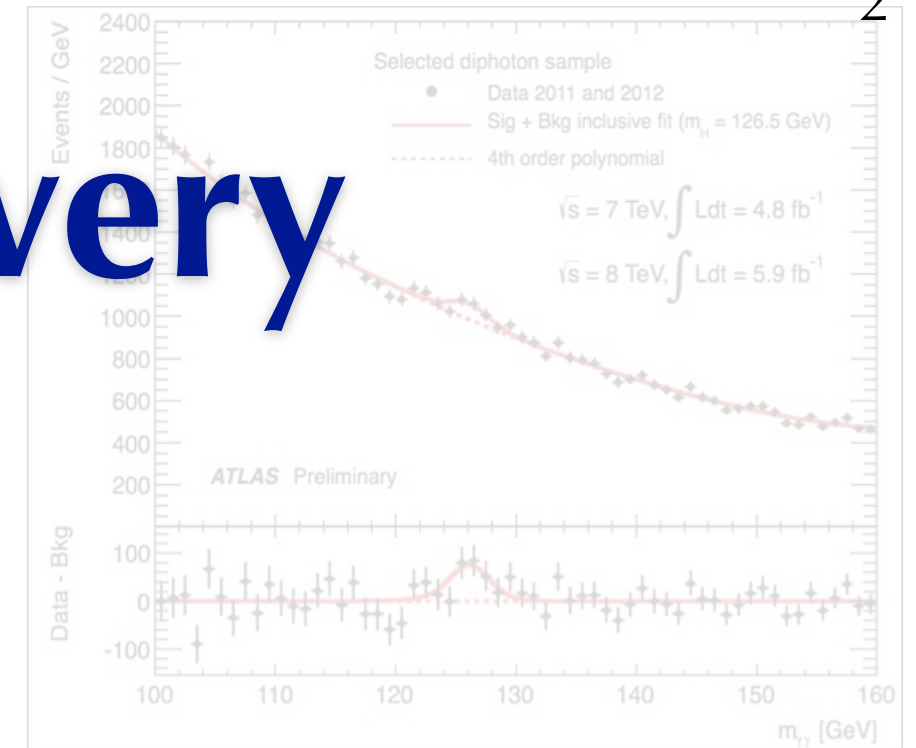
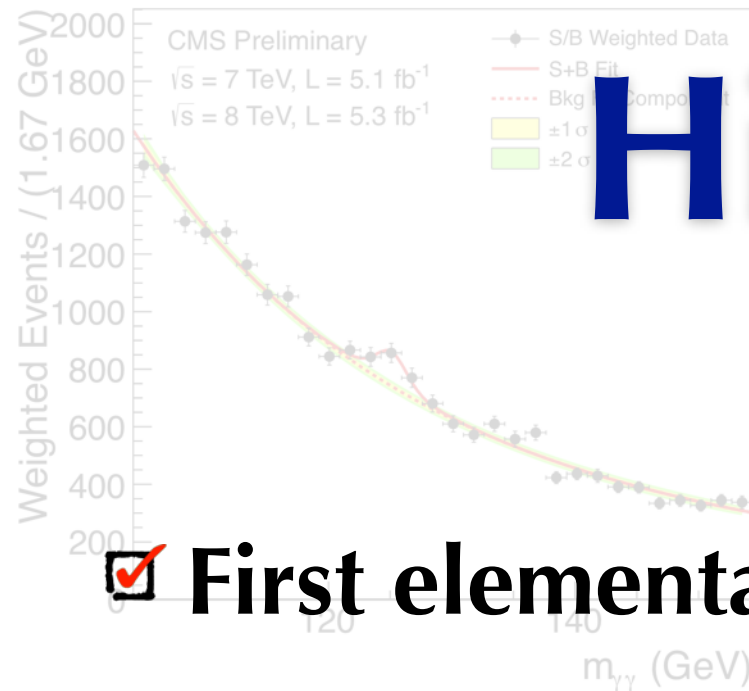


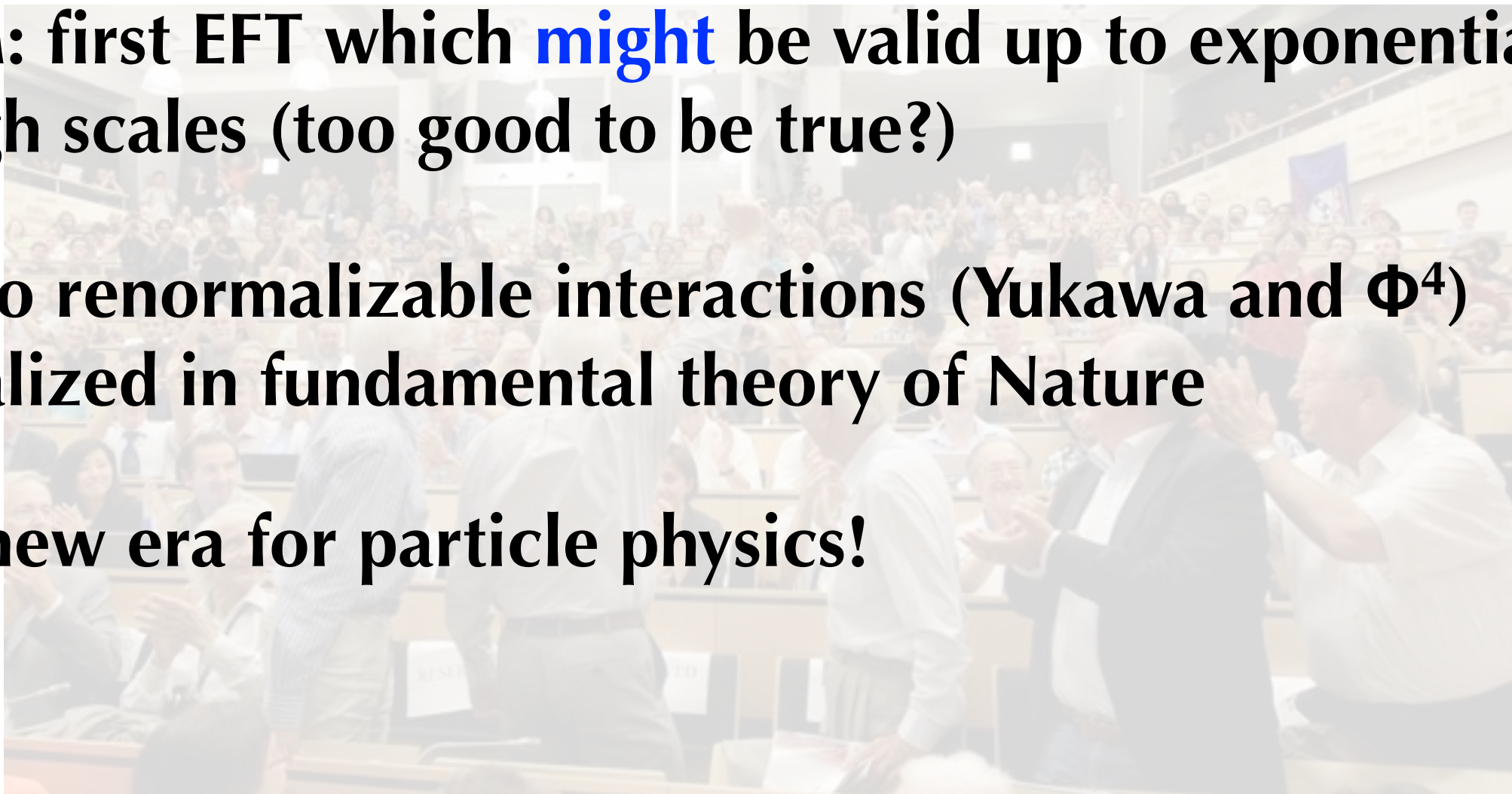
Precision Higgs Production

Li Lin Yang
Peking University

Higgs discovery



- ☑ First elementary(?) spin-0 particle
- ☑ SM: first EFT which **might** be valid up to exponentially high scales (too good to be true?)
- ☑ Two renormalizable interactions (Yukawa and Φ^4) realized in fundamental theory of Nature
- ☑ A new era for particle physics!



Open questions

* Is it (NOT) the SM Higgs?

Priority!

* Is it elementary or composite?

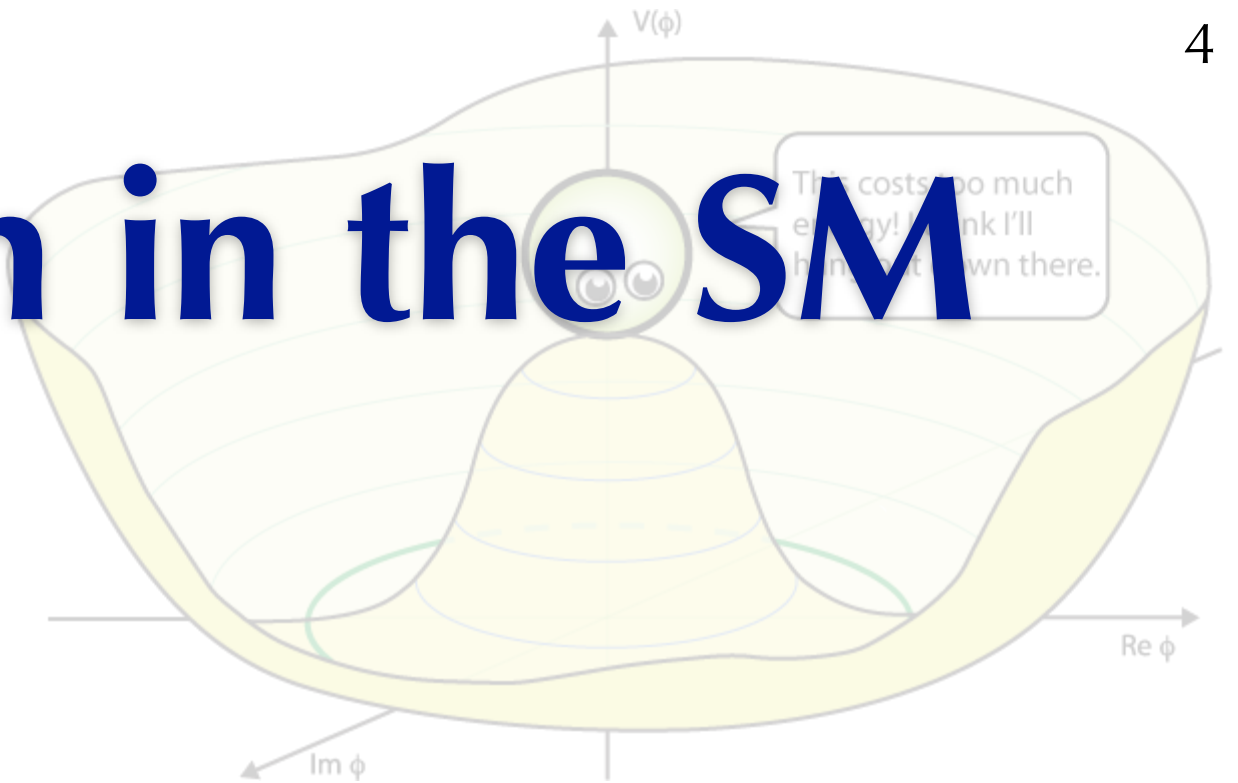
* Are there more than one Higgs bosons?

* Phase transition? Vacuum stability? Naturalness?

* Relations to inflation / dark matter / matter-antimatter asymmetry / neutrino masses / ... ?

 **Precision measurements of Higgs properties!**

Higgs boson in the SM



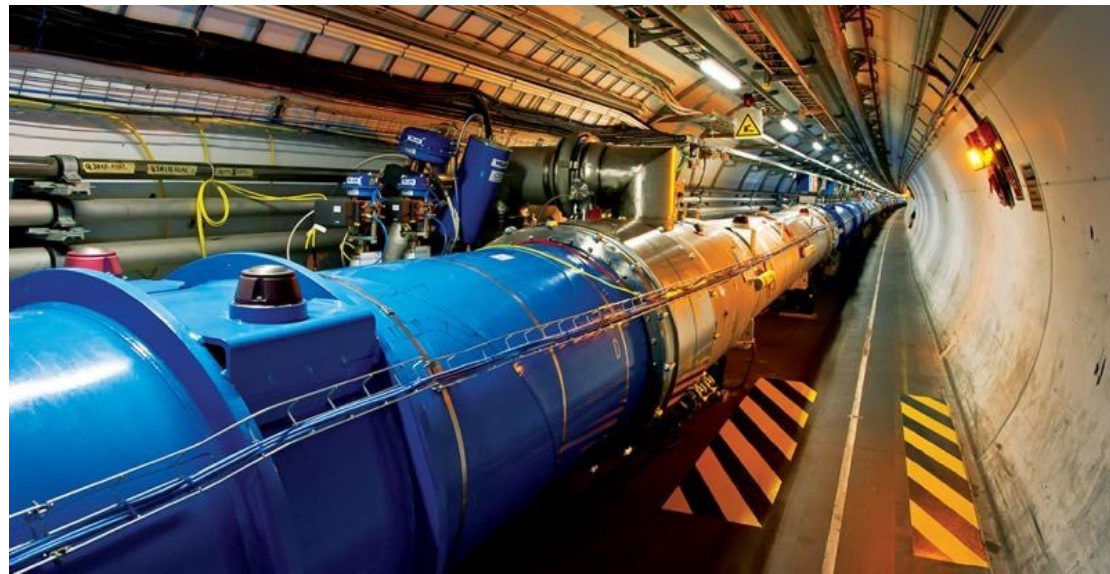
fermion $\frac{m_f}{v} \bar{f} f h$

gauge $\frac{m_W^2}{v^2} W_\mu^+ W_-^\mu (v + h)^2 + \frac{m_Z^2}{2v^2} Z_\mu Z^\mu (v + h)^2$

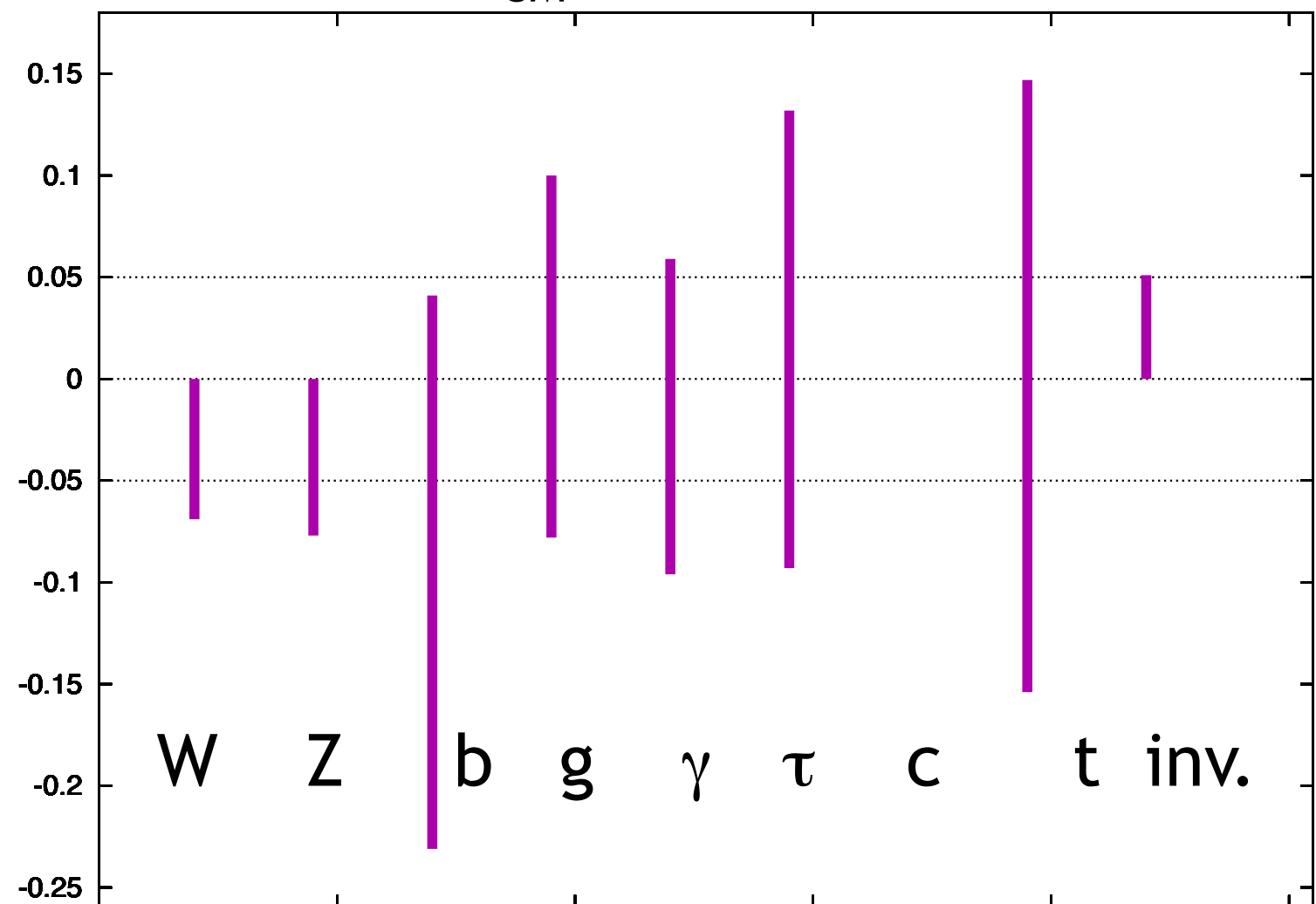
potential $\frac{m_h^2}{2} h^2 + \frac{m_h^2}{2v} h^3 + \frac{2m_h^2}{v^2} h^4$

simple, elegant!
predictive, testable!

