

Resistive wall impedance and wake

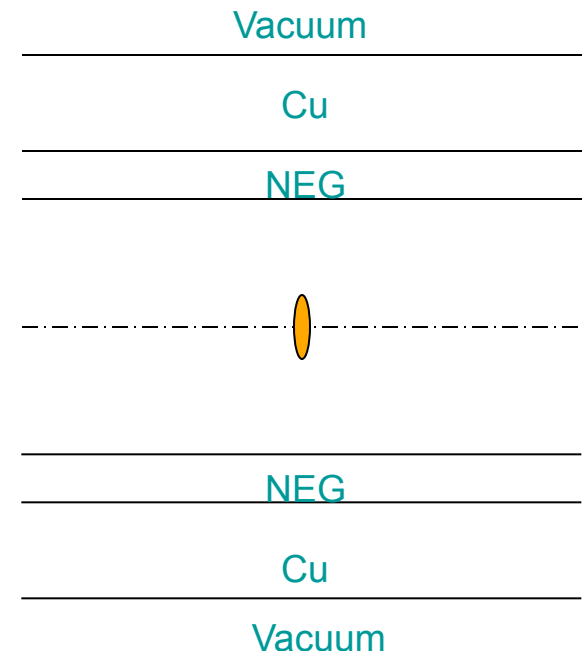
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WANG Na

Contents

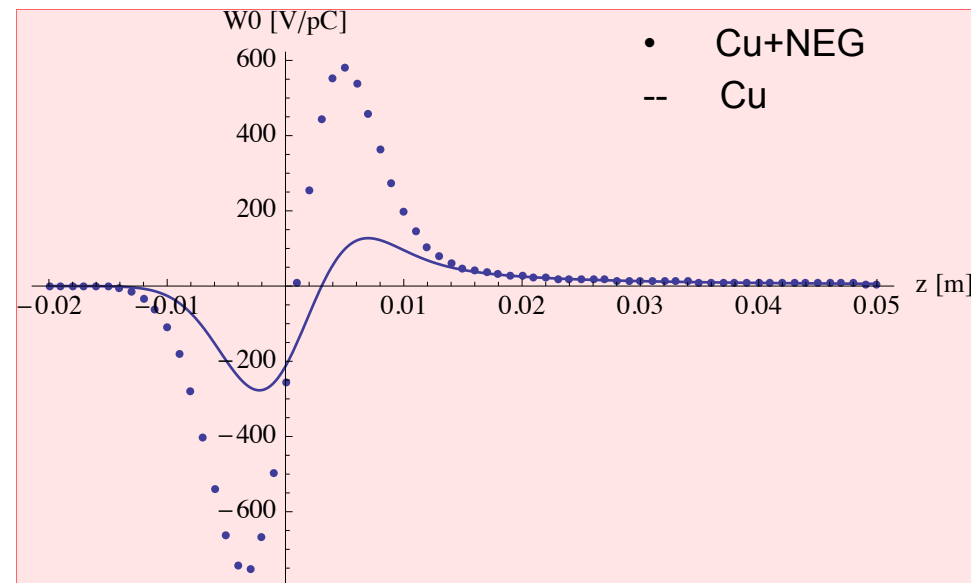
- Longitudinal impedance and wake contribution from NEG coating.
- Transverse wake potential of a Gaussian bunch.
- Transverse impedance and wake contribution from NEG coating.

Layers	Thickness, mm	Conductivity, S/m	ϵ_r	μ_r
Cu	1	5.9×10^7	1	1
NEG	0.001	1.0×10^6	1	1
Vacuum	∞	0	1	1



