

Flavor and top physics @ 100 TeV Workshop, IHEP/CAS, MARCH 5, 2015

Seung J. Lee (KAIST)

Precision (B)SM Higgs Studies @ future colliders

1. Study of SM Higgs boson partial widths and branching fractions

2. Higgs potentials and more: Higgs from a quantum phase transition

1. With L. Almeida, S.L., S. Porkorski, J. Wells arXiv:1311.6721v3

2. With B. Bellazzini, C. Csaki, J. Hubisz, S.L., J. Serra, J. Terning work in progress (to appear)

Nothing but Higgs, with ~ 10-20% Precision for Higgs couplings so far



New era of precision studies of the Higgs sector

(from Snowmass Higgs working group report): Higgs precision will approach that of EWP



@ 100 TeV

4. Higgs cross sections for HE-LHC

SM Higgs production cross sections at \sqrt{s} = 14, 33, 40, 60, 80 and 100 TeV (M_H=125 GeV)

Process	√s = 14 TeV	√s = 33 TeV	√s = 40 TeV	√s = 60 TeV	√s = 80 TeV	√s = 100 TeV
ggF ª	50.35 pb	178.3 pb (3.5)	231.9 pb (4.6)	394.4 pb (7.8)	565.1 pb (11.2)	740.3 pb (14.7)
VBF ^b	4.40 pb	16.5 pb (3.8)	23.1 pb (5.2)	40.8 pb (9.3)	60.0 pb (13.6)	82.0 pb (18.6)
WH °	1.63 pb	4.71 pb (2.9)	5.88 pb (3.6)	9.23 pb (5.7)	12.60 pb (7.7)	15.90 pb (9.7)
ZH °	0.904 pb	2.97 pb (3.3)	3.78 pb (4.2)	6.19 pb (6.8)	8.71 pb (9.6)	11.26 pb (12.5)
ttH ^d	0.623 pb	4.56 pb (7.3)	6.79 pb (11)	15.0 pb (24)	25.5 pb (41)	37.9 pb (61)
$gg \rightarrow HH^{e}(\lambda=1)$	33.8 fb	207 fb (6.1)	298 fb (8.8)	609 fb (18)	980 fb (29)	1.42 pb (42)

PDF is NNLO(NLO) MSTW2008 set. Numbers in () parentheses are the cross-section ratio wrt 14 TeV.

a) NNLO+NNLL QCD + NLO EW corrections. QCD scale and PDF+ α_s uncertainties remain constant about +-8% for both (D. de Florian).

b) NNLO QCD only with VBF@NNLO (M. Zaro).

c) NNLO QCD only with VH@NNLO (R. Harlander).

d) NLO QCD. (M. Spira).

e) NLO QCD with HPAIR. The central scale is the invariant mass of the Higgs pair. The scale is varied by a factor 2 up and down. (M. Spira).

https://twiki.cern.ch/twiki/bin/view/LHCPhysics/HiggsEuropeanStrategy2012

@ 100 TeV

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Part I: Precision Higgs Analysis: expansion formalism of the Higgs boson partial widths and branching fractions

L. Almeida, S.L., S. Porkorski, J. Wells arXiv:1311.6721v3

- The sub-percent-level determination of the Higgs boson mass now enables a complete set of input observables whereby any perturbative high-energy observable involving the Higgs boson can be predicted.
 - careful exposition of the decay partial widths and branching fractions of a SM Higgs boson with mass near 125 GeV.
 - state-of-the-art formulas that can be used in any precision electroweak analysis to investigate compatibility of the data with the SM predictions in these most fundamental and sensitive observables

What's new in our expansion formalism?

- Other calculations exist in the literature, mostly notably from the computer program HDECAY; however, we wish to provide an independent calculation that includes the latest advances and allows us to <u>vary the renormalization</u> <u>scale in all parts of the computations</u>. This flexibility will be useful in discussions regarding **Uncertainties**
- We also aim to detail the <u>errors that each input into the</u> <u>computation propagates to the final answer</u> for each observable

Taylor expand the full expressions for partial width around the input observables. This expansion is made possible by the fact that with the discovery of the Higgs boson, and knowledge of its mass, all input observables are now known to good enough accuracy to render an expansion of this nature useful and accurate.

