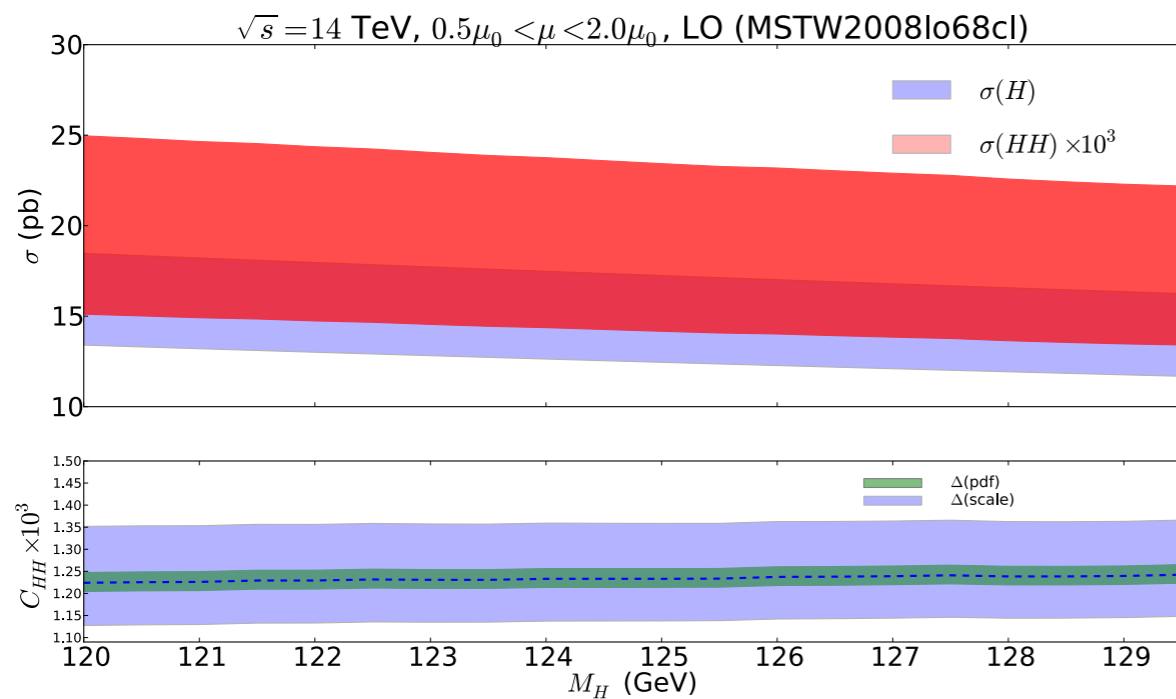


Higgs Self-coupling

Li Lin Yang

$$C_{HH} = \frac{\sigma(pp \rightarrow HH)}{\sigma(pp \rightarrow H)}$$

$\frac{2}{1}$ method



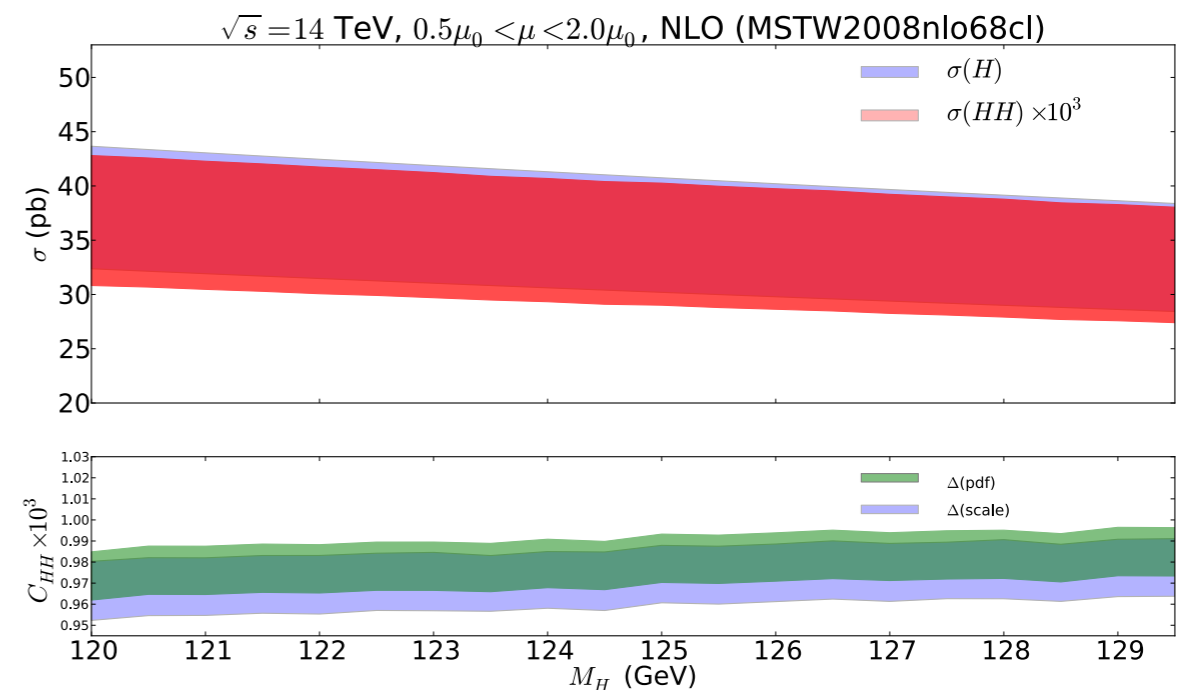
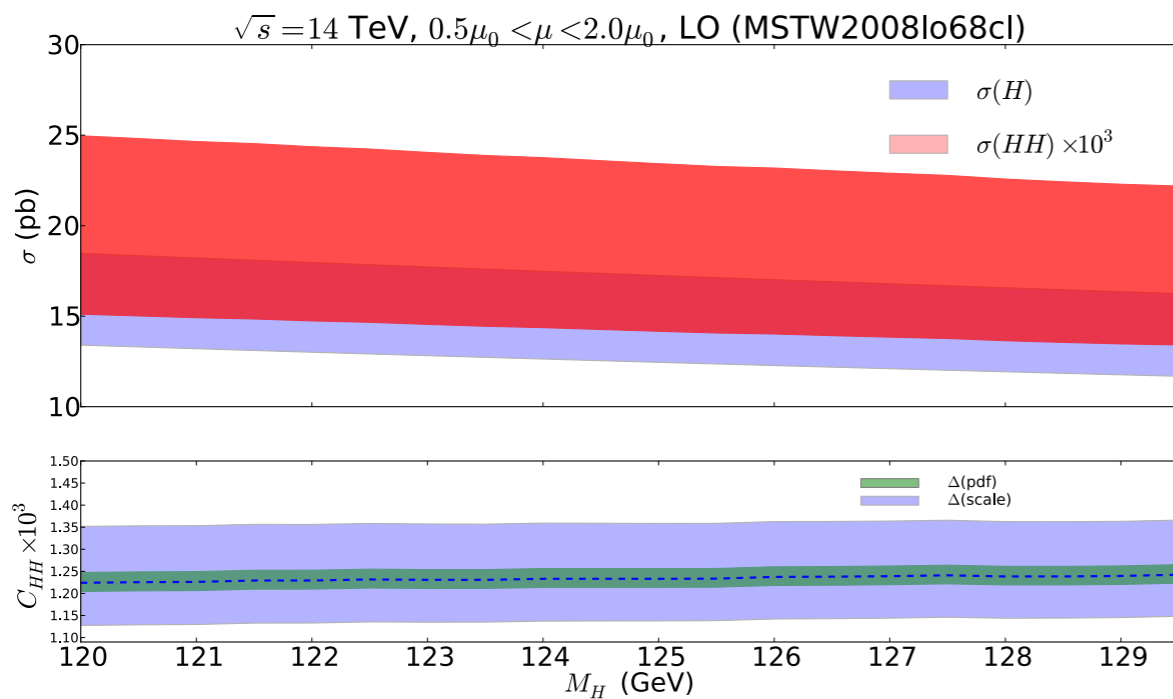
Channel	S/B (600 fb^{-1})	$\Delta C_{HH}/C_{HH}$ (600 fb^{-1})	$\Delta C_{HH}/C_{HH}$ (3000 fb^{-1})
$b\bar{b}\tau^+\tau^-$	50/104	0.400	0.279
$b\bar{b}W^+W^-$	11.2/7.4	0.513	0.314
$b\bar{b}\gamma\gamma$	6/12.5	0.964	0.490

