

# *Proton Charge Radius*

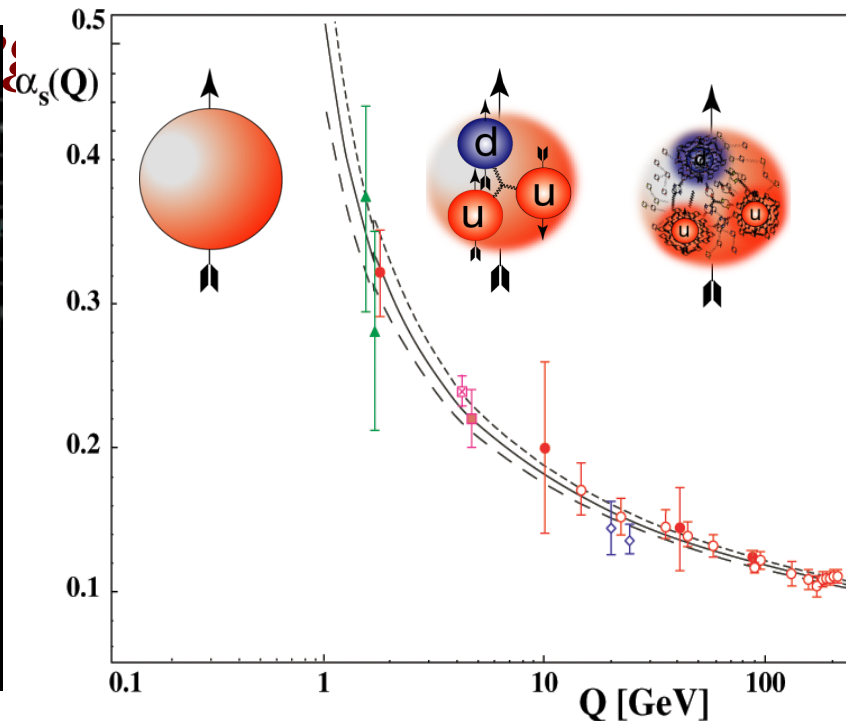
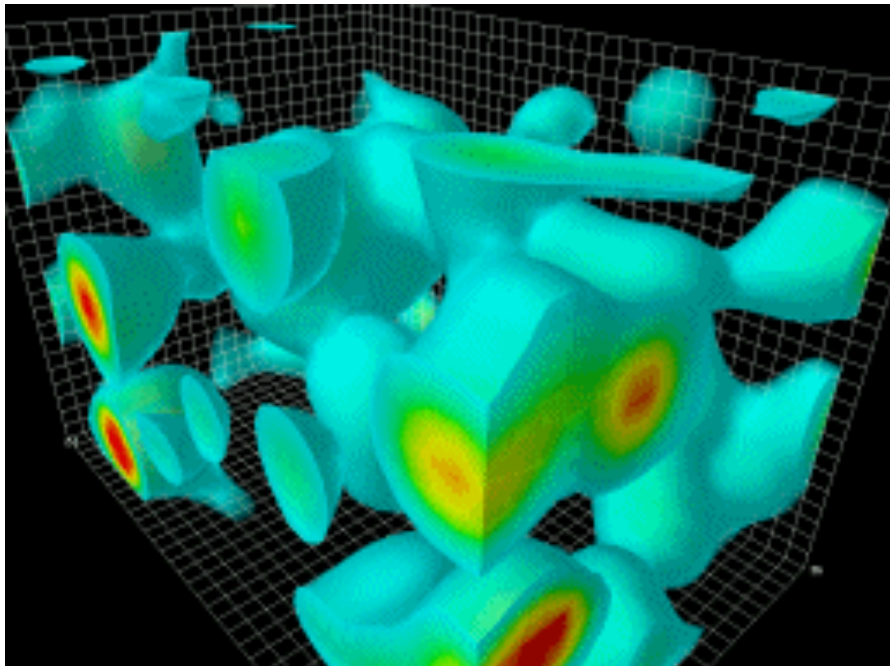
*7<sup>th</sup> Workshop on Hadron Physics in China and  
Opportunities Worldwide  
Kunshan, August 3-7, 2015*

*Haiyan Gao*

*Duke University and Duke Kunshan University*



# *QCD: still unsolved in non-perturbative*



*Gauge bosons: gluons (8)*

- **2004 Nobel prize for “asymptotic freedom”**
- **non-perturbative regime QCD ?????**
- **One of the top 10 challenges for physics!**
- **QCD: Important for discovering new physics beyond SM**
- **Nucleon structure is one of the most active areas**

# What is inside the proton/neutron?

1933: Proton's magnetic moment



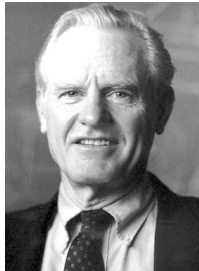
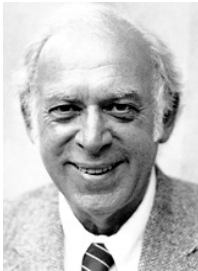
Nobel Prize  
In Physics 1943

Otto Stern

"for ... and for his discovery of the magnetic moment of the proton".

$$g \neq 2$$

1969: Deep inelastic e-p scattering



Nobel Prize in Physics 1990

Jerome I. Friedman,

Henry W. Kendall,

Richard E. Taylor

"for their pioneering investigations concerning deep inelastic scattering of electrons on protons ...".

1960: Elastic e-p scattering

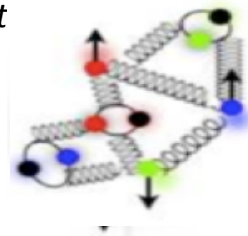


Nobel Prize  
In Physics 1961

Robert Hofstadter

"for ... and for his thereby achieved discoveries concerning the structure of the nucleons"

Form factors → Charge distributions



1974: QCD Asymptotic Freedom



Nobel Prize in Physics 2004

David J. Gross,

H. David Politzer,

Frank Wilczek

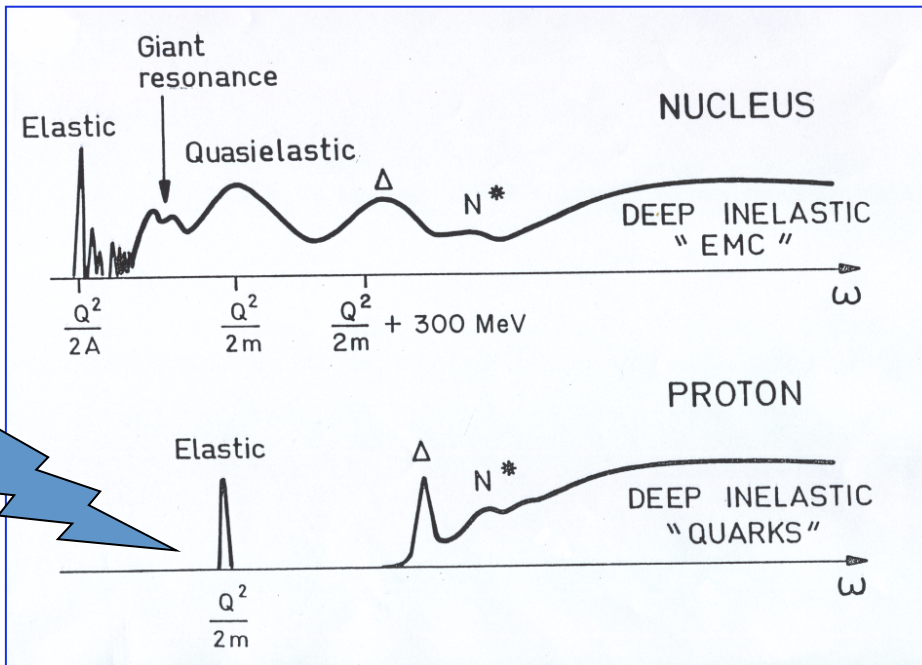
"for the discovery of asymptotic freedom in the theory of the strong interaction".

# Lepton scattering: powerful microscope!

- Clean probe of hadron structure
- Electron (lepton) vertex is well-known from QED
- **Vary probe wave-length to view deeper inside**



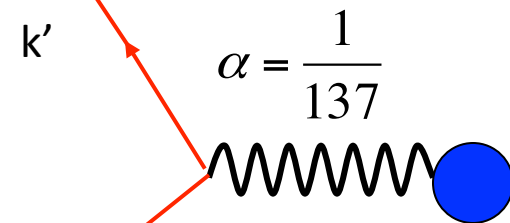
$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4E^2 \sin^4 \frac{\theta}{2}} \frac{E'}{E} \left( \frac{G_E^2 + \tau G_M^2}{1 + \tau} \cos^2 \frac{\theta}{2} + 2\tau G_M^2 \sin^2 \frac{\theta}{2} \right) \quad \tau = -q^2 / 4M^2$$



Virtual photon 4-momentum

$$q = k - k' = (\vec{q}, \omega)$$

$$Q^2 = -q^2$$



# Unpolarized electron-nucleon scattering

## (Rosenbluth Separation)

- Elastic e-p cross section

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \cos^2 \frac{\theta}{2}}{4E^2 \sin^4 \frac{\theta}{2}} \frac{E'}{E} \left( \frac{G_E^{p,2} + \tau G_M^{p,2}}{1 + \tau} + 2\tau G_M^{p,2} \tan^2 \frac{\theta}{2} \right)$$

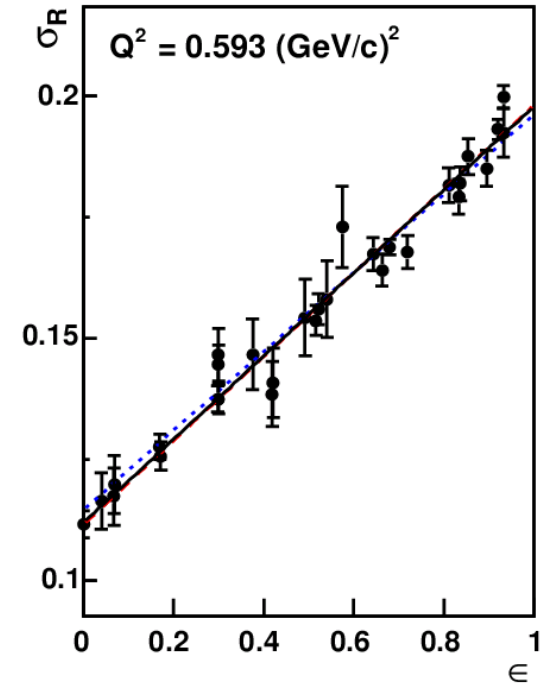
$$= \sigma_M f_{rec}^{-1} \left( A + B \tan^2 \frac{\theta}{2} \right)$$

