

An Updated Analysis on Lepton Flavor Violating Radiative Decays in Non-sterile Electroweak-scale Right-handed Neutrino Model

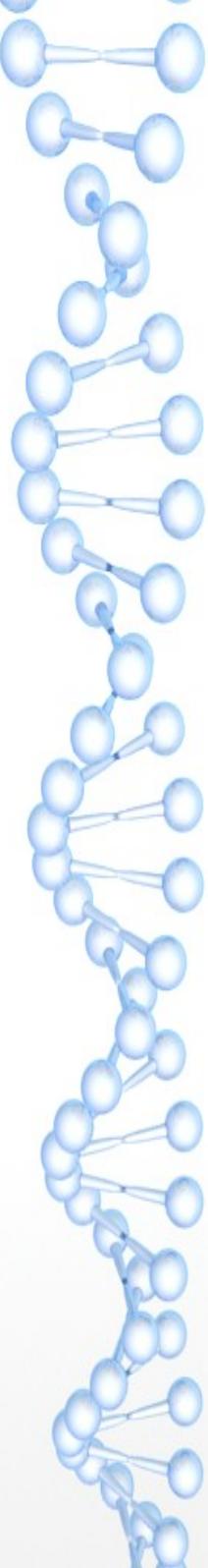
Van Que Tran

In collaboration with P.Q Hung (UVA), Trinh Le (UVA), T.C Yuan (AS)

Summer Institute 2015, Beijing, China

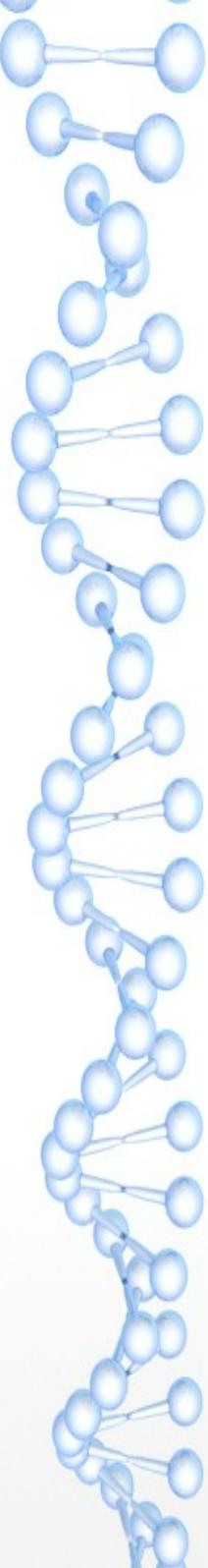
1-7 August 2015





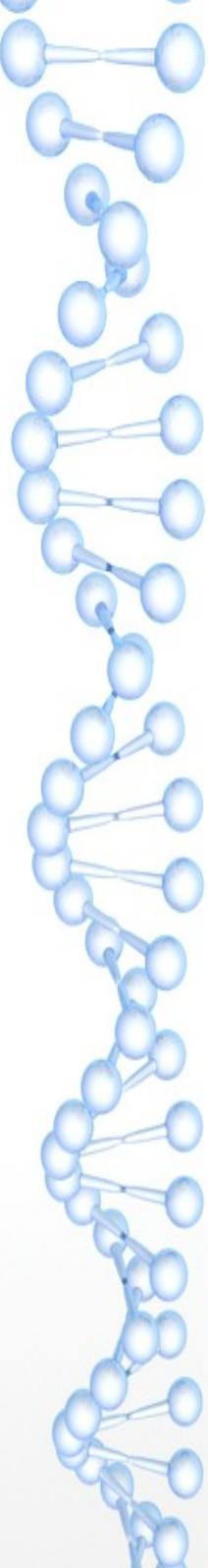
Outline

- 1. Motivation
- 2. The Model
- 3. The calculation
 - Process $l_i \rightarrow l_j + \gamma$
 - Magnetic Dipole Moment and Electric Dipole Moment
- 4. Analysis and discussion
- 5. Summary



Motivation

- The Standard Model can explain most of the experimental results. However, there are many undetermined parameters and issues → BSM



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	$<2.2 \text{ eV}$ 0 $\frac{1}{2}$ ν_e electron neutrino	$<0.17 \text{ MeV}$ 0 $\frac{1}{2}$ ν_μ muon neutrino	$<15.5 \text{ MeV}$ 0 $\frac{1}{2}$ ν_τ tau neutrino
Leptons	0.511 MeV -1 $\frac{1}{2}$ e electron	105.7 MeV -1 $\frac{1}{2}$ μ muon	1.777 GeV -1 $\frac{1}{2}$ τ tau

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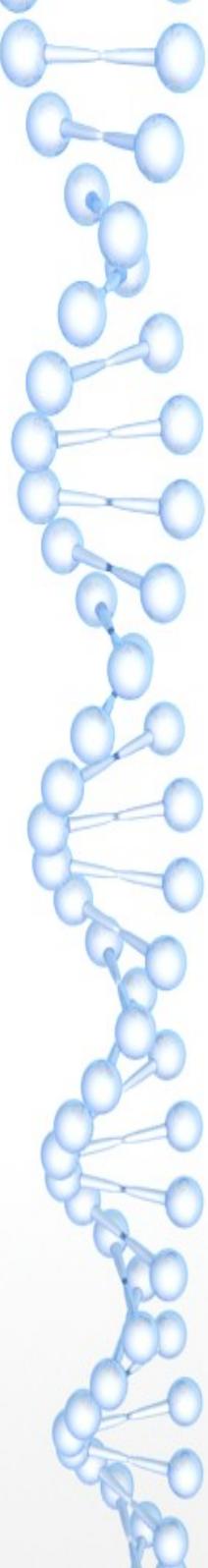
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→ Why not have **charged lepton flavour violation (cLFV)** ?

- If observed:
 - Probe the origin of lepton mixing
 - Probe the origin of new physics

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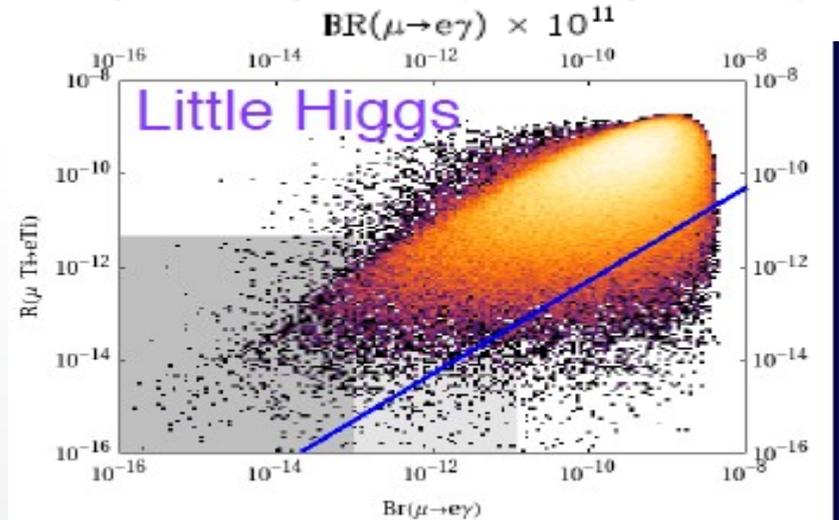
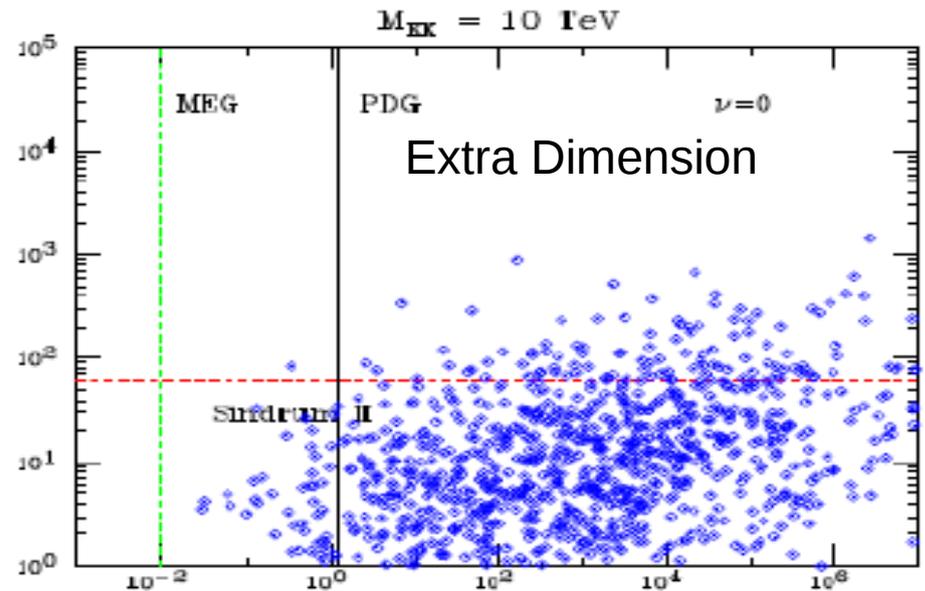
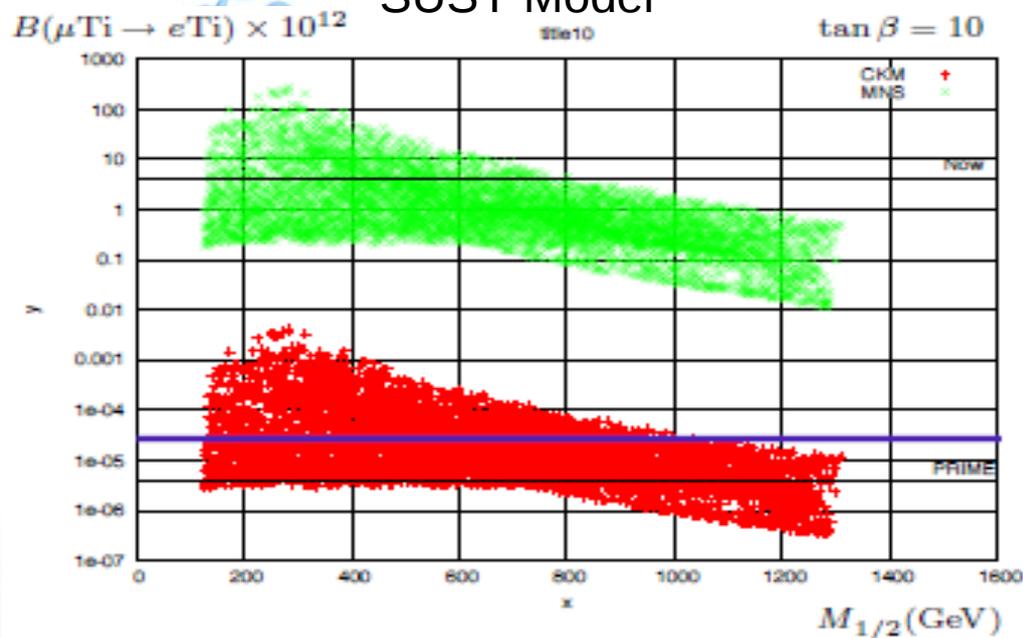
Motivation

Indeed, many well-motivated new physics scenarios predict large flavour violations in the charged lepton sector:

Motivation

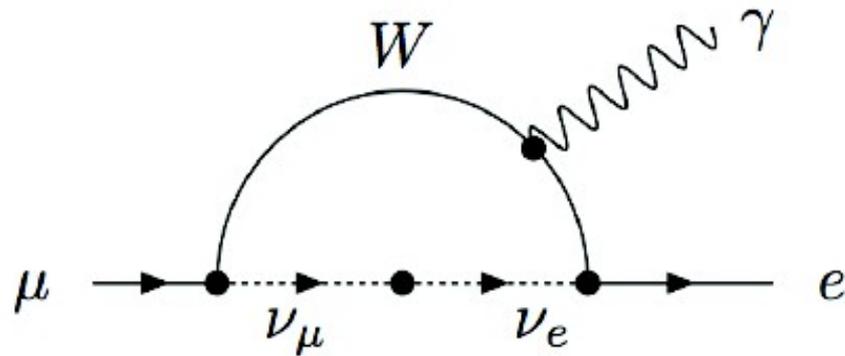
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SUSY Model



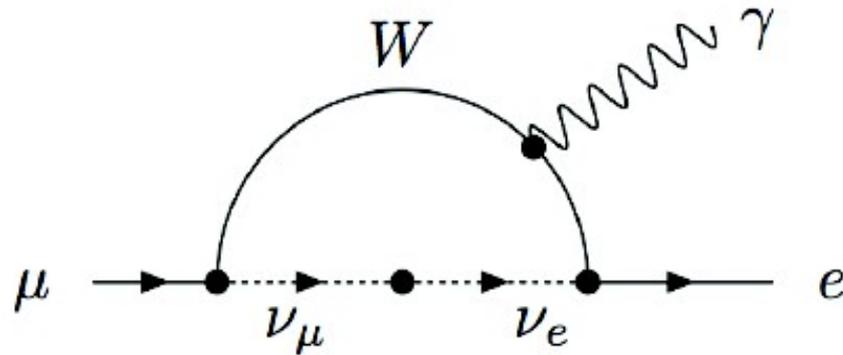
Motivation

Neutrino-mediated LFV is un-observably small



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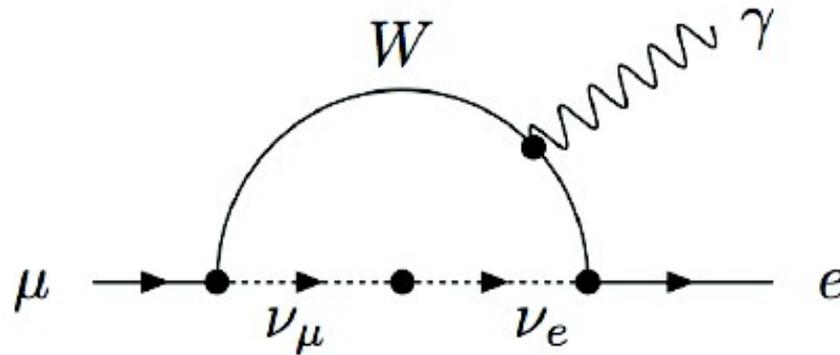
Neutrino-mediated LFV is un-observably small



$$B(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left| \sum_l (V_{MNS})_{\mu l}^* (V_{MNS})_{el} \frac{m_{\nu l}^2}{M_W^2} \right|^2 \sim O(10^{-54})$$

Motivation

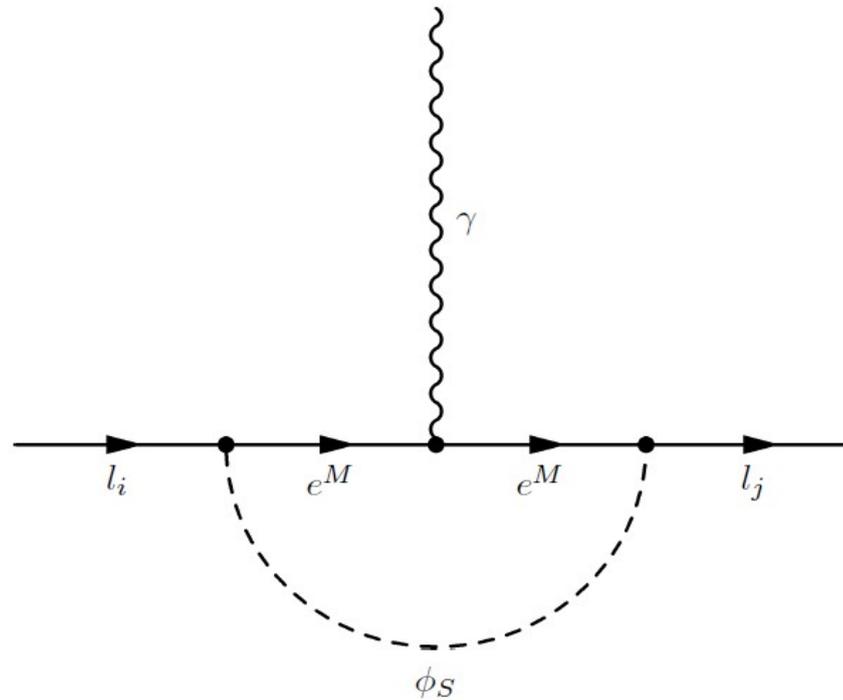
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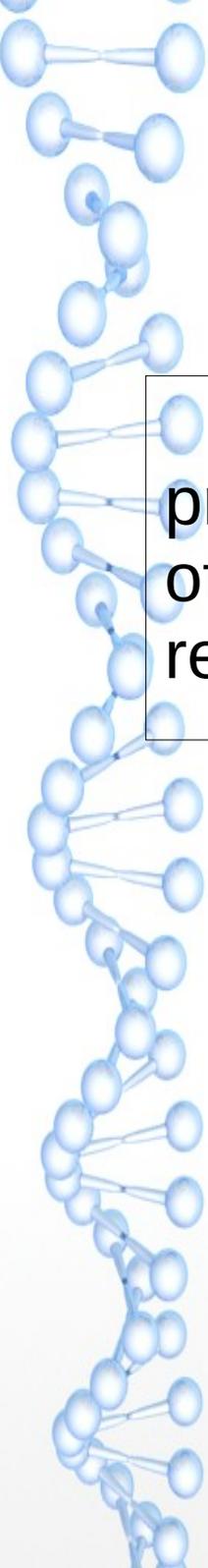
Could there be other mechanisms for LFV?