Higgs Self-coupling

Li Lin Yang

$$C_{HH} = \frac{\sigma(pp \rightarrow HH)}{\sigma(pp \rightarrow H)}$$

$\frac{2}{1}$ method



14TeV $y_t = y_t^{\text{SM}}$

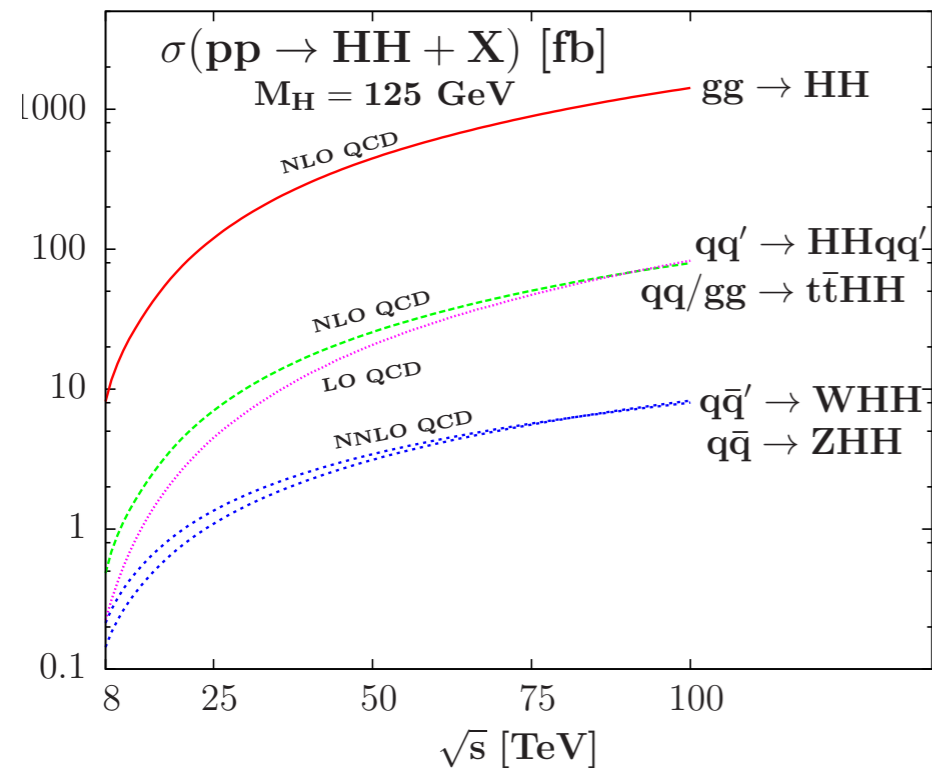
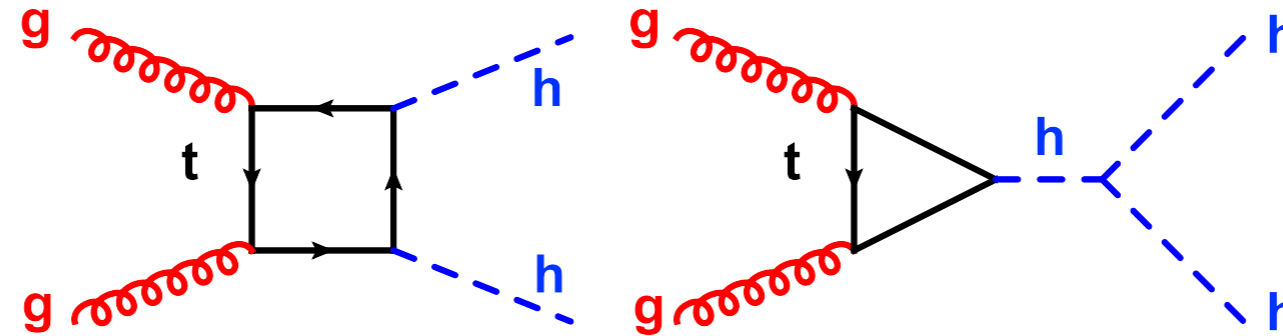
Channel	600 fb ⁻¹ (2 σ)	600 fb ⁻¹ (1 σ)	3000 fb ⁻¹ (2 σ)	3000 fb ⁻¹ (1 σ)
$b\bar{b}\tau^+\tau^-$	(0.22, 4.70)	(0.57, 1.64)	(0.42, 2.13)	(0.69, 1.40)
$b\bar{b}W^+W^-$	(0.04, 4.88)	(0.46, 1.95)	(0.36, 4.56)	(0.65, 1.46)
$b\bar{b}\gamma\gamma$	(-0.56, 5.48)	(0.09, 4.83)	(0.08, 4.84)	(0.48, 1.87)

