

# Polarization issues and schemes for energy calibration

I.Koop  
Novosibirsk State University,  
Novosibirsk State Technical University,  
Budker Institute of Nuclear Physics,  
630090, Novosibirsk, Russia

55<sup>th</sup> ICFA Advanced Beam Dynamics Workshop on  
High Luminosity Circular e<sup>+</sup>e<sup>-</sup> Colliders – Higgs Factory  
(HF2014), 9 – 12 October 2014, Beijing

# General remarks

- Resonant depolarization is limited for the use of up to 80-100 GeV per beam
- Non-polarization methods of the energy monitoring will be presented at WG8 session by Nikolai Muchnoi and Sergey Nikitin. Polarization shall validate these approaches for the use at higher energies.
- CERN's team experience and vision will also be presented there by Mike Koratzinos

# Outline

- Physics request to polarization in FCC-ee collider
- Our approach to energy calibration
- Maintaining polarization in a booster synchrotron
- Solenoid type snakes
- Depolarization rates
- Compton scattering based polarimetry
- Conclusion

- ❑ highest possible luminosity for a wide physics program ranging from the Z pole to the  $t\bar{t}$  production threshold
  - *beam energy range from 45 GeV to 175 GeV*
- ❑ main physics programs / energies:
  - *Z (45.5 GeV): Z pole, 'TeraZ' and high precision  $M_Z$  &  $\Gamma_Z$ ,*
  - *W (80 GeV): W pair production threshold,*
  - *H (120 GeV): ZH production (maximum rate of H's),*
  - *t (175 GeV):  $t\bar{t}$  threshold*
- ❑ some polarization up to  $\geq 80$  GeV for beam energy calibration
- ❑ optimized for operation at 120 GeV?!

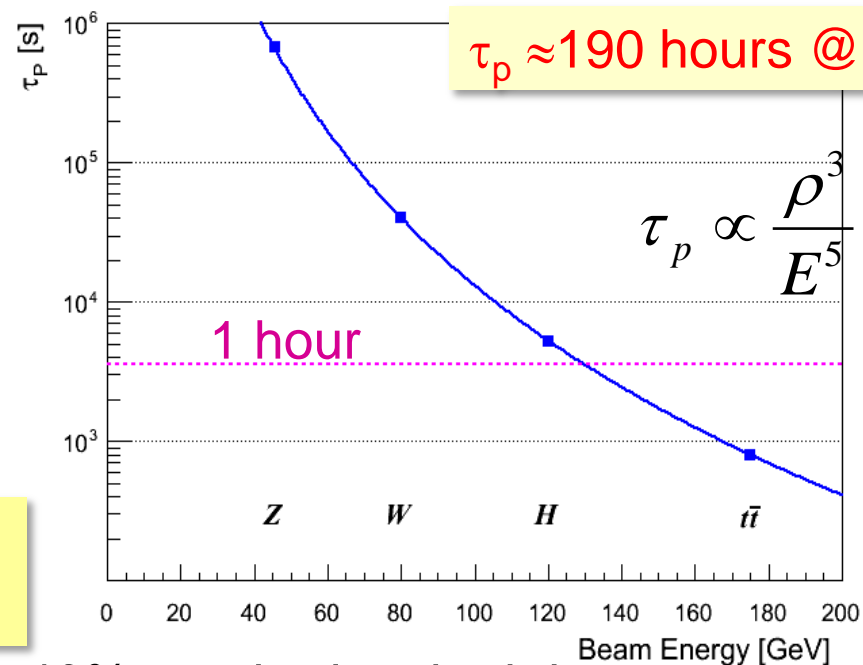
transverse polarization build-up (Sokolov-Ternov) is slow at FCC-ee (large bending radius  $\rho$ )

build-up is ~40 times slower than at LEP

wigglers may lower  $\tau_p$  to ~12 h, limited by  $\sigma_E \leq 60$  MeV and power

*due to power loss the wigglers can only be used to pre-polarize some bunches (before main injection)*

→  $\approx$  OK for energy calibration (few % P sufficient)



longitudinal polarization: levels of  $\geq 40\%$  required on both beams; excellent resonant compensation needed