Motivation



Dominant diagram for $l_i \rightarrow l_j + \gamma$

Such processes have been discussed in a generic fashion in **EW vR Model** (*arXiv:0711.0733 [hep-ph]*, *P. L. B.* 659, 585 (2008))



Motivation

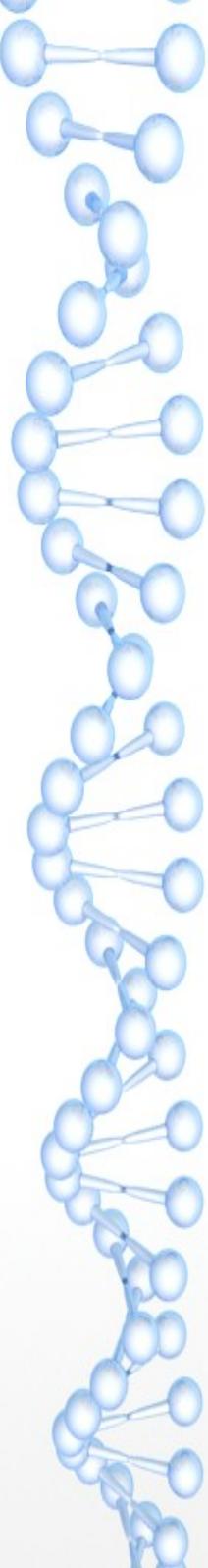
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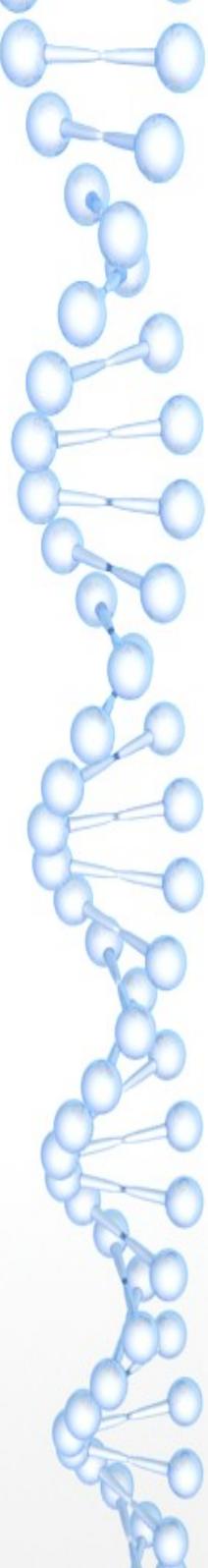


Let's Go!



The Model

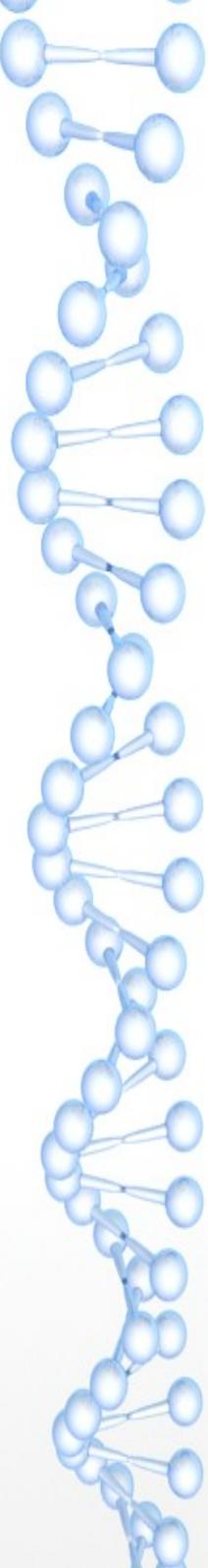
**Non-sterile Electroweak-scale Right-handed
Neutrino Model (The EW ν_R Model) [P.Q
*Hung 2007]***



The Model

The EW vR Model [PQ Hung 2007]

What is it?



The Model

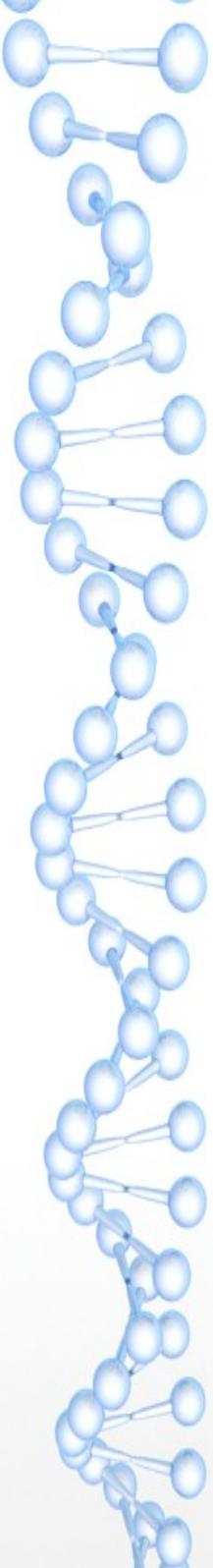
The EW ν R Model [PQ Hung 2007]

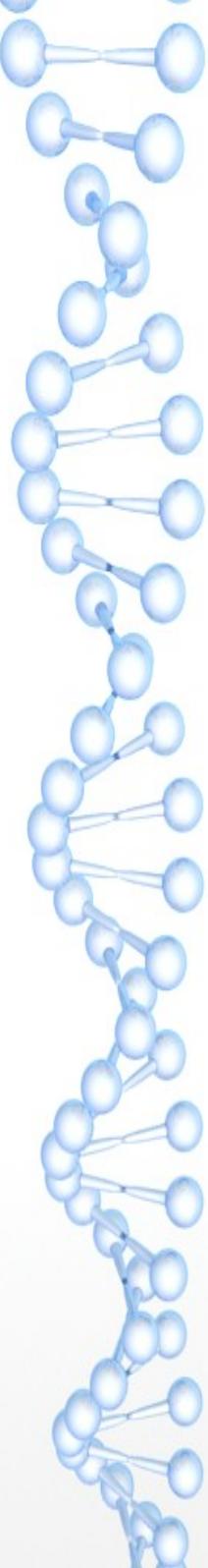
What is it?

Model in which right-handed neutrinos have Majorana masses of the order of Λ_{EW} **naturally.**

The EW vR Model

Gauge group

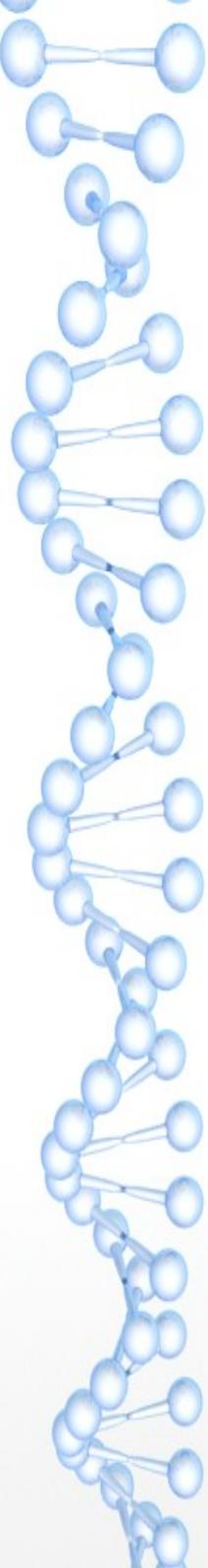




The EW vR Model

Gauge group

$$SU(3)_C \times SU(2) \times U(1)_Y$$

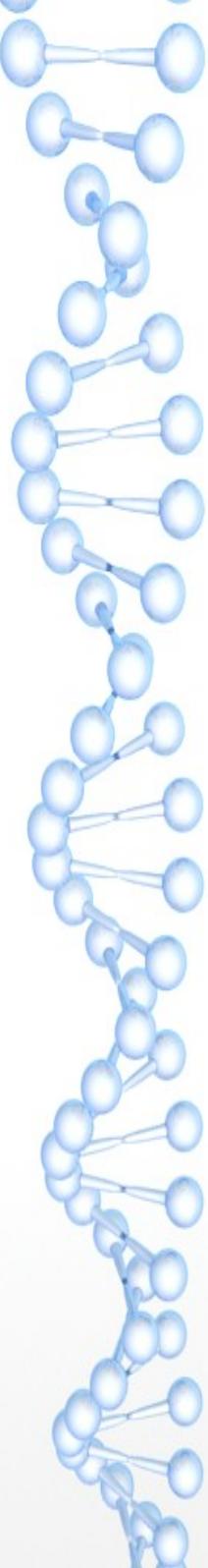


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Model Content



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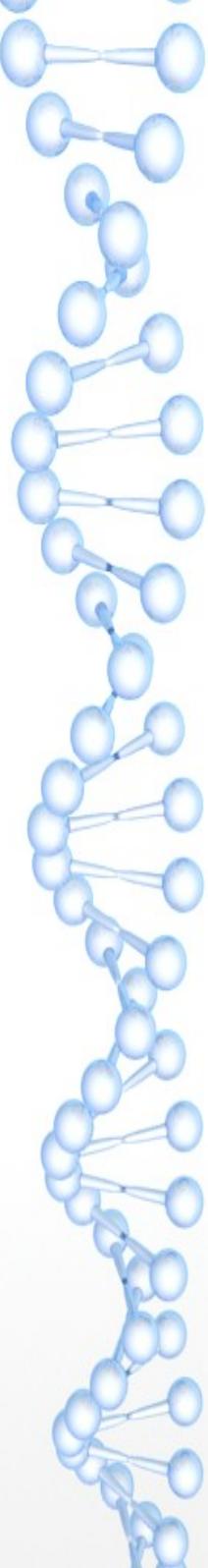
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Model Content

Leptons

$$l_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$$

e_R



The EW ν_R Model

Gauge group

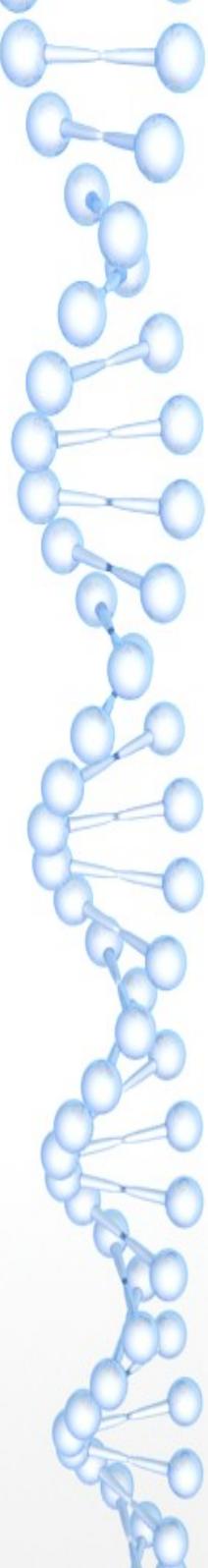
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Model Content

Leptons

$$l_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \longleftrightarrow l_R^M = \begin{pmatrix} \nu_R \\ e_R^M \end{pmatrix},$$

$$e_R \longleftrightarrow e_L^M$$



The EW vR Model

Quarks

$$q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix}$$

u_R, d_R

The EW vR Model

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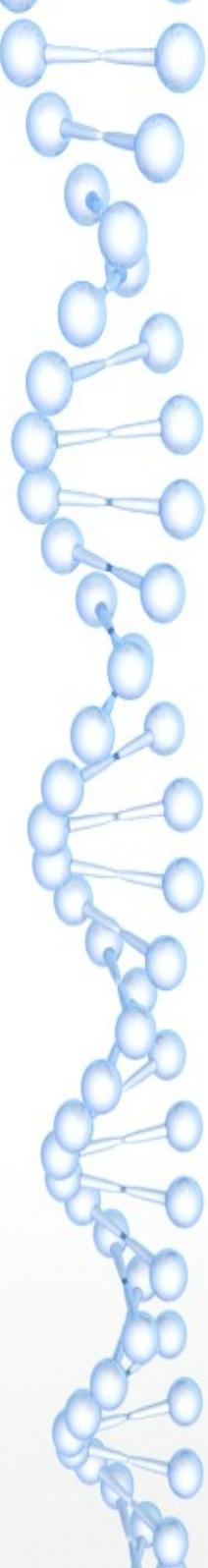
The EW νR Model

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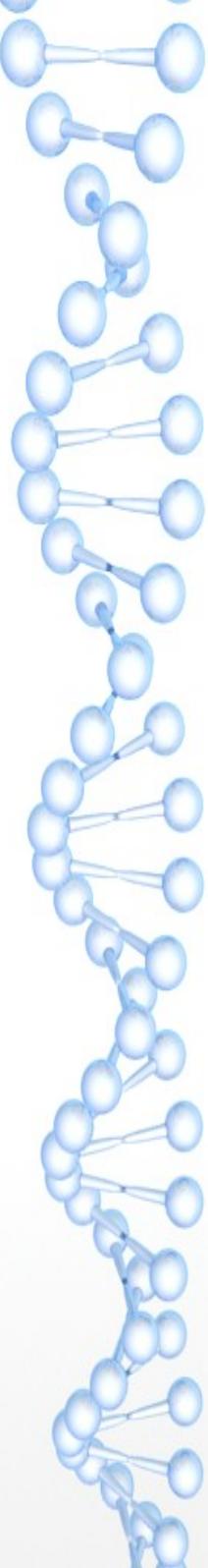
$$u_R, d_R \longleftrightarrow u_L^M, d_L^M$$

Mirror particles are totally different from the SM particles!



The EW ν R Model

Higgs Sector:



The EW ν R Model

Higgs Sector:

- **Doublet** → give masses to all charged fermions

The EW vR Model

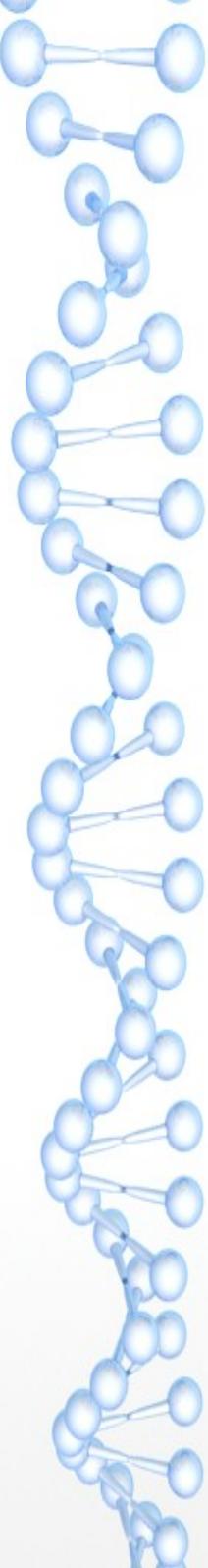
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$$L_{Y_l} = g_l \bar{l}_L \phi e_R + h.c.$$

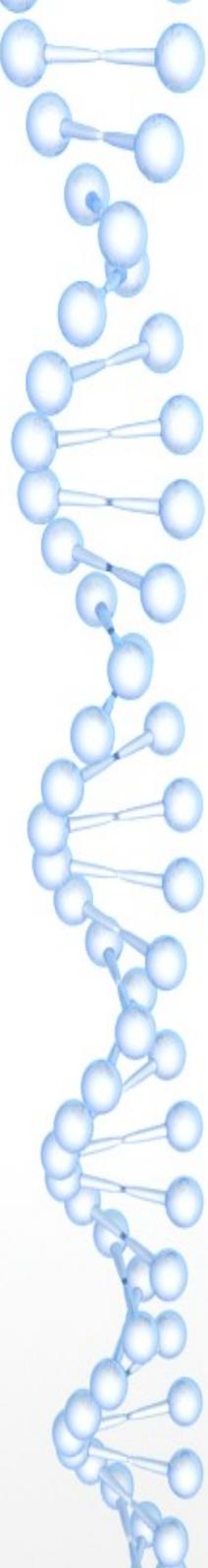
$$L_{Y_q} = g_q \bar{q}_L \phi u_R + h.c.$$

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}, \quad \langle \phi^0 \rangle = \frac{v_2}{\sqrt{2}}$$



The EW ν R Model

Higgs Sector: **Triplets**



The EW ν R Model

Higgs Sector: **Triples**

- $Y/2 = 1$ triplet \rightarrow gives an electroweak-scale Majorana mass to the right-handed neutrino

The EW vR Model

Higgs Sector: Triplets

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$$\tilde{\chi} = (3, Y/2 = 1)$$

$$\tilde{\chi} = \frac{1}{\sqrt{2}} \vec{\tau} \cdot \vec{\chi} = \begin{pmatrix} \frac{1}{\sqrt{2}} \chi^+ & \chi^{++} \\ \chi^0 & -\frac{1}{\sqrt{2}} \chi^+ \end{pmatrix}$$

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$$\begin{aligned} L_M &= g_M \left(l_R^{M,T} \sigma_2 \right) (i \tau_2 \tilde{\chi}) l_R^M \\ &= g_M \nu_R^T \sigma_2 \nu_R \chi^0 - \frac{1}{\sqrt{2}} \nu_R^T \sigma_2 e_R^M \chi^+ + \dots \end{aligned}$$

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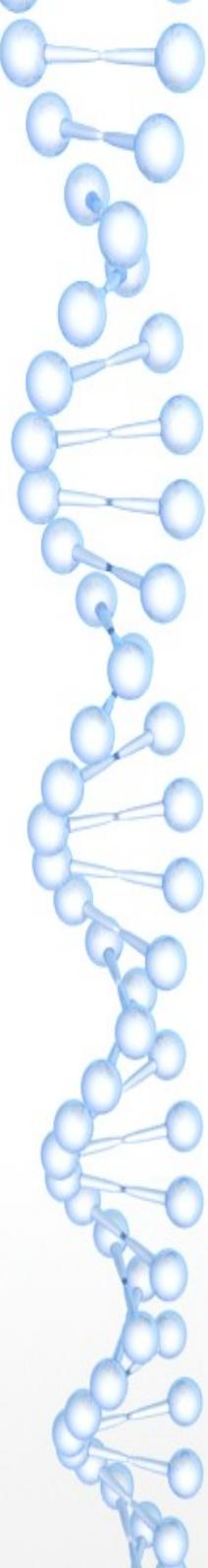
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If $\langle \chi^0 \rangle = v_M \sim \Lambda_{EW} \rightarrow$ Majorana mass $M_R = g_M v_M$

