SUSY Searches at Collider Experiments

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(Julius Wess and Bruno Zumino, 1974)



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Outline



- SUSY Introduction
- The LHC and ATLAS
- SUSY search strategy
 - ··· Coffee Break ···
- Overview of SUSY search results
- Outlook









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SM and Beyond





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François Englert

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Photo: G-M Greuel via Wikimedia Commons Peter W. Higgs

- □ Higgs boson observed, SM fits the experimental data very well → big success in EW scale
- □ While has problem in Planck scale:
 - naturalness and "hierarchy" problem
 - Unification of gauge coupling
 - Dark Matter

□ Need a more fundamental theory of which SM is only a low-energy approximation → New Physics

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New Physics beyond the SM



SUSY Introduction



- A symmetry which unified fermions (mater) and bosons (forces)
- A more fundamental theory: compatible with SM in EW scale, solve most problems in Planck scale
- Good candidate for Dark Matter

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SUSY Introduction

Solve hierarchy problem without "fine tuning"

 SUSY contributions to Higgs mass cancel SM contributions

Unification of gauge couplings

 New particle content changes running of couplings

Provide Dark Matter candidate

 Lightest SUSY particle (LSP) can be stable and only weekly interacting

Some of the arguments are most convincing for SUSY particles at ~TeV scale



Dark Matter寻找与SUSY寻找的关系

- 只要dark matter不仅仅是引力相互作用现象,它都 将可能在LHC实验中表现为large missing Et 现象
- R宇称守恒SUSY寻找包括了各种large missing Et 的topology.
- 因此,即使SUSY理论不一定正确,但是dark matter的large missing Et 信号一定会在SUSY寻 找中显示。

→超对称粒子的寻找不仅对寻找超对称粒子本身有重要意义,也对寻找暗物质实验证据具有重要意义

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大型强子对撞机(LHC) 位于欧洲核子研究中心(CERN)

Large Hadron Collider



•LHGb

ATLAS and CMS detector @ LHC

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ATLAS and CMS: two multi-purpose detectors @LHC

A Toroidal LHC ApparatuS

- 42m×22m, 7000 ton
- Solenoid + Toroidal magnet (2T)

- Fine granularity liquid Ar/Tile calorimeters

Large Hadron Collider (LHC):

- Proton-Proton synchrotron
- World's highest and largest collider

ATLAS

Compact Muon Spectrometer

- 21m×15m, 125000 ton
- All silicon trackers, 4T solenoid magnet
- PbWO4+Tile calorimeters 11

ATLAS and CMS



Collisions at LHC



Detector requirements

- Excellent position and momentum resolution in central tracker
 - b-jets, taus
- Excellent ECAL performance
 - electrons, photons
 - good granularity (energy and position
- Good HCAL performance



- jets, Etmiss (neutrinos, SUSY stable LSP, etc)
- good granularity (energy and position measurements)
- good η coverage (hermeticity for Etmiss measurements)

Excellent muon identification and momentum resolution

- from "combined" muons in external spectrometer + central tracker _{iSTEP 2014}

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SUSY Signature

Conserved R parity (originally introduced for stability of proton, R=+1 for SM, -1 for SUSY)

 $R = (-1)^{3(B-L)+2S}$

- SUSY particles produced/annihilated in pairs
- Lightest SUSY particle (LSP) stable (DM candidate)
- Typical signature: jets/leptons + MET (key signature: large MET)



