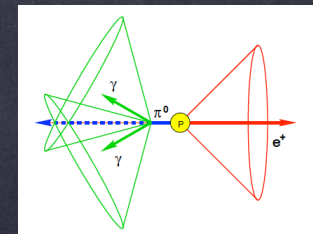


# New Physics and Proton Decay

Pavel Fileviez Perez



NNN16, Beijing, Nov 2016





# Main References

P. F. P., Physics Reports 597 (2015) 1

P. Nath, P. F. P., Physics Reports 441 (2007) 191

P. F. P., C. Murgui, Phys.Rev. D94 (2016) 7, 075014



# The Desert Hypothesis in Particle Physics

L  
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**B and L Violation:**

Seesaw Camel

$$\frac{c}{\Lambda^2} QQQQL \quad (\tau_p > 10^{32-34} \text{ years} \implies \Lambda > 10^{15} \text{ GeV})$$

$$p \rightarrow e^+ \gamma$$

P. Fileviez Perez

Standard Model

$$\Lambda_{\text{Weak}} \sim 100 \text{ GeV}$$

GUTs, Strings ?

$$\Lambda \sim 10^{15-19} \text{ GeV}$$



## Unity of All Elementary-Particle Forces

Howard Georgi\* and S. L. Glashow

*Lyman Laboratory of Physics, Harvard University, Cambridge, Massachusetts 02138*

(Received 10 January 1974)

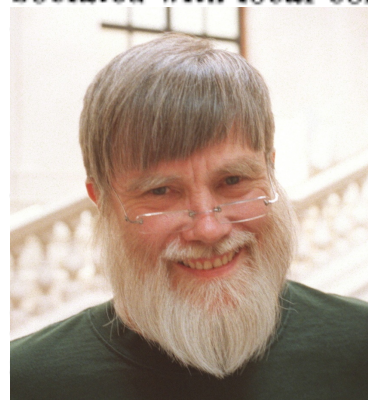
Strong, electromagnetic, and weak forces are conjectured to arise from a single fundamental interaction based on the gauge group SU(5).

We present a series of hypotheses and speculations leading inescapably to the conclusion that SU(5) is the gauge group of the world—that all elementary particle forces (strong, weak, and electromagnetic) are different manifestations of the same fundamental interaction involving a single coupling strength, the fine-structure constant. Our hypotheses may be wrong and our speculations idle, but the uniqueness and simplicity of our scheme are reasons enough that it be taken seriously.

Our starting point is the assumption that *weak and electromagnetic forces are mediated by the vector bosons of a gauge-invariant theory with spontaneous symmetry breaking*. A model describing the interactions of leptons using the gauge group  $SU(2) \otimes U(1)$  was first proposed by Glashow, and was improved by Weinberg and Salam who incorporated spontaneous symmetry breaking.<sup>1</sup> This scheme can also describe had-

of the GIM mechanism with the notion of colored quarks<sup>4</sup> keeps the successes of the quark model and gives an important bonus: Lepton and hadron anomalies cancel so that the theory of weak and electromagnetic interactions is renormalizable.<sup>5</sup>

The next step is to include strong interactions. We assume that *strong interactions are mediated by an octet of neutral vector gauge gluons associated with local color SU(3) symmetry*, and



actions are associated with a non-Abelian theory, they may be asymptotically free.<sup>9</sup>

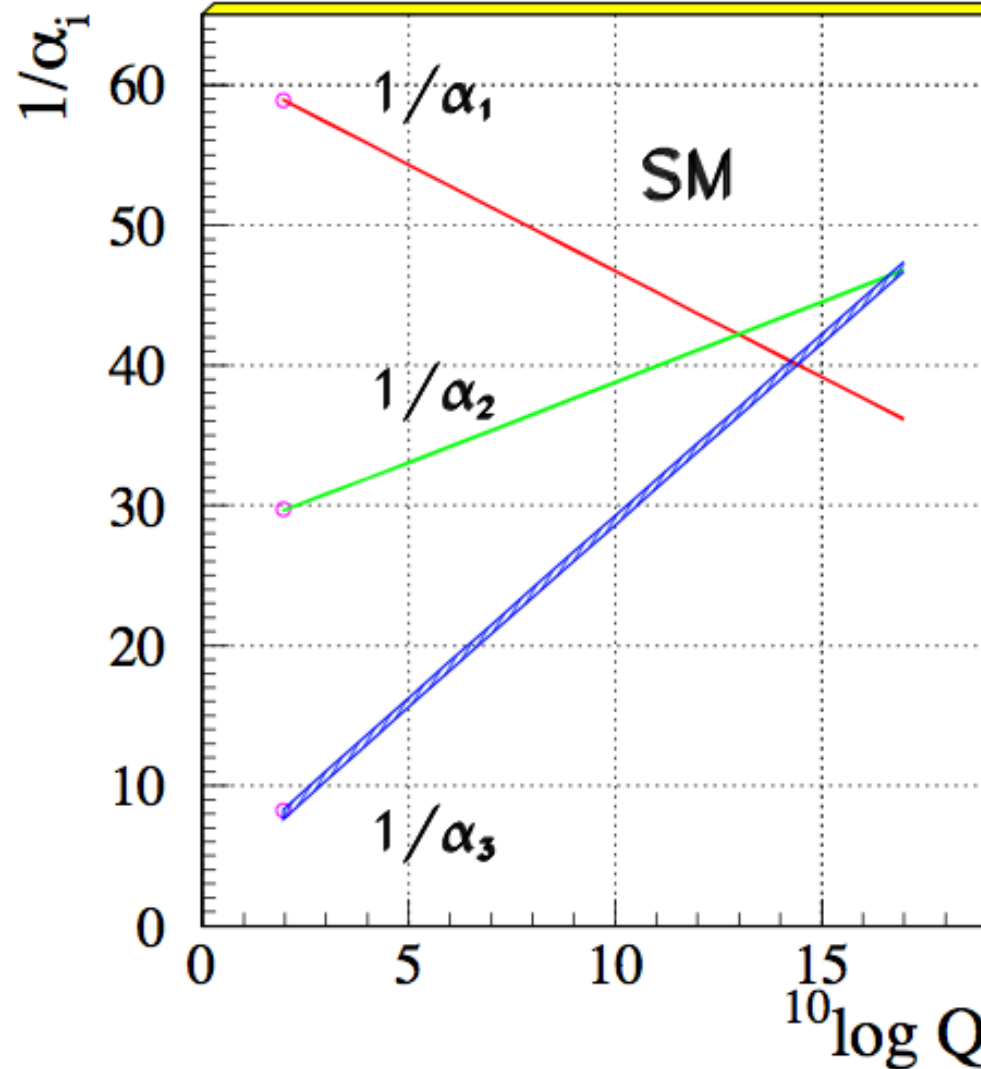


# Running of the gauge couplings in the SM

Lyman L

We present strong interaction breakdown at Planck mass

The scaling observed in deep inelastic scattering suggests that the strong interaction becomes asymptotically free at high energies. Asymptotic freedom is the explanation: The gluon self-energy is finite as the value of the renormalization scale  $\mu$  is GeV or larger, but becomes small, through the perturbative calculation<sup>2</sup> a fit was [in a color SU(3) model]  $\mu \simeq 2$  GeV.



ttt 02138

which make the strong, and weak interactions asymptotically free almost the

is. In order to supersede, Georgi and Glashow<sup>7</sup> that some theory. The simple gauge group unification of electromagnetic interaction. However, as we shall show, the success in an understanding of the obvious disparity between the strong and the weak and electromagnetic interactions at ordinary energies is present in this paper calculation of such

effects. This will lead us to an estimate of the



# The Desert Hypothesis and Supersymmetry

LOW  
SCALE

HIGH  
SCALE

P. Fileviez Perez

**B and L Violation:**

Seesaw Camel

$$\frac{c_5}{\Lambda} \hat{Q}\hat{Q}\hat{Q}\hat{L} \quad (\tau_p > 10^{32-34} \text{ years} \implies \Lambda > 10^{16-17} \text{ GeV})$$

What about the  $\hat{L}\hat{H}_u, \hat{L}\hat{L}\hat{e}^c, \hat{Q}\hat{L}\hat{d}^c$  and  $\hat{u}^c\hat{d}^c\hat{d}^c$  interactions?