We represent the partial width expansion by

$$\Gamma_{H\to X} = \Gamma_X^{(\text{ref})} \left(1 + \sum_i a_{\tau_i, X} \overline{\delta \tau_i} \right)$$
(7)

where

$$\overline{\delta\tau_i} = \frac{\tau_i - \tau_{i,ref}}{\tau_{i,ref}},\tag{8}$$

and τ_i are the $\{m_H, M_Z, \Delta \alpha_{had}^{(5)}, \alpha_S(M_Z), m_f\}$ for the calculation. The total width is the sum of all the partial widths and for convenience we present dedicated expansion parameters for that as well:

$$\Gamma_{\text{tot}} = \sum_{X} \Gamma_{H \to X} = \Gamma_{\text{tot}}^{(\text{ref})} \left(1 + \sum_{i} a_{\tau_i, \text{tot}} \overline{\delta \tau_i} \right).$$
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	$\Gamma_X^{(\mathrm{Ref})}/\mathrm{GeV}$	$a_{m_t,X}$	$a_{mH,X}$	$a_{\alpha(M_Z),X}$	$a_{\alpha_S(M_Z),X}$	$a_{m_b,X}$	$a_{M_Z,X}$	$a_{m_c,X}$	$a_{m_{\tau},X}$	$a_{G_F,X}$
total	4.17×10^{-3}	-3.3×10^{-2}	4.34	8.35×10^{-1}	-5.05×10^{-1}	1.32	-3.21	7.80×10^{-2}	1.24×10^{-1}	8.49×10^{-1}
<u>gg</u>	3.61×10^{-4}	-1.62×10^{-1}	2.89	0.	2.48	-6.51×10^{-2}	3.76×10^{-1}	0.	0.	1.00
$\gamma\gamma$	1.08×10^{-5}	-2.69×10^{-2}	4.32	2.56	1.80×10^{-2}	8.29×10^{-3}	-1.86	0.	0.	7.24×10^{-1}
$b\overline{b}$	2.35×10^{-3}	8.07×10^{-3}	8.09×10^{-1}	3.76×10^{-2}	-1.12	2.36	-2.72×10^{-1}	0.	0.	9.53×10^{-1}
$c\bar{c}$	1.22×10^{-4}	-4.52×10^{-2}	7.99×10^{-1}	1.02×10^{-2}	-3.10	0.	-4.89×10^{-1}	2.67	0.	9.70×10^{-1}
$\tau^+\tau^-$	2.58×10^{-4}	4.71×10^{-2}	9.95×10^{-1}	-2.09×10^{-2}	-2.14×10^{-3}	0.	-1.61×10^{-2}	0.	2.01	1.02
WW^*	9.43×10^{-4}	-1.13×10^{-1}	1.37×10^{1}	3.66	9.04×10^{-3}	0.	-1.21×10^{1}	0.	0.	2.49×10^{-1}
ZZ^*	1.17×10^{-4}	2.27×10^{-2}	1.53×10^{1}	-7.37×10^{-1}	-1.82×10^{-3}	0.	-1.12×10^{1}	0.	0.	2.53
$Z\gamma$	6.89×10^{-6}	-1.52×10^{-2}	1.11×10^{1}	8.45×10^{-1}	0.	-7.93×10^{-3}	-4.82	0.	0.	2.62
$\mu^+\mu^-$	8.93×10^{-7}	4.82×10^{-2}	9.92×10^{-1}	-4.31×10^{-2}	-2.19×10^{-3}	0.	-1.62×10^{-2}	0.	0.	1.02

Input Parameters for our expansion

Inputs :
$$\left\{ m_H, M_Z, \Delta \alpha_{had}^{(5)}, \alpha_S(M_Z), m_f \right\},$$
 (1)

