

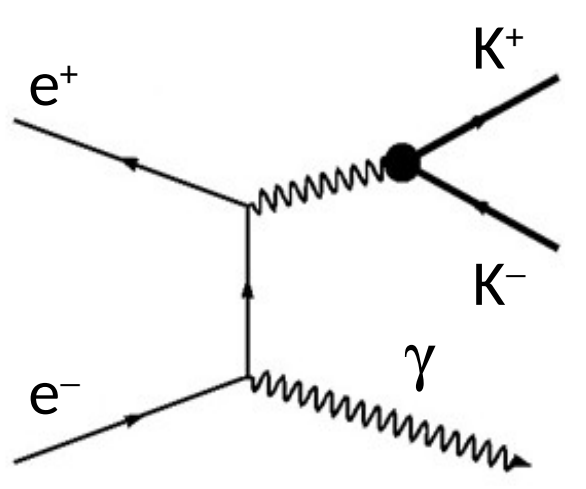
Study of interference effects in the decays of ψ mesons in K⁺K⁻

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ABSTRACT: Using the ISR technique with an undetected photon, the $e^+e^- \rightarrow K^+K^-$ cross section and the charged kaon electromagnetic form factor have been measured in the energy region 2.6-7.5 GeV in the BABAR experiment. The BABAR measurements together with data from other experiments are used to perform a model-independent determination of the relative phases between single-photon and three-gluon amplitudes in J/ψ and $\psi(2S) \rightarrow K\bar{K}$ decays. The values of the branching fractions measured in the $e^+e^- \rightarrow K^+K^-$ reaction are shifted due to interference of resonant and nonresonant amplitudes. We have determined the absolute values of the shifts to be 5% for J/ψ and 15% for $\psi(2S)$ decay. The interference patterns near the $\psi(3770)$ and $\psi(4160)$ resonances have been also studied. For the $\psi(3770)$ the resonant cross section is determined to be $\sigma(e^+e^- \rightarrow \psi(3770) \rightarrow K^+K^-) = 0.073^{+0.061}_{-0.044}$ pb with 3.2σ statistical significance. For the $\psi(3770)$ the upper limit $\sigma(e^+e^- \rightarrow \psi(4160) \rightarrow K^+K^-) < 0.062$ pb is set at 90% CL.

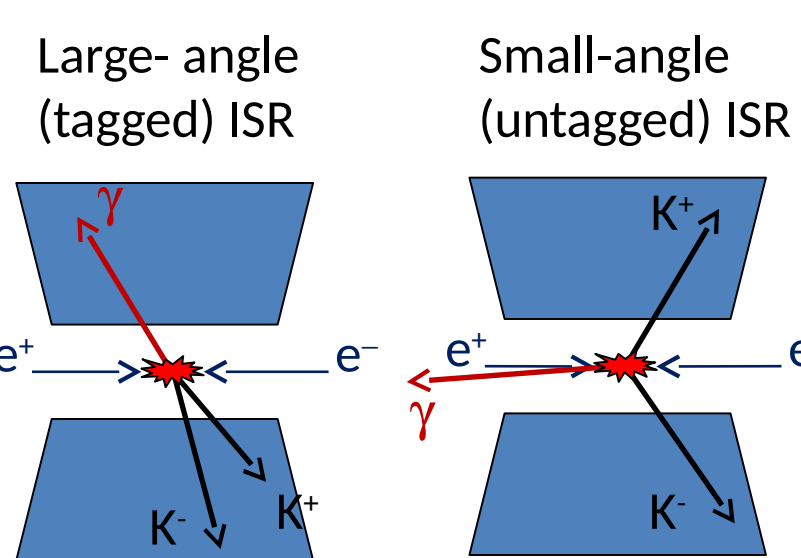
I. Measurement of the $e^+e^- \rightarrow K^+K^-$ cross section at BABAR



The BABAR detector collected data at center-of-mass energy of 10.6 GeV. The initial-state-radiation (ISR) technique is used to measure exclusive hadronic cross section at lower energies. The mass spectrum of the K^+K^- system produced in the reaction $e^+e^- \rightarrow K^+K^- \gamma$ is related to the cross section for the nonradiative process $e^+e^- \rightarrow K^+K^-$.