How to test: the LHC



$g(hAA)/g(hAA)|_{SM}^{-1}$ LHC Peskin: 1207.2516



Not quite enough!

Beyond LHC: the future

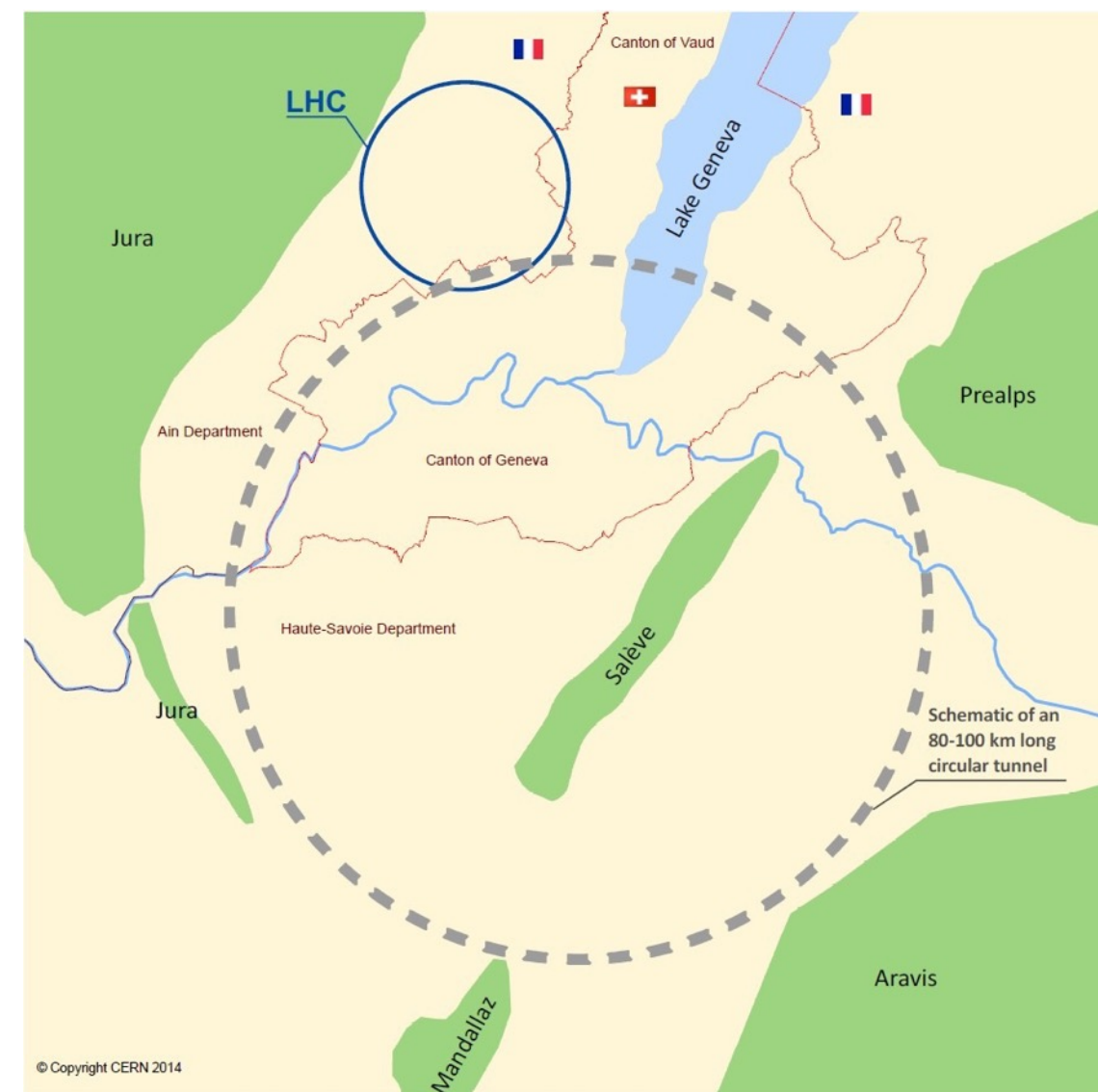
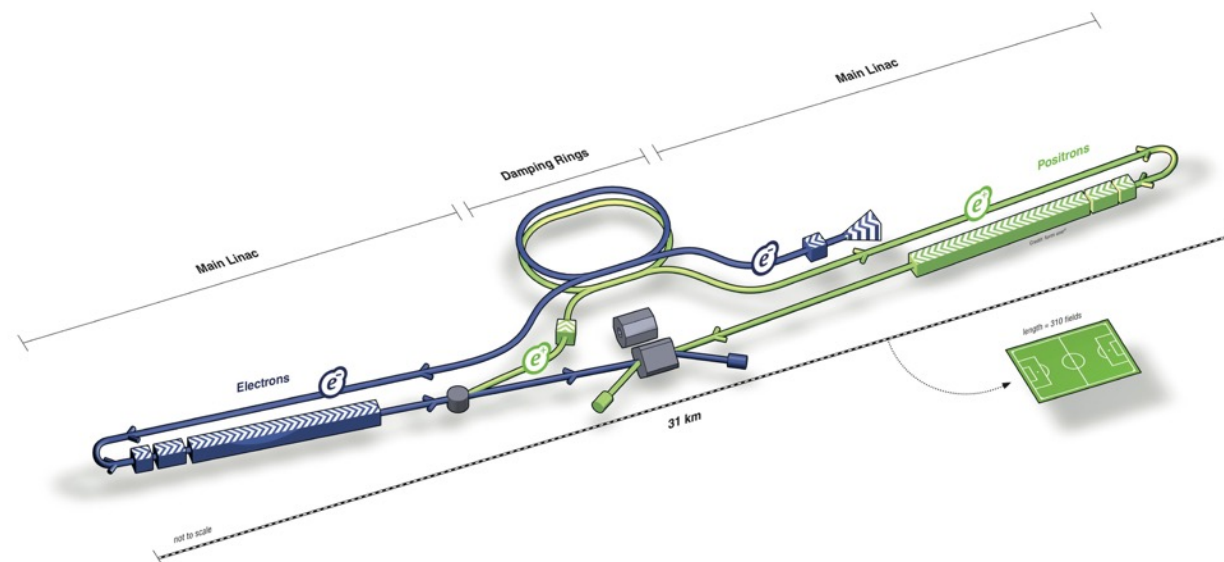
安装在同一隧道里的环形希格斯工厂（首期）+ 超级质子对撞机（二期）

SppC : 超级质子对撞机

CEPC : 240 - 250 GeV

SppC : 50 - 70 TeV

CEPC : 正负电子环形希格斯工厂



HXS at CEPC

High precision measurements of ZH cross section (and HZZ coupling) at CEPC

CEPC preCDR

Z decay mode	ΔM_H (MeV)	$\Delta\sigma(ZH)/\sigma(ZH)$	$\Delta g(HZZ)/g(HZZ)$
ee	14	2.1%	
$\mu\mu$	6.5	0.9%	
$ee + \mu\mu$	5.9	0.8%	0.4%
$q\bar{q}$		0.65%	0.32%
$ee + \mu\mu + q\bar{q}$		0.51%	0.25%

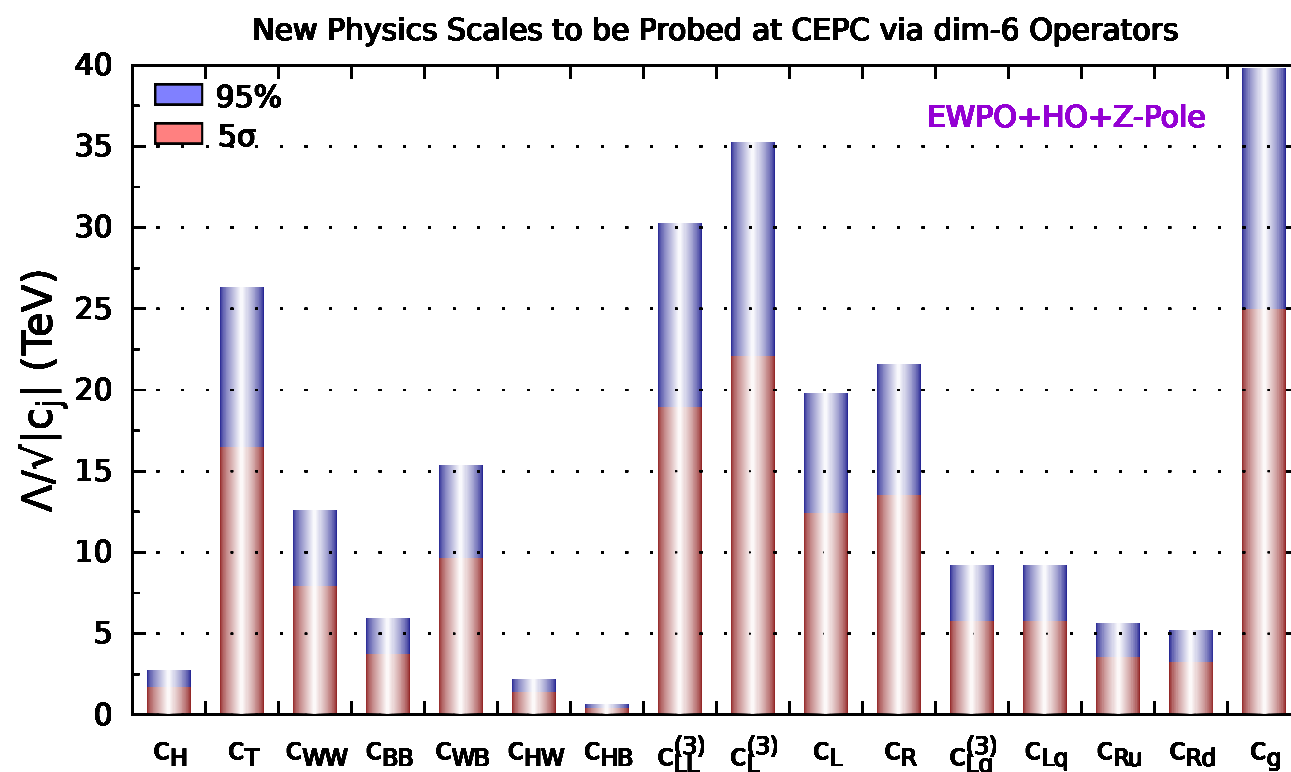
Even higher accuracies claimed by FCC-ee!

Bicer et al.: 1308.6176;
d'Enterria: 1601.06640; 1602.05043

Precision measurements and new physics

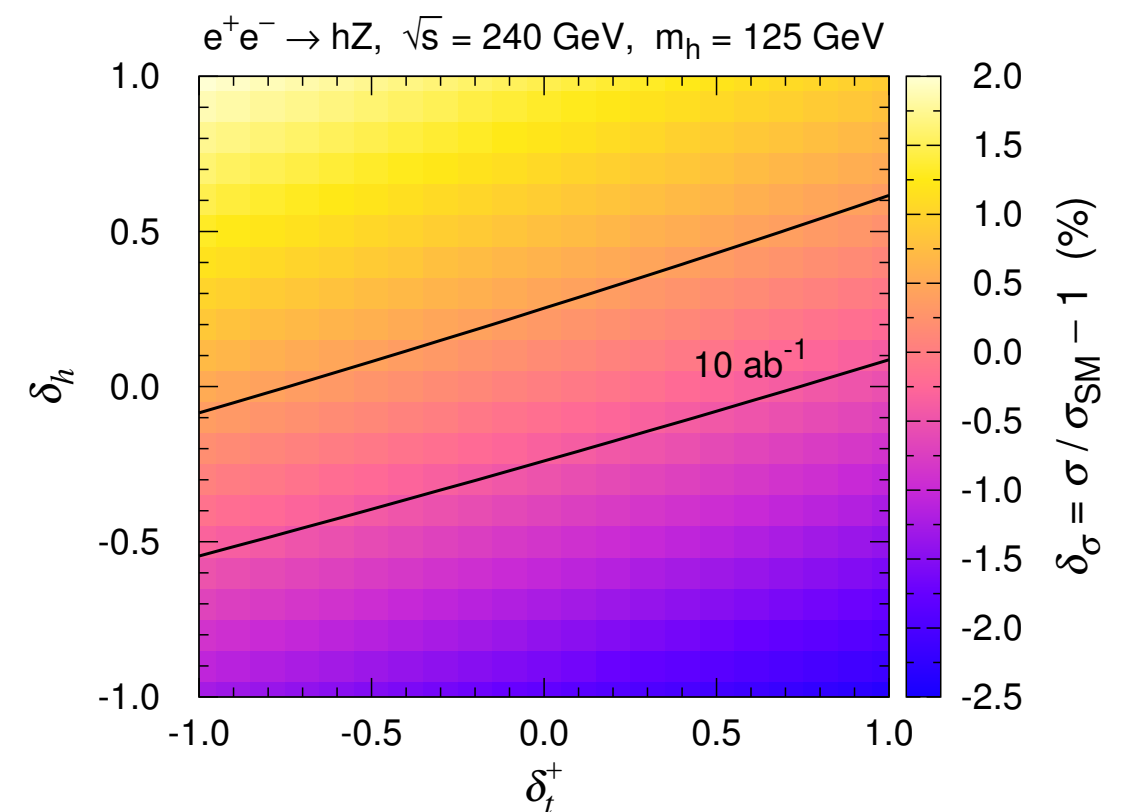
Lots of discussions on probing new physics using precision measurements at Higgs factories; sorry that I can't cover all!

