Analysis of $\Lambda_C^+ \to \Lambda + X$

On behalf of BESIII Collaboration

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Introduction

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Heavy Quark Effective Theory

Heavy quark physics plays an important role in testing the Standard Model and searching for new physics. This study is concerned on the measurement of inclusive branching fraction(BF) of $\Lambda_C^+ \rightarrow \Lambda + X$, which can be used to test the Heavy Quark Effective Theory (HQET).



Motivation

PDG Results

The averaged BF in the latest PDG is $(35 \pm 11)\%$, of which the uncertainty is relatively large and the result is relative to the $\mathcal{B}(\Lambda_C^+ \to pK^-\pi^+)$.

The summary of the BFs of known decay modes of $\Lambda_C^+ \rightarrow \Lambda + X$ is not consistent with the inclusive measurement.

Decay modes	Branching fractions
$\Lambda_c^+ \to \Lambda \pi^+$	$(1.46 \pm 0.13)\%$
$\Lambda_c^+ \to \Lambda \pi^+ \pi^0$	$(5.0 \pm 1.3)\%$
$\Lambda_c^+ \to \Lambda \pi^+ \pi^+ \pi^-$	$(3.59 \pm 0.28)\%$
$\Lambda_c^+\to\Lambda\pi^+\pi^+\pi^-\pi^0$	$(2.5 \pm 0.9)\%$
$\Lambda_c^+ \to \Lambda K^+ \bar{K}^0$	$(6.4 \pm 1.3) \times 10^{-3}$
$\Lambda_c^+ \to \Sigma^0 \pi^+, \Sigma^0 \to \gamma \Lambda$	$(1.43 \pm 0.14)\%$
$\Lambda_c^+ \to \Sigma^0 \pi^+ \pi^0, \ \Sigma^0 \to \gamma \Lambda$	$(2.5 \pm 0.9)\%$
$\Lambda_c^+ \to \Sigma^0 \pi^+ \pi^+ \pi^-, \ \Sigma^0 \to \gamma \Lambda$	$(1.13 \pm 0.31)\%$
$\Lambda_c^+ \to \Xi^0 K^+, \Xi^0 \to \Lambda \pi^0$	$(5.3 \pm 1.3) \times 10^{-3}$
$\Lambda_c^+ \to \Xi^- K^+ \pi^+, \ \Xi^- \to \Lambda \pi^-$	$(7.0 \pm 0.8) \times 10^{-3}$
$\Lambda_c^+ \to \Lambda K^+$	$(6.9 \pm 1.4) \times 10^{-4}$
$\Lambda_c^+ \to \Sigma^0 K^+, \ \Sigma^0 \to \gamma \Lambda$	$(5.7 \pm 1.0) \times 10^{-4}$
$\Lambda_c^+ \to \Lambda l^+ \nu_l$	$(2.8 \pm 0.4)\%$
Total	$(22.35 \pm 1.93)\%$
$\Lambda_c^+ \to \Sigma^0 K^+ \pi^+ \pi^-, \ \Sigma^0 \to \gamma \Lambda$	$<2.9\times10^{-4}$
$\Lambda_c^+ \to \Lambda K^+ \pi^+ \pi^-$	$< 6 \times 10^{-4}$
$\Lambda_c^+ \to \Lambda \rho^+$	< 6%

Table 1: Summary of the known decay modes of $\Lambda_c \to \Lambda + X$.

CP Violation

In c-quark sector, the contribution to CP violation from the CKM mechanism is small, which makes it an excellent place to look for new physics(NP). Precise measurement of the CP violation parameter in charm sector is important.





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Samples

Data sample :

 $0.567 f b^{-1}$ at $\sqrt{s} = 4.5995$ GeV (2014).

MC sample : inclusive MC at $\sqrt{s} = 4.5995$ GeV. (including the process of $\Lambda_c^+ \Lambda_c^-, \tau^+ \tau^-, D/D_s + X, q\overline{q}, ISR$)

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 $p - |cos\theta|$ bins to obtain the efficiency.