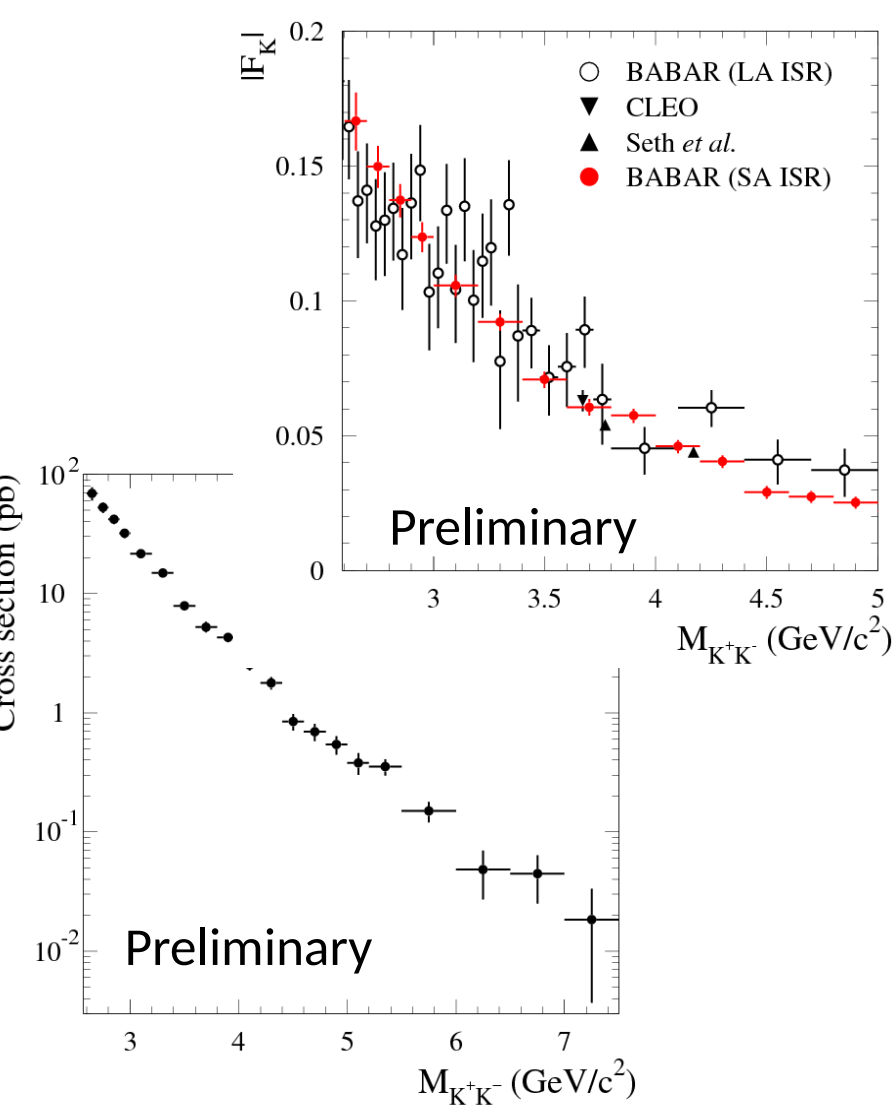
$$\frac{d\sigma_{e^+e^- \rightarrow K^+K^-}}{dm} = \frac{2m}{s} W(s, x) \sigma_{e^+e^- \rightarrow K^+K^-}(m), \quad x = \frac{2E_\gamma}{\sqrt{s}} = 1 - \frac{m^2}{s},$$

The radiator function $W(s, x)$ is calculated in QED with a high accuracy (better than 0.5%).

