

XYZ revisited (mainly Charmonia)

IHEP-Beijing, May 11, 2015

Luciano Maiani, Universita' di Roma La Sapienza, and INFN, Roma, Italia

1. Introduction

Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqqq\bar{q})$, etc., while mesons are made out of $(q\bar{q})$, $(qq\bar{q}\bar{q})$, etc.

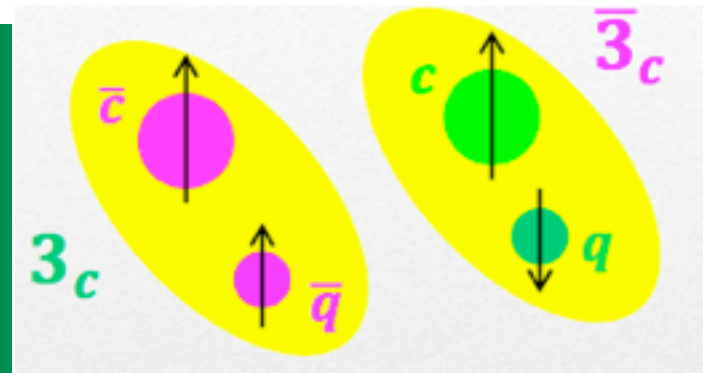
M. Gell-Mann, A Schematic Model of Baryons and Mesons, PL **8**, 214, 1964

- For long, we lived with the simplest paradigm:

$$\text{mesons} = q\bar{q}, \quad \text{baryons} = qqq$$

- Paradigm rested on the absence of $I=2$, $\pi\pi$ resonances and of $S>0$ baryons.
- The case had to be revisited, because the lowest lying, octet of scalar mesons- $f_0(980)$, $a_0(980)$, $\kappa(800)$ and $\sigma(600)$ - does not fit in the picture.
- The $X(3872)$, narrow width, with decays into $J/\Psi + 2\pi/3\pi$, discovered by Belle in 2003, does not fit into the “charmonium” states,
- since then, Belle, BaBar, BES and LHCb have reported many other states that do not fit the charmonium picture, called $X(1^{++})$ and $Y(1^{-})$ states: molecules? hybrids? tetraquarks?
- In 2007, Belle observed a charged “charmonium”, $Z^+(4430) \rightarrow \psi(2S) + \pi$, that could not be interpreted as molecule, but later Babar suggested it was simply a reflection of K^* states
- LHCb has confirmed the $Z^+(4430)$ while other similar states, $Z^+(3900)$ and $Z^+(4020)$, have been established.

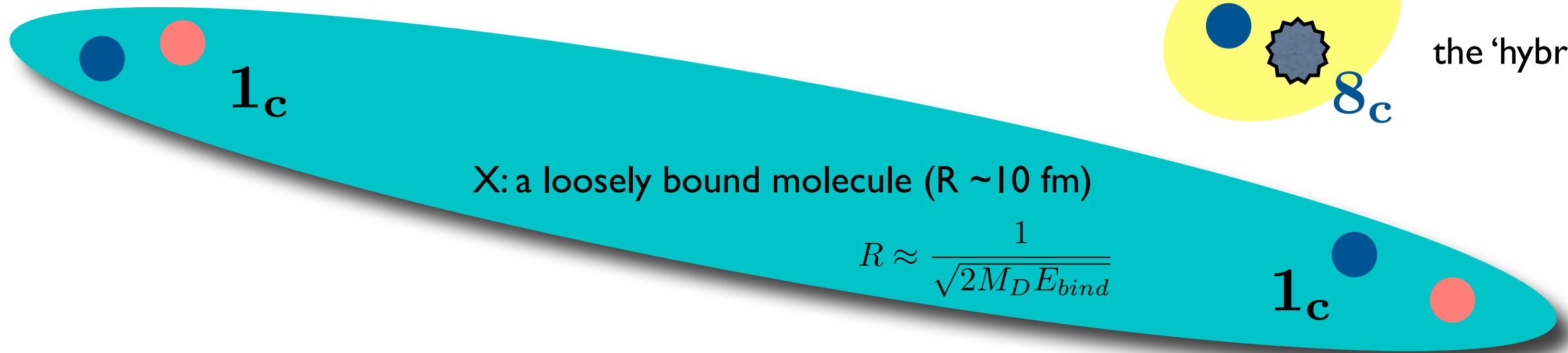
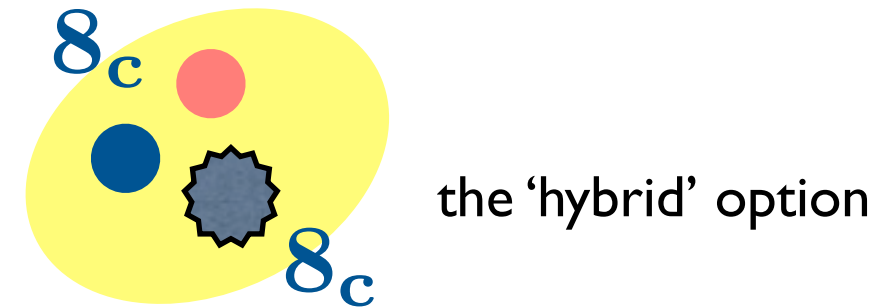
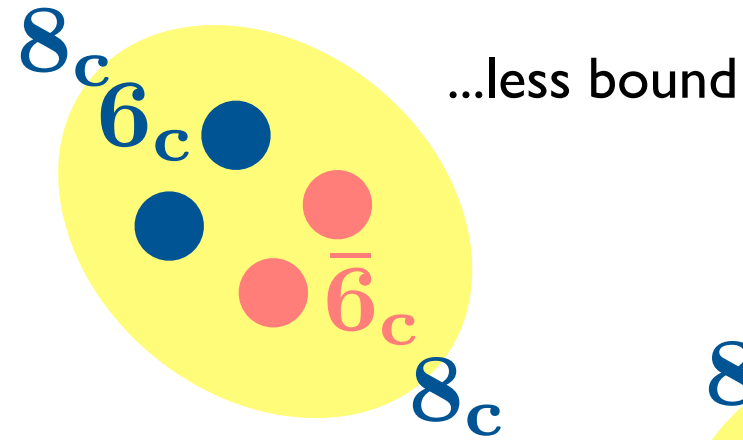
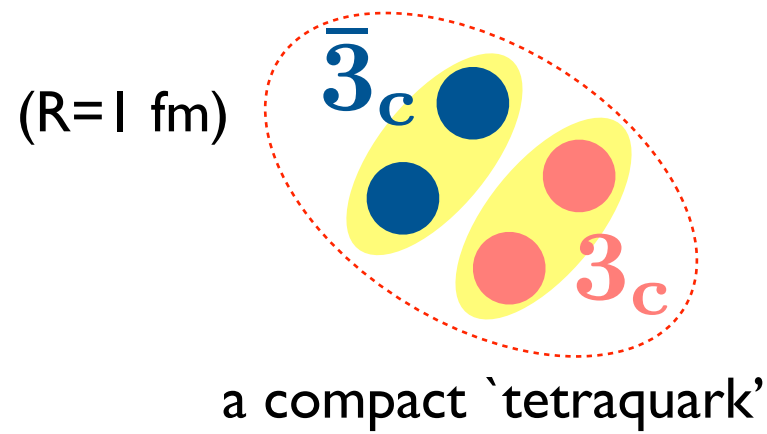
I shall follow the idea that X , Y , and Z states belong to a new spectroscopy of mesons, made by diquark-antidiquark pairs. For Beauty see also A. Ali, Belle II TIP, Krakov (slides available).



Models for X Y Z mesons

see e.g. M.Cleven, F.K.Guo, C.Hanhart, Q.Wang and Q.Zhao, arXiv:1505.01771 and refs. therein

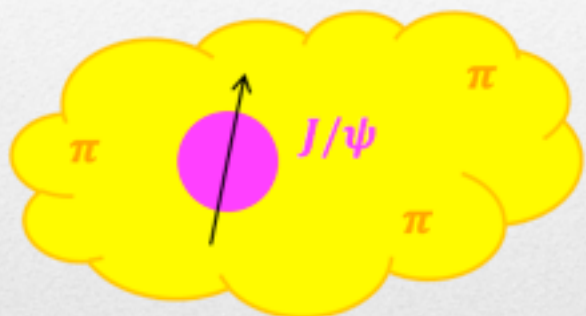
courtesy of A. Polosa



Hadro-charmonium




X.Li, M.B.Voloshin, Mod. Phys. Lett. 29(2014) 12, 1450060 and refs. therein

Voloshin arXiv:1304.0380



A $c\bar{c}$ state surrounded by light matter

Decay into $\eta_c \rho$ forbidden by HQSS

-  quark (heavy or light)
-  antiquark
-  gluon

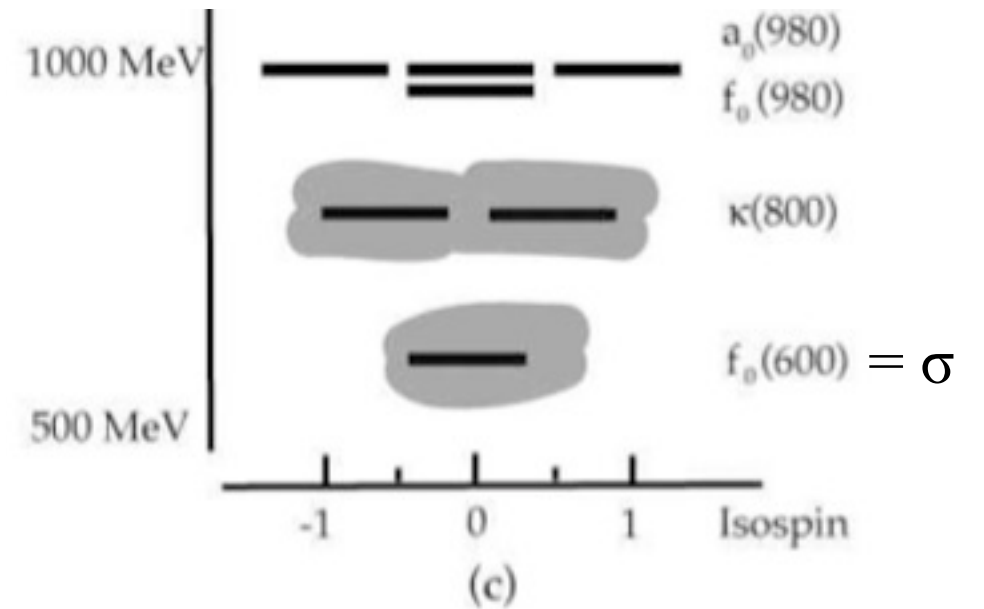
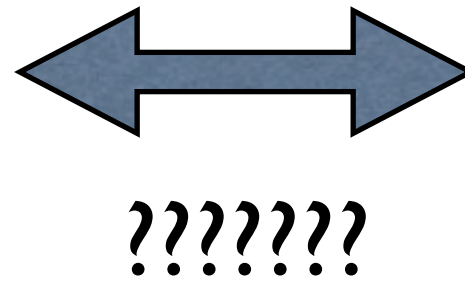
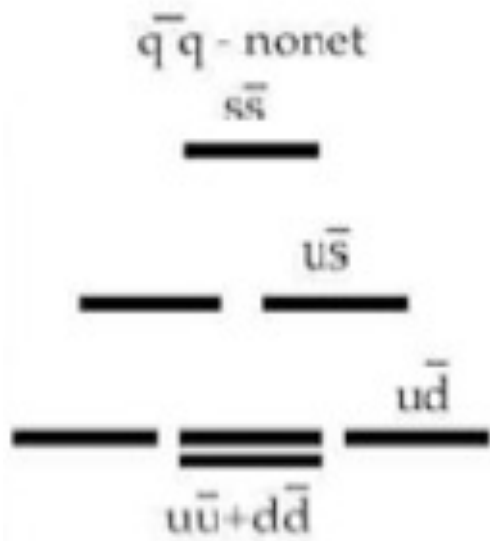
Few think X, Y, Z are only kinematic effects due to the opening of new channels. For one, see:

E. S. Swanson, Cusps and Exotic Charmonia, arXiv:1504.07952 [hep-ph]

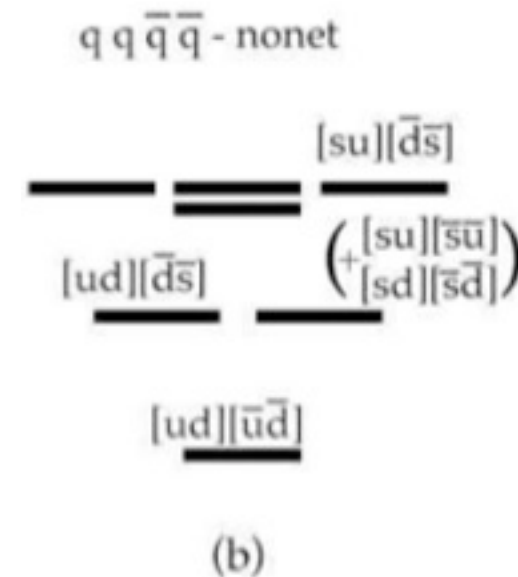
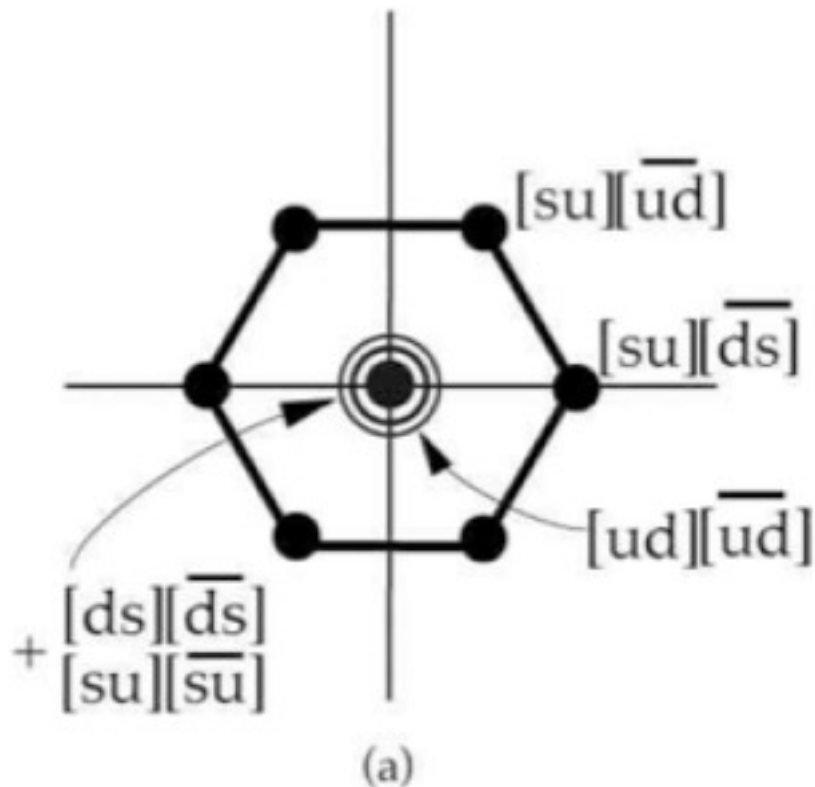
I think it takes a lot of unconventional dynamics to produce the X(3872) as a “cusp”

Also, the phase of Z(4430) seems to go at 90^0 at the peak, like a well-behaved Breit-Wigner resonance...

