Automated EW Corrections with MG5_aMC@NLO (and Top Quark)

mainly based on: arXiv:1407.0823, arXiv:1504.03446, arXiv:1507.05640
and preliminary work for 100 TeV processes

Davide Pagani

IHEP, Beijing, China

Miniworkshop

20-11-2015

OUTLINE

Automation of the EW corrections in MG5_aMC@NLO

- Status and technical aspects

NLO QCD and EW corrections to $t\bar{t}V$

- Completely automated results at 8, 13, 100 TeV and in a boosted regime

EW corrections at 100 TeV

- Sudakov logs at high scales
- Effects from the Photon PDF

Conclusions and Outlook

Automation of NLO corrections in Madgraph5_aMC@NLO

What do we mean with automation of EW corrections?

The possibility of calculating QCD and EW corrections for SM processes (matched to shower effects) with a process-independent approach.

```
generate process [QCD]
output process_QCD
```

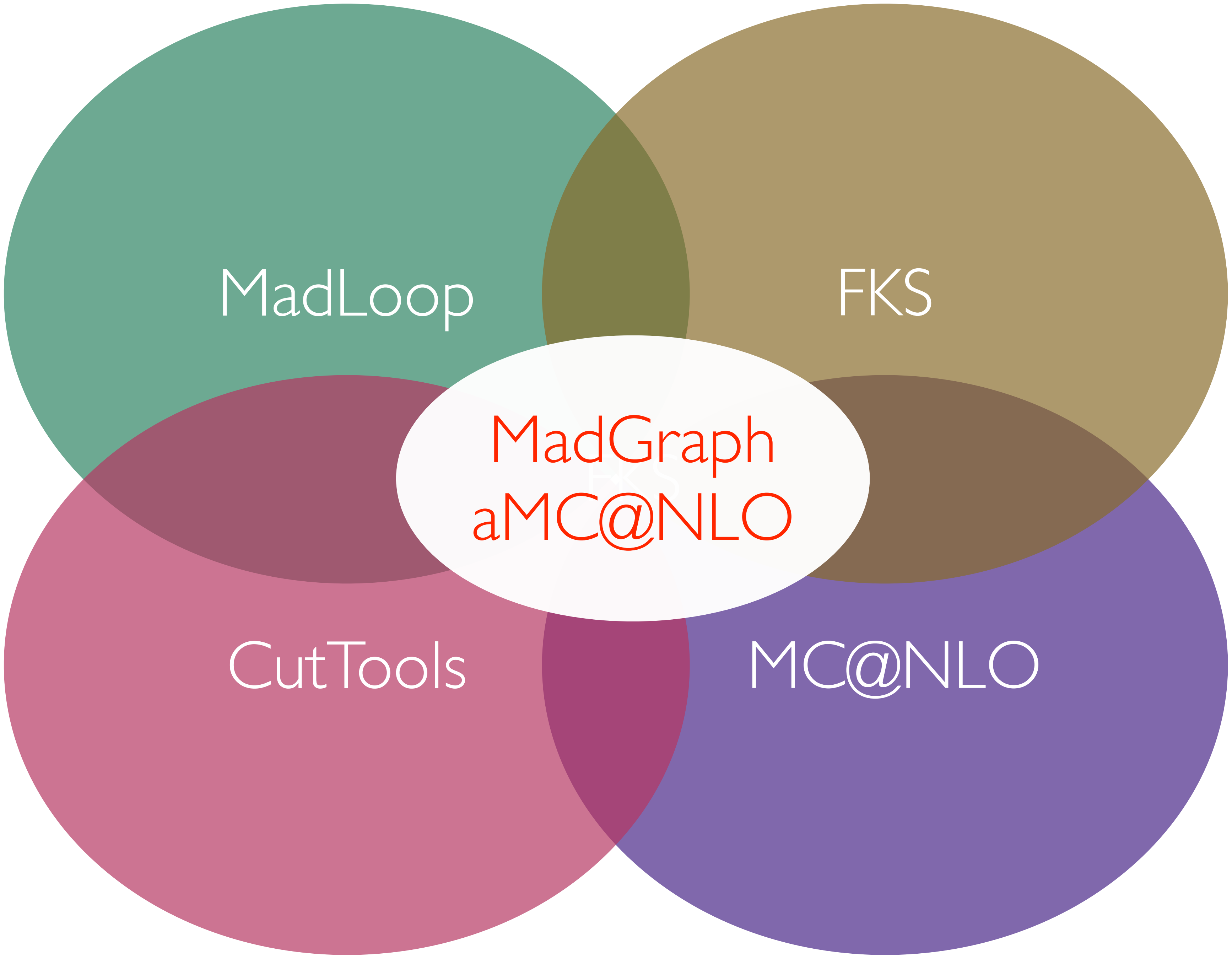
```
generate process [QCD EW]
output process_QCD_EW
```

The automation of NLO QCD has been achieved, but we need higher precision to match the experimental accuracy at the LHC and future colliders.

- NNLO QCD automation is out of our theoretical capabilities at the moment.
- NLO EW corrections are of the same order ($\alpha_s^2 \sim \alpha$), the Sudakov logarithms can enhance their size. NLO QCD and EW corrections **can be automated.**

Automation of NLO corrections in Madgraph5_aMC@NLO

The **complete automation** has already been achieved for **QCD**.



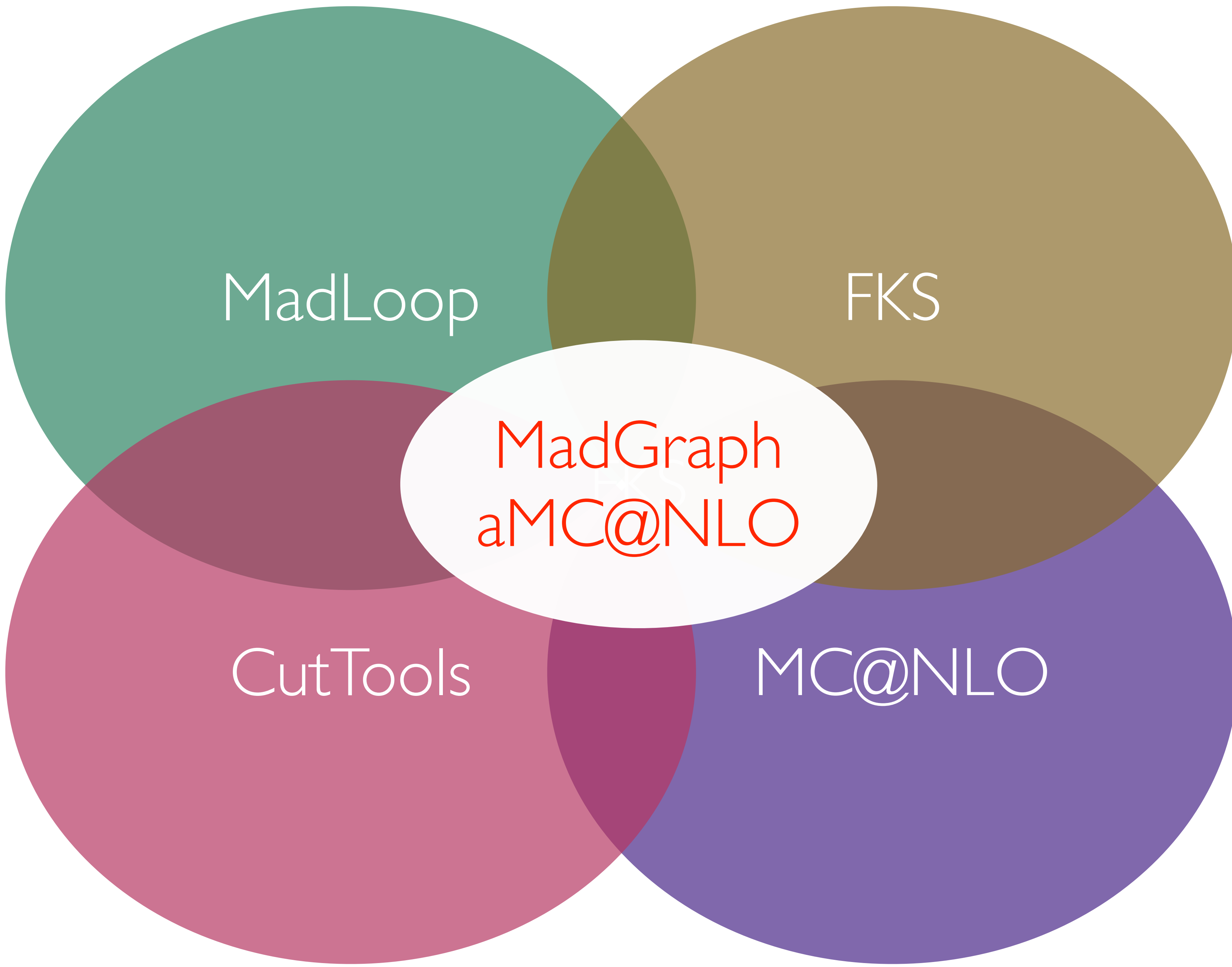
Alwall, Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Shao, Stelzer, Torrielli, Zaro '14

Automation of NLO corrections in Madgraph5_aMC@NLO

The **complete automation** for **QCD+EW** is in progress.

DONE!

in progress
(almost DONE)



DONE!

in progress

Amplitudes and matrix elements

NLO UFO models:	- SM-alpha(mZ)	(EW+QCD, Weak+QCD)
(UV CT, R2)	- SM-Gμ	(EW+QCD, Weak+QCD)

Weak = EW without photonics corrections (to be used when gauge invariant).

The matrix element calculation is completely automated. Example: $t\bar{t}V$

NLO orders of $t\bar{t}V$

$\alpha_s^3\alpha$ $\alpha_s^2\alpha^2$ $\alpha_s\alpha^3$ α^4

Amplitudes and matrix elements

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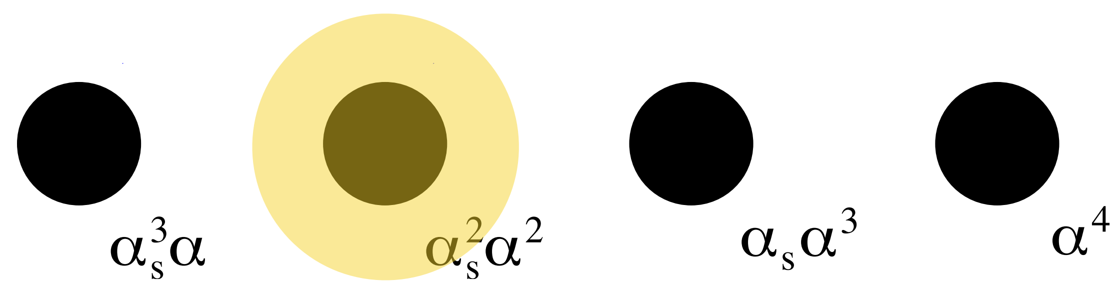
NLO orders of $t\bar{t}V$



Processes with only final-state massive particles

The generation of EW-QCD loops, real emission of gluons, quarks and photons is completely automated.

FKS IR counterterms completely automated. Also for photons in the initial state.

Heavy Boson Radiation (HBR)

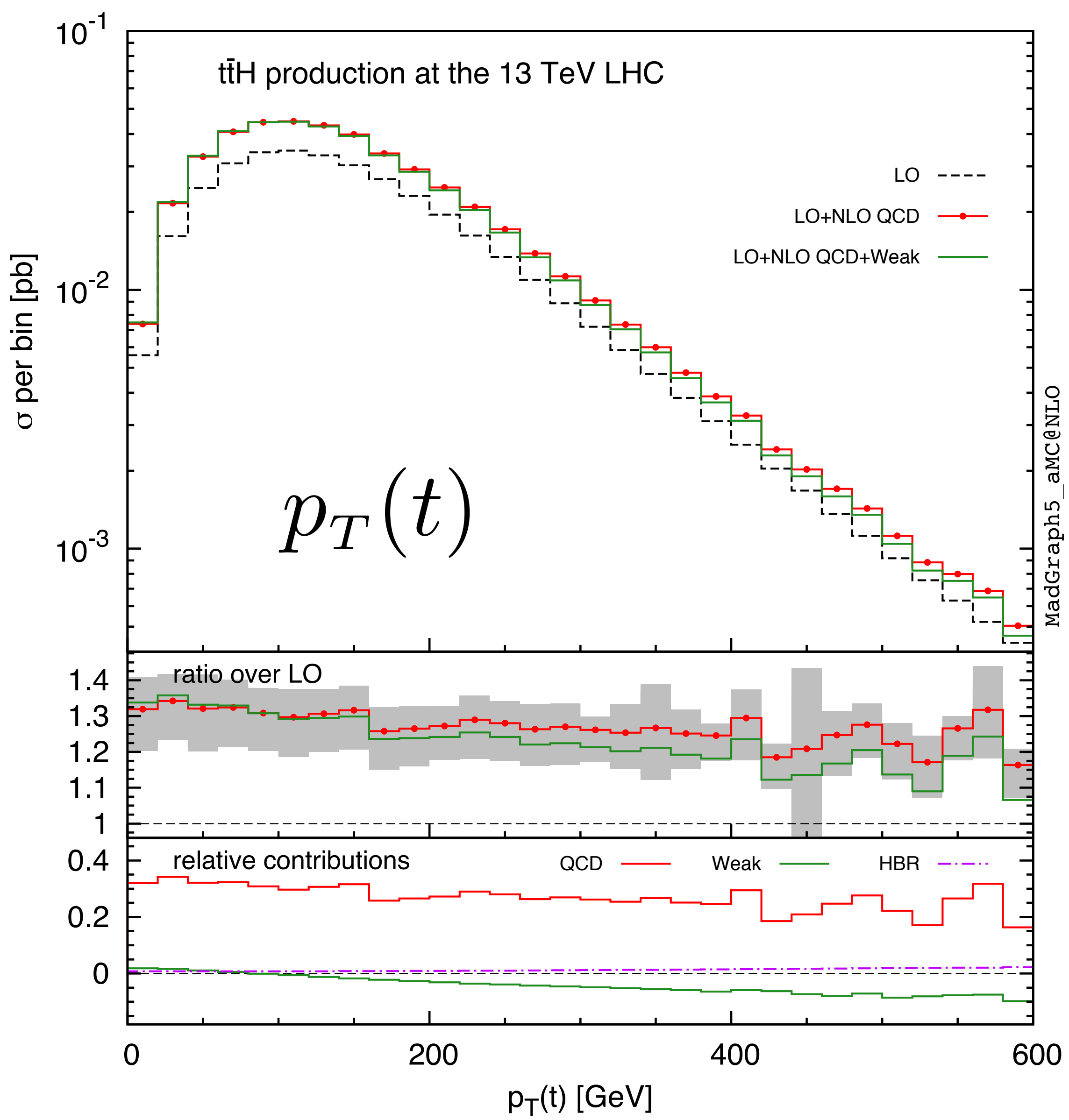
$$pp \to t\bar{t}H + V$$
$$V = H, W, Z$$

Formally of order $\alpha_S^2\alpha^2$

Pheno studies

NLO purely Weak and QCD corrections to $t\bar{t}H$ production have been produced "assembling by hand" the FKS counterterms.

Frixione, Hirschi, DP, Shao, Zaro '14



Now, for the complete NLO QCD and EW corrections, with photons in the initial state, we need to type:

```
define p = p b b~ a
generate p p > t t~ h [QCD QED]
output ttbarh_QCD_QED
```

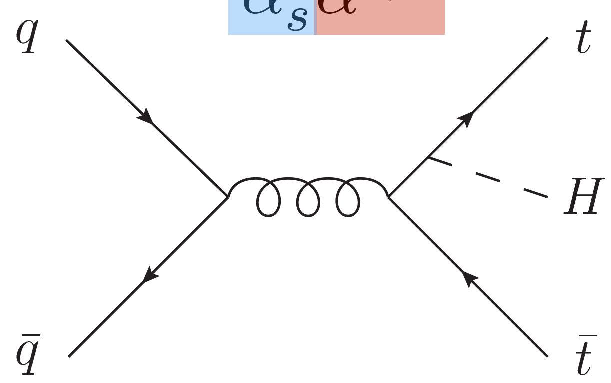
In this talk I present results for NLO QCD and EW corrections to

$t\bar{t}V \qquad V = H, W, Z$

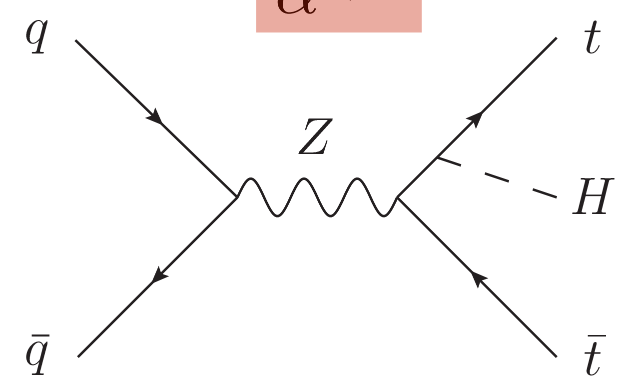
Frixione, Hirschi, DP, Shao, Zaro '15

Structure of NLO EW-QCD corrections

$\alpha_s^1 \alpha^{1/2}$

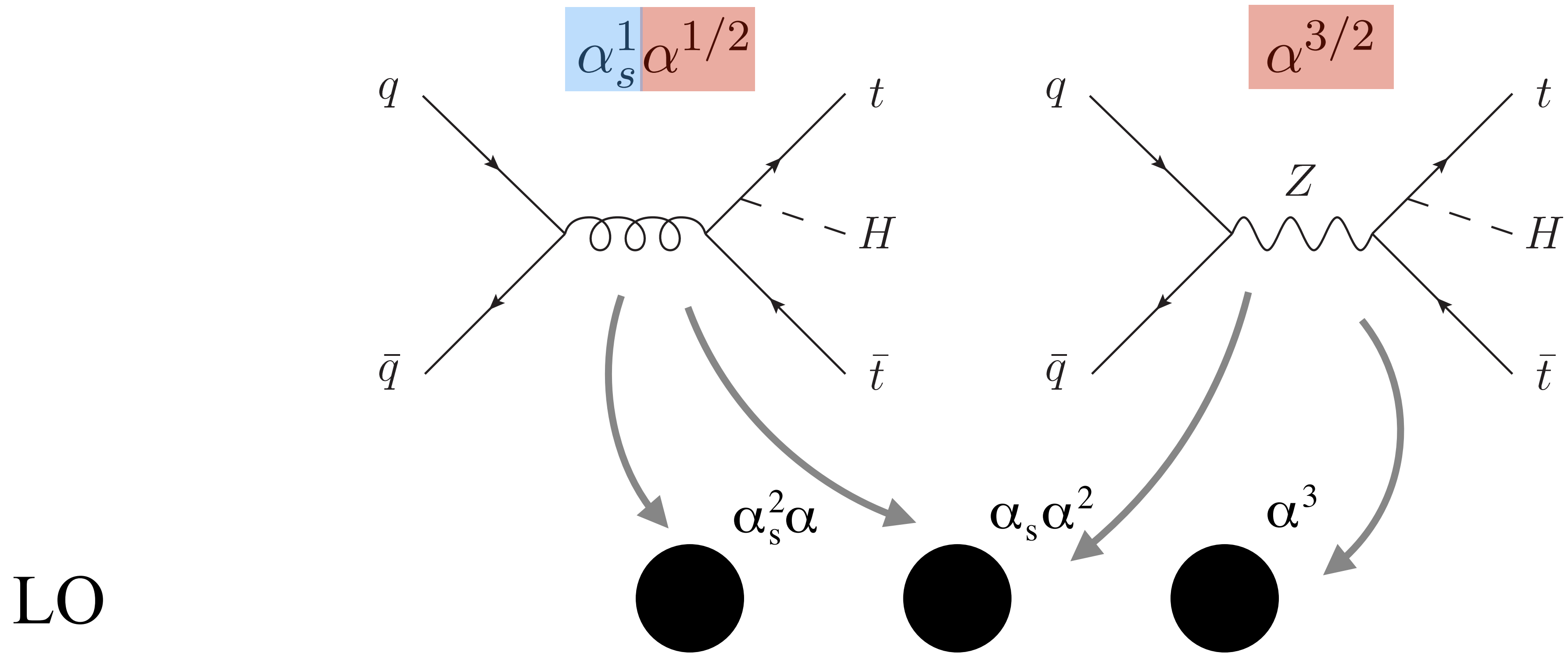


$\alpha^{3/2}$

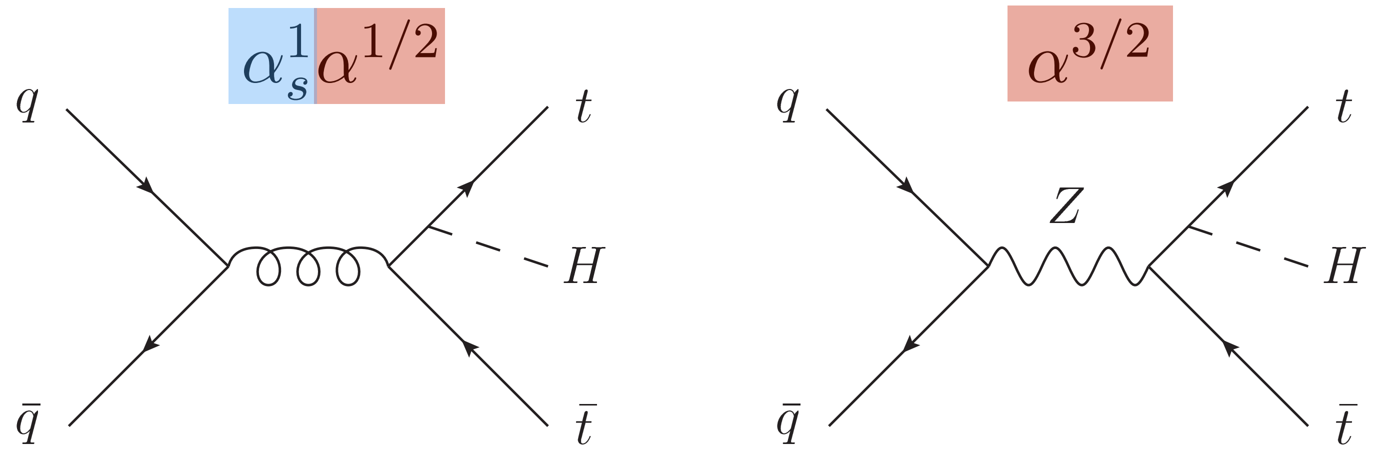


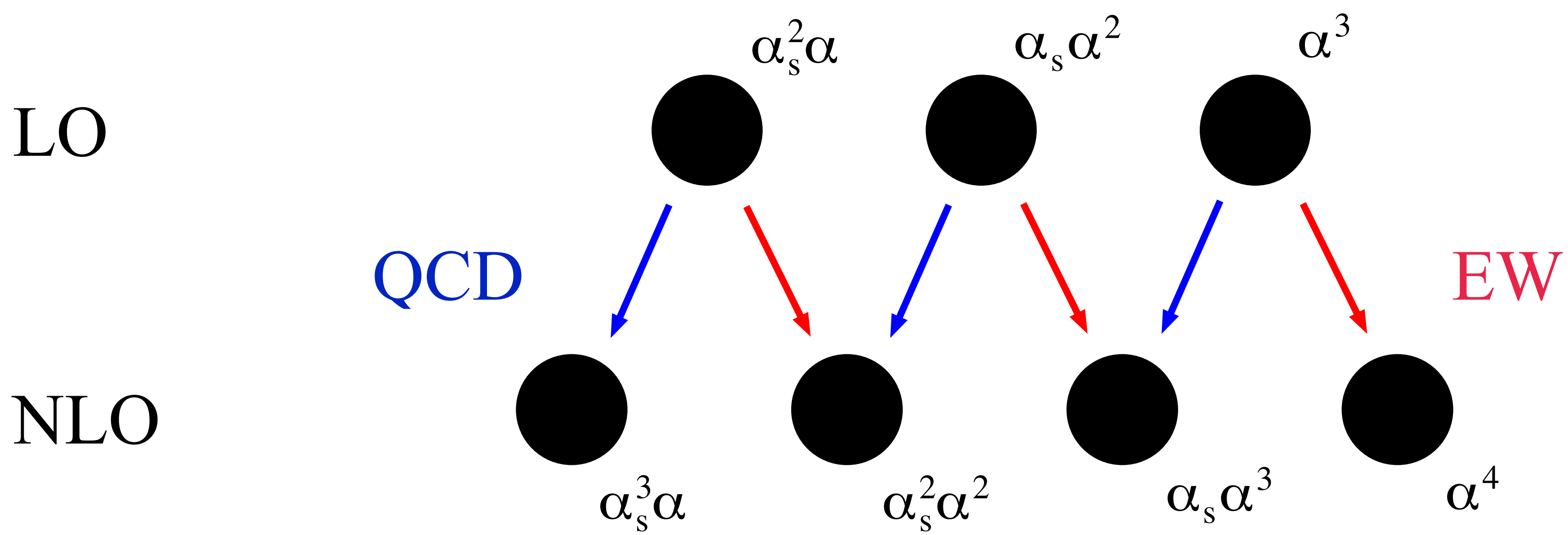
LO $\quad \alpha_s^2\alpha \quad \alpha_s\alpha^2 \quad \alpha^3$

