

# TWO TOPICS ON CHARMONIUM-LIKE STATES

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2015.6.  
Jinan, Shandong

# TOPIC I: DISTINGUISHING CUSP EFFECTS AND NEAR-THRESHOLD-POLE EFFECTS

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In collaboration with Zhiguang Xiao(肖志广) USTC

[arXiv:1505.05761](https://arxiv.org/abs/1505.05761)

# MOTIVATION

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- *More and more near-threshold charmonium-like and bottomonium-like structures, dubbed  $Z_c$ 's and  $Z_b$ 's, are observed.*
- *Since these signals are near thresholds, there are debates on the origin of these signals.*

*The threshold cusp effects.*

**Bugg, EPL 96,11002(2011)   Chen et.al., PRD 84,034032(2011)   Swanson, PRD 91,034009(2015)**

*Importance of higher-order contributions*

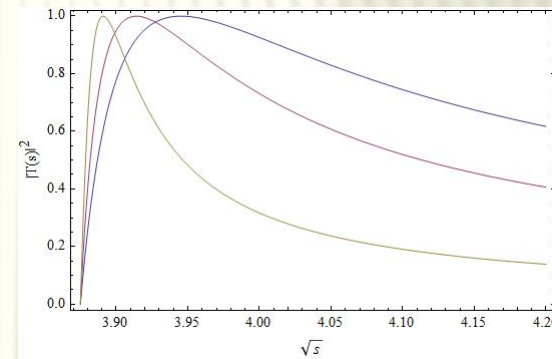
**Guo et.al., PRD91,051504(2015)**

*No pole even including higher-order contributions.*

**Swanson, arXiv:1504.07952**

# OUR OPINION

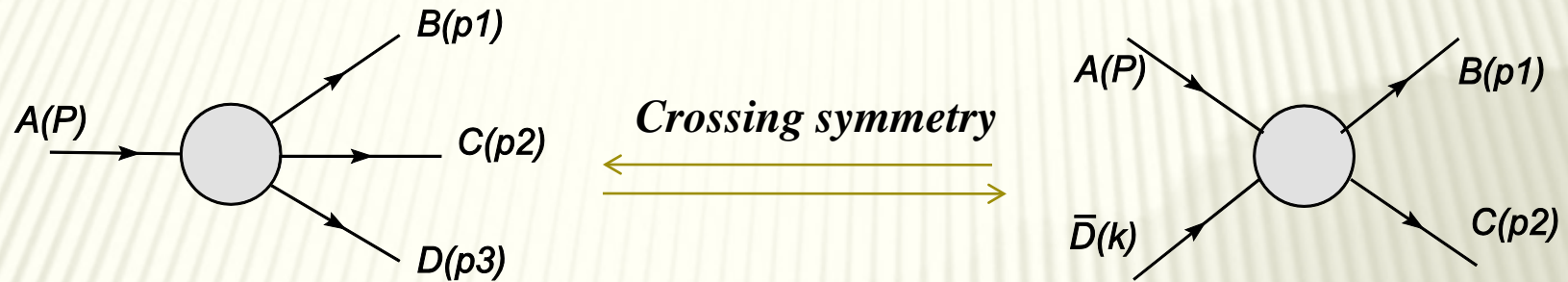
- *Threshold cusps come from the unitarity cut. It always be there. How to distinguish the threshold cusp effect and the near-threshold-pole effects? Establishing a model with correct general properties and determining the signal by data.*



- *Unitarity and analyticity play important roles in non-perturbative analyses. Coupled-channel unitarity also put more constraints to the model parameters. It also provides us a chance to analyze the data with different final states at the same time.*
- *Summing up higher-order diagrams is a consensus of theorists in studying nonperturbative problems.*



# THE MODEL



*Crossing symmetry requires that the decay amplitude and the scattering amplitude are the same functions with the Mandelstam variables in different physical regions.*

$$s = (p_1 + p_2)^2, t = (p_1 + p_3)^2, u = (p_2 + p_3)^2,$$

$$\text{where } s + t + u = m_A^2 + m_B^2 + m_C^2 + m_D^2.$$

*We build a factorization form for a two-body scattering process first.*

# THE MODEL

*Factorization form of T matrix in “Argand unit”*

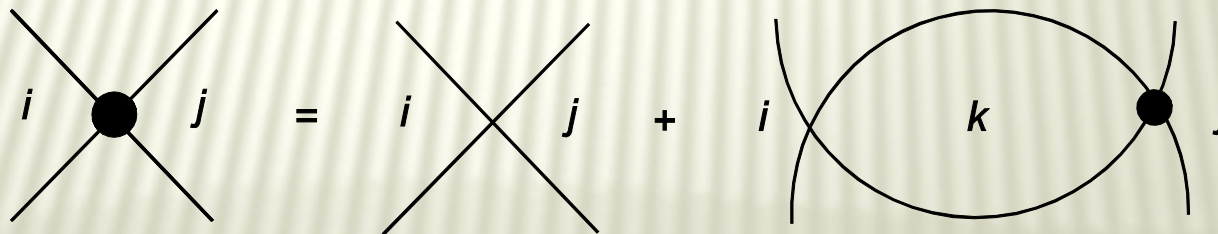
$$T = G^+ \Sigma G \quad \text{in a matrix form}$$

$$G = \left\{ \begin{array}{ccc} G_1(s) & 0 & 0 \\ 0 & G_2(s) & 0 \\ 0 & 0 & G_3(s) \\ & & \ddots \end{array} \right\} \quad \text{where} \quad G_n(s) = \sqrt{\rho_n(s)} f_n(s) \theta(s - s_{th,n})$$