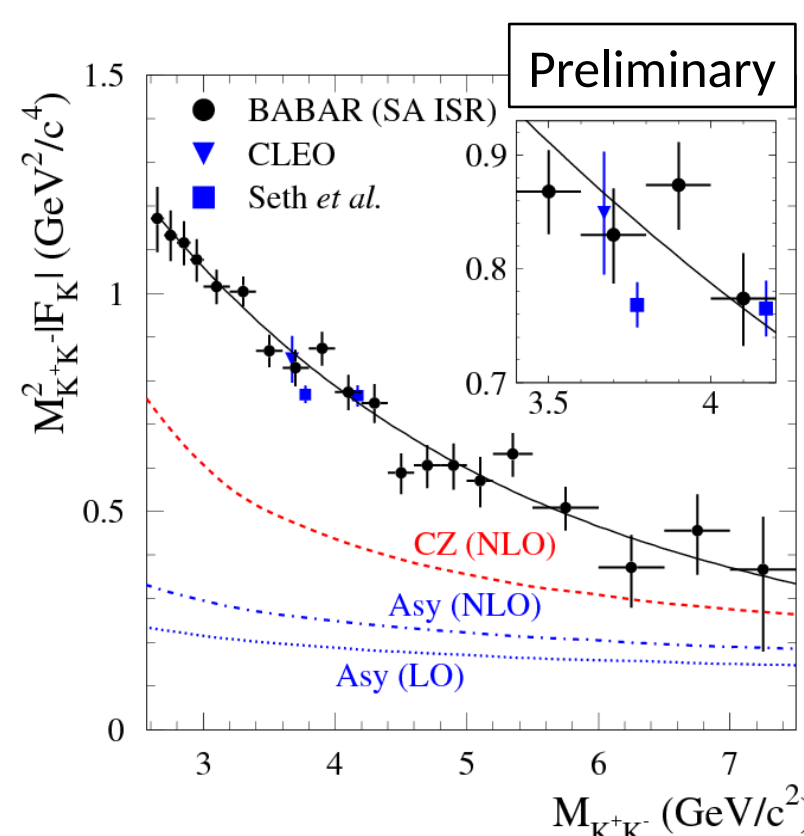


The produced hadron system is boosted against the ISR photon. Due to limited detector acceptance the mass region below 2.5 GeV can be studied only with detected photon.

Above 3 GeV statistics may be significantly increased with use of small-angle ISR.



$$\sigma_{K^+K^-}(m) = \frac{\pi\alpha^2\beta^3}{3m^2} |F_K(m)|^2$$



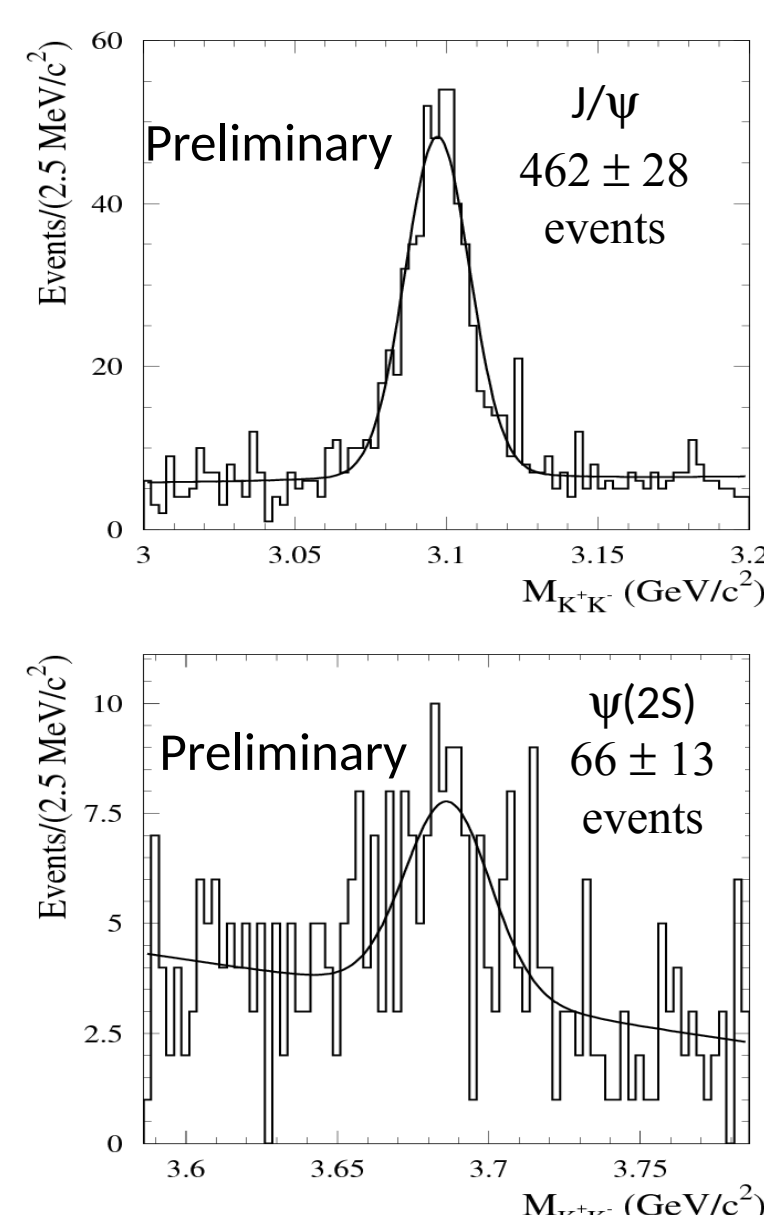
The measured continuum cross section may be used to calculate electromagnetic (single-photon) contribution to $\psi \rightarrow K^+K^-$ decay and effect of interference between resonant and nonresonant $e^+e^- \rightarrow K^+K^-$ amplitudes.