Structure of NLO EW-QCD corrections



Structure of NLO EW-QCD corrections





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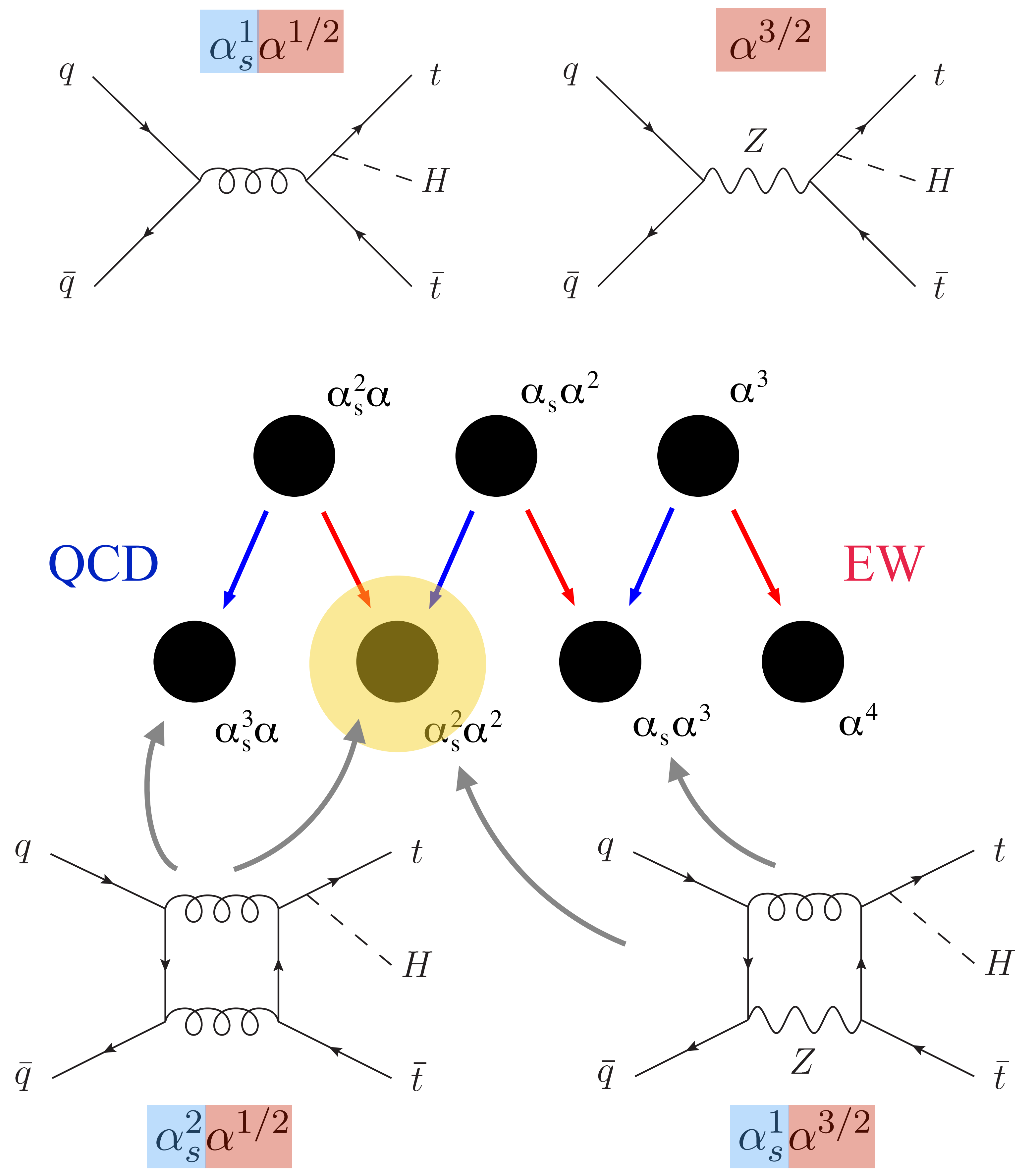
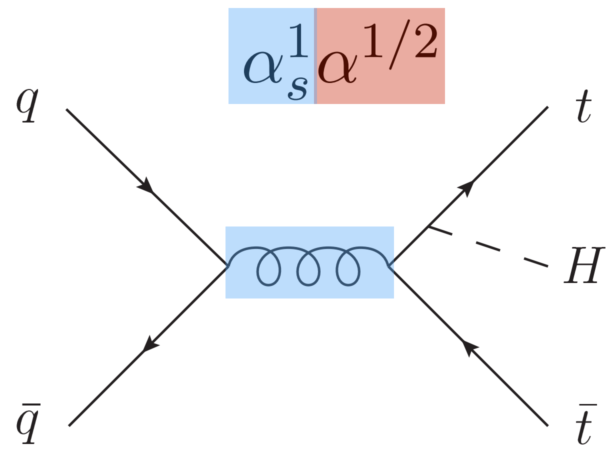
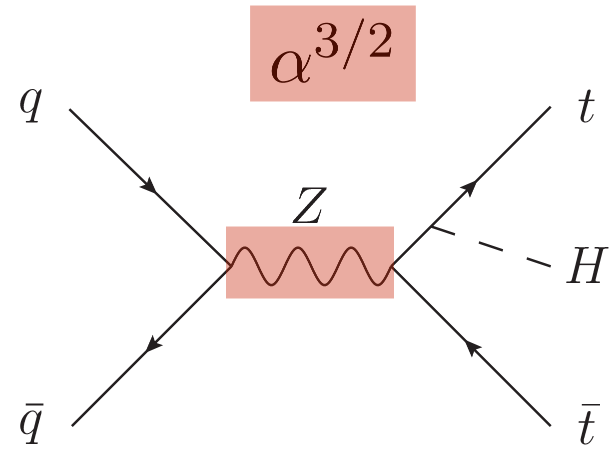
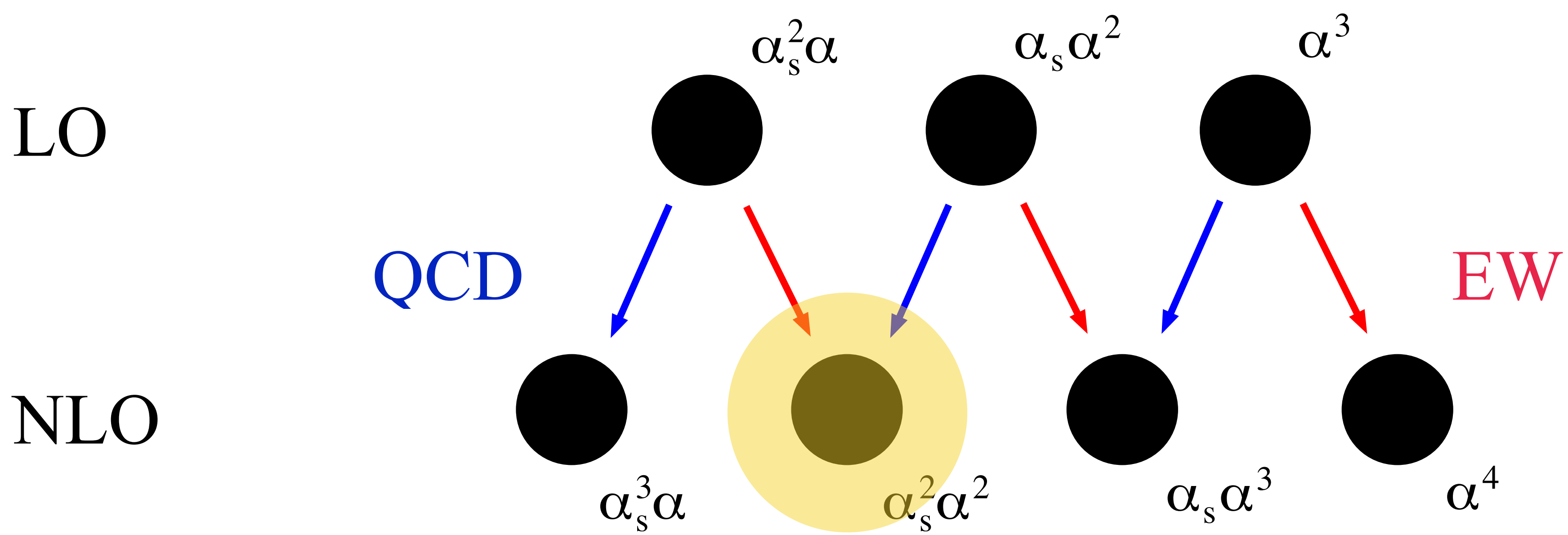
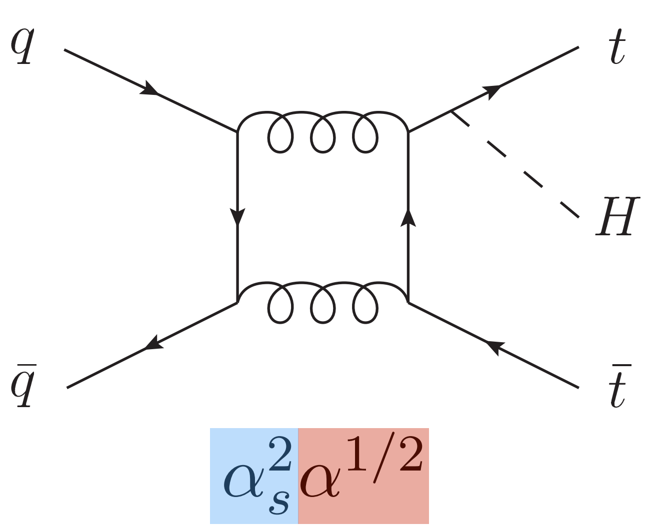


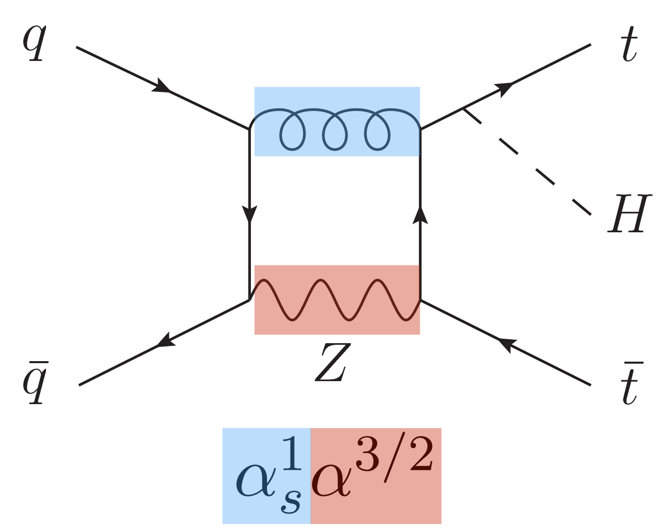
Structure of NLO EW-QCD corrections



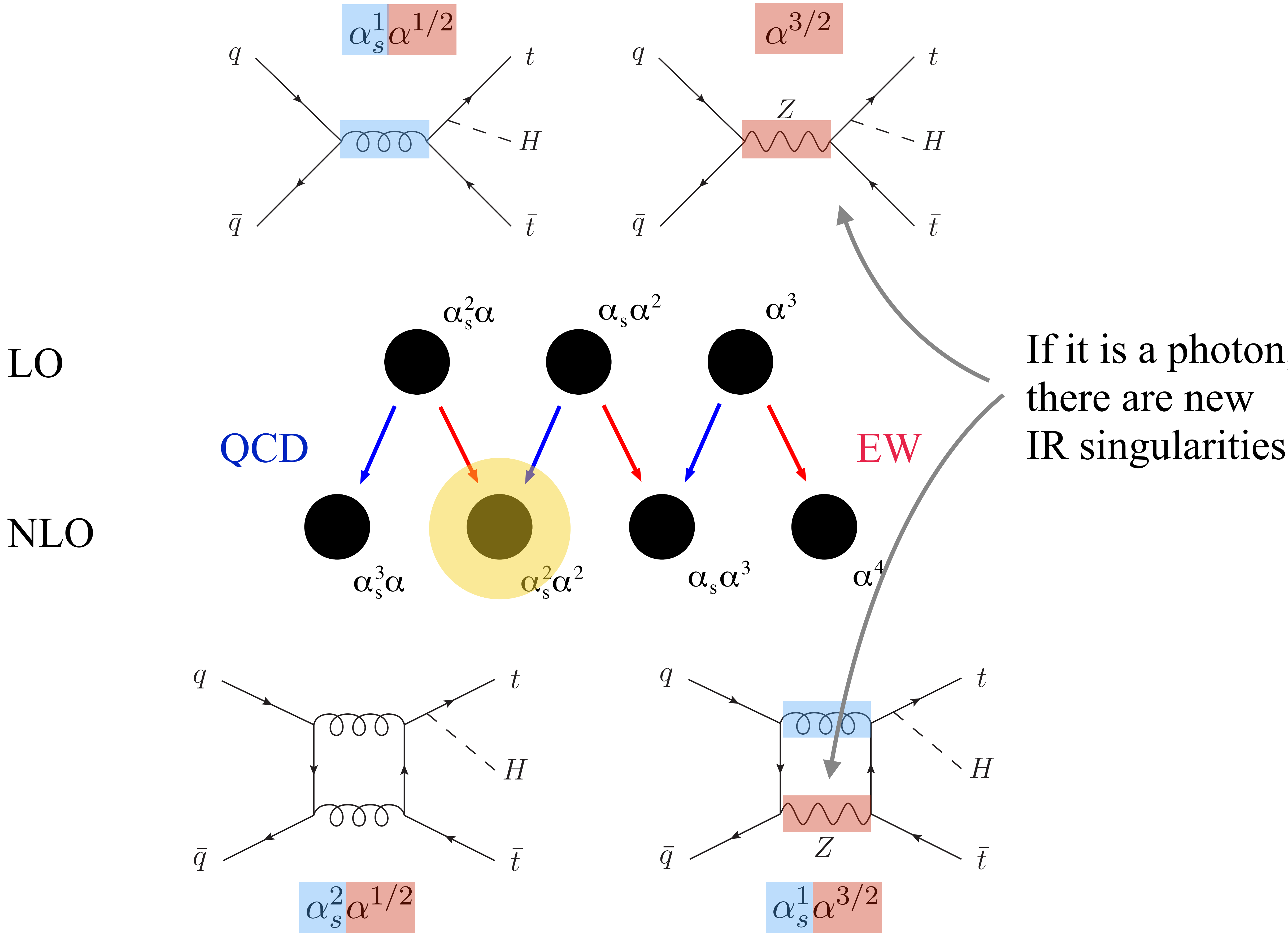








Structure of NLO EW-QCD corrections



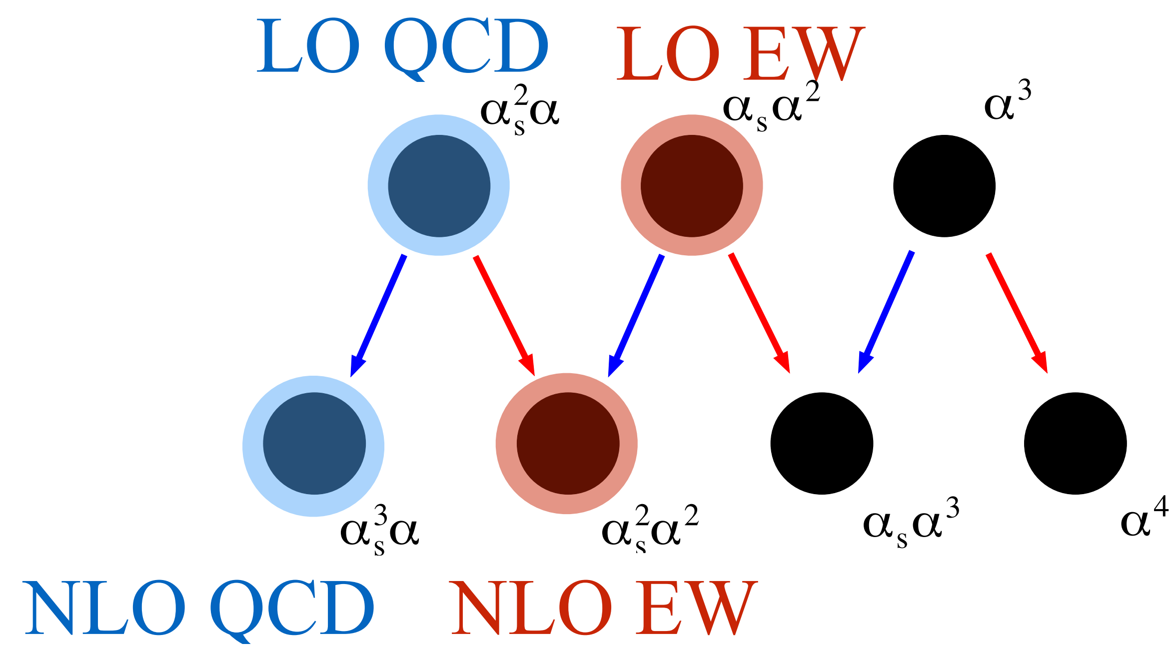
$t\bar{t}V$ production: numerical results

Alpha(mZ)-scheme, NNPDF2.3_QED, $\mu = \frac{H_T}{2}$, $\frac{1}{2}\mu \le \mu_R, \mu_F \le 2\mu$

Contributions

HBR ($pp \to t\bar{t}V + V'$) is of the same order of NLO EW.

The Photon PDF (with large uncertainties) enters in LO EW and NLO EW.




```
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output ttbarh_QCD_QED
```

$t\bar{t}V$ production: numerical results

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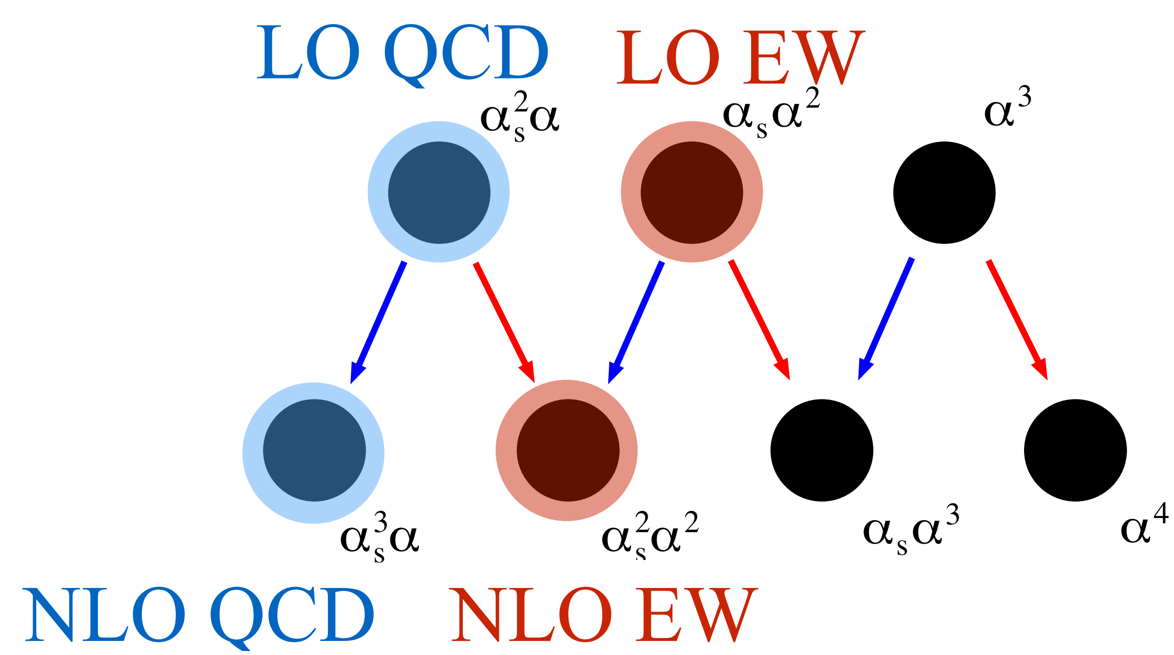


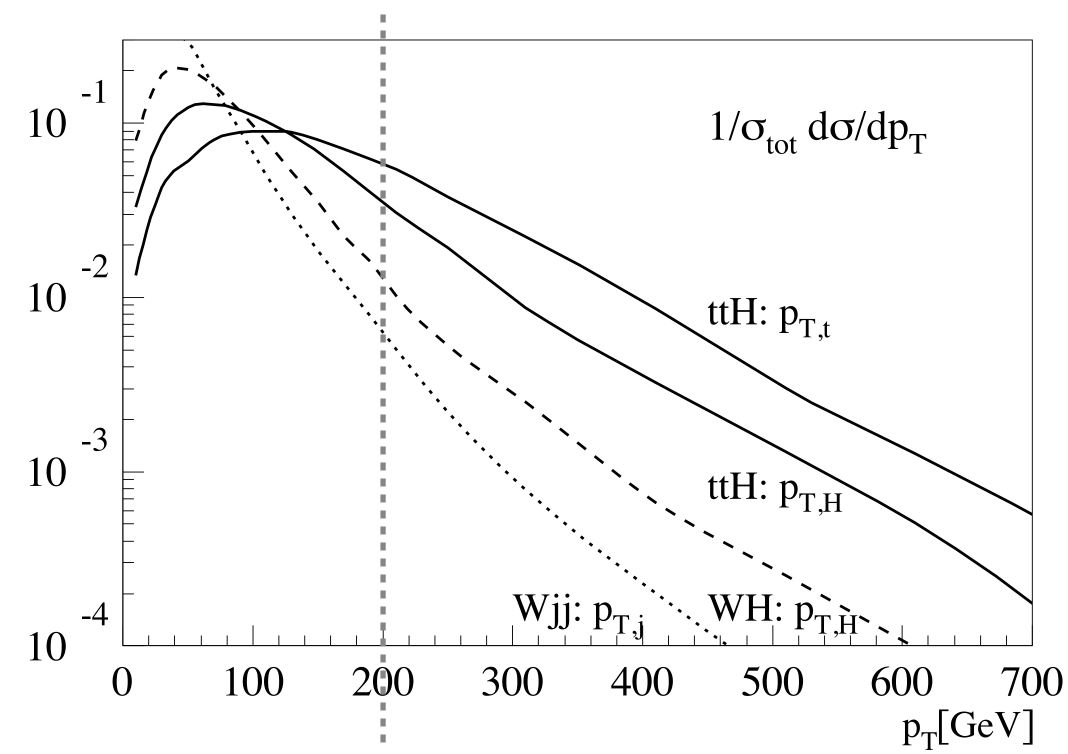
Boosted regime

$p_T(t) \geq 200$ GeV, $p_T(\bar{t}) \geq 200$ GeV, $p_T(H) \geq 200$ GeV

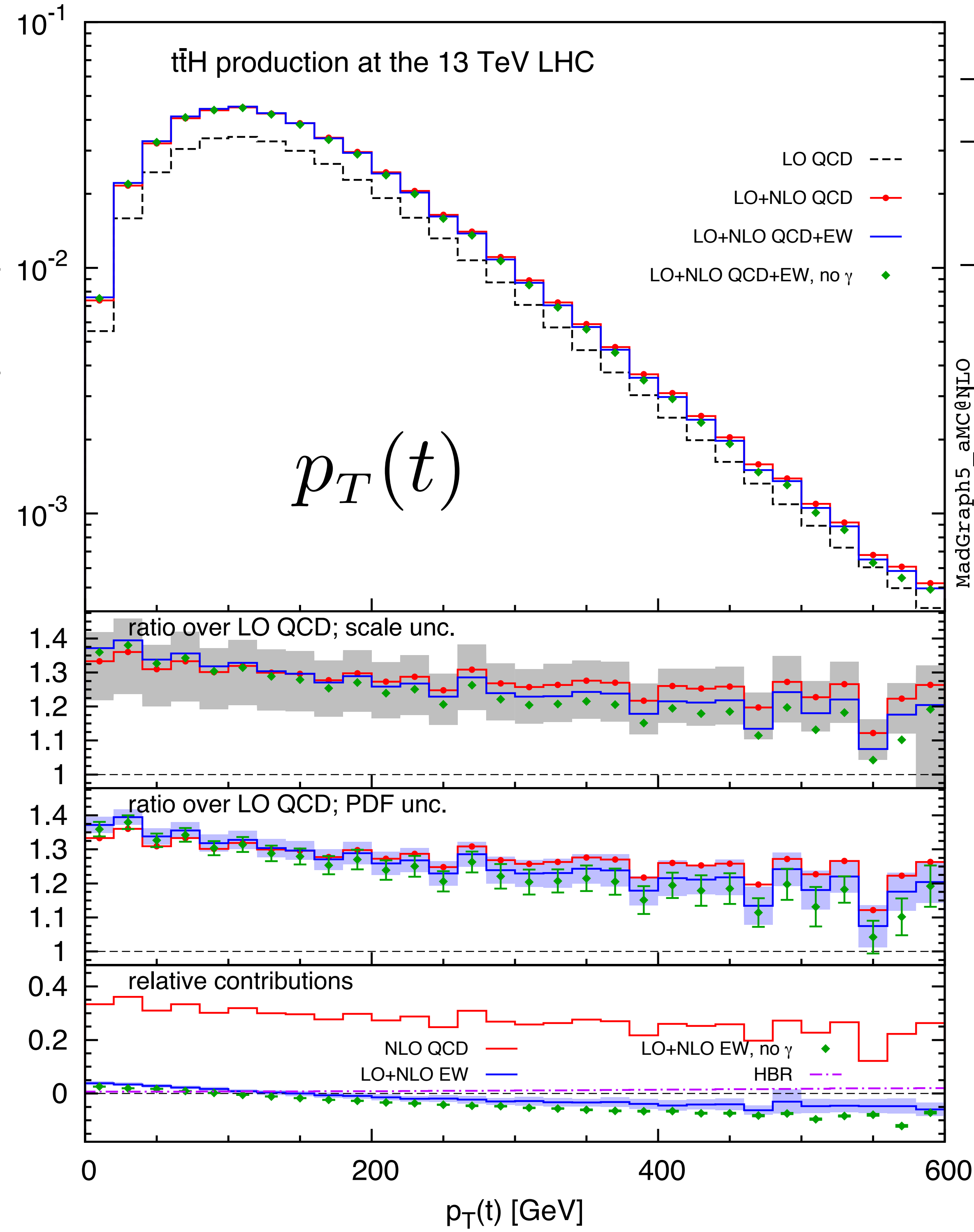
S/B increases for boosted tops and Higgs.

Plehn, Salam, Spannowsky '10

Sudakov logs are relevant in these regions!



Numerical results



$t\bar{t}H$: $\delta(\%)$	8 TeV	13 TeV	100 TeV
NLO QCD	$25.9^{+5.4}_{-11.1}$	$29.7^{+6.8}_{-11.1}$ $(24.2^{+4.8}_{-10.6})$	$40.8^{+9.3}_{-9.1}$
LO EW	1.8 ± 1.3	1.2 ± 0.9 (2.8 ± 2.0)	0.0 ± 0.2
LO EW no γ	-0.3 ± 0.0	-0.4 ± 0.0 (-0.2 ± 0.0)	-0.6 ± 0.0
NLO EW	-0.6 ± 0.1	-1.2 ± 0.1 (-8.2 ± 0.3)	-2.7 ± 0.0
NLO EW no γ	-0.7 ± 0.0	-1.4 ± 0.0 (-8.5 ± 0.2)	-2.7 ± 0.0
HBR	0.88	0.89 (1.87)	0.91

(Boosted regime in brackets)

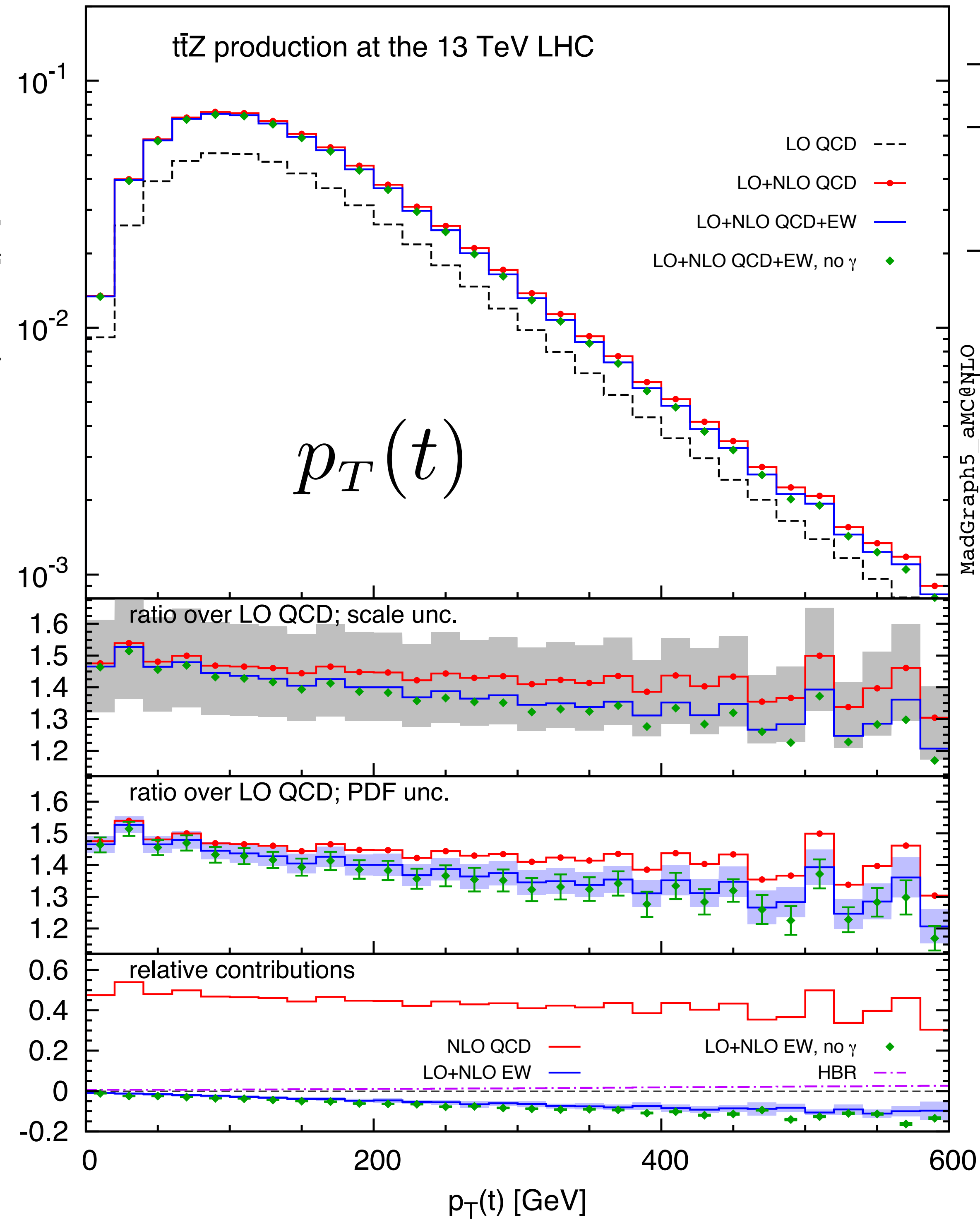
Scale variation

(NLO QCD+EW) PDF var.

