

第二届中国LHC物理研讨会/北京大学

Higgs-messenger coupling extended Gauge mediated SUSY-breaking

based on arXiv:1610.06024 by ZF Kang &
Phys. Rev. D 86, 095020 (2012) by ZF Kang, T. Li, T.
Liu, C. Tong and J. M. Yang.

Zhaofeng Kang(康昭峰), KIAS(韩国高等研究院), 10/25/2016

Outline

- ✦ GMSB: the good & the bad
- ✦ GMSB with H_u -messenger couplings
- ✦ GMSB with $H_{u,d}$ -messenger couplings
- ✦ Conclusions

GMSB: gauge mediated SUSY-breaking

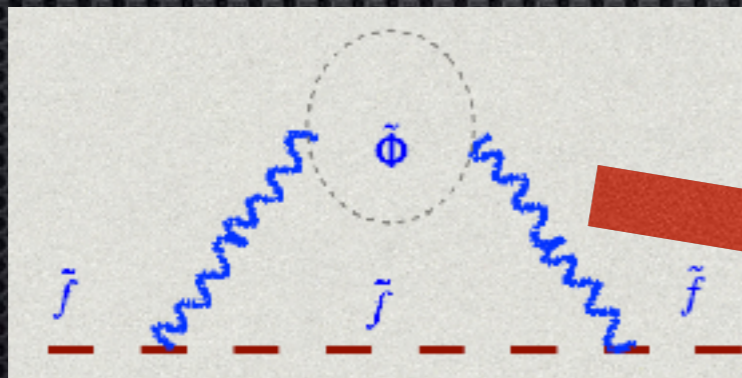
GMSB utilizes flavor universal of gauge interactions

- The best idea to overcome the flavor problem

hidden sector breaking SUSY, described by the spurion $X=M+F\theta^2$

messenger sector $X\Phi\bar{\Phi}$

A soft SUSY breaking sector in the MSSM automatically respects MFV



$$M_a = \frac{\alpha_a}{4\pi} \Lambda, \quad (a = 1, 2, 3), \quad \Lambda = \frac{F}{M}$$

$$m_{\phi_i}^2 = 2\Lambda^2 \left[\left(\frac{\alpha_3}{4\pi} \right)^2 C_3(i) + \left(\frac{\alpha_2}{4\pi} \right)^2 C_2(i) + \left(\frac{\alpha_1}{4\pi} \right)^2 C_1(i) \right]$$

$$0\tilde{Q}H_u\tilde{U}^c + 0\tilde{Q}H_d\tilde{D}^c + 0\tilde{L}H_d\tilde{E}^c$$

GMSB: gauge mediated SUSY-breaking

Post h(125), awkward....