$\Sigma$  satisfies several iterative equations in a matrix form

$$\Sigma = \lambda + \lambda \Pi \Sigma$$

which could be represented pictorially as



*It could be regarded as a Simplification of Lippmann-Schwinger equation.*

**Kaiser et.al., NPA594,325(1995) Oller and Oset, NPA620,438(1997)**

# THE MODEL

*Coupled-channel unitarity leads to*

$$\text{Im } \Sigma^{-1} = -GG^+$$

$$\Sigma^{-1} = \lambda^{-1}(I - \lambda\Pi)$$

$$\text{Im } \Pi = GG^+$$

*which means the imaginary part of  $\Pi$*

$$\text{Im } \Pi_n = \rho_n(s) f_n^2(s) \theta(s - s_{th,n}).$$

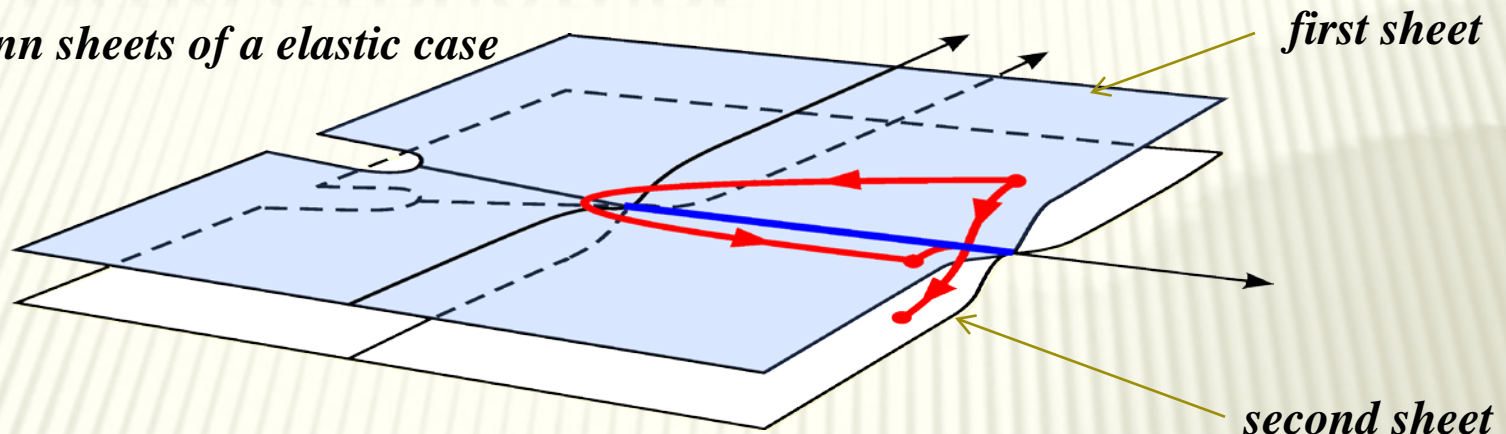
*The real part of  $\Pi$  could be represented by a dispersion relation*

$$\text{Re } \Pi_n = \frac{1}{\pi} \int_{s_{th,n}}^{\infty} \frac{\text{Im } \Pi_n(s)}{z - s} dz.$$

*One can easily analytically continue the amplitudes to complex  $s$ -plane and study its analytic structure.*

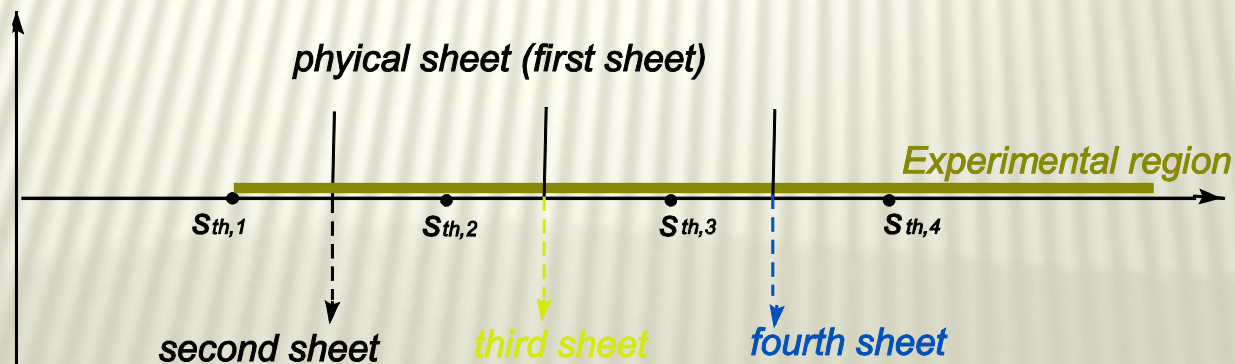
# ANALYTIC STRUCTURE

*Riemann sheets of a elastic case*



*For a  $n$ -channel case, there are  $2^n$  Riemann sheets, but only the closest sheets are important.*