Ge, He, Xiao: 1603.03385



Probing new physics scales

Huang, Gu, Yin, Yu, Zhang: 1511.03969

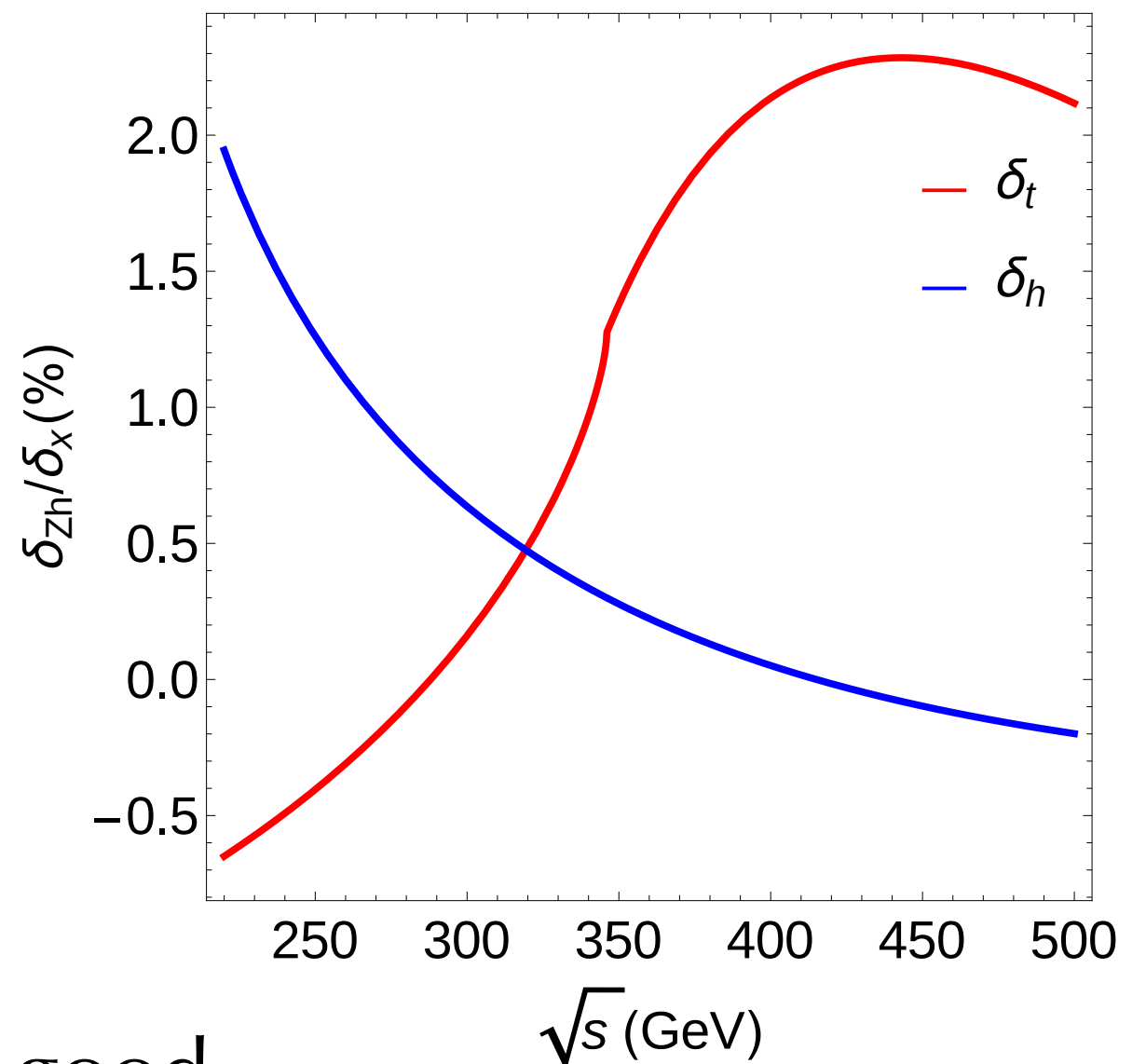
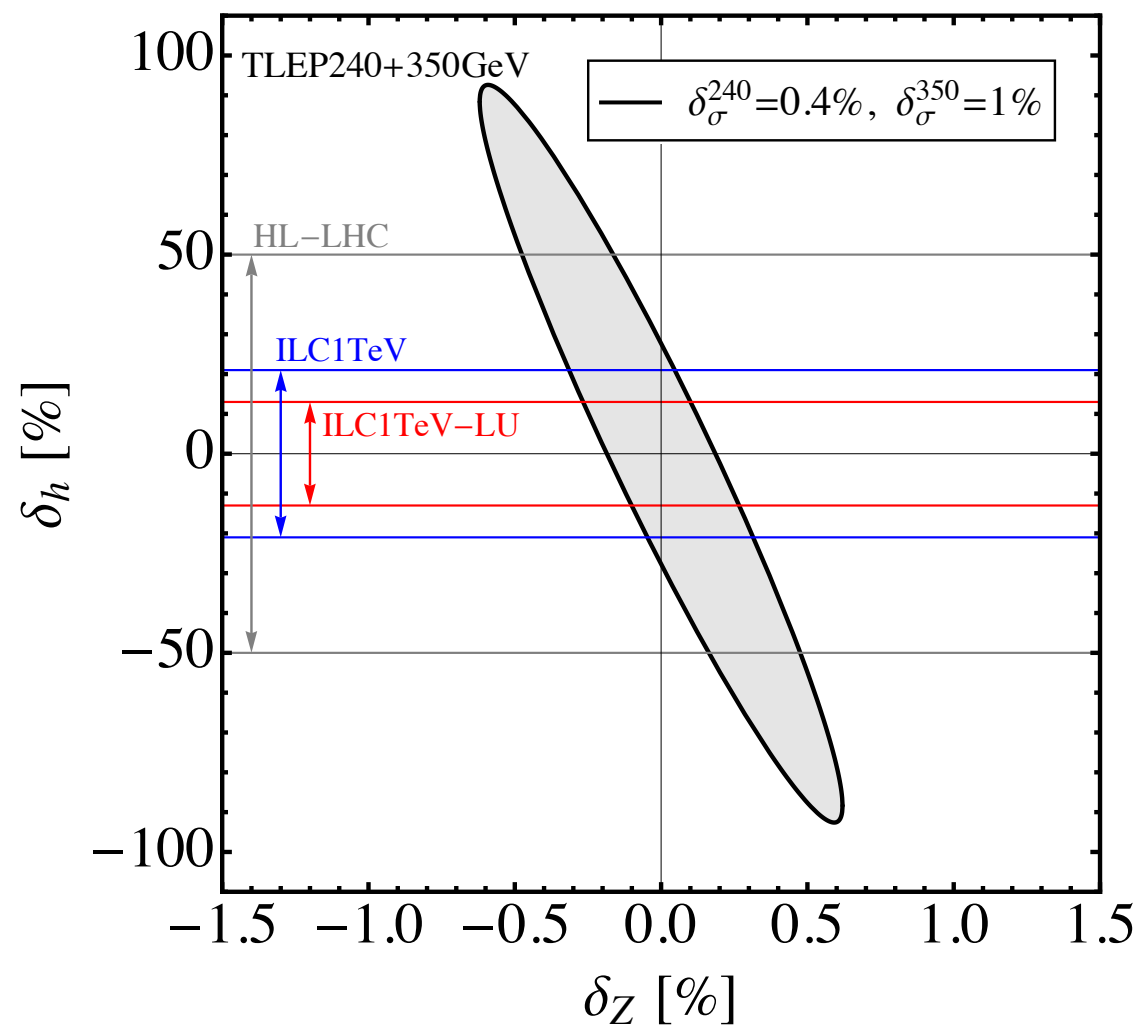


Testing EWPT

Indirect probe of Higgs self-coupling

McCullough: 1312.3322

Shen, Zhu: 1504.05626

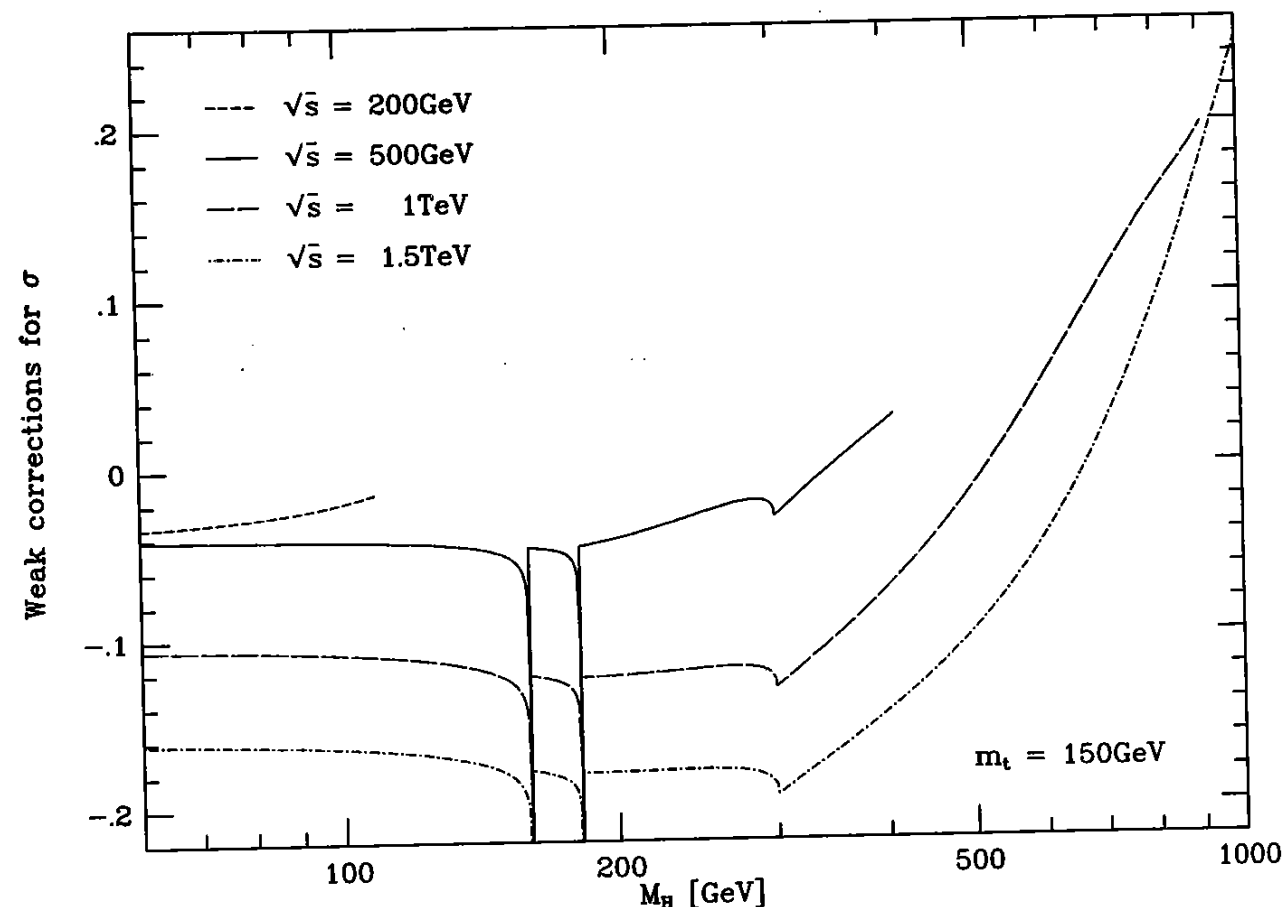


Model-dependent: requires good knowledges of HZZ and Htt couplings!

Precision theory for precision measurements

How well do we know $\sigma(ZH)$ in the SM?

NLO weak corrections known for decades



Fleischer, Jegerlehner
(1983); Kniehl (1992);
Denner, Küblbeck,
Mertig, Böhm (1992)

$\sim -3\%$ for 240 GeV

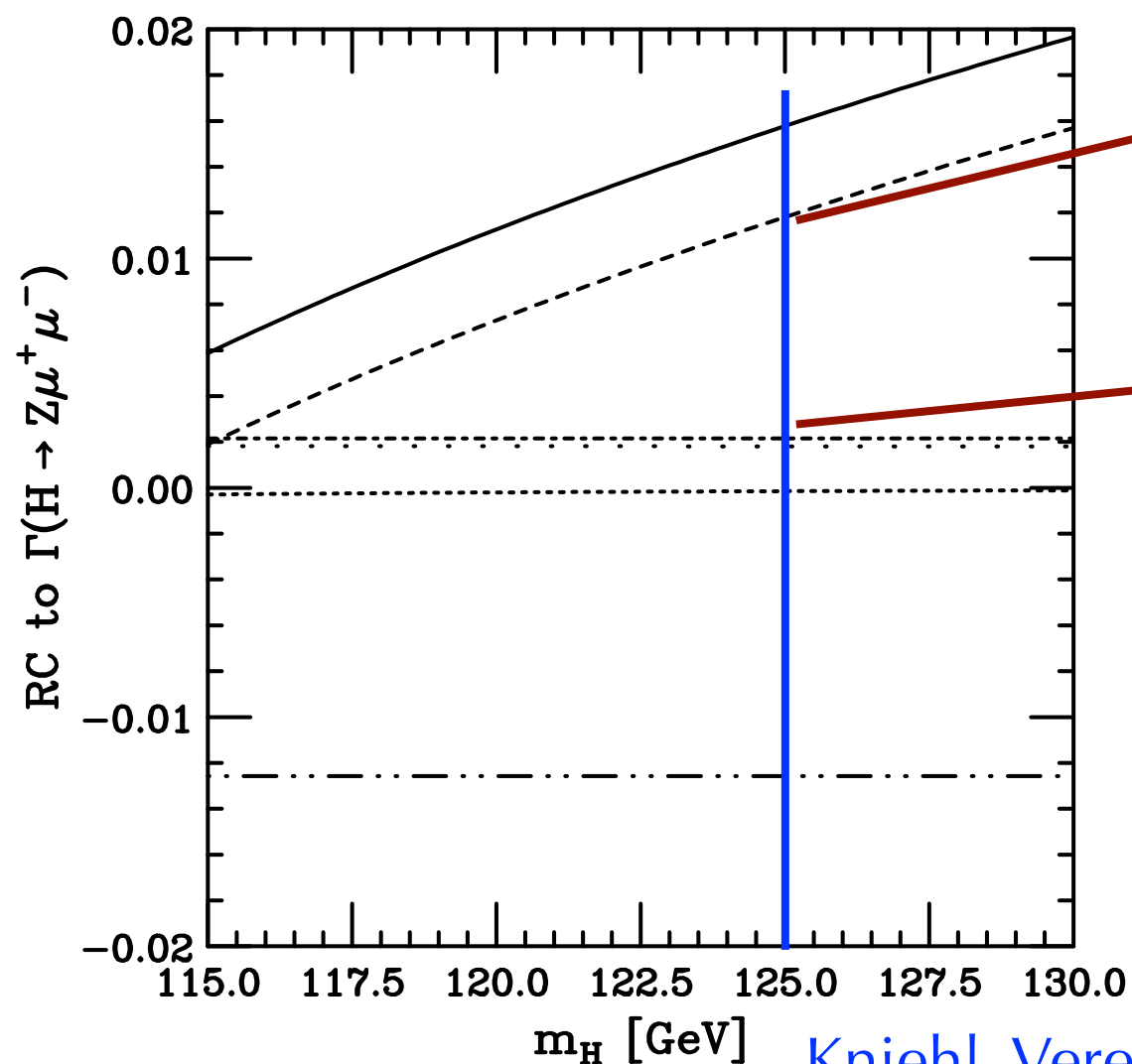
QED corrections also negative; size depends on cut on photon energy

**No improvement was attempted since then
(possibly because LEP2 didn't find the Higgs 😂)**

Precision theory for precision measurements

How well do we know $\sigma(ZH)$ in the SM?