$t\bar{t}H$

Frixione, Hirschi, DP, Shao, Zaro ‘15

Numerical results



$t\bar{t}Z$: $\delta(\%)$	8 TeV	13 TeV	100 TeV
NLO QCD	$43.2^{+12.8}_{-15.9}$	$\boxed{45.9^{+13.2}_{-15.5}\ (40.2^{+11.1}_{-15.0})}$	$50.4^{+11.4}_{-10.9}$
LO EW	0.5 ± 0.9	$\boxed{0.0 \pm 0.7\ (2.1 \pm 1.6)}$	-1.1 ± 0.2
LO EW no γ	-0.8 ± 0.1	$-1.1 \pm 0.0\ (-0.3 \pm 0.0)$	-1.6 ± 0.0
NLO EW	-3.3 ± 0.3	$\boxed{-3.8 \pm 0.2\ (-11.1 \pm 0.5)}$	-5.2 ± 0.1
NLO EW no γ	-3.7 ± 0.1	$-4.1 \pm 0.1\ (-11.5 \pm 0.3)$	-5.4 ± 0.0
HBR	0.95	0.96 (2.13)	0.85

(Boosted regime in brackets)

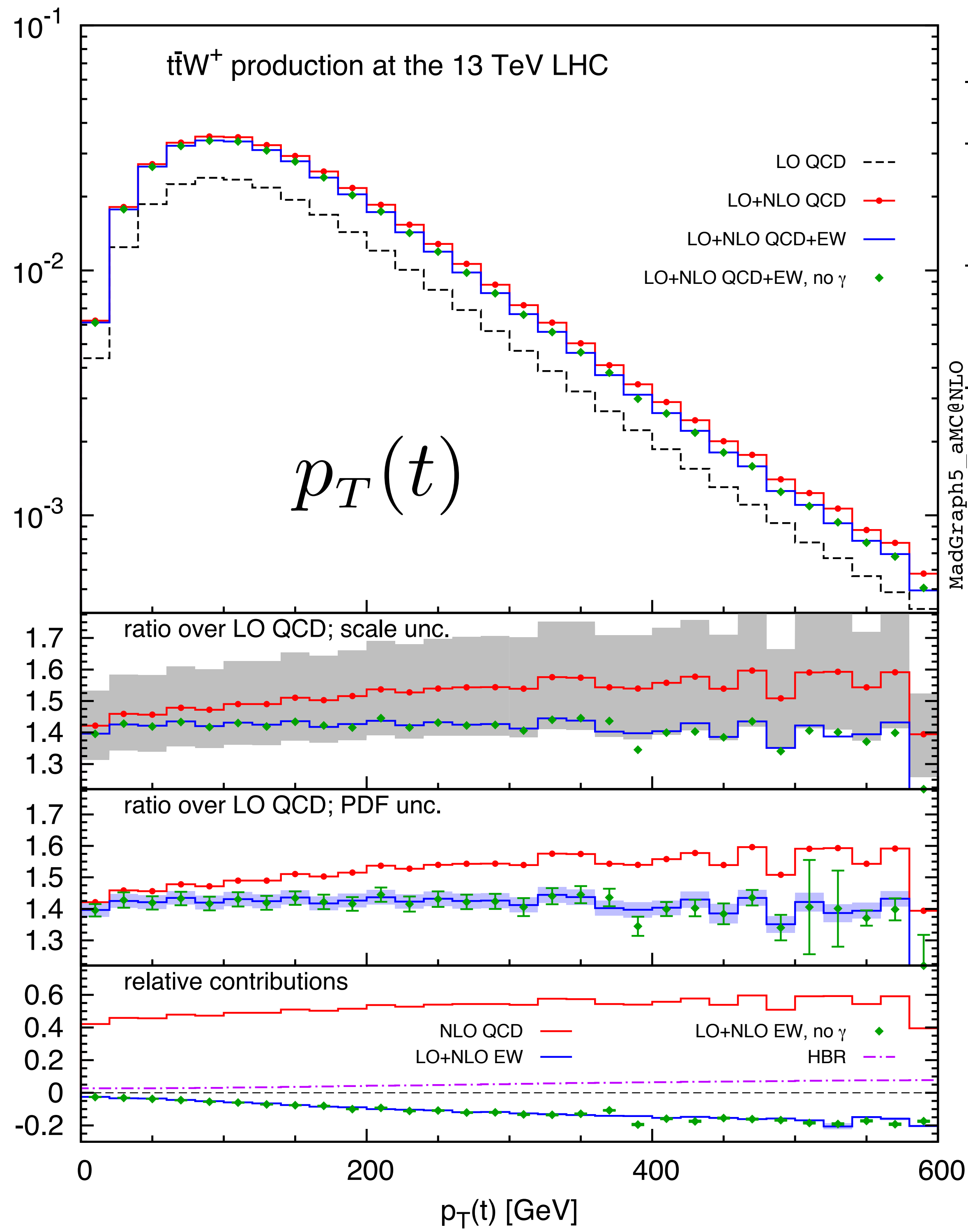
Scale variation

(NLO QCD+EW) PDF var.

$$t\bar{t}Z$$

Frixione, Hirschi, DP, Shao, Zaro '15

Numerical results



$t\bar{t}W^+$: $\delta(\%)$	8 TeV	13 TeV	100 TeV
NLO QCD	$40.8^{+11.2}_{-12.3}$	$\boxed{50.1^{+14.2}_{-13.5}\ (59.7^{+18.9}_{-17.7})}$	$156.4^{+38.3}_{-35.0}$
LO EW	0	0	0
LO EW no γ	0	0	0
NLO EW	-6.9 ± 0.2	$\boxed{-7.7 \pm 0.2\ (-19.2 \pm 0.7)}$	-9.3 ± 0.2
NLO EW no γ	-7.1 ± 0.2	$-8.0 \pm 0.2\ (-20.0 \pm 0.5)$	-9.6 ± 0.1
HBR	2.41	3.88 (7.41)	21.52

(Boosted regime in brackets)

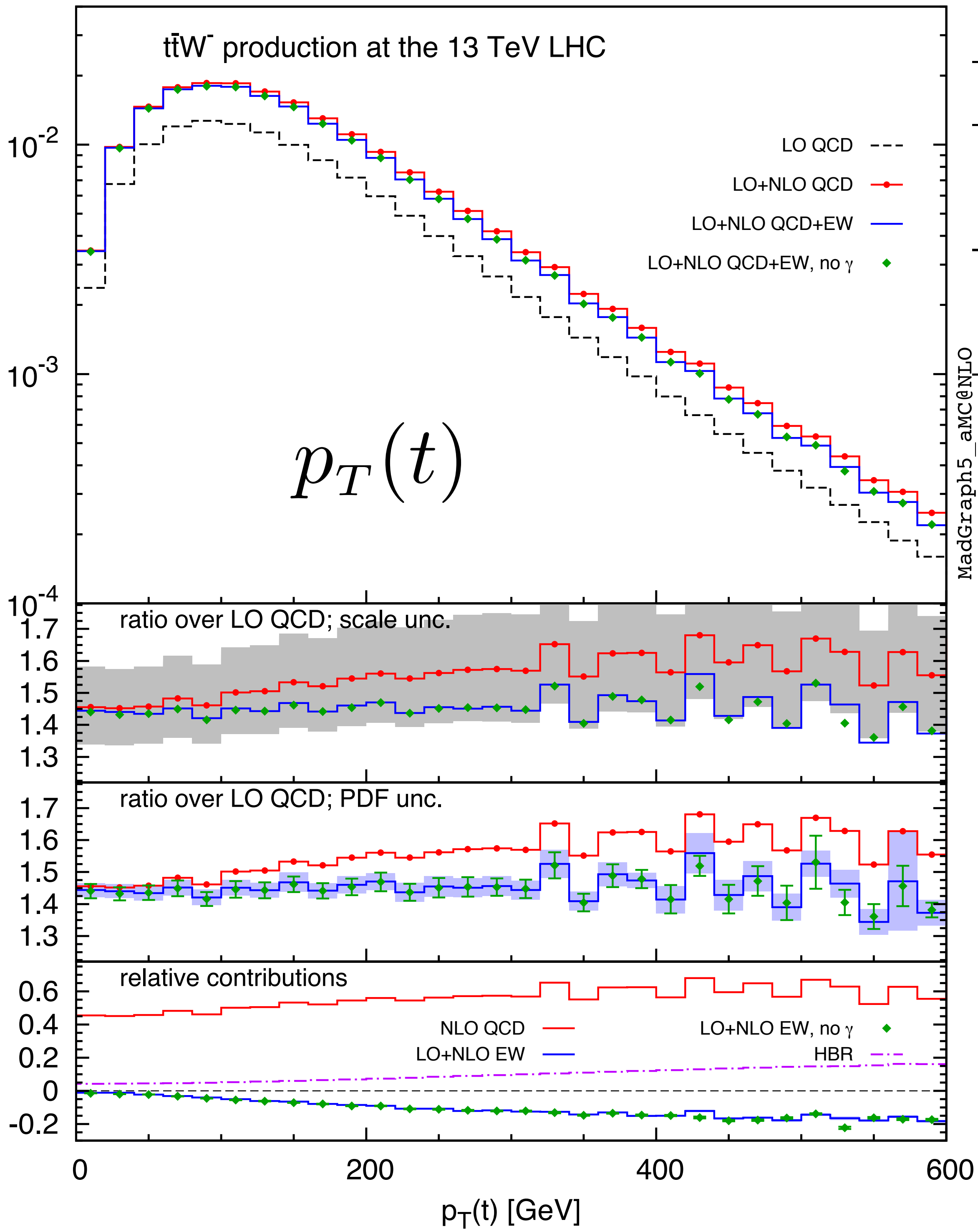
Scale variation

(NLO QCD+EW) PDF var.

$$t\bar{t}W^+$$

Frixione, Hirschi, DP, Shao, Zaro '15

Numerical results



$t\bar{t}W^-$: $\delta(\%)$	8 TeV	13 TeV	100 TeV
NLO QCD	$42.2^{+11.9}_{-12.7}$	$\boxed{51.5^{+14.8}_{-13.8}\ (66.3^{+21.7}_{-19.6})}$	$153.6^{+37.7}_{-34.9}$
LO EW	0	0	0
LO EW no γ	0	0	0
NLO EW	-6.0 ± 0.3	$\boxed{-6.7 \pm 0.2\ (-18.3 \pm 0.8)}$	-8.5 ± 0.2
NLO EW no γ	-6.2 ± 0.2	$-7.0 \pm 0.2\ (-19.1 \pm 0.6)$	-8.8 ± 0.1
HBR	4.35	6.50 (15.01)	$\boxed{28.91}$

(Boosted regime in brackets)

Scale variation

(NLO QCD+EW) PDF var.

$$t\bar{t}W^-$$

Frixione, Hirschi, DP, Shao, Zaro ‘15

100 TeV

We want to estimate the typical size of EW corrections at 100 TeV by looking at similar distributions in different “simple processes”:

transverse momenta and invariant masses in: WZ, HW, $t\bar{t}$

At the same time, we want to also estimate the impact of the photon PDF (central value and errors) at 100 TeV.

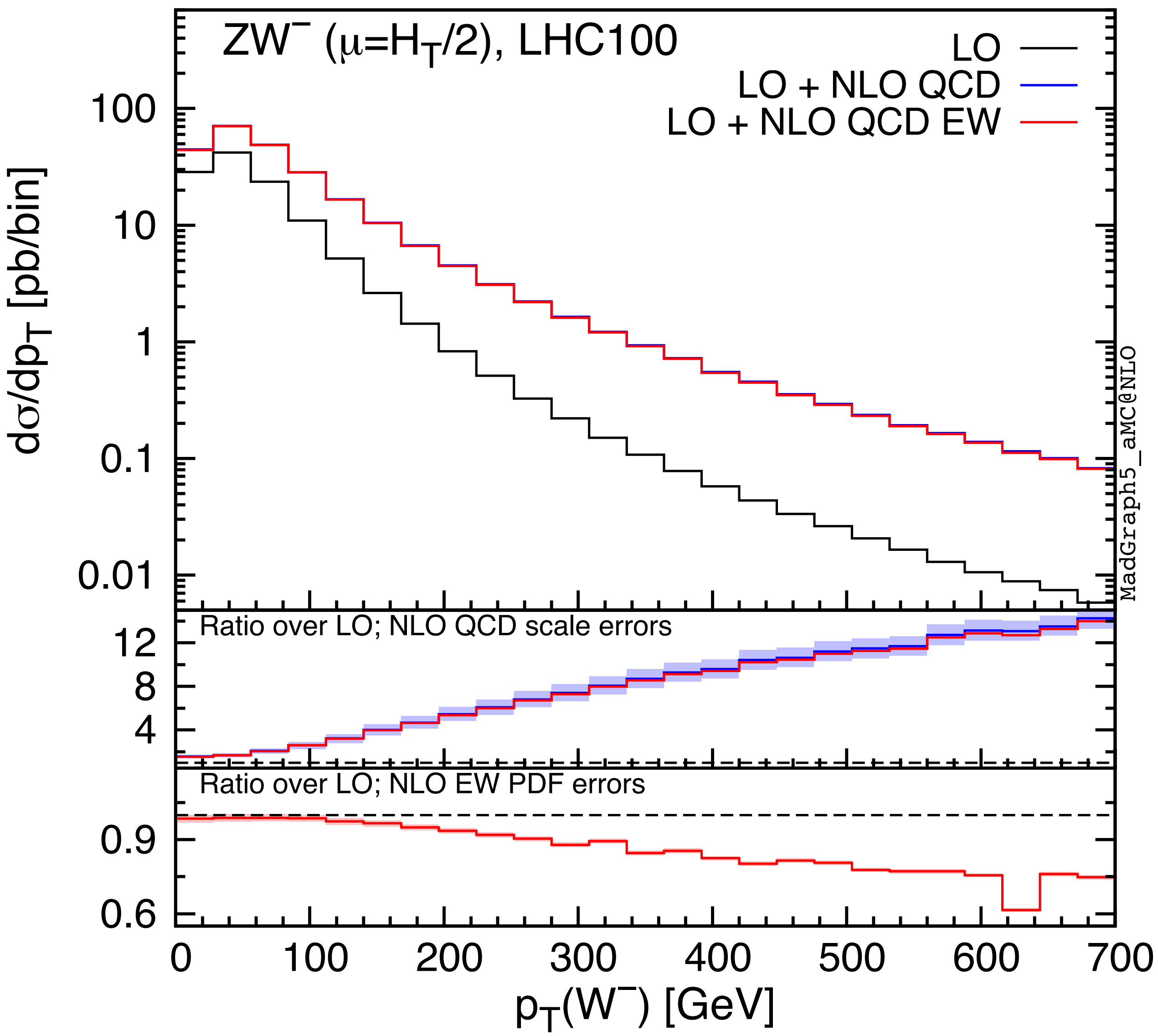
Disclaimer

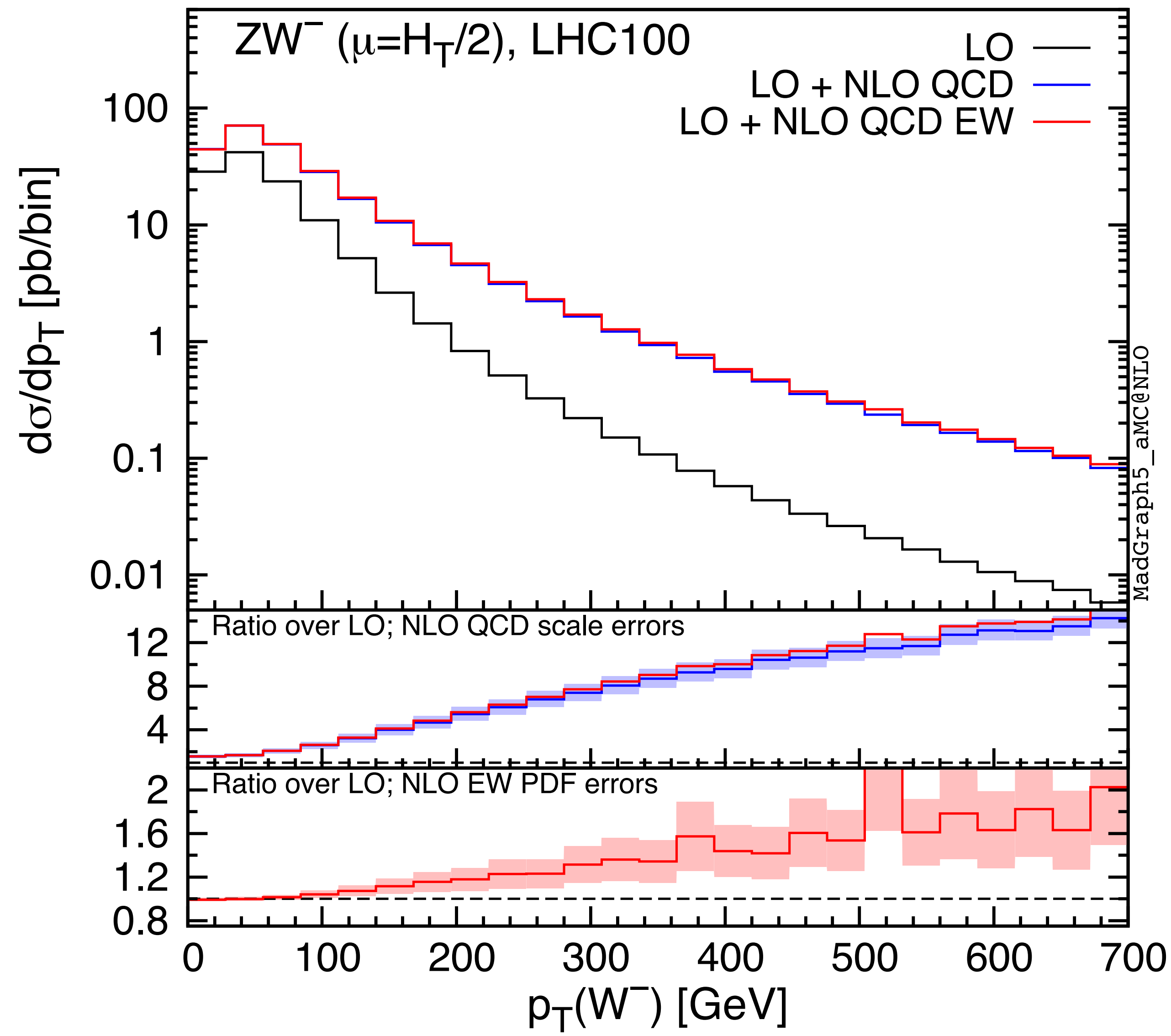
We want to raise possible issues related to NLO EW corrections at 100 TeV. No final answers or definitive statements will be given!

WZ

WZ

differential plots



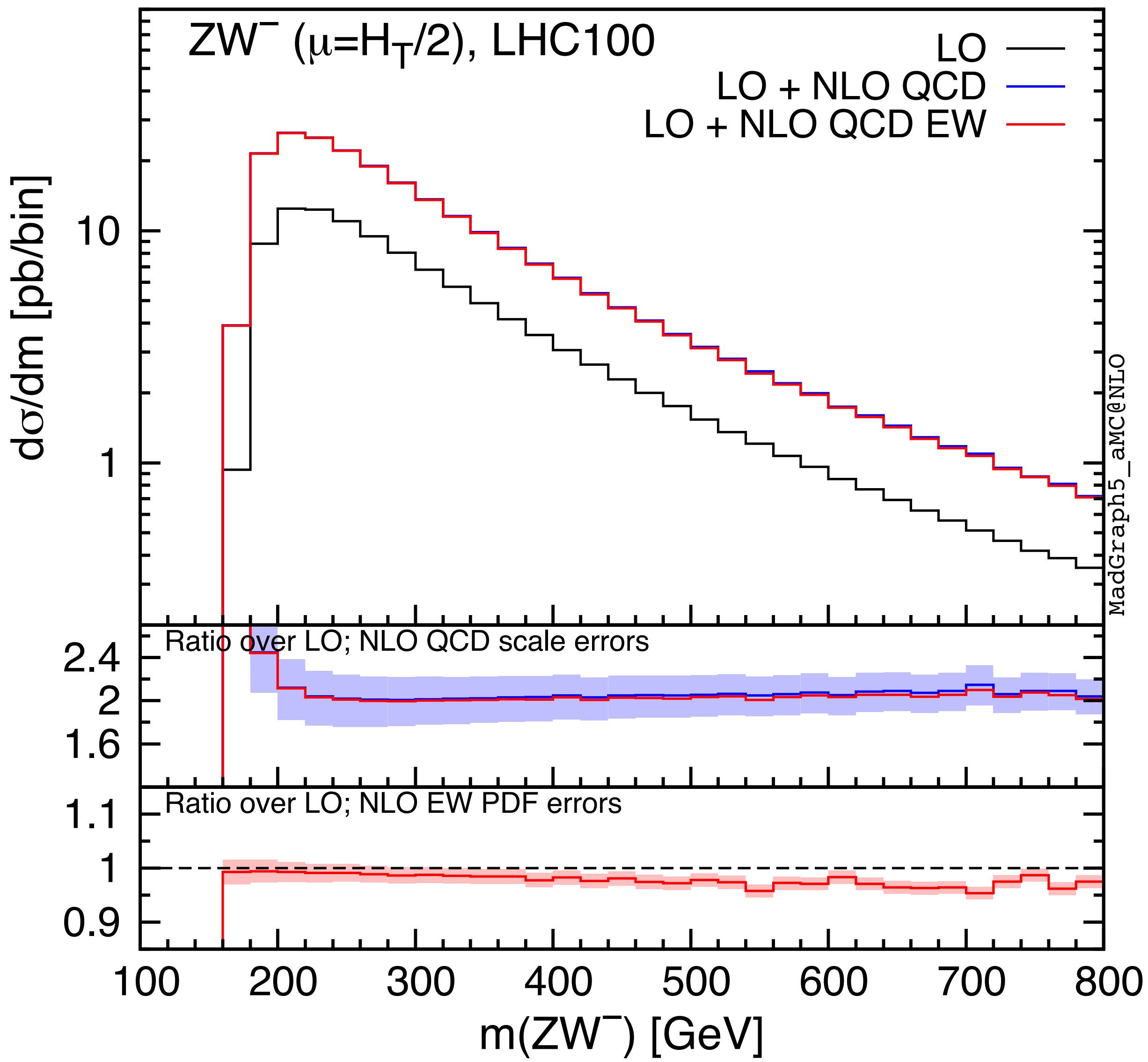


photon PDF **NO**

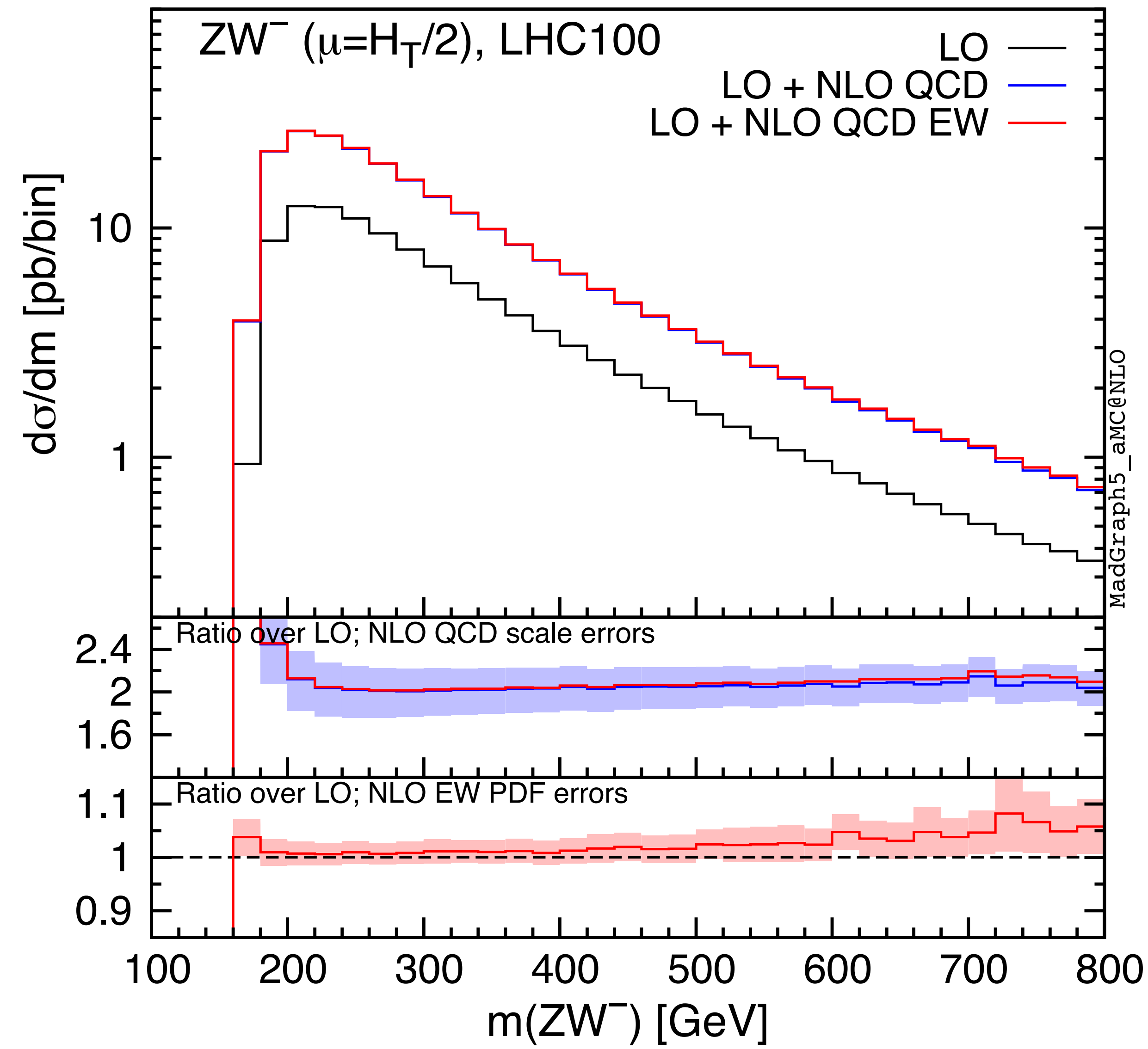
photon PDF **YES**

WZ

differential plots



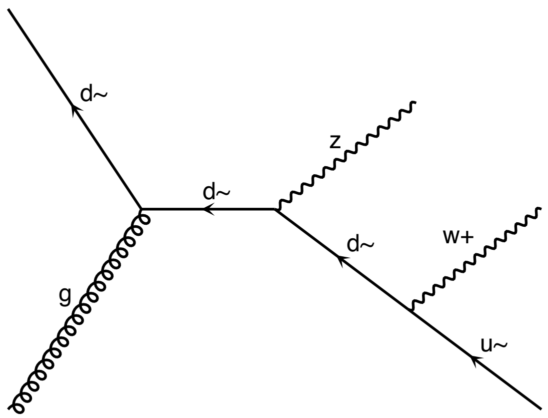
photon PDF **NO**



photon PDF **YES**

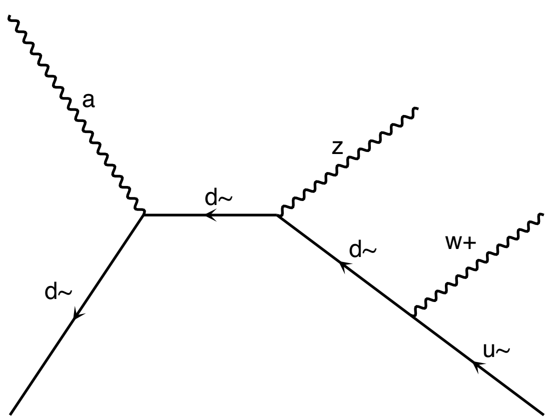
WZ

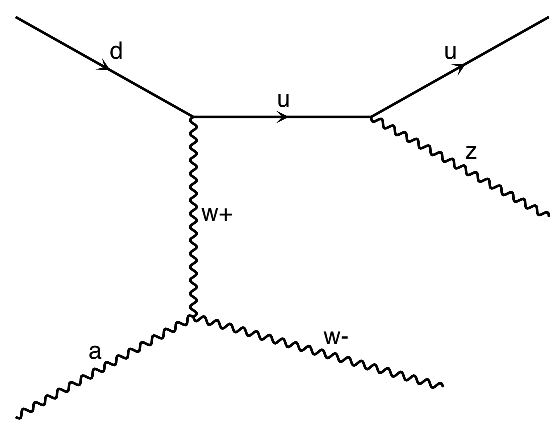
what's going on?



$$d\sigma^{dg\to W^- Zu} = c^d_{WZ} d\sigma^{dg\to Zd}_L \frac{\alpha}{2\pi} \log^2\left[\frac{(p_T^Z)^2}{M_W^2}\right]$$

Zj +
soft and collinear W





$$d\sigma^{d\gamma\to W^- Zu} = \frac{c^2_{L,d} c^d_{WZ}}{a_W^2} d\sigma^{d\gamma\to W^- u}_L \frac{\alpha}{2\pi} \log^2\left[\frac{(p_T^{W^-})^2}{M_Z^2}\right]$$

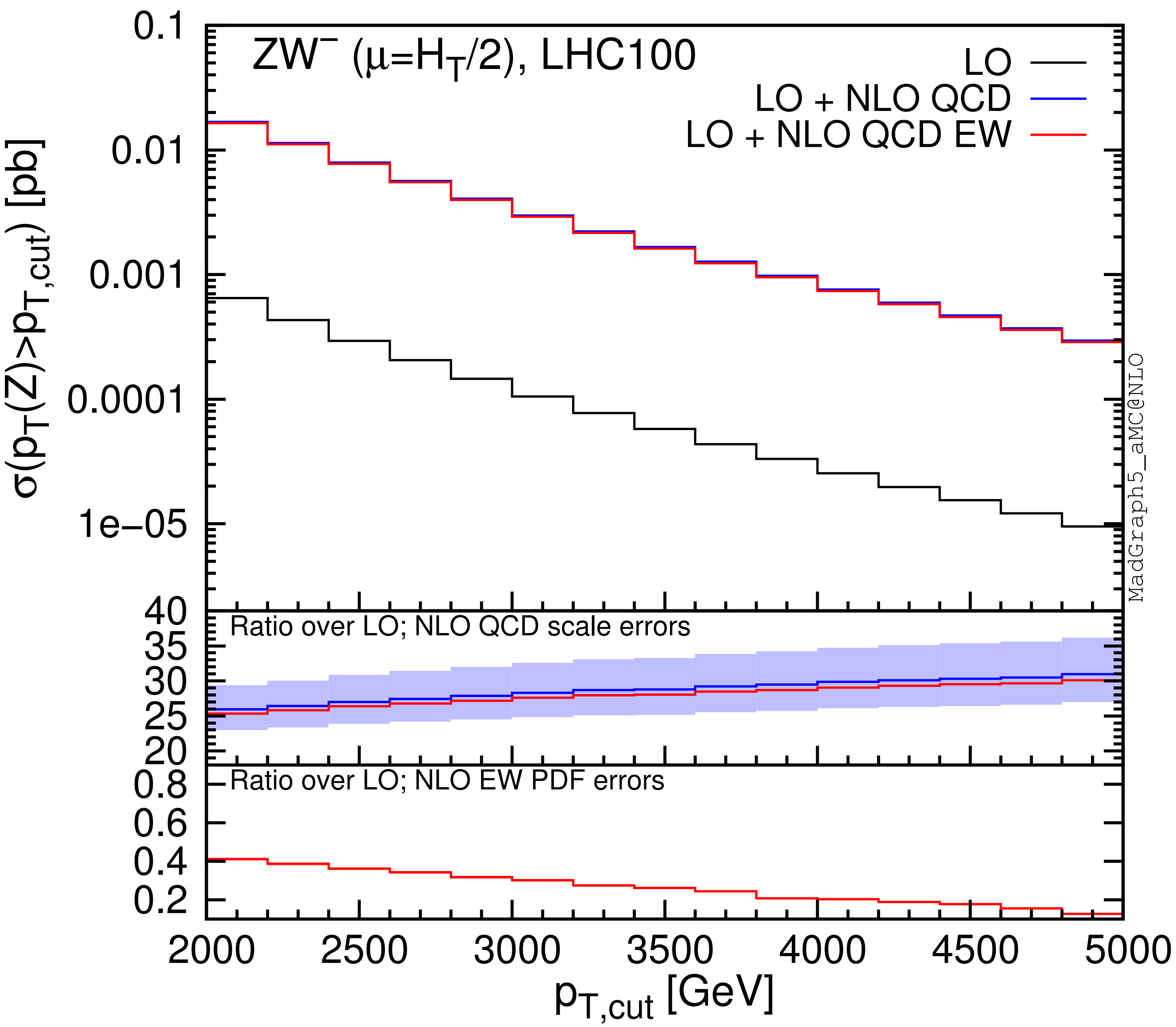
See also Baglio, Ninh,Weber '13

- The large growth for high pt in NLO QCD corrections and photon-quark in NLO EW have similar origins: the same cuts may suppress both effects.

