

Nature of Light Scalars through Photon-Photon Collisions

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ABSTRACT

The surprising thing is that arising almost 50 years ago from the linear sigma model (LSM) with spontaneously broken chiral symmetry, **the light scalar meson problem** has become central in the nonperturbative quantum chromodynamics (QCD) for it has been made clear that LSM could be the low energy realization of QCD.

First we review briefly signs of four-quark nature of light scalars.

Then we show that the light scalars are produced in the two photon collisions via four-quark transitions in contrast to the classic P wave tensor $q\bar{q}$ mesons that are produced via two-quark transitions

$\gamma\gamma \rightarrow q\bar{q}$. Thus we get new evidence of the four-quark nature of these states.

OUTLINE

1. Introduction.
2. Confinement, chiral dynamics and **light scalar mesons**.
3. Chiral shielding, $\sigma(600)$ and $f_0(980)$ in $\pi\pi \rightarrow \pi\pi$.
4. The ϕ -meson radiative decays **about light scalars**.
5. Light scalars in $\gamma\gamma$ collisions.
 - i) The forecast of the four-quark model.
 - ii) The $\sigma(600)$ and $f_0(980)$ production in $\gamma\gamma \rightarrow \pi\pi$.
 - iii) The $a_0(980)$ production in $\gamma\gamma \rightarrow \pi^0\eta$.
6. Conclusion.

Introduction

The scalar channels in the region up to 1 GeV became **a stumbling block** of **QCD**. The point is that both perturbation theory and sum rules do not work in these channels because there are not solitary resonances in this region.

At the same time the question on the nature of the light scalar mesons is major for understanding the mechanism of the chiral symmetry realization, arising from the confinement, and hence for understanding the confinement itself.

QCD, Chiral Limit, Confinement, σ -models

$$L = -(1/2)\text{Tr} (G_{\mu\nu}(x)G^{\mu\nu}(x)) + \bar{q}(x)(i\hat{D} - M)q(x).$$

M **mixes** Left and Right Spaces $q_L(x)$ and $q_R(x)$. But in **chiral limit** $M \rightarrow 0$ these spaces separate realizing $U_L(3) \times U_R(3)$ flavour symmetry.

As **Experiment** suggests, **Confinement** forms colourless observable hadronic fields and spontaneous breaking of chiral symmetry with massless pseudoscalar fields.

There are two possible scenarios for **QCD** at low energy.

1. $U_L(3) \times U_R(3)$ non-linear σ -model.

2. $U_L(3) \times U_R(3)$ linear σ -model.

The experimental nonet of the light scalar mesons suggests

$U_L(3) \times U_R(3)$ linear σ -model.

History of Light Scalar Mesons

Hunting the light σ and κ mesons had begun in the sixties already. But long-standing unsuccessful attempts to prove their existence in a **conclusive** way entailed general disappointment and an information on these states disappeared from PDG Reviews. One of principal reasons against the σ and κ mesons was the fact that both $\pi\pi$ and πK scattering phase shifts **do not pass** over 90° at putative resonance masses. [Meanwhile, there were discovered the narrow light scalar resonances, the isovector $a_0(980)$ and isoscalar $f_0(980)$.]

$SU_L(2) \times SU_R(2)$ linear σ model

Situation **changes** when we showed that in the **linear** σ -model

$$\begin{aligned} \mathcal{L} = & \frac{1}{2} [(\partial_\mu \sigma)^2 + (\partial_\mu \vec{\pi})^2] - \frac{m_\sigma^2}{2} \sigma^2 - \frac{m_\pi^2}{2} \vec{\pi}^2 \\ & - \frac{m_\sigma^2 - m_\pi^2}{8f_\pi^2} \left[(\sigma^2 + \vec{\pi}^2)^2 + 4f_\pi \sigma (\sigma^2 + \vec{\pi}^2) \right]^2 \end{aligned}$$

there is a **negative** background phase which **hides** the σ meson (1993, 1994). It has been made clear that **shielding** wide lightest scalar mesons in chiral dynamics is very **natural**. This idea was picked up and triggered new wave of theoretical and experimental searches for the σ and κ mesons.

Our approximation

Diagrammatic equation for $T_0^{0(tree)}$ with four external π lines. The left side is a circle labeled $T_0^{0(tree)}$. The right side is a sum of four diagrams enclosed in large square brackets, with $I=0$ at the top right and $l=0$ at the bottom right. The diagrams are:

- A simple four-point vertex (cross).
- A four-point vertex with a horizontal double line connecting the two internal vertices, labeled σ .
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Diagrammatic equation for T_0^0 with four external π lines. The left side is a circle labeled T_0^0 . The right side is a sum of two diagrams:

- A circle labeled $T_0^{0(tree)}$ with four external π lines.
- A diagram consisting of two circles, each labeled $T_0^{0(tree)}$, connected by a vertical dashed line. The top and bottom vertices of the dashed line are labeled π .

Our approximation

$$T_0^{0(\text{tree})} = \frac{m_\pi^2 - m_\sigma^2}{32\pi f_\pi^2} \left[5 - 3 \frac{m_\sigma^2 - m_\pi^2}{m_\sigma^2 - s} - 2 \frac{m_\sigma^2 - m_\pi^2}{s - 4m_\pi^2} \ln \left(1 + \frac{s - 4m_\pi^2}{m_\sigma^2} \right) \right],$$

$$T_0^0 = \frac{T_0^{0(\text{tree})}}{1 - i\rho_{\pi\pi} T_0^{0(\text{tree})}} = \frac{e^{2i(\delta_{\text{bg}} + \delta_{\text{res}})} - 1}{2i\rho_{\pi\pi}} = \frac{1}{\rho_{\pi\pi}} \left(\frac{e^{2i\delta_{\text{bg}}} - 1}{2i} \right) + e^{2i\delta_{\text{bg}}} T_{\text{res}},$$

$$\rho_{\pi\pi} \equiv \rho_{\pi\pi}(m) = \sqrt{1 - 4m_\pi^2/m^2}.$$

Our approximation

$$T_{res} = \frac{1}{\rho_{\pi\pi}} \cdot \frac{\sqrt{s}\Gamma_{res}(s)}{M_{res}^2 - s + \text{Re}\Pi_{res}(M_{res}^2) - \Pi_{res}(s)} = \frac{e^{2i\delta_{res}} - 1}{2i\rho_{\pi\pi}}$$

$$T_{bg} = \frac{e^{2i\delta_{bg}} - 1}{2i\rho_{\pi\pi}} = \frac{\lambda(s)}{1 - i\rho_{\pi\pi}\lambda(s)}, \quad \lambda(s) = \frac{m_\pi^2 - m_\sigma^2}{32\pi f_\pi^2} \left[5 - \right.$$

$$\left. - 2 \frac{m_\sigma^2 - m_\pi^2}{s - 4m_\pi^2} \ln \left(1 + \frac{s - 4m_\pi^2}{m_\sigma^2} \right) \right], \quad g_{\sigma\pi^+\pi^-} = -\frac{m_\sigma^2 - m_\pi^2}{f_\pi}$$

$$\text{Im}\Pi_{res}(s) = \frac{g_{res}^2(s)}{16\pi} \rho_{\pi\pi}, \quad \text{Re}\Pi_{res}(s) = -\frac{g_{res}^2(s)}{16\pi} \lambda(s) \rho_{\pi\pi}^2,$$

$$g_{res}(s) = \frac{g_{\sigma\pi\pi}}{|1 - i\rho_{\pi\pi}\lambda(s)|}, \quad M_{res}^2 = m_\sigma^2 - \text{Re}\Pi_{res}(M_{res}^2).$$

Results in our approximation

$$T_0^2 = \frac{T_0^{2(tree)}}{1 - i\rho_{\pi\pi}T_2^{0(tree)}} = \frac{e^{2i\delta_0^2} - 1}{2i\rho_{\pi\pi}}, \quad g_{\sigma\pi\pi} = \sqrt{\frac{3}{2}} g_{\sigma\pi^+\pi^-},$$

$$T_0^{2(tree)} = \frac{m_\pi^2 - m_\sigma^2}{32\pi f_\pi^2} \left[2 - 2 \frac{m_\sigma^2 - m_\pi^2}{s - 4m_\pi^2} \ln \left(1 + \frac{s - 4m_\pi^2}{m_\sigma^2} \right) \right].$$

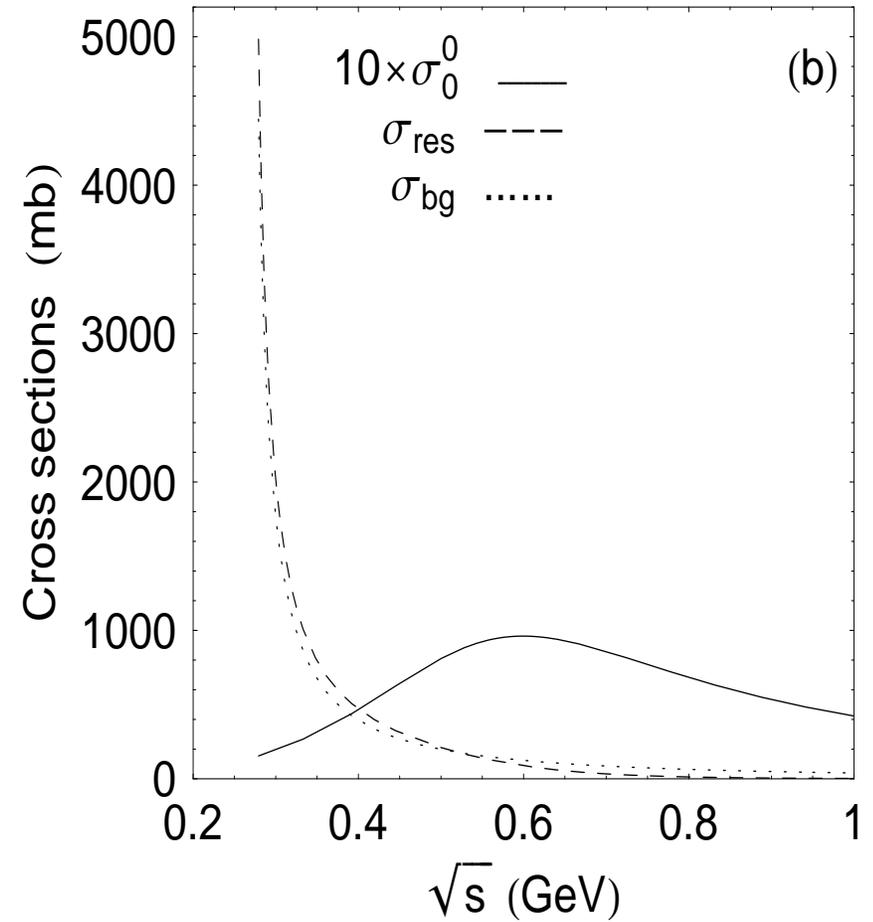
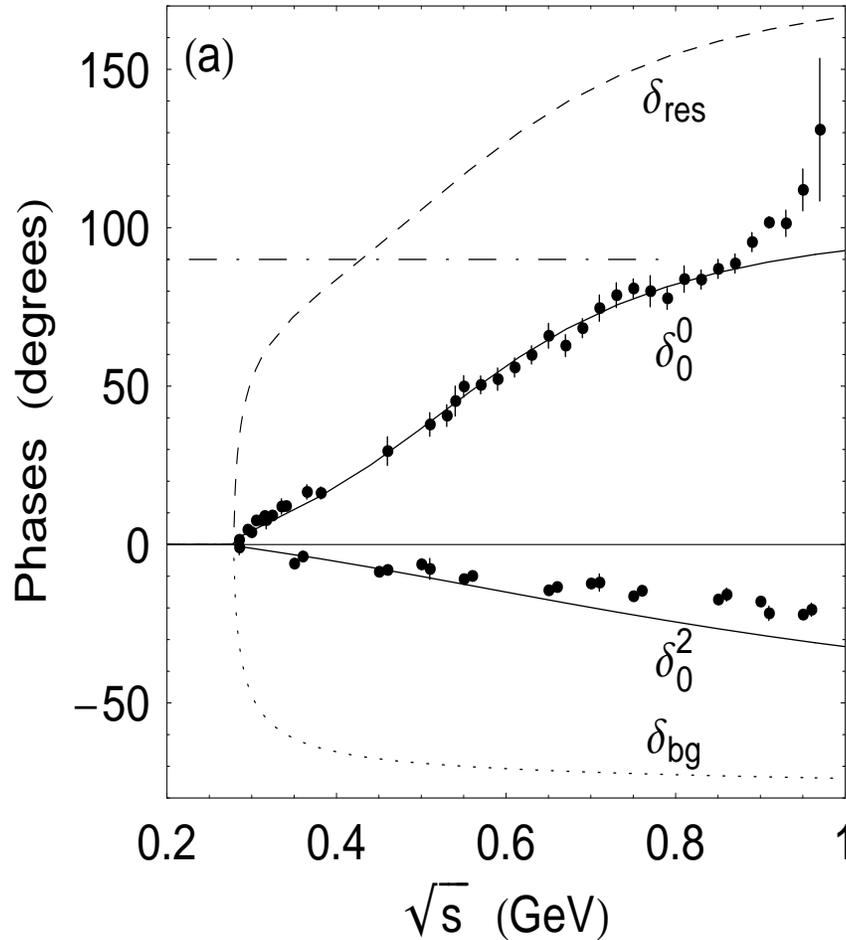
$$M_{res} = 0.43 \text{ GeV}, \quad \Gamma_{res}(M_{res}^2) = 0.67 \text{ GeV}, \quad m_\sigma = 0.93 \text{ GeV},$$