Update for a closely related process: $H \rightarrow ZZ^* \rightarrow Zl^+l^-$



One-loop weak corrections

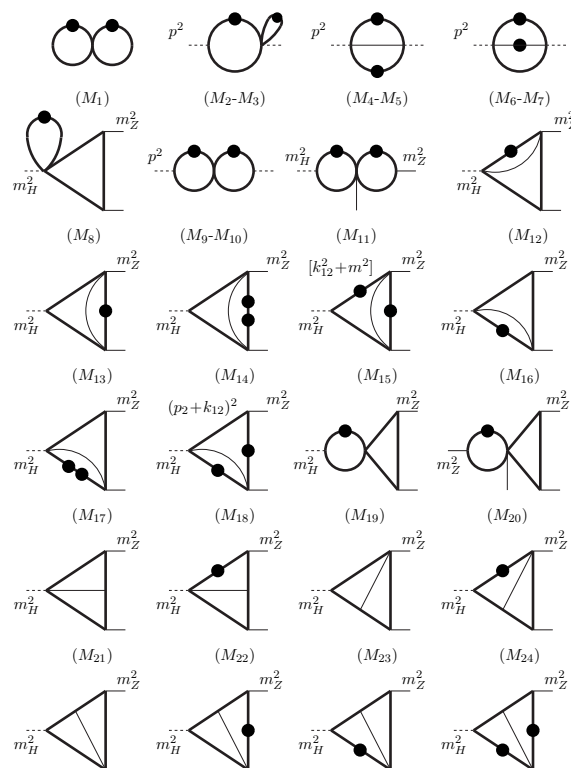
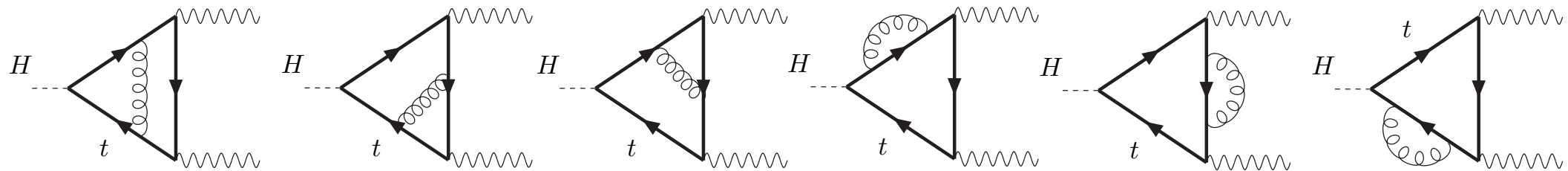
Top-mass enhanced
higher-order contributions

**For $\sigma(ZH)$ need to go
beyond large m_t !**

Towards NNLO $\sigma(ZH)$

Gong, Li, Xu, LLY: 1609.xxxxxx

The “simpler”: $O(\alpha\alpha_s)$



Figures from
Bonciani et al.
(1505.00567)

- 41 master integrals
- Many involve 4 mass scales:
difficult to obtain analytic
solutions

Sector decomposition

Binoth, Heinrich (hep-ph/0004013, hep-ph/0305234)

Efficient method for evaluating loop integrals in dimensional regularization

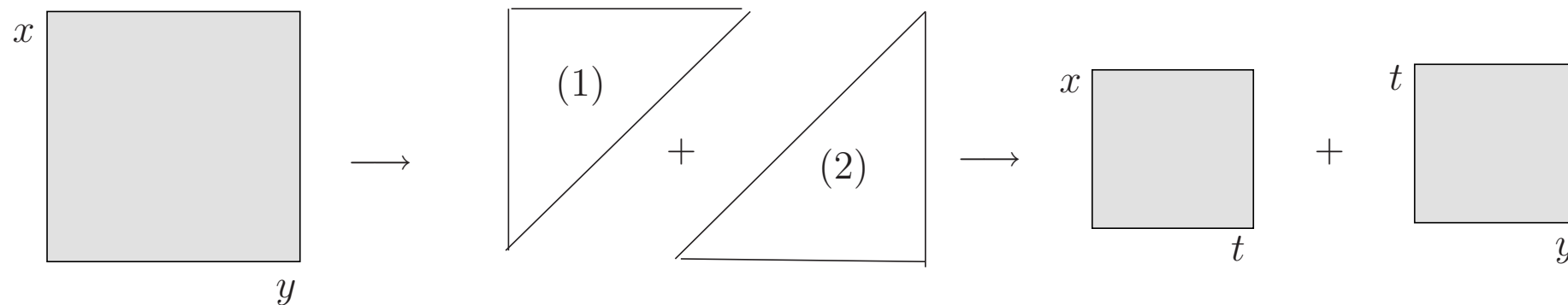


Figure from Heinrich (0803.4177)

Many public tools: FIESTA, SecDec, ...

A new fast code:

Li, Wang, Yan, Zhao (1508.02512)

	Vegas/CPU	QMC/GPU
P_2	$-3.848 \pm 0.004 + 0.0005i \pm 0.003i$	$-3.8482 \pm 0.0007 + 0.0004i \pm 0.0003i$
P_1	$3.81 \pm 0.03 - 6.41i \pm 0.03i$	$3.83 \pm 0.02 - 6.40i \pm 0.02i$
P_0	$77.2 \pm 0.2 + 20.1i \pm 0.2i$	$77.2 \pm 0.1 + 19.9i \pm 0.1i$
Integration Time	54290s	20s

Result

Gong, Li, Xu, LLY: 1609.xxxxx

Correction $\sim 1\%$ for CEPC (240 GeV); important effect!

Alternative: expansion in $1/m_t$

m_t^2	m_t^0	m_t^{-2}	m_t^{-4}
$\sim 82\%$	$\sim 16\%$	$\sim 1\%$	$< 1\%$

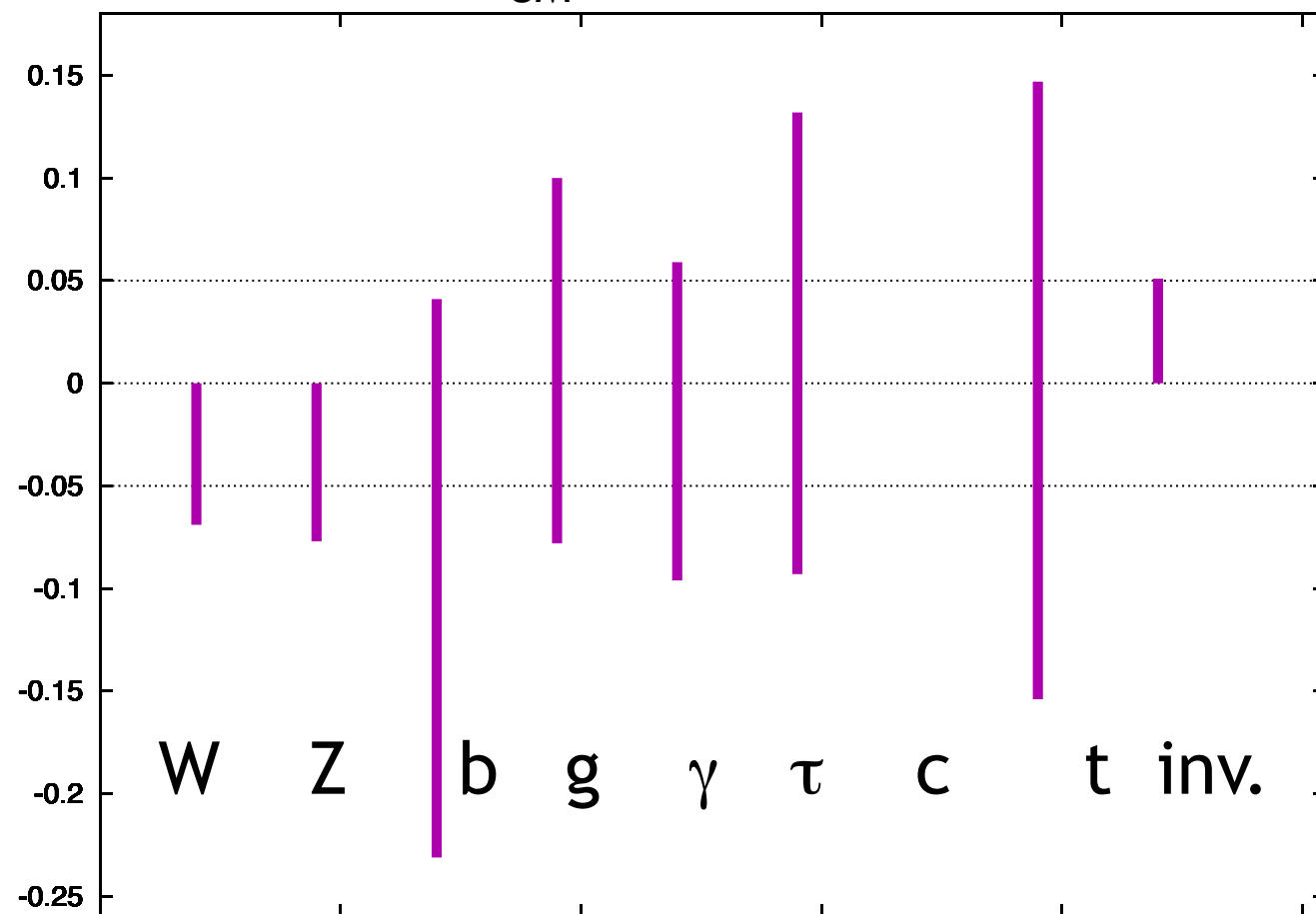
Fast convergence

Expansion in $1/m_t$ will not work for higher energies (e.g. ILC and FCC-ee)!

Future: the more difficult (but also important) $O(\alpha^2)$ correction

Towards SppC

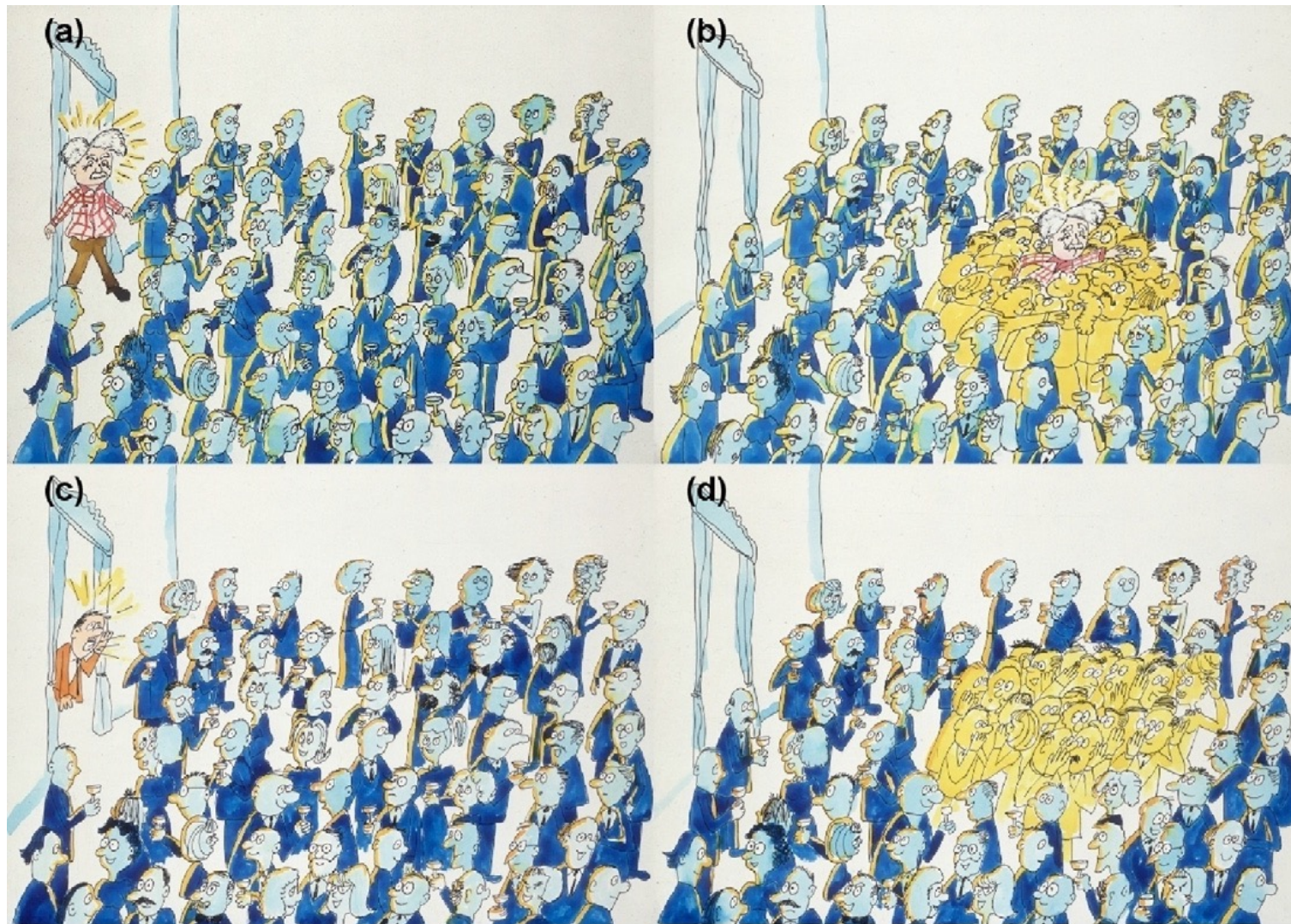
$g(hAA)/g(hAA)|_{SM}-1$ LHC



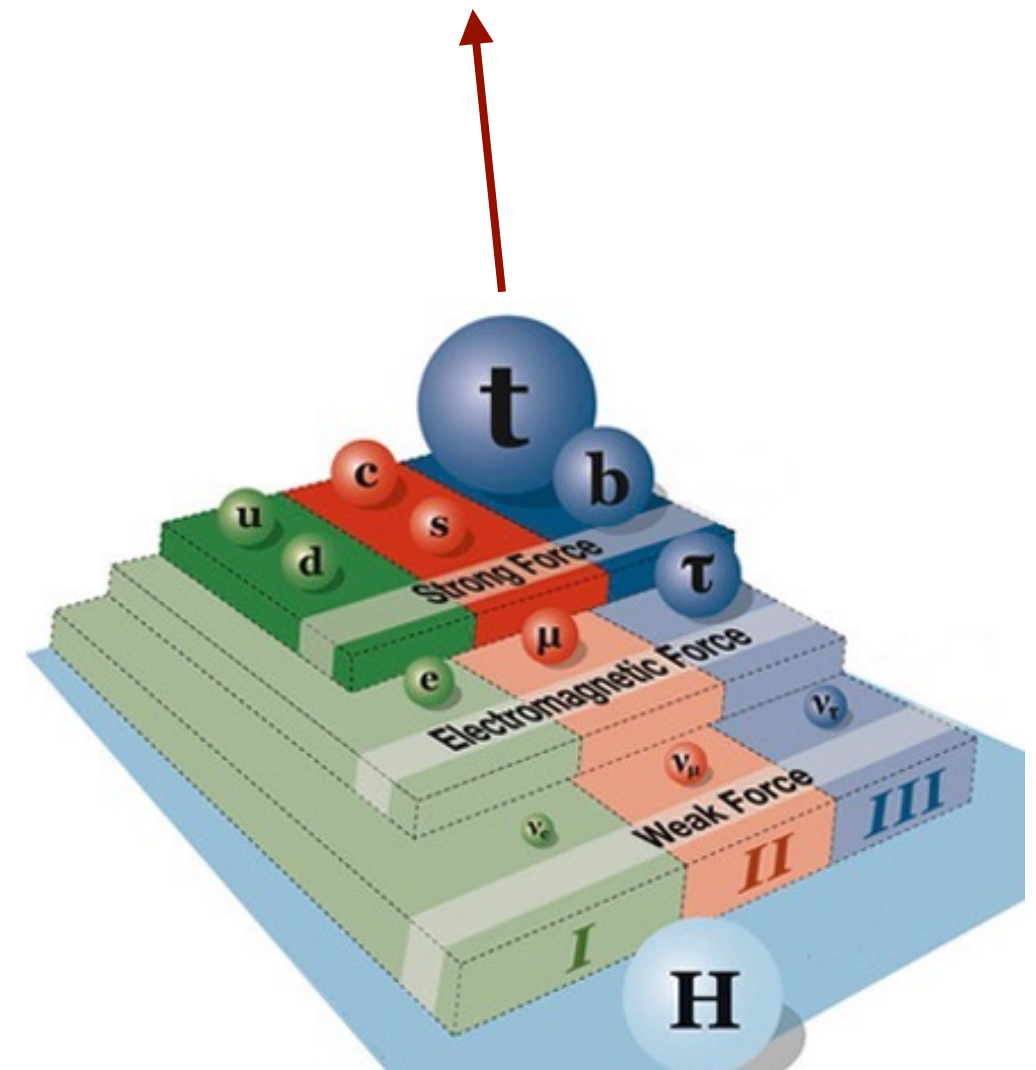
Two important things that LHC and CEPC will not tell us very precisely