2. The octet of light scalar mesons and diquarks



Antisymmetric tetraquarks work better



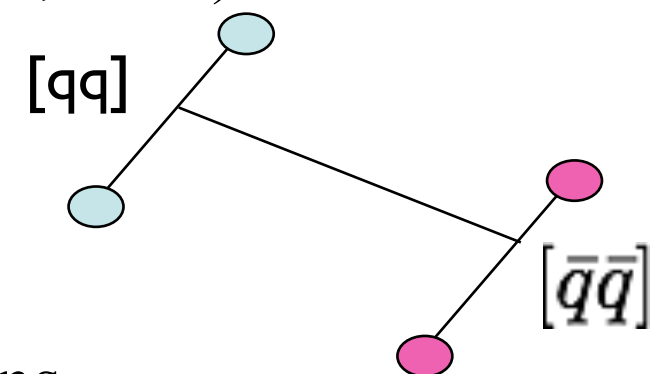
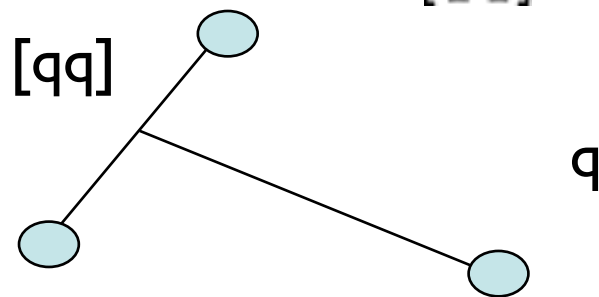
Diquarks vs molecules

QCD attractive in 1 gluon approx. for diquark $[qq']$: color = $3\bar{b}$,
 SU(3) flavour = $3\bar{b}$, spin=0, spin-spin force also attractive: *good diquark* (Jaffe, 1977)
 - makes a simple unit to form color singlets (Jaffe & Wilcezc, 2003)
 - $[cq]$ may make a stable configuration even for spin 1, *bad diquark*, since spin-spin interactions, repulsive in spin 1, decrease with mass)

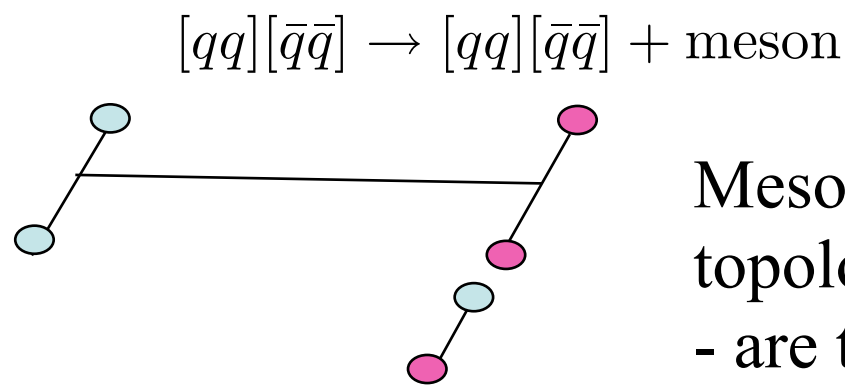
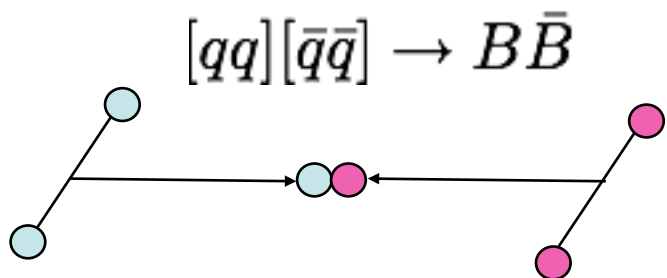
Diquark needs to combine with other colored objects:

with $q \rightarrow$ baryon (e.g. Λ), Y-shape

with $[\bar{q}\bar{q}] \rightarrow$ scalar meson, H-shape (Rossi&Veneziano, 1980)



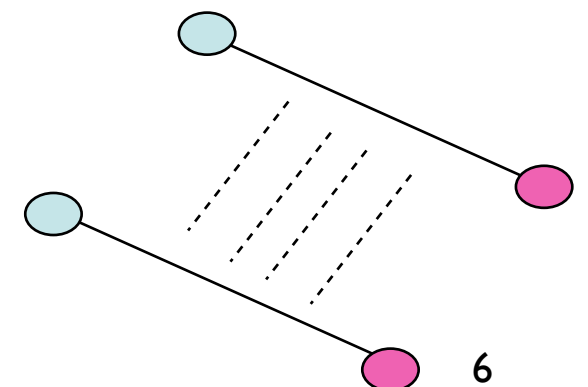
Many states: tetraquarks may have radial and orbital excitations
 string topology is more related to Baryon-antiBaryon:
 if you break the string,



A. De Rujula, H. Georgi and S. L. Glashow,
 Phys. Rev. Lett. 38 (1977) 317.

Meson-meson molecules have a different string topology:

- are they bound?
- very few states



X(3872) production @ LHC

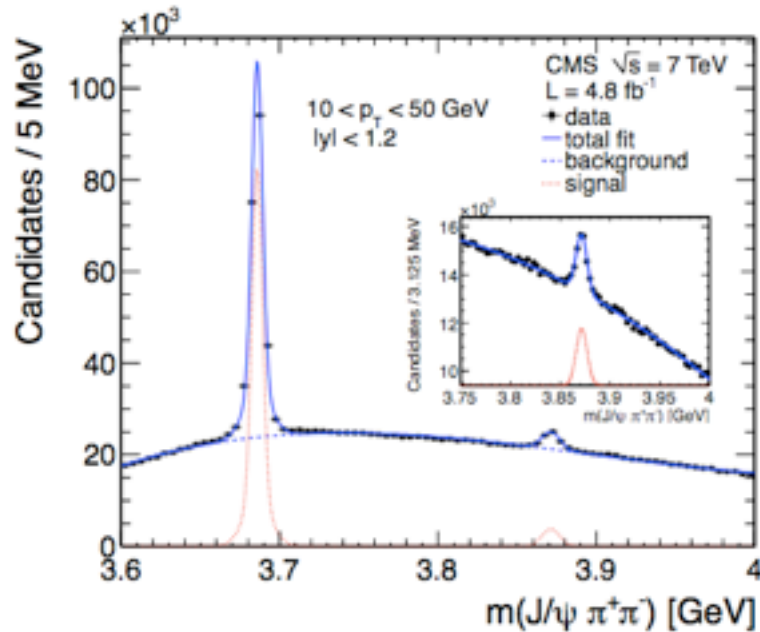
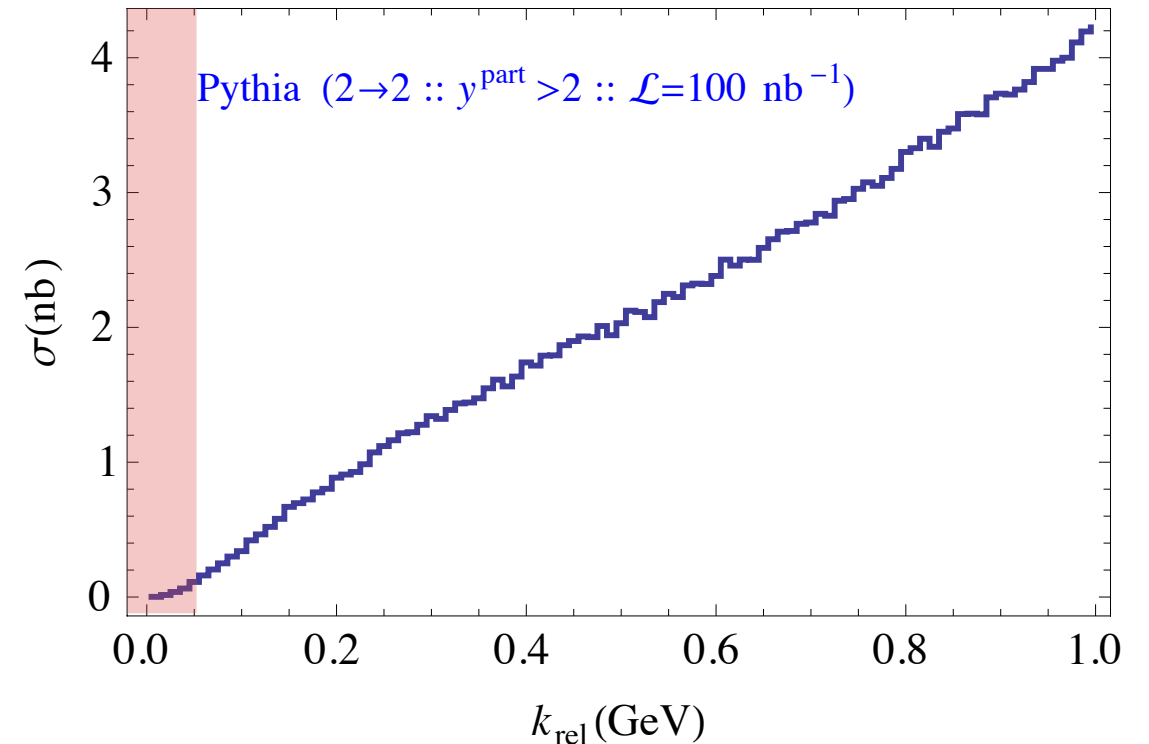
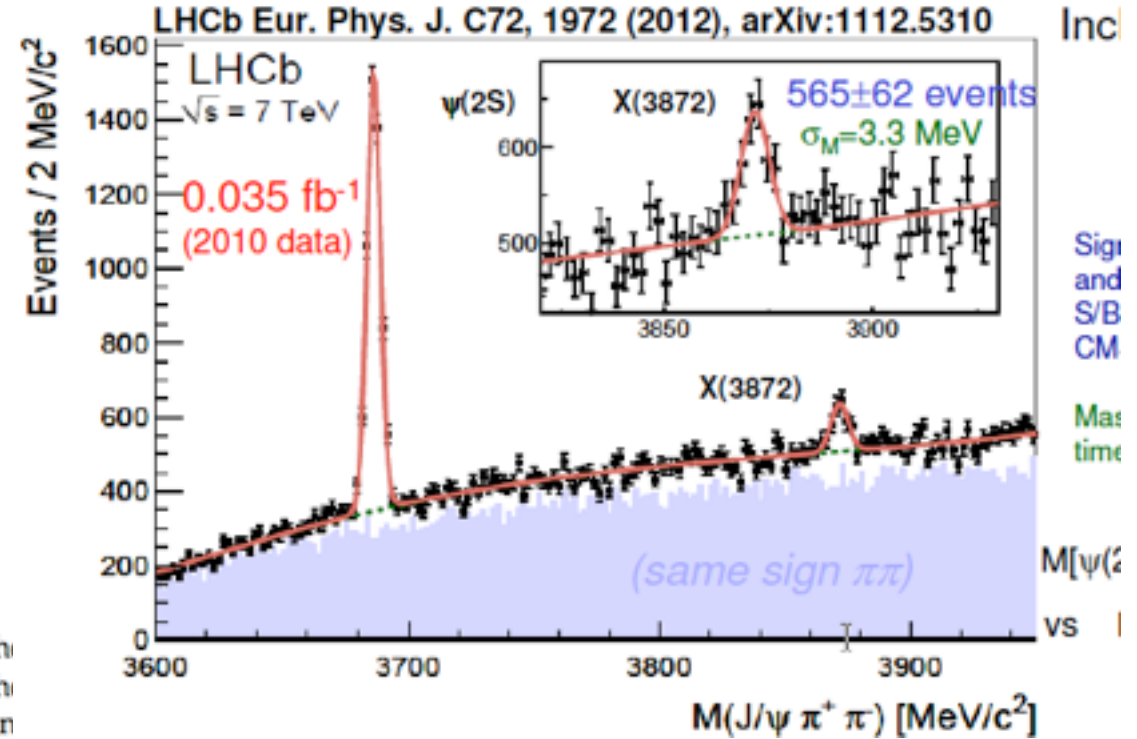


Figure 1: The $J/\psi\pi^+\pi^-$ invariant-mass spectrum for $10 < p_T < 50$ GeV and $|y| < 1.2$. The lines represent the signal-plus-background fits (solid), the background-only (dashed), and the signal-only (dotted) components. The inset shows an enlargement of the X(3872) mass region

- Production at Colliders speaks against extended objects;
- using Pythia to estimate the probability to find a D-Dbar pair in the relevant phase space, factors of 10^{-2} are found with respect to the X(3872) cross section measured by CDF (~ 30 nb).



