



Preliminary results  
on pion form factor  
at CMD-3

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# Motivation

Cross section  $e^+e^- \rightarrow \pi^+\pi^-$  is the main channel for  $e^+e^- \rightarrow$  hadron production at  $2E < 1 \text{ GeV}$

Total hadronic cross section:

$$R(s) = \frac{\sigma^0(e^+ e^- \rightarrow \gamma^* \rightarrow \text{hadrons})}{\sigma^0(e^+ e^- \rightarrow \gamma^* \rightarrow \mu^+ \mu^-)}$$

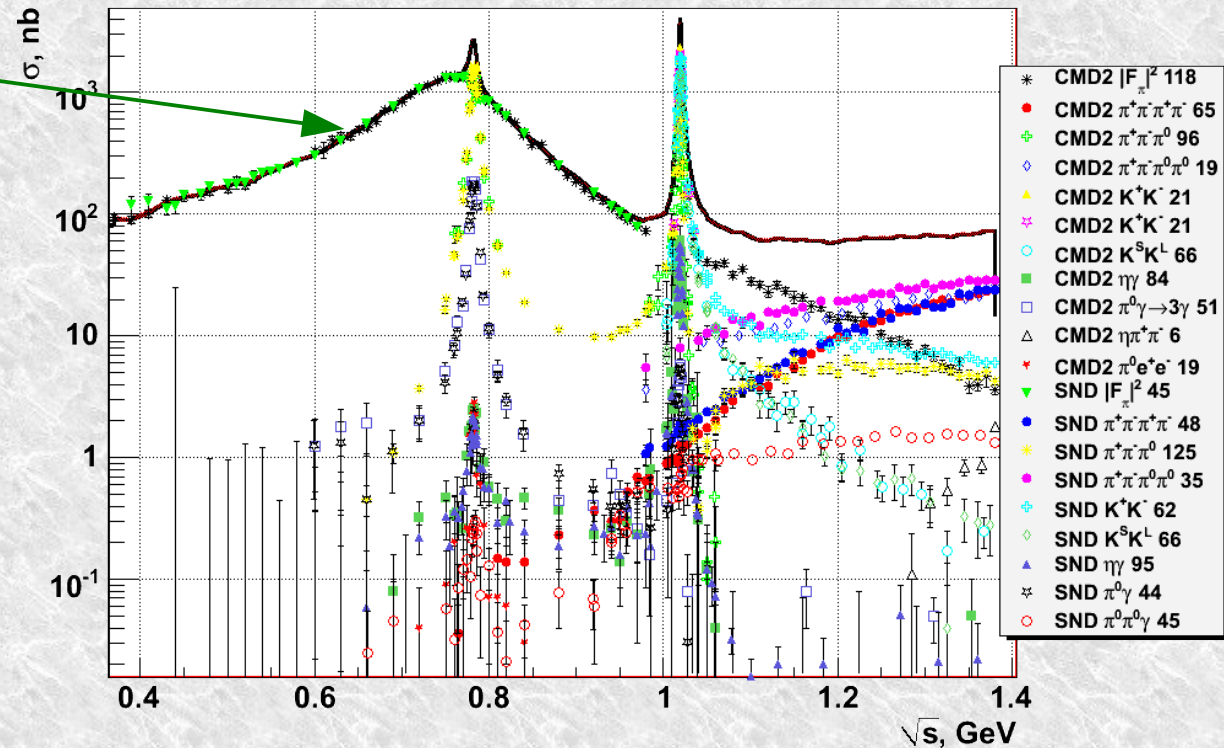
should be known for calculation of:

$\alpha_{\text{QED}}(M_Z)$  - used in precise predictions of EW physics,

(better precision is required in case of ILC physics)

it is essential for the interpretation of precision measurements of:

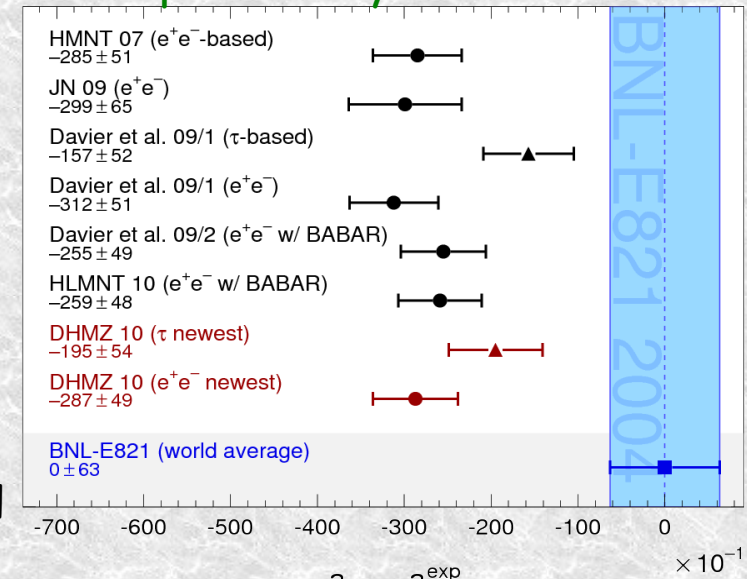
muon  $(g-2)$  - good test of SM



# SM prediction for muon g-2

ArXiv:1010.4180, arXiv:1105.3149

$\Delta \text{Exp} - \text{Theory} \sim 3.3 - 3.6\sigma$



The anomalous magnetic moment of the muon

$$a_{\mu}^{\text{experimental}} = (g-2)_{\mu} / 2$$

Experimental world average  $a_{\mu} = 11\,659\,208.9 \pm 6.3 \times 10^{-10}$

Theoretical prediction  $\delta a_{\mu} = \pm 4.9 \times 10^{-10}$

HLMNT 11

Hadronic content of  $a_{\mu}$  calculated

From measured cross-section by dispersion integral

LO hadronic  $694.1 \pm 4.3 \times 10^{-10}$  HLMNT 11

main channels contribution to precision at  $\sqrt{s} < 1.8 \text{ GeV}$

From direct integration  
Without model constraints

$\pi^+\pi^-$	$505.65 \pm 3.09$	
$\pi^+\pi^-2\pi^0$	$\pm 1.15$	
$\pi^+\pi^-\pi^0$	$\pm 0.99$	(mostly from omega region)
.....		

Light-by-light  $10.5 \pm 2.6$  Prades, de Rafael & Vainshtein

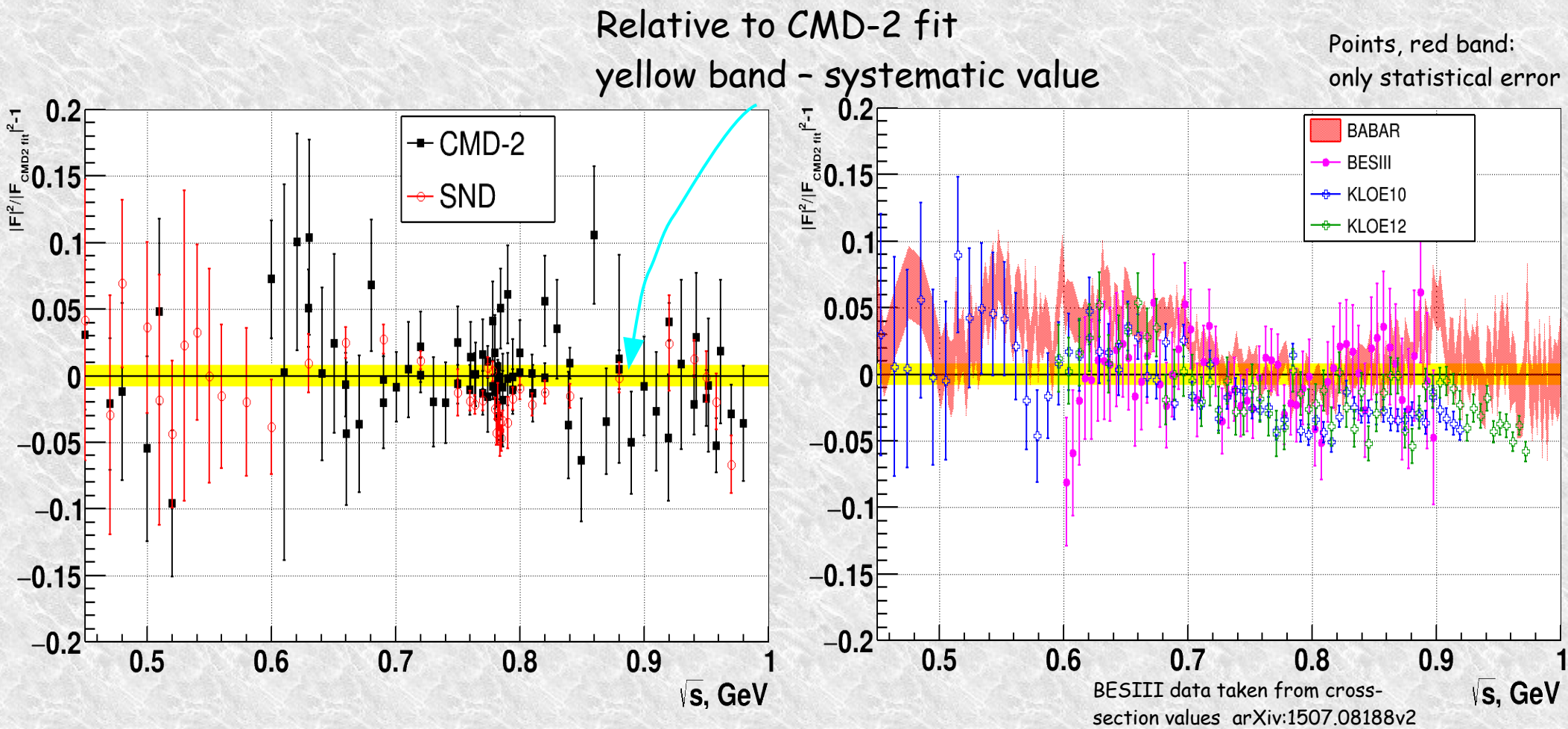
need more theory input,

with help of experimental transition form factors

New g-2 experiments at FNAL and J-PARC have plans to reduce error to  $1.5 \times 10^{-10}$

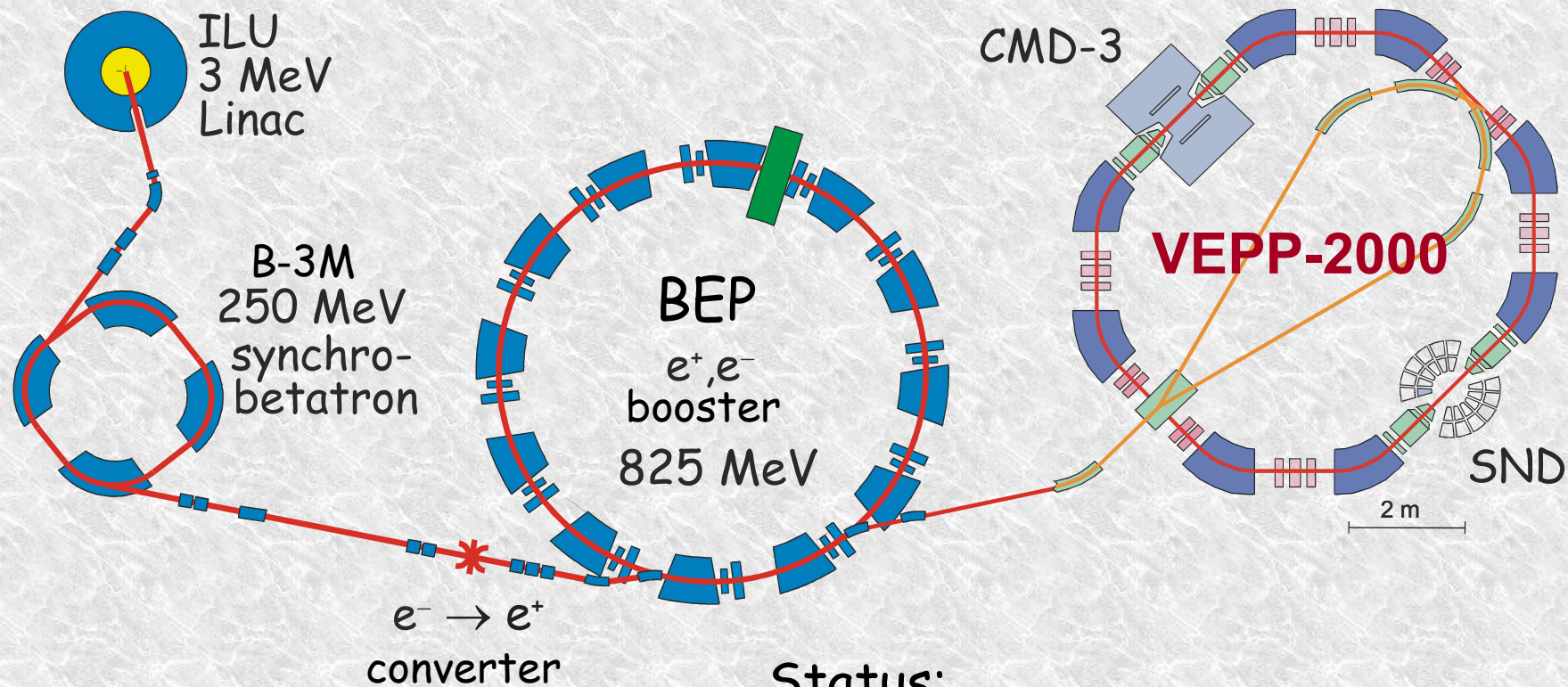
$\pi^+\pi^-$  gives the main contribution to hadronic value and overall theoretical precision of  $a_{\mu}$

# Published cross section $e^+ e^- \rightarrow \pi^+ \pi^-$



Local inconsistencies larger than claimed systematic errors seen

# VEPP-2000 collider



- Up to 2 GeV c.m. Energy
- VEPP-2000 uses unique "round beams" optic, which gives additional gain in luminosity and will provide:

$$L=10^{32} \text{ cm}^{-2}\text{s}^{-1}, \sqrt{s}=2.0 \text{ GeV}$$

Status:

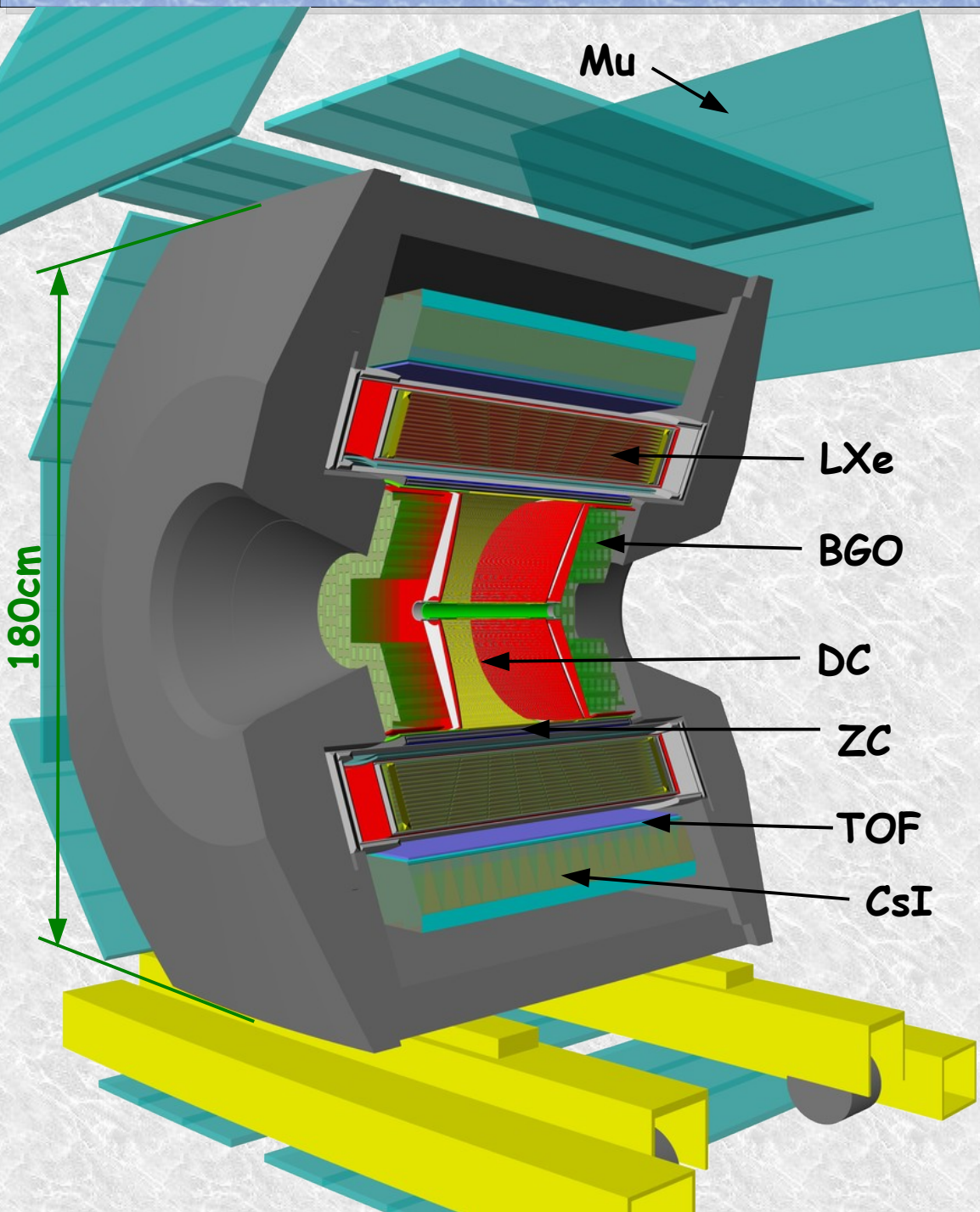
2010 - start of experiments

2013-2015 - upgrade of positron injection facility

Plans:

$\approx 100 \text{ pb}^{-1}$  per detector per year

# CMD-3 Detector



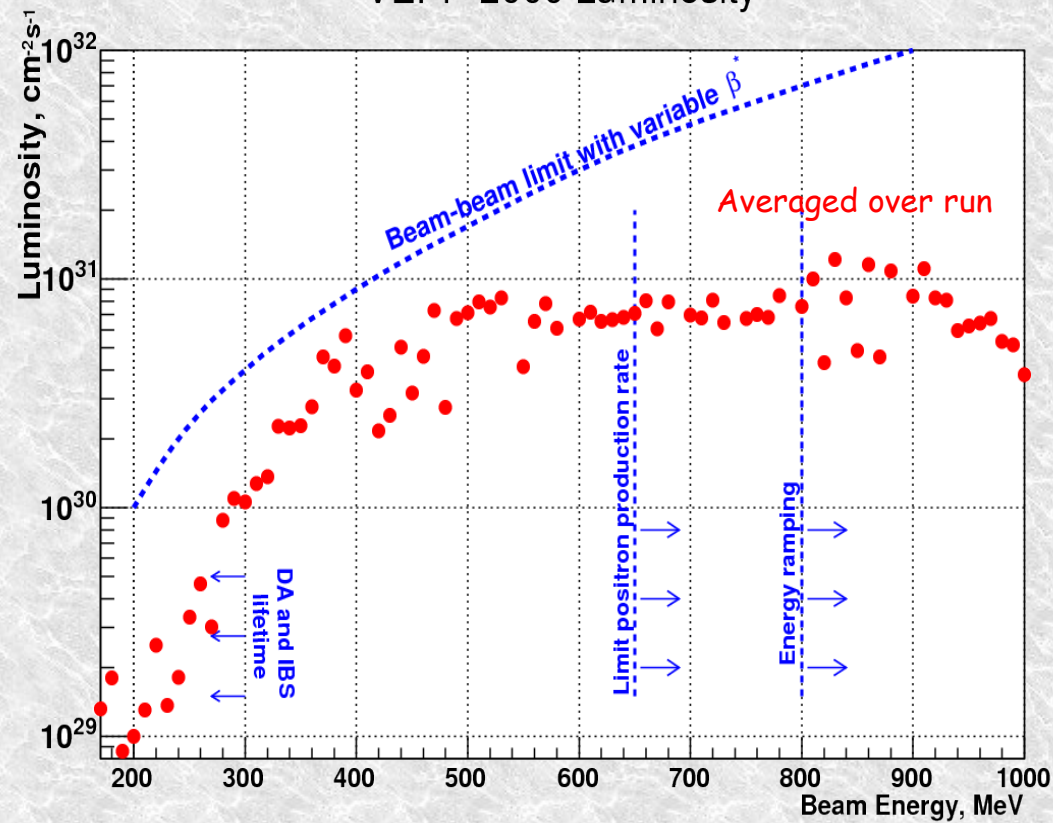
Advantages for this analysis compared to previous CMD-2:

- x new drift chamber with x2 better spatial resolution, higher B field
- better efficiency
- better momentum resolution

- x Unique LXe calorimeter with 7 ionization layers with strip readout
- ~2mm measurement of conversion point, tracking capability, shower profile (from 7 layers + CsI)

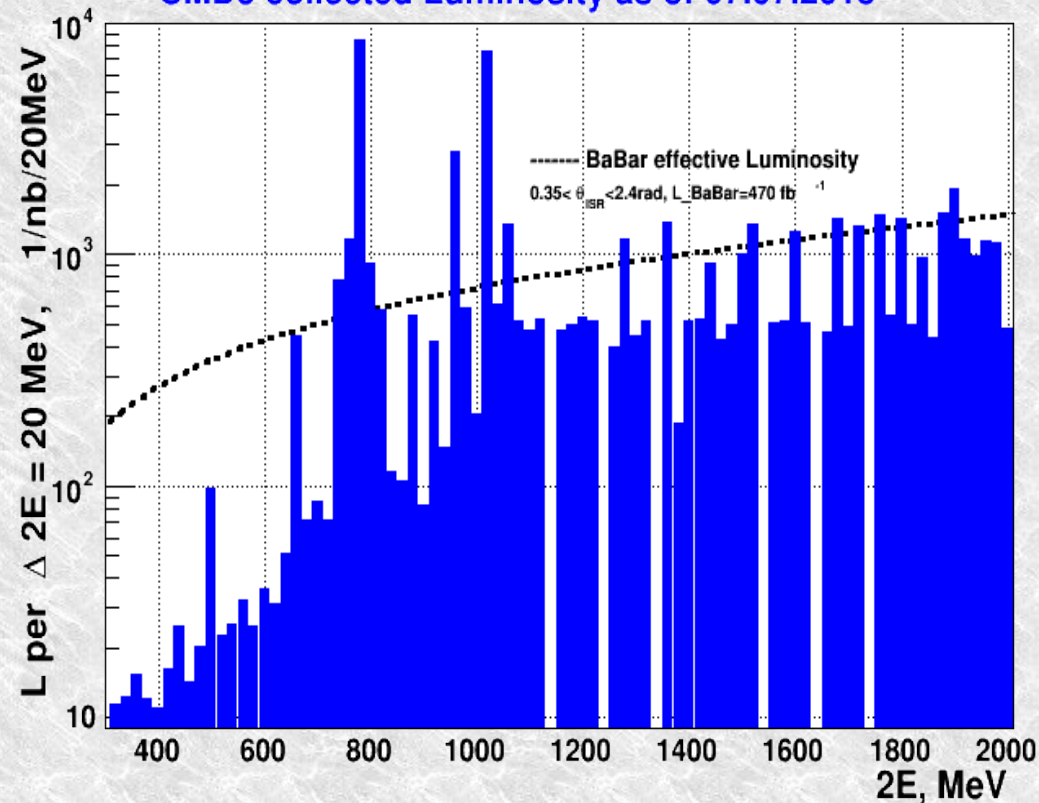
# Collected Luminosity

VEPP-2000 Luminosity



The  $10^{31} \text{ cm}^{-2} \text{ s}^{-1}$  luminosity at  $\sqrt{s}=2.0 \text{ GeV}$  was reached  
 Currently the luminosity at high energy is limited by a deficit of positrons and maximum energy of the booster (now 825 MeV), after upgrade it will gain a factor of 10

CMD3 collected Luminosity as of 07.07.2013



Collected L  $\sim 60 \text{ pb}^{-1}$  per detector

- 8.3  $\text{pb}^{-1}$   $\omega$  - region
- 9.4  $\text{pb}^{-1}$   $< 1 \text{ GeV}$  (except  $\omega$ )
- 8.4  $\text{pb}^{-1}$   $\phi$  - region
- 34.5  $\text{pb}^{-1}$   $> 1.04 \text{ GeV}$

# $e+e^- \rightarrow \pi^+\pi^-$ by CMD3

Very challenging channel as needs to be measured at best systematical precision ~ a few per mil

But... Clean topology of collinear events (mostly without physical background)

Overall corrections at the level of a few percent

Plans to reduce systematic error from 0.6-0.8% (by CMD2)  $\rightarrow$  0.35% (CMD3)

## 3 Key components for this precise measurement:

1) PID - particle separation

2) Acceptance determination  
spatial angle of detection

3) Radiative correction, MC generators

... efficiencies

... beam energy precision

Many systematic studies rely on high statistics



# Event selection

- Two charged collinear tracks:

$$|\Delta \varphi| < 0.15, \quad |\Delta \theta| < 0.25$$

$$Q_1 + Q_2 = 0$$

- Vertex position close to interaction point:

$$\rho_{\text{average}} < 0.3 \text{ cm}, \quad |Z_{\text{average}}| < 5 \text{ cm}$$

$$|\Delta \rho| < 0.3 \text{ cm}, \quad |\Delta Z| < 5 \text{ cm}$$

- Fiducial volume inside good region of DCh:

$$1. < (\pi + \theta^+ - \theta^-) / 2 < \pi - 1.$$

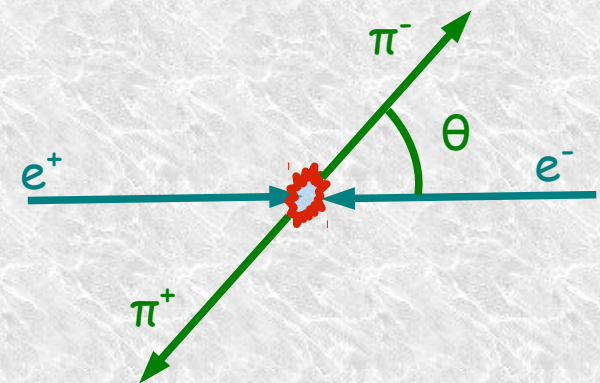
- Quality of selected tracks:

$$\chi^2 / \text{ndf} < 10, \quad N_{\text{hits}} \geq 10$$

- Filtration of low momentum and cosmic background:

$$0.45 E_{\text{beam}} < p^+, p^- < E_{\text{beam}} + 100 \text{ MeV}/c$$

Simple event signature with  
2 back to back charged particles



Data sample includes events with:  $e^+e^-$ ,  $\mu^+\mu^-$ ,  $\pi^+\pi^-$ , cosmic muons  
Mostly doesn't have any other background at  $\sqrt{s} < 1 \text{ GeV}$

# Event separation

Particle ID can be done by momentum or energy deposition

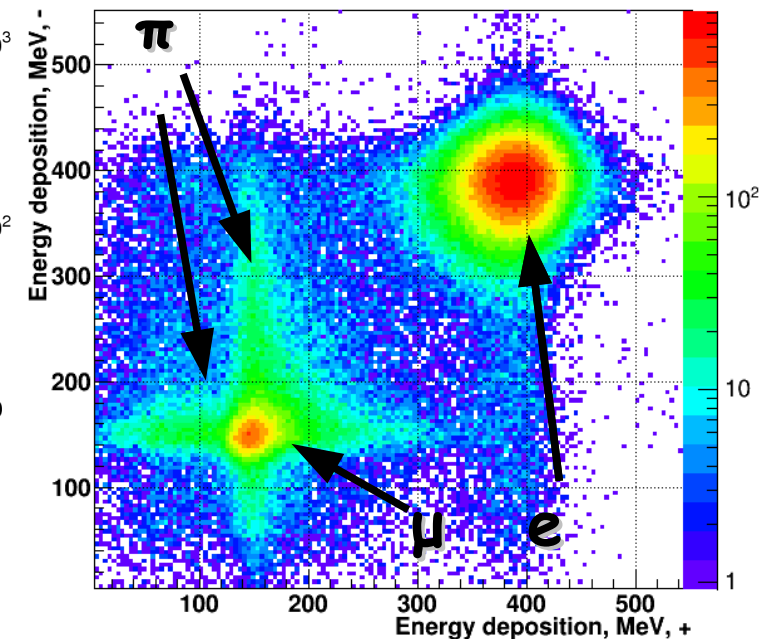
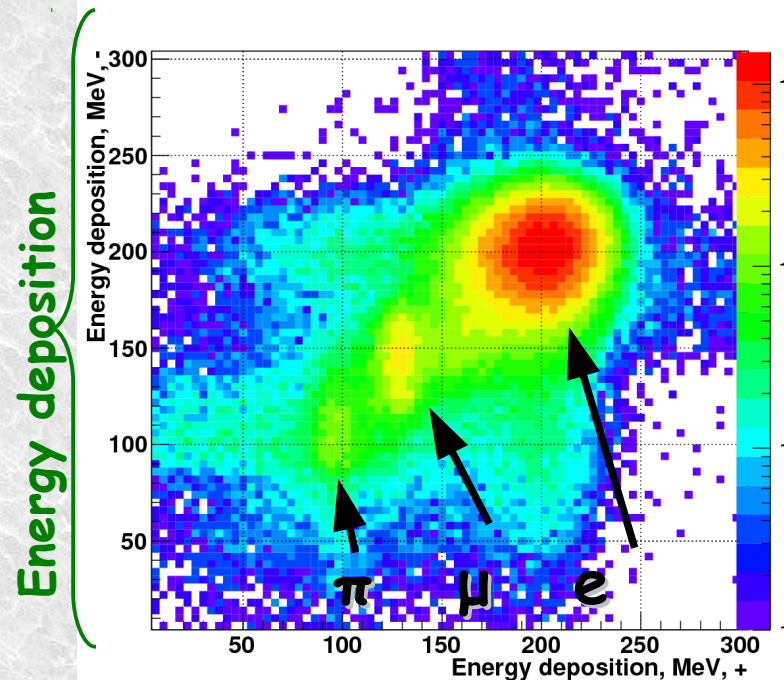
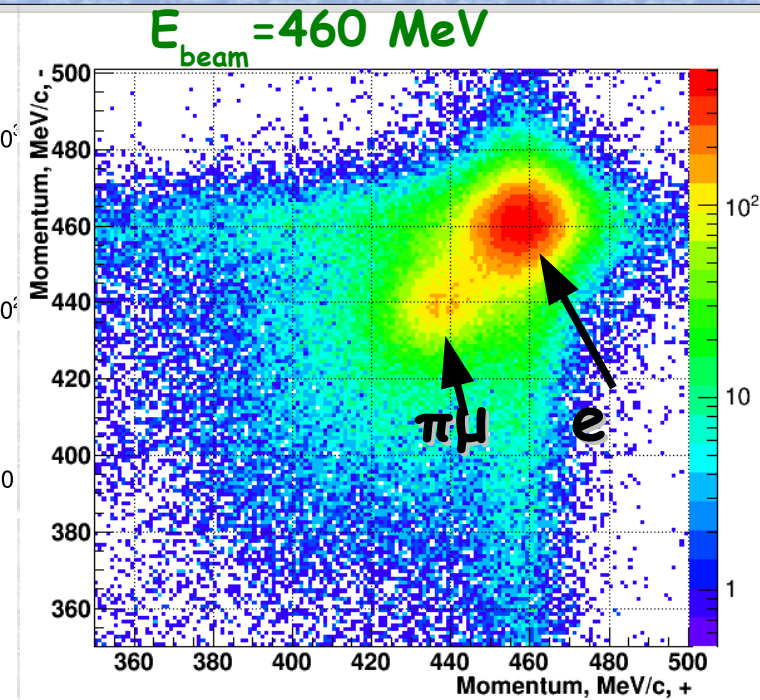
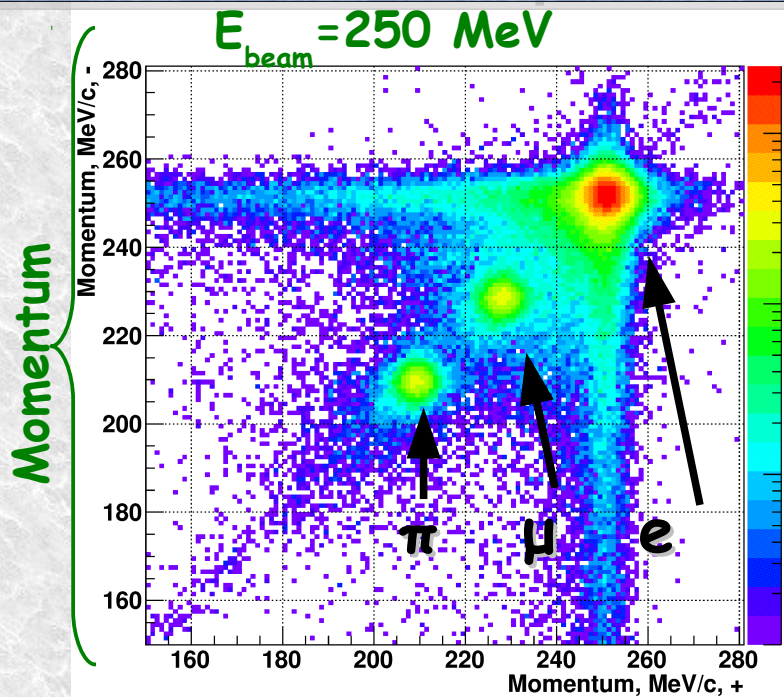
At low energies momentum resolution of DCh enough to separate different types

At higher energies Electron shower in calorimeter far away from MIPs

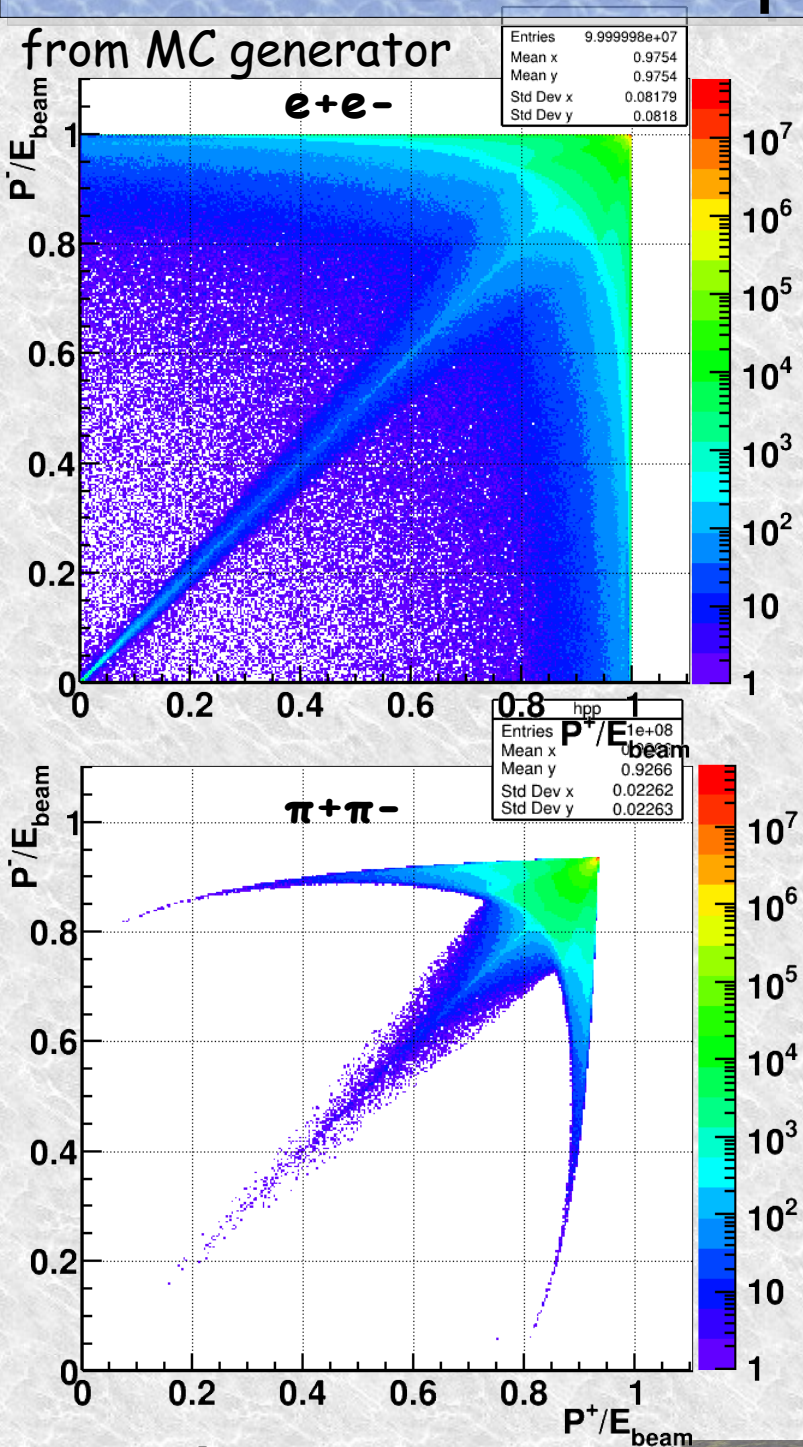
Both methods can be used separately for cross-check

$N_{\mu\mu}$  can be fixed (or not) from QED

23 September 2015, PHIPSI15, Hetero



# Event separation by momentum



For particle separation:

As input: momentum spectra for  $ee, \pi\pi, \mu\mu$  events from MC generator (in applied selection criteria) + cosmic,  $3\pi$  background from data(MC)

Generated distributions are convoluted with detector response function which include (with mostly all free parameters in it):

- x momentum resolution,
- x bremsstrahlung of electron on vacuum tube,
- x pion decay in flight

$N_{\pi\pi}/N_{ee}$  obtained as result of binned likelihood minimization

# Event separation by energy deposition

At this moment: Full energy deposition in LXe+CsI calorimeter is used for particle separation

