

Hydrodynamic flow in small systems

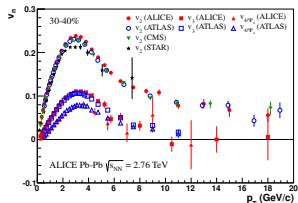
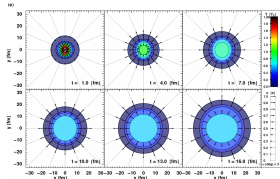
Piotr Bożek

AGH University of Science and Technology, Kraków

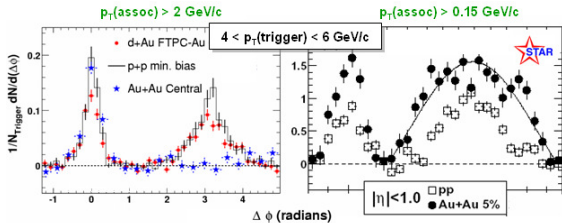


QGP formed in A-A collisions - sQGP

elliptic and triangular flow



Jet quenching

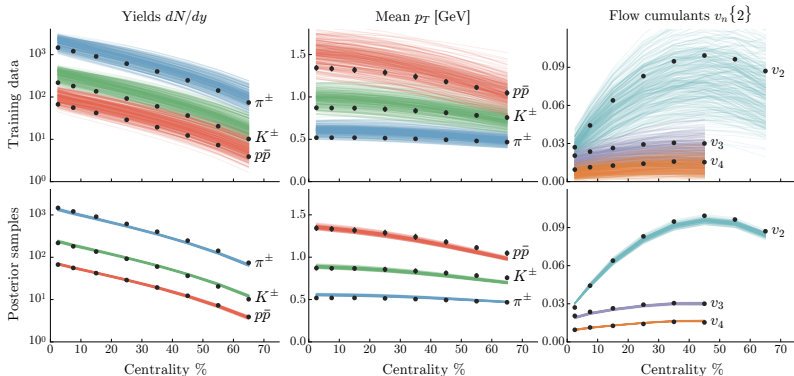


$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos(2(\phi - \Psi_2)) + 2v_3 \cos(3(\phi - \Psi_3)) + \dots$$

p-p and p-A as reference systems!

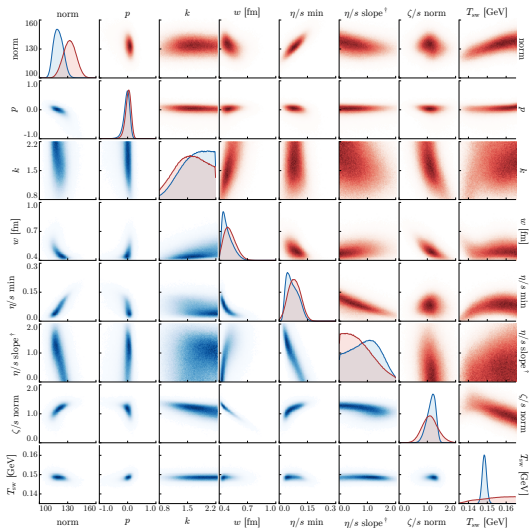
Bayesian parameter estimation

fitting initial densities AND medium parameters
hydrodynamic simulations compared to data



Bernhard et al. 1605.03954

Bayesian parameter estimation - results



involved analysis, many parameters, necessary to extract physical parameters

Proton-Nucleus Collisions at the LHC: Scientific Opportunities and Requirements

Editor: C. A. Salgado¹

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Abstract

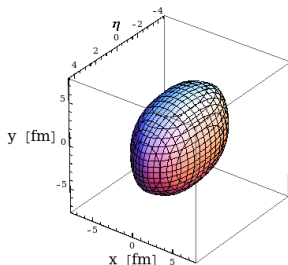
Proton-nucleus (p+A) collisions have long been recognized as a crucial component of the physics programme with nuclear beams at high energies, in particular for their reference role to interpret and understand nucleus-nucleus data as well as for their potential to elucidate the partonic structure of matter at low parton fractional momenta (small- x). Here, we summarize the main motivations that make a proton-nucleus run a decisive ingredient for a successful heavy-ion programme at the Large Hadron Collider (LHC) and we present unique scientific opportunities arising from these collisions. We also review the status of ongoing discussions about operation plans for the p+A mode at the LHC.

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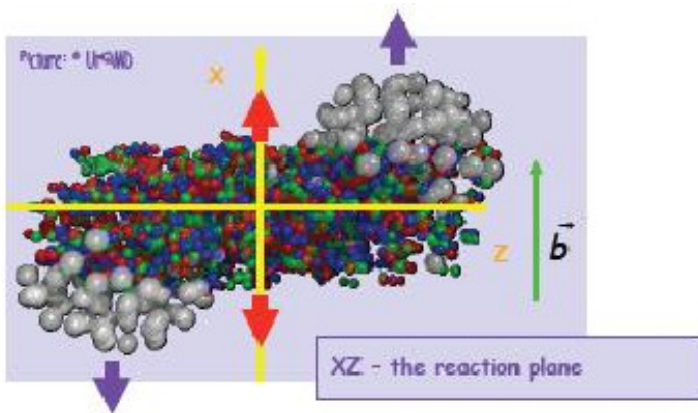
- ▶ expansion of dense matter
- ▶ close to local equilibrium
- ▶ initial conditions
- ▶ equation of state
- ▶ flow + thermal emission + decays + rescattering

can hydrodynamics work in small systems?



Large fireball in AA collisions

hydrodynamic model sensible

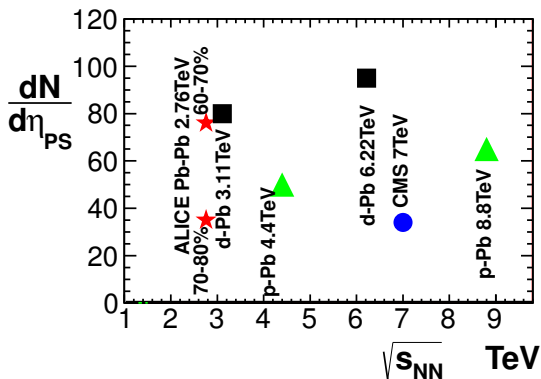




pA collision

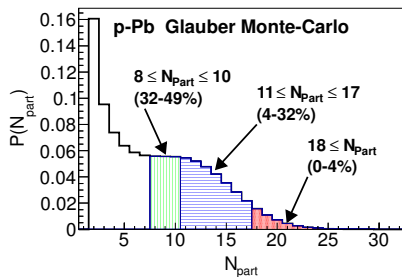
p-Pb at 5.02TeV

small dense fireball formed ?

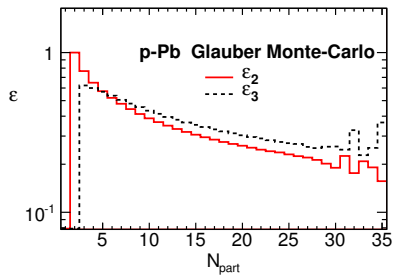


large multiplicity - large fireball - collective expansion?

Fireball in p-Pb



PB, arXiv:1112.0912



Collective elliptic flow in **p-Pb**?

- ▶ Large enough density? **yes**
- ▶ Large enough eccentricity **yes?**
- ▶ Large enough size? **yes???**
but should and can be tested
- ▶ Small enough gradients? **no?**
- beyond viscous hydro

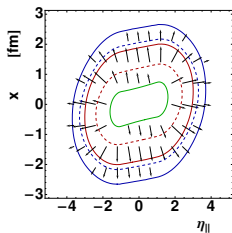
Collective elliptic flow in p-Pb?

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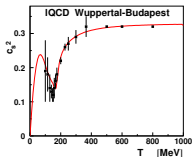
in p-p?

yes (high mult.)
(?)
(???)
no!

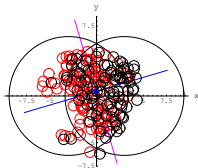
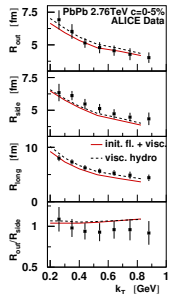
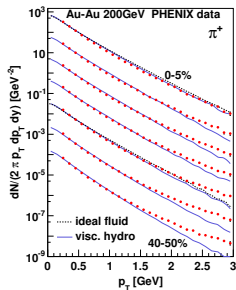
3+1D hydrodynamics



3+1D visc. hydro

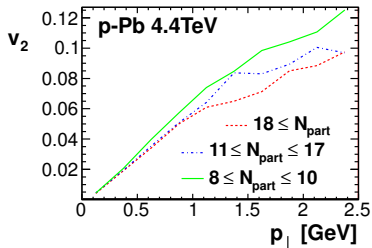


IQCD + Hadron Gas

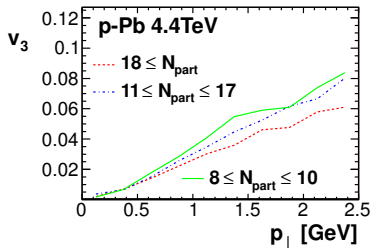


- ▶ Glauber Initial state - M. Rybczynski, G. Stefanek, W. Broniowski, PB -1310.5475
- ▶ Statistical emission - M. Chojnacki, A. Kisiel, W. Florkowski, W. Broniowski - 1102.0273

collective flow in p-Pb 2011 prediction



elliptic flow in p-Pb



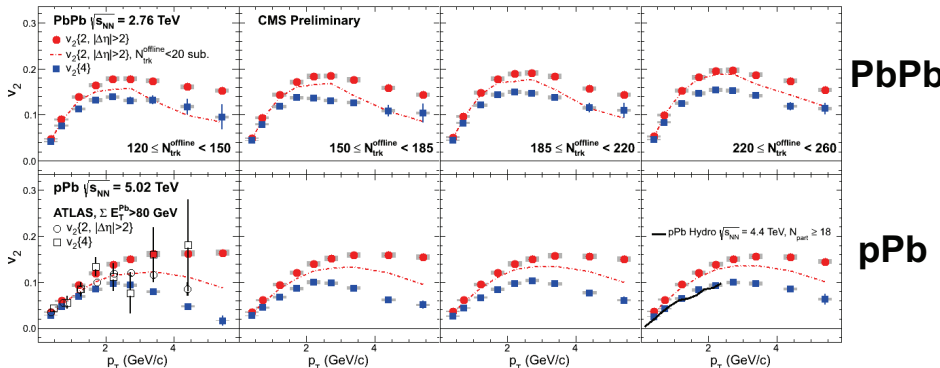
triangular flow

PB, arXiv:1112.0912

v_2 in pPb and PbPb

Dash-dot line: peripheral subtracted

multiplicity \longrightarrow



v_2 shows similar shape in pPb and PbPb, but is smaller in pPb

$v_2\{4\}$ is only 20% smaller than $v_2\{2\}$ below 2 GeV/c

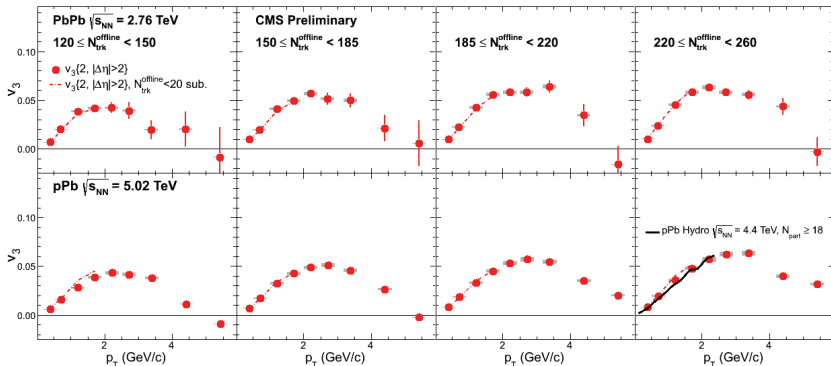
“Peripheral subtraction” has small effect at high multiplicity



v_3 in pPb and PbPb

Dash-dot line: peripheral subtracted

multiplicity \longrightarrow



PbPb

pPb

v_3 has similar shape in pPb and PbPb; magnitude comparable

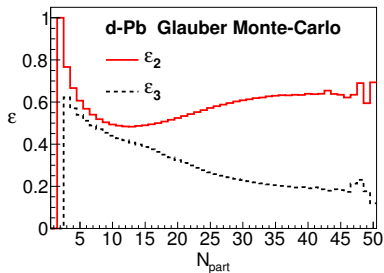
“Peripheral subtraction” makes essentially no difference