To achieve same sensitivity

L/3.4 (50TeV)
L/5.8 (100TeV)

Higgs Self-coupling

$$V(H) = \frac{1}{2}M_H^2 H^2 + \lambda_{HHH}vH^3 + \frac{1}{4}\lambda_{HHHH}H^4$$



E_{cm}	8 TeV	14 TeV	33 TeV	100 TeV
σ_{NNLO}	9.76 fb	40.2 fb	243 fb	1638 fb
Scale [%]	+9.0 - 9.8	+8.0 - 8.7	+7.0 - 7.4	+5.9 - 5.8
PDF [%]	+6.0 - 6.1	+4.0 - 4.0	+2.5 - 2.6	+2.3 - 2.6
PDF + α_s [%]	+9.3 - 8.8	+7.2 - 7.1	+6.0 - 6.0	+5.8 - 6.0

Daniel de Florian, Javier Mazzitelli
1309.6594

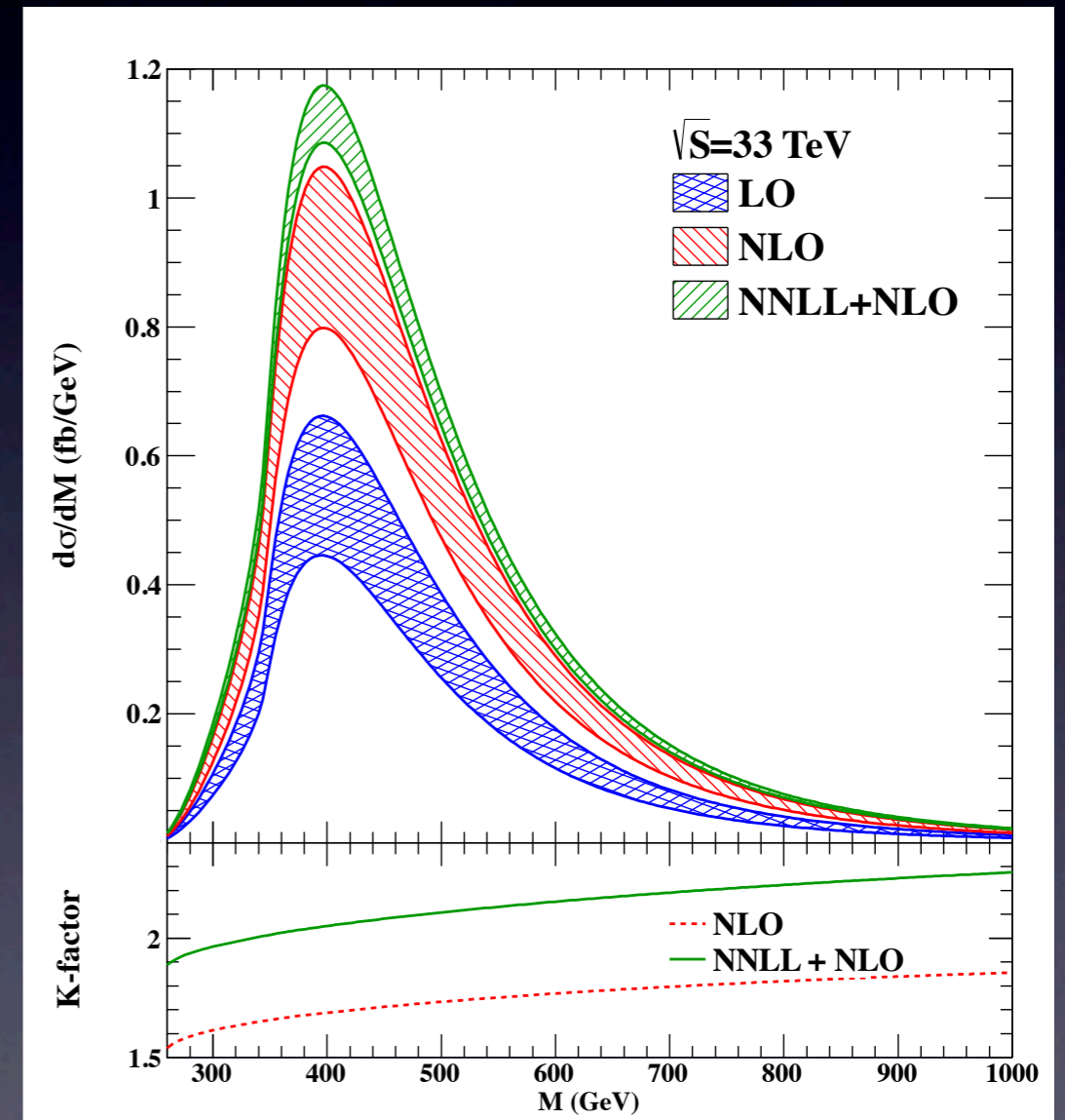
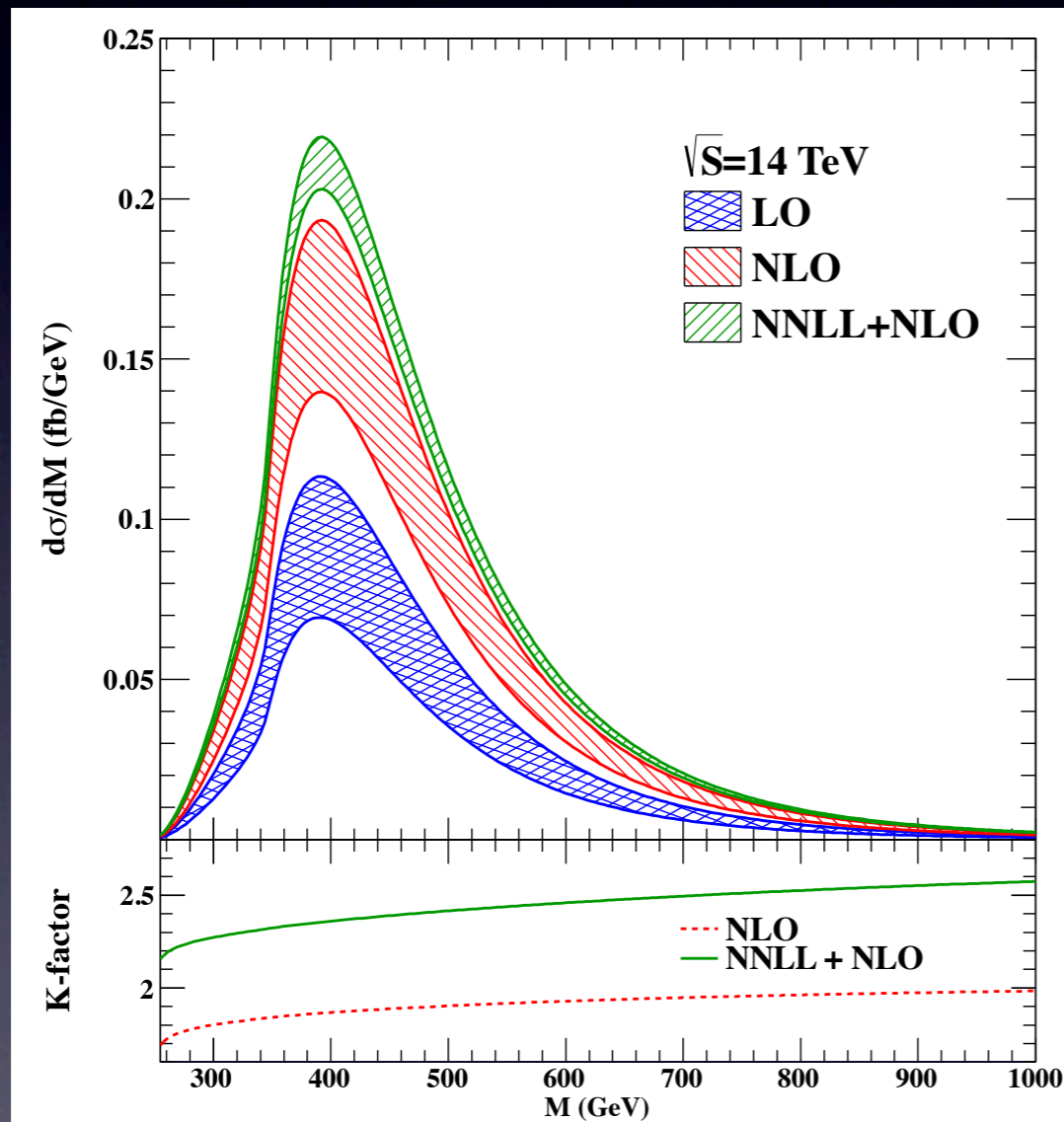
Baglio, Djouadi et al,
1212.5581