$$\Gamma_{res}^{norm}(M_{res}^2) = \frac{\Gamma_{res}(M_{res}^2)}{(1 + d\text{Re}\Pi_{res}(s)/ds|_{s=M_{res}^2})} = 0.53 \text{ GeV},$$

$$\Gamma_{res}(s) = \frac{g_{res}^2(s)}{16\pi\sqrt{s}} \rho_{\pi\pi}, \quad a_0^0 = 0.18 m_\pi^{-1}, \quad a_0^2 = -0.04 m_\pi^{-1},$$

$$g_{res}(M_{res}^2)/g_{\sigma\pi\pi} = 0.33, \quad (s_A)_0^0 = 0.45 m_\pi^2, \quad (s_A)_0^2 = 2.02 m_\pi^2.$$

Chiral Shielding in $\pi\pi \rightarrow \pi\pi$



The σ model. Our approximation. $\delta = \delta_{res} + \delta_{bg}$.

The σ pole in $\pi\pi \rightarrow \pi\pi$

$$T_0^0 \rightarrow \frac{g_\pi^2}{s - s_R},$$

$$g_\pi^2 = (0.12 + i0.21)\text{GeV}^2,$$

$$s_R = (0.21 - i0.26)\text{GeV}^2,$$

$$\sqrt{s_R} = M_R - i\frac{\Gamma_R}{2} = (0.52 - i0.25)\text{GeV}.$$

Considering the residue of the σ pole in T_0^0 as the square of its coupling constant to the $\pi\pi$ channel is not a clear guide to understand the σ meson nature for its great obscure imaginary part.

The σ propagator

$$\frac{1}{D_\sigma(s)} = \frac{1}{M_{res}^2 - s + \text{Re}\Pi_{res}(M_{res}^2) - \Pi_{res}(s)}.$$

The σ meson self-energy $\Pi_{res}(s)$ is caused by the intermediate $\pi\pi$ states, that is, by **the four-quark intermediate states**. This contribution shifts the Breit-Wigner (BW) mass greatly $m_\sigma - M_{res} = 0.50$ GeV. So, half the BW mass is determined by **the four-quark contribution** at least. The imaginary part dominates the propagator modulus in the region $300 \text{ MeV} < \sqrt{s} < 600 \text{ MeV}$. So, the σ field is described by its four-quark component at least in this energy (**virtuality**) region.

Chiral shielding in $\gamma\gamma \rightarrow \pi^+\pi^-$

$$\begin{aligned} T_S(\gamma\gamma \rightarrow \pi^+\pi^-) &= T_S^{Born}(\gamma\gamma \rightarrow \pi^+\pi^-) \\ &+ 8\alpha I_{\pi^+\pi^-} T_S(\pi^+\pi^- \rightarrow \pi^+\pi^-) \\ &= T_S^{Born}(\gamma\gamma \rightarrow \pi^+\pi^-) + 8\alpha I_{\pi^+\pi^-} \left(\frac{2}{3} T_0^0 + \frac{1}{3} T_0^2 \right) \end{aligned}$$

in elastic region

$$\begin{aligned} &= \frac{2}{3} e^{i\delta_0^0} \left\{ T_S^{Born}(\gamma\gamma \rightarrow \pi^+\pi^-) \cos \delta_0^0 + 8 \frac{\alpha}{\rho_{\pi\pi}} \text{Re} I_{\pi^+\pi^-} \sin \delta_0^0 \right\} \\ &+ \frac{1}{3} e^{i\delta_0^2} \left\{ T_S^{Born}(\gamma\gamma \rightarrow \pi^+\pi^-) \cos \delta_0^2 + 8 \frac{\alpha}{\rho_{\pi\pi}} \text{Re} I_{\pi^+\pi^-} \sin \delta_0^2 \right\} \end{aligned}$$

Chiral shielding in $\gamma\gamma \rightarrow \pi^0\pi^0$

$$T_S(\gamma\gamma \rightarrow \pi^0\pi^0) = 8\alpha I_{\pi^+\pi^-} T_S(\pi^+\pi^- \rightarrow \pi^0\pi^0)$$

$$= 8\alpha I_{\pi^+\pi^-} \left(\frac{2}{3} T_0^0 - \frac{2}{3} T_0^2 \right)$$

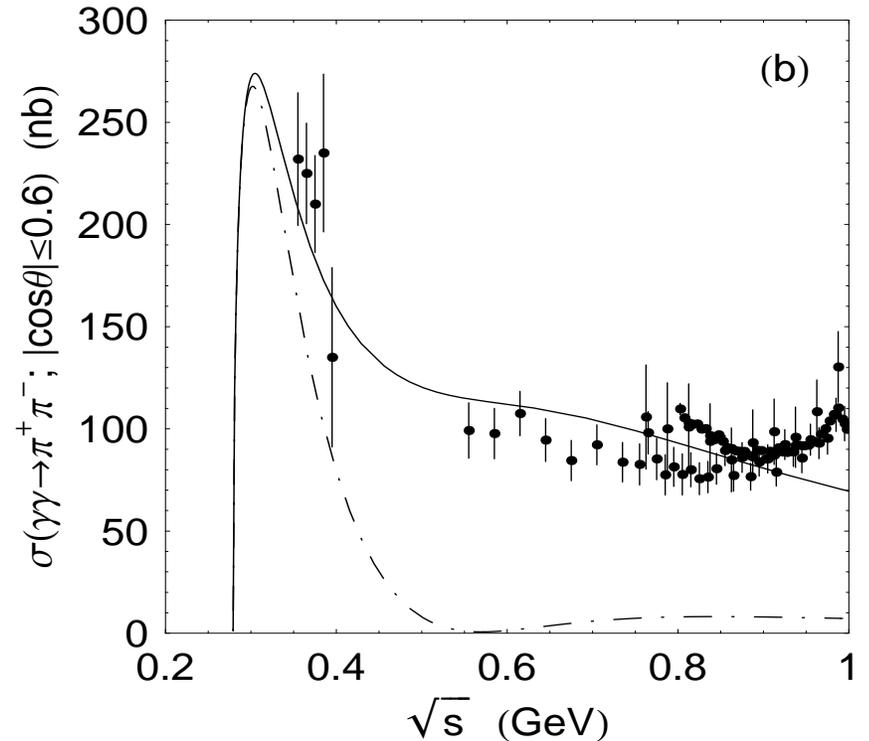
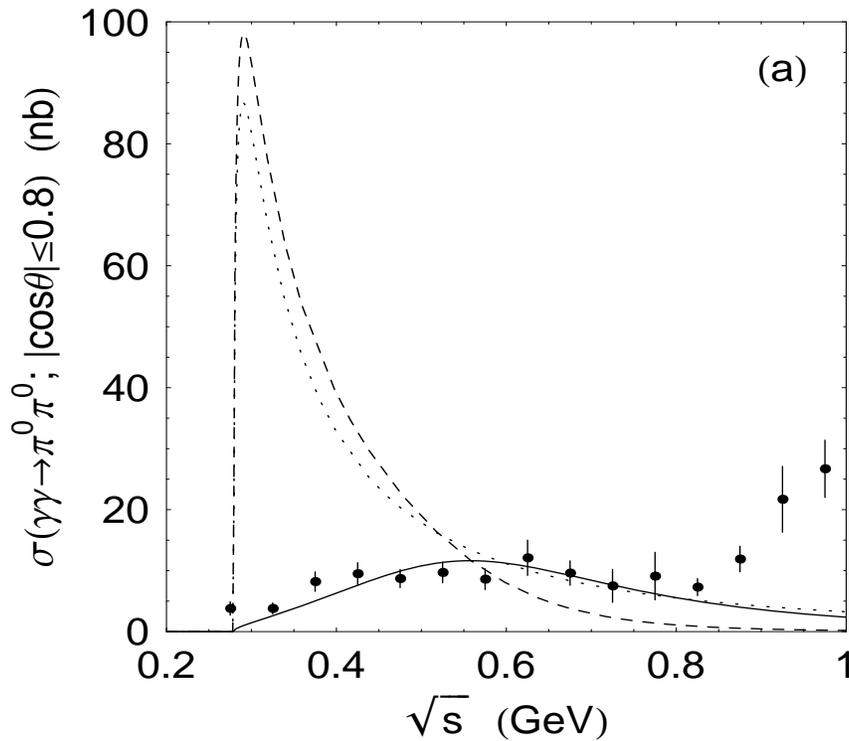
$$= \frac{2}{3} e^{i\delta_0^0} \left\{ T_S^{\text{Born}}(\gamma\gamma \rightarrow \pi^+\pi^-) \cos \delta_0^0 + 8 \frac{\alpha}{\rho_{\pi\pi}} \text{Re} I_{\pi^+\pi^-} \sin \delta_0^0 \right\}$$

$$- \frac{2}{3} e^{i\delta_0^2} \left\{ T_S^{\text{Born}}(\gamma\gamma \rightarrow \pi^+\pi^-) \cos \delta_0^2 + 8 \frac{\alpha}{\rho_{\pi\pi}} \text{Re} I_{\pi^+\pi^-} \sin \delta_0^2 \right\}$$

$$I_{\pi^+\pi^-} = \frac{m_\pi^2}{s} \left(\pi + i \ln \frac{1 + \rho_{\pi\pi}}{1 - \rho_{\pi\pi}} \right)^2 - 1, \quad s \geq 4m_\pi^2,$$

$$T_S^{\text{Born}}(\gamma\gamma \rightarrow \pi^+\pi^-) = \frac{8\alpha}{\rho_{\pi^+\pi^-}} \text{Im} I_{\pi^+\pi^-}.$$