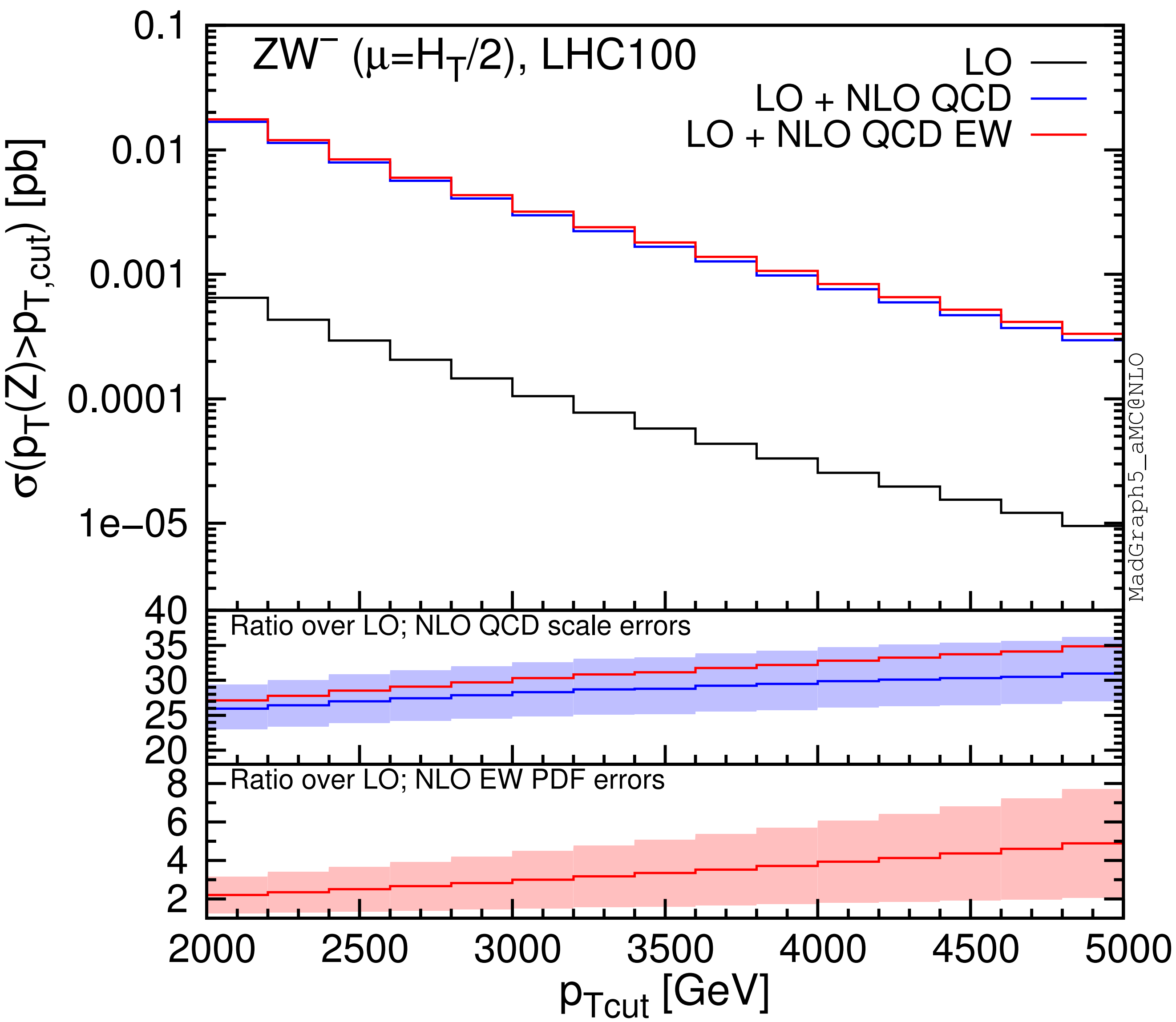
- The photon couples to the W, originating new t-channel configurations that enhance the relative size of photon-quark contributions in NLO EW. NLO QCD corrections do not exhibit similar features.