 $\mathbf{\mathbf{\mathbf{x}}}$

**

 \mathbf{x}

Now that we have established our convention that M_W is an output observable, when the W mass appears in formulas below, we should view it as a short-hand notation for the full computation of the W mass within the theory in terms of our agreed-upon inputs. In the SM this substitution is

 $\begin{array}{rcl} M_W & \xrightarrow{SM} & (80.368 \, \mathrm{GeV}) \left(1 + 1.42 \, \delta M_Z + 0.21 \, \delta G_F - 0.43 \, \delta \alpha \right. \\ & & \left. + 0.013 \, \delta M_t - 0.0011 \, \delta \alpha_S - 0.00075 \, \delta M_H \right). (3) \end{array}$

m_H	125.7(4)	pole mass m_t	173.07(89)
$\overline{\text{MS}}$ mass m_c	1.275(25)	$\overline{\mathrm{MS}}$ mass m_b	4.18(3)
pole mass m_{τ}	1.77682(16)	$\alpha_S(M_Z)$	0.1184(7)
$\alpha(M_Z)$	1/128.96(2)	$\Delta \alpha_{had}^{(5)}$	0.0275(1)

$$\delta \tau \equiv (\tau - \tau_{ref}) / \tau_{ref}$$

Expansion of BR and ratio of BRs

$$B(H \to X) = B(X)^{(ref)} \left(1 + \sum_{i} b_{\tau_i, X} \overline{\delta \tau_i} \right), \quad (12)$$

where τ_i represents the $\{m_H, M_Z, \Delta \alpha_{had}^{(5)}, \alpha_S(M_Z), m_f\}$. Expansion parameters $b_{\tau_i, X}$ are related to $a_{\tau_i, X}$ by

$$b_{\tau_i,X} = a_{\tau_i,X} - a_{\tau_i,tot}.\tag{13}$$

$$\frac{\mathcal{B}(H \to \mathbf{X})}{\mathcal{B}(H \to \mathbf{Y})} = \frac{\mathcal{B}(\mathbf{X})^{(\text{ref})}}{\mathcal{B}(\mathbf{Y})^{(\text{ref})}} \left(1 + \sum_{i} r_{\tau_i, X, Y} \overline{\delta \tau_i}\right),$$

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The table of expansion coefficients enables us to compute the uncertainty in a final state branching ratio due to each input parameter. The percent uncertainty Δ_i^X on branching fraction B(X) due to input parameter τ_i is

$$\Delta_i^X = (100\%) \times |b_{\tau_i,X}| \frac{\Delta \tau_i}{\tau_i^{ref}} \tag{14}$$

where $\Delta \tau_i$ are the current experimental uncertainties in input parameter τ_i . For example, the percentage uncertainty in the $H \rightarrow gg$ branching fraction is

$$\Delta_b^{gg} = (100\%)(1.389) \frac{0.03 \,\text{GeV}}{4.18 \,\text{GeV}} = 1.00\%. \tag{15}$$

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the uncertainty in the b-quark mass input observable constitutes the largest uncertainty in the branching ratio computations.

The large uncertainty of the charm quark mass where $\Delta \tau_i$ are th parameter τ_i . Fo $H \rightarrow gg$ brane

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How well can we predict SM observables?

Percent relative uncertainty, P_Q : $Q = Q_0 (1 + 0.01 P_Q)$.

	$P_{\Gamma}^{\pm}(\text{par.add.})$	$P_{\Gamma}^{\pm}(\text{par.quad.})$	$(P_{\Gamma}^{+}, P_{\Gamma}^{-})(\mu)$
total	2.82(1.79)	1.71(1.07)	(0.08, 0.10)
gg	2.52(1.83)	1.74(1.49)	(0.05, 0.03)
$\gamma\gamma$	1.45(0.42)	1.38(0.35)	(1.31, 0.60)
$b\bar{b}$	2.62(2.43)	1.84(1.82)	(0.29, 0.01)
$c\bar{c}$	7.34 (7.15)	5.55(5.54)	(0.45, 0.35)
$\tau^+\tau^-$	0.36(0.12)	0.32(0.08)	(0.01, 0.01)
WW^*	4.41 (1.17)	4.97(1.25)	(0.25, 0.31)
ZZ^*	4.90(1.25)	4.42 (1.11)	(0.,0.)
$Z\gamma$	3.56(0.92)	3.52(0.88)	(0.56, 0.23)
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() => if the Higgs mass uncertainty were 0.1 GeV (instead of 0.4 GeV)