Complex  $s$ -plane





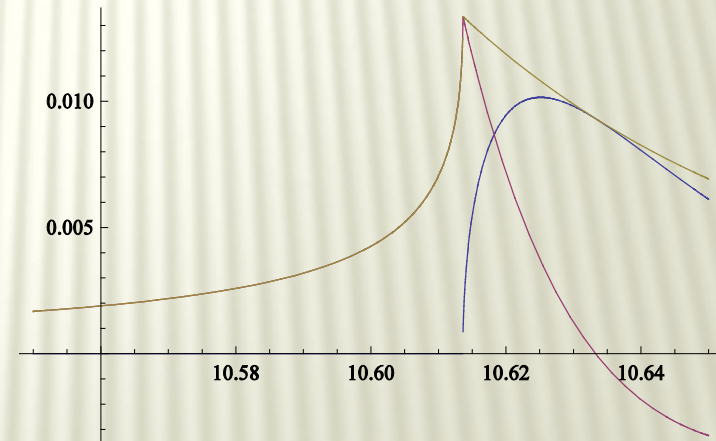
# PICTURE

*The poles appear at the zero points of determinant of  $(I - \lambda\Pi)$ , since*

$$\Sigma^{-1} = \lambda^{-1}(I - \lambda\Pi)$$

*For a elastic case (only one channel), if the coupling constant is stronger than  $\Pi(s_{th})$ , there exists a bound-state pole on the first sheet. When the coupling becomes weaker, the pole moves to the threshold, crosses it, and become a virtual-state pole on the second sheet.*

*For a inelastic case, the poles usually move to the complex  $s$ -plane and become resonance poles.*

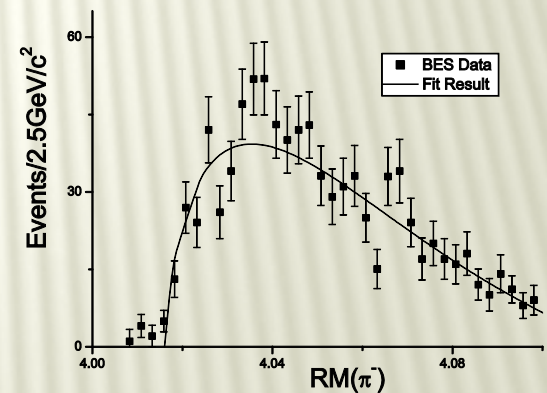
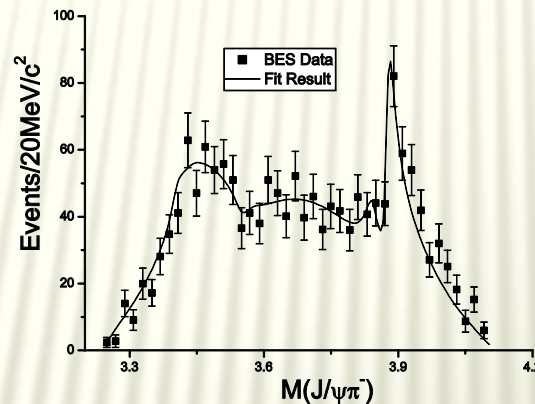
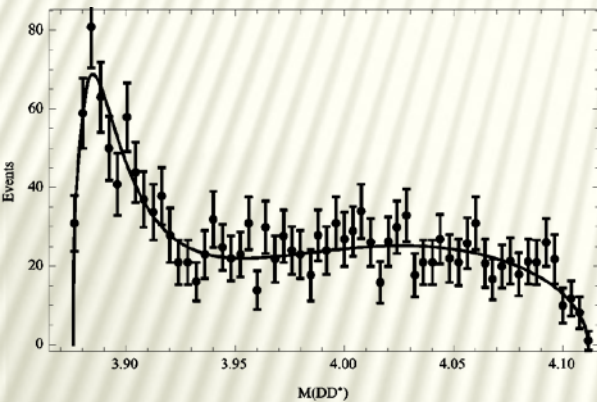


*Typical behavior of  $\text{Re}\Pi$ ,  $\text{Im}\Pi$ , and  $|\Pi|$*

# NUMERICAL RESULTS OF A COMBINED FIT

*We consider a four-channel case. The channels  $J/\psi\pi$ ,  $DD^*$ ,  $D^*D^*$ , and  $X(4260)\pi$  are referred to channel “1”, “2”, “3”, and “4”. The channel  $X(4260)\pi$  is always virtual, but it provides a background contribution.*