Higgs Self-coupling

Threshold resummation effects at the NNLL

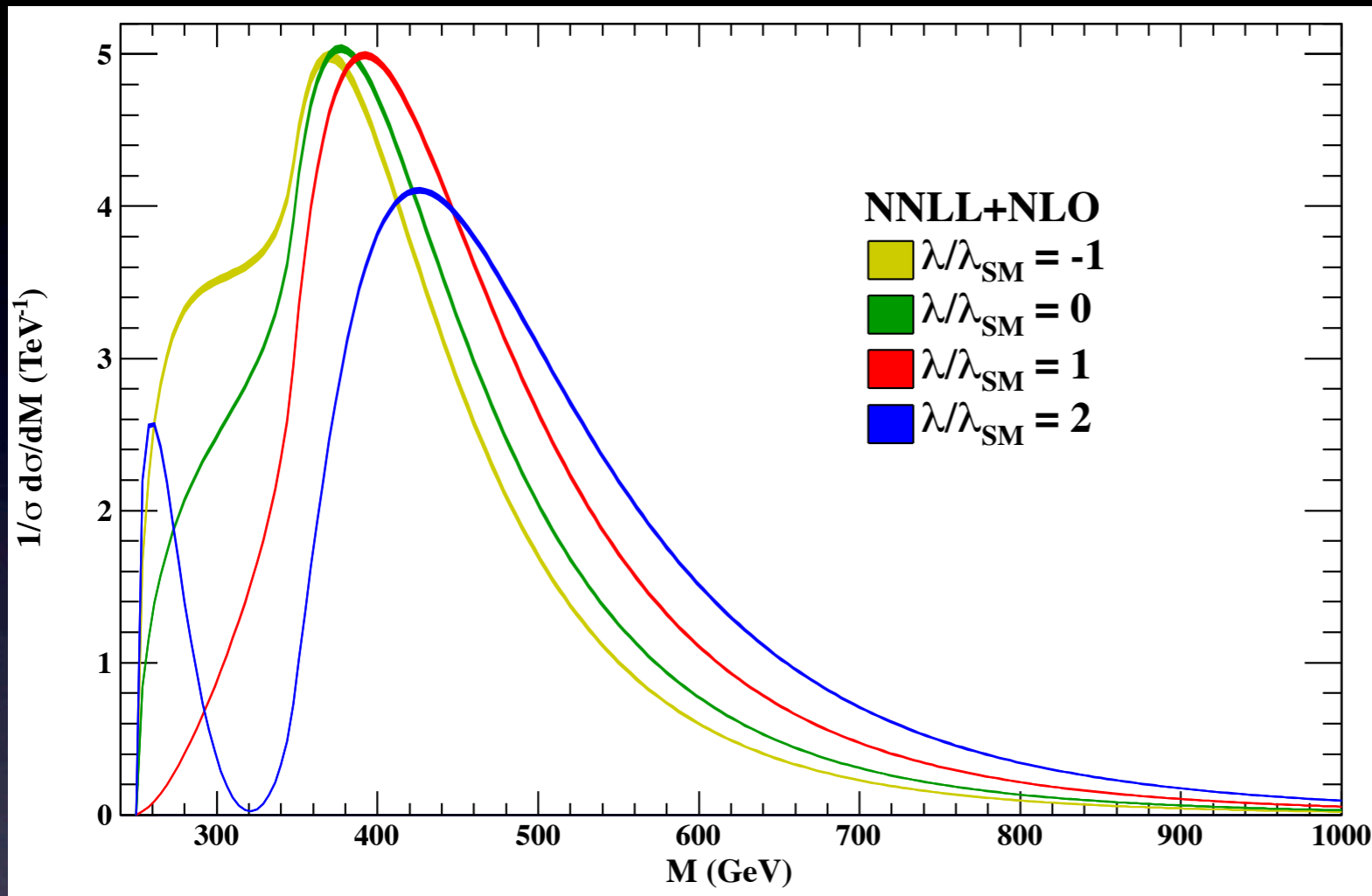
Ding Yu Shao, Chong Sheng Li, Hai Tao Li, Jian Wang, JHEP07(2013)169