As input: PDF distributions are taken from MC or data itself (fitted by analytical function, and used with some free parameters)

x Electron - described by mostly free function

x Muons - from simulation + additional smearing (plan to be taken from data)

x Pions - from  $\phi \rightarrow 3\pi$ ,  $\omega \rightarrow 3\pi$  events

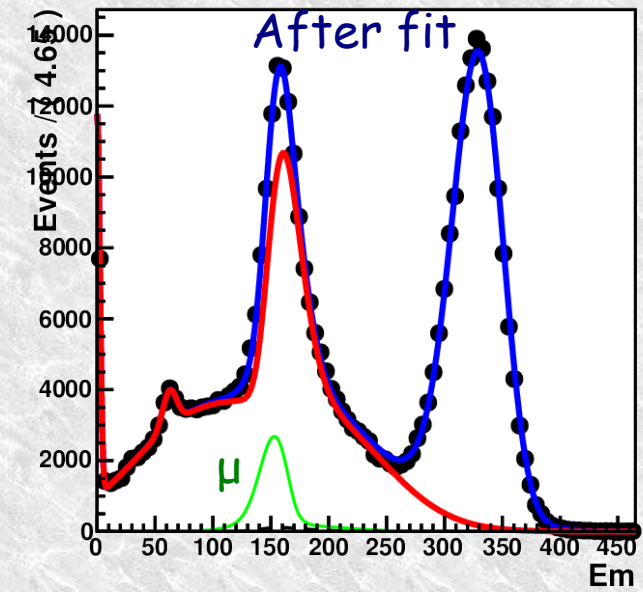
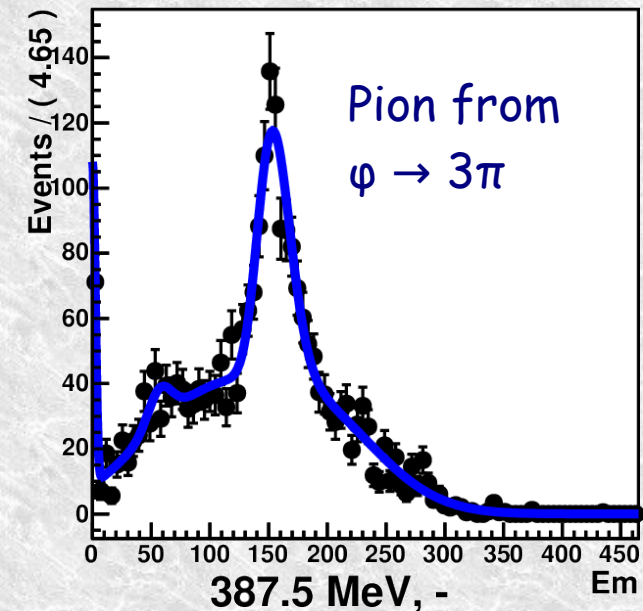
x Cosmic - from data itself (events are selected by vertex position)

$N_{\pi\pi}/N_{ee}$  obtained as result of binned likelihood minimization

As plans: to exploit information about shower profile (energy deposition in 7 layers of LXe, + CsI)

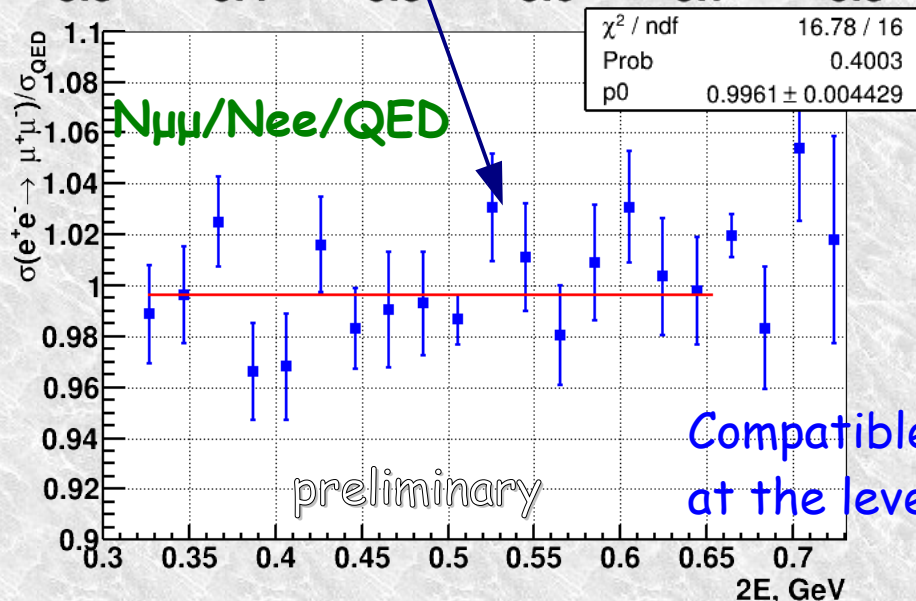
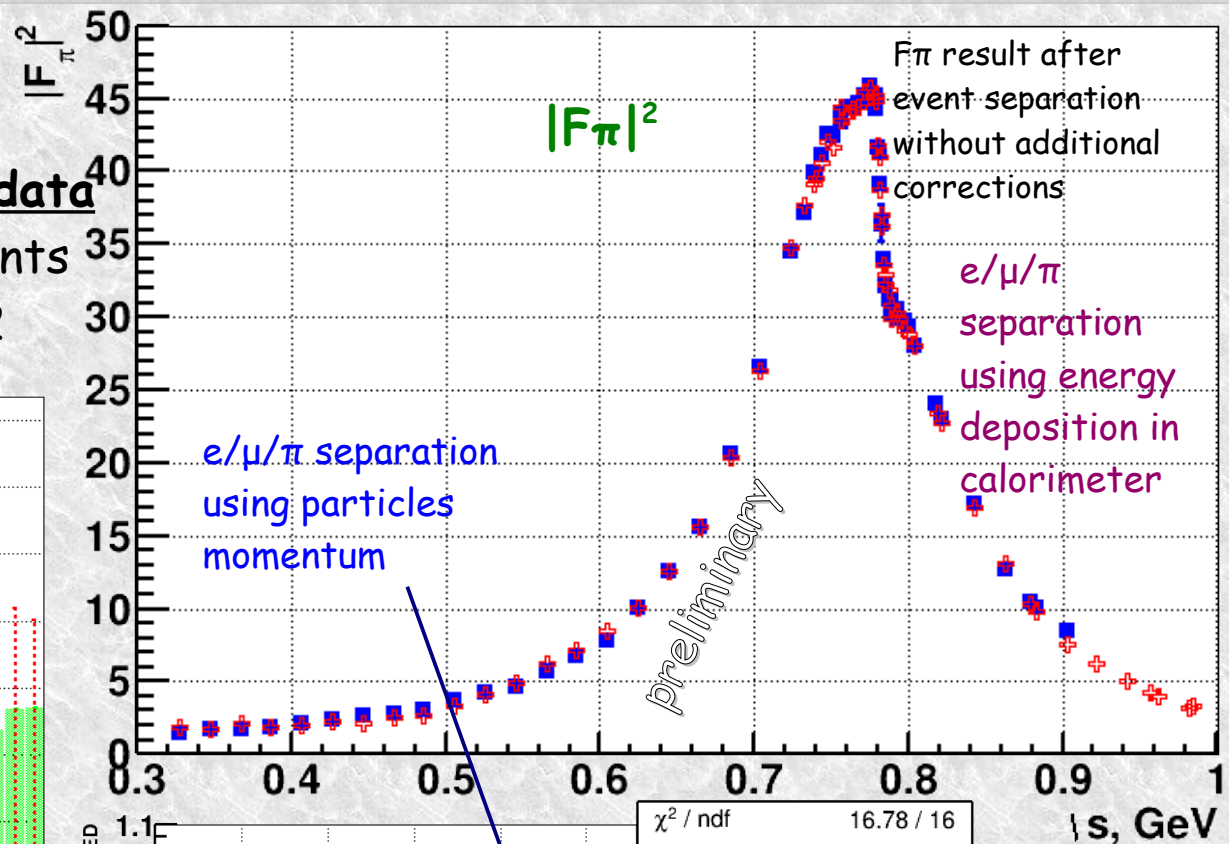
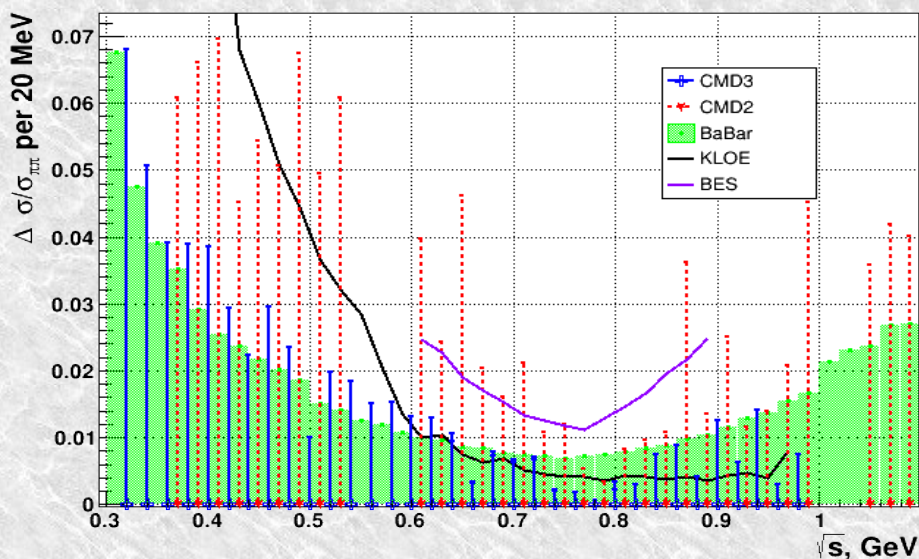
Neural net can be used for event classification

387.5 MeV, pi-



# $e^+e^- \rightarrow \pi^+\pi^-$ by CMD-3

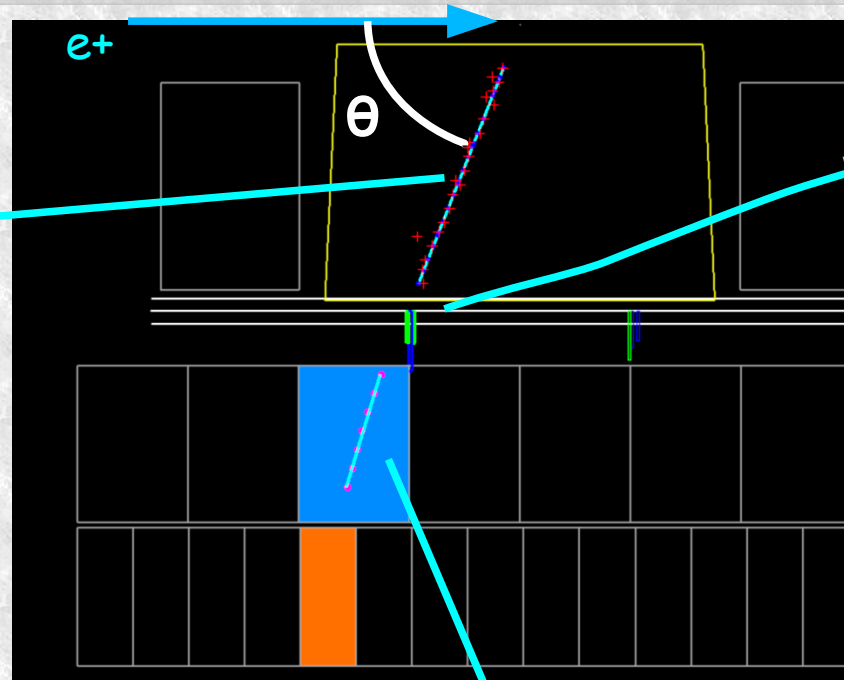
Statistical precision of cross section measurement for **2013 data** is at the same level as other experiments and a few times better than at CMD-2



# Precision of fiducial volume

Polar angle measured by DC chamber

with help of charge division method (Z resolution  $\sim 2\text{mm}$ ),  
Unstable, depends on calibration and thermal stability of electronic  
Calibration done relative to ZC (LXe)



## ZC chamber

multiwire chamber with 2 layers and with strip readout along Z coordinate

strip size: 6mm

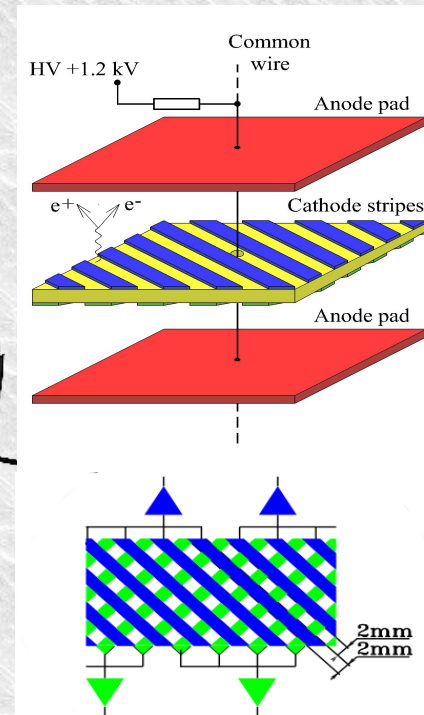
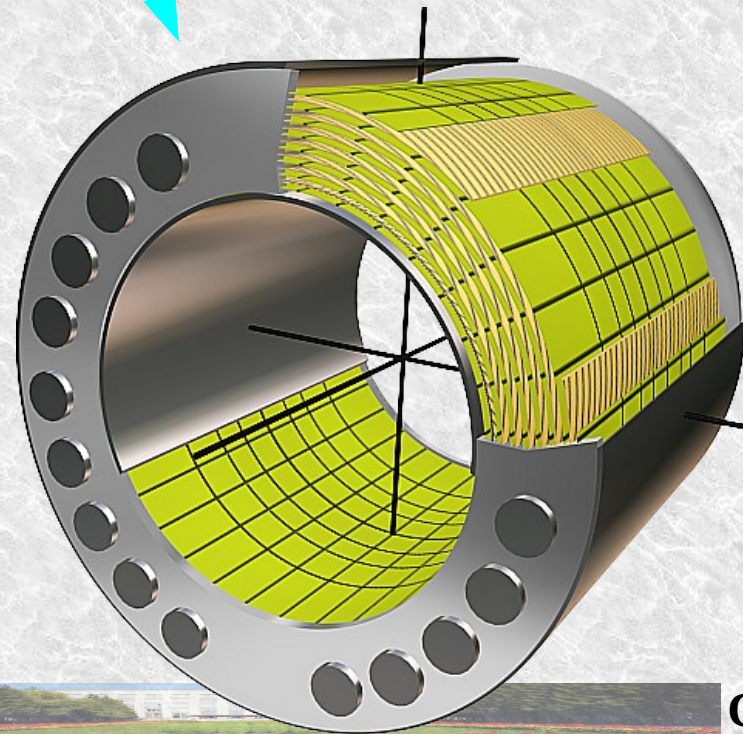
Z coordinate resolution  $\sim 0.7\text{ mm}$  (for  $\theta_{\text{track}} \sim 1\text{ rad}$ )

## LXe calorimeter

ionization collected in 7 layers with cathode strip readout,

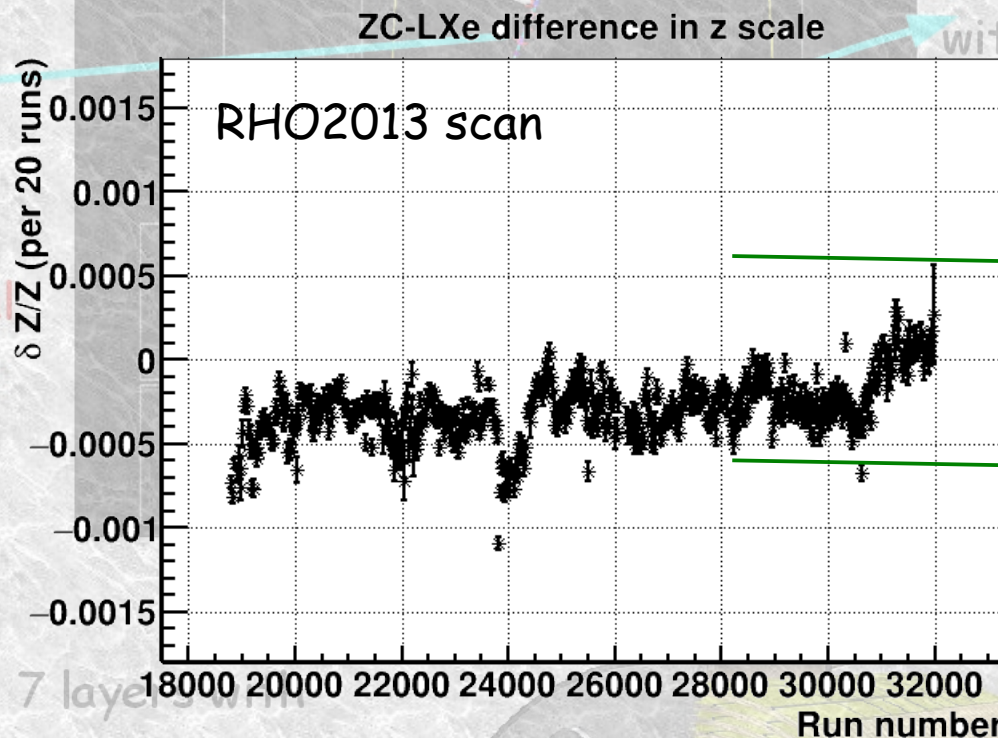
combined strip size: 10-15 mm  
Coordinate resolution  $\sim 2\text{mm}$

Both subsystem with strip precision  $< 100\ \mu\text{m}$   
give  $< 0.1\%$  in Luminosity determination



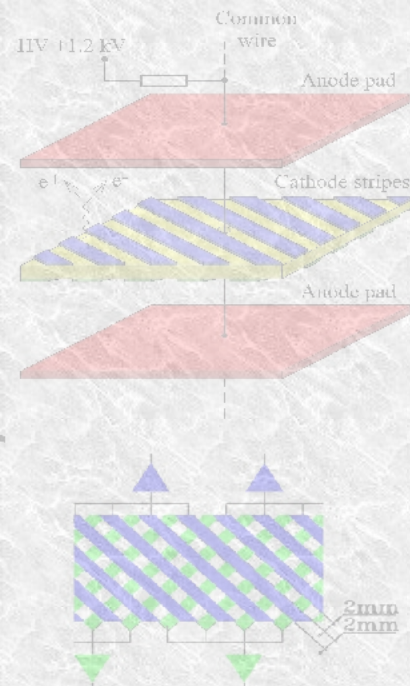
# Precision of fiducial volume

Monitoring of z-measurement between ZC vs LXe



Variation because of  
DCh instability,  
different B field,  
ZC noise level

$\pm 0.1\%$  Luminosity  
determination at  $\theta > 1\text{rad}$



Polar angle measured by  
DC chamber  
with help of charge  
division method  
(Z resolution  $\sim 2\text{mm}$ ),  
Unstable, depend on  
calibration and thermal  
stability of electronic  
Calibration done  
relative to ZC (LXe)