- Top Yukawa coupling
- Higgs self-coupling

Top and Higgs

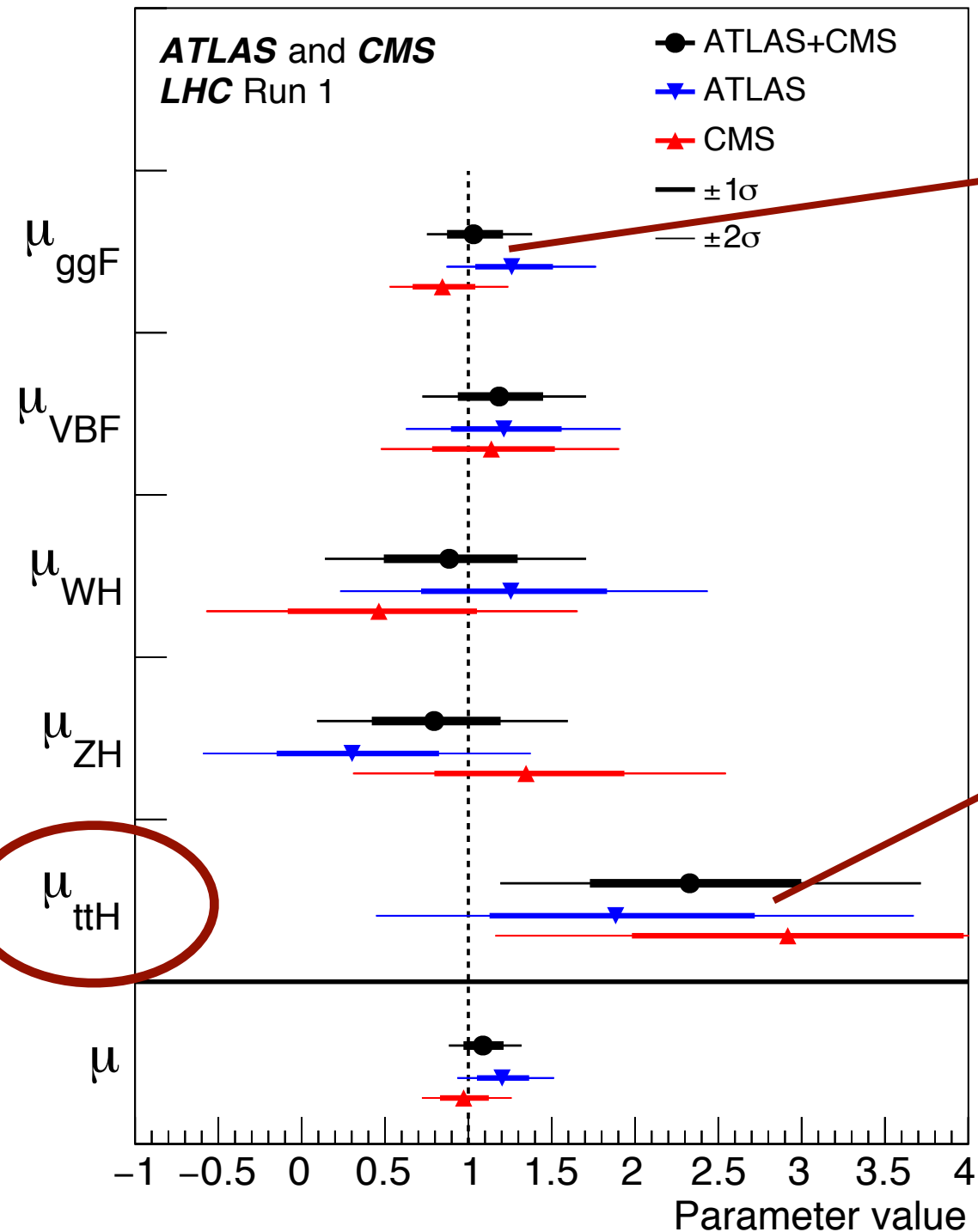


Strong Yukawa coupling!



Top Yukawa

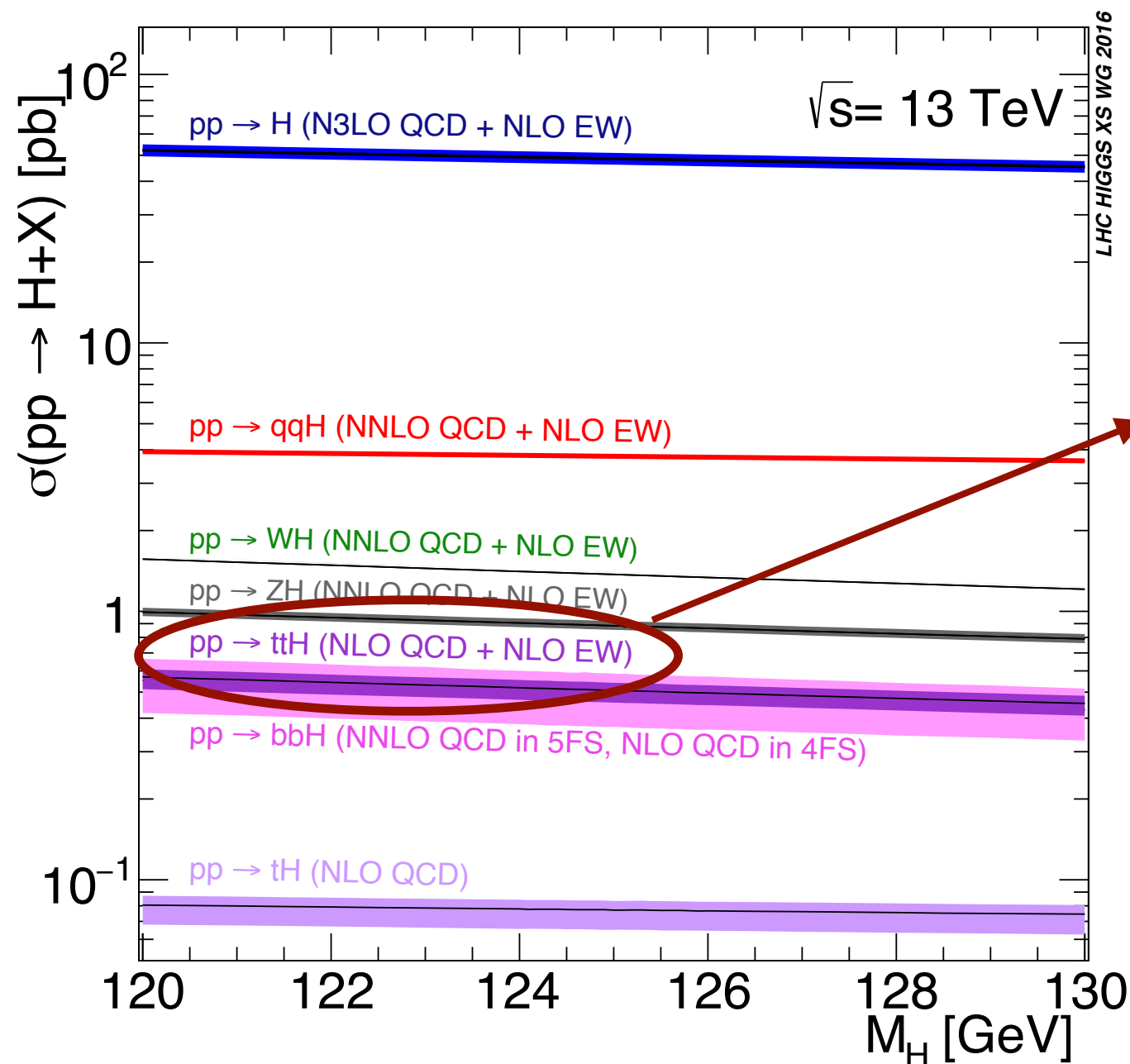
ATLAS and CMS: 1606.02266



$gg \rightarrow H$ cannot distinguish modified top Yukawa and new particles in the loop

- Direct information on top Yukawa
- Statistics limited (Run 2 physics)

Theoretical uncertainty (again)



LHC HXSWG report 4 (to appear)

NLO only! Higher orders?

NNLO
extremely
difficult!

Resummation?

Resummation for top pairs

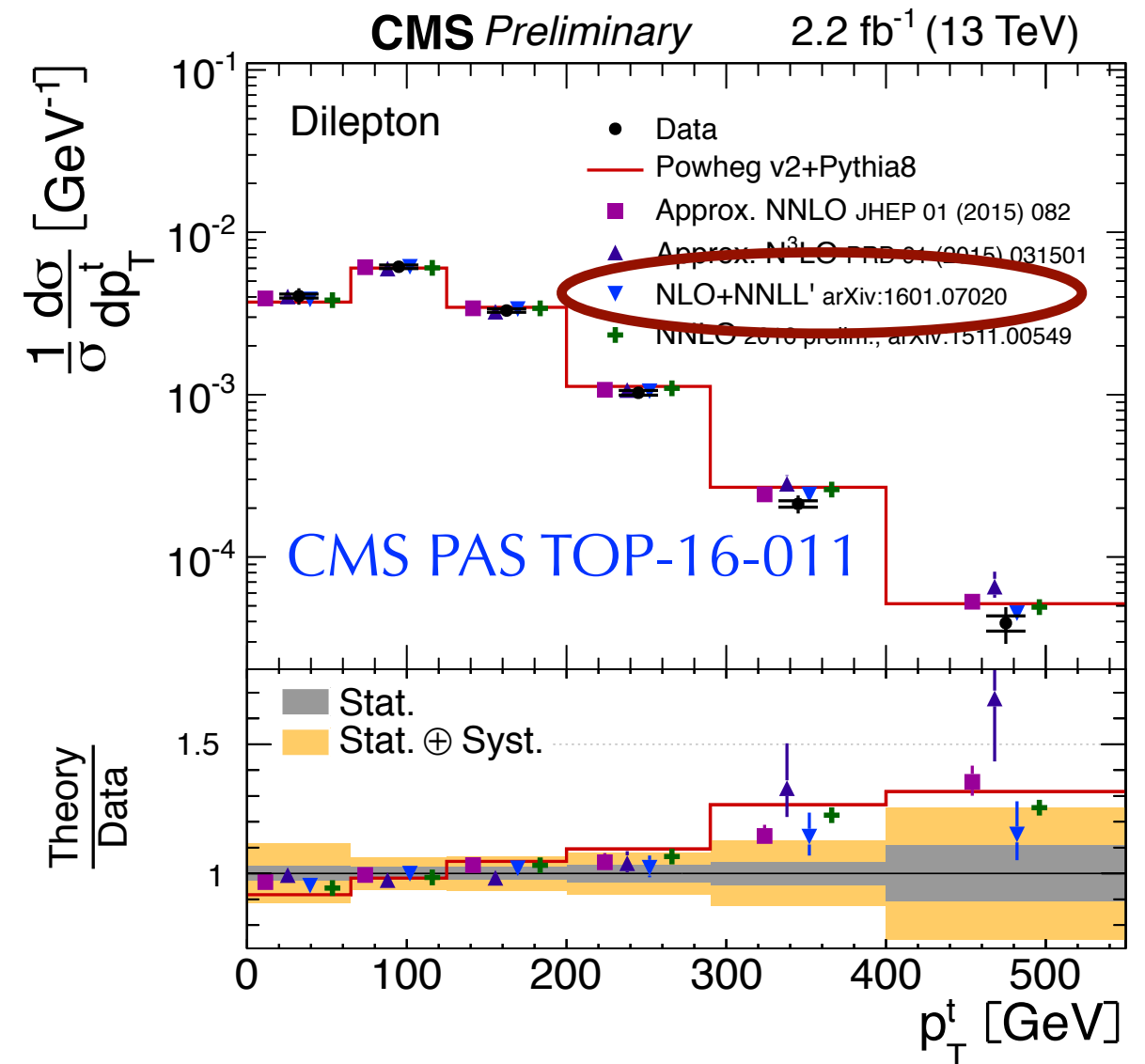
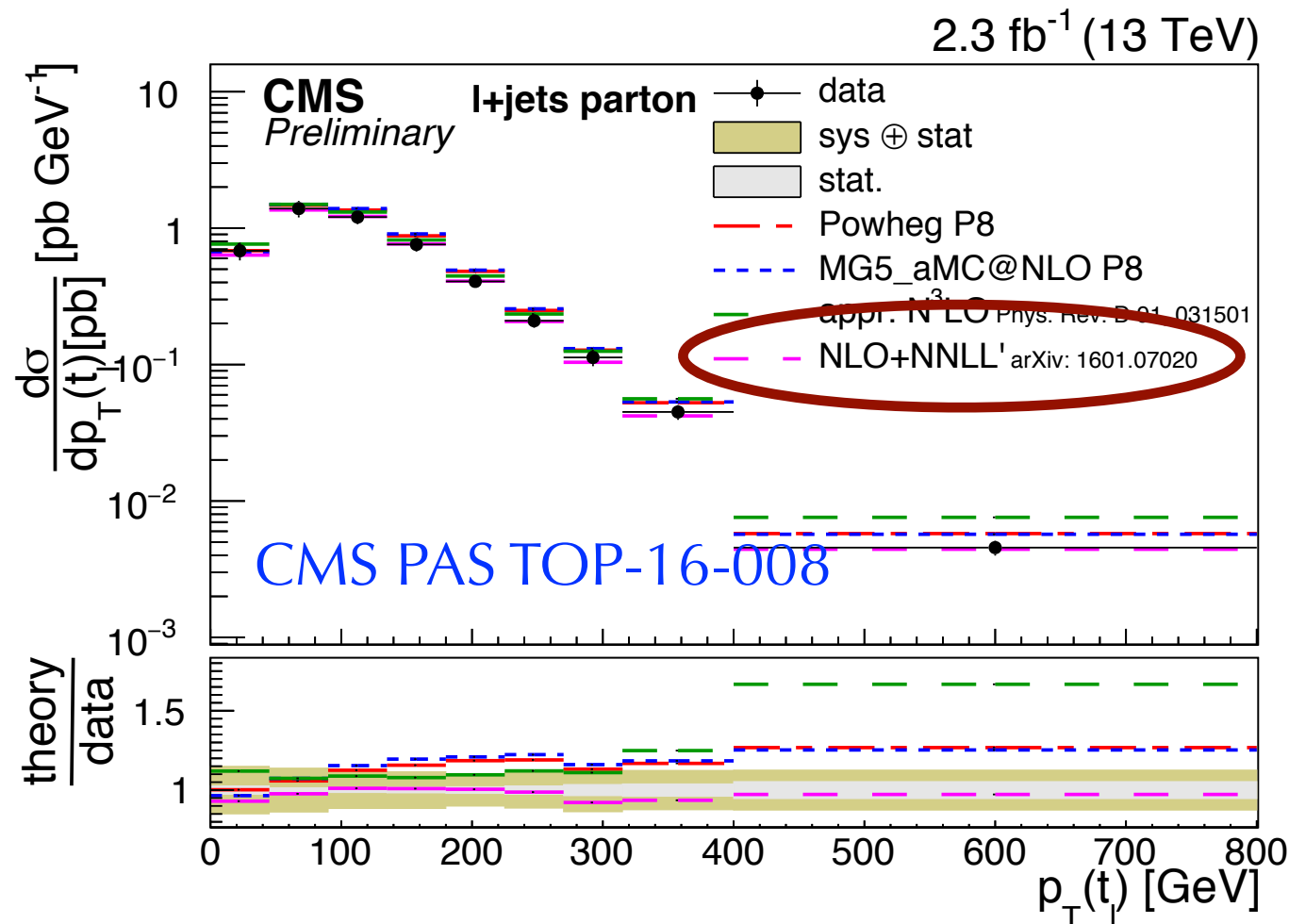
Ferrogia, Neubert, Pecjak, **LLY**: 0907.4791