Hydro prediction: Bozek, $v_3\{PP\}$, not including fluctuations

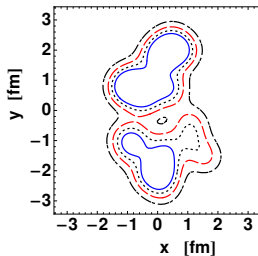
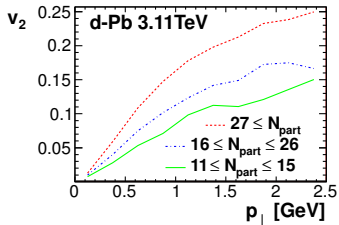


d-Pb

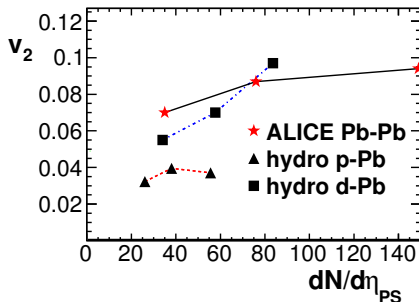
- ▶ small deformed projectile
- ▶ well defined initial deformation
- ▶ multiplicity controls eccentricity



large elliptic flow



PB, arXiv:1112.0912

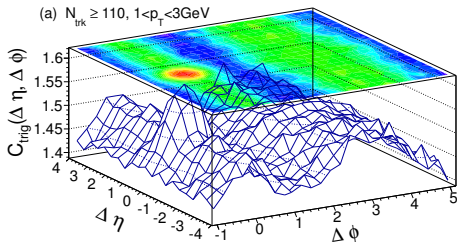
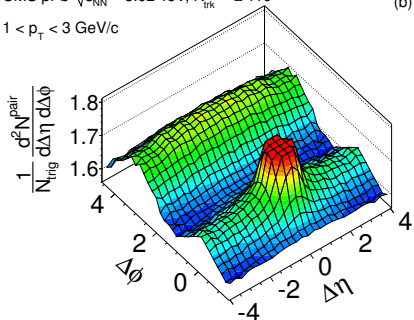


- ▶ collective flow effects \simeq peripheral Pb-Pb
- ▶ can be observed
- ▶ p-Pb is not p-p superposition
- ▶ d-Pb small deformed projectile
 - control of the initial shape!
- ▶ only p-p as baseline
 - or is it really a reference w/o FSI??

Ridge in p-Pb

CMS pPb $\sqrt{s_{NN}} = 5.02$ TeV, $N_{trk}^{offline} \geq 110$

$1 < p_T < 3$ GeV/c



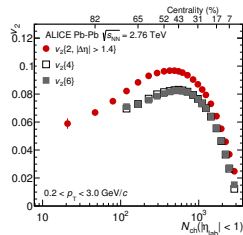
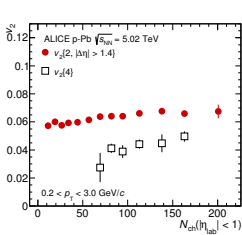
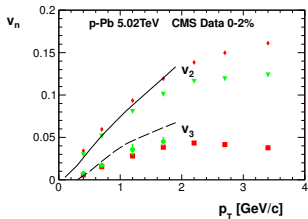
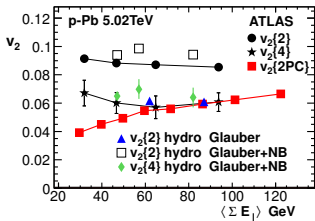
PB, W.Broniowski, arXiv:1211.0845

symmetric ridge also from CGC, K.Dusling, R. Venugopalan, arXiv:1210.3890, 1211.3701, 1302.7018

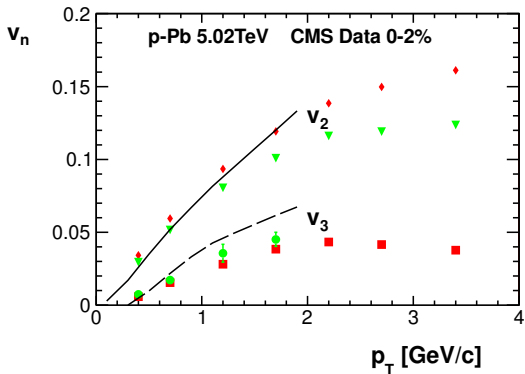
Indications of collective flow in p-A, d-A, He-A

1. **Elliptic and triangular flow**
2. **Hierarchy of v_2 and v_3 in p-A, d-A, He-A**
collective response to geometry (final state effect)
3. **Flow from higher cumulants**
4. **Interferometry radii**
5. **Factorization at intermediate p_{\perp} and large $\Delta\eta$**
particles at intermediate p_{\perp} , large η , correlated to geometry
6. **Mass splitting of v_2**
7. Mass hierarchy of spectra ($\langle p_{\perp} \rangle$)

1) Elliptic and triangular flow observed in p-Pb



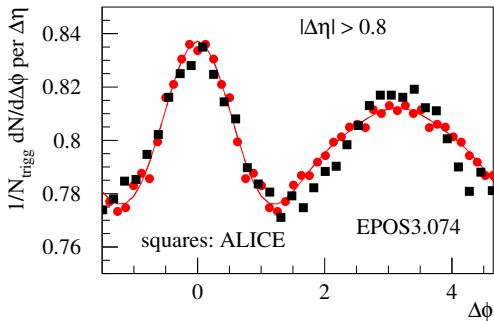
- Glauber MC initial cond. - agreement with data



PB, W.Broniowski, G. Torrieri arXiv:1306.5442; G.Y. Qin, B. Müller 1306.3439; I. Kozlov et al. 1405.3976; A. Bzdak et al. 1304.34003, ...

- ▶ v_2 , v_3 consistent with hydro (Glauber MC)
- ▶ sensitive probe of init. cond.

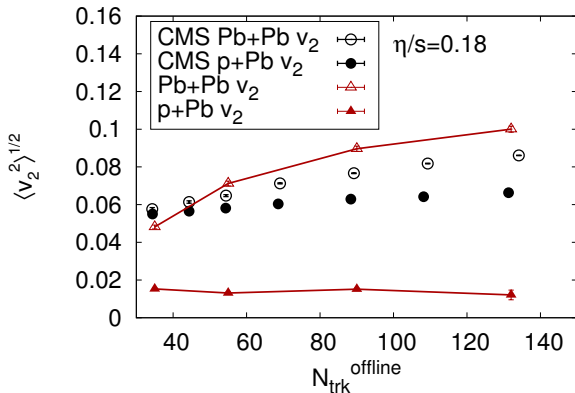
- EPOS3 - agreement with data



Double ridge from EPOS simulation

K. Werner et al. 1307.4379

- IP-Glasma initial cond. - small v_2 !

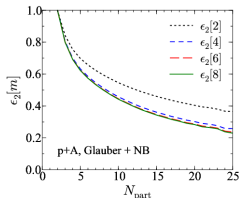


B. Schenke, R. Venugopalan 1405.3605

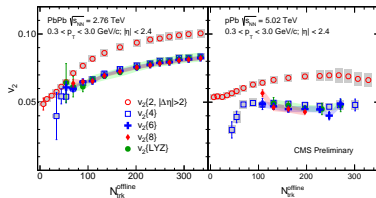
2) Flow from higher cumulants

- hierarchy of cumulants

$$\epsilon_2\{4\} \simeq \epsilon_2\{6\} \simeq \epsilon_2\{8\} < \epsilon_2\{2\} \rightarrow \text{hydro response} \rightarrow v_2\{4\} \simeq v_2\{6\} \simeq v_2\{8\} < v_2\{2\}$$



A. Bzdak, PB, L. McLerran, 1311.7325

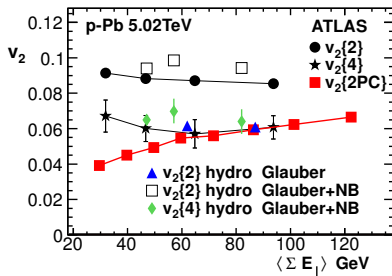


CMS 1502.05382

- **detailed** hierarchy of cumulants - consistent with data

$v_2\{n\}$ - hydro response to fluctuations of initial shape !

$v_2\{4\}$ and $v_2\{2\}$ - hydro calculation



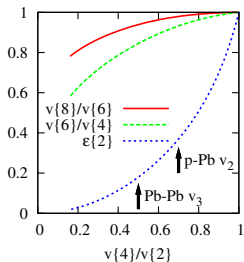
PB, W. Broniowski 1304.3044

hierarchy $v_2\{2\} > v_2\{4\} > 0$ confirmed in full hydro calculation

also: I. Kozlov et al. 1412.3147

Note: $\epsilon_n + \text{hydro response} \rightarrow$ correct centrality dependence of v_n

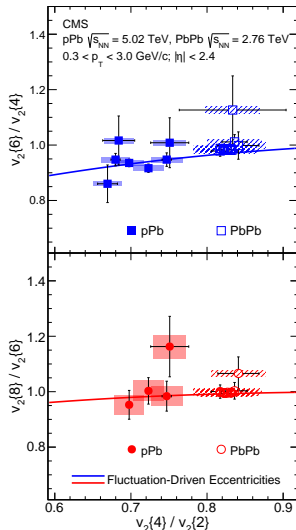
Detailed hierarchy of cumulants



L. Yan, J.Y. Ollitrault 1312.6555

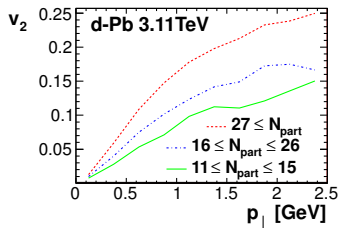
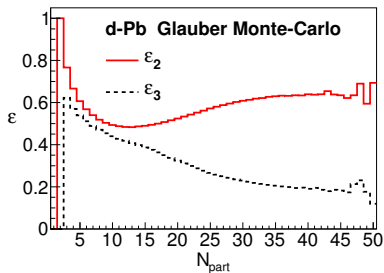
universal prediction for differences
 $v_2\{4\} \neq v_2\{6\} \neq v_2\{8\}$
 power-elliptic eccentricity distributions

$$\epsilon\{4\} = \epsilon\{2\}^{3/2} \left(\frac{2}{1 + \epsilon\{2\}^2} \right)$$