The meaning of " P_{Γ}^{\pm} (par.add.)" is that all input parameters have been allowed to range over their 1σ errors and the maximum percent relative errors are recorded. The meaning of " P_{Γ}^{\pm} (par.quad.)" is that the uncertainties of each parameter are added in Gaussian quadrature. In other words, $P_{\Gamma_i}^{\pm}$ (par.quad.) = $100 \Delta \Gamma_i / \Gamma_i$, where

$$(\Delta\Gamma_i)^2 = \left(\frac{\partial\Gamma_i}{\partial m_t}\right)^2 (\Delta m_t)^2 + \left(\frac{\partial\Gamma_i}{\partial\alpha_s}\right)^2 (\Delta\alpha_s)^2 + \cdots . \quad (11)$$

The uncertainties in varying the scale parameter μ in the calculation, attempts to capture the uncertainty in not knowing higher order corrections. A full calculation at all orders would give a result that does not depend on μ but a finite-order calculation does, and the uncertainty of dropping the higher order calculations are assumed to be approximated reasonably well by noting how much the result changes by varying μ by a factor of two upward and downward: $m_H/2 < \mu < 2m_H$. The meaning of " $P_{\Gamma}^{\pm}(\mu)$ " in Table 4 concerns the relative percent uncertainties associated with this scale dependence algorithm.

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quark	at $\mu = m_H (m_H/2, 2m_H)$	$P_m(\Delta m)$
$m_c(\mu)$	$0.638 \ (0.675, \ 0.603) \ { m GeV}$	2.62%
$m_b(\mu)$	2.79 (2.96, 2.64) GeV	0.85%
$m_t(\mu)$	$166.5 \ (176.8, 157.8) \ { m GeV}$	0.56%

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SM vs. New Physics? Uncertainties in BRs

	Δ_{m_t}	Δ_{m_H}	$\Delta_{\alpha(M_Z)}$	$\Delta_{\alpha_S(M_Z)}$	Δ_{m_b}	Δ_{M_Z}	Δ_{m_c}	$\Delta_{m_{\tau}}$	Δ_{G_F}
<u>gg</u>	0.07	0.46(0.12)	0.01	1.77	1.00	0.01	0.15	-	-
$\gamma\gamma$	-	0.01 (-)	0.03	0.31	0.94	-	0.15	-	-
$\gamma\gamma \ bar{b}$	0.02	1.13(0.28)	0.01	0.36	0.74	0.01	0.15	-	-
$c\bar{c}$	0.01	1.13(0.28)	0.01	1.53	0.95	0.01	5.08	-	-
$\tau^+\tau^-$	0.04	1.07(0.27)	0.01	0.30	0.95	0.01	0.15	0.02	-
WW^*	0.04	2.97(0.74)	0.04	0.30	0.95	0.02	0.15	-	-
ZZ^*	0.03	3.48(0.87)	0.02	0.30	0.95	0.02	0.15	-	-
$Z\gamma$	0.01	2.14(0.53)	-	0.30	0.96	-	0.15	-	-
$\mu^+\mu^-$	0.04	1.07(0.27)	0.01	0.30	0.95	0.01	0.15	-	-

$$\Delta_i^X = (100\%) \times |b_{\tau_i,X}| \frac{\Delta \tau_i}{\tau_i^{ref}}$$