From P. Athron, J. h. Park, T. Steudtner, D. Stckinger and A. Voigt, 1609.00371

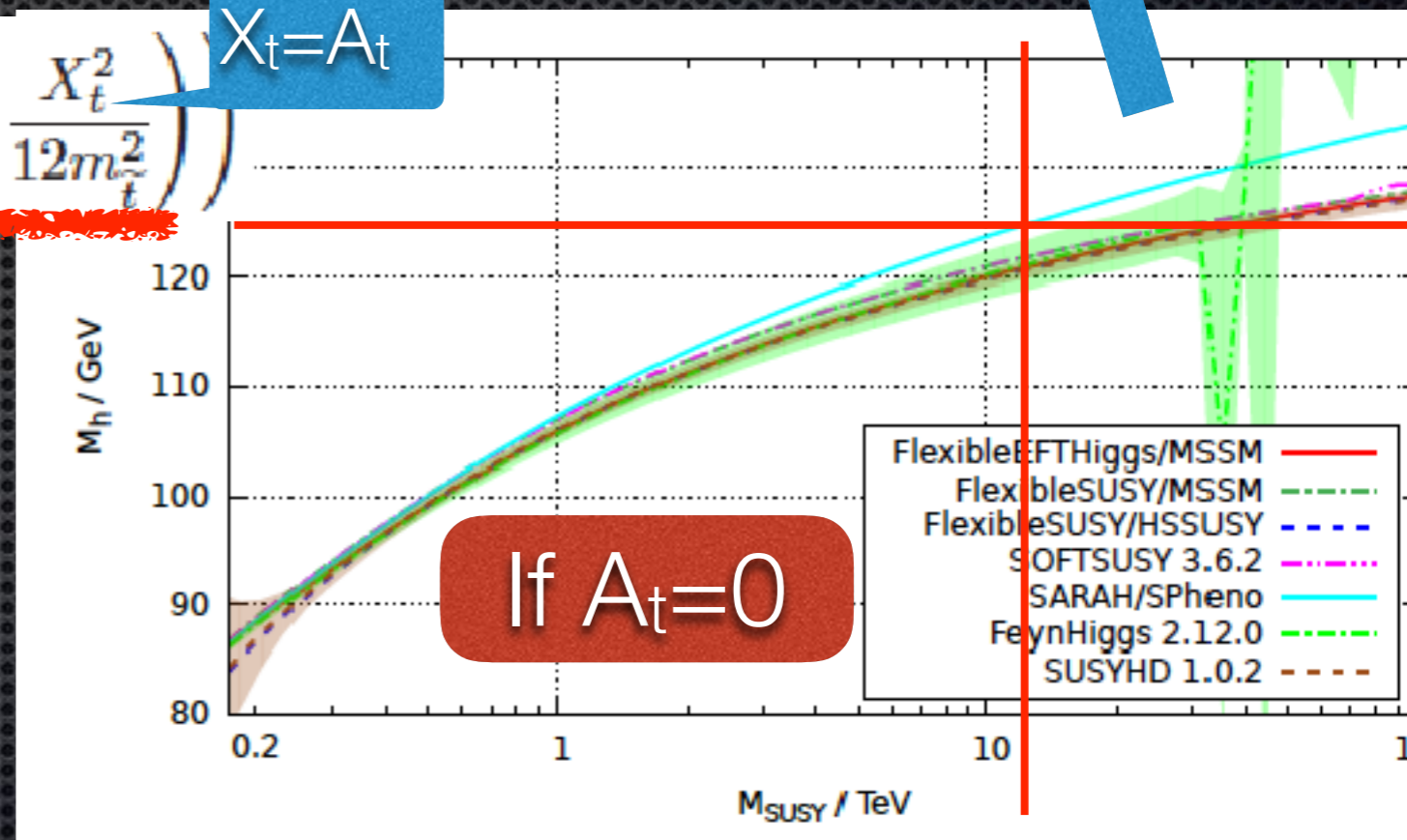
- VERY serious fine-tuning (at least in the MSSM)!

$$\delta_t^2 \simeq \frac{3m_t^4}{4\pi^2 v^2} \left(\log \left(\frac{m_{\tilde{t}}^2}{m_t^2} \right) + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right)$$

$X_t = A_t$

$$\Delta m_{H_u}^2 \sim -\frac{3y_t^2}{4\pi^2} m_{\tilde{t}}^2 \log \frac{\Lambda_{UV}}{m_{\tilde{t}}}$$

$$\frac{m_Z^2}{2} \simeq \frac{m_{H_u}^2 - \tan^2 \beta m_{H_d}^2}{\tan^2 \beta - 1} - \mu^2$$



- Fail in explaining $(g-2)_\mu$, because sleptons are very heavy!

GMSB: gauge mediated SUSY-breaking

Post h(125), awkward....

NOT mentioning to the long-standing $\mu/B\mu$ problem, that will be presented latter

HGMSB: GMSB with H_u -messenger couplings

Want a large A_t ? Coupling H_u to messengers: $\lambda_u H_u \mathcal{O}_u$

- choosing messenger $10=(Q_\Phi, U_\Phi, E_\Phi)$ of $SU(5)$ with couplings

$$W_{10} = \lambda_u Q_\Phi H_u U_\Phi + \cancel{\lambda_u Q_\Phi H_u U_\Phi} + \lambda_u H_u \mathcal{O}_u + X (\lambda_Q Q_\Phi \bar{Q}_\Phi + \lambda_U \bar{U}_\Phi U_\Phi) + W_{\text{MSSM}},$$