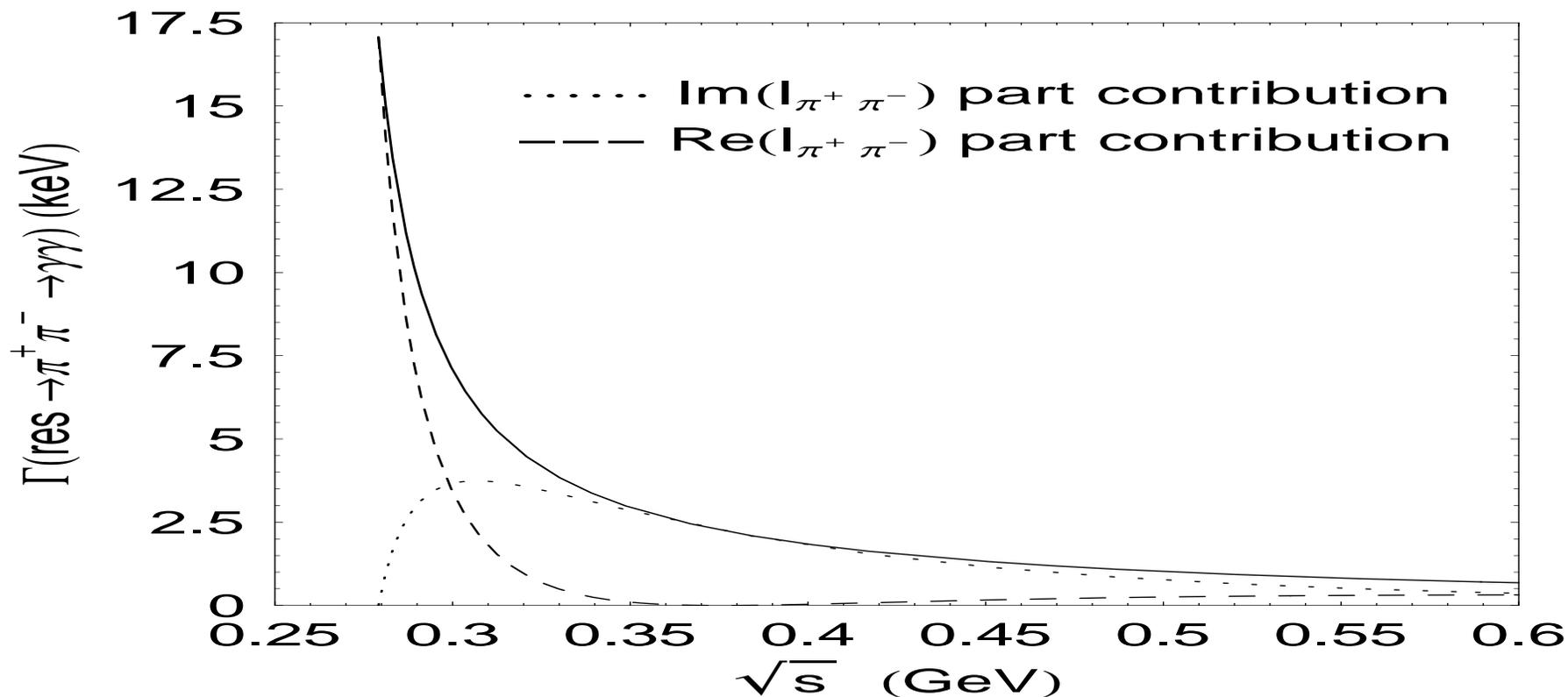
Chiral Shielding in $\gamma\gamma \rightarrow \pi\pi$



(a) The solid, dashed, and dotted lines are $\sigma_S(\gamma\gamma \rightarrow \pi^0\pi^0)$, $\sigma_{res}(\gamma\gamma \rightarrow \pi^0\pi^0)$, and $\sigma_{bg}(\gamma\gamma \rightarrow \pi^0\pi^0)$.

(b) The dashed-dotted line is $\sigma_S(\gamma\gamma \rightarrow \pi^+\pi^-)$. The solid line includes the higher waves from $T^{Born}(\gamma\gamma \rightarrow \pi^+\pi^-)$.

The $\sigma \rightarrow \gamma\gamma$ decay.



$$g(\sigma \rightarrow \pi^+ \pi^- \rightarrow \gamma\gamma, s) = (\alpha/2\pi) I_{\pi^+ \pi^-} \times g_{\text{res} \pi^+ \pi^-}(s),$$

$$\Gamma(\sigma \rightarrow \pi^+ \pi^- \rightarrow \gamma\gamma, s) = \frac{1}{16\pi\sqrt{s}} |g(\sigma \rightarrow \pi^+ \pi^- \rightarrow \gamma\gamma, s)|^2$$

Four-quark transition $\sigma \rightarrow \gamma\gamma$

So, the the $\sigma \rightarrow \gamma\gamma$ decay is described by the triangle $\pi^+\pi^-$ -loop diagram $res \rightarrow \pi^+\pi^- \rightarrow \gamma\gamma (I_{\pi^+\pi^-})$.
Consequently, it is due to the four-quark transition because we imply a low energy realization of the two-flavour QCD by means of the the $SU_L(2) \times SU_R(2)$ linear σ model. As the previous Fig. suggests, the real intermediate $\pi^+\pi^-$ state dominates in $g(res \rightarrow \pi^+\pi^- \rightarrow \gamma\gamma)$ in the σ region $\sqrt{s} < 0.6$ GeV.

Thus the picture in the physical region is clear and informative. But, what about the pole in the complex s -plane? Does the pole residue reveal the σ indeed?

The σ pole in $\gamma\gamma \rightarrow \pi\pi$

$$\frac{1}{16\pi} \sqrt{\frac{3}{2}} T_S(\gamma\gamma \rightarrow \pi^0\pi^0) \rightarrow \frac{g_\gamma g_\pi}{s - s_R},$$

$$g_\gamma g_\pi = (-0.45 - i0.19) \times 10^{-3} \text{ GeV}^2,$$

$$g_\gamma/g_\pi = (-1.61 + i1.21) \times 10^{-3},$$

$$\Gamma(\sigma \rightarrow \gamma\gamma) = |g_\gamma|^2/M_R \approx 2 \text{ keV}.$$

It is hard to believe that anybody could learn the complex but physically clear dynamics of the $\sigma \rightarrow \gamma\gamma$ decay described above from the residues of the σ pole.

First Lessons

Heiri Leutwyler and collaborators obtained

$$\sqrt{s_R} = M_R - i\Gamma_R/2 = \left(441_{-8}^{+16} - i272_{-9}^{+12.5}\right) \times \text{MeV}$$

with the help of the Roy equation.

Our result agrees with the above only qualitatively.

$$\sqrt{s_R} = M_R - i\Gamma_R/2 = (518 - i250) \times \text{MeV}.$$

This is natural, because our approximation gives only a semiquantitative description of the data at $\sqrt{s} < 0.4 \text{ GeV}$. We do not regard also for effects of the $K\bar{K}$ channel, the $f_0(980)$ meson, and so on, that is, do not consider the $SU_L(3) \times SU_R(3)$ linear σ model.

First Lessons

Could the above scenario incorporate the primary lightest scalar **Bob Jaffe four-quark state**? Certainly the direct coupling of this state to $\gamma\gamma$ via neutral vector pairs ($\rho^0\rho^0$ and $\omega\omega$), contained in its wave function, is negligible

$$\Gamma(q^2\bar{q}^2 \rightarrow \rho^0\rho^0 + \omega\omega \rightarrow \gamma\gamma) \approx 10^{-3} \text{ keV}$$

as we showed in 1982. But its coupling to $\pi\pi$ is strong and leads

to $\Gamma(q^2\bar{q}^2 \rightarrow \pi^+\pi^- \rightarrow \gamma\gamma)$ similar to

$\Gamma(res \rightarrow \pi^+\pi^- \rightarrow \gamma\gamma)$ in the above Fig..

Let us add to $T_S(\gamma\gamma \rightarrow \pi^0\pi^0)$ the amplitude for the the direct coupling of σ to $\gamma\gamma$ conserving unitarity

$$T_{direct}(\gamma\gamma \rightarrow \pi^0\pi^0) = sg_{\sigma\gamma\gamma}^{(0)}g_{res}(s)e^{i\delta_{bg}} / D_{res}(s),$$

where $g_{\sigma\gamma\gamma}^{(0)}$ is the direct coupling constant of σ to $\gamma\gamma$, the factor s

is caused by gauge invariance.

First Lessons

Fitting the $\gamma\gamma \rightarrow \pi^0\pi^0$ data gives a negligible value of $g_{\sigma\gamma\gamma}^{(0)}$,

$$\Gamma_{\sigma\gamma\gamma}^{(0)} = \left| M_{res}^2 g_{\sigma\gamma\gamma}^{(0)} \right|^2 / (16\pi M_{res}) \approx 0.0034 \text{ keV},$$

in astonishing agreement with our prediction (1982).

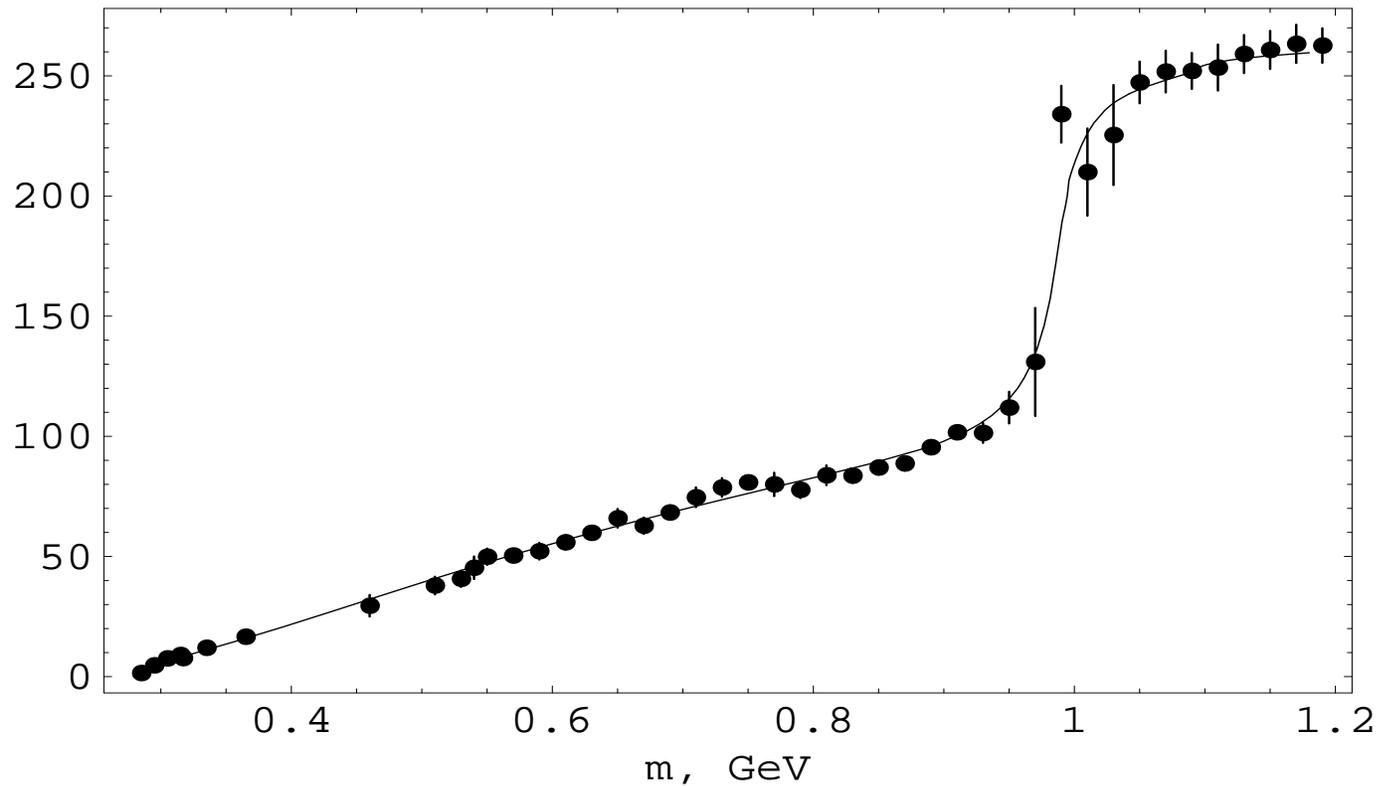
The majority of current investigations of the mass spectra in scalar channels does not study **particle production mechanisms**. That is why such investigations are **only preprocessing experiments**, and the derivable information is **very relative**.

