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陈自强 陈龙斌 乔从丰

中国科学院大学 物理学院

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Outline

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Introduction

• J/ψ Inclusive Production in Photon-Photon Collision

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- NLO QCD Corrections to $\gamma\gamma \rightarrow J/\psi + c\bar{c}$
- $J/\psi + ggg$ Final State Subprocess

Summary

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Introduction

 In non-relativistic QCD(NRQCD), heavy quarkonium is treated as a nonrelativistic system. Then we get a hierarchy of energy scales: (M_Qv²)² << (M_Qv)² << M²_Q

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- NRQCD factorization model is not so intuitive as color-singlet(CS) model for the introduction of color-octet(CO) mechanism(QQ can be CO state).
- CERN LEPII $\gamma\gamma \rightarrow J/\psi + X$ data provide direct evidence for CO mechanism. But the importance of CO mechanism in this process is still being researched.

 $-J/\psi$ Inclusive Production in Photon-Photon Collision

J/ψ Inclusive Production in Photon-Photon Collision

Experimental Data

• LEPII $\gamma \gamma \rightarrow J/\psi + X$ Data

Theoretical Calculations

- Three Classes of Subprocesses
- The LO Calculations
- The NLO Corrections
- $J/\psi + c\bar{c}$ Final State Subprocess

LEPII $\gamma\gamma \rightarrow J/\psi + X$ Data

In 2001, the DELPHI Collaboration presented preliminary data on the J/ψ inclusive cross section in photon-photon collision ($e^+e^- \rightarrow e^+e^-J/\psi + X$) at LEPII.

 $- J/\psi$ Inclusive Production in Photon-Photon Collision Experimental Data

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Figure: "DELPHI Collaboration, Phys. Lett. B 565(2003)76-86".

The requirement of at least 4 reconstructed tracks suppress the $J/\psi + \gamma$ final state.

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- Theoretical Calculations

Three Classes of Subprocesses

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i direct process:

$$\begin{split} &\gamma\gamma\to c\bar{c} \left[{}^3S_1^{(8)}\right]g,\\ &\gamma\gamma\to c\bar{c} \left[{}^3S_1^{(1)}\right]\gamma \quad \text{(suppressed at at LEPII)} \end{split}$$

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ii single-resolved process:

$$\begin{split} \gamma g &\to c \bar{c} \left[{}^3S_1^{(1)} \right] g, c \bar{c} [8] g, \\ \gamma q &\to c \bar{c} [8] q \end{split}$$

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$$\gamma g \to c \bar{c} \begin{bmatrix} 3S_1^{(1)} \end{bmatrix} g, c \bar{c}[8]g,$$

 $\gamma q \to c \bar{c}[8]q$

iii double-resolved process:

$$\begin{split} gg &\to c\bar{c} \begin{bmatrix} {}^3S_1^{(1)} \end{bmatrix} g, c\bar{c} \begin{bmatrix} {}^3P_J^{(1)} \end{bmatrix} g, c\bar{c}[8]g, \\ gq &\to c\bar{c} \begin{bmatrix} {}^3P_J^{(1)} \end{bmatrix} q, c\bar{c}[8]q, \\ q\bar{q} &\to c\bar{c} \begin{bmatrix} {}^3S_1^{(8)} \end{bmatrix} \end{split}$$

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The LO Calculations

The LO calculations for direct process was finished early[1]. And full LO calculations was finished soon after the presentation of DELPHI data[2].

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The LO results indicate that DELHPI data are not explainable by the CS model alone, and the CO mechanism is evidently necessary. But investigations on NLO corrections and NLO subprocesses are still needed to clarify the situation.

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- [1] Michael Klasen et al., Nucl. Phys. B 609 (2001).
- [2] Michael Klasen et al., Phys. Rev. Lett. 89, 032001(2002).

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L Theoretical Calculations

The NLO Corrections

There has been a lot of research on the NLO corrections for the corresponding parton processes, but no one is performed in LEPII photon-photon collision condition.

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Many researches on J/ψ inclusive production at hadron colliders: J.Campbell, F.Maltoni, and F.Tramontano, Phys. Rev. Lett. 98, 252002 (2007), B.Gong, X.-Q.Li, J.-X.Wang, Phys. Lett. B 673, 5 (197-200),

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For the single-resolved channel, the NLO corrections in CS model are moderate. But the discrepancy between DELPHI data and CS model prediction is too large to be removed.