Formula

$$\mathcal{B}^{\rm sig} = \frac{\sum_{ij} N_{ij}^{\rm sig} / \varepsilon_j^{\rm sig}}{\sum_i N_i^{\rm tag}},$$

Work flow





 ΔE cut



The signals are fitted by Crystal Ball function convoluted with a Gaussian function, while the backgrounds are described using polynomial function, 3σ cut criteria is taken.

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Background study

We generate fake data to study the origin of background. The fake data is produced by sampling from the inclusive Monte Carlo, each process has been scaled to be corresponding with the luminosity of data at $\sqrt{s} = 4.5995$ GeV.

From the figure, we can see that there are no peaking background events in the M_{bc} distribution of tagged Λ_c . We can use Argus function to describe the background.



Tag yields



The signals of Λ_c are fitted by the shape obtained from signal Monte Carlo, while the backgrounds are described using Argus function.

Tag modes	$\Delta E({ m GeV})$	$M_{ m bc}({ m GeV/c^2})$	Yields
$\bar{\Lambda}_c^- \to \bar{p} K_S^0$	[-0.021, 0.019]	[0.000_0.200]	1220 ± 37
$\bar{\Lambda}_c^- \to \bar{p} K^+ \pi^-$	[-0.020, 0.015]	[2.282, 2.300]	6088 ± 85



Reconstruction of Λ

Background study



We take a look at the distribution of M_{Λ} in fake data and find that there are peaking background events in the signal region.

Background study



 $N_{sig} = N_S - (N_A + N_B)/2 - r \cdot N_D + r \cdot (N_C + N_E)/2$

The normalization factor between the sideband region and signal region of M_{bc} is estimated to be 0.58 ± 0.06.

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Signal yields



The signal yield is summed to be $N_{sig} = 706 \pm 29$, which is consistent with result obtained by directly fitting the invariant mass of $p\pi^-$, which is $N_{sig} = 738 \pm 38$.

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Control sample

 $J/\psi \to \overline{p}K^+\Lambda$ and c.c.

The requirements to select out the control sample are:

Selection of control sample

- kaon PID: prob(K) > 0.01, prob(K) > prob(π), prob(K) > prob(p)

- proton PID: prob(p) > 0.01, prob(p) > prob(π), prob(p) > prob(K)

- Recoiling mass of $pK^-:M_{pK^-}\in[1.094,1.138]\,GeV/c^2$





Efficiency

We also divide the control sample into 4×4 bins according to the recoiling momentum and $|cos\theta|$ of p and K, then fit the recoiling mass to obtain the number of control sample in each bin. The number of reconstructed Λ in each bin is obtained by subtracting the number of events in sideband region from those in signal region of M_{Λ} .





Efficiency

The distribution of momentum and polar angle of Λ in the control sample are different with those in the process of $\Lambda_C^+ \to \Lambda + X$, which may cause difference in the reconstruction efficiency. We **re-weight** the control sample to make sure that the distribution of $p-\cos\theta$ are the same with those in the process of $\Lambda_C^+ \to \Lambda + X$, as shown in the backup slides.

$\epsilon_{data}(\%)$	$P({ m GeV/c})$				
$ \cos \theta $	(0, 0.3)	(0.3, 0.5)	(0.5, 0.7)	(0.7, 1.0)	
(0.00, 0.20)	8.64 ± 0.23	29.52 ± 0.36	36.12 ± 0.39	40.52 ± 0.57	
(0.20, 0.40)	8.50 ± 0.23	28.77 ± 0.36	35.71 ± 0.39	40.24 ± 0.56	
(0.40, 0.65)	8.14 ± 0.20	26.92 ± 0.31	34.06 ± 0.35	38.05 ± 0.50	
(0.65, 1.00)	4.69 ± 0.13	15.38 ± 0.19	20.90 ± 0.23	25.69 ± 0.36	