Minimal Supersymmetric Standard Model

Standard Model Particles and Fields		Supersymmetric Partners			
		Interaction Eigenstates		Mass Eigenstates	
Symbol	Name	Symbol	Name	Symbol	Name
q = u, d, c, s, t, b	quark	$\widetilde{q}_{\scriptscriptstyle L}, \widetilde{q}_{\scriptscriptstyle R}$	squark	$\widetilde{q}_1, \widetilde{q}_2$	squark
$l = e, \mu, \tau$	lepton	$\widetilde{l}_R, \widetilde{l}_L$	slepton	$\widetilde{l_1}, \widetilde{l_2}$	slepton
$l = v_e, v_\mu, v_\tau$	neutrino	$\widetilde{\mathbf{v}}$	sneutrino	\widetilde{v}	sneutrino
g	gluon	\widetilde{g}	gluino	\widetilde{g}	gluino
W^{\pm}	W-boson	\widetilde{W}^{\pm}	wino	\sim +	
H_u^+, H_d^-	charged Higgs boson	$\widetilde{H}_{u}^{+},\widetilde{H}_{d}^{-}$	charged higgsino	$\chi_{1,2}^{\perp}$	chargino
В	B-field	\widetilde{B}	bino		
W^0	W ⁰ -field	\widetilde{W}^{0}	wino	$\widetilde{\chi}^{0}_{1,2,3,4}$	neutralino
H_u^0, H_d^0	neutral Higgs boson	$\widetilde{H}^0_u, \widetilde{H}^0_d$	neutral higgsino		

Reconstructed Objects

- Photons: no track but energy in el-m (and not in the hadronic) calorimeter
- Electrons: track and energy in el-m (and not in the hadronic) calorimeter
- Muons: track in inner tracker and muon chamber
- Jets: cluster in hadronic calorimeter



MET: Missing Transverse Energy

- At the LHC an unknown proportion of the energy of the colliding protons escapes down the beam-pipe
- Invisible particles (neutrinos, neutralinos?) are created their momentum can be constrained in the plane transverse to the beam direction

 $\boldsymbol{E}_T^{\mathrm{miss}} = -\sum \boldsymbol{p}_T(i)$



Why do we need SUSY models?

- Different masses different phase space different search region – different final state particles to search for...
- We need some model for signal region definition and optimization ...
- If we don't see anything, we (the experimentalists) also like to set limits, and limits can only be set on certain models...

SUSY models: good sale in market

□ Simplified Models:

- Not really a model (Br~100%, most masses fixed at high scales)
- Important tool for interpretation
- □ Phenomenological MSSM:
 - 19 free parameters
 - ✓ M1,M2,M3
 - ✓ tan β, μ and m_A
 - ✓ 10 sfermion mass parameters
 - $\checkmark \quad A_t, A_b \text{ and } A_{\scriptscriptstyle T}$
 - pMSSM captures "most" of phenomenologic features of R-parity conserving MSSM
 - Comprehensive and computationally realistic approximation of the MSSM with neutralino LSP

SUSY Search Strategy

SUSY search strategy: search for deviation from SM

SUSY sensitive variables: Try to establish excess of events in some sensitive kinematic distribution



- SM background: the discovery of new physics can only be claimed when SM backgrounds are understood well or under control
 - Background estimation should better be estimated from data (use <u>Data-Driven Method</u>) because of imperfect knowledge of underlying event, parton showering, parton distribution functions, limited MC statistics ...

SUSY Sensitive Variables



SM Background

- SM bkgs: multi-jets, top, bosons (W,Z), dibosons (WW,WZ,ZZ), tribosons, Higgs
 - SM bgs understood very well
- **B**G estimation strategy:
 - Dominant systematics: datadriven method
 - sub-dominant BG: MC estimation

SM "backgrounds"- the big picture



Data-Driven-Method (ABCD method)

One approach to data-driven bg **estimation** is to use uncorrelated model-independent variables to *extrapolate* the background from a background-dominated control region A to the signal region D.