MSSM

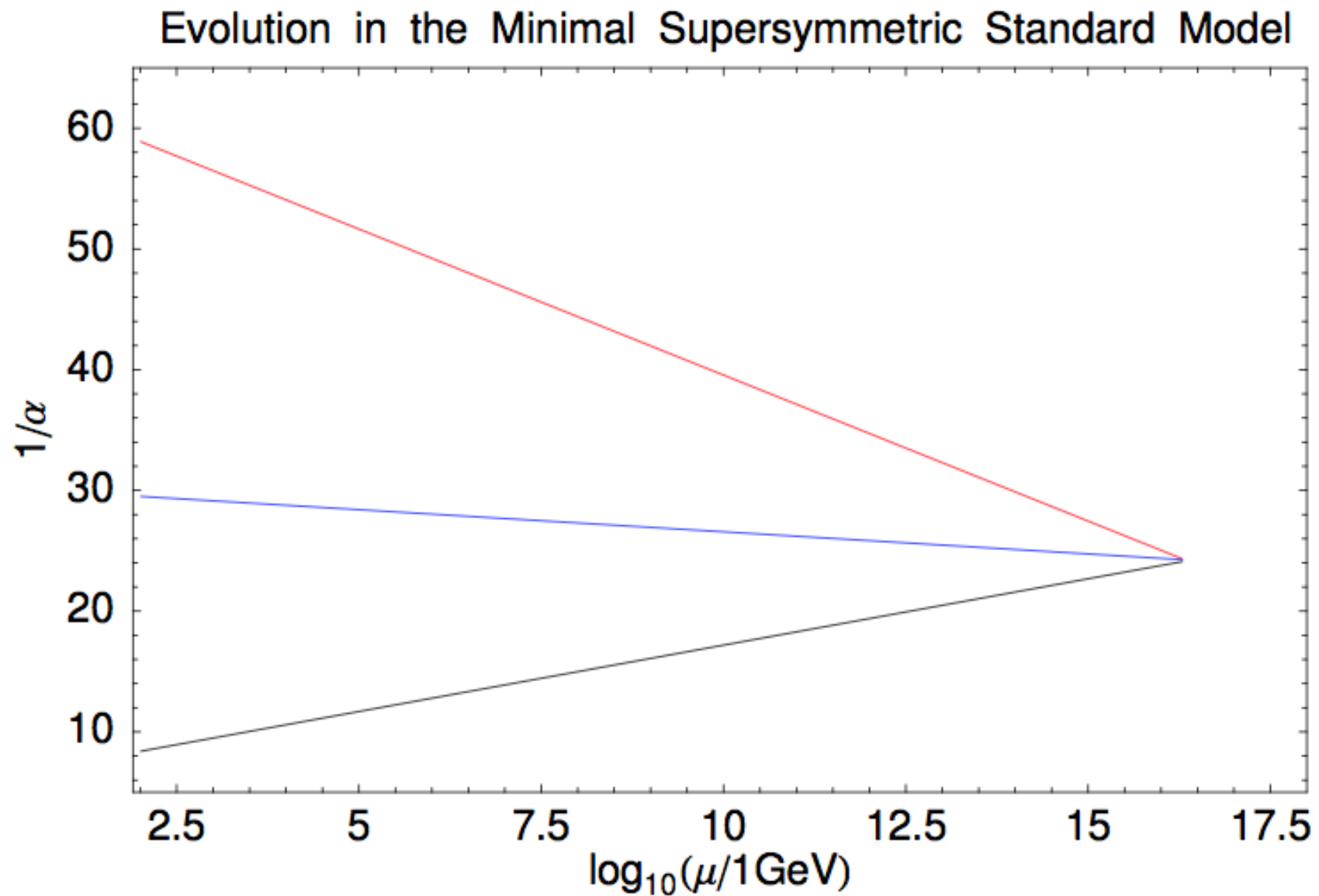
Unification of Gauge Couplings !

GUTs, Strings ?

10 TeV ? 100 TeV ? ...



## Running of the gauge couplings in the MSSM





# The Desert Hypothesis in Particle Physics

P.F.P., M.B.Wise, 2009

B and L Violation:

Seesaw Camel

$$\frac{c}{\Lambda^2} QQQQL \quad (\tau_p > 10^{32-34} \text{ years} \implies \Lambda > 10^{15} \text{ GeV})$$

Stable Proton

P. Fileviez Perez

Standard Model

$$\Lambda_{\text{Weak}} \sim 100 \text{ GeV}$$

GUTs, Strings ?

$$\Lambda \sim 10^{15-19} \text{ GeV}$$



# Aim

Physics beyond the SM vs. Proton Decay

```
graph TD; A([Physics beyond the SM vs. Proton Decay]) --> B([Proton Decay in Grand Unified Theories]); A --> C([Maybe the proton is stable and the great Desert is not needed]);
```

**Proton Decay in Grand  
Unified Theories**

**Maybe the proton is *stable*  
and the great Desert is not  
needed**

Main focus of this talk !



# Outline

- Introduction
- Grand Unification vs. Proton Decay
- Nucleon Decay in Supersymmetry
- Summary



# Introduction



# Proton Stability

**SM:** In the renormalizable SM the proton is stable !  
Baryon number is a global symmetry broken at the quantum level by SU(2) instanton processes in 3 units ( $\Delta B = 3$ )

**Matter Unification:** In theories where quarks and leptons are unified one could have B violating interactions which mediate proton decay (Pati, Salam, 1973)

$$p \rightarrow \gamma e^+, \pi^0 e^+, \dots (\Delta B = 1)$$

**GUTs:** In grand unified theories ( SU(5), SO(10),...) B is **explicitly** broken at the high scale and generically one predicts proton decay.