The only progress in understanding the particle production mechanisms could essentially advance us in revealing the light scalar meson nature, as is evident from the foregoing.

Troubles and Expectancies

In theory the **principal** problem is **impossibility** to use the linear σ -model in the **tree level** approximation inserting widths into σ meson propagators because such an approach **breaks** the both **unitarity** and **Adler** self-consistency conditions. The **comparison** with the experiment **requires** the **non-perturbative** calculation of the process amplitudes. **Nevertheless**, now there are the possibilities to estimate **odds** of the $U_L(3) \times U_R(3)$ linear σ -model to **underlie** physics of light scalar mesons **in phenomenology**, taking into account **the idea of chiral shielding**, our treatment of $\sigma(600)$ - $f_0(980)$ mixing based on quantum field theory ideas, and Adler's conditions.

Phenomenological Treatment, $\delta_0^0 = \delta_B^{\pi\pi} + \delta_{res}$



$$g_{\sigma\pi^+\pi^-}^2/4\pi = 0.99 \text{ GeV}^2, \quad g_{\sigma K^+K^-}^2/4\pi = 2 \cdot 10^{-4} \text{ GeV}^2$$

$$g_{f_0\pi^+\pi^-}^2/4\pi = 0.12 \text{ GeV}^2, \quad g_{f_0 K^+K^-}^2/4\pi = 1.04 \text{ GeV}^2$$

$$m_\sigma = 679 \text{ MeV}, \quad \Gamma_\sigma = 498 \text{ MeV}, \quad m_{f_0} = 989 \text{ MeV},$$

$$\text{the } l = \text{I} = 0 \text{ } \pi\pi \text{ scattering length } a_0^0 = 0.223 m_{\pi^+}^{-1}$$

Four-quark Model

The **nontrivial** nature of the well-established light scalar resonances $f_0(980)$ and $a_0(980)$ is no longer denied practically anybody. As for the nonet as a whole, even a **cursory** look at PDG Review gives an idea of the **four-quark** structure of the light scalar meson nonet, $\sigma(600)$, $\kappa(700 - 900)$, $f_0(980)$, and $a_0(980)$, inverted in comparison with the classical ***P*-wave** $q\bar{q}$ tensor meson nonet, $f_2(1270)$, $a_2(1320)$, $K_2^*(1420)$, $f_2'(1525)$. Really, while the scalar nonet **cannot** be treated as the ***P*-wave** $q\bar{q}$ nonet in the naive quark model, it can be easy understood as the $q^2\bar{q}^2$ nonet, where σ has **no** strange quarks, κ has the **s** quark, f_0 and a_0 have the **$s\bar{s}$ -pair**. Similar states were found by Jaffe in 1977 in the MIT bag.

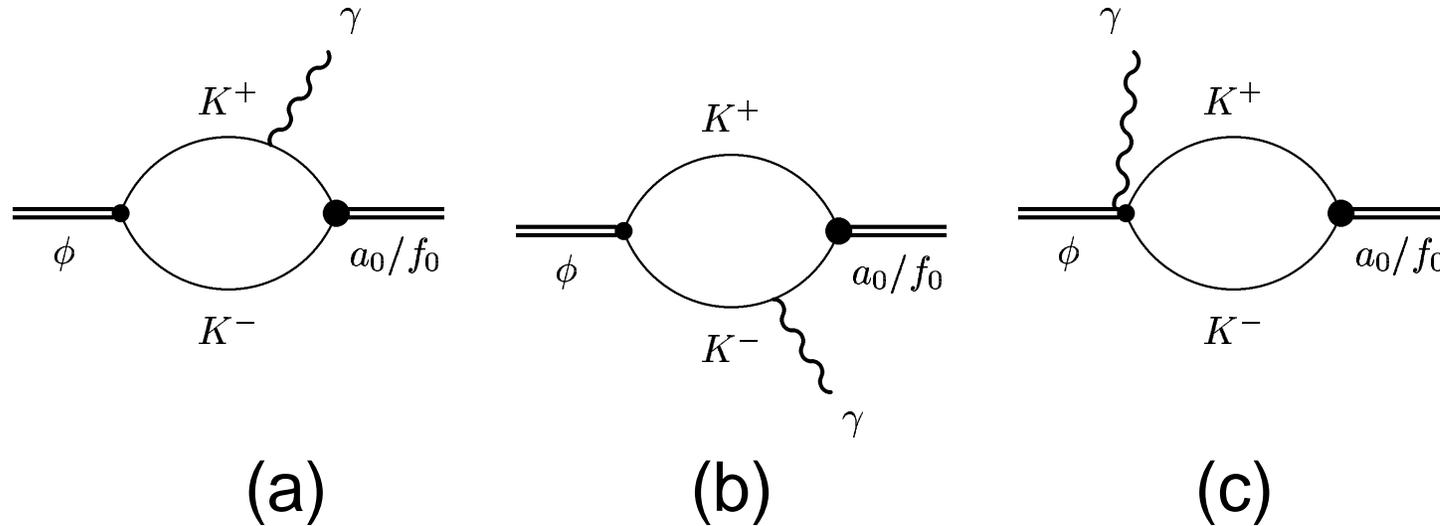
Radiative Decays of ϕ -Meson

Ten years later (1989) we showed that $\phi \rightarrow \gamma a_0 \rightarrow \gamma \pi \eta$ and $\phi \rightarrow \gamma f_0 \rightarrow \gamma \pi \pi$ can shed light on the problem of $a_0(980)$ and $f_0(980)$ mesons.

Now these decays are studied not only theoretically but also experimentally. The first measurements (1998, 2000) were reported by SND and CMD-2. After (2002) they were studied by KLOE in agreement with the Novosibirsk data but with a considerably smaller error.

Note that $a_0(980)$ is produced in the radiative ϕ meson decay as intensively as $\eta'(958)$ containing $\approx 66\%$ of $s\bar{s}$, responsible for $\phi \approx s\bar{s} \rightarrow \gamma s\bar{s} \rightarrow \gamma \eta'(958)$. It is a clear qualitative argument for the presence of the $s\bar{s}$ pair in the isovector $a_0(980)$ state, i.e., for its four-quark nature.

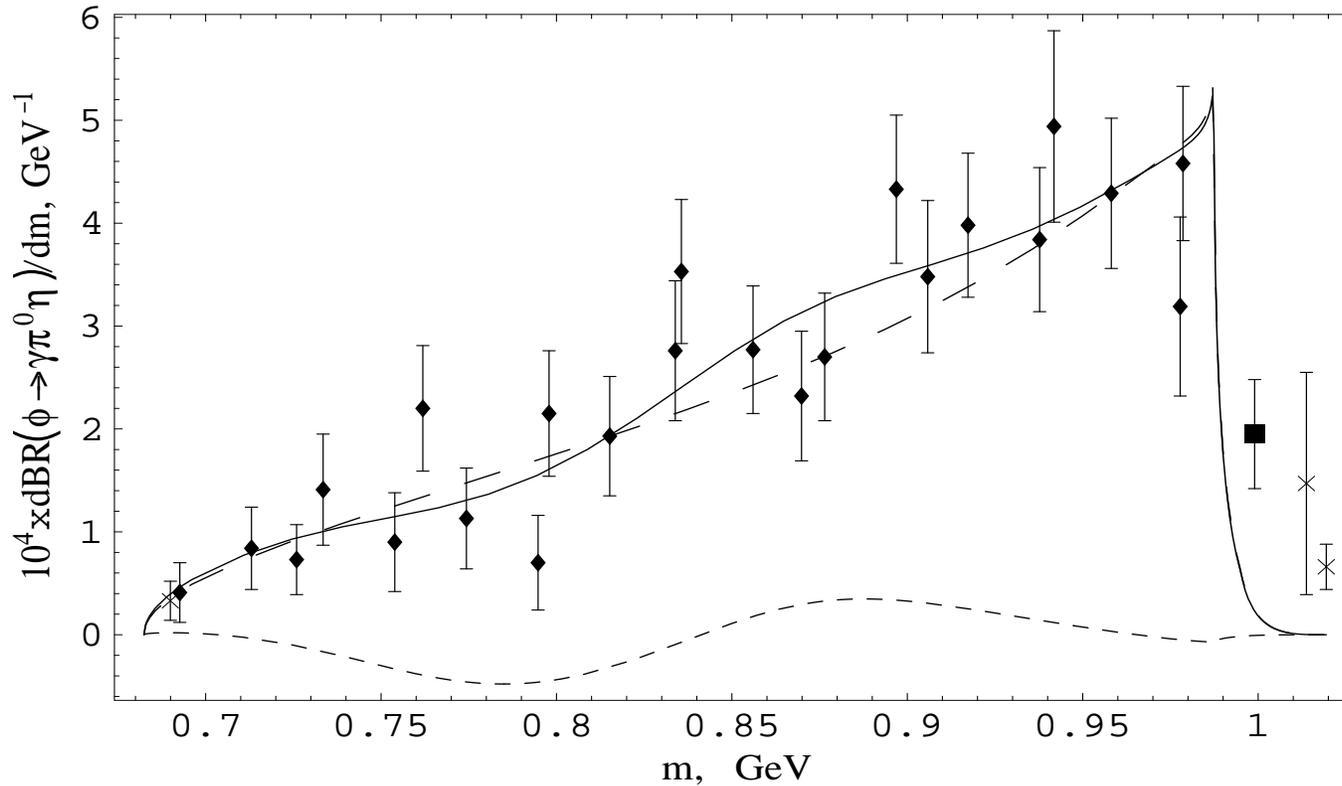
$K^+ K^-$ -Loop Model



When basing the experimental investigations, we suggested one-loop model $\phi \rightarrow K^+ K^- \rightarrow \gamma a_0/f_0$. This model is used in the data treatment and is ratified by experiment.