Data-Driven-Method (Replacement Method)

- Many other DDM, while based on ABCD method: e.g. replacement method, Matrix Method, simultaneously fit method ...
- **D** one example: $Z \rightarrow vv$ estimated from $Z \rightarrow \mu\mu$ (replacement method)
 - A method to get a control sample:
 - Seed Sample: reconstructed Z \rightarrow ee or Z \rightarrow µµ events
 - Replacement: replace charged leptons by neutrinos (E_T^{miss} is estimated by p_T^(Z))
 - Apply corrections for lepton efficiency (from data) and acceptance (from MC)
 - Derive $Z \rightarrow \vee \vee$ MET distribution (shape from Zmm, TF from low MET region)



Data-Driven-Method (others)



$$\text{QCD BG} = \frac{1}{1/\epsilon_{\text{fake}} - 1/\epsilon_{\text{real}}} \cdot N_{\text{fail}} - \frac{1/\epsilon_{\text{real}} - 1}{1/\epsilon_{\text{fake}} - 1/\epsilon_{\text{real}}} \cdot N_{\text{pass}}$$

- *N*_{pass}: Events passing the signal selection cuts (*tight*)
 - N_{fail}: Events satisfying relaxed lepton isolation criteria but not passing the signal selection cuts (*loose-but-not-tight*)

 ϵ_{real} : Probability that a loose non-QCD event passes also the tight selection cuts

Loose

Ereal

Tight

 ϵ_{fake} : Probability that a loose QCD event passes also the tight selection cuts

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→… Coffee Break … ←

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SUSY Searches @ LHC



SUSY Searches @ LHC



Since 2010, ATLAS&CMS have invested huge efforts in SUSY search @LHC : Great Luminosity recorded



Analysis Procedure

Pre-selection: select good objects (e, mu, tau, jet, ...), apply trigger depending on analysis, remove bad events (bad runs, not from pp collisions, in transition region ...)

□ SR definition and optimization

- Define signal regions based on decay topologies occurring in generic models
- Set final cut on discriminating variables (e.g. M_{eff}) to optimize sensitivity to reference models with appropriate mass scale
- □ SM Background estimations (data-driven + MC)
- Compare SM predictions with data
- □ If no excess, interpret results in different SUSY models

Signal Grids

E.g.: >=2tau + MET (direct gaugino/stau production)



3tau + MET

2tau + MET



- Final states: >= 2tau + MET (e.x.: C1N2)
- Only consider tau decay hadronically (e, mu vetoed)
- Results published in <u>arXiv:1407.0350</u>
- Assuming selectron and smuon are heavy, only stau is light, which is sensitive for light stau model



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N_τ

 τ/ν_{τ}

 $\tau/
u_{\tau}$

- Final states: >=2tau +MET
- Trigger: di-tau trigger (only select interested events with at least 2 taus)
- At least **2 OS taus** (e, mu veto $\frac{4}{2}$ 10⁹
- bjet veto (Nbjet =0)
 - suppress top, cover signal events with ISR jet



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- Z-veto: suppress Z+jets BGs
- MET>40 GeV: suppress QCD/Z
- MT2>100 GeV: further suppress all SM BGs and enhance SUSY sensitivity





Background Composition



- Dominant Background: multi-jet, W+jets and diboson
- multi-jet BG: ABCD data-driven method
- Others: MC prediction

Fake tau BG estimation: ABCD method

- Two weak correlated Variables:
 - X-axis: TaulD
 - Y-axis: mT2
- Signal Region
 - SR D
- Baseline Control Regions
 - QCD+W CR-A/B/C
 - TF obtained from QCD event (low mT2 region from Data): <u>TF=C/B</u>
 - Extrapolation performed from <u>A</u> to <u>D through TF</u>
- Validation Region (W VR-EF)



ABCD method check:

Correlation between TaulD and mT2





No strong correlation between TauID and Mt2.

The residual correlation is estimated as systematic uncertainty using validation region E,F.



In fake tau BG CR, QCD purity is high.

Non-fake tau BGs in CR has been subtracted using MC and taken into account as syst.