3. Conventional and less conventional Quarkonia

- The accuracy with which the spectra of $Q\bar{Q}$ states ($Q=c, b$) are predicted and measured makes it possible to discover new states “by difference”
- Terminology of $Q\bar{Q}$ states in S and P wave:

spin = S , orb. ang. mom. = L , tot. ang. mom. = J : $2S+1 L_J$

radial excitation = n

$\eta_c(1S) = {}^1S_0$; $J/\Psi(1S) = {}^3S_1$

$h_c(1P) = {}^1P_1$, $\chi_c(1P) = {}^3P_J$

Particle Data Group:

S. Eidelman et al., DEVELOPMENTS IN HEAVY QUARKONIUM SPECTROSCOPY

Updated March 2014;

Quarkonium Working Group:

N. Brambilla et al., arXiv:1404.3723v1 [hep-ph] 14 Apr 2014

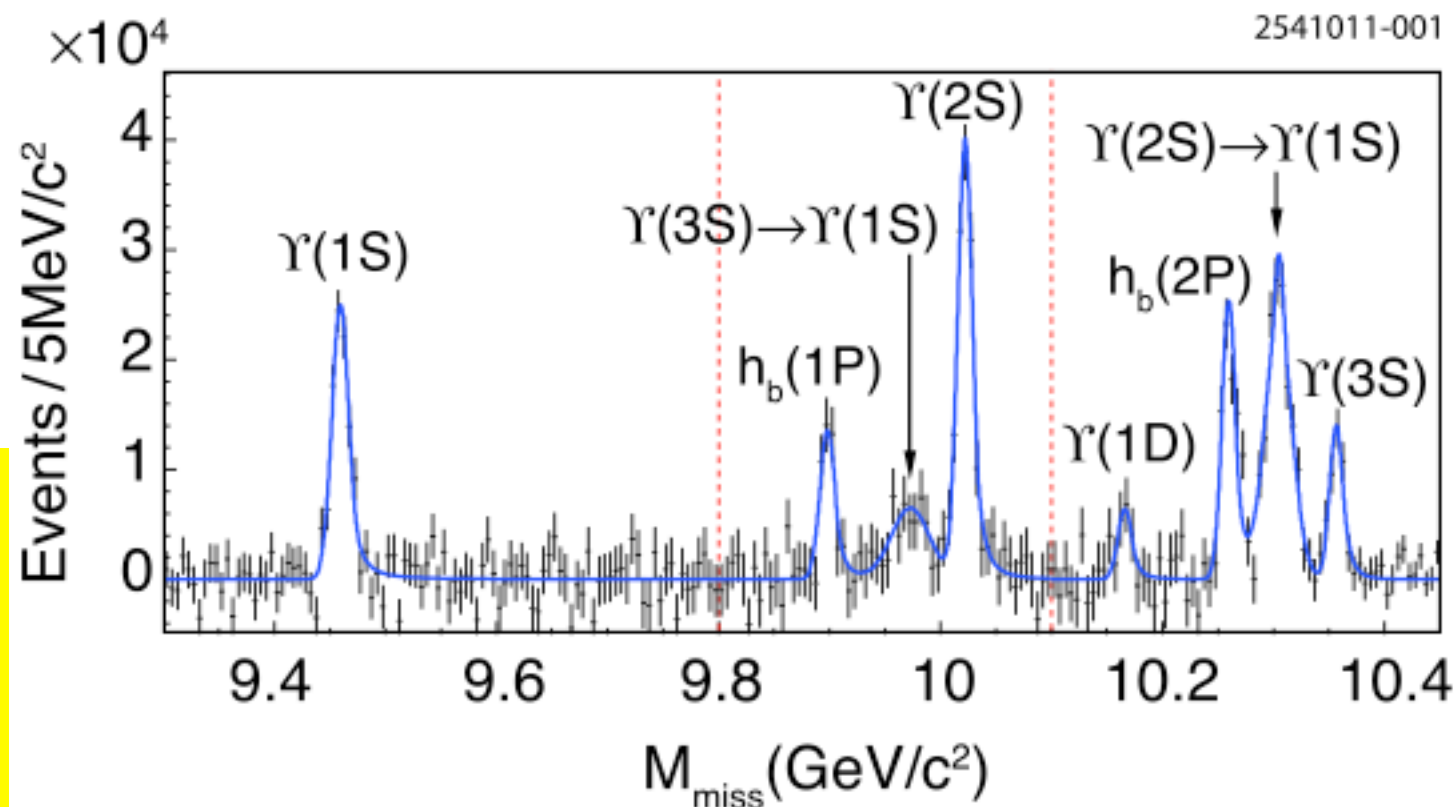
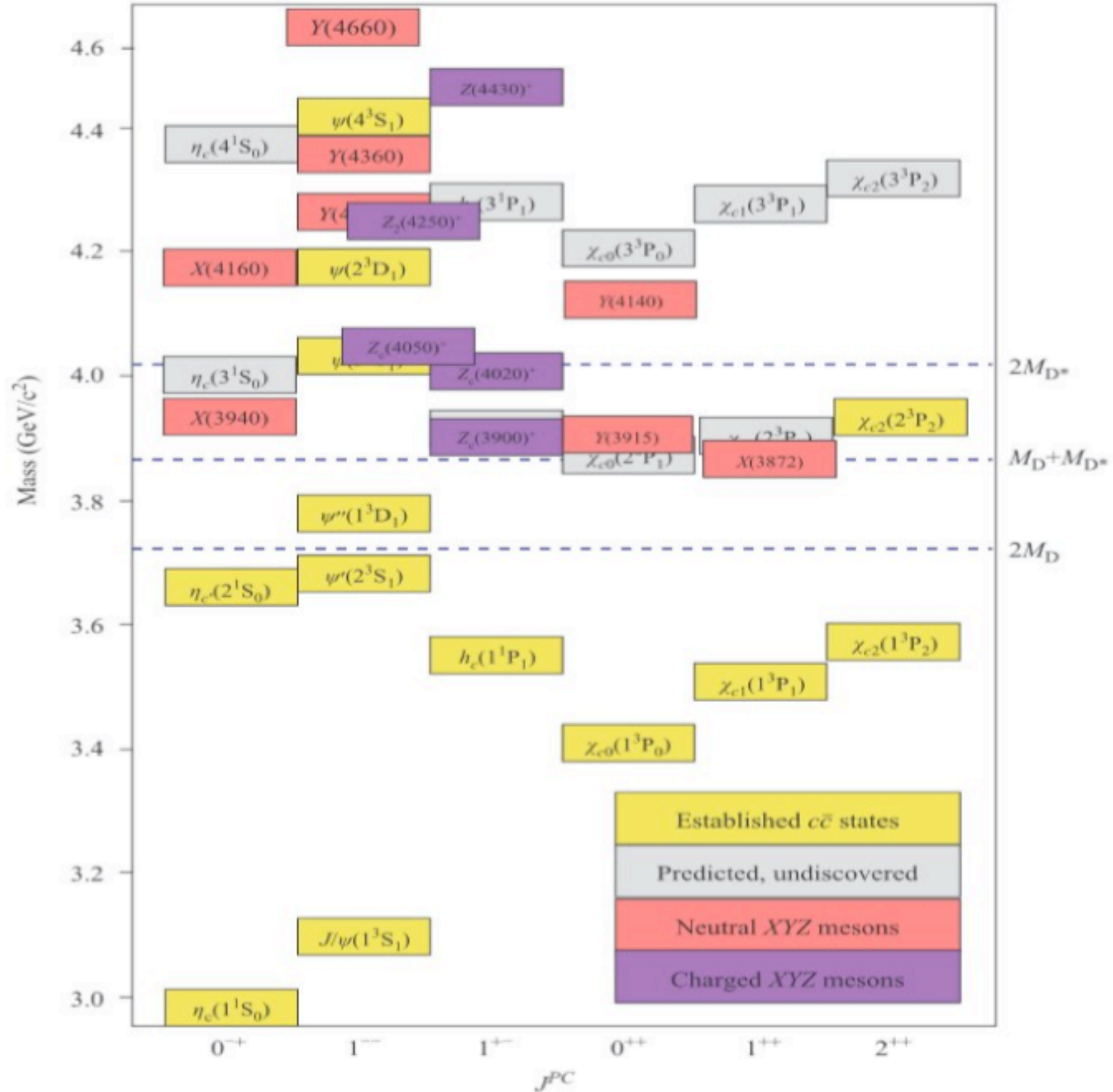


Figure 1: From Belle [31], the mass recoiling against $\pi^+\pi^-$ pairs, M_{miss} , in e^+e^- collision

Charmonia and Charmonium-like Hadrons (Olsen, arxiv:1411.7738)

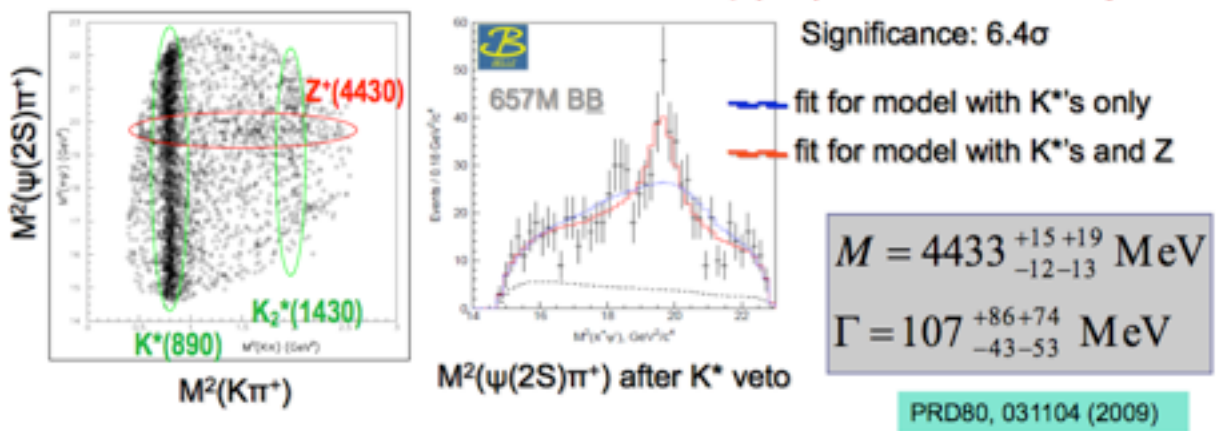


terminology of unanticipated charmonia

- X, e.g. X(3872): neutral, typically seen in J/Psi+pions, positive parity, $J^{PC}=0^{++}, 1^{++}, 2^{++}$
- Y, e.g. Y(4260): neutral, seen in e^+e^- annihilation with Initial State Radiation, therefore $J^{PC}=1^{--}$
- Z, eg. Z(4430): charged/neutral, typically positive parity, mostly seen in J/Psi+pion and some in $h_c(1P) + \text{pion}$

- Found in $\psi(2S)\pi^+$ from $B \rightarrow \psi(2S)\pi^+K$. Z parameters from fit to $M(\psi(2S)\pi^+)$
- Confirmed through Dalitz-plot analysis of $B \rightarrow \psi(2S)\pi^+K$
- $B \rightarrow \psi(2S)\pi^+K$ amplitude: coherent sum of Breit-Wigner contributions
- Models: all known $K^* \rightarrow K\pi^+$ resonances only**

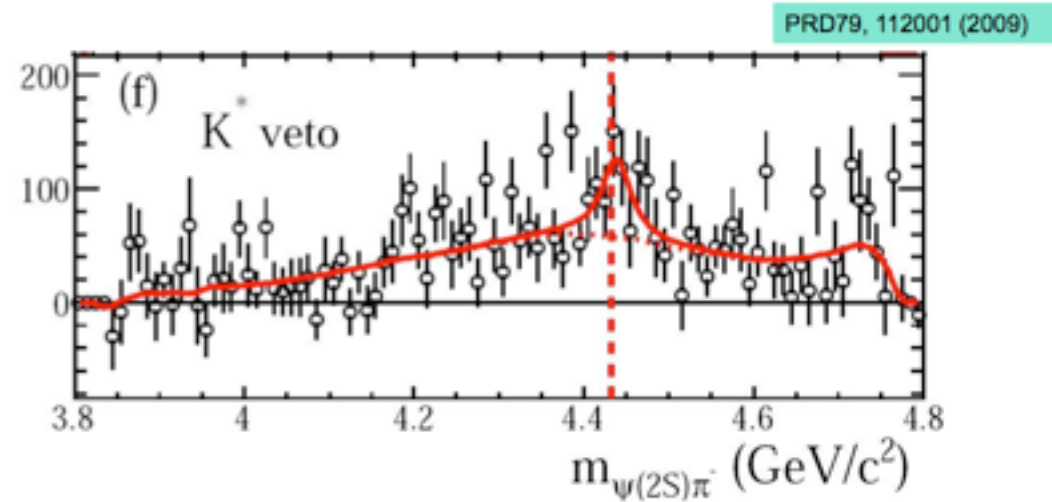
all known $K^* \rightarrow K\pi^+$ and $Z^+ \rightarrow \psi(2S)\pi^+ \Rightarrow$ favored by data