CMS 1502.05382

small system with large deformation d-Pb

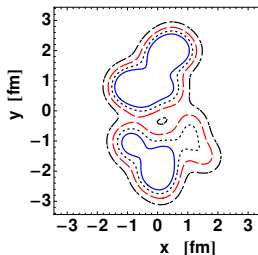


large elliptic flow

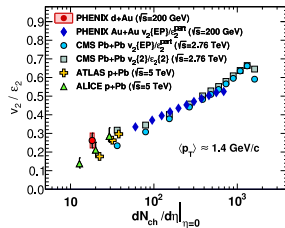
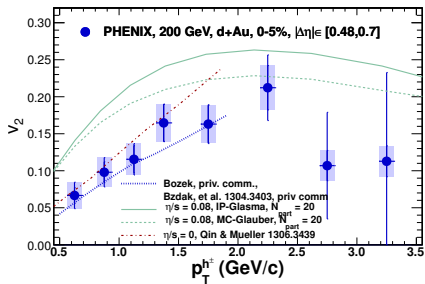
PB, arXiv:1112.0912

control of initial geometry,

central collisions - deformed fireball



3a) Elliptic flow observed in d-Au at 200GeV

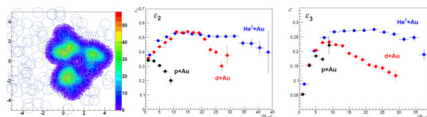


PHENIX, arXiv:1303.1794

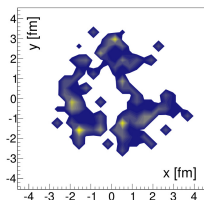
large eccentricity - large elliptic flow

small on big collisions

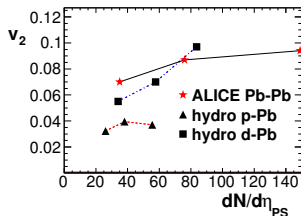
^3He -Au collisions



PHENIX proposal $\rightarrow v_3$, Sickles et al. arXiv:1401.2432



α clusters in ^{12}C Broniowski, Arriola arXiv:1312.0289



PB, arXiv:1112.0912

strong effect for d-A

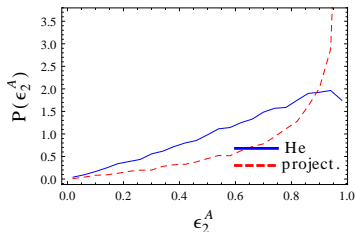
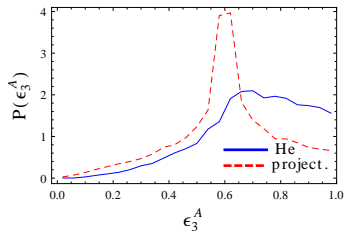
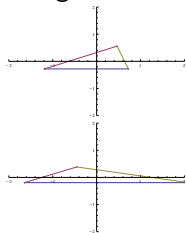
intrinsic deformation dominates
over fluctuations

effect for v_3 in ^3He -A,

Nagle et al. arXiv:1312.4565

^3He configurations

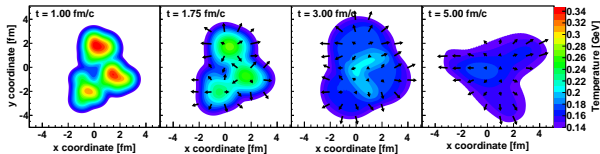
elongated He configurations



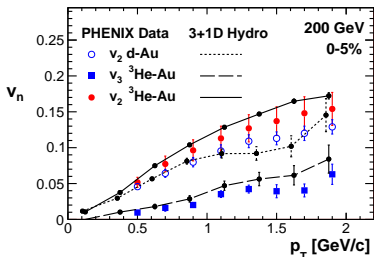
- large ϵ_2
- even larger after projection
- broad distribution of ϵ_3
- after projection $\epsilon_3 \simeq 0.6$

Expect large v_2 and smaller v_3 in $^3\text{He-Au}$

3b) Triangular flow in $^3\text{He-Au}$



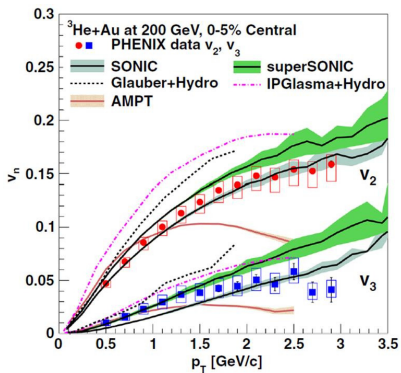
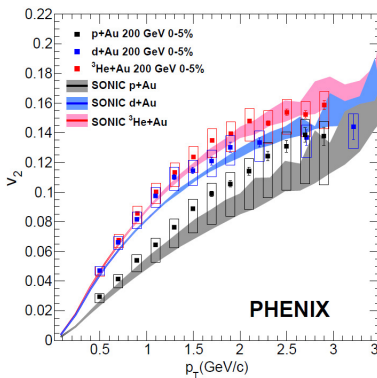
Nagle et al. 1312.4565



- ▶ observed v_3 \rightarrow collectivity
- ▶ hierarchy of v_2 and v_3 consistent with collective response on fireball geometry
- ▶ large v_2 in He-Au

Consistent with hydrodynamics

Comparing p-Au, d-Au, He-Au – PHENIX



-strong v_2 in d-Au and $^3\text{He-Au}$

-small v_2 in p-Au

-strong v_3 in $^3\text{He-Au}$

Collective response to initial geometry !

Factorization breaking

Flow yields two-particle correlations in angle

$$C(\Delta\phi) = 1 + 2v_2^2 \cos(2\Delta\phi)$$

For two particles with different momenta -

Factorization if correlation due to flow) Gardim et al. 1211.0989

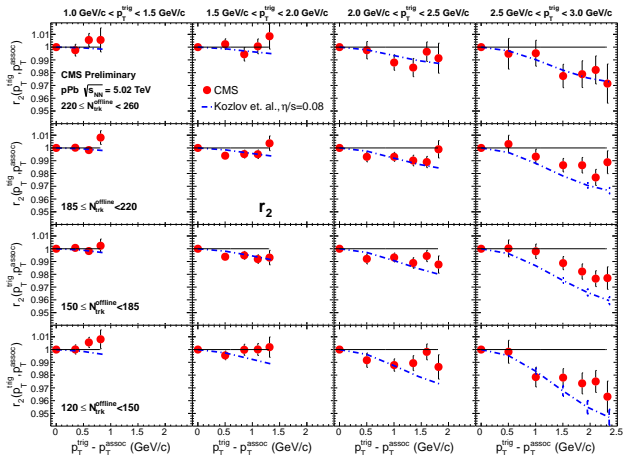
$$\begin{aligned} C(\Delta\phi, p_1, p_2) &= 1 + 2V_2(p_1, p_2) \cos(2\Delta\phi) = \\ (\text{if flow}) &\simeq 1 + 2v_2(p_1)v_2(p_2) \cos(2\Delta\phi) \end{aligned}$$

in flow scenario **small factorization breaking** expected
(event plane decorrelation)

$$r = \frac{V_2(p_1, p_2)}{v_2(p_1)v_2(p_2)} \simeq \cos(\Psi_{p_1} - \Psi_{p_2}) < 1$$

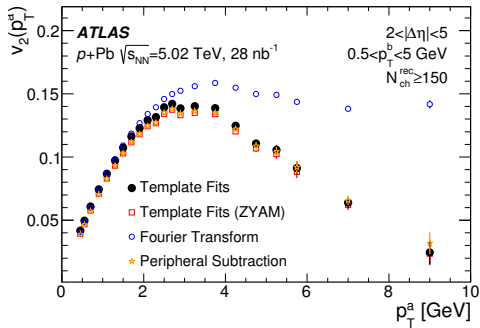
Slightly different event planes expected for particles at different p_\perp
(or rapidity Bozek et al. 1011.3354) due to fluctuations

4a) Factorization at intermediate p_{\perp}



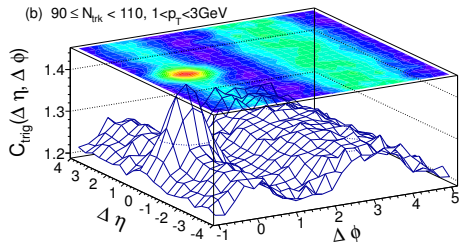
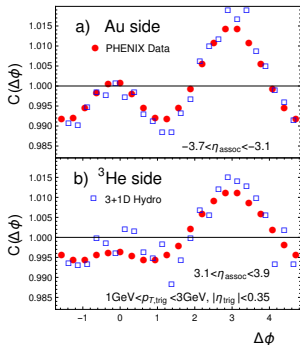
- factorization holds for v_2 and v_3 up to 3 GeV
- **small** deviations explained by hydro+Glauber Kozlov, Luzum, Denicol, Jeon, Gale, 1405.3976
- geometry driven origin of correlations at small **and** intermediate p_{\perp}

Correlations between soft and hard particles



- correlations between soft (bulk) particles and intermediate p_{\perp} particles
- soft particles flow driven by geometry \implies high p_{\perp} particles geometry driven (at least partly)
- possibly some final state interaction other than hydrodynamics

4c) Correlations at large $\Delta\eta$ (Ridge)



PB, Broniowski 1211.0845

- correlations between particles at different η
- flow driven by geometry at $\eta \simeq 0 \implies$ flow driven by geometry at forward rapidities
- well described by hydrodynamics
- similar mechanism in AMPT: Ma, Bzdak-arXiv: 1404.4129, Koop, Adare, Nagle-arXiv: 1501.06880

Interferometry correlations

Hanbury Brown Twiss (1956) - measure of star diameter

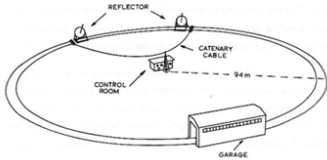
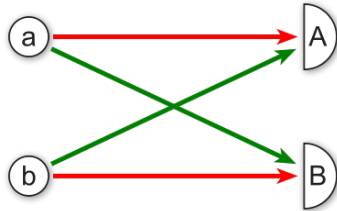


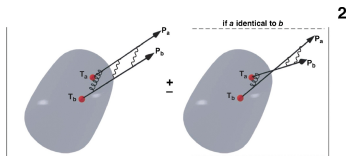
Figure 1. Aerial photo and illustration of the original HBT apparatus. They have been extracted from Ref.[1].