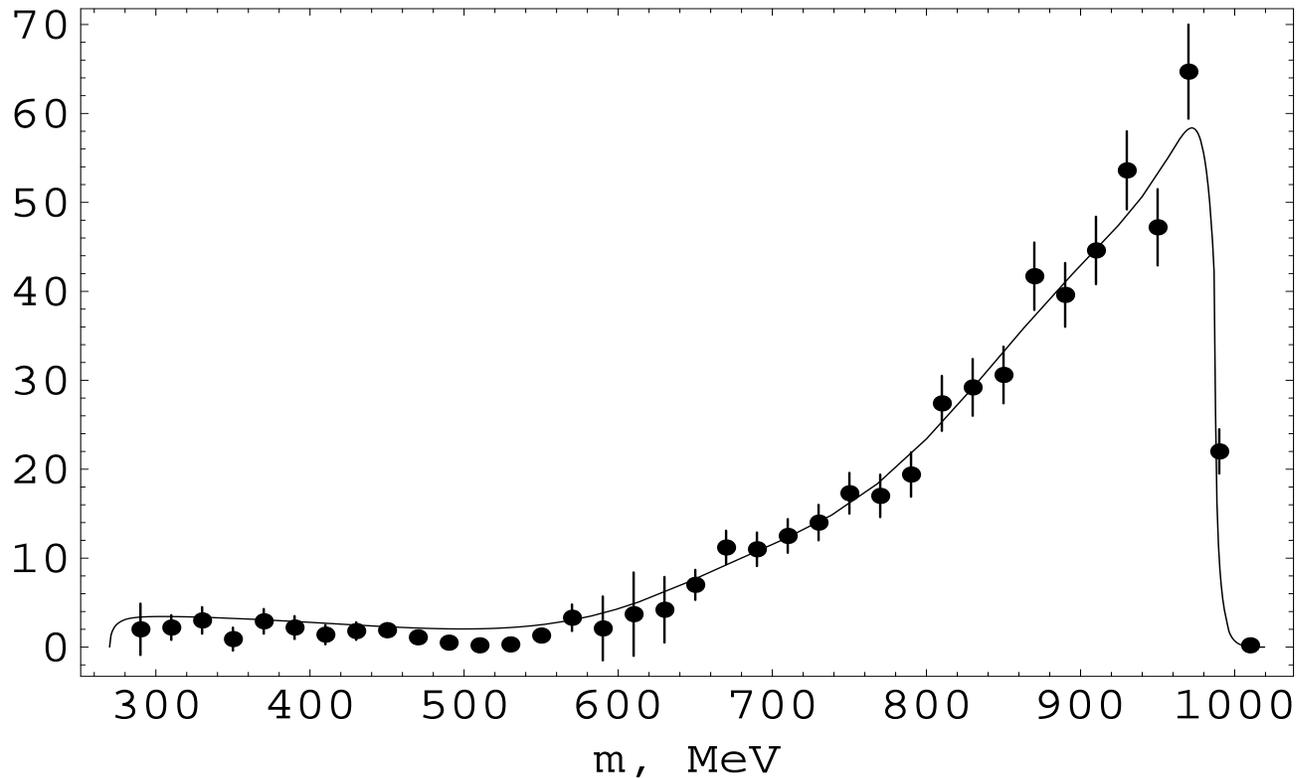
Gauge invariance gives the conclusive arguments in favor of the $K^+ K^-$ - loop transition as the principal mechanism of $a_0(980)$ and $f_0(980)$ meson production in the ϕ radiative decays.

$\phi \rightarrow \gamma\pi^0\eta$, KLOE



$$\begin{aligned}
 & \frac{d\text{BR}(\phi \rightarrow K^+K^- \rightarrow \gamma a_0 \rightarrow \gamma\pi^0\eta, m)}{dm} = \\
 & = \frac{4|g(m)|^2 \omega(m) p_{\pi\eta}(m)}{\Gamma_\phi 3(4\pi)^3 m_\phi^2} \left| \frac{g_{a_0 K^+K^-} - g_{a_0 \pi\eta}}{D_{a_0}(m)} \right|^2
 \end{aligned}$$

$\phi \rightarrow \gamma\pi^0\pi^0$, KLOE



$$\begin{aligned} & \frac{dBR(\phi \rightarrow K^+K^- \rightarrow \gamma(\sigma + f_0) \rightarrow \gamma\pi^0\pi^0, m)}{dm} = \\ & = \frac{16|g(m)|^2\omega(m)p_{\pi\eta}(m)}{\Gamma_\phi 3\pi m_\phi^2} |T_0^0(K^+K^- \rightarrow \pi^0\pi^0)|^2 \end{aligned}$$

$K^+ K^-$ -Loop Mechanism is established

In truth this means that $a_0(980)$ and $f_0(980)$ are seen in the radiative decays of ϕ meson owing to $K^+ K^-$ intermediate state.

So, the mechanism of production of $a_0(980)$ and $f_0(980)$ mesons in the ϕ radiative decays is established at a physical level of proof.

WE ARE DEALING WITH THE FOUR-QUARK TRANSITION.

A radiative four-quark transition between two $q\bar{q}$ states requires creation and annihilation of an additional $q\bar{q}$ pair, i.e., such a transition is forbidden according to the **OZI** rule, while a radiative four-quark transition between $q\bar{q}$ and $q^2\bar{q}^2$ states requires only creation of an additional $q\bar{q}$ pair, i.e., such a transition is allowed according to the **OZI** rule. The large N_C expansion supports this conclusion.

$a_0(980)/f_0(980) \rightarrow \gamma\gamma$ & $q^2\bar{q}^2$ -Model

Twenty seven years ago we predicted the suppression of $a_0(980) \rightarrow \gamma\gamma$ and $f_0(980) \rightarrow \gamma\gamma$ in the $q^2\bar{q}^2$ MIT model,
 $\Gamma(a_0(980) \rightarrow \gamma\gamma) \sim \Gamma(f_0(980) \rightarrow \gamma\gamma) \sim 0.27 \text{ keV}$.

Experiment supported this prediction

$$\Gamma(a_0 \rightarrow \gamma\gamma) = (0.19 \pm 0.07_{-0.07}^{+0.1}) / B(a_0 \rightarrow \pi\eta) \text{ keV, Crystal Ball}$$

$$\Gamma(a_0 \rightarrow \gamma\gamma) = (0.28 \pm 0.04 \pm 0.1) / B(a_0 \rightarrow \pi\eta) \text{ keV, JADE.}$$

$$\Gamma(f_0 \rightarrow \gamma\gamma) = (0.31 \pm 0.14 \pm 0.09) \text{ keV, Crystal Ball,}$$

$$\Gamma(f_0 \rightarrow \gamma\gamma) = (0.24 \pm 0.06 \pm 0.15) \text{ keV, MARK II.}$$

When in the $q\bar{q}$ model it was anticipated

$$\begin{aligned} \Gamma(a_0 \rightarrow \gamma\gamma) &= (1.5 - 5.9)\Gamma(a_2 \rightarrow \gamma\gamma) \\ &= (1.5 - 5.9)(1.04 \pm 0.09) \text{ keV.} \end{aligned}$$

$$\begin{aligned} \Gamma(f_0 \rightarrow \gamma\gamma) &= (1.7 - 5.5)\Gamma(f_2 \rightarrow \gamma\gamma) \\ &= (1.7 - 5.5)(2.8 \pm 0.4) \text{ keV.} \end{aligned}$$

Scalar Nature and Production Mechanisms in $\gamma\gamma$ collisions

Recently the experimental investigations have made great qualitative advance. The Belle Collaboration published data on $\gamma\gamma \rightarrow \pi^+\pi^-$ (2007), $\gamma\gamma \rightarrow \pi^0\pi^0$ (2008), and $\gamma\gamma \rightarrow \pi^0\eta$ (2009), whose statistics are more huge. They not only proved the theoretical expectations based on the four-quark nature of the light scalar mesons, but also have allowed to elucidate the principal mechanisms of these processes. Specifically, the direct coupling constants of the $\sigma(600)$, $f_0(980)$, and $a_0(980)$ resonances with the $\gamma\gamma$ system are small with the result that their decays in the two photon are the four-quark transitions caused by the rescatterings $\sigma \rightarrow \pi^+\pi^- \rightarrow \gamma\gamma$, $f_0(980) \rightarrow K^+K^- \rightarrow \gamma\gamma$ and $a_0(980) \rightarrow K^+K^- \rightarrow \gamma\gamma$

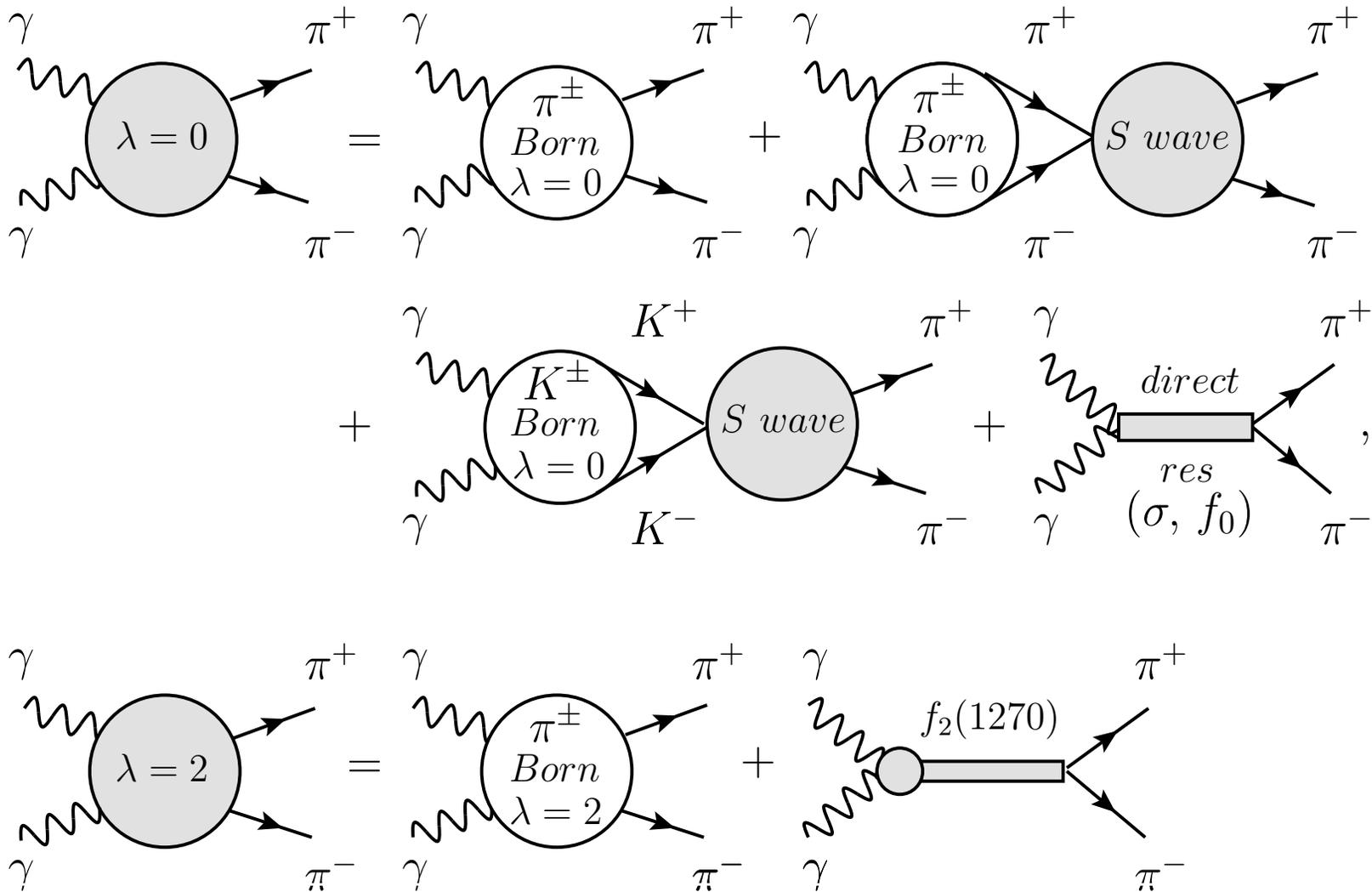
Scalar Nature and Production Mechanisms in $\gamma\gamma$ collisions

in contrast to the two-photon decays of the classic P wave tensor $q\bar{q}$ mesons $a_2(1320)$, $f_2(1270)$ and $f_2'(1525)$, which are caused by the direct two-quark transitions $q\bar{q} \rightarrow \gamma\gamma$ in the main. As a result the practically model-independent prediction of the $q\bar{q}$ model $g_{f_2\gamma\gamma}^2 : g_{a_2\gamma\gamma}^2 = 25 : 9$ agrees with experiment rather well.