Also see 1401.1101

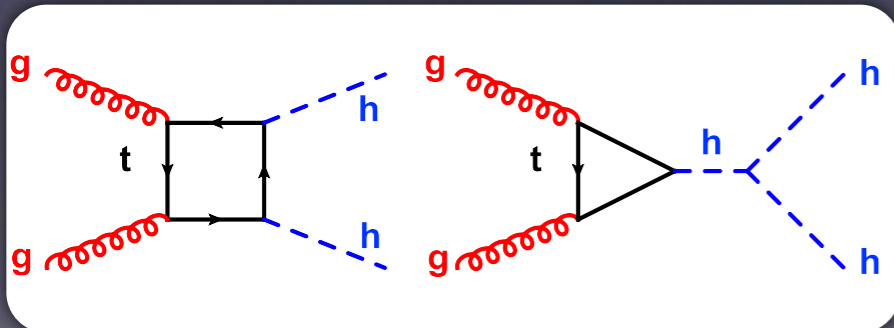


Scale Error $\sim 8\%$, PDF + alphas Error $\sim 10\%$

Invariant Mass of Higgs-Boson Pair



$$\mathcal{L}_{\text{eff}} = \frac{\alpha_s(\mu^2)}{12\pi v} C_t(\mu^2) G_{\mu\nu}^a G^{a\ \mu\nu} h - \frac{\alpha_s(\mu^2)}{24\pi v^2} C_t(\mu^2) G_{\mu\nu}^a G^{a\ \mu\nu} h^2$$

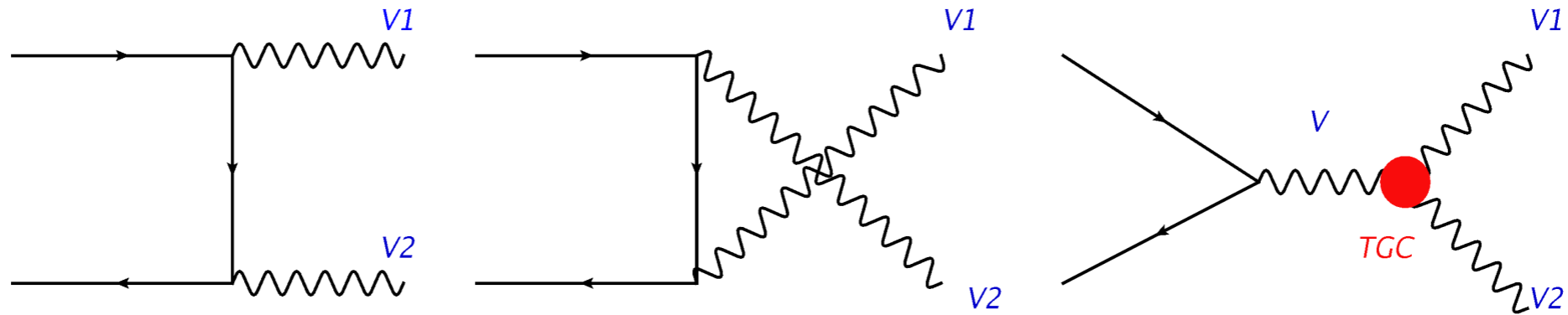


$\lambda/\lambda_{\text{SM}}$	NLO [fb]	$\sqrt{S} = 14 \text{ TeV}$ NLO + NNLL [fb]	K-factor
-1	$127.9^{+23.1+8.7 (+3.8)}_{-18.8-7.7 (-3.3)}$	$161.6^{+9.8+12.0 (+6.0)}_{-3.1-11.4 (-4.9)}$	1.26
0	$71.1^{+12.8+4.8 (+2.1)}_{-10.5-4.3 (-1.8)}$	$90.0^{+5.4+6.8 (+3.3)}_{-1.7-6.4 (-2.8)}$	1.27
1	$33.9^{+6.1+2.3 (+1.0)}_{-5.0-2.0 (-0.9)}$	$42.9^{+2.6+3.3 (+1.6)}_{-0.8-3.1 (-1.3)}$	1.27
2	$16.1^{+2.9+1.1 (+0.5)}_{-2.4-1.0 (-0.4)}$	$20.4^{+1.2+1.6 (+0.8)}_{-0.4-1.5 (-0.7)}$	1.27

Quartic Gauge Coupling and Triple Gauge Coupling

(Important for testing the SM)

Triple Gauge Coupling



	ZWW	AWW	HWW	HZZ	HZA	HAA	WWWW	ZZWW	ZAWW	AAWW
\mathcal{O}_{WWW}	X	X					X	X	X	X
\mathcal{O}_W	X	X	X	X	X		X	X	X	
\mathcal{O}_B	X	X		X	X					
$\mathcal{O}_{\Phi d}$			X	X						
$\mathcal{O}_{\Phi W}$			X	X	X	X				
$\mathcal{O}_{\Phi B}$				X	X	X				
$\mathcal{O}_{\tilde{W}WW}$	X	X					X	X	X	X
$\mathcal{O}_{\tilde{W}}$	X	X	X	X	X					
$\mathcal{O}_{\tilde{W}W}$			X	X	X	X				
$\mathcal{O}_{\tilde{B}B}$				X	X	X				

$$\mathcal{O}_{WWW} = \text{Tr}[W_{\mu\nu}W^{\nu\rho}W_{\rho}^{\mu}]$$

$$\mathcal{O}_W = (D_{\mu}\Phi)^{\dagger}W^{\mu\nu}(D_{\nu}\Phi)$$

$$\mathcal{O}_B = (D_{\mu}\Phi)^{\dagger}B^{\mu\nu}(D_{\nu}\Phi),$$

$$\mathcal{O}_{\Phi d} = \partial_{\mu}(\Phi^{\dagger}\Phi)\partial^{\mu}(\Phi^{\dagger}\Phi)$$

$$\mathcal{O}_{\Phi W} = (\Phi^{\dagger}\Phi)\text{Tr}[W^{\mu\nu}W_{\mu\nu}]$$

$$\mathcal{O}_{\Phi B} = (\Phi^{\dagger}\Phi)B^{\mu\nu}B_{\mu\nu}$$

$$\mathcal{O}_{\tilde{W}WW} = \text{Tr}[\tilde{W}_{\mu\nu}W^{\nu\rho}W_{\rho}^{\mu}]$$

$$\mathcal{O}_{\tilde{W}} = (D_{\mu}\Phi)^{\dagger}\tilde{W}^{\mu\nu}(D_{\nu}\Phi)$$