*A perfect fit to the experimental data for charged  $DD^*$ ,  $D^*D^*$ , and  $J/\psi\pi$  mass-distribution data at the same time in  $e^+e^-$  collision at about  $s^{1/2}=4.26\text{GeV}$ .*



$$\frac{\chi^2}{d.o.f} = 1.03$$

# NUMERICAL RESULTS

Two nearby poles are found  $s^{II} = (3.846 \pm 0.019i)^2 \text{ GeV}^2$ ,

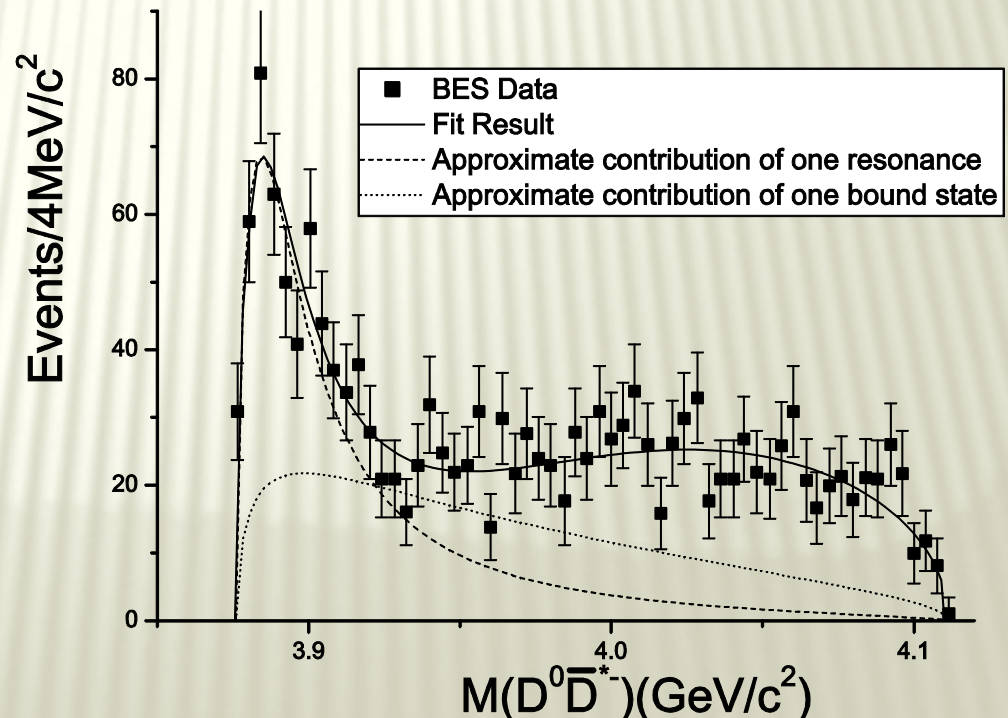
$$s^{III} = (3.875 \pm 0.016i)^2 \text{ GeV}^2.$$

No nearby pole is found near the  $D^*D^*$  threshold.

There is no method to precisely isolate the contribution of a pole in multichannel scattering .

We propose that the third-sheet pole might contribute dominantly. If we omit the  $J/\psi\pi$  threshold, the number of Riemann sheet become 8. A third-sheet pole will become a second-sheet pole. We might use a second-sheet pole of the PKU factorization form (Zheng et al., NPA 733, 235(2004)) to mimick the contribution of

$$s^{III} = (3.875 \pm 0.016i)^2 \text{ GeV}^2.$$





# SUMMARY I

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- *The model could perfectly reproduce the mass distribution data of different final states of  $X(4260)$  at the same time.*
- *The best numerical result of a combined analysis prefers the  $Z_c(3900)$  signal is formed by the combined effect of two poles and the  $DD^*$  threshold. Although the two poles are “shadow” poles, the third-sheet one at  $s^{III} = (3.875 \pm 0.016i)^2 \text{ GeV}^2$  contributes dominantly. But no pole related to the  $Z_c(4025)$  in  $D^*D^*$  mass distribution.*
- *This scheme satisfies the coupled –channel unitarity and the higher-order contributions are included. Its analytic structure is easily analyzed. The scheme is simply operated. It may be generalized and used in experiment analyses.*
- *Combined analyses are suggested, which will provide more informations.*