WZ

cumulative plots



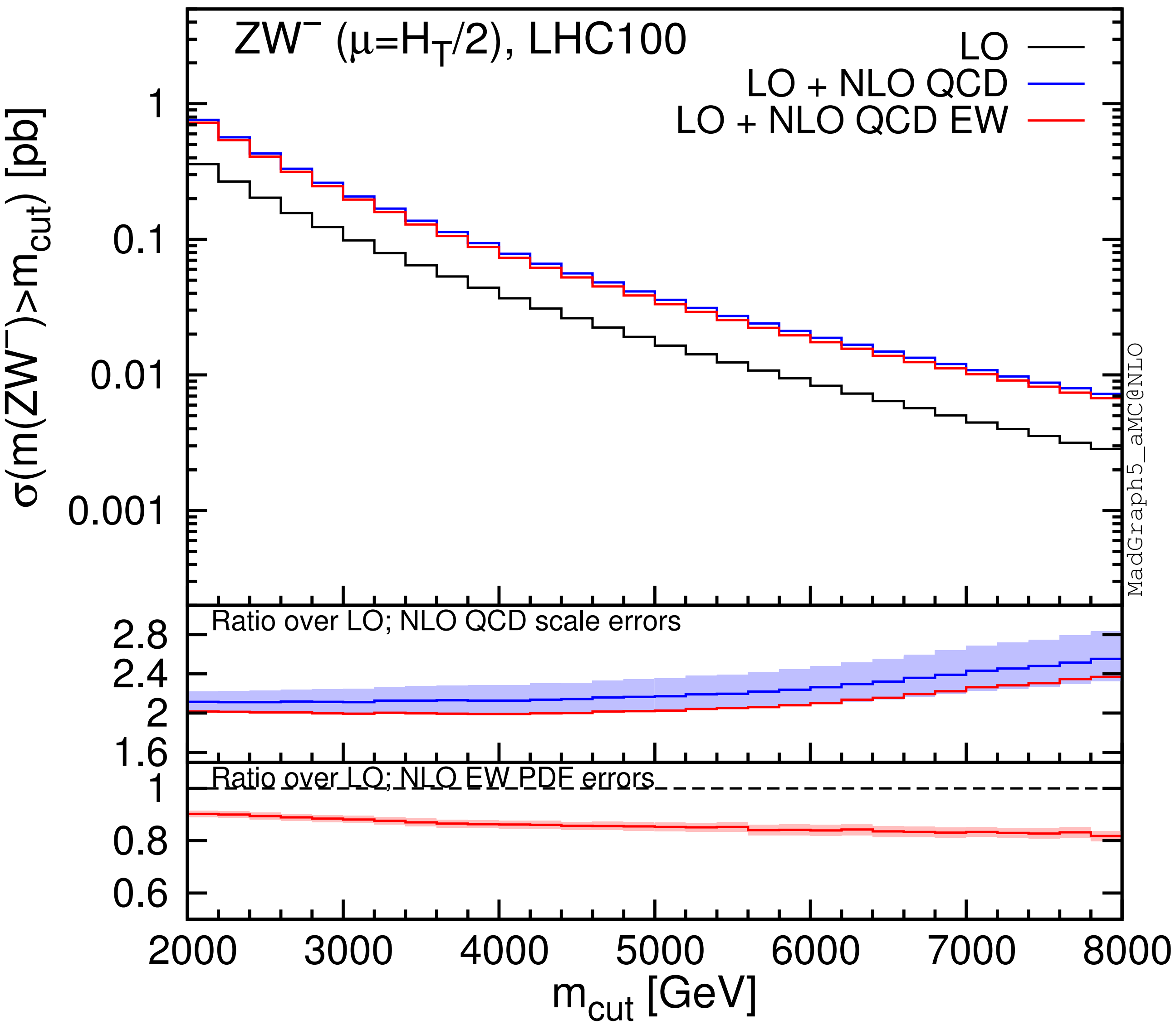
photon PDF **NO**

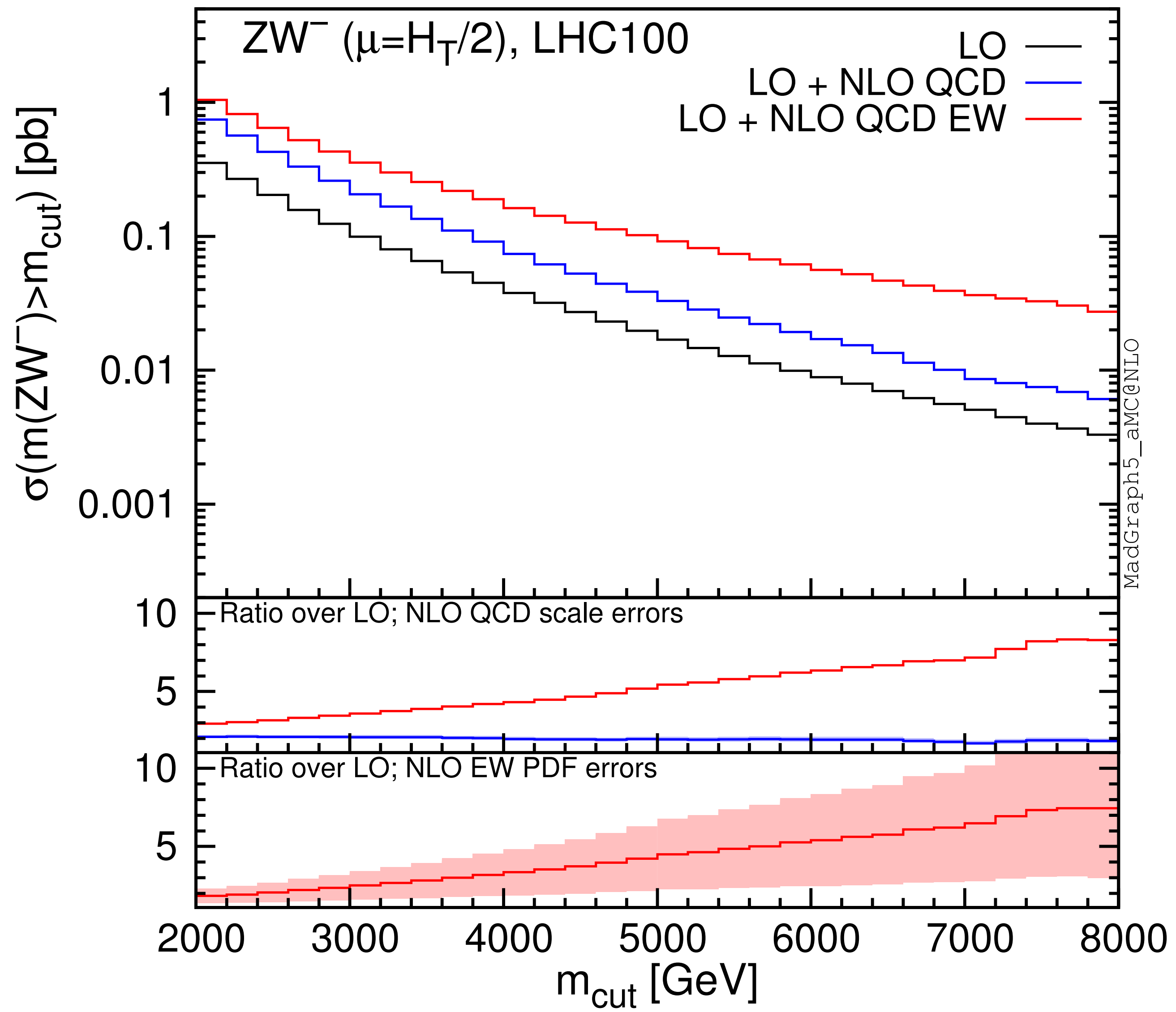


photon PDF **YES**

WZ

cumulative plots



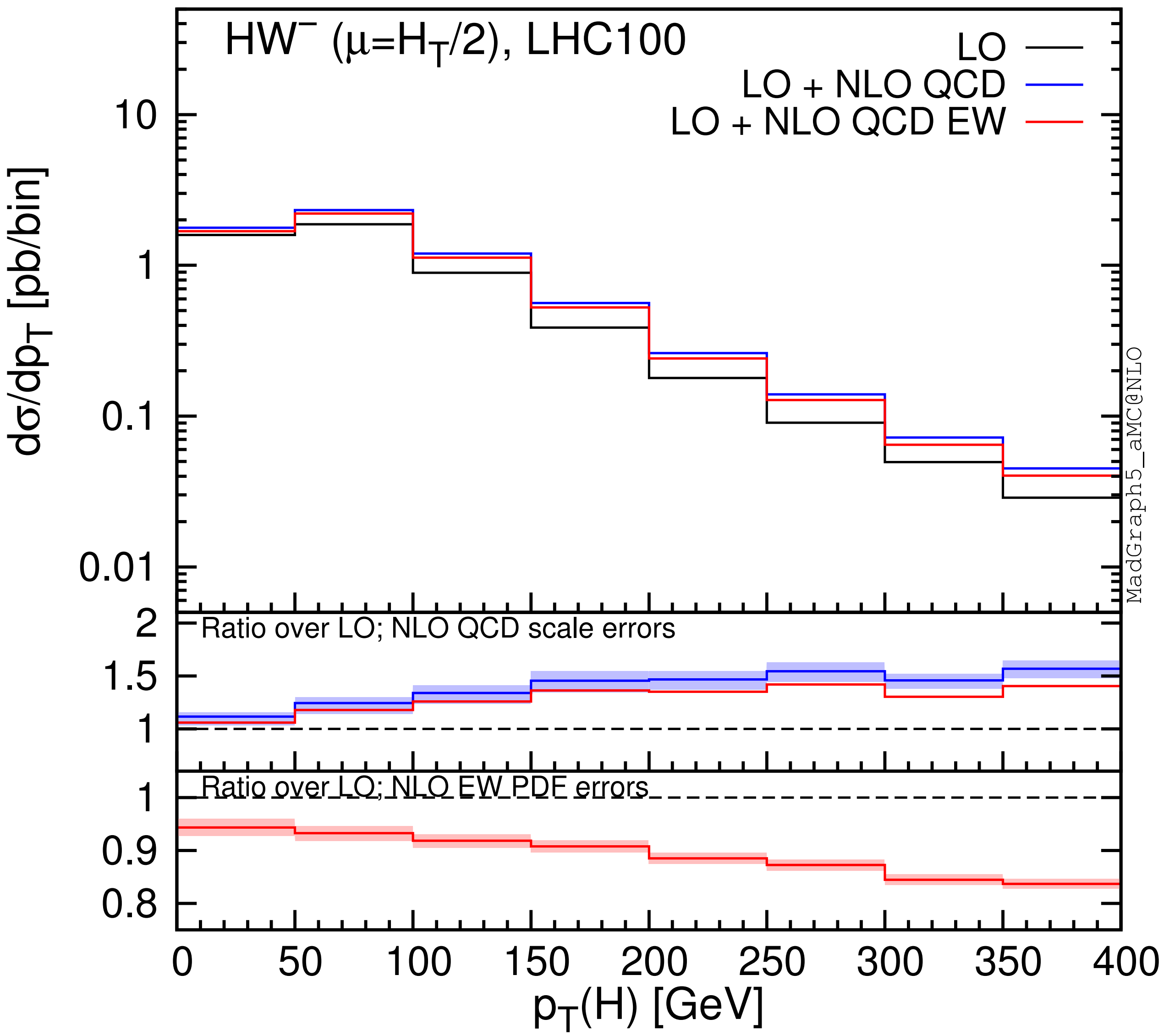


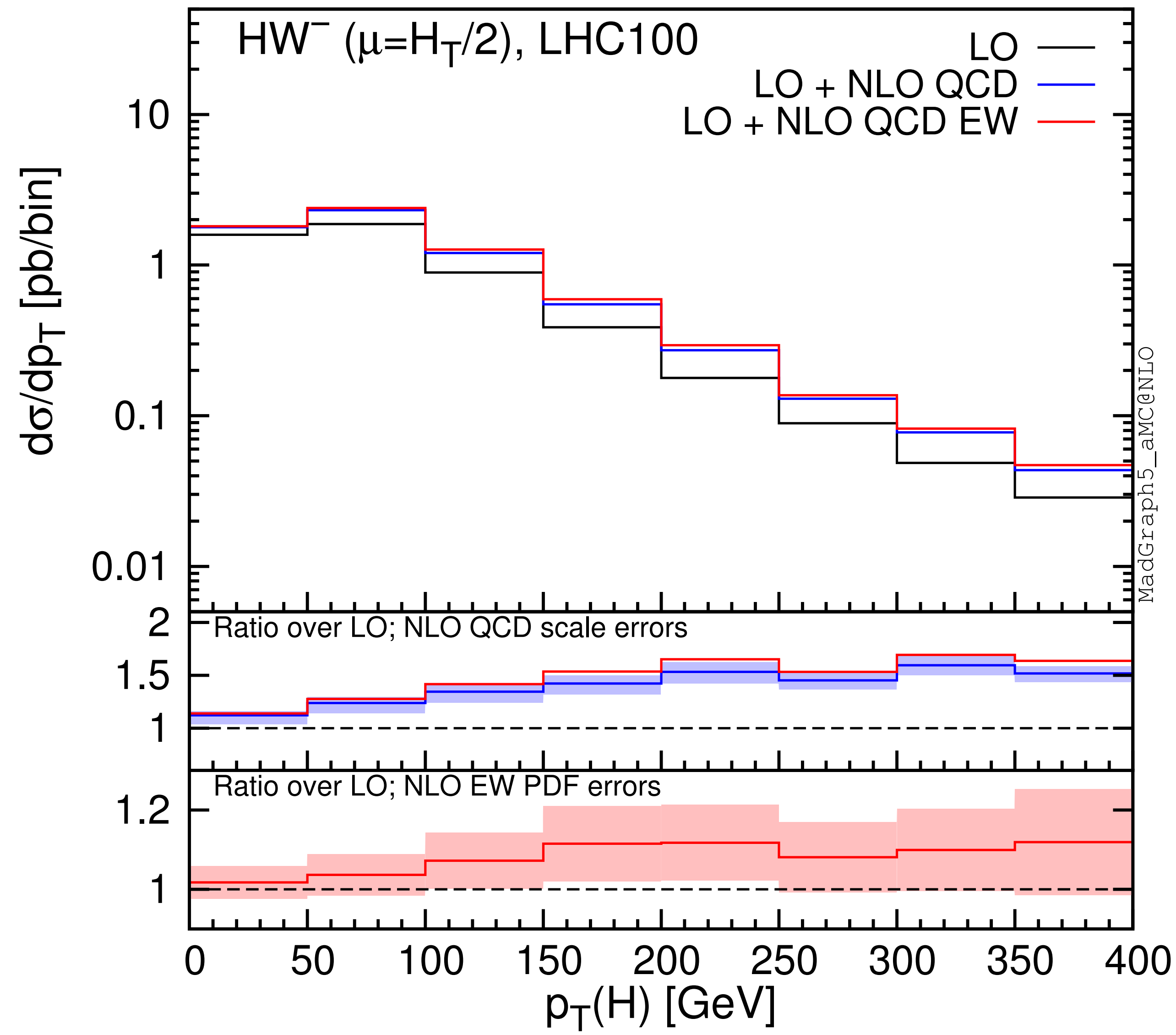
photon PDF **NO** photon PDF **YES**

HW

HW

differential plots

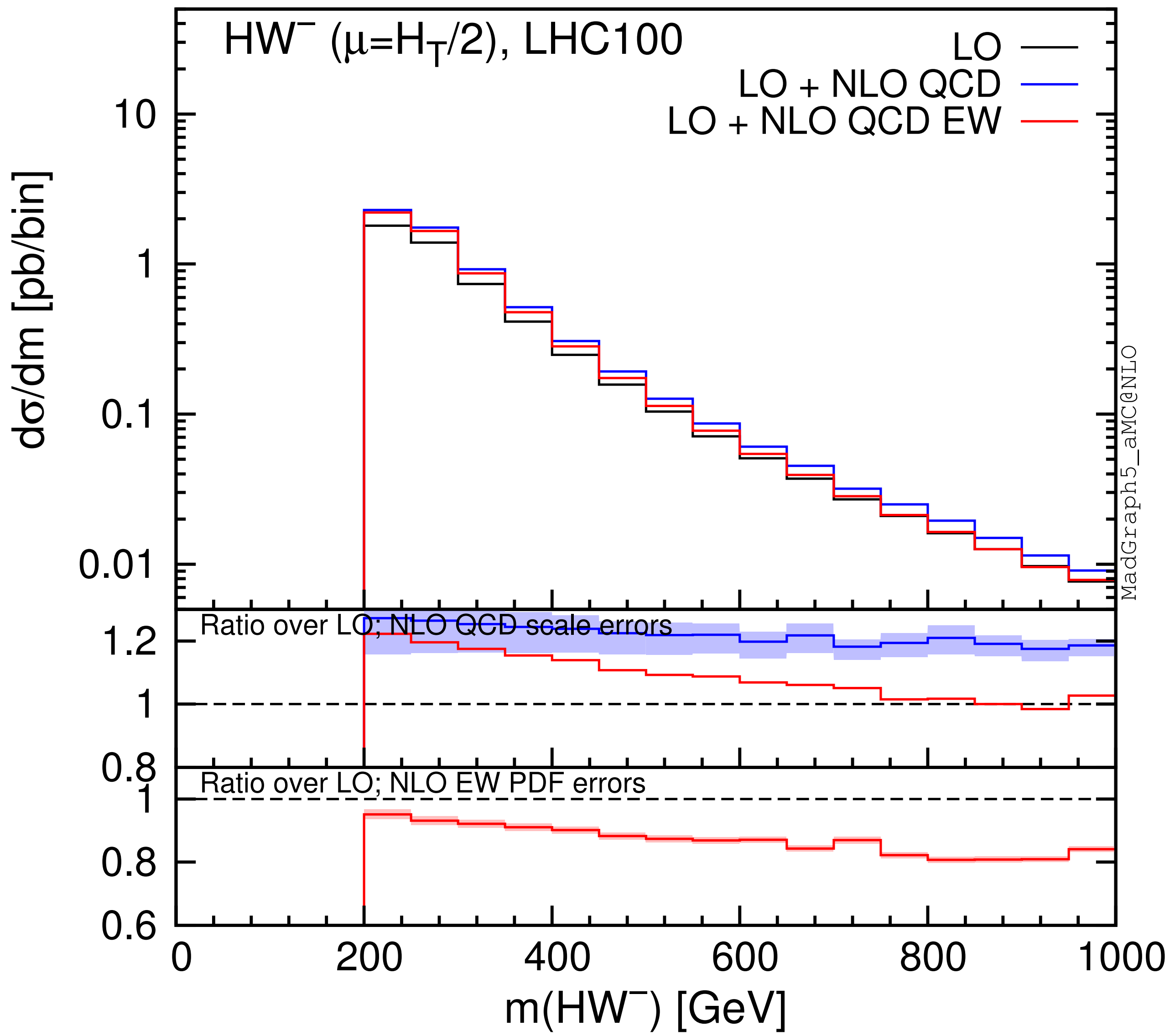




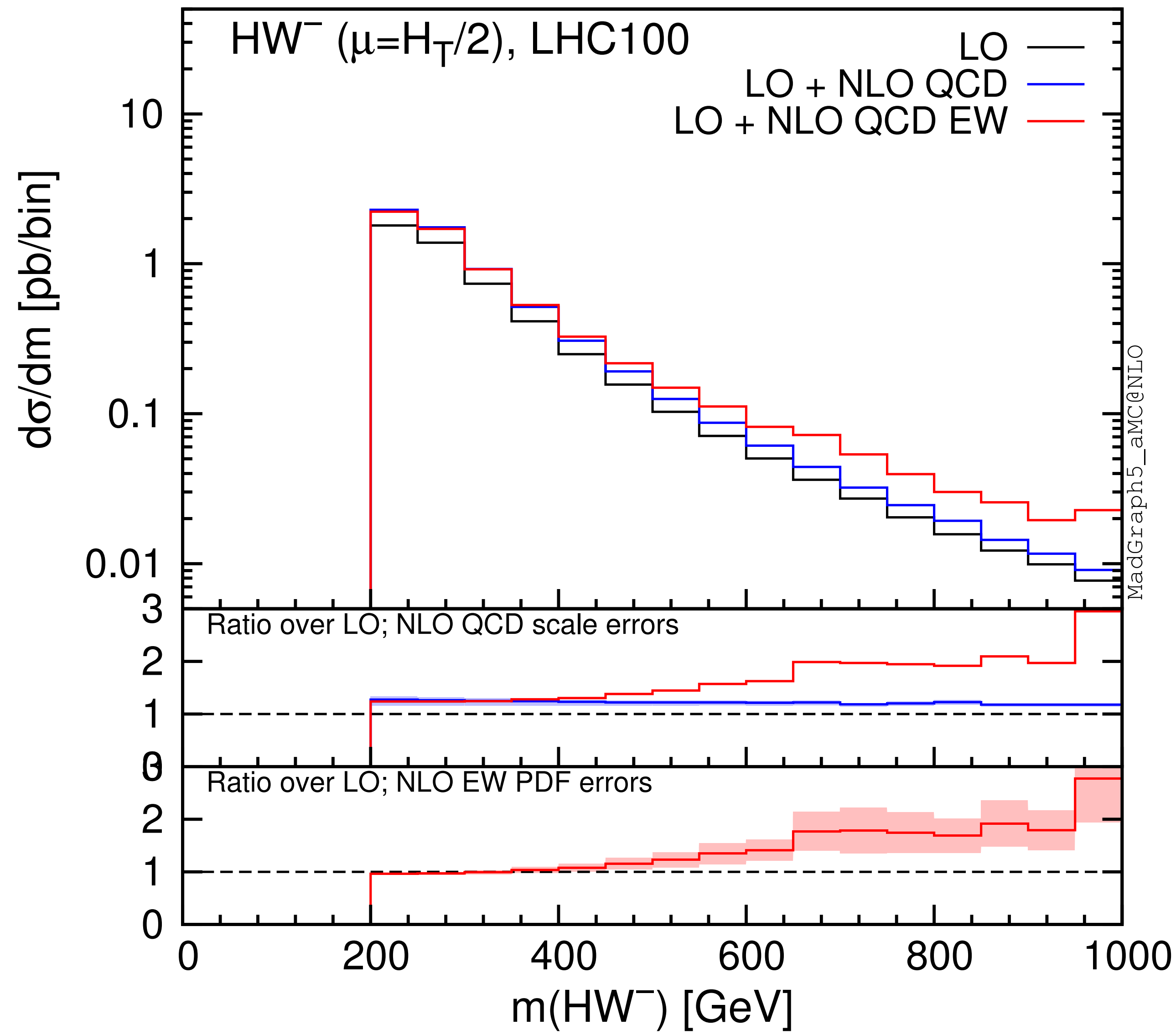
photon PDF **NO** photon PDF **YES**

HW

differential plots



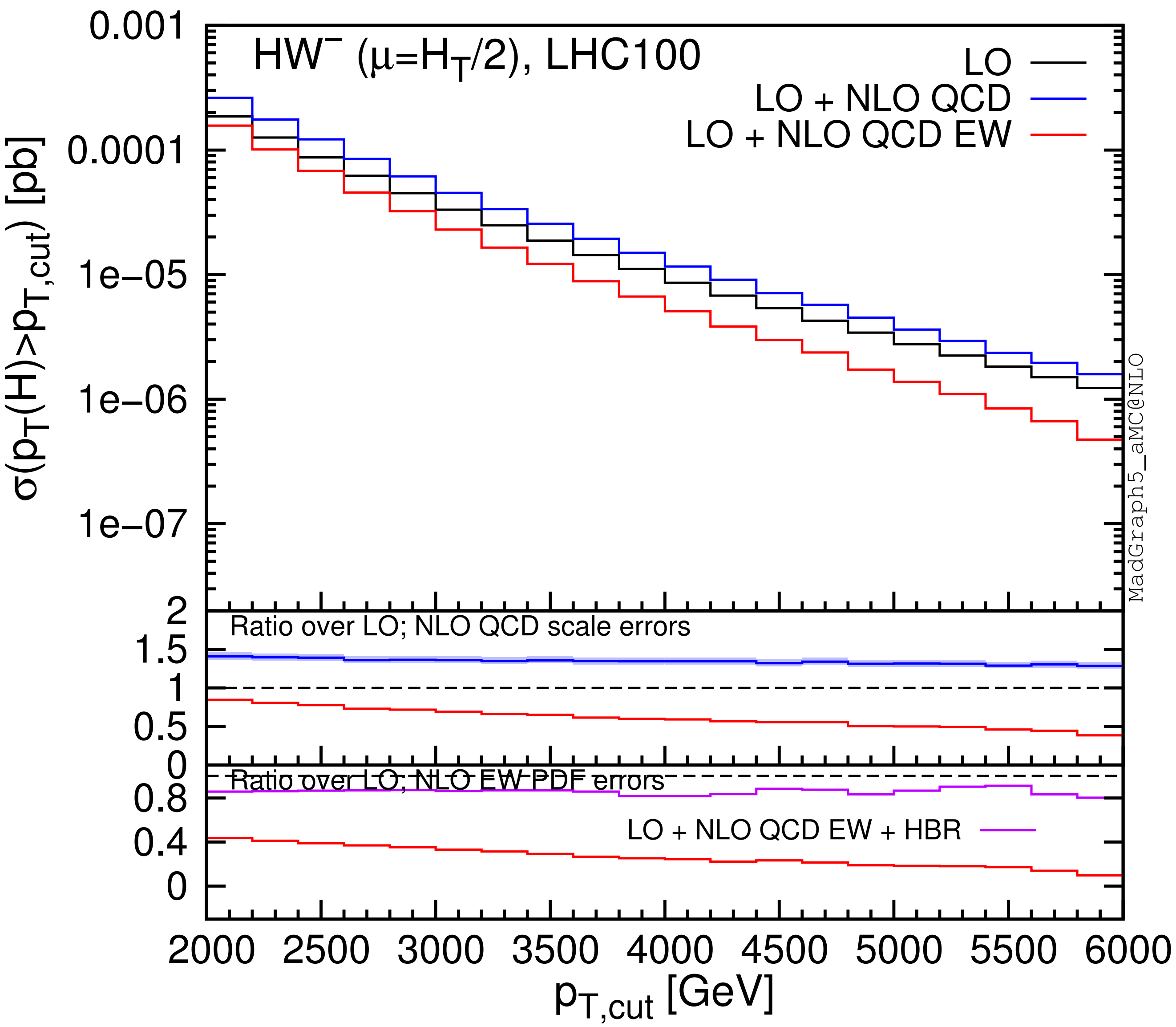
photon PDF **NO**

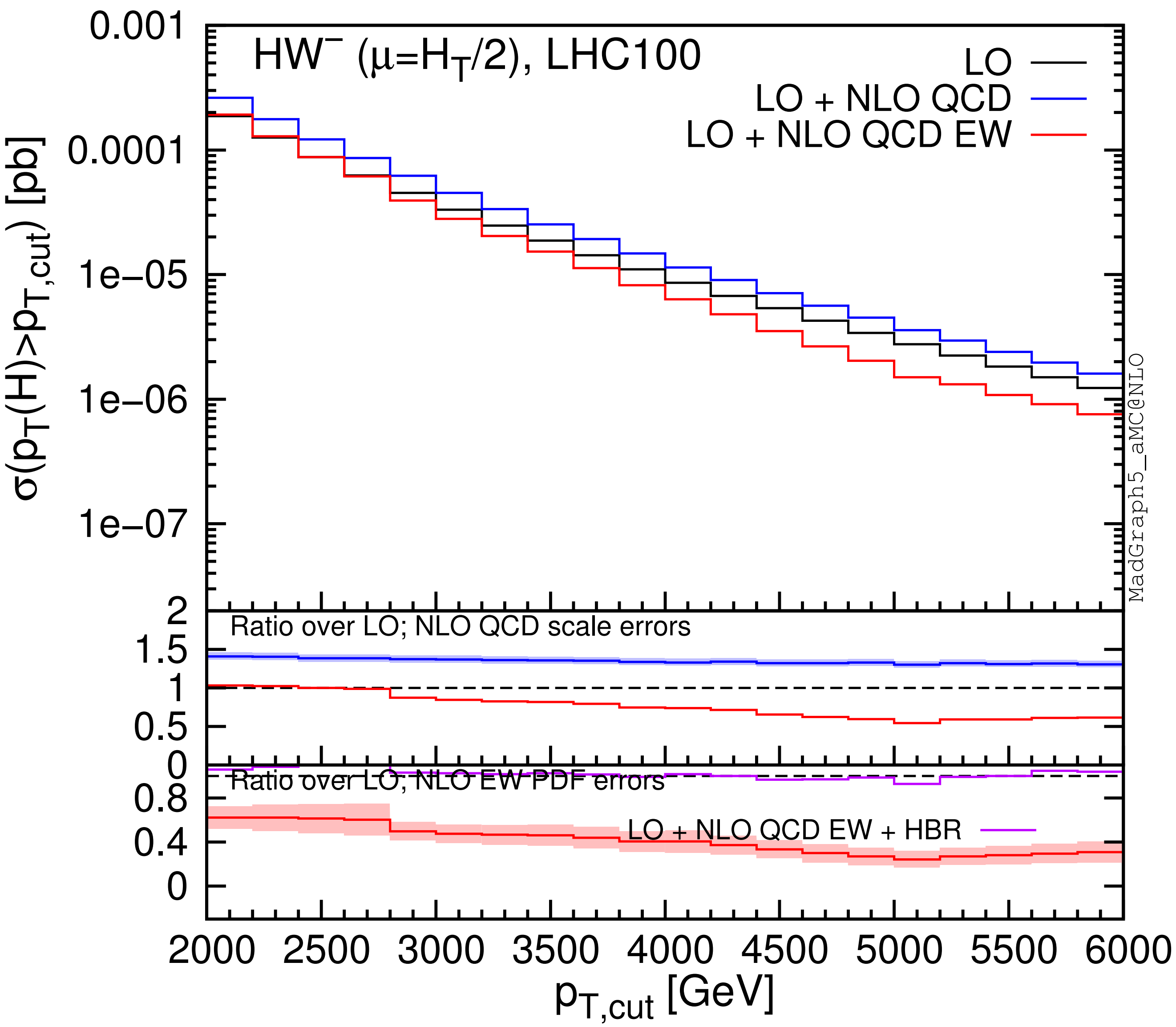


photon PDF **YES**

HW

cumulative plots



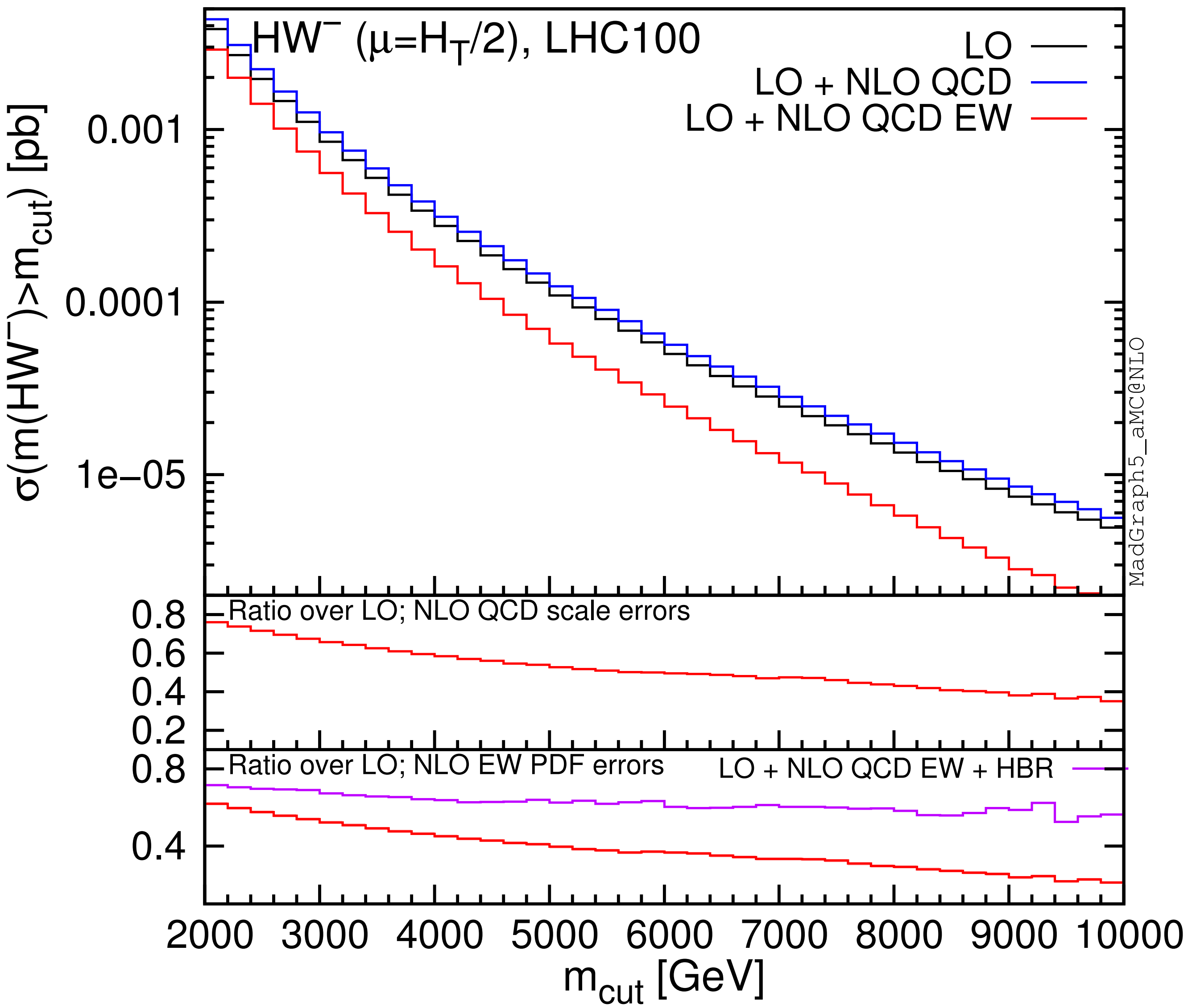


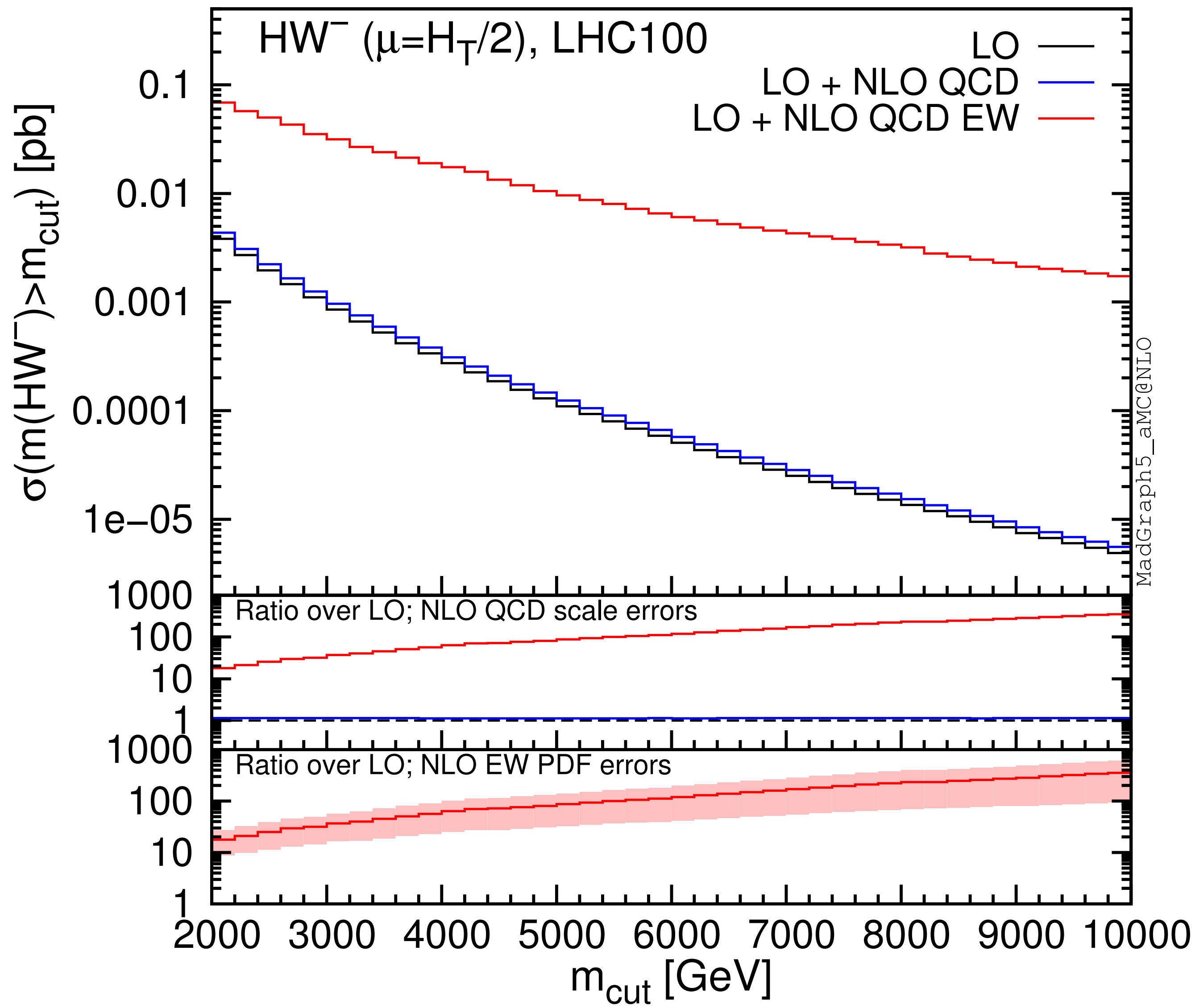
photon PDF **NO**

photon PDF **YES**

HW

cumulative plots

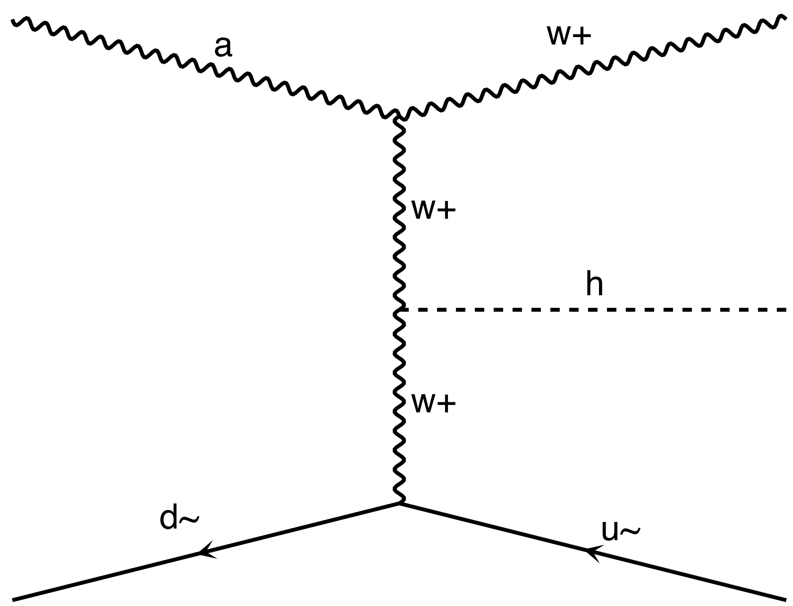




photon PDF **NO**

photon PDF **YES**

HW
what's going on?



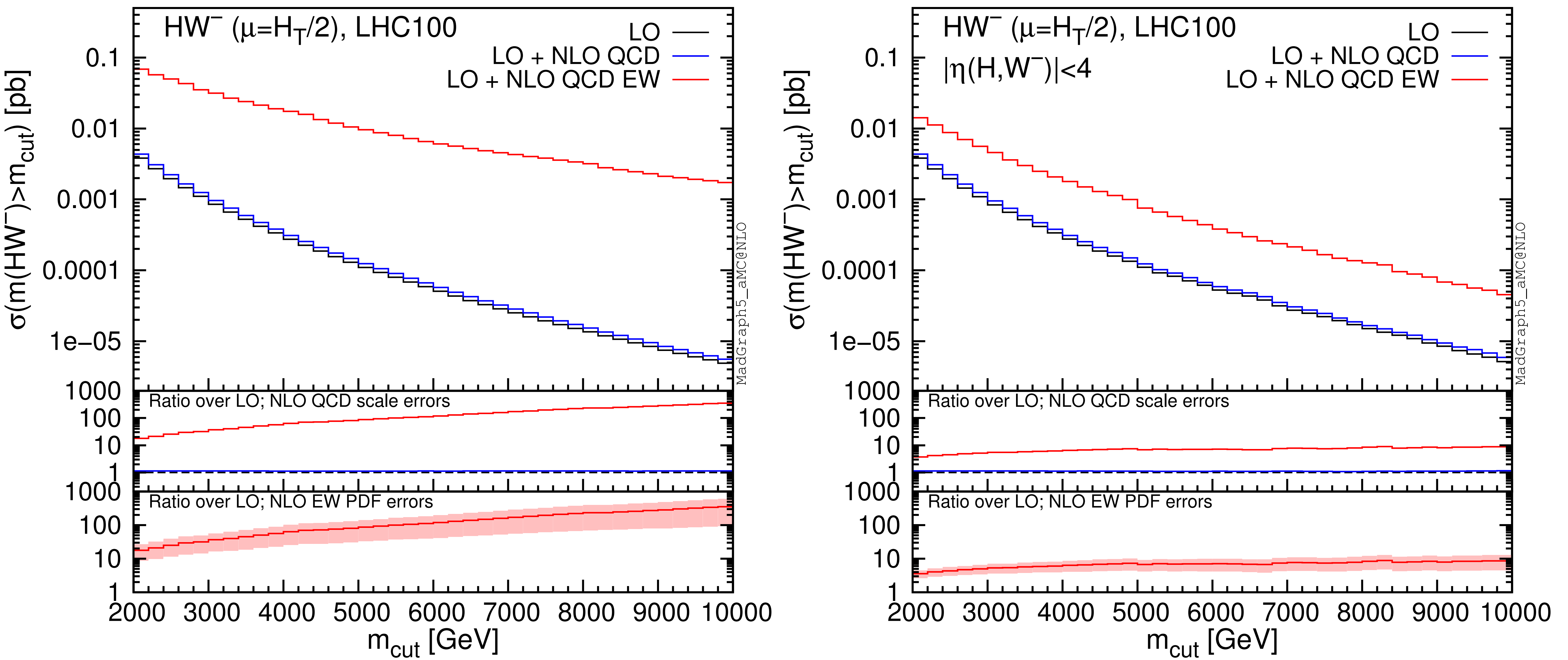
At variance with VV processes, Log^2 enhancements in pt distributions are not present at NLO QCD or EW; there is not photon-quark or gluon-quark to Higgs + jet at tree level that can factorize W or Z soft and collinear emission.

However, HW is produced only via s-channel at LO, while the photon-quark initial state introduces t-channels via W and photon interaction, which are much less suppressed for high m(HW) and lead to huge (100-600) K-factors.

Heavy Boson Radiation (HBR) is of the same perturbative order and the same numerical size of "genuine" NLO EW corrections.

HW

what if additional cuts are applied?

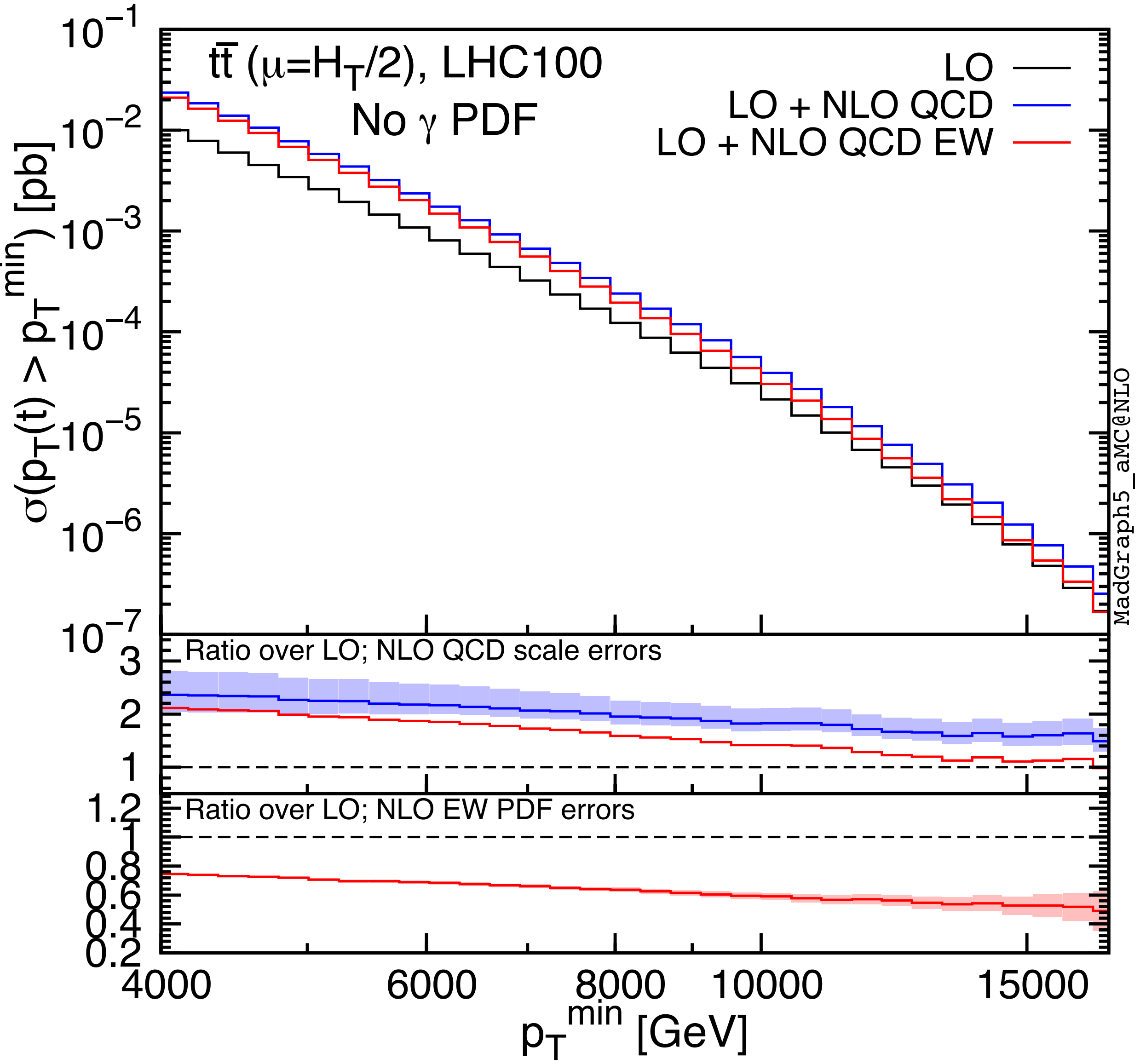


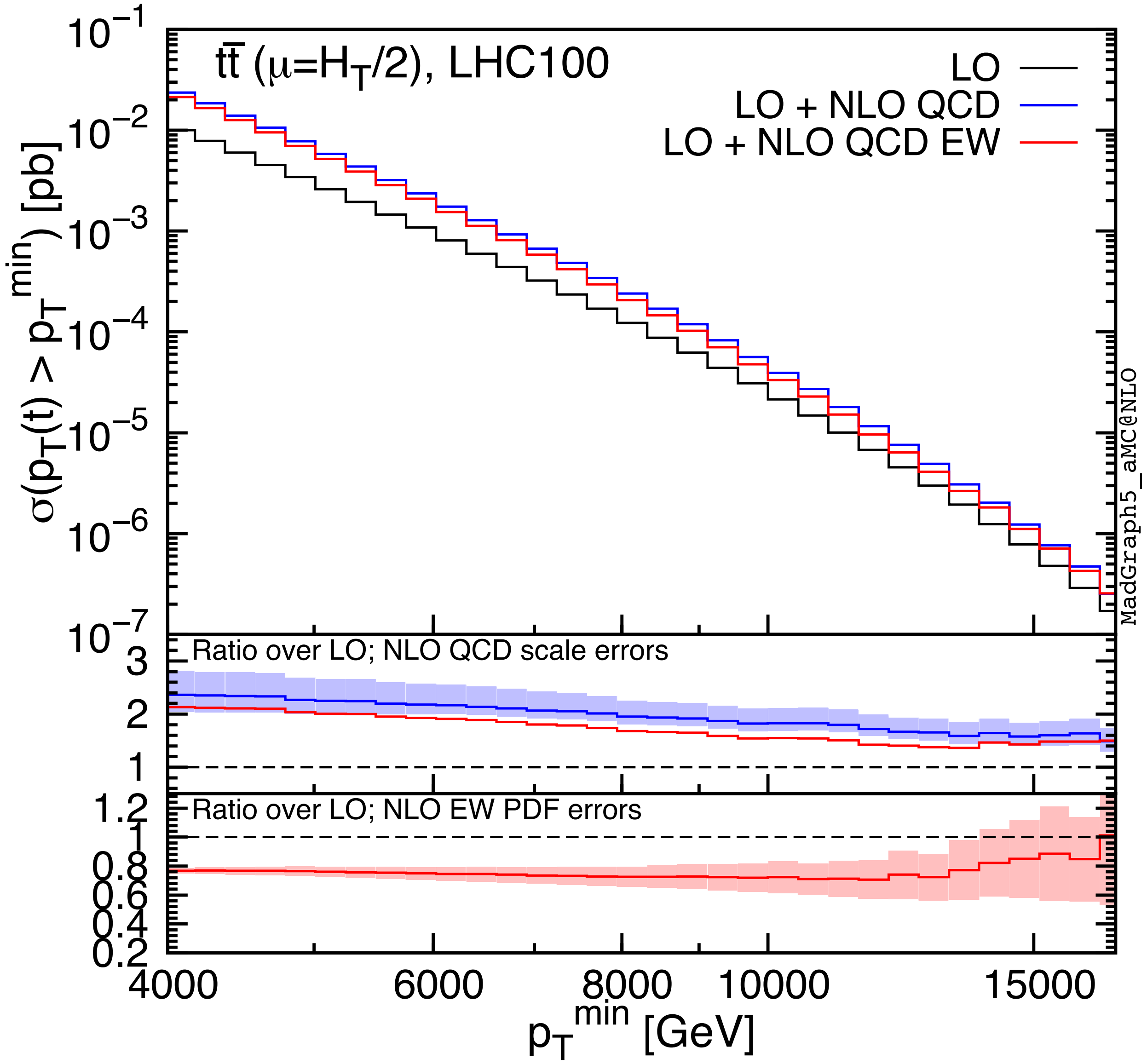
Cuts on H and W pseudo rapidities strongly reduce the photon-quark contribution at high m(HW), without affecting LO and NLO QCD results. Besides HW, **cuts can in general strongly affect size of radiative corrections: Which cuts and on which particles at 100 TeV?**