Fake Tau BGs Estimation: Results

■ D = A * T (T=C/B)



		region A	region B	region C	$\mathcal{T} = C/B$	multi-jet in SR
	Data	6	36907	24601		
	Z+jets	0.3 ± 0.15	726 ± 261	3981 ± 1060		
	W+jets	1.0 ± 0.4	252 ± 82	587 ± 182		
SR-	diboson	0.5 ± 0.26	14.6 ± 4.8	72±20	0.554	2.3
C1N2	top	0.1 ± 0.06	17.3 ± 6.1	68.0 ± 22.3	± 0.031	± 1.4
	multi-jet	4.1 ± 2.5	35897 ± 334	19893 ± 1087		
	Ref. Point 1	1.9 ± 0.85	1.4 ± 0.7	17.8 ± 6.2		

ABCD method validation





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m, [GeV]



Theory syst. Systematics from ABCD method: Fake tau BG (multi-jet BG) systematics

Systematic Source Correlation Non-multi-jet subtraction in Region A Non-multi-jet subtraction in Region B Non-multi-jet subtraction in Region C Number of events in Region A Number of events in Regions C and B

experimental syst.

Systematics from MC prediction PDF other theory uncer. down other theory uncer. up lumi TESDOWN TESUP TEVSFDOWN TEVSFDOWN TEVSFUP TEVSFDOWN TEVSFUP TEVSFDOWN TEVSFUP

TFAKESFUP TIDSFDOWN TIDSFUP TTRIGSFDOWN TTRIGSFUP BJETDOWN BJETUP CJETDOWN CJETUP MistagDOWN MistagUP PILEUPDOWN PILEUPUP JERR JESM JESP MET_RESOST MET_SCALESTDOWN MET_SCALESTUP

Results

 ≥ 2 OS taus b-jet veto Z-veto

 $E_{\rm T}^{\rm miss} > 40 {
m ~GeV}$

 $m_{\mathrm{T2}} > 100~\mathrm{GeV}$

SR-C1N2

 0.9 ± 0.5

 2.2 ± 0.8

 2.2 ± 0.9

 2.3 ± 2.0

 7.9 ± 2.4

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 11.3 ± 2.8

 9.2 ± 2.1

 0.8 ± 0.5

SR-C1N2

Diboson Top quarks SM process $(m_{\tilde{\gamma}^0}, m_{\tilde{\gamma}^0}) = (250, 100) \text{ GeV}$ $(m_{\chi^{\pm}}^{2}, m_{\chi^{0}}) = (250, 50) \text{ GeV}$ 0.30 ± 0.19 Top $(m_{\tilde{\tau}}, m_{\tilde{\tau}^0}) = (127, 0) \text{ GeV}$ Z+jetsW+jetsATLAS Diboson $\sqrt{s} = 8 \text{ TeV}, 20.3 \text{ fb}^{-1}$ Multi-jet SM total Observed Ref. point 1 Ref. point 2 Ref. point 3 No significant excess...



iet l	imit	

Exclusion Limits: simplified model $\int_{1}^{p} \sqrt{\frac{\chi^{2}}{2}}$



 $\frac{\nu_{\tau}/\tau}{\tau/\nu_{\tau}}$

 $ilde{\chi}_1^0$

 $\frac{\tau/\nu_{\tau}}{\tau/\nu_{\tau}}$

 $\tilde{\tau}/\tilde{\nu}_{\tau}$ $\tilde{\tau}/\tilde{\nu}_{\tau}$

X2

p

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 High energy running in 2015 will significantly increase our sensitivity to many SUSY scenarios, especially cover difficult SUSY regions

Ready for new physics !!!





SUSY Search at HL-LHC

- Limits set by Run-1 LHC: $m_{\tilde{q}} < 0.7$ TeV, $m_{\tilde{g}} < 1.3$ TeV
- Less stringent limits on sleptons, 3rd generation squark, weak gauginos
 - → Accessible at HL-LHC



mT2 Optimization



Discovery and exclusion

 P-value=probability that result is as/less compatible with the hypothesis

DISCOVERY:

- The <u>null hypothesis</u> H₀ describes <u>background only</u>
 - If the *p*-value of H₀ is found below a given threshold, one can consider looking for a better model
 - In HEP, $Z \ge 5$ is conventionally required to claim a discovery
- The alternative hypothesis H₁ describes signal + background
 - The alternative hypothesis is supposed to fit the data very well for claiming a discovery

