# Study of the $e^+e^- \rightarrow VP$ reactions at the VEPP-2000 $e^+e^-$ collider with the SND detector

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**Abstract:** The reactions  $e^+e^- \rightarrow \rho\pi$ ,  $\omega\pi$ ,  $\rho\eta$ ,  $\omega\eta$  have been studied in the energy region 1.05–2.00 GeV. The experiment has been carried out at the VEPP-2000  $e^+e^-$  collider with the SND detector. The measured cross sections have been fitted in the vector meson dominance model.

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### 1 Introduction

The transitions into the VP final states, where V and P denote vector and pseudoscalar mesons, respectively, are dominant decay modes for excited states of the vector  $\rho$ ,  $\omega$ , and  $\phi$  mesons. In the center-of-mass (c.m.) energy region  $\sqrt{s} = 1-2$  GeV, where these vector resonances are located, the reactions  $e^+e^- \rightarrow VP$  constitute a significant part of the cross section  $e^+e^- \rightarrow hadrons$ . In this paper we study the reactions of this type with  $VP = \rho \pi$ ,  $\omega \pi$ ,  $\rho \eta$ ,  $\omega \eta$  in the c.m. energy region 1.05-2.00 GeV with the SND detector [1] at the VEPP-2000  $e^+e^-$  collider [2]. The measured cross sections are fitted with the vector meson dominance (VMD) model.

## 2 Processes overview

2.1 
$$e^+e^- \rightarrow \rho \pi$$

The cross section of the process  $e^+e^- \rightarrow \rho\pi$  with the decay  $\rho \rightarrow \pi\pi$  has been measured in the energy range  $1.05 \leq \sqrt{s} \leq 2.00$  GeV [3]. The following criteria are applied to selected  $\pi^+\pi^-\pi^0$  events :

- exactly 2 charged tracks originating from the  $e^+e^-$  interaction region;
- exactly 2 photons with energies  $E_{\gamma} > 30$  MeV;
- the total energy deposition in the detector calorimeter  $0.3 < E_{tot}/\sqrt{s} < 0.8$ .

Selected events are fitted to a common vertex. The quality of the vertex fit is characterized by the parameter  $\chi_R^2$ , which is required to be less than 40. Then the kinematic fit to the hypothesis  $e^+e^- \rightarrow \pi^+\pi^-\gamma\gamma$  is performed with requirements of the energy and momentum balance, and events are further selected with the following conditions:

- $\chi_E^2 < 30$ , where  $\chi_E^2$  is the  $\chi^2$  of the kinematic fit;
- z coordinate of the vertex  $|z_{vertex}| < 10$  cm;
- the polar angles of the charged tracks  $30^{\circ} < \theta_{track} < 150^{\circ}$ ;
- the difference of charged track azimuthal angles

 $|\Delta \phi_{tracks}| > 10^{\circ};$ 

- the energy deposition in the calorimeter associated with the charged pions  $(E_{\pi^+} + E_{\pi^-})/\sqrt{s} < 0.6;$
- the total energy deposition in the calorimeter not associated with two charged particles and two photons  $E_{tot}^{outer} < 70$  MeV.

The number of signal events is determined from the fit to the two-photon mass spectrum with a sum of signal  $(\pi^0 \text{ resolution function})$  and background distributions, which shapes are obtained using signal and background  $(e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0, e^+e^- \rightarrow \pi^+\pi^-\gamma, \text{ etc.})$  simulation. The measured  $e^+e^- \rightarrow \pi^+\pi^-\pi^0$  cross section is shown in Fig. 1. Our results is in agreement with SND at VEPP-2M and BABAR measurements, but has the better accuracy. The curve in Fig. 1 represents the result of the VMD fit with  $\omega(782)$ ,  $\phi(1020)$ ,  $\omega(1450)$ , and  $\omega(1680)$ resonances.



Fig. 1. The cross section for the process  $e^+e^- \rightarrow \rho\pi$ measured in this work [SND(2011)] together with previous measurements in the DM2 [4], SND at VEPP-2M ([SND(2003)], [5]), and BABAR [6] experiments. The curve is the result of the VMD fit described in the text.