II. J/ψ and $\psi(2S)$ decays

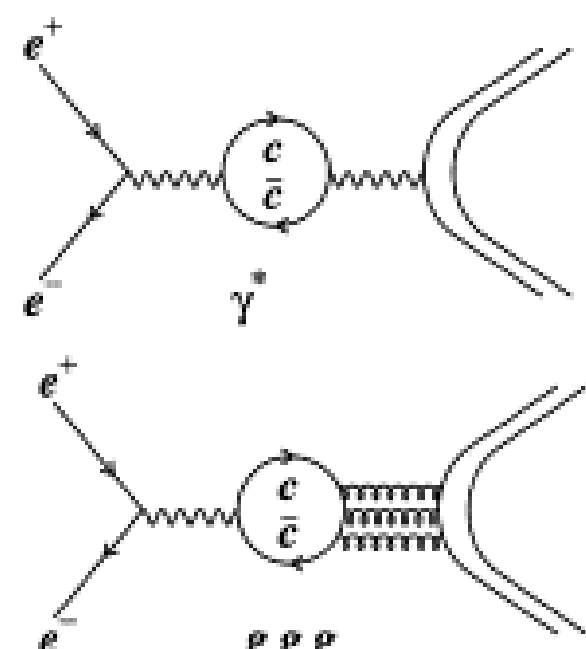
	$B(\psi \rightarrow K^+K^-)$	WA
J/ψ	$(3.36 \pm 0.20 \pm 0.12) \times 10^{-4}$	2.43 ± 0.25
$\psi(2S)$	$(0.73 \pm 0.15 \pm 0.02) \times 10^{-4}$	0.71 ± 0.05

To calculate the world average for the J/ψ , data obtained in the $e^+e^- \rightarrow K^+K^-$ reaction are used.

There is also the measurement [4], in which J/ψ 's were produced in the $\psi(2S) \rightarrow J/\psi \pi^+ \pi^-$ decay: $B(J/\psi \rightarrow K^+K^-) = (2.86 \pm 0.21) \times 10^{-4}$



III. Phenomenology of $\psi \rightarrow K\bar{K}$



$$B(\psi \rightarrow K^+K^-) = |A_\gamma^{K^+K^-} + A_s e^{i\varphi}|^2,$$

$$B(\psi \rightarrow K_S K_L) = |A_\gamma^{K_S K_L} + A_s e^{i\varphi}|^2$$

$$|A_\gamma|^2 = B_{ee} \frac{|F_K(M_\psi)|^2}{4} \beta^3$$

In previous analyses [4,5,6] the single-photon $K_S K_L$ amplitude was assumed to be zero, while the single photon K^+K^- amplitude was assumed to be equal to the same amplitude for $\pi^+ \pi^-$, which is determined from the $\psi \rightarrow \pi^+ \pi^-$ decay.

$$B(\psi \rightarrow K^+K^-) = |A_\gamma^{K^+K^-} + A_s e^{i\varphi}|^2, \quad \text{with } A_\gamma^{K^+K^-} \approx A_\gamma^{\pi^+ \pi^-}$$

$$B(\psi \rightarrow K_S K_L) = |A_\gamma^{K_S K_L} + A_s e^{i\varphi}|^2, \quad \text{with } A_\gamma^{K_S K_L} \approx 0 \Rightarrow \varphi \approx \pm 90^\circ$$

We perform a model-independent determination of the phase:
✓ A_γ 's are calculated from the measured values of kaon form factors.
✓ From data we estimate that the ratio of the neutral and charged form factors (κ) is equal to 0.2 ± 0.1 at J/ψ and 0.15 ± 0.07 at $\psi(2S)$.