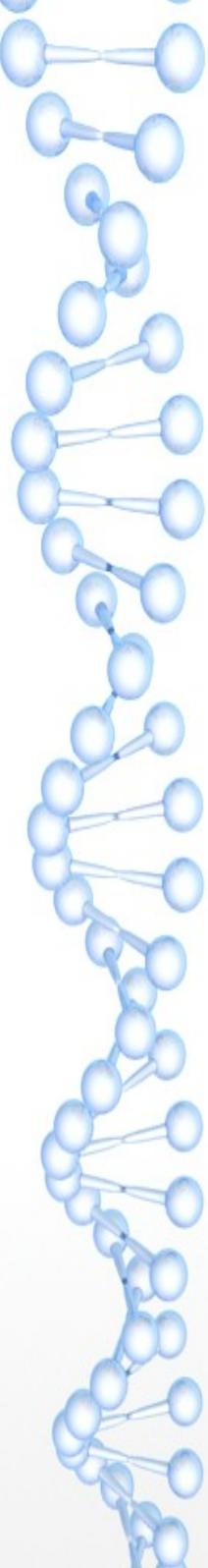


The EW ν R Model

Higgs Sector: **Triples**

- $Y/2 = 0$ triplet

$$\xi (Y/2 = 0) = (\xi^+, \xi^0, \xi^-)$$



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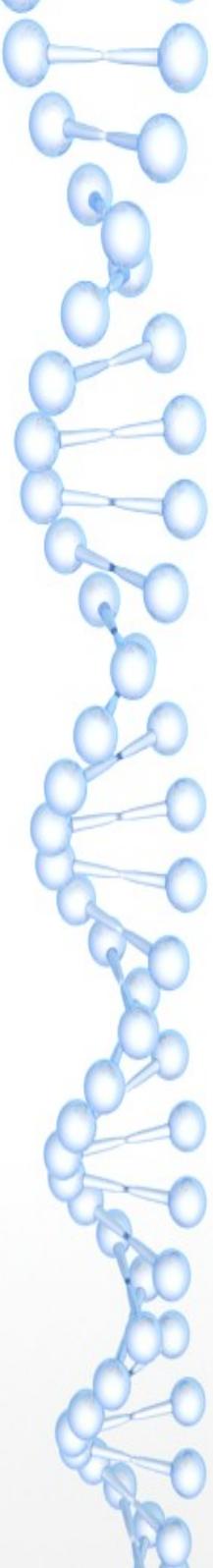
- In order to restore the Custodial Symmetry ($\rho = 1$) (*Chanowitz, Golden and Georgi, Machacek*)

$$\langle \chi^0 \rangle = \langle \xi^0 \rangle = v_M$$

The EW vR Model

Higgs Sector: One Singlet (in original Model)

$$\phi_S (1, Y/2 = 0)$$



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$$= g_{Sl} (\bar{\nu}_L \nu_R + \bar{e}_L e_R^M) \phi_S + h.c..$$

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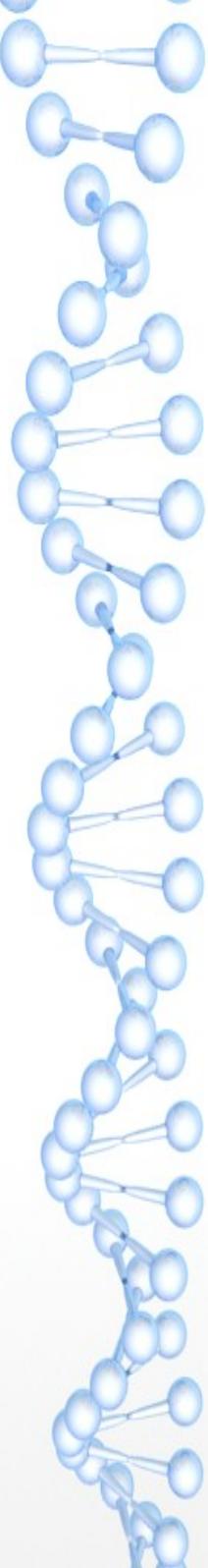
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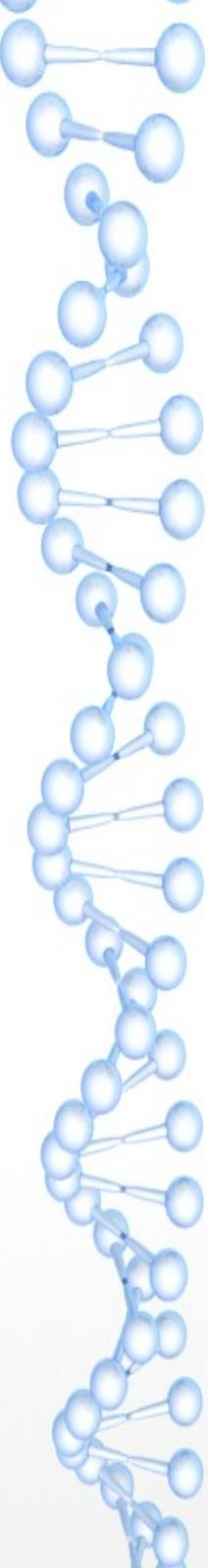
$$= g_{SI} (\bar{\nu}_L \nu_R + \bar{e}_L e_R^M) \phi_S + h.c..$$

With $\langle \phi_S \rangle = v_S$, \rightarrow gives the Dirac mass $m^D = g_{SI} v_S$



The EW ν R Model

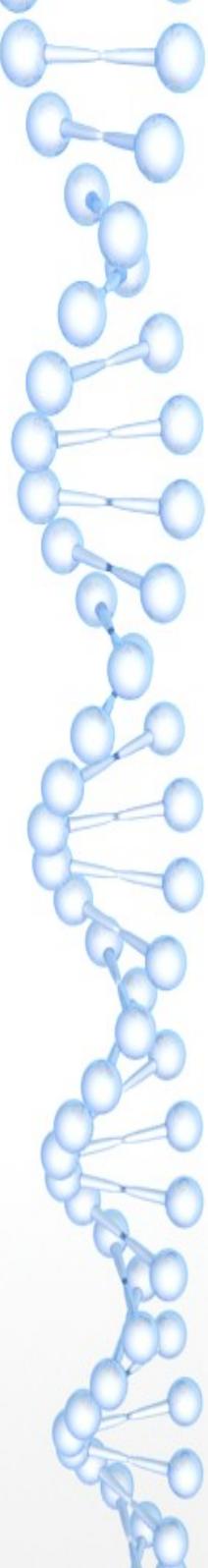
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The EW vR Model

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By using the **A4 symmetry** we obtain **four Higgs Singlet**: an A4 singlet Φ_{oS} and A4-triplets $\{\Phi_{iS}\}$ ($i = 1, 2, 3$). With the VEVs v_0 and v_i respectively



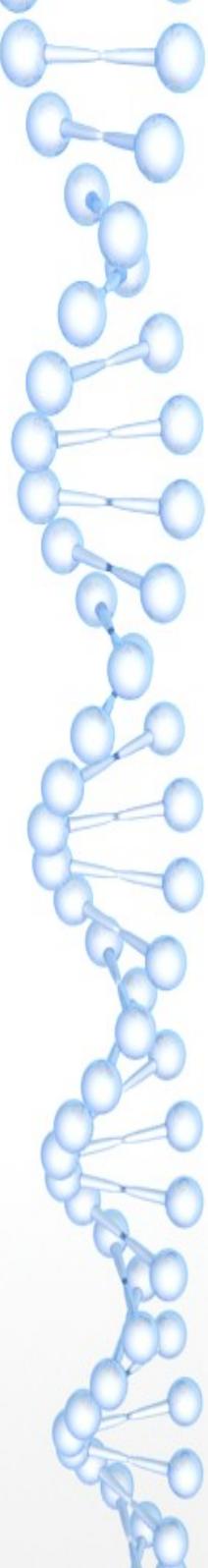
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The Yukawa interactions

$$L_S = \bar{l}_L^0 (g_{0S}\phi_{0S} + g_{1S}\tilde{\phi}_S + g_{2S}\tilde{\phi}_S) l_R^{M,0} + H.c. ,$$



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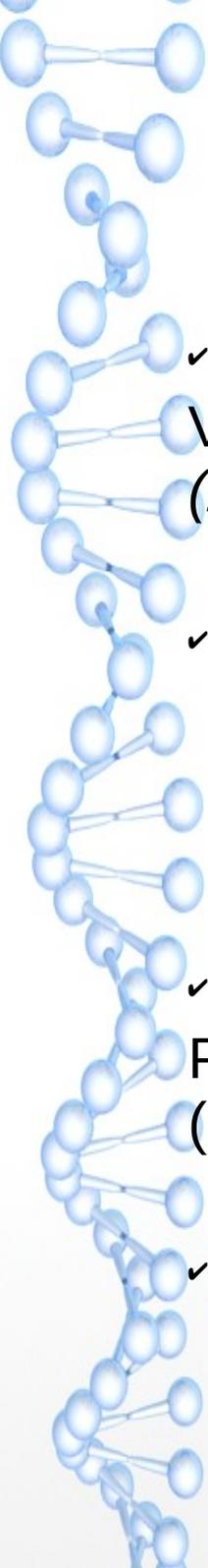
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Obtain the neutrino mass matrix

$$M_\nu^D = \begin{pmatrix} g_{0S}v_0 & g_{1S}v_3 & g_{2S}v_2 \\ g_{2S}v_3 & g_{0S}v_0 & g_{1S}v_1 \\ g_{1S}v_2 & g_{2S}v_1 & g_{0S}v_0 \end{pmatrix}$$



The EW vR Model

Some works done on this Model:

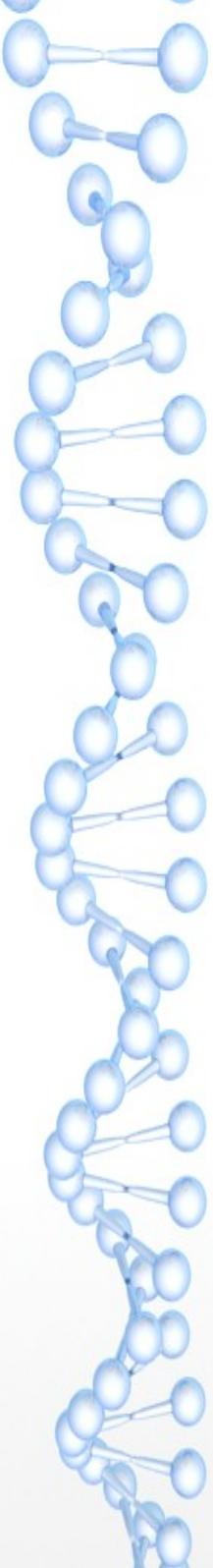
- ✓ **EW precision**

V. Hoang, P. Q. Hung and A. S. Kamat, *Nucl. Phys. B* 877, 190 (2013) [*arXiv:1303.0428 [hep-ph]*].

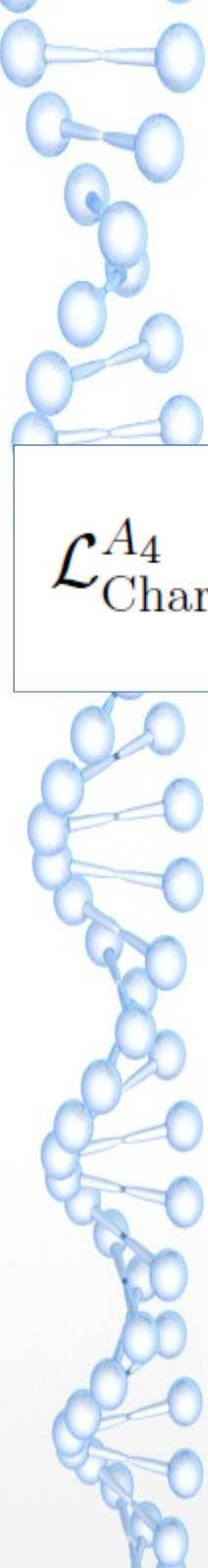
- ✓ **Implications of the 125-GeV SM-like scalar:** Dr Jekyll (SM-like) and Mr Hyde (very different from SM) V. Hoang, P. Q. Hung and A. S. Kamat, *arXiv:1412.0343 [hep-ph]* (To appear in *Nuclear Physics B*).

- ✓ **Signals of mirror fermions** (Paper in preparation)
P.Q. Hung, Trinh Le (UVA); Nandi, Chakdar, Gosh (Oklahoma State University).

- ✓ **On neutrino and charged lepton masses and mixings: A view from the electroweak-scale right-handed neutrino model** P. Q. Hung and T. Le, *arXiv:1501.02538 [hep-ph]*.

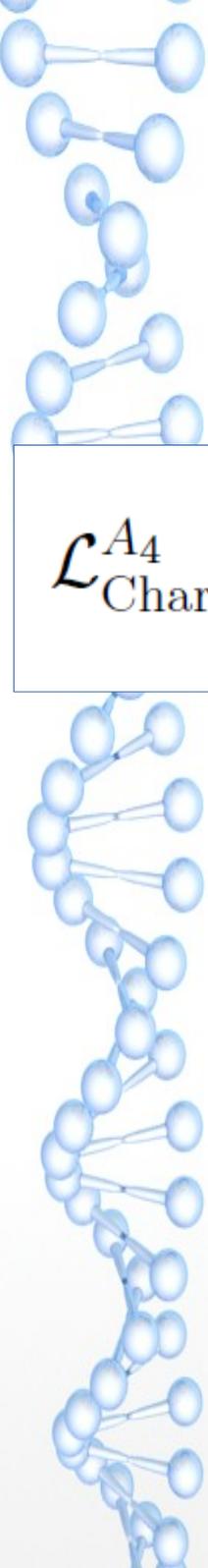


The calculation


$$l_i \rightarrow l_j + \gamma$$

The Yukawa interaction can be cast into the following form:

$$\mathcal{L}_{\text{Charged},S}^{A_4} = - \sum_{k=0}^3 \sum_{i,m=1}^3 \left(\overline{l_{Li}} \mathcal{U}_{im}^{Lk} l_{Rm}^M + \overline{l_{Ri}} \mathcal{U}_{im}^{Rk} l_{Lm}^M \right) \phi_{Sk} + \text{H.c.}$$


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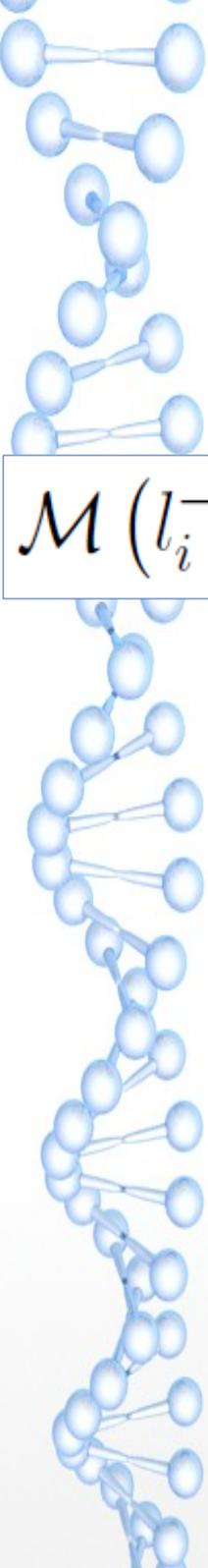
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Where

$$\mathcal{U}_{im}^{Lk} = \left(U_{\text{PMNS}}^\dagger \cdot M^k \cdot U_{\text{PMNS}}^{lM} \right)_{im}$$

$$\mathcal{U}_{im}^{Rk} = \left(U'_{\text{PMNS}}{}^\dagger \cdot M'^k \cdot U'_{\text{PMNS}}{}^{lM} \right)_{im}$$


$$l_i \rightarrow l_j + \gamma$$

The Lorentz-invariant amplitude for the process $l_i(p) \rightarrow l_j(p') + \gamma(q)$ is

$$\mathcal{M}(l_i^- \rightarrow l_j^- \gamma) = \epsilon_\mu^*(q) \bar{u}_j(p') \left\{ i\sigma^{\mu\nu} q_\nu [C_L^{ij} P_L + C_R^{ij} P_R] \right\} u_i(p)$$

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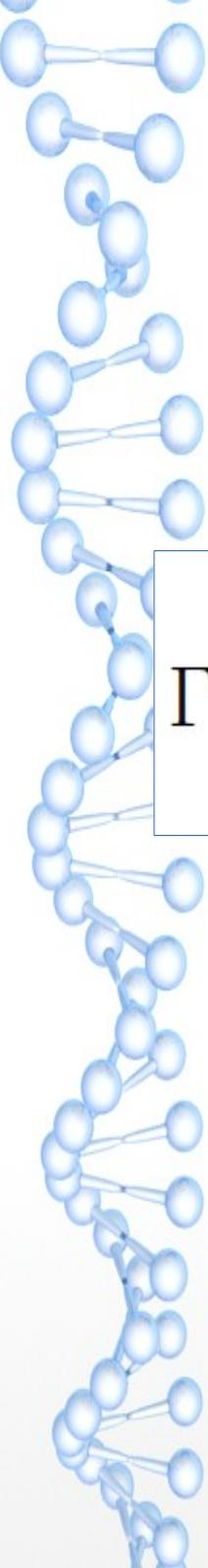
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Where $P_{R,L} = 1/2 (1 \pm \gamma^5)$ and

$$C_L^{ij} = + \frac{e}{16\pi^2} \sum_{k=0}^3 \sum_{m=1}^3 \left\{ \frac{1}{m_{l_m}^2} \left[m_i \mathcal{U}_{jm}^{Rk} (\mathcal{U}_{im}^{Rk})^* + m_j \mathcal{U}_{jm}^{Lk} (\mathcal{U}_{im}^{Lk})^* \right] \mathcal{I} \left(\frac{m_{\phi_{Sk}}^2}{m_{l_m}^2} \right) + \frac{1}{m_{l_m}^2} \mathcal{U}_{jm}^{Rk} (\mathcal{U}_{im}^{Lk})^* \mathcal{J} \left(\frac{m_{\phi_{Sk}}^2}{m_{l_m}^2} \right) \right\}$$

