

# KLOE measurement of $Ke^2/K\mu^2$ and $K \rightarrow e\nu\gamma$

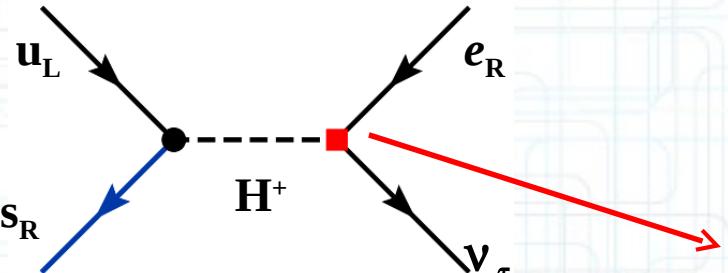
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for the KLOE collaboration

International Workshop on  $e^+e^-$  collisions from Phi to Psi  
Beijing, China – 13-16 October 2009

# NP potential of $R_K = \Gamma(K e 2) / \Gamma(K \mu 2)$

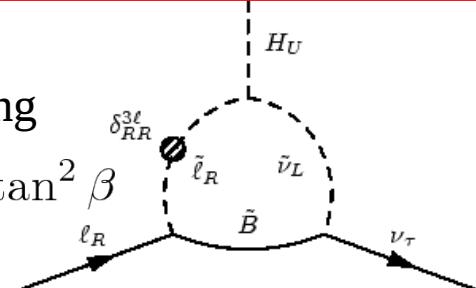
- SM prediction with 0.04% precision, benefits of cancellation of hadronic uncertainties (no  $f_K$ ):  $R_K = 2.477(1) \times 10^{-5}$  [Cirigliano-Rosell arXiv:0707:4464].
- Helicity suppression can boost NP [Masiero-Paradisi-Petronzio PRD74(2006)011701].



$$R_K^{\text{LFV}} \approx \frac{\Gamma(K \rightarrow e \bar{\nu}_e) + \Gamma(K \rightarrow e \bar{\nu}_\tau)}{\Gamma(K \rightarrow \mu \bar{\nu}_\mu)}$$

LFV from loop generates an effective  $e H^+ \bar{\nu}_\tau$  coupling

$$e H^+ \bar{\nu}_\tau \rightarrow \frac{g_2}{\sqrt{2}} \frac{m_\tau}{M_W} \Delta_R^{31} \tan^2 \beta$$



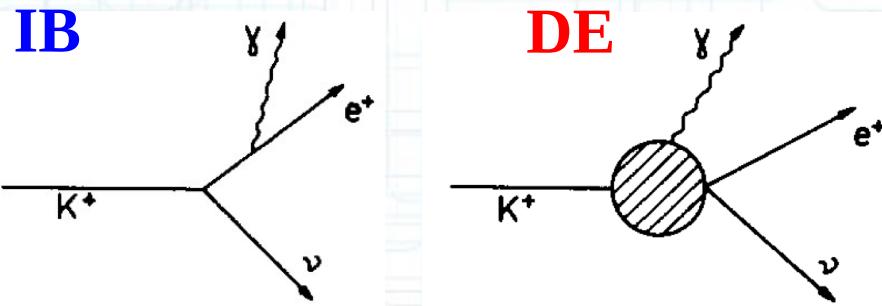
$$R_K^{\text{LFV}} \approx R_K^{\text{SM}} \left( 1 + \frac{m_K^4}{m_H^4} \frac{m_\tau^4}{m_e^4} |\Delta_R^{31}|^2 \tan^6 \beta \right)$$

LFV can give **O(1%) deviation from SM ( $\Delta_R^{31} \sim 5 \times 10^{-4}$ ,  $\tan \beta \sim 40$ ,  $m_H \sim 500 \text{ GeV}$ )**

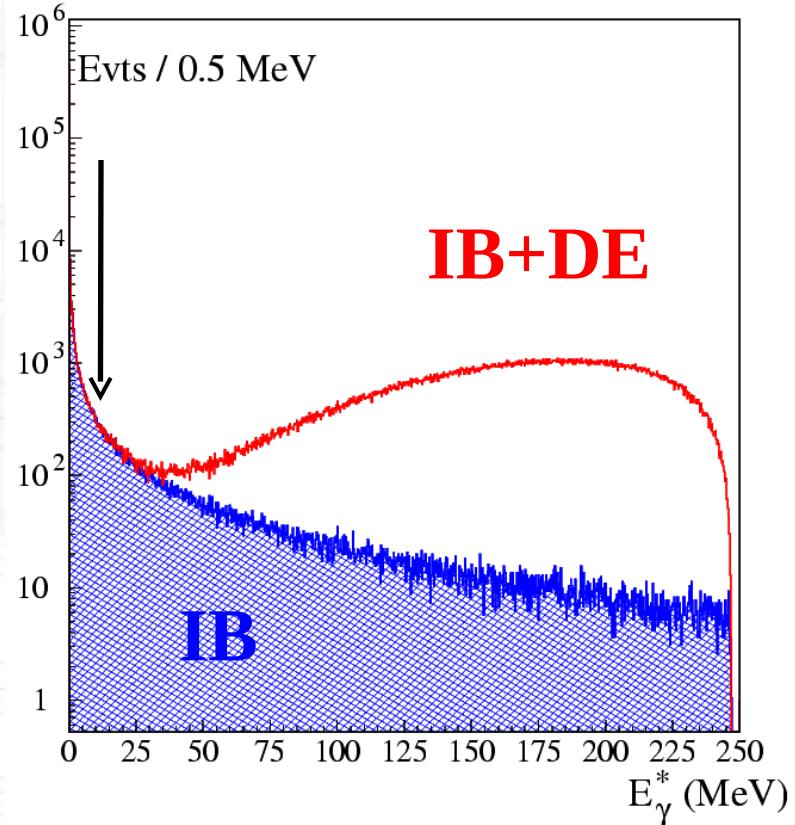
- Exp. accuracy on  $R_K$  (before KLOE and NA62 results) at 5% level.
- New measurements of  $R_K$  can be very interesting, **if error at 1% level or better**.

# Ke2( $\gamma$ ): signal definition

SM prediction is defined to be inclusive of **IB** (ignoring **DE** contributions).



From theory (ChPT) expect **DE** ~ **IB** for Ke2, but experimental knowledge is poor:  **$\delta DE/DE \sim 15\%$**



- Define as “signal” events with  $E_\gamma < 10$  MeV.
- Evaluating **IB** spectrum ( $O(\alpha)$ +resummation of leading logs) obtain a 0.0625(5) correction for the IB tail.
- Under 10 MeV, the **DE** contribution is expected to be negligible.

# Charged kaon at KLOE

$\phi$  decay at rest provides pure kaon beams of known momentum

$$p_K \sim 100 \text{ MeV}$$

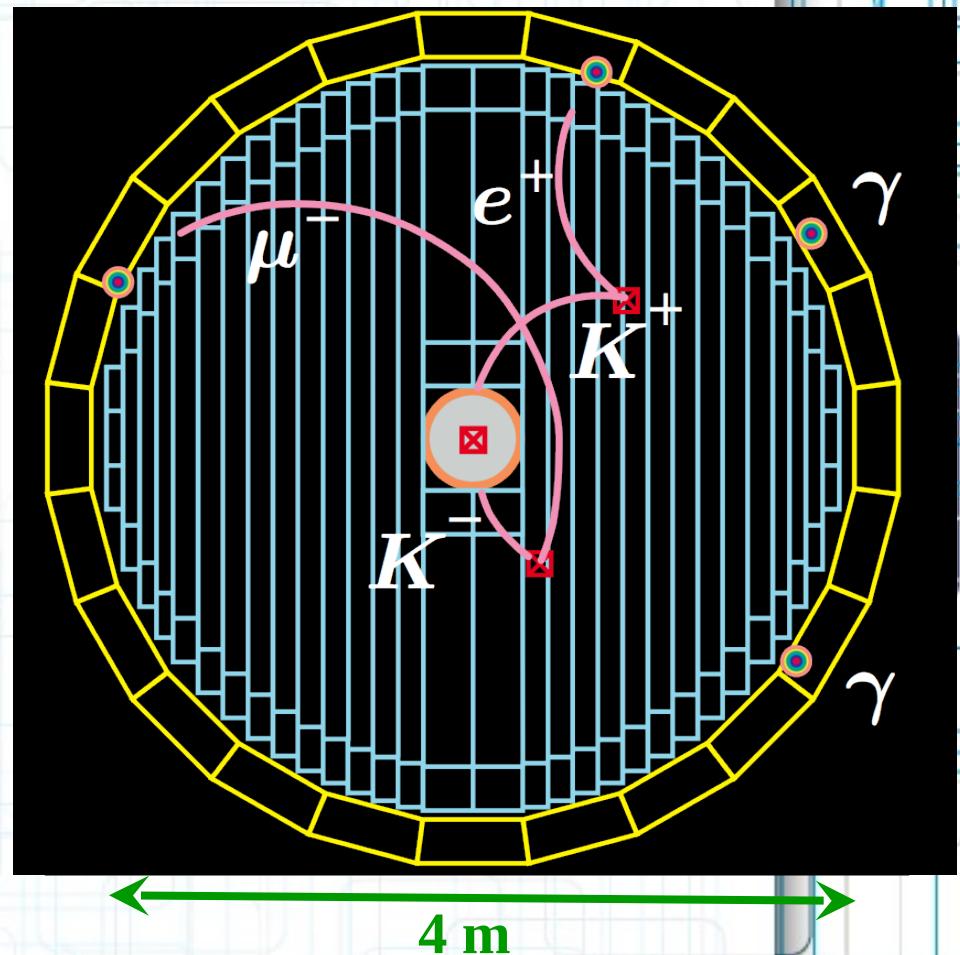
$\lambda \sim 90 \text{ cm}$  (**56% of  $K^\pm$  decay in DC**).

Kaon momentum measured (event by event) with 1 MeV resolution in DC.

Constraints from  $\phi$  2-body decay.

Particle ID with kinematics, energy deposition and ToF.

Tagging provides unbiased control samples for efficiency measurement.



# Analysis basic principles

$$R_K = \frac{N_{Ke2}}{N_{K\mu 2}} \left[ \frac{\varepsilon_{K\mu 2}^{\text{REC}}}{\varepsilon_{Ke2}^{\text{REC}}} C^{\text{TRG}} C^{\text{REC}} \right] \frac{1}{\epsilon^{\text{IB}}}$$

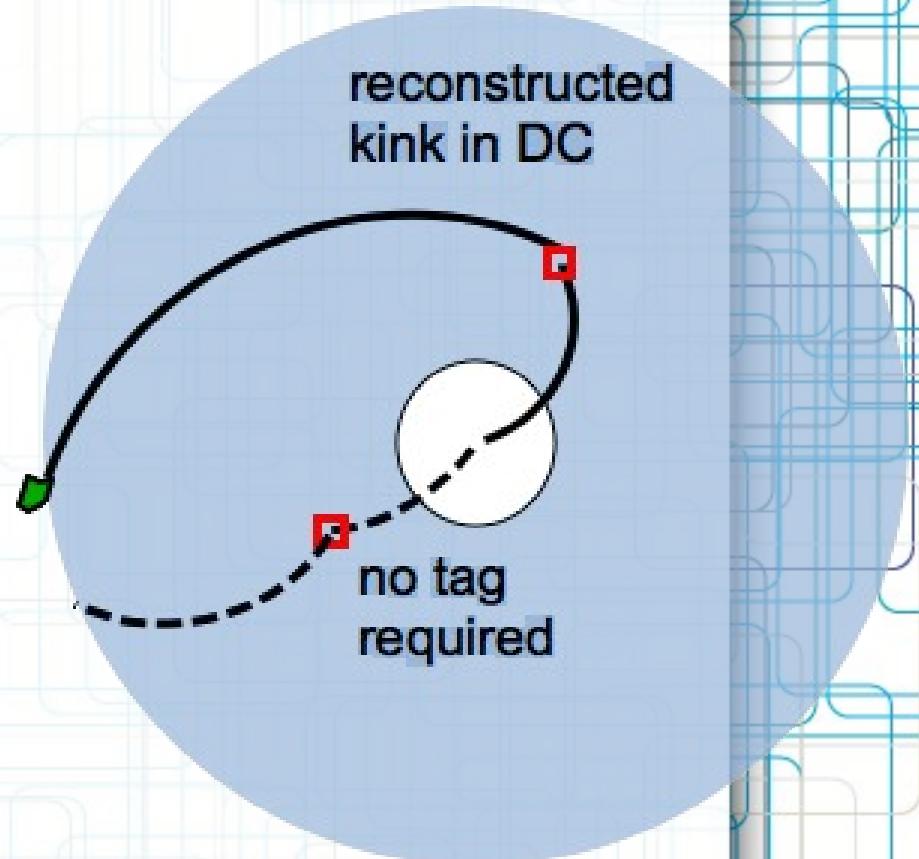
1) Select kinks in DC ( $\sim$  fiducial volume)

- K track from IP
- secondary with  $p_{\text{lep}} > 180$  MeV

for decays occurring in the FV;  
the reconstruction efficiency is  $\sim 51\%$ .

2) No tag required on the opposite  
“hemisphere” (as we usually do!)

$\rightarrow$  gain  **$\times 4$  of statistics**

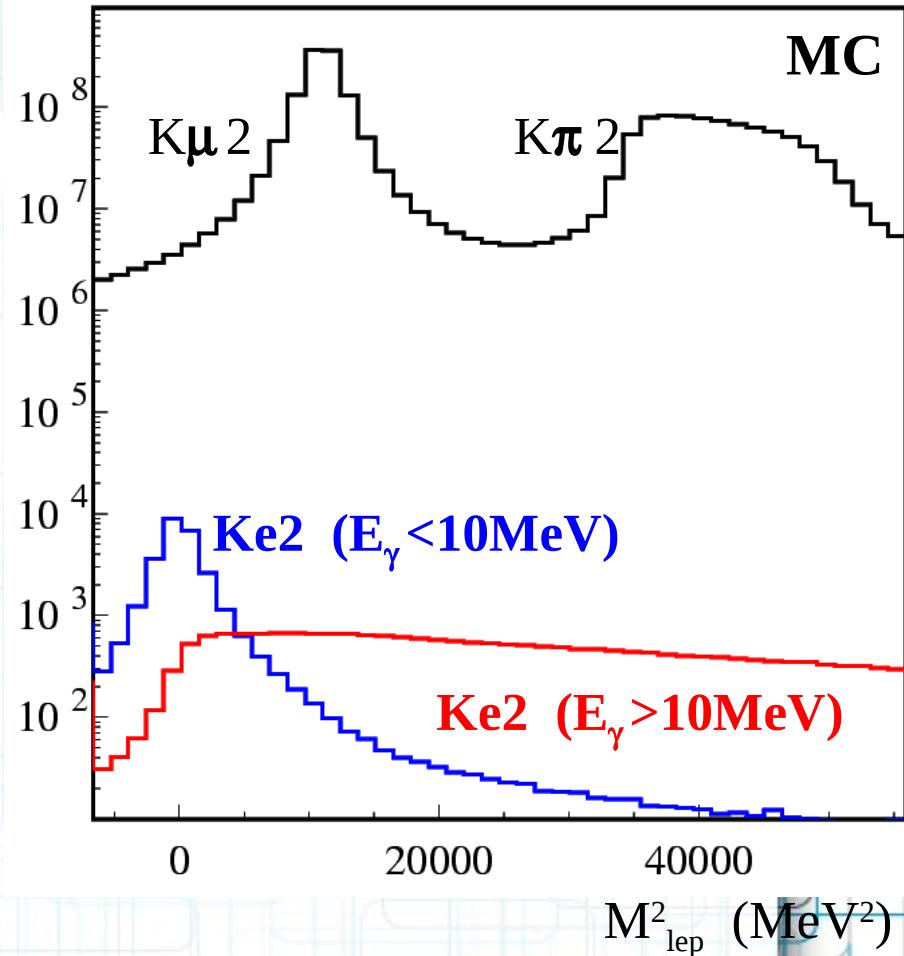


# Analysis basic principles

3) Exploit tracking of K and secondary: assuming  $m_\nu=0$  get  $M_{\text{lep}}^2$ :