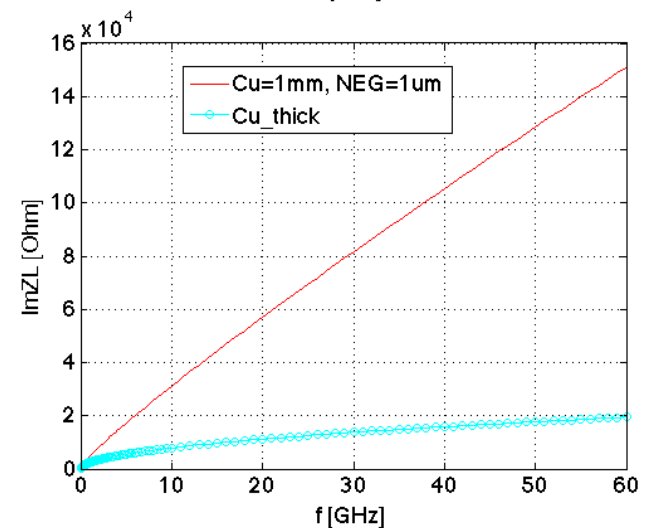
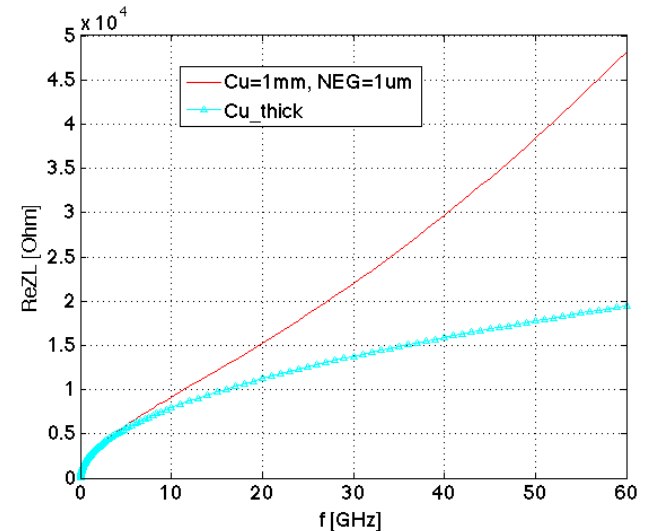
Longitudinal impedance and wake contribution from NEG coating

- Longitudinal wake



$\sigma_z = 4\text{mm}$

- Longitudinal impedance



Compute transverse bunch wake from impedance

$$W_{\perp} = \frac{-i}{2\pi} \int_{-\infty}^{\infty} d\omega e^{i\omega z/c} Z_{\perp}(\omega)$$

$$W_{\perp\lambda}(\tau) = \int_{-\infty}^{\infty} dt \lambda(\tau - t) W_{\perp}(t)$$



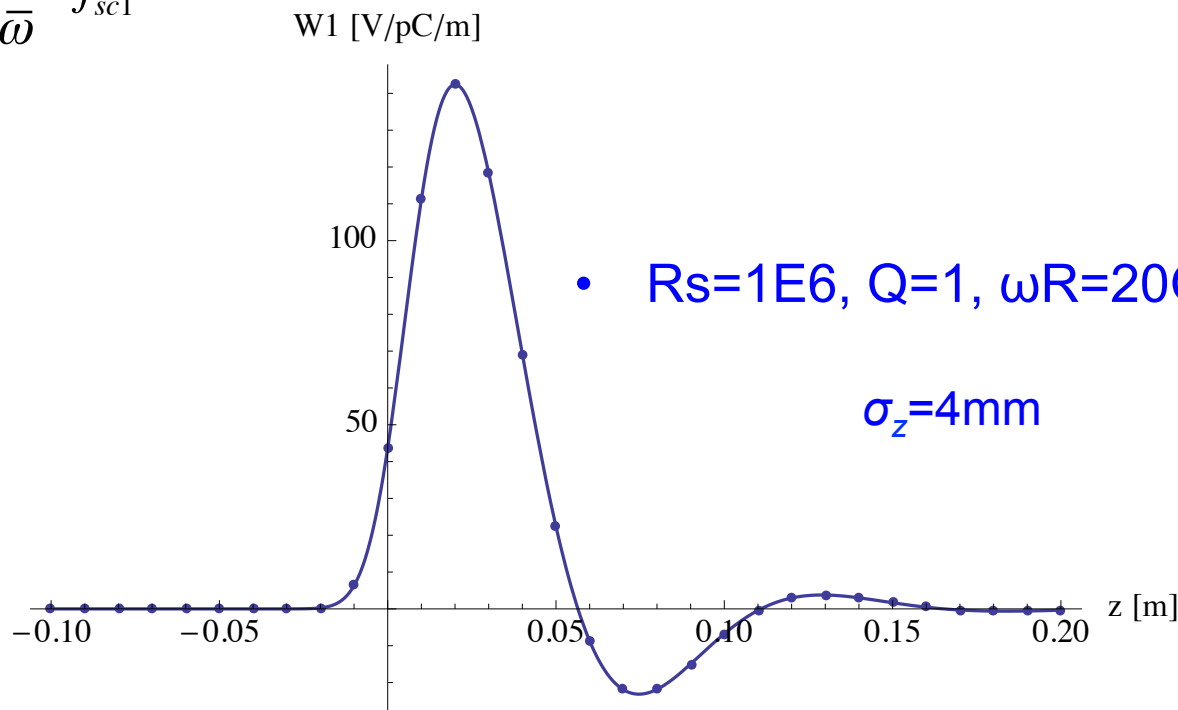
$$W_{\perp\lambda}(\tau) = \int_{-\infty}^{\infty} dt \lambda(\tau - t) \frac{-i}{2\pi} \int_{-\infty}^{\infty} d\omega e^{i\omega t} Z_{\perp}(\omega)$$