## LXe calorimeter

ionization collected in 7 layers  
cathode strip readout,

combined strip size: 10-15 mm  
Coordinate resolution  $\sim 2\text{mm}$

Both subsystem  
with strip precision  $< 100\ \mu\text{m}$   
give  $< 0.1\%$  in Luminosity determination

# MC generators

High experimental precision relies on theoretical precision of MC tools:

Most recent  $e^+e^- \rightarrow e^+e^-$  (gamma) generators

include exact  $O(\alpha)$  + some parts from High Order terms:

MCGPJ (VEPP-2000) - accuracy 0.2% for  $e^+e^-$ ,  $\pi^+\pi^-$  etc

1 real photon (from any particle)

+ photon jets along all particles (collinear Structure function)

BabaYaga@NLO (KLOE, BaBar) - 0.1% for  $e^+e^-$ ,  $\mu^+\mu^-$

Parton shower approach: n photons with angle distribution  
interference for 1 photon radiation

BHWIDE (LEP) - 0.5% ( $\sim 0.1\%$ ?),  $e^+e^-$

n real photons by Yennie-Frautschi-Suura (YFS) exponentiation method  
interference on  $O(\alpha)$  level

And there are other generators for different channels:

PHOKHARA (KLOE)  $\mu^+\mu^-$ ,  $\pi^+\pi^-$  etc

KKMC ( $\mu^+\mu^-$ ),

etc



# BabaYaga@NLO vs MCGPJ generators

BabaYaga@NLO used by KLOE, BaBar

MCGPJ used by Novosibirsk group

Selection cuts:

$$|\Delta\varphi| < 0.15, |\Delta\theta| < 0.25$$

$$1 < \theta_{\text{average}} < \pi - 1$$

$$P^{+-} > 0.45 E_{\text{beam}}$$

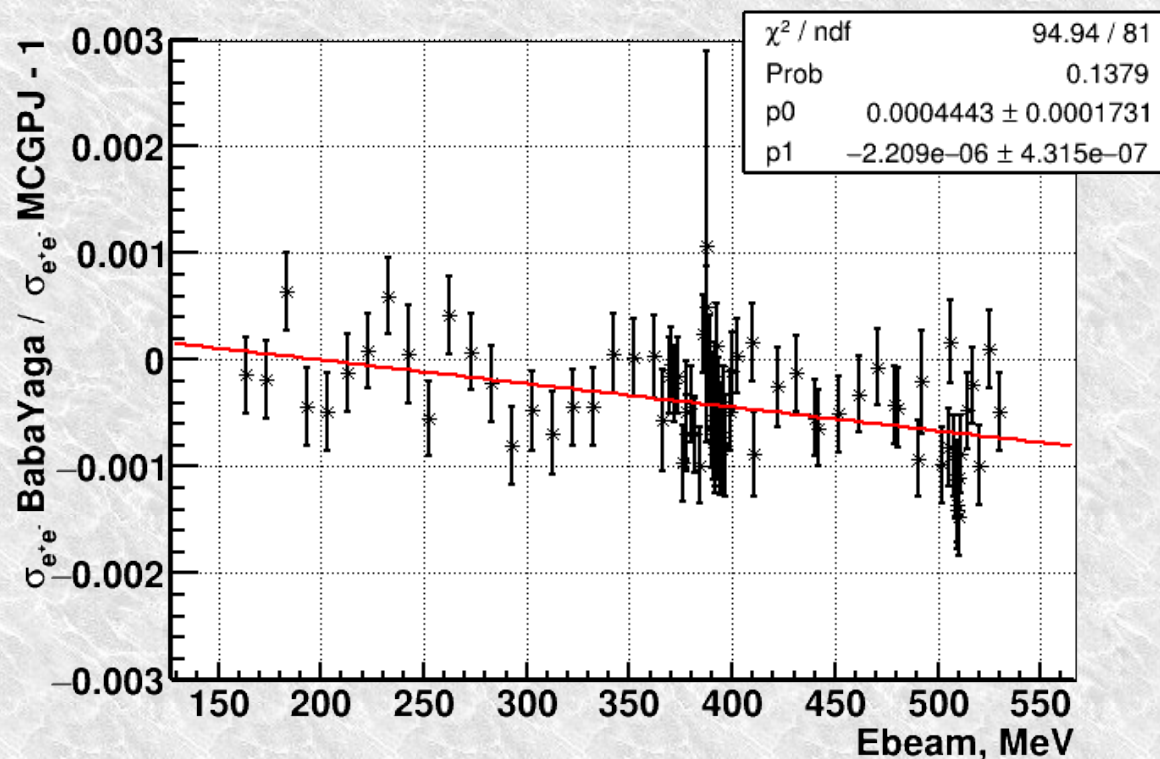
Calculated cross-section

at  $E_{\text{beam}} = 391.48 \text{ MeV}$

MCGPJ :  $751.671 \pm 0.034 \text{ nb}$

BabaYaga@NLO :  $751.218 \pm 0.059 \text{ nb}$

$$\Delta \sim 0.06\%$$



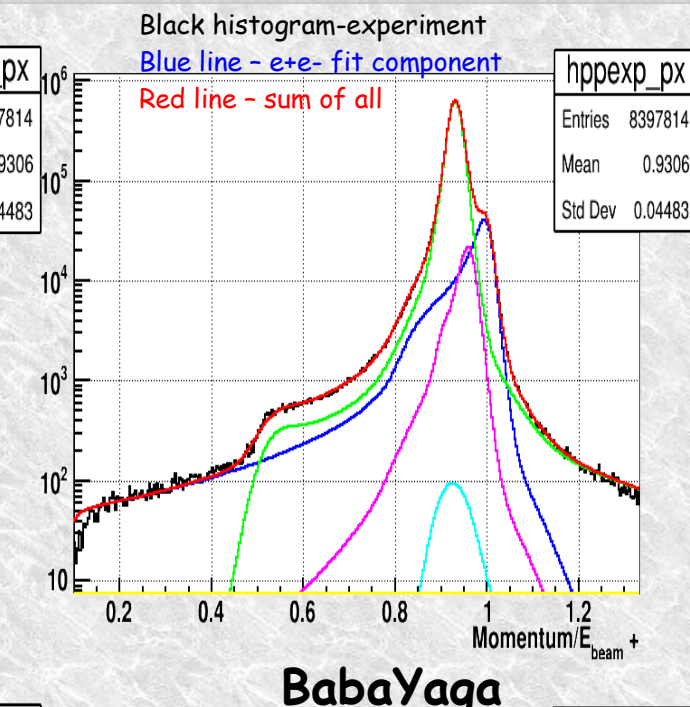
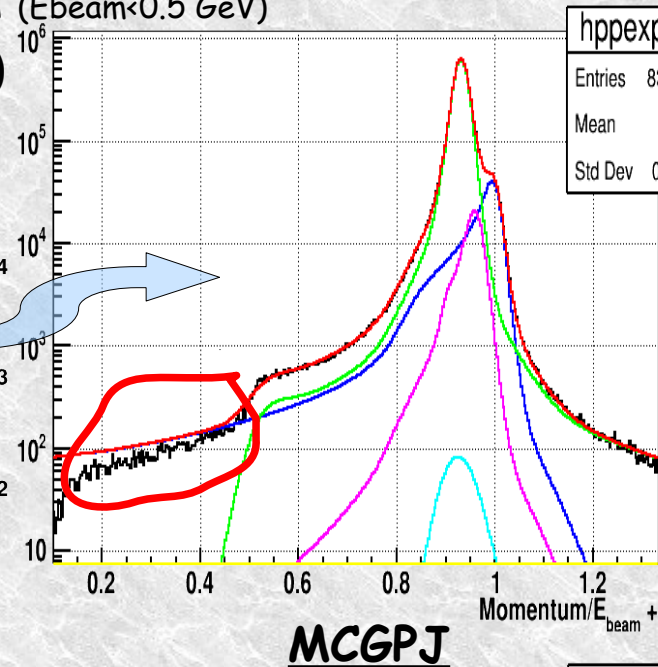
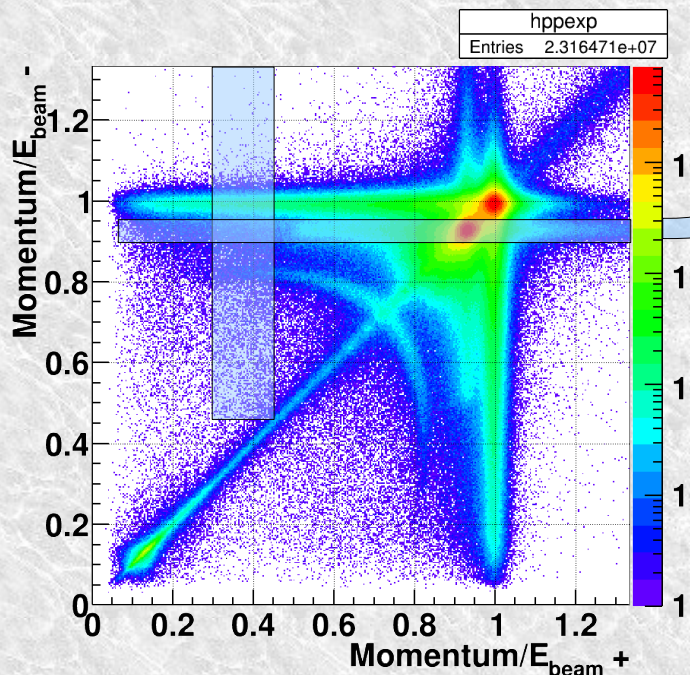
Integrated cross-section  
consistent at the level  $< 0.1\%$

BabaYaga@NLO  $\sim$  x1000 slower than MCGPJ

A discrepancy was observed in momentum distribution of experimental data vs fitted functions with input from MCGPJ

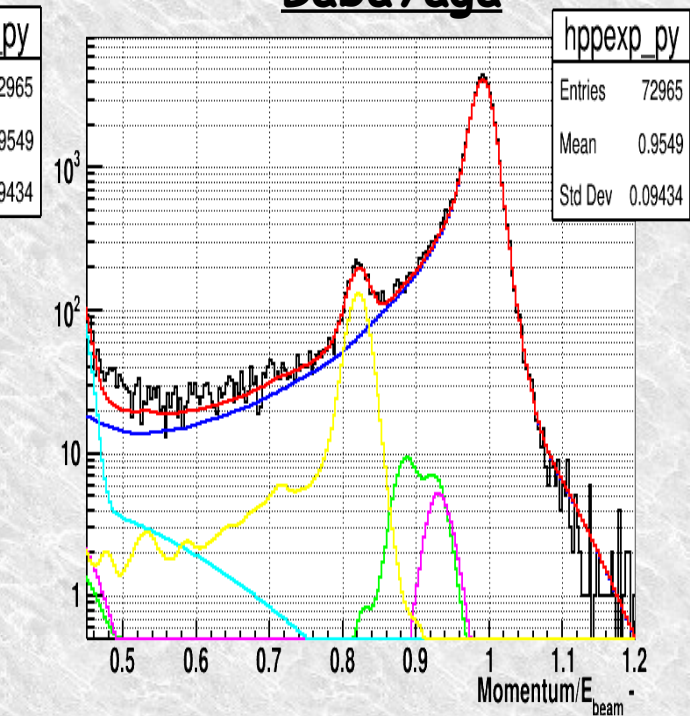
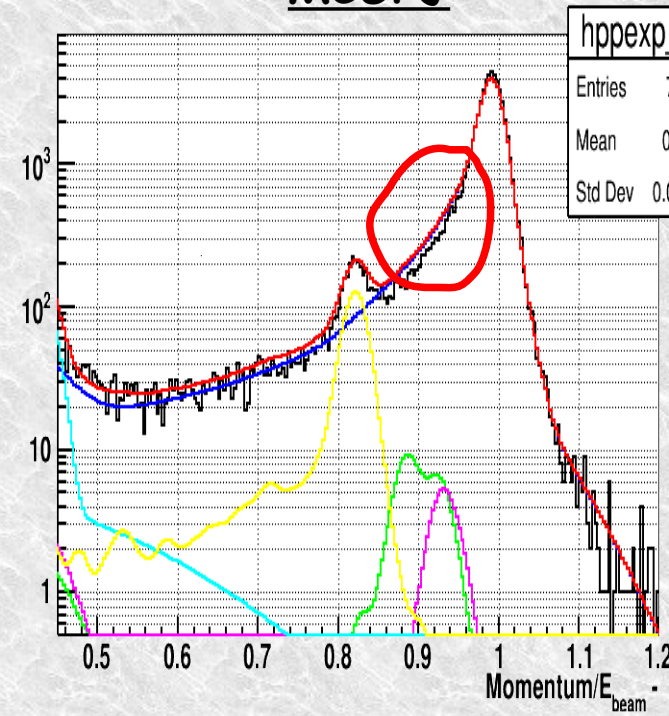
# BabaYaga @ NLO vs MCGPJ VS experiment

All events from RHO2013 scan ( $E_{\text{beam}} < 0.5 \text{ GeV}$ )  
 (~ 10 millions of  $e^+e^-$  and  $\pi^+\pi^-$ )



BabaYaga better describe experimental data

Looks like MCGPJ should be improved by adding angular distribution to photon jets



# $\pi^+\pi^-\pi^0$ background

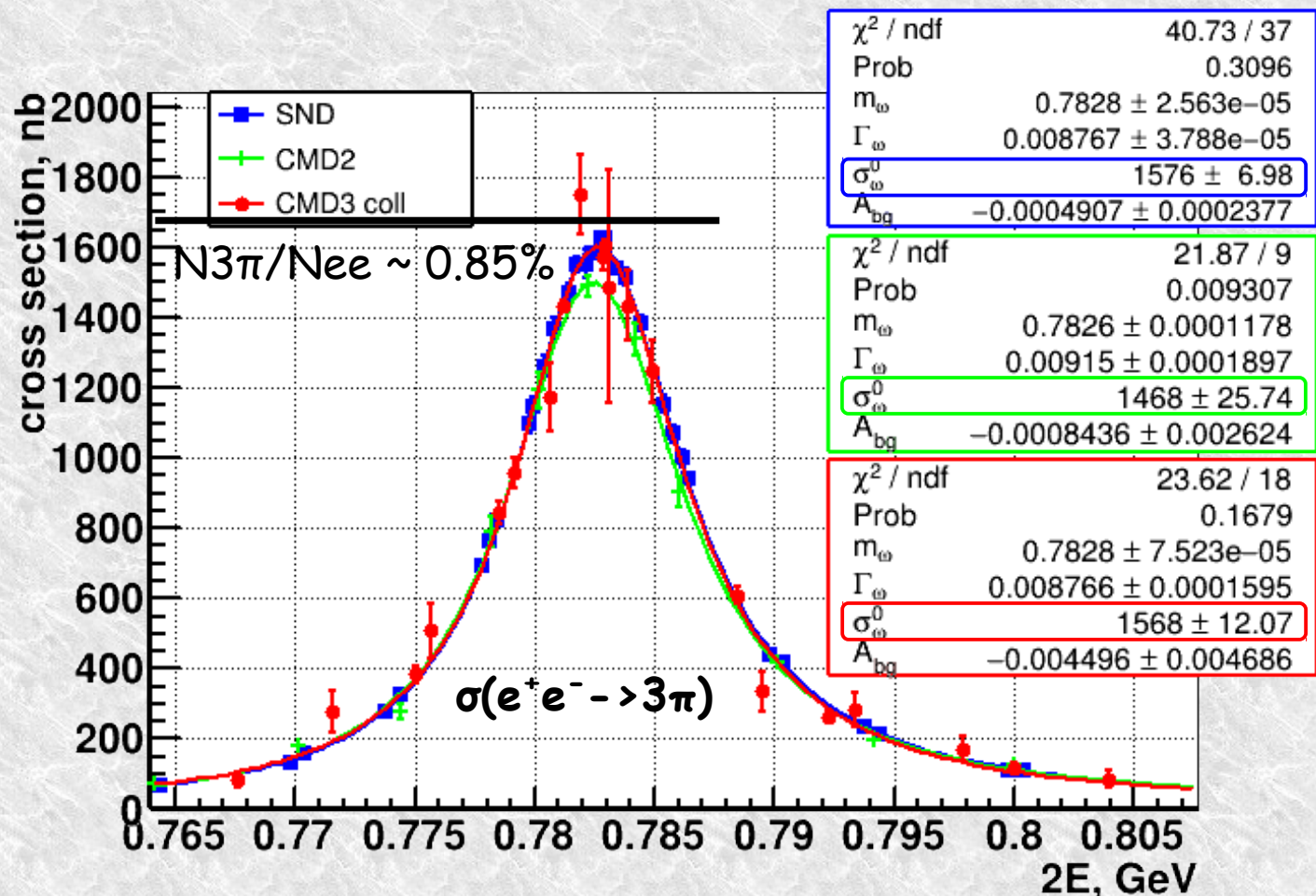
Only significant physical background in selected data sample:

$\pi^+\pi^-\pi^0$  on  $\omega$ -resonance

Contribution < 1%

This events well seen during particle separation by momentum distributions

Extracted  $\sigma(e^+e^- \rightarrow 3\pi)$  from collinear events (in phase space model) compatible with published results

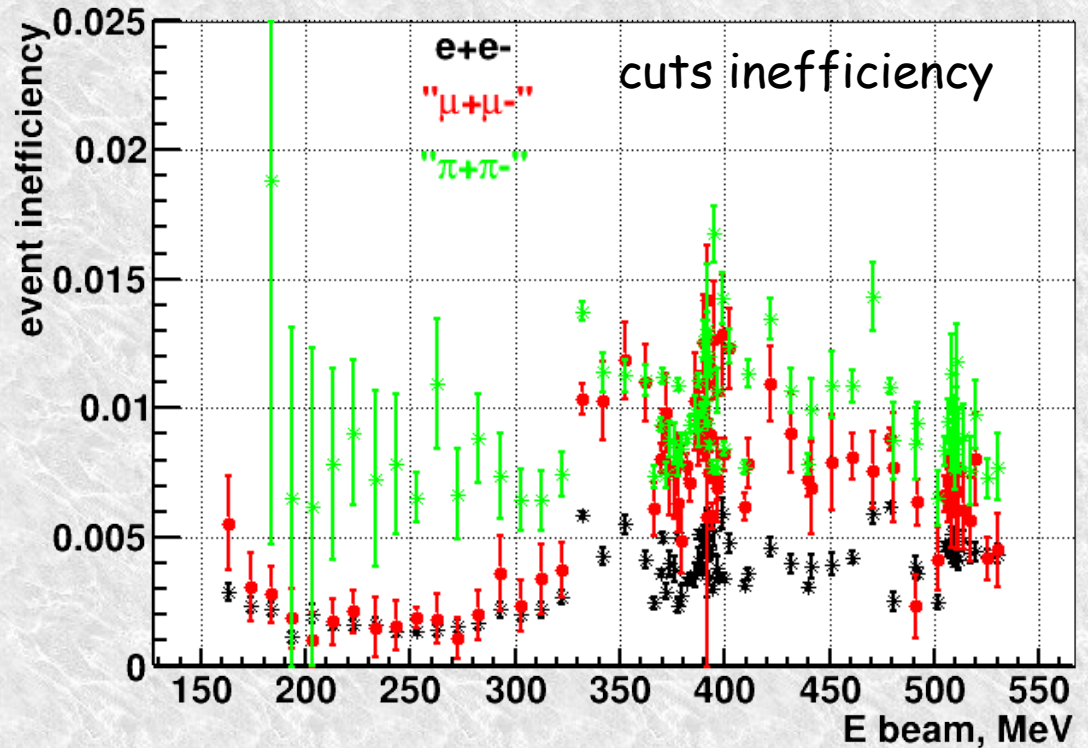


$\epsilon(3\pi) = 0.4833\%$  acceptance efficiency from simulation by phase space model

