

# Charmless B decays in Factorization Assisted Topological amplitude approach

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Based on work collaborated with [Cai-Dian Lü](#) and [Qi-An Zhang](#)  
*(arXiv:1608.02819)*

# Outline

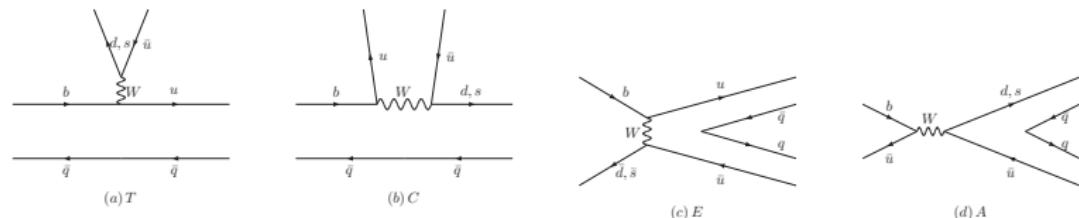
- ▶ Introduction/Motivation
- ▶ Factorization Assisted Topological Amplitude approach
- ▶ Numerical results for  $B \rightarrow PP, PV$  decays and Analysis
- ▶ Summary

## $B \rightarrow PP, VP$ and $PV$ in QCD-methods

$$\mathcal{H}_{eff} = \frac{G_F}{\sqrt{2}} \{ V_{ub} V_{ud(s)}^* C_{1,2}(\mu) O_{1,2}^u(\mu) - V_{tb} V_{td(s)}^* \Sigma_{i=3}^{10} C_i(\mu) O_i(\mu) \}$$

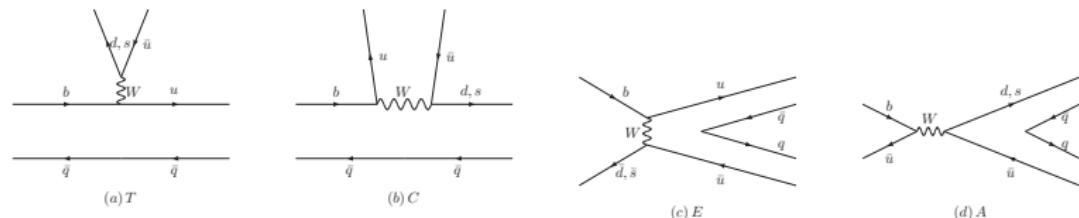
- ▶ Collinear QCD Factorization approach need to include a **large penguin annihilation contribution** (as free parameter) to enhance the branching fractions and direct CP asymmetry of penguin-dominated charmless B decays.
- ▶ penguin annihilation contribution replaced by the **power suppressed nonperturbative charming penguin effect** in Soft-Collinear Effective Theory.
- ▶ Calculated in Perturbative QCD approach based on  $k_T$  factorization.
- ▶ Although some soft and sub-leading effects were considered,  **$\pi\pi$  and  $\pi K$  puzzle** etc was still left in the conventional factorization approaches

# Topological diagrammatic approach [Cheng, Chiang and Kuo 2015]



1. Distinct by **weak interaction** and flavor flows with **all strong interaction encoded**, including non-perturbative ones.
  2. Amplitudes with strong phases extracted from data.
  3. Based on flavor  $SU(3)$  symmetry.  **$SU(3)$  breaking effect was lost.**
  4.  $B \rightarrow PP, VP$  and  $PV$  fitted separately,  $13 + 19 = 32$  parameters.  
**Less predictive** (*Phys. Rev. D* **91**, no. 1, 014011 (2015).)
- Improved by Factorization Assisted Topological amplitude (FAT) approach.
- ★ keep flavor  $SU(3)$  symmetry breaking effect.
  - ★ further **reducing** the number of free parameters by fitting **all** the decay channels

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# Factorization Assisted Topological amplitude approach first applied in hadronic D decays

[H. n. Li, C. D. Lu and F. S. Yu, Phys. Rev. D **86**, 036012 (2012), Phys. Rev. D **89**, no. 5, 054006 (2014)]

- Was in great success to resolve the long-standing puzzle from the large difference of  $D_0 \rightarrow \pi^+\pi^-$  and  $D_0 \rightarrow K^+K^-$  branching fractions.
- Also predicted 0.1% of direct CP asymmetry difference between them.

NEW

LHCb-PAPER-2015-055  
to be submitted to PRL

$$\Delta A_{CP} \text{ prompt} = (-0.10 \pm 0.08(\text{stat}) \pm 0.03(\text{syst}))\%$$

- "Analysis of Two-body Charmed  $B$  meson decays in Factorization Assisted Topological amplitude approach,"

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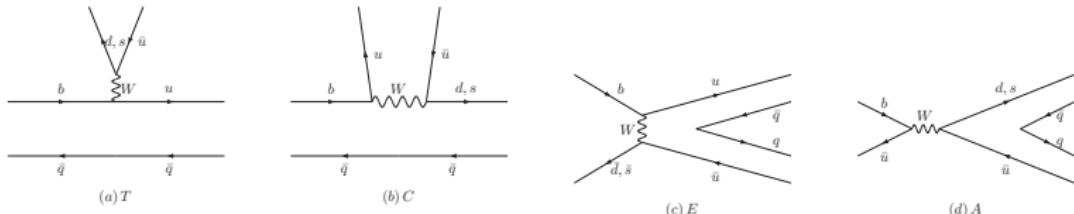
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# Factorization Assisted Topological amplitude approach in $B \rightarrow PP$ , $VP$ and $PV$ decays