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BF without systematic error

Then the branching fraction of $\Lambda_C^+ \to \Lambda + X$ is calculated to be:

 $\mathcal{B}(\Lambda_{C}^{+}\rightarrow\Lambda+X)=(37.0\pm2.2)\%$



Input-output check

Result from fake data



Tag modes	$\Delta E({\rm GeV})$	$M_{\rm bc}({\rm GeV/c^2})$	Yields
$\bar{\Lambda}_c^- \rightarrow \bar{p} K_S^0$	[-0.017, 0.017]	[9.989.9.300]	1280 ± 39
$\bar{\Lambda}_c^- \to \overline{p} K^+ \pi^-$	[-0.022, 0.016]	[2.202, 2.300]	6795 ± 96

		ϵ_{dat}	a(%)	
$ \cos\theta $		<i>P</i> (G	eV/c)	
	(0.0, 0.3)	(0.3, 0.5)	(0.5, 0.7)	(0.7, 1.0)
(0.00, 0.20)	7.73 ± 0.16	27.23 ± 0.26	34.43 ± 0.29	38.16 ± 0.40
(0.20, 0.40)	7.19 ± 0.16	26.65 ± 0.26	33.48 ± 0.28	37.53 ± 0.39
(0.40, 0.65)	6.84 ± 0.14	24.56 ± 0.22	31.50 ± 0.25	35.08 ± 0.34
(0.65, 1.00)	3.71 ± 0.09	13.38 ± 0.13	18.36 ± 0.15	21.92 ± 0.22
		N_{s}	ignal	
$ \cos\theta $		<i>P</i> (G	eV/c)	
	(0.0, 0.3)	(0.3, 0.5)	(0.5, 0.7)	(0.7, 1.0)
(0.00, 0.20)	7.8 ± 4.8	40.2 ± 8.7	56.8 ± 9.6	37.6 ± 8.9
(0.20, 0.40)	5.4 ± 4.4	30.7 ± 7.9	56.2 ± 8.9	63.8 ± 9.6
(0.40, 0.65)	8.7 ± 4.7	57.1 ± 9.8	75.6 ± 10.5	46.7 ± 8.9
(0.65, 1.00)	-1.1 ± 3.9	34.7 ± 8.1	56.5 ± 9.1	36.8 ± 8.8

 $\mathcal{B}_{input} = 33.2\%$

$$\mathcal{B}_{output} = (30.7 \pm 2.5)\%$$



 $\Lambda' s$ efficiency



Fitting of tag yields: signal shape

The signal shape we used to fit the M_{bc} of $\overline{\Lambda}_{c}$ is obtained from signal Monte Carlo. To estimate the uncertainty due to the choice of the shape, we change the signal shape used in the fitting procedure and regain the tag yields.



The systematic uncertainty due to this is 0.94% relatively.



Fitting of tag yields: fitting range

We also try different fitting range to see if there are any changes of the tag yields. The range of M_{bc} is changed to [2.255,2.300] GeV/c^2 and the fits are redone.



The systematic uncertainty due to this is 0.10% relatively.

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Fitting of tag yields: endpoint of Argus function

The endpoint of the Argus function is set floated now, we fix it to the beam energy 2.2995 GeV/c^2 and redo the fit to see the influence on the tag yields.



The systematic uncertainty due to this is 0.98% relatively.

Systematic Error

Choice of the sideband region

The choice of sideband region may influence the estimation of the peaking background. We try to estimate the systematic error due to this by varying the sideband region and recalculating the branching fraction.

The uncertainty due to the choice of sideband region is estimated to be 0.10%, which is negligible.



Statistic of the control sample

The limited statistic of the control sample $J/\psi \rightarrow \overline{p}K^+\Lambda$ may bring systematic uncertainty into the reconstruction efficiency of Λ , which can be calculated out from the table of efficiency using the following equation.