# efficiencies

Part of track reconstruction inefficiency  
from test events  
selected only by 2 collinear clusters in  
calorimeter  
-> check if a track was reconstructed  
or not

Inefficiency  $\sim 0.2-1\%$   
3-10 times less than was at CMD-2



Pion specific loss of events:

x decay in flight ( $\sim 6\%$  at 160 MeV)

(dominated at low energies)

x nuclear interaction on vacuum tube ( $< 1\%$ )

will be checked from  $\varphi \rightarrow 3\pi$ ,  $\omega \rightarrow 3\pi$  events

# Systematic $e^+e^- \rightarrow \pi^+\pi^-$ by CMD3

As our grand total(not reached yet)

Our goals are to reach systematic level up to 0.35%:

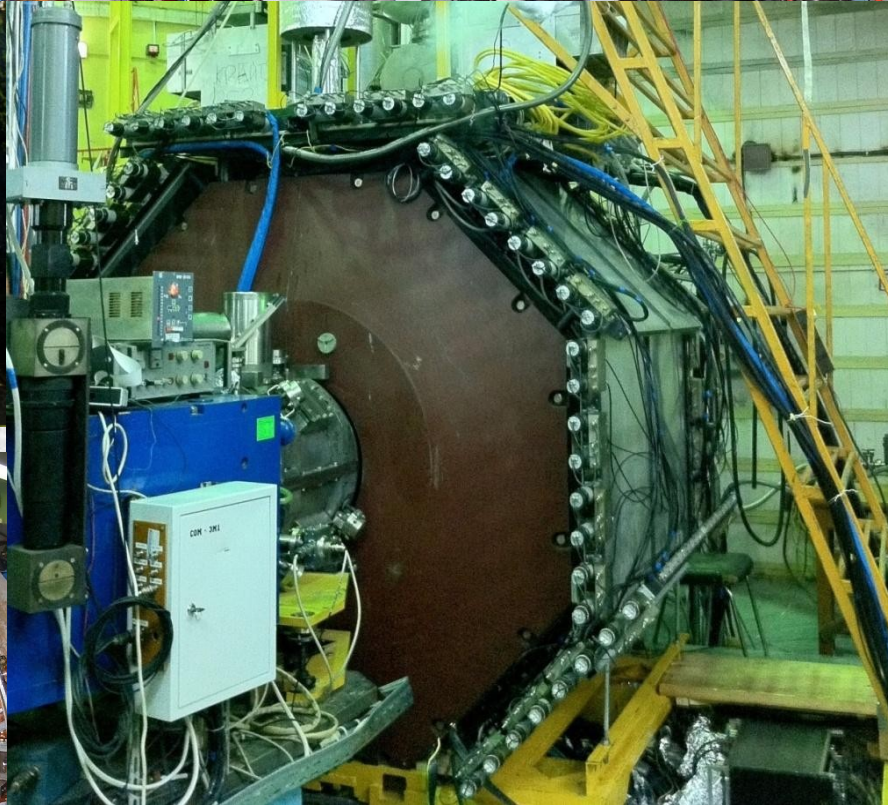
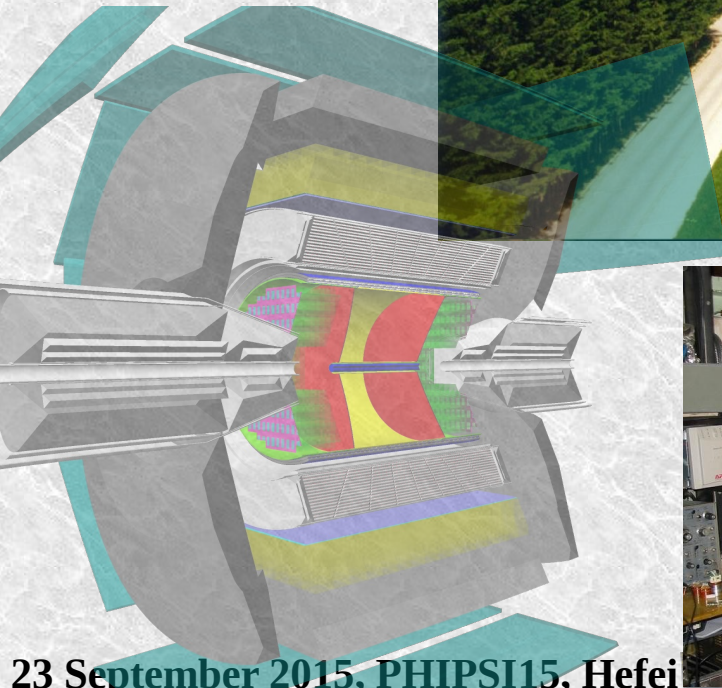
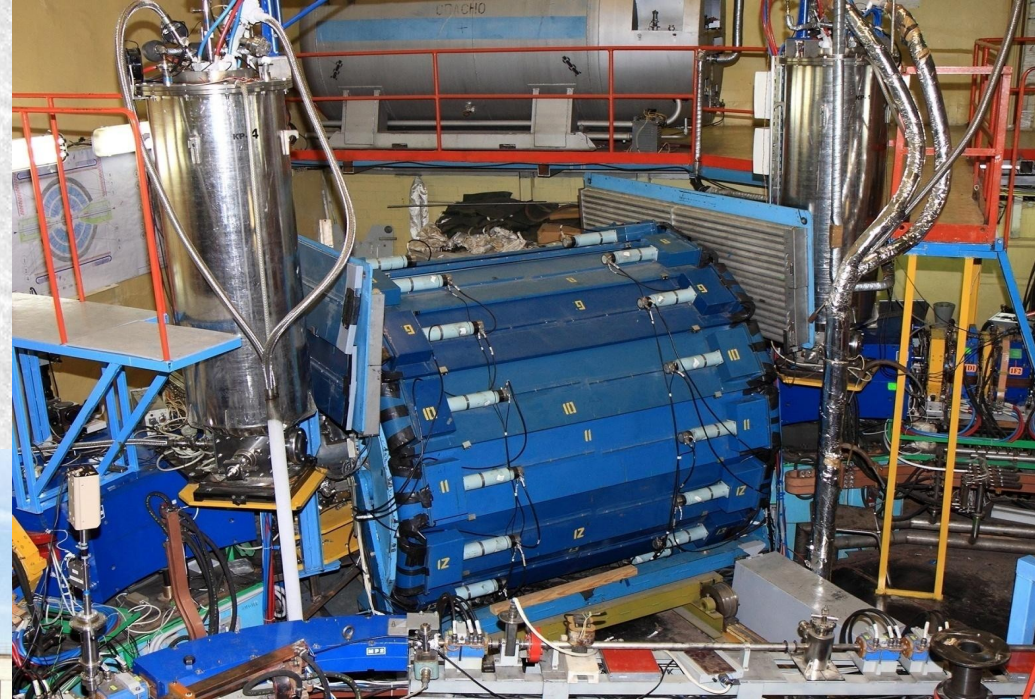
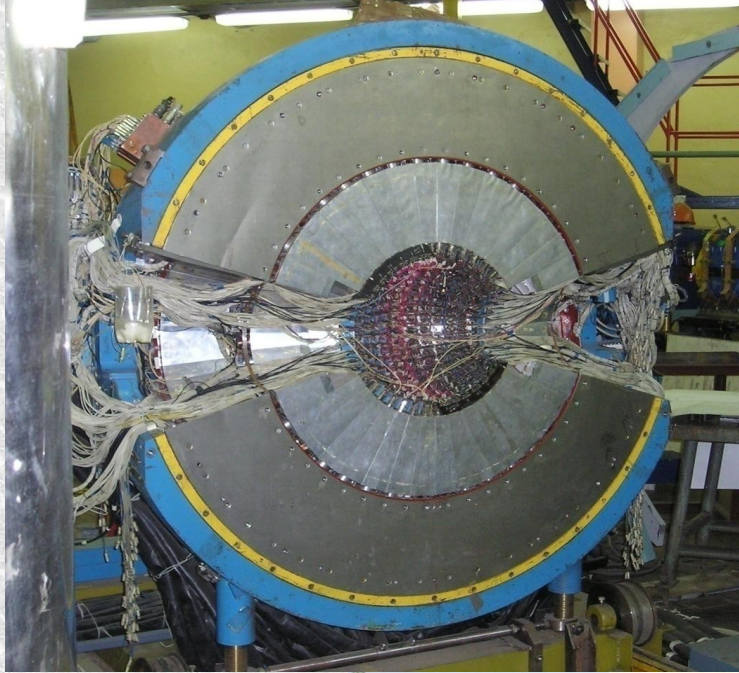
- x  $e/\mu/\pi$  separation - 0.2%  
can be checked and combined from different methods
- x Radiative corrections - 0.1%  
more proof from data
- x Fiducial volume - 0.1%  
controlled independently by LXe and ZC subsystems
- x Beam Energy - 0.1 %  
measured by method of Compton back scattering  
of the laser photons( $\sigma_E < 50$  keV)
- x Pion specific correction - 0.1%  
decay, nuclear interaction taken from data

First publication expected with systematic level  $\sim < 1\%$

Many systematic studies rely on high statistics

# Conclusion

- x VEPP-2000 collider successfully operates with a goal to get  $\sim 1\text{fb}^{-1}$  in 5-10 years which should provide new precise results on the hadron production
- x We have upgraded the CMD-3 detector, with much better performance and monitoring of different detector subsystems
- x First scan  $< 1\text{ GeV}$  for  $\pi^+\pi^-$  measurement was done
- x High statistics allow us to study and to control better different systematic contributions, with final goal up to 0.35%
- x More data expected after VEPP-2000 upgrade with new positron injection facility



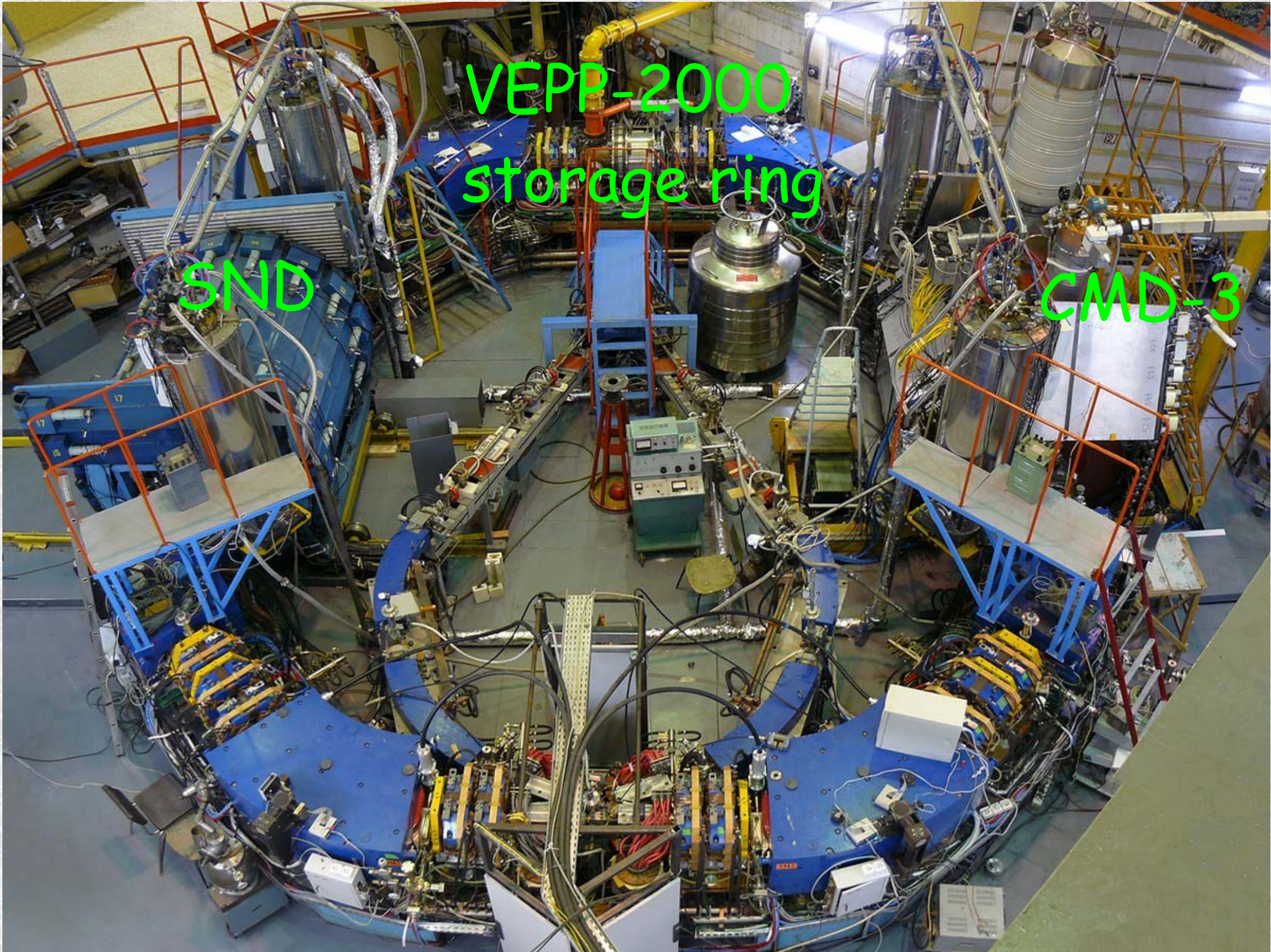
23 September 2015, PHIPSI15, Hefei

CMD-3 Collaboration

VEPP-2000  
storage ring

SND

CMD-3





# CMD-3 Detector

Advantages compared to previous CMD-2:

- x new drift chamber with x2 better resolution, higher B field better tracking better momentum resolution

- x thicker barrel calorimeter ( $8.3X_0 \rightarrow 13.5X_0$ )

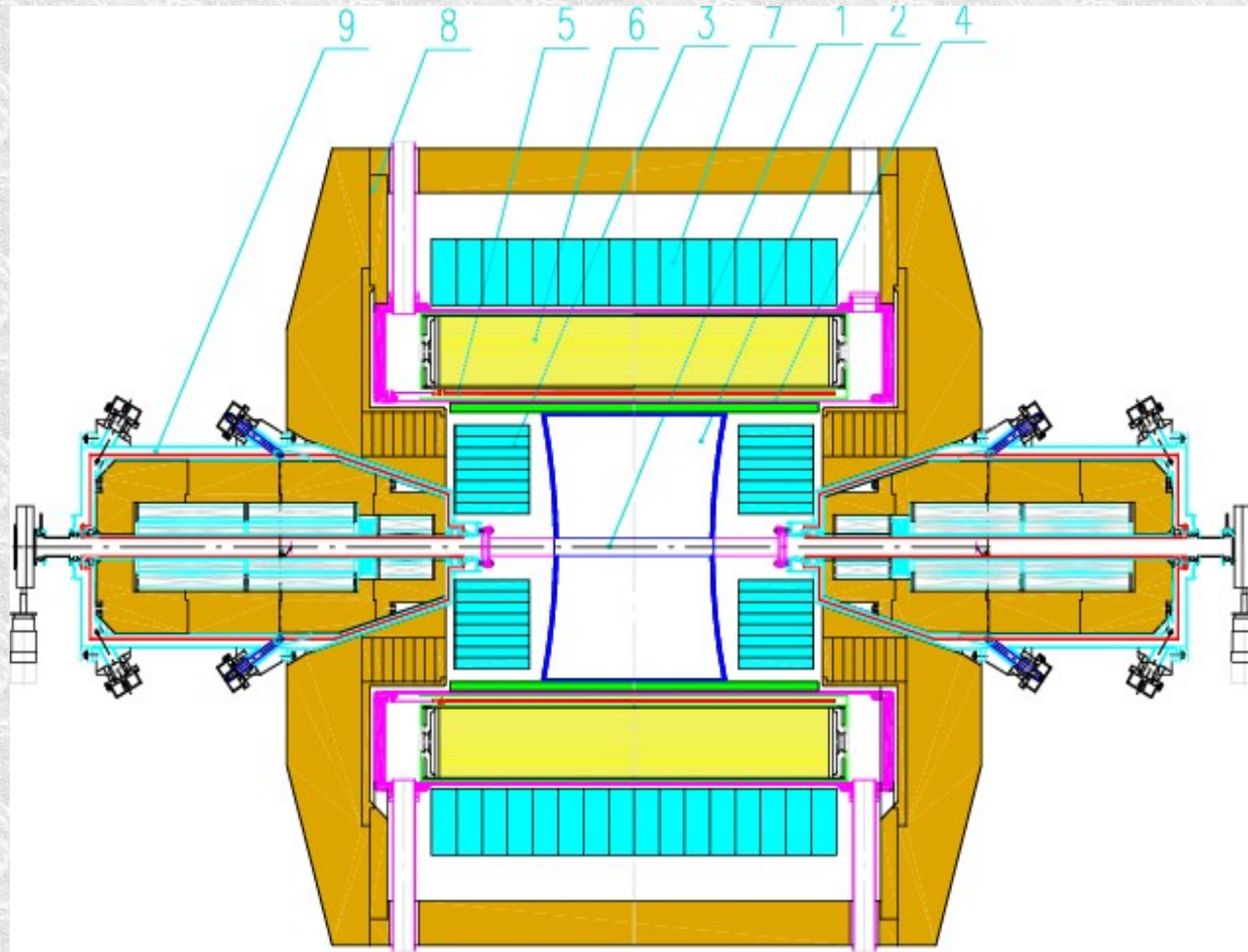
  - better particle separation

- x LXe calorimeter

  - ~2mm measurement of conversion point for  $\gamma$ 's, tracking capability shower profile

- x TOF system

  - time separation for  $\bar{n}$

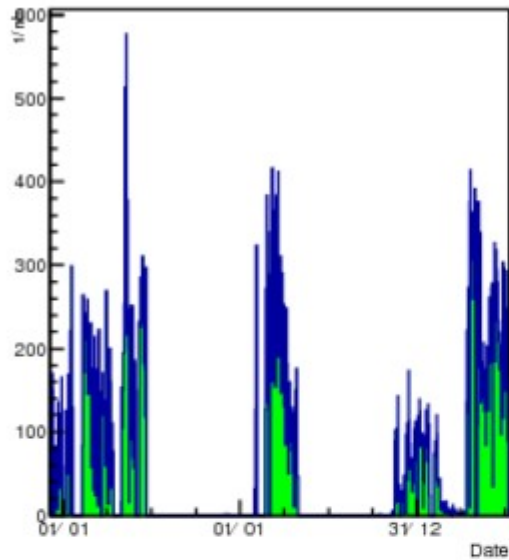


1 - vacuum tube, 2 - drift chamber, 3 - calorimeter BGO (680 crystals), 4 - Z-chamber, 5 - CMD-3 superconducting solenoid, 6 - calorimeter LXe (400 liters), 7 - calorimeter CsI (1152 crystals), 8 - magnet yoke, 9 - solenoids of VEPP-2000, (not shown) muon range and TOF systems