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#### $e^+e^- \rightarrow \omega \pi$ $\mathbf{2.2}$

The process  $e^+e^- \rightarrow \omega \pi^0$  is studied in the decay mode  $\omega \to \pi^0 \gamma$  in the same energy range. Five-photon events are selected using the following conditions:

- at least 5 photons;
- no charged particles;
- less than 6 hits in the detector drift chamber;
- the total energy deposition in the calorimeter  $E_{tot}/\sqrt{s} > 0.5.$

For selected events the kinematic fits to the hypotheses  $e^+e^- \rightarrow 5\gamma$  and  $e^+e^- \rightarrow \pi^0\pi^0\gamma$  are performed, which qualities are characterized by the parameters  $\chi^2_{5\gamma}$  and  $\chi^2_{\pi^0\pi^0\gamma}$ , respectively. Further selection is based on the following criteria:

- $\chi^2_{5\gamma} < 30;$   $\chi^2_{\pi^0\pi^0\gamma} \chi^2_{5\gamma} < 10;$  at least one of the two  $\pi^0\gamma$  invariant masses  $|m_{\pi^0\gamma} M_{\omega} | < 200 \text{ MeV.}$

The invariant masses in the latter condition is calculated using photon parameters obtained in the  $e^+e^- \rightarrow \pi^0\pi^0\gamma$ fit. The number of signal events is obtained from the fit to the  $m_{\pi^0\gamma}$  spectrum with a sum of signal and background distributions. The measured cross section is shown in Fig. 2. It should be noted that the CLEO cross section is calculated under the CVC hypothesis from the  $\omega\pi$  spectral function in the  $\tau \to \omega\pi\nu_{\tau}$  decay. In Fig. 2 we present the result based on SND data collected in 2010–2012 runs. Our previous measurement based on 2010–2011 data was published in ref. [7]. From the measured cross section the  $\gamma^* \to \omega \pi$  transition form factor shown in Fig. 3 is extracted. The curves in Figs. 2 and 3 are the result of the SND data VMD fit with the  $\rho(770)$ ,  $\rho(1450)$ , and  $\rho(1700)$  resonances. The dashed curve in Fig. 3 is the fit result with the  $\rho(770)$  only. It is seen that the VMD model cannot describe simultaneously our data on the transition form factor and data obtained in the NA60 from the  $\omega \rightarrow \pi^0 \mu^+ \mu^-$  decay also shown in Fig. 3.



Fig. 2. The cross section for the process  $e^+e^- \rightarrow$  $\omega\pi$  measured in this work (SND 2015) in compar-

ison with previous measurements in the SND at VEPP-2M (SND 2000) [8] and CLEO [9] experiments. The curve is the result of the VMD fit described in the text.



Fig. 3. The  $\gamma^* \to \omega \pi$  transition form factor measured in this work (SND 2015) in comparison with previous measurements in the SND at VEPP-2M (SND 2000) [8] and NA60 [10] experiments. The curves are the result of the fit described in the text.

# **2.3** $e^+e^- \rightarrow \rho \eta$

The process  $e^+e^- \rightarrow \rho\eta \rightarrow \pi^+\pi^-\eta$  has been studied in the decay mode  $\eta \to \gamma \gamma$  in the energy range 1.22-2.00 GeV [11]. The following criteria are used to select  $\pi^+\pi^-\eta$  events:

- exactly 2 charged tracks originated from the interaction region;
- exactly 2 photons with polar angles  $36^{\circ} < \theta < 144^{\circ}$ ;
- the total energy deposition in the calorimeter 0.4 < $E_{tot}/\sqrt{s} < 0.9;$
- the energy deposition of charged particles  $E_{tracks}/\sqrt{s} < 0.65.$

The vertex fit and kinematic fit to the  $e^+e^- \rightarrow \pi^+\pi^-\gamma\gamma$ hypothesis are performed for selected events. The final selection uses the following conditions:

•  $\chi_R^2 < 200$  and  $\chi_E^2 < 60$ ;