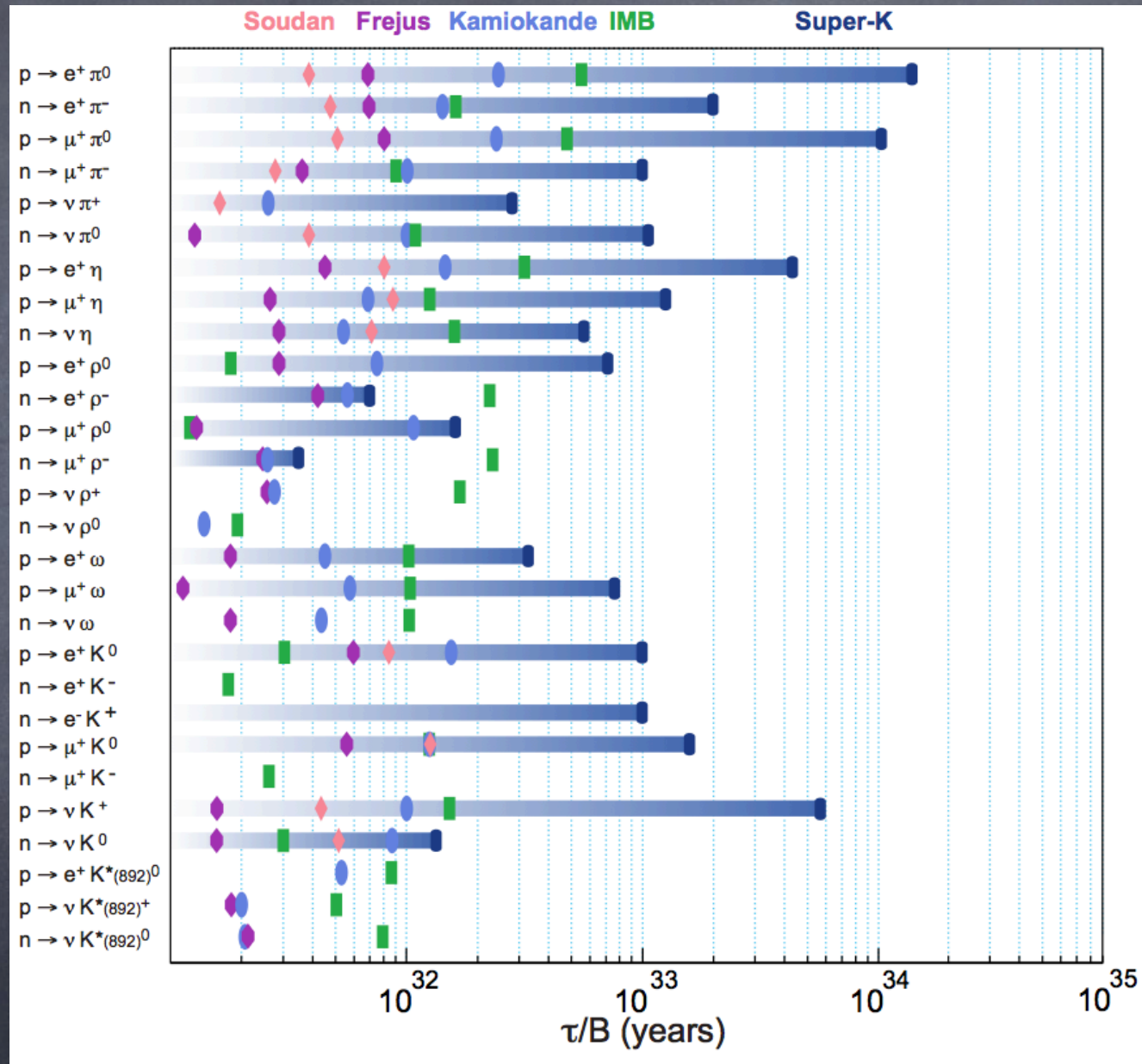
**SUSY:** In the MSSM B and L are explicitly broken at the renormalizable level by RpV interactions and generically one predicts proton decay.

$$R = (-1)^{3(B-L)+2S}$$

P. Fileviez Perez



# Experimental Results: $\Delta B = 1, \Delta L = \text{odd}$





# Grand Unification vs. Proton Decay



# Non-SUSY GUTs

**d=6 gauge:**

$$\begin{aligned}
 O(e_\alpha^C, d_\beta) &= c(e_\alpha^C, d_\beta) \epsilon_{ijk} \overline{u_i^C} \gamma^\mu u_j \overline{e_\alpha^C} \gamma_\mu d_{k\beta}, \\
 O(e_\alpha, d_\beta^C) &= c(e_\alpha, d_\beta^C) \epsilon_{ijk} \overline{u_i^C} \gamma^\mu u_j \overline{d_{k\beta}^C} \gamma_\mu e_\alpha, \\
 O(\nu_l, d_\alpha, d_\beta^C) &= c(\nu_l, d_\alpha, d_\beta^C) \epsilon_{ijk} \overline{u_i^C} \gamma^\mu d_{j\alpha} \overline{d_{k\beta}^C} \gamma_\mu \nu_l
 \end{aligned}$$

after integrating out the superheavy gauge bosons.

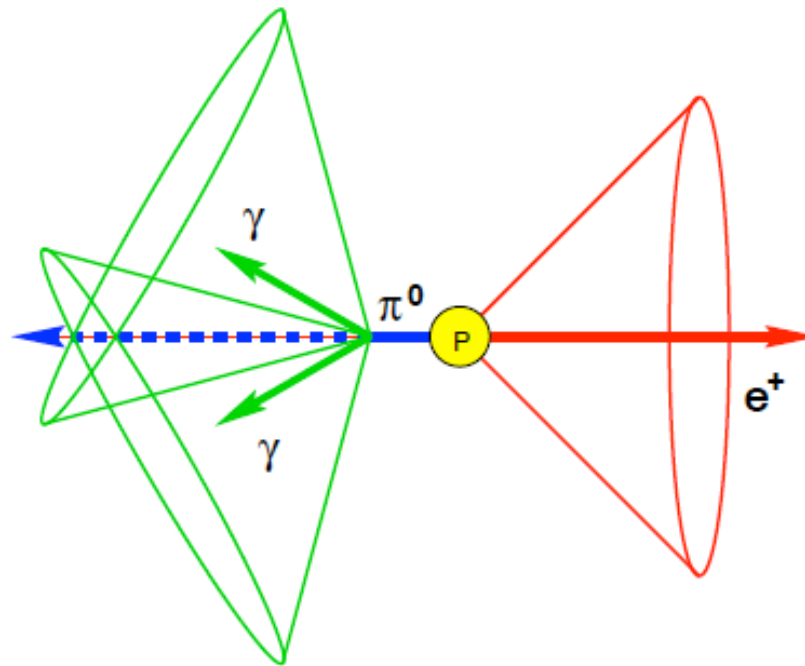
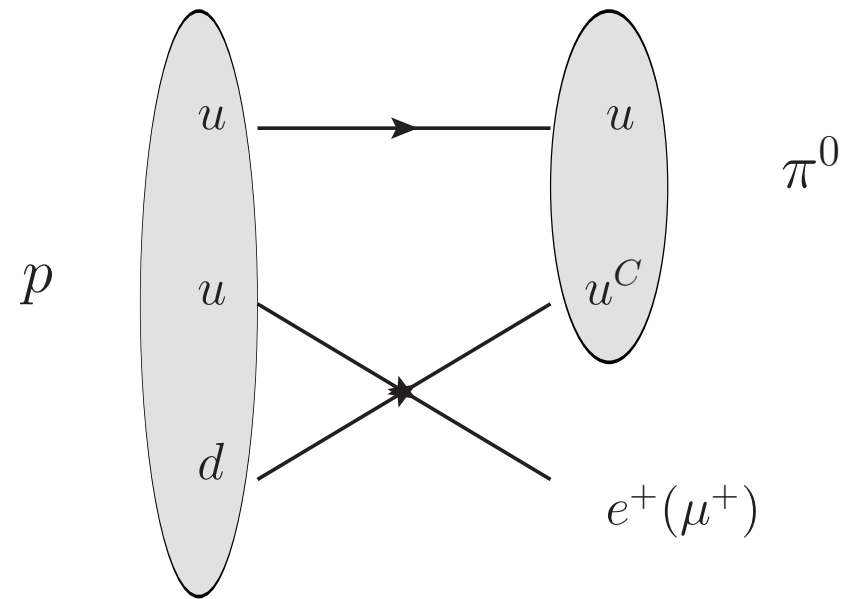
$$c(e^c, d), c(e, d^c) \ \& \ c(\nu, d, d^c) \ \sim \ g_{GUT}^2 / M_V^2$$

$$M_V > 10^{14-15} \text{ GeV} \quad \text{naive !}$$

in agreement with gauge coupling unification at the high scale.