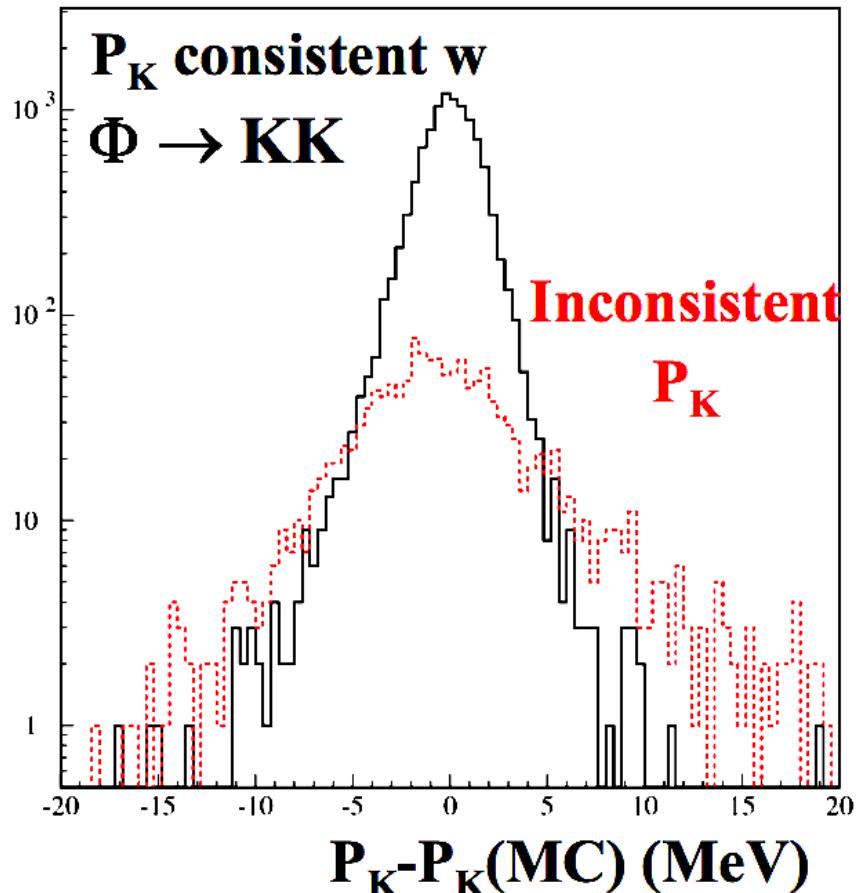
$$M_{\text{lep}}^2 = (E_K - p_{\text{miss}})^2 - p_{\text{lep}}^2.$$

Around  $M_{\text{lep}}^2=0$  we get  $\text{S/B} \sim 10^{-3}$ , mainly due to tails on the momentum resolution of  $K\mu 2$  events.



# Background rejection (track quality)

Background composition:  $K\mu 2$  events with bad  $p_K$ ,  $p_{\text{lep}}$ , or decay vertex position reconstruction



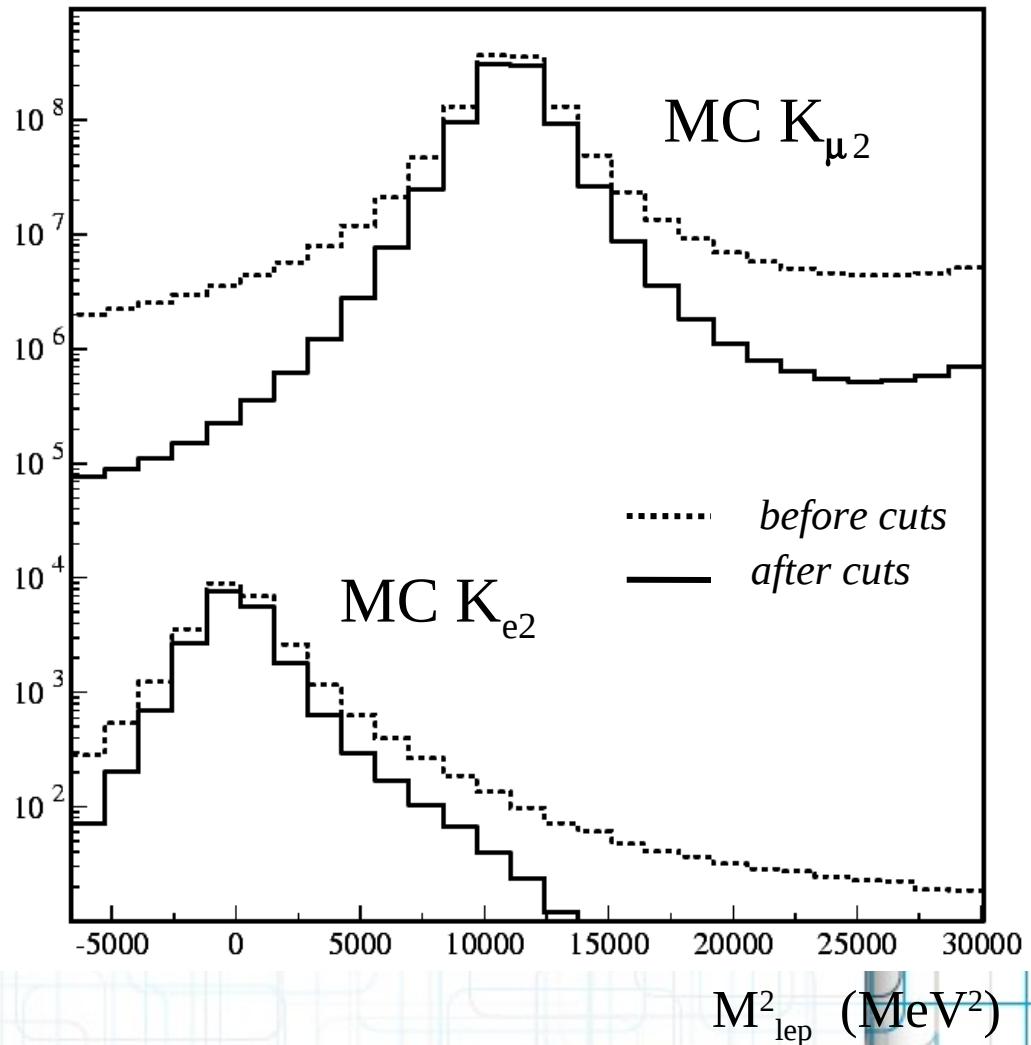
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- require good quality vertex and secondary track ( $\chi^2$ cut);
- reduce  $K_{\mu 2}$  tails cutting on the error on  $M_{\text{lept}}^2$  expected from track parameters;
- quality cuts for K: the kinematic of  $\Phi \rightarrow K^+ K^-$  2-body decay allows redundant  $p_K$  determinartion.

# Background rejection (track quality)

- after cuts, we accept  
~ 35% of decays in the FV
- most of Ke2 events lost  
have bad resolution
- **S/B ~ 1/20**, not enough!
- require the lepton track to  
be extrapolable to the  
calorimeter surface and to  
be associated to an energy  
release (cluster).



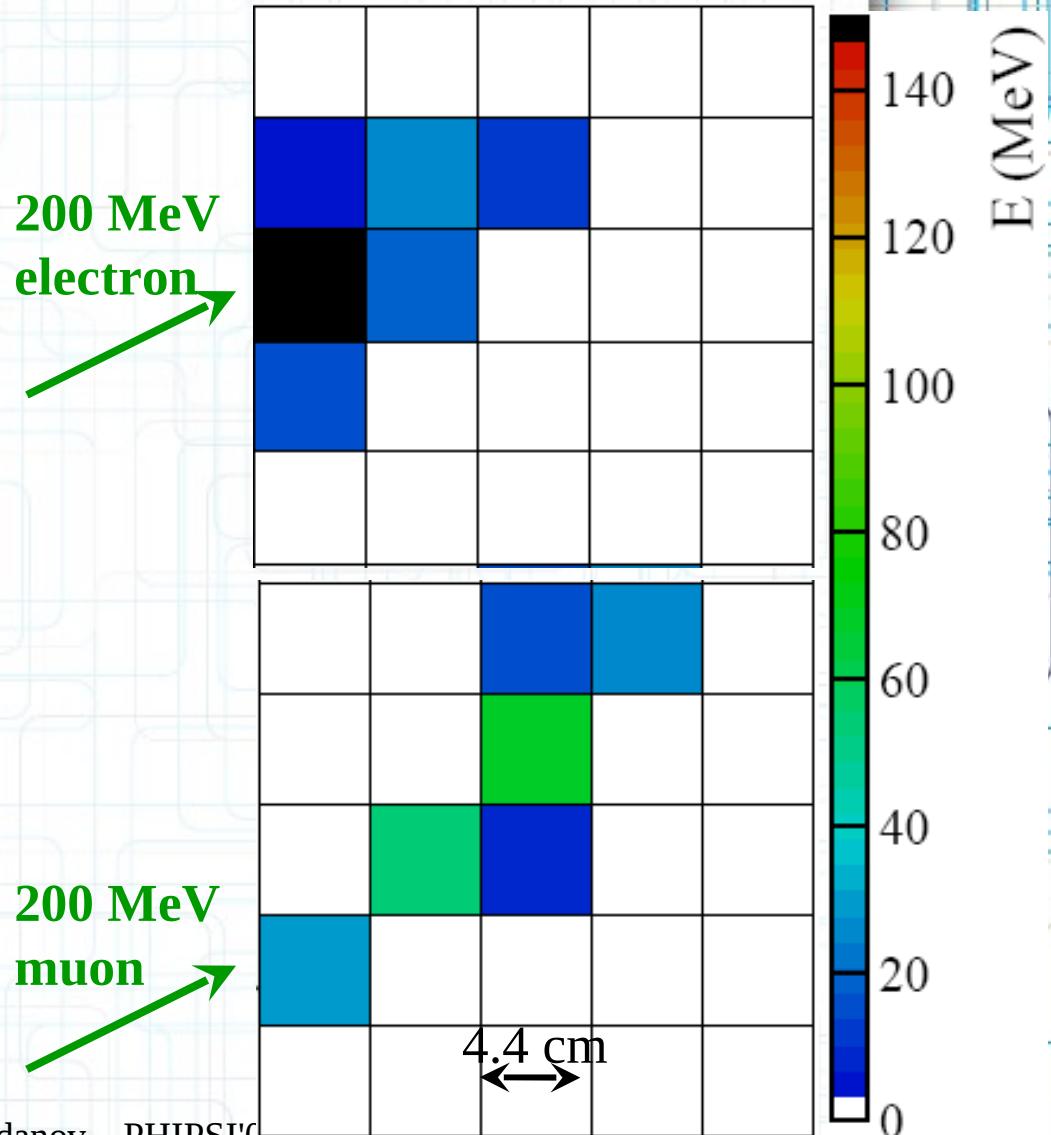
# Background rejection (PID)

1) Particle ID exploits EMC granularity (energy deposits into 5 layers in depth):

the energy distribution and the position along the shower axis of all cells associated to the cluster allow for  $e/\mu$  PID (define 11 descriptive variables).

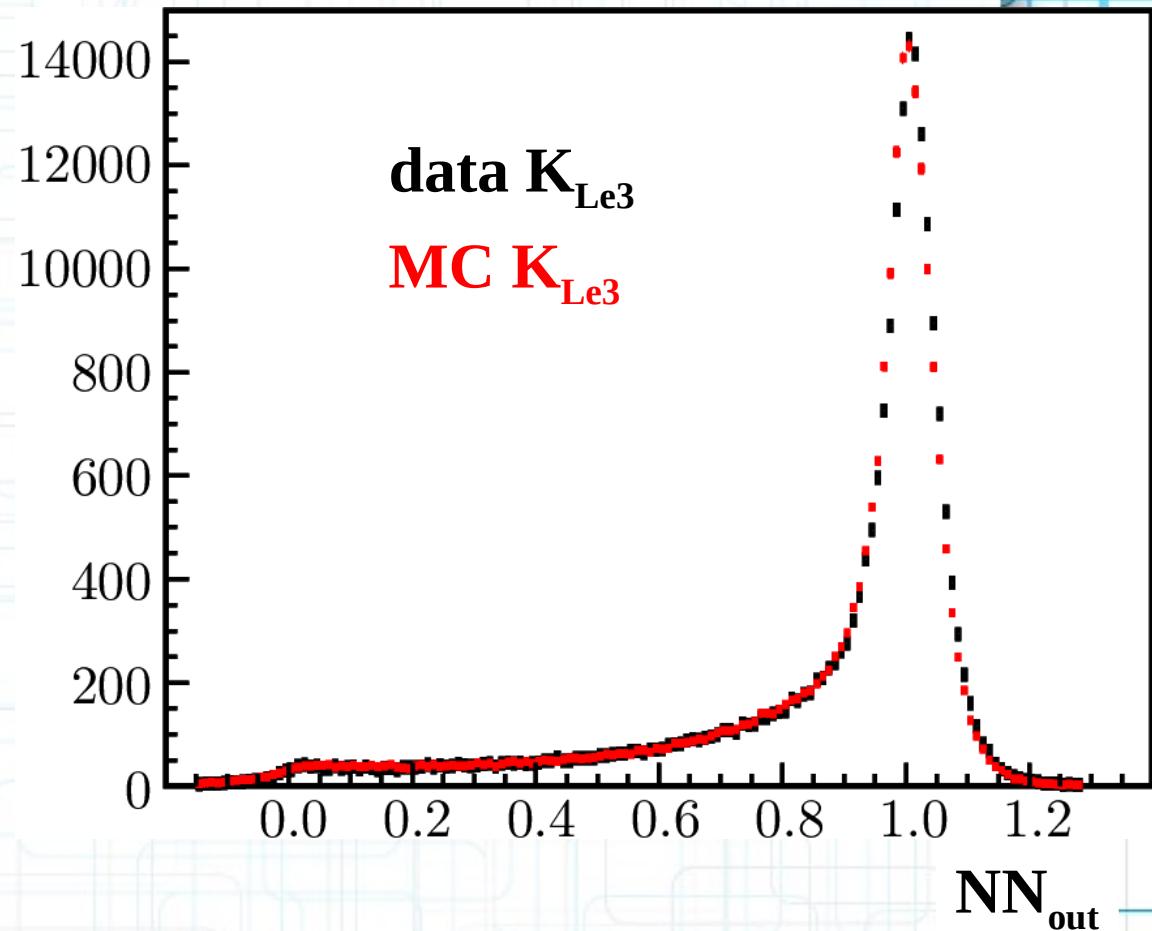
2) Add  $E/p$  and ToF.

3) Combine all information in a neural network (NN).