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On the other hand, a new process, $J/\psi + c\bar{c}$ final state process is very necessary to be included in the full NLO calculation. And the experimentally distinguishable final state also make this process worth to study.

 $-J/\psi$ Inclusive Production in Photon-Photon Collision

- Theoretical Calculations

$J/\psi + c\bar{c}$ Final State Subprocess

C.F. Qiao and J.X. Wang are the first two to notice the importance of $\gamma\gamma \rightarrow J/\psi + c \bar{c}$ process[1].

A comparison is also made between pure fragmentation result and full calculation in [1]. It is found that this process cannot be mimicked by simple fragmentation scheme.



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After including this process, the CO mechanism is still necessary but with a shrunken contribution to explain the DELPHI experimental result.

[1] C.F. Qiao and J.X. Wang, Phys. Rev. D 69, 014015(2004).

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$J/\psi + c\bar{c}$ Final State Subprocess

Further studies:

 $-J/\psi$ Inclusive Production in Photon-Photon Collision

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i R. Li and K.-T. Chao, Phys. Rev. D 79, 114020(2009): $\gamma g \rightarrow J/\psi + c\bar{c}, q\bar{q} \rightarrow J/\psi + c\bar{c}, gg \rightarrow J/\psi + c\bar{c},$ $\gamma \gamma \rightarrow J/\psi + c\bar{c}$

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photon-photon collisions at LHC

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 $\gamma\gamma \rightarrow [Q\bar{Q}] + Q\bar{Q}$ at ILC

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These researches indicate that the contributions of single-resolved and double-resolved are significantly less important than the direct one with in the CS prescription. The CO mechanism is still needed to explain experimental data.

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To seek further clarification, NLO corrections for these processes, especially for $\gamma\gamma \rightarrow J/\psi + c\bar{c}$, are very necessary.

NLO QCD Corrections to J/ψ Inclusive Production in Photon-Photon Collision <u>NLO QCD Corrections</u> to $\gamma\gamma \rightarrow J/\psi + c\bar{c}$

NLO QCD Corrections to $\gamma\gamma \rightarrow J/\psi + c\bar{c}$

Formalism and Calculation

Numerical Results

 \square NLO QCD Corrections to $\gamma\gamma \rightarrow J/\psi + c\bar{c}$

Formalism and Calculation

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□ NLO QCD Corrections to $\gamma \gamma \rightarrow J/\psi + c\bar{c}$

Formalism and Calculation

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The overall differential cross section can be written as

$$d\sigma = \int dx_1 dx_2 f_{\gamma}(x_1) f_{\gamma}(x_2) d\hat{\sigma}(\gamma\gamma \to c\bar{c}[{}^3S_1] + c\bar{c}) \langle \mathcal{O}^{J/\psi}({}^3S_1) \rangle$$

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NLO QCD Corrections to J/ψ Inclusive Production in Photon-Photon Collision \square NLO QCD Corrections to $\gamma\gamma \rightarrow J/\psi + c\bar{c}$

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To NLO calculation, the cross section is

$$d\hat{\sigma}(\gamma\gamma \to c\bar{c}[{}^{3}S_{1}] + c\bar{c}) = d\hat{\sigma}_{born} + d\hat{\sigma}_{virtual} + d\hat{\sigma}_{real} + O(\alpha^{2}\alpha_{s}^{4})$$

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The quarkonium spin projection operator is

$$v(P/2)\bar{u}(P/2) = \frac{1}{4\sqrt{2}E(E+2m_c)} (\frac{P}{2} - m_c) \ \epsilon_S^* (P+2E) (\frac{P}{2} + m_c)$$

□ NLO QCD Corrections to $\gamma \gamma \rightarrow J/\psi + c\bar{c}$

Formalism and Calculation

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Virtual corrections (582 Diagrams)
► NLO QCD Corrections to $\gamma \gamma \rightarrow J/\psi + c\bar{c}$.