*expected to be difficult, requires spin rotators or snakes, most likely only possible at lower intensity and luminosity*

SLIM, PETROS, SITF simulations being prepared

E. Gianfelice

# The proposed scenario

- **No** self-polarization in a collider - too slow with  $r=11$  km :  $\tau=190$  hours at Z
- Request for the **longitudinal polarization at Z** demands: use of a source of polarized e- and acceleration of a beam by linac (to 10-20 GeV) and then by a **synchrotron** (to 45-175 GeV)
- Preservation of a polarization in a booster ring by the use of **odd** number of **Siberian Snakes** , then spin tune is  $\nu=0.5$ .

# The proposed scenario, cont.

- Injection of a polarized beam in the collider with spins lying in the **horizontal** plane
- Measuring of **free precession** frequency using Compton backscattering of a laser light and subsequent **Fourier** analysis like in the muon  **$g-2$**
- Advantage: **determination** of the energy **every short!**
- $e^+$  self-polarization in 1-2 GeV intermediate damping ring (for energy calibration use only!)

# Polarized beam acceleration with Siberian Snakes

Derbenev, Kondratenko, 1973

$$\tau_p^{-1} = \frac{5\sqrt{3}}{8} \lambda_e r_e c \gamma^5 \left\langle \frac{1 - \frac{2}{9} (\vec{n}\vec{v})^2 + \frac{11}{18} \vec{d}^2}{|\mathbf{r}|^3} \right\rangle$$

$$\vec{d} = \gamma \frac{\partial \vec{n}}{\partial \gamma} \text{ is}$$

the spin – orbit  
coupling vector

With N spin transparent snakes:  $\langle \vec{d}^2 \rangle = \frac{\pi^2}{3} \frac{v_0^2}{N^2}$

Betatron oscillations could increase  $|d|$ !  
Spin transparency for the snake is desirable.

For  $E = 45.5 \text{ GeV}$  ( $v_0 = \gamma a = 103.28$ ),  $r = 11 \text{ km}$ ,  $\tau_p = 320 \text{ s}$

Equilibrium selfpolarization degree  $\zeta \sim \vec{b}\vec{n} = 0!!!$  (Here  $\vec{b} = \vec{B}/B$ )