$P({ m GeV/c})$	$ \cos\theta $	$N_{\rm S}$	$N_{\rm A}$	$N_{\rm B}$	$N_{\rm C}$	$N_{\rm D}$	$N_{\rm E}$	N_{signal}
	(0.00, 0.20)	12.0 ± 3.5	8.0 ± 2.8	9.0 ± 3.0	0.0 ± 0.0	0.0 ± 0.0	1.0 ± 1.0	3.9 ± 4.0
(0 0 0 2)	(0.20, 0.40)	17.0 ± 4.1	3.0 ± 1.7	7.0 ± 2.6	3.0 ± 1.7	3.0 ± 1.7	0.0 ± 0.0	10.9 ± 4.6
(0.0, 0.3)	(0.40, 0.65)	14.0 ± 3.7	5.0 ± 2.2	7.0 ± 2.6	0.0 ± 0.0	2.0 ± 1.4	0.0 ± 0.0	6.5 ± 4.3
	(0.65, 1.00)	12.0 ± 3.5	6.0 ± 2.4	8.0 ± 2.8	1.0 ± 1.0	1.0 ± 1.0	3.0 ± 1.7	5.7 ± 4.1
	(0.00, 0.20)	77.0 ± 8.8	15.0 ± 3.9	15.0 ± 3.9	4.0 ± 2.0	4.0 ± 2.0	2.0 ± 1.4	61.3 ± 9.4
(0.2.0.5)	(0.20, 0.40)	61.0 ± 7.8	14.0 ± 3.7	21.0 ± 4.6	1.0 ± 1.0	4.0 ± 2.0	6.0 ± 2.4	43.1 ± 8.5
(0.5, 0.5)	(0.40, 0.65)	89.0 ± 9.4	13.0 ± 3.6	22.0 ± 4.7	1.0 ± 1.0	4.0 ± 2.0	1.0 ± 1.0	69.3 ± 10.0
	(0.65, 1.00)	47.0 ± 6.9	18.0 ± 4.2	17.0 ± 4.1	1.0 ± 1.0	4.0 ± 2.0	2.0 ± 1.4	27.6 ± 7.6
	(0.00, 0.20)	97.0 ± 9.8	5.0 ± 2.2	5.0 ± 2.2	0.0 ± 0.0	4.0 ± 2.0	0.0 ± 0.0	89.0 ± 10.1
(05.07)	(0.20, 0.40)	87.0 ± 9.3	8.0 ± 2.8	14.0 ± 3.7	0.0 ± 0.0	3.0 ± 1.7	1.0 ± 1.0	74.2 ± 9.7
(0.5, 0.7)	(0.40, 0.65)	81.0 ± 9.0	3.0 ± 1.7	9.0 ± 3.0	1.0 ± 1.0	8.0 ± 2.8	0.0 ± 0.0	69.5 ± 9.4
	(0.65, 1.00)	65.0 ± 8.1	5.0 ± 2.2	13.0 ± 3.6	1.0 ± 1.0	7.0 ± 2.6	3.0 ± 1.7	52.3 ± 8.6
	(0.00, 0.20)	68.0 ± 8.2	9.0 ± 3.0	21.0 ± 4.6	0.0 ± 0.0	4.0 ± 2.0	1.0 ± 1.0	50.4 ± 8.8
(0.7, 1.0)	(0.20, 0.40)	59.0 ± 7.7	7.0 ± 2.6	12.0 ± 3.5	1.0 ± 1.0	6.0 ± 2.4	0.0 ± 0.0	45.4 ± 8.2
	(0.40, 0.65)	71.0 ± 8.4	7.0 ± 2.6	17.0 ± 4.1	1.0 ± 1.0	2.0 ± 1.4	2.0 ± 1.4	58.6 ± 8.9
	(0.65, 1.00)	57.0 ± 7.5	6.0 ± 2.4	16.0 ± 4.0	0.0 ± 0.0	3.0 ± 1.7	2.0 ± 1.4	44.5 ± 8.0

$$\delta \varepsilon^{\rm sig} = \frac{\sqrt{\sum_{ij} (\delta \varepsilon^{\rm sig}_j \cdot N^{\rm sig}_{ij} / (\varepsilon^{\rm sig}_j)^2)^2}}{\sum_{ij} (N^{\rm sig}_{ij} / \varepsilon^{\rm sig}_j)},$$