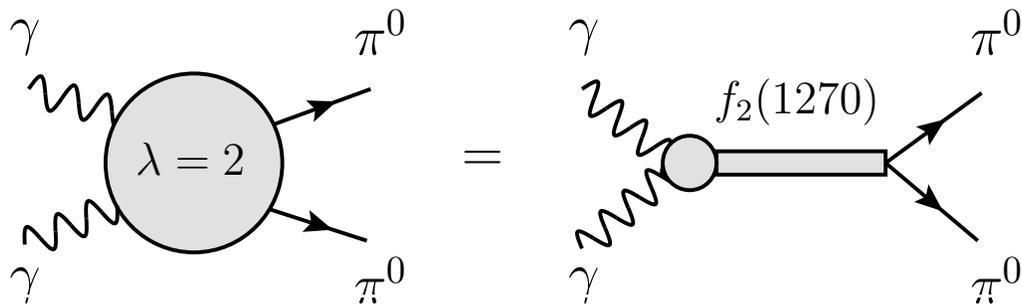
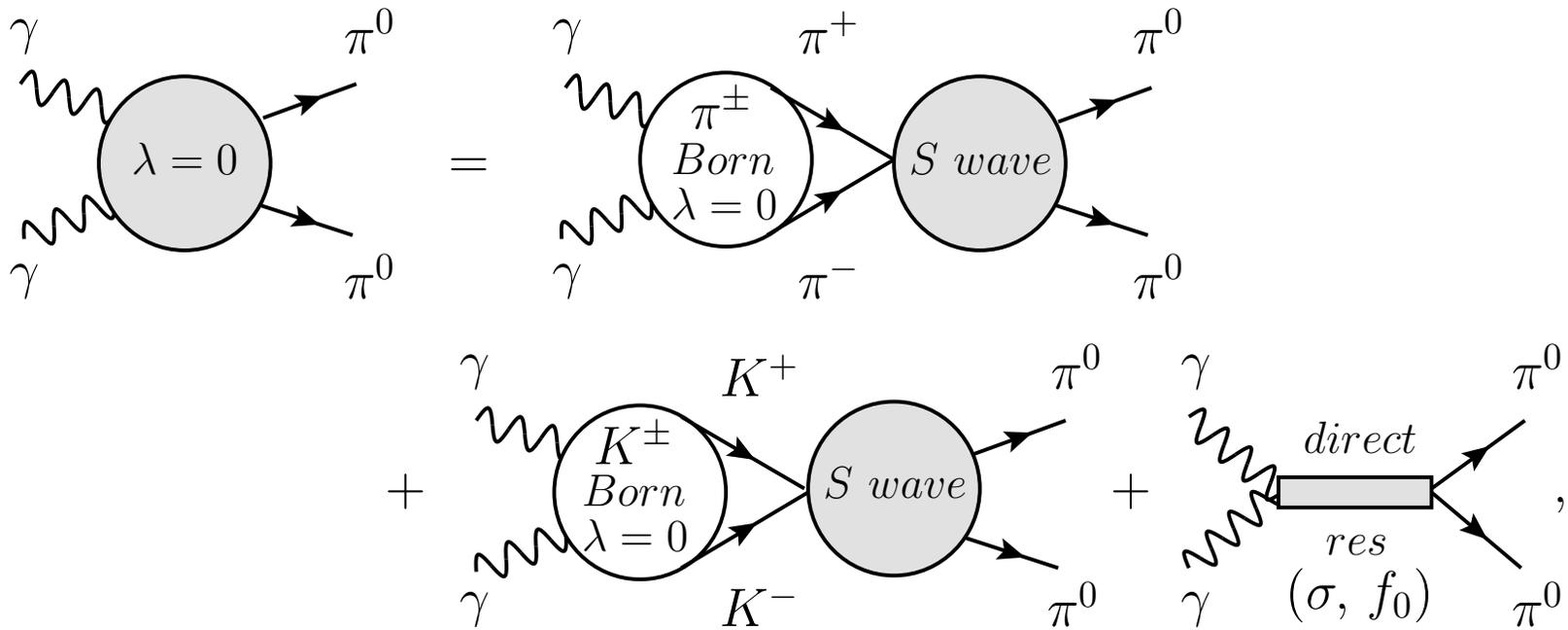
The two-photon light scalar widths averaged over resonance mass distributions $\langle \Gamma_{f_0 \rightarrow \gamma\gamma} \rangle_{\pi\pi} \approx 0.19$ keV, $\langle \Gamma_{a_0 \rightarrow \gamma\gamma} \rangle_{\pi\eta} \approx 0.3$ keV and $\langle \Gamma_{\sigma \rightarrow \gamma\gamma} \rangle_{\pi\pi} \approx 0.45$ keV.

As to the ideal $q\bar{q}$ model prediction $g_{f_0\gamma\gamma}^2 : g_{a_0\gamma\gamma}^2 = 25 : 9$, this excluded by experiment.

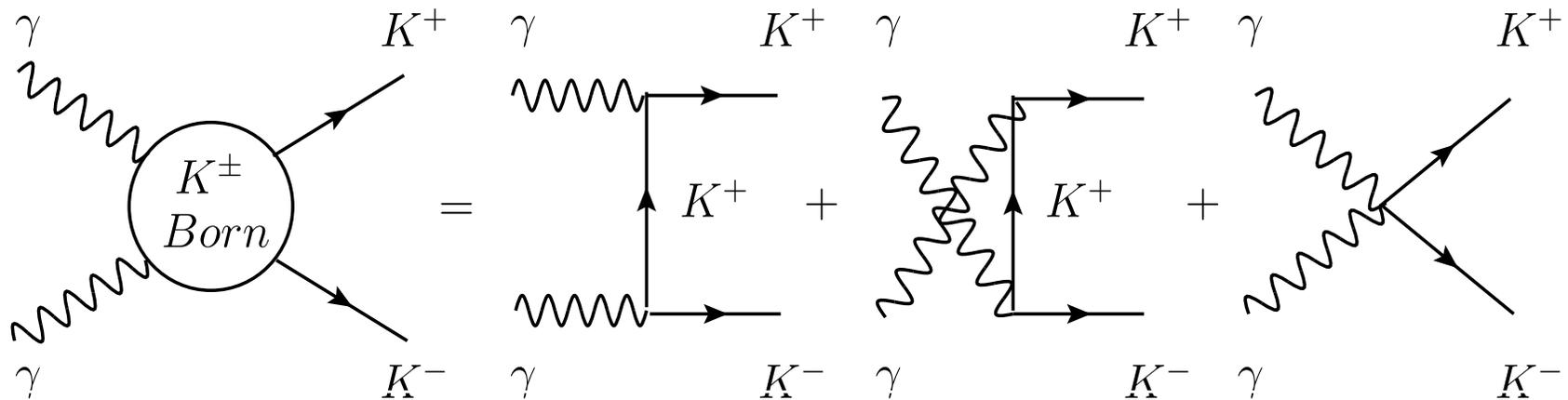
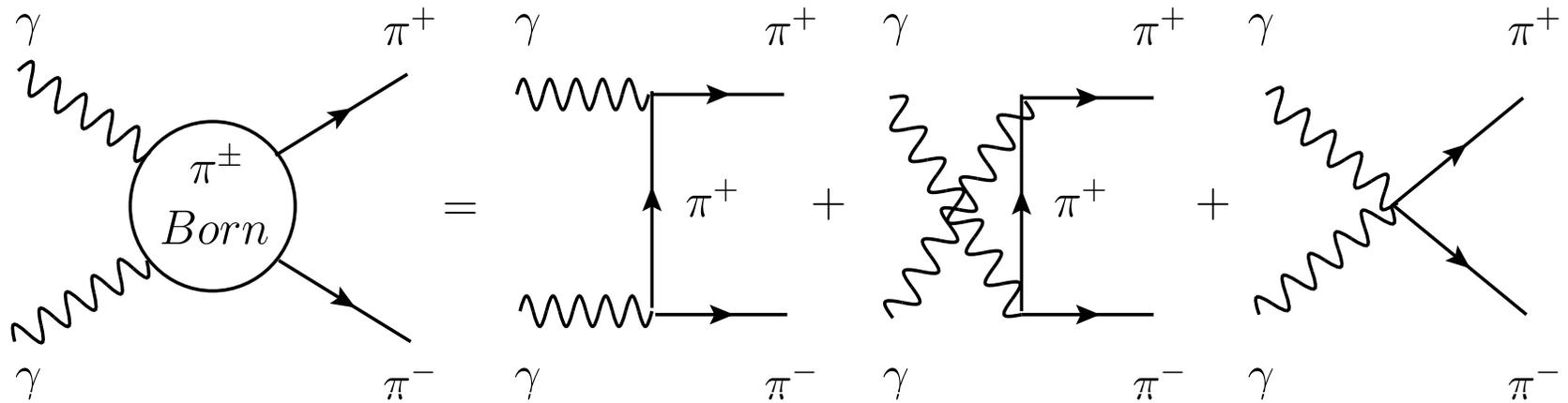
Dynamics of $\gamma\gamma \rightarrow \pi^+\pi^-$



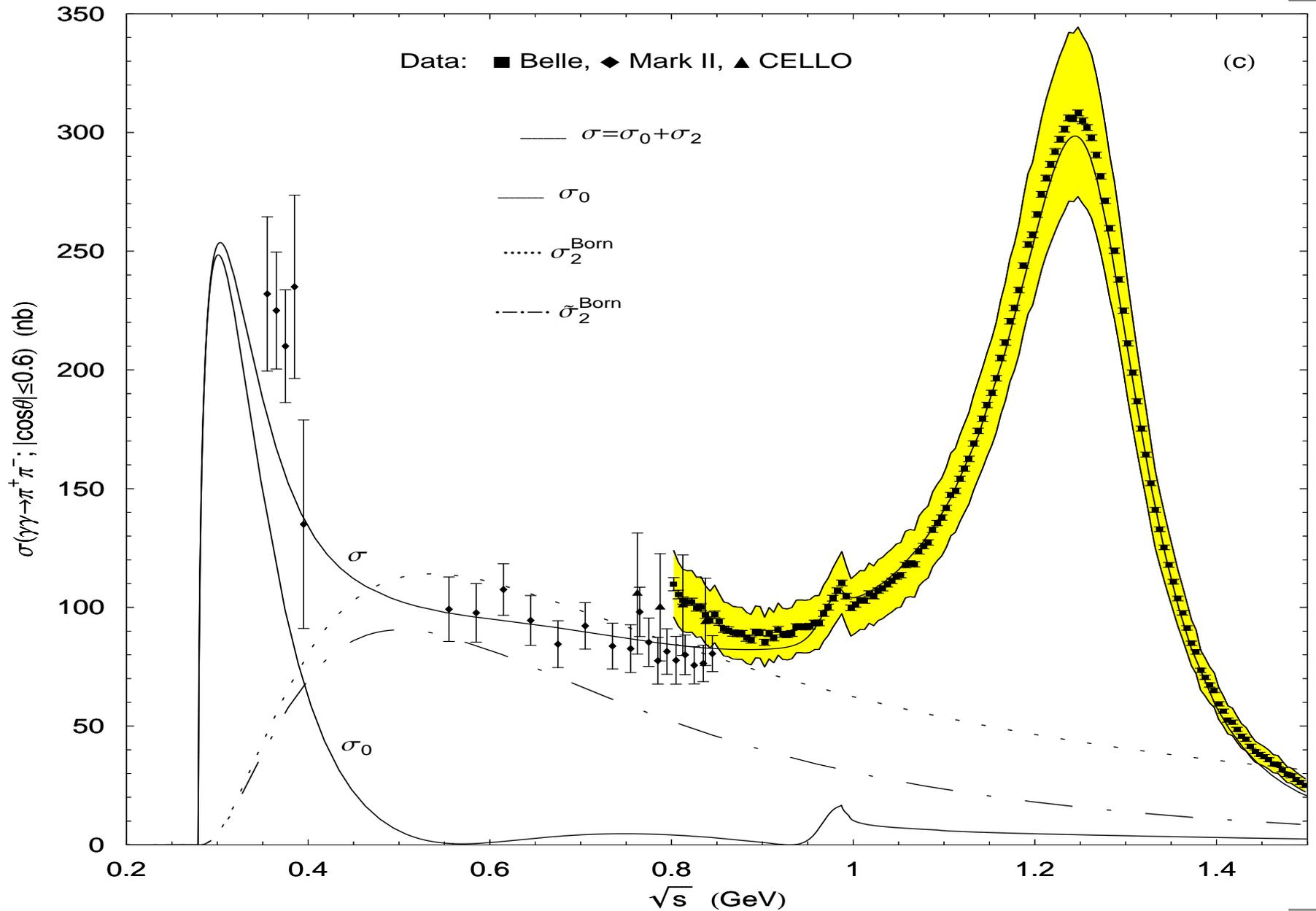
Dynamics of $\gamma\gamma \rightarrow \pi^0\pi^0$