Ahrens, Ferrogia, Neubert, Pecjak, **LLY**: 1003.5827; 1105.5824; 1106.6051

Ferrogia, Pecjak, **LLY**: 1205.3662; 1207.4798; 1306.1537

Zhu, Li, Li, Shao, **LLY**: 1208.5774; 1307.2464

Pecjak, Scott, Wang, **LLY**: 1601.07020



Essence of the calculation

Two dangerous contributions for production of highly-boosted top quarks at LHC and SppC

soft gluons

$$\ln \frac{\hat{s} - M_{t\bar{t}}^2}{M_{t\bar{t}}^2}$$

quasi-collinear
gluons

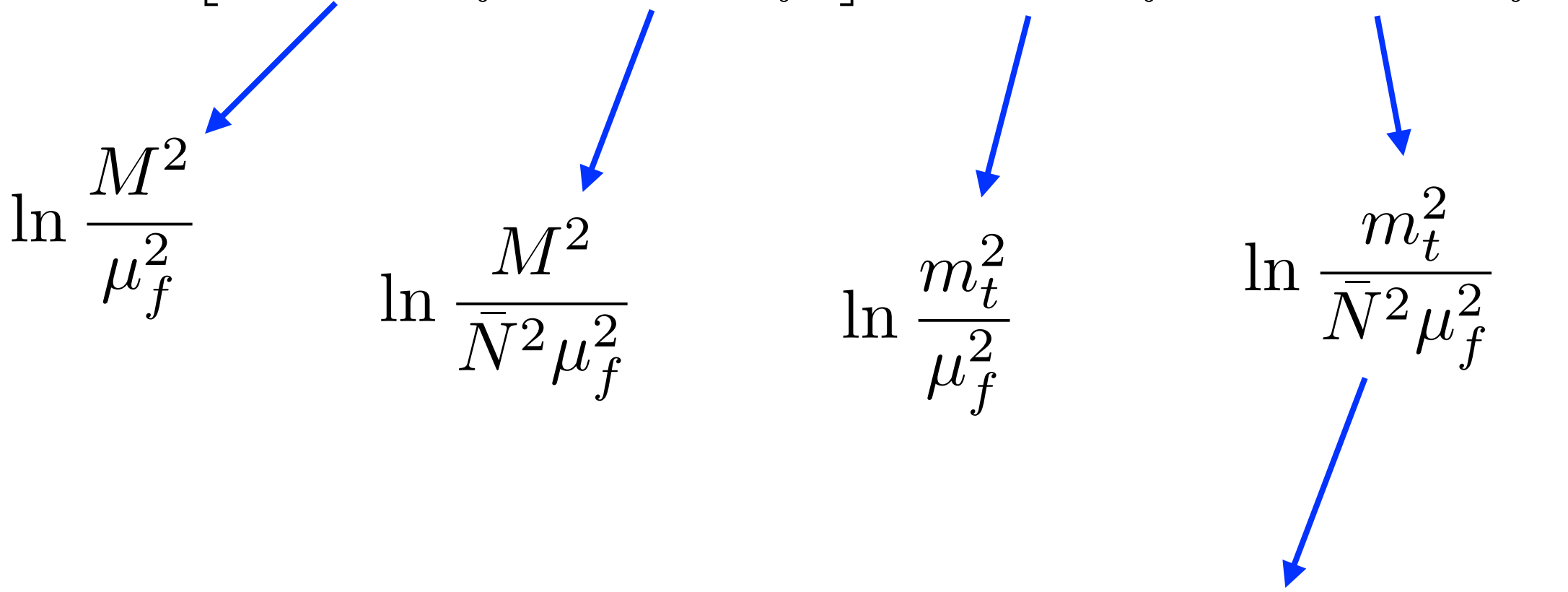
$$\ln \frac{m_t^2}{M_{t\bar{t}}^2}$$

Double factorization

Ferroglia, Pecjak, **LLY**: 1205.3662

Boosted limit: $M \gg M/N, m_t$

$$\hat{\sigma}(N, \mu_f) \sim \text{Tr}[\mathbf{H}(L_h, \mu_f) \mathbf{S}(L_s, \mu_f)] C_D^2(L_c, \mu_f) S_D^2(L_{sc}, \mu_f)$$


$$\ln \frac{M^2}{\mu_f^2}$$

$$\ln \frac{M^2}{\bar{N}^2 \mu_f^2}$$

$$\ln \frac{m_t^2}{\mu_f^2}$$

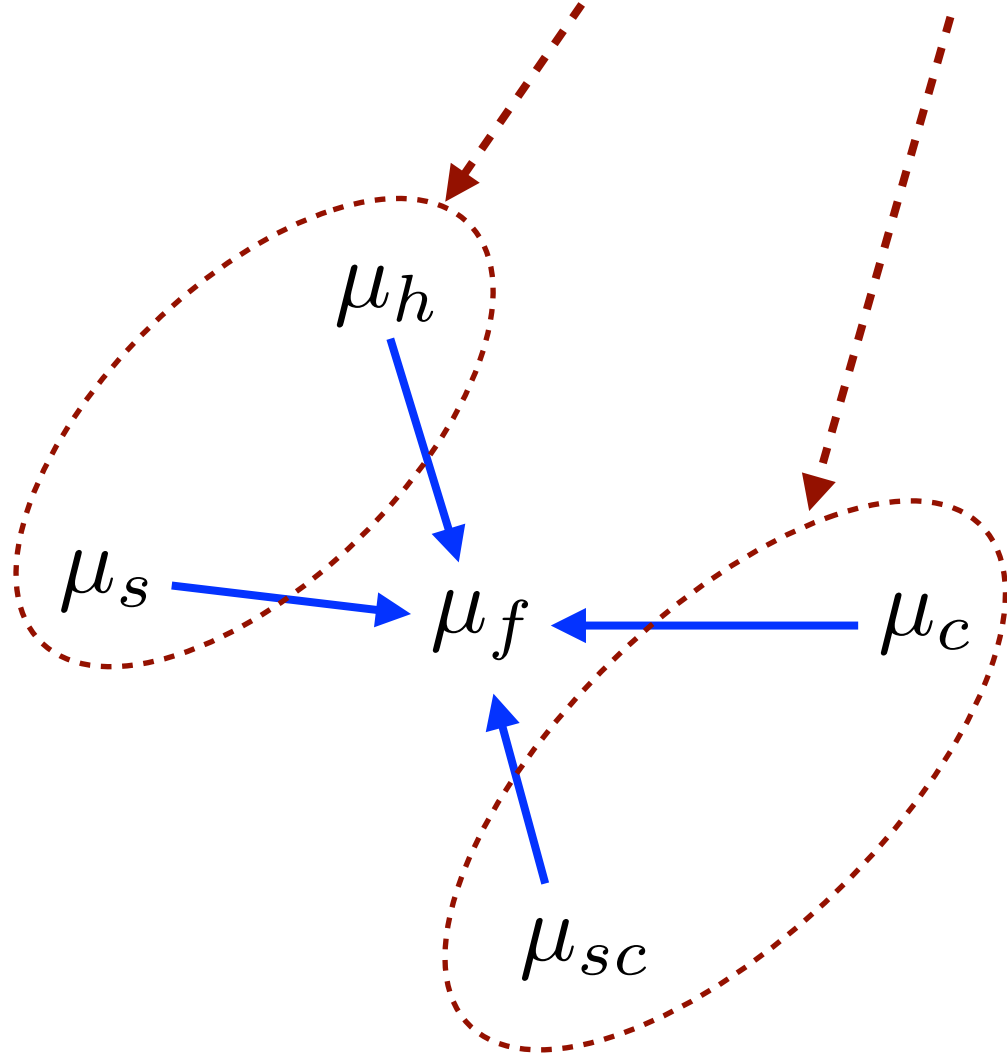
$$\ln \frac{m_t^2}{\bar{N}^2 \mu_f^2}$$

Emergence of a soft-collinear scale m_t/N !

Resummation

Pecjak, Scott, Wang, **LLY**: 1601.07020

$$\hat{\sigma}(N, \mu_f) \sim \text{Tr} \left[\mathbf{U}(\mu_f, \mu_h, \mu_s) \mathbf{H}(L_h, \mu_h) \mathbf{U}^\dagger(\mu_f, \mu_h, \mu_s) \mathbf{S}(L_s, \mu_s) \right] \\ \times U_D^2(\mu_f, \mu_c, \mu_{sc}) C_D^2(L_c, \mu_c) S_D^2(L_{sc}, \mu_{sc})$$

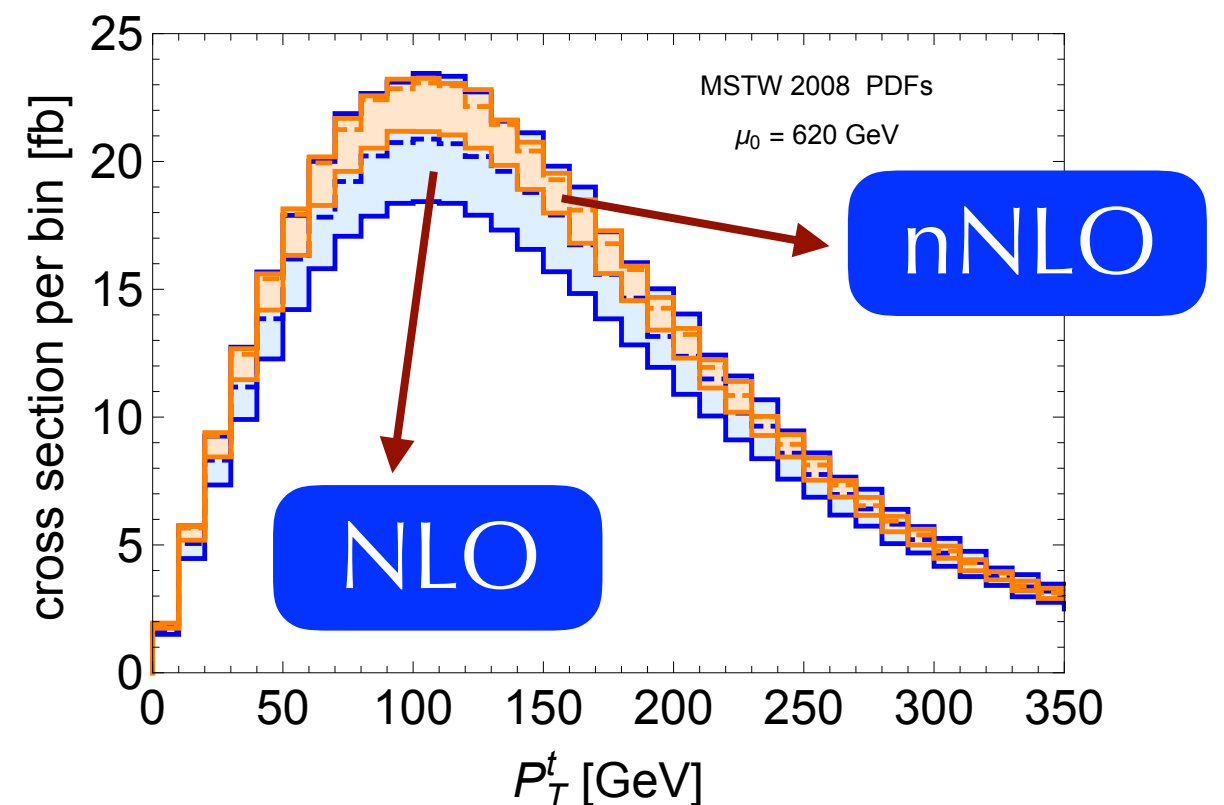
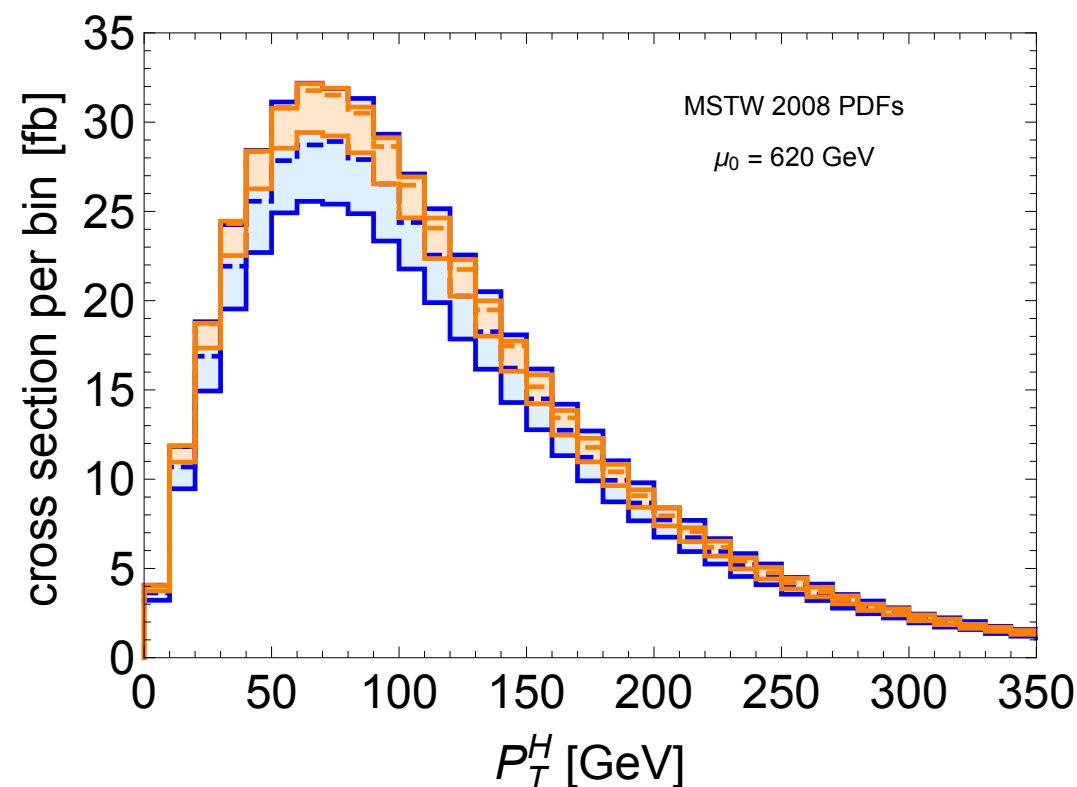


$pp \rightarrow ttH$ very similar to $pp \rightarrow tt$,
but some ingredients are missing:
performing soft resummation first

ttH: approximate NNLO

Broggio, Ferroglia, Pecjak, Signer, [LLY: 1510.01914](#)

Exact NNLO for ttH unlikely to be available very soon!



First fully differential prediction beyond NLO!