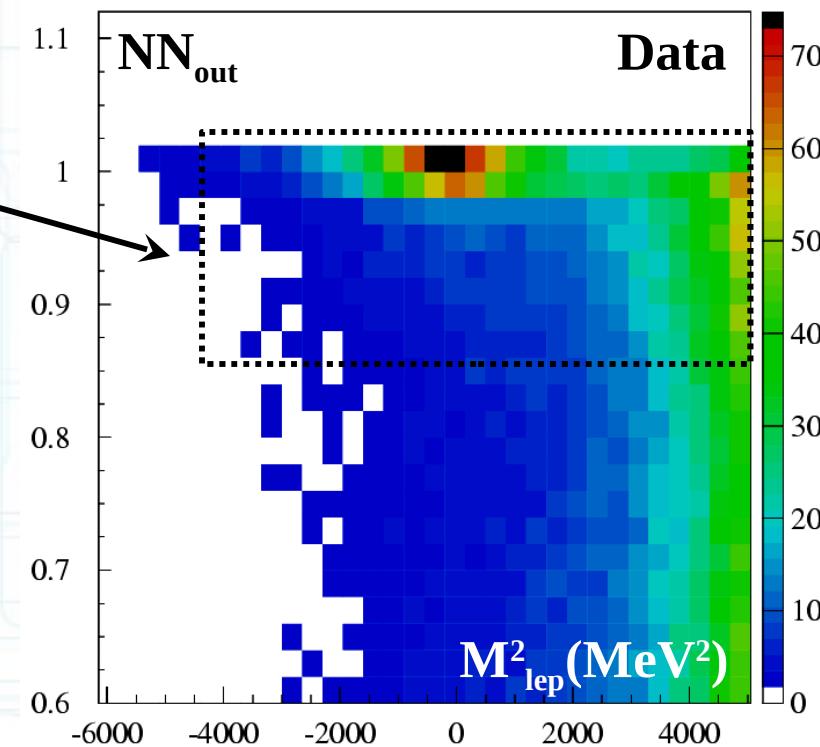
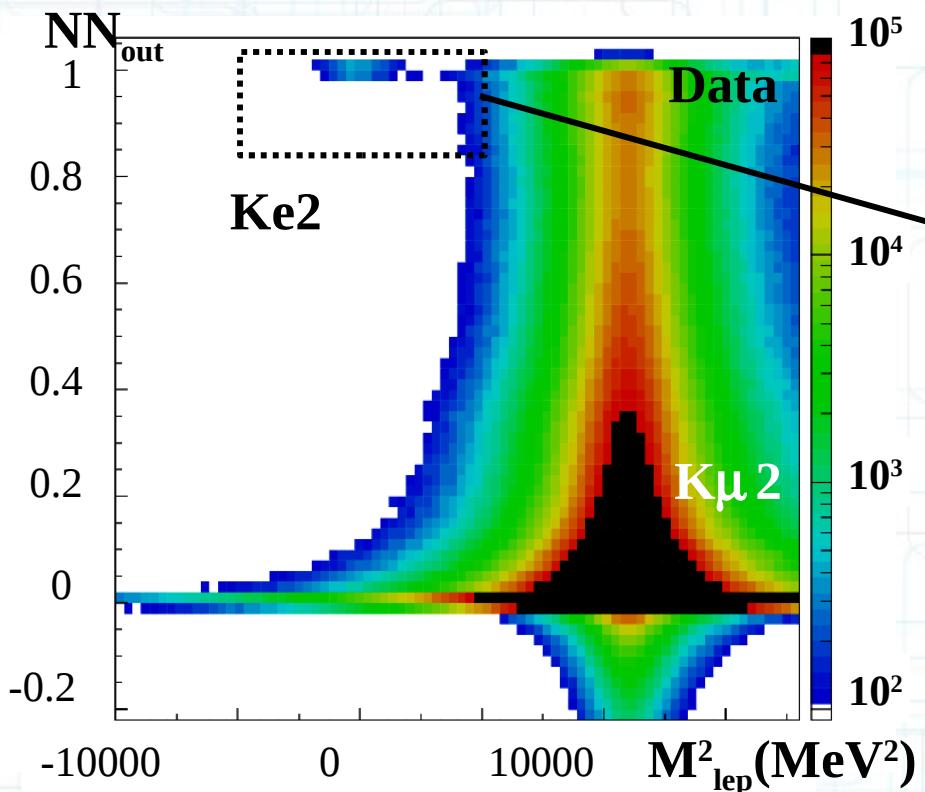
# Background rejection (PID)

- Use a pure sample of  $K_L e3$  to correct cell response in MC.
- $K_L e3$  and  $K\mu 2$  for NN training.



# Background rejection (PID)

Select a region with good S/B ratio in the  $M^2_{\text{lep}} - \text{NN}_{\text{out}}$  plane



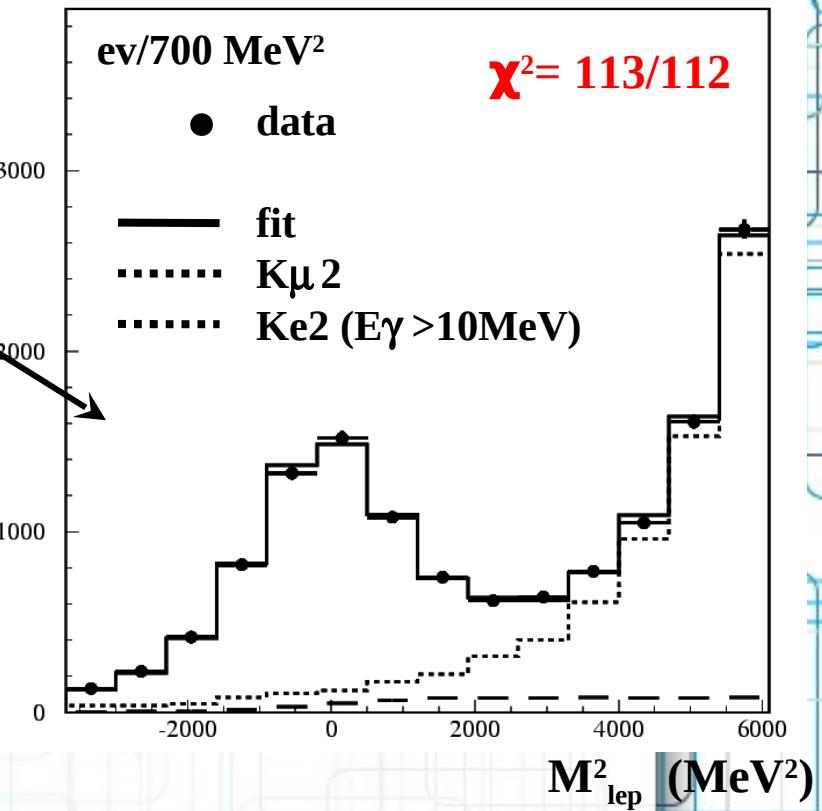
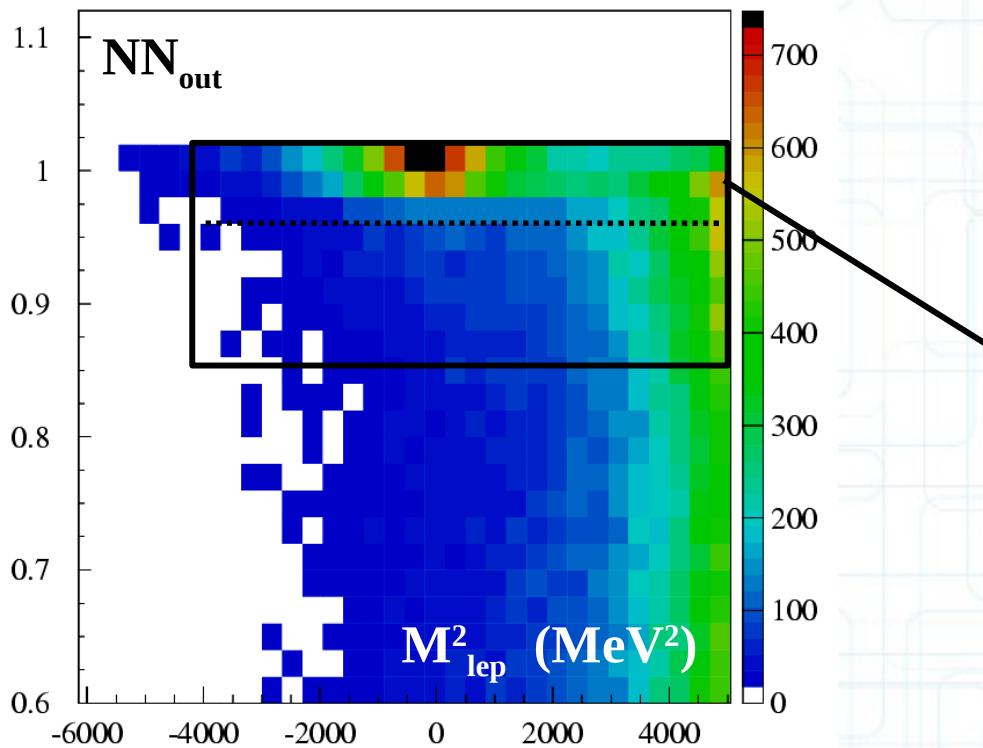
after selection:  $\epsilon \sim 30\% \ (\sim 15,000 \text{ } K_{e2})$

S/B  $\sim 5$

# $K_{e2}$ event counting

Two-dimensional binned likelihood fit in the  $M^2_{\text{lep}}$ – $NN_{\text{out}}$  plane  
in the region  $-4000 < M^2_{\text{lep}} < 6100$  and  $0.86 < NN_{\text{out}} < 1.02$

Ke2+ fit;  $M^2_{\text{lep}}$  proj for  $NN_{\text{out}} > 0.96$



We count **7060 (102) Ke2+** **6750 (101) Ke2-** ( $\sigma_{\text{STAT}} = 1\%, 0.85\%$  from Ke2)

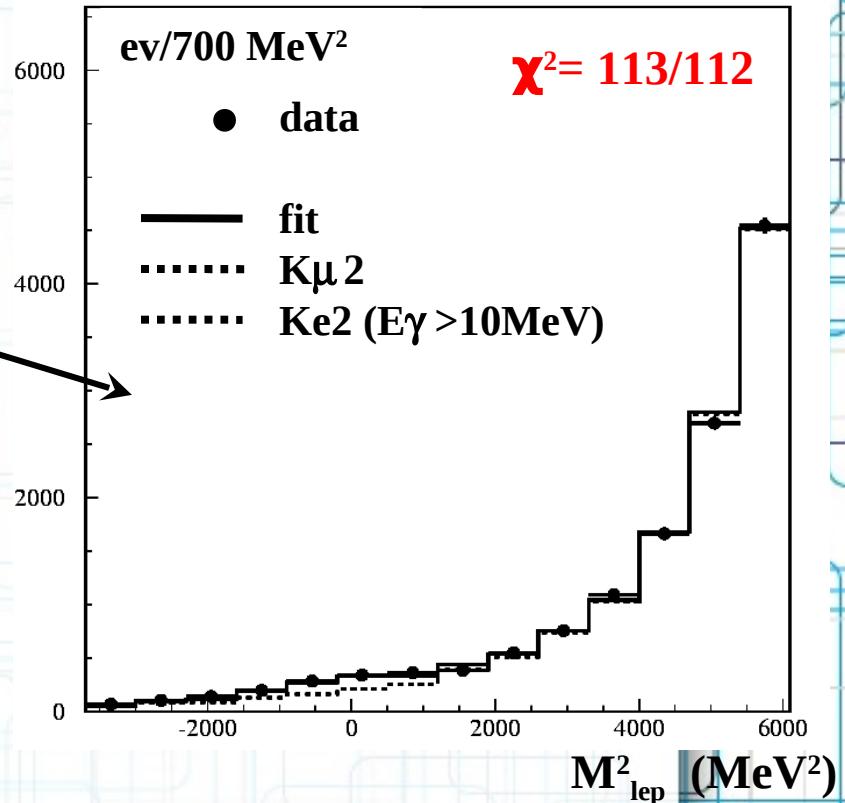
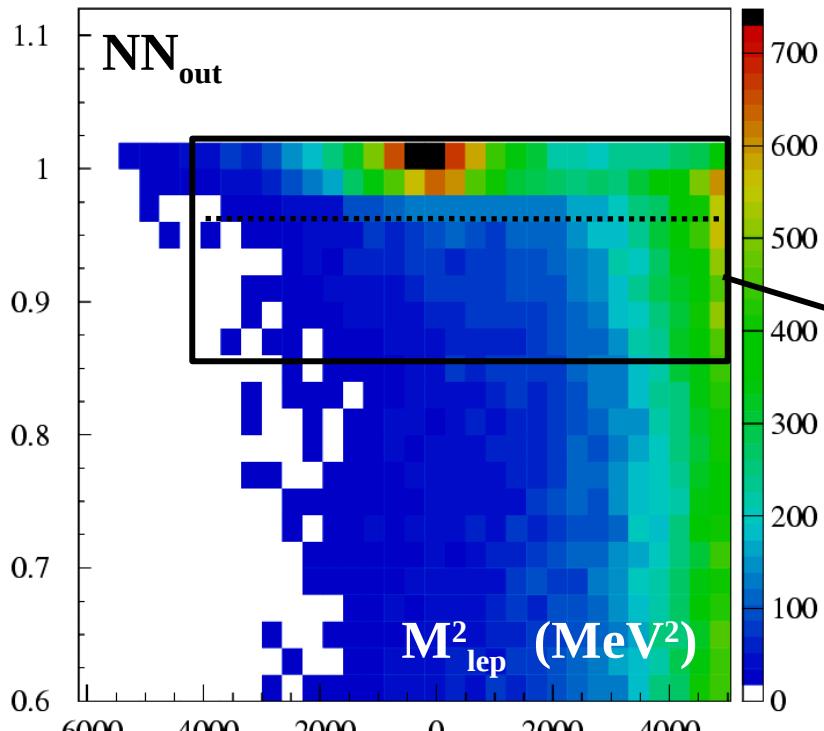
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# $K_{e2}$ event counting

Two-dimensional binned likelihood fit in the  $M^2_{\text{lep}}$ – $NN_{\text{out}}$  plane  
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Ke2+ fit;  $M^2_{\text{lep}}$  proj for  $NN_{\text{out}} < 0.96$



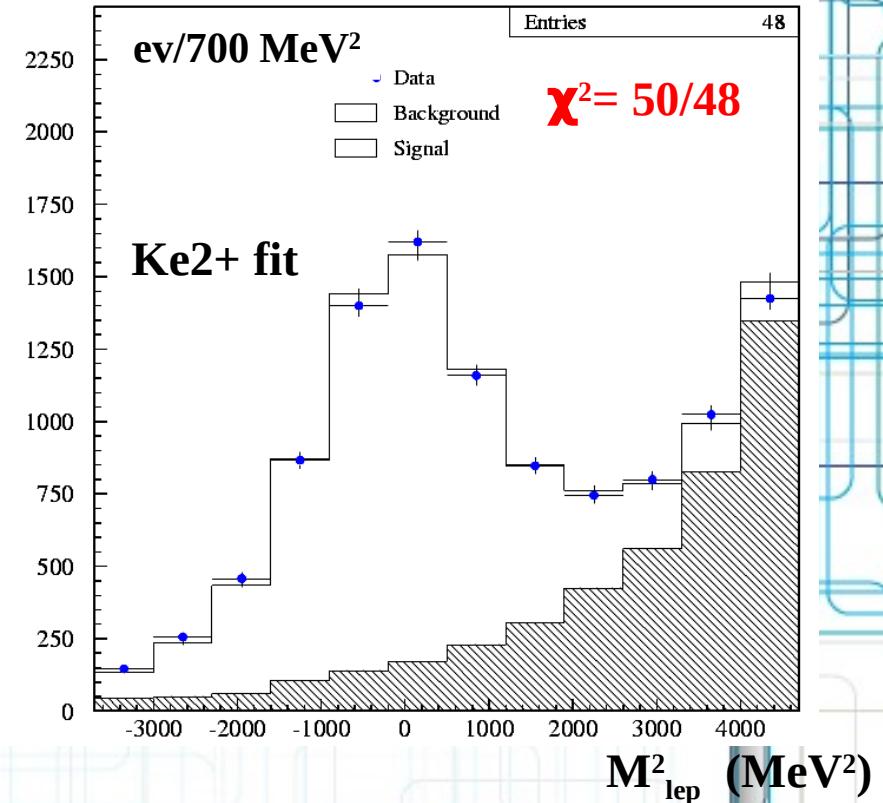
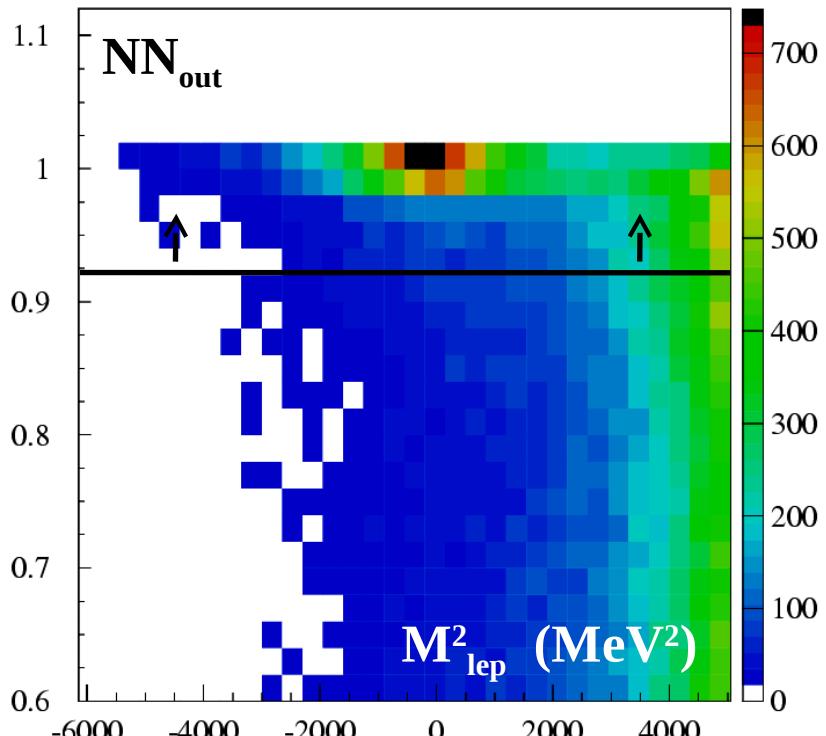
We count **7060 (102) Ke2+**   **6750 (101) Ke2-** ( $\sigma_{\text{STAT}} = 1\%$ , 0.85% from Ke2)