- [cu][cd] tetraquark? neutral partner in $\psi'\pi^0$ expected**
- $D^*D_1(2420)$ molecule? should decay to $D^*D^*\pi$**



BaBar doesn't see a significant $Z(4430)^+$



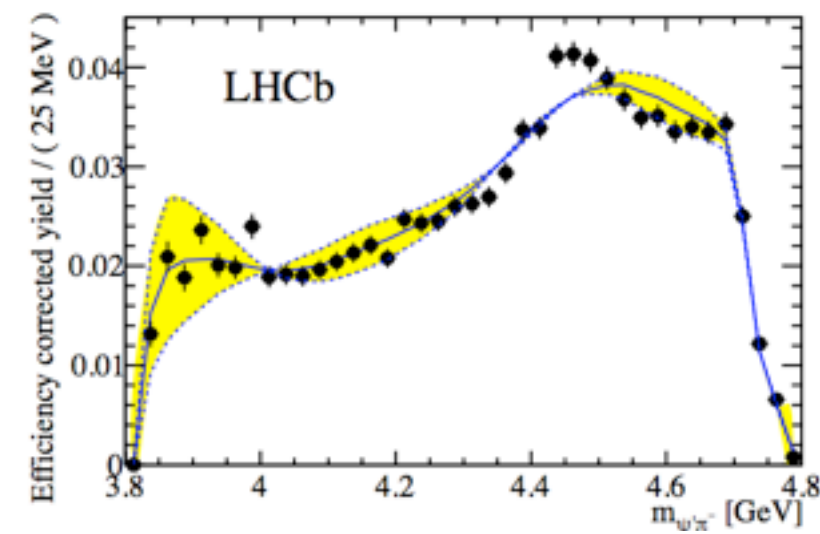
"For the fit ... equivalent to the Belle analysis...we obtain mass & width values that are consistent with theirs,... but only $\sim 1.9\sigma$ from zero; fixing mass and width increases this to only $\sim 3.1\sigma$."

$BF(B^0 \rightarrow Z^+K) \times BF(Z^+ \rightarrow \psi(2S)\pi^+) < 3.1 \times 10^{-5}$

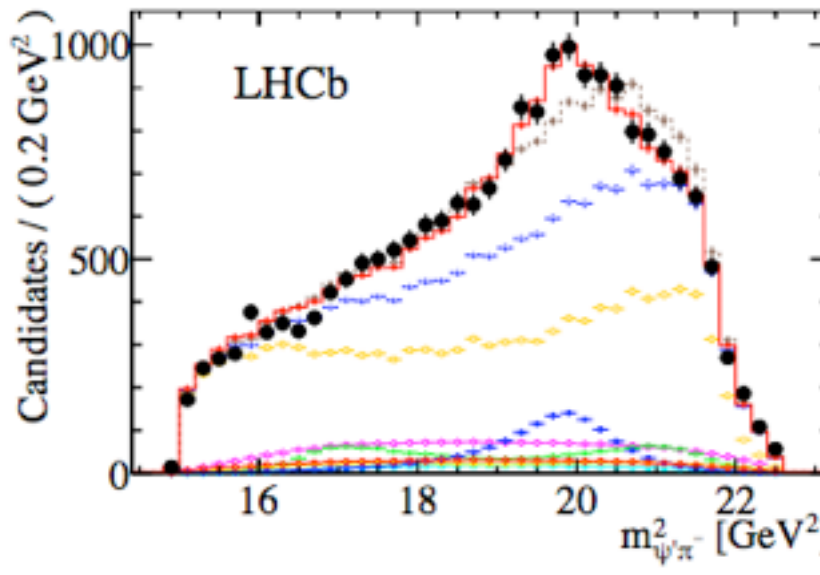
Belle PRL: $(4.1 \pm 1.0 \pm 1.4) \times 10^{-5}$

- Babar inserts in the fit all K^* resonances
- is Belle effect due to K^* reflections ???

4. The $Z^\pm(4430)$ saga



no Z



with Z

- $D^*D_1 =$ in S-Wave: may have $J=1$ but has negative parity
- Argand Plot shows 90° phase: Z is a genuine resonance

Z(4430) as a radially excited tetraquark

- There *are* 4 quarks in Z(4430)
- in 2007 we classified the Z(4430) as a tetraquark, the radial excitation of the S-wave companion of X(3872)
- this was because of its decay into $\psi(2S)^+ \pi$ and its mass ~ 550 MeV larger than the X
- We noted then: *A crucial consequence of a Z(4430) charged particle is that a charged state decaying into $\psi(1S) \pi^\pm$ or $\eta_c \rho^\pm$ should be found around 3880 MeV (i.e. almost degenerate with X(3872))*
- The $Z_c(3900)$ has been seen later by BES III and Belle with the anticipated decay:
 - $Z^+(3900) \rightarrow \psi(1S) \pi^+$
- a neutral partner was suggested by CLEO,
- The further observation of Z(4020) by the BES III Collaboration reinforces the tetraquark picture, which looks more attractive and constrained as compared to some years ago
- The Z(4430) decay into $\psi(2S)$ as indication of a radially excited tetraquark has been confirmed by S. Brodski *et al.* (arXiv:1406.7281 [hep-ph])

Radial excitations

Spacing of radial excitations are the same in Charmonia and Bottomonia;

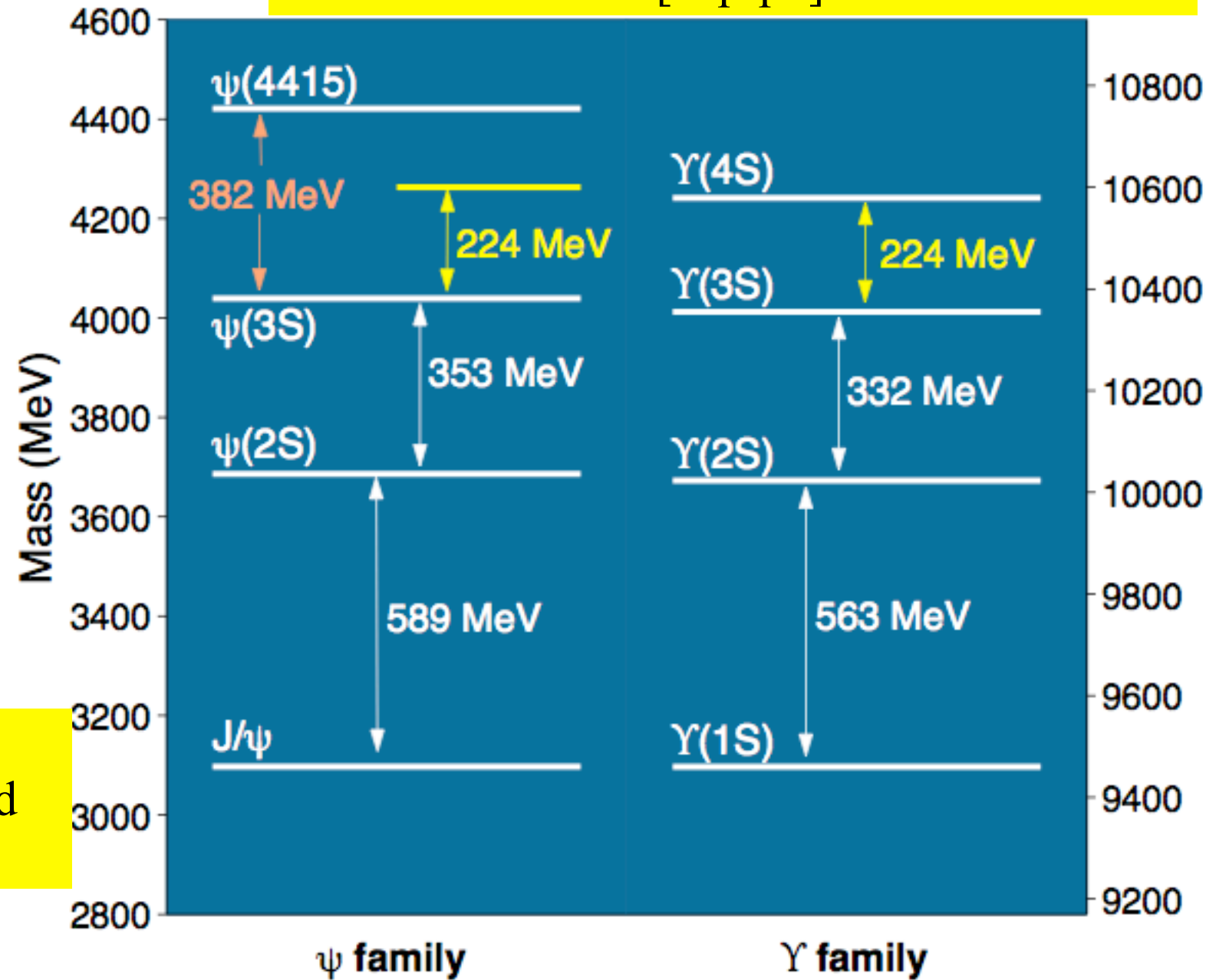
- gap between 1P-2P states is smaller :

$$\chi_{bJ}(2P) - \chi_{bJ}(1P) \approx 360 \text{ MeV}$$

$$\chi_{cJ}(2P) - \chi_{cJ}(1P) \approx 437 \text{ MeV}$$

Is a diquark-antidiquark pair similar to a quark-antiquark pair? a very tightly bound diquark?

L.-P. He, D.-Y. Chen, X. Liu and T. Matsuki
arXiv:1405.3831 [hep-ph].



5. Tetraquarks in the large N expansion

- Reputation of tetraquarks was somehow tarnished by a theorem of S. Coleman: *tetraquarks correlators for $N \rightarrow \infty$ reduce to disconnected meson-meson propagators*

S. Coleman, *Aspects of Symmetry* (Cambridge University Press, Cambridge, England, (1985), pp. 377–378

- The argument was reexamined by S. Weinberg who argued that if the connected tetraquark correlator develops a pole, it will be irrelevant that it is of order $1/N$ with respect to the disconnected part: *at the pole the connected part will dominate anyhow;*

S. Weinberg, PRL 110, 261601 (2013)

- the real issue is the width of the tetraquark pole: it may increase for large N, to the point of making the state undetectable;
- Weinberg's conclusion is that the decay rate goes like $1/N$, making tetraquarks a respectable possibility.
- Weinberg's discussion has been enlarged by M. Knecht and S. Peris (arXiv:1307.1273) and further considered by T. Cohen and R. Lebed et al. (arXiv: 1401.1815, arXiv: 1403.8090).

What is not forbidden is NECESSARY

Decay amplitudes in 1/N expansion

- By Fierz rearrangements, tetraquark operators can be reduced to products of color singlet bilinears;
- interpolating field operators have to be multiplied by powers of N, such as to make the connected two-point correlators to be normalized to unity;
- one loop amplitude with insertions of quark color singlet operators gives a factor N.

$$Q = \frac{1}{\sqrt{N}} [cu][\bar{c}\bar{u}] \left\{ \begin{array}{l} \frac{1}{\sqrt{N}} (\bar{u}c) (D, D^*) \\ \frac{1}{\sqrt{N}} (\bar{c}u) (\bar{D}, \bar{D}^*) \\ + (c \leftrightarrow u) \\ \frac{1}{\sqrt{N}} (\bar{c}c) (\eta_c, J/\Psi, \chi_c, h_c, \dots) \\ \frac{1}{\sqrt{N}} (\bar{u}u) (\pi, \eta, \rho, \omega, \dots) \end{array} \right. \quad \bullet \text{ two independent amplitudes}$$

- The result is that *decay amplitudes into two mesons are of order:* $\frac{1}{N^{3/2}} N = \frac{1}{\sqrt{N}}$
- These two amplitudes were introduced long ago for tetraquark light scalar decay: reassuringly, they turn out both to be leading in 1/N.