NLO+NNLL resummation in progress

Future: predictions for SppC (boosted tops and Higgs)

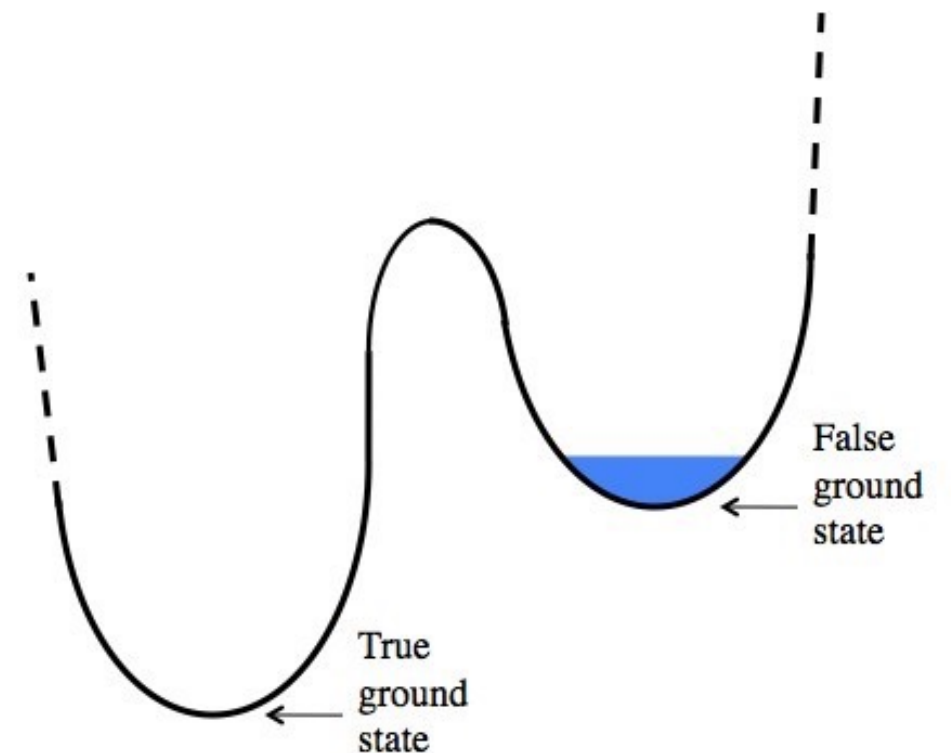
Higgs self-couplings

$$\frac{m_h^2}{2}h^2 + \frac{m_h^2}{2v}h^3 + \frac{2m_h^2}{v^2}h^4$$

“6th force”

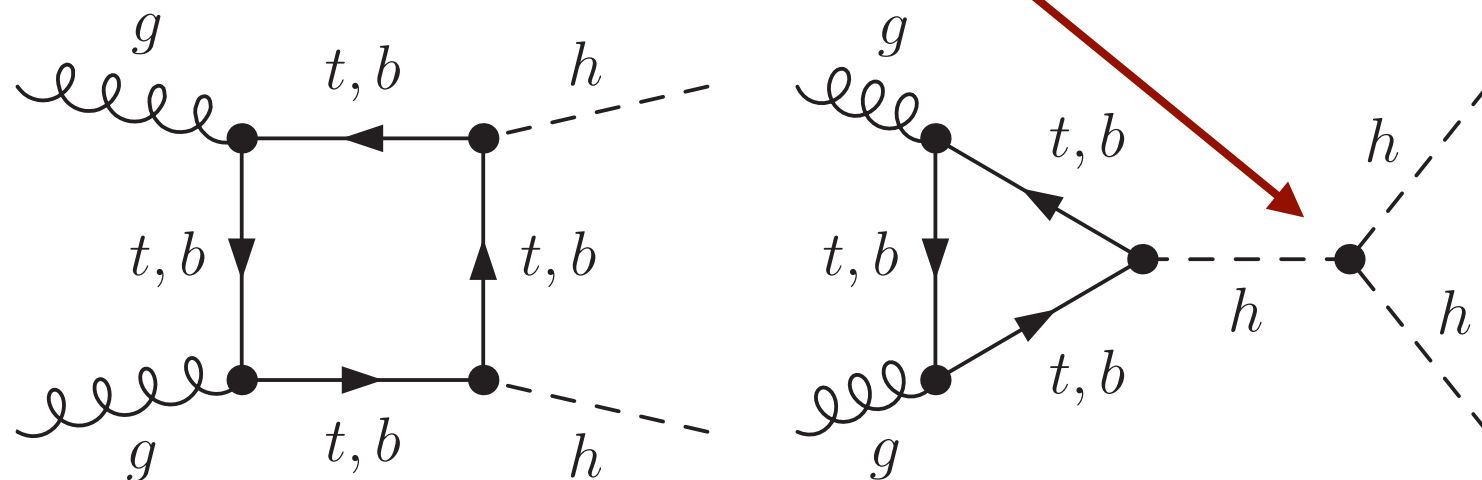
**How can we verify
these two interactions?**

Important for EW phase transition
as well as vacuum stability!



Higgs pair & self-coupling

$$\frac{m_h^2}{2}h^2 + \frac{m_h^2}{2v}h^3 + \frac{2m_h^2}{v^2}h^4$$

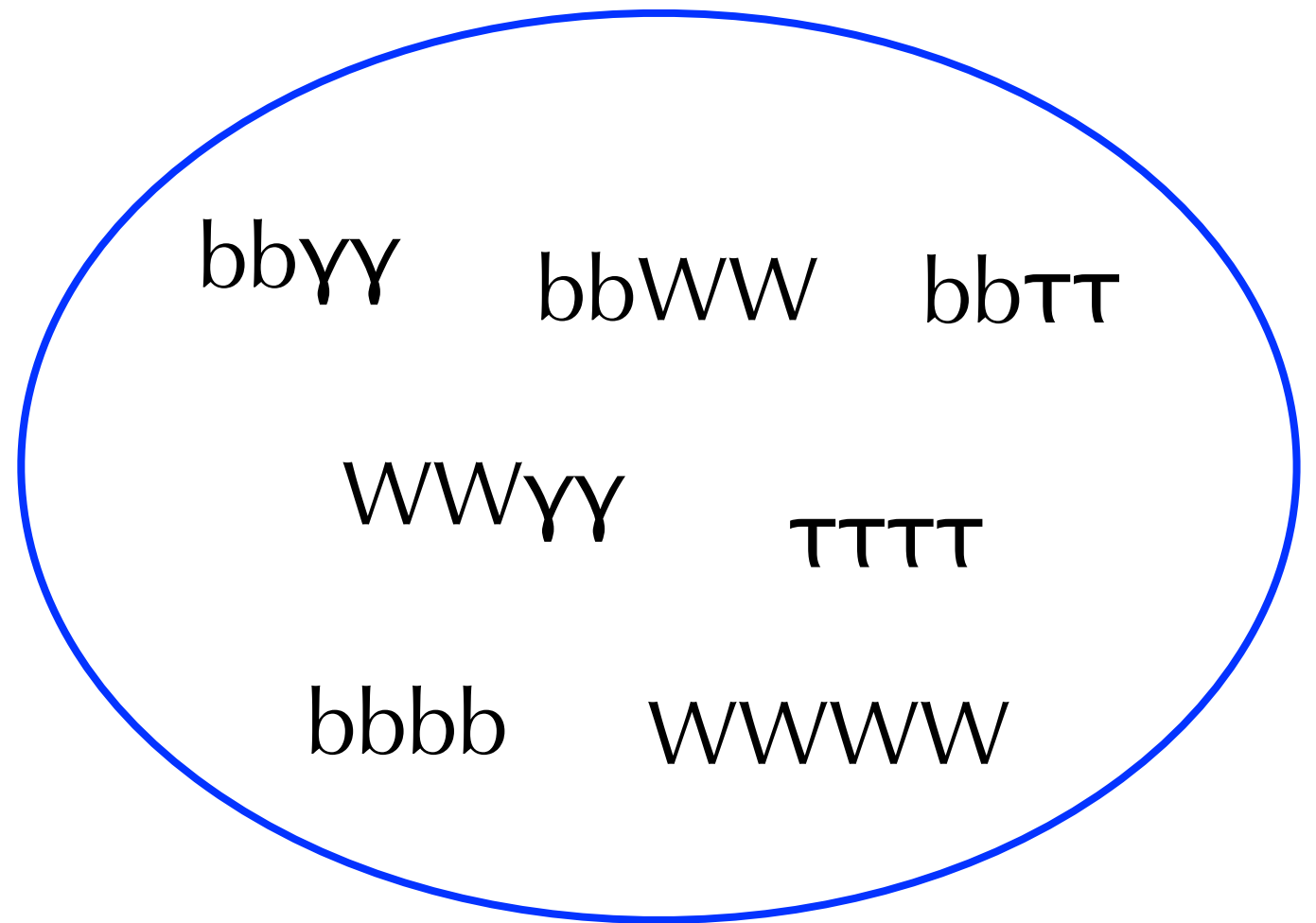
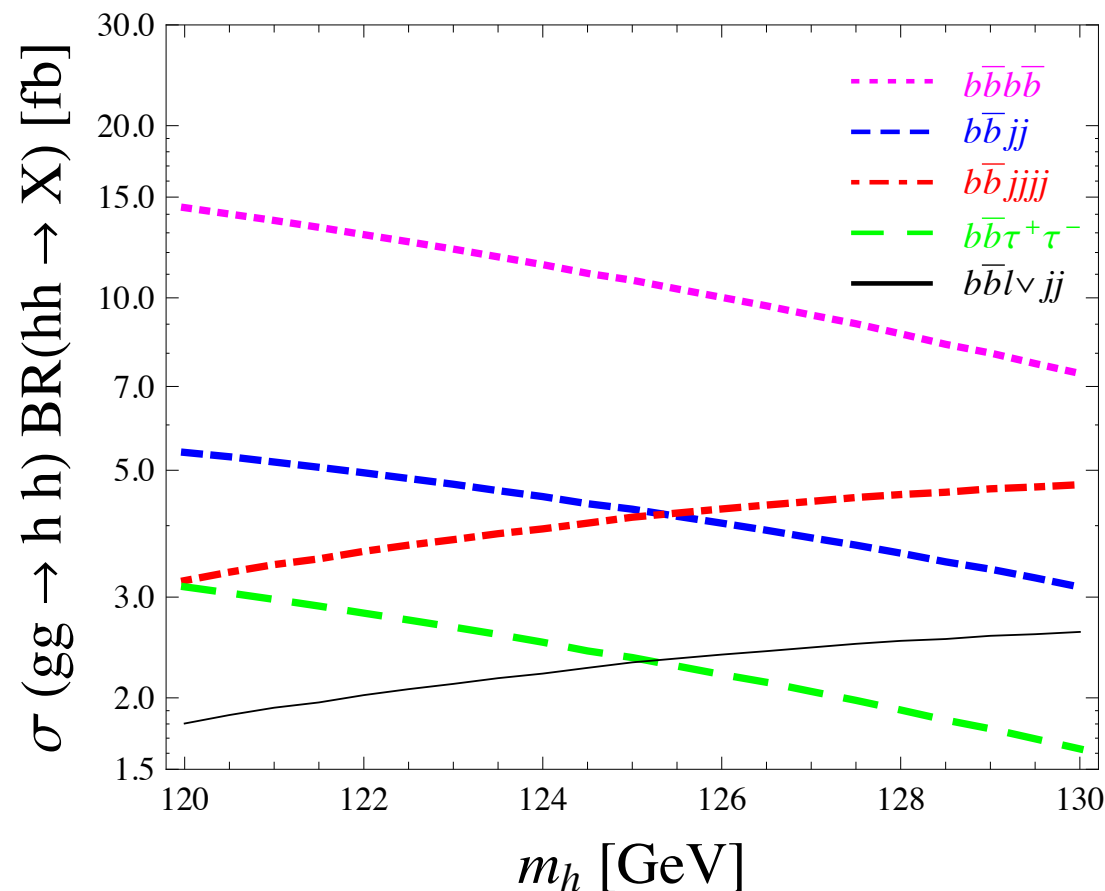


However, notoriously difficult to detect!

HL-LHC and 100 TeV physics!

Detecting HH production

Requires combination of various decay channels!