IV. Effect of interference

$$\sigma = \sigma_0 \left| 1 - \sqrt{\frac{\sigma_\psi B(\psi \rightarrow f)}{\sigma_0}} \frac{m\Gamma}{m^2 - E^2 - im\Gamma} \right|^2 = \sigma_0 \left| 1 - \sqrt{\frac{\sigma_\psi}{\sigma_0}} (A_\gamma + A_s e^{i\varphi}) \frac{m\Gamma}{m^2 - E^2 - im\Gamma} \right|^2 =$$

$$\sigma_0 + \sigma_\psi \left[B(\psi \rightarrow f) + 2 \sqrt{\frac{\sigma_0}{\sigma_\psi}} A_\gamma \sin \phi \right] \frac{m^2 \Gamma^2}{(m^2 - E^2)^2 + m^2 \Gamma^2} -$$

$$2 \sqrt{\sigma_0 \sigma_\psi} \frac{m\Gamma(m^2 - E^2)}{(m^2 - E^2)^2 + m^2 \Gamma^2} (A_\gamma + A_s \cos \phi), \quad \sigma_\psi = \frac{12\pi}{m^2} B(\psi \rightarrow e^+e^-)$$

For narrow resonances the interference term proportional to $(m^2 - E^2)$ integrates to zero due to the beam energy spread in direct e^+e^- experiments and detector resolution in ISR measurements. The remaining interference term has a Breit-Wigner shape and causes a shift of the measured $B(\psi \rightarrow K^+K^-)$ relative to its true value by

$$\delta B = 2 \sqrt{\frac{\sigma_0}{\sigma_\psi}} A_s \sin \phi$$

The values of the branching fraction for $J/\psi \rightarrow K^+K^-$ measured in the reaction $e^+e^- \rightarrow K^+K^-$ and in the decay $\psi(2S) \rightarrow \pi\pi J/\psi \rightarrow \pi\pi K^+K^-$ differ by δB .

V. Relative phases and interference shifts

For the J/ψ we perform calculations for two values of $B(J/\psi \rightarrow K_S K_L)$, $(2.62 \pm 0.21) \times 10^{-4}$ [4] and $(1.82 \pm 0.14) \times 10^{-4}$ [7], and two signs of $\sin \phi$.

$J/\psi \rightarrow K_S K_L$	φ	$\varphi(\kappa=0)$	$\delta B(J/\psi \rightarrow K^+K^-) \times 10^4$
BES [28]	$(96 \pm 6)^\circ$	$(97 \pm 4)^\circ$	0.13 ± 0.01
	$-(96 \pm 5)^\circ$	$-(95 \pm 4)^\circ$	-0.13 ± 0.01
NU [20]	$(111 \pm 5)^\circ$	$(108 \pm 4)^\circ$	0.15 ± 0.01
	$-(109 \pm 5)^\circ$	$-(106 \pm 4)^\circ$	-0.15 ± 0.01

For J/ψ , we confirm the results of the previous works [4,5,6] that the strong amplitude for the $\psi \rightarrow K^+K^-$ decay has a large imaginary part.

The ϕ and δB values depend weakly on $\kappa = (A_\gamma^{K_S K_L}/A_\gamma^{K^+K^-})$.

φ	$\varphi(\kappa=0)$	$\delta B(\psi(2S) \rightarrow K^+K^-) \times 10^4$
$(81 \pm 13)^\circ$	$(91 \pm 10)^\circ$	0.11 ± 0.01
$-(56 \pm 15)^\circ$	$-(55 \pm 13)^\circ$	-0.10 ± 0.01

For $\psi(2S)$, the result on the relative phase strongly depends on the sign of $\sin \phi$.