top-quark pair production

$t\bar{t}$

cumulative plots

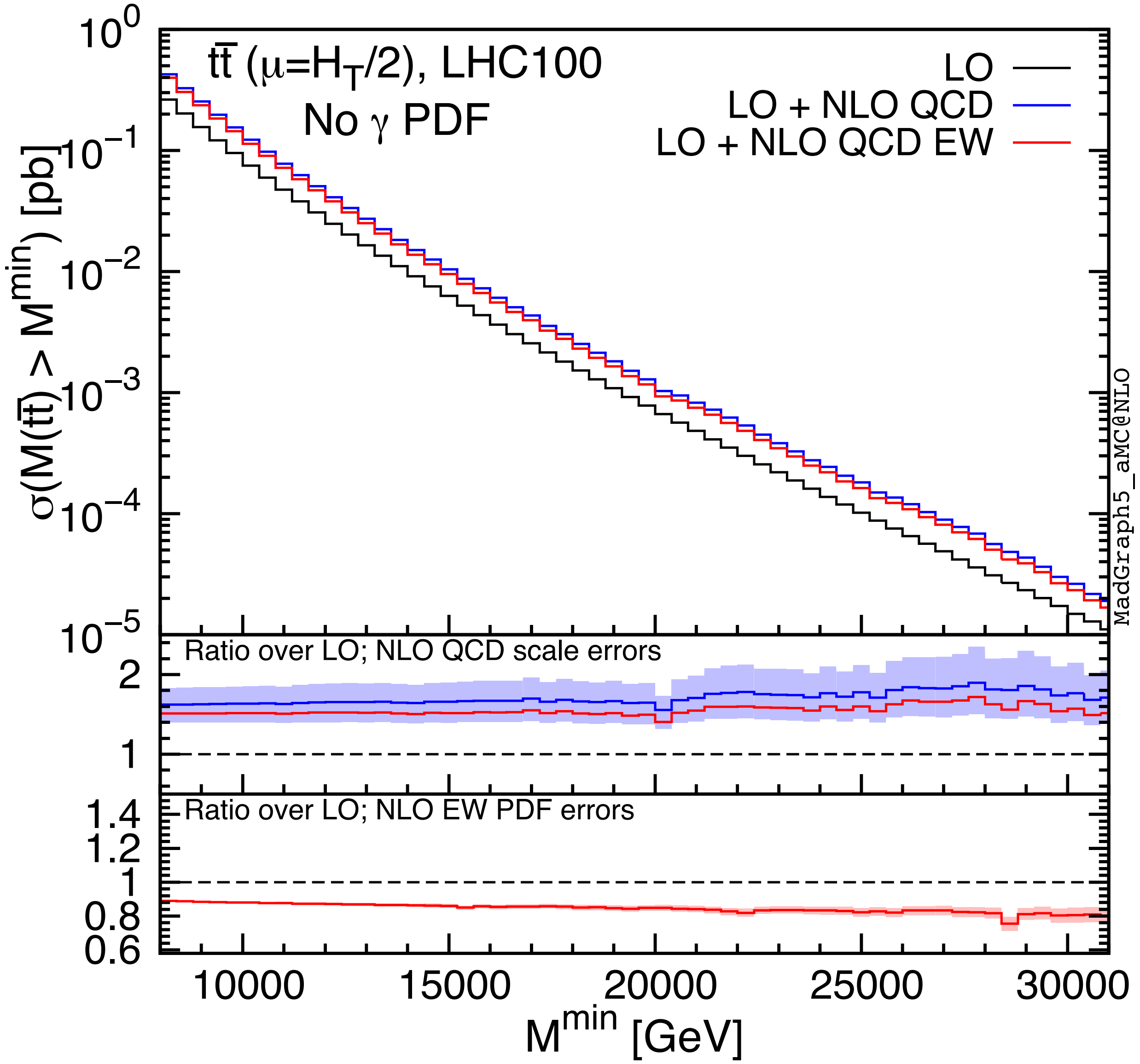


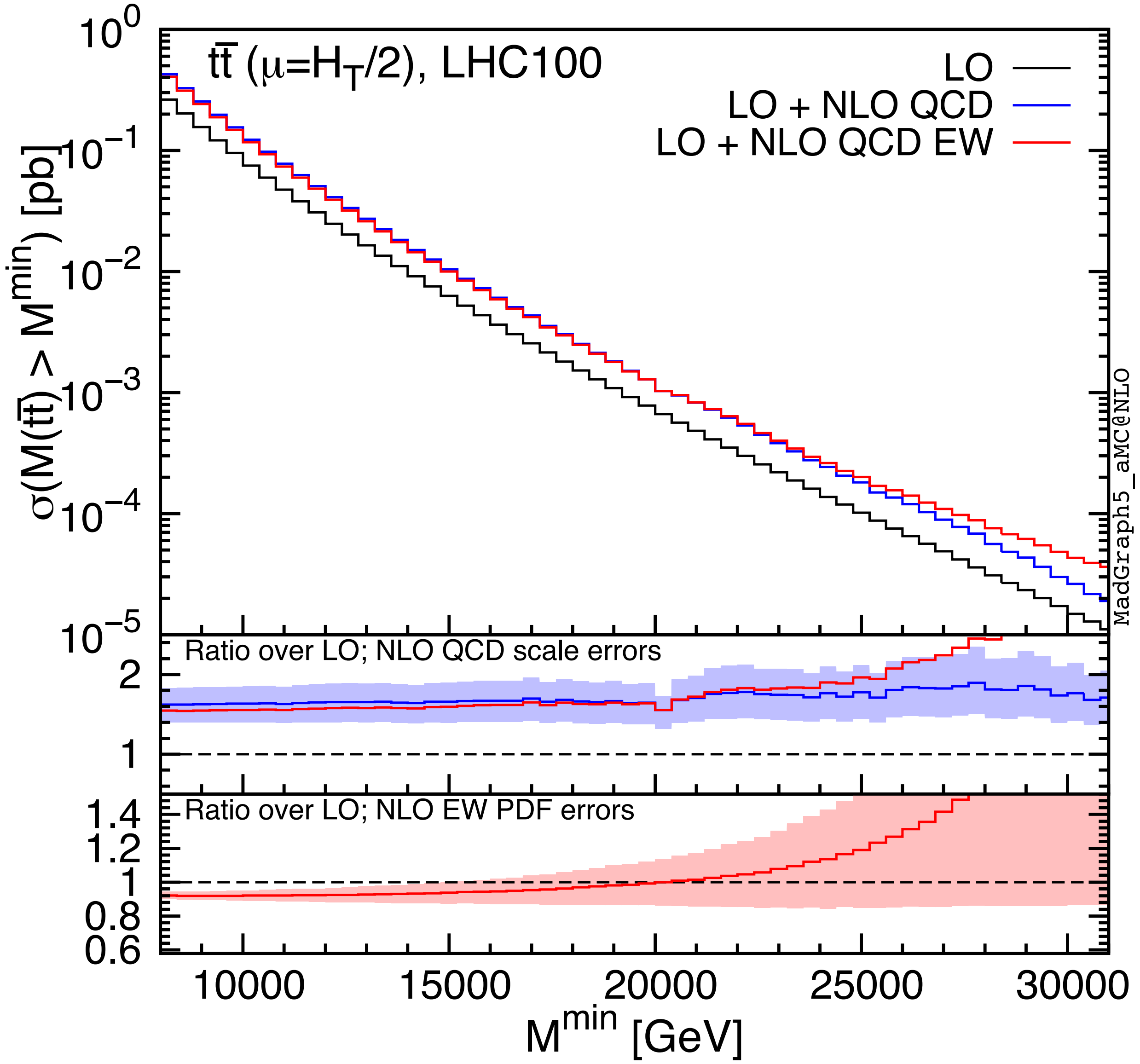


photon PDF **NO** photon PDF **YES**

$t\bar{t}$

cumulative plots





photon PDF **NO**

photon PDF **YES**

CONCLUSION

The **automation** of NLO EW and QCD corrections in **MadGraph5_aMC@NLO** is in progress. NLO QCD and EW corrections to the $t\bar{t}V$ processes have been calculated in a completely automated approach. It is in general possible with **massive final states**.

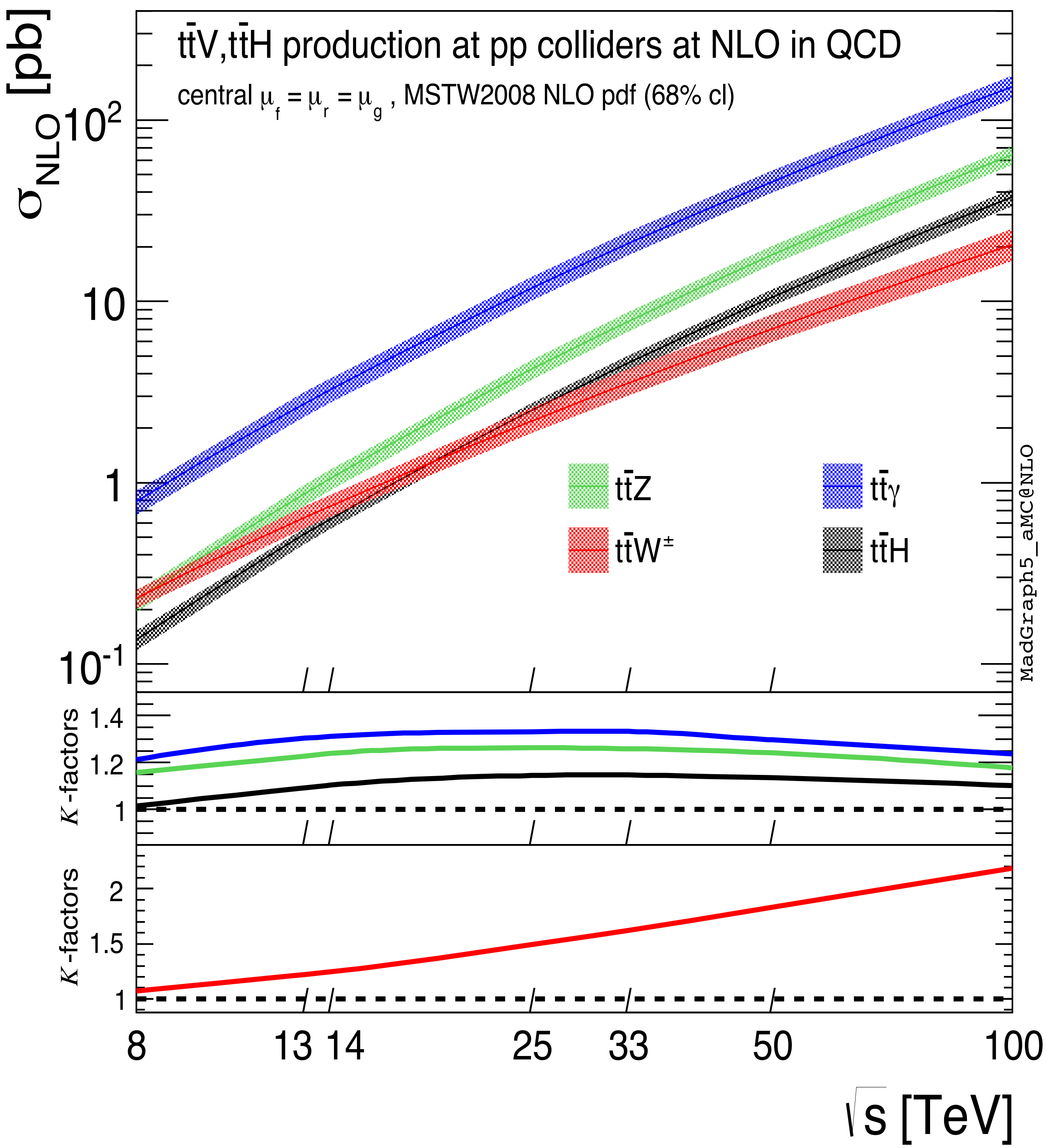
NLO EW corrections at high energies can involve large negative contributions from Sudakov logs, which point to the necessity of going beyond NLO and resumming the logs.
The contribution from photon-induced processes can be huge and with very large uncertainties. However, this does not necessarily apply to all processes and distributions. Cuts may be essential for a realistic prediction.

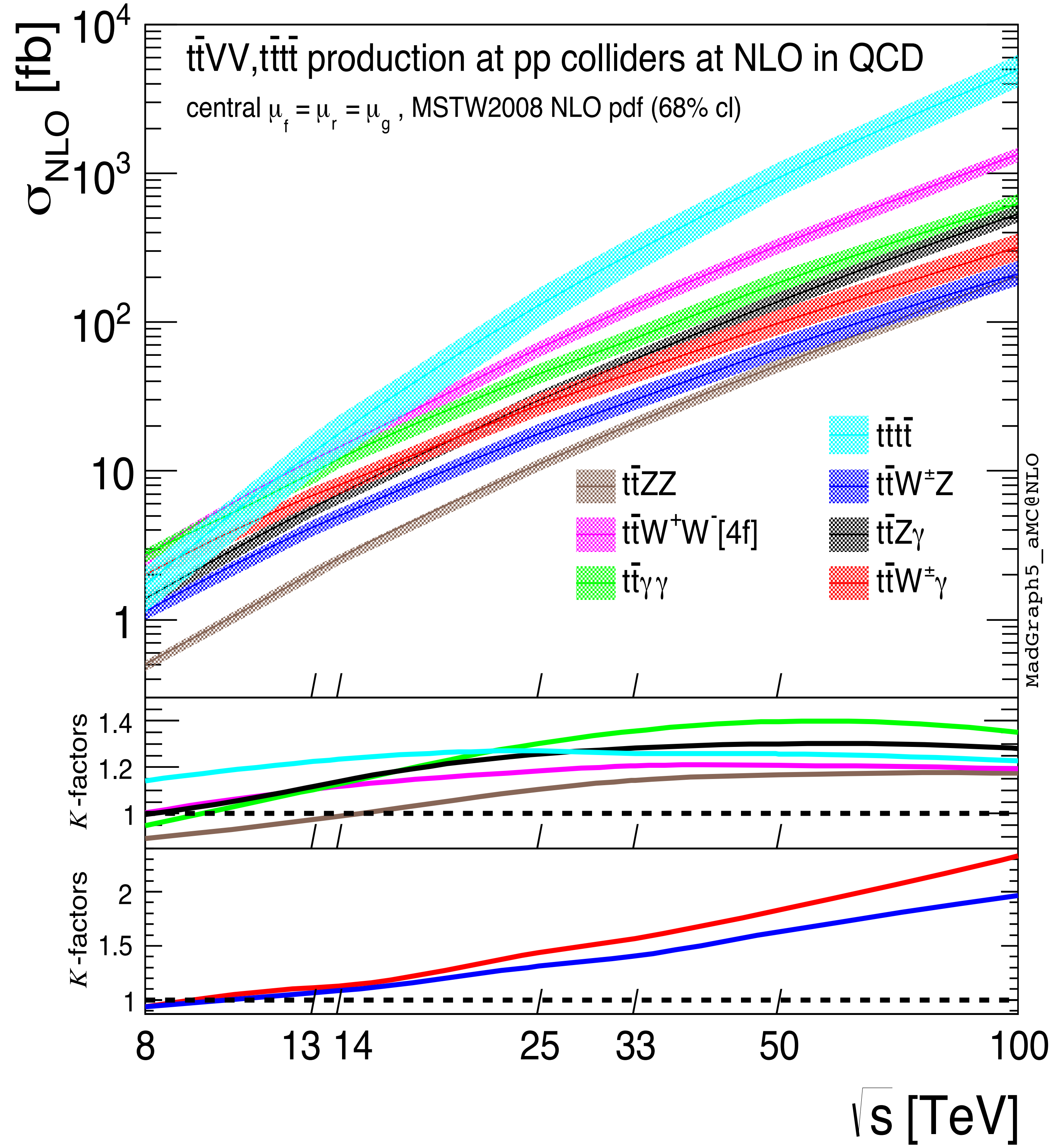
OUTLOOK

- Complete the automation of EW+QCD corrections for all processes
- Match NLO EW corrections to shower effects
- More pheno studies, playing with the tools

EXTRA SLIDES

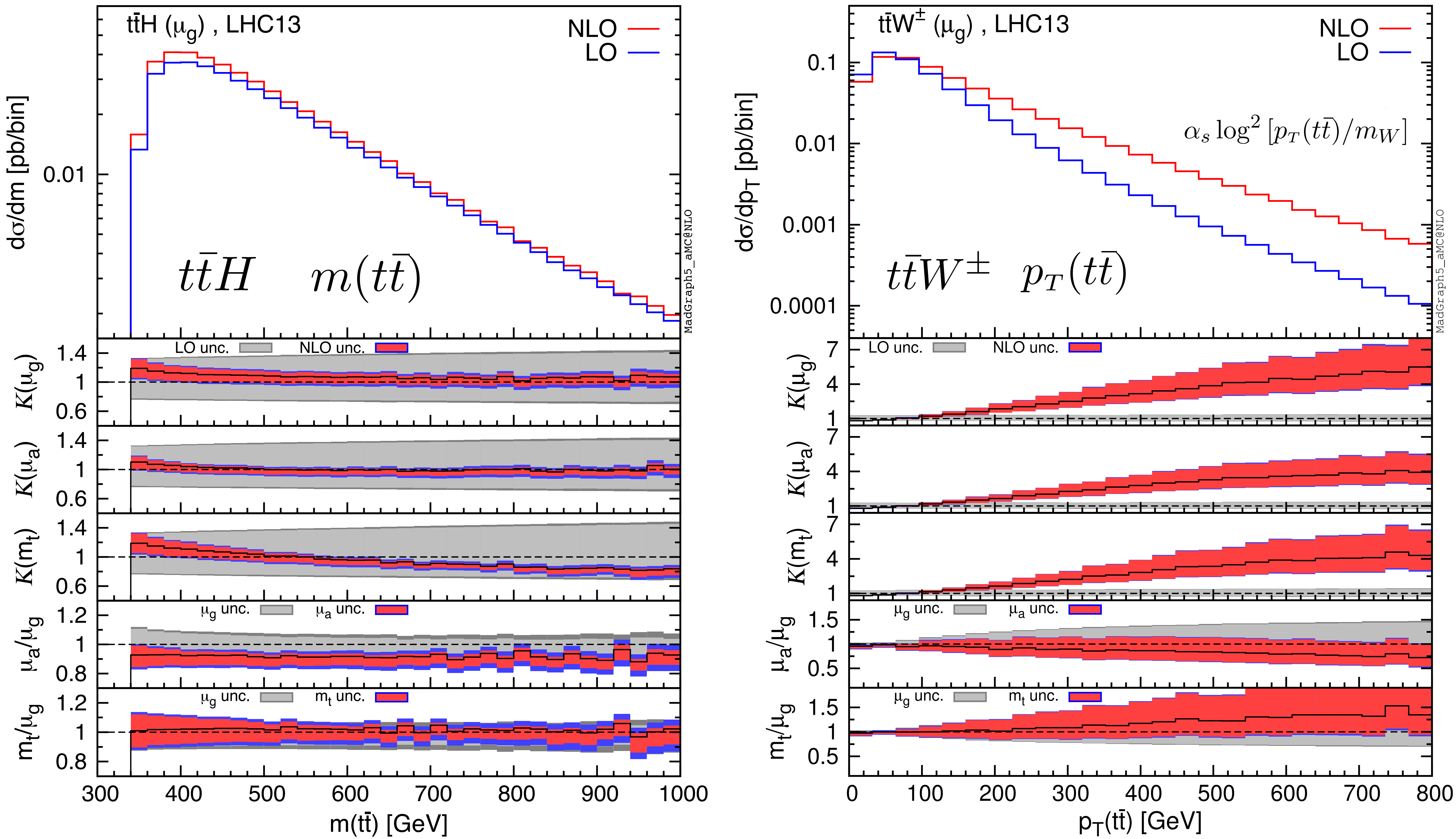
Energy dependence





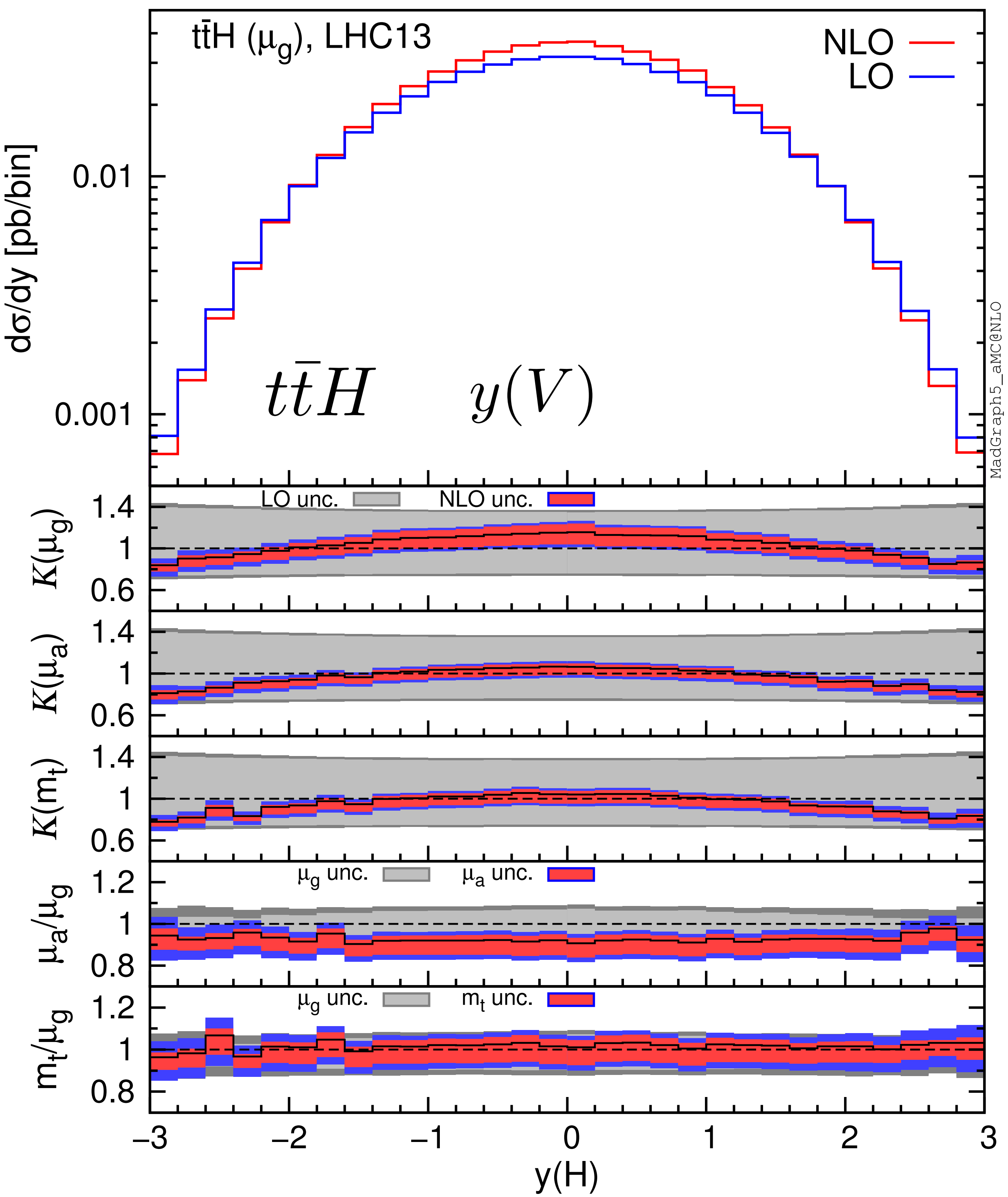
Maltoni, DP, Tsinikos '15

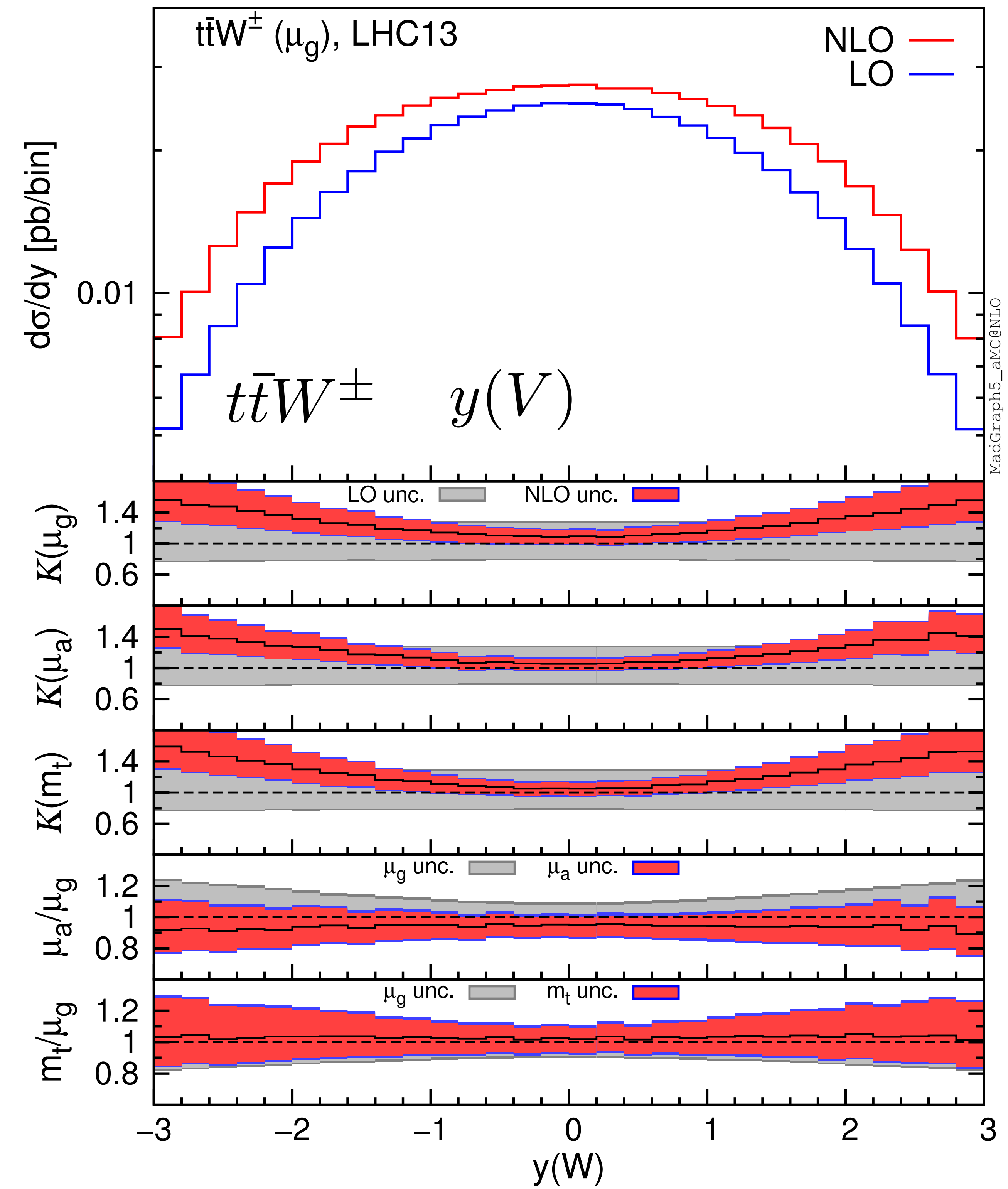
Distributions: representative results at fixed order



Maltoni, DP, Tsinikos '15

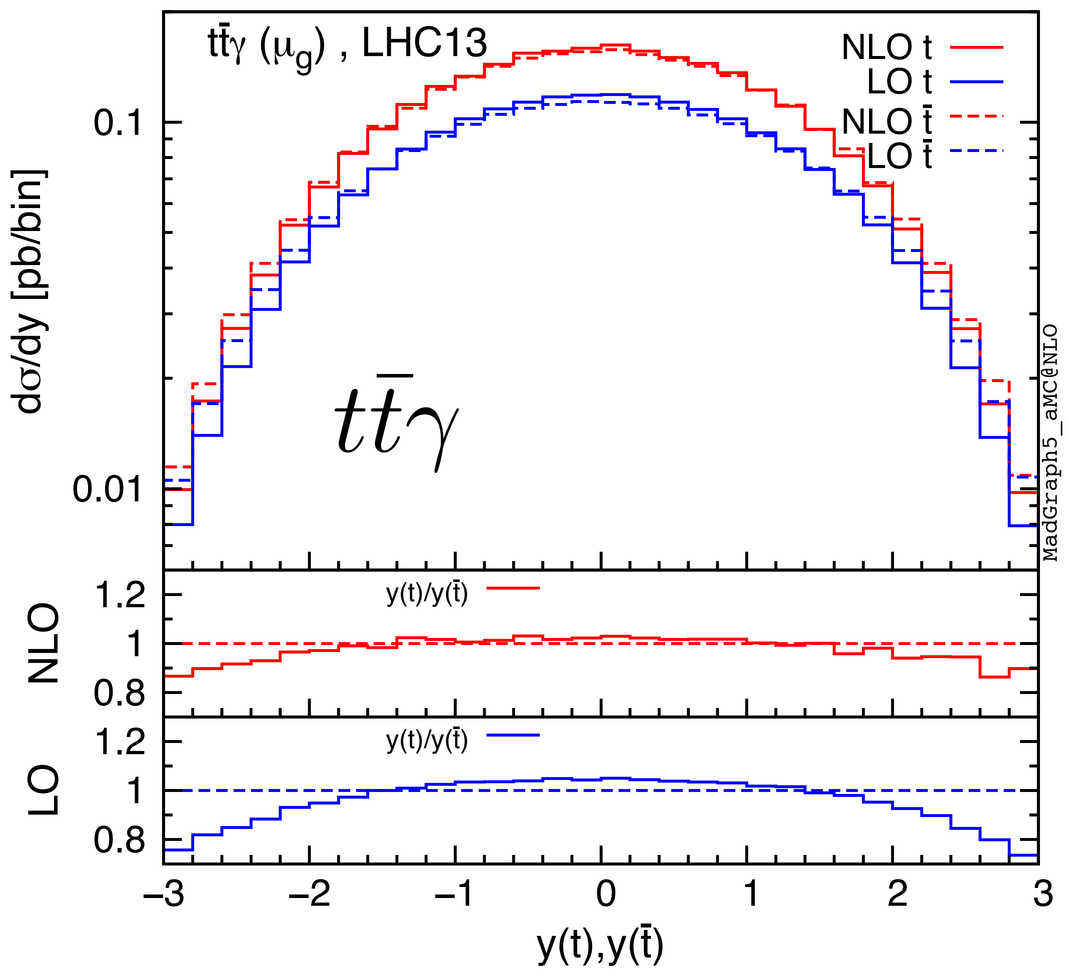
Distributions: representative results at fixed order

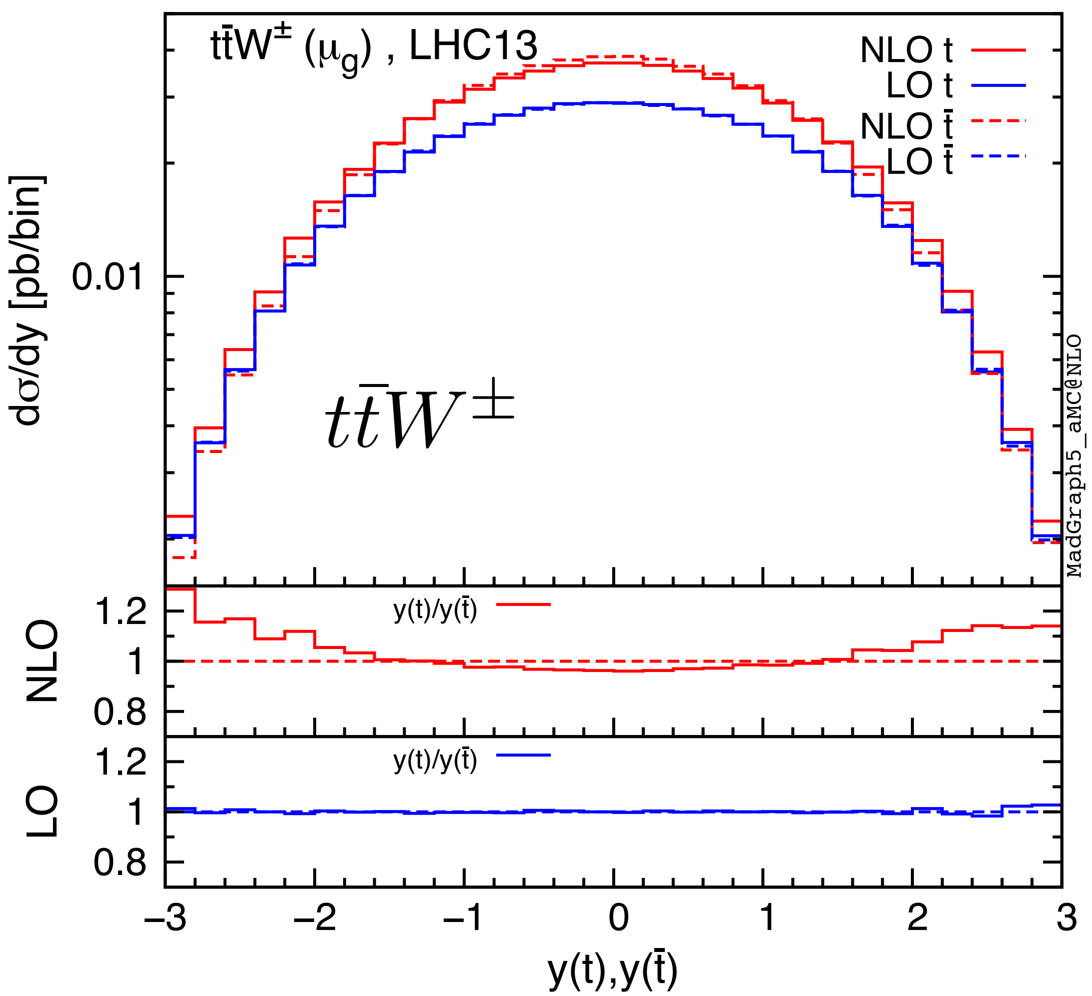




Maltoni, DP, Tsinikos '15

Distributions: representative results at fixed order





Central Asymmetries

13 TeV A_c [%]	$t\bar{t}H$	$t\bar{t}Z$	$t\bar{t}W^{\pm}$	$t\bar{t}\gamma$
LO	-	$-0.12^{+0.01}_{-0.01}\ {}^{+0.01}_{-0.02} \pm 0.03$	-	$-3.93^{+0.26}_{-0.23}\ {}^{+0.14}_{-0.11} \pm 0.03$
NLO	$1.00^{+0.30}_{-0.20}\ {}^{+0.06}_{-0.04} \pm 0.02$	$0.85^{+0.25}_{-0.17}\ {}^{+0.06}_{-0.05} \pm 0.03$	$2.90^{+0.67}_{-0.47}\ {}^{+0.06}_{-0.07} \pm 0.07$	$-1.79^{+0.50}_{-0.39}\ {}^{+0.06}_{-0.09} \pm 0.06$

Maltoni, DP, Tsinikos ‘15

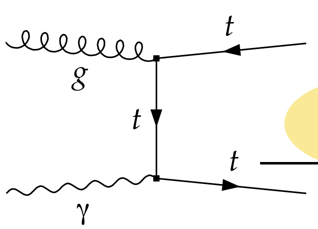
Why do we care about photons in the proton?