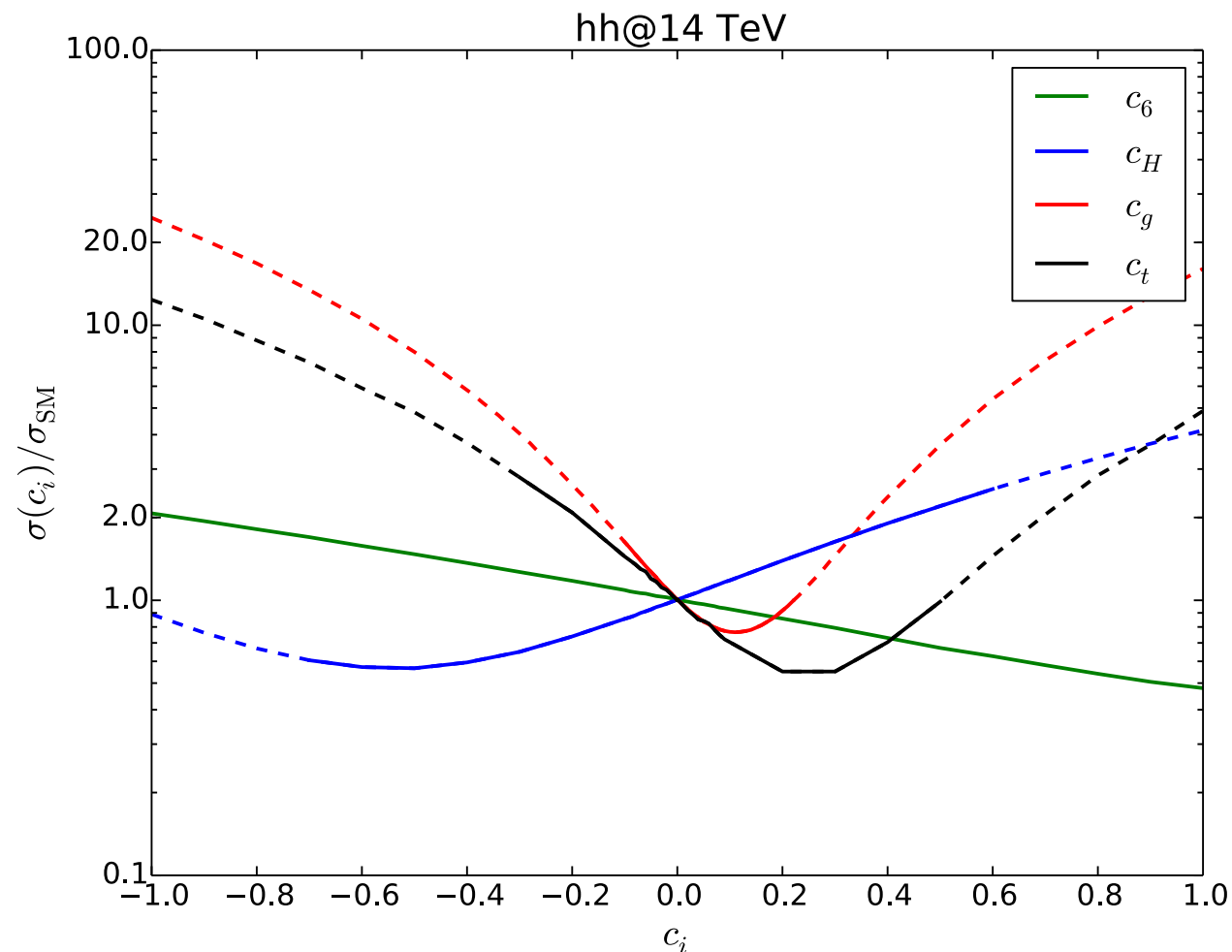


**Hot topic since
Higgs discovery!**

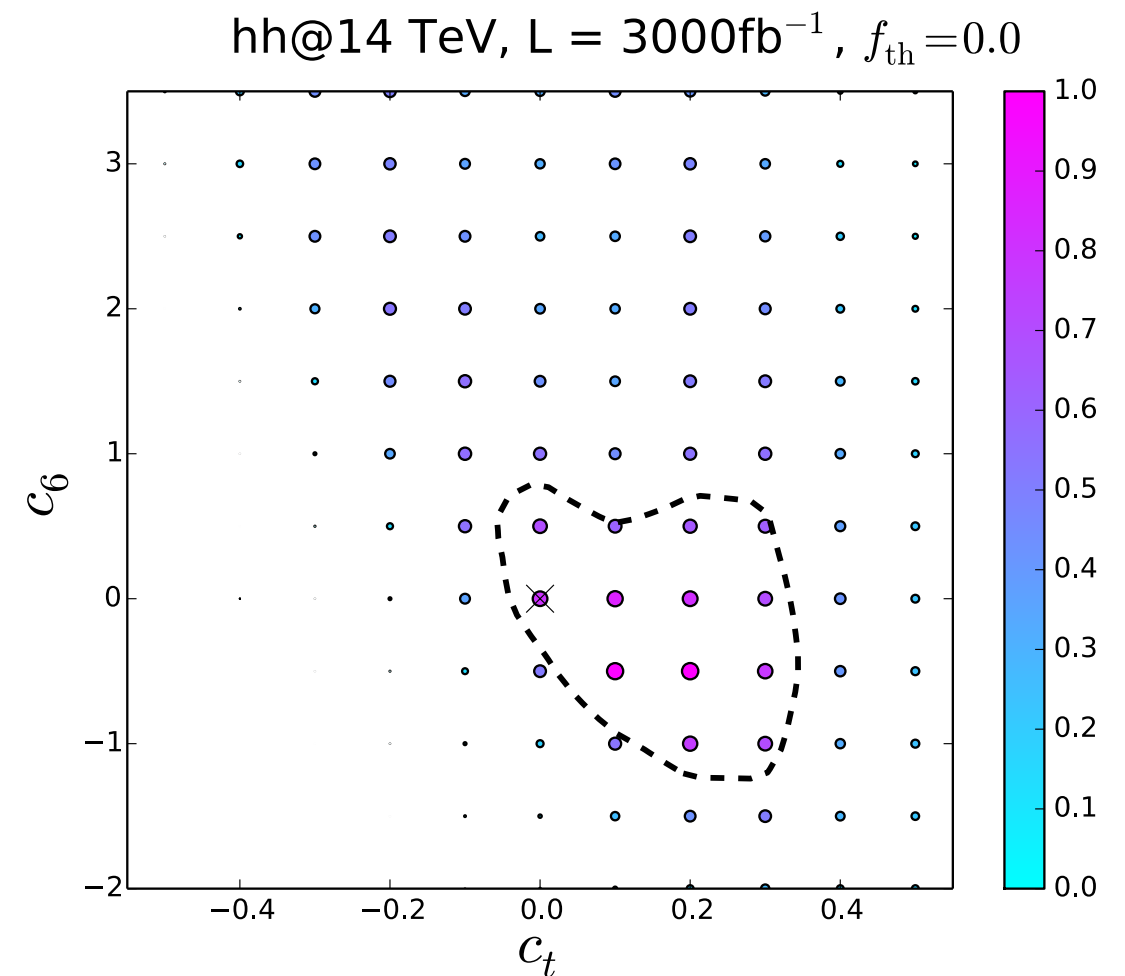
Dolan et al.: 1206.5001; Papaefstathiou, **LLY**, Zurita: 1209.1489;
Baglio et al.: 1212.5581; Barr et al.: 1309.6318; de Lima et al.:
1404.7131; Barr et al.: 1412.7154; Li, Li, Yan, Zhao: 1503.07616;
Papaefstathiou: 1504.04621; Kotwal et al.: 1504.08042; He, Ren, Yao:
1506.03302; Lü, Du, Fang, He, Zhang: 1507.02644; Zhao, Li, Li, Yan:
1604.04329; Kling et al.: 1607.07441; ...; sorry for limited space!

HH constraints on EFT

Goertz, Papaefstathiou, **LLY**, Zurita: 1410.3471



Rate sensitive to
new physics

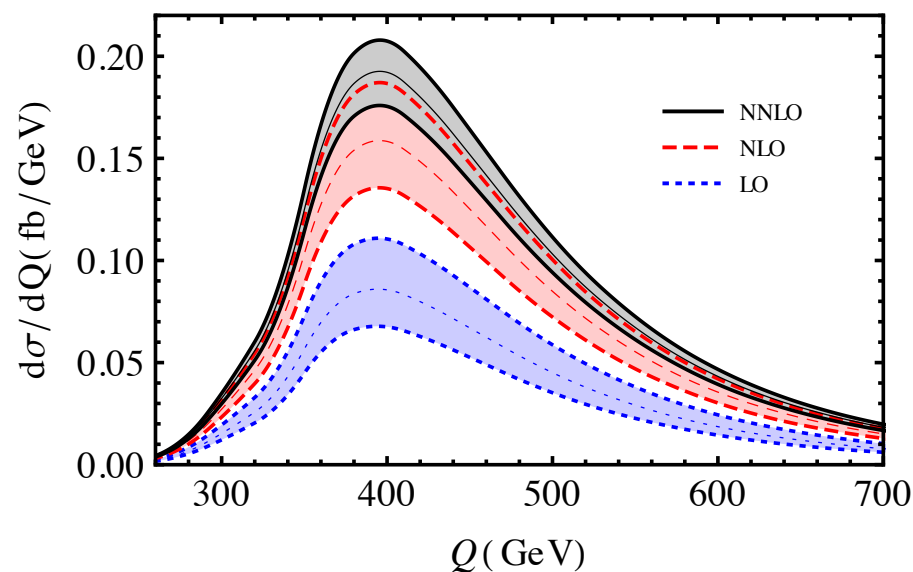


Can be used to constrain
EFT parameters

See also: Azatov, Contino, Panico, Son (1502.00539); He, Ren, Yao (1506.03302);
Cao, Yan, Zhang, Zhang (1508.06512)

NNLO for Higgs pair

de Florian, Mazzitelli: 1309.6594; de Florian, Grazzini et al.: 1606.09519



\sqrt{s} [TeV]	σ_{LO} [fb]	σ_{NLO} [fb]	σ_{NNLO} [fb]
13	13.8059(13) $^{+31.5\%}_{-22.5\%}$	25.829(3) $^{+17.8\%}_{-15.4\%}$	30.38(3) $^{+5.2\%}_{-7.7\%}$
14	17.0778(16) $^{+30.7\%}_{-22.1\%}$	31.934(3) $^{+17.5\%}_{-15.1\%}$	37.52(4) $^{+5.2\%}_{-7.6\%}$

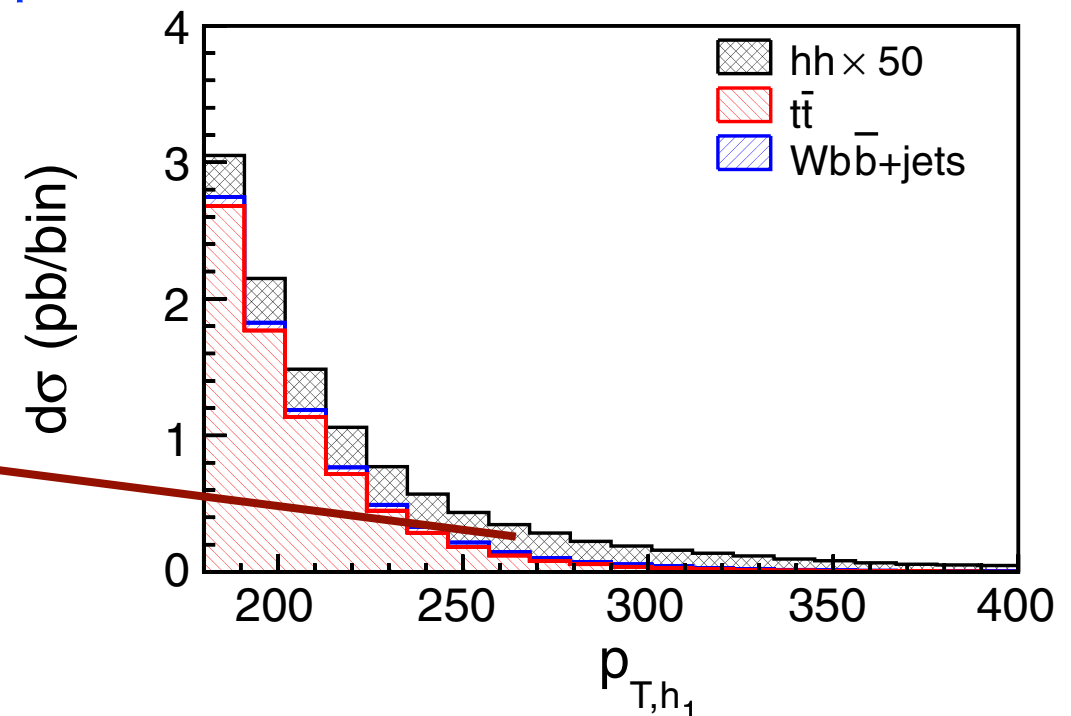
~20% correction

However, tagging $H \rightarrow b\bar{b}$ typically requires jet substructure techniques!

High p_T to suppress QCD backgrounds

Validity of HEFT?

Papaefstathiou, LLY, Zurita: 1209.1489



Higgs pair at NLO with top-mass dependence

A highly non-trivial calculation!

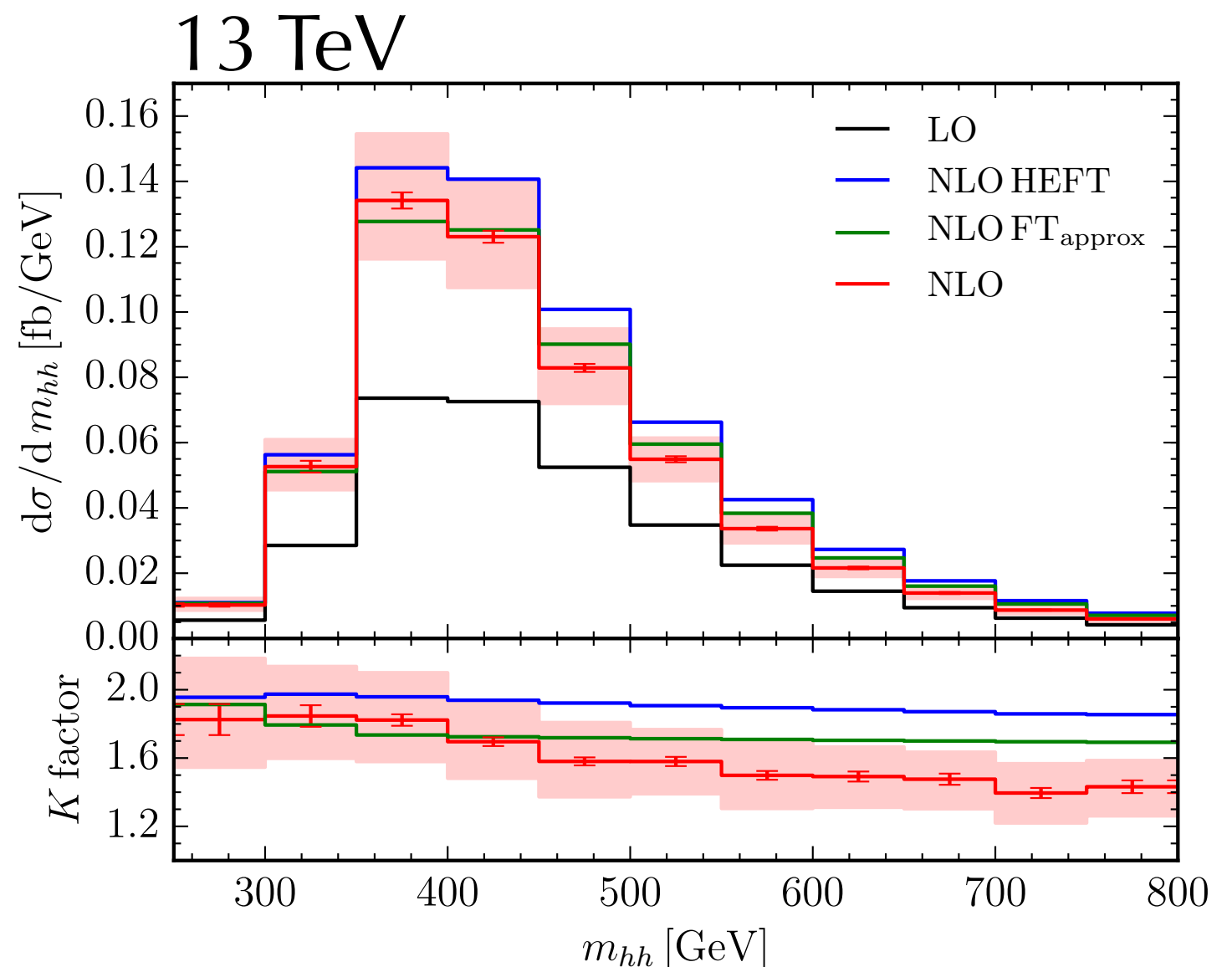
Borowka, Greiner, Heinrich et al.: 1604.06447

$$\sigma^{\text{NLO}} = 27.80^{+13.8\%}_{-12.8\%} \text{ fb}$$

14% smaller than Born-improved HEFT result



Prospect of observing this process at LHC reduced!



Higgs self-coupling from ratios of cross sections

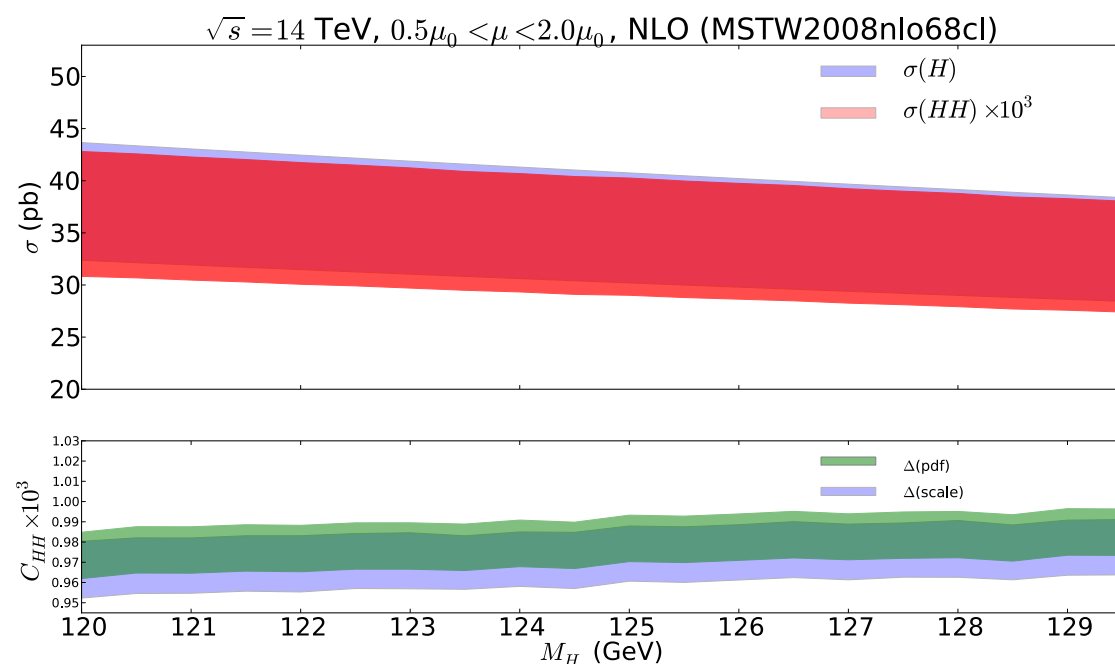
Goertz, Papaefstathiou, **LLY**, Zurita: 1301.3492

- NNLO corrections to HH cross section are **large**, but suffer from **uncertainties related to top-mass**
- May use **ratios of cross sections** to reduce theoretical uncertainties!

$$\rightarrow C_{HH} = \frac{\sigma(gg \rightarrow HH)}{\sigma(gg \rightarrow H)}$$



- Now known with exact top-mass dependence at NLO!
- Smaller higher order corrections and PDF/ α_s dependences
- An idea worth reconsidering (and extending) for SppC!



Summary

- * A new era for particle physics after Higgs discovery
- * Many things waiting to be explored (gauge couplings, Yukawa couplings, Higgs self-couplings, ...): requires CEPC and SppC beyond LHC!
- * Precision $\sigma(e^+e^- \rightarrow ZH)$: fundamental theoretical input for CEPC
- * Precision observables to extract H_{tt} and HHH couplings at SppC

Thank you!