# TOPIC II: REIDENTIFYING THE QUANTUM NUMBER OF X(3915)

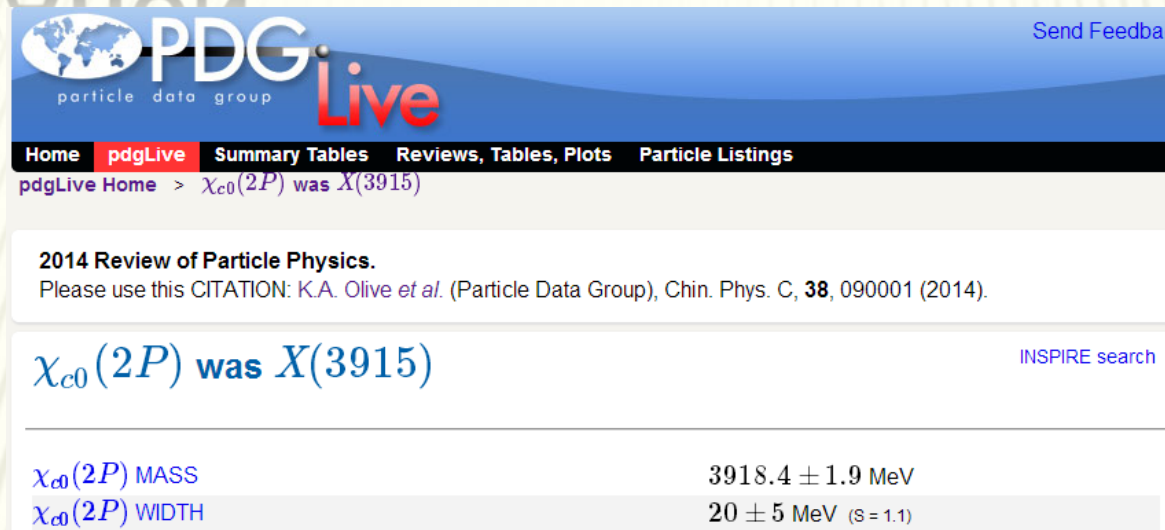
----Is X(3915) really a scalar state?

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In collaboration with Zhiguang Xiao(肖志广) USTC  
and Hai-Qing Zhou (周海清) SEU

arXiv:1501.00879

# MOTIVATION



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pdgLive Home >  $\chi_{c0}(2P)$  was  $X(3915)$

**2014 Review of Particle Physics.**  
Please use this CITATION: K.A. Olive *et al.* (Particle Data Group), Chin. Phys. C, **38**, 090001 (2014).

$\chi_{c0}(2P)$  was  $X(3915)$  [INSPIRE search](#)

$\chi_{c0}(2P)$ MASS	$3918.4 \pm 1.9$ MeV
$\chi_{c0}(2P)$ WIDTH	$20 \pm 5$ MeV ( $s = 1.1$ )

- *The famous Godfrey-Isgur model (PRD 32,189(1985)) predict the mass of  $\chi_{c0}(2P)$  to be about 3915MeV, but the predicted mass values of this model are usually higher than the observed values for the states above the open-flavor threshold.*
- *Guo and Meissner doubted that this state is far beyond the expectations to  $\chi_{c0}(2P)$ . PRD 86,091501.*
- *Olsen argued that this assignment implies a conflictions between the branch fraction of  $\chi_{c0}(2P) \rightarrow J / \psi \omega$  from different experiment processes. PRD 91, 057501.*
- *We wish to solve this puzzle in a different aspect.*

# EXAMINING THE EXPERIMENTS

- *Belle reported this state in  $\gamma\gamma \rightarrow J/\psi\omega$  first, and they claimed that both the  $J^{PC} = 0^{++}$  and  $2^{++}$  are both possible.*

**PRL 104,092001**

- *BaBar confirmed this observation, and made an angular distribution analysis of final leptonic and pionic states. They claim the angular distribution data highly prefer the  $J^{PC} = 0^{++}$  assignment based on the helicity-2-dominance assumption. It is the only experiment to identify its quantum numbers.*

**PRD 86,072002**

- *The PDG table quotes the  $X(3915)$  as  $\chi_{c0}(2P)$ .*



# QUESTIONS

- Helicity-2 dominance is a result of the quark model, (Krammer and Krasemann, PLB 73, 58(1978). Li et al., PRD 43,2161(1991).) but above the open-flavor thresholds, the predictions of quark model is not consistent with the observed values, which means that it is hard to regard them to be pure  $q\bar{q}$  states. The states above the open-flavor thresholds could be described well by the coupled-channel models.*

*Eichten et al., PRD 17, 3090(1978). PRD 21, 203(1980).  
Heikkila et al., PRD 29,110(1984) Van Beveren et al., Z.Phys.C19,275(1983)  
Pennington and Wilson, PRD 76,077502(2007) Zhou, Xiao, EPJA 50,165(2014)*
- The only experiment to verify the helicity-2 dominance assumption for the states above the open-flavor threshold is the measurements of  $X(3930)$  in  $\gamma\gamma \rightarrow D\bar{D}$  processes by Belle and BaBar. It is like a **circular reasoning**.*
- Check whether the experiment analysis is over-restricted.*
- Whether the helicity-2 amplitude is dominant or not should be determined by data.*



# THE THEORETICAL FRAME

$$\frac{d\sigma}{d\Omega} = \frac{1}{64\pi^2\rho(s)s} (|\mathcal{M}_{++}|^2 + |\mathcal{M}_{+-}|^2), \quad (1)$$

where  $\rho(s) = \sqrt{(s - 4m_D^2)}/s$ . The partial wave expansions of  $\mathcal{M}_{+\pm}$  are [16]

$$\begin{aligned} \mathcal{M}_{++}(s, \cos\theta) &= 16\pi \sum_{J \geq 0} (2J + 1) F_{J0}(s) d_{0,0}^J(\cos\theta), \\ \mathcal{M}_{+-}(s, \cos\theta) &= 16\pi \sum_{J \geq 2} (2J + 1) F_{J2}(s) d_{2,0}^J(\cos\theta), \end{aligned} \quad (2)$$