**Unfortunately, the values of the Wilson coefficients can change dramatically in different models !**





# Georgi-Glashow Model

Georgi, Glashow, Phys.Rev.Lett.32:438-441,1974

$$G_{SM} = SU(3) \otimes SU(2) \otimes U(1) \subset SU(5)$$

$$\alpha_3 \quad \alpha_2 \quad \alpha_1 \quad \rightarrow \quad \alpha_5$$

Matter Assignment

$$\bar{\mathbf{5}} = \begin{pmatrix} d_1^C \\ d_2^C \\ d_3^C \\ e \\ -\nu \end{pmatrix}_L \quad \mathbf{10} = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & u_3^C & -u_2^C & u_1 & d_1 \\ -u_3^C & 0 & u_1^C & u_2 & u_2 \\ u_2^C & -u_1^C & 0 & u_3 & d_3 \\ -u_1 & -u_2 & -u_3 & 0 & e^C \\ -d_1 & -d_2 & -d_3 & -e^C & 0 \end{pmatrix}_L$$

Higgs Bosons

$$\mathbf{5}_H = \begin{pmatrix} T_1 \\ T_2 \\ T_3 \\ H^+ \\ H^0 \end{pmatrix} \quad \mathbf{24}_H = \begin{pmatrix} \Sigma_8 & \Sigma_{(3,2)} \\ \Sigma_{(\bar{3},2)} & \Sigma_3 \end{pmatrix} + \frac{1}{2\sqrt{15}} \begin{pmatrix} 2 & 0 \\ 0 & -3 \end{pmatrix} \Sigma_{24}$$



# Georgi-Glashow Model

Georgi, Glashow, Phys.Rev.Lett.32:438-441,1974

$$A_\mu = \frac{1}{2}\lambda_a A_\mu^a = \frac{1}{2} \begin{pmatrix} G_\mu, B_\mu & \textcolor{red}{V}_\mu \\ \textcolor{red}{V}_\mu^* & W_\mu, B_\mu \end{pmatrix} \quad V_\mu = \sqrt{2} \begin{pmatrix} X_{1\mu} & Y_{1\mu} \\ X_{2\mu} & Y_{2\mu} \\ X_{3\mu} & Y_{3\mu} \end{pmatrix}$$

– New B violating interactions → **THE PROTON IS UNSTABLE !!!**

$$\bar{5}^\dagger \gamma^0 i \gamma^\mu D_\mu \bar{5} \rightarrow g_5 \overline{(d^C)}_L \gamma^\mu (\textcolor{blue}{X}_\mu e_L - \textcolor{blue}{Y}_\mu \nu_L) / \sqrt{2}$$

$$\text{Tr} \bar{10} i \gamma^\mu D_\mu 10 \rightarrow g_5 \overline{(e^C)}_L \gamma^\mu (\textcolor{blue}{X}_\mu d_L - \textcolor{blue}{Y}_\mu u_L) / \sqrt{2} +$$

$$g_5 \left( \bar{u}_L \gamma^\mu \textcolor{blue}{X}_\mu (u^C)_L + \bar{d}_L \gamma^\mu \textcolor{blue}{Y}_\mu (u^C)_L \right) / \sqrt{2}$$



$$\mathcal{O}(e_\alpha^C, d_\beta) = k_1^2 \textcolor{red}{c}(e_\alpha^C, d_\beta) \epsilon_{ijk} \overline{u}_i^C \gamma^\mu u_j \overline{e}_\alpha^C \gamma_\mu d_{k\beta}$$

## Why the Georgi-Glashow model is ruled out ?

- The unification of gauge couplings in disagreement with the experiments
- $M_E = M_D^T$  at the GUT scale in disagreement with the experiments
- $M_\nu = 0$

## What are the simplest realistic extensions of the Georgi-Glashow Model ?

**Type II-SU(5)**

I. Dorsner, [P. F. P.](#), Nucl. Phys. B723 (2005)53

**Type III-SU(5)**

B. Bajc, G. Senjanovic, Nucl. Phys. B723 (2005)53

**Minimal Renormalizable SU(5)**

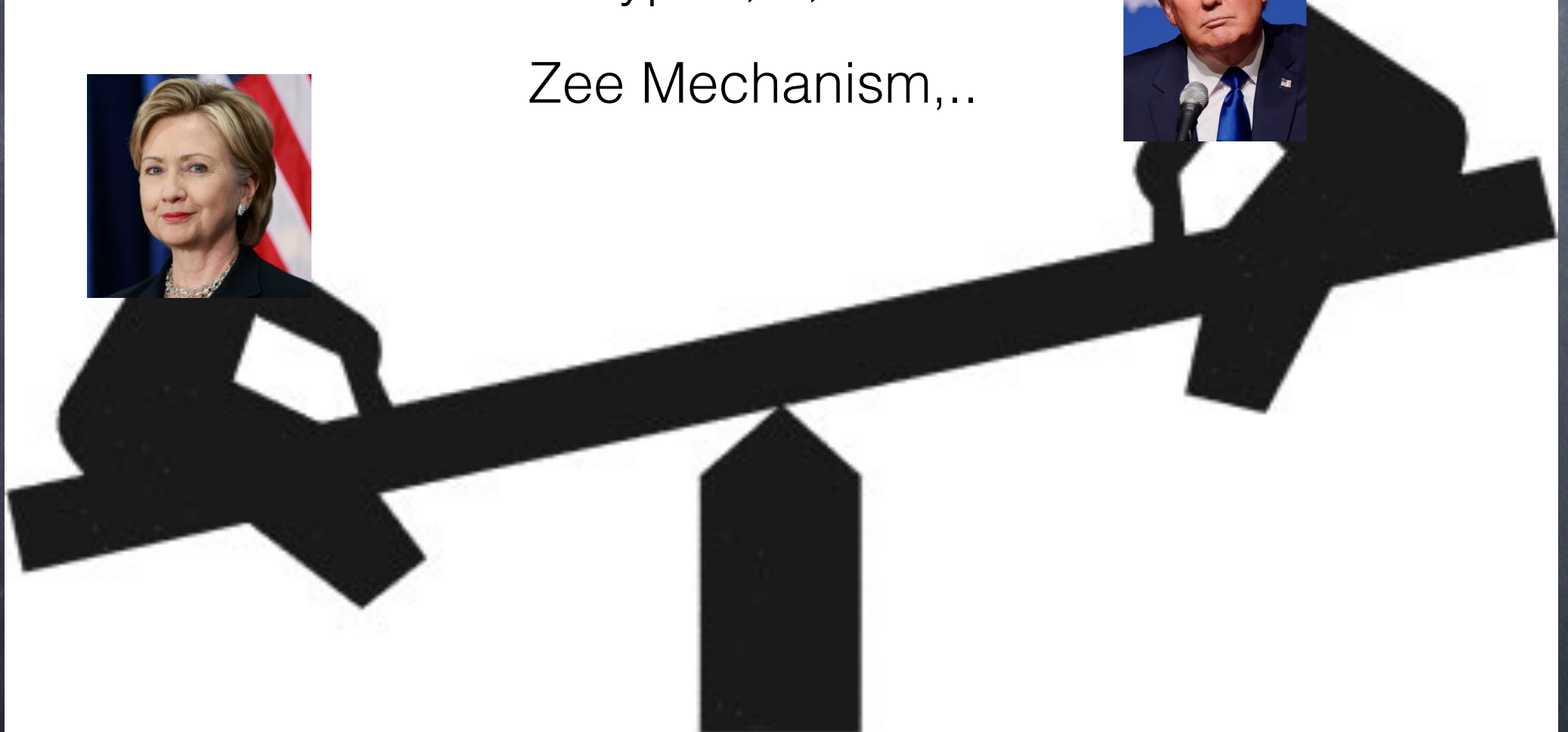
[P. F. P.](#), C. Murgui, Phys.Rev. D94 (2016) 7, 075014



# Seesaw Mechanism

Type I, II, III

Zee Mechanism,..