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# $K_{e2}$ event counting: systematics

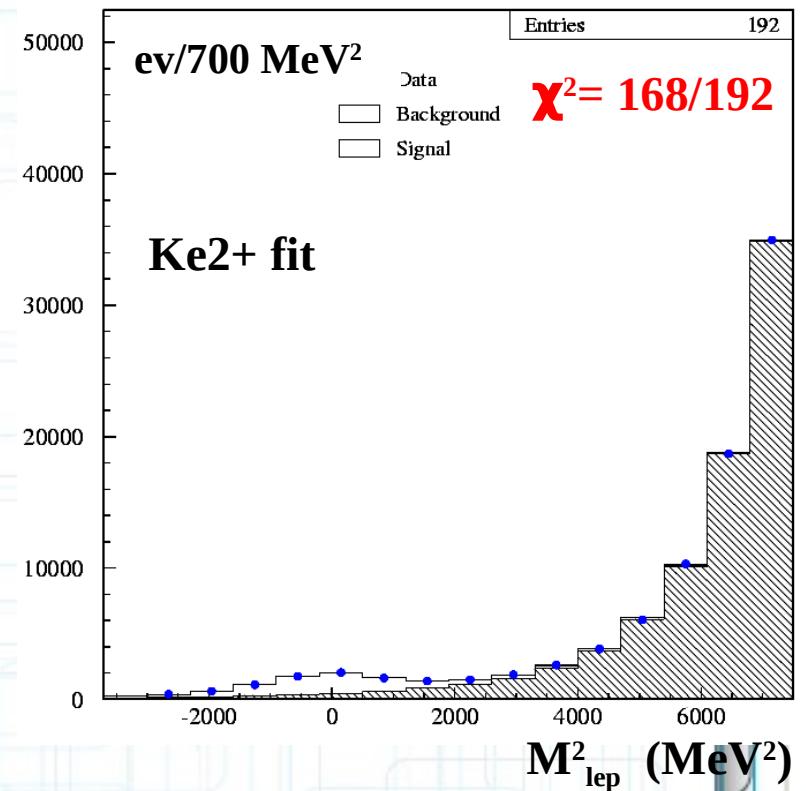
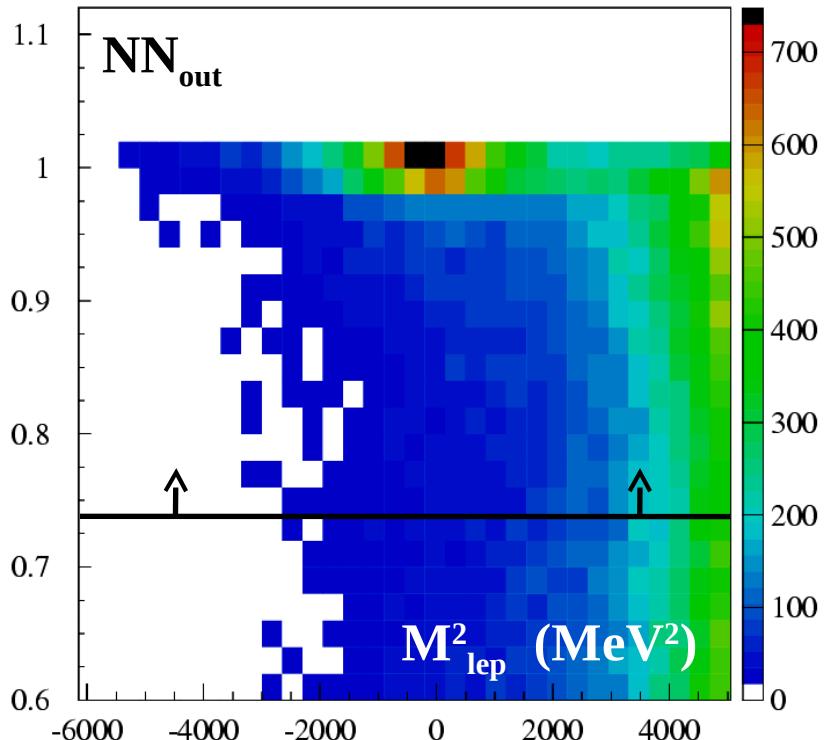
Repeat fit with different values of  $\text{max}(M_{\text{lep}}^2)$  and  $\text{min}(\text{NN}_{\text{out}})$ :  
vary significantly ( $\times 20$ ) bkg contamination + lever arm.



minimal bkg with:  $-4000 < M_{\text{lep}}^2 < 4650$  and  $0.94 < \text{NN}_{\text{out}} < 1.02$

# $K_{e2}$ event counting: systematics

Repeat fit with different values of  $\text{max}(M_{\text{lep}}^2)$  and  $\text{min}(NN_{\text{out}})$ :  
vary significantly ( $\times 20$ ) bkg contamination + lever arm.



maximum bkg with:  $-4000 < M_{\text{lep}}^2 < 7500$  and  $0.78 < NN_{\text{out}} < 1.02$

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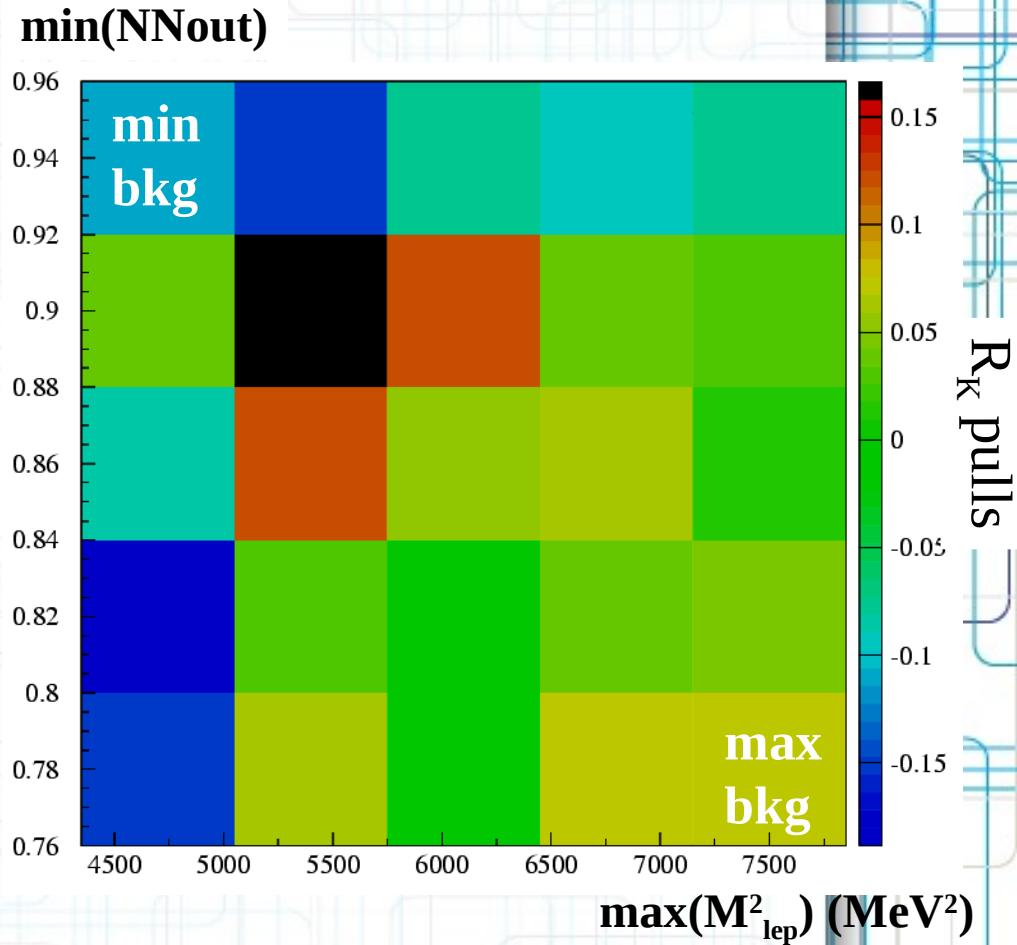
# $K_{e2}$ event counting: systematics

We change by a factor of 20 the amount of bkg falling in the fit region by moving

- $\min(\text{NNout})$
- $\max(M^2_{\text{lep}})$ .

Signal counts change by 15%.

From the pulls of the  $R_K$  measurements we evaluated a 0.3% systematic error.



# Ke2 fit: radiative corrections

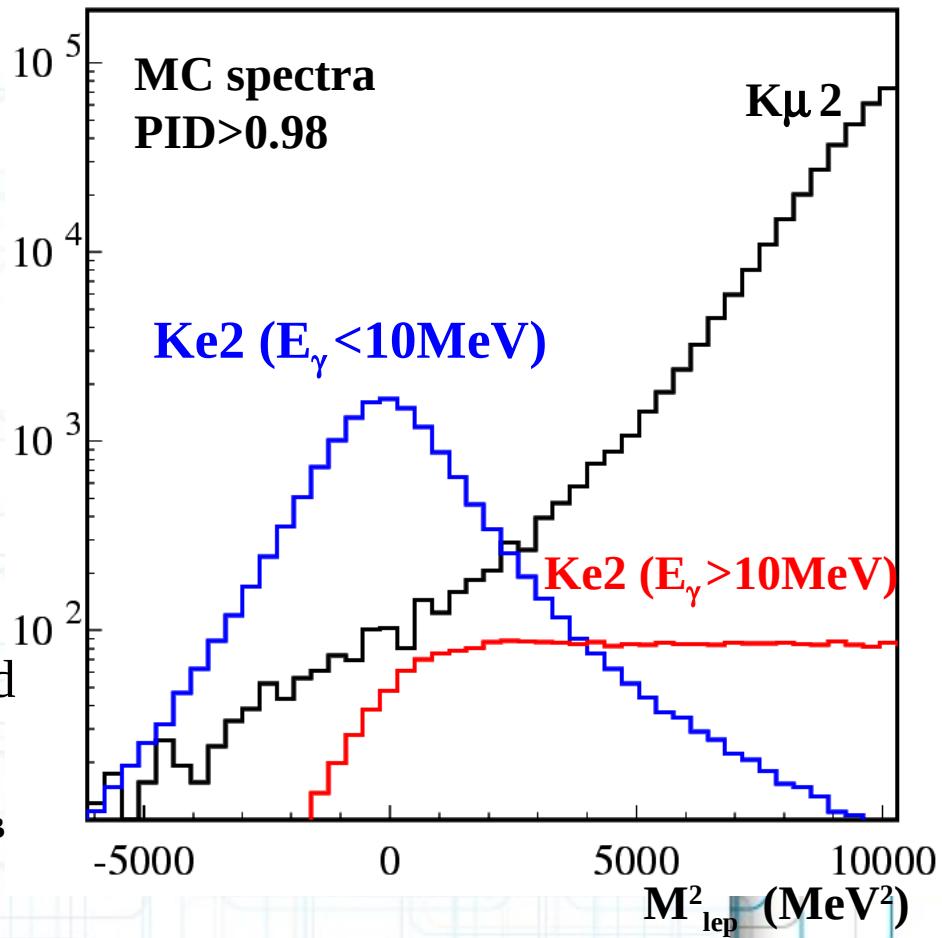
- Analysis is inclusive of photons in the final state. In our fit region we expect:

$$\frac{\text{Ke2 } (E_\gamma > 10 \text{ MeV})}{\text{Ke2 } (E_\gamma < 10 \text{ MeV})} \sim 10\%$$

- Repeat fit by varying Ke2  $(E_\gamma > 10 \text{ MeV})$  by 15% (DE uncertainty) get 0.5% error.

We performed a **dedicated study of the Ke2 $\gamma$  differential decay rate**:

- $E_\gamma$  spectrum measured for the first time
- confirm DE content of our MC, evaluated with ChPT O( $p^4$ ), within  $\sim 4\%$  accuracy
- obtain 0.2% systematic error on Ke2<sub>IB</sub>

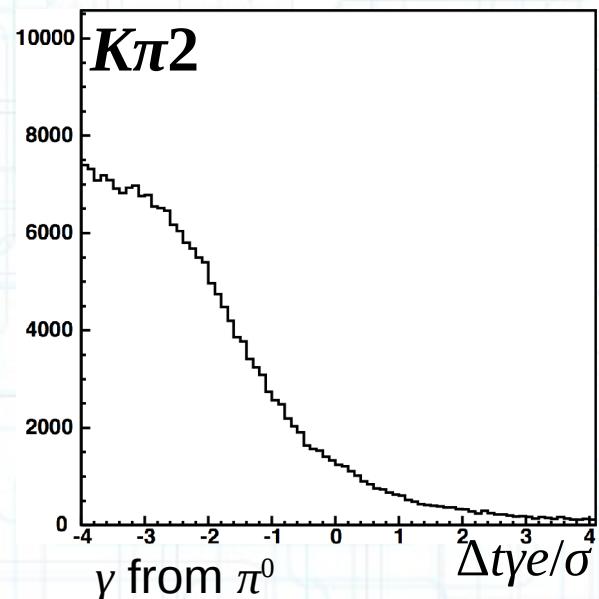
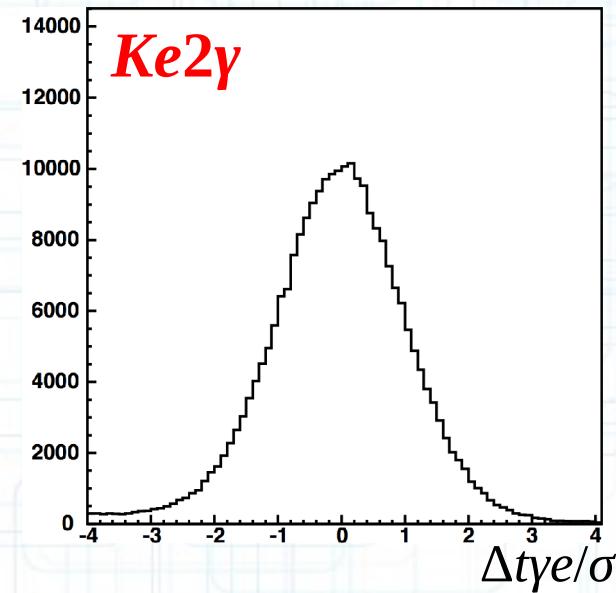


# Ke2 $\gamma$ selection

To select Ke2 $\gamma$  events additional selection criteria were applied:

- Harder cut on NN output to reject K $\mu$ 2 with accidental  $\gamma$
- Explicit detection of  $\gamma$  with  $E > 20$  MeV
- Time for  $\gamma$  and e in EMC must be compatible:

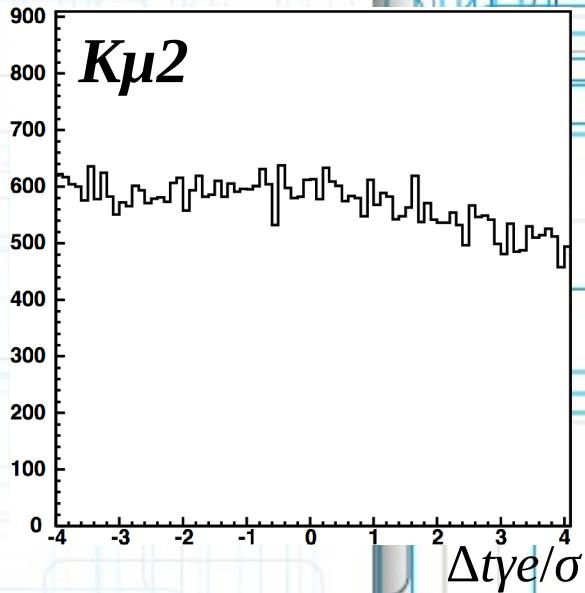
$$|\Delta t_{\gamma e}| = |(t_\gamma - L_\gamma/c) - (t_e - L_e/c)| \leq 2\sigma$$



$$\beta(\pi^+) \approx 0.8, \text{ not } 1$$

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Accidentals flat in time

# Ke<sub>2</sub>γ selection

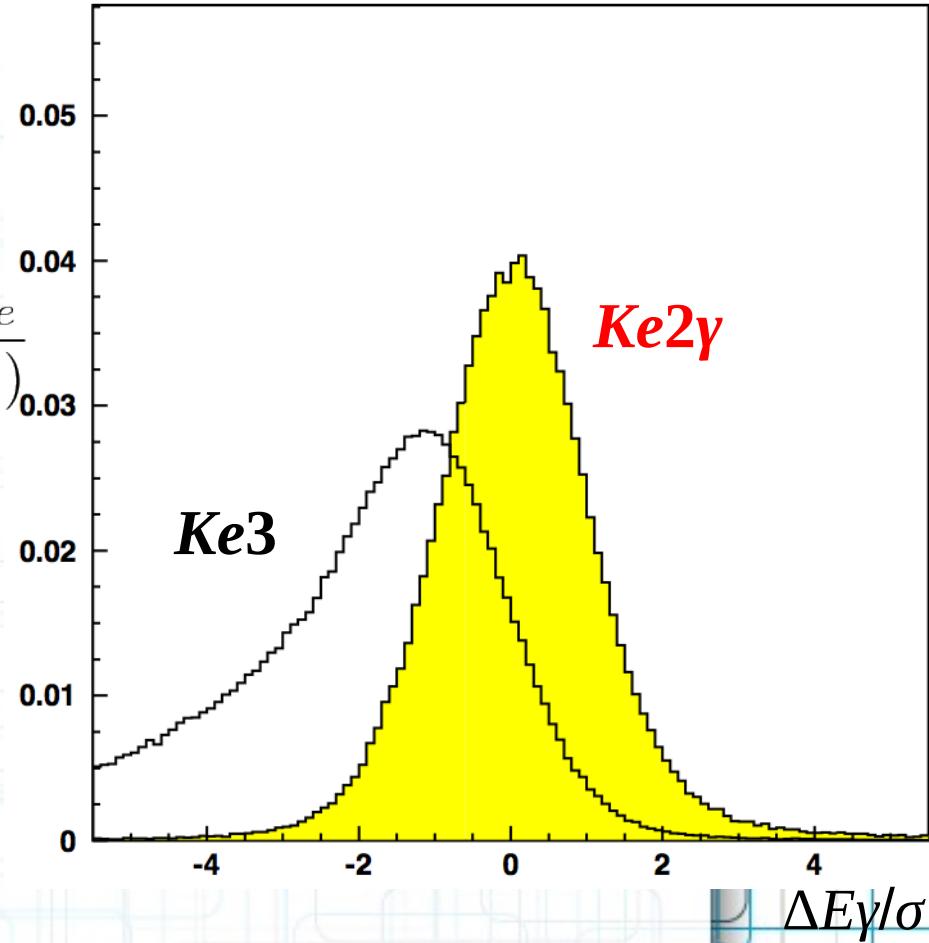
Difference between measured and expected γ energy can be useful in bkg/signal separation:

$$E_{\gamma}^{\text{lab}} = \frac{m_K^2 + m_e^2 - 2E_K E_e + 2\mathbf{p}_K \cdot \mathbf{p}_e}{2(E_K - E_e - \mathbf{p}_K \cdot \mathbf{n}_{\gamma} + \mathbf{p}_e \cdot \mathbf{n}_{\gamma})}$$

$$\sigma_E^{\text{lab}} \approx 12 \text{ MeV}$$

$$\sigma_E^{\text{EMC}} \approx 30 \text{ MeV}$$

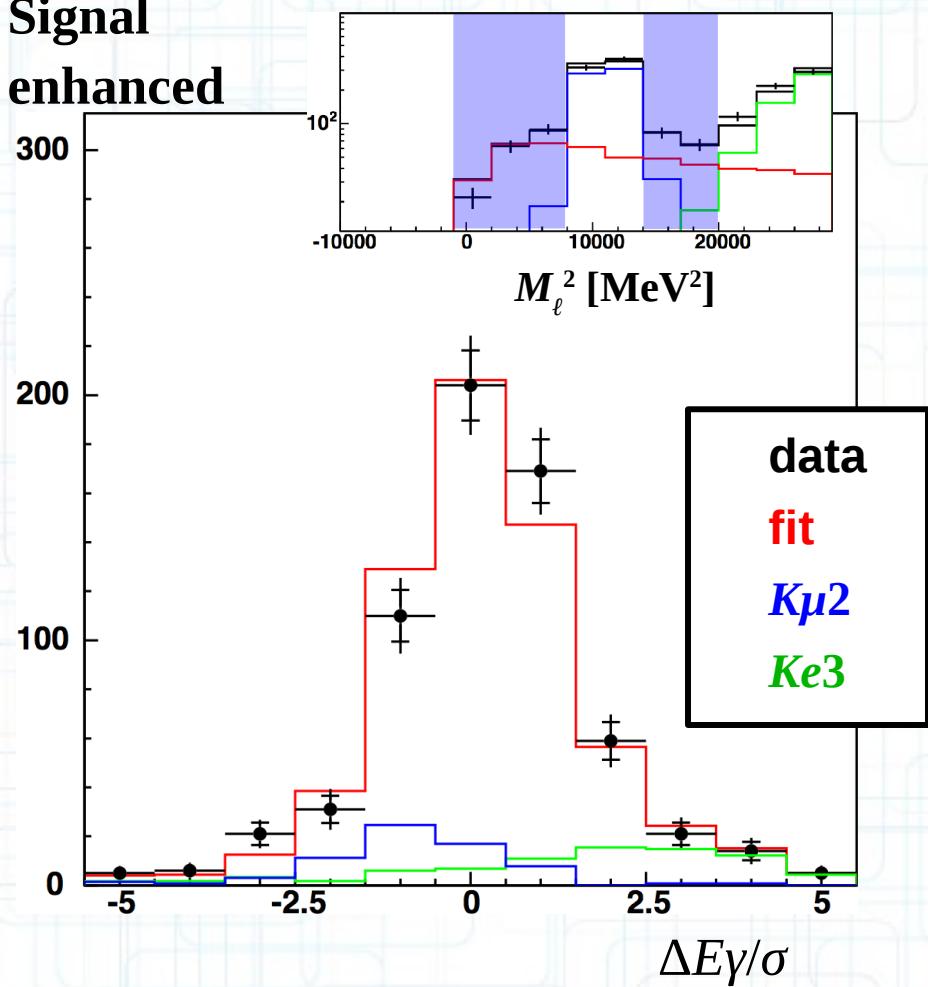
Perform 2-dimensional fit binned likelihood fit  $M_l^2$ ,  $\Delta E_{\gamma}/\sigma$  in 5 bins of  $E_{\gamma}^*$



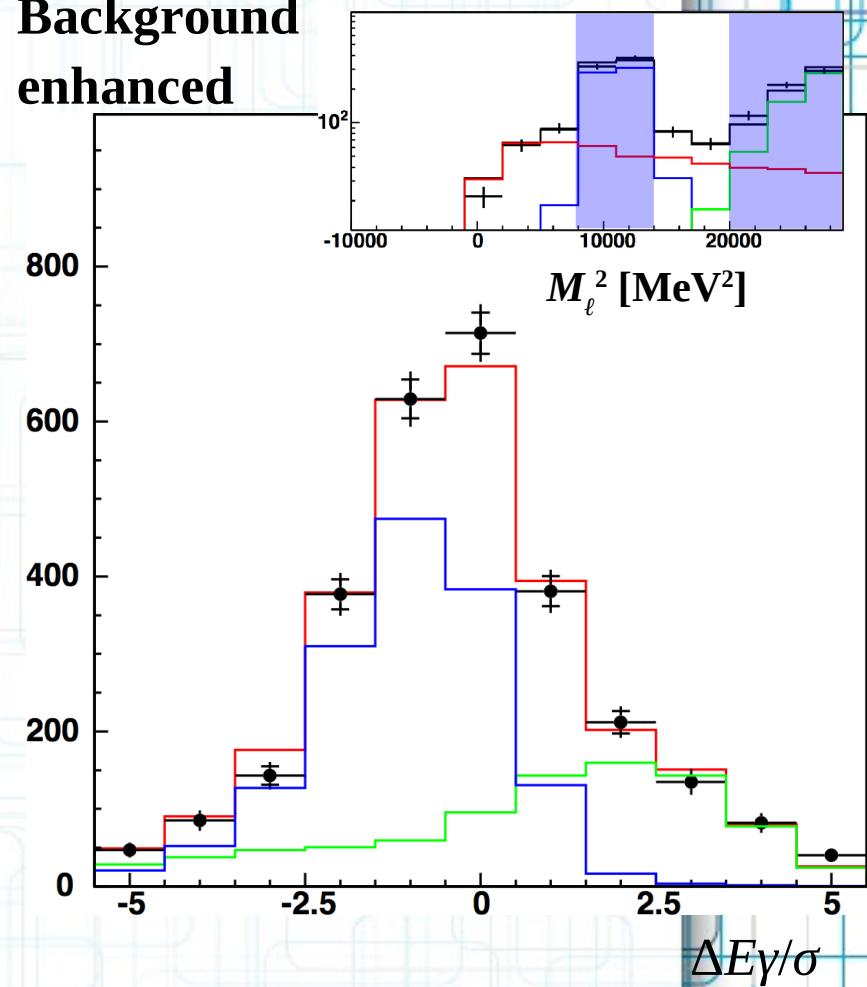
# Ke $2\gamma$ fit result

Projections on  $\Delta E_\gamma / \sigma$  axis for all 5  $E_\gamma^*$  bins, with cuts on  $M_\ell^2$

Signal  
enhanced



Background  
enhanced



# Ke $2\gamma$ spectrum

We measure  $\frac{1}{\Gamma(K_{\mu 2})} \frac{d\Gamma_{SD+}(K_{e2\gamma})}{dE_\gamma}$ , where “SD+” means:

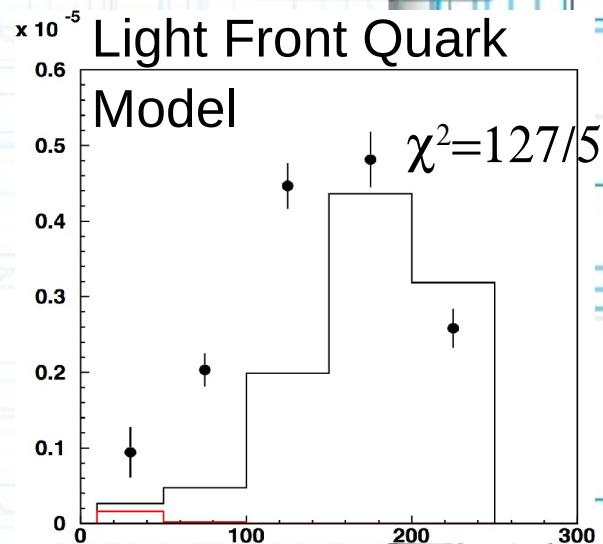
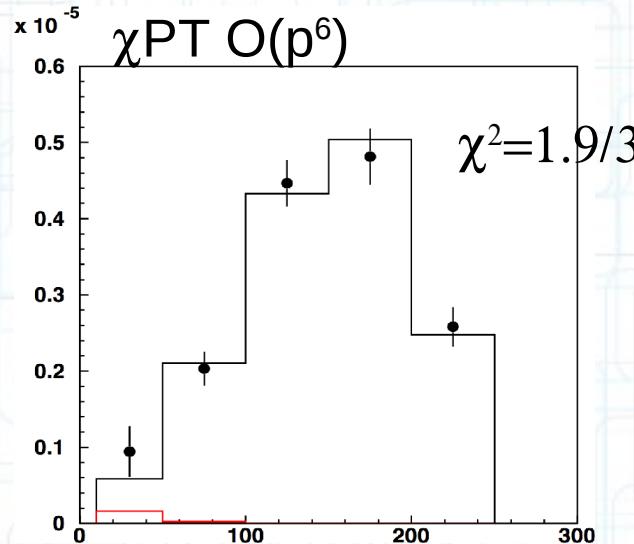
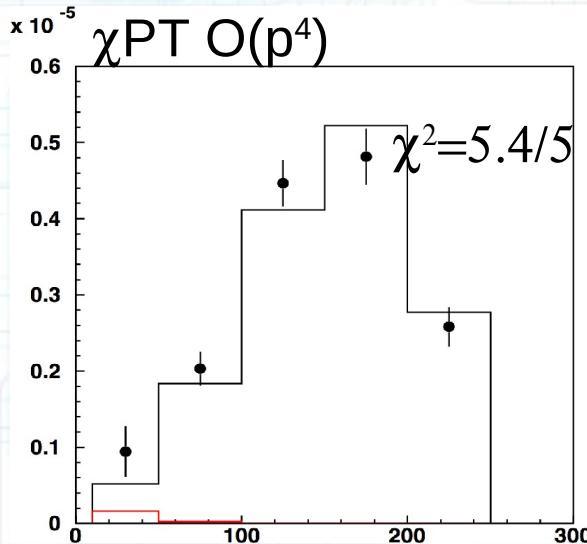
$$E_\gamma^* > 10 \text{ MeV}, \cos \theta_{e\gamma}^* < 0.9, p_e^* > 200 \text{ MeV}/c$$

$$N_{SD+}(\text{Ke}2\gamma) = 1378 \pm 63 \Rightarrow \Gamma_{SD+}(\text{Ke}2\gamma)/\Gamma(K\mu 2) = 1.484(66)_{\text{stat}}(16)_{\text{syst}} \times 10^{-5},$$

which is in agreement with  $\chi$ PT O( $p^4$ ) prediction

$$1.447 \times 10^{-5} [\text{Bijnens, Ecker, Gasser '93}]$$

KLOE MC was validated to within 4.6%  $\Rightarrow$  systematic error on  $R_K$  is 0.2%



# Reconstruction efficiencies

The ratio of Ke2 to K $\mu$  2 efficiencies is evaluated with MC and corrected using data control samples

- 1) kink reconstruction (tracking):  $K^+e3$  and  $K^+\mu 2$  data control samples selected using the tagging and additional criteria based on EMC information only (next slide)
- 2) cluster efficiency ( $e, \mu$ ):  $K_L$  control samples, selected with tagging and kinematic criteria based on DC information only
- 3) trigger: exploit the OR combination of EMC and DC triggers (almost uncorrelated); downscaled samples are used to measure efficiencies for cosmic-ray and machine background vetoes

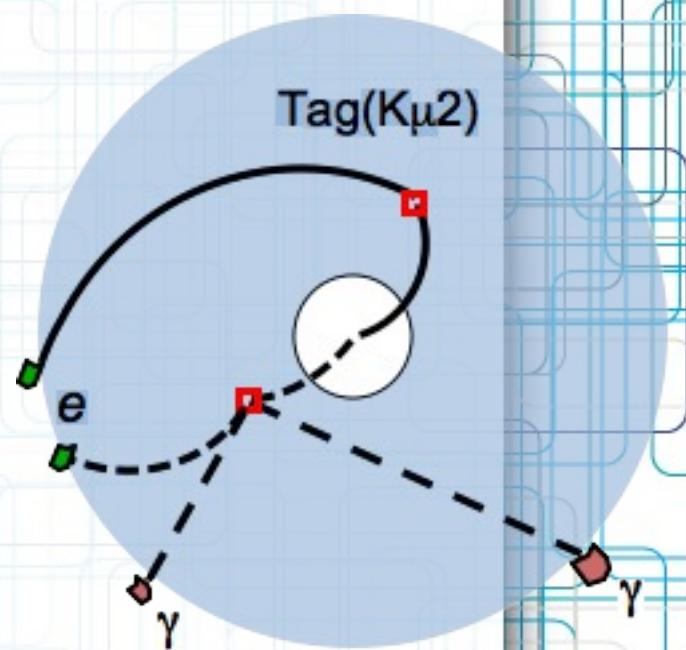
We obtain:  $\epsilon(Ke2)/\epsilon(K\mu 2) = 0.946 \pm 0.007$