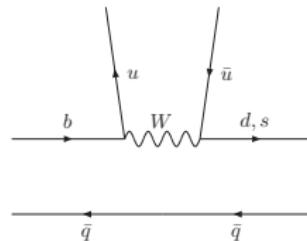
- ▶ Color-favored tree emission diagram ( $T$ )
  - ★ It is proved factorization to all order of  $\alpha_s$  expansion in QCDF, PQCD and SCET.

$$\begin{aligned} T^{P_1 P_2} &= i \frac{G_F}{\sqrt{2}} V_{ub} V_{uq'} \textcolor{magenta}{a_1(\mu)} f_{p_2}(m_B^2 - m_{p_1}^2) F_0^{BP_1}(m_{p_2}^2), \\ T^{PV} &= \sqrt{2} G_F V_{ub} V_{uq'} \textcolor{magenta}{a_1(\mu)} f_V m_V F_1^{B-P}(m_V^2) (\varepsilon_V^* \cdot p_B), \\ T^{VP} &= \sqrt{2} G_F V_{ub} V_{uq'} \textcolor{magenta}{a_1(\mu)} f_P m_V A_0^{B-V}(m_P^2) (\varepsilon_V^* \cdot p_B), \end{aligned} \quad (1)$$

- ★ The  $SU(3)$  breaking effect is automatically kept
  - ★ No free parameter

- For other diagrams dominated by non-factorization contributions.
  - ★ We factorize out the decay constants and form factor to keep the  $SU(3)$  breaking effect.
  - ★ we extract the amplitude and strong phase from experimental data by  $\chi^2$  fit.

- color-suppressed tree emission diagram( $C$ )

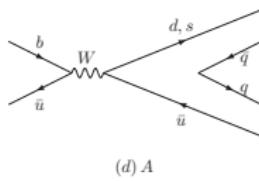
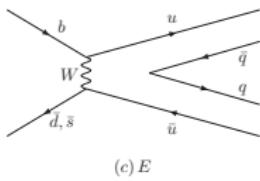


(b)  $C$

$$\begin{aligned}
 C^{P_1 P_2} &= i \frac{G_F}{\sqrt{2}} V_{ub} V_{uq'} \chi^C e^{i\phi^C} f_{p_2} (m_B^2 - m_{p_1}^2) F_0^{BP_1}(m_{p_2}^2), \\
 C^{VP} &= \sqrt{2} G_F V_{ub} V_{uq'} \chi^C e^{i\phi^C} f_P m_V A_0^{B-V}(m_P^2) (\varepsilon_V^* \cdot p_B), \\
 C^{PV} &= \sqrt{2} G_F V_{ub} V_{uq'} \chi^{C'} e^{i\phi^{C'}} f_V m_V F_1^{B-P}(m_V^2) (\varepsilon_V^* \cdot p_B),
 \end{aligned} \quad (2)$$

- ★  $\chi^C, e^{i\phi^C}$  and  $\chi^{C'}, e^{i\phi^{C'}}$  to distinguish cases in which the emissive meson is **pseudo-scalar** or **vector** respectively.

► The annihilation type diagrams( $E$  and  $A$ )



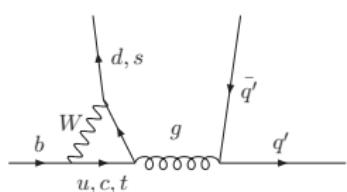
- ★ W-exchange topology ( $E$ ) is **non-factorization** in QCD factorization approach(NLO)

$$E^{P_1 P_2} = i \frac{G_F}{\sqrt{2}} V_{ub} V_{uq'} \chi^E e^{i\phi^E} f_B m_B^2 \left( \frac{f_{p_1} f_{p_2}}{f_\pi^2} \right),$$

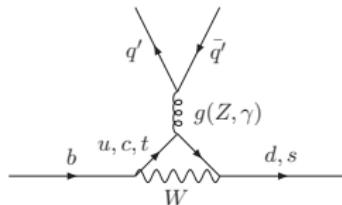
$$E^{PV, VP} = \sqrt{2} G_F V_{ub} V_{uq'} \chi^E e^{i\phi^E} f_B m_V \left( \frac{f_P f_V}{f_\pi^2} \right) (\varepsilon_V^* \cdot p_B), \quad (3)$$

- ★ As discussed in conventional topological diagram approach, W-annihilation diagram ( $A$ ) contribution **is negligible**.

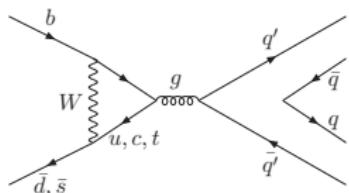
The penguin topological diagrams are grouped into QCD penguin and electro-weak penguin topologies.



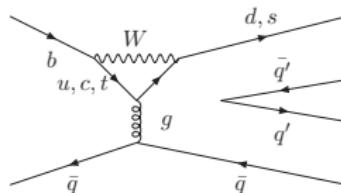
(a)  $P$



(b)  $P_C(P_{EW})$

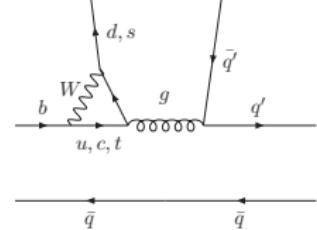


(c)  $P_E$



(d)  $P_A$

- ▶ color-favored penguin emission diagram ( $P$ )



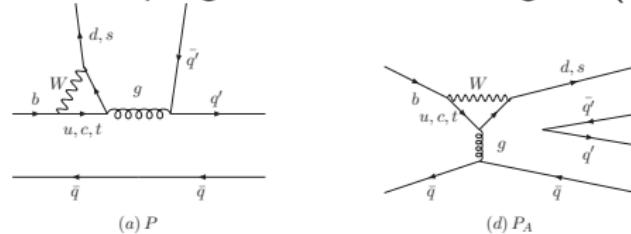
1. The leading contribution from topology

$P$  diagram is similar to diagram  $T$ , which is proved factorization in various QCD-inspired approaches.