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$$l_i \rightarrow l_j + \gamma$$

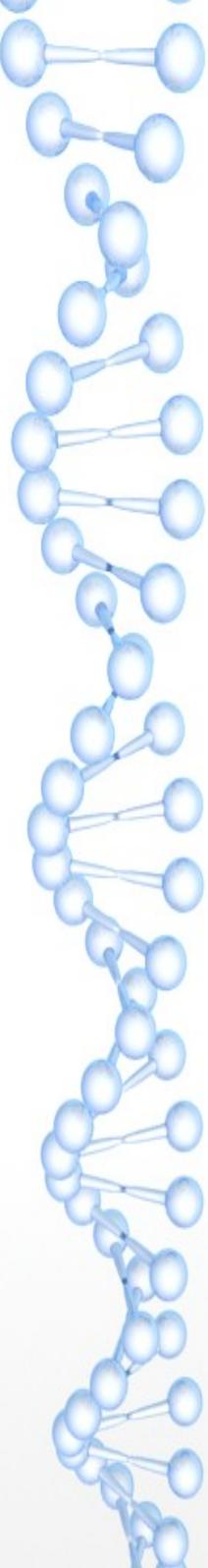
The partial width

$$\Gamma(l_i \rightarrow l_j \gamma) = \frac{1}{16\pi} m_{l_i}^3 \left(1 - \frac{m_{l_j}^2}{m_{l_i}^2}\right)^3 (|C_L^{ij}|^2 + |C_R^{ij}|^2)$$

The magnetic dipole moment anomaly for lepton l_i

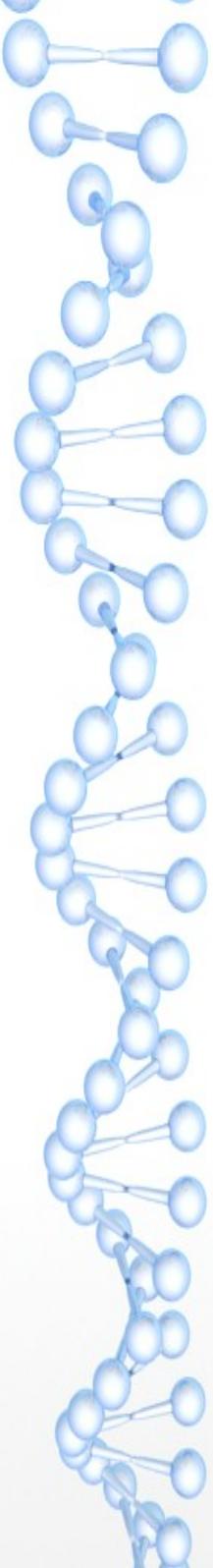
$$\Delta a_{l_i} = \frac{2m_{l_i}}{e} \left(\frac{C_L^{ii} + C_R^{ii}}{2} \right)$$

$$= + \frac{1}{16\pi^2} \left\{ \sum_{k=0}^3 \sum_{m=1}^3 2 (|\mathcal{U}_{im}^{Lk}|^2 + |\mathcal{U}_{im}^{Rk}|^2) \frac{m_{l_i}^2}{m_{l_M}^2} \mathcal{I} \left(\frac{m_{\phi_{Sk}}^2}{m_{l_M}^2} \right) + \sum_{k=0}^3 \sum_{m=1}^3 \text{Re} \left(\mathcal{U}_{im}^{Lk} (\mathcal{U}_{im}^{Rk})^* \right) \frac{m_{l_i}}{m_{l_M}} \mathcal{J} \left(\frac{m_{\phi_{Sk}}^2}{m_{l_M}^2} \right) \right\}$$

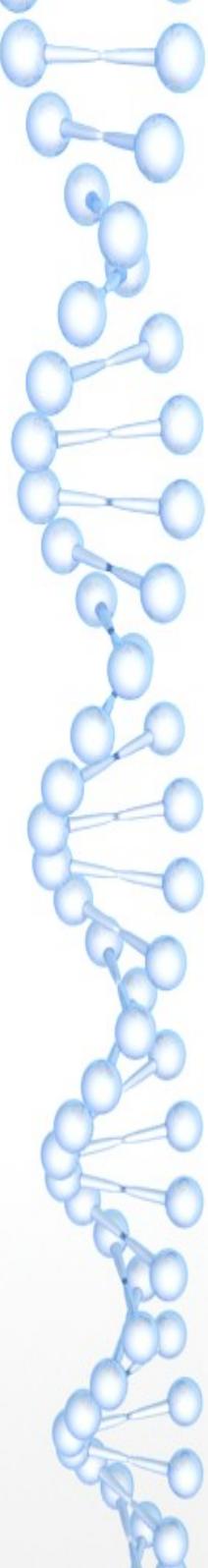


The electric dipole moment for lepton l_i

$$d_{l_i} = \frac{i}{2} (C_L^{ii} - C_R^{ii}) ,$$
$$= + \frac{e}{16\pi^2} \sum_{k=0}^3 \sum_{m=1}^3 \frac{1}{m_{l_m^M}} \text{Im} \left(\mathcal{U}_{im}^{Lk} (\mathcal{U}_{im}^{Rk})^* \right) \mathcal{J} \left(\frac{m_{\phi_{Sk}}^2}{m_{l_m^M}^2} \right)$$

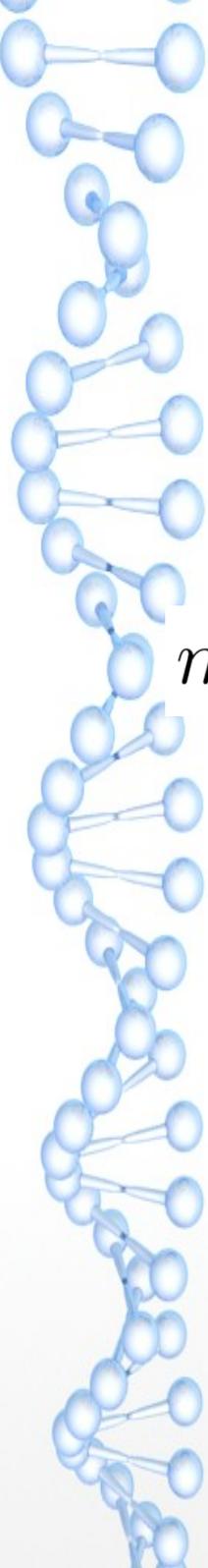


Analysis and Discussion



Analysis and Discussion

In our numerical analysis, we will adopt the following approach:



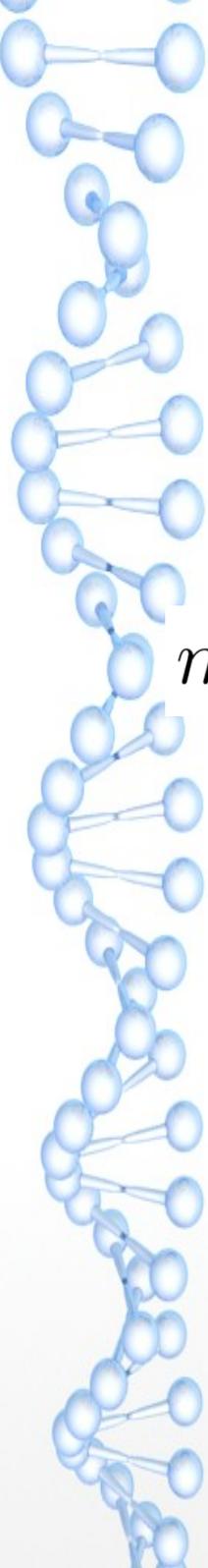
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with a fixed common mass $M_S = 10$ MeV.



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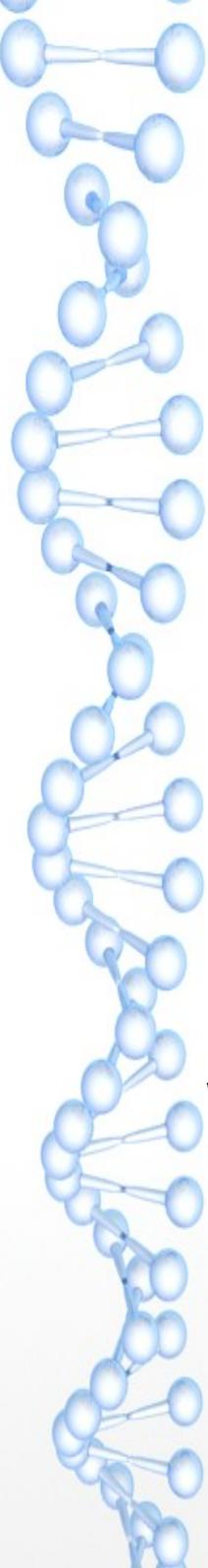
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- We assume all the Yukawa couplings $g_{0S'}$, $g_{1S'}$, $g_{2S'}$, $g'_{S0'}$, $g'_{S1'}$, and g'_{S2} to be all real and we also take $g_{0S} = g'_{S0'}$, $g_{1S} = g'_{S1'}$, $g_{S2} = (g_{1S})^*$ and $g'_{S2} = (g'_{S1'})^*$



Analysis and Discussion

For the three unknown mixing matrices, we consider 2 scenarios

– Scenario 1

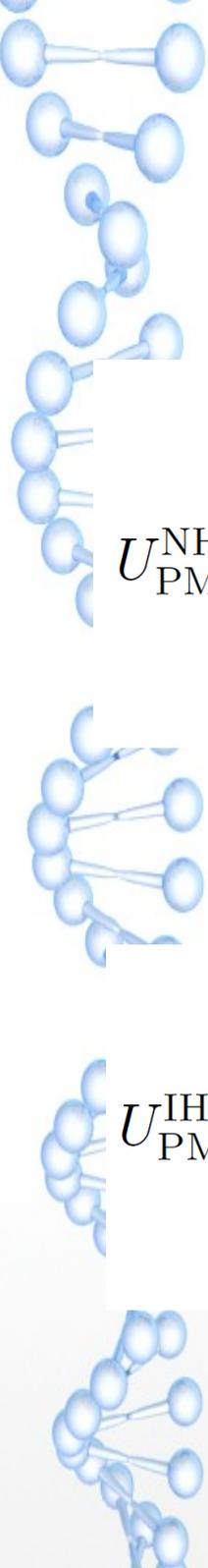
$$U_{\text{PMNS}}^{lM} = U'_{\text{PMNS}} = U''_{\text{PMNS}} = U_{\text{CW}}^\dagger$$

– Scenario 2

$$U_{\text{PMNS}}^{lM} = U'_{\text{PMNS}} = U''_{\text{PMNS}} = U_{\text{PMNS}}$$

Where the Cabibbo-Wolfenstein matrix

$$U_{\text{CW}} = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 1 & 1 \\ 1 & \omega & \omega^2 \\ 1 & \omega^2 & \omega \end{pmatrix}$$



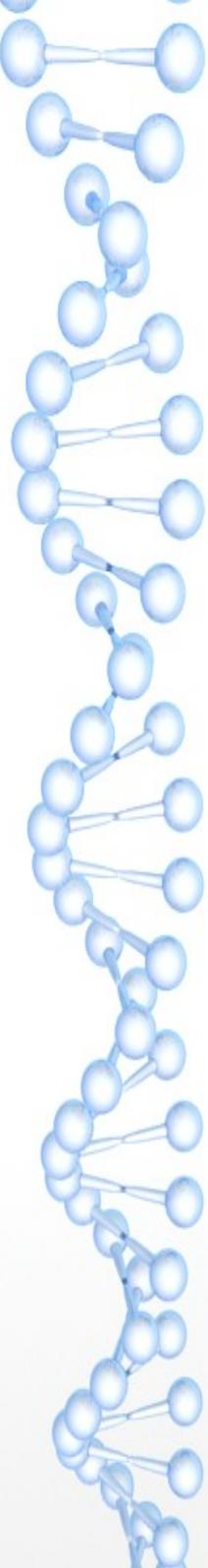
And PMNS matrix:

For Normal Hierarchy (NH)

$$U_{\text{PMNS}}^{\text{NH}} = \begin{pmatrix} 0.8221 & 0.5484 & -0.0518 + 0.1439i \\ -0.3879 + 0.07915i & 0.6432 + 0.0528i & 0.6533 \\ 0.3992 + 0.08984i & -0.5283 + 0.05993i & 0.7415 \end{pmatrix}$$

For Inverted Hierarchy (IH)

$$U_{\text{PMNS}}^{\text{IH}} = \begin{pmatrix} 0.8218 & 0.5483 & -0.08708 + 0.1281i \\ -0.3608 + 0.0719i & 0.6467 + 0.04796i & 0.6664 \\ 0.4278 + 0.07869i & -0.5254 + 0.0525i & 0.7293 \end{pmatrix}$$

- 
- Limit on $B(\mu \rightarrow e\gamma)$ from MEG experiment:

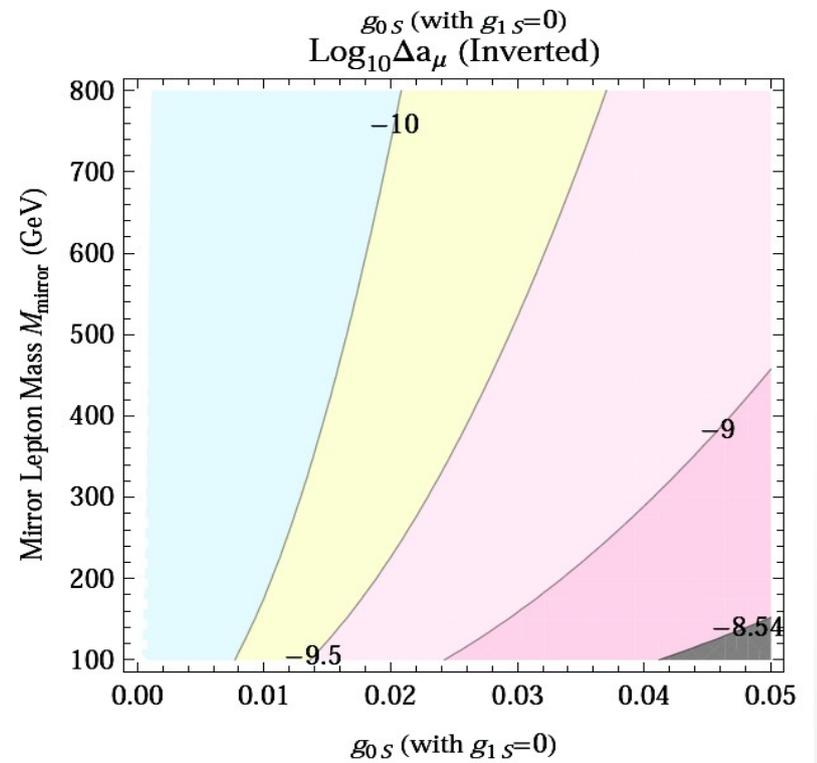
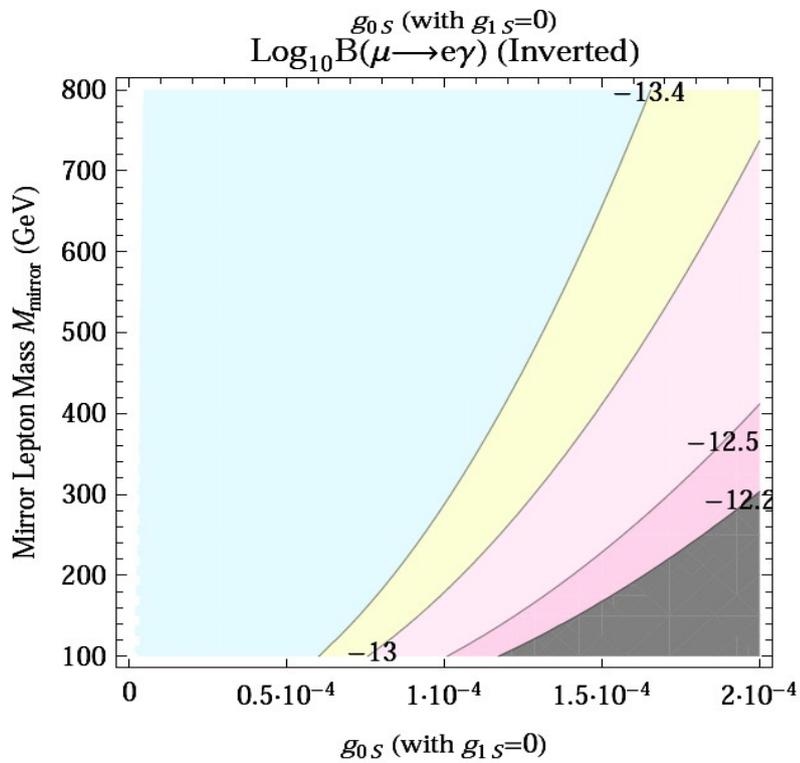
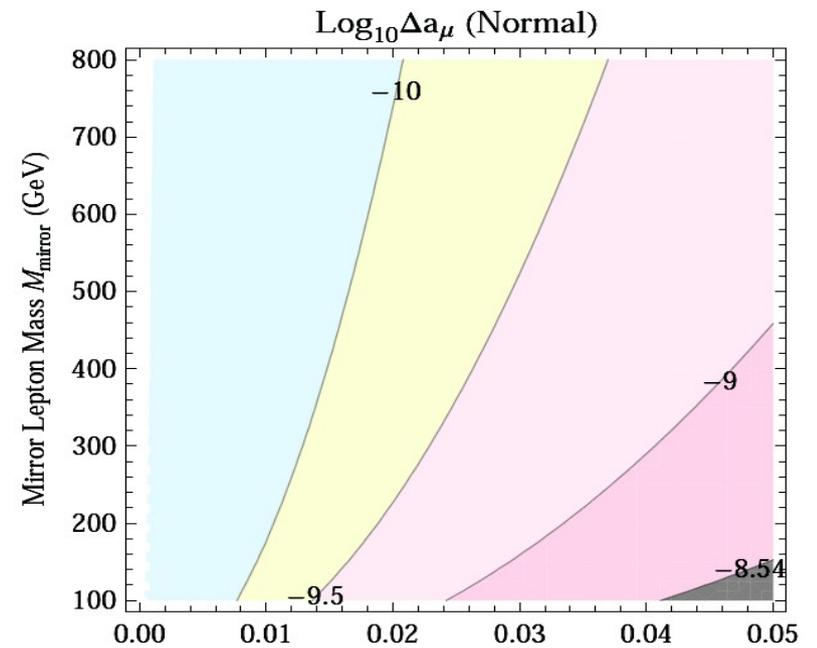
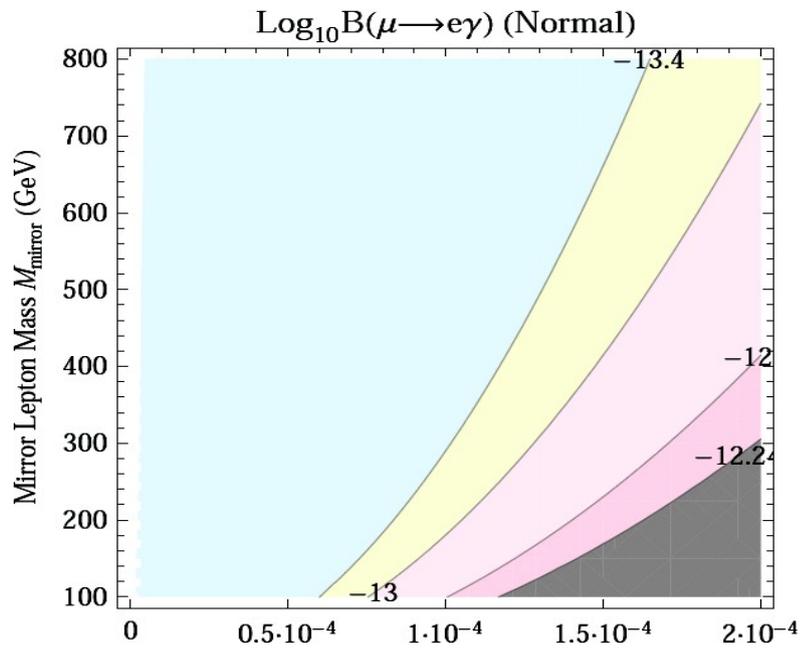
$$B(\mu \rightarrow e\gamma) \leq 5.7 \times 10^{-13} \text{ (90 C.L.) [MEG, 2013]}$$