VI. Corrected branching fraction for J/ψ and $\psi(2S) \rightarrow K^+K^-$

BABAR results for two signs of $\sin \phi$:

$$B(J/\psi \rightarrow K^+K^-) = (3.22 \pm 0.20 \pm 0.12) \times 10^{-4}, \quad \sin \varphi > 0,$$

$$(3.50 \pm 0.20 \pm 0.12) \times 10^{-4}, \quad \sin \varphi < 0,$$

For J/ψ the $\sin \phi$ sign can be chosen from comparison of the branching fractions measured in the $e^+e^- \rightarrow K^+K^-$ reaction and $\psi(2S) \rightarrow J/\psi \pi^+ \pi^-$ decay. Comparison our data with the measurement of Ref.[4] $(2.86 \pm 0.21) \times 10^{-4}$ gives an indication that the sign is positive.

$$B(\psi(2S) \rightarrow K^+K^-) = (0.62 \pm 0.15 \pm 0.02) \times 10^{-4}, \quad \sin \varphi > 0,$$

$$(0.83 \pm 0.15 \pm 0.02) \times 10^{-4}, \quad \sin \varphi < 0,$$

For $\psi(2S)$ a theoretical argument can be used. The ratio of the $|A_\gamma|^2$ for $\psi(2S)$ and J/ψ decay is 0.192 ± 0.026 for the negative sign and 0.170 ± 0.23 for the positive. The latter value is closer to the expectation that this ratio is approximately equal to the ratio $B(\psi(2S) \rightarrow e^+e^-)/B(J/\psi \rightarrow e^+e^-) = 0.131$.

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VII. $\psi(3770)$ decays to light hadrons

The $\psi(3770)$ meson is the lowest-mass $c\bar{c}$ state above open-charm threshold. It is expected to decay predominantly to DD pairs. Assuming that $c\bar{c}$ annihilation into light hadrons is proportional to $|\Psi(0)|^2$ we estimate

$$B(\psi(3770) \rightarrow f) \approx B(\psi(2S) \rightarrow f) \frac{B(\psi(3770) \rightarrow e^+e^-)}{B(\psi(2S) \rightarrow e^+e^-)} \approx 10^{-3} B(\psi(2S) \rightarrow f) \quad (1)$$

About 90 light-hadron final states were studied, but only two decays, to $\phi\eta$ [8] and $p\bar{p}$ [9], were observed. The measured branching fractions are significantly exceed the above prediction. The mechanism explaining relatively large values of branching fractions is production of light hadrons via intermediate DD loops [10,11]. The predicted $B(\psi(3770) \rightarrow K^+K^-) \approx 9 \times 10^{-5}$ [10] is larger than the above prediction by about three orders of magnitude. The branching fraction for the single-photon mechanism of this decay is calculated to be about 5×10^{-9} and negligible.

VIII. Interference pattern near the $\psi(3770)$ resonance

With $B(\psi(3770) \rightarrow K^+K^-) \sim 10^{-4}$ [10] the decay reveals itself as an interference pattern in the energy dependence of the $e^+e^- \rightarrow K^+K^-$ cross section near the $\psi(3770)$ resonance.

$$\sigma_{K^+K^-}(E) = \left| \sqrt{\sigma_{\text{cont}}} - \sqrt{\sigma_\psi} e^{i\phi} \frac{m_\psi \Gamma_\psi}{D} \right|^2 =$$