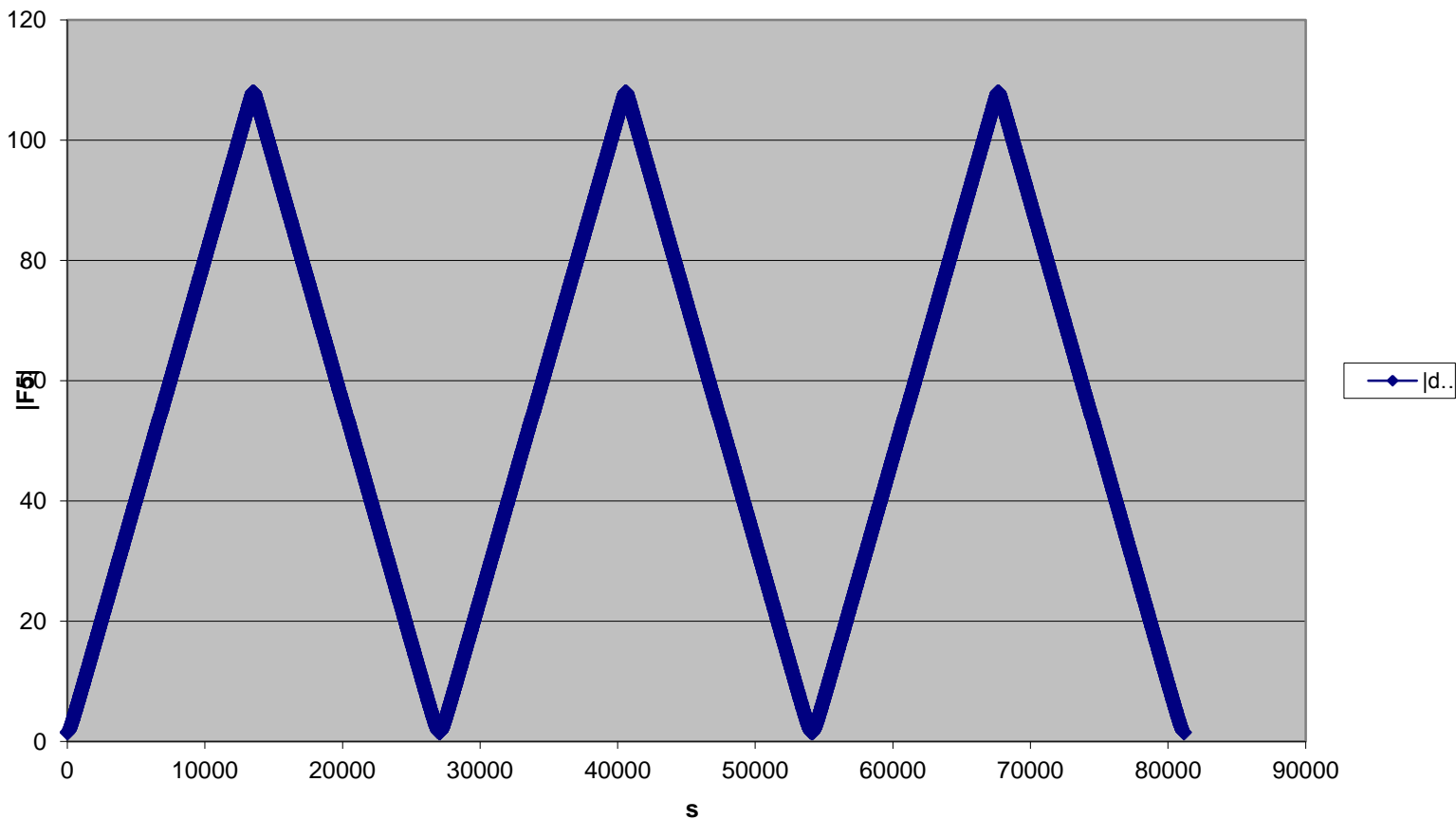


# Spin response function $|F_5| = |d|$

Calculated by the code ASPIRRIN written by V.Ptitsyn, upgraded by S.R.Mane

## Booster storage ring with 3 full snakes, $E=45.5$ GeV

$|dndg|$  around ring



# Spin transparent rotator for the solenoid type Snake

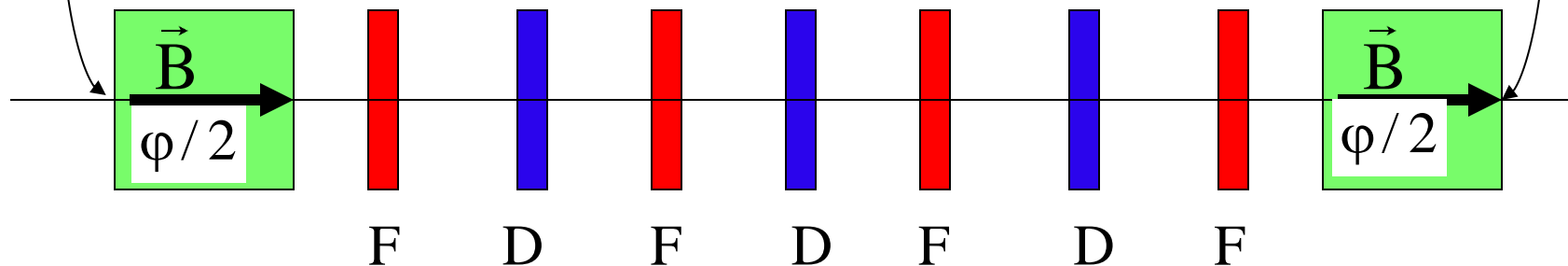
For decoupling should be  $T_x = -T_y$

← Litvinenko, Zholentz, 1980

$$T_x = \begin{pmatrix} -\cos \varphi & -2r \sin \varphi \\ (2r)^{-1} \sin \varphi & -\cos \varphi \end{pmatrix}$$

for the spin transparency!

$$r = pc / eB$$



Two solenoids, each  $L=40$  m  $B=5$  T, provide spin rotation by  $\varphi = 180^\circ$  at  $E=45.5$  GeV. Extension to 120 GeV with  $B=10$  T looks feasible.