2. “chiral enhanced” penguin contributions need to be fitted.

$$\begin{aligned}
 P^{PP} &= -i \frac{G_F}{\sqrt{2}} V_{tb} V_{tq'}^* [a_4(\mu) + \chi^P e^{i\phi^P} r_\chi] f_{p_2} (m_B^2 - m_{p_1}^2) F_0^{BP_1}(m_{p_2}^2), \\
 P^{PV} &= -\sqrt{2} G_F V_{tb} V_{tq'}^* a_4(\mu) f_V m_V F_1^{B-P} m_V^2 (\varepsilon_V^* \cdot p_B), \\
 P^{VP} &= -\sqrt{2} G_F V_{tb} V_{tq'}^* [a_4(\mu) - \chi^P e^{i\phi^P} r_\chi] f_P m_V A_0^{B-V}(m_P^2) (\varepsilon_V^* \cdot p_B).
 \end{aligned} \tag{4}$$

- ▶ power correction to  $P$ -penguin annihilation diagram ( $P_A$ )



- ★  $P_A$  is similar with  $P$  and the difference is only at QCD not EW.

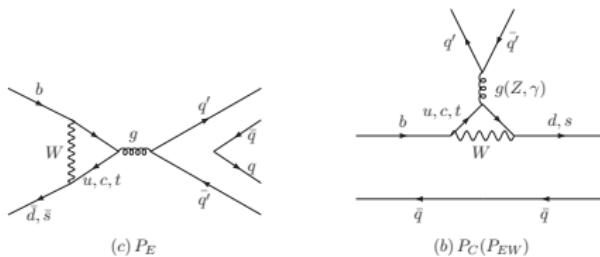
$$\begin{aligned}
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 \end{aligned} \tag{5}$$

- ★ The contribution of  $P_A$  can be included in  $\chi^P$ , except for  $B \rightarrow PV$  decays, where we need two more parameters

$$P_A^{PV} = -\sqrt{2} G_F V_{tb} V_{tq'}^* \chi^{P_A} e^{i\phi^{P_A}} f_B m_V \left( \frac{f_P f_V}{f_\pi^2} \right) (\varepsilon_V^* \cdot p_B). \tag{6}$$

- $P_E$  diagram is argued smaller than  $P_A$  diagram, which can be ignored reliably in decay modes not dominated by it, except  $B_s \rightarrow \pi^+ \pi^-$  decay.

$$Br(B_s \rightarrow \pi^+ \pi^-) = (0.76 \pm 0.19) \times 10^{-6}$$

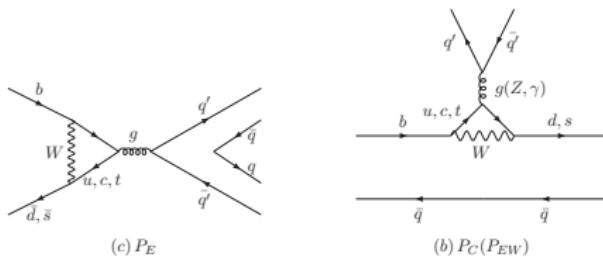


- The flavor-singlet QCD penguin diagram  $P_C$  only contribute to the isospin singlet mesons  $\eta$ ,  $\eta'$ ,  $\omega$  and  $\phi$ .

$$\begin{aligned}
 P_C^{PP} &= -i \frac{G_F}{\sqrt{2}} V_{tb} V_{tq'}^* \chi^{P_C} e^{i\phi^{P_C}} f_{p_2} (m_B^2 - m_{p_1}^2) F_0^{BP_1} (m_{p_2}^2), \\
 P_C^{VP} &= -\sqrt{2} G_F V_{tb} V_{tq'}^* \chi^{P_C} e^{i\phi^{P_C}} f_{PMV} A_0^{B-V} (m_P^2) (\varepsilon_V^* \cdot p_B), \\
 P_C^{PV} &= -\sqrt{2} G_F V_{tb} V_{tq'}^* \chi^{P'_C} e^{i\phi^{P'_C}} f_{VMV} F_1^{B-P} (m_V^2) (\varepsilon_V^* \cdot p_B), \quad (7)
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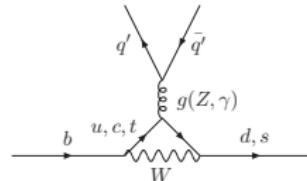
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- The **EW-penguin** unnegligiblely contribute to the neutral isospin 1 meson emission decays.



- ★  $P_{EW}$  is very similar to the  $T$  diagram-Factorization

$(b) P_C(P_{EW})$

$$\begin{aligned}
 P_{EW}^{PP} &= -i \frac{G_F}{\sqrt{2}} V_{tb} V_{tq'}^* e_q \frac{3}{2} a_9(\mu) f_{p_2} (m_B^2 - m_{p_1}^2) F_0^{BP_1}(m_{p_2}^2), \\
 P_{EW}^{PV} &= -\sqrt{2} G_F V_{tb} V_{tq'}^* e_q \frac{3}{2} a_9(\mu) f_V m_V F_1^{B-P}(m_V^2) (\varepsilon_V^* \cdot p_B), \\
 P_{EW}^{VP} &= -\sqrt{2} G_F V_{tb} V_{tq'}^* e_q \frac{3}{2} a_9(\mu) f_P m_V A_0^{B-V}(m_P^2) (\varepsilon_V^* \cdot p_B),
 \end{aligned} \quad (8)$$