Thus, the helicity amplitudes of  $\gamma\gamma \rightarrow D\bar{D}$  are represented phenomenologically as

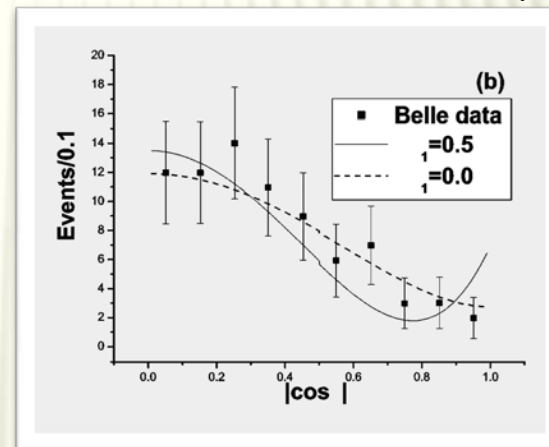
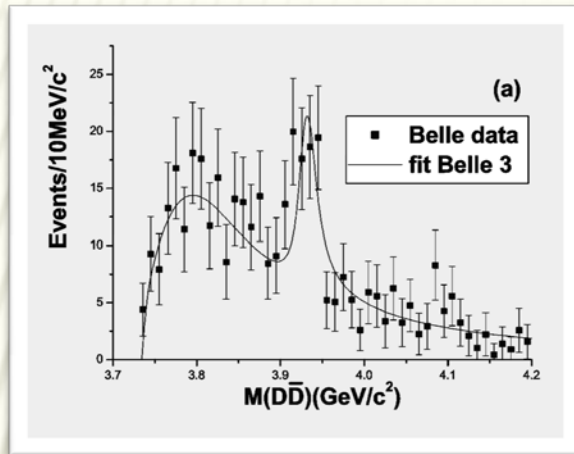
$$\begin{aligned} \mathcal{M}_{++} &= 16\pi(\mathcal{A}_0(s) + \beta_1 e^{i\phi_1} \mathcal{A}_2(s) \times 5 \times d_{0,0}^2(\cos\theta)), \\ \mathcal{M}_{+-} &= 16\pi(\beta_2 e^{i\phi_2} \mathcal{B}_2(s) \times 5 \times d_{2,0}^2(\cos\theta)), \end{aligned} \quad (4)$$

where  $\mathcal{A}_0(s) = \frac{M_{\chi_{c0'}} \Gamma_{\chi_{c0'}}(s)}{M_{\chi_{c0'}}^2 - s - iM_{\chi_{c0'}} \Gamma_{\chi_{c0'}}(s)}$ ,  $\mathcal{A}_2(s) = \mathcal{B}_2(s) = \frac{M_{\chi_{c2'}} \Gamma_{\chi_{c2'}}(s)}{M_{\chi_{c2'}}^2 - s - iM_{\chi_{c2'}} \Gamma_{\chi_{c2'}}(s)}$ . One could use these amplitudes

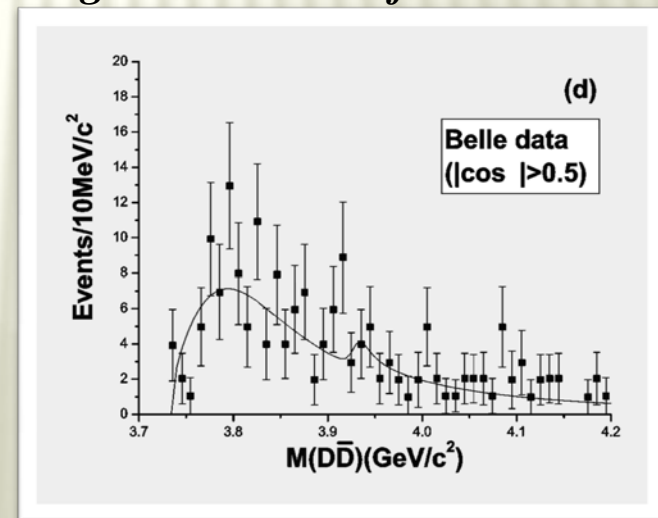
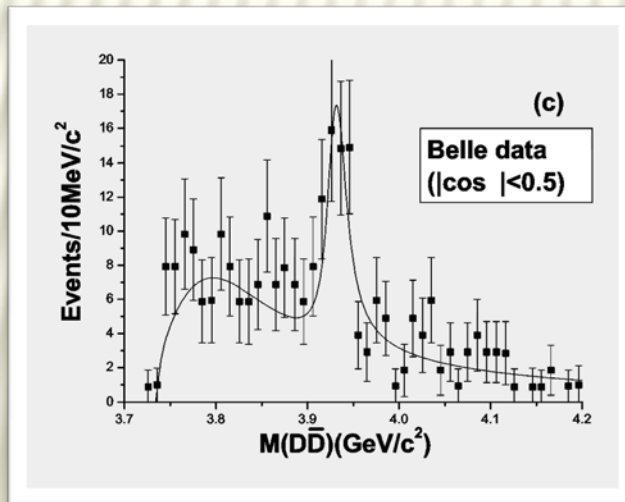
# CHECK THE NECESSITY OF ASSUMPTION OF HELICITY-2 DOMINANCE