Formalism and Calculation

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Virtual corrections (582 Diagrams)

Selfenergies, Triangles, Boxes, Pentagons, Hexagons and Counter terms



□ NLO QCD Corrections to $\gamma \gamma \rightarrow J/\psi + c\bar{c}$

- Formalism and Calculation

Formalism and Calculation

Real corrections (200 Diagrams)

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□ NLO QCD Corrections to $\gamma \gamma \rightarrow J/\psi + c\bar{c}$

Formalism and Calculation

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Real corrections (200 Diagrams)

 $\gamma\gamma \to J/\psi + c\bar{c} + g$



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According to B. W. Harris and J. F. Owens, "Two cutoff phase space slicing method", Phys. Rev. D 65, 094032 (2002),

$$d\sigma_{real} = d\sigma_{soft}^{IR}|_{p_g^0 < \delta} + d\sigma_{hard}^{IR-free}|_{p_g^0 > \delta}$$

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Formalism and Calculation

Formalism and Calculation

Cancellation of singularities

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□ NLO QCD Corrections to $\gamma \gamma \rightarrow J/\psi + c\bar{c}$

Formalism and Calculation

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- Cancellation of singularities
 - i Ultraviolet singularities are canceled by renormalization



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Formalism and Calculation

## Formalism and Calculation

- Cancellation of singularities
  - i Ultraviolet singularities are canceled by renormalization



ii Infrared singularities involved in virtual corrections and real emissions are canceled each other



iii Coulombic singularities are attributed to NRQCD long-distance matrix elements



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 $\square$  NLO QCD Corrections to  $\gamma \gamma \rightarrow J/\psi + c\bar{c}$ 

— Numerical Results

## Numerical Results

 $\ \ \, \bigsqcup_{\text{NLO QCD Corrections to } \gamma \gamma \to J/\psi + c\bar{c} }$ 

— Numerical Results

## Numerical Results

LEPII collider energy

□ NLO QCD Corrections to  $\gamma \gamma \rightarrow J/\psi + c\bar{c}$ 

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#### LEPII collider energy



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− NLO QCD Corrections to  $\gamma \gamma \rightarrow J/\psi + c\bar{c}$ 

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### Numerical Results

#### LEPII collider energy



The shaded band is the NLO result of  $\gamma\gamma \rightarrow J/\psi + c\bar{c}$  process with its upper bound obtained at  $r=0.5,\,m_c=1.4 {\rm GeV}$  and lower bound at  $r=2,\,m_c=1.6 {\rm GeV}.$  The solid and dashed lines represent the NLO and LO results with  $r=1,\,m_c=1.5 {\rm GeV}.$ 

$$u = r\sqrt{4m_c^2 + p_t^2}$$

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$$\mu = r\sqrt{4m_c^2 + p_t^2}$$

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The NLO correction is moderate but not big enough to remove the huge discrepancy between CS model prediction and experimental observation.

□ NLO QCD Corrections to  $\gamma \gamma \rightarrow J/\psi + c\bar{c}$ 

-Numerical Results

## Numerical Results

LEPII collider energy

While integrated over the range  $1 \leq p_t^2 \leq 10 {\rm GeV^2}$  ,

| $\sigma(pb)$ | $m_c = 1.4 {\rm GeV}$ | $m_c = 1.5 {\rm GeV}$ | $m_c = 1.6 {\rm GeV}$ |
|--------------|-----------------------|-----------------------|-----------------------|
| r = 0.5      | 0.766(0.436)          | 0.459(0.283)          | 0.299(0.187)          |
| r = 1        | 0.363(0.236)          | 0.227(0.156)          | 0.152(0.105)          |
| r=2          | 0.216(0.152)          | 0.138(0.101)          | 0.093(0.069)          |

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Table: NLO(LO) results of total cross sections with different renormalization scale and cham quark mass. The K factor of central value is about 1.46.

- NLO QCD Corrections to  $\gamma \gamma \rightarrow J/\psi + c\bar{c}$ 

-Numerical Results

## Numerical Results

LEPII collider energy

While integrated over the range  $1 \leq p_t^2 \leq 10 {\rm GeV^2}$  ,

| $\sigma(pb)$ | $m_c = 1.4 {\rm GeV}$ | $m_c = 1.5 {\rm GeV}$ | $m_c = 1.6 {\rm GeV}$ |
|--------------|-----------------------|-----------------------|-----------------------|
| r = 0.5      | 0.766(0.436)          | 0.459(0.283)          | 0.299(0.187)          |
| r = 1        | 0.363(0.236)          | 0.227(0.156)          | 0.152(0.105)          |
| r=2          | 0.216(0.152)          | 0.138(0.101)          | 0.093(0.069)          |

Table: NLO(LO) results of total cross sections with different renormalization scale and cham quark mass. The K factor of central value is about 1.46.