where  $a_9(\mu)$  is the effective Wilson coefficient

- ▶ All together we have **14 parameters** to be fitted for all  $B \rightarrow PP, PV$  and  $VP$  decays.
  - The 6 parameters for tree diagrams are:  
Color suppressed tree diagram amplitude  $\chi^C, \chi^{C'}$  and their phases  $\phi^C, \phi^{C'}$ ;  
W-exchange diagram amplitude  $\chi^E$  and its phase  $\phi^E$ .
  - The 8 parameters for penguin diagrams are:  
Chiral enhanced penguin amplitude  $\chi^P$  and its phase  $\phi^P$  ;  
flavor singlet penguin amplitude  $\chi^{P_C}, \chi^{P'_C}$  and their phases  $\phi^{P_C}, \phi^{P'_C}$  for the pseudo-scalar and vector meson emission, respectively;  
the penguin annihilation amplitude  $\chi^{P_A}$  and its phase  $\phi^{P_A}$  for the vector meson emission only.
- ★ After keeping flavor  $SU(3)$  breaking effect and factorization approaches, the number of theoretical parameters to be fitted from experimental data is reduced.

## Global Fit for all $B \rightarrow PP, VP$ and $PV$ decays

- ▶ 37 branching Ratios and 11 CP violation observations data are used for the fit.
- ▶ the best-fitted parameters as:

$$\begin{aligned}\chi^C &= 0.48 \pm 0.06, & \phi^C &= -1.58 \pm 0.08, \\ \chi^{C'} &= 0.42 \pm 0.16, & \phi^{C'} &= 1.59 \pm 0.17, \\ \chi^E &= 0.057 \pm 0.005, & \phi^E &= 2.71 \pm 0.13, \\ \chi^P &= 0.10 \pm 0.02, & \phi^P &= -0.61 \pm 0.02. \\ \chi^{P_C} &= 0.048 \pm 0.003, & \phi^{P_C} &= 1.56 \pm 0.08, \\ \chi^{P'_C} &= 0.039 \pm 0.003, & \phi^{P'_C} &= 0.68 \pm 0.08, \\ \chi^{P_A} &= 0.0059 \pm 0.0008, & \phi^{P_A} &= 1.51 \pm 0.09,\end{aligned}\tag{9}$$

with  $\chi^2/\text{d.o.f} = 45.2/34 = 1.3$ .

- ★ Large strong phase
- ★ This  $\chi^2$  per degree of freedom is smaller than the conventional flavor diagram approach.

# Hierarchy of Topology

- ▶  $B \rightarrow \pi\pi$  and  $B \rightarrow \pi\rho$

$$T^{\pi\pi} : C^{\pi\pi} : E^{\pi\pi} : P^{\pi\pi} = 1 : 0.47 : 0.29 : 0.32$$

$$T^{\rho\pi} : C'^{\pi\rho} : P^{\rho\pi} : P_{EW}^{\pi\rho} = 1 : 0.54 : 0.25 : 0.04$$

$$T^{\pi\rho} : C^{\rho\pi} : P^{\rho\pi} : P_{EW}^{\rho\pi} = 1 : 0.36 : 0.19 : 0.03.$$

$$T > C(C') > E \sim P > P_{EW}.$$

- ★ In agreement with those QCD inspired approaches

- ▶  $B \rightarrow \pi K$  and  $B \rightarrow \pi K^*$

$$T^{\pi K} : C^{\pi K} : P^{\pi K} : P_{EW}^{\pi K} = 1 : 0.4 : 6.0 : 0.6$$

$$T^{\pi K^*} : C^{K^*\pi} : P^{\pi K^*} : P_A^{\pi K^*} : P_{EW}^{K^*\pi} = 1 : 0.37 : 2.87 : 1.44 : 0.52.$$