*With an appropriate parametrization method*

## Belle data of $\gamma\gamma \rightarrow D\bar{D}$

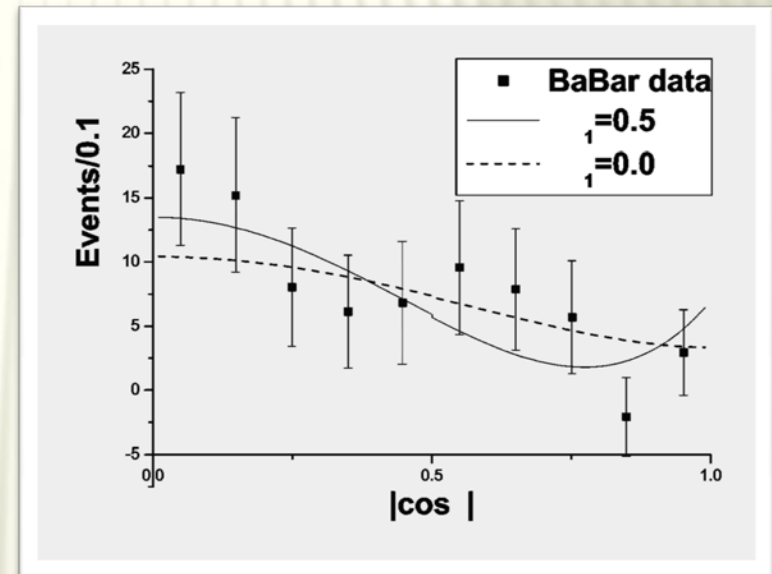
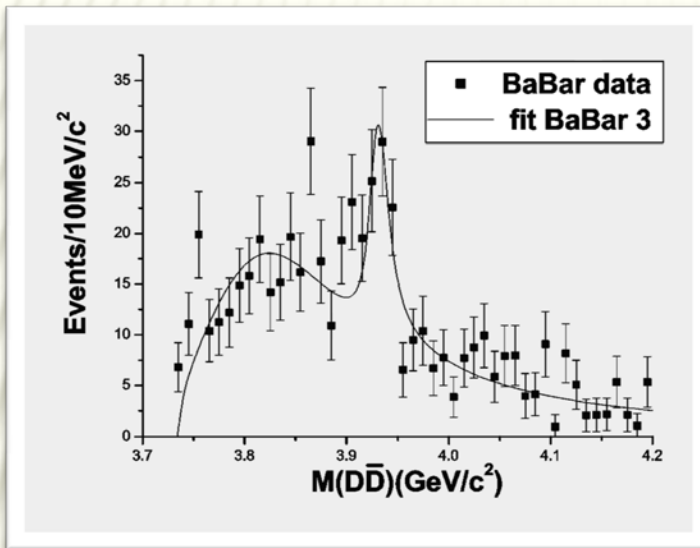


*Reproduce the mass distribution in different  $\cos\theta$  region. It is not a fit!*



# CHECK THE NECESSITY OF ASSUMPTION OF HELICITY-2 DOMINANCE

BaBar data of  $\gamma\gamma \rightarrow D\bar{D}$



# FIT PARAMETERS

Parameters	“fit Belle 1”	“fit Belle 2”	“fit Belle 3”	“fit BaBar 1”	“fit BaBar 2”	“fit BaBar 3”
$\chi^2/d.o.f$	44.8/(47+10-9)	45.2/(47+10-7)	55.5/(47+10-8)	71.9/(47+10-9)	73.7/(47+10-7)	73.1/(47+10-8)
$M_{\chi_{c0'}}$ (GeV)	$3.817 \pm 0.009$	$3.814 \pm 0.006$	$3.820 \pm 0.009$	$3.853 \pm 0.009$	$3.851 \pm 0.009$	$3.853 \pm 0.009$
$\Gamma_{\chi_{c0'}}$ (GeV)	$0.163 \pm 0.033$	$0.155 \pm 0.020$	$0.201 \pm 0.019$	$0.229 \pm 0.031$	$0.227 \pm 0.032$	$0.233 \pm 0.030$
$M_{\chi_{c2'}}$ (GeV)	$3.925 \pm 0.003$	$3.925 \pm 0.005$	$3.924 \pm 0.009$	$3.932 \pm 0.001$	$3.932 \pm 0.001$	$3.932 \pm 0.001$
$\Gamma_{\chi_{c2'}}$ (GeV)	$0.035 \pm 0.005$	$0.036 \pm 0.005$	$0.031 \pm 0.005$	$0.021 \pm 0.004$	$0.021 \pm 0.005$	$0.020 \pm 0.004$
$\beta_1$	$0.147 \pm 0.201$	0	0.5	$0.290 \pm 0.237$	0	0.5
$\phi_1$ (Rad)	$2.850 \pm 0.513$		$3.653 \pm 0.389$	$3.713 \pm 1.326$		$3.700 \pm 0.597$
$\beta_2$	$0.559 \pm 0.077$	$0.586 \pm 0.051$	$0.388 \pm 0.086$	$0.514 \pm 0.151$	$0.599 \pm 0.056$	$0.330 \pm 0.101$