N_f sets of messengers

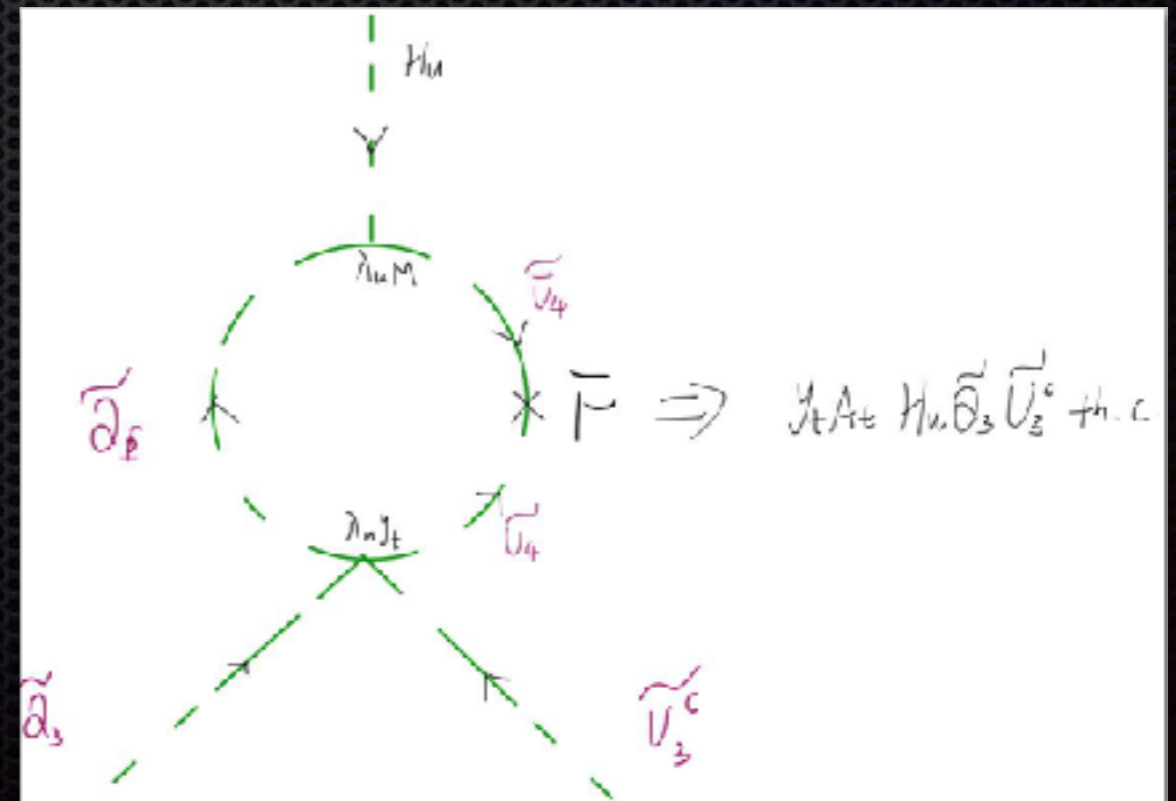
Z. Kang, T. Li, T. Liu, C. Tong and J. M. Yang, Phys.Rev. D 86, 095020 (2012).

Rev. D 86, 095020 (2012)

- Feynmann digram demonstration of one-loop A_t

$$A_t = -N_m \alpha_u \Lambda, \quad N_m \equiv 3N_f$$

$$\Lambda \equiv F/(4\pi M) \sim \mathcal{O}(10\text{TeV})$$



HGMSB: GMSB with H_u -messenger couplings

Higgs-messenger **VS** matter-messenger coupling

J. L. Evans, M. Ibe, S. Shirai and T. T. Yanagida, Phys. Rev. D 85, 095004 (2012);
A. Basirnia, D. Egana-Ugrinovic, S. Knapen and D. Shih, JHEP 1506, 144 (2015)...

Although A_t also arises if the matters Q_3 / U_3 couple to messengers, HGMSB **naturally maintains MFV**, the most important feature of GMSB.