$$P > P_A > T > P_{EW} > C.$$

- ★  $P_{EW}$  is even more larger than  $C$

# Predict branching fractions for $B \rightarrow PP, VP$ and $PV$ and $CP$ violation.

Mode	Amplitudes	Exp	This work	Flavor diagram
$\pi^-\pi^0$	$T, C, P_{EW}$	$\star 5.5 \pm 0.4$	$5.08 \pm 0.39 \pm 1.02 \pm 0.02$	$5.40 \pm 0.79$
$\pi^-\eta$	$T, C, P, P_C, P_{EW}$	$\star 4.02 \pm 0.27$	$4.13 \pm 0.25 \pm 0.64 \pm 0.01$	$3.88 \pm 0.39$
$\pi^-\eta'$	$T, C, P, P_C, P_{EW}$	$\star 2.7 \pm 0.9$	$3.37 \pm 0.21 \pm 0.49 \pm 0.01$	$5.59 \pm 0.54$
$\pi^+\pi^-$	$T, E, (P_E), P$	$\star 5.12 \pm 0.19$	$5.15 \pm 0.36 \pm 1.31 \pm 0.14$	$5.17 \pm 1.03$
$\pi^0\pi^0$	$C, E, P, (P_E), P_{EW}$	$\star 1.91 \pm 0.22$	$1.94 \pm 0.30 \pm 0.28 \pm 0.05$	$1.88 \pm 0.42$
$\pi^0\eta$	$C, E, P_C, (P_E), P_{EW}$	$< 1.5$	$0.86 \pm 0.08 \pm 0.08 \pm 0.04$	$0.56 \pm 0.03$
$\pi^0\eta'$	$C, E, P_C, (P_E), P_{EW}$	$1.2 \pm 0.6$	$0.87 \pm 0.08 \pm 0.10 \pm 0.03$	$1.21 \pm 0.16$
$\eta\eta$	$C, E, P_C, (P_E), P_{EW}$	$< 1.0$	$0.44 \pm 0.09 \pm 0.08 \pm 0.005$	$0.77 \pm 0.12$
$\eta\eta'$	$C, E, P_C, (P_E), P_{EW}$	$< 1.2$	$0.77 \pm 0.13 \pm 0.14 \pm 0.008$	$1.99 \pm 0.26$
$\eta'\eta'$	$C, E, P_C, (P_E), P_{EW}$	$< 1.7$	$0.38 \pm 0.05 \pm 0.07 \pm 0.003$	$1.60 \pm 0.20$
$K^-K^0$	$P$	$\star 1.31 \pm 0.17$	$1.32 \pm 0.04 \pm 0.26 \pm 0.01$	$1.03 \pm 0.02$
$K^0\bar{K}^0$	$P$	$\star 1.21 \pm 0.16$	$1.23 \pm 0.03 \pm 0.25 \pm 0.01$	$0.89 \pm 0.11$
$\pi^-K^0$	$P$	$\star 23.7 \pm 0.8$	$23.2 \pm 0.6 \pm 4.6 \pm 0.2$	$23.53 \pm 0.42$
$\pi^0K^-$	$T, C, P, P_{EW}$	$\star 12.9 \pm 0.5$	$12.8 \pm 0.32 \pm 2.35 \pm 0.10$	$12.71 \pm 1.05$
$\eta K^-$	$T, C, P, P_C, P_{EW}$	$\star 2.4 \pm 0.4$	$2.0 \pm 0.13 \pm 1.19 \pm 0.03$	$1.93 \pm 0.31$
$\eta' K^-$	$T, C, P, P_C, P_{EW}$	$\star 70.6 \pm 2.5$	$70.1 \pm 4.7 \pm 11.3 \pm 0.22$	$70.92 \pm 8.54$
$\pi^+K^-$	$T, P$	$\star 19.6 \pm 0.5$	$19.8 \pm 0.54 \pm 4.0 \pm 0.2$	$20.2 \pm 0.39$
$\pi^0\bar{K}^0$	$C, P, P_{EW}$	$\star 9.9 \pm 0.5$	$8.96 \pm 0.26 \pm 1.96 \pm 0.09$	$9.73 \pm 0.82$
$\eta\bar{K}^0$	$C, P, P_C, P_{EW}$	$\star 1.23 \pm 0.27$	$1.35 \pm 0.10 \pm 1.02 \pm 0.03$	$1.49 \pm 0.27$
$\eta' K^0$	$C, P, P_C, P_{EW}$	$\star 66 \pm 4$	$66.4 \pm 4.5 \pm 10.6 \pm 0.21$	$66.51 \pm 7.97$