	$P_{\rm BR}^{\pm}({\rm paradd.})$	$P_{\rm BR}^{\pm}(\text{parquad.})$	$(P_{\rm BR}^+, P_{\rm BR}^-)(\mu)$
<u>gg</u>	3.47(3.12)	2.09(2.04)	(0.03, 1.38)
$\gamma\gamma$	1.45(1.44)	1.01(1.01)	(1.81, 1.83)
$b\bar{b}$	2.43(1.58)	1.41(0.89)	(0.21, 0.)
$c\bar{c}$	8.72 (7.87)	5.51(5.40)	(0.54, 0.44)
$\tau^+\tau^-$	2.55(1.75)	1.47(1.04)	(0.09, 0.07)
WW^*	4.48 (2.26)	3.13(1.25)	(0.10, 0.08)
ZZ^*	4.96(2.34)	3.63(1.33)	(0.10, 0.08)
$Z\gamma$	3.56(1.96)	2.36(1.15)	(0.83, 0.80)
$\mu^+\mu^-$	2.53(1.73)	1.47(1.04)	(0.07, 0.06)

() => if the Higgs mass uncertainty were 0.1 GeV (instead of 0.4 GeV)

SM vs. New Physics? Uncertainties in BRs

	Δ_{m_t}	Δ_{m_H}	$\Delta_{\alpha(M_Z)}$	$\Delta_{\alpha_S(M_Z)}$	Δ_{m_b}	Δ_{M_Z}	Δ_{m_c}	$\Delta_{m_{\tau}}$	Δ_{G_F}
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$$\Delta_i^X = (100\%) \times |b_{\tau_i,X}| \frac{\Delta \tau_i}{\tau_i^{ref}}$$

For example, if the data at a later stage of the LHC, or ILC, or CLIC suggests that the branching fraction into b quarks can be determined to better than 1%, this does not mean that we are sensitive to new physics contributions of 1% to $H \rightarrow b\bar{b}$. The reason can be seen from Tables 6 and 7 that the SM uncertainty in computing $B(H \rightarrow b\bar{b})$ is presently 2.4% (sum of absolute values of all errors) and expected to not get better than 1.6%, with most of that coming from uncertainty of the bottom Yukawa coupling determination stemming from the uncertainty of the measured bottom quark $\overline{\text{MS}}$ mass

	$P_{\rm BR}^{\pm}({\rm paradd.})$	$P_{\rm BR}^{\pm}({\rm parquad.})$	$(P_{\rm BR}^+, P_{\rm BR}^-)(\mu)$		
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WW^*	0.04	2.9
ZZ^*	0.03	3.48
$Z\gamma$	0.01	2.1^{4}
$\mu^+\mu^-$	0.04	1.07

SM vs

Thus, without reducing this error, any new physics contribution to the bb branching fraction that is not at least a factor of three or four larger than 1% cannot be discerned from SM. Thus, a deviation of at least 3% is required of detectable new physics.

However, the lattice QCD calculation could improve it to match the experimental improvement on time. (arXiv:1404.0319v1, Lepege, Mechenzie, Peskin)

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Summary I

- * Higgs Precision can be reaching at the level of EWP
- With improved theoretical tools (e.g. expansion formalism), SM will be tested at per mille level
- * SM Higgs vs. BSM Higgs can be tested @ FCC (and ILC) beyond the typical direct search limit
- Recently a further study on low energy observables were done (see arXiv:1501.02803v1 by Petrov, Porkoski, Wells, Zhang)

Part II: Quantum Critical Higgs

B. Bellazzini, C. Csaki, J. Hubisz, S.L., J. Serra, J. Terning work in progress (to appear)

- * With the observation of a scalar with properties close to the SM Higgs, we are now confident that the interactions of the Higgs boson with gauge bosons and fermions are mainly dictated by its kinetic term and Yukawa coupling $\mathcal{L}_H = |D_\mu H|^2 \bar{\psi}^{\alpha} H \psi^{\beta}$
- * Higher-dimensional operators predict relations between the mass of a given particle and its coupling to the Higgs that deviate O(1) from the ones derived from the above Lagrangian. $|D_{\mu}H|^{2}|H|^{2}, F_{\mu\nu}^{2}|H|^{2}, \text{ or } \bar{\psi}H\psi|H|^{2}$
- * The observation at the LHC of Higgs couplings consistent with the above Lagrangian implies that such higher-dimensional operators must be treated as small perturbations.
- * The situation is however different in what regards the last part of the SM Lagrangian, the Higgs potential, $V(H) = -\mu^2 |H|^2 + \lambda |H|^4$