Intensity correlations in two detectors



$$\langle I_A I_B \rangle = \langle I_A \rangle \langle I_B \rangle (1 + C(r_{AB}))$$

Hanbury Brown-Twiss correlations(HBT)



Lisa MA, et al. 2005.
Annu. Rev. Nucl. Part. Sci. 55:357-402

- ▶ quantum correlation for (anti)symmetrization of production amplitudes
- ▶ we observe pairs of identical particles , $\pi^+ - \pi^+$

$$C(p_1, p_2) = \frac{\int d^4x_1 d^4x_2 S(x_1, p_1) S(x_2, p_2) |e^{i(x_1 p_1 + x_2 p_2)} + e^{i(x_2 p_1 + x_1 p_2)}|^2}{\int d^4x_1 S(x_1, p_1) \int d^4x_2 S(x_1, p_2)}$$

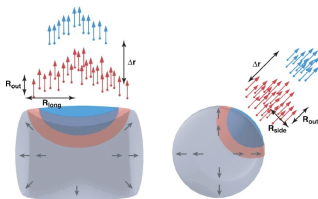
- ▶ experimentally we reconstruct

$$C(\mathbf{k}, \mathbf{q}) = \frac{N(p_1, p_2)}{N(p_1)N(p_2)}$$

using *mixed event pairs* in the denominator

- ▶ pair correlations in relative momentum ($q = p_1 - p_2$) are measured for different average pair momenta $\mathbf{k} = \frac{p_1 + p_2}{2}$
- ▶ in most general case we have 6 momentum variables
- ▶ in the pair wave function final-state interactions can be taken into account (like Columb interactions)

Bertsch-Pratt parameterization



Lisa MA, et al. 2005.
Annu. Rev. Nucl. Part. Sci. 55:357-402

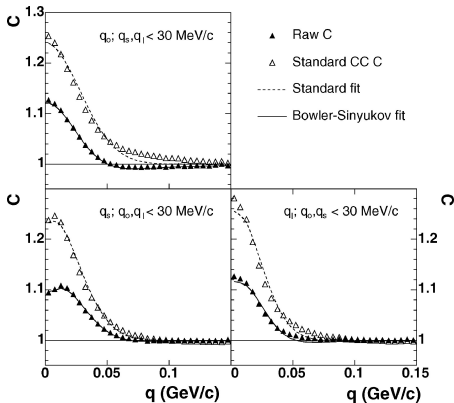
- ▶ correlations for a fixed average pair momentum $k = (p_1 + p_2)/2$
- ▶ we go to the *local comoving system* LCMS with $k_z = 0$ (pair momentum along the beam axis), which gives $k = (k_{\perp}, 0)$
- ▶ the relative momentum vector is split into 3 component $q_{long} = q_z$, q_{out} (parallel to k_{\perp}) i q_{side} perpendicular to long and out directions

HBT radii

the correlations function after subtracting final state interaction effects

$$C(q) = 1 + \lambda e^{-R_{out}^2 q_{out}^2 - R_{side}^2 q_{side}^2 - R_{long}^2 q_{long}^2}$$

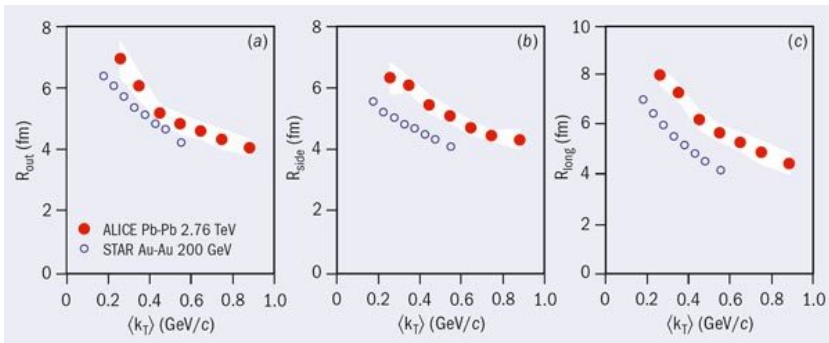
The parameters R measure the size of the emission region
interferometry, femtoscopy, HBT



Lisa MA, et al. 2005.
Annu. Rev. Nucl. Part. Sci. 55:357–402

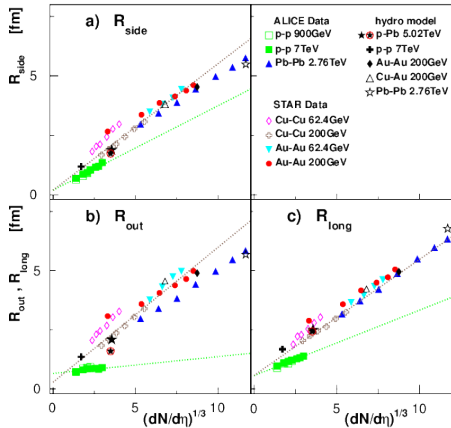
Dependence on pair momentum

- ▶ particle pairs with similar momenta are emitted from the same fluid region (with flow velocity along the pair momentum)
- ▶ the larger the average pair momentum the more colimated are the momenta of the two particles which means they must be emitted from a smaller region
- ▶ the emission region is called *homogeneity region* and its size the *homogeneity length*
- ▶ for a finite average pair momentum we measure the size of only a small part of the total fireball
- ▶ HBT radii get smaller with increasing k_{\perp}



Dependence of multiplicity and size

- ▶ HBT radii get larger with multiplicity $R \propto (dn/d\eta)^{1/3}$
- ▶ emission from a larger region of similar freeze-out density
- ▶ + some dependence on the amount of transverse flow



Calculating HBT correlations in models

- ▶ list of generated particles with momenta p_i and positions of last scattering r_i
- ▶ generate symmetrized pairs for all pairs of identical particles $\{(x_k, p_k), (x_l, p_l)\}$

$$A_{bin} = \frac{1}{N_{pairs}} \sum_{pairs} \Psi(q, x_k - x_l) \delta_{bin}$$

for all pairs that fall into a given q - k_{\perp} bin

- ▶ generate mixed pairs for denominator

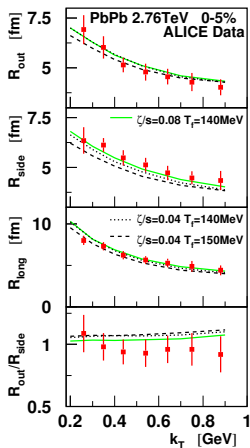
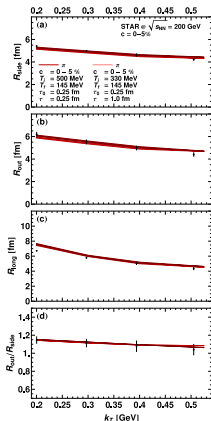
$$B = \frac{1}{N_{mixed\ pairs}} \sum_{pairs} \delta_{bin}$$

for all pairs that fall into a given q - k_{\perp} bin using particles from different events



$$C_{bin} = \frac{A_{bin}}{B_{bin}}$$

Hanbury Brown-Twiss (HBT) correlations in AA

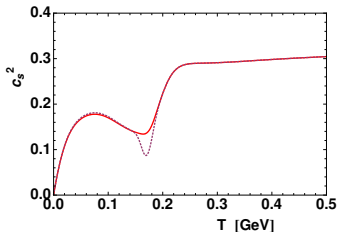


Broniowski, Chojnacki, Florkowski, Kisiel 2008,

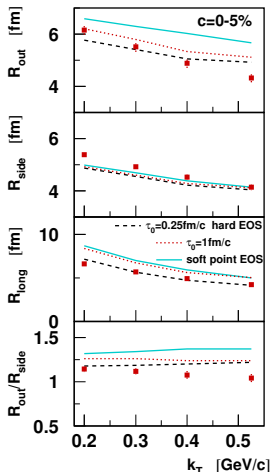
Pratt, 2009

PB, Wyskiel 1203.6513

HBT - hard equation of state



soft EOS - wrong HBT



Heavy-ion experiments consistent with lattice QCD

HBT indicates explosive expansion : hard EOS, pre-equilibrium flow, viscosity

correlations in event by event hydrodynamics

- ▶ combine several (many) events

$$C(q_a, k_b) = \frac{\frac{1}{N_{pairs,num}} \sum_{j=1}^{N_h} \sum_{m,l=1}^{N_e} \sum_{s=1}^{M_l} \sum_{f=1}^{M_m} \delta_{q_a} \delta_{k_b} \Psi(q, x_1 - x_2)}{\frac{1}{N_{pairs,den}} \sum_{i \neq j=1}^{N_h} \sum_{l,m=1}^{N_e} \sum_{s=1}^{M_l} \sum_{f=1}^{M_m} \delta_{q_a} \delta_{k_b}}$$

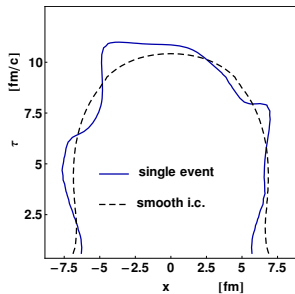
numerator - sum over different hydro events

denominator - sum over different hydro event pairs

increases the effective number of pairs (d-Au 5000×)

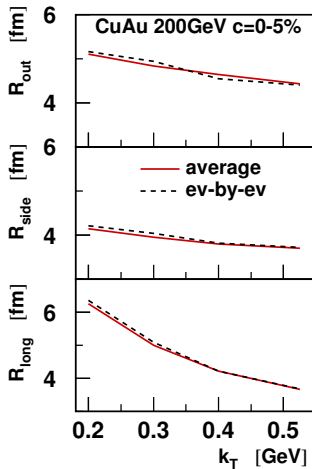
- ▶ azimuthally sensitive HBT possible with reasonable cost
- ▶ perfect event plane resolution

HBT of fluctuating fireballs



can the lumpy surface be observed?

NO



HBT of fluctuating fireballs II

- ▶ event by event emission function

$$C(q, k) = \frac{\int d^4x_1 d^4x_2 \langle S(x_1, p_1) S(x_2, p_2) \rangle |\Psi(k, (x_1 - x_2))|^2}{\int d^4x_1 \langle S(x_1, p_1) \rangle \int d^4x_2 \langle S(x_2, p_2) \rangle}$$

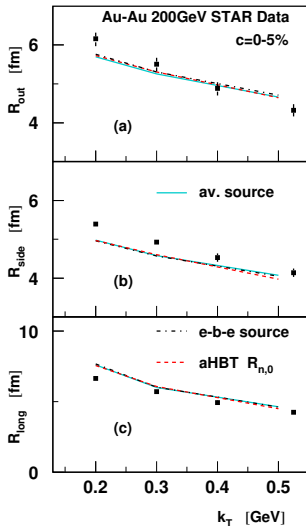
- ▶ average emission function

$$C_{av}(q, k) = \frac{\int d^4x_1 d^4x_2 \langle S(x_1, p_1) \rangle \langle S(x_2, p_2) \rangle |\Psi(k, (x_1 - x_2))|^2}{\int d^4x_1 \langle S(x_1, p_1) \rangle \int d^4x_2 \langle S(x_2, p_2) \rangle}$$

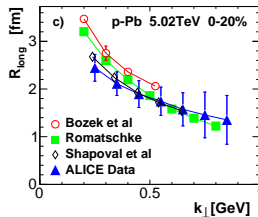
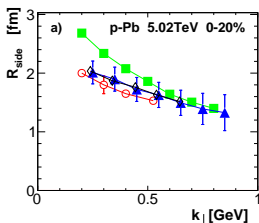
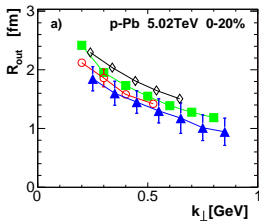
- ▶ emission function fluctuations

HBT of fluctuating fireballs II

- ▶ event by event emission function similar to average emission function
- ▶ small source fluctuations
- ▶ spectra do not fluctuate event by event much

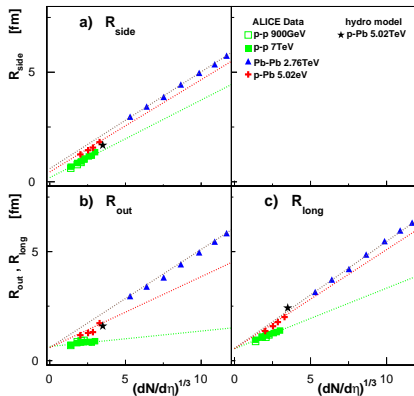


5) Interferometry radii



k_{\perp} dependence of $R_{o,l,s}$
 R_{side}, R_{out} consistent with hydro

Interferometry radii - pp, pA, AA

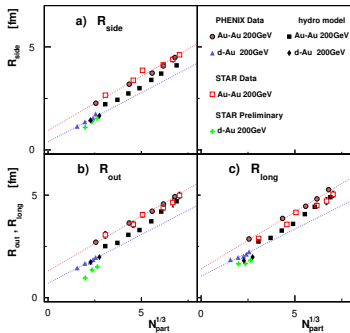


- pA system size in between pp and AA
(differences in flow strength, initial size, flow profile)

- HBT in pA consistent with hydrodynamics

Interferometry radii (d-Au, He-Au)

d-Au (PHENIX data)