# Control samples for tracking efficiencies

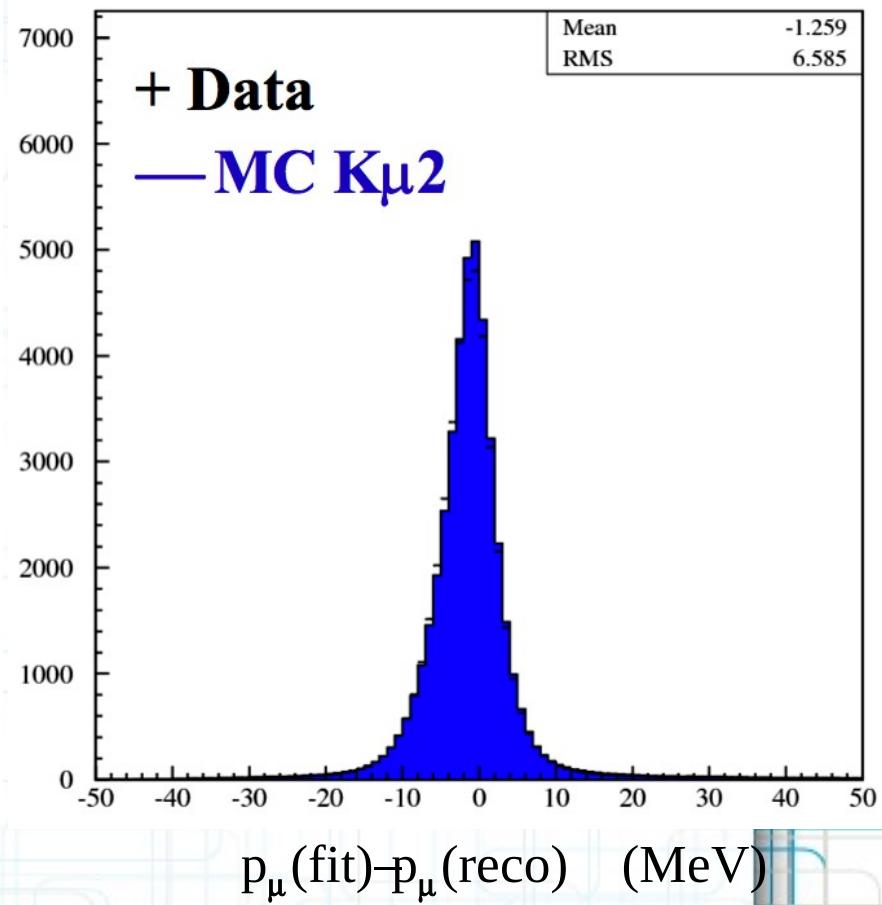
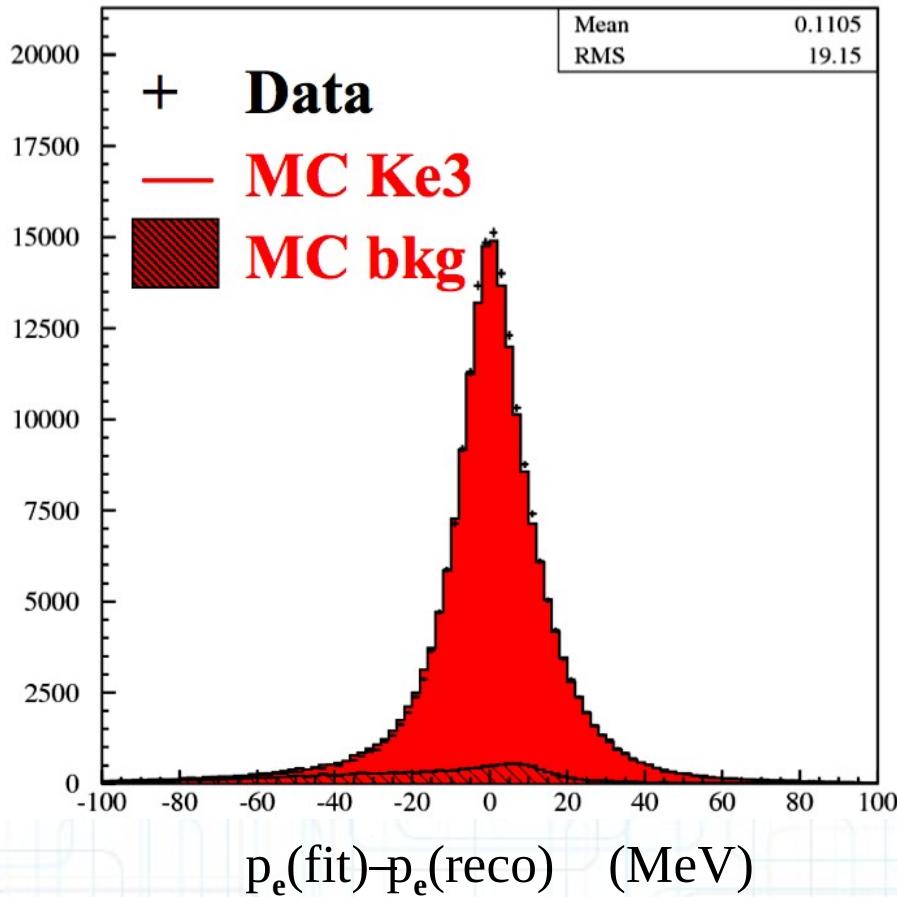
Just an example: selection of  $K^+e3$  control sample to measure tracking efficiency for electrons

- 0) Tagging decay ( $K\mu 2$  or  $K\pi 2$ );
- 1) Tagging decay ( $K\mu 2$  or  $K\pi 2$ ):  
reconstruction of the opposite charge kaon flight path;
- 2) Using a ToF technique a  $\pi^0 \rightarrow \gamma\gamma$  decay vertex is reconstructed along the K decay path;
- 3) Require an electron cluster:  $p_e$  estimated from a kinematic fit with constraints on  $E/p$ , ToF, cluster position, and  $E_{miss} - P_{miss}$ .

Evaluate the  $K +$  electron kink reconstruction efficiency



# Control samples for tracking efficiencies



- For electron tracks obtain a resolution  $\sigma \sim 19$  MeV
- With a similar method, get  $\sigma \sim 7$  MeV for muon tracks

# Systematics and checks

**Cross-check on efficiencies:** use same algorithms to measure  $R_{l3} = \Gamma(\text{Ke3})/\Gamma(\text{K}\mu 3)$

$$R_{l3} = 1.507 \pm 0.005 \text{ for } K^+$$

$$R_{l3} = 1.510 \pm 0.006 \text{ for } K^-$$

SM expectation (FlaviaNet)

$$R_{l3} = 1.506 \pm 0.003$$

## Summary of systematics:

<b>Tracking</b>	<b>0.6%</b>	$K^+$ control samples
<b>Trigger</b>	<b>0.4%</b>	downscaled events
<b>syst on Ke2 counts</b>	<b>0.3%</b>	fit stability
<b>Ke2<math>\gamma</math> DE component</b>	<b>0.2%</b>	measurement on data
<b>Clustering for e, <math>\mu</math></b>	<b>0.2%</b>	$K_L$ control samples

**Total Syst**      **0.8%**

(0.6% from statistics of control samples)

# $R_K$ : KLOE result

$$R_K = (2.493 \pm 0.025 \pm 0.019) \times 10^{-5}$$

Total error:

$$1.3\% = 1.0\%_{\text{stat}} + 0.8\%_{\text{syst}}$$

**0.9% from 14k Ke2 dominated  
+ bkg subtraction by statistics**

Accepted for publication on EPJC

PDG 2008:

$$R_K = (2.45 \pm 0.11) \times 10^{-5}$$

4.5% accuracy

NA62 preliminary result:

$$R_K = (2.500 \pm 0.012 \pm 0.011) \times 10^{-5}$$

World average with NA62 result:

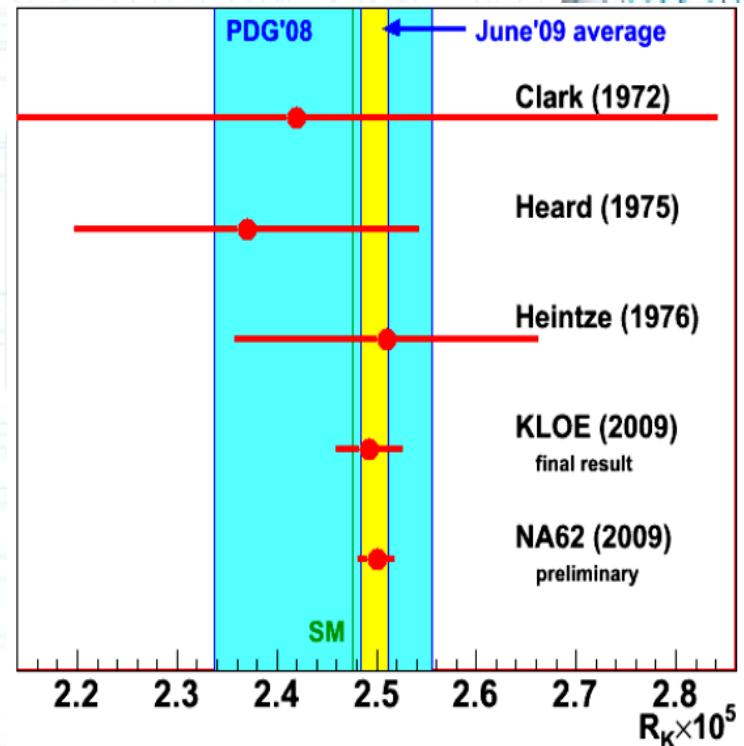
$$R_K = (2.498 \pm 0.014) \times 10^{-5}$$

0.56% accuracy

$$R_K^{\text{SM}} = 2.477(1) \times 10^{-5}$$

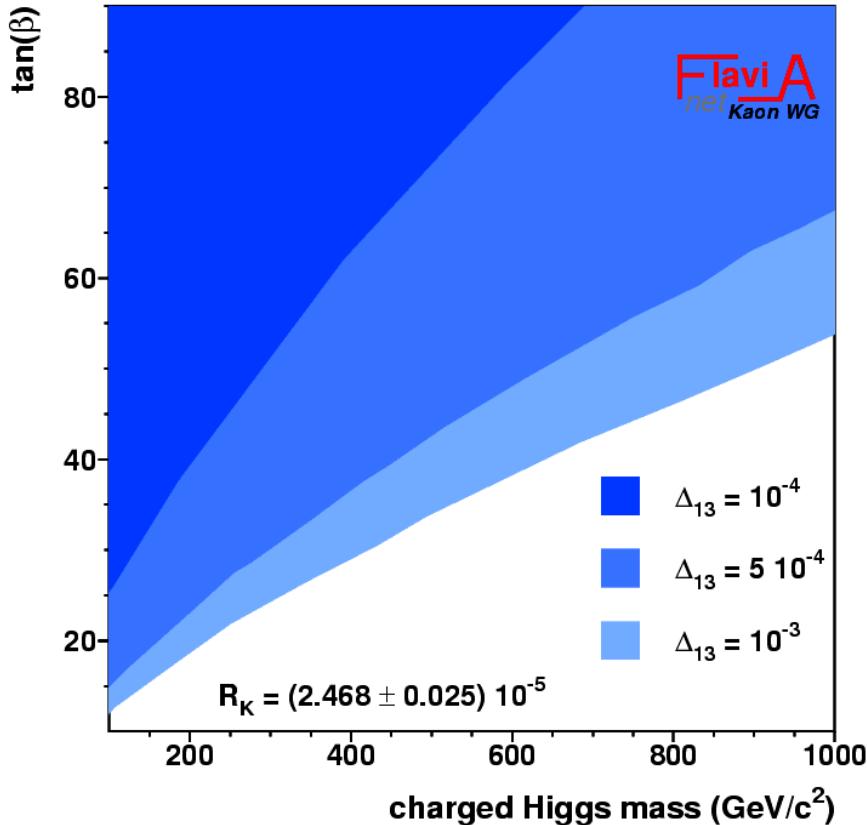
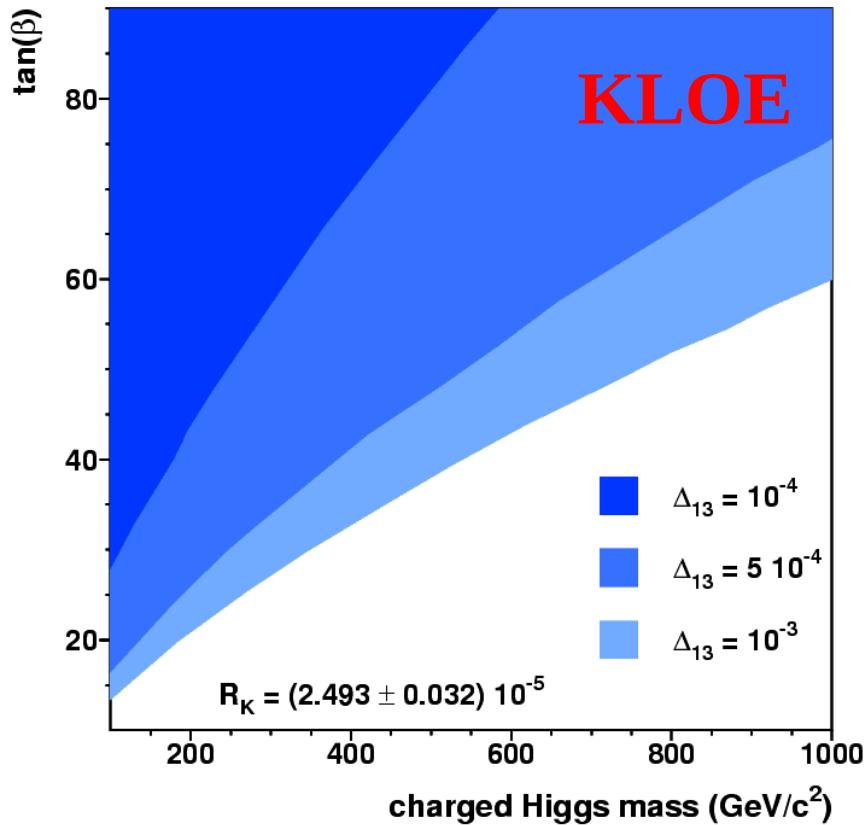
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- The result does not depend upon the kaon charge:  
 $K^+$ : 2.496(37) vs  $K^-$ : 2.490(38)  
(uncorrelated errors only)
- Agrees with SM prediction