- At fixed  $Q^2$ , fit  $d\sigma/d\Omega$  vs.  $\tan^2(\theta/2)$

– Measurement of absolute cross section

– **Dominated by either  $G_E$  or  $G_M$**

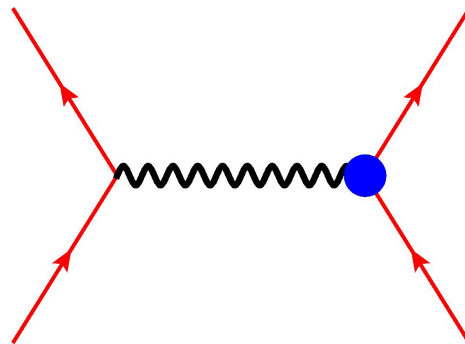
- Low  $Q^2$  by  $G_E$
- High  $Q^2$  by  $G_M$



$$\sigma_R = \tau G_M^2 + \epsilon G_E^2$$

$$\tau = \frac{Q^2}{4M^2}$$

$$\epsilon = (1 + 2(1 + \tau) \tan^2 \frac{\theta}{2})^{-1}$$



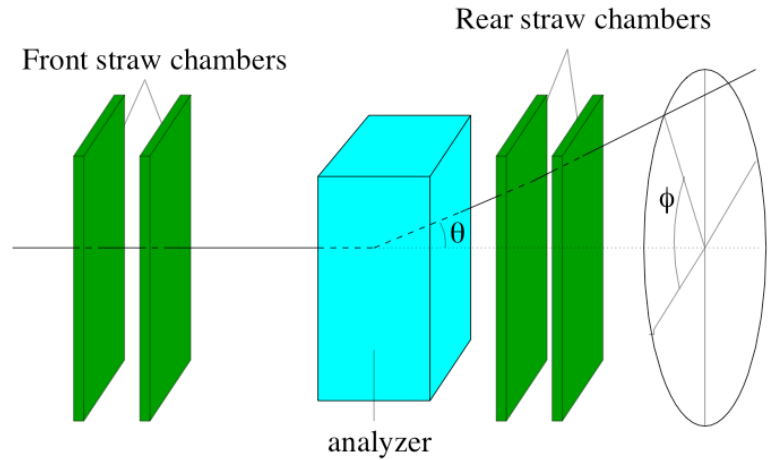
super Rosenbluth Separation (Jlab Hall A experiment)

# Recoil proton polarization measurement from e-p elastic scattering

Polarization Transfer



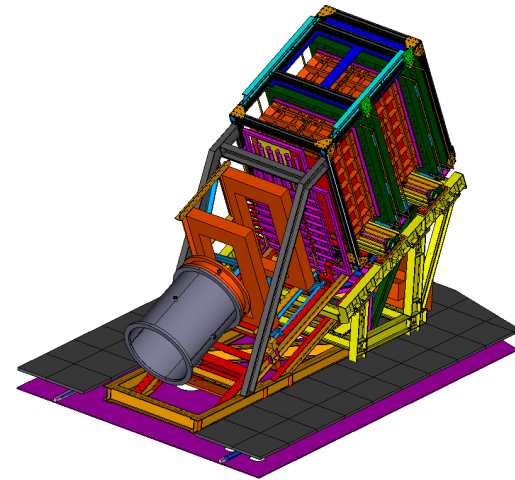
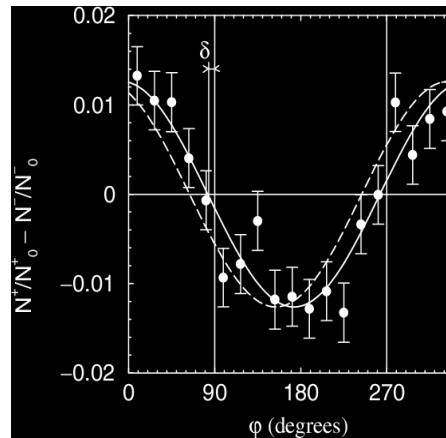
$$\frac{G_E^p}{G_M^p}$$



- Recoil proton polarization

$$\frac{G_E^p}{G_M^p} = -\frac{P_t E + E'}{P_l 2M} \tan \frac{\theta}{2}$$

- recoil proton scatters off secondary  $^{12}\text{C}$  target
- $P_t$ ,  $P_l$  measured from  $\phi$  distribution
- $P_b$ , and analyzing power cancel out in ratio



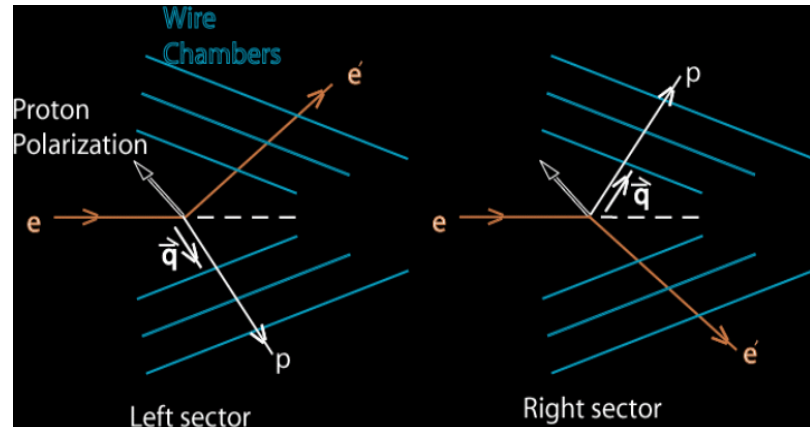
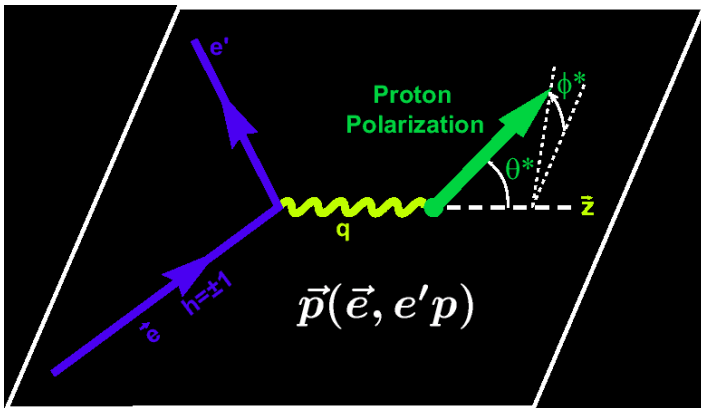
Focal-plane polarimeter

# Asymmetry Super-ratio Method

Polarized electron-polarized proton elastic scattering

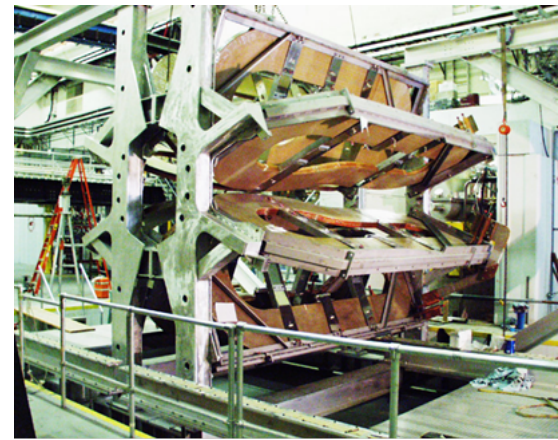
- Polarized beam-target asymmetry

$$A_{exp} = P_b P_t \frac{-2\tau v_{T'} \cos \theta^* G_M^p{}^2 + 2\sqrt{2\tau(1+\tau)} v_{TL'} \sin \theta^* \cos \phi^* G_M^p G_E^p}{(1+\tau) v_L G_E^p{}^2 + 2\tau v_T G_M^p{}^2}$$



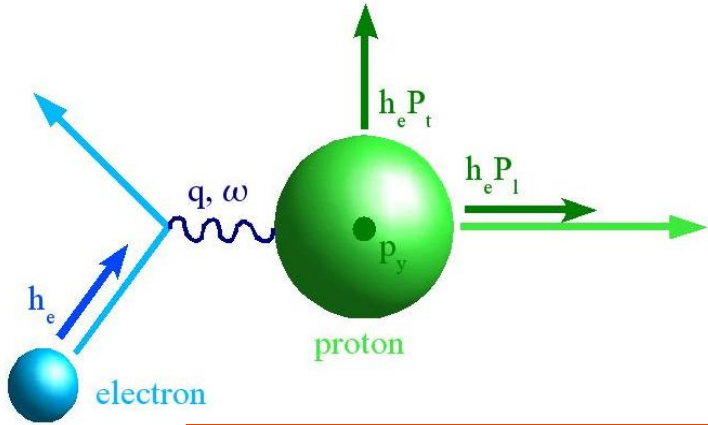
- Super-ratio

$$R_A = \frac{A_1}{A_2} = \frac{a_1 - b_1 \cdot G_E^p / G_M^p}{a_2 - b_2 \cdot G_E^p / G_M^p}$$

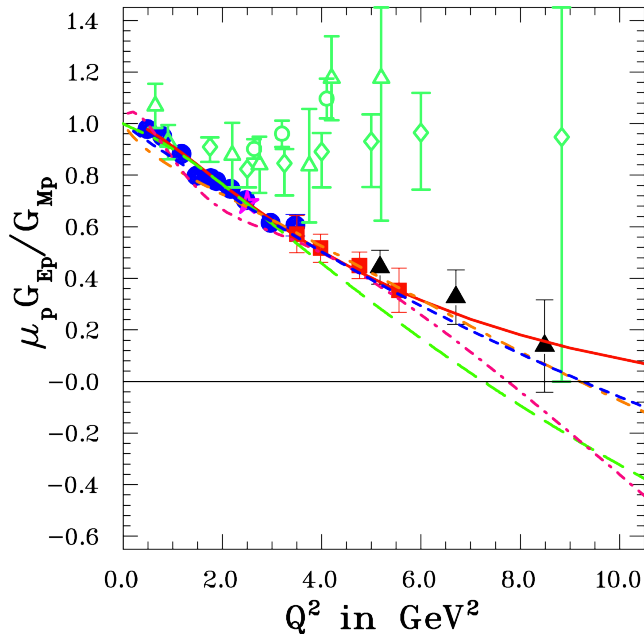


BLAST pioneered this technique, later also used in Jlab Hall A experiment

# Tremendous advances in electron scattering

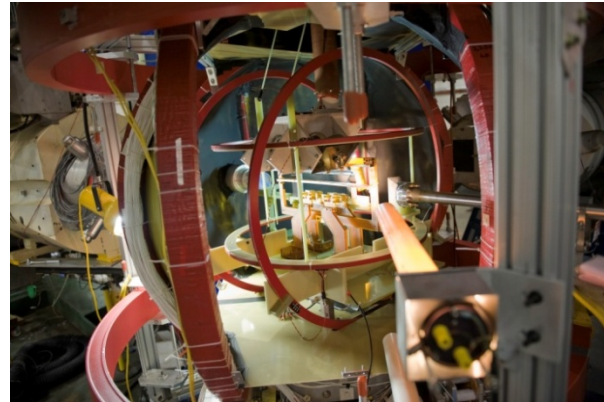


$$\frac{G_{Ep}}{G_{Mp}} = -\frac{P_t}{P_l} \frac{(E_e + E_{e'})}{2M} \tan\left(\frac{\theta_e}{2}\right)$$