L. Maiani, F. Piccinini, A. D. Polosa, V. Riquer, PRL **B93**, 212002 (2004)

further decay amplitudes

- tetraquark de-excitation amplitudes by meson emission, e.g. $Y(4260) \rightarrow Z_c(3900) + \pi$, are also of order $1/\sqrt{N}$

$$Y(4260) = \frac{1}{\sqrt{N}} [cu][\bar{c}\bar{u}] \left\{ \begin{array}{l} \bar{c}u \\ \bar{u}c \end{array} \right. \left. \begin{array}{l} u \\ u \end{array} \right\} \left\{ \begin{array}{l} \bar{u}c \\ \bar{c}d \\ \bar{d}u \end{array} \right. \left. \begin{array}{l} c \\ d \end{array} \right\}$$

$$Z_c^-(3900) = \frac{1}{\sqrt{N}} [cd][\bar{c}\bar{u}]$$

$$\pi^+ = \frac{1}{\sqrt{N}} (u\bar{d})$$

- however, e.m. currents need no normalization factor, so that the de-excitation amplitudes via photon emission are of order $eQ \times 1$.

$$Y(4260) = \frac{1}{\sqrt{N}} [cu][\bar{c}\bar{u}] \left\{ \begin{array}{l} \bar{c}u \\ \bar{u}c \end{array} \right. \left. \begin{array}{l} u \\ u \end{array} \right\} \left\{ \begin{array}{l} \bar{u}c \\ \bar{c}u \end{array} \right. \left. \begin{array}{l} c \\ u \end{array} \right\}$$

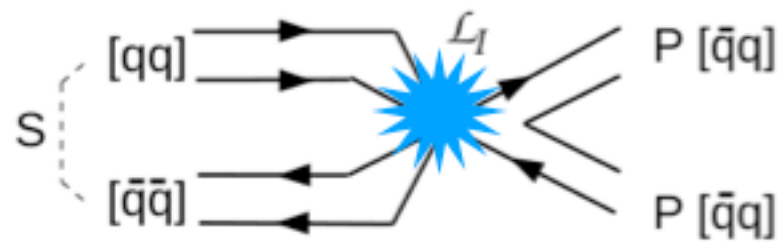
$$X(3872) = \frac{1}{\sqrt{N}} [cu][\bar{c}\bar{u}]$$

$$eQ \quad \gamma$$

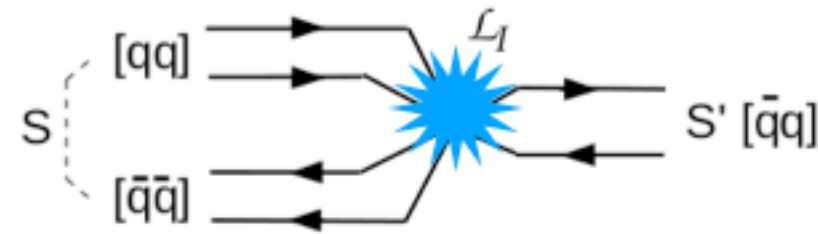
Non-perturbative instantons: may explain two or three further puzzles

G. 't Hooft, G. Isidori, L. Maiani, A. D. Polosa and V. Riquer, PL **B662** (2008) 424.

A. H. Fariborz, R. Jora and J. Schechter, PR **D77** (2008) 094004.



(a)



(b)

- (a) the decay $f_0(980) \rightarrow 2\pi$ ($f_0 = \frac{([su][\bar{s}\bar{u}] + u \rightarrow d)}{\sqrt{2}}$)
- (b) the mixing of light (tetraquark) scalar mesons with q - q bar mesons, the latter being made by $a_0(1474)$ ($I=1$), $K_0(1412)$, ($I=1/2$), and three isosinglets: $f_0(1370)$, $f_0(1507)$ and $f_0(1714)$ (one could be a glueball);
- (c)= (b) in the reverse:

- with: $Y(4260) = \frac{([cu][\bar{c}\bar{u}] + u \rightarrow d)}{\sqrt{2}}$, the u - u bar or d - d bar pair in Y may give rise to the observed decay:

$$Y(4260) \rightarrow J/\Psi + f_0(q\bar{q})_{off-shell} \rightarrow J/\Psi + f_0([qq][\bar{q}\bar{q}])$$

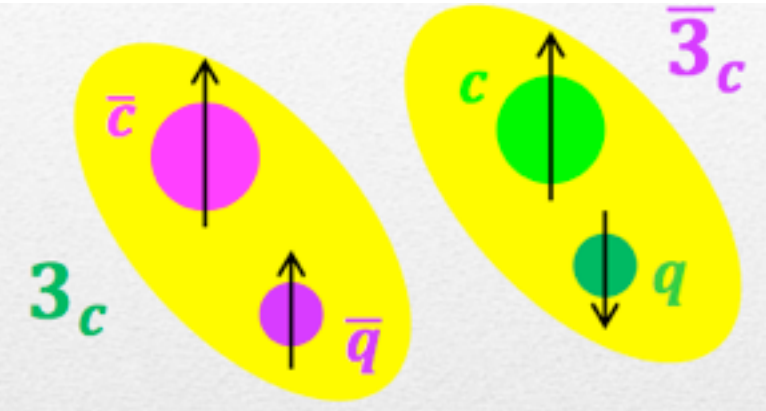
Selection rules

- Conservation of the heavy quark spin is well established in QCD: decays indicate the value of c-cbar spin in the initial wave function:
 - X(3872): $S(c\text{-cbar})=1 \rightarrow J/\Psi$ yes, but no η_c
 - Y(4230): both χ_c ($S(c\text{-cbar})=1$) and h_c ($S(c\text{-cbar})=0$)
- conservation of light quark spin is not reliable:
 - initial spin composition not necessarily reflected in $K K^*$ vs $K^* K^*$ decay modes
- observed X, Y, Z in the new paradigm of spin-spin coupling respect these rules, as far as we can see !
- more precise measurements of different decay channel will be of the utmost importance.

6. Tetraquark picture of unexpected quarkonia

L.Maiani, F.Piccinini, A.D.Polosa and V.Riquer, Phys. Rev. D 71 (2005) 014028

$$[cQ]_{s=0,1} [\bar{c}\bar{q}']_{\bar{s}=0,1}$$



- $I=1, 0$
- S-wave: positive parity
- total spin of each diquark, $S=1, 0$
- neutral states may be mixtures of isotriplet and isosinglet
- mass splitting due to spin-spin interactions (e.g. the non-relativistic constituent quark model)

$$H = 2M_{diquark} - 2 \sum_{i<j} \kappa_{ij} (\vec{s}_i \cdot \vec{s}_j) \frac{\lambda_i^A}{2} \frac{\lambda_j^A}{2}$$

The S-wave, $J^P=1^+$ charmonium tetraquarks

- use the basis $|s, \bar{s}\rangle_J$

$$J^P = 0^+ \quad C = + \quad X_0 = |0, 0\rangle_0, \quad X'_0 = |1, 1\rangle_0$$

$$J^P = 1^+ \quad C = + \quad X_1 = \frac{1}{\sqrt{2}} (|1, 0\rangle_1 + |0, 1\rangle_1)$$

$$J^P = 1^+ \quad C = + \quad Z = \frac{1}{\sqrt{2}} (|1, 0\rangle_1 - |0, 1\rangle_1), \quad Z' = |1, 1\rangle_1$$

$$J^P = 2^+ \quad C = + \quad X_2 = |1, 1\rangle_2$$

$$X(3872)=X_1$$

Z(3900), Z(4020)=lin. combs. of Z&Z' that diagonalize H

$$X(3940)=X_2 ??$$

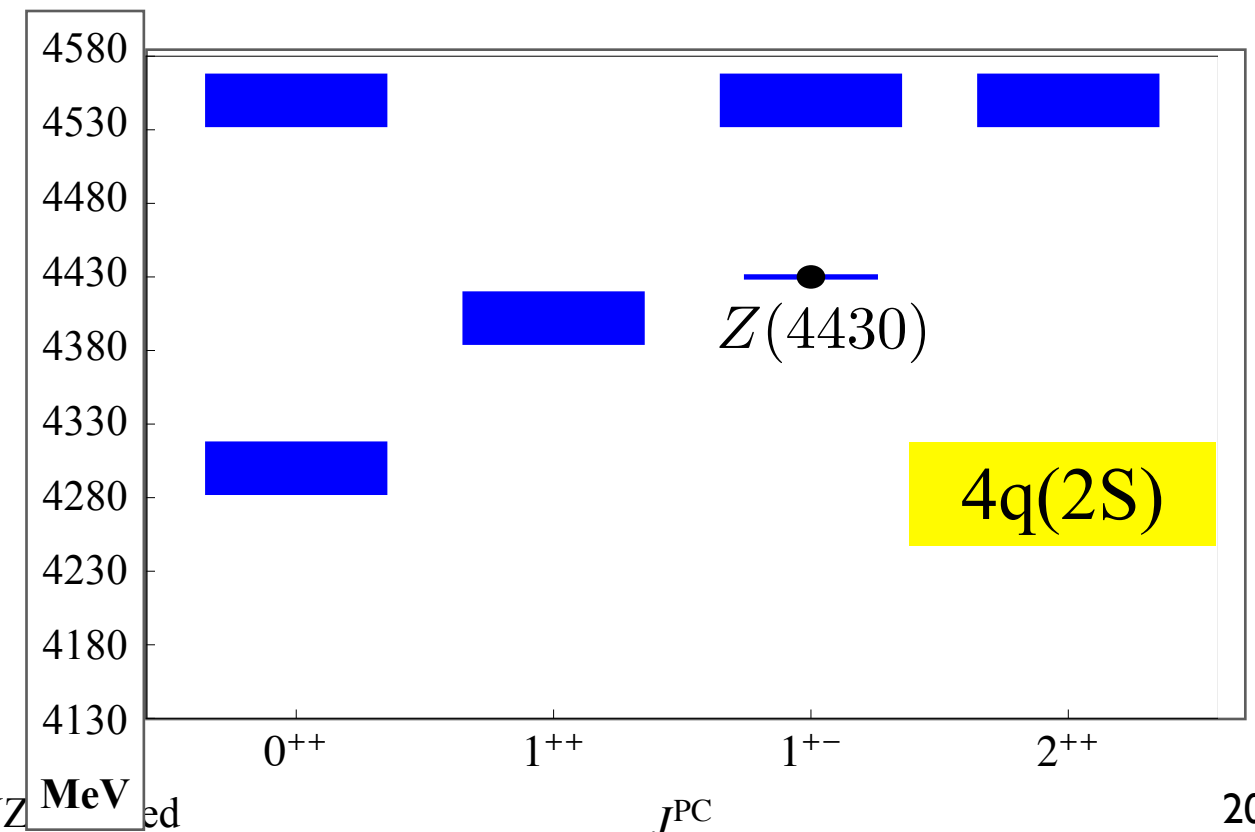
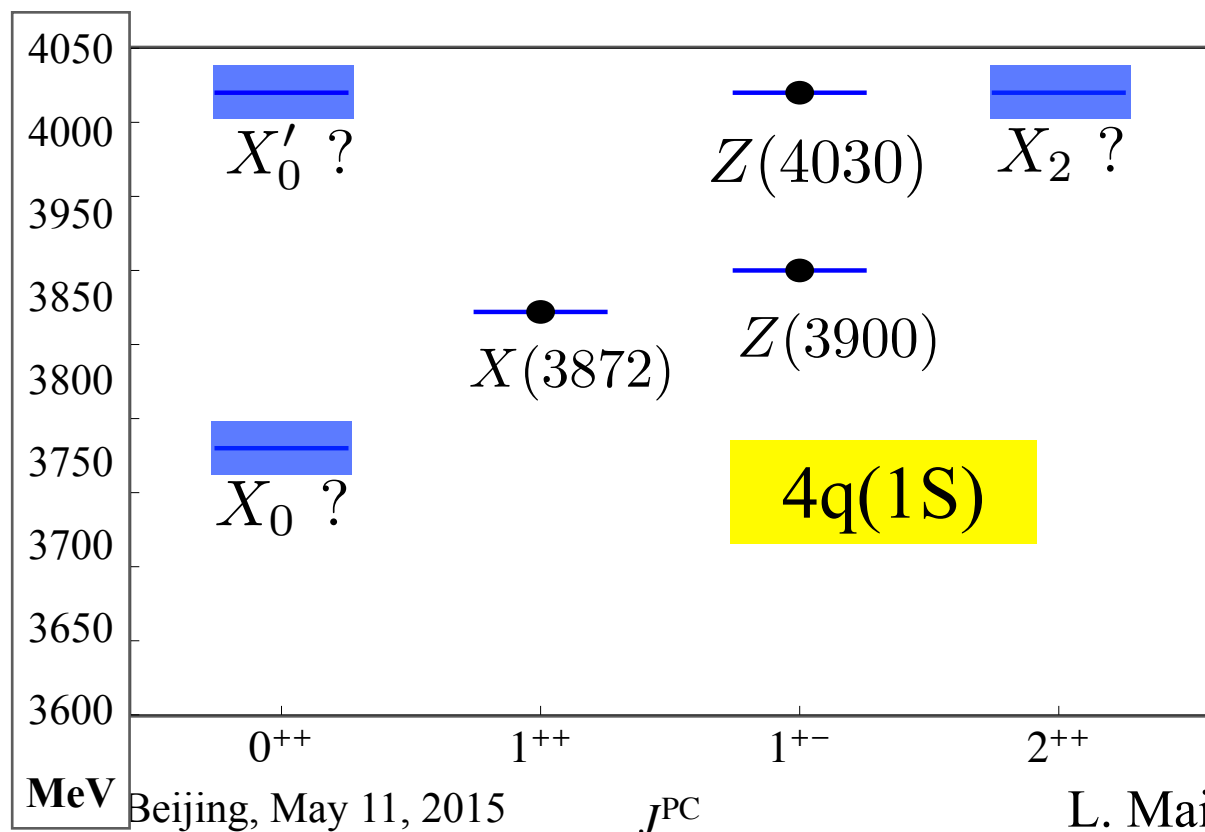
Mass spectrum: the new paradigm

A. Polosa, V. Riquer, F. Piccinini, PRD **89**, 114010 (2014)

- A tentative mass spectrum for the S-wave tetraquarks was derived in the 2005 paper, based on an extrapolation of the spin-spin interactions in conventional S-wave mesons and baryons.
- Does NOT agree with the observed level ordering of X(3872), Z(3900) and Z(4020)
- A new, simple paradigm accounts for the observed pattern: dominant interactions are those *between quarks in the same (tightly bound?) diquark* (or antiquarks in the same antidiquark):