• the  $\gamma\gamma$  invariant mass 400 MeV  $< m_{\gamma\gamma} < 700$  MeV. The number of signal events is obtained from the fit to the  $m_{\gamma\gamma}$  spectrum with a sum of signal and background distributions. The measured cross section is shown in Fig. 4. Our result agrees with BABAR data, but has better accuracy. The solid curve in Fig. 4 is the result of the VMD fit with  $\rho(770)$  and  $\rho(1450)$  resonances, while the dashed curve represents the fit with the  $\rho(1700)$  contribution added. It is seen that the  $\rho(1700)$  contribution is small. It is usually assumed that the dominant mechanism of the  $e^+e^- \rightarrow \pi^+\pi^-\eta$  reaction is transition via  $\rho^0(770)\eta$  intermediate state. We

however observe a contribution of other mechanism, presumably  $\rho^0(1450)\eta$  [11]. From our cross section measurement, using the CVC hypothesis the branching ratio  $B_{CVC}(\tau^- \to \eta \pi^- \pi^0 \nu_{\tau}) = (0.156 \pm 0.011)\%$  is calculated, which is in agreement with the measured value  $B_{exp}(\tau^- \to \eta \pi^- \pi^0 \nu_\tau) = (0.139 \pm 0.010)\%.$ 



Fig. 4. The cross section for the process  $e^+e^- \rightarrow \rho\eta$ measured in this work (SND@VEPP2000) in comparison with previous measurements in the SND at VEPP-2M (SND@VEPP2M) [12] and BABAR [13] experiments. The curves are the results of the VMD fits described in the text.

### 2.4 $e^+e^- \rightarrow \omega \eta$

The process  $e^+e^- \rightarrow \omega \eta$  is studied in the decay mode  $\omega \to \pi^+ \pi^- \pi^0$  and  $\eta \to \gamma \gamma$  in the energy range 1.34-2.00 GeV. Events are selected using the following criteria:

- at least 2 charged tracks originated from the inter-• action region;
- at least 4 photons;
- the total energy deposition in the calorimeter  $E_{tot} > 300$  MeV.

The vertex fit and kinematic fits to the  $e^+e^- \rightarrow$  $\pi^+\pi^-\pi^0\gamma\gamma$  hypothesis with the additional condition that the two photon invariant mass must be in the range  $400 \leqslant m_{\gamma\gamma} \leqslant 700$  MeV and to the  $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0(\gamma)$ hypothesis are performed. The quality of the kinematic fits are characterized by the parameters  $\chi^2_{\pi^+\pi^-\pi^0\gamma\gamma}$  and  $\chi^2_{\pi^+\pi^-\pi^0\pi^0(\gamma)}$ . The  $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$  process is the main source of background for the process under study. The following conditions are applied on the parameters obtained in the fits:

- $\chi^2_{\pi^+\pi^-\pi^0\gamma\gamma} < 30$  and  $\chi^2_{\pi^+\pi^-\pi^0\pi^0(\gamma)} > 200;$  the mass recoiling against  $\gamma\gamma$  0.65 <  $m^{rec}_{\gamma\gamma}$  < 0.9 GeV for the  $e^+e^- \rightarrow \pi^+\pi^-\pi^0\gamma\gamma$  fit.

The  $\omega\eta$  signal is extracted from the fit to the  $m_{\gamma\gamma}$  and  $m_{\gamma\gamma}^{rec}$  distributions. The measured cross section is shown in Fig. 5 in comparison with the previous BABAR measurement. It is fitted with a sum of the  $\omega(1420)$  and  $\omega(1650)$  contributions. Destructive interference between these two contributions is responsible for a very low level of the cross section observed above 1.8 GeV.



Fig. 5. The cross section for the process  $e^+e^- \rightarrow \omega \eta$ measured in this work (SND) in comparison with previous measurement in the BABAR [14] experiment. The curve is the result of the VMD fit described in the text.

#### 3 Summary

The cross sections for the processes  $e^+e^- \rightarrow \rho \pi$ ,  $\omega \pi$ ,  $\rho\eta$ ,  $\omega\eta$  have been measured in the SND experiment at the VEPP-2000  $e^+e^-$  collider. All of these measurements have the best accuracies to date. This work is partially supported in the framework of the State order of the Russian Ministry of Science and Education and the RFBR Grant No. 15-02-01037. Part of this work related to the photon reconstruction algorithm in the electromagnetic calorimeter is supported by the Russian Science Foundation (Project No. 14-50-00080).