Moreover, HGMSB has the potential to be embedded in the framework which dynamically generates the μ term by coupling Higgs to the messengers, though the $\mu/B\mu$ problem

HGMSB: GMSB with $H_{u,d}$ -messenger couplings

A_t/m_{H_u} problem: Not only a large A_u but **also large m_{H_u}**

- Soft parameters of Higgs and any MSSM fields coupling to Higgs acquire Yukawa-mediated SUSY-breaking effects

- Systematic calculation: wave function renormalization method

G. F. Giudice and R. Rattazzi,
Nucl. Phys. B 511 (1998)

$$\begin{aligned}\Delta m_{\tilde{Q}_3}^2 &= -\frac{N_m}{3} (3\alpha_t\alpha_u + 3\alpha_b\alpha_d + \alpha_b\alpha'_d) \Lambda^2, \\ \Delta m_{\tilde{U}_3}^2 &= -2N_m\alpha_t\alpha_u\Lambda^2, \\ \Delta m_{\tilde{D}_3}^2 &= -2\frac{N_m}{3}\alpha_b(3\alpha_d + \alpha'_d)\Lambda^2.\end{aligned}$$

- In particular, H_u receives a large & positive contribution

$$\Delta m_{H_u}^2 = N_m\alpha_u \left[(N_m + 3)\alpha_u - \frac{16}{3}\alpha_3 - 3\alpha_2 - \frac{13}{15}\alpha_1 \right] \Lambda^2$$

- radiative EWSB probably fails
- originally, cancelation between Yukawa and QCD gauge parts is the reason for introducing messenger 10

HGMSB: GMSB with $H_{u,d}$ -messenger couplings

What if includes $\lambda_d H_d \mathcal{O}_d$?

- The model with $H_{u,d}$ -messenger couplings:

$$W_{10} = \lambda_u Q_\Phi H_u U_\Phi + \lambda_d \bar{Q}_\Phi H_d \bar{U}_\Phi + \lambda_d \bar{Q}_\Phi H_d \bar{U}_\Phi + \lambda_d \bar{Q}_\Phi H_d \bar{U}_\Phi + X (\lambda_Q Q_\Phi \bar{Q}_\Phi + \lambda_U \bar{U}_\Phi U_\Phi) + W_{\text{MSSM}},$$

turned off before to avoid $\mu/B\mu$ problem

- Dynamically generate $\mu H_u H_d$ & $B\mu H_u H_d$ at one loop with

$$\begin{aligned} \mu &= f(\lambda_Q/\lambda_U) N_m \sqrt{\alpha_u \alpha_d} \Lambda, \\ B\mu &= f(\lambda_Q/\lambda_U) N_m 4\pi \times \sqrt{\alpha_u \alpha_d} \Lambda^2, \end{aligned}$$

$$\sin 2\beta = \frac{2B\mu}{m_{H_u}^2 + m_{H_d}^2 + 2\mu^2}$$

Great! It explains the the origin of μ , the unique massive coupling in MSSM superpotential

But $B\mu$ has dimension 2! TOO BIG TO FILL the EWSB equation — — the $\mu/B\mu$ problem

HGMSB: GMSB with $H_{u,d}$ -messenger couplings

Nonradiative EWSB as a common solution

- In the A_t/m_{H_u} problem we encounter a too large $m_{H_u} > 0$, which hampers the conventional radiative EWSB

$$\frac{m_Z^2}{2} = -\mu^2 + \frac{m_{H_d}^2 - \tan^2 \beta m_{H_u}^2}{\tan^2 \beta - 1} \quad \longrightarrow \quad -\mu^2 - m_{H_u}^2 \approx m_Z^2/2,$$

- Similarly, in the μ/B_μ problem above we encounter a too large B_μ and thus EWSB fails:

$$\sin 2\beta = \frac{2B_\mu}{m_{H_u}^2 + m_{H_d}^2 + 2\mu^2}$$

C. Csaki, A. Falkowski, Y. Nomura and T. Volansky, Phys. Rev. Lett. 102 (2009) 111801.

Phys. Rev. Lett. 102 (2009) 111801.

However, what if $m_{H_d}^2$ is NOT negligible ? !!

Both equations can be satisfied by this large & positive $m_{H_d}^2$

HGMSB: GMSB with $H_{u,d}$ -messenger couplings

Generate a huge $m_{H_d}^2$!!