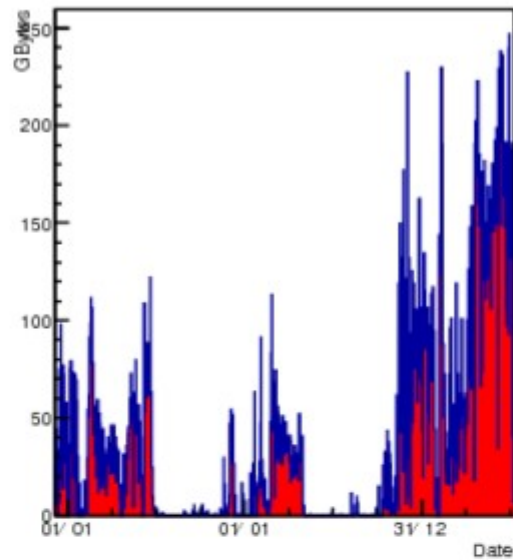
# CMD3 data collecting history

■ - all data, ■ - cosmic and beam data

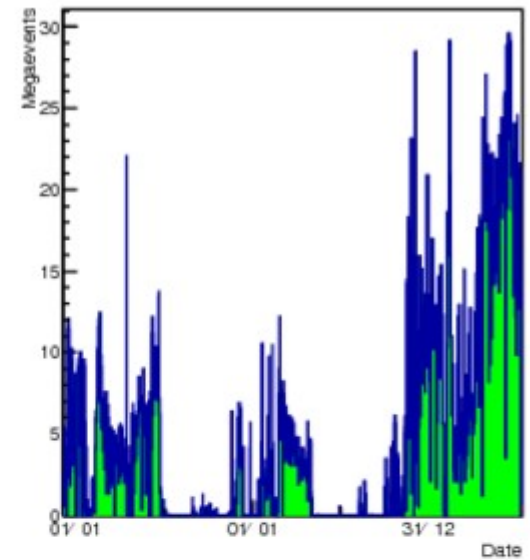
### 1/nb per day



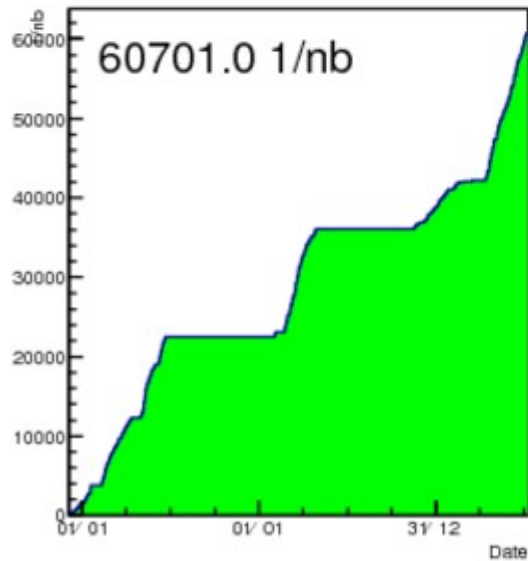
### GBytes per day



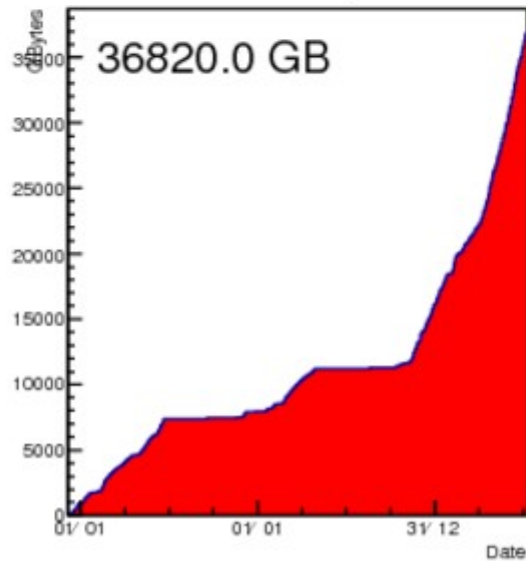
### Events (\*10\*\*6) per day



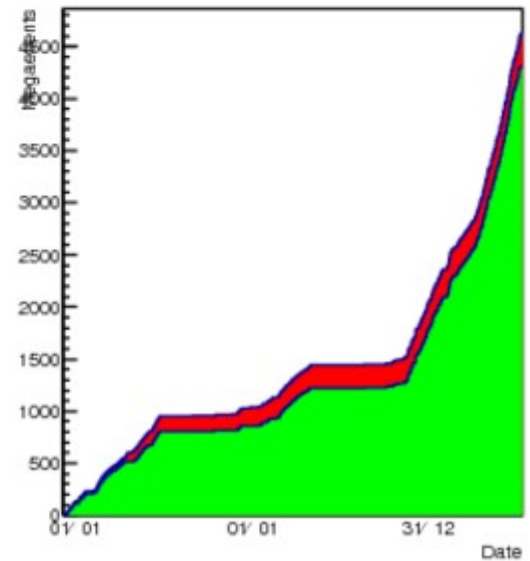
### Collected 1/nb



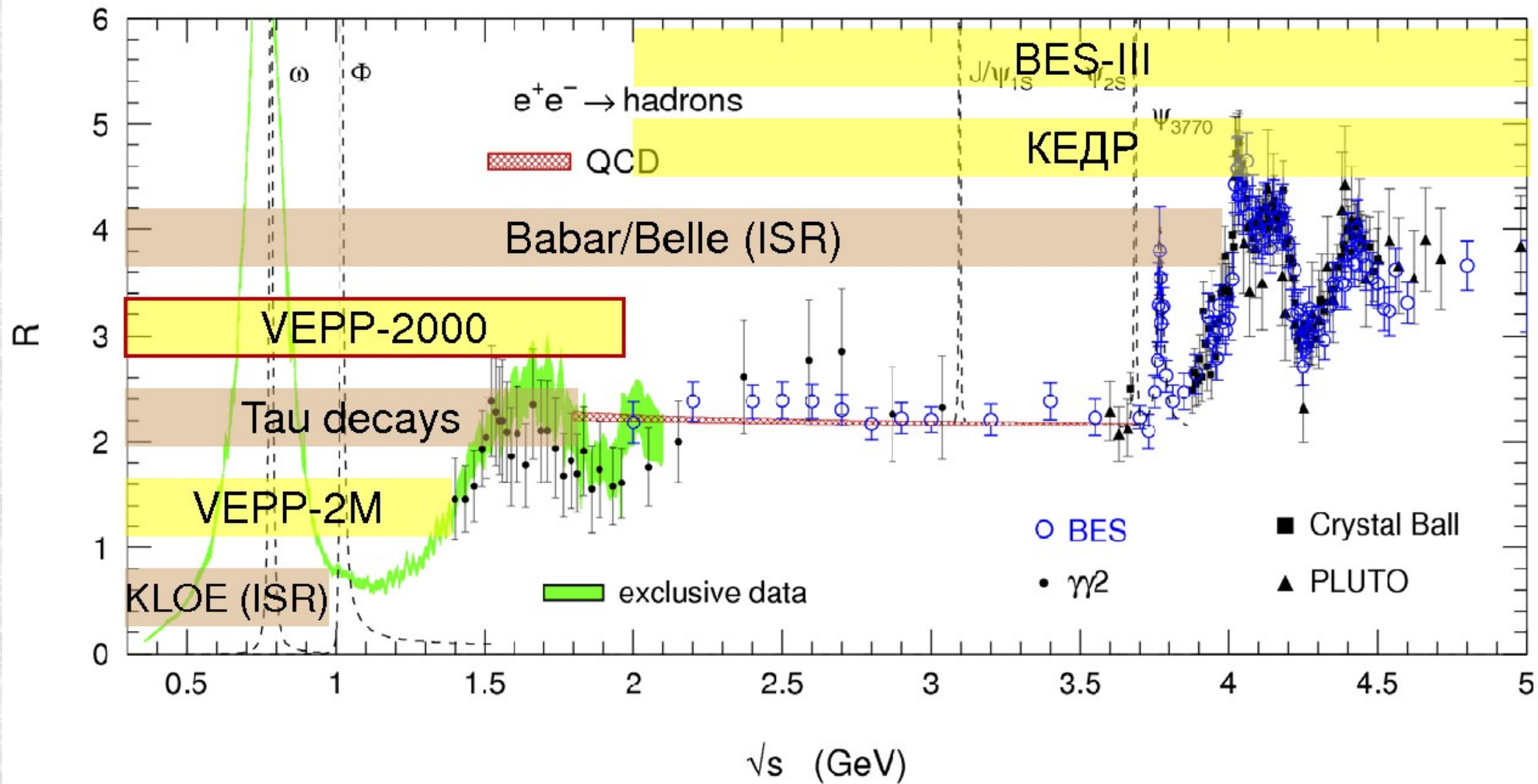
### Collected GBytes



### Collected Events (\*10\*\*6)

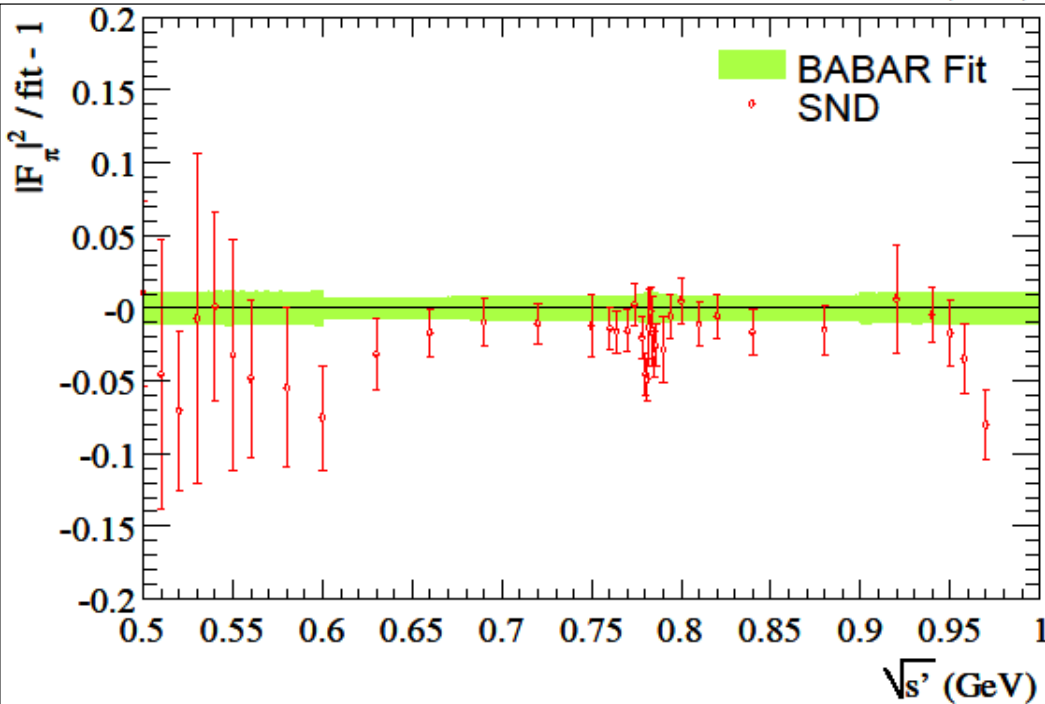
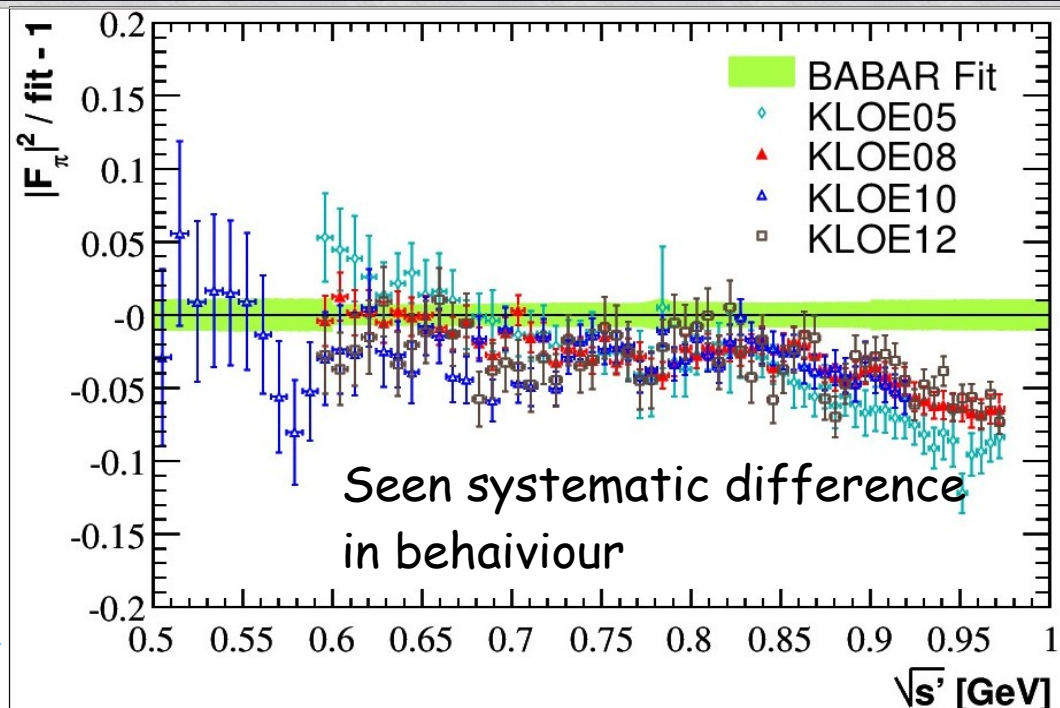
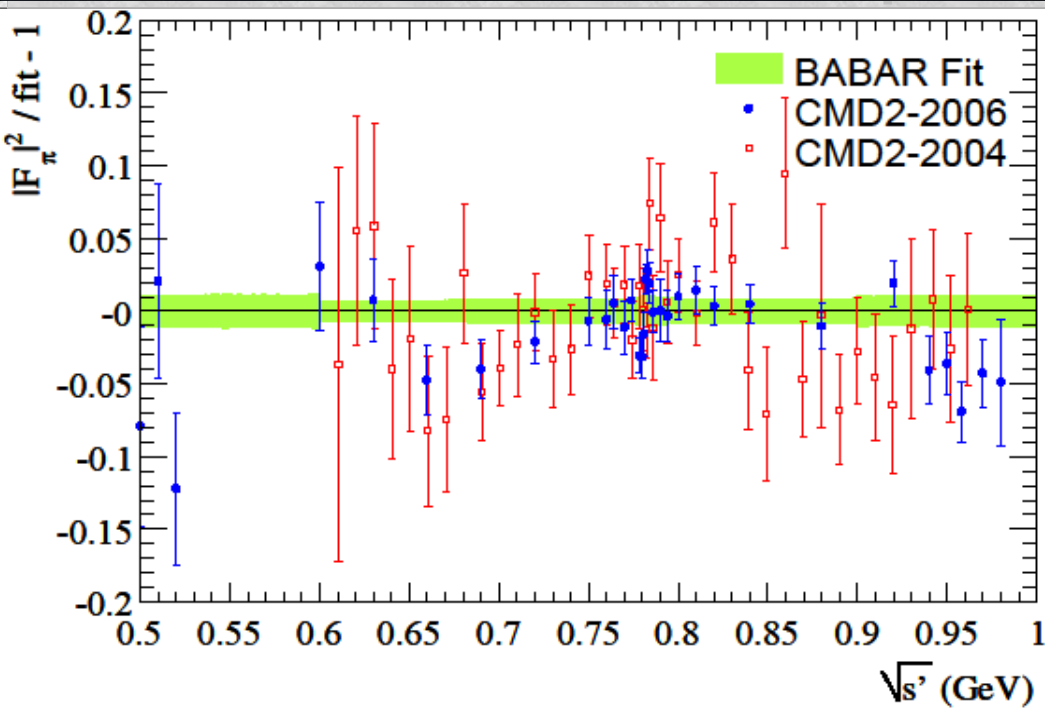


# R(s) measurements at low s



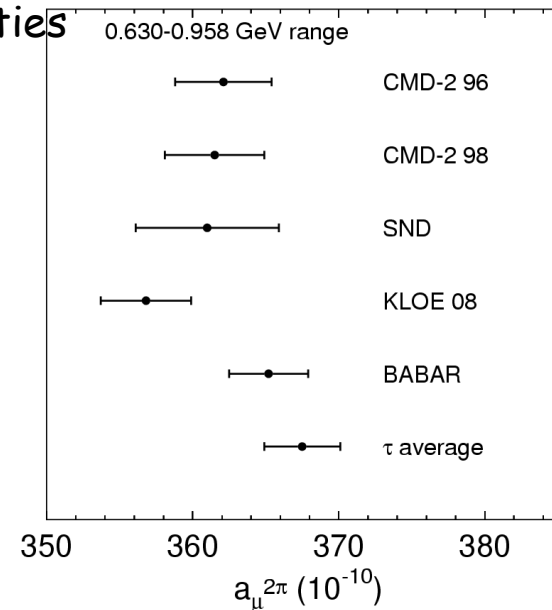
The value and the error of the hadronic contribution to muon ( $g-2$ ) are dominated by low energy  $R(s)$  ( $<2\text{GeV}$  gives 92% of the value).  
 $\alpha_{\text{QED}}(M_Z)$  - half of error comes from  $2E < 4 \text{ GeV}$

# $\pi^+\pi^-$ published data



## Systematic Uncertainties ( $\rho$ -region)

B A B A R : 0.5%  
 C M D 2 : 0.6-0.8%  
 S N D : 1.5%  
 K L O E : 0.8%



B.Malaescu, Moriond 2014

# SM prediction for muon g-2

ArXiv:1010.4180, arXiv:1105.3149

$$a_{\mu}^{\text{experimental}} = (g-2)_{\mu} / 2$$

11 659 208.9  $\pm 6.3 \times 10^{-10}$  world average

$$a_{\mu}^{\text{theory}} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{hadron}}$$

QED contribution	11 658 471.808 $\pm 0.015$	Kinoshita & Nio, Aoyama et al
EW contribution	15.4 $\pm 0.2$	Czarnecki et al
NLO hadronic	-9.8 $\pm 0.1$	HLMNT11

## Hadronic contributions

From measured cross-section by dispersion integral

LO hadronic  $694.1 \pm 4.3 \times 10^{-10}$  HLMNT 11

main channels contribution to precision at  $\sqrt{s} < 1.8 \text{ GeV}$

$\pi^+\pi^-$	505.65 $\pm 3.09$	
$\pi^+\pi^-2\pi^0$	18.62 $\pm 1.15$	
$\pi^+\pi^-\pi^0$	47.38 $\pm 0.99$	(mostly from omega region)
$2\pi^+2\pi^-$	13.64 $\pm 0.36$	(BaBar)
$K^+K^-$	22.95 $\pm 0.26$	(BaBar)

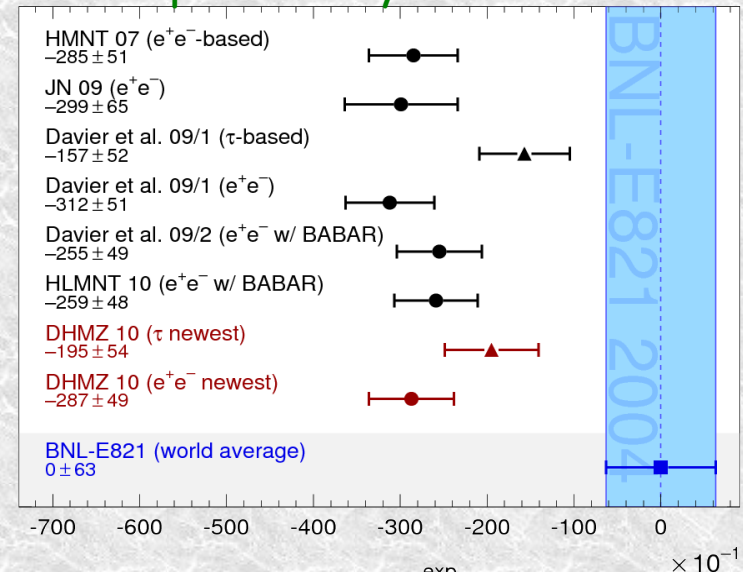
from Isospin relations  $5.98 \pm 0.42$  for not measured  $KK\pi, KK2\pi, 2\pi4\pi^0, 2\pi3\pi^0$   
 (or  $12.46 \pm 0.76$  for  $\sqrt{s} < 2 \text{ GeV}$ ) (contribution at 1.5-3 $\sigma$  of total error -

Rqcd<sub>[2-11.09GeV]</sub>  $41.19 \pm 0.82$  crucial if something is wrong with used isospin relations)

Light-by-light  $10.5 \pm 2.6$  Prades, de Rafael & Vainshtein

Theory TOTAL  $\pm 4.9$

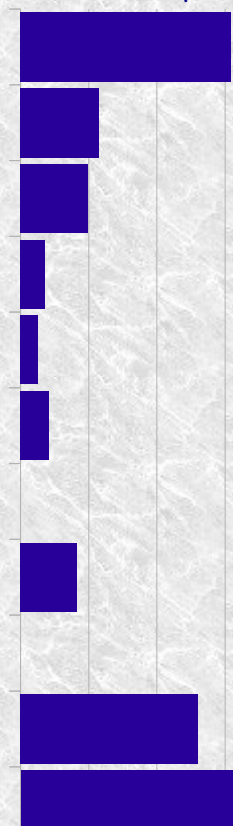
$\Delta \text{Exp} - \text{Theory} \sim 3.3 - 3.6\sigma$



New g-2 experiments at FNAL and J-PARC have plans to reduce error to  $1.5 \times 10^{-10}$

need more theory input, probably with help of experimental transition form factors

From direct integration  
Without model constraints  
 $\delta a_{\mu}$



# R measurement: systematic errors

What systematic error can be achieved for R measurement at CMD-3?