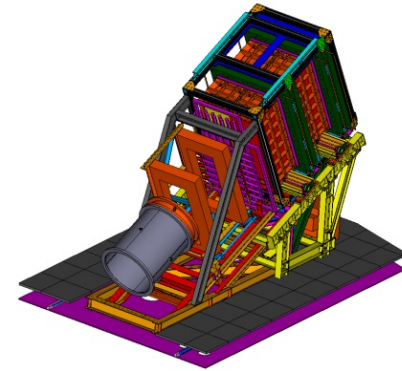


## Unprecedented capabilities:

- High Intensity and duty factor
- High quality polarized beams
- Large acceptance detectors
- State-of-the-art polarimetry, polarized targets



Polarized  $^3\text{He}$  target



Focal plane polarimeter  
– Jefferson Lab

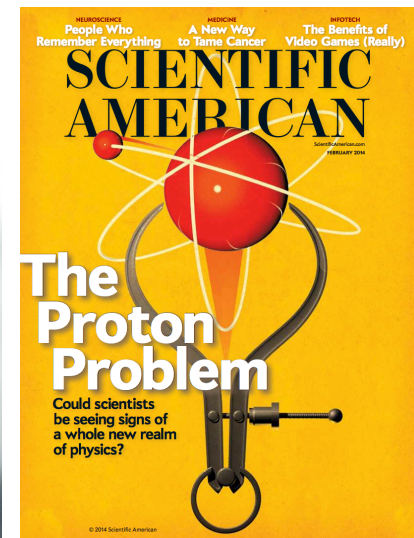


# *Proton Charge Radius*

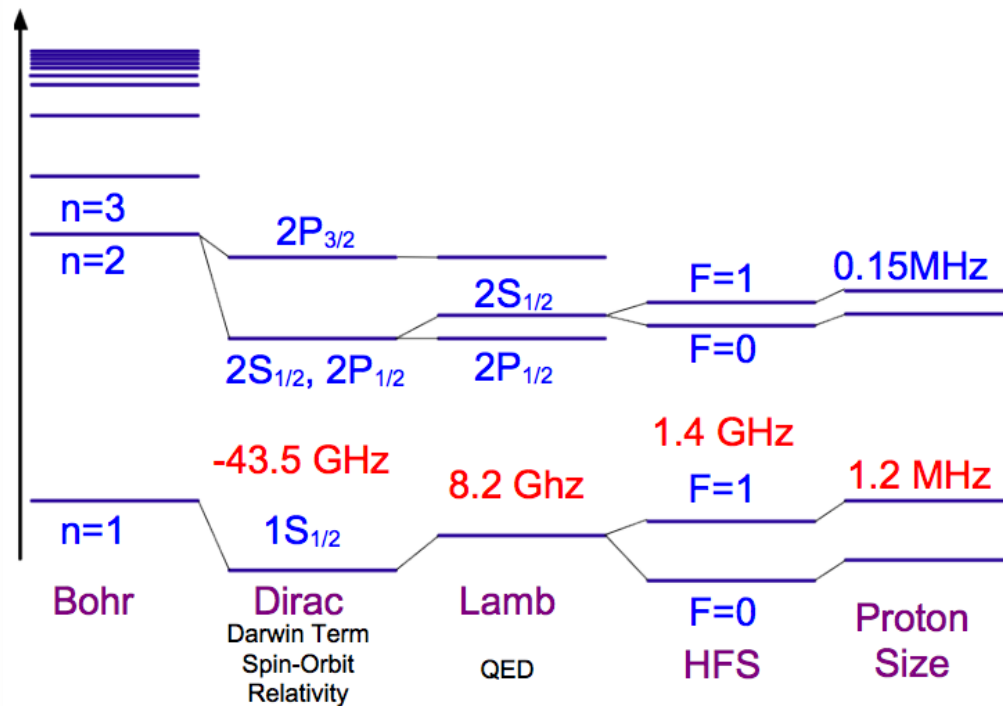
- An important property of the nucleon
  - Important for understanding how QCD works
  - An important input to bound state QED calculations, affects muonic H Lamb shift ( $2S_{1/2} - 2P_{1/2}$ ) by as much as 2%
- Electron-proton elastic scattering to determine electric form factor (Nuclear Physics)

$$\sqrt{\langle r^2 \rangle} = \sqrt{-6 \frac{dG(q^2)}{dq^2} \Big|_{q^2=0}}$$

- Spectroscopy (Atomic Physics)
  - Hydrogen Lamb shift
  - Muonic Hydrogen Lamb shift



# Hydrogen Spectroscopy



The absolute frequency of H energy levels has been measured with an accuracy of  $1.4$  part in  $10^{14}$  via comparison with an **atomic cesium fountain clock** as a primary frequency standard.

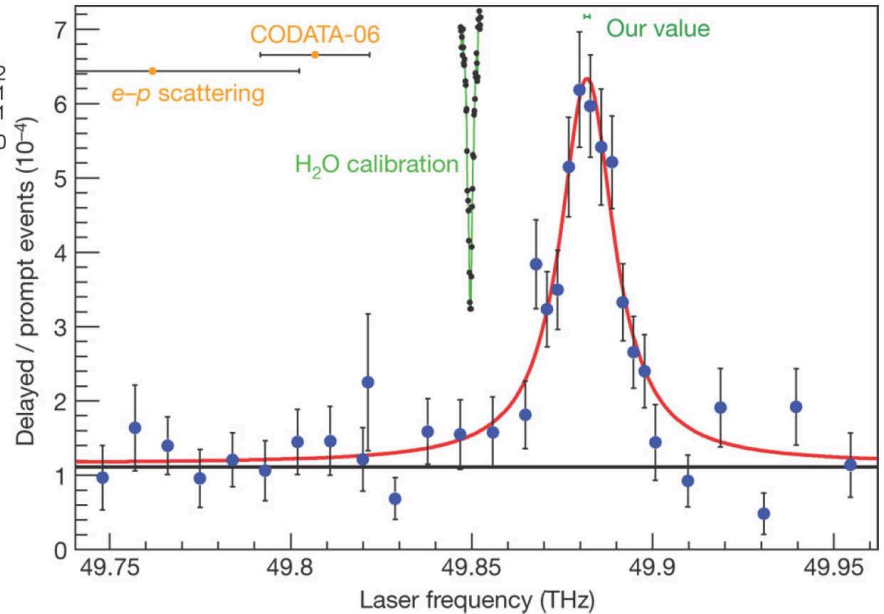
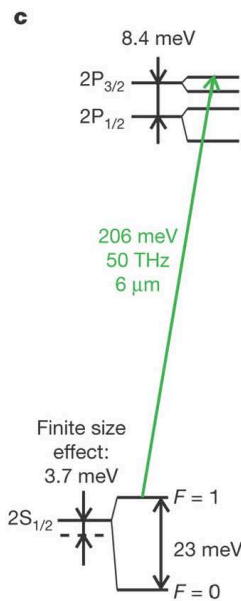
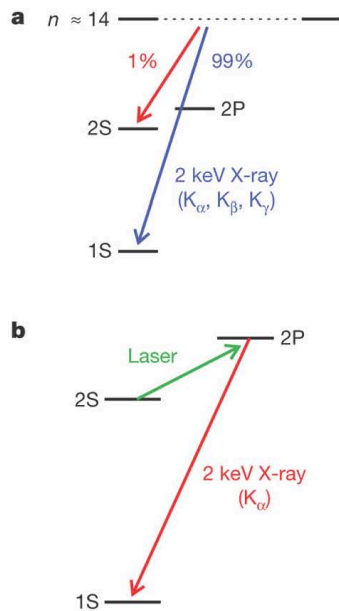
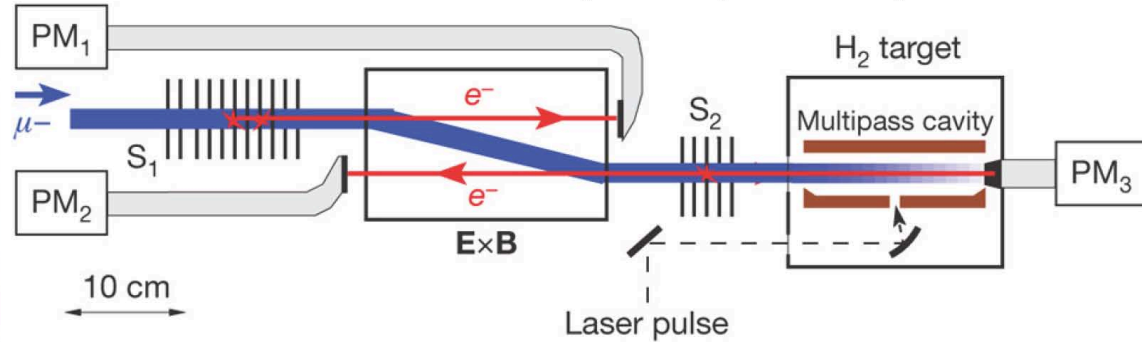
Yields  $R_\infty$  (the most precisely known constant)

Comparing measurements to QED calculations that include corrections for the finite size of the proton provide an **indirect** but very precise value of the **rms proton charge radius**