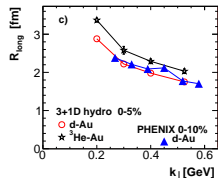
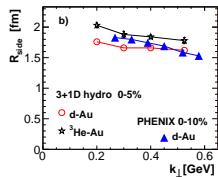
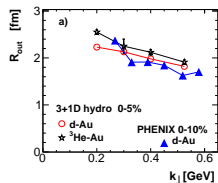


k_{\perp} dependence of $R_{O,l,s}$

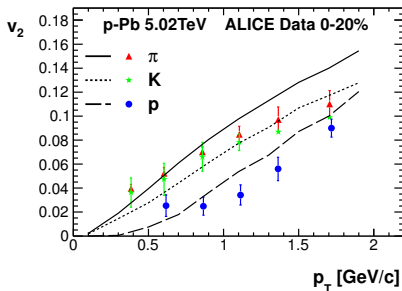
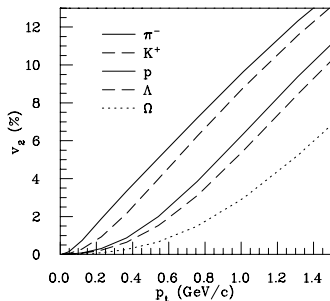
R_{side} consistent with hydro

PB, 1408.1264

Romatschke 1502.04745



Mass splitting of v_2

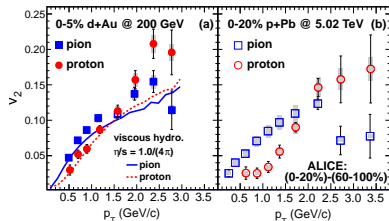
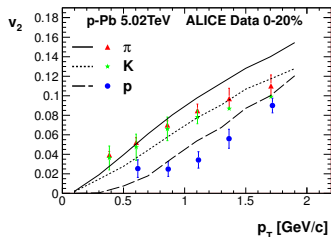


mass splitting of v_2 in hydro models

Huovinen et al. 2001

Observed in p-Pb

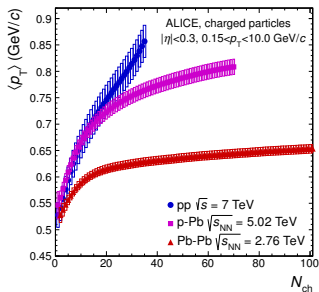
6) Mass splitting of v_2



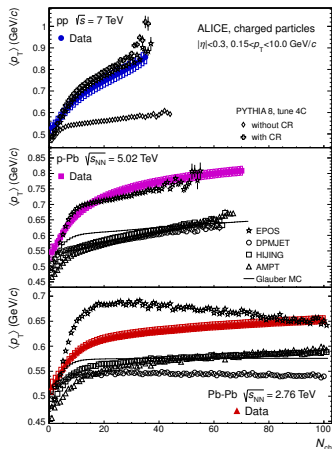
PB, Broniowski, Torrieri, 1307.5060

-mass splitting of v_2 as expected from hydrodynamics

7a) Large $\langle p_{\perp} \rangle$

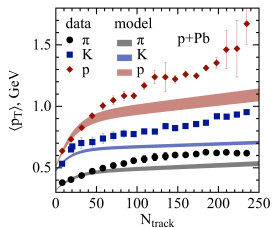
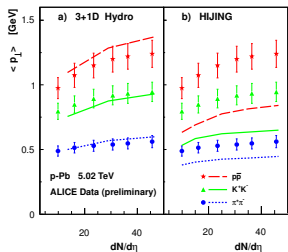


larger $\langle p_{\perp} \rangle$ in smaller systems



- additional stronger transverse push in p-Pb and Pb-Pb
- in pp increase of p_{\perp} can be explained by color reconnection

7b) Mass hierarchy of $\langle p_{\perp} \rangle$



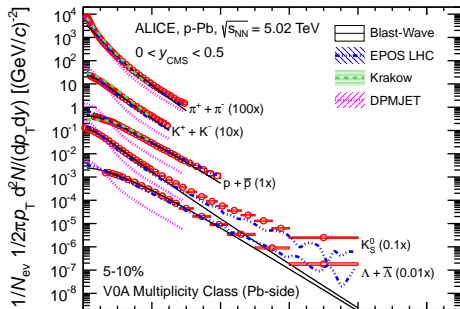
PB, W.Broniowski, G. Torrieri arXiv:1306.5442

larger $\langle p_{\perp} \rangle$ in smaller systems

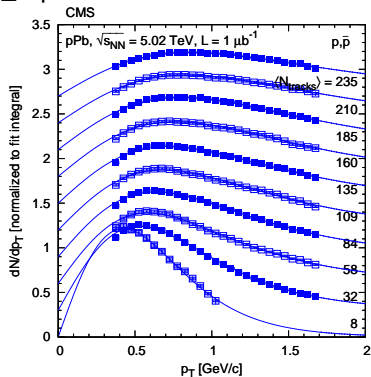
Bzdak, Skokov, arXiv:1306.5442

additional transverse push stronger for heavy particles

transverse flow in p_{\perp} spectra



p_{\perp} spectra well described by hydrodynamic models



- spectra become harder with multiplicity
- hardening strongest for heavy particles
- consistent with strong collective transverse flow increasing for central events

Experiments indicate a collective response to initial geometry

1. **Elliptic and triangular flow**
2. **Hierarchy of v_2 and v_3 in p-A, d-A, He-A**
collective response to geometry (final state effect)
3. **Flow from higher cumulants**
4. **Interferometry radii**
5. **Factorization at intermediate p_{\perp} and large $\Delta\eta$**
particles at intermediate p_{\perp} , large η , correlated to geometry
6. **Mass splitting of v_2**
7. **Mass hierarchy of spectra ($\langle p_{\perp} \rangle$)**

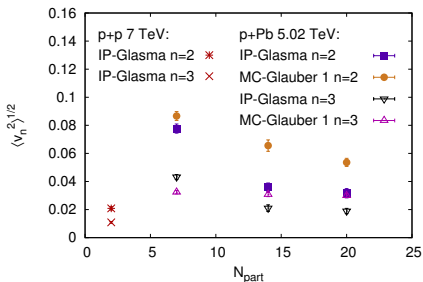
these effects can be described by hydrodynamics

what does it mean?

can hydrodynamics be applied to small systems?

Hydrodynamic flow in p-p?

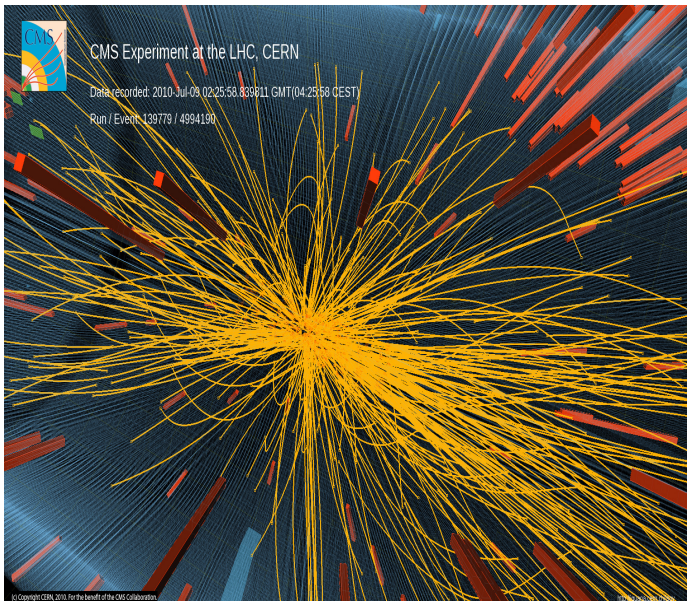
- ▶ Humanic-nucl-th/0612098 (pythia, cascade)
- ▶ Romatschke, Luzum-arXiv:0901.4588 (overlap)
- ▶ Prasad, Roy, Chattopadhyay, Chaudhuri -arXiv: 0910.4844 (overlap)
- ▶ Bozek-arXiv: 0911.2393 (flux-tubes)
- ▶ Yan, Dong, Zhou, Li, Ma, Sa- arXiv: 0912.3342 (transport)
- ▶ **CMS ridge in pp** arxiv: 10094122
- ▶ Werner, Karpenko, Pierog, Bleicher, Mikhailov-arXiv: 1010.0400 (EPOS)
- ▶ Deng, Xu, Greiner-arXiv: 1112.0470 (hot-spots, transport model)
- ▶ Shuryak, Zahed-arXiv:1301.4470 (symmetric)
- ▶ Bzdak, Schenke, Tribedy, Venugopalan-arXiv: 1304.3403 (IP-Glasma)
- ▶ **many other** estimates without full dynamics



Bzdak et al. arXiv: 1304.3403

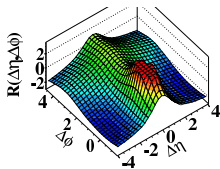
- Is hydrodynamics valid?
- What is the initial eccentricity?

High multiplicity events in pp

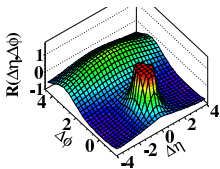


Ridge in pp

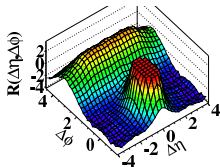
(a) CMS MinBias, $p_T > 0.1 \text{ GeV}/c$



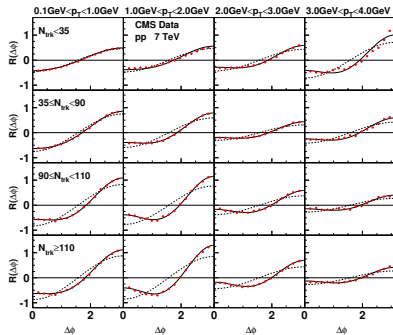
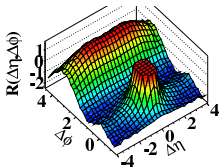
(b) CMS MinBias, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



(c) CMS $N \geq 110$, $p_T > 0.1 \text{ GeV}/c$



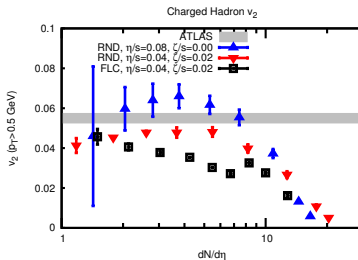
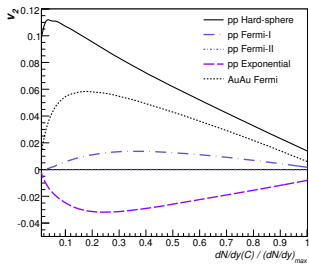
(d) CMS $N \geq 110$, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



PB arXiv:1010.0405

can we measure (or calculate) v_2 in p-p

pp collisions V_n in optical Glauber + hydro(response)

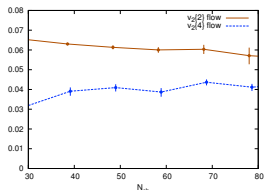
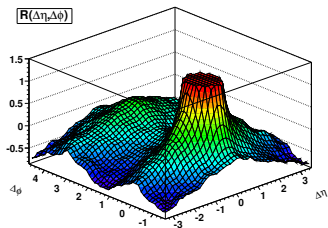


D'Enterria et al, 0910.3029

Habich et al. 1512.05354

- ▶ D'Enterria et al., 2009 ; hydro response, $v_2 \simeq 1\%$, wrong centrality dependence
- ▶ Luzumu, Romatschke, 2010 ; viscous hydro, $v_2 < 2\%$ wrong centrality dependence
- ▶ Habich et al. 2015, ; viscous hydro, $v_2 \simeq 3 - 4\%$, wrong centrality dependence

pp collisions v_n in fluctuating source + hydro(response)(...)