* Let's consider the following potential

$$\tilde{V}(H) = -\lambda |H|^4 + c_6 |H|^6$$

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Quantum Phase Transition



Higgs field near a second order Quantum Phase Transition

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- While there is no previous particle physics precedent, <u>condensed matter</u> <u>systems can produce a light scalar</u> by tuning the parameters (like temperature) close to a critical value where a continuous (second order) phase transition occurs.
- * Phase transitions happening at zero temperature are usually referred to as quantum phase transitions (QPT). It is thus natural to use a condensed matter analogy and describe the Higgs in terms of a second order QPT. <u>At</u> the second order QPT all masses vanish and the theory is scale invariant, characterized by the scaling dimensions of the field

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 a change in 1 part in 10³⁰ can push us through the phase
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If there is new physics beyond the SM then the relevant questions are: Does the underlying theory also have a QPT?"

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and, "If so, is it more interesting than mean-field theory?"

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We assume the field is not free field (assuming that the theory is close to an interacting fixed point), such that scaling dimension do not add up => our theory is not corresponding to generalized free fields theory

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 There must be a pole at m_H = 125 GeV corresponding to the observed Higgs particle

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- * One can move the cut away from the origin by shifting the kinetic term by μ : $-\mathcal{H}^{\dagger} \left[\partial^2 + \mu^2\right]^{2-\Delta} \mathcal{H}$
- * This however gives a large contribution to the potential in the $p \rightarrow 0$ limit, removing all light degrees of freedom. A light pole can be reintroduced (while leaving the cut starting at μ by subtracting the mass term:

$$-\mathcal{H}^{\dagger}\left[D^{2}+\mu^{2}\right]^{2-\Delta}\mathcal{H}+\mu^{4-2\Delta}\mathcal{H}^{\dagger}\mathcal{H}$$

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Higgs is mixing with the states of the

One can move the

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μ:

we are neglecting small SM couplings such as gauge couplings and Yukawas that represent an external deformation of the CFT: treat such deformations as small perturbations that are accounted by higher loops involving insertions of these small couplings.

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the propagator tha branch point at zero (but no pole).

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- * The upshot is that there is a CFT (QPT), it has non-trivial dynamics that will have a non-trivial 4-point function *H*⁴ which will have momentum dependence
- * the effective potential will be the $p \rightarrow 0$ limit of the momentum space 4-pt function $-\mathcal{H}^{\dagger} \left[D^2 + \mu^2 \right]^{2-\Delta} \mathcal{H} + \mu^{4-2\Delta} \mathcal{H}^{\dagger} \mathcal{H} - V(|\mathcal{H}|)$

 $\langle \mathcal{H} \rangle = \frac{\tilde{v}^{\Delta}}{\sqrt{2}}$

* We will parameterize the Higgs VEV as

$$V(\tilde{h}) = \tilde{v}^{2\Delta} \tilde{m}^{4-2\Delta} \sum_{n=0}^{\infty} \frac{c_n}{n!} \left(\frac{\tilde{h}}{\tilde{v}^{\Delta}}\right)^n$$

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completely free parameter

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The momentum space propagator for the physical Higgs scalar

$$G_h(p) = -\frac{i}{(-p^2 + \mu^2 + i\epsilon)^{2-\Delta} - \mu^{4-2\Delta} + \tilde{m}^{4-2\Delta}}$$

Location of pole (Higgs mass of 125 GeV)

$$m_h^2 = \mu^2 - \left[\mu^{4-2\Delta} - \tilde{m}^{4-2\Delta}\right]^{\frac{1}{2-\Delta}} \approx \frac{\tilde{m}^2}{2-\Delta} \left(\frac{\tilde{m}}{\mu}\right)^{2-2\Delta} \text{ for } \mu \gg \tilde{m}$$