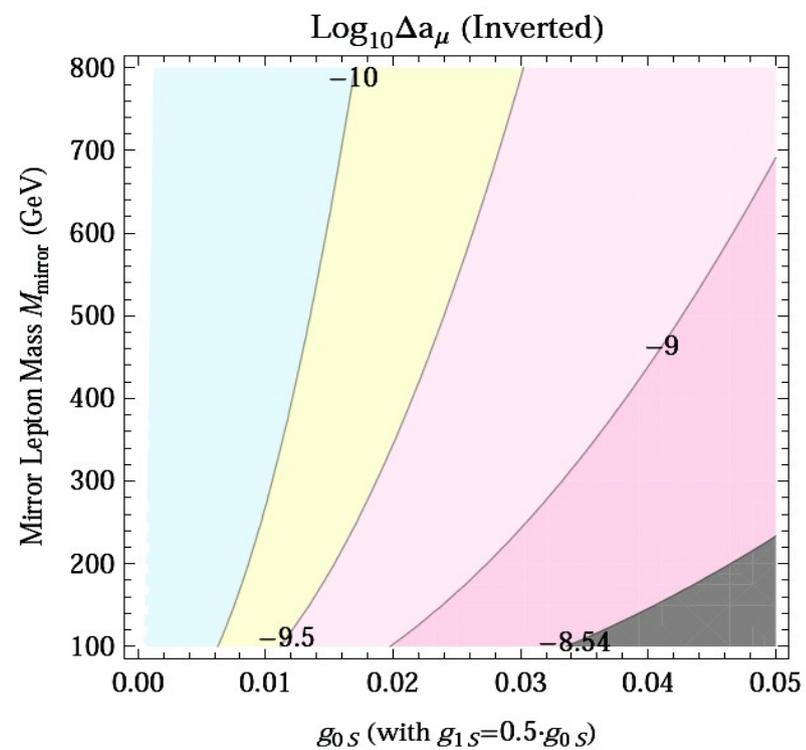
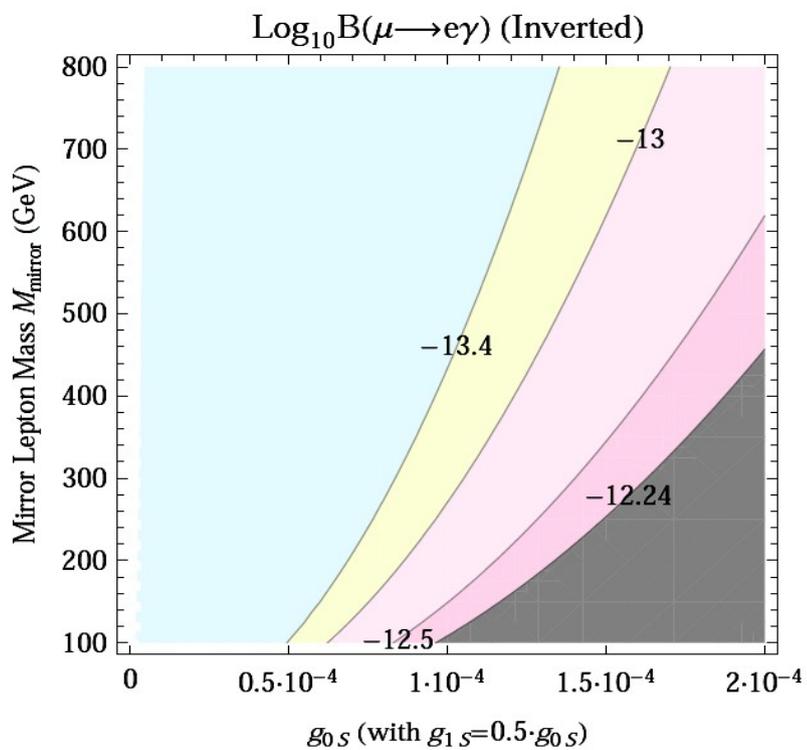
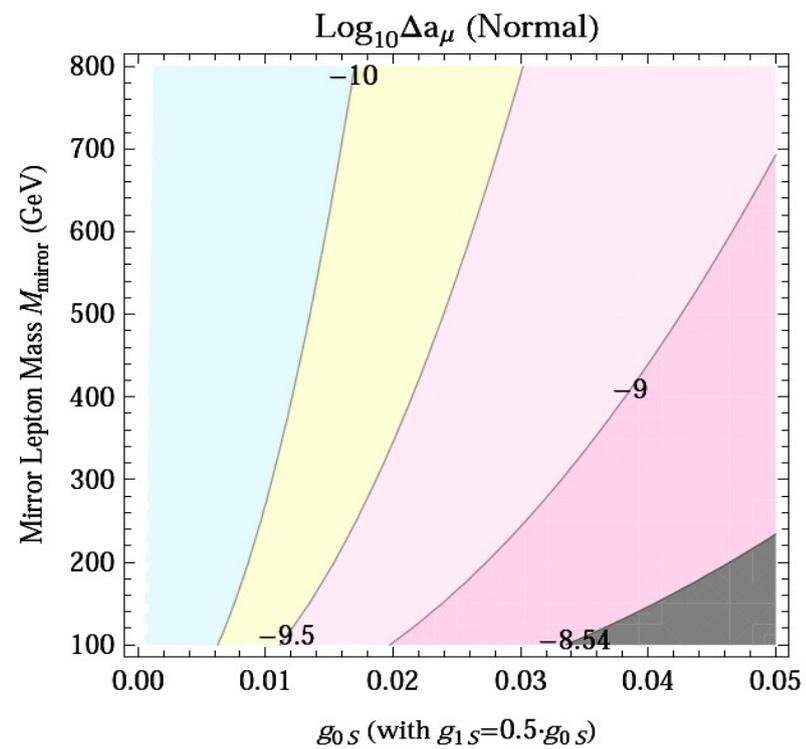
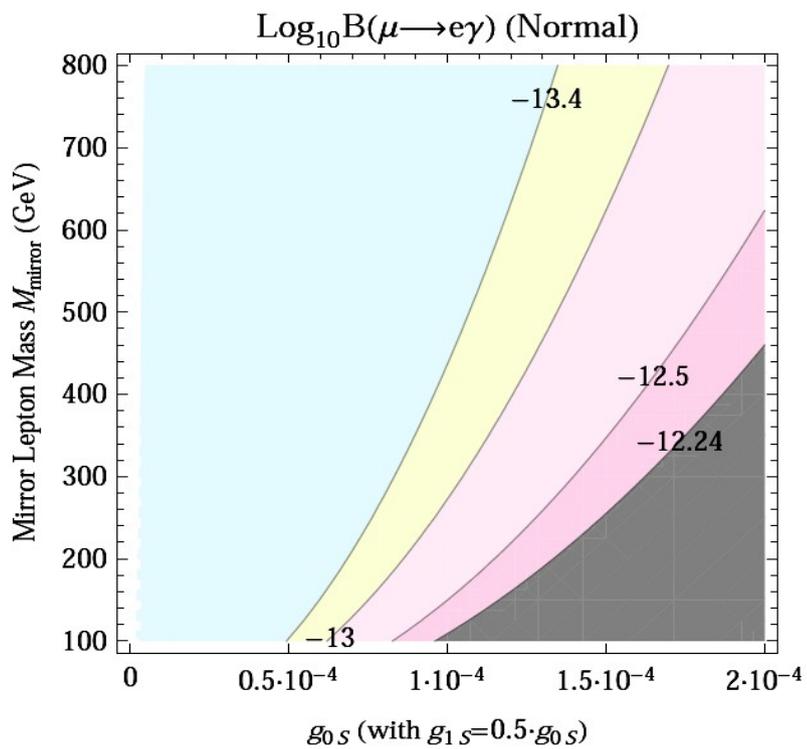
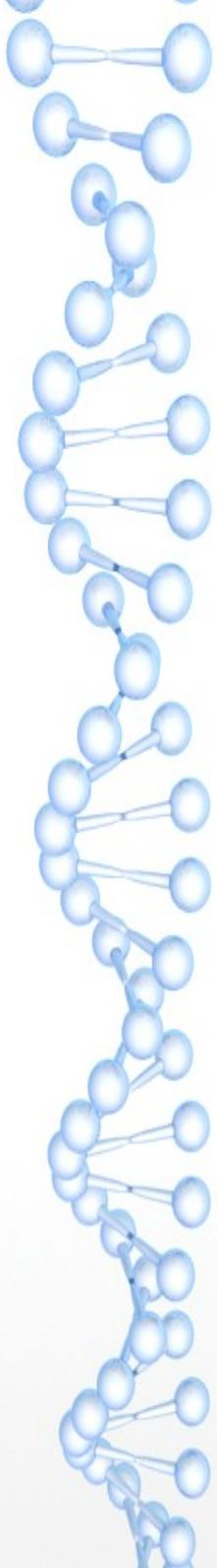
$$B(\mu \rightarrow e\gamma) \sim 4 \times 10^{-14} \text{ [Projected Sensitivity]}$$

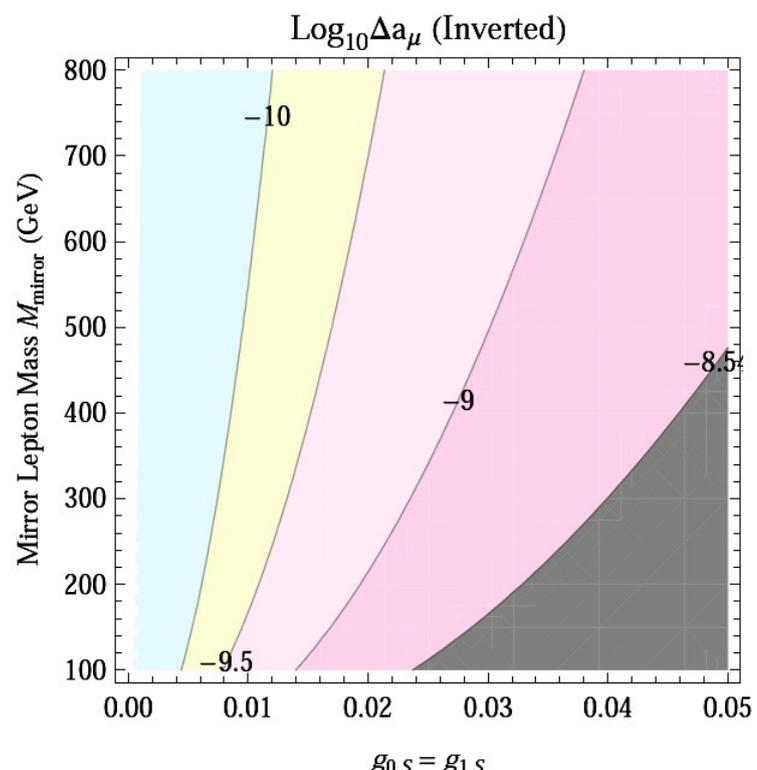
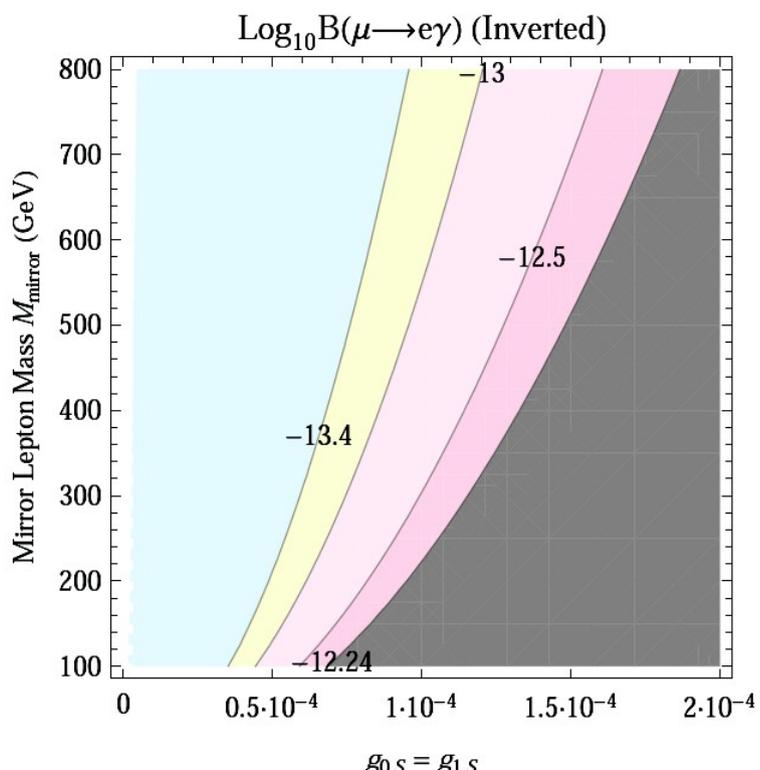
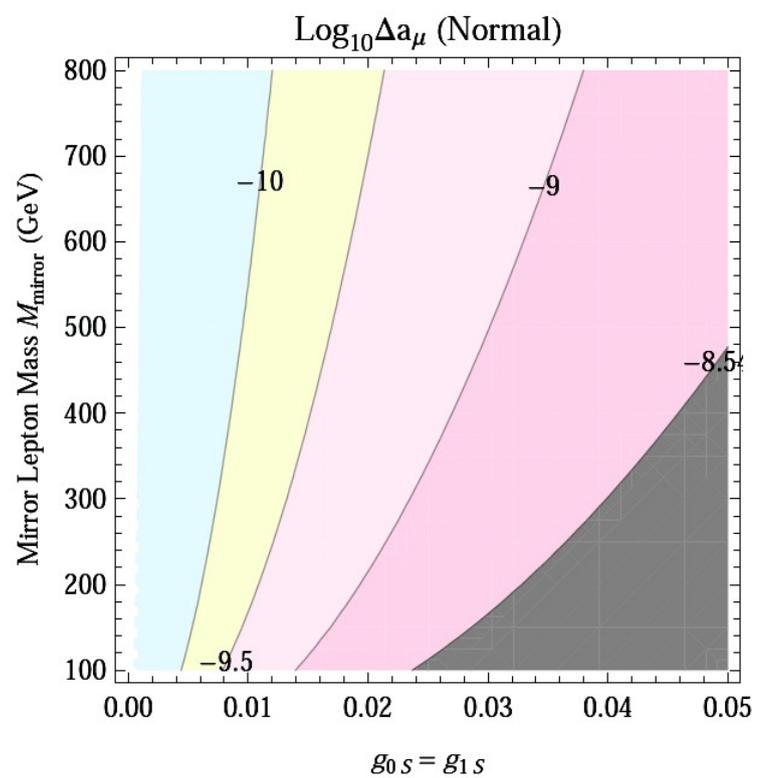
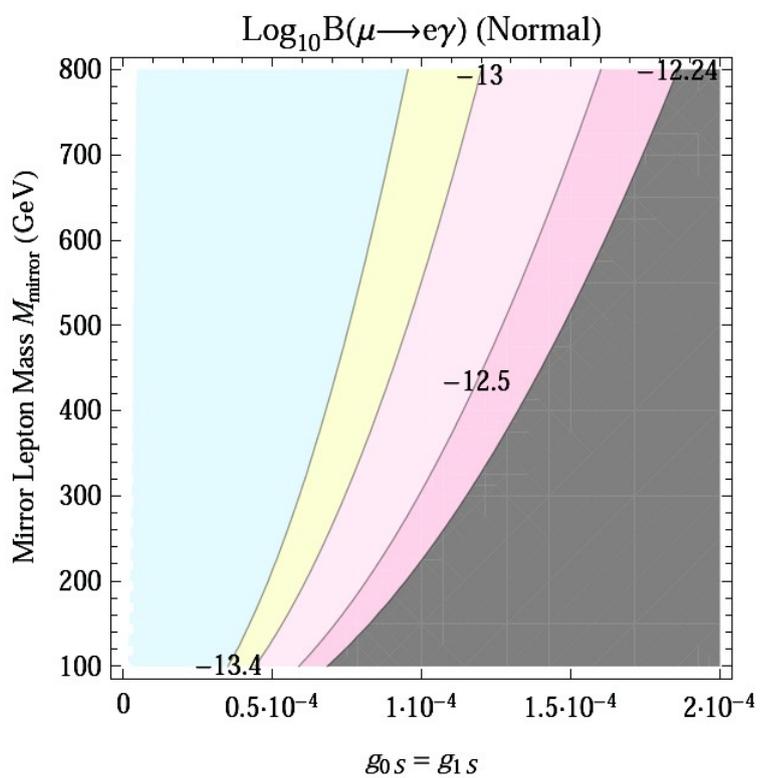
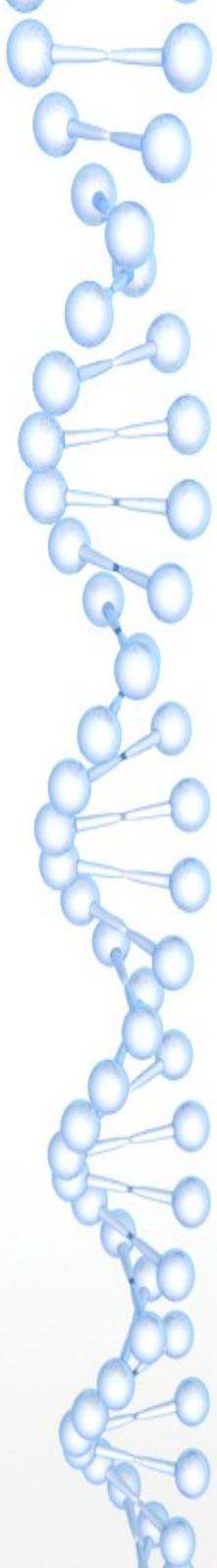
- Δa_μ from E821 experiment