# Muonic hydrogen Lamb shift at PSI (2010, 2013)

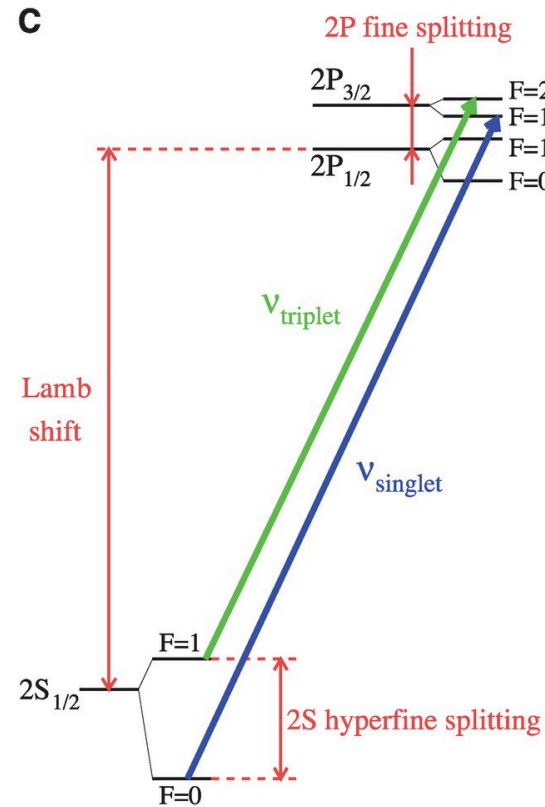
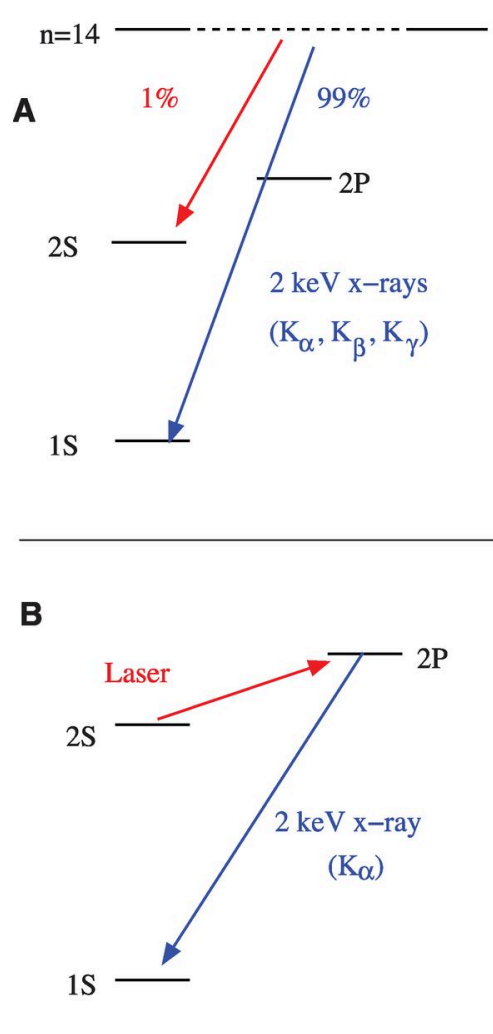


*Nature* **466**, 213-216 (8 July 2010)



2010: new value is  $r_p = 0.84184(67)$  fm

# New PSI results reported in Science 2013



$$r_p = 0.84087(39) \text{ fm,}$$

A. Antognini *et al.*, Science 339, 417 (2013)

# Recent ep Scattering Experiments

Three spectrometer facility of the A1 collaboration:

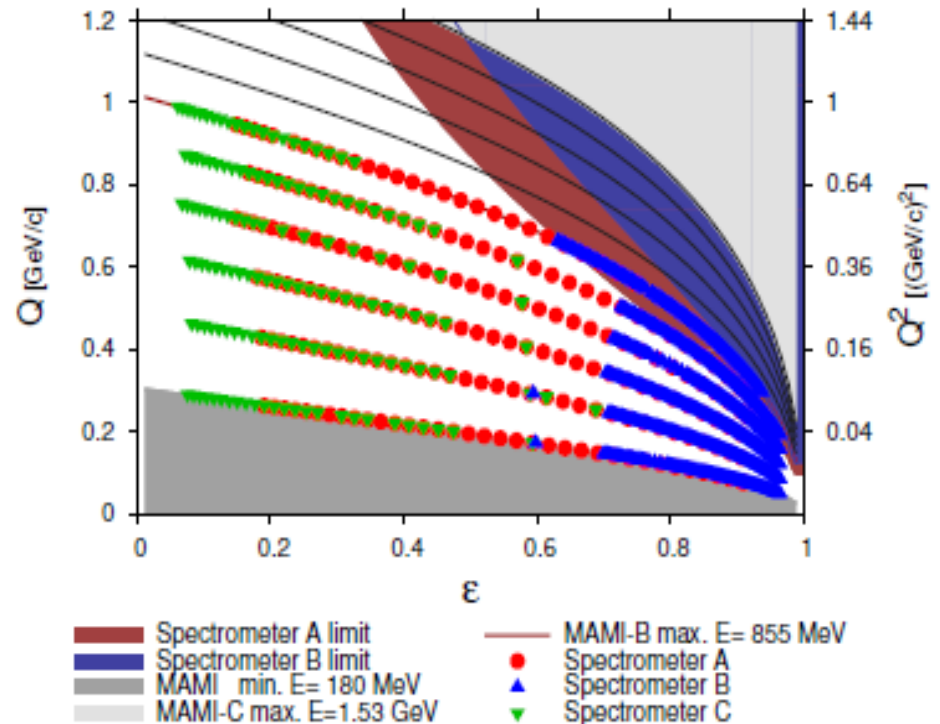


- Large amount of overlapping data sets
- Cross section measurement
- Statistical error  $\leq 0.2\%$
- Luminosity monitoring with spectrometer

■  $Q^2 = 0.004 - 1.0 \text{ (GeV/c)}^2$   
 result:  $r_p = 0.879(5)_{\text{stat}}(4)_{\text{sys}}(2)_{\text{mod}}(4)_{\text{group}}$

J. Bernauer, PRL 105,242001, 2010

Measurements @ Mainz



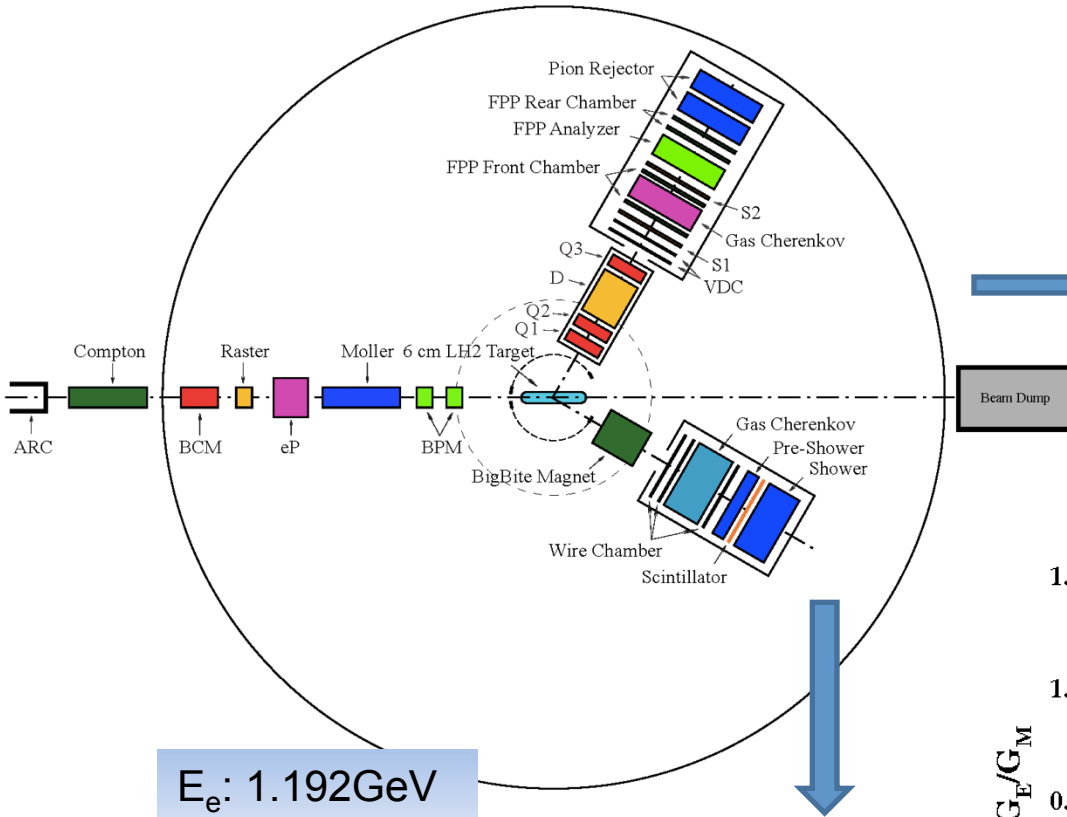
5-7 $\sigma$  higher than muonic hydrogen result !

(J. Bernauer)

# Jlab Recoil Proton Polarization Experiment

## LHRS

- $\Delta p/p_0: \pm 4.5\%$  ,
- out-of-plane:  $\pm 60$  mrad
- in-plane:  $\pm 30$  mrad
- $\Delta\Omega: 6.7$ msr
- QQDQ
- Dipole bending angle  $45^\circ$
- VDC+FPP
- $P_p: 0.55 \sim 0.93$  GeV/c