$$\mathcal{O}_{\tilde{W}W} = \Phi^{\dagger}\tilde{W}_{\mu\nu}W^{\mu\nu}\Phi$$

$$\mathcal{O}_{\tilde{B}B} = \Phi^{\dagger}\tilde{B}_{\mu\nu}B^{\mu\nu}\Phi$$

Snowmass
EW
1310.6708

Quartic Gauge Coupling

Important for testing the SM

	WWWW	WWZZ	ZZZZ	WWAZ	WWAA	ZZZA	ZZAA	ZAAA	AAAA
$\mathcal{O}_{S,0}, \mathcal{O}_{S,1}$	X	X	X						
$\mathcal{O}_{M,0}, \mathcal{O}_{M,1}, \mathcal{O}_{M,6}, \mathcal{O}_{M,7}$	X	X	X	X	X	X	X		
$\mathcal{O}_{M,2}, \mathcal{O}_{M,3}, \mathcal{O}_{M,4}, \mathcal{O}_{M,5}$		X	X	X	X	X	X		
$\mathcal{O}_{T,0}, \mathcal{O}_{T,1}, \mathcal{O}_{T,2}$	X	X	X	X	X	X	X	X	X
$\mathcal{O}_{T,5}, \mathcal{O}_{T,6}, \mathcal{O}_{T,7}$		X	X	X	X	X	X	X	X
$\mathcal{O}_{T,8}, \mathcal{O}_{T,9}$			X			X	X	X	X

$$\mathcal{O}_{T,0} = \text{Tr} [W_{\mu\nu} W^{\mu\nu}] \times \text{Tr} [W_{\alpha\beta} W^{\alpha\beta}] ,$$

$$\mathcal{O}_{T,1} = \text{Tr} [W_{\alpha\nu} W^{\mu\beta}] \times \text{Tr} [W_{\mu\beta} W^{\alpha\nu}] ,$$

$$\mathcal{O}_{T,2} = \text{Tr} [W_{\alpha\mu} W^{\mu\beta}] \times \text{Tr} [W_{\beta\nu} W^{\nu\alpha}] ,$$

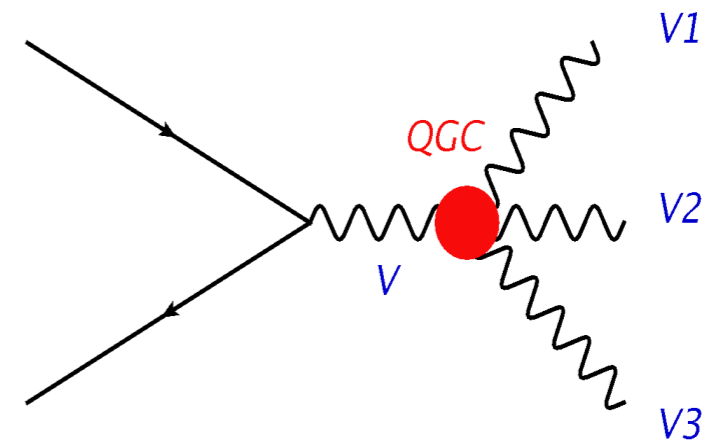
$$\mathcal{O}_{T,5} = \text{Tr} [W_{\mu\nu} W^{\mu\nu}] \times B_{\alpha\beta} B^{\alpha\beta} ,$$

$$\mathcal{O}_{T,6} = \text{Tr} [W_{\alpha\nu} W^{\mu\beta}] \times B_{\mu\beta} B^{\alpha\nu} ,$$

$$\mathcal{O}_{T,7} = \text{Tr} [W_{\alpha\mu} W^{\mu\beta}] \times B_{\beta\nu} B^{\nu\alpha} ,$$

$$\mathcal{O}_{T,8} = B_{\mu\nu} B^{\mu\nu} B_{\alpha\beta} B^{\alpha\beta}$$

$$\mathcal{O}_{T,9} = B_{\alpha\mu} B^{\mu\beta} B_{\beta\nu} B^{\nu\alpha} .$$



Snowmass
EW
1310.6708

Rare Decays

Top-Quark Rare Decay

expectations from theory

Process	SM	2HDM(FV)	2HDM(FC)	MSSM	RPV	RS
$t \rightarrow Zu$	7×10^{-17}	-	-	$\leq 10^{-7}$	$\leq 10^{-6}$	-
$t \rightarrow Zc$	1×10^{-14}	$\leq 10^{-6}$	$\leq 10^{-10}$	$\leq 10^{-7}$	$\leq 10^{-6}$	$\leq 10^{-5}$
$t \rightarrow gu$	4×10^{-14}	-	-	$\leq 10^{-7}$	$\leq 10^{-6}$	-
$t \rightarrow gc$	5×10^{-12}	$\leq 10^{-4}$	$\leq 10^{-8}$	$\leq 10^{-7}$	$\leq 10^{-6}$	$\leq 10^{-10}$
$t \rightarrow \gamma u$	4×10^{-16}	-	-	$\leq 10^{-8}$	$\leq 10^{-9}$	-
$t \rightarrow \gamma c$	5×10^{-14}	$\leq 10^{-7}$	$\leq 10^{-9}$	$\leq 10^{-8}$	$\leq 10^{-9}$	$\leq 10^{-9}$
$t \rightarrow hu$	2×10^{-17}	6×10^{-6}	-	$\leq 10^{-5}$	$\leq 10^{-9}$	-
$t \rightarrow hc$	3×10^{-15}	2×10^{-3}	$\leq 10^{-5}$	$\leq 10^{-5}$	$\leq 10^{-9}$	$\leq 10^{-4}$

current limits

Process	Br Limit	Search	Dataset	Reference
$t \rightarrow Zq$	7×10^{-4}	CMS $t\bar{t} \rightarrow Wb + Zq \rightarrow \ell\nu b + \ell\ell q$	19.5 fb ⁻¹ , 8 TeV	[130]
$t \rightarrow Zq$	7.3×10^{-3}	ATLAS $t\bar{t} \rightarrow Wb + Zq \rightarrow \ell\nu b + \ell\ell q$	2.1 fb ⁻¹ , 7 TeV	[137]
$t \rightarrow gu$	3.1×10^{-5}	ATLAS $qg \rightarrow t \rightarrow Wb$	14.2 fb ⁻¹ , 8 TeV	[131]
$t \rightarrow gc$	1.6×10^{-4}	ATLAS $qg \rightarrow t \rightarrow Wb$	14.2 fb ⁻¹ , 8 TeV	[131]
$t \rightarrow \gamma u$	6.4×10^{-3}	ZEUS $e^\pm p \rightarrow (t \text{ or } \bar{t}) + X$	474 pb ⁻¹ , 300 GeV	[134]
$t \rightarrow \gamma q$	3.2×10^{-2}	CDF $t\bar{t} \rightarrow Wb + \gamma q$	110 pb ⁻¹ , 1.8 TeV	[132]
$t \rightarrow hq$	8.3×10^{-3}	ATLAS $t\bar{t} \rightarrow Wb + hq \rightarrow \ell\nu b + \gamma\ell q$	20 fb ⁻¹ , 8 TeV	[135]
$t \rightarrow hq$	2.7×10^{-2}	CMS* $t\bar{t} \rightarrow Wb + hq \rightarrow \ell\nu b + \ell\ell qX$	5 fb ⁻¹ , 7 TeV	[136]
$t \rightarrow \text{invis.}$	9×10^{-2}	CDF $t\bar{t} \rightarrow Wb$	1.9 fb ⁻¹ , 1.96 TeV	[133]