EXCLUSION:

- The <u>null hypothesis</u> H₀ describes <u>signal + background</u>
 - One is interested into setting an upper limit to the intensity of the signal alone
- The alternative hypothesis H₁ describes background only
 - No real need to test for it
 - The background-only model becomes important only in case of discovery

Simultaneous fit II

- Input: Probability density function (Signal and background are described by a binned PDF in CRs, SRs and VRs -- technically it is implemented by a collection of histograms).
 - The number of observed events (described using a Poisson)
 - The ttbar and W(Z)+jets backgrounds: MC prediction
 - →samples of all fit regions are scaled by "free parameters" mu_wz/ mu_top (un-constrained scaling factors) to get an overall normalization.
 - The QCD multi-jet background estimate: data-driven prediction
 - \rightarrow only allowed to vary within its uncertainties in the fit.
 - Smaller backgrounds as single top, dibosons and ttbar+vector boson: MC prediction.
 - \rightarrow only allowed to vary within uncertainties.
 - Signal samples of fit regions are scaled by <u>"free parameter"</u> <u>mu_SIG</u>.
 - Statistical and systematic uncertainties are included as nuisance parameters, typically constrained by a Gaussian. Correlations between the systematics are considered.
- The product of the various PDF forms the likelihood.
- The fit maximizes the likelihood by adjusting parameters → the optimal value/error of the free parameters and nuisance parameters are determined simultaneously when the PDF is fitted to Data.

背景联合拟合

技术主旨:本底在背景区域具有较高的统计量。通过联合拟合背景区域CR与信号区域SR,有效提高信号区域中本底估计的可信度。该技术被SUSY各个分析广泛使用。

■ 具体方案:优化似然函数(Profile Likelihood):

- 考虑各区域中观测值,背景估算值,误差及其关联
- 主要本底在拟合中可自由浮动
- 误差在拟合中为nuisance parameters
- 不同拟合类型:



- Background-only/仅背景拟合:在验证区域检验拟合。
- Discovery/发现拟合:与模型无关Non-SM信号强度上限。
- Exclusion/排除拟合:不同信号模型的SUSY信号排除上限。



- 扫描SUSY信号 二维参量空间
- 基于似然函数 建立test statistic, 通过 假设检验获得 CLs
- 判定信号是否 在相应置信度 被排除
 - 给出信号排除 区域图 14-8-25

Interpretation strategy: Exclusion fit

From the constructed

distribution of test statistic

** SUSY signal model contains a set of signal grid points, corresponding to different mass scale in the parameter space. Hypothesis tests are done for each grid point to draw an exclusion contour line.

Based on the number of observed, expected events in all regions with all uncertainties: **Probability density** function (PDF)

Likelihood function: $L(\mu, \theta)$ µ: signal strength (POI); θ: nuisance parameters(NP) Profile Likelihood: constrain uncertainty (NP) as part of a likelihood fit

Construct test statistics t, based on likelihood ratio A: $\frac{L(\mu, \hat{\theta}(\mu))}{L(\hat{\mu}, \hat{\theta})}$ $\hat{\mu} \ge 0$,

 $\frac{L(\mu, \hat{\theta}(\mu))}{L(\alpha, \hat{\theta}(m))}$

 $t_{\mu} = -2 \ln \lambda(\mu)$



Construct the PDF of test statistic t_{u:} generate toy Monte Carlo or using asymptotic formula