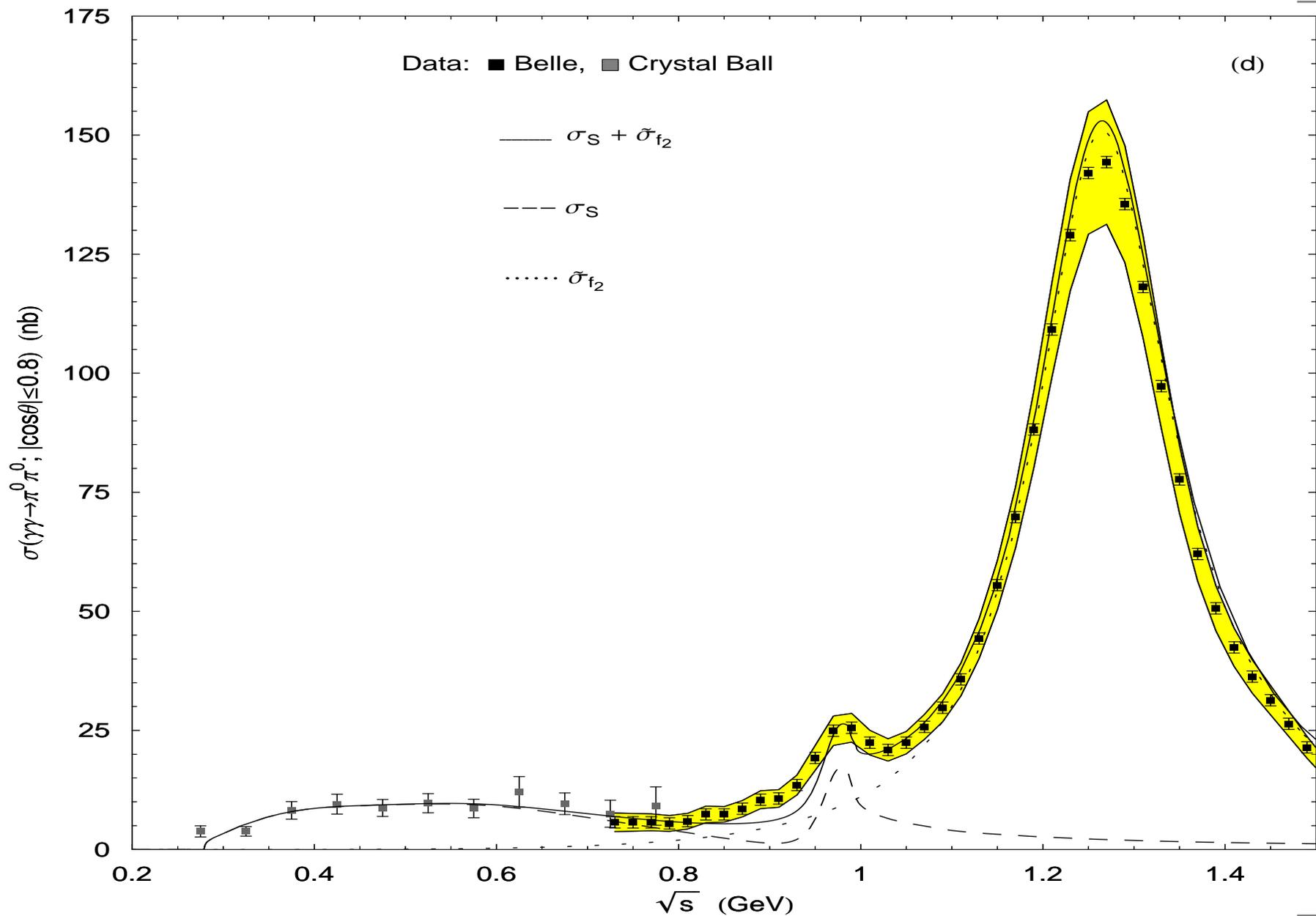
The π^\pm and K^\pm Born contributions



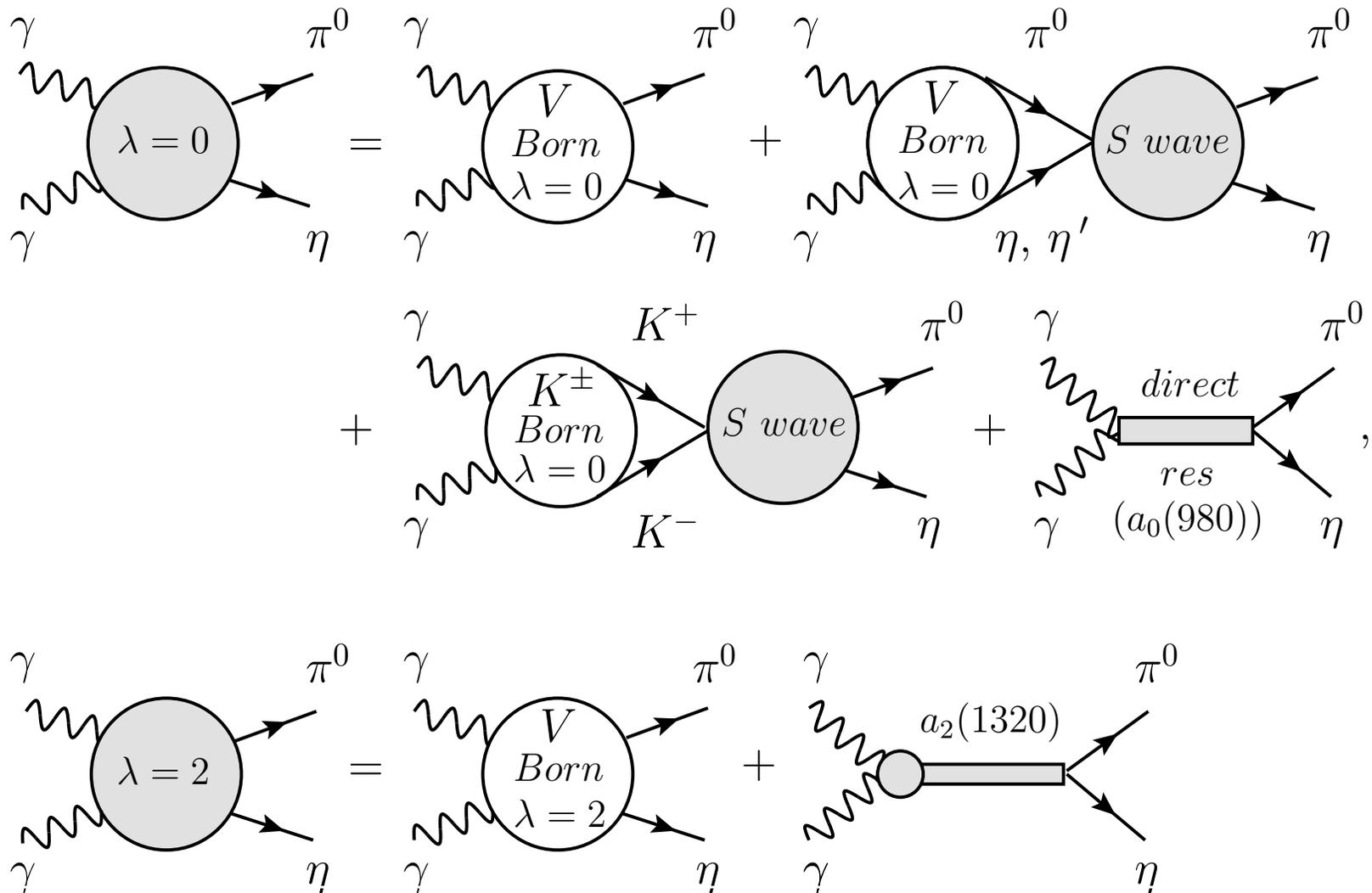
The Belle data on $\gamma\gamma \rightarrow \pi^+\pi^-$



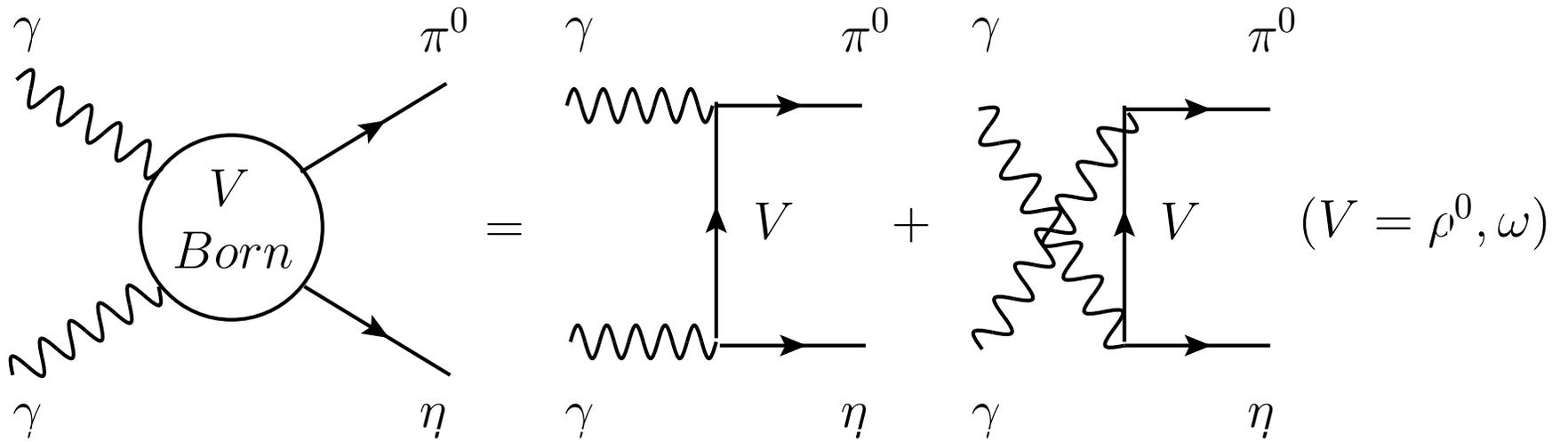
The Belle data on $\gamma\gamma \rightarrow \pi^0\pi^0$