Cross check with High Order modes

$$Z_{\perp} = \frac{c}{\omega} \frac{R_s}{1 + iQ \left(\frac{\omega_R}{\omega} - \frac{\omega}{\omega_R} \right)}$$

$$f_{sc1} = \frac{1}{2} e^{-\frac{\sigma_z^2}{2}(k_r^2 - \alpha_r^2) - \alpha_r \sigma_z x} \text{Im}(e^{ik_r \sigma_z (x - \alpha_r \sigma_z)} (1 + \text{Erf}(\frac{(ik_r - \alpha_r)\sigma_z + x}{\sqrt{2}})))|_{x=s/\sigma_z}$$

$$W_{\perp}(z) = \frac{cR_s\omega_R}{Q\bar{\omega}} f_{sc1}$$

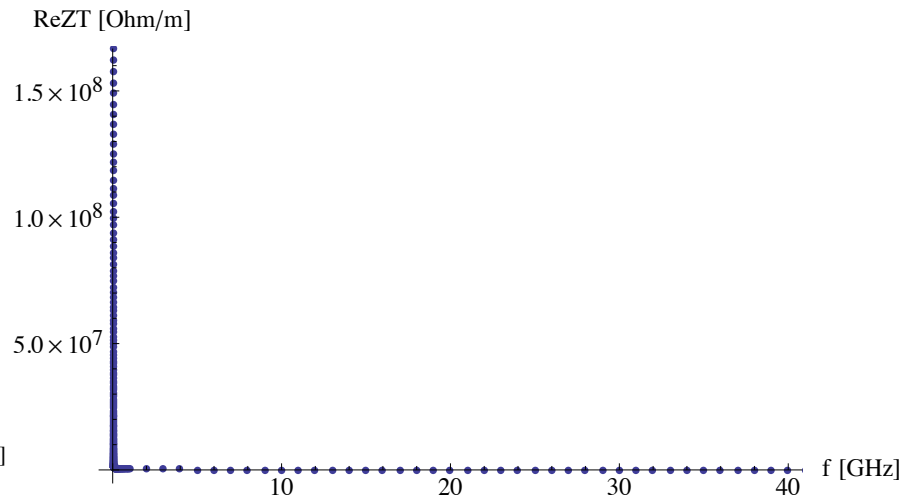
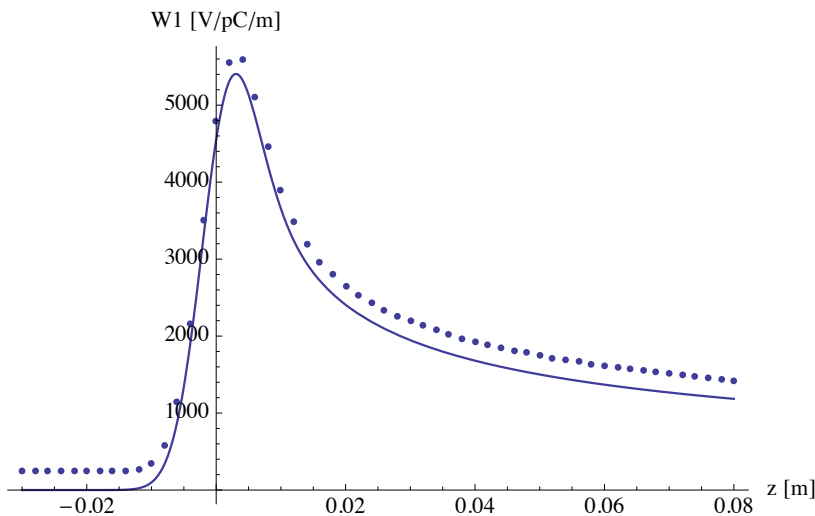


Cross check with Single layer thick wall

$$Z_{\perp} = \frac{c_0}{\omega} \frac{L}{\pi b_0^3} \sqrt{\frac{Z_0}{2\sigma_c c_0}} (1 + \text{sign}(\omega)i) \sqrt{|\omega|}$$

$$W_{\perp} = \frac{c_0 L}{2\sqrt{2}\pi b_0^3} \frac{1}{\sigma_z^{0.5}} \sqrt{\frac{Z_0}{\sigma_c}} f_{sc}$$

$$f_{sc} = \sqrt{|x|} e^{-y} (I_{-1/4}(y) \pm I_{1/4}(y)) \Big|_{y=(s/\sigma_z)^2/4, x=s/\sigma_z}$$