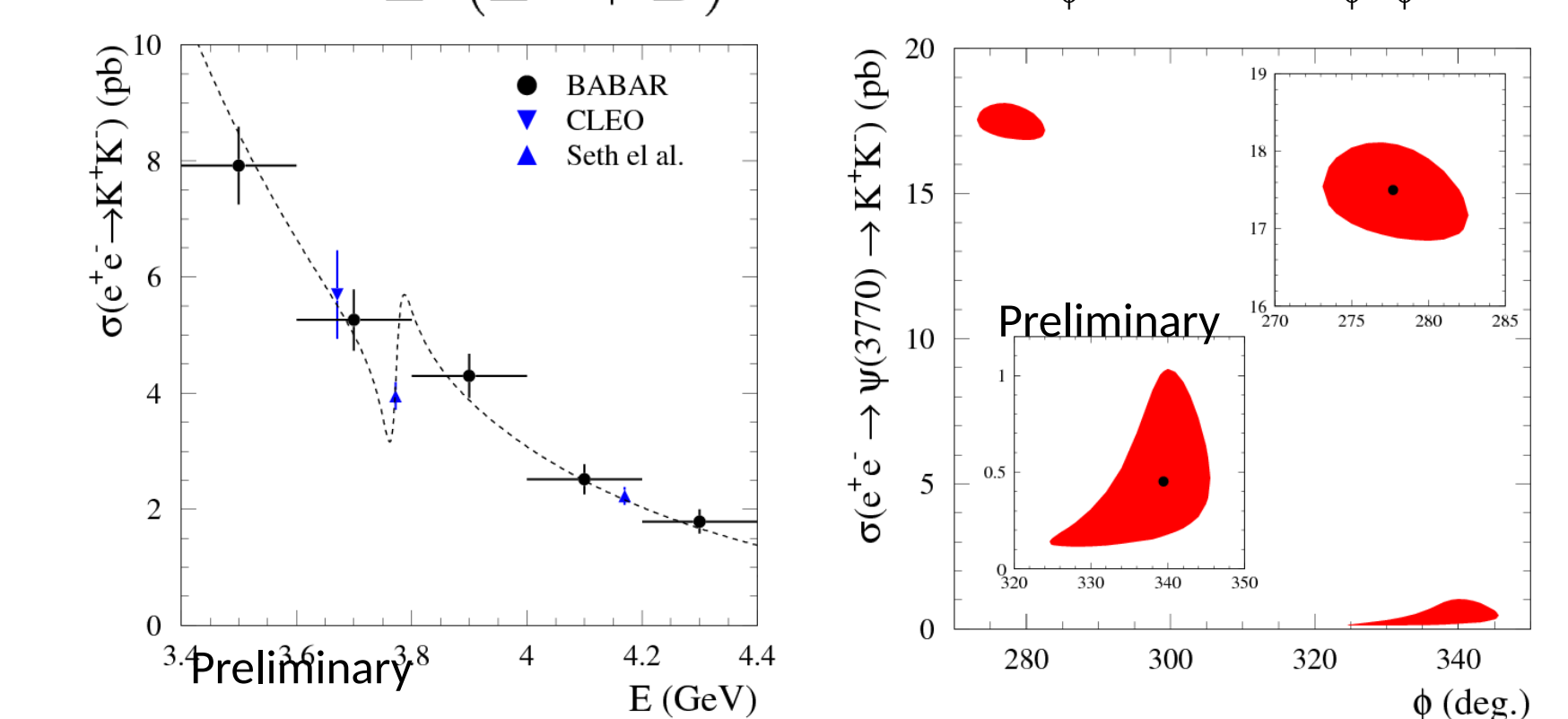
$$\sigma_{\text{cont}} + (\sigma_\psi + 2\sqrt{\sigma_{\text{cont}}\sigma_\psi} \sin \phi) \frac{m_\psi^2 \Gamma_\psi^2}{|D|^2} -$$

$$2\sqrt{\sigma_{\text{cont}}\sigma_\psi} \cos \phi \frac{m_\psi \Gamma_\psi (m_\psi^2 - E^2)}{|D|^2},$$