## Type II-SU(5)

Matter:  $\bar{5} = (d^C, e, \nu)$ ,  $10 = (u^C, Q, e^C)$

Higgs Sector:  $5_H, 24_H, 15_H$

$$\tau_p < 2 \times 10^{36} \text{ years}$$

$$15 = \underbrace{(1, 3, 1)}_{\Delta} \oplus \underbrace{(3, 2, 1/6)}_{\Phi_b} \oplus \underbrace{(6, 1, -2/3)}_{\Phi_c}$$

Neutrino Mass through the Type II seesaw mechanism:

$$Y_\nu \bar{5} \bar{5} 15_H + \mu 5_H^* 5_H^* 15_H + \text{h.c.}$$

$$M_\nu = Y_\nu \langle \Delta \rangle = Y_\nu \mu v_W^2 / M_\Delta^2$$

Charged Fermion Masses:  $Y_E \neq Y_D^T$  higher-dimensional operators

Unification: O.K. [The theory predicts a light scalar leptoquark  \$\Phi\_b\$](#)

See also: I. Dorsner, [P.F.P](#), R. González Felipe, Nucl.Phys.B747:312-327,2006

I. Dorsner, [P.F.P](#), G. Rodrigo, Phys. Rev. D75 (2007) 125007



# Type III seesaw and Non-SUSY Unification

B. Bajc, G. Senjanović, hep-ph/0612029

Matter:  $\bar{5} = (d^C, e, \nu)$ ,  $10 = (u^C, Q, e^C)$ ,  $24$

Higgs Sector:  $5_H, 24_H$

$$\tau_p < 10^{36-37} \text{ years}$$

$$24 = \underbrace{(8, 1, 0)}_{\rho_8} \oplus \underbrace{(1, 3, 0)}_{\rho_3} \oplus \underbrace{(3, 2, -5/6)}_{\rho(3,2)} \oplus \underbrace{(\bar{3}, 2, 5/6)}_{\rho(\bar{3},2)} \oplus \underbrace{(1, 1, 0)}_{\rho_0}$$

*Neutrino Mass:*

$$Y_0^i \bar{5}_i 24 5_H + \frac{1}{\Lambda} \bar{5}_i \times (Y_1^i 24 24_H + Y_2^i 24_H 24 + Y_3^i \text{Tr}(24 24_H)) 5_H$$

Charged Fermion Masses:  $Y_E \neq Y_D^T$  using higher-dimensional operators

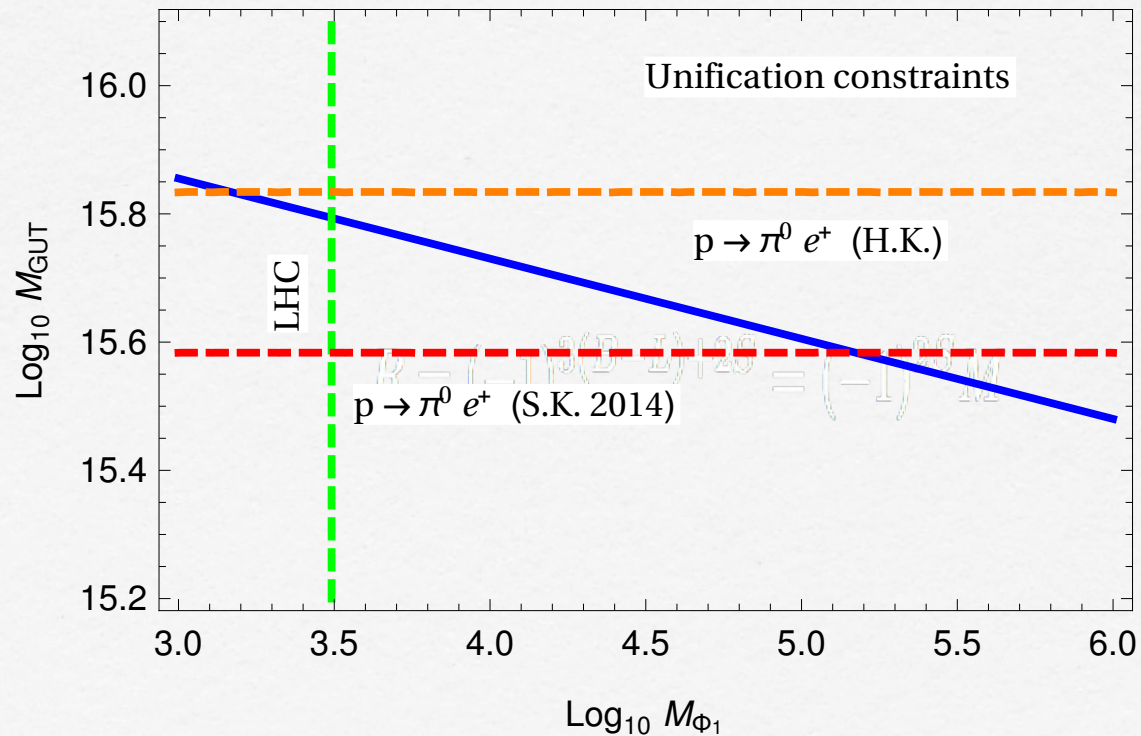
Unification: O.K. The theory predicts a light fermionic SU(2) triplet  $\rho_3$

See also: I. Dorsner, P.F.P, JHEP 0706:029,2007.