- Include the “full” $H_{u,d}$ -messenger couplings:

$$W_{10} = \lambda_u Q_\Phi H_u U_\Phi + \lambda_d \bar{Q}_\Phi H_d \bar{U}_\Phi + \frac{\lambda'_d}{2} E_\Phi H_d H_d + X (\lambda_Q Q_\Phi \bar{Q}_\Phi + \lambda_U \bar{U}_\Phi U_\Phi) + W_{\text{MSSM}},$$

messenger 10 admits such a term

$$\Delta m_{H_d}^2 \approx \frac{N_m}{3} \alpha'_d (N_m \alpha'_d + 2N_m \alpha_d + 3\alpha_b - 3\alpha_2) \Lambda^2$$

$$\lambda'_d \simeq 1.7 \left(\frac{\xi_S}{0.85} \frac{\tan \beta}{5} \frac{81}{N_m^2} \right)^{\frac{1}{4}} \left(\frac{\mu}{0.2 \text{ TeV}} \frac{10 \text{ TeV}}{\Lambda} \right)^{\frac{1}{4}}$$

HGMSB: GMSB with $H_{u,d}$ -messenger couplings

Features of nonradiative EWSB

- ✦ A large $m_{H_d} \sim 10$ TeV thus heavy $H/A/H_{\pm}$

$$m_{H_d}^2 \simeq 2B_{\mu} / \sin 2\beta \approx \tan \beta B_{\mu}$$

H/A/H $_{\pm}$ at LHC

- ✦ $\tan \beta$ is favored to be not very large, thus alleviating the need for a superhuge $m_{H_d}^2$

$$m_{H_d}^2 / \tan^2 \beta - m_{H_u}^2 \sim \mu^2$$

- ✦ A small μ is strongly favored, but:

1. a small μ term does not guarantee naturalness
2. cancelation is hidden between $m_{H_u}^2 > 0$ and $m_{H_d}^2$

HGMSB: GMSB with $H_{u,d}$ -messenger couplings

Bonus: filling the $(g-2)_\mu$ discrepancy by light stau

- Nonradiative EWSB with a huge $m_{H_d}^2$ leads to

$$S = \text{Tr}(Y_f \hat{m}_f^2) \sim m_{H_d}^2 / 2 > 0 \Rightarrow \frac{dm_{\tilde{L}}^2}{dt} = -\frac{1}{16\pi^2} \frac{3}{5} g_1^2 S + \dots$$

Sparticles with negative hyper charge such as left-handed sleptons will be decreased significantly