# $R_K$ : sensitivity to new physics

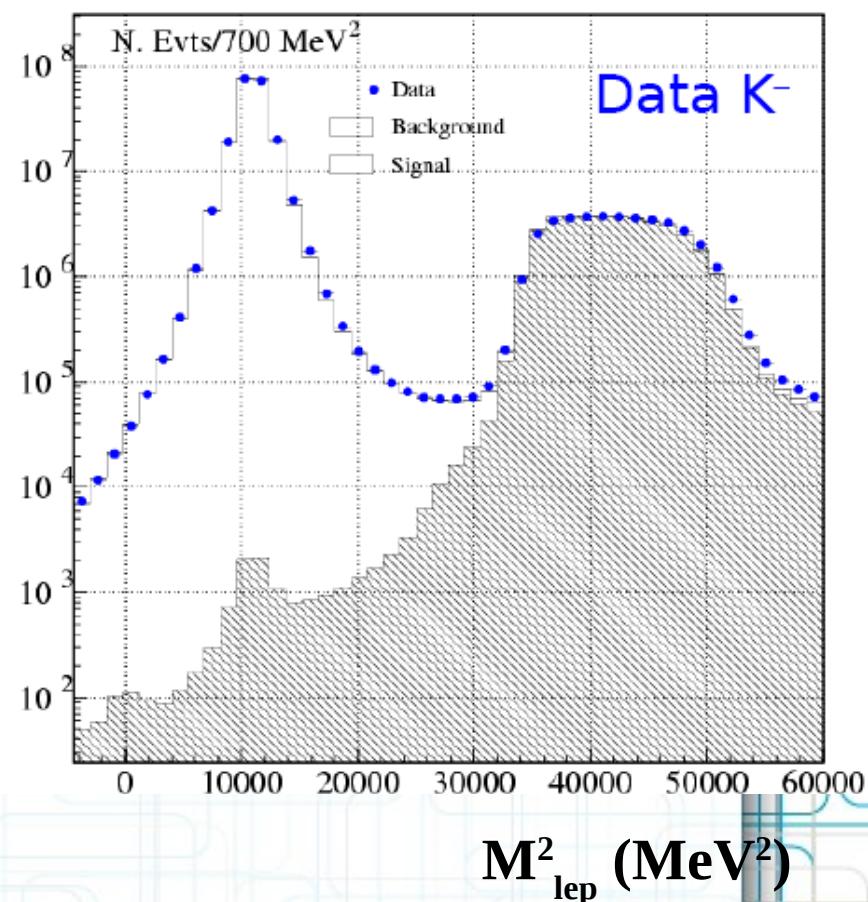
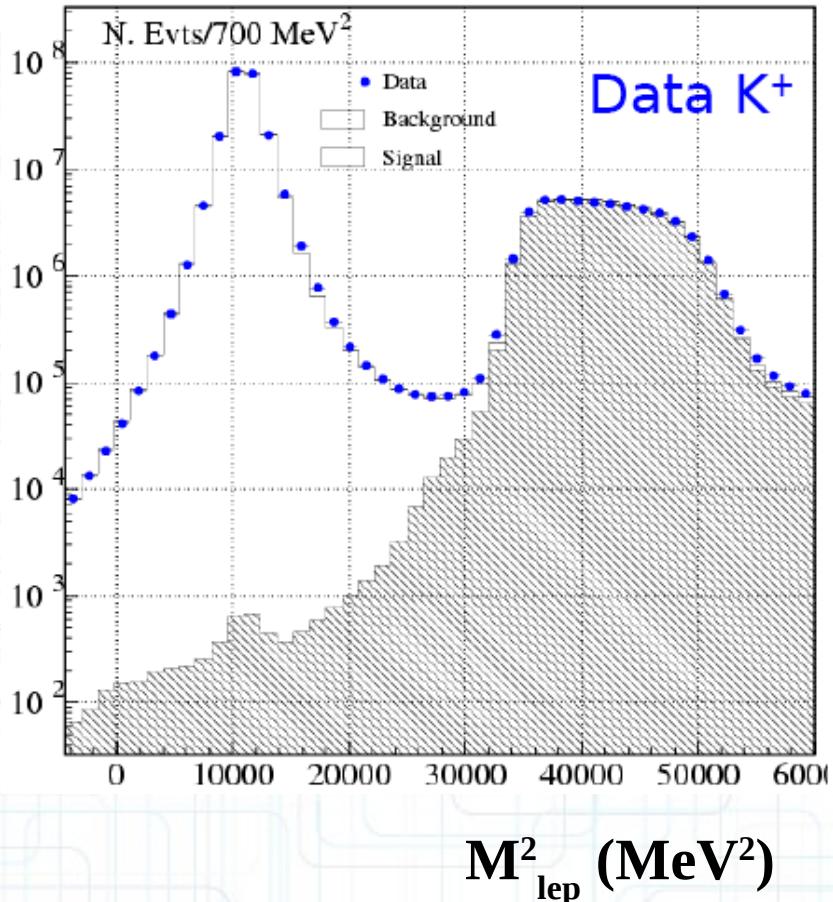
Sensitivity shown as 95% CL excluded regions in the  $\tan\beta$ - $M_H$  plane, for different values of the LFV effective coupling,  $\Delta_{13} = 10^{-3}, 5 \times 10^{-4}, 10^{-4}$



# Conclusion

- Using  $2.2 \text{ fb}^{-1}$  of data acquired at the  $\phi$  peak, KLOE measured:  
 $R_K = (2.493 \pm 0.025_{\text{stat}} \pm 0.019_{\text{syst}}) \times 10^{-5}$
- This results confirms the SM prediction within the 1.3% accuracy
- Systematic error from DE model of KLOE MC on  $R_K$  is 0.2%
- $E_\gamma$  spectrum measured for the first time
- The error is dominated by the **counting** and the **control samples statistics**.
- Can contribute to set constraints on the parameter space of MSSM with LFV.

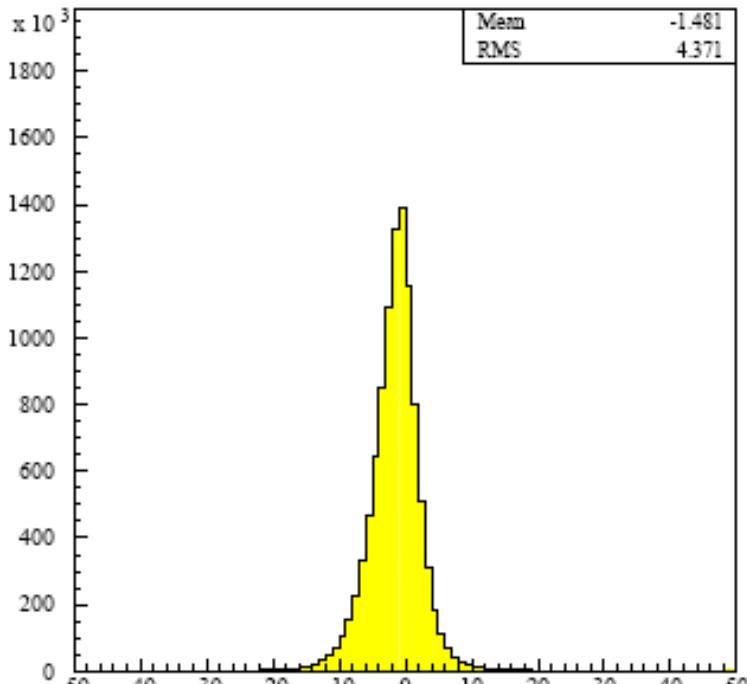
# K $\mu$ 2 event counting



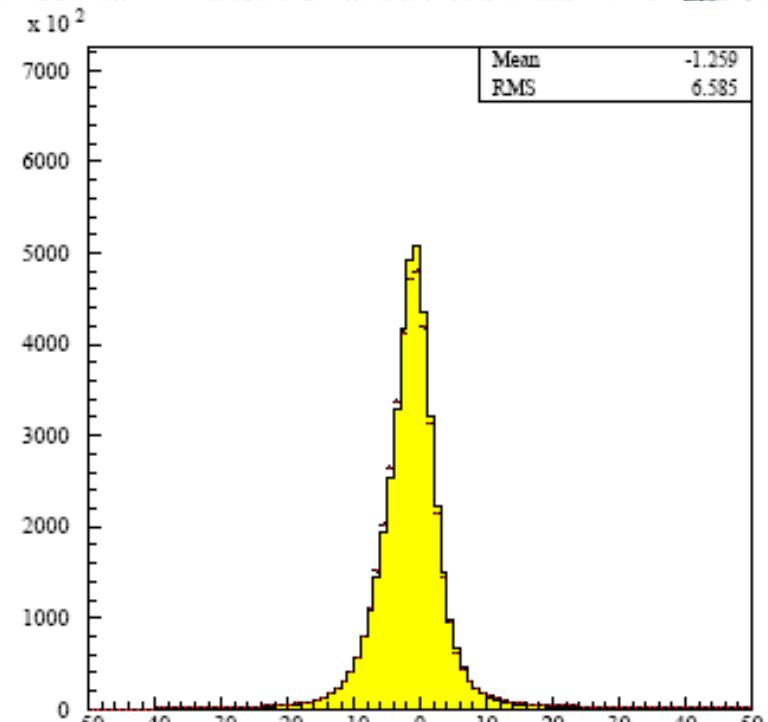
Fit to  $M_{\text{lept}}^2$  distribution: 300 million K $\mu$  2 events per charge

Background under the peak <0.1%, from MC

# Tracking efficiency



$p_\mu(\text{fit}) - p_\mu(\text{MC})$  (MeV)



$p_\mu(\text{fit}) - p_\mu(\text{reco})$  (MeV)

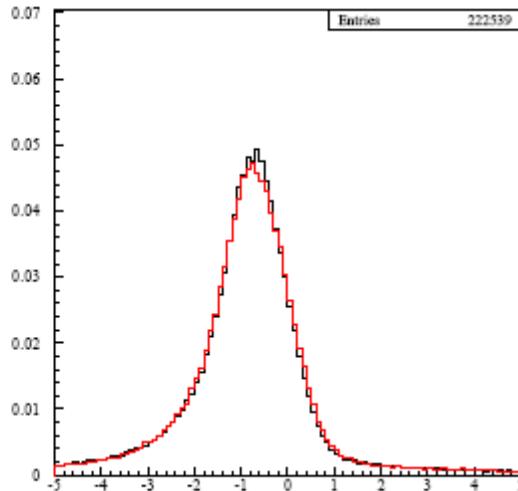
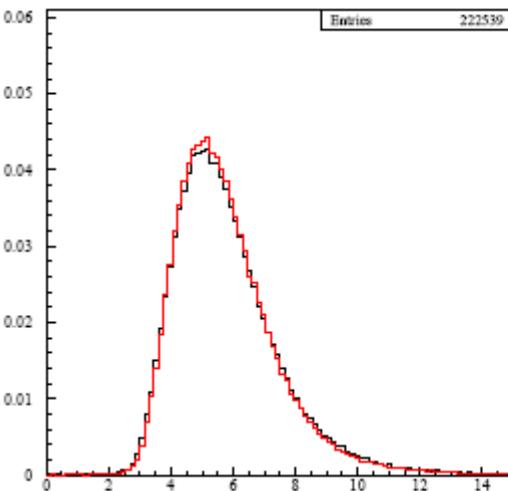
# NN details

- 1) E/P;
- 2) 1st momentum of the distribution of the longitudinal energy path deposition (cluster centroid depth) evaluated at cell level;
- 3) the 3rd momentum of the longitudinal energy path deposition (skewness);
- 4,5) asymmetry of energy lost in first two innermost (outermost) planes;
- 6) RMS of energy plane distribution;
- 7) energy lost in the 1st plane;
- 8) number of the plane with largest energy deposition;
- 9) largest energy deposition in a single plane;
- 10) slope of the  $E_{\text{int}}(x)$  energy distribution;
- 11) curvature of the  $E_{\text{int}}(x)$  energy distribution;
- 12)  $dE/dx$  i.e. value of  $E_{\text{int}}(x)/x|_{x<15 \text{ cm}}$

Additional separation using ToF information: difference  $\delta T$  of the time measured in the EMC with that expected from the DC measurements in electron mass hypothesis has been included in the final version of the NN: 12-25-20-1 becomes 13-25-20-1

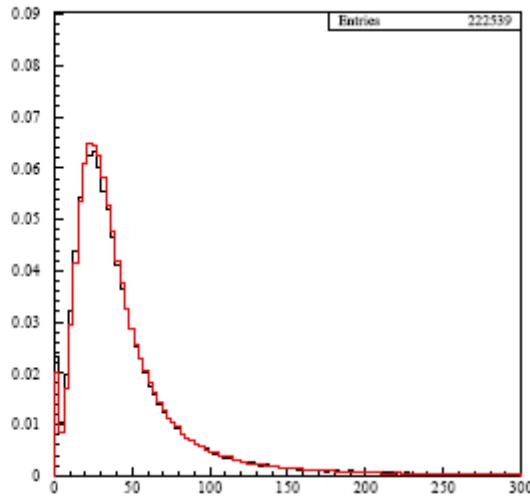
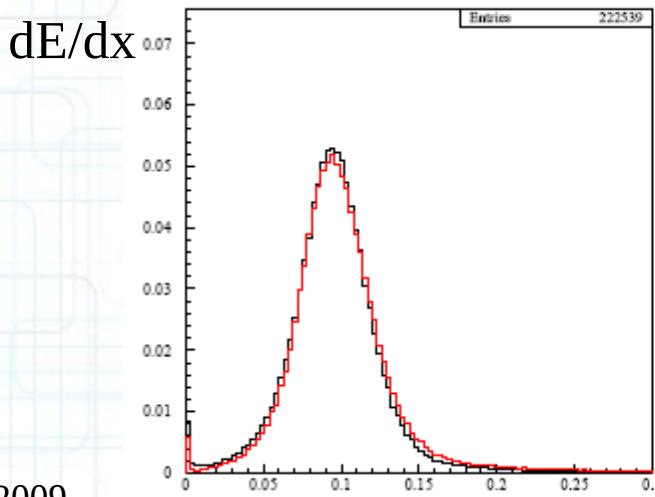
# NN input distributions: some example

Cluster  
centroid  
depth



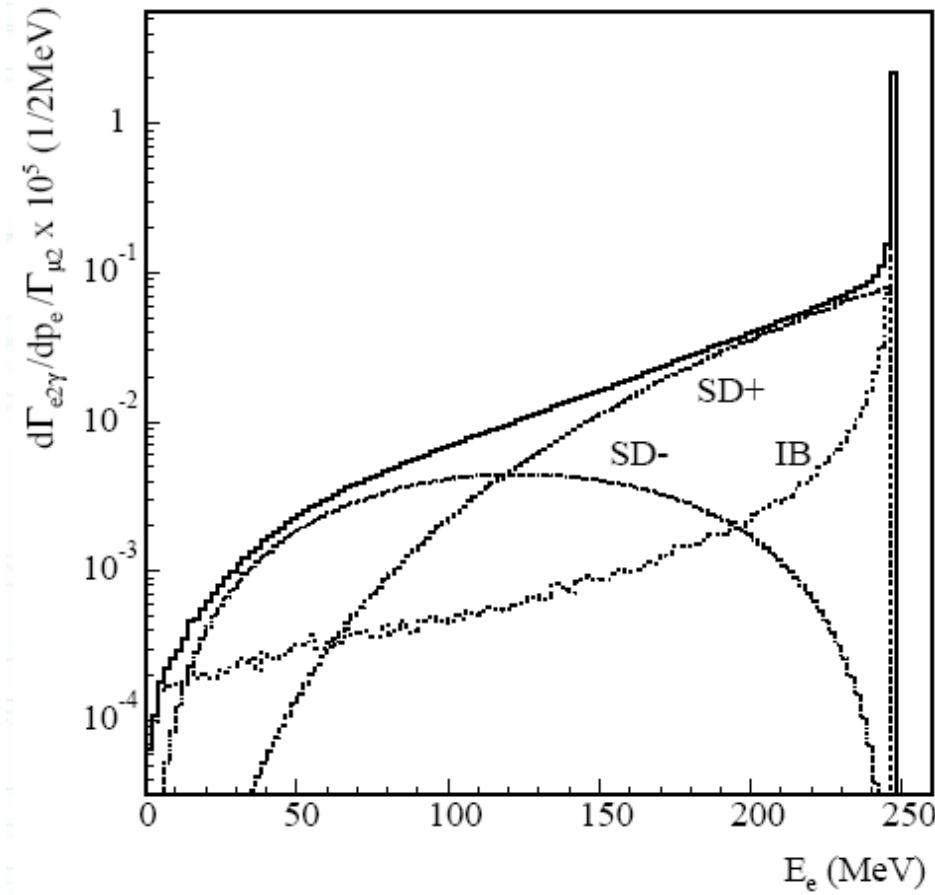
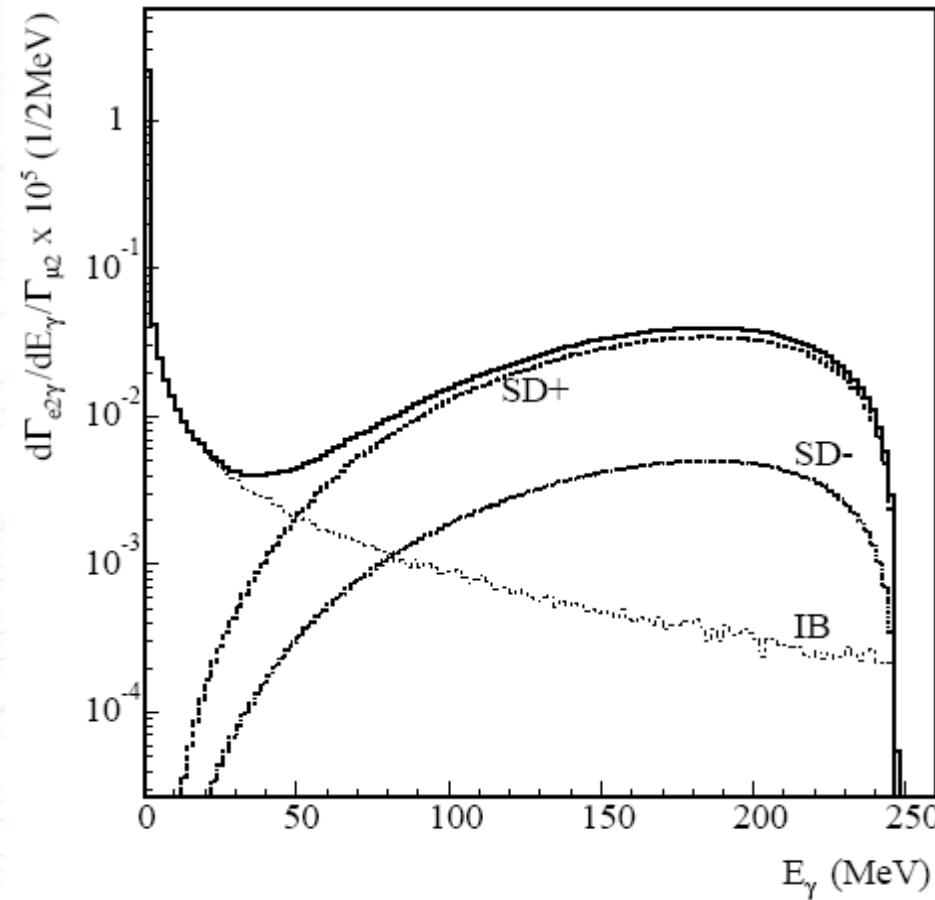
Asymmetry  
of energy lost  
in first two  
innermost  
planes

Data and MC



$E_{INT}(x)$  slope

# Distributions for $\text{Ke}2\gamma$ decay



For  $\text{Ke}2\gamma$  generator, the IB component is described with  $\chi_{\text{PT}}$  at  $O(e^2 p^2)$  including resummation of leading logarithms, while DE component is described with  $\chi_{\text{PT}}$  at  $O(e^2 p^4)$ .