All quads don't need to be skewed! Spin transparency require:

Full Snake:  $\cos \varphi = -1$ ,  $\sin \varphi = 0$ ;  $90^\circ$  - spin rotator:  $\cos \varphi = 0$ ,  $\sin \varphi = 1$

# Compton scattering of a laser light

F.Lipps and H.A.Tolhoek, Physica 20,85,395,(1954)

The scattered photon energy in electron mass units  $m_e$  is:

$$\omega(x) = \frac{\gamma a(1-x)}{1+a(1-x)} \quad \text{with} \quad a = 2\gamma\omega_0, \quad x = \cos\theta$$

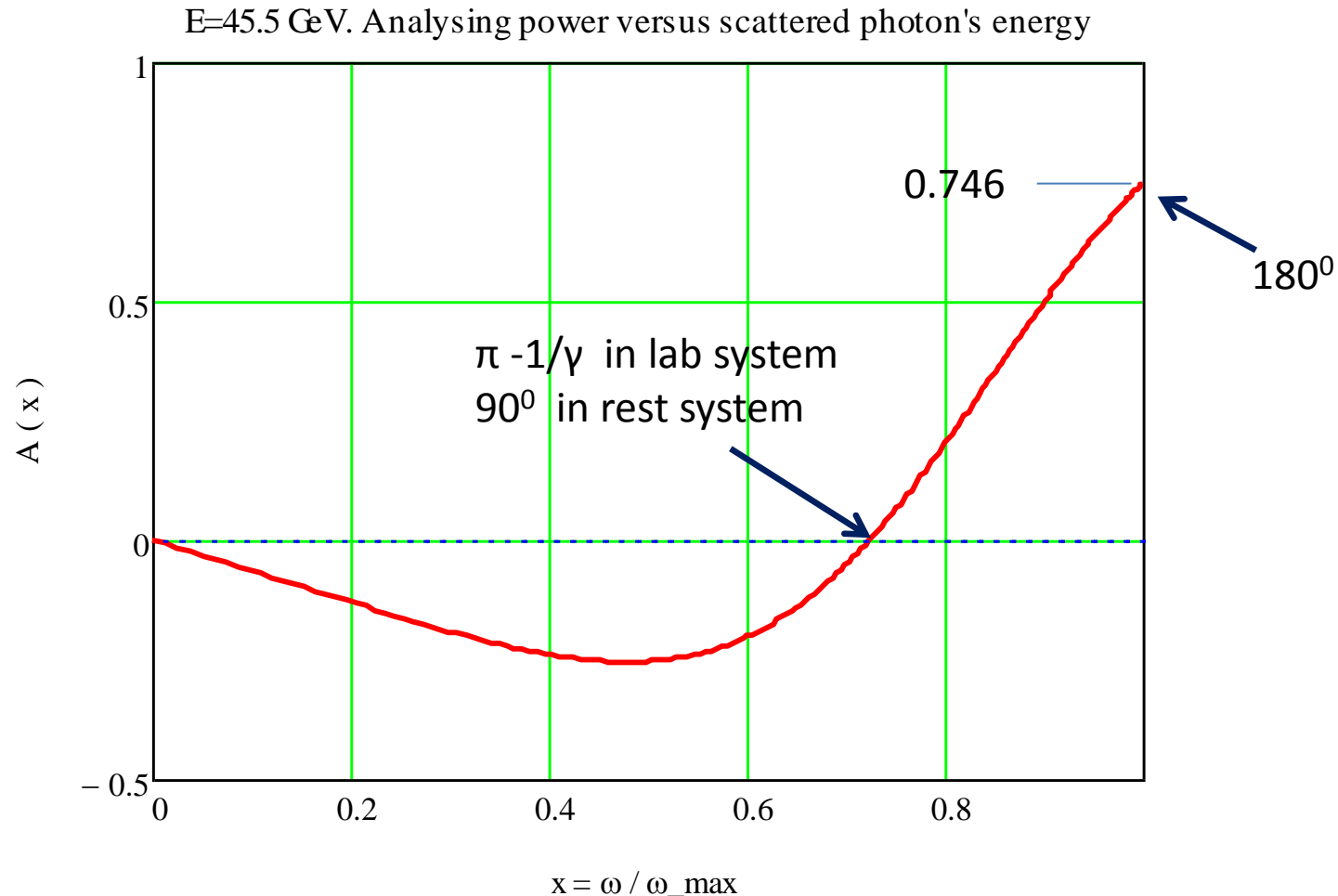
Differential unpolarized/polarized light scattering cross-sections:

$$\sigma_0(a, x) / \pi r_e^2 = \frac{1}{1+a(1-x)} + \frac{1}{[1+a(1-x)]^2} - \frac{1-x^2}{[1+a(1-x)]^3}$$

$$\sigma_1(a, x) / \pi r_e^2 = -a \left[ 1 + \frac{1}{1+a(1-x)} \right] \frac{x(1-x)}{[1+a(1-x)]^2}$$

At  $E = 45.5 \text{ GeV}$   $a = 0.812$ ,  $\omega_{\max} = 28 \text{ GeV}$  if  $\omega_0 = 2.33 \text{ eV}$ .

# Compton scattering of a laser light, cont.



We shall select events with the highest energy loss by the scattered electrons – get larger asymmetry! Magnetic momentum analysis, like used for two photon physics.

# Compton scattering of a laser light, cont.2

Integrated over  $x = \cos(\theta)$  unpolarized/polarized cross-sections:

$$\Sigma_0(a) / \pi r_e^2 = \frac{1}{a} \ln(1+2a) - \frac{2(1+a)}{a^3} \ln(1+2a) + \frac{4}{a^2} + \frac{2(1+a)}{(1+2a)^2}$$

$$\Sigma_1(a) / \pi r_e^2 = \frac{2(1+4a+5a^2)}{a(1+2a)^2} - \frac{(1+a) \ln(1+2a)}{a^2}$$

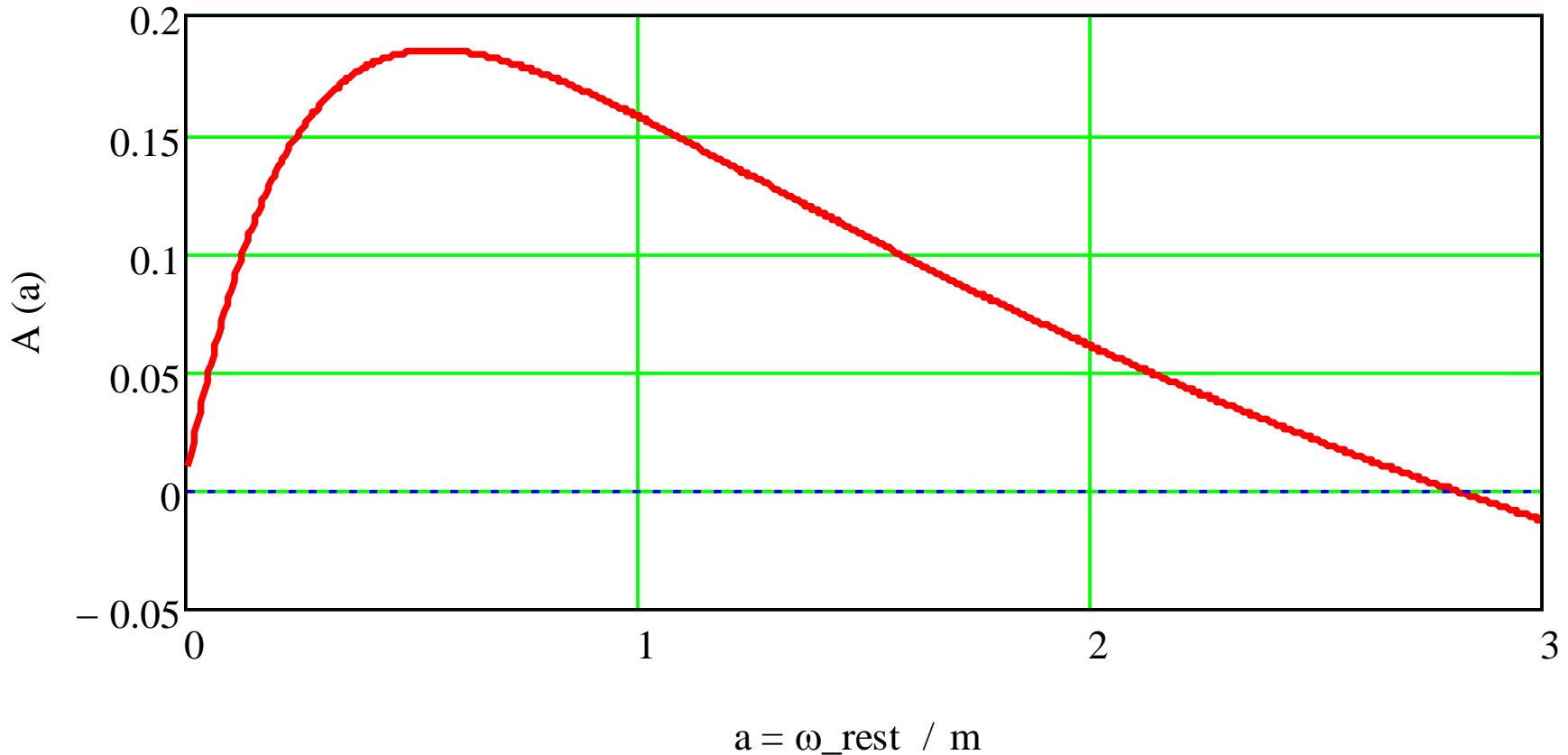
Integrated over full spectrum asymmetry:

$$A(a) = \Sigma_1(a) / \Sigma_0(a)$$

Is much smaller than the highest differential!

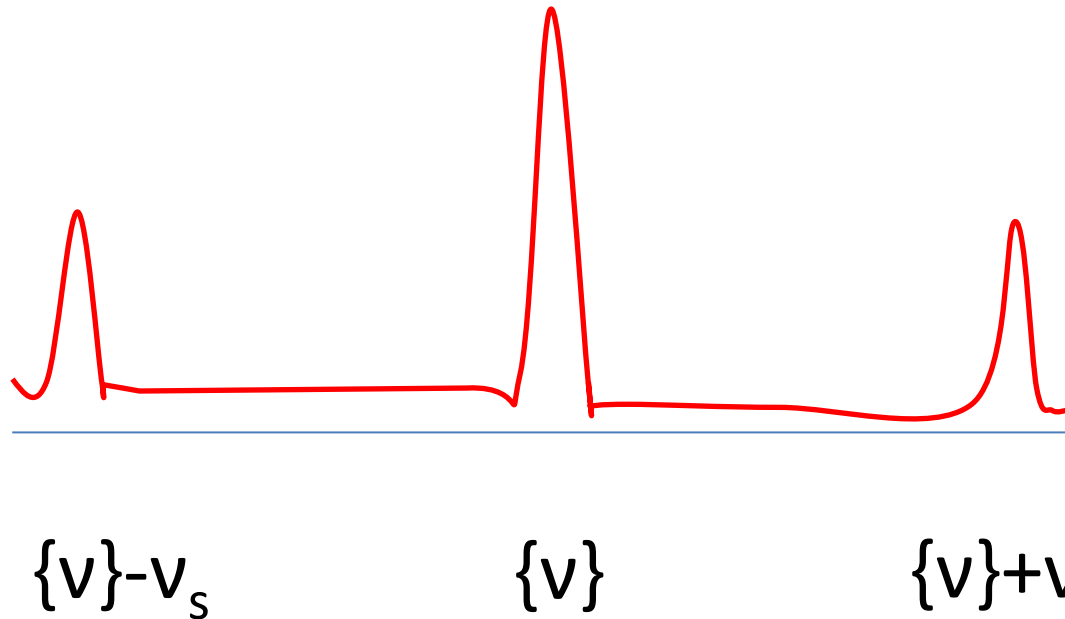
# Compton scattering of a laser light, cont.3

Integrated over full photon spectrum analysing power versus  $\omega_{\text{rest}} / m$



Here  $a$  – incident photon energy in a rest system of an electron.  $A(0.555) = 0.185$ , while the differential analysing power for scattering at  $180^\circ$  asymptotically approaches the unity for extreme values of gamma-factors.