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 Using Cauchy's integral theorem, the above propagator can be rewritten as a single pole plus a contribution of the continuum, corresponding to the usual spectral decomposition

$$-iG_h(p) = \frac{Z_h}{p^2 - m_h^2} + \int_{\mu^2}^{\infty} \frac{\rho_h(M^2)dM^2}{p^2 - M^2}$$
$$Z_h = \frac{1}{(2 - \Delta)(\mu^2 - m_h^2)^{1 - \Delta}}$$

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$$Z_h = \frac{1}{(2 - \Delta)(\mu^2 - m_h^2)^{1 - \Delta}}$$

* Rescaling field to go into a basis corresponding to canonical normalization

$$\mathcal{H} \to \frac{1}{\sqrt{2-\Delta}} \mu^{\Delta-1} H \qquad \qquad Z_h = \left(\frac{\mu^2}{\mu^2 - m_h^2}\right)^{1-\Delta} = 1 - (\Delta - 1)\frac{m_h^2}{\mu^2} + \mathcal{O}\left(\frac{m_h^4}{\mu^4}\right)$$

$$\rho_h(M^2) = \frac{\theta(M^2 - \mu^2)(2 - \Delta)\mu^{2-2\Delta}\sin\left(\pi(2 - \Delta)\right)(M^2 - \mu^2)^{2-\Delta}}{\pi\left(2\cos\left(\pi(2 - \Delta)\right)(M^2 - \mu^2)^{2-\Delta}(\mu^2 - m_h^2)^{2-\Delta} + (M^2 - \mu^2)^{4-2\Delta} - (\mu^2 - m_h^2)^{4-2\Delta}\right)}$$

$$G_h(p) = -\frac{i}{(-p^2 + \mu^2 + i\epsilon)^{2-\Delta} - \mu^{4-2\Delta} + \tilde{m}^{4-2\Delta}}$$

 Using Cauchy's integral theorem, the above prop single pole plus a contribution of the continuum, spectral decomposition

$$-iG_h(p) = \frac{Z_h}{p^2 - m_h^2} + \int_{\mu^2}^{\infty} \frac{\rho_h(M^2)dM^2}{p^2 - M^2}$$
$$Z_h = \frac{1}{(2 - \Delta)(\mu^2 - m_h^2)^{1 - \Delta}}$$

For the propagators of the Nambu-Goldstone bosons of EWSB (the longitudinal polarization of the W and Z), also contain a pole, at zero momentum, and a continuum => set m=0

* Rescaling field to go into a basis corresponding to canonical normalization

$$\mathcal{H} \to \frac{1}{\sqrt{2-\Delta}} \mu^{\Delta-1} H \qquad \qquad Z_h = \left(\frac{\mu^2}{\mu^2 - m_h^2}\right)^{1-\Delta} = 1 - (\Delta - 1) \frac{m_h^2}{\mu^2} + \mathcal{O}\left(\frac{m_h^4}{\mu^4}\right)$$

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$$-\mathcal{H}^{\dagger} \left[D^{2} + \mu^{2} \right]^{2-\Delta} \mathcal{H} + \mu^{4-2\Delta} \mathcal{H}^{\dagger} \mathcal{H} - V(|\mathcal{H}|)$$

$$[\partial^2 - \mu^2]^{2-\Delta}\delta(x-y)$$



 $-\mathcal{H}^{\dagger} \left[D^{2} + \mu^{2} \right]^{2-\Delta} \mathcal{H} + \mu^{4-2\Delta} \mathcal{H}^{\dagger} \mathcal{H} - V(|\mathcal{H}|)$

 $[\partial^2 - \mu^2]^{2-\Delta} \delta(x - y)$ $W(x, y) = P \exp\left[-igT^a \int_x^y A^a_\mu d\omega^\mu\right]$



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similar to SCET!