Mode	Amplitudes	Exp	This work	Flavor diagram
$\pi^- \rho^0$	$T, C', P, P_A, P_{EW}$	$\star 8.3 \pm 1.2$	$8.6 \pm 1.81 \pm 1.38 \pm 0.03$	$7.59 \pm 1.41$
$\pi^- \omega$	$T, C', P, P'_C, P_A, P_{EW}$	$\star 6.9 \pm 0.5$	$6.78 \pm 1.46 \pm 1.09 \pm 0.02$	$7.03 \pm 1.42$
$\pi^- \phi$	$P'_C, P_{EW}$	$< 0.15$	$0.28 \pm 0.004 \pm 0.055 \pm 0.003$	$0.04 \pm 0.02$
$\pi^0 \rho^-$	$T, C, P, P_A, P_{EW}$	$\star 10.9 \pm 1.4$	$12.9 \pm 0.73 \pm 2.30 \pm 0.12$	$12.15 \pm 2.52$
$\eta \rho^-$	$T, C, P, P_C, P_A, P_{EW}$	$7.0 \pm 2.9$	$8.16 \pm 0.48 \pm 1.43 \pm 0.07$	$5.26 \pm 1.19$
$\eta' \rho^-$	$T, C, P, P_C, P_A, P_{EW}$	$\star 9.7 \pm 2.2$	$6.0 \pm 0.34 \pm 0.97 \pm 0.05$	$5.66 \pm 1.25$
$\pi^+ \rho^-$	$T, E, P, (P_E), P_A$	$\star 14.6 \pm 1.6$	$12.4 \pm 0.64 \pm 3.20 \pm 0.38$	$15.20 \pm 1.52$
$\pi^- \rho^+$	$T, E, P, (P_E)$	$\star 8.4 \pm 1.1$	$6.04 \pm 0.47 \pm 1.70 \pm 0.25$	$8.22 \pm 1.06$
$\pi^0 \rho^0$	$C, C', E, P, P_A, (P_E), P_{EW}$	$\star 2 \pm 0.5$	$1.32 \pm 0.47 \pm 0.09 \pm 0.14$	$2.24 \pm 0.93$
$\pi^0 \omega$	$C, C', E, P, P_A, (P_E), P_{EW}$	$< 0.5$	$2.31 \pm 0.88 \pm 0.24 \pm 0.07$	$1.02 \pm 0.66$
$\pi^0 \phi$	$P'_C, P_{EW}$	$< 0.15$	$0.13 \pm 0.002 \pm 0.025 \pm 0.001$	$0.02 \pm 0.01$
$\eta \rho^0$	$C, C', E, P, P_C, P'_C, P_A, (P_E), P_{EW}$	$< 1.5$	$4.41 \pm 1.15 \pm 0.39 \pm 0.17$	$0.54 \pm 0.32$
$\eta \omega$	$C, C', E, P, P_C, P'_C, P_A, (P_E), P_{EW}$	$0.94^{+0.40}_{-0.31}$	$0.89 \pm 0.30 \pm 0.08 \pm 0.09$	$1.12 \pm 0.44$
$\eta' \phi$	$P'_C, P_{EW}$	$< 0.5$	$0.077 \pm 0.001 \pm 0.015 \pm 0.0008$	$0.01 \pm 0.01$
$\eta' \rho^0$	$C, C', E, P, P_C, P'_C, (P_E), P_{EW}$	$< 1.3$	$3.19 \pm 0.77 \pm 0.29 \pm 0.12$	$0.63 \pm 0.33$
$\eta' \omega$	$C, C', E, P, P_C, P'_C, (P_E), P_{EW}$	$1.0^{+0.5}_{-0.4}$	$0.95 \pm 0.21 \pm 0.05 \pm 0.06$	$1.24 \pm 0.47$
$\eta' \phi$	$P'_C, P_{EW}$	$< 0.5$	$0.05 \pm 0.0008 \pm 0.01 \pm 0.0005$	$0.01 \pm 0.01$
$K^- K^{*0}$	$P, P_A$	$< 1.1$	$0.59 \pm 0.06 \pm 0.10 \pm 0.01$	$0.46 \pm 0.03$
$K^0 K^{*-}$	$P$		$0.44 \pm 0.03 \pm 0.09 \pm 0.004$	$0.31 \pm 0.03$
$K^0 K^{*0}$	$P$		$0.41 \pm 0.02 \pm 0.08 \pm 0.004$	$0.29 \pm 0.03$
$\bar{K}^0 K^{*0}$	$P, P_A$		$0.55 \pm 0.05 \pm 0.09 \pm 0.01$	$0.43 \pm 0.02$
$\pi^- K^{*0}$	$P, P_A$	$\star 10.1 \pm 0.9$	$10.0 \pm 0.95 \pm 1.78 \pm 0.15$	$10.47 \pm 0.60$
$\pi^0 K^{*-}$	$T, C, P, P_A, P_{EW}$	$\star 8.2 \pm 1.9$	$6.23 \pm 0.51 \pm 0.98 \pm 0.07$	$9.79 \pm 2.95$
$\eta K^{*-}$	$T, C, P, P_C, P_A, P_{EW}$	$\star 19.3 \pm 1.6$	$17.3 \pm 0.8 \pm 2.4 \pm 0.3$	$16.57 \pm 2.58$
$\eta' K^{*-}$	$T, C, P, P_C, P_A, P_{EW}$	$4.8^{+1.8}_{-1.6}$	$3.31 \pm 0.44 \pm 0.38 \pm 0.13$	$3.43 \pm 1.43$
$K^- \rho^0$	$T, C', P, P_{EW}$	$\star 3.7 \pm 0.5$	$3.97 \pm 0.25 \pm 0.80 \pm 0.04$	$3.97 \pm 0.90$
$K^- \omega$	$T, C', P, P'_C, P_{EW}$	$\star 6.5 \pm 0.4$	$6.52 \pm 0.73 \pm 1.13 \pm 0.06$	$6.43 \pm 1.49$
$K^- \phi$	$P, P'_C, P_A, P_{EW}$	$\star 8.8 \pm 0.7$	$8.38 \pm 1.21 \pm 0.69 \pm 0.50$	$8.34 \pm 1.31$
$\bar{K}^0 \rho^-$	$P$	$\star 8 \pm 1.5$	$7.74 \pm 0.47 \pm 1.55 \pm 0.07$	$7.09 \pm 0.77$
$\pi^+ K^{*-}$	$T, P, P_A$	$\star 8.4 \pm 0.8$	$8.40 \pm 0.77 \pm 1.46 \pm 0.14$	$8.35 \pm 0.50$
$\pi^0 \bar{K}^{*0}$	$C, P, P_A, P_{EW}$	$\star 3.3 \pm 0.6$	$3.35 \pm 0.36 \pm 0.65 \pm 0.08$	$3.89 \pm 1.98$
$\eta \bar{K}^{*0}$	$C, P, P_C, P_A, P_{EW}$	$\star 15.9 \pm 1$	$16.6 \pm 0.7 \pm 2.3 \pm 0.3$	$16.34 \pm 2.48$
$\eta' \bar{K}^{*0}$	$C, P, P_C, P'_C, P_A, P_{EW}$	$\star 2.8 \pm 0.6$	$3.0 \pm 0.5 \pm 0.3 \pm 0.1$	$3.14 \pm 1.24$
$K^- \rho^+$	$T, P$	$\star 7 \pm 0.9$	$8.27 \pm 0.44 \pm 1.65 \pm 0.07$	$8.28 \pm 0.80$
$\bar{K}^0 \rho^0$	$C', P, P_{EW}$	$\star 4.7 \pm 0.4$	$4.59 \pm 0.34 \pm 0.79 \pm 0.04$	$4.97 \pm 1.14$
$\bar{K}^0 \omega$	$C', P, P'_C, P_{EW}$	$\star 4.8 \pm 0.6$	$4.80 \pm 0.61 \pm 0.95 \pm 0.05$	$4.82 \pm 1.26$
$\bar{K}^0 \phi$	$P, P'_C, P_A, P_{EW}$	$\star 7.3 \pm 0.7$	$7.77 \pm 1.12 \pm 0.64 \pm 0.46$	

# CP asymmetry

- ▶ The direct CP asymmetry parameter is also proportional to the strong phase difference
- ▶ The mixing induced CP asymmetries are dominated by the  $B_0 - \bar{B}_0$  mixing phase with little dependence on strong phases, searching possible new physics.