Avsar, Flensburg, Hatta, Ollitrault, Ueda, 1009.5643

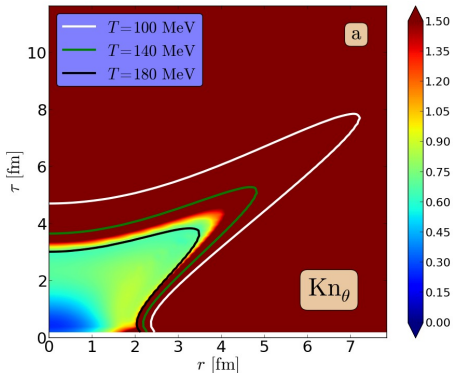
Werner, Karpenko, Pierog, 1011.0375

- ▶ Casalderrey-Solana, Wiedemann, 2010, Avsar et al. 2010, hot-spots (DIPSY) + hydro response, $v_2 \simeq 6\%$, **correct centrality dependence**
- ▶ Werner et al., 2010, EPOS + hydro, ridge
- ▶ Deng et al. 2011, hot spots + parton cascade (BAMPS), large $v_2 \geq 5\%$, $v_3 \geq 1\%$
- ▶ Bzdak et al. 2013, IP-Glasma+Hydro $v_2 \simeq 2\%$
- ▶ Ma, Bzdak, 2014, AMPT, ridge (semi-quantitative)

Observed v_n in pp are not in opposition to collective scenario or CGC

Hydrodynamics in small systems?

$$\text{Hydrodynamics } K = \frac{l_{\text{micro}}}{L_{\text{macro}}} < 1$$

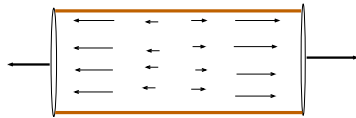


H. Niemi, G. Denicol 1404.7327

large gradients in the evolution
higher order corrections,

effective viscosity reduced

early times - longitudinal expansion - pressure asymmetry

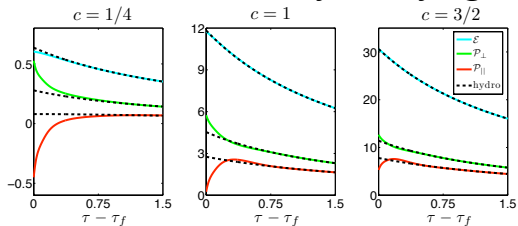


$$T^{\mu\nu} = \begin{pmatrix} \epsilon + p & 0 & 0 & 0 \\ 0 & p + \frac{2}{3} \frac{\eta}{\tau} & 0 & 0 \\ 0 & 0 & p + \frac{2}{3} \frac{\eta}{\tau} & 0 \\ 0 & 0 & 0 & p - \frac{4}{3} \frac{\eta}{\tau} \end{pmatrix}$$

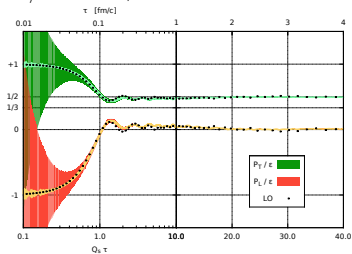
deviations from local equilibrium in early times
asymmetry between longitudinal and transverse pressure
intensively studied in kinetic theory and *asymmetric* hydrodynamics

Florkowski, Martinez, Ryblewski, Strickland, ...

Pressure asymmetry - generic feature



AdS/CFT Chesler, Yaffe 0907.4503

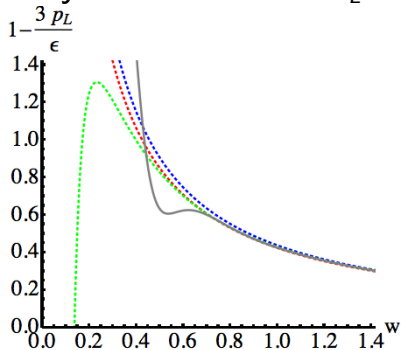


weak coupling Epelbaum, Gelis 1307.2214

Why hydrodynamic works I

Hydrodynamics works even for large pressure asymmetry

Hydrodynamics works with $P_L \ll P_\perp$

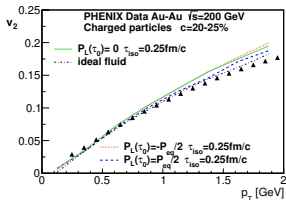
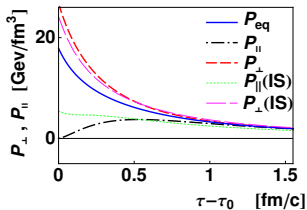


Heller, Janik, Witaszczyk 1103.3452

full solution converges to hydro

Why hydrodynamic works II

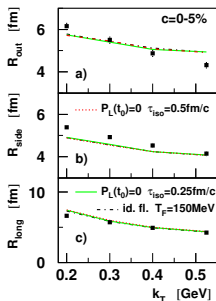
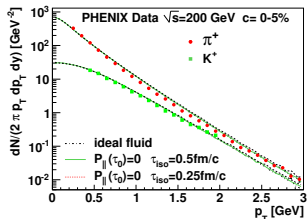
pressure anisotropy irrelevant for flow



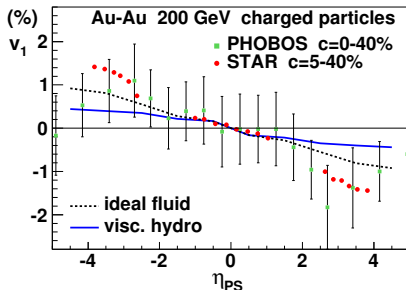
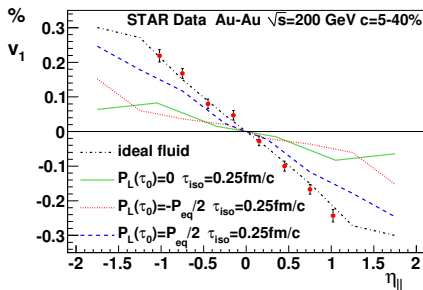
PB, I. Wyskiel - arXiv:1009.0701

- early pressure anisotropy irrelevant!

Vredevoogd, Pratt, 0810.4325



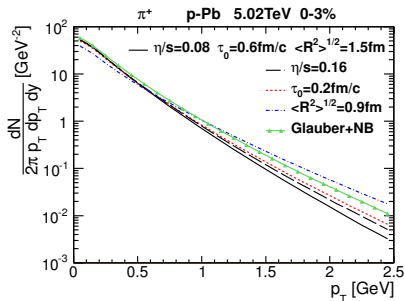
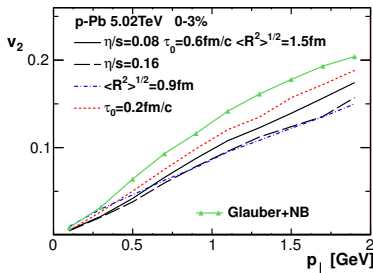
Pressure anisotropy - directed flow



PB, I. Wyskiel - arXiv:1009.0701

- v_1 could be used to estimate isotropization time
- large model uncertainties
- same for bottomonia, dileptons
- asymmetry from viscosity compatible v_1 data in AA

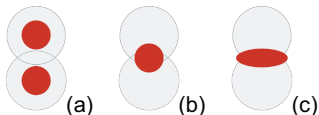
dependence on model details



response strength depends on details (more than in AA!)

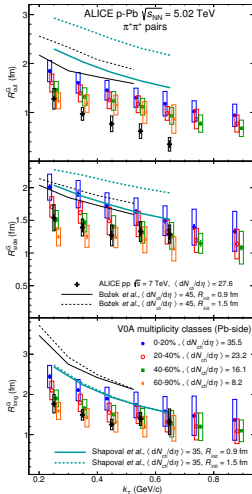
- ▶ initial eccentricity
- ▶ initial size 'compact' vs 'standard'
- ▶ viscosity
- ▶ initial time for expansion

compact source



Bzdak et al. 1304.3403

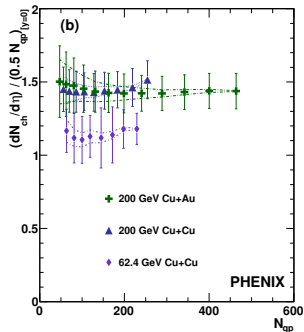
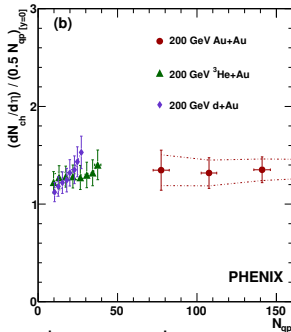
compact source 0.9fm
standard source 1.5fm



HBT \rightarrow initial size of the fireball in pA small

Constituent quark model - PHENIX

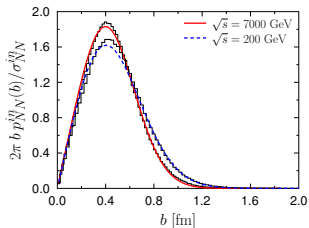
PHENIX 2015



- three quarks per nucleon
- Q distribution in N from electron-proton
- hard-sphere Q-Q scattering (8.17mb at 200GeV)
- fairly good scaling with N_Q , problem with p-p point
- recent (2016) calculations : Lacey et al., Zheng et al. , Loizides, Mitchell et al.

Wounded quark model - pp scattering

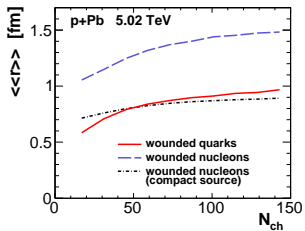
- three quarks distributed in each nucleon $\rho(r) \simeq e^{-r/b}$
- recentering
- Gaussian Q-Q wounding profile
- parameters fitted to reproduce N-N scattering



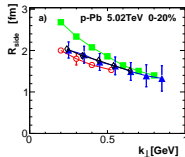
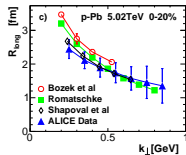
(200GeV, $\sigma_{QQ} = 7\text{mb}$, $r_{QQ} = 0.29\text{fm}$) (7000GeV, $\sigma_{QQ} = 14.3\text{mb}$, $r_{QQ} = 0.30\text{fm}$)

- small change of nucleon size with \sqrt{s}
- increase of σ_{QQ} with \sqrt{s}

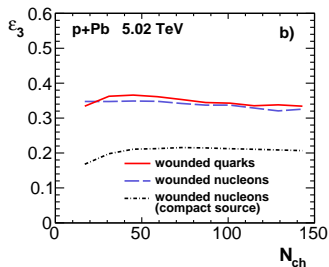
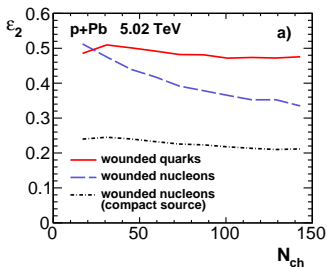
Fireball size in p-Pb



- wounded quark model gives small fireball size
- *compact source* consistent with p-Pb data (HBT, $\langle p_{\perp} \rangle$)

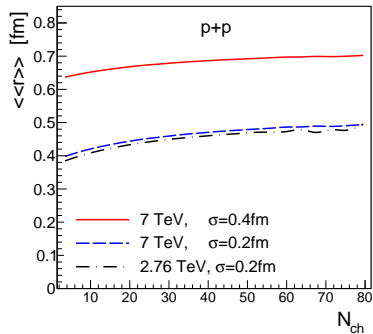
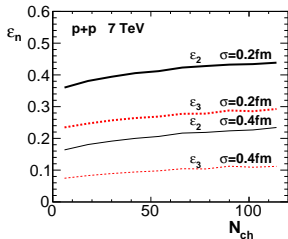