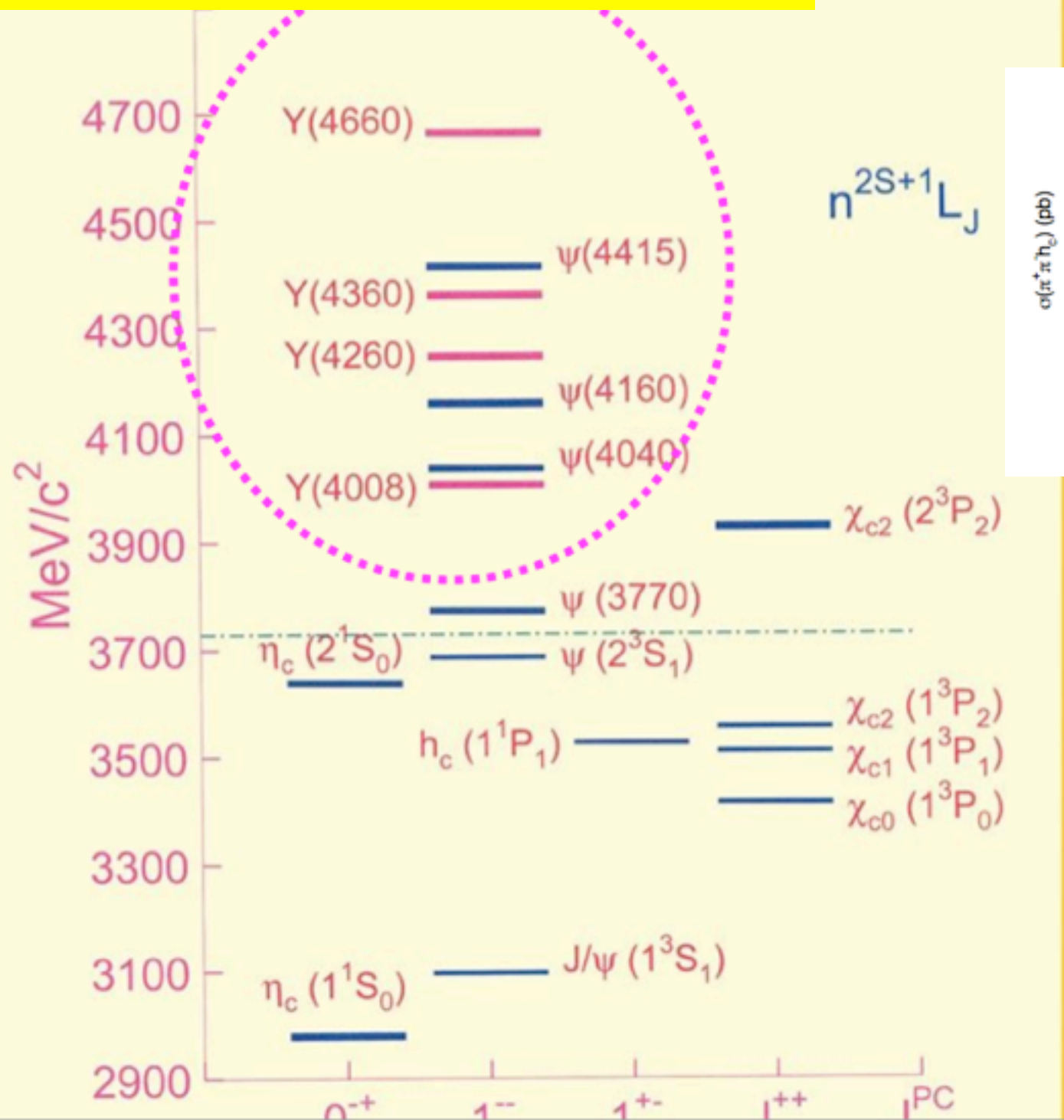
$$H \approx 2\kappa_{qc} (s_q \cdot s_c + s_{\bar{q}} \cdot s_{\bar{c}}) = \kappa_{qc} [s(s+1) + \bar{s}(\bar{s}+1) - 3]$$

- H is diagonal in the basis of diquark total spin and counts the number of spin=1 diquarks
- one Z is degenerate with X(3872), the other is heavier;
- $\kappa_{qc} \sim 60$ MeV from fit (larger than κ_{qc} in baryons).

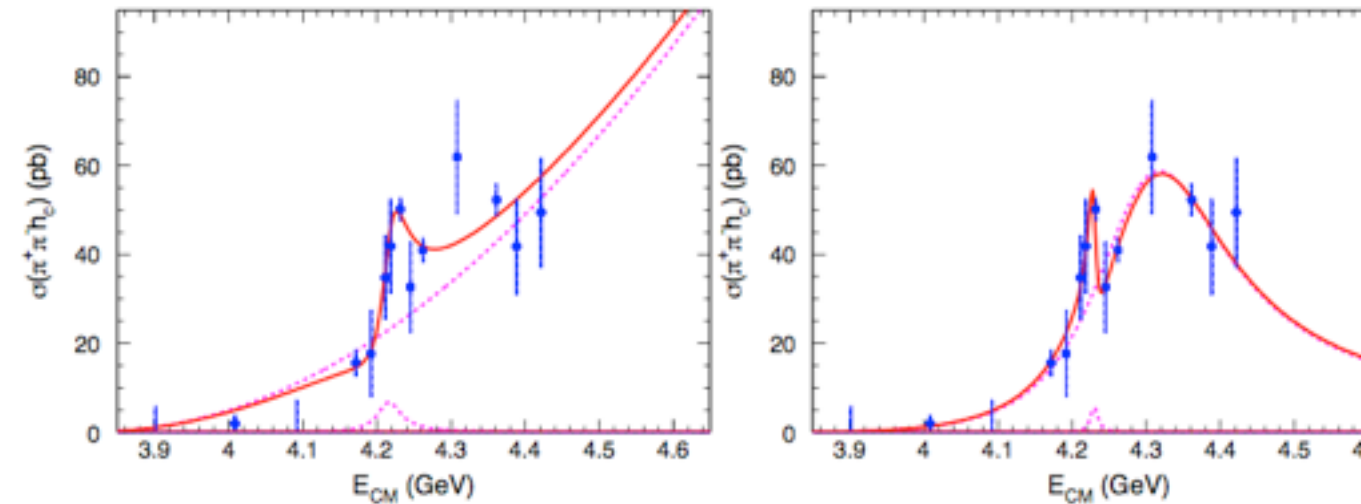


7. What are the Y states?

Changzheng YUAN, IHEP Beijing, 2014



later BES III has observed another one: Y(4230) which decays in $h_c \pi \pi$



or maybe two? (narrow and wide)

Our survey:

- Y(4660) and Y(4360), decaying into $\psi(2S)\pi$
- Y(4630) decaying into $\Lambda_c \bar{\Lambda}_c$
- Y(4220), narrow (and Y(4290), wide ???) in $h_c(1P) + \pi$, BES III
- Y(4260) and Y(4008) decaying into $J/\psi + \pi$,

Y- tetraquarks

- Tetraquark states with $J^{PC}=1^-$ can be obtained with odd values of the orbital angular momentum $L=1, 3$ and diquark and antidiquark spins $s, \bar{s}=0, 1$.
- use the notation: $|s, \bar{s}; S, L\rangle_{J=1}$, and charge conjugation invariance we get four states with $L=1$:

| | spin composition: $ s, \bar{s}, S, L\rangle_J$ | $P(s_{c\bar{c}} = 1)$ | $P(s_{c\bar{c}} = 0)$ | assign. |
|-------|---|-----------------------|-----------------------|-----------|
| Y_1 | $ 0, 0; 0, 1\rangle_1$ | 0.75 | 0.25 | $Y(4008)$ |
| Y_2 | $\frac{1}{\sqrt{2}}(1, 0; 1, 1\rangle_1 + 0, 1; 1, 1\rangle_1)$ | 1 | 0 | $Y(4260)$ |
| Y_3 | $ 1, 1; 0, 1\rangle_1$ | 0.25 | 0.75 | $Y(4230)$ |
| Y_4 | $ 1, 1; 2, 1\rangle_1$ | 1 | 0 | $Y(4630)$ |

Interpretation of Y states:

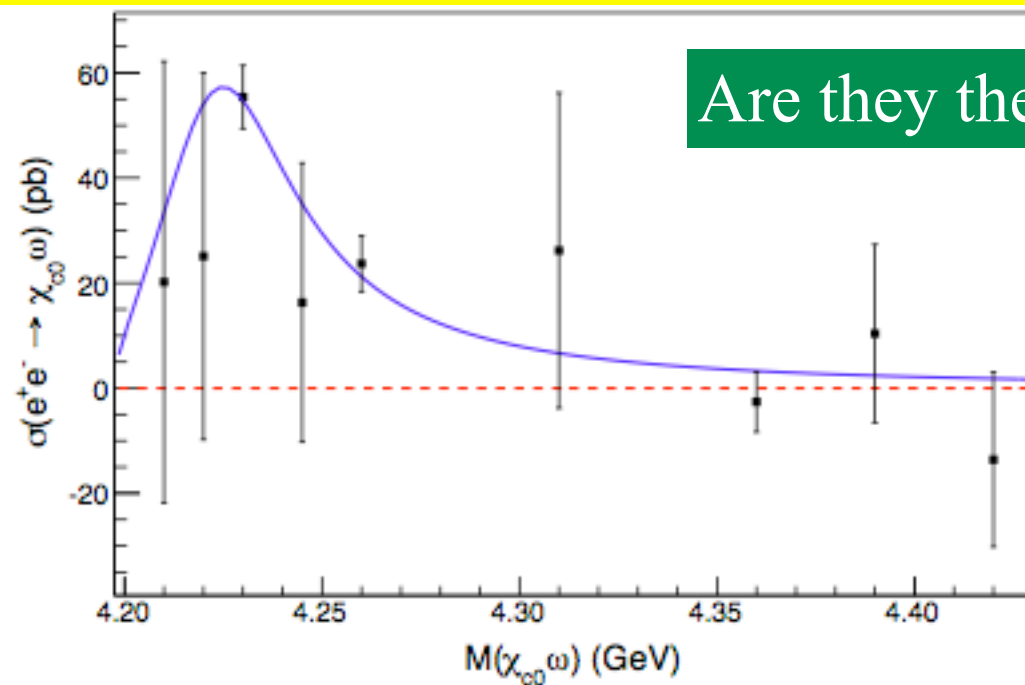
- leave aside the $L = 3$ state (too heavy);
- $Y(4360)$ and $Y(4660)$ = radial excitations of $Y(4008)$ and $Y(4260)$ (decay into $\psi(2S)$, $\Delta M \sim 350, 400$ MeV in the range of ΔM of $L = 1$ charmonia and bottomonia);
- the 4 states Y_{1-4} identified with $Y(4008)$, $Y(4260)$, $Y(4220)$ (the narrow structure in the h_c channel) and $Y(4630)$.

Y states, decay patterns and very tentative assignments

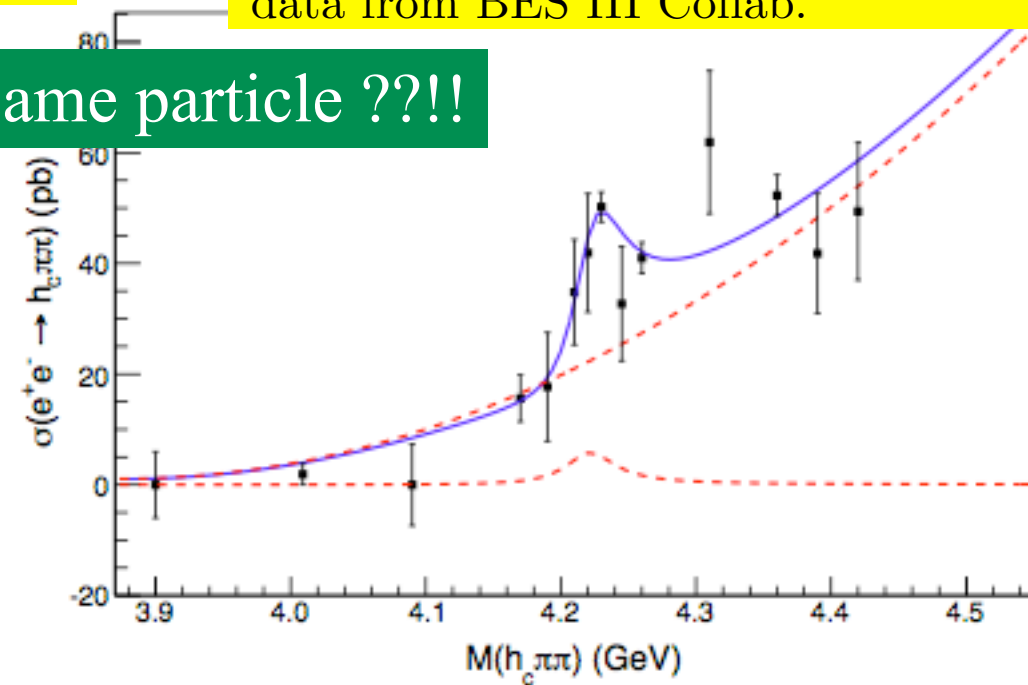
| | $J/\Psi + \pi\pi$ | $\psi(2S) + \pi\pi$ | $h_c + \pi\pi$ | $\chi_{c0} + \omega$ | $\Lambda_c + \bar{\Lambda}_c$ | | $P(S_{c\bar{c}}=1)$ | $P(S_{c\bar{c}}=0)$ |
|----------------|-------------------|---------------------|----------------|----------------------|-------------------------------|--------|---------------------|---------------------|
| $S_{c\bar{c}}$ | 1 | 1 | 0 | 1 | 1 | | | |
| Y(4008) | seen | - | - | - | - | Y_1 | 0.75 | 0.25 |
| Y(4230) | - | - | seen | seen | - | Y_3 | 0.25 | 0.75 |
| Y(4260) | seen | - | - | - | - | Y_2 | 1 | 0 |
| Y(4360) | - | seen | - | - | - | Y'_1 | 1 | 0 |
| Y(4630) | - | - | - | - | seen | Y_4 | 1 | 0 |
| Y(4660) | - | seen | - | - | - | Y'_2 | 1 | 0 |

M. Ablikim *et al.* [BESIII Collaboration], arXiv:1410.6538 [hep-ex].

C. Z. Yuan, Chin. Phys. C **38** (2014) 043001
data from BES III Collab.



$$Y(4230) \rightarrow \chi_c + \omega$$



$$Y(4230) \rightarrow h_c + \pi^+ + \pi^-$$

Are they the same particle ???!