Mode	$\mathcal{A}_{\text{exp}}$	$\mathcal{A}_{\text{this work}}$	$\mathcal{S}_{\text{exp}}$	$\mathcal{S}_{\text{this work}}$
$\pi^+ \pi^-$	$\star 0.31 \pm 0.05$	$0.31 \pm 0.04$	$\star - 0.67 \pm 0.06$	$-0.60 \pm 0.03$
$\pi^0 \pi^0$	$0.43 \pm 0.24$	$0.57 \pm 0.06$		$0.58 \pm 0.06$
$\pi^0 \eta$		$-0.16 \pm 0.16$		$-0.98 \pm 0.04$
$\pi^0 \eta'$		$0.39 \pm 0.14$		$-0.90 \pm 0.07$
$\eta \eta$		$-0.85 \pm 0.06$		$0.33 \pm 0.12$
$\eta \eta'$		$-0.97 \pm 0.04$		$-0.20 \pm 0.15$
$\eta' \eta'$		$-0.87 \pm 0.07$		$-0.46 \pm 0.14$
$\pi^0 K_s$	$0.00 \pm 0.13$	$-0.14 \pm 0.03$	$\star 0.58 \pm 0.17$	$0.73 \pm 0.01$
$\eta K_s$		$-0.30 \pm 0.10$		$0.68 \pm 0.04$
$\eta' K_s$	$0.06 \pm 0.04$	$0.030 \pm 0.004$	$\star 0.63 \pm 0.06$	$0.69 \pm 0.00$
$K^0 \bar{K}^0$		$-0.057 \pm 0.002$	$0.8 \pm 0.5$	$0.099 \pm 0.002$
$\pi^- \pi^0$	$0.03 \pm 0.04$	$-0.026 \pm 0.003$		
$\pi^- \eta$	$-0.14 \pm 0.07$	$-0.081 \pm 0.074$		
$\pi^- \eta'$	$0.06 \pm 0.16$	$0.374 \pm 0.087$		
$\pi^- \bar{K}^0$	$-0.017 \pm 0.016$	$0$		
$\pi^0 K^-$	$0.037 \pm 0.021$	$0.047 \pm 0.025$		
$\eta K^-$	$\star - 0.37 \pm 0.08$	$-0.426 \pm 0.043$		
$\eta' K^-$	$0.013 \pm 0.017$	$-0.027 \pm 0.008$		
$K^- \bar{K}^0$	$-0.21 \pm 0.14$	$0$		
$\pi^+ K^-$	$\star - 0.082 \pm 0.006$	$-0.080 \pm 0.011$		

## Estimate the $SU(3)$ breaking effect in FAT

- ▶  $SU(3)$  breaking effects in amplitudes for  $B \rightarrow PP$  to be around 10%

$$\left| \frac{T(B^- \rightarrow \pi^0 K^-)}{V_{ub} V_{us}^*} \right| : \left| \frac{T(B^- \rightarrow \pi^0 \pi^-)}{V_{ub} V_{ud}^*} \right| = 1 : 0.83,$$

$$\left| \frac{C(B^- \rightarrow \pi^0 K^-)}{V_{ub} V_{us}^*} \right| : \left| \frac{C(B^- \rightarrow \pi^0 \pi^-)}{V_{ub} V_{ud}^*} \right| = 1 : 0.91,$$

$$\left| \frac{P(\bar{B}^0 \rightarrow \pi^+ K^-)}{V_{tb} V_{ts}^*} \right| : \left| \frac{P(\bar{B}^0 \rightarrow \pi^+ \pi^-)}{V_{tb} V_{td}^*} \right| = 1 : 0.89,$$

$$\left| \frac{P_C(B^- \rightarrow \eta K^-)}{V_{tb} V_{ts}^*} \right| : \left| \frac{P_C(B^- \rightarrow \eta \pi^-)}{V_{tb} V_{td}^*} \right| = 1 : 0.91.$$

- ▶  $SU(3)$  breaking effects in amplitudes for  $B \rightarrow PV$  are larger than 20%.

$$\left| \frac{T(B^- \rightarrow \pi^0 K^{*-})}{V_{ub} V_{us}^*} \right| : \left| \frac{T(B^- \rightarrow \pi^0 \rho^-)}{V_{ub} V_{ud}^*} \right| = 1 : 0.83,$$

$$\left| \frac{C(B^- \rightarrow K^{*-} \pi^0)}{V_{ub} V_{us}^*} \right| : \left| \frac{C(B^- \rightarrow \rho^- \pi^0)}{V_{ub} V_{ud}^*} \right| = 1 : 0.80,$$

$$\left| \frac{P(\bar{B}^0 \rightarrow \pi^+ K^{*-})}{V_{tb} V_{ts}^*} \right| : \left| \frac{P(\bar{B}^0 \rightarrow \pi^+ \rho^-)}{V_{tb} V_{td}^*} \right| = 1 : 0.74,$$

$$\left| \frac{P_C(B^- \rightarrow K^{*-} \eta)}{V_{tb} V_{ts}^*} \right| : \left| \frac{P_C(B^- \rightarrow \rho^- \eta)}{V_{tb} V_{td}^*} \right| = 1 : 0.80,$$

$$\left| \frac{P_A(\bar{B}^0 \rightarrow \pi^+ K^{*-})}{V_{tb} V_{ts}^*} \right| : \left| \frac{P_A(\bar{B}^0 \rightarrow \pi^+ \rho^-)}{V_{tb} V_{td}^*} \right| = 1 : 0.84.$$

## Summary

- ▶ studied  $B \rightarrow PP, PV$  in factorization assisted topological amplitude approach.
- ▶  $T$  was in factorization without free parameters.  $P_{EW}$  was also included.
- ▶ For most other topological diagrams, the corresponding decay constants, form factors were factorized out from them before  $\chi^2$  fit assisted by factorization hypothesis to indicate the flavor  $SU(3)$  breaking effect.
- ▶ Only 14 universal non-perturbative parameters to be fitted from all  $B \rightarrow PP, PV$  decay channels. the  $\chi^2$  per degree of freedom is smaller than the conventional flavor diagram approach.
- ▶ predict branching fractions and  $CP$  asymmetry parameters of nearly 100  $B_{u,d}$  and  $B_s$  decay modes. The long-standing puzzles of  $\pi\pi$  branching ratios has been resolved consistently.