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* e.g. for the trilinear interaction in momentum space: $\mathcal{H}^{\dagger}(p+q)A^{a}_{\mu}(q)\mathcal{H}(p)\Gamma^{\mu,a}(p,q)$

$$\Gamma^{\mu,a}(p,q) = gT^a \left(2p^{\mu} + q^{\mu}\right) F(p,q) ,$$

$$F(p,q) = -\frac{(\mu^2 - (p+q)^2)^{2-\Delta} - (\mu^2 - p^2)^{2-\Delta}}{2p \cdot q + q^2}$$

similar to SCET!

* Off-shell Higgs can be tested via interference.



 Single Higgs production: Production of the cut modifies Higgs cross sections for energies above μ => modifies any cross sections that involve the (tree-level) exchange of the components of Higgs



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Double Higgs production



$$\frac{\mathrm{d}\hat{\sigma}}{\mathrm{d}\hat{t}} = \frac{\alpha_{\mathrm{w}}^2 \alpha_{\mathrm{s}}^2}{2^{15} \pi M_{\mathrm{W}}^4 \hat{s}^2} (|\mathrm{gauge1}|^2 + |\mathrm{gauge2}|^2)$$

gauge1 = box + triangle (negative interference)
gauge2 = box (largest contribution)

* Double Higgs production: correction on triangle diagram



$$\mathcal{L}_{\tilde{h}\tilde{h}\tilde{h}} = -C_3 \frac{\sqrt{2-\Delta}}{2v} \mu^{1-\Delta} \left(\mu^{4-2\Delta} - \left(\mu^2 - m_h^2\right)^{2-\Delta}\right) \tilde{h}^3$$

C₃=1 if the first two terms dominate we get SM-like potential (if there is small parameter expansion: unlikely that the dimensions differ from 1 very much)

C₃≠1 we can have an arbitrary potential ((or an arbitrary function of |H|^2)) if the coupling that controls the various terms is not small (presumably some CFT coupling)

$$V(|\mathcal{H}|) = -m_{\mathcal{H}}^{4-2\Delta} |\mathcal{H}|^2 + \frac{\lambda_{\mathcal{H}}}{\Lambda_V^{4(\Delta-1)}} |\mathcal{H}|^4$$

$$V(\tilde{h}) = \tilde{v}^{2\Delta} \tilde{m}^{4-2\Delta} \sum_{n=0}^{\infty} \frac{c_n}{n!} \left(\frac{\tilde{h}}{\tilde{v}^{\Delta}}\right)^n$$

Double Higgs production: correction on triangle diagram



 $|\mathcal{H}|^2 + rac{\lambda_{\mathcal{H}}}{\Lambda^{4(\Delta-1)}}|\mathcal{H}|^4$

$$\mathcal{L}_{\tilde{h}\tilde{h}\tilde{h}} = -C_3 \frac{\sqrt{2-\Delta}}{2v} \mu^{1-\Delta} \left(\mu^{4-2\Delta} - \left(\mu^2 - m_h^2\right)^{2-\Delta}\right) \tilde{h}^3$$

C₃=1 if the These expansion can be trusted only for SM-like pot expansio above ~ μ , momentum dependent terms from CFT will appear

C₃≠1 we can have an arbitrary potential ((or an arbitrary function of |H|^2)) if the coupling that controls the various terms is not small (presumably some CFT coupling)

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Direct Signals

Double Higgs production



We don't know what the CFT is: We want to learn as much as possible about it The quatities { μ , Δ , C_3 } would be a good start

but if it turns out this is indeed the right direction then one would need to study many more processes involving Higgs and momentum dependence to see if the CFT can eventually be reconstructed

* D



Summary II: Have we really discovered a SM-like Higgs boson?

- With improved theoretical tools, SM will be tested at per mille level.
- * Meanwhile we are quite ignorant about the form of Higgs potential, or even kinetic term.
- It's interesting whether the Higgs sector is close to a quantum critical point with non-mean-field behavior, that is with non-trivial critical exponents and scaling dimensions
- * LHC and FCC will explore these questions!