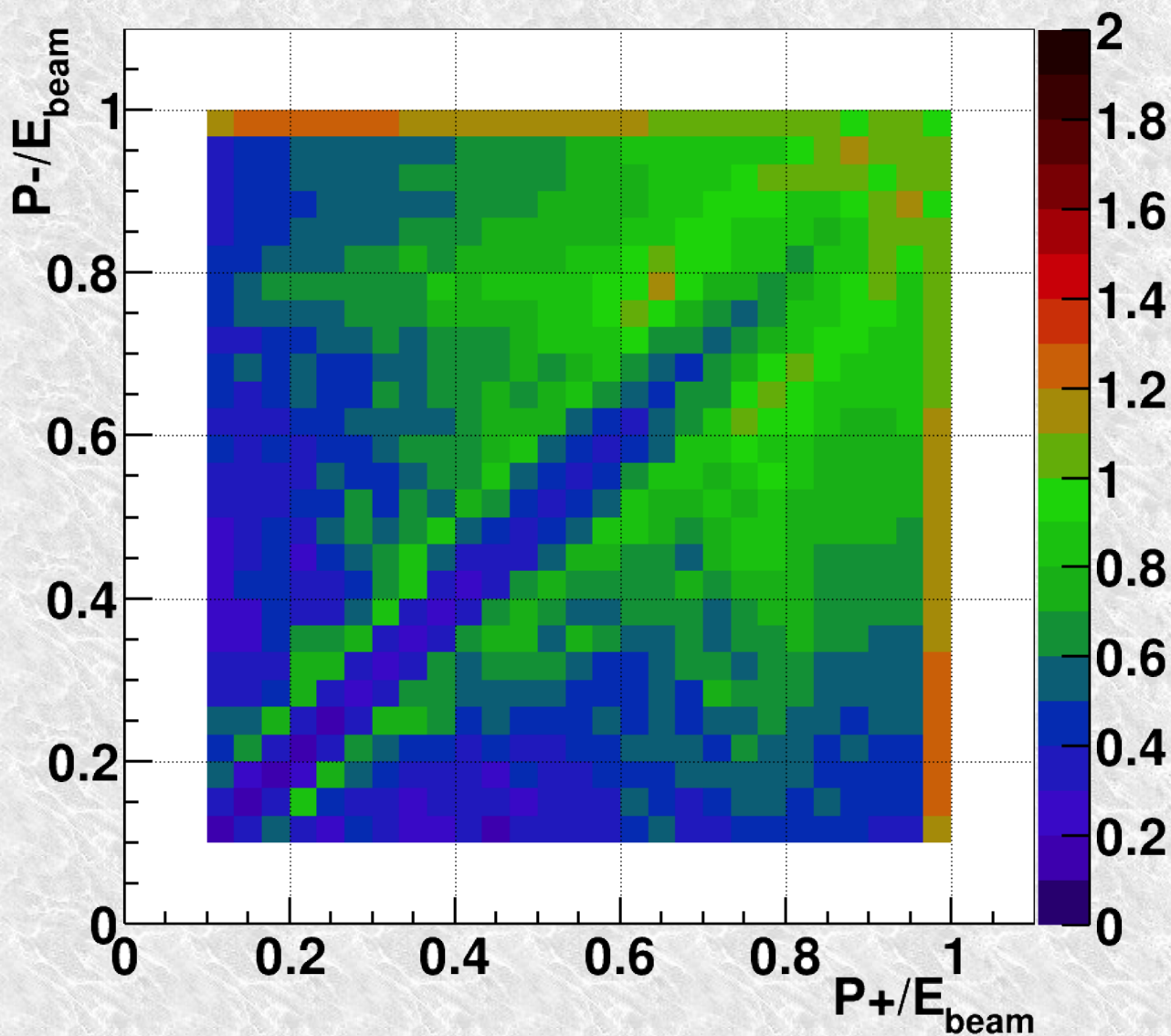
Source of error	CMD2, $2\pi$ $\sqrt{s} < 1 \text{ GeV}$	SND, $2\pi$ $\sqrt{s} < 1 \text{ GeV}$	CMD2, $4\pi$ $\sqrt{s} > 1.1 \text{ GeV}$	CMD3, $2\pi$ $\sqrt{s} < 1 \text{ GeV}$	CMD3, $4\pi$ $\sqrt{s} > 1.1 \text{ GeV}$
Event separation	0.2-0.4%	0.5%	2% (cuts)	0.2%	1% (cuts)
Fiducial volume	0.2%	0.8%	3% (model)	0.2%	2% (model)
Energy calibration	0.1-0.3%	0.3%	1%	0.1%	
Efficiency correction	0.2%-0.5%	0.6%	2% (tr+bg)	0.1%	1% (tr+bg)
Pion losses (decay, NI)	0.2%	0.2%		0.1%	
Other		0.5%	2%		0.3% (lum)
Radiative corrections	0.3-0.4%	0.2%	1%	0.1%	1%
Total syst.	0.6-0.8%	1.3%	5%	<b>0.35%</b>	<b>2.5%</b>
Stat.+Syst.	0.7%	1.5%	7%		

# BabaYaga @ NLO vs MCGPJ

Ebeam = 391.48 MeV

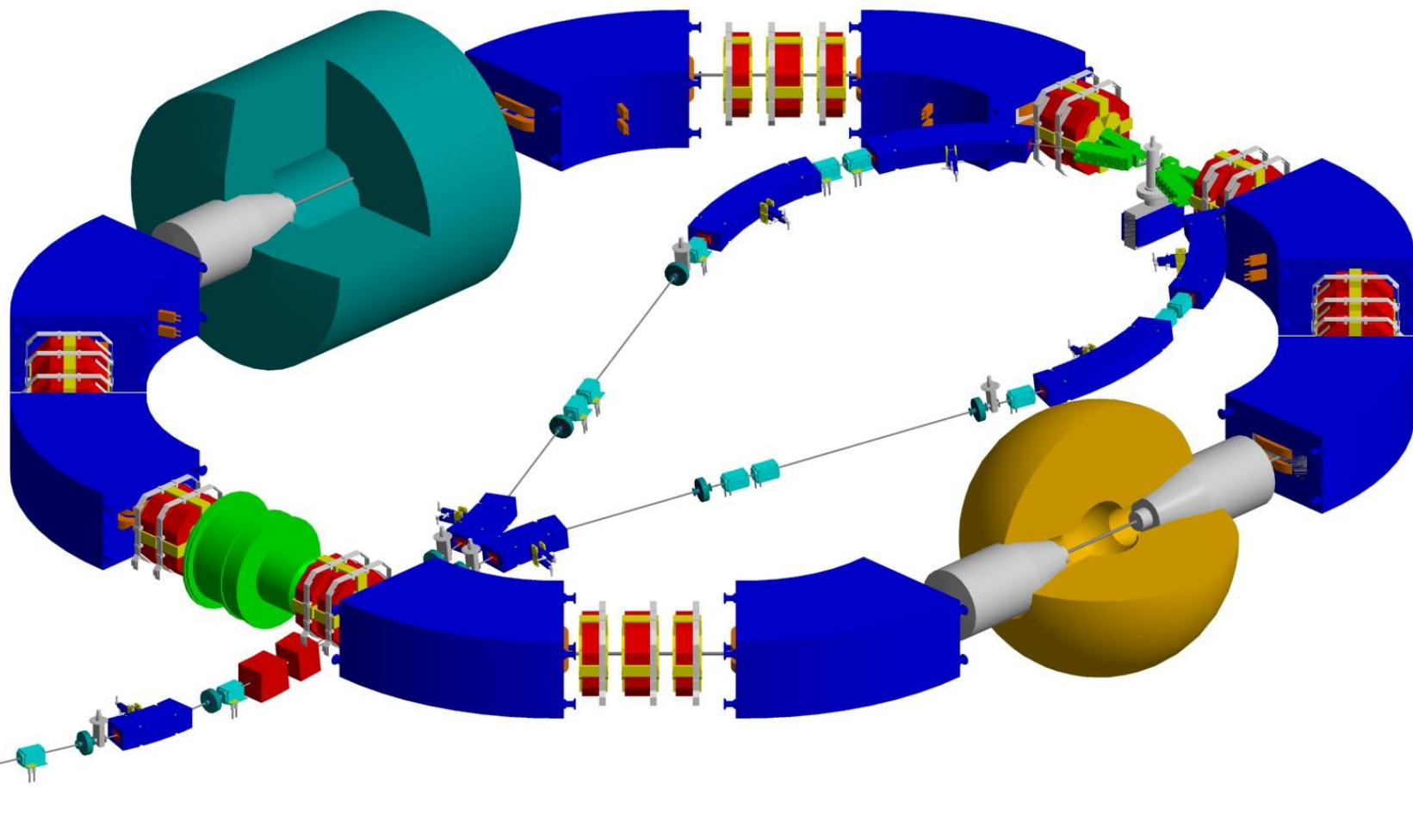
Comparison of momentum spectrum from generators

$$\frac{\partial^2 \sigma}{\partial p^+ \partial p^-} \text{ BabaYaga/MCGPJ}$$



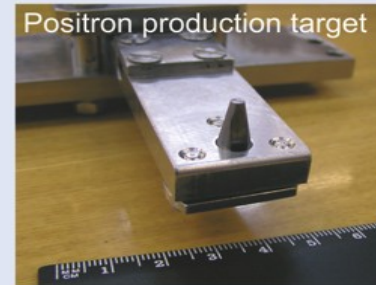
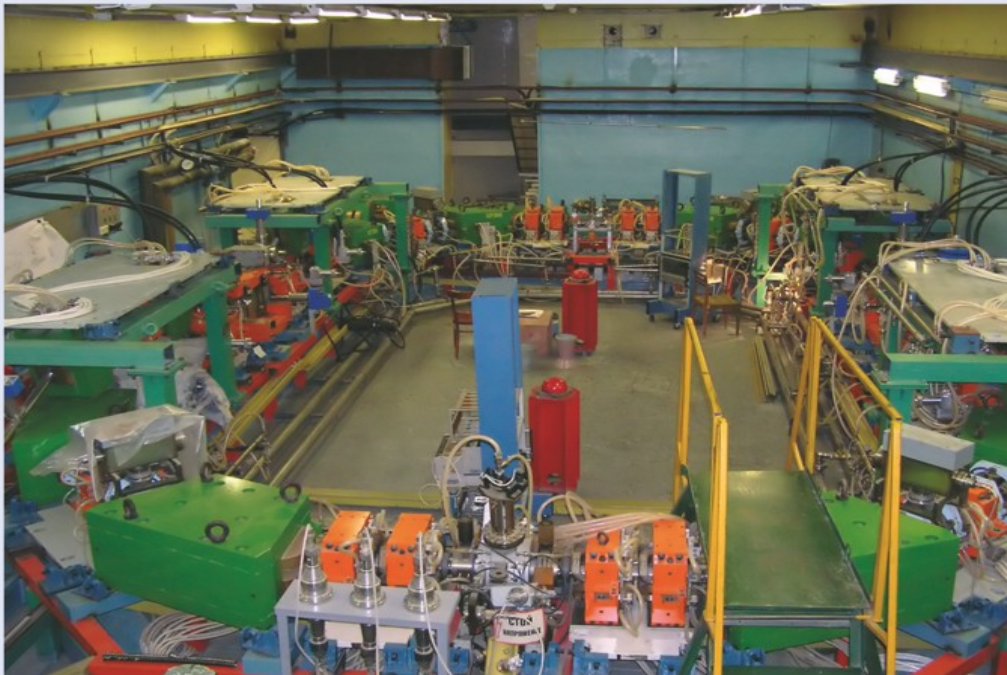
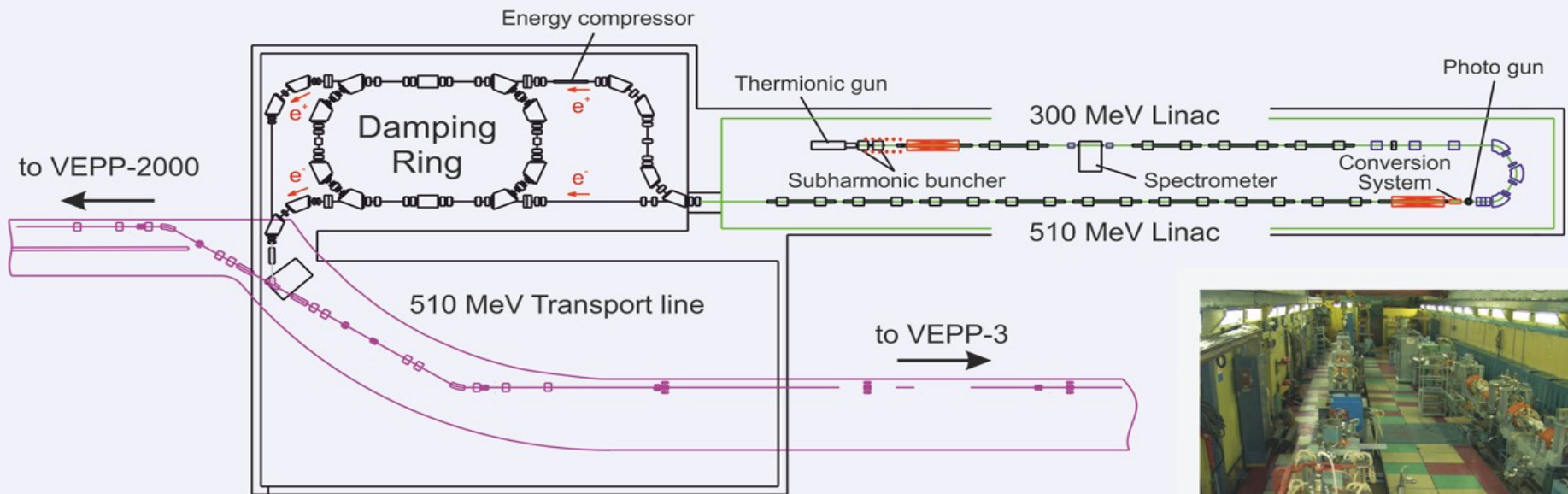
# VEPP-2000 parameters

$L = 24.39 \text{ m}$   
 $f_{acc} = 172 \text{ MHz}$   
 $V_{acc} = 120 \text{ kV}$   
 $E = 0.2 - 1 \text{ GeV}$   
 $B_{bend} = 2.4 \text{ T}$   
 $B_{sol} = 13 \text{ T}$   
 $\beta^* = 2 - 10 \text{ cm}$   
 $\sigma_s = 3 \text{ cm}$   
 $\varepsilon = 1.4 \cdot 10^{-7} \text{ mrad}$   
 $v_{x,z} = 2.1; 4.1$   
 $\alpha = 0.036$   
 $\xi = 0.15$   
 $N_{\pm} = 1011$   
 $L = 1 \cdot 10^3 \text{ cm}^{-2} \text{ s}^{-1}$   
1