# Renormalizable $SU(5)$

P. F. P. C. Murgui, Phys.Rev. D94 (2016) 7, 075014

$5_H, 24_H, 45_H$



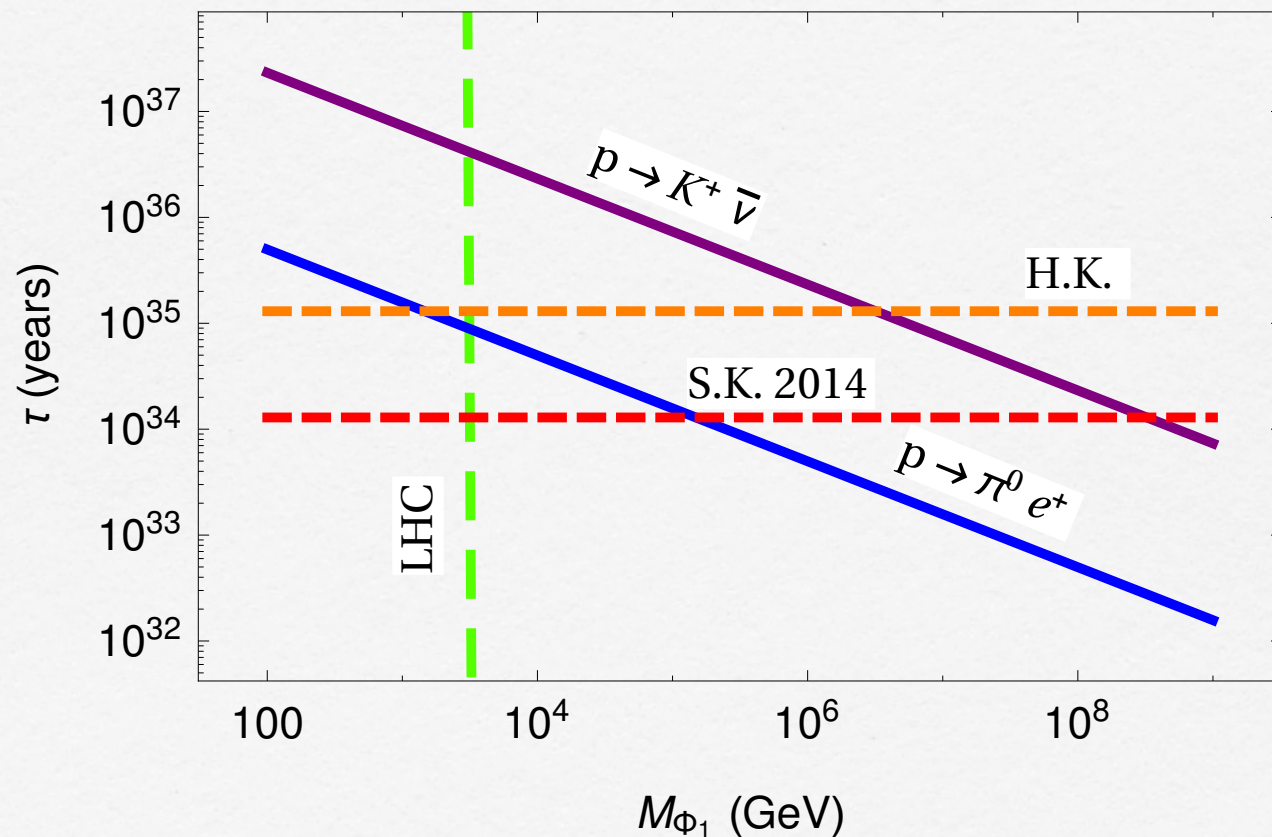
$45_H \subset \Phi_1 \sim (8, 2, 1/2)$

P. Fileviez Perez



# Proton decay in Minimal Renormalizable SU(5)

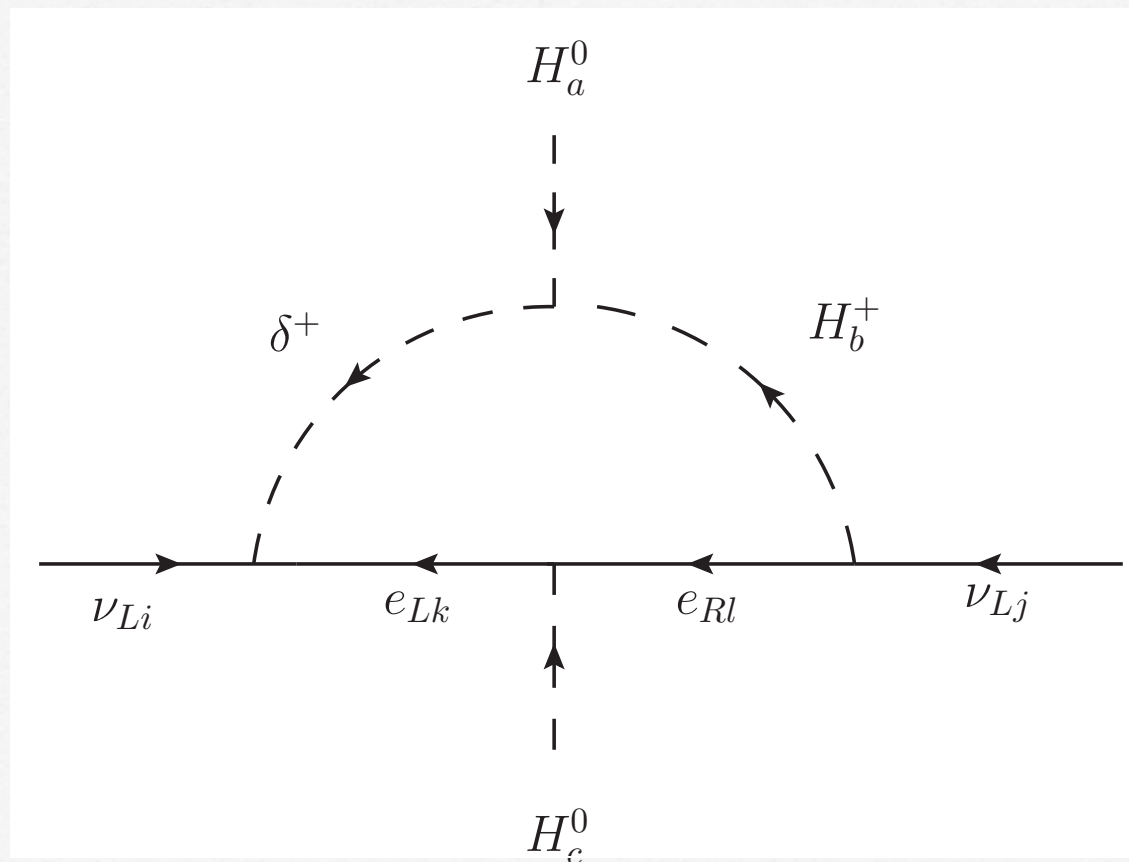
P. F. P., C. Murgui, Phys.Rev. D94 (2016) 7, 075014



$$45_H \subset \Phi_1 \sim (8, 2, 1/2)$$

# Neutrino Mass - Minimal Renormalizable SU(5)

P. F. P., C. Murgui, Phys.Rev. D94 (2016) 7, 075014





# Nucleon Decay in Supersymmetry


## MSSM Interactions

$$\mathcal{W}_{RpC} = Y_u Q H_u u^c + Y_d Q H_d d^c + Y_e L H_d e^c + \mu H_u H_d$$

$$\mathcal{W}_{RpV} = \epsilon L H_u + \lambda L L e^c + \lambda' Q L d^c + \lambda'' u^c d^c d^c$$

$$R = (-1)^{3(B-L)+2S} = (-1)^{2S} M$$

**LSP**  $\tilde{\chi}_1^0 = (\tilde{B}, \tilde{W}, \tilde{H}_u^0, \tilde{H}_d^0)$   **Cold Dark Matter !**

$\nu_i$   **Massless Neutrinos !**



## B and L violation in the MSSM

$$\mathcal{W}_{RpV} = \epsilon LH_u + \lambda LLe^c + \lambda' QLd^c + \lambda'' u^c d^c d^c$$

$$\mathcal{W}_{RPC}^5 = \frac{\lambda_\nu}{\Lambda} LLH_u H_u + \frac{\lambda_L}{\Lambda} QQQQL + \frac{\lambda_R}{\Lambda} u^c d^c u^c e^c$$