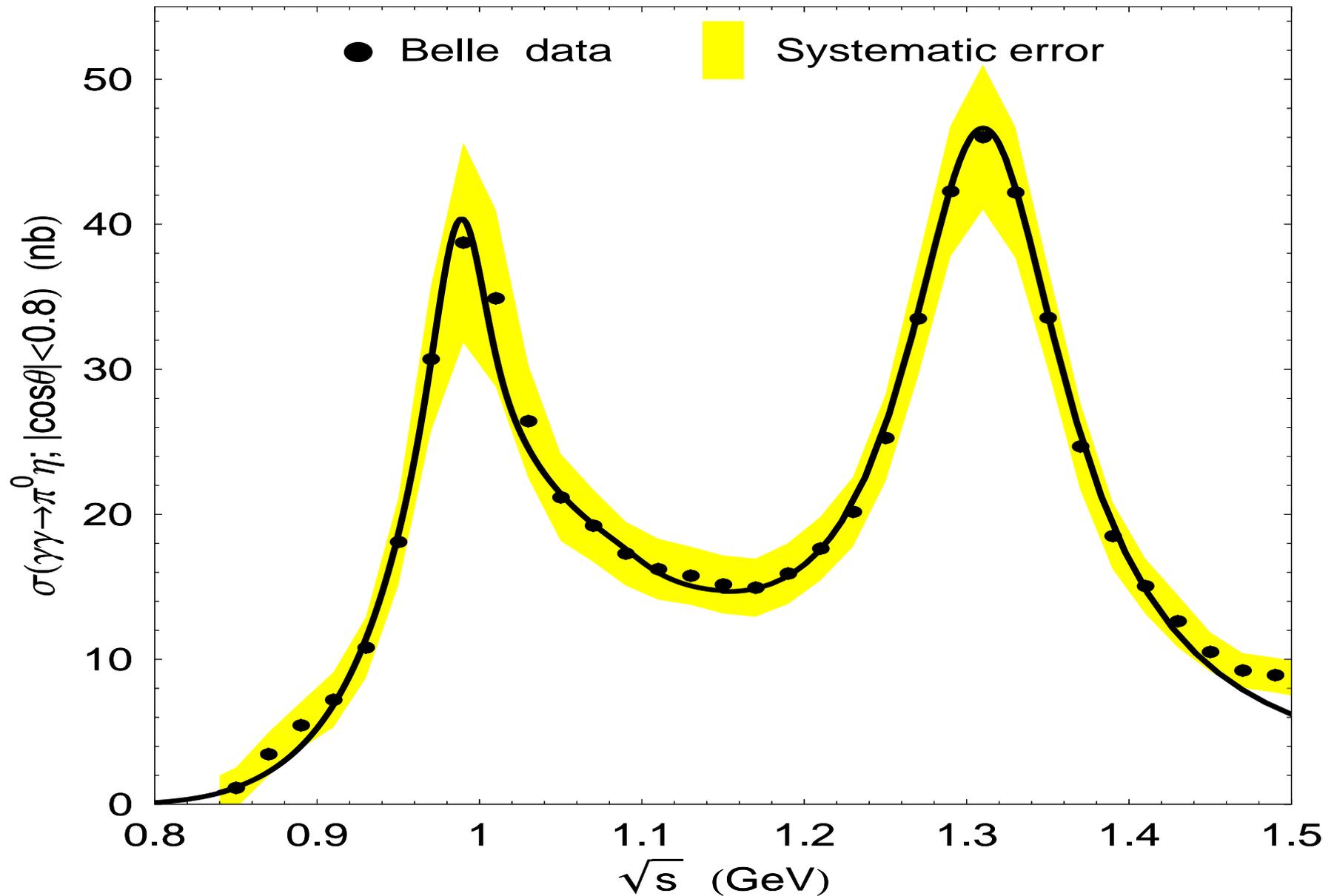
Dynamics of $\gamma\gamma \rightarrow \pi^0\eta$



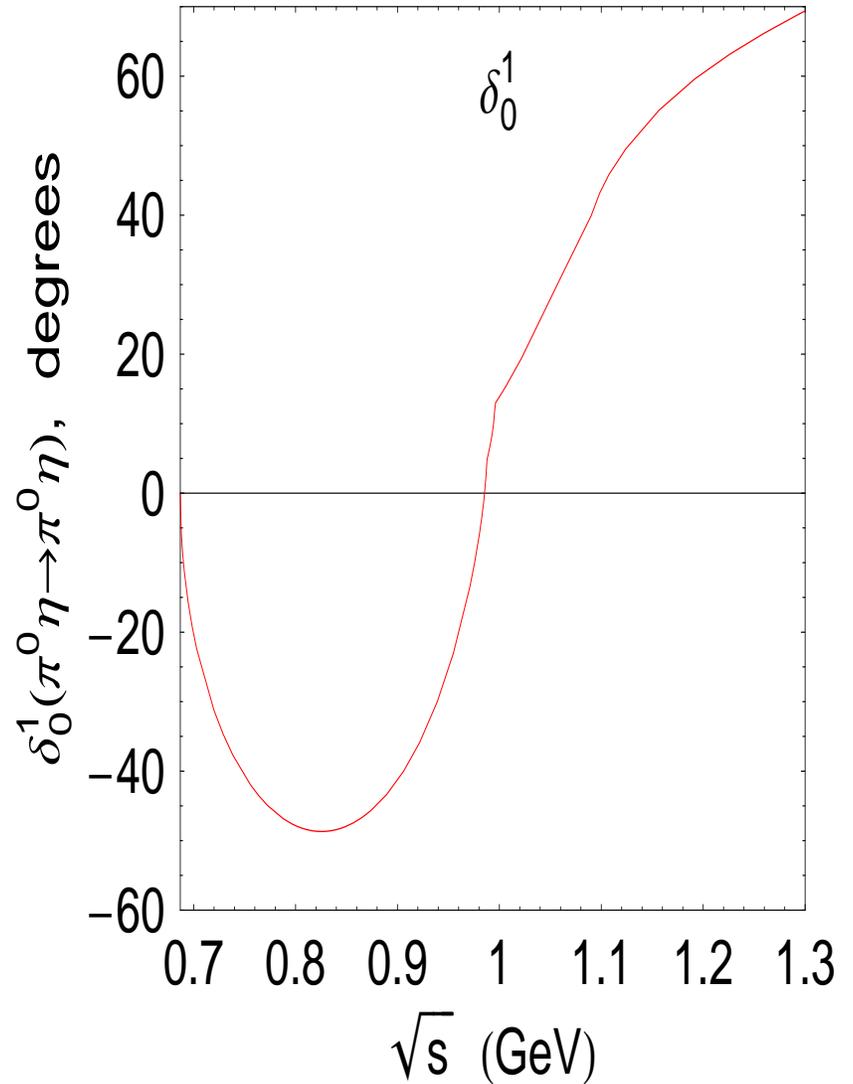
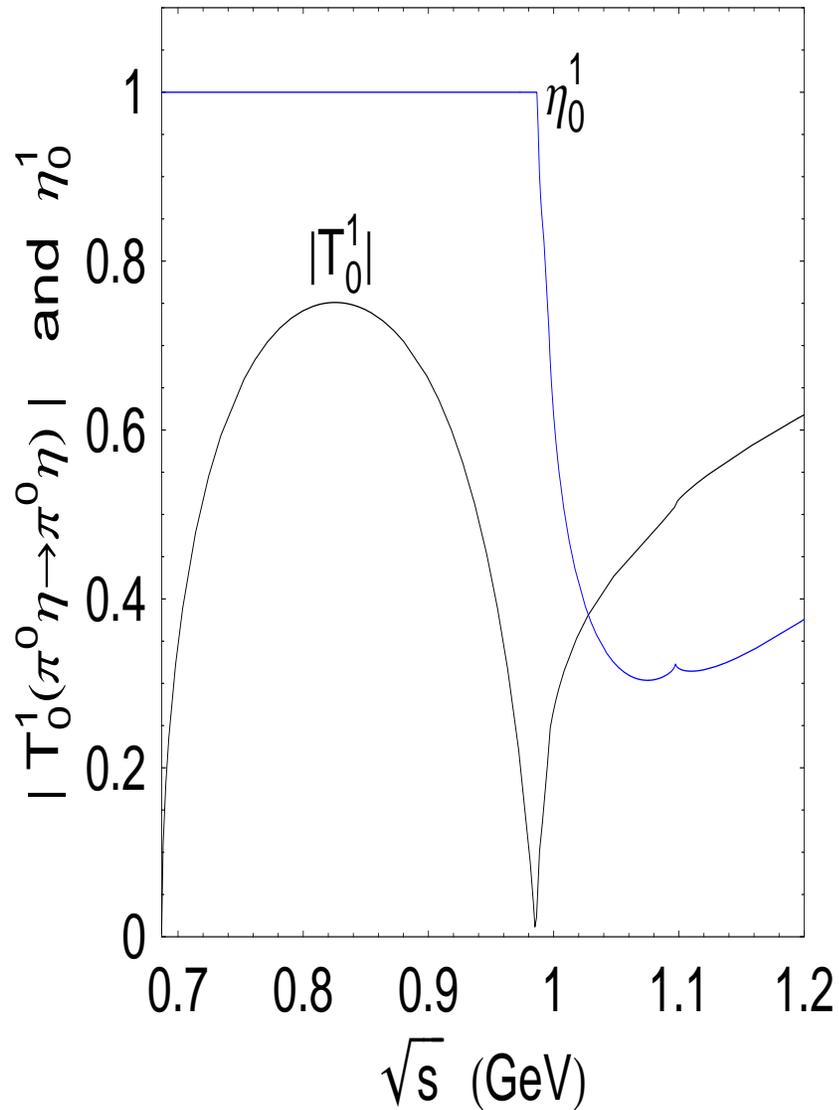
The V Born contribution



The Belle data on $\gamma\gamma \rightarrow \pi^0\eta$



The very preliminary $\pi^0\eta \rightarrow \pi^0\eta$



Summary

The mass spectrum of the light scalars, $\sigma(600)$, $\kappa(800)$, $f_0(980)$, $a_0(980)$, gives an idea of their $q^2\bar{q}^2$ structure.

Both intensity and mechanism of the $a_0(980)/f_0(980)$ production in the radiative decays of $\phi(1020)$, the $q^2\bar{q}^2$ transitions $\phi \rightarrow K^+K^- \rightarrow \gamma[a_0(980)/f_0(980)]$, indicate their $q^2\bar{q}^2$ nature.

Both intensity and mechanism of the scalar meson decays into $\gamma\gamma$, the $q^2\bar{q}^2$ transitions, $\sigma(600) \rightarrow \pi^+\pi^- \rightarrow \gamma\gamma$, $f_0(980)/a_0(980) \rightarrow K^+K^- \rightarrow \gamma\gamma$, indicate their $q^2\bar{q}^2$ nature also.

In addition, the **absence** of $J/\psi \rightarrow \gamma f_0(980)$, $a_0(980)\rho$, $f_0(980)\omega$ in contrast to the intensive $J/\psi \rightarrow \gamma f_2(1270), \gamma f_2'(1525)$, $a_2(1320)\rho$, $f_2(1270)\omega$ decays intrigues **against** the P wave $q\bar{q}$ structure of $a_0(980)$ and $f_0(980)$ also.