$$\Delta a_\mu \equiv a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 288(63)(49) \times 10^{-11}$$

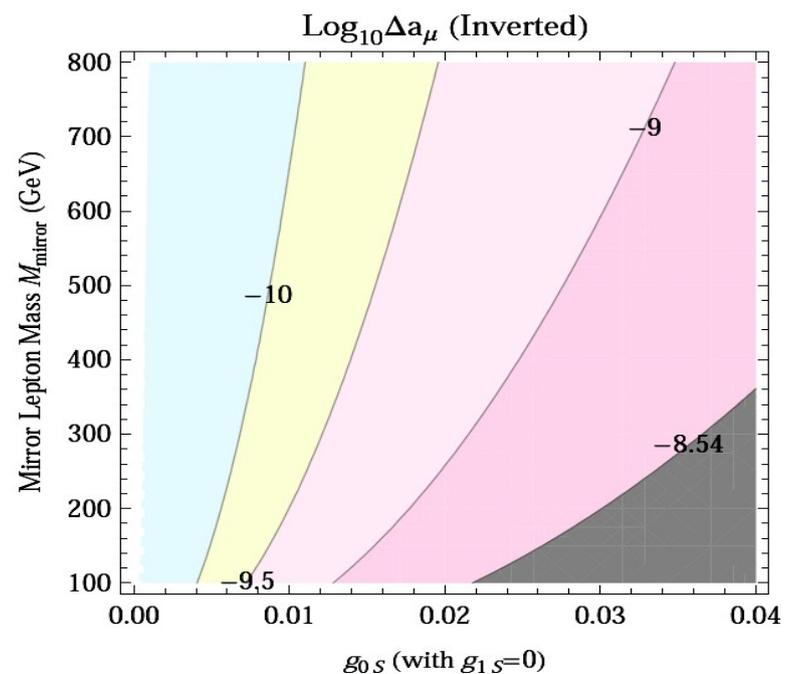
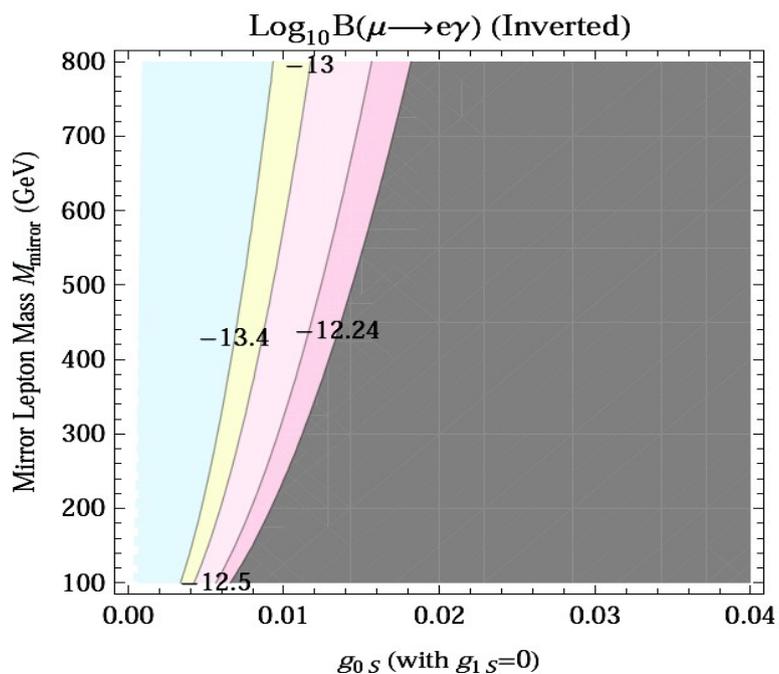
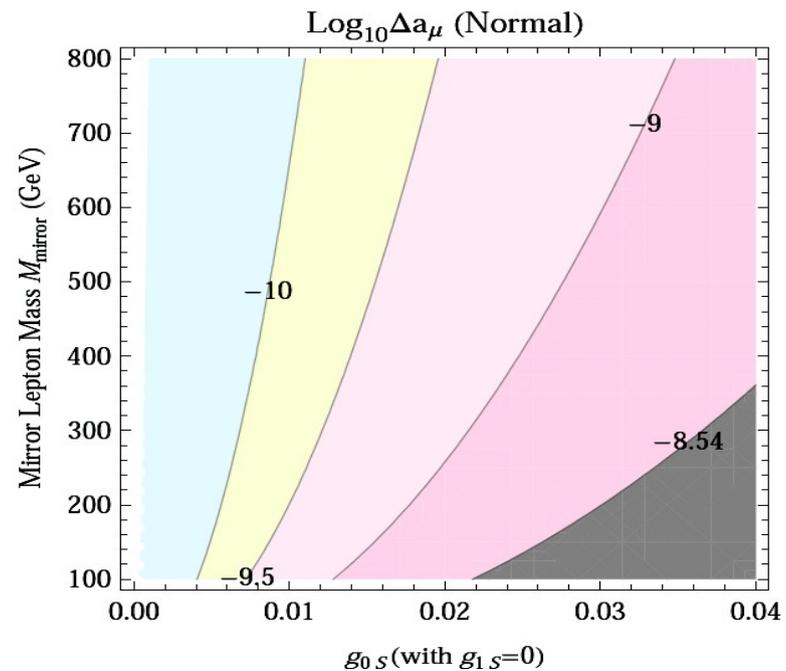
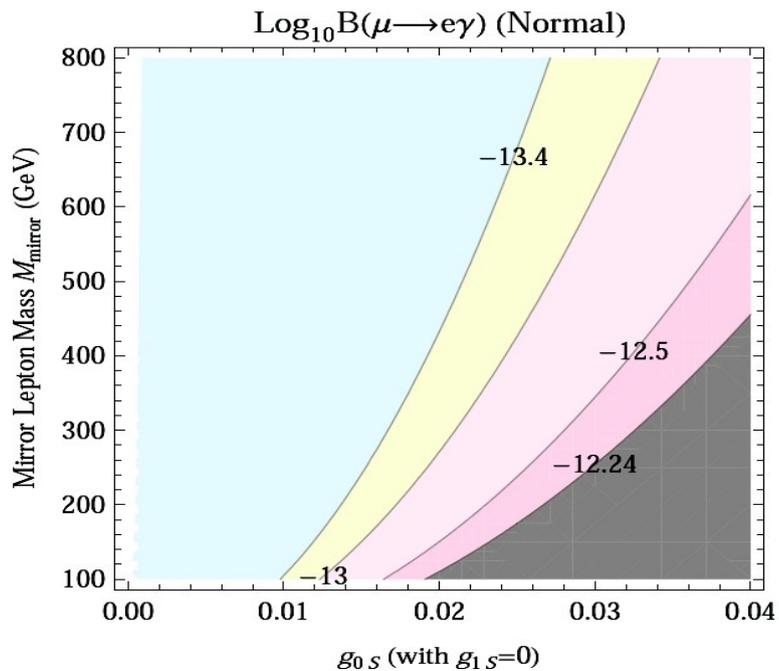
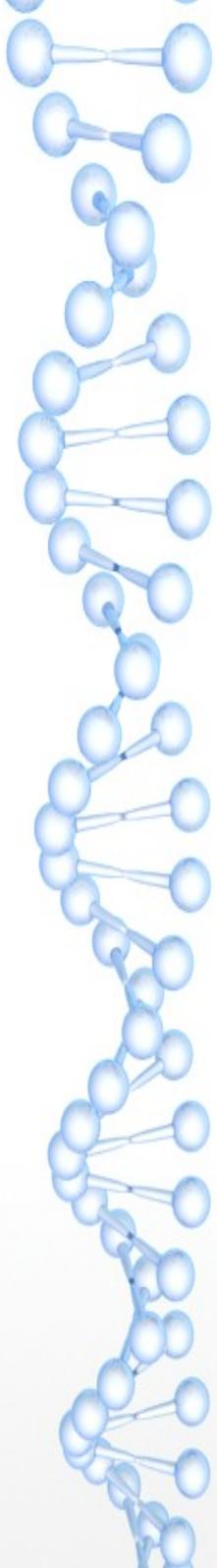
Scenario 1

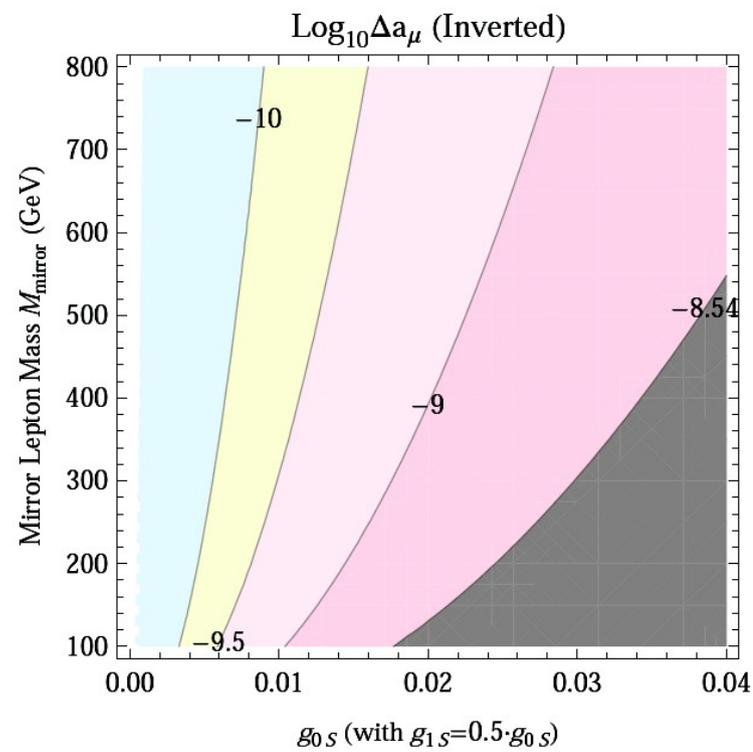
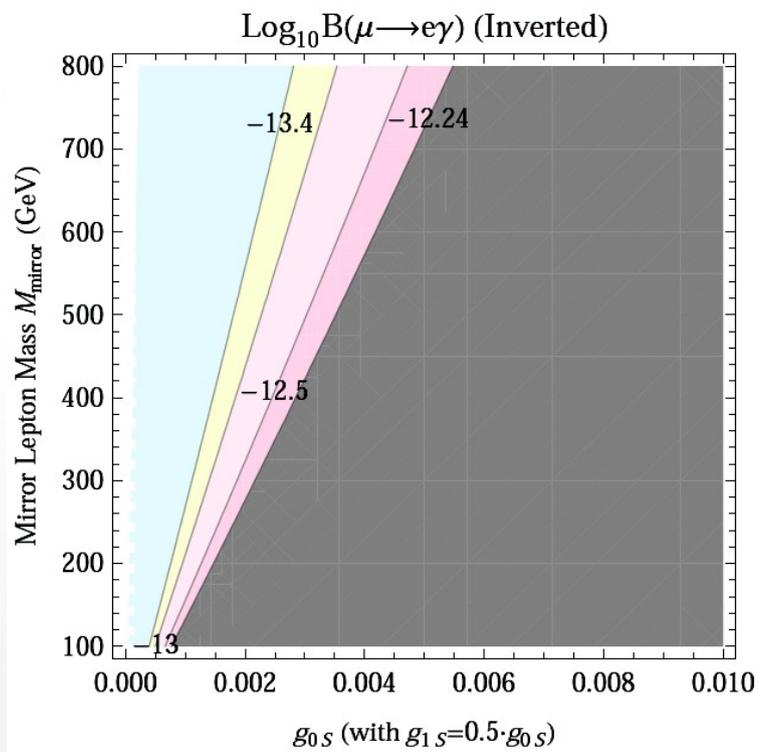
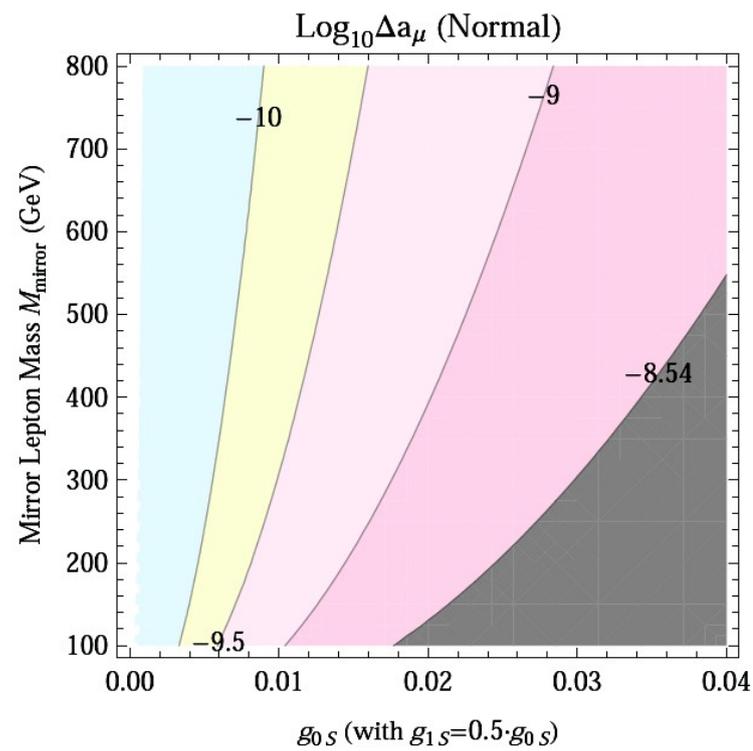
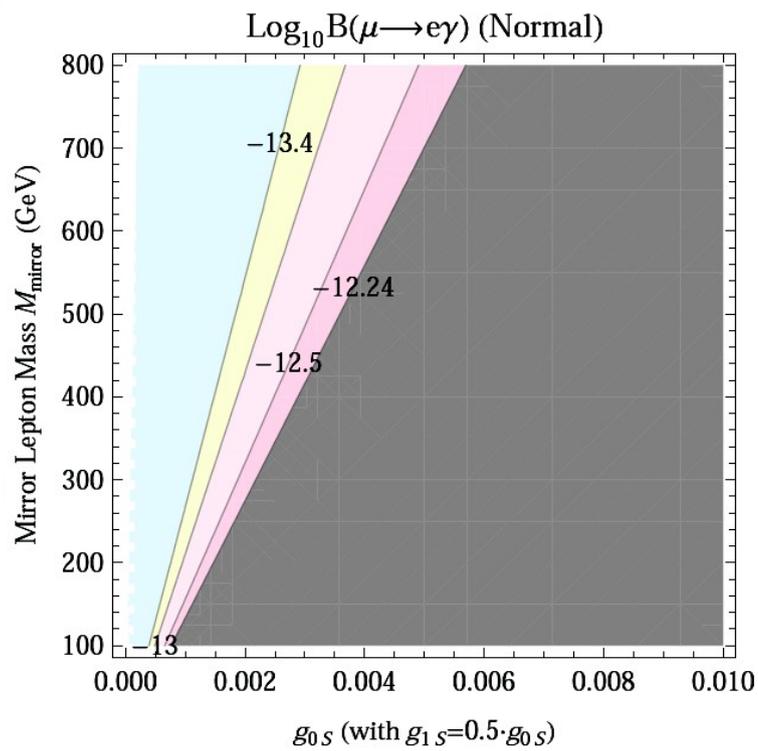
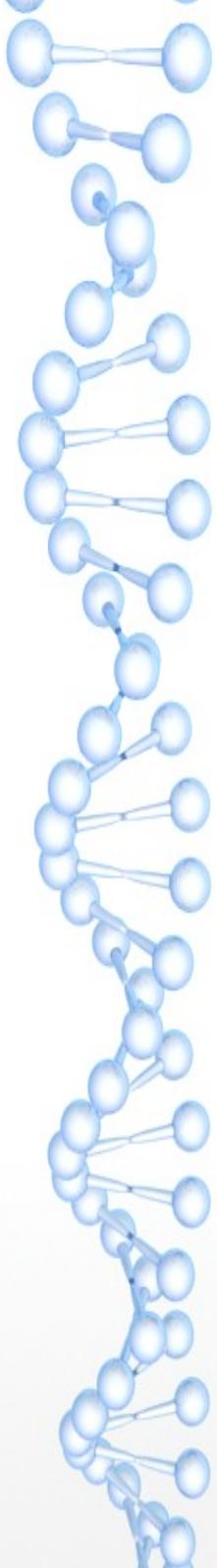