Process	Br Limit	Search	Dataset	Reference
$t \rightarrow Zq$	2.2×10^{-4}	ATLAS $t\bar{t} \rightarrow Wb + Zq \rightarrow \ell\nu b + \ell\ell q$	300 fb ⁻¹ , 14 TeV	[140]
$t \rightarrow Zq$	7×10^{-5}	ATLAS $t\bar{t} \rightarrow Wb + Zq \rightarrow \ell\nu b + \ell\ell q$	3000 fb ⁻¹ , 14 TeV	[140]
$t \rightarrow Zq$	$5 (2) \times 10^{-4}$	ILC single top, $\gamma_\mu (\sigma_{\mu\nu})$	500 fb ⁻¹ , 250 GeV	Extrap.
$t \rightarrow Zq$	$1.5 (1.1) \times 10^{-4(-5)}$	ILC single top, $\gamma_\mu (\sigma_{\mu\nu})$	500 fb ⁻¹ , 500 GeV	[141]
$t \rightarrow Zq$	$1.6 (1.7) \times 10^{-3}$	ILC $t\bar{t}$, $\gamma_\mu (\sigma_{\mu\nu})$	500 fb ⁻¹ , 500 GeV	[141]
$t \rightarrow \gamma q$	8×10^{-5}	ATLAS $t\bar{t} \rightarrow Wb + \gamma q$	300 fb ⁻¹ , 14 TeV	[140]
$t \rightarrow \gamma q$	2.5×10^{-5}	ATLAS $t\bar{t} \rightarrow Wb + \gamma q$	3000 fb ⁻¹ , 14 TeV	[140]
$t \rightarrow \gamma q$	6×10^{-5}	ILC single top	500 fb ⁻¹ , 250 GeV	Extrap.
$t \rightarrow \gamma q$	6.4×10^{-6}	ILC single top	500 fb ⁻¹ , 500 GeV	[141]
$t \rightarrow \gamma q$	1.0×10^{-4}	ILC $t\bar{t}$	500 fb ⁻¹ , 500 GeV	[141]
$t \rightarrow gu$	4×10^{-6}	ATLAS $qg \rightarrow t \rightarrow Wb$	300 fb ⁻¹ , 14 TeV	Extrap.
$t \rightarrow gu$	1×10^{-6}	ATLAS $qg \rightarrow t \rightarrow Wb$	3000 fb ⁻¹ , 14 TeV	Extrap.
$t \rightarrow gc$	1×10^{-5}	ATLAS $qg \rightarrow t \rightarrow Wb$	300 fb ⁻¹ , 14 TeV	Extrap.
$t \rightarrow gc$	4×10^{-6}	ATLAS $qg \rightarrow t \rightarrow Wb$	3000 fb ⁻¹ , 14 TeV	Extrap.
$t \rightarrow hq$	2×10^{-3}	LHC $t\bar{t} \rightarrow Wb + hq \rightarrow \ell\nu b + \ell\ell qX$	300 fb ⁻¹ , 14 TeV	Extrap.
$t \rightarrow hq$	5×10^{-4}	LHC $t\bar{t} \rightarrow Wb + hq \rightarrow \ell\nu b + \ell\ell qX$	3000 fb ⁻¹ , 14 TeV	Extrap.
$t \rightarrow hq$	5×10^{-4}	LHC $t\bar{t} \rightarrow Wb + hq \rightarrow \ell\nu b + \gamma\ell q$	300 fb ⁻¹ , 14 TeV	Extrap.
$t \rightarrow hq$	2×10^{-4}	LHC $t\bar{t} \rightarrow Wb + hq \rightarrow \ell\nu b + \gamma\ell q$	3000 fb ⁻¹ , 14 TeV	Extrap.

extrapolations

$t \rightarrow Zq, \gamma q, Zc$

so many possibilities for the large integrated lumi and clean environment of FCCee

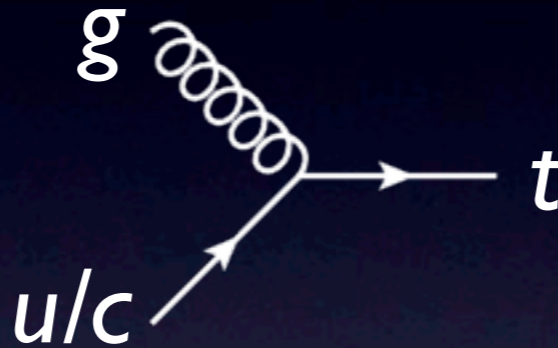
Top-Rare-decay and Direct Top-Production

- Anomalous g-q-t FCNC coupling

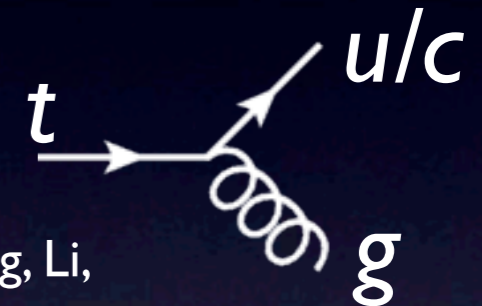
$$\mathcal{L} = g_s \sum_{q=u,c} \frac{\kappa_{tqg}}{\Lambda} \bar{t} \sigma^{\mu\nu} T^a (f_q^L P_L + f_q^R P_R) q G_{\mu\nu}^a + h.c.$$