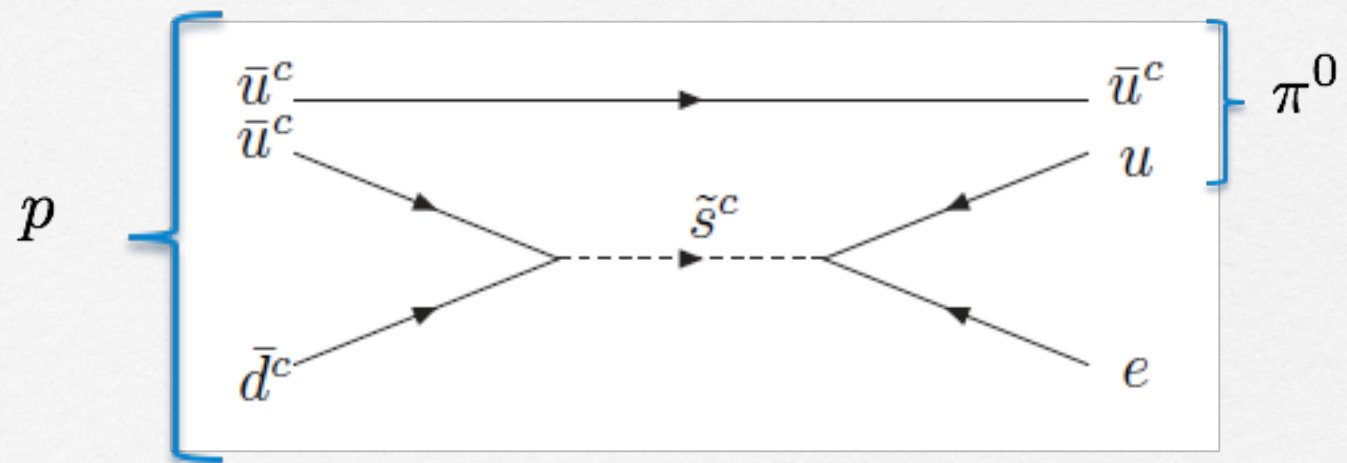
**Missing energy at the LHC (DM) vs Neutrino Masses ?**

See e.g. P. Nath, [P. Fileviez Perez](#), Physics Reports 441:191,2007

## Proton Decay and M-Parity

$$\lambda' QLd^c$$

$$\lambda'' u^c d^c d^c$$



Channel :  $\tau_{p \rightarrow \pi^0 e^+} > 10^{33}$  years

$$M_{\tilde{q}} \sim 10^3 \text{ GeV}$$



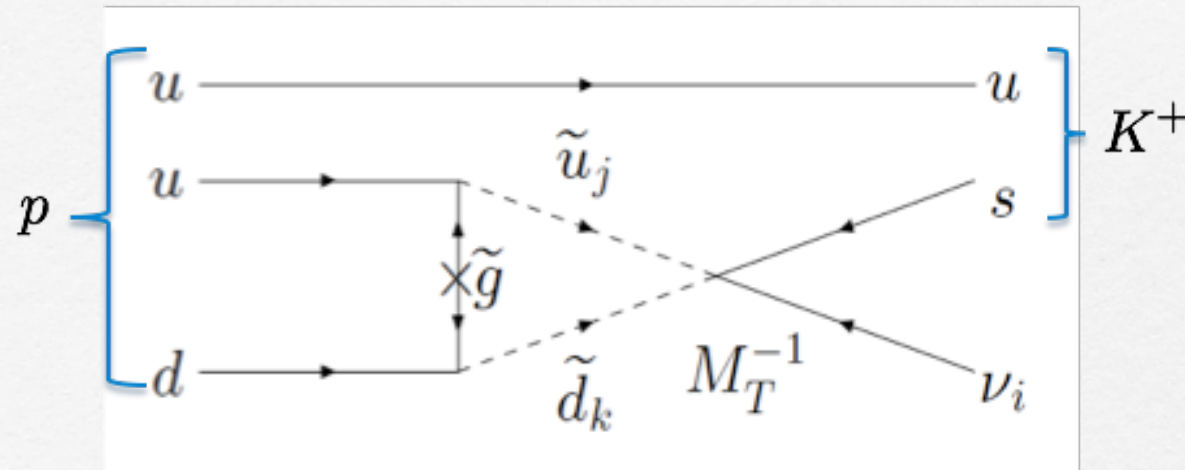
$$\tau_4 \sim 10^{-20} \text{ years}$$



## $d=5$ operators

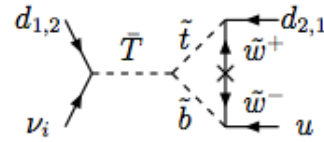
Example:  $p \rightarrow K^+ \bar{\nu}$  ( $\tau > 2.3 \times 10^{33}$  years)

$$\frac{\lambda_L}{M_T} QQQ L$$

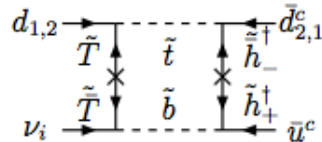


$$M_T > 10^{17} \text{ GeV (NAIVE)}$$

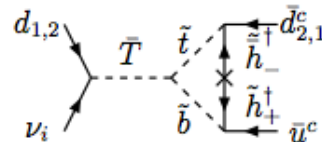
Dimopoulos, Raby, Wilczek; Arnowitt,  
Chamseddine, Nath; Goto, Nihei; Lucas, Raby;  
Bajc, P.F.P., Senjanovic



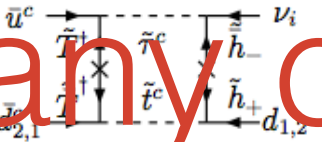
$$\propto (D^T \underline{C} N)_{1i,2i} (U^T \tilde{D}^*)_{13} (\tilde{D}^T \underline{A} \tilde{U})_{33} (\tilde{U}^\dagger D)_{32,31}$$



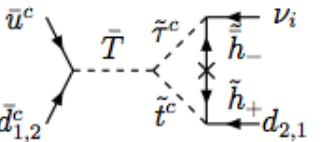
$$\propto (D^T \underline{A} \tilde{U})_{13,23} (\tilde{U}^\dagger Y_D^* D_c^*)_{32,31} (U_c^\dagger Y_U^\dagger \tilde{D}^*)_{13} (\tilde{D}^T \underline{C} N)_{3i}$$



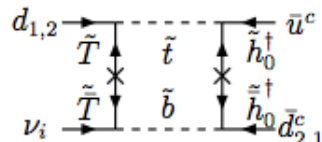
$$\propto (D^T \underline{C} N)_{1i,2i} (U_c^\dagger Y_U^\dagger \tilde{D}^*)_{13} (\tilde{D}^T \underline{A} \tilde{U})_{33} (\tilde{U}^\dagger Y_D^* D_c^*)_{32,31}$$



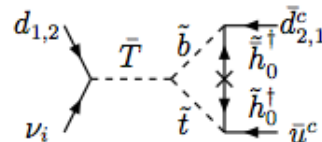
$$\propto (U_c^\dagger \underline{D}^* D_c^*)_{11,12} (D^T Y_U \tilde{U}_c)_{23,13} (\tilde{U}_c^\dagger \underline{B}^* \tilde{E}_c^*)_{33} (\tilde{E}_c^T Y_E N)_{3i}$$



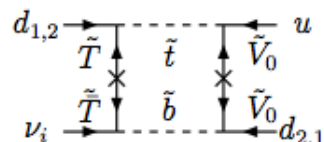
$$\propto (U_c^\dagger \underline{D}^* D_c^*)_{11,12} (D^T Y_U \tilde{U}_c)_{23,13} (\tilde{U}_c^\dagger \underline{B}^* \tilde{E}_c^*)_{33} (\tilde{E}_c^T Y_E N)_{3i}$$



$$\propto (D^T \underline{A} \tilde{U})_{13,23} (\tilde{U}^\dagger Y_U^* U_c^*)_{31} (D_c^\dagger Y_D^\dagger \tilde{D}^*)_{23,13} (\tilde{D}^T \underline{C} N)_{3i}$$



$$\propto (D^T \underline{C} N)_{1i,2i} (U_c^\dagger Y_U^\dagger \tilde{U}^*)_{13} (\tilde{U}^T \underline{A} \tilde{D})_{33} (\tilde{D}^\dagger Y_D^* D_c^*)_{32,31}$$



$$\propto (D^T \underline{A} \tilde{U})_{13,23} (\tilde{U}^\dagger U)_{31} (D^T \tilde{D}^*)_{23,13} (\tilde{D}^T \underline{C} N)_{3i}$$

Many contributions !