# Free spin precession data analysis

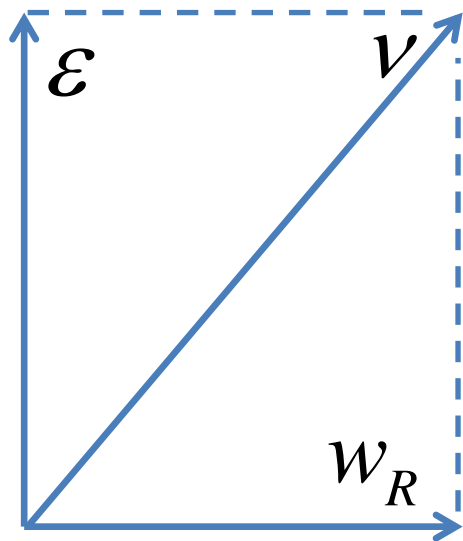


Could be observed also other picks, say from coherent betatron oscillations. But the central pick always will dominate.

# Free spin precession data analysis, cont.

Resonance frequency:  $\nu_R = k \pm \nu_s \pm m\nu_x \pm n\nu_y$

Detuning:  $\varepsilon = \nu_0 - \nu_R$  with  $\nu_0 = \gamma a$



Resonance perturbation  $W_R$

Corrected energy formula:

$$\nu_0 = \nu_R \pm \sqrt{\nu^2 - W_R^2}$$

Energy can not be determined

without measuring  $W_R$  !!!

Spin precession frequency must be measured in few energy points near a point of interest!  
Spin Harmonic Matching should be applied to minimize the nearby resonances strength!



# Free spin precession data analysis, cont.2

- Spin **decoherence** may limit energy determination accuracy achievable in one injection short.

Some very rough estimation for Z-peak :

$$\sigma_{\langle\delta\rangle} \simeq \sigma_{\delta}^2 \simeq 1.6 \cdot 10^{-7} \quad - \quad \text{energy spread} \quad \left( \sigma_{\delta} \equiv \sigma_{\Delta E/E} \simeq \pm 4 \cdot 10^{-4} \right)$$

$$\sigma_{\langle\nu\rangle} = \sigma_{\langle\delta\rangle} \cdot \nu_0 \simeq 1.6 \cdot 10^{-5} \quad - \quad \text{spread of average spin tunes}$$

$$N_{Cohr} = \frac{1}{2\pi\sigma_{\langle\nu\rangle}} \approx 1 \cdot 10^4 \quad - \quad \text{spin coherence time (in turns)}$$

Is sufficient to determine  $E_b$  with 44 keV or  $10^{-6}$  accuracy!

# Energy limits for polarization

- First limit comes from the high order synchrotron satellites. Can be cured by the use of Siberian Snakes in the booster ring! Still the collider shall operate without any snake!
- The second limit is more fundamental: due to high rate of the spin tune diffusion, caused by fluctuations of SR. For FCC-ee it is 80-100 GeV ?  
(see talk by Yu.Shatunov at the SPIN14 conference)
- Above that limit only Compton based methods could work, be proofed at lower energies.

# Conclusion

- Polarization is useful for direct energy calibration of up to W threshold. Free precession method, based on use of the Compton polarimeter, shall provide the energy determination with  $10^{-6}$  accuracy in one shot!
- Polarization will help calibrate@validate Compton based methods of the energy control/monitoring.
- Acceleration of a polarized e-beam in a synchrotron, equipped with Siberian Snakes, opens possibility to perform experiments with longitudinal polarization at IP (Z-peak).