Fireball eccentricities in p-Pb



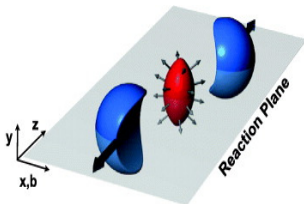
- significant eccentricities in p-Pb
- consistent experimental observation of v_2 and v_3 in p-Pb

p-p scattering



- significant eccentricities in p-p
- small size of the interaction region **0.4fm**

azimuthally-sensitive HBT



correlation measured at fixed angle w.r. to the event plane

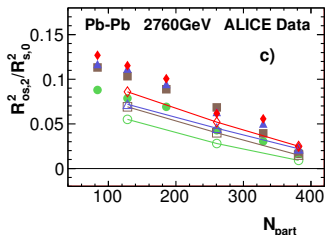
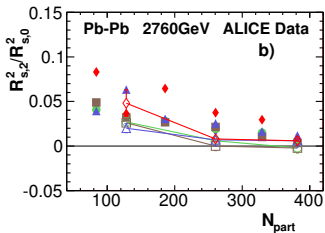
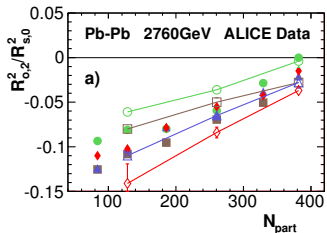
$$C(k_{\perp}, \phi, q) = 1 + \lambda e^{-R_o^2 q_o^2 - R_s^2 q_s^2 - R_l^2 q_l^2 - R_{os}^2 q_o q_s}$$

- dependence on ϕ

$$R_i(\phi)^2 = R_{i,0}^2 + 2\cos(2\phi)R_{i,2}^2$$

- new radius parameter R_{os}

azHBT in Pb-Pb at 2.76TeV (second order reaction plane)



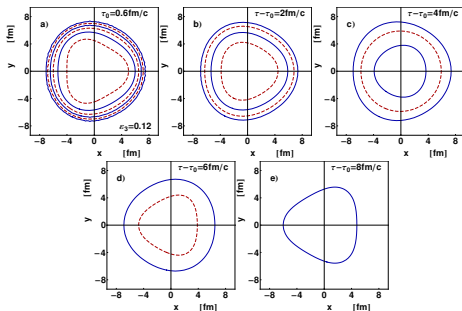
- ▶ eccentricity and elliptic flow give azimuthal angle dependence
- ▶ fair agreement with data

- Further confirmation of elliptic flow and deformation

azHBT in Au-Au at 200GeV (third order event plane)

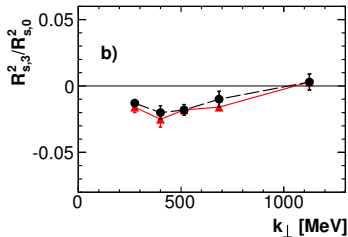
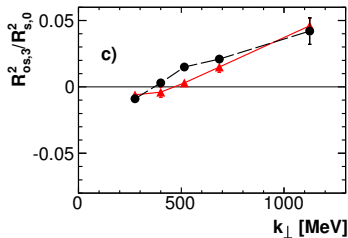
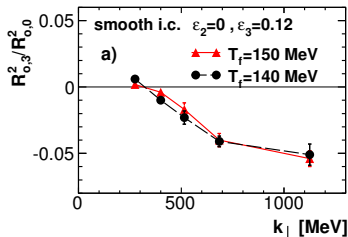
what is the origin of the $\cos(3\Phi)$ angular dependence (Plumberg, Shen, Heinz, 2013)

- ▶ deformed geometry + radial flow
- ▶ triangular flow



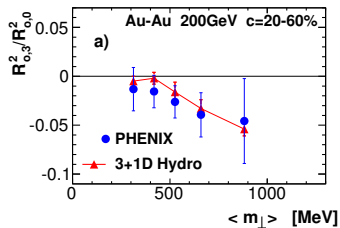
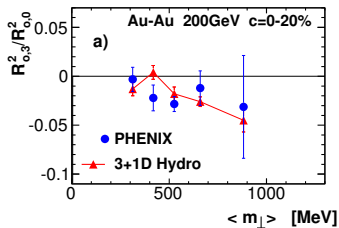
- ▶ OR both flow and geometry
- ▶ OR both flow and inverted geometry (example)

HBT third order reaction plane, smooth density (example)



- negative, k_{\perp} depend. $R_{o,3}^2$
- positive, k_{\perp} depend. $R_{os,3}^2$
- small, negative $R_{s,3}^2$

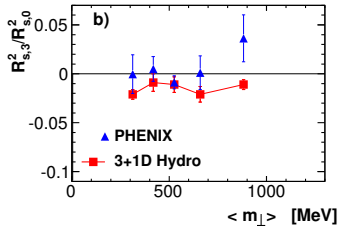
HBT third order reaction plane $R_{O,3}^2$



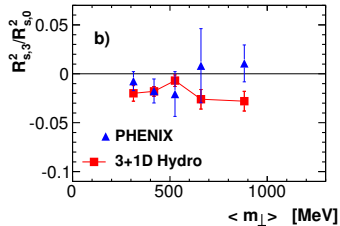
fair agreement with PHENIX

HBT third order reaction plane $R_{s,3}^2$

0-20%

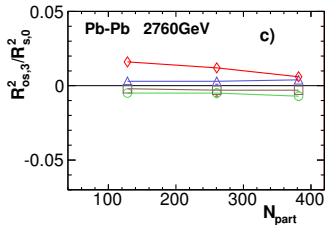
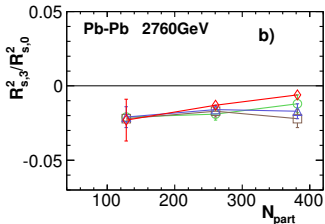
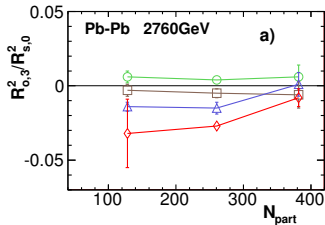


20-60%



compatible with PHENIX data for 20-60%, tension for 0-20%

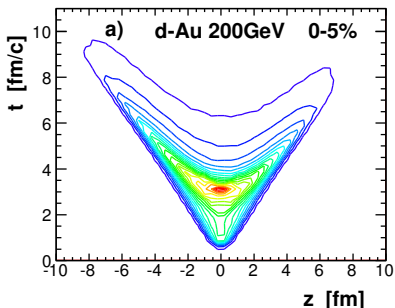
azHBT in Pb-Pb at 2.76TeV (third order reaction plane)



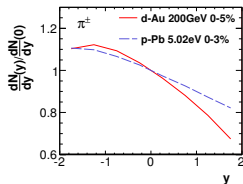
- ▶ similar as Au-Au at RHIC
- ▶ small negative $R_{s,3}^2$
- ▶ negative, k_{\perp} depend. $R_{o,3}^2$

Asymmetric collisions p-Pb, d-Au

different emission times in forward-backward hemispheres

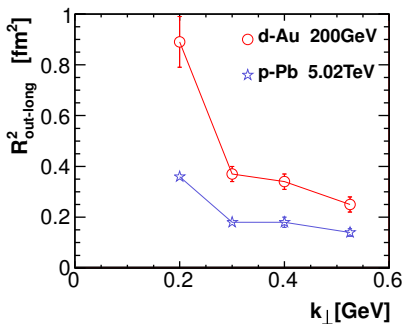


FB asymmetry



lcms of the pion

$R_{out-long} \neq 0$ in asymmetric collisions

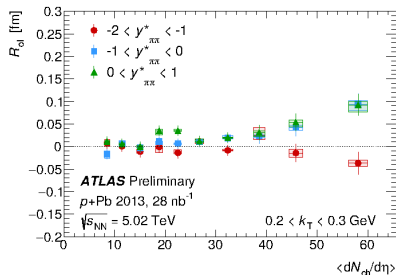
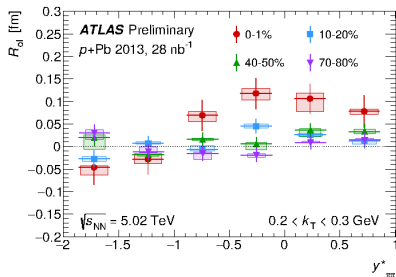


$$C(q, k_{\perp}) = 1 + \lambda e^{-R_o^2 q_o^2 - R_s^2 q_s^2 - R_l^2 q_l^2 - 2R_{ol}^2 q_o q_l}$$

$$R_{ol}^2 = H_1 + I_1 - G_0 \beta_{\perp} + (I_1 + \dots) \cos(2\Phi)$$

$$\langle zxcos(\Phi) \rangle, \langle zysin(\Phi) \rangle, \langle zt \rangle$$

R_{ol} cross term

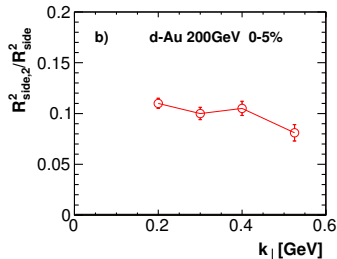
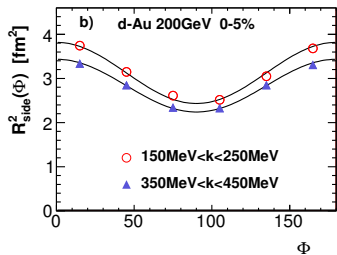


In *central events* on the *forward* side, there is strong evidence of a positive R_{ol} (4.8σ combined significance in 0–1% centrality)

- ▶ demonstrates breaking of boost invariance: z-asymmetry is manifest in proton-going side.
- ▶ requires both longitudinal and transverse expansion in hydrodynamic models

azimuthally sensitive HBT in d-Au

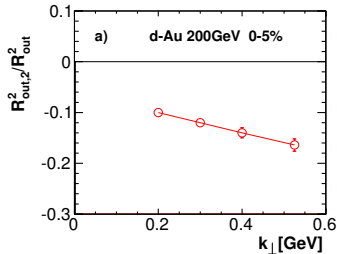
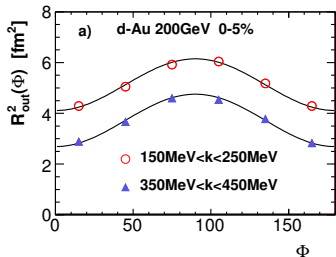
$$R_s^2(\Phi) = R_{s,0}^2 + 2R_{s,2}^2 \cos(2\Phi)$$



R_{side} larger in-plane

azimuthally sensitive HBT in d-Au - R_{out}

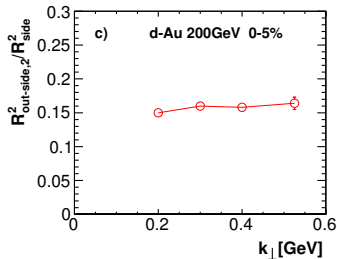
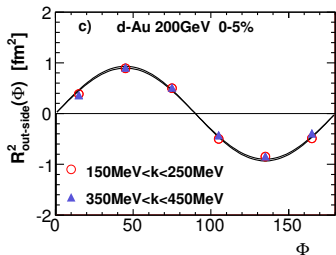
$$R_{out}^2(\Phi) = R_{o,0}^2 + 2R_{o,2}^2 \cos(2\Phi)$$