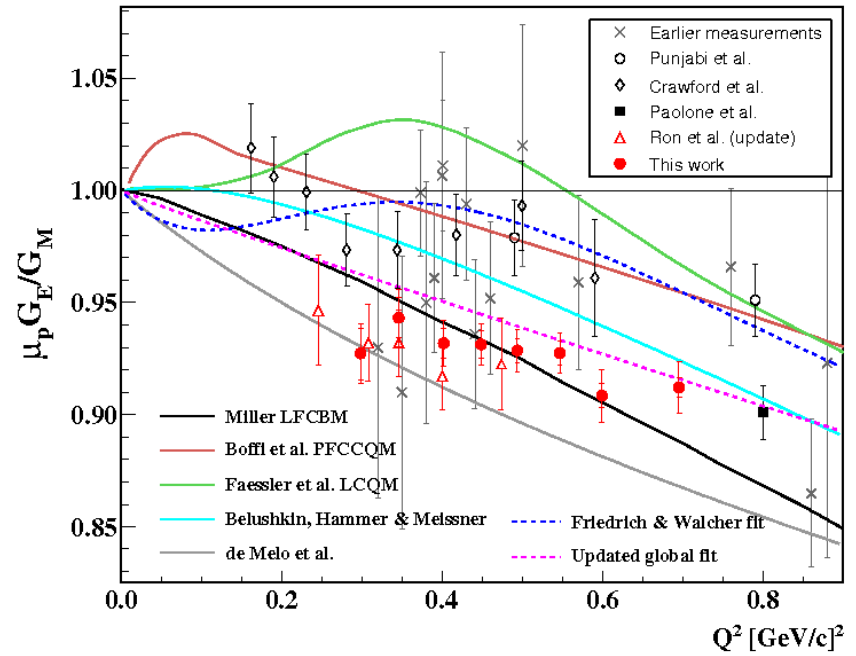


$E_e: 1.192$ GeV  
 $P_b: \sim 83\%$

## BigBite

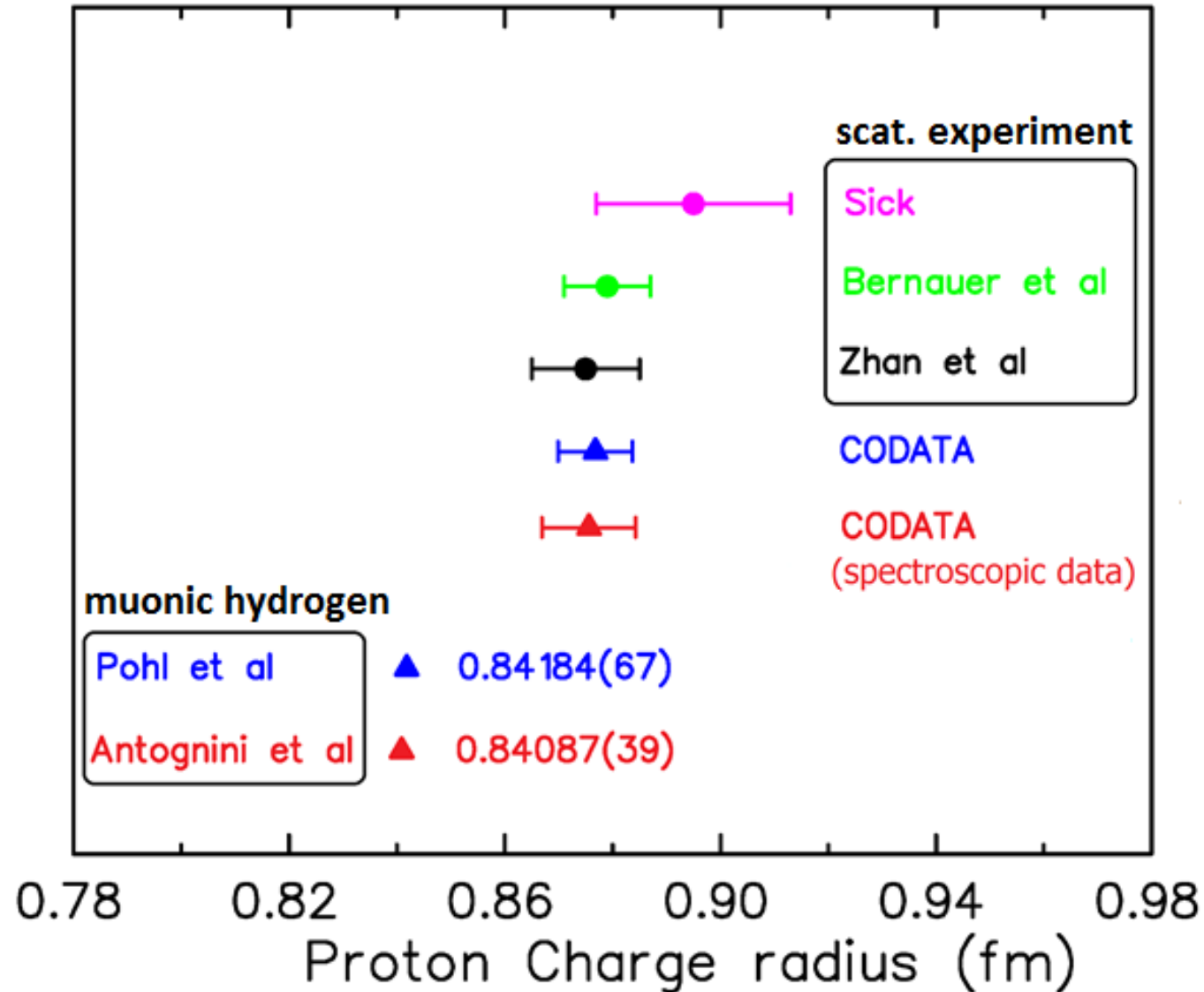
- Non-focusing Dipole
- Big acceptance.
  - $\Delta p: 200-900$ MeV
  - $\Delta\Omega: 96$ msr
- PS + Scint. + SH

**New pol. Target data soon from Hall A**



*X. Zhan et al. Phys. Lett. B 705 (2011) 59-64*  
*C. Crawford et al. PRL98, 052301 (2007)*

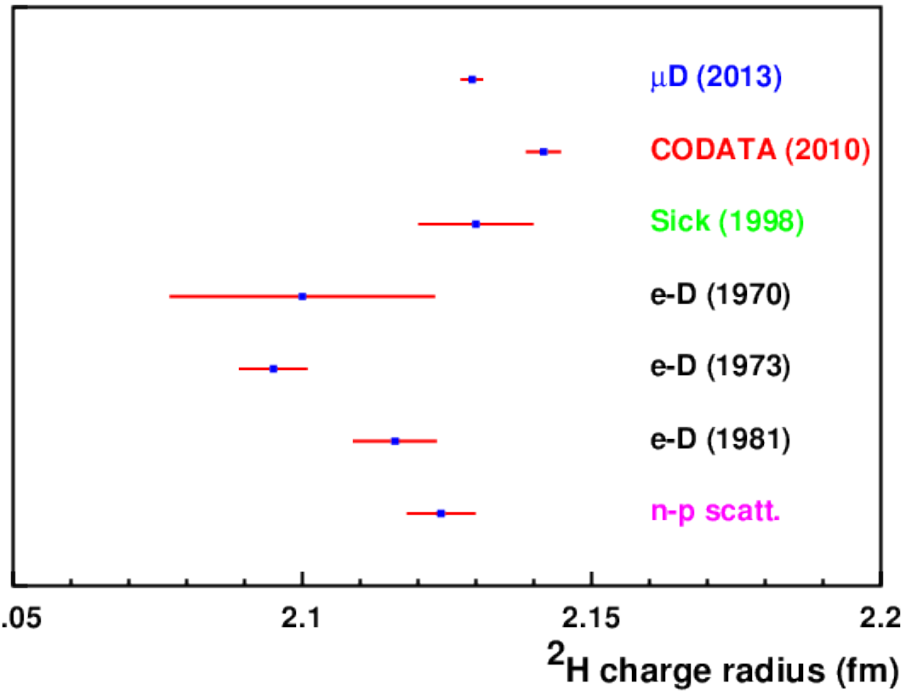
# *The proton radius puzzle intensified*



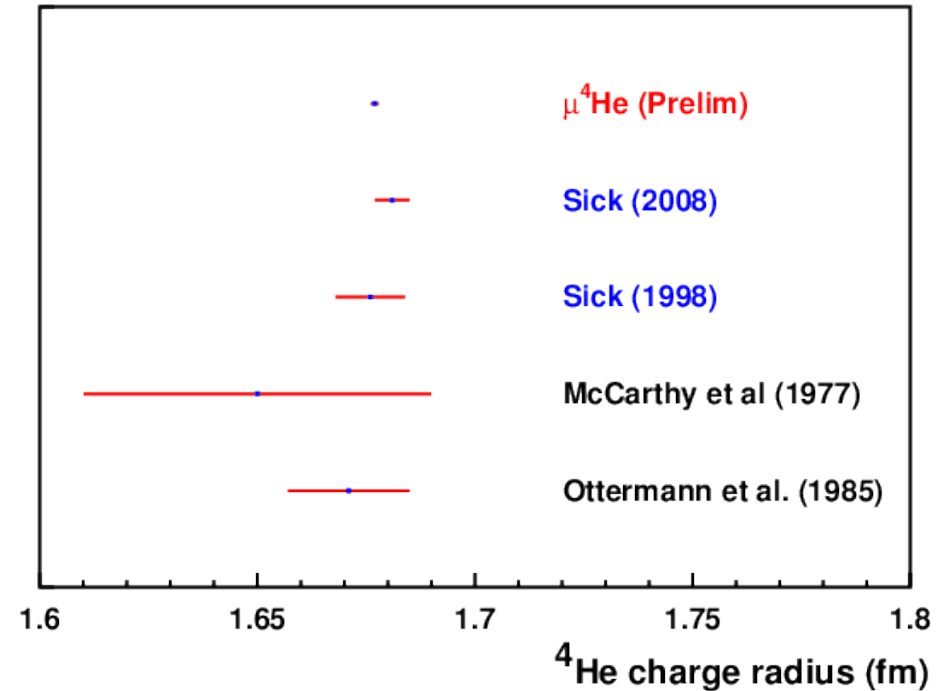
$r_p = 0.879(11)$  fm by Arrington and Sick (2015) from reanalysis of ep data

# Charge Radius of Other Light Nuclei

## Deuterium



## Helium



Electron scattering consistent with  $\mu$ -spectroscopy



# Revisits of QED Calculations....

An additional 0.31 meV to match CODATA value

Contribution	Value [meV]	Uncertainty [ $10^{-4}$ meV]
Uehling	205.0282	
Källen–Sabry	1.5081	
VP iteration	0.151	
Mixed $\mu - e$ VP	0.00007	
Hadronic VP [21, 23]	0.011	20
Sixth order VP [24]	0.00761	
Whichmann–Kroll	-0.00103	
Virtual Delbrück	0.00135	
Light-by-light	-	10
Muon self-energy and muonic VP (2 <sup>nd</sup> order)	-0.66788	
Fourth order electron loops	-0.00169	
VP insertion in self energy [17]	-0.0055	10
Proton self-energy [18]	-0.0099	
Recoil [17, 43]	0.0575	
Recoil correction to VP (one-photon)	-0.0041	
Recoil (two-photon) [19]	-0.04497	
Recoil higher order [19]	-0.0096	
Recoil finite size [32]	0.013	10
Finite size of order $(Z\alpha)^4$ [32]	$-5.1975(1) r_p^2$	(620)
Finite size of order $(Z\alpha)^5$	$0.0347(30) r_p^3$	(20)
Finite size of order $(Z\alpha)^6$	-0.0005	
Correction to VP	$-0.0109 r_p^2$	
Additional size for VP [19]	$-0.0164 r_p^3$	
Proton polarizability [18, 33]	0.015	40
Fine structure $\Delta E(2P_{3/2} - 2P_{1/2})$	8.352	10
$2P_{3/2}^{F=2}$ hyperfine splitting	1.2724	
$2S_{1/2}^{F=1}$ hyperfine splitting [42], $(-22.8148/4)$	-5.7037	20

Evaluation by Jentschura, Annals Phys. 326, 500 (2011)  
Recent summary by A. Antognini et al., arXiv:1208.2637

Birse and McGovern, arXiv:1206.3030  
0.015(4) meV (proton polarizability)