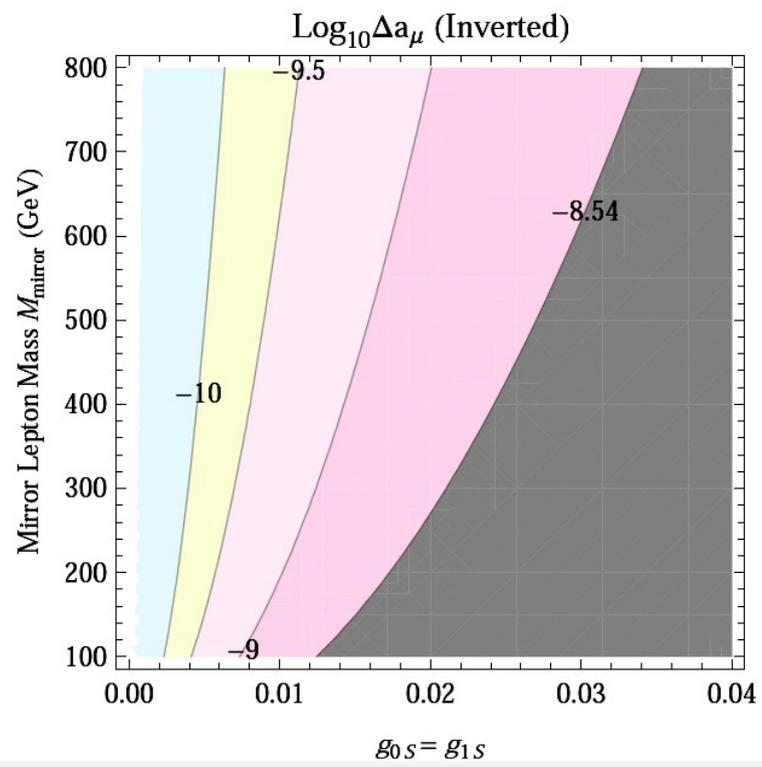
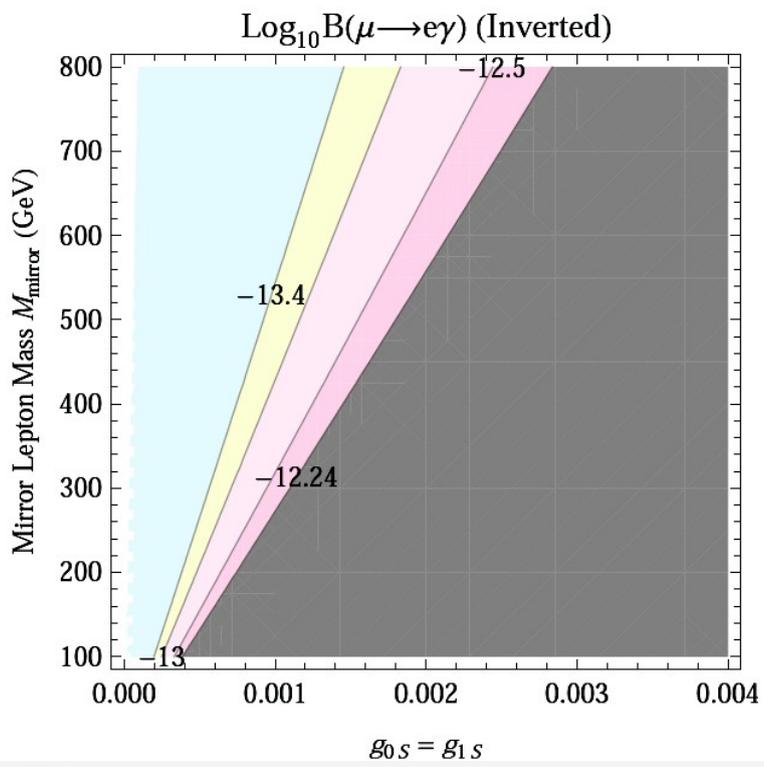
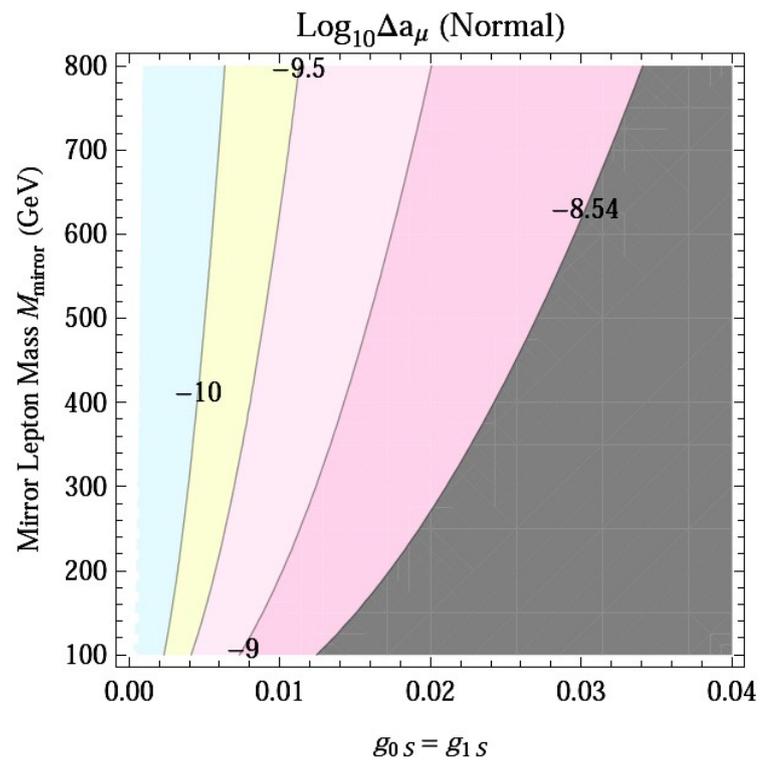
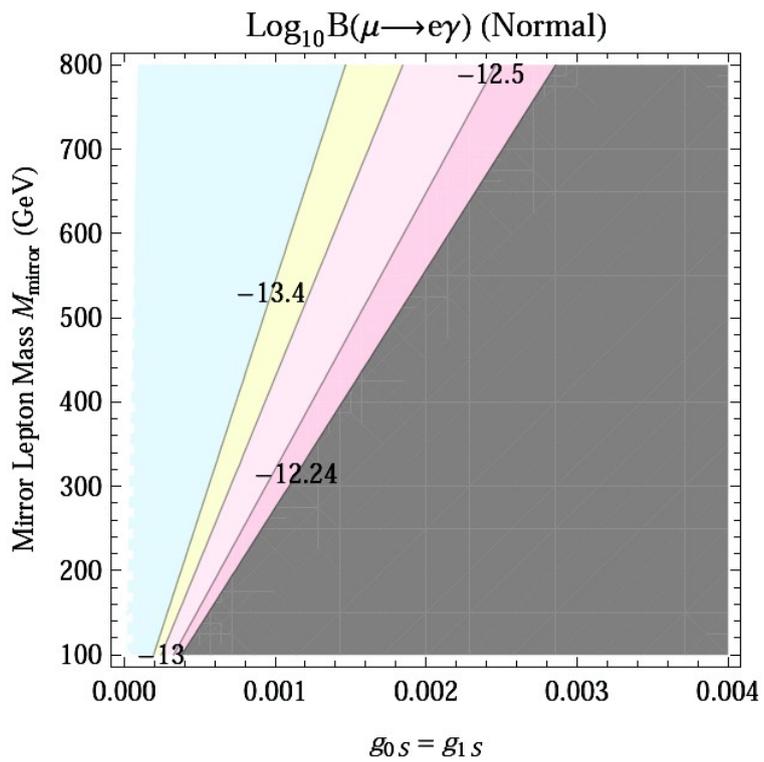
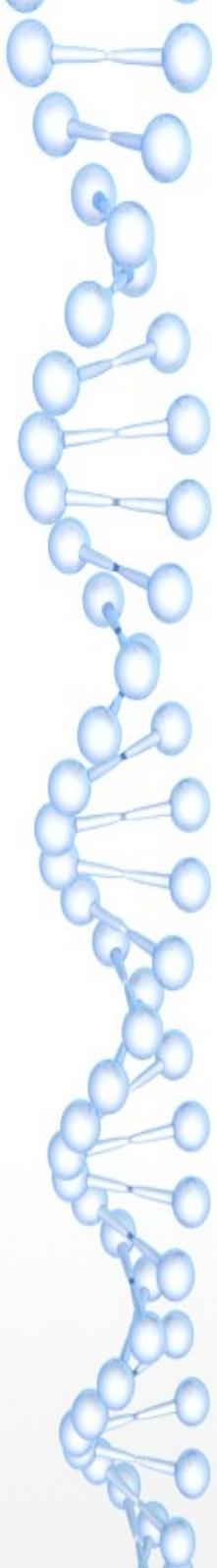


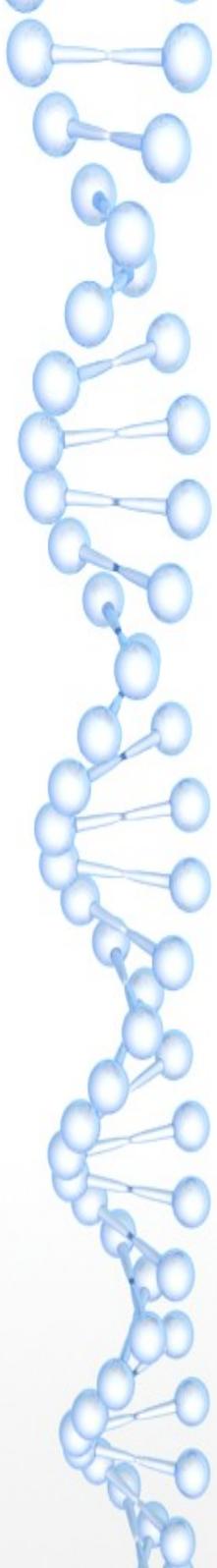


Scenario 2

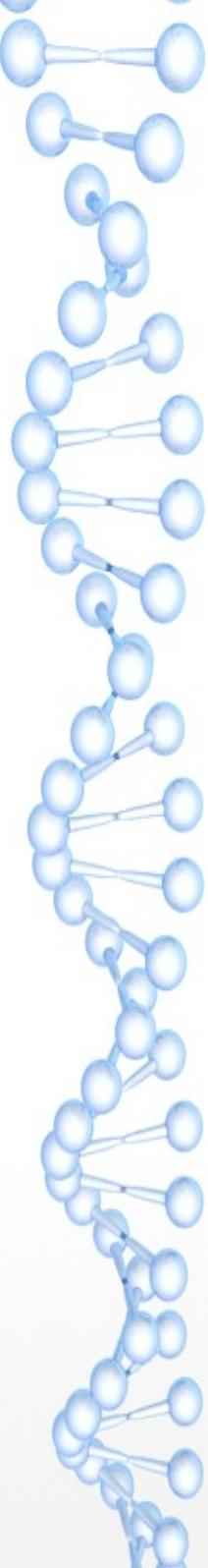






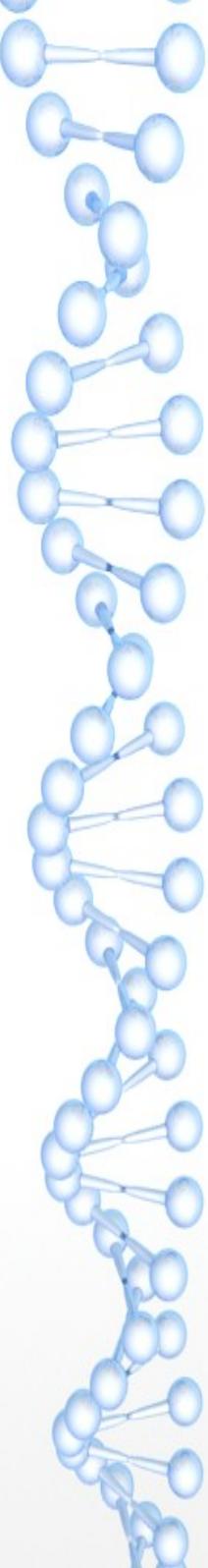


From these plots, we observe the following:



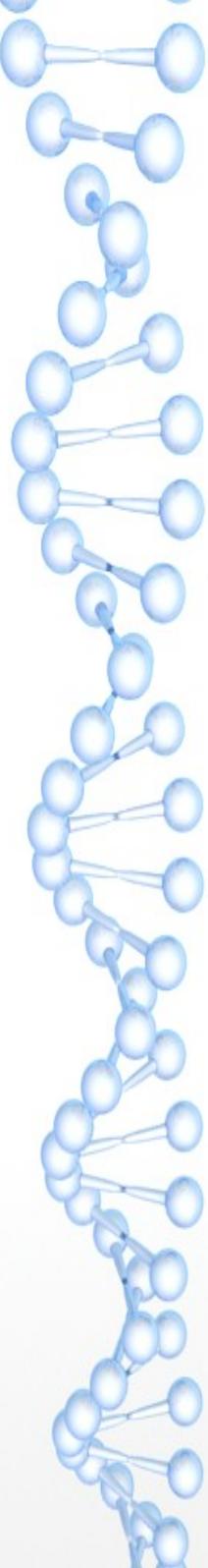
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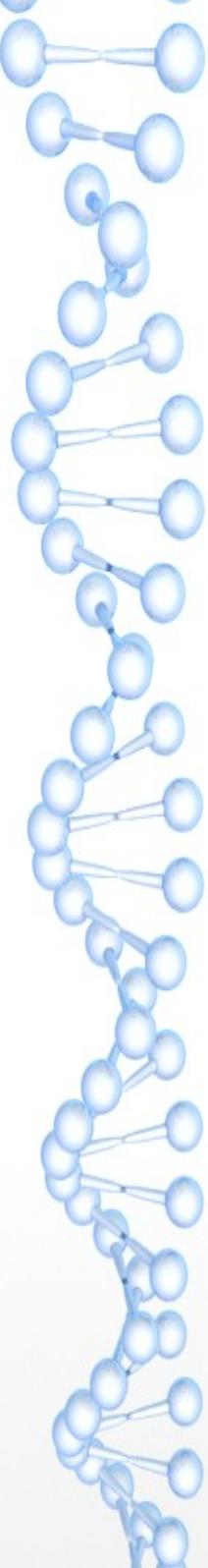
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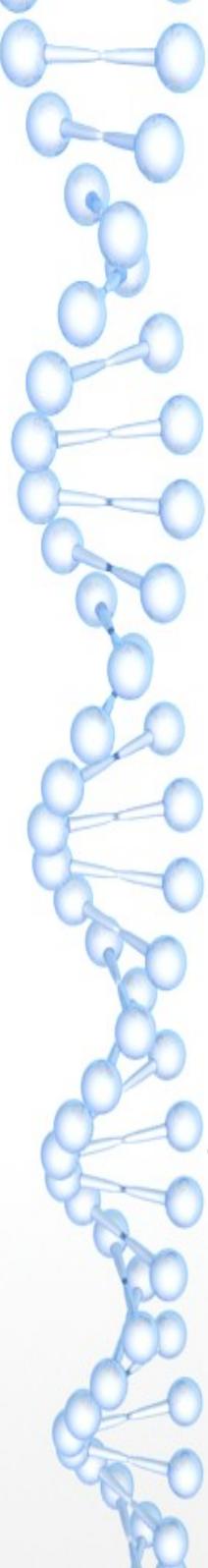
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3. However, for Scenario 2, there is slightly different between normal and inverted cases. These differences depend on these couplings, for $g_{1S} \geq 0.5 \times g_{0S}$, these differences diminish.