# Minimal Supersymmetric $SU(5)$

S. Dimopoulos and H. Georgi NPB(1981); N. Sakai Z. Phys. C (1981)

Chiral Superfields:  $\hat{\mathbf{5}}_i, \hat{\mathbf{10}}_i, \hat{\mathbf{5}}_H, \hat{\mathbf{5}}_H, \hat{\mathbf{24}}_H$

Vector Superfields:  $\hat{\mathbf{24}}_G$

$$\hat{\mathbf{10}} = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & U_3^C & -U_2^C & U_1 & D_1 \\ -U_3^C & 0 & U_1^C & U_2 & U_2 \\ U_2^C & -U_1^C & 0 & U_3 & D_3 \\ -U_1 & -U_2 & -U_3 & 0 & E^C \\ -D_1 & -D_2 & -D_3 & -E^C & 0 \end{pmatrix}_L$$

$$\hat{\mathbf{5}} = \begin{pmatrix} D_1^C \\ D_2^C \\ D_3^C \\ E \\ -N \end{pmatrix}_L \quad \hat{\mathbf{5}}_H = \begin{pmatrix} T_1 \\ T_2 \\ T_3 \\ H_2^+ \\ H_2^0 \end{pmatrix} \quad \hat{\mathbf{5}}_H = \begin{pmatrix} \bar{T}_1 \\ \bar{T}_2 \\ \bar{T}_3 \\ H_1^- \\ -H_1^0 \end{pmatrix}$$

$$\hat{\mathbf{24}}_H = \begin{pmatrix} \Sigma_8 & \Sigma_{(3,2)} \\ \Sigma_{(\bar{3},2)} & \Sigma_3 \end{pmatrix} + \frac{1}{2\sqrt{15}} \begin{pmatrix} 2 & 0 \\ 0 & -3 \end{pmatrix} \Sigma_{24}$$

- Unification: O.K.
- $M_E = M_D^T$  ( $b - \tau$  unification O.K.)
- $M_\nu = 0$  if R-parity is conserved

The Minimal Renormalizable SUSY  $SU(5)$  is ruled out !!

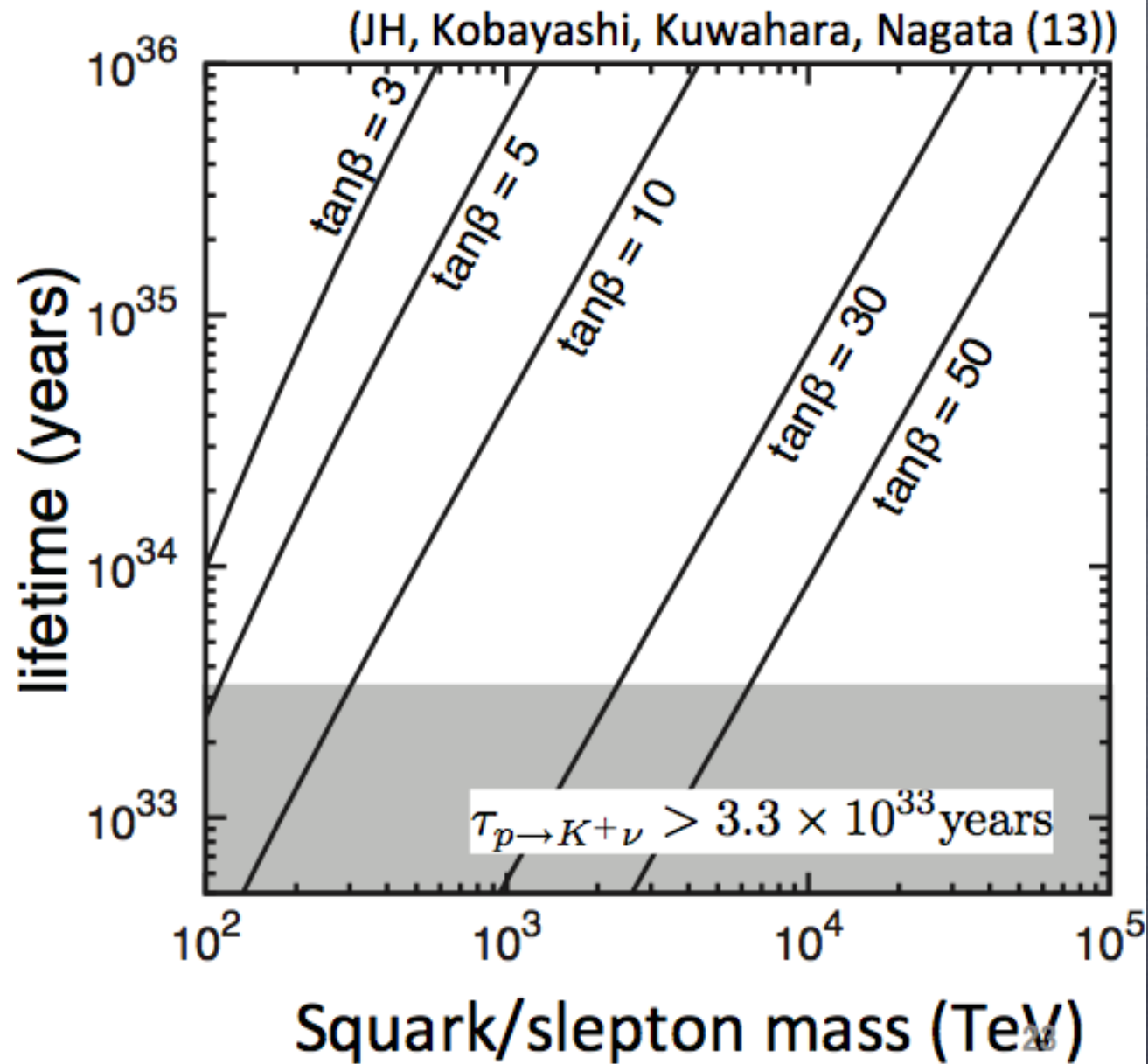
The non-renormalizable SUSY  $SU(5)$  model is OK,  
see: Bajc, P.F.P., Senjanovic, 0210374; 0204311.

Unfortunately, the proton decay lifetime cannot be predicted in SUSY because one needs to know the full spectrum of supersymmetric particles !

In minimal SUSY  $SU(5)$ , assuming  $m_{\tilde{q}, \tilde{l}} \sim 1$  TeV:  $M_T > 10^{17}$  GeV

Note that in general we do not know  $(\tilde{U}^\dagger U)_{j1}(\tilde{D}^\dagger D)_{k1}!!!$





J. Hisano @ BLV2013

# SO(10) GUTs and proton decay

$$16_F, 10_H, 126_H, 210_H, \dots$$

These theories are considered very appealing because the fermions are unified in the 16 representation. However, one has different breaking scales and it is very difficult to predict the lifetime of the proton.

For recent studies see:

K.S. Babu, S. Khan, 2015

H. Kolesova, M. Malinsky, 2014

Mohapatra et al, 2012

Babu, Pati, Tavartkiladze, 2010



# Summary

P. Fileviez Perez

The idea of grand unification is one of the most appealing ideas we have for new physics.

One can predict the lifetime of the proton in the simplest non-supersymmetric grand unified theories.

The minimal renormalizable  $SU(5)$  predictions could be tested at Hyper-Kamiokande or other experiments.

More experimental effort is needed to search for proton decay in the near future. Young people, new ideas and new techniques are needed in this field.

非常感謝你

Fēicháng gǎnxiè nǐ