$$\sigma_{\text{cont}}(E) = \frac{\pi\alpha^2\beta^3}{3E^2} |F_K(E)|^2,$$

$$|F_K(E)| = \frac{A}{E^2(E\gamma + B)},$$

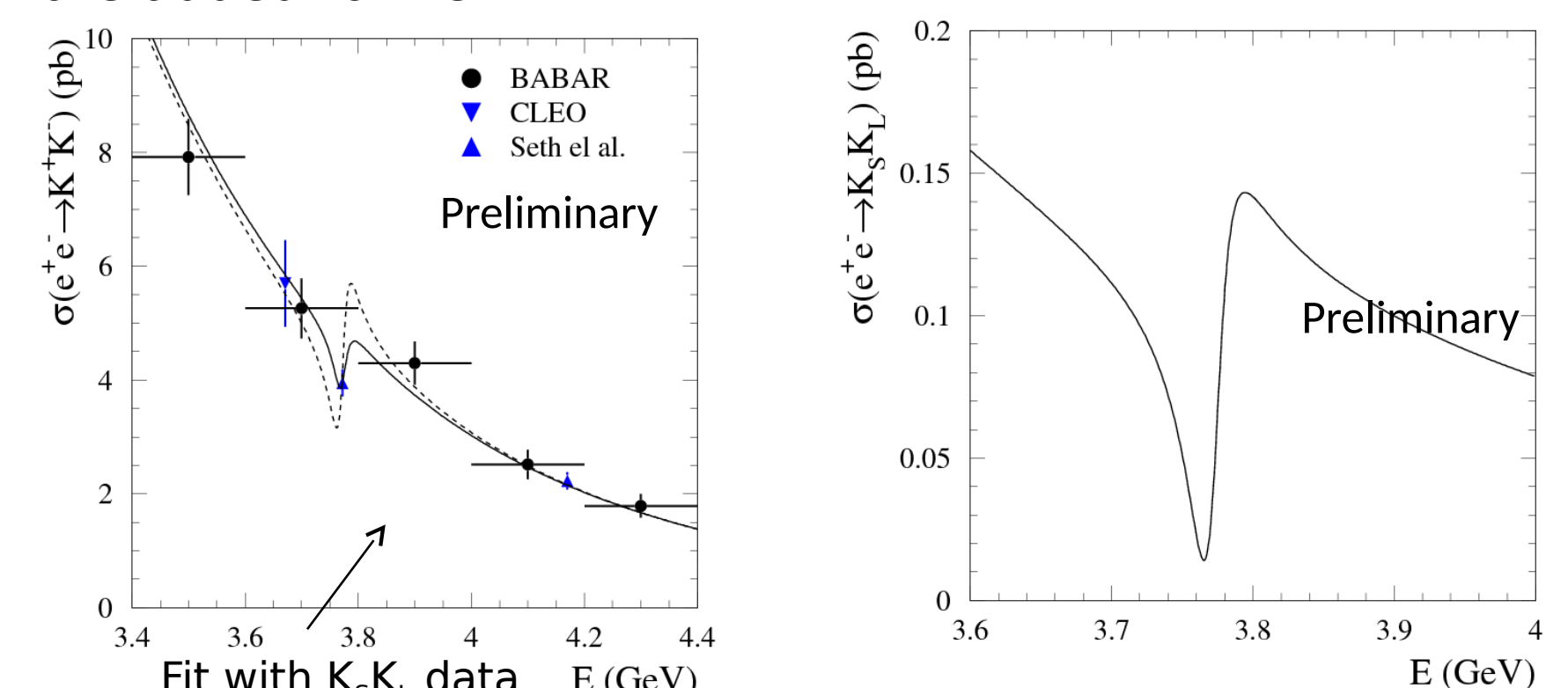
where $\sigma_\psi \equiv \sigma_{\psi(3770)}$ is the cross section for the process $e^+e^- \rightarrow \psi(3770) \rightarrow K^+K^-$ in the resonance maximum, and $D = m_\psi^2 - E^2 - im_\psi \Gamma_\psi$



The fit yields two solutions for $\sigma_{\psi(3770)}$ and φ with statistical significance of 3.2σ . They corresponds to branching fractions of about 10^{-4} and 10^{-3} .

IX. Constraints from $e^+e^- \rightarrow K_S K_L$

Since the single-photon contribution is small, $B(\psi(3770) \rightarrow K_S K_L) = B(\psi(3770) \rightarrow K^+K^-)$, but the nonresonant $e^+e^- \rightarrow K_S K_L$ cross section is significantly, at least by an order of magnitude, lower than that for K^+K^- . The interference pictures are strongly different for $K_S K_L$ and K^+K^- . The data $\sigma(e^+e^- \rightarrow K_S K_L)(m_\psi) < 0.07$ pb at 90% CL [12] and $\sigma_{\text{cont}}(K_S K_L) / \sigma_{\text{cont}}(K^+K^-) = 0.030 \pm 0.015$ at $E = m_\psi$ [13,14,15] are added to the fit.



The fit with $K_S K_L$ data yields a single solution:

$$\sigma_{\psi(3770)} = 0.073^{+0.62}_{-0.44} \text{ pb},$$

$$\phi = (308^{+17}_{-34})^\circ.$$

The values of $\sigma_{\psi(3770)}$ and φ are shifted from those for the fit without $K_S K_L$ constraints by about 1.5σ . The statistical significance is the same, 3.2σ . The branching fraction $B(\psi(3770) \rightarrow K^+K^-)$ corresponding to the measured cross section is about 10^{-5} .

The same fitting procedure is used in the energy region of the $\psi(4160)$ resonance. The upper limit on the $e^+e^- \rightarrow \psi(3770) \rightarrow K^+K^-$ cross section is set

$$\sigma_{\psi(4160)} < 0.062 \text{ pb at 90\% CL.}$$

The corresponding limit on the branching fraction is $B(\psi(4160) \rightarrow K^+K^-) < 2 \times 10^{-5}$ at 90% CL.