$\epsilon_{data}(\%)$	P(GeV/c)					
$ \cos\theta $	(0, 0.3)	(0.3, 0.5)	(0.5, 0.7)	(0.7, 1.0)		
(0.00, 0.20)	8.64 ± 0.23	29.52 ± 0.36	36.12 ± 0.39	40.52 ± 0.57		
(0.20, 0.40)	8.50 ± 0.23	28.77 ± 0.36	35.71 ± 0.39	40.24 ± 0.56		
(0.40, 0.65)	8.14 ± 0.20	26.92 ± 0.31	34.06 ± 0.35	38.05 ± 0.50		
(0.65, 1.00)	4.69 ± 0.13	15.38 ± 0.19	20.90 ± 0.23	25.69 ± 0.36		

The systematic uncertainty due to this is 0.36% relatively.

Size of the bins

To study the systematic error due to binning, we change the number of bins and see how the branching fraction will change with it.

We divide the control sample of $J/\psi \rightarrow \overline{p}K^+\Lambda$ into $3 \times 4, 4 \times 3, 4 \times 5$ and 5×4 $p-|cos\theta|$ bins to obtain the corresponding efficiency, then divide the data sample to get the signal yields.

Bin number of p	Bin number of $ \cos\theta $	$\mathcal{B}(\Lambda_c^+ \to \Lambda + X)(\%)$
3	4	37.34 ± 1.95
4	3	37.24 ± 2.16
4	5	37.02 ± 2.18
5	4	37.05 ± 2.18
A	veraged	37.16 ± 1.06

The systematic uncertainty due to this is 0.49% relatively.

The bias of efficiency in different tag modes

We assume that the reconstruction efficiency of Λ is independent of the tag modes, which may cause systematic error. We use the inclusive Monte Carlo of $\Lambda_c^+\Lambda_c^-$ to obtain the signal efficiency in different tag modes.

Tag modes	$\operatorname{Efficiency}(\%)$
$\bar{\Lambda}_c^- \to \bar{p} K^0_S$	29.9 ± 0.6
$\bar{\Lambda}_c^- \to \overline{p} K^+ \pi^-$	30.3 ± 0.2
Averaged	30.2 ± 0.5

The systematic error due to this is estimated to be 1.10% relatively.

Systematic Error

Summary of the systematic error

Categories	Systematic Uncertainties(%)
Statistics of the control sample	0.36
Tag bias of Λ 's efficiency	1.10
Fitting of the tag yields	0.98
The size of the bins	0.49
Choice of the sideband region	0.1
Total	1.60

Thus the systematic uncertainty is $37.0\% \times 1.6\% = 0.6\%$.

BF with systematic error

$$\mathcal{B}(\Lambda_C^+ \to \Lambda + X) = (37.0 \pm 2.2 \pm 0.6)\%$$

CP violation in Λ_C decay

Definition



The tag yields, signal yields and efficiencies are reobtained separately.

	$\epsilon_{\Lambda}(\%)$				
$ \cos\theta $	P (GeV/c)				
	(0.0, 0.3)	(0.3, 0.5)	(0.5, 0.7)	(0.7, 1.0)	
(0.00, 0.20)	8.35 ± 0.33	30.80 ± 0.54	36.68 ± 0.59	41.00 ± 0.86	
(0.20, 0.40)	8.47 ± 0.32	29.97 ± 0.53	36.56 ± 0.58	40.30 ± 0.85	
(0.40, 0.65)	7.91 ± 0.28	27.44 ± 0.45	35.10 ± 0.52	38.00 ± 0.73	
(0.65, 1.00)	4.04 ± 0.17	15.97 ± 0.29	21.17 ± 0.33	25.87 ± 0.51	
		Λ	VΛ		
$ \cos\theta $		<i>P</i> (G	eV/c)		
	(0.0, 0.3)	(0.3, 0.5)	(0.5, 0.7)	(0.7, 1.0)	
(0.00, 0.20)	2.5 ± 2.5	27.9 ± 6.5	47.5 ± 7.3	25.0 ± 6.2	
(0.20, 0.40)	4.6 ± 3.2	20.5 ± 5.6	36.5 ± 6.5	22.0 ± 5.8	
(0.40, 0.65)	5.8 ± 3.1	44.6 ± 7.4	25.6 ± 6.3	32.6 ± 6.3	
(0.65, 1.00)	7.2 ± 3.2	10.0 ± 4.8	28.4 ± 6.3	20.5 ± 5.8	