# VEPP-5 INJECTION COMPLEX

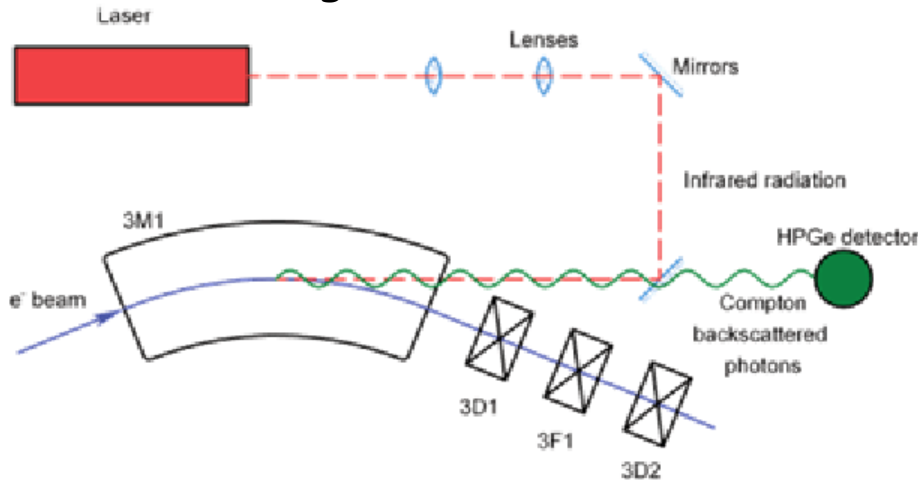


Parameters at  $E_{\text{beam}} = 510 \text{ MeV}$

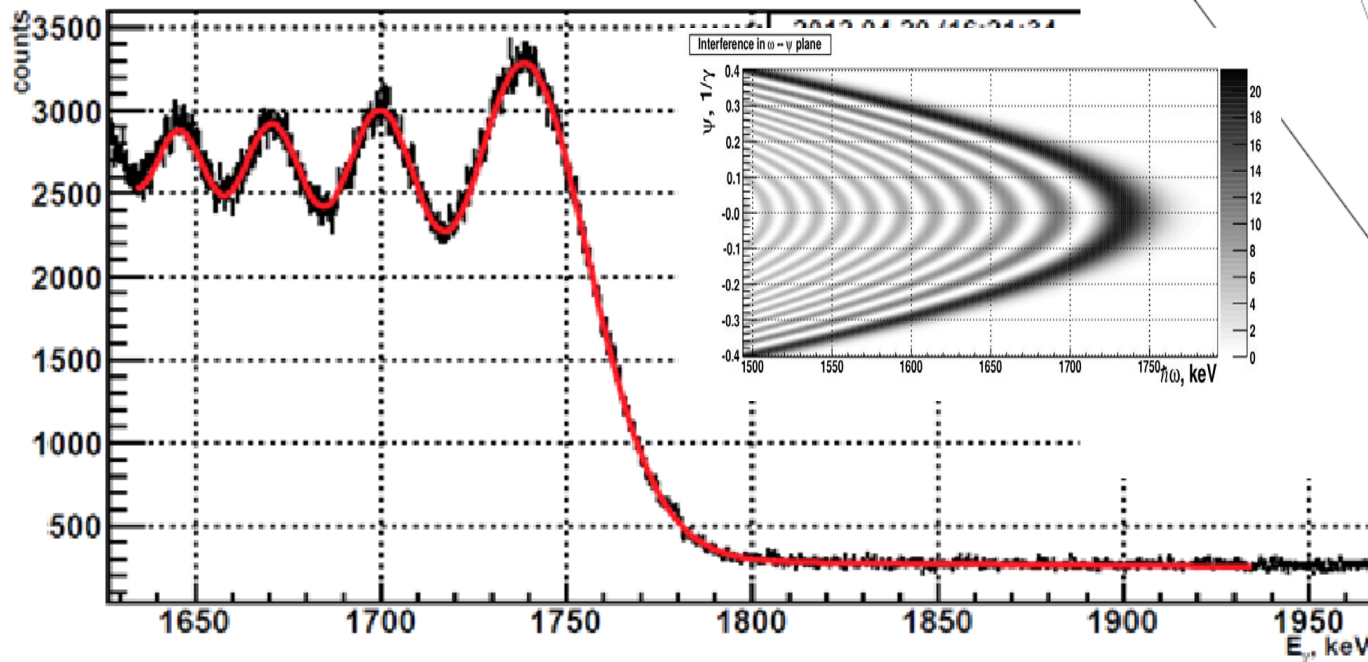
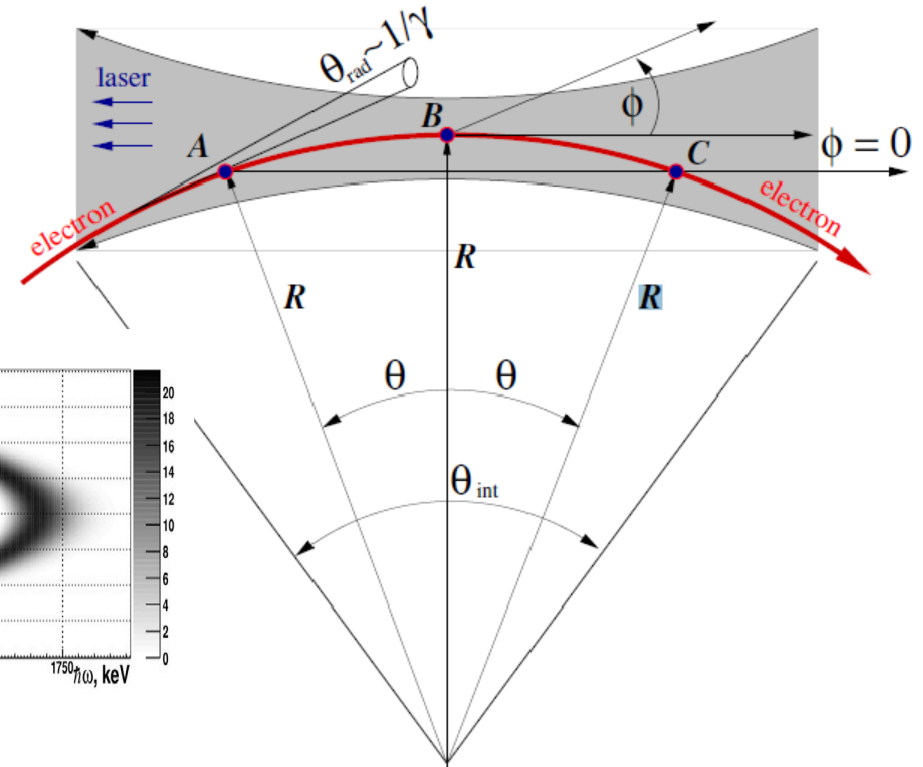
Number of electrons per bunch	$2 \cdot 10^{10}$
Number of positrons per bunch	$2 \cdot 10^{10}$
Repetition rate	1 Hz
Electron bunch energy spread	0.07%
Positron bunch energy spread	0.07%
Vertical emittance	$5 \cdot 10^{-9} \text{ m-rad}$
Horizontal emittance	$23 \cdot 10^{-9} \text{ m-rad}$

# Energy measurement by Compton back scattering

Starting from 2012, energy is monitored continuously using compton backscattering



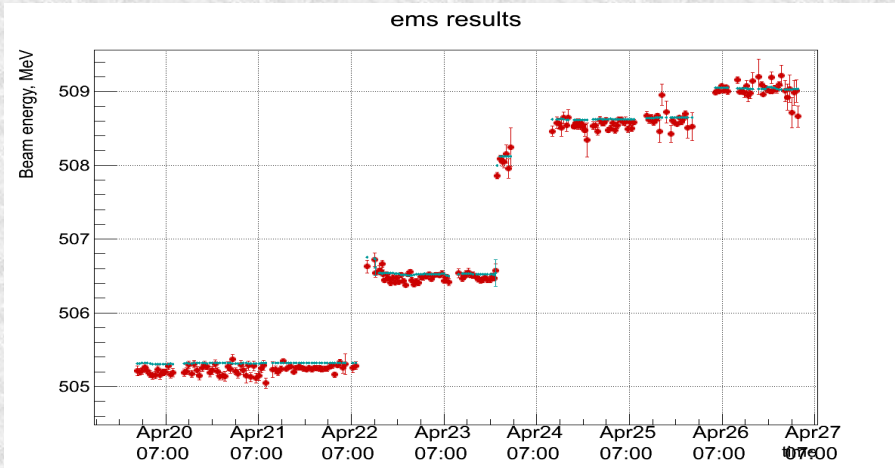
Излучение из точек А и С под углом  $\phi = 0$  интерферирует



$$E = 993.662 \pm 0.016 \text{ МэВ}$$

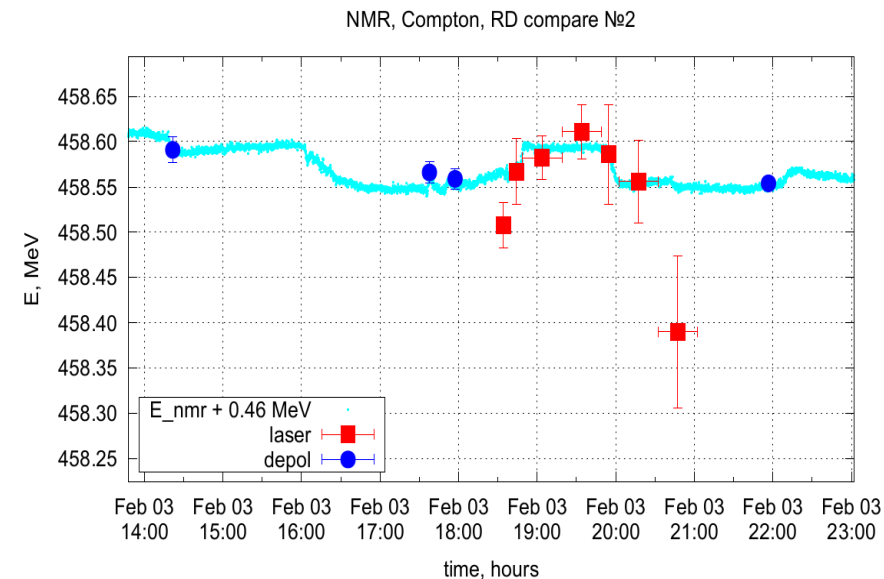
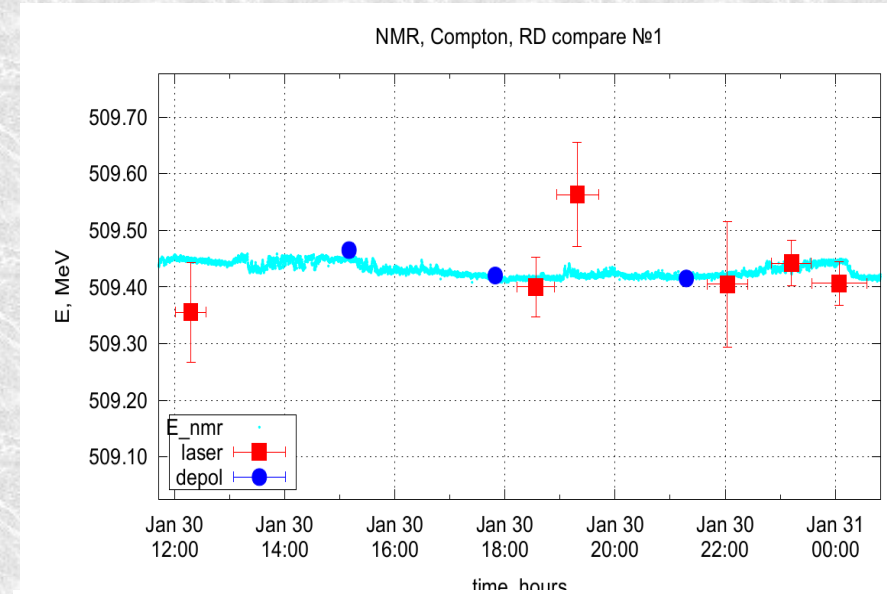
# Beam energy measurement at VEPP-2000

- **Magnetic field control in bending magnets**
  - 8x2 NMR probes, continuous control
  - Absolute calibration using:
    - $\phi$ -meson ( $1019.455 \pm 0.020$  MeV),
    - $\omega$ -meson ( $782.65 \pm 0.12$  MeV).
- **Measurement of photon energy from back scattering laser light**
  - Installed in 2012.
  - Needs beam current (20  $\mu$ A),  $\sim$ 20-50 keV accuracy in 10 min
  - Energy control during data taking.

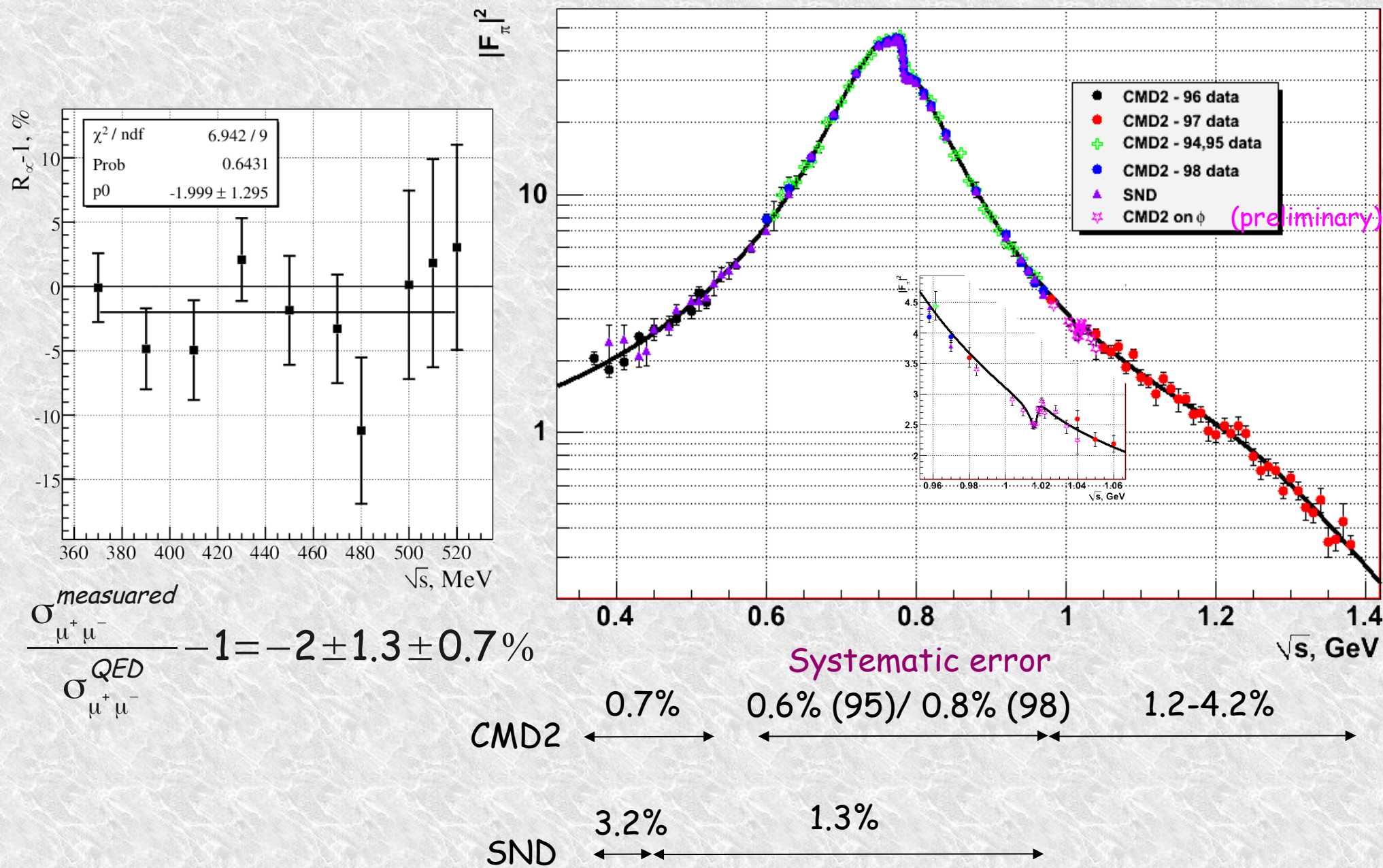


- **Resonance depolarization method**
  - Very high accuracy ( $\delta E/E < 10^{-5}$ ).
  - Special configuration of VEPP-2000: "warm"

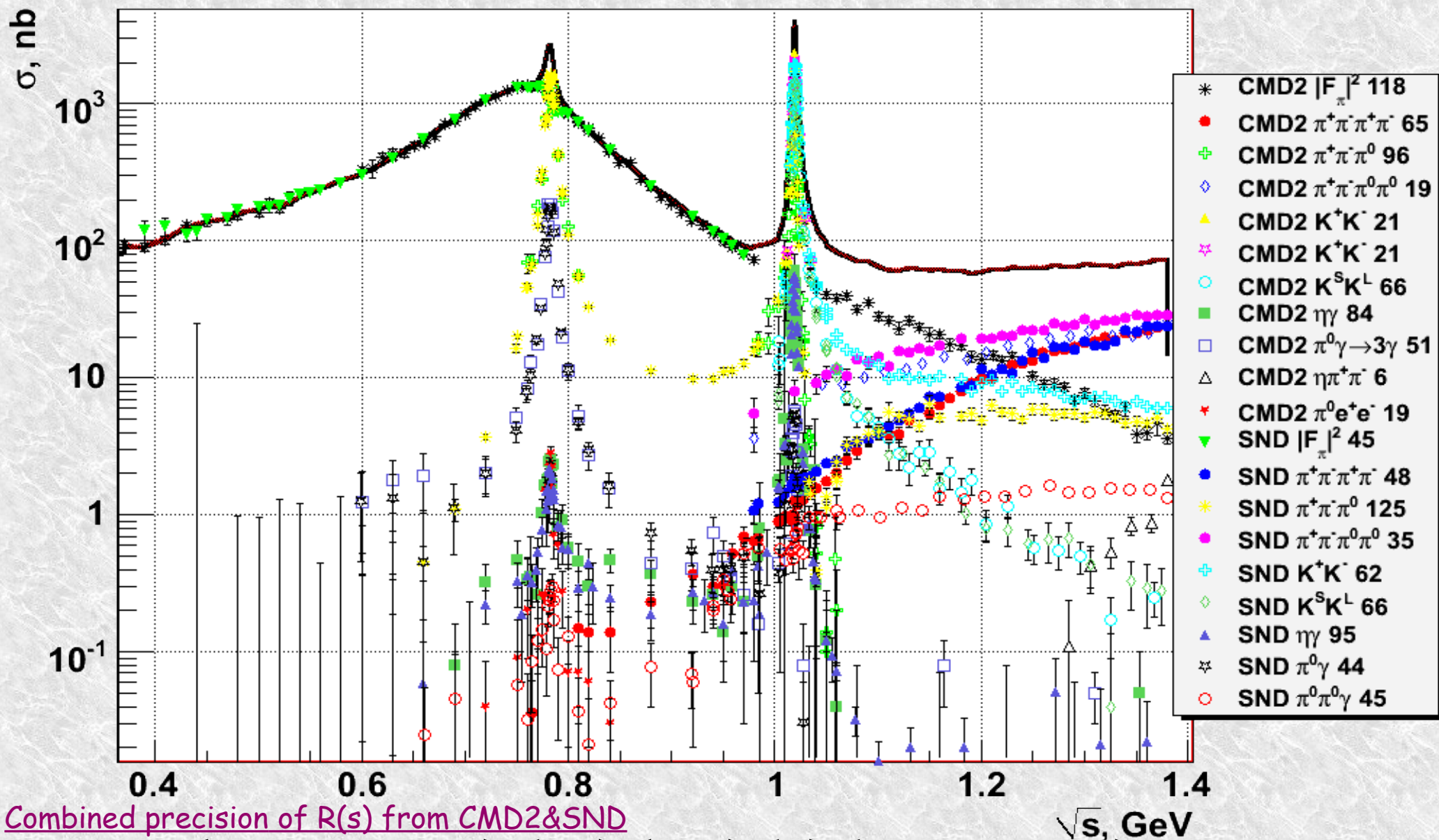
## Methods comparison:



# Pion formfactor



# Inclusive Hadronic Cross-Sections with CMD2&SND



Combined precision of  $R(s)$  from CMD2&SND

Systematic error: ~0.6-0.7%      1.0%      0.6%      1.5%      1.5 -- 3.5 %  
 Total error:                      ~ 6 -- 1%      1.5%      1--2%      2.0%      2.5 -- 3.5 %

The uncertainty in  $a_\mu(\text{had})$  was improved by factor 3 as the result of VEPP-2M measurements