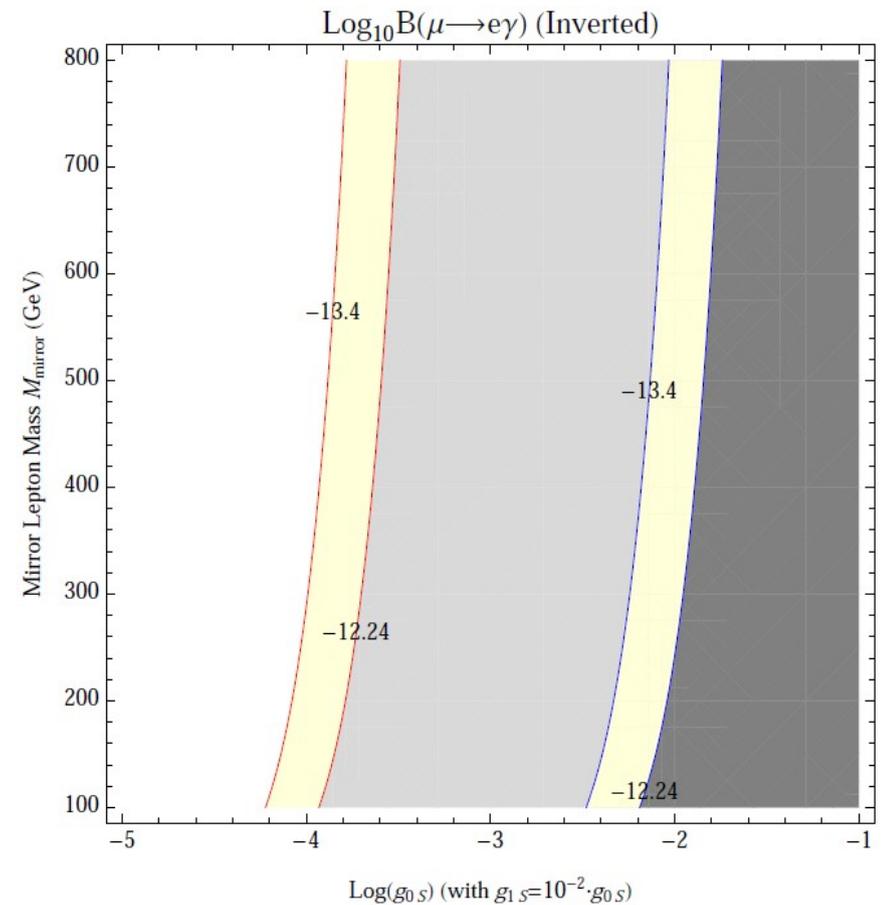
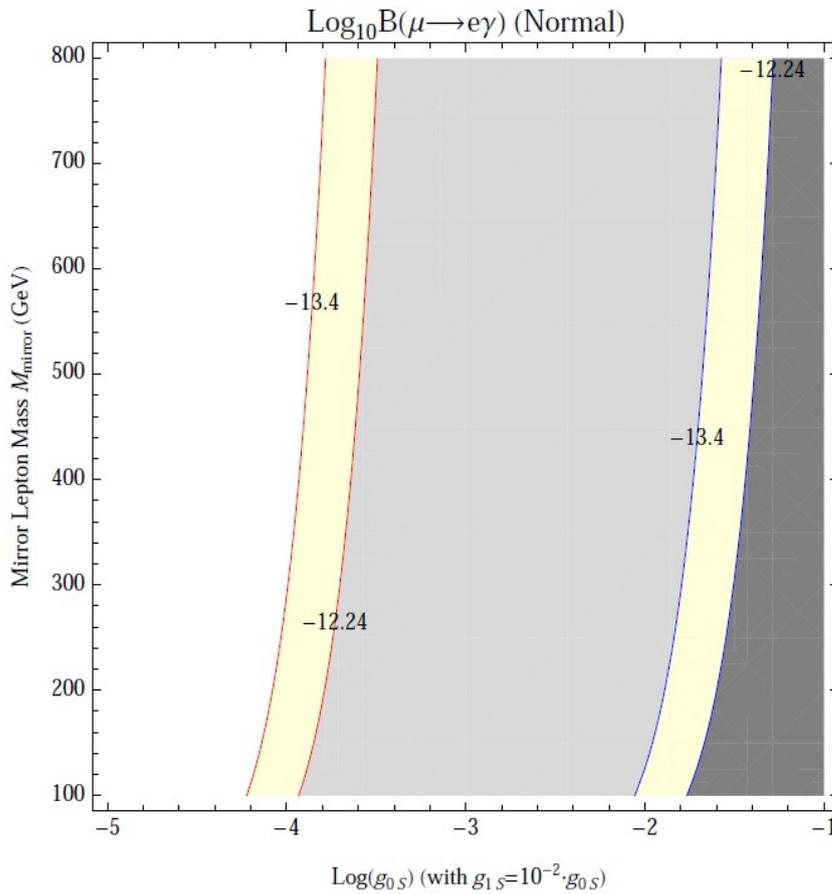
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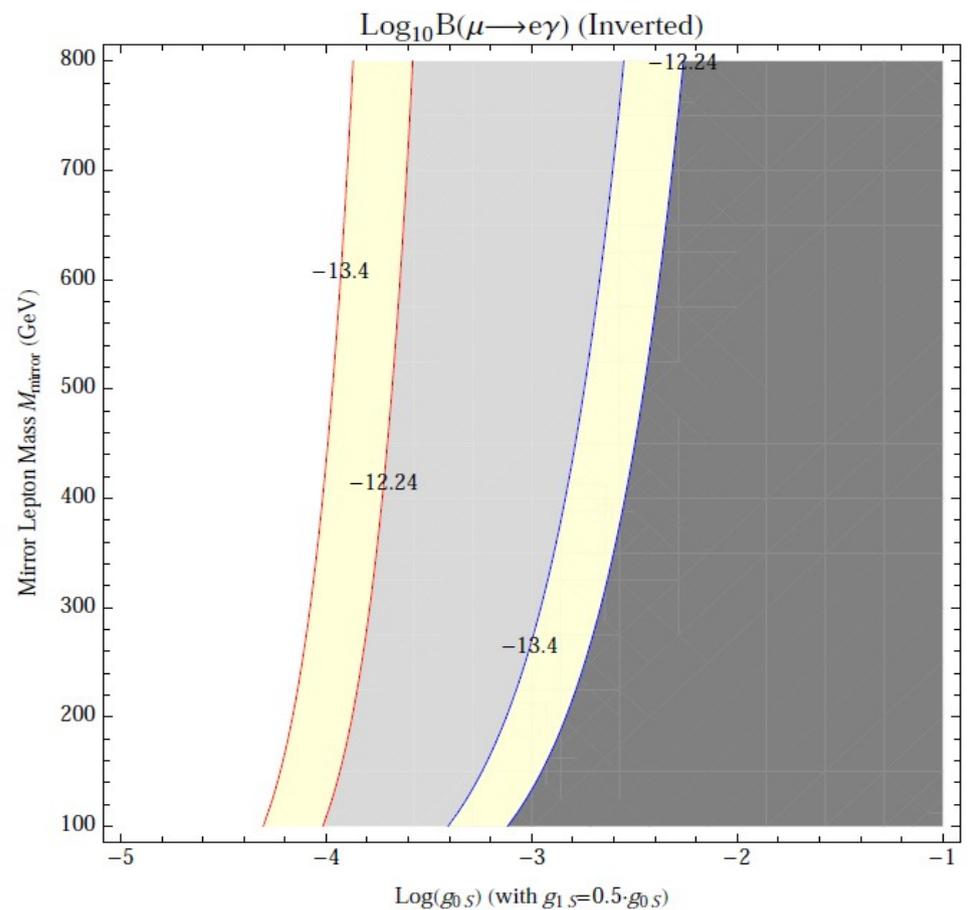
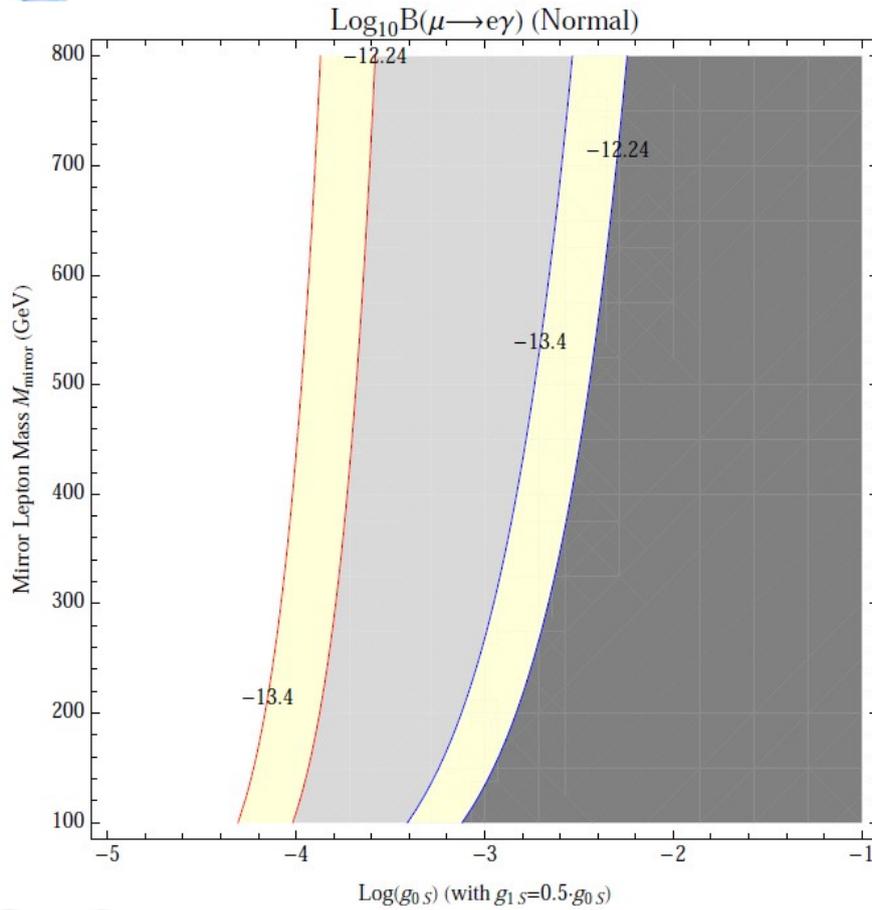


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4. The sensitivity of the couplings in the $B(\mu \rightarrow e + \gamma)$ has been weakened by one to two order of magnitudes for scenario 2, while for the muon anomalous magnetic moment it stays more or less the same.

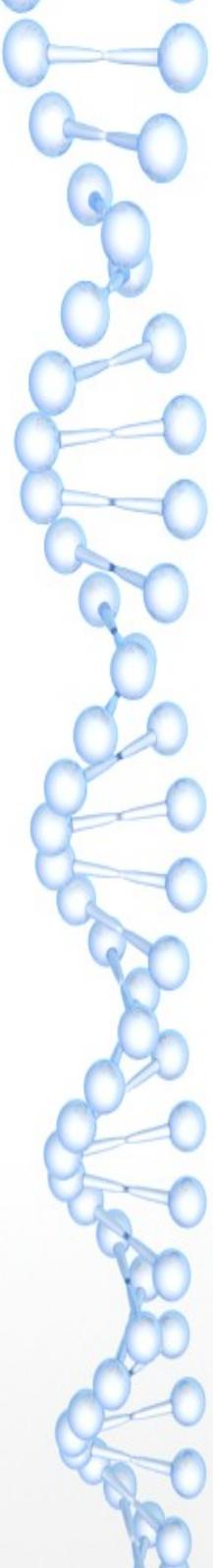


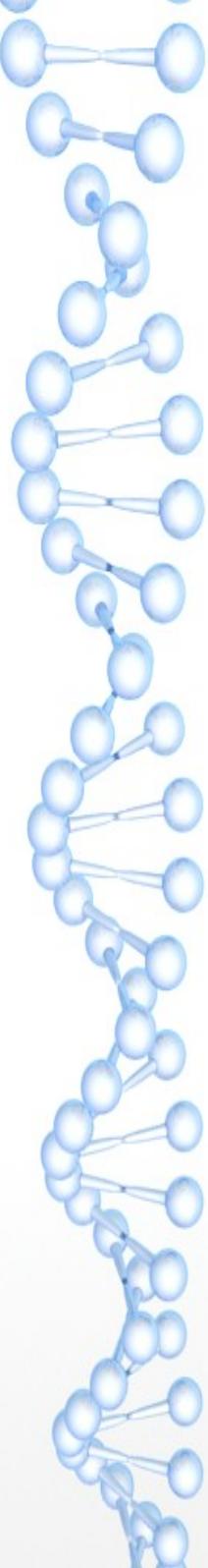
Contour plots of $\text{Log}_{10}B(\mu \rightarrow e + \gamma)$ on the $(\text{Log}_{10}g_{0S}; M_{\text{mirror}})$ plane for normal (left panel) and inverted (right panel) hierarchy in Scenario 1 (red) and 2 (blue) with $g_{0S} = g'_{0S}$ and $g_{1S} = g'_{1S} = 10^{-2} g_{0S}$.



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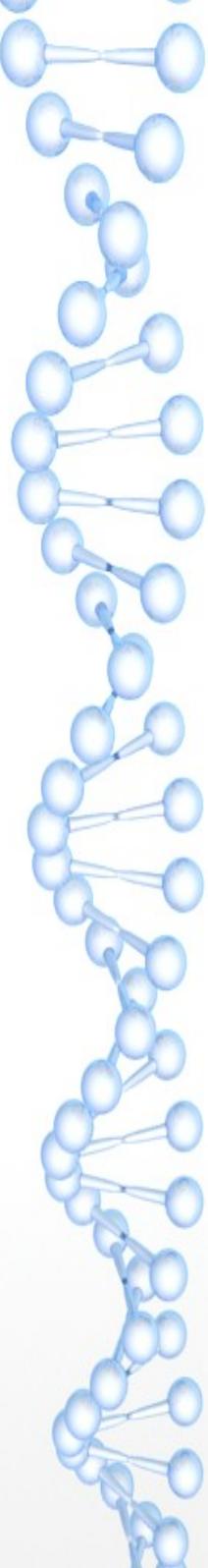
Summary





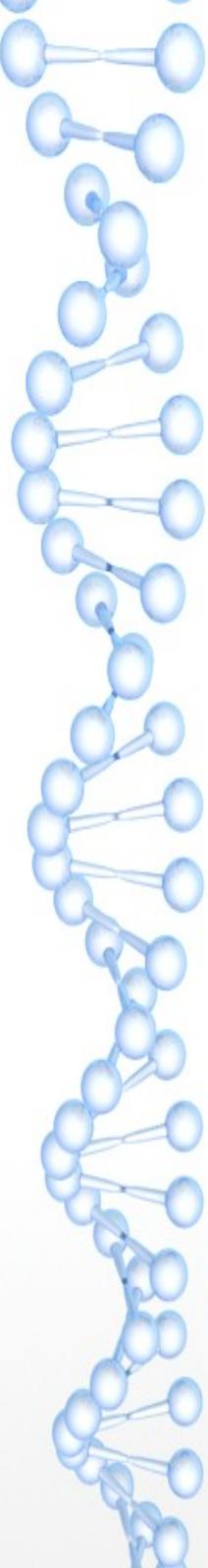
Summary

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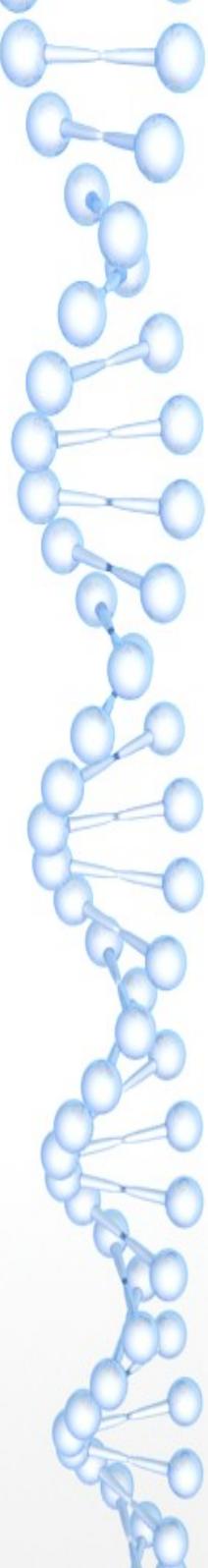
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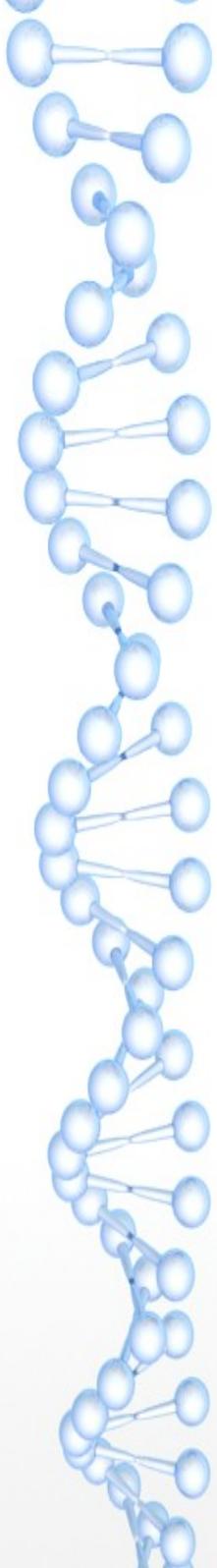
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- ✓ We calculated the LFV processes ($\mu \rightarrow e + \gamma$) as well as anomalous magnetic dipole moment in framework of an extended of Electroweak-scale Right-handed neutrino Model
- ✓ By the recent and future expectation data at MEG we figured out some interesting constraints on the model



THANK YOU