	$\epsilon_{\bar{\Lambda}}(\%)$				
$ \cos\theta $	$P ({ m GeV/c})$				
	(0.0, 0.3)	(0.3, 0.5)	(0.5, 0.7)	(0.7, 1.0)	
(0.00, 0.20)	8.91 ± 0.33	28.38 ± 0.48	35.64 ± 0.53	40.14 ± 0.76	
(0.20, 0.40)	8.53 ± 0.31	27.71 ± 0.48	34.98 ± 0.53	40.20 ± 0.75	
(0.40, 0.65)	8.35 ± 0.28	26.45 ± 0.42	33.18 ± 0.46	38.08 ± 0.68	
(0.65, 1.00)	5.27 ± 0.19	14.84 ± 0.26	20.67 ± 0.31	25.52 ± 0.50	
	$N_{\bar{\Lambda}}$				
$ \cos\theta $	P (GeV/c)				
	(0.0, 0.3)	(0.3, 0.5)	(0.5, 0.7)	(0.7, 1.0)	
(0.00, 0.20)	1.4 ± 3.2	33.4 ± 6.7	41.5 ± 7.0	25.4 ± 6.2	
(0.20, 0.40)	6.3 ± 3.4	22.6 ± 6.5	37.6 ± 7.2	23.4 ± 5.8	
(0.40, 0.65)	0.8 ± 3.0	24.6 ± 6.7	43.9 ± 7.0	26.0 ± 6.2	
(0.65, 1.00)	-1.5 ± 2.5	17.6 ± 6.0	23.9 ± 5.9	24.0 ± 5.6	

Tag mode	Tag yield
$\Lambda_c^+ \to p K_S^0$	606 ± 26
$\Lambda_c^+ \to p K^- \pi^+$	2915 ± 60
$\bar{\Lambda}_c^- \to \bar{p} K_S^0$	614 ± 26
$\bar{\Lambda}_c^- \to \bar{p} K^+ \pi^-$	3172 ± 59

Result

Decay mode	Branching fraction(%)	$\mathcal{A}_{ ext{CP}}$	
$\Lambda_c^+ \to \Lambda + X$	$38.02 \pm 3.24 \pm 0.61$	$0.02 \pm 0.06 \pm 0.01$	
$\bar{\Lambda}_c^- \to \bar{\Lambda} + X$	$36.70 \pm 3.04 \pm 0.59$		

OutlineIntroductionAnalysisSystematic ErrorSummaryBackupSummary

- Using double tag method and the technique of data driven, we have measured the branching fraction of $\Lambda_c^+ \rightarrow \Lambda + X$ to be $(37.0 \pm 2.2 \pm 0.6)\%$, which is more precise than the latest PDG value, which is $(35 \pm 11)\%$.
- We also study the CP violation in the decay $\Lambda_C^+ \rightarrow \Lambda + X$, the CP violation parameter \mathcal{A}_{CP} is measured to be $0.02 \pm 0.06 \pm 0.01$.
- The reconstruction efficiency of Λ has been studied detailedly. The table for the systematic error of Λ 's reconstruction efficiency is available.

Thanks for your attention !

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Backup: Λ 's efficiency in different MC samples









Backup: Efficiency of Λ with different data for realization