THANK YOU

## backup

- ▶ input parameters

$V_{CKM}$  with the Wolfenstein parameters:

$$\lambda = 0.22537 \pm 0.00061, \quad A = 0.814^{+0.023}_{-0.024}$$

$$\bar{\rho} = 0.117 \pm 0.021, \quad \bar{\eta} = 0.353 \pm 0.013.$$

**Table:** The decay constants of light pseudo-scalar mesons and vector mesons (in unit of MeV). (5% uncertainty)

$f_\pi$	$f_K$	$f_B$	$f_{B_s}$	$f_\rho$	$f_{K^*}$	$f_\omega$	$f_\phi$
130	156	190	225	213	220	192	225

**Table:** The transition form factors of  $B$  meson decays at  $q^2=0$  and dipole model parameters(10 % uncertainty)

	$F_0^{B \rightarrow \pi}$	$F_0^{B \rightarrow K}$	$F_0^{B_s \rightarrow K}$	$F_0^{B \rightarrow \eta_q}$	$F_0^{B_s \rightarrow \eta_s}$
$F(0)$	0.27	0.29	0.25	0.21	0.30
$\alpha_1$	0.50	0.53	0.54	0.52	0.53
$\alpha_2$	-0.13	-0.13	-0.15	0	0
	$F_1^{B \rightarrow \pi}$	$F_1^{B \rightarrow K}$	$F_1^{B_s \rightarrow K}$	$F_1^{B \rightarrow \eta_q}$	$F_1^{B_s \rightarrow \eta_s}$
$F(0)$	0.27	0.29	0.25	0.21	0.30
$\alpha_1$	0.52	0.54	0.57	1.43	1.48
$\alpha_2$	0.45	0.50	0.50	0.41	0.46
	$A_0^{B \rightarrow \rho}$	$A_0^{B \rightarrow \omega}$	$A_0^{B \rightarrow K^*}$	$A_0^{B_s \rightarrow K^*}$	$A_0^{B_s \rightarrow \phi}$
$A(0)$	0.29	0.25	0.36	0.27	0.30
$\alpha_1$	1.56	1.60	1.51	1.74	1.73
$\alpha_2$	0.17	0.22	0.14	0.47	0.41

For the  $q^2$  dependence of the transition form factors, we use the dipole parametrization:

$$F_i(q^2) = \frac{F_i(0)}{1 - \alpha_1 \frac{q^2}{M_{\text{pole}}^2} + \alpha_2 \frac{q^4}{M_{\text{pole}}^4}},$$

$B \rightarrow P_1 P_2$  ( $P$  represent  $\pi, K, \eta, \eta'$ )

$$\begin{aligned}\mathcal{H}_{eff} = & \frac{G_F}{\sqrt{2}} \{ \Sigma_{q'=d,s} V_{ub} V_{uq}^* [C_1(\mu) O_1^u(\mu) + C_2(\mu) O_2^u(\mu)] \\ & - V_{tb} V_{tq'}^* \Sigma_{i=3}^{10} C_i(\mu) O_i(\mu) \}\end{aligned}$$

$$\begin{aligned}O_1^u &= (\bar{q}'_\alpha u_\beta)_{V-A} (\bar{u}_\beta b_\alpha)_{V-A}, O_2^u = (\bar{q}' u)_{V-A} (\bar{u} b)_{V-A} \\ O_3 &= (\bar{q}' b)_{V-A} (\bar{q} q)_{V-A}, O_4 = (\bar{q}'_\alpha b_\beta)_{V-A} (\bar{q}_\beta q_\alpha)_{V-A} \\ O_5 &= (\bar{q}' b)_{V-A} (\bar{q} q)_{V+A}, O_6 = (\bar{q}'_\alpha b_\beta)_{V-A} (\bar{q}_\beta q_\alpha)_{V+A} \\ O_7 &= \frac{3}{2} (\bar{q}' b)_{V-A} e_q (\bar{q} q)_{V+A}, O_8 = \frac{3}{2} (\bar{q}'_\alpha b_\beta)_{V-A} e_q (\bar{q}_\beta q_\alpha)_{V+A} \\ O_9 &= \frac{3}{2} (\bar{q}' b)_{V-A} e_q (\bar{q} q)_{V-A}, O_{10} = \frac{3}{2} (\bar{q}'_\alpha b_\beta)_{V-A} e_q (\bar{q}_\beta q_\alpha)_{V-A}\end{aligned}$$

$O_7 - O_{10}$  QED penguin contribution is not ignore although  $\alpha_{em}$  is smaller than QCD.

Penguin contribution from quark loops correction  $O_{1-6}$ ,  $O_{8g}$ .

$\mu = 2.1$ .

$$C_1(\mu) = -0.29, C_2(\mu) = 1.14;$$

$$C_3(\mu) = 0.02, C_4(\mu) = -0.05;$$

$$C_5(\mu) = 0.011, C_6(\mu) = -0.067;$$

$$C_7(\mu) = -1.02e - 5, C_8(\mu) = 0.00073;$$

$$C_9(\mu) = -0.0098, C_{10}(\mu) = 0.0025;$$

$$a_1(\mu) = 1.045, a_4(\mu) = -0.044, a_6(\mu) = -0.064;$$

$$a_7(\mu) = 0.00023, a_8(\mu) = 0.0007;$$

$$\textcolor{red}{a_9(\mu)} = -0.009, a_{10}(\mu) = -0.0008;$$