J.M. Alarcon, et al. 1312.1219  
0.008 meV

G.A. Miller, arXiv:1209.4667

New experiments at HIGS and Mainz on proton polarizabilities

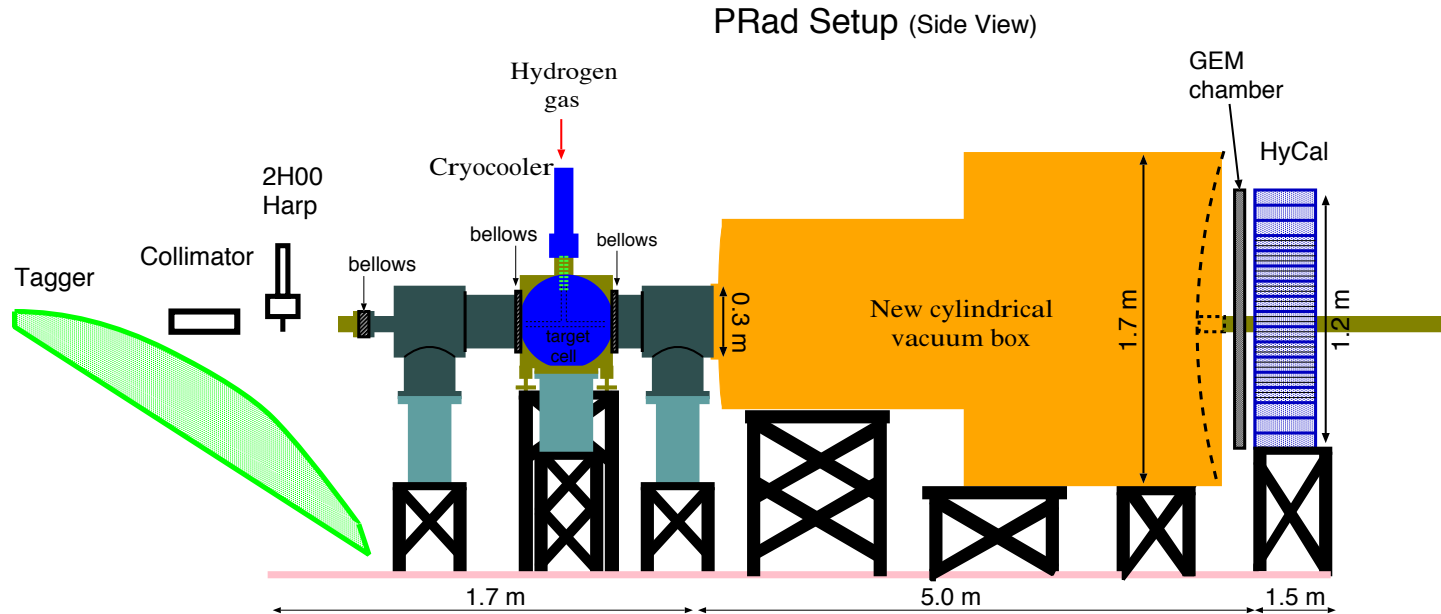
# *Incomplete list*

- **New physics: new particles**, Barger et al., Carlson and Rislw; Liu and Miller,.....  
New PV muonic force, Batell et al.; Carlson and Freid; Quantum gravity at the Fermi scale R. Onofrio;.....
- **Contributions to the muonic H Lamb shift**: Carlson and Vanderhaeghen,; Jentschura, Borie, Carroll et al, Hill and Paz, Birse and McGovern, G.A. Miller, J.M. Alarcon,.....
- **Higher moments of the charge distribution and Zemach radii**, Distler, Bernauer and Walcher,.....
- J.A. Arrington, G. Lee, J. R. Arrington, R. J. Hill discuss systematics in extraction from ep data, no resolution on discrepancy
- Donnelly, Milner and Hasell discuss interpretation of ep data,.....

**Discrepancy explained by some but others disagree**

- Dispersion relations: Lorentz et al.
- Frame transformation: D. Robson
- **New experiments: Mainz (e-d, ISR), JLab (PRad), PSI (Lamb shift, and MUSE), H Lamb shift**

# *PRad Experimental Setup in Hall B at JLab*



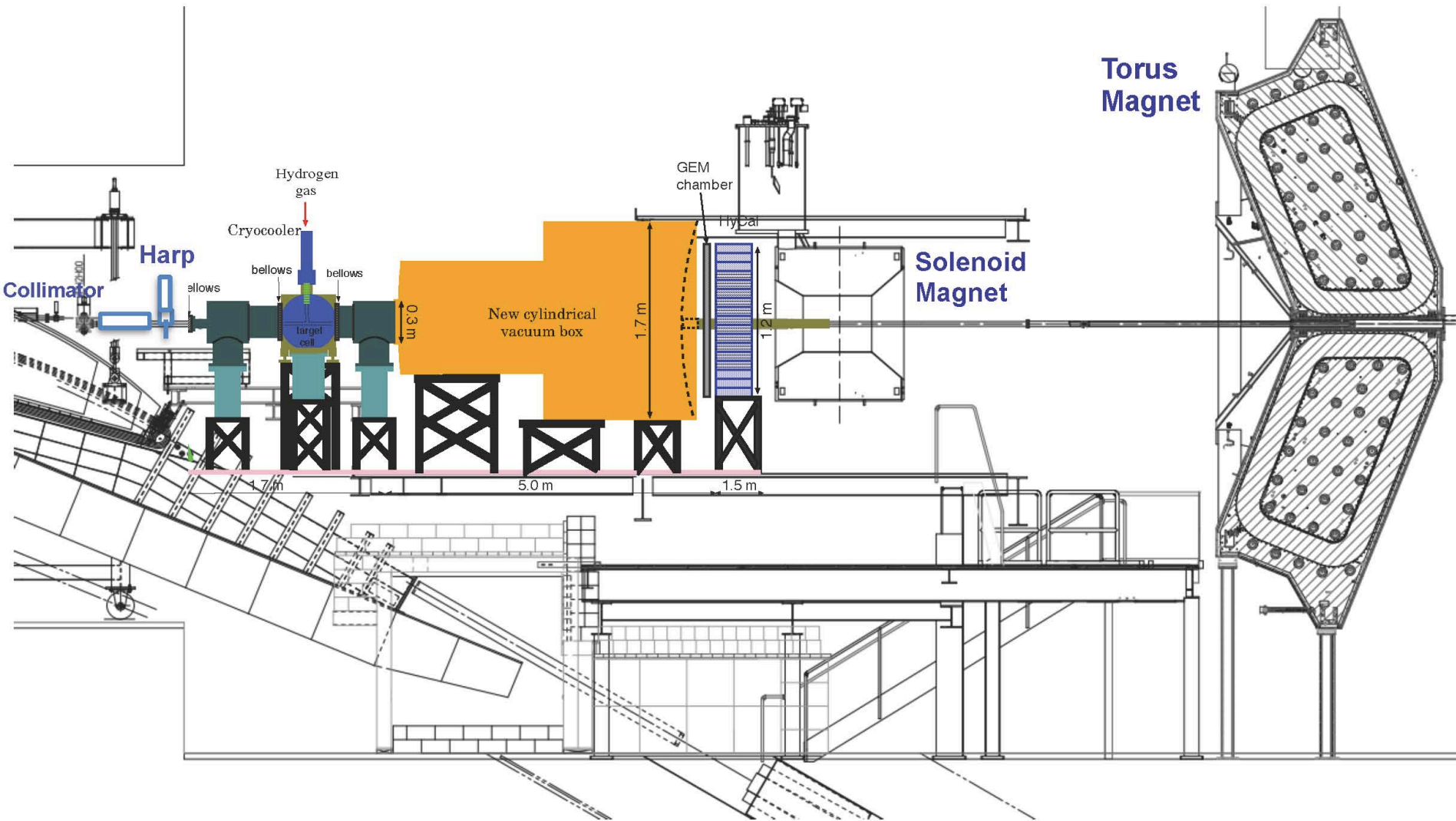
- **High resolution, large acceptance calorimeter**
- **Windowless H<sub>2</sub> gas flow target**
- **Simultaneous detection of elastic and Moller electrons**
- **GEM detectors**
- **Q<sup>2</sup> range of  $2 \times 10^{-4} - 0.14 \text{ GeV}^2$**

Future sub 1% measurements:

- (1) ep elastic scattering at Jlab (PRad)
- (2)  $\mu p$  elastic scattering at PSI - 16 U.S. institutions! (MUSE)
- (3) ISR experiments at Mainz

Ongoing H spectroscopy experiments

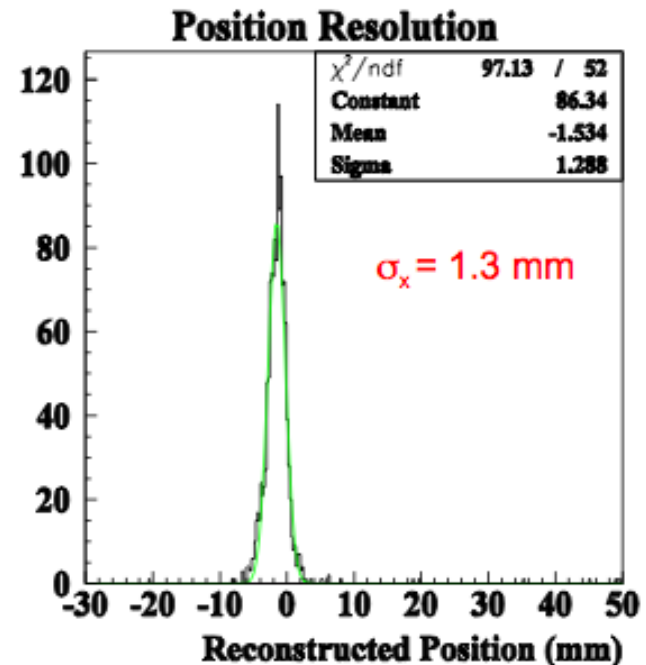
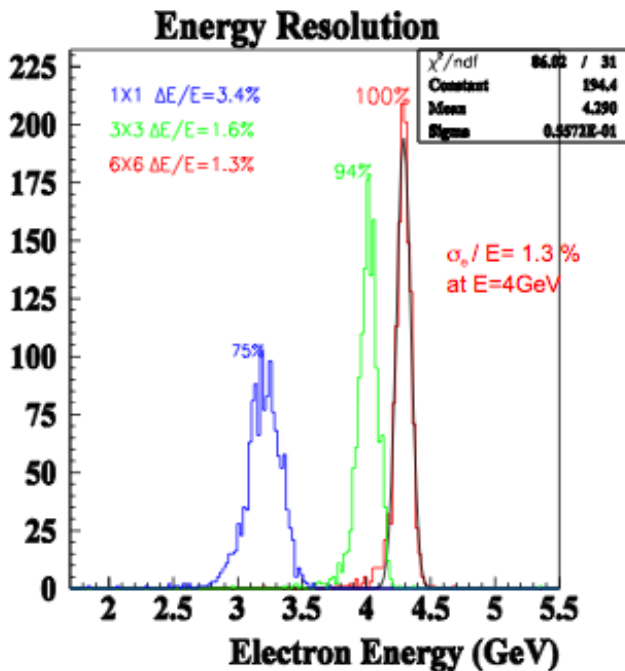
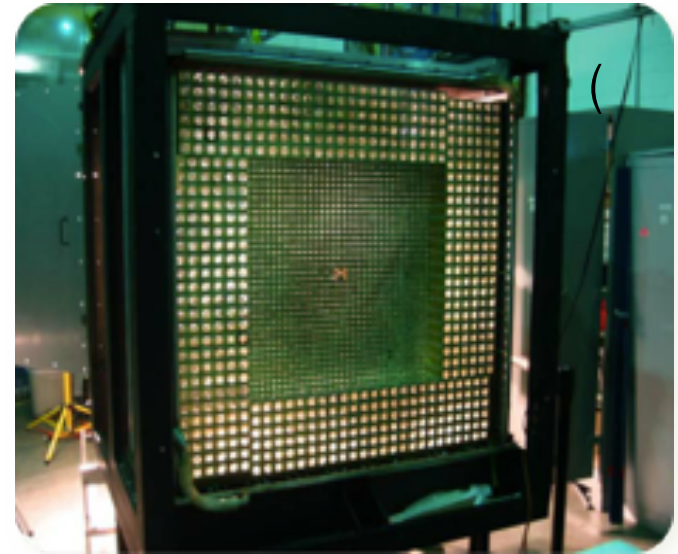
# PRad Running Setup