- ★ NLO $K_F \sim 1.3-1.5$
- ★ promising at the LHC

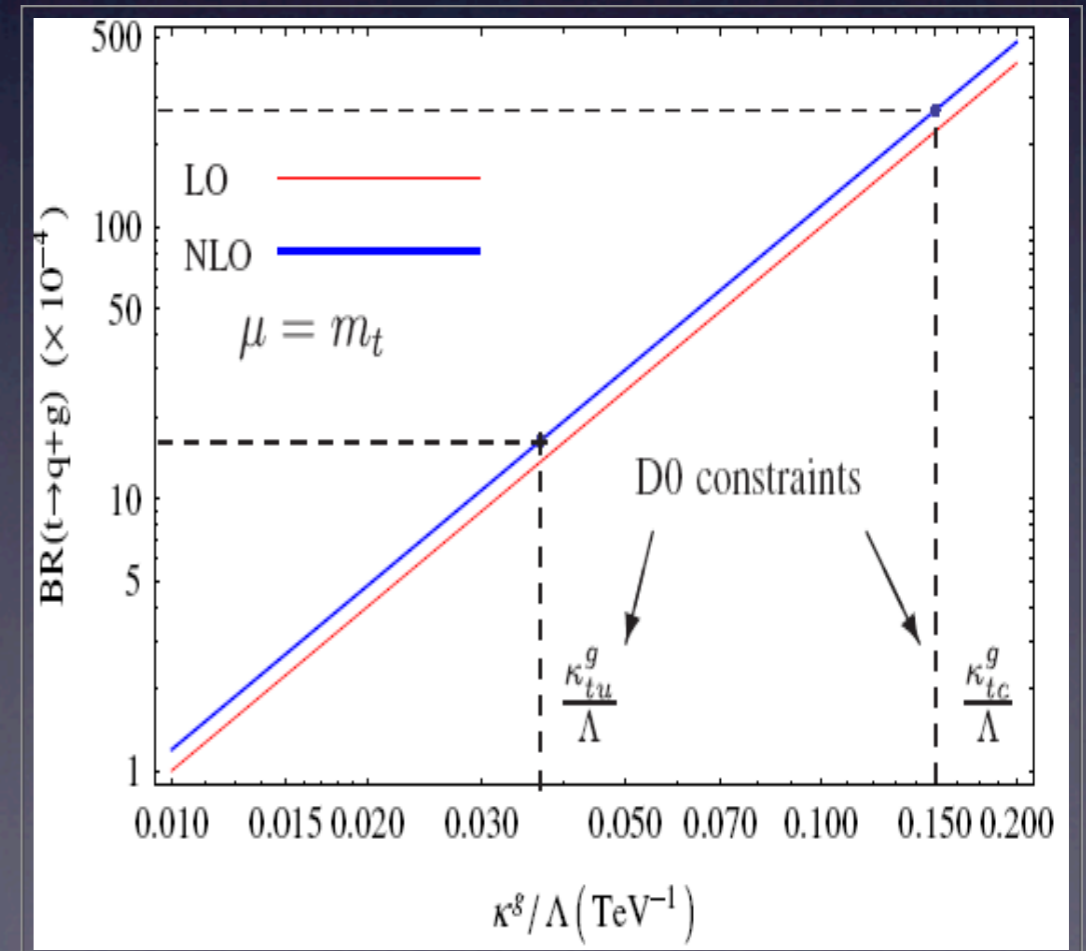
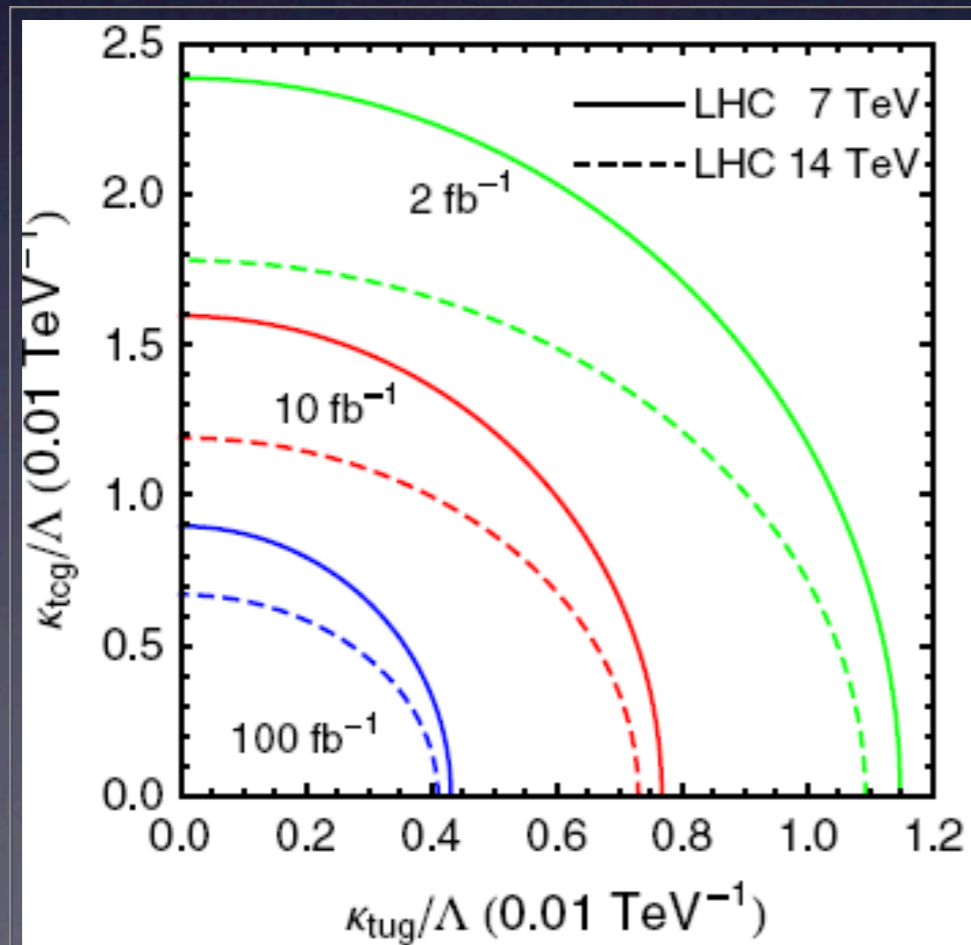
Gao, C. S. Li, Yang, Zhang,
PRL 107 (2011) 092002



- ★ NLO $K_F \sim 1.2$



Zhang, C. S. Li, Gao, Zhang, Li,
PRL 102 (2009) 072001



Summary

Untested Aspects of the SM

Higgs electroweak couplings

SM Higgs?

Higgs boson self-coupling

Boosted object techniques

Triple-gauge-coupling / Quartic-gauge-coupling

Dim-6 and Dim-8 operators in linear realization

Weak interaction of the 3rd generation quarks

Fully understanding top- and bottom-quark
chirality structure of couplings, $V_{tb}=1?$...