#### References

- 1 M.N. Achasov et al. (SND Collaboration) Spherical neutral detector for VEPP-2M collider. Nucl. Instrum. and Methods in Phys. Research, 2000, A449(1-2): 125-139.
- Yu.M. Shatunov et al. Proceedings of the 7th European Particle Accelerator Conference, Vienna, 2000. EPS, Geneva, 2000: 439.
- V.M. Aul'chenko et al. (SND Collaboration) Study of the 3  $e^+e^- \rightarrow \pi^+\pi^-\pi^0$  process in the energy range 1.05–2.00 GeV. Journal of Experimental and Theoretical Physics, 2015, 121(1): 27 - 34.
- A. Antonelli, R. Baldini, M.E. Biagini et al. (DM2 Collabo-4 ration) Measurement of the  $e^+e^- \rightarrow \pi^+\pi^-\pi^0$  and  $e^+e^$ reactions in the energy interval 1350–2400 MeV. Z.  $\omega \pi^+ \pi^-$ Phys., 1992, C56: 15-20.

- 5 M.N. Achasov, V.M. Aulchenko, K.I. Beloborodov et al. (SND Collaboration) Study of the process  $e^+e^- \rightarrow \pi^+\pi^-\pi^0$  in the energy region  $\sqrt{s}$  from 0.98 GeV to 1.38 GeV. Phys. Rev., 2002, D66: 032001.
- 6 B. Aubert, R. Barate, D. Boutigny et al. (BABAR Collaboration) Study of  $e^+e^- \rightarrow \pi^+\pi^-\pi^0$  process using initial state radiation with BaBar. Phys. Rev., 2004, D70: 072004.
- 7 M.N. Achasov et al. (SND Collaboration) Study of  $e^+e^- \rightarrow \omega \pi^0 \rightarrow \pi^0 \pi^0 \gamma$  in the energy range 1.05–2.00 GeV with SND. Phys. Rev., 2013, D88: 054013.
- 8 M.N. Achasov et al. (SND Collaboration) The Process  $e^+e^- \rightarrow \omega \pi^0 \rightarrow \pi^0 \pi^0 \gamma$  up to 1.4 GeV. Phys. Lett., 2000, B486: 29–34.
- 9 K.W. Edwards et al. (CLEO Collaboration) Resonant structure of  $\tau \to 3\pi\pi^0 \nu_{\tau}$  and  $\tau \to \omega \pi \nu_{\tau}$  decays. Phys. Rev., 2000, D61: 072003.
- 10 R. Arnaldi et al. (NA60 Collaboration) Study of the electromagnetic transition form factors in  $\eta \to \mu^+ \mu^- \gamma$  and  $\omega \to \mu^+ \mu^- \pi^0$  decays with NA60. Phys. Lett., 2009, B677: 260–266.

- 11 V.M. Aul'chenko et al. (SND Collaboration) Measurement of the  $e^+e^- \rightarrow \eta \pi^+\pi^-$  cross section in the center-of-mass energy range 1.22–2.00 GeV with the SND detector at the VEPP-2000 collider. Phys. Rev., 2015, D91: 052013.
- 12 M.N. Achasov et al. (SND Collaboration) Measurement of the  $e^+e^- \rightarrow \eta \pi^+\pi^-$  cross section in the  $\sqrt{s} = 1.04$  GeV–1.38 GeV energy range with a spherical neutral detector at the VEPP-2M collider. JETP Lett., 2010, 92: 80.
- 13 B. Aubert et al. (BABAR Collaboration) The  $e^+e^- \rightarrow 2(\pi^+\pi^-)pi^0$ ,  $2(\pi^+\pi^-)\eta$ ,  $K^+K^-\pi^+\pi^-\pi^0$  and  $K^+K^-\pi^+\pi^-\eta$ Cross Sections Measured with Initial-State Radiation. Phys. Rev., 2007, D76: 092005 [Erratum ibid, 2008, D77: 119902].
- 14 B. Aubert et al. (BABAR Collaboration) The  $e^+e^- \rightarrow 3(\pi^+\pi^-)$ ,  $2(\pi^+\pi^-\pi^0)$  and  $K^+K^-2(\pi^+\pi^-)$  cross sections at center-of-mass energies from production threshold to 4.5 GeV measured with initial-state radiation. Phys. Rev., 2006, D73: 052003.