**Distance: 2H00 wire harp to Solenoid support frame ~13.7 m**

# High Resolution Calorimeter

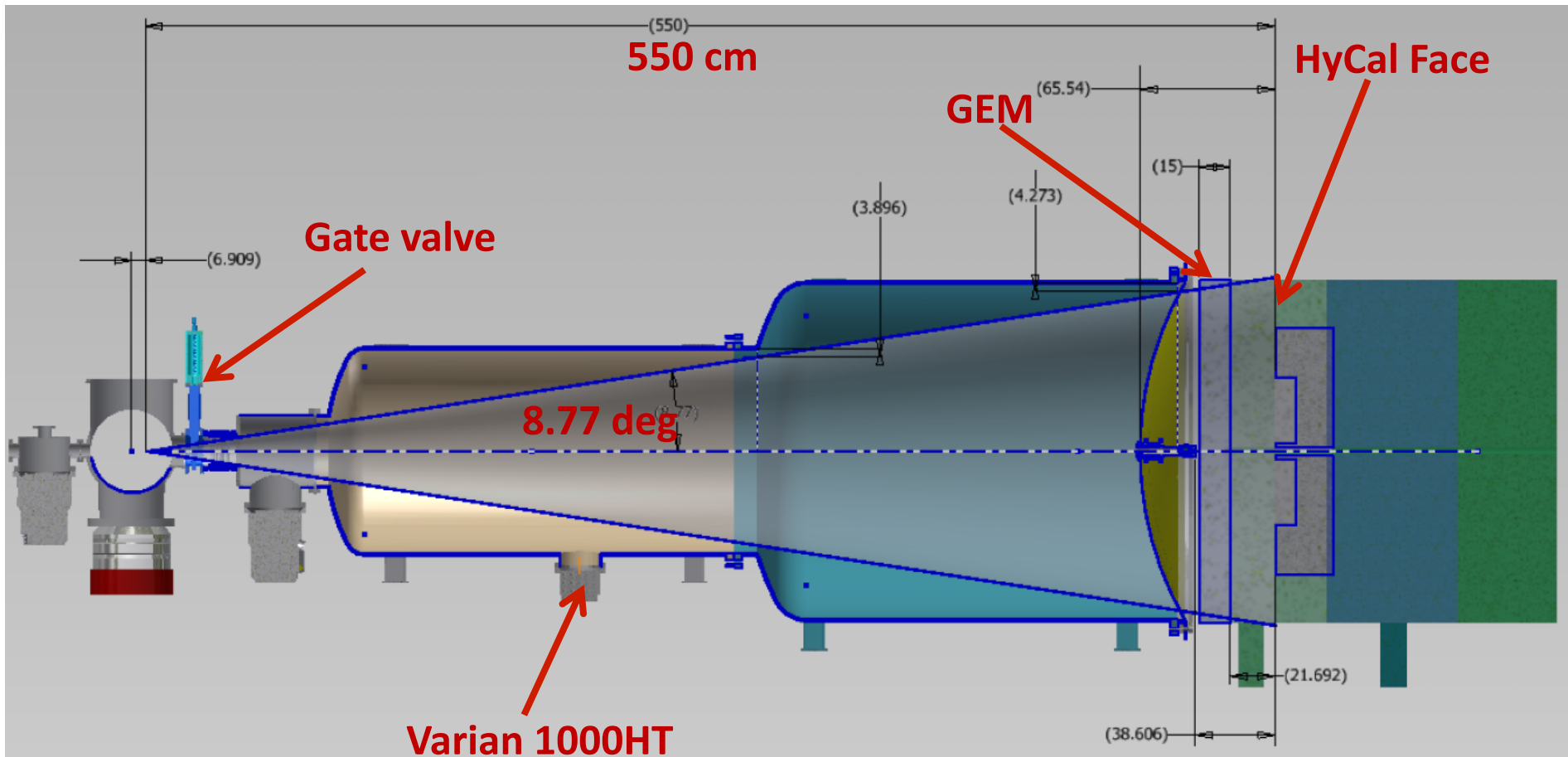
- HyCal is a  $\text{PbWO}_4$  and Pb-glass calorimeter
- $2.05 \times 2.05 \text{ cm}^2 \times 18 \text{ cm}$  (20 rad. Length)
- 1152 modules arranged in  $34 \times 34$  matrix
- $\sim 5 \text{ m}$  from the target,
- $0.5 \text{ sr}$  acceptance



# *Vacuum Box and GEM*

**Two-cylinder design for vacuum box**

**GEM detector to replace veto counter to improve Q2 resolution  
(particularly with using lead blocks)**

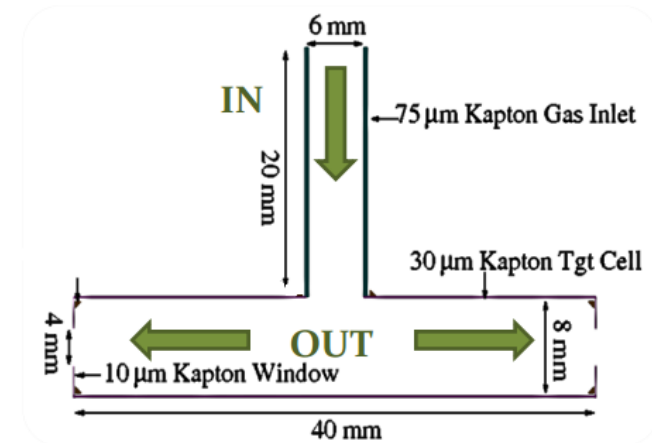


■ **GEM detector funded by DOE**

# Windowless $H_2$ Gas Flow Target

## Target cell (original design):

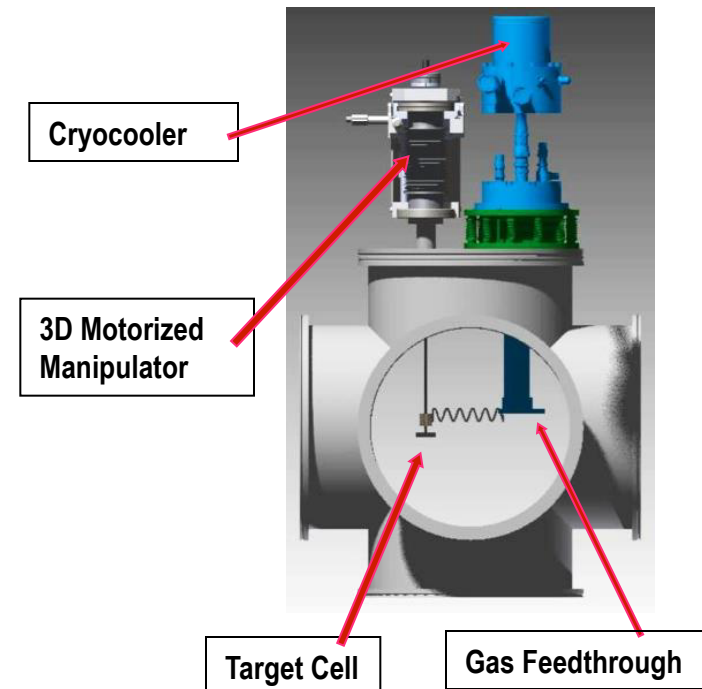
- cell length 4.0 cm
- cell diameter 8.0 mm
- cell material 30  $\mu\text{m}$  Kapton
- input gas temp. 25 K
- target thickness  $1 \times 10^{18}$  H/cm<sup>2</sup>
- average density  $2.5 \times 10^{17}$  H/cm<sup>3</sup>
- gas mass-flow rate 6.3 Torr-l/s  $\approx$  430 sccm