Transverse wake ($\sigma_z=4\text{mm}$)

Solid line: wake potential formula

Dots: transformation from impedance spectrum ($df=0.5\text{MHz}$)

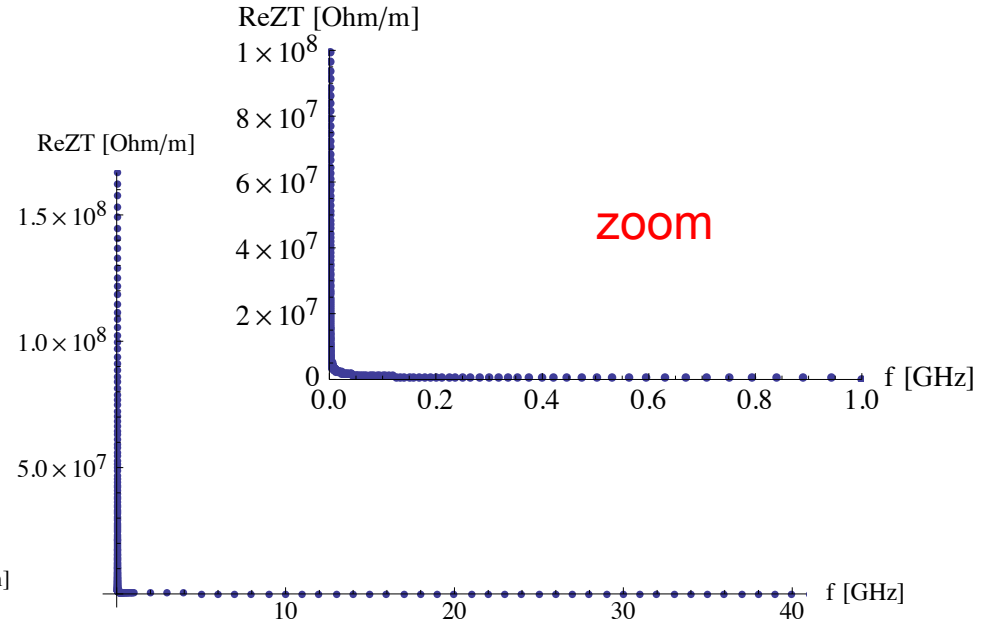
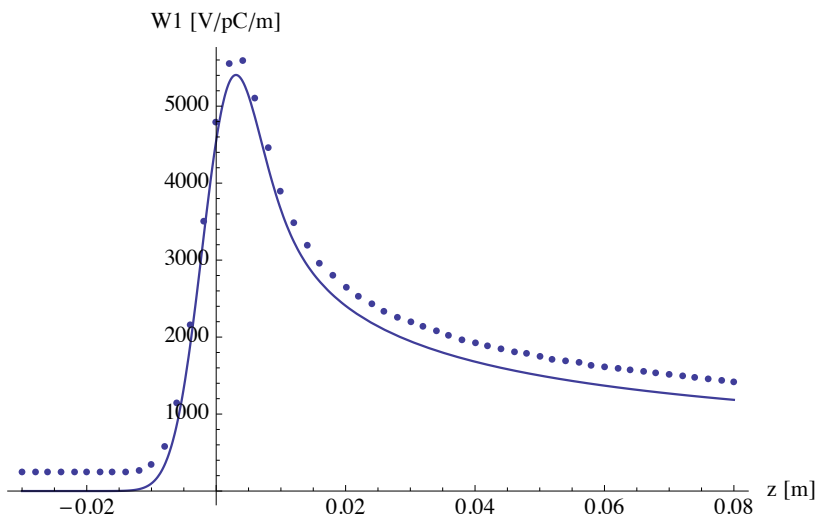
Beam spectrum goes to 40GHz

Cross check with Single layer thick wall

$$Z_{\perp} = \frac{c_0}{\omega} \frac{L}{\pi b_0^3} \sqrt{\frac{Z_0}{2\sigma_c c_0}} (1 + \text{sign}(\omega)i) \sqrt{|\omega|}$$

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Transverse wake ($\sigma_z=4\text{mm}$)