Y(4230) has $S_{c\bar{c}} = 1$ and $S_{c\bar{c}} = 0$ decays, as required by Y_3

Radiative decays

- The identical spin structure implied in the model for $Y(4260)$ and $X(3872)$ suggests the decay

$$Y(4260) \rightarrow X(3872) + \gamma$$

M.Ablikim et al. [BESIII Collaboration], arXiv:1310.4101 [hep-ex]

to be an *unsuppressed E_1 transition*, with $\Delta L=1$ and $\Delta \text{Spin}=0$, similar to the observed transitions of charmonium χ states.

- The decay rate could provide a first estimate of the radius of the tetraquark.
- A comparison of the spin structures in Y and X states provides selection rules for E_1 transitions that should provide a better identification of the levels.
- The assignments we have made produce the table:

$$Y_4 = Y(4630) \rightarrow \gamma + X_2 \quad (J^{PC} = 2^{++}) = \gamma + X(3940), \quad ??$$

$$Y_3 = Y(4220) \rightarrow \gamma + X'_0 \quad (J^{PC} = 0^{++}) = \gamma + X(3916), \quad ??$$

$$Y_2 = Y(4260) \rightarrow \gamma + X_1 \quad (J^{PC} = 1^{++}) = \gamma + X(3872), \quad \text{seen}$$

$$Y_1 = Y(4008) \rightarrow \gamma + X_0 \quad (J^{PC} = 0^{++}) = \gamma + X(3770 ??), \quad ??$$

8. Hidden beauty tetraquarks

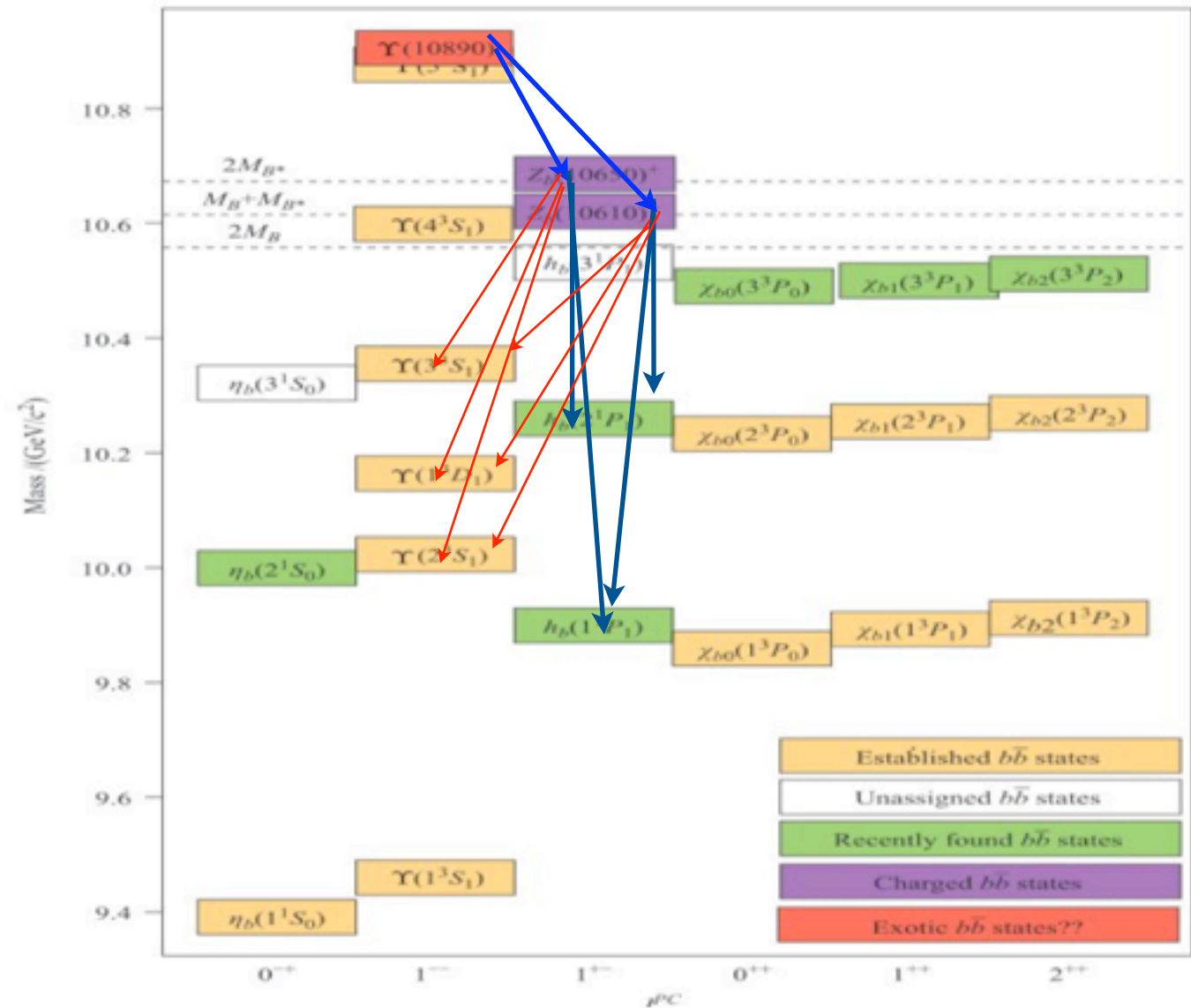
A. Ali, C. Hambrock, I. Ahmed and M. J. Aslam, Phys. Lett. B 684, 28 (2010);

A. Ali, C. Hambrock and M. J. Aslam, Phys. Rev. Lett. 104, 162001 (2010) [Erratum-ibid. 107, 049903 (2011)];

A. Ali, BELLE II ITIP, Krakow, 2015

Bottomonia and Bottomonium-like Hadrons (Olsen, arxiv:1411.7738)

- note: $\Delta M(Z_b)/\Delta M(Z_c) \sim m_c/m_b$, as expected
- Y(10850) usually identified with Y(5S)
- however Ali et al suggest Y(5S) is superimposed to the b-analog of Y(4260) with the decays:
 - $Y_b \rightarrow Z_b/Z_b' \pi \rightarrow h_b(nP) \pi \pi$
 - $Y_b \rightarrow Z_b/Z_b' \pi \rightarrow Y(nS) \pi \pi$
- simultaneous decay in h_b and Y *is compatible* with heavy quark spin conservation, since Z_b are not degenerate and each has both $S_{(b \bar{b})} = 0, 1$ components



Ahmed Ali (DESY, Hamburg)

$$|Z_b\rangle = \frac{|1_{bq}, 0_{\bar{b}\bar{q}}\rangle - |0_{bq}, 1_{\bar{b}\bar{q}}\rangle}{\sqrt{2}} = \frac{\alpha|1_{q\bar{q}}, 0_{b\bar{b}}\rangle - \beta|0_{q\bar{q}}, 1_{b\bar{b}}\rangle}{\sqrt{2}}$$

$$|Z'_b\rangle = |1_{bq}, 1_{\bar{b}\bar{q}}\rangle_{J=1} = \frac{\beta|1_{q\bar{q}}, 0_{b\bar{b}}\rangle + \alpha|0_{q\bar{q}}, 1_{b\bar{b}}\rangle}{\sqrt{2}}$$

$$\alpha \approx \beta \approx 1$$

- heavy quark spin conservation implies:

- $Y \rightarrow h_b (nP) \quad S = 1 \rightarrow S = 0 :$

$$g_Z = g(\Upsilon \rightarrow Z_b \pi) g(Z_b \rightarrow h_b \pi) \propto -\alpha \beta \langle h_b | 1_{q\bar{q}}, 0_{b\bar{b}} \rangle \langle 0_{q\bar{q}}, 1_{b\bar{b}} | \Upsilon \rangle$$

$$g_{Z'} = g(\Upsilon \rightarrow Z'_b \pi) g(Z'_b \rightarrow h_b \pi) \propto \alpha \beta \langle h_b | 1_{q\bar{q}}, 0_{b\bar{b}} \rangle \langle 0_{q\bar{q}}, 1_{b\bar{b}} | \Upsilon \rangle = -g_Z$$

- $Y \rightarrow Y(nS)$

$$f_Z = f(\Upsilon \rightarrow Z_b \pi) f(Z_b \rightarrow \Upsilon(nS) \pi) \propto |\beta|^2 \langle \Upsilon(nS) | 0_{q\bar{q}}, 1_{b\bar{b}} \rangle \langle 0_{q\bar{q}}, 1_{b\bar{b}} | \Upsilon \rangle$$

$$f_{Z'} = f(\Upsilon \rightarrow Z'_b \pi) f(Z'_b \rightarrow \Upsilon(nS) \pi) \propto |\alpha|^2 \langle \Upsilon(nS) | 0_{q\bar{q}}, 1_{b\bar{b}} \rangle \langle 0_{q\bar{q}}, 1_{b\bar{b}} | \Upsilon \rangle = \frac{\alpha^2}{\beta^2} f_Z$$

- in agreement, within still large errors, with Belle data:

| Final State | $\Upsilon(1S)\pi^+\pi^-$ | $\Upsilon(2S)\pi^+\pi^-$ | $\Upsilon(3S)\pi^+\pi^-$ | $h_b(1P)\pi^+\pi^-$ | $h_b(2P)\pi^+\pi^-$ |
|-------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|-----------------------------|
| Rel. Norm. | $0.57 \pm 0.21^{+0.19}_{-0.04}$ | $0.86 \pm 0.11^{+0.04}_{-0.10}$ | $0.96 \pm 0.14^{+0.08}_{-0.05}$ | $1.39 \pm 0.37^{+0.05}_{-0.15}$ | $1.6^{+0.6+0.4}_{-0.4-0.6}$ |
| Rel. Phase | $58 \pm 43^{+4}_{-9}$ | $-13 \pm 13^{+17}_{-8}$ | $-9 \pm 19^{+11}_{-26}$ | 187^{+44+3}_{-57-12} | $181^{+65+74}_{-105-109}$ |

Table 1: Relative normalizations and relative phases (in degrees), for $s_{b\bar{b}} : 1 \rightarrow 1$ and $1 \rightarrow 0$ transitions, as reported by Belle.

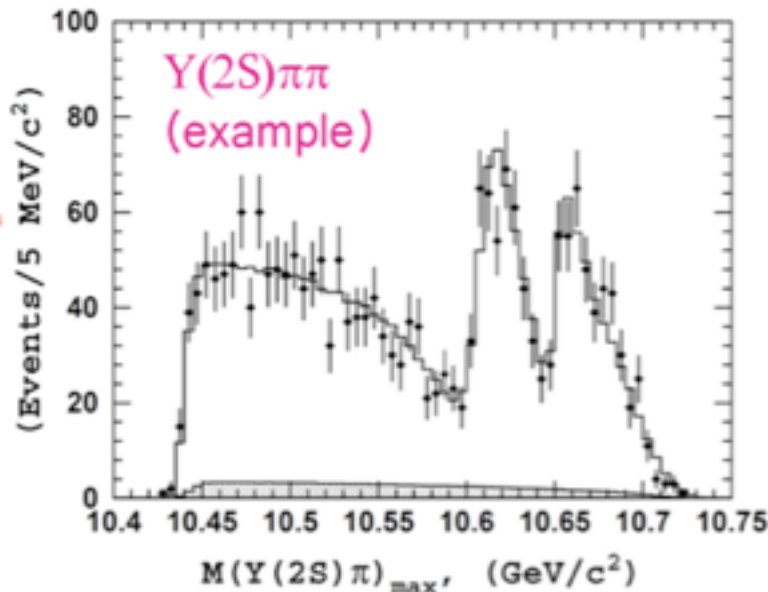
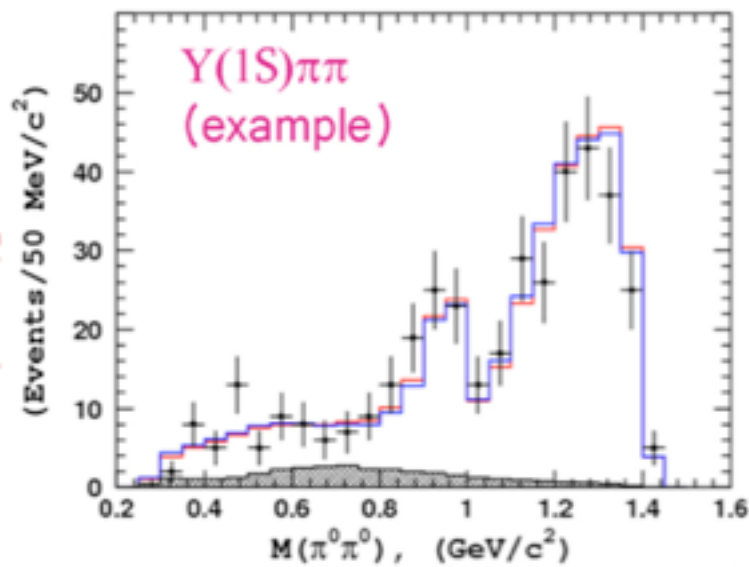
$$\begin{aligned} \overline{s_{b\bar{b}} : 1 \rightarrow 1 \text{ transition}} : \\ \overline{\text{Rel.Norm.}} &= 0.85 \pm 0.08 = |\alpha|^2 / |\beta|^2 \\ \overline{\text{Rel.Phase}} &= (-8 \pm 10)^\circ \end{aligned}$$

$$\begin{aligned} \overline{s_{b\bar{b}} : 1 \rightarrow 0 \text{ transition}} : \\ \overline{\text{Rel.Norm.}} &= 1.4 \pm 0.3 \\ \overline{\text{Rel.Phase}} &= (185 \pm 42)^\circ \end{aligned}$$