## Target components:

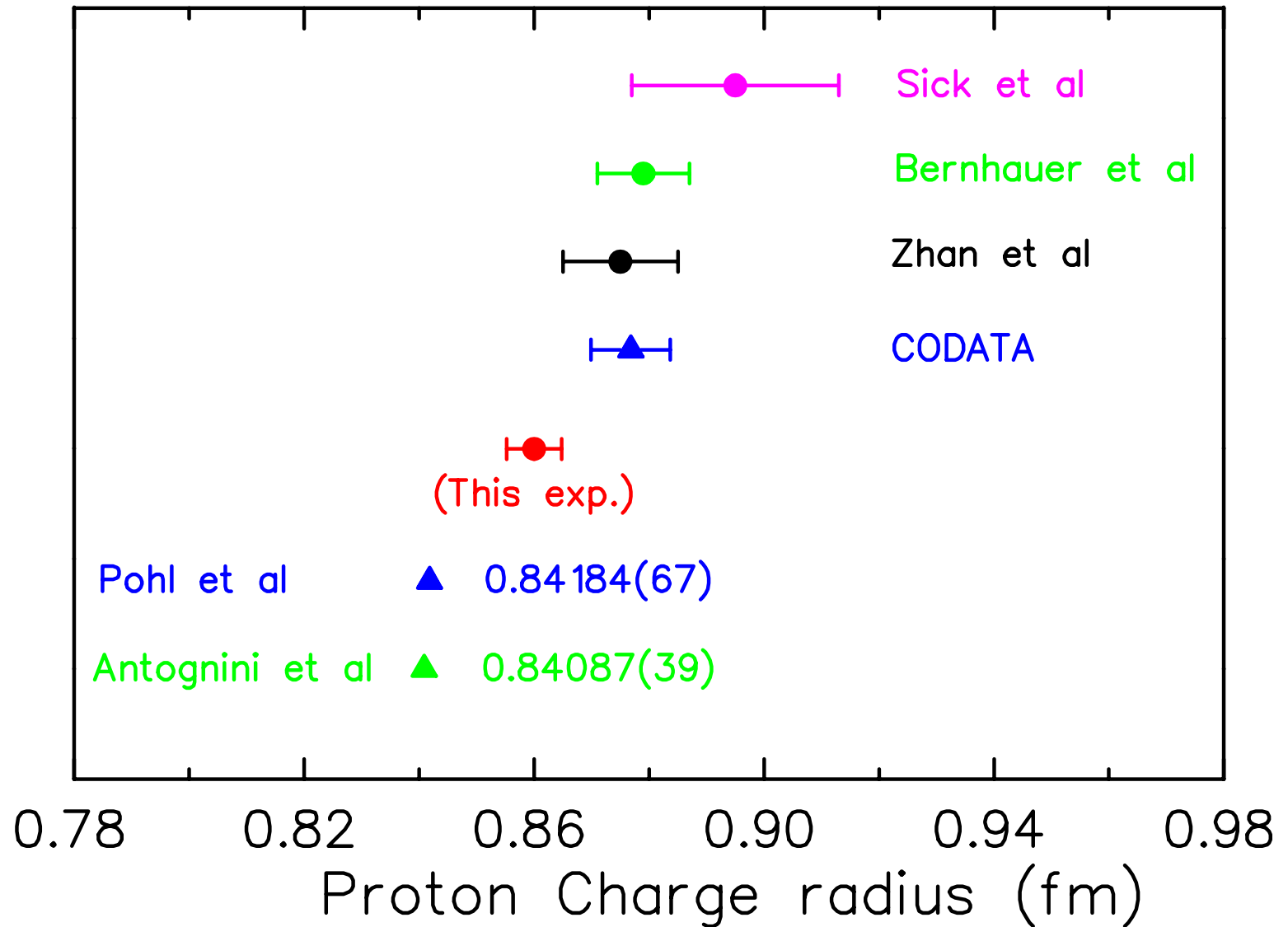
- pumping system
- cryocooler
- motorized Manipulator
- chillers for pumps and cryocooler
- Target and secondary chambers

## Kapton cell



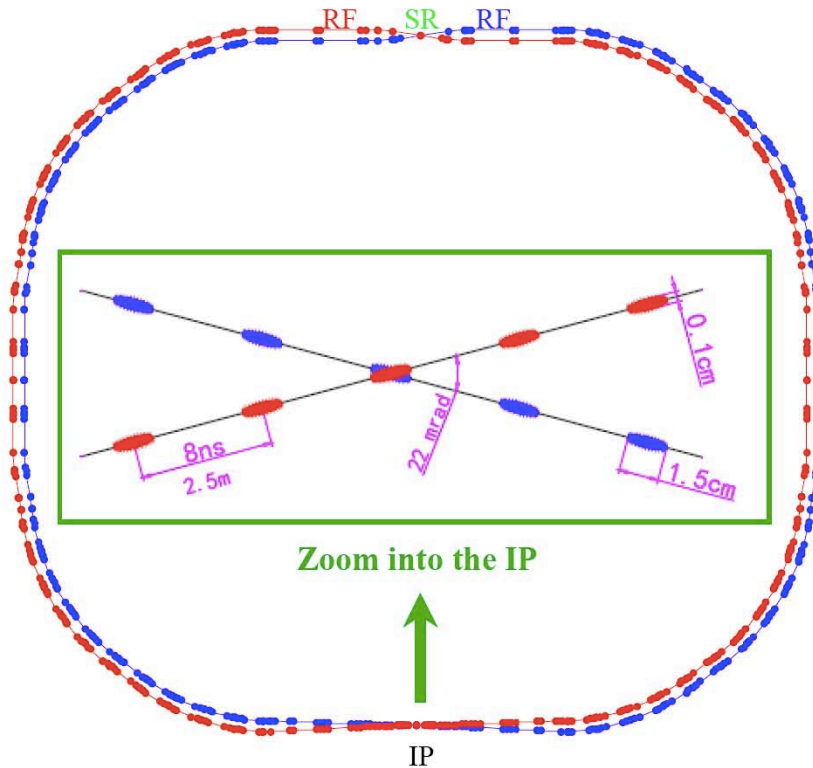
Target supported by NSF - MRI grant and is complete

# *PRad Projected Result*





# The BEPCII electron-positron double storage rings



<b>Beam energy:</b>	<b>1.0-2.3 GeV</b>
<b>Design Luminosity:</b>	<b><math>1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}</math></b>
<b>Optimum energy:</b>	<b>1.89 GeV</b>
<b>Energy spread:</b>	<b><math>5.16 \times 10^{-4}</math></b>
<b>No. of bunches:</b>	<b>93</b>
<b>No. <math>e^+</math> or <math>e^-</math>/bunch</b>	<b><math>4.5 \times 10^{12}</math></b>
<b>Bunch length:</b>	<b>1.5 cm</b>
<b>Bunch distance</b>	<b>2 m</b>
<b>Beam size <math>\sigma_x/\sigma_y</math></b>	<b>380/5.7 <math>\mu\text{m}</math></b>
<b>Current/bunch</b>	<b>9.8 mA</b>
<b>Total current:</b>	<b>0.91 A</b>
<b>Circumference:</b>	<b>237m</b>
<b>Injection rate for <math>e^+</math></b>	<b>50 mA/s</b>
<b>Injection rate for <math>e^-</math></b>	<b>200 mA/s</b>

**Only running experiment: BESIII**

**Start data taking: 2009**

**Estimated end of BESIII life time: 2022**

**Can we do more experiments with BEPCII?**

2015-8-7

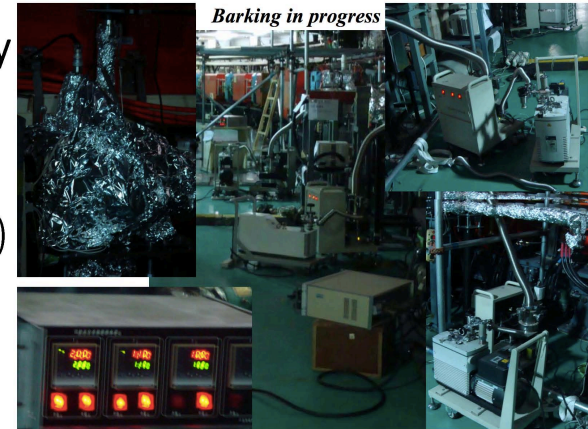
## PRad at BEPCII?

# Beam energy measurement

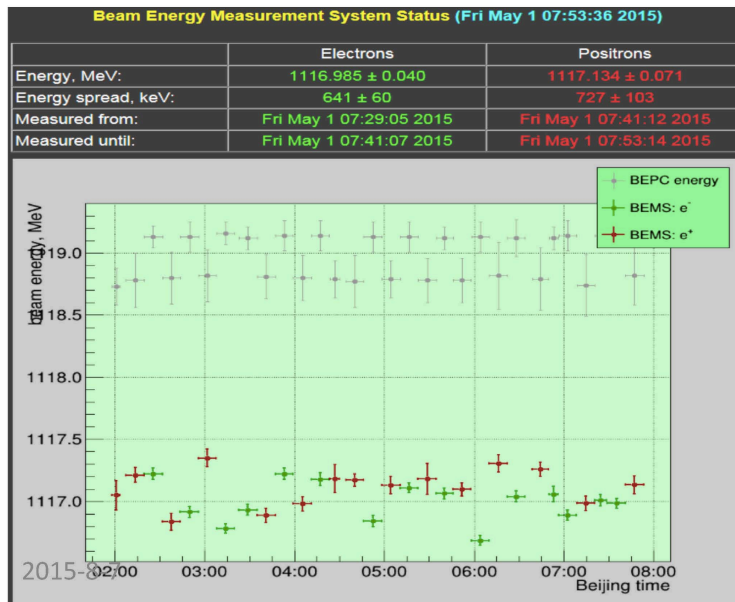
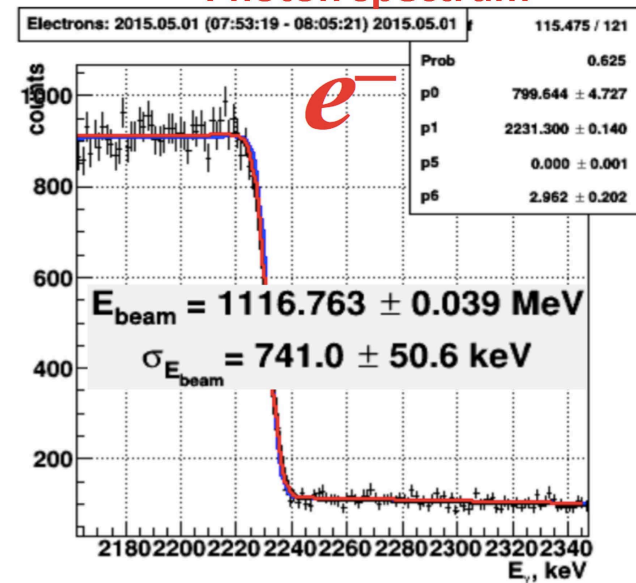
- ◆ Reconstruction of the beam energy from an energy spectrum of laser photons backscattered on beam particles:

$$E_{beam} = \frac{\omega_{max}}{2} \times \left(1 + \sqrt{1 + m_e^2 / \omega_0 \omega_{max}}\right)$$

- ◆ Achieved accuracy is  $\Delta E/E \approx 4 \times 10^{-5}$
- ◆ This allows us to tune the BEPCII operation regimes, to monitor the beam energy, and to apply corrections during data analysis .



Photon spectrum



# *Summary*

- Proton charge radius puzzle still unresolved awaiting new results
- The PRad Experiment at Jefferson Lab will be ready to take data by the end of 2015
- Potential opportunities: Mainz, and BEPII?
- Stay tuned

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