2 representative examples:

$t\bar{t}$

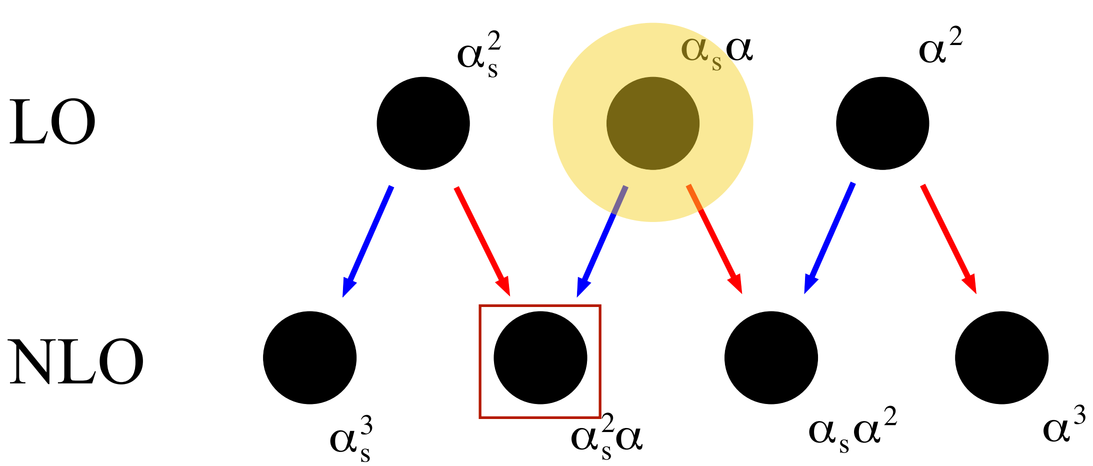
Process	$\sigma_{\rm tot}$ without cuts [pb]	
	Born	correction
$u\bar{u}$	34.25	-1.41
$d\bar{d}$	21.61	-0.228
$s\bar{s}$	4.682	-0.0410
$c\bar{c}$	2.075	-0.0762
gg	407.8	2.08
$g\gamma$		4.45
pp	470.4	4.78

NLO QED



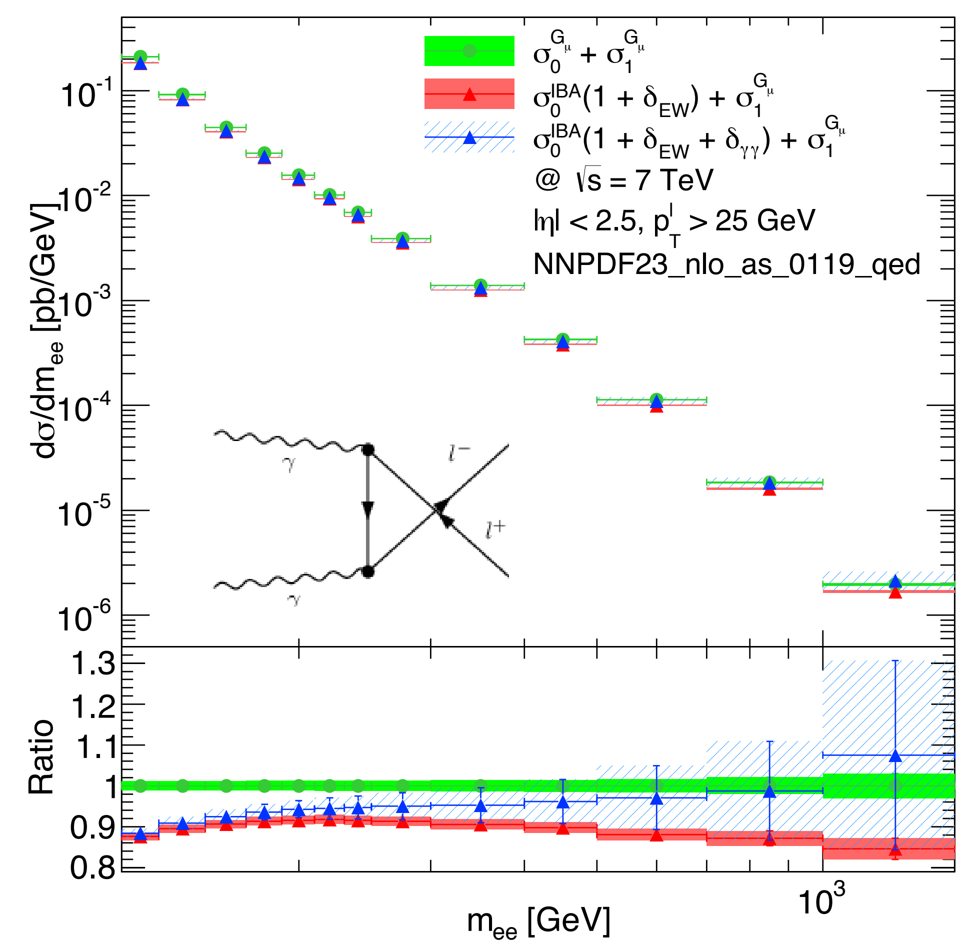
Integrated hadronic cross section for $t\bar{t}$ production at the LHC, at NLO QED

Hollik, Kollar '07 MRST2004QED

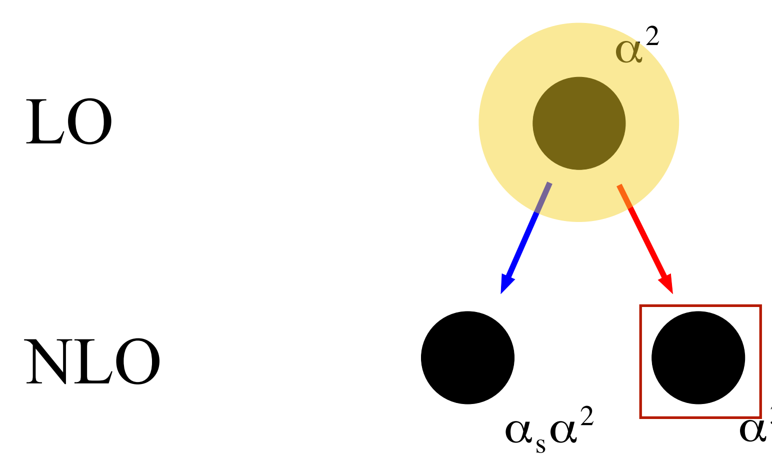


NLO EW

High-mass Drell-Yan, $Z \to e^+e^-$



Carrazza '14 NNPDF2.3QED

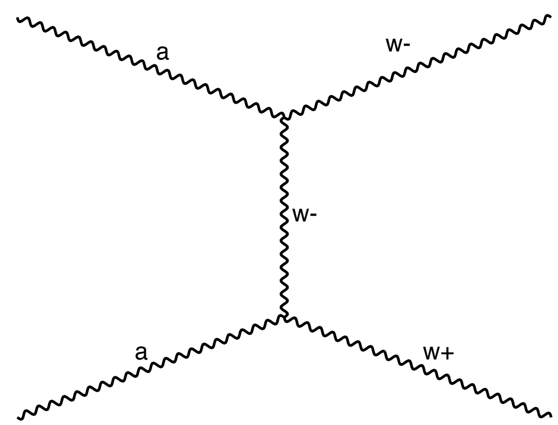


NLO EW

Set-up and photon-PDF perturbative orders

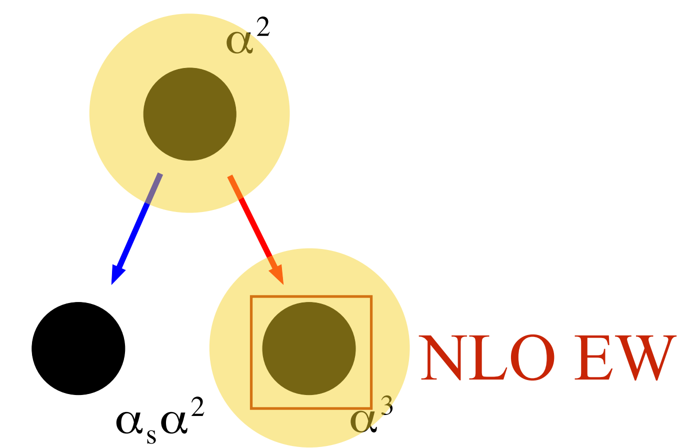
G_μ scheme, NNPDF2.3_QED, $\mu = \frac{H_T}{2}$, $\frac{1}{2}\mu \leq \mu_R, \mu_F \leq 2\mu$

WW

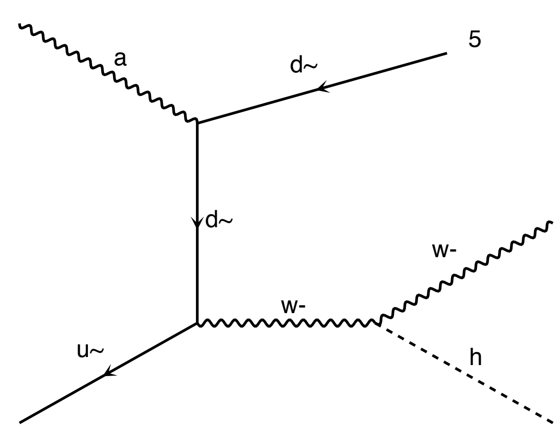


LO

NLO

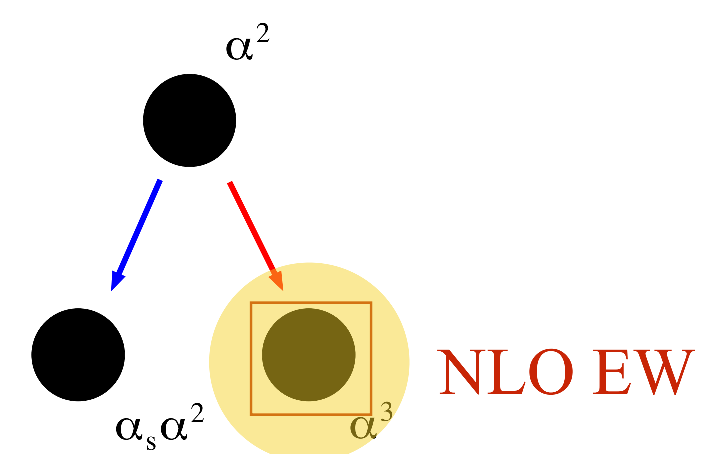


ZZ, ZW,
HZ, HW

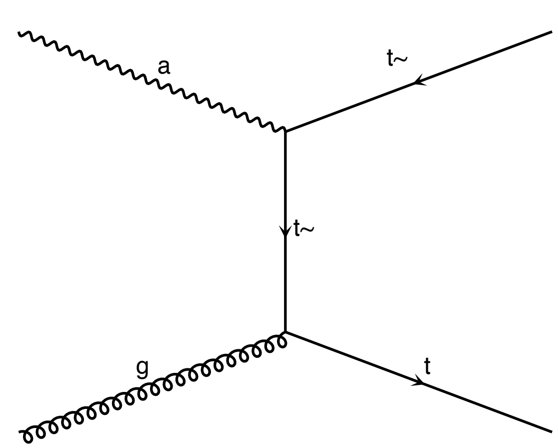


LO

NLO

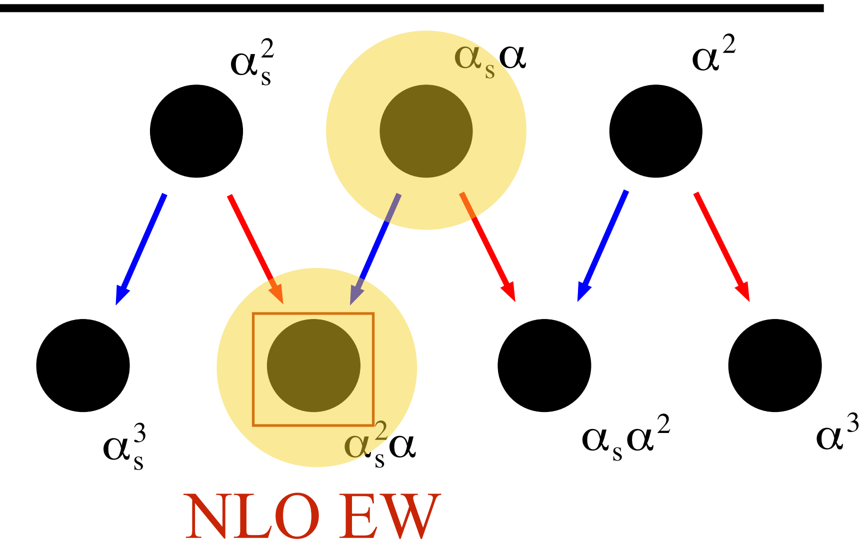


$t\bar{t}$

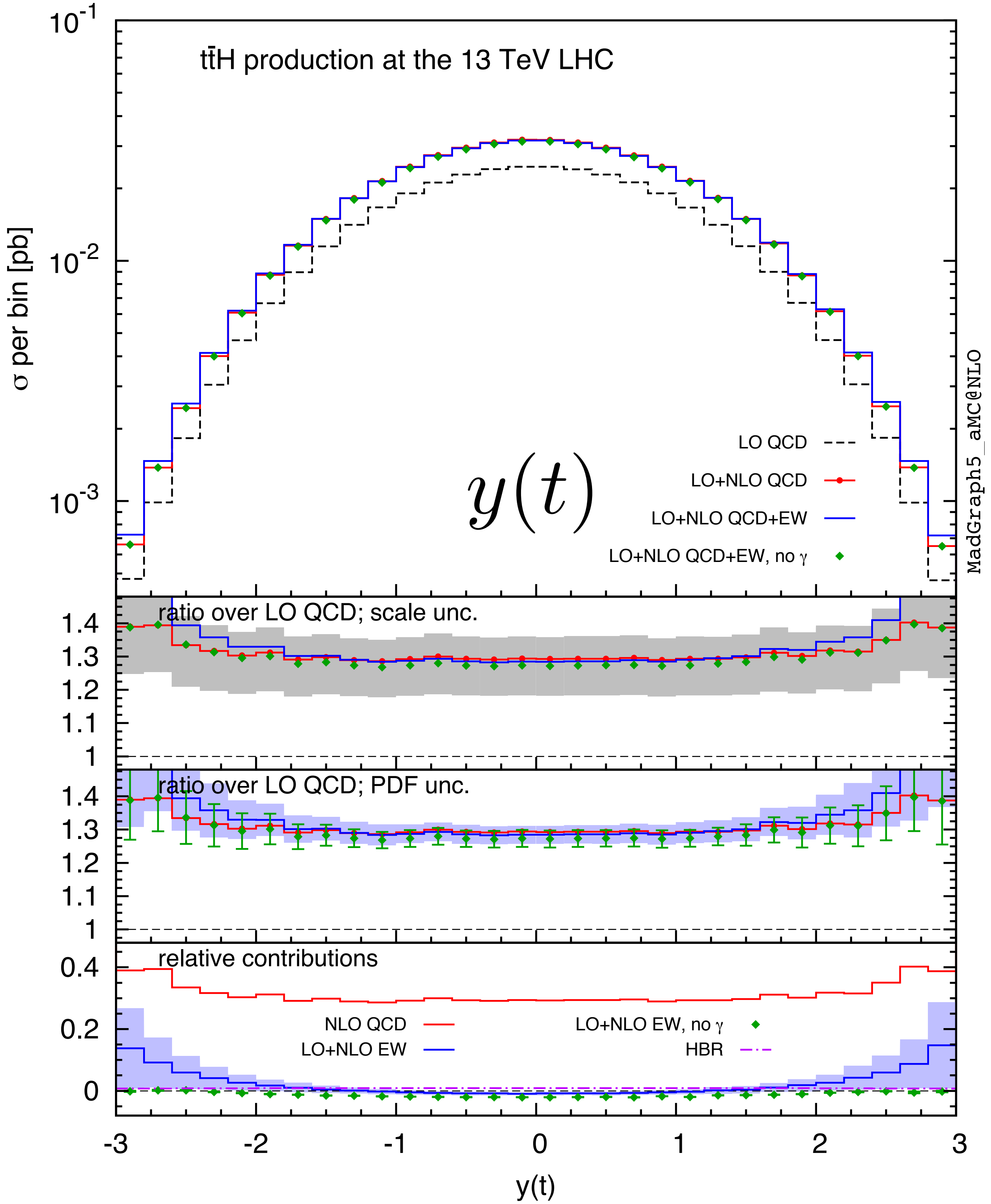


LO

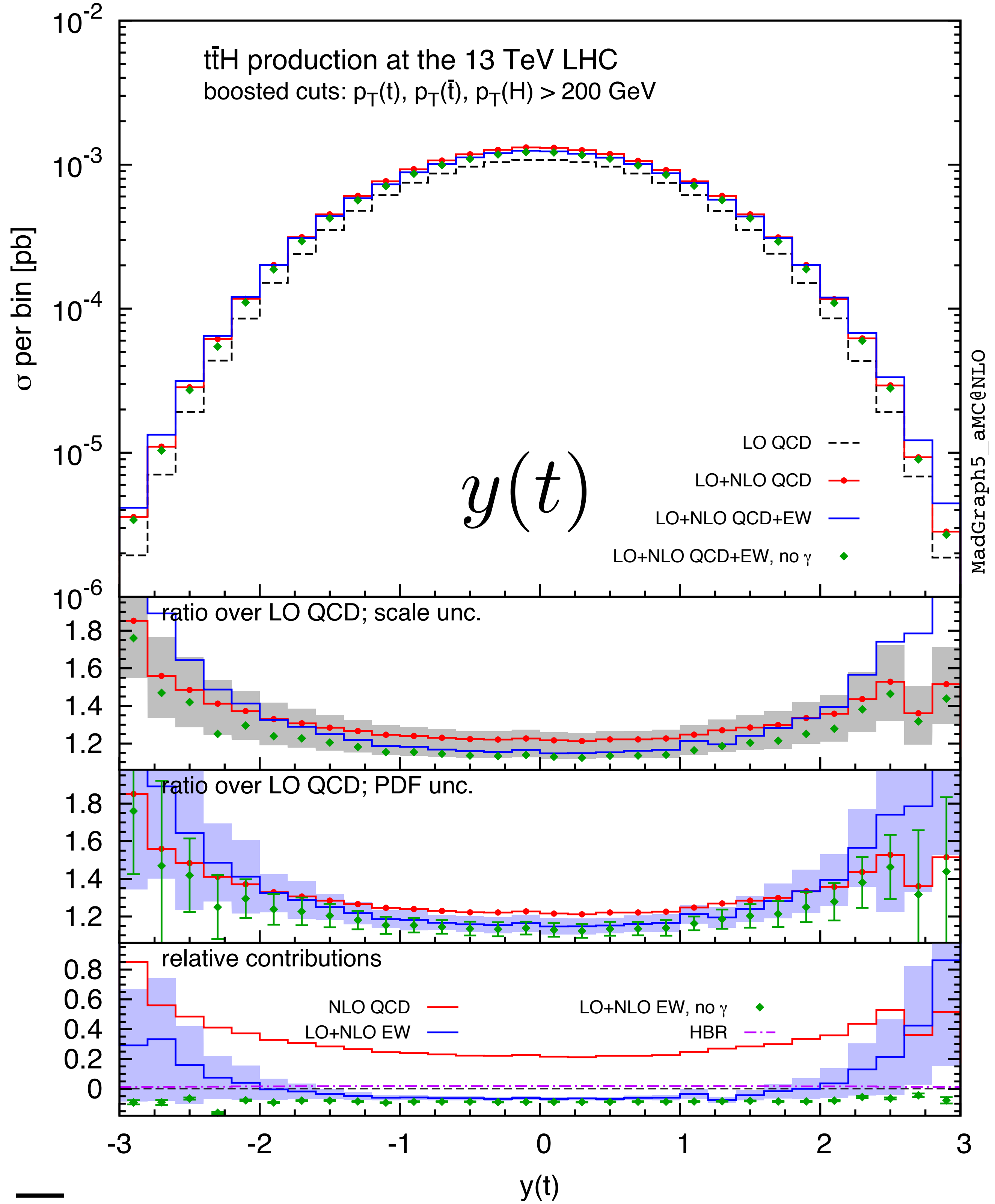
NLO



Rapidity distributions: unboosted vs. boosted



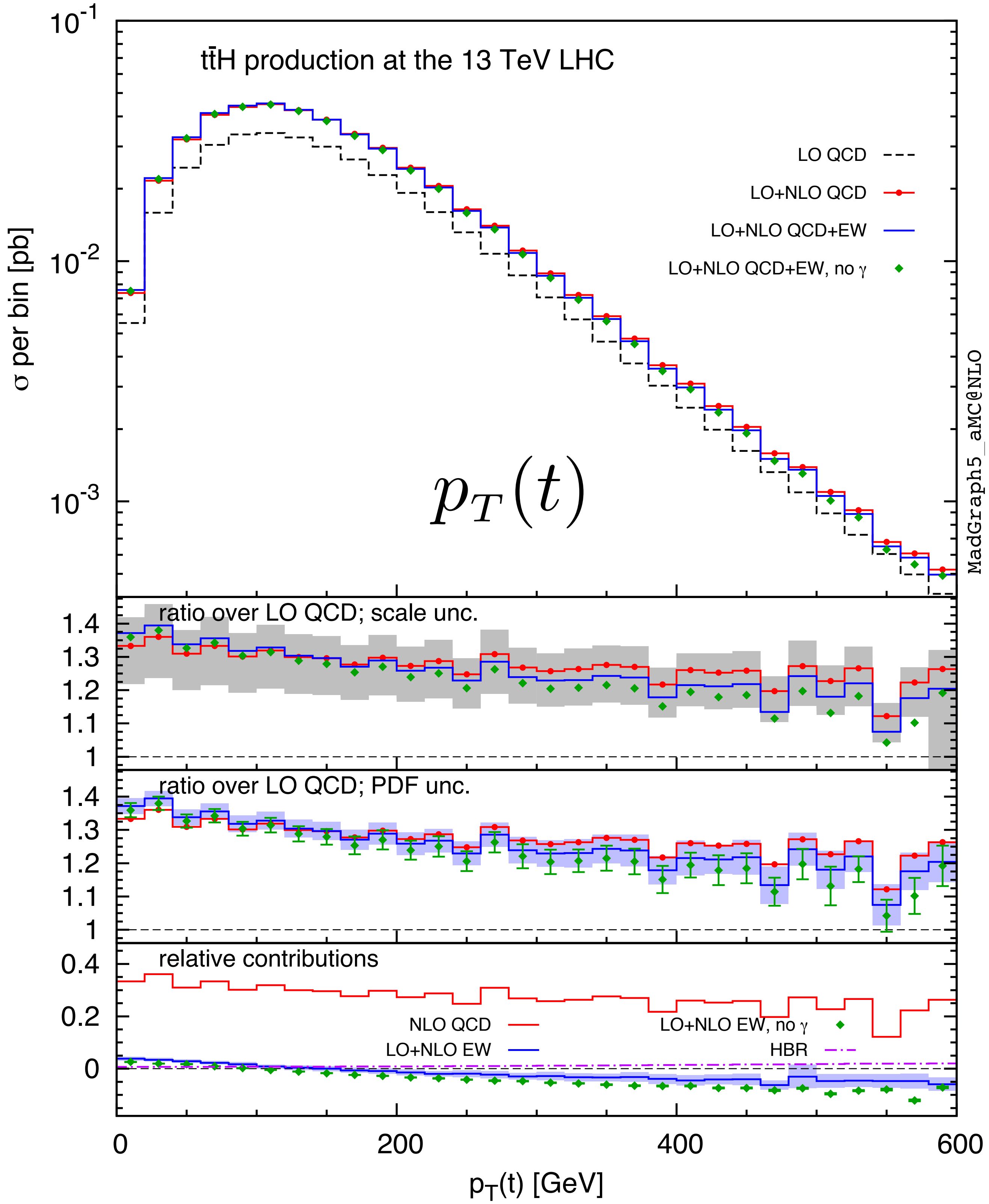
13 TeV



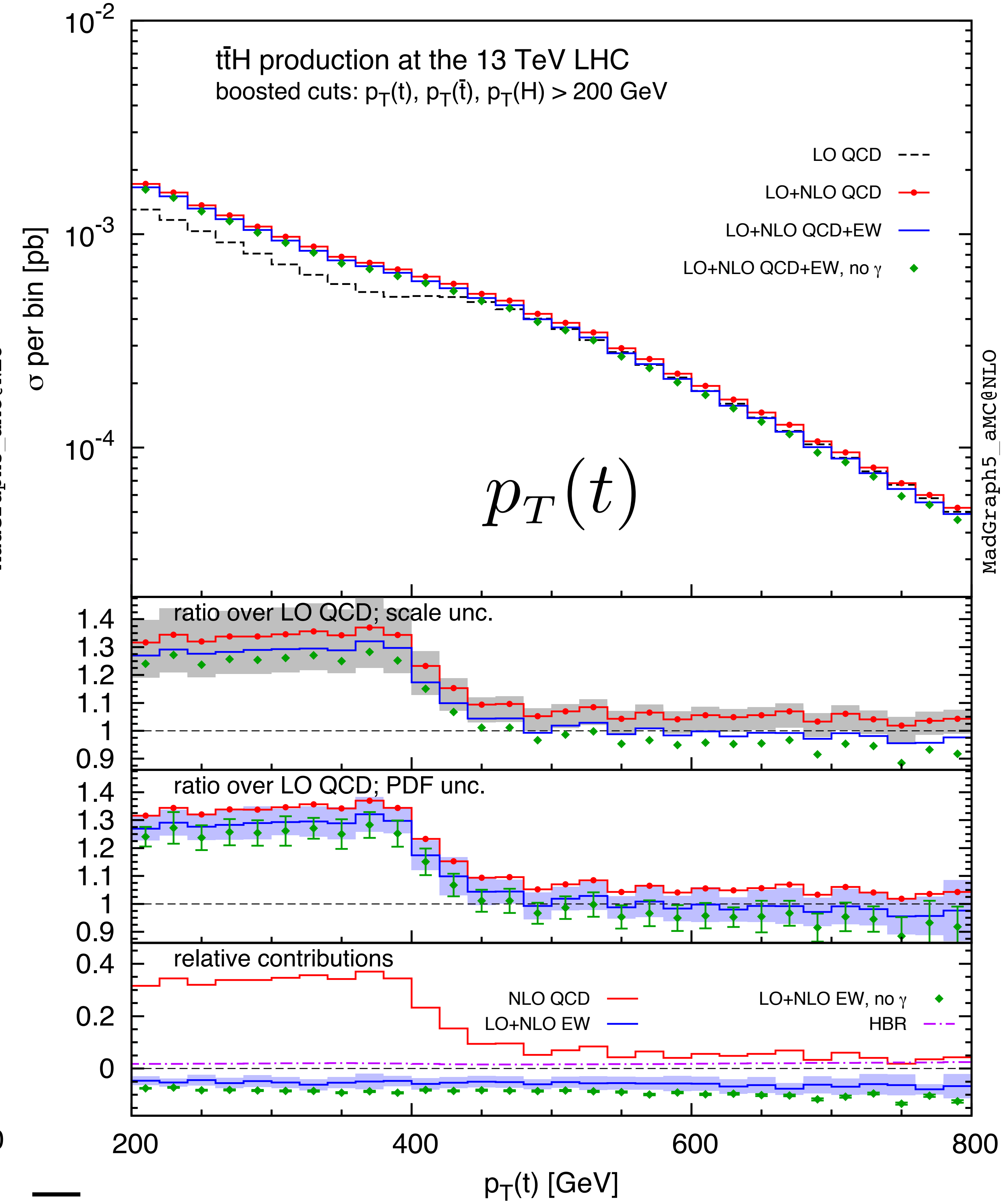
13 TeV

$$t\bar{t}H$$

Transverse momentum distributions: unboosted vs. boosted



13 TeV



13 TeV

$t\bar{t}H$

Comparison between different schemes

$$m_W = 80.385 \ \text{GeV}\,, \qquad m_Z = 91.188 \ \text{GeV}$$

$\alpha(m_Z)$ scheme → $\frac{1}{\alpha(m_Z)} = 128.93$

G_μ scheme → $G_\mu = 1.16639 \cdot 10^{-5} \longrightarrow \frac{1}{\alpha} = 132.23$

	$t\bar{t}H$	$t\bar{t}Z$	$t\bar{t}W^+$	$t\bar{t}W^-$
$\sigma_{\text{LO QCD}}(\text{pb})$	$3.617 \cdot 10^{-1}$	$5.282 \cdot 10^{-1}$	$2.496 \cdot 10^{-1}$	$1.265 \cdot 10^{-1}$
$\sigma^{G_\mu}_{\text{LO QCD}}(\text{pb})$	$3.527 \cdot 10^{-1}$	$5.152 \cdot 10^{-1}$	$2.433 \cdot 10^{-1}$	$1.234 \cdot 10^{-1}$
$\Delta^{G_\mu}_{\text{LO QCD}}(\%)$	2.5	2.5	2.5	2.5
$\delta_{\text{LO EW}}(\%)$	1.2	0.0	0	0
$\delta^{G_\mu}_{\text{LO EW}}(\%)$	1.2	0.0	0	0
$\Delta^{G_\mu}_{\text{LO EW}}(\%)$	2.5	2.5	2.5	2.5
$\delta_{\text{NLO EW}}(\%)$	-1.2	-3.8	-7.7	-6.7
$\delta^{G_\mu}_{\text{NLO EW}}(\%)$	1.8	-0.7	-4.5	-3.5
$\Delta^{G_\mu}_{\text{NLO EW}}(\%)$	-0.5	-0.7	-0.9	-0.9

Table 11: Comparison between results in the $\alpha(m_Z)$ and G_μ scheme, at 13 TeV.

$$\Delta^{G_\mu}_{\text{LO QCD}} = \frac{\sigma_{\text{LO QCD}} - \sigma^{G_\mu}_{\text{LO QCD}}}{\sigma_{\text{LO QCD}}}$$

$$\delta_{\text{X}} = \frac{\sigma_{\text{X}}}{\sigma_{\text{LO QCD}}}$$

Why Weak corrections to $t\bar{t}H$ production?