# Ke $2\gamma$ process

Dalitz density

$$\frac{d\Gamma(Ke2\gamma)}{dxdy} = \rho_{IB}(x, y) + \rho_{DE}(x, y) + \rho_{INT}(x, y)$$

*helicity suppressed*   *negligible*

$$x = 2E_\gamma/M_K, \quad y = 2E_e/M_K$$

$E_\gamma, E_e$  in the K rest frame

## Structure Dependent

$$\rho_{DE}(x, y) = \frac{G_F^2 |V_{us}|^2 \alpha}{64\pi^2} M_K^5 ((f_V + f_A)^2 f_{SD+}(x, y) + (f_V - f_A)^2 f_{SD-}(x, y))$$

$f_V, f_A$  : effective vector  
and axial couplings

SD+ = V+A :  $\gamma$  polarization +  
SD- = V-A :  $\gamma$  polarization -

# Ke $2\gamma$ : theory predictions

1) ChPT at O( $p^4$ ):

$$f_V \approx 0.0945$$

$$f_A \approx 0.0425$$

no dependence on photon energy

Bijnens, Ecker, Gasser 93

2) ChPT at O( $p^6$ ):

$$f_V \approx 0.082(1+\lambda(1-x))$$

$$f_A \approx 0.034$$

V linear x dependence ( $\lambda \approx 0.4$ )

Ametller, Bijnens, Bramon, Cornet 93

Geng, Ho, Wu 04

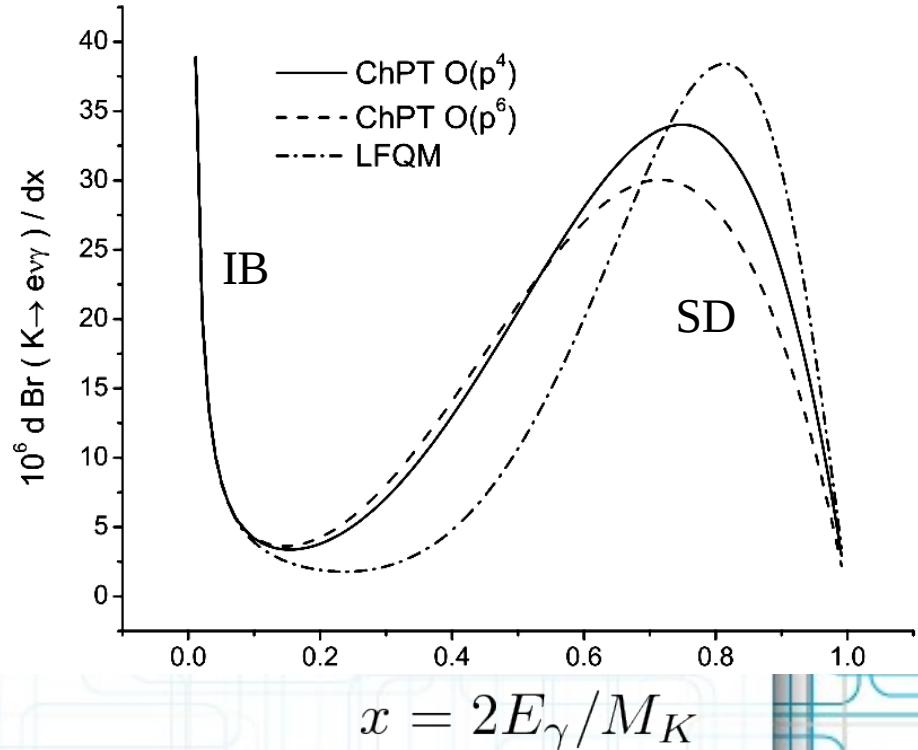
Chen, Geng, Lih 08

3) LFQM:

non trivial x dependence

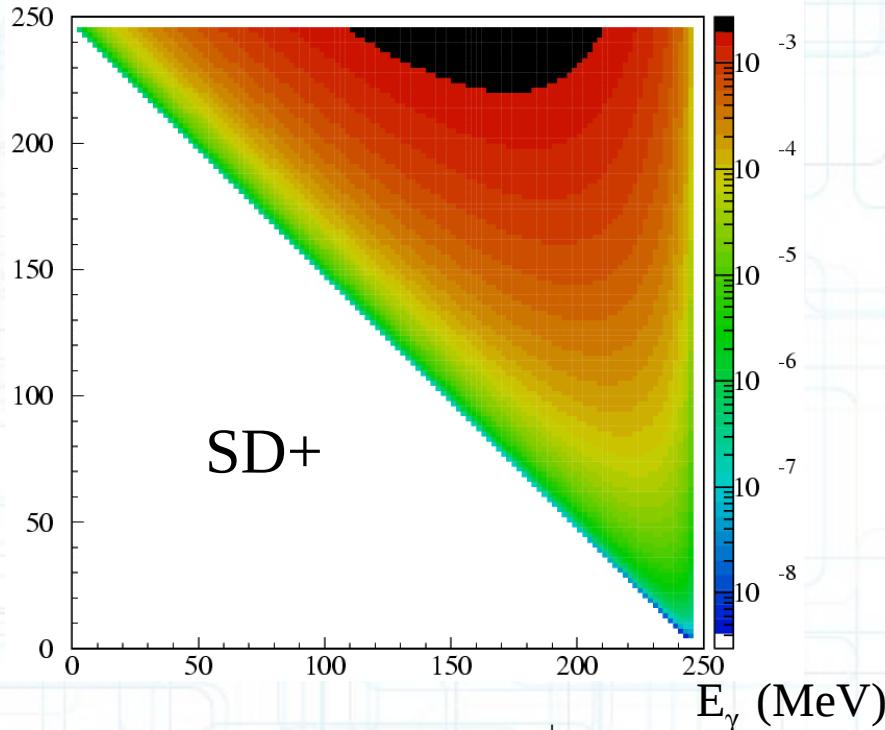
$$f_V = f_A = 0 \text{ at } x=0$$

Chen, Geng, Lih 08

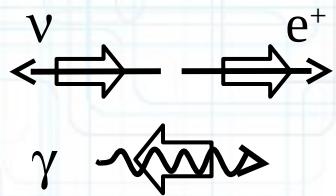


# Dalitz plots for SD+ and SD-

$p_e$  (MeV)



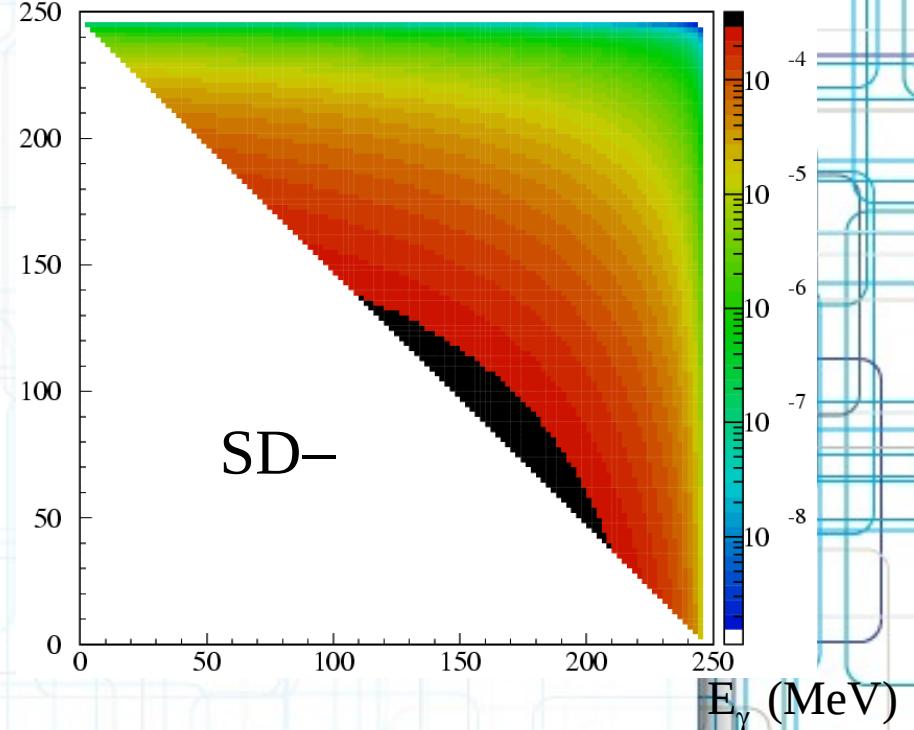
SD+



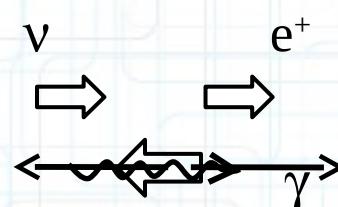
electron peaks at 250 MeV,  
e- $\gamma$  antiparallel

13.10.2009

$p_e$  (MeV)



SD-



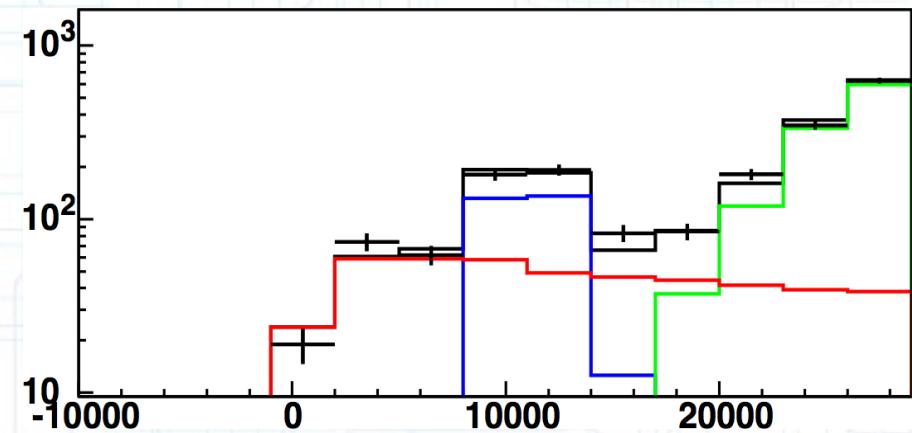
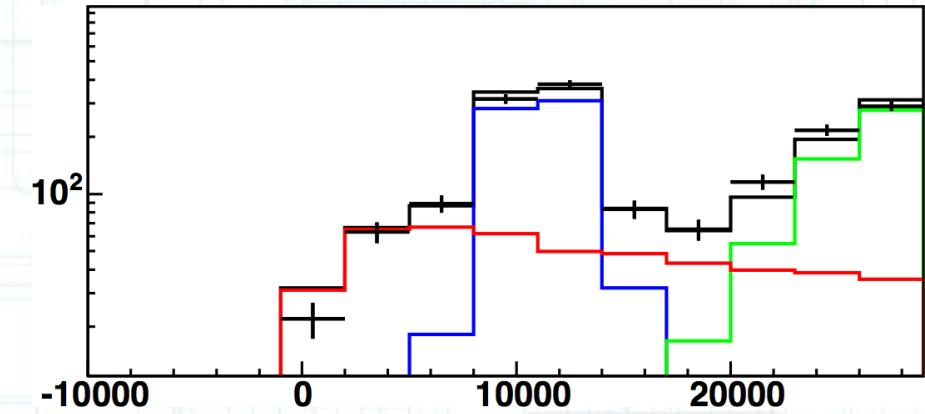
electron peaks at 100 MeV: **very bad**,  
since Ke3 endpoint is 230 MeV

A.Sibidanov – PHIPSI'09  
IHEP, Beijing, China, 13-16 October, 2009

# Ke2γ fit results

Projections on  $M\ell 2$  axis for 2 most populated  $E\gamma^*$  bins

+ data  
- fit  
Ke2γ  
Kμ2  
Ke3



13.10.2009

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IHEP, Beijing, China, 13-16 October, 2009

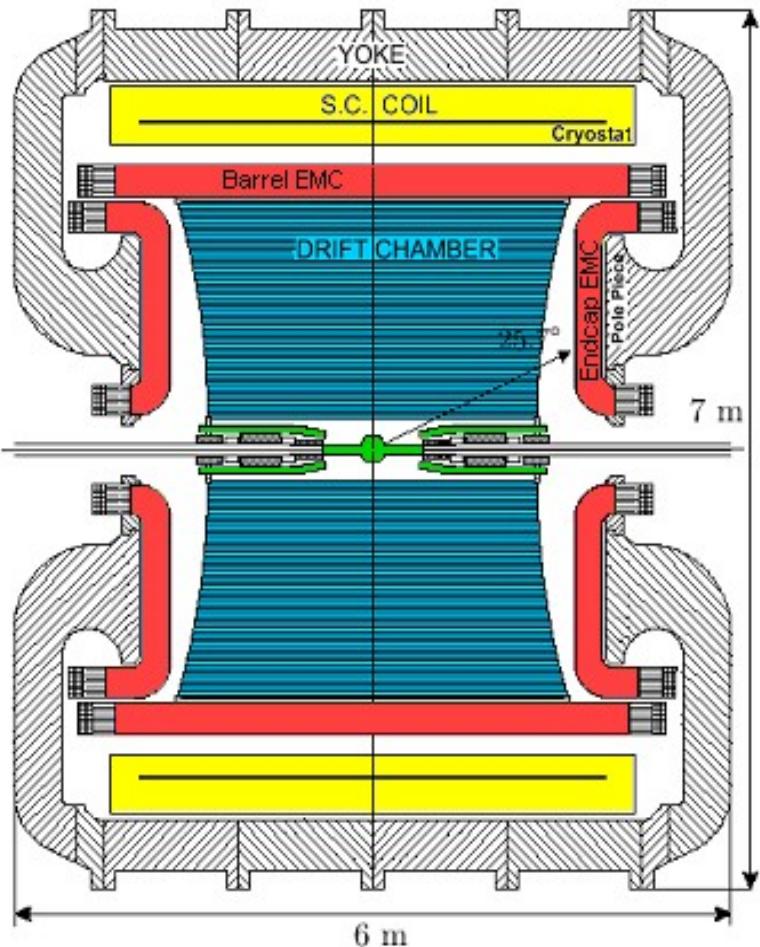
$1500 < E\gamma < 1750$  MeV

$$M_{\ell\ell} = 41931 \pm 32$$

$M\ell 2$

$$\chi^2/\text{ndf} = 870 [16.62]$$

# The KLOE experiment



**Be beam pipe (0.5 mm thick)**  
**Instrumented permanent magnet quadrupoles (32 PMTs)**

**Drift chamber (4 m  $\varnothing \times 3.3$  m)**

90%He+10% iC<sub>4</sub>H<sub>10</sub>, composite frame, 12582 stereo sense wires

**Electromagnetic calorimeter**

Lead/scintillating fibers

4880 PMTs

**Superconducting coil (5 m bore)**

$B = 0.52 \text{ T}$  ( $B dl = 2 \text{ T}\cdot\text{m}$ )