Find the observed test statistic for tested µ: t_{µ,obs}



If CLs<0.05: the value

of signal is excluded at

Minimal Supersymmetric Standard Model

Standard Model Particles and Fields		Supersymmetric Partners			
		Interaction Eigenstates		Mass Eigenstates	
Symbol	Name	Symbol	Name	Symbol	Name
q = u, d, c, s, t, b	quark	$\widetilde{q}_L, \widetilde{q}_R$	squark	$\widetilde{q}_1,\widetilde{q}_2$	squark
$l = e, \mu, \tau$	lepton	$\overline{\widetilde{l}_R},\widetilde{l}_L$	slepton	$\widetilde{l_1}, \widetilde{l_2}$	slepton
$l = v_e, v_\mu, v_\tau$	neutrino	$\widetilde{oldsymbol{ u}}$	sneutrino	\widetilde{v}	sneutrino
g	gluon	$\widetilde{\mathcal{O}}$	gluino	\widetilde{g}	gluino
W^{\pm}	W-boson	\widetilde{W}^{\pm}	wino	\sim +	
H_u^+, H_d^-	charged Higgs boson	$\widetilde{H}_{u}^{+},\widetilde{H}_{d}^{-}$	charged higgsino	$\chi_{1,2}^{\perp}$	chargino
В	B-field	\widetilde{B}	bino		
W^0	W ⁰ -field	\widetilde{W}^0	wino	$\widetilde{\chi}^{0}_{1,2,3,4}$	neutralino
H_u^0, H_d^0	neutral Higgs boson	$\widetilde{H}^0_u, \widetilde{H}^0_d$	neutral higgsino		



Inner Detector: Highly segmented silicon strips, determine very accurately charged particles trajectories

Solenoid Magnet: Solenoid coil that generates a 2T magnetic field in the region of the Inner Detector

Electromagnetic Calorimeter: Electron

and photon energies are measured through electromagnetic showers

- Hadronic Calorimeter: Hadrons interact with dense material and produce a shower of charged particles
- Toroid Magnets: 8 toroidal coils that create a 0,4T magnetic field in the area of the Muon Spectrometer
- Muon Spectrometer: Muons traverse the rest of the detector and are measured in its outer layers

Hadronic Taus



BDT score

- Tau decays:
 - Leptonic (35%): $au
 ightarrow
 u_{ au} \ell \overline{
 u}_{\ell}$
 - Hadronic (65%): decay to one or three charged pions, neutrinos and π^{0} 's
- Need to separate τ 's from hadronic jets:
 - \circ τ decay tends to be well collimated
 - $\circ~$ Large electromagnetic component from $\pi^{0} \rightarrow \gamma \gamma~{\rm decay}$

Tau Object

- ho $p_{
 m T}$ > 20 GeV, $|\eta|$ < 2.5
- \triangleright 1 or 3 tracks with total charge ± 1
- Boosted decision tree (BDT) using variables sensitive to the longitudinal and transverse shower shape
- Working points:
 - Loose: efficiency: 60%; jet rejection: 20-50

Tight: efficiency: 30-50%; jet rejection: 30-200

Data-Driven-Method (simultaneously fit)

- Background estimates in SRs are obtained by a *simultaneous fit* in each channel based on the profile likelihood method.
 - Fit for all BG-CRs
- Comments:
 - □ Shape from MC (CR), NF from fit
 - Advantage:
 - Considered correlations between different BG CRs and VRs, SRs;
 - considered correlated syst. from detector
 - □ Disadvantage: shape is depending on MC (semi-data-driven method)



$$\begin{split} \mathbf{N}_{pred_{j}}^{\mathrm{SR}} &= (\mathbf{N}_{data}^{\mathrm{CR}_{j}} - \mathbf{N}_{other\ bkg}^{\mathrm{CR}_{j}}) \times \frac{\mathbf{N}_{pred}(MC^{j}, \mathrm{SR})}{\mathbf{N}_{pred}(MC^{j}, \mathrm{CR}_{i})} \\ &= (\mathbf{N}_{data}^{\mathrm{CR}_{j}} - \mathbf{N}_{other\ bkg}^{\mathrm{CR}_{j}}) \times C_{\mathrm{CR}_{j} \to \mathrm{SR}}^{j} \end{split}$$

$$\begin{aligned} \mathbf{N}_{other\ bkg} = \mathbf{N}_{other\ bkg}^{\mathrm{CR}_{j}} + \mathbf{N}_{other\ bkg$$