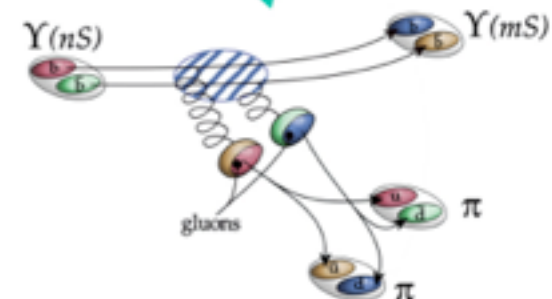
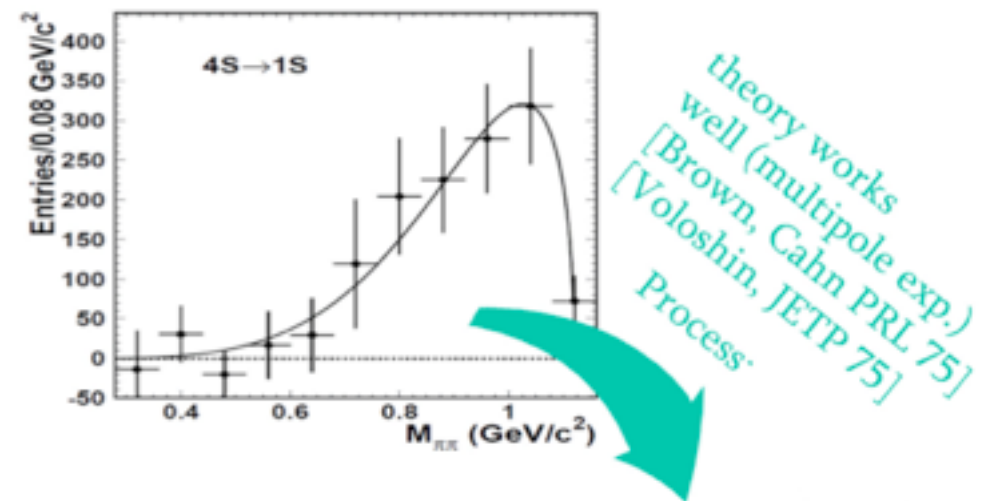
has the $Y_b(10850)$ bump a 4quark component, besides the $Y(5S)$ one, as proposed by Ali and coworkers?

Dipion mass distributions in $Y(5S) \rightarrow Y(nS)\pi\pi$ decays?

[Belle Collaboration (2012)]

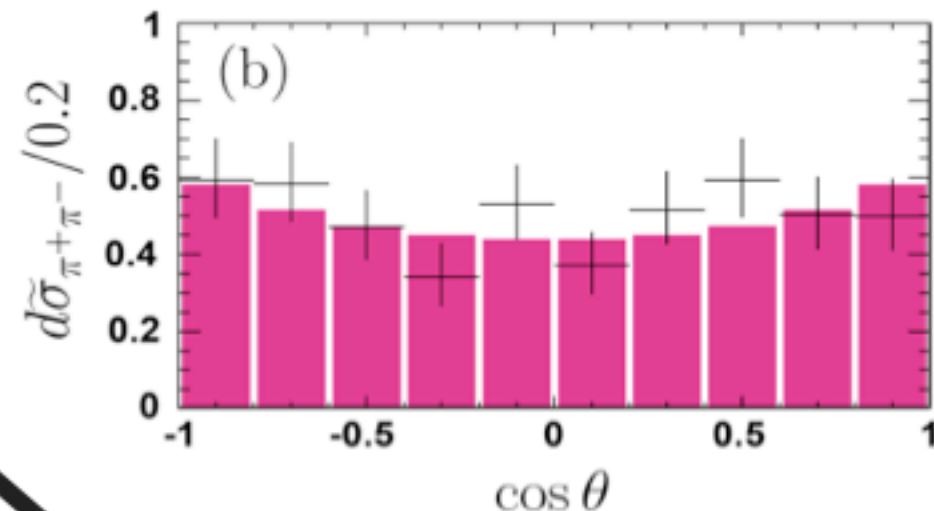
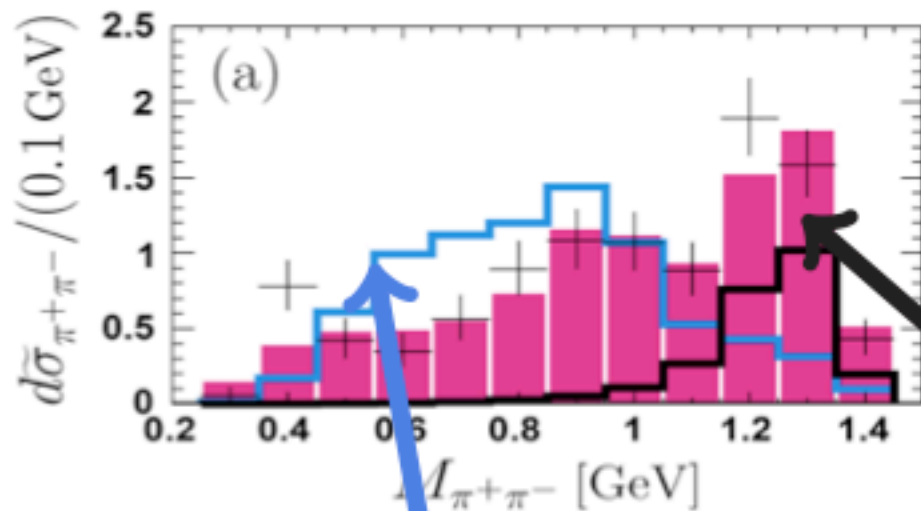


- the dipion spectrum strongly suggestive of the characteristic processes:
 - 4quark decay in $Y(1S)+q \bar{q} \rightarrow f_2(1270)$
 - same with $f_0(1370) \rightarrow f_0(990)$ by instanton mixing [$f_0(1370)$ goes essentially in 4π only]
 - hint of de-excitation in $Y_b(b \bar{b})+4\text{quark } f_0(500)$
 - note the difference w.r.t. the 2 pion spectrum in the decay of $Y_b(4S)$!!



Ahmed Ali (DESY, Hamburg)

Fit to $\sigma(e^+e^- \rightarrow Y_b \rightarrow Y(1S)\pi^+\pi^-)$



0^{++} tetraquarks $\sigma(500) + f_0(980)$
 2^{++} meson $f_2(1270)$

- Fit results, data from [\[Belle, PRL 08\]](#)
- $\chi^2/\text{d.o.f.} = 21.5/15 \rightarrow$ Good agreement with data
- Clear **resonance dominance!**

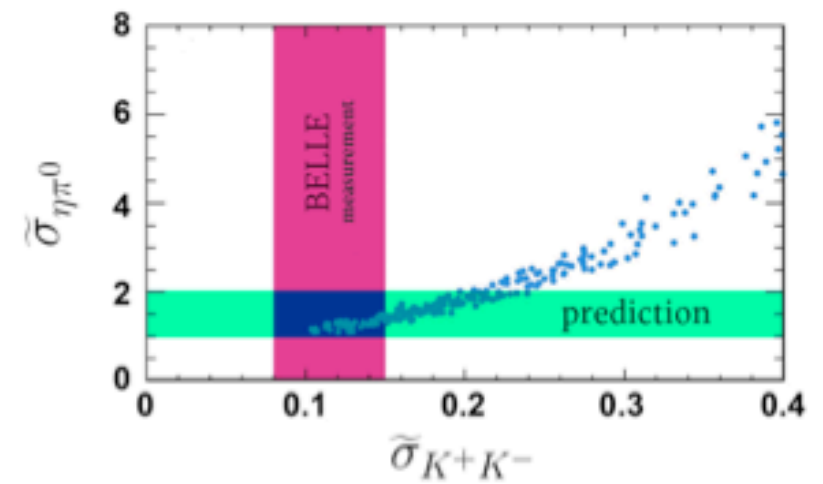
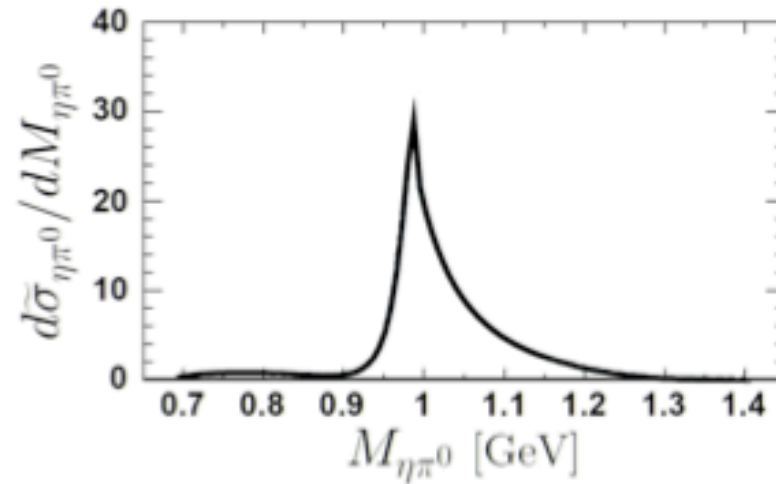
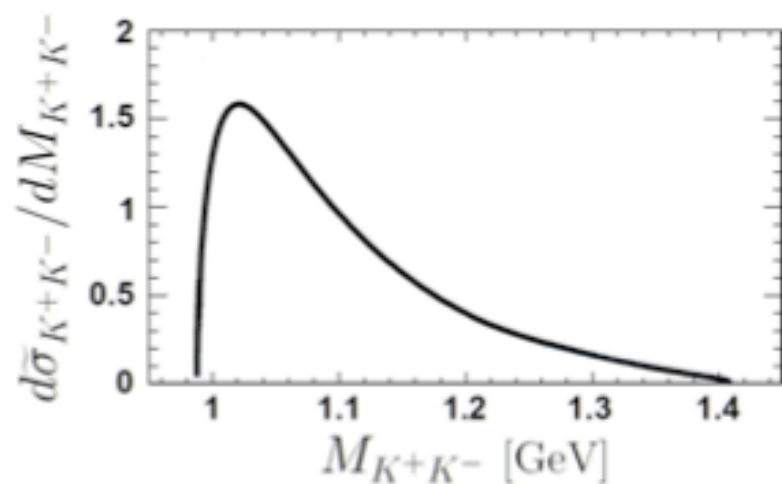
($\tilde{\sigma}$: normalized to measurement)

Ahmed Ali (DESY, Hamburg)

Predictions for : $Y(10850) \rightarrow Y(1S) + K^+ K^-$, or $\eta \pi^0$

Fit determines couplings (assume $SU(3)$ flavor symmetry for couplings $(\sigma(500), f_0(980), a_0(980)) \rightarrow PP'$, [t Hooft, Isidori, Maiani, Polosa, Riquer, PLB 08])

predictions for spectra:



■ Agreement with $\tilde{\sigma}_{K^+K^-} = 0.11^{+0.04}_{-0.03}$ (BELLE)

➤ $1.0 \lesssim \tilde{\sigma}_{\eta\pi^0} \lesssim 2.0$ predicted

■ Resonance dominance

➤ Characteristic shape

➤ **Good tests (relying on Y_b has 2 flavor states)**

9. To be convinced that we *do see* a new spectroscopy....

- Complete the 1S tetraquark multiplet (masses estimated with ± 40 MeV ?):
 - X_0 : 3780, X_0 , X_2 : 4020, decay: $J/\Psi \pi \pi$
- Fill the 2S multiplet
 - $Z'(2S)$: 4550, decay $\psi(2S) \pi$, $h_c(2S) \pi$
 - $X(2S)$: 4430
 - $X_0(2S)$: 4310, $X'_0(2S)$, $X_2(2S)$: 4550 decay $\psi(2S) \pi$
- $Y(4660) \rightarrow \psi(2S) \pi \pi$ decay:
 - does it go via $Z(4430) + \pi$? and there is a trace of $Z'(2S) + \pi$?
- $Y(4660) \rightarrow \gamma + \dots$ to discover $X(2S)$??
- Is there the $I=1$ (i.e. charged) companion of $X(3872)$? is it very wide?
- are there $Y_b(10850) \rightarrow Y(1S) \eta \pi^0$ decays?
- Can LHCb see the X, Y, Z states seen by Belle and BES?
-

Many Thanks !!