Solid line: wake potential formula

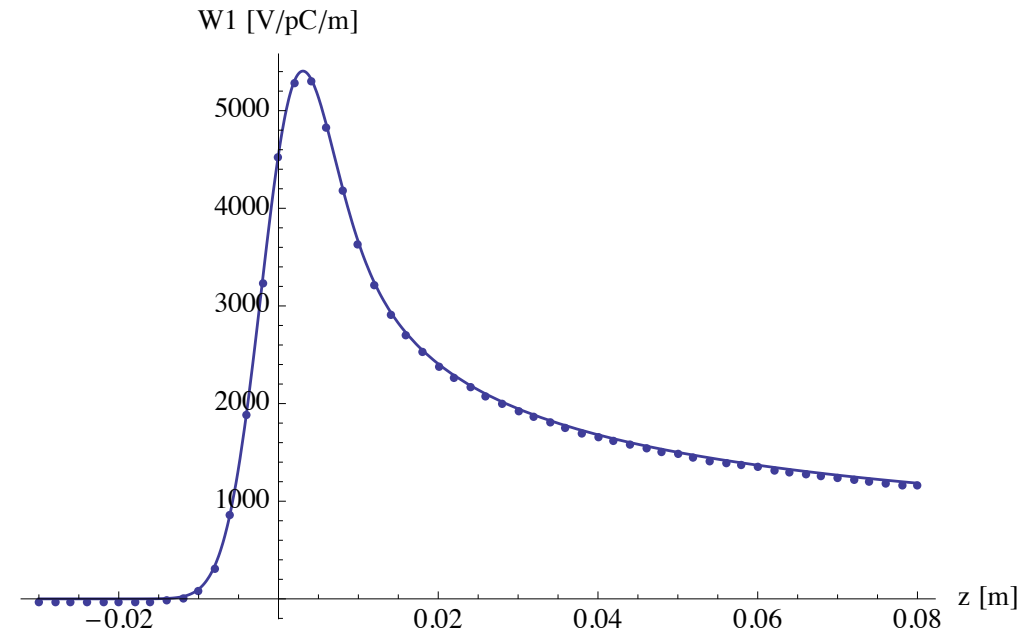
Dots: transformation from impedance spectrum ($df=0.5\text{MHz}$)

Beam spectrum goes to 40GHz

Redefinition of df

100Hz~10MHz: log increase
100 points per magnitude

10MHz~40GHz: linear increase
(df=10MHz)



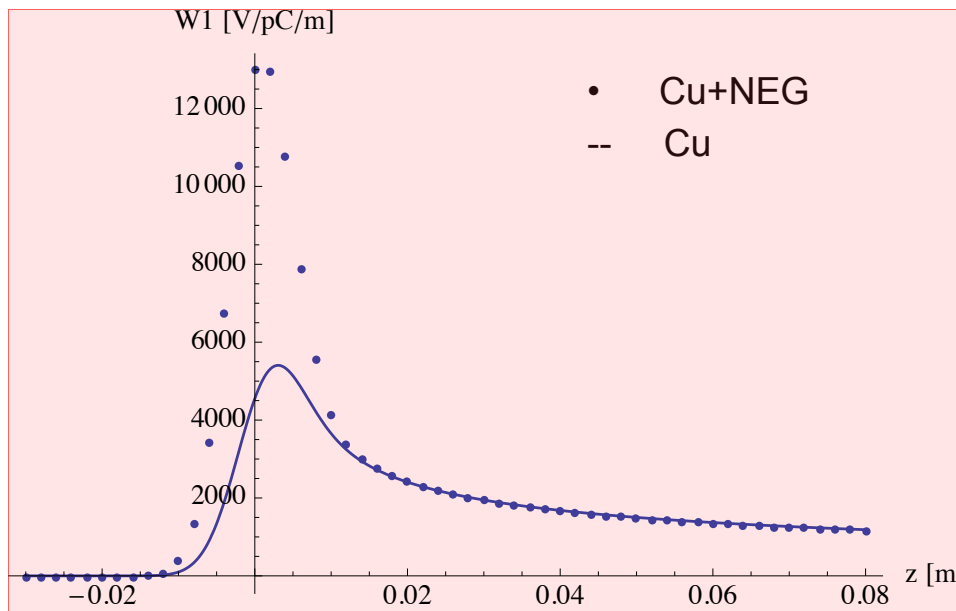
Transverse wake ($\sigma_z=4\text{mm}$)

Solid line: wake potential formula

Dots: transformation from impedance spectrum

Transverse impedance and wake contribution from NEG coating

- Transverse wake



$\sigma_z = 4\text{mm}$

- Transverse impedance