***Large errorbars imply that this experiment do not verify the helicity-2 dominance. Belle and BaBar’s analyses might be over-restricted by using this assumption.***

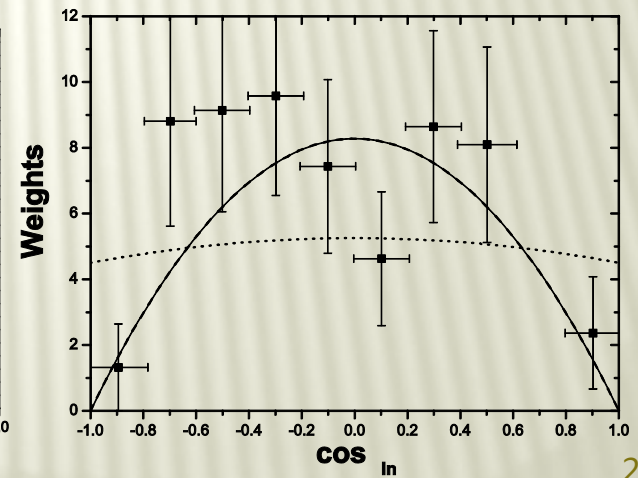
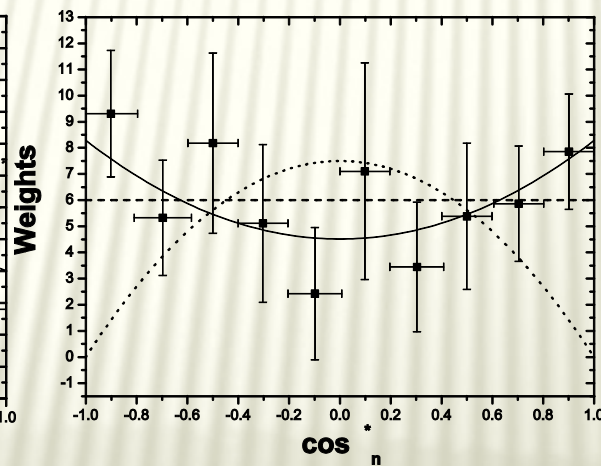
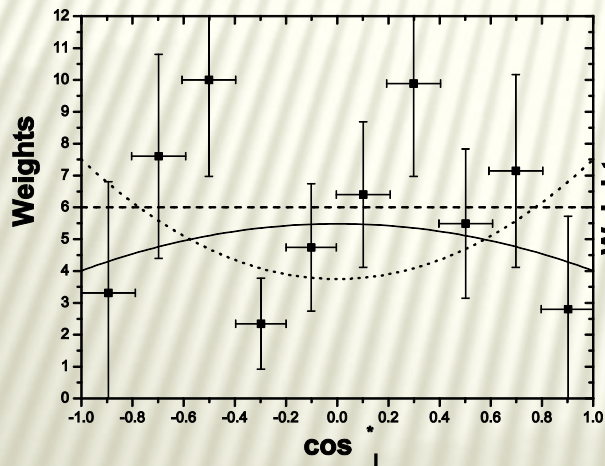
***To check this assumption again, by fixing the  $\beta_1$  value, one obtains fit results with similar qualities. This means the helicity-2 dominance assumption is not necessary in determining the X(3930), and the related experiment can not be regarded as the evidence of this assumption.***



# ANGULAR DISTRIBUTIONS

*Coupled-channel unitarity could give a constraint to the helicity ratios of different channels at the pole position.*

*The angular distribution of the final leptons, pions, and the angle between leptons and pions of  $X(3915)$  signal. A combined fit of  $\gamma\gamma \rightarrow D\bar{D}, J/\psi\pi$  data favors  $\beta_1 / \beta_2 = 0.48 / 0.30$ , which means a sizable helicity-0 contribution. The fit also provide a better description to the angular-distribution data.*



**Preliminary result**

# SUMMARY II

- *We pointed out that, by abandoning the helicity-2 assumption, the experimental data prefer the  $X(3915)$  to be a  $J^{PC}=2^{++}$  state than a  $J^{PC}=0^{++}$  state. Its mass and width is coinciding with the  $X(3930)$  state.  $X(3915)$  and  $X(3930)$  are the same tensor state.*
- *It may suggest a sizable non- $q\bar{q}$  components of the  $X(3930)$  state, as other states above the open-flavor thresholds.*
- *Further experimental measurements are suggested.*
- *Several theoretical efforts on coupled-channel models predict  $\chi_{c0}(2P)$  at about  $3850\text{GeV}$*

**Pennington and Wilson, PRD 6,077502(2007)**

**Danilkin and Simonov, PRL 105,102002(2010)**

**Zhou, Xiao, EPJA 50,165(2014)**

**THANKS FOR YOUR PATIENCE!**