SO

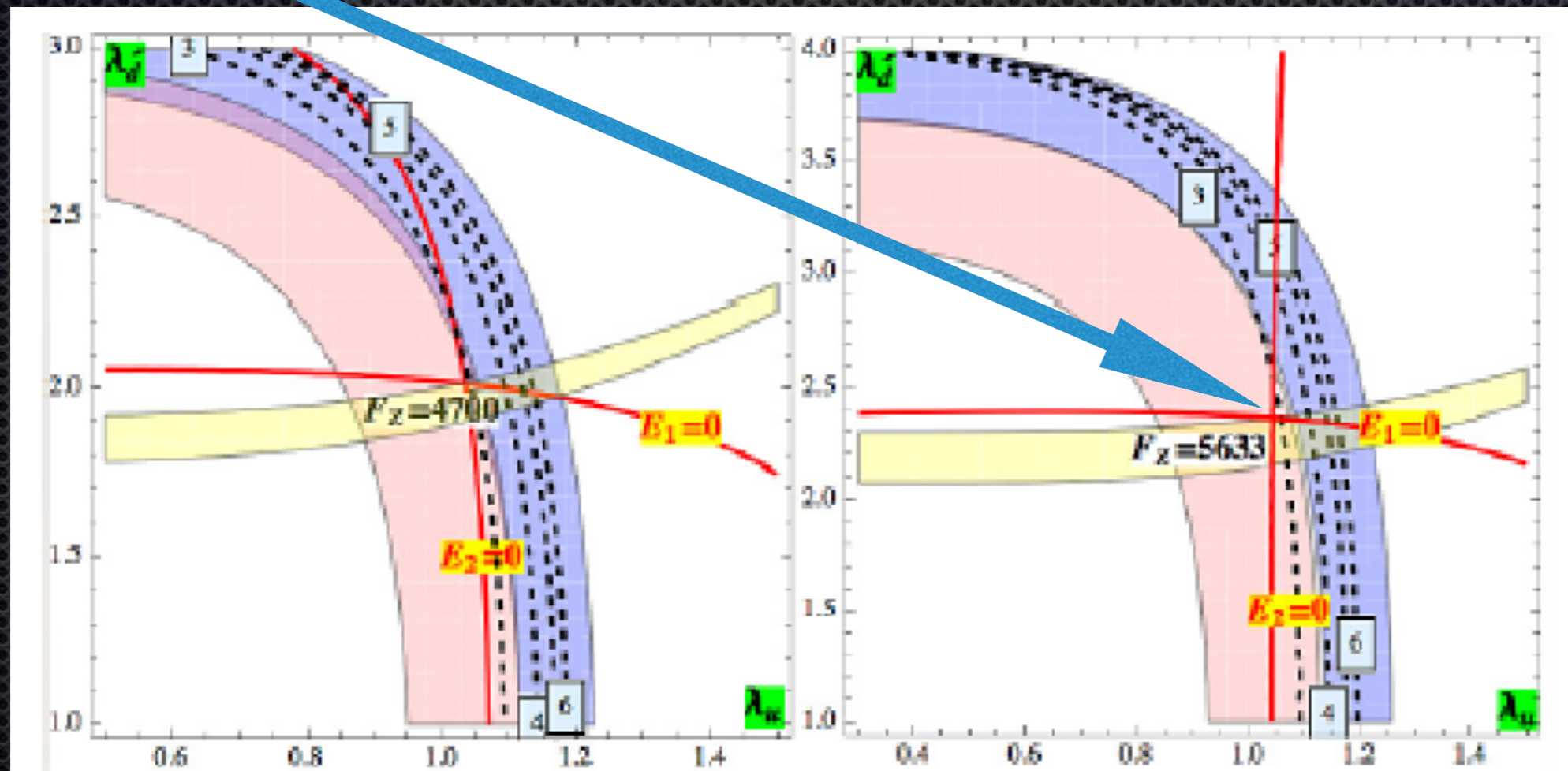
$\tilde{\nu}_\tau$ tends
to the NLSP

$$\delta a_\mu \approx \frac{\alpha_2}{2\pi} \frac{m_\mu^2 M_{\lambda_2} \mu \tan \beta}{m_{\tilde{\nu}_\mu}^4} F_a \left(\frac{M_{\lambda_2}^2}{m_{\tilde{\nu}_\mu}^2}, \frac{\mu^2}{m_{\tilde{\nu}_\mu}^2} \right)$$

HGMSB: GMSB with $H_{u,d}$ -messenger couplings

Two benchmarks with $M=10^{12}$ GeV and 10^7 GeV

- The cross points of two red lines are the solutions to EWSB



and $m_{\tilde{\nu}_\tau} = 90.7(82.8)$ GeV, $m_{\tilde{\tau}} = 120.9(114.9)$ GeV, $m_{\chi_1} = 105.0(100.7)$ GeV and $m_{\chi_2} = 113.0(109.1)$ GeV.

$\delta a_\mu = 1.4 \times 10^{-9} (1.3 \times 10^{-9})$

HGMSB: GMSB with $H_{u,d}$ -messenger couplings

A light Higgsino & slepton world for $(g-2)_\mu$

Light but quite degenerate Higgsinos currently are hidden at LHC (missing energy+soft leptons/jets), even forever?

C. Han, D. Kim, S. Munir and M. Park, *JHEP* 1504,132 (2015).

Light sleptons are even less hopeful. But in one scenario where the sneutrino is not far above $m_Z/2$, the relatively hard leptons says from charginos still can be hunted, e.g.,

$$pp \rightarrow \chi^\mp \chi^\pm \rightarrow \tau^+ \tau^- + \text{MET}(= \tilde{\nu}_\tau \tilde{\nu}_\tau^*).$$

Conclusions

GMSB offer the best idea to organize soft SUSY, but it suffers the $\mu/B\mu$ problem, and serious fine-tuning problem post $h(125)$

HGMSB including both H_u & H_d coupling to messengers can address these problems, via nonradiative EWSB; as a bonus, the $(g-2)_\mu$ puzzle can be addressed, too.

The light Higgsino & slepton world satisfying $(g-2)_\mu$ can be tested in certain scenarios

*Thank you
for your attention!*