We calculated NLO corrections of mixed QCD-Weak origin, ignoring QED effects. We compared them to NLO QCD corrections.

Phenomenology motivations

Electroweak corrections are in general small. However, the Sudakov logarithms $\alpha_W \ln^2 s/M_W^2$ can enhance their size. They originate only from Weak corrections

The cross section of $t\bar{t}H$ depends directly on $\lambda^2_{t\bar{t}H}$. At NLO, only Weak corrections introduce a dependence on other Higgs couplings.

Automation of NLO corrections

Without QED (photons), the structure of IR singularities is simpler
$t\bar{t}H$ was the first pheno study of EW corrections in the **MG5_aMC@NLO** framework.

Numerical results weak corrections

Inclusive rates

(Boosted regime in brackets)

NLO corrections

$\delta_{\mathrm{NLO}}(\%)$	8 TeV	13 TeV	100 TeV
QCD	$+25.6^{+6.2}_{-11.8}$ $(+19.6^{+3.7}_{-11.0})$	$\boxed{+29.3^{+7.4}_{-11.6}\ (+23.9^{+5.4}_{-11.2})}$	$+40.4^{+9.9}_{-11.6}$ $(+39.1^{+9.7}_{-10.4})$
weak	-1.2 (-8.3)	$\boxed{-1.8\ (-8.2)}$	-3.0 (-7.8)

Heavy Boson Radiation

$\delta_{\mathrm{HBR}}(\%)$	8 TeV	13 TeV	100 TeV
W	$+0.42(+0.74)$	$+0.37(+0.70)$	$+0.14(+0.22)$
Z	$+0.29(+0.56)$	$+0.34(+0.68)$	$+0.51(+0.95)$
H	$+0.17(+0.43)$	$+0.19(+0.48)$	$+0.25(+0.53)$
sum	$+0.88(+1.73)$	$\boxed{+0.90(+1.86)}$	$+0.90(+1.70)$

Partial compensation of Sudakov logs

NLO weak subchannels

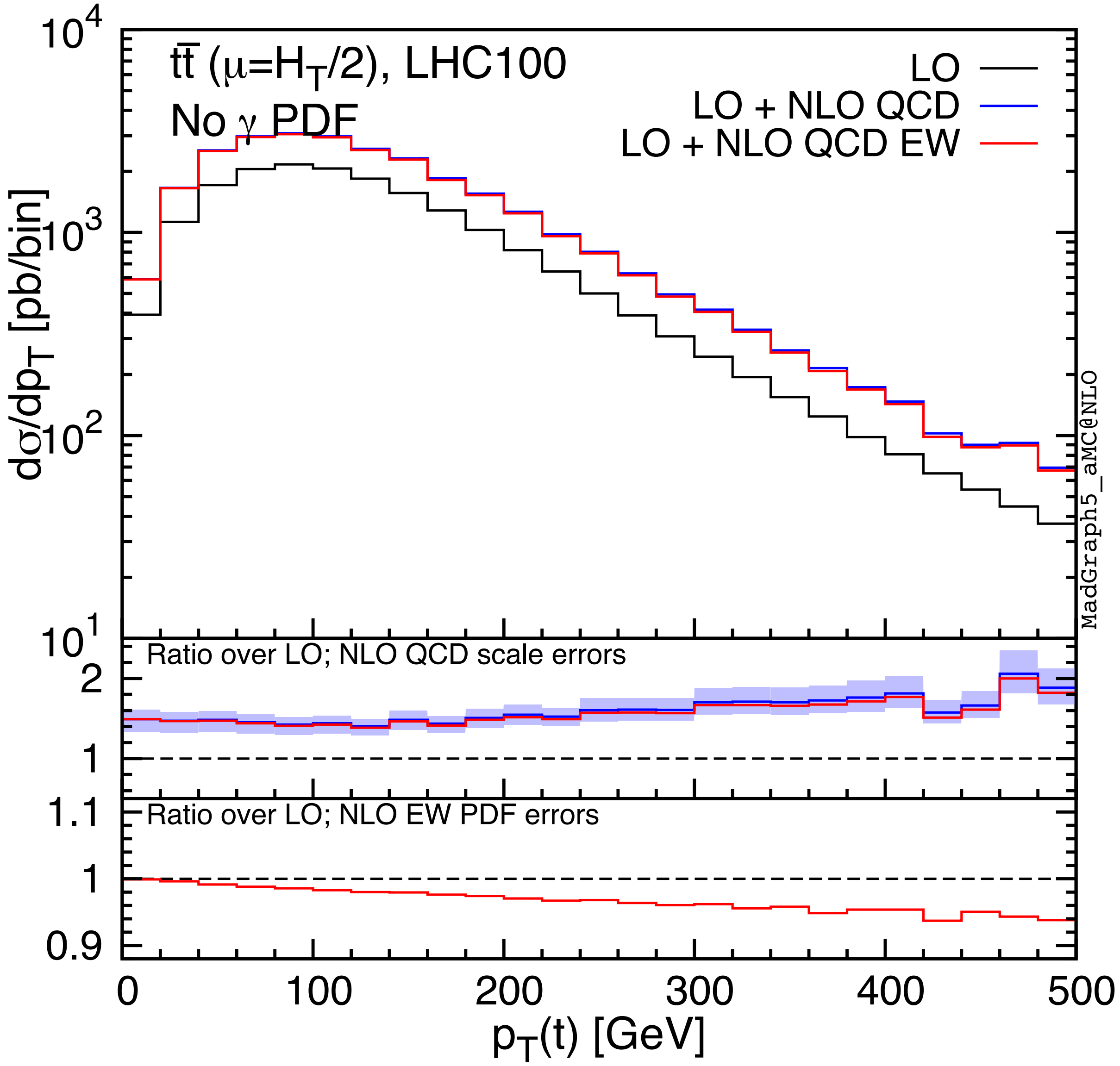
$\delta_{\mathrm{NLO}}(\%)$	8 TeV	13 TeV	100 TeV
gg	-0.67 (-2.9)	-1.12 (-4.0)	-2.64 (-6.8)
$u\bar{u}$	-0.01 (-3.2)	-0.15 (-2.3)	-0.10 (-0.5)
$d\bar{d}$	-0.55 (-2.2)	-0.52 (-1.9)	-0.23 (-0.5)

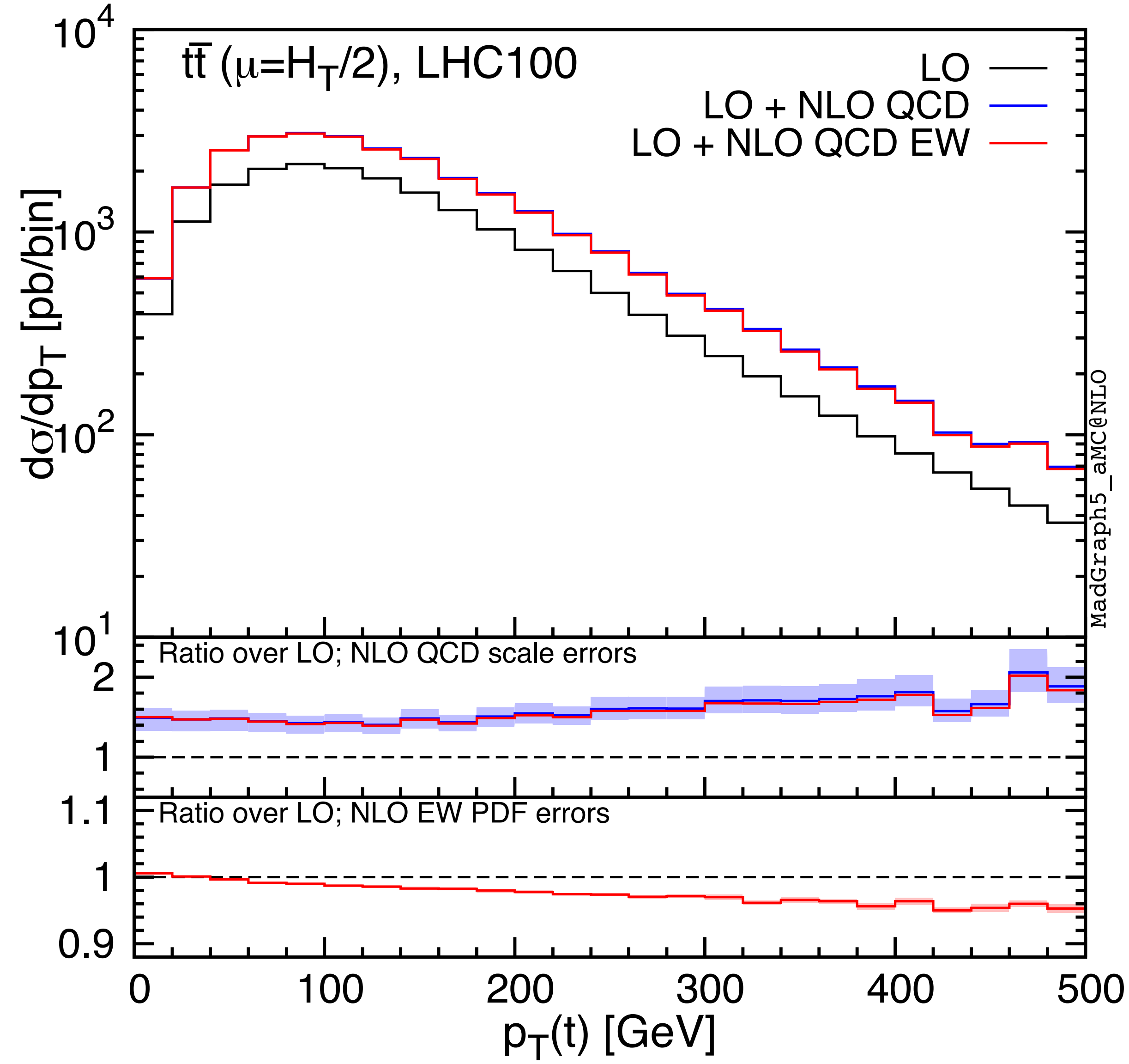
σ [fb]	8 TeV	13 TeV	14 TeV	25 TeV	33 TeV	50 TeV	100 TeV
$t\bar{t}ZZ$	$0.502^{+2.9\%}_{-8.6\%}{}^{+2.7\%}_{-2.2\%}$	$2.12^{+3.8\%}_{-8.6\%}{}^{+1.9\%}_{-1.8\%}$	$2.59^{+4.3\%}_{-8.7\%}{}^{+1.8\%}_{-1.8\%}$	$11.1^{+6.9\%}_{-9.1\%}{}^{+1.2\%}_{-1.4\%}$	$21.1^{+8.1\%}_{-9.4\%}{}^{+1.1\%}_{-1.3\%}$	$51.6^{+9.9\%}_{-9.8\%}{}^{+0.9\%}_{-1.1\%}$	$204^{+11.3\%}_{-9.9\%}{}^{+0.8\%}_{-1.0\%}$
$t\bar{t}W^+W^-$[4f]	$2.67^{+6.2\%}_{-11.1\%}{}^{+2.9\%}_{-2.7\%}$	$11.8^{+8.3\%}_{-11.2\%}{}^{+2.3\%}_{-2.4\%}$	$14.4^{+12.2\%}_{-12.8\%}{}^{+2.6\%}_{-2.9\%}$	$66.6^{+9.5\%}_{-10.8\%}{}^{+1.6\%}_{-2.0\%}$	$130^{+10.2\%}_{-10.8\%}{}^{+1.5\%}_{-1.8\%}$	$327^{+10.9\%}_{-10.6\%}{}^{+1.3\%}_{-1.6\%}$	$1336^{+10.3\%}_{-9.9\%}{}^{+1.0\%}_{-1.3\%}$
$t\bar{t}\gamma\gamma$	$2.77^{+6.4\%}_{-10.5\%}{}^{+1.9\%}_{-1.5\%}$	$10.3^{+13.9\%}_{-13.3\%}{}^{+1.3\%}_{-1.3\%}$	$12^{+12.5\%}_{-12.6\%}{}^{+1.2\%}_{-1.2\%}$	$44.8^{+15.7\%}_{-13.5\%}{}^{+0.9\%}_{-0.9\%}$	$78.2^{+16.4\%}_{-13.6\%}{}^{+0.8\%}_{-0.9\%}$	$184^{+19.2\%}_{-14.7\%}{}^{+0.8\%}_{-0.9\%}$	$624^{+15.5\%}_{-13.4\%}{}^{+0.7\%}_{-1.0\%}$
$t\bar{t}W^{\pm}Z$	$1.13^{+5.8\%}_{-9.8\%}{}^{+3.1\%}_{-2.1\%}$	$4.16^{+9.8\%}_{-10.7\%}{}^{+2.2\%}_{-1.6\%}$	$4.96^{+10.4\%}_{-10.8\%}{}^{+2.1\%}_{-1.6\%}$	$17.8^{+15.1\%}_{-12.6\%}{}^{+1.5\%}_{-1.1\%}$	$30.2^{+18.3\%}_{-14.1\%}{}^{+1.2\%}_{-0.9\%}$	$66^{+18.9\%}_{-14.3\%}{}^{+1.1\%}_{-0.8\%}$	$210^{+21.6\%}_{-15.8\%}{}^{+1.0\%}_{-0.8\%}$
$t\bar{t}Z\gamma$	$1.39^{+6.9\%}_{-11.2\%}{}^{+2.5\%}_{-2.2\%}$	$5.77^{+10.5\%}_{-12.1\%}{}^{+1.8\%}_{-1.9\%}$	$6.95^{+10.7\%}_{-12.1\%}{}^{+1.8\%}_{-1.9\%}$	$29.9^{+12.9\%}_{-12.4\%}{}^{+1.3\%}_{-1.5\%}$	$56.5^{+13.2\%}_{-12.2\%}{}^{+1.2\%}_{-1.4\%}$	$138^{+13.7\%}_{-12.0\%}{}^{+1.0\%}_{-1.1\%}$	$533^{+13.3\%}_{-11.1\%}{}^{+0.8\%}_{-1.0\%}$
$t\bar{t}W^{\pm}\gamma$	$2.01^{+7.9\%}_{-10.5\%}{}^{+2.6\%}_{-1.8\%}$	$6.73^{+12.0\%}_{-11.6\%}{}^{+1.8\%}_{-1.4\%}$	$7.99^{+12.8\%}_{-11.9\%}{}^{+1.7\%}_{-1.3\%}$	$27.6^{+18.7\%}_{-14.4\%}{}^{+1.2\%}_{-0.9\%}$	$46.3^{+20.2\%}_{-15.1\%}{}^{+1.1\%}_{-0.8\%}$	$98.4^{+21.9\%}_{-15.9\%}{}^{+1.0\%}_{-0.7\%}$	$318^{+22.5\%}_{-17.7\%}{}^{+1.0\%}_{-0.7\%}$
$t\bar{t}t\bar{t}$	$1.71^{+24.9\%}_{-26.2\%}{}^{+7.9\%}_{-8.4\%}$	$13.3^{+25.8\%}_{-25.3\%}{}^{+5.8\%}_{-6.6\%}$	$17.8^{+26.6\%}_{-25.4\%}{}^{+5.5\%}_{-6.4\%}$	$130^{+26.7\%}_{-24.3\%}{}^{+3.8\%}_{-4.6\%}$	$297^{+25.5\%}_{-23.3\%}{}^{+3.1\%}_{-3.9\%}$	$929^{+24.9\%}_{-22.4\%}{}^{+2.4\%}_{-3.0\%}$	$4934^{+25.0\%}_{-21.3\%}{}^{+1.7\%}_{-2.1\%}$

σ [pb]	8 TeV	13 TeV	14 TeV	25 TeV	33 TeV	50 TeV	100 TeV
$t\bar{t}Z$	$0.226^{+9.0\%}_{-11.9\%}{}^{+2.6\%}_{-3.0\%}$	$0.874^{+10.3\%}_{-11.7\%}{}^{+2.0\%}_{-2.5\%}$	$1.057^{+10.4\%}_{-11.7\%}{}^{+1.9\%}_{-2.4\%}$	$4.224^{+11.0\%}_{-11.0\%}{}^{+1.5\%}_{-1.8\%}$	$7.735^{+11.2\%}_{-10.8\%}{}^{+1.3\%}_{-1.5\%}$	$18^{+11.1\%}_{-10.2\%}{}^{+1.1\%}_{-1.3\%}$	$64.17^{+11.1\%}_{-11.0\%}{}^{+0.9\%}_{-1.2\%}$
$t\bar{t}W^{\pm}$	$0.23^{+9.6\%}_{-10.6\%}{}^{+2.3\%}_{-1.7\%}$	$0.645^{+13.0\%}_{-11.6\%}{}^{+1.7\%}_{-1.3\%}$	$0.745^{+13.5\%}_{-11.8\%}{}^{+1.6\%}_{-1.3\%}$	$2.188^{+17.0\%}_{-13.2\%}{}^{+1.3\%}_{-0.9\%}$	$3.534^{+18.1\%}_{-13.7\%}{}^{+1.2\%}_{-0.8\%}$	$7.03^{+19.2\%}_{-14.3\%}{}^{+1.1\%}_{-0.8\%}$	$20.55^{+21.5\%}_{-18.1\%}{}^{+1.1\%}_{-0.8\%}$
$t\bar{t}\gamma$	$0.788^{+12.7\%}_{-13.5\%}{}^{+2.1\%}_{-2.4\%}$	$2.746^{+14.2\%}_{-13.5\%}{}^{+1.6\%}_{-1.9\%}$	$3.26^{+14.2\%}_{-13.4\%}{}^{+1.6\%}_{-1.9\%}$	$11.77^{+14.5\%}_{-12.7\%}{}^{+1.2\%}_{-1.4\%}$	$20.84^{+14.9\%}_{-12.5\%}{}^{+1.1\%}_{-1.3\%}$	$45.68^{+14.2\%}_{-11.7\%}{}^{+1.0\%}_{-1.2\%}$	$152.6^{+14.3\%}_{-13.7\%}{}^{+0.9\%}_{-1.2\%}$
$t\bar{t}H$	$0.136^{+3.3\%}_{-9.1\%}{}^{+2.8\%}_{-3.2\%}$	$0.522^{+6.0\%}_{-9.4\%}{}^{+2.1\%}_{-2.6\%}$	$0.631^{+6.3\%}_{-9.4\%}{}^{+2.0\%}_{-2.5\%}$	$2.505^{+8.3\%}_{-9.4\%}{}^{+1.6\%}_{-1.9\%}$	$4.567^{+8.8\%}_{-9.2\%}{}^{+1.4\%}_{-1.7\%}$	$10.55^{+9.5\%}_{-9.0\%}{}^{+1.2\%}_{-1.4\%}$	$37.65^{+10.0\%}_{-9.8\%}{}^{+1.0\%}_{-1.3\%}$

$t\bar{t}$

differential plots

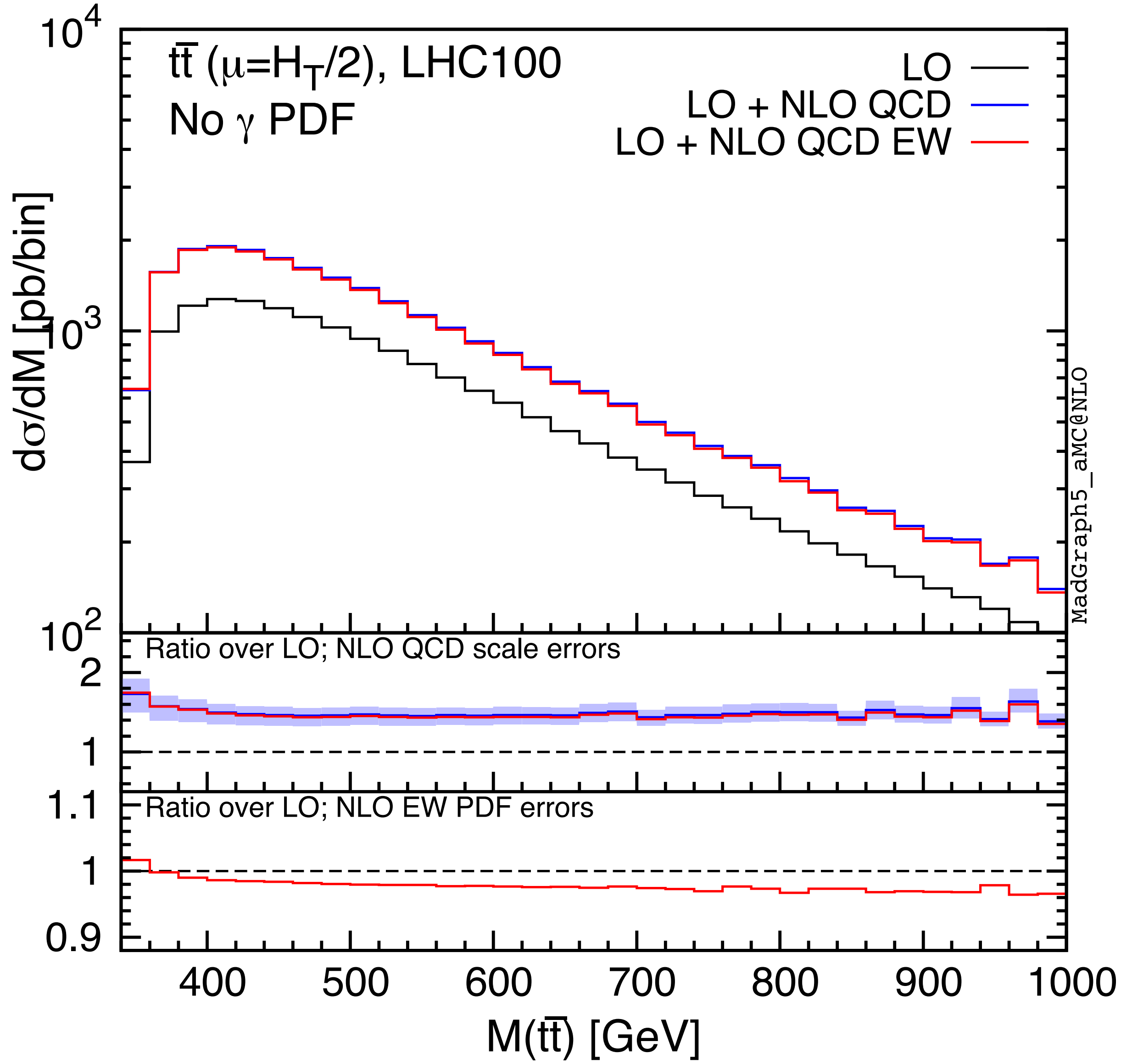


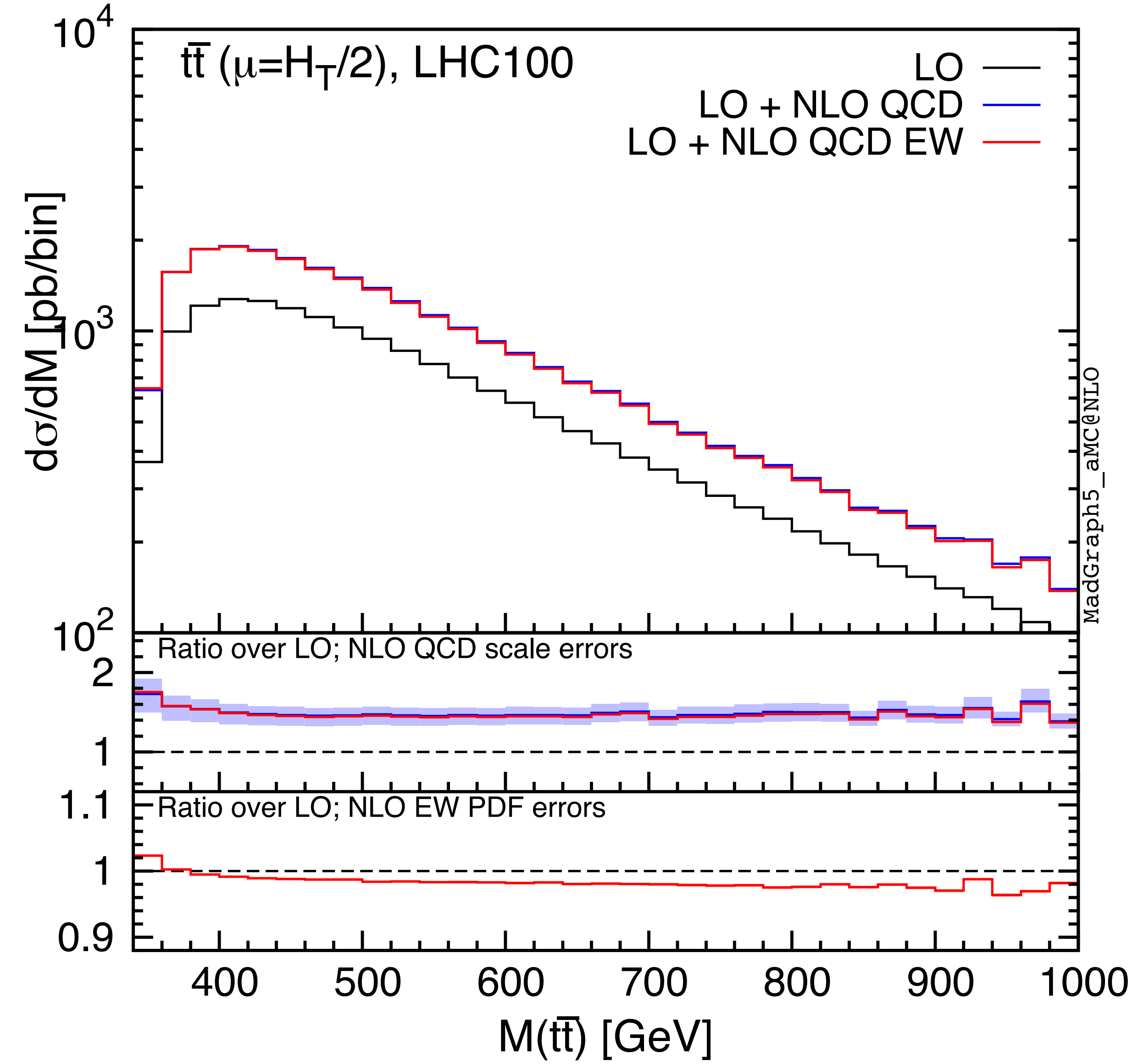


photon PDF **NO** photon PDF **YES**

$t\bar{t}$

differential plots





photon PDF **NO** photon PDF **YES**