The result of DELPHI and other CS processes read  $(6.4\pm2.0)\rm{pb}$  and  $0.39^{+0.16}_{-0.09}\rm{pb}$ , respectively. The CO mechanism is still needed to explain the DELPHI data.

□ NLO QCD Corrections to  $\gamma \gamma \rightarrow J/\psi + c\bar{c}$ 

-Numerical Results

## Numerical Results

CEPC collider energy

In the future, the  $e^+e^-$  collider CEPC will run at  $\sqrt{s}=250{\rm GeV},$ 

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└─ Numerical Results

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-Numerical Results

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The  $p_t^2$  distribution of  $J/\psi+c\bar{c}$  production through  $\gamma\gamma$  collision at CEPC. The solid and dashed lines represent the NLO and LO results with  $r=1,\,m_c=1.5 {\rm GeV}.$ 

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 $J/\psi + ggg$  Final State Subprocess

 $\blacksquare~\gamma\gamma\rightarrow J/\psi+gg$  Process and Furry's Theorem

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- Feynman Diagrams
- Numerical Results

 $-J/\psi + ggg$  Final State Subprocess

 $\Box \gamma \gamma \rightarrow J/\psi + gg$  Process and Furry's Theorem

# $\gamma\gamma \rightarrow J/\psi + gg$ Process and Furry's Theorem

Process  $\gamma\gamma \rightarrow J/\psi + gg$  is of the same order as  $\gamma\gamma \rightarrow J/\psi + c\bar{c}$ . But this process is forbidden by Furry's theorem based on charge conjugation invariance.



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This was also verified by explicit calculation.



## Feynman Diagrams

#### So, the Feynman diagrams of this process are



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Other diagrams can be obtained by exchange gluons and photons.

 $J/\psi + ggg$  Final State Subprocess Numerical Results

## Numerical Results

 $J/\psi + ggg$  Final State Subprocess

## Numerical Results

LEPII collider energy

 $J/\psi + ggg$  Final State Subprocess

## Numerical Results

#### LEPII collider energy



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 $J/\psi + ggg$  Final State Subprocess

## Numerical Results

#### LEPII collider energy



The shaded band is the cross section of  $\gamma\gamma \rightarrow J/\psi + ggg$  process with its upper bound obtained at r = 0.5,  $m_c = 1.4 \text{GeV}$  and lower bound at r = 2,  $m_c = 1.6 \text{GeV}$ . The solid lines represent the results with r = 1,  $m_c = 1.5 \text{GeV}$ .

 $J/\psi + ggg$  Final State Subprocess

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Integrated over the range  $1 \le p_t^2 \le 10 {\rm GeV^2}$ ,

| $\sigma(fb)$ | $m_c = 1.4 {\rm GeV}$ | $m_c = 1.5 {\rm GeV}$ | $m_c = 1.6 {\rm GeV}$ |
|--------------|-----------------------|-----------------------|-----------------------|
| r = 0.5      | 1.32                  | 0.82                  | 0.54                  |
| r = 1        | 0.52                  | 0.33                  | 0.22                  |
| r=2          | 0.26                  | 0.17                  | 0.12                  |

 $J/\psi + ggg$  Final State Subprocess

## Numerical Results

- CEPC collider energy
  - At the  $e^+e^-$  collider CEPC,

 $J/\psi + ggg$  Final State Subprocess

## Numerical Results

CEPC collider energy

At the  $e^+e^-$  collider CEPC,



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 $J/\psi + ggg$  Final State Subprocess

## Numerical Results

CEPC collider energy

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The  $p_t^2$  distribution of  $J/\psi + ggg$  production through  $\gamma\gamma$  collision at CEPC. The solid lines represent the cross section with r=1,  $m_c=1.5 {\rm GeV}.$  Integrated over  $p_t^2 \geq 1 {\rm GeV}^2$ , the total cross section is  $0.39 {\rm fb}.$ 

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#### Summary

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• We have calculated the NLO QCD corrections to  $\gamma\gamma \rightarrow J/\psi + c\bar{c}$  process. This is the first truly NLO calculation of 2 to 3 inclusive process for heavy quarkonium production.

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According to Furry's theorem, CS process  $\gamma\gamma \rightarrow J/\psi + gg$  is forbidden. The cross section of  $\gamma\gamma \rightarrow J/\psi + ggg$  is relatively small.