R_{out} smaller in-plane

azimuthally sensitive HBT in d-Au - $R_{out-side}$

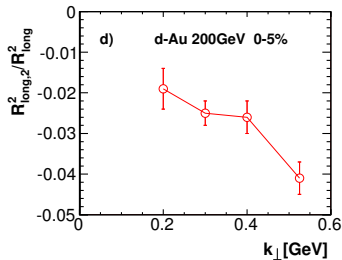
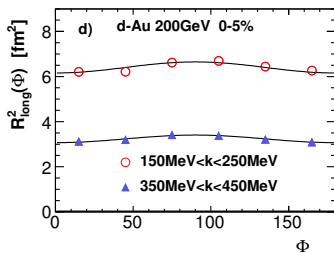
$$R_{os}^2(\Phi) = 2R_{os,2}^2 \sin(2\Phi)$$



$$R_{out-side} \neq 0$$

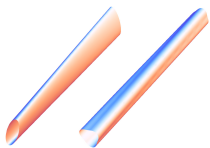
azimuthally sensitive HBT in d-Au - R_{long}

$$R_l^2(\Phi) = R_{l,0}^2 + 2R_{l,2}^2 \cos(2\Phi)$$

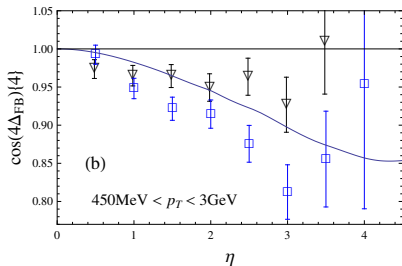


$$R_{long,2} \neq 0$$

event by event twist of the reaction plane



Fluctuating RP twist
can be measured



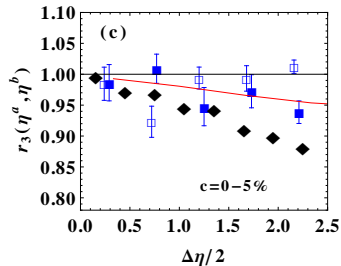
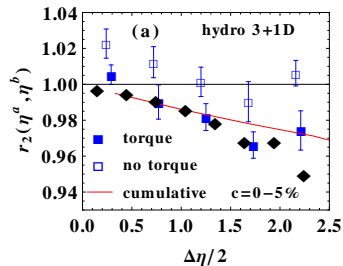
PB, Broniowski, Moreira, Phys. Rev. C83, 034911 (2011)

$$\cos(2k\Delta_{FB})\{4\} \equiv \frac{\langle e^{ik[(\phi_{F,1}+\phi_{F,2})-(\phi_{B,1}+\phi_{B,2})]} \rangle}{\langle e^{ik[(\phi_{F,1}-\phi_{F,2})-(\phi_{B,1}-\phi_{B,2})]} \rangle} = \langle \cos(2k\Delta_{FB}) \rangle_{\text{events}} + \text{nonflow}$$

3-bin measure of event-plane decorrelation (CMS)

$$r_2(\eta_a, \eta_b) = \frac{\langle\langle \cos[n(\phi_i(-\eta_a) - \phi_j(\eta_b))] \rangle\rangle}{\langle\langle \cos[n(\phi_i(\eta_a) - \phi_j(\eta_b))] \rangle\rangle} \simeq \frac{\cos[n(\Psi(-\eta_a) - \Psi(\eta_b))]}{\cos[n(\Psi(\eta_a) - \Psi(\eta_b))]}$$

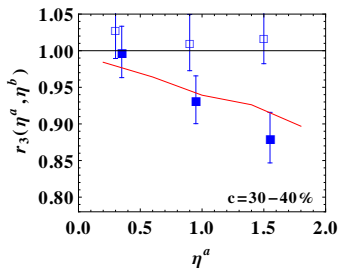
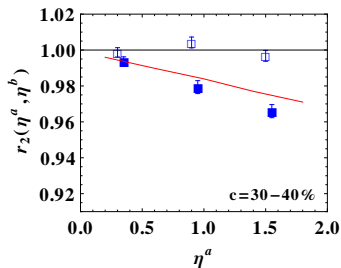
only pairs with large rapidity gap $\eta_a - \eta_b$



- nonflow under control
- torque effect seen in the CMS data
- semiquantitative agreement, but need more fluctuations
- other calculation (hybrid hydro, AMPT) reproduce the data

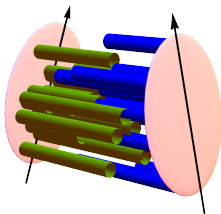
$r_n(\eta_a, \eta_b)$ Au-Au at 200GeV

predictions ($3 < \eta_b < 4.5$)



- larger twist angle at RHIC energies

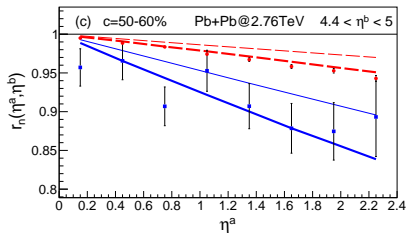
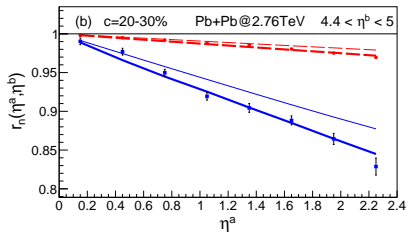
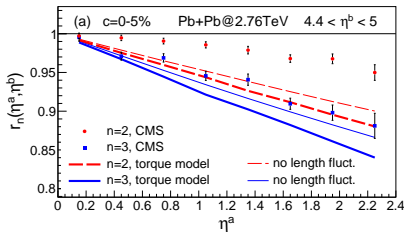
Fluctuations in energy deposition from each source



- the position (in rapidity) of string ends is random
- long range fluctuations
- each source fluctuates differently \longrightarrow event-plan decorrelation in p-Pb
- short range fluctuations possible, but irrelevant for the CMS r_2
- average deposition same as in old model (linear in η)

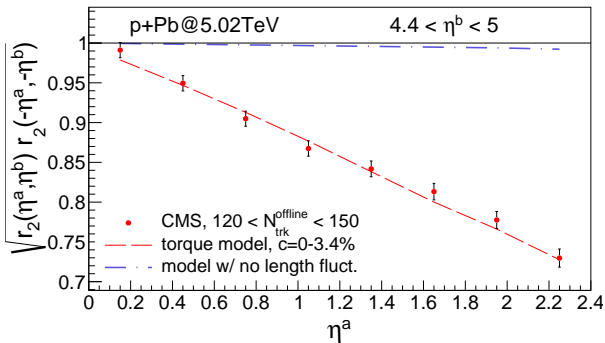
PB, Broniowski 1503.03655; Monnai, Schenke 1509.04362

Fluctuating strings $r_n(\eta_a, \eta_b)$ (initial state only)



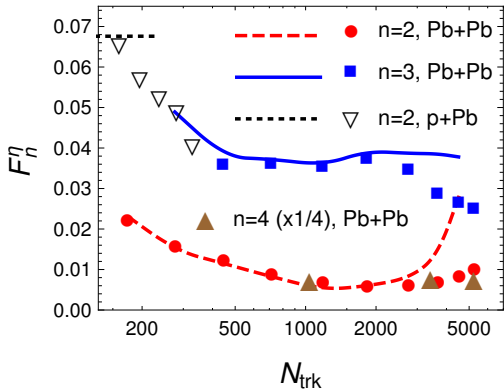
fluctuations improve description of r_2
in Pb-Pb
except for r_2 in central collisions

Fluctuating strings p-Pb



- fluctuations essential to describe event-plane decorrelation in p-Pb

F slope



- fair description of mid-central collisions
- overestimates decorrelation in central collisions
- $F_4 \simeq 4F_2$

Can hydrodynamic work in small systems

1. Mean free path

- ▶ for $\eta/s = 0.08$

$$L_{mfp} = \frac{3s}{4\pi np} \simeq 0.15 - 0.3 fm$$

2. Quantitative hydrodynamic model requires dominance of hydrodynamic modes

- ▶ estimate of minimal size R (Spalinski 1607.06381)

$$RT > 2\pi \sqrt{2T\tau_\pi \eta/s} \simeq 1 - 3$$

3. AdS/CFT

- ▶ in numerical AdS/CFT: $RT > 1$, (Chesler 1601.01583)
- ▶ minimal size $R > 0.5 fm$

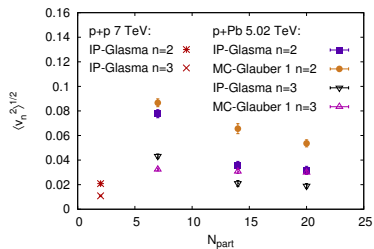
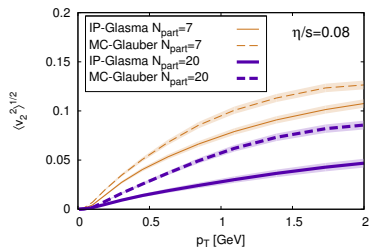
Hydrodynamics works down to $N_{ch} = 10 - 30$ (ATLAS, CMS)

Success of hydrodynamics not accidental!

Relativistic viscous hydrodynamics describes the evolution of the fireball in small systems

1. Collective response to geometry
2. Hydrodynamic model describes the data
3. Using hydrodynamics in small systems “not absurd”
4. Small systems with collectivity \rightarrow many further studies possible: HBT, mapping of production mechanism via correlations, jets, check for chiral magnetic effect, . . .

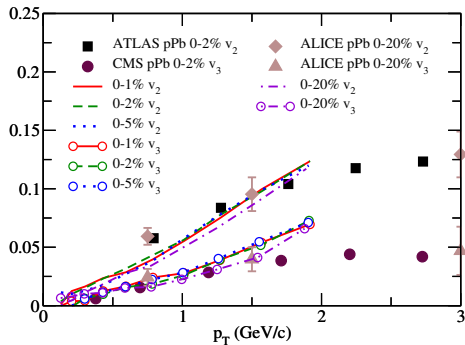
3+1D visc. hydro



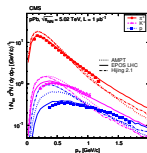
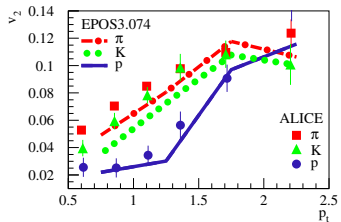
dependence on initial model, v_n small for IP-Glasma i.c.

A.Bzdak, B.Schenke, P.TribeDY, R.Venugopalan - arXiv: 1304.3403

3+1D hydro



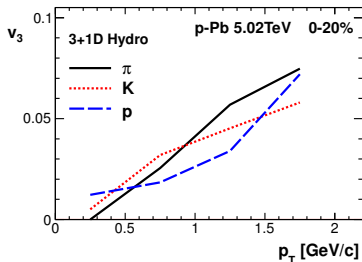
G-Y.Qin, B. Müller arXiv: 1306.3439



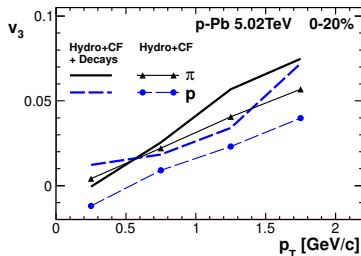
excellent description of spectra

K. Werner, M. Bleicher, B. Guiot, Iu. Karpenko, T. Pierog - arXiv:1307.4379

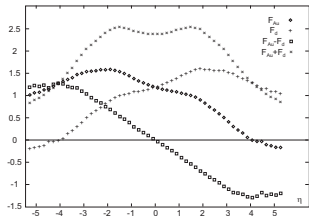
v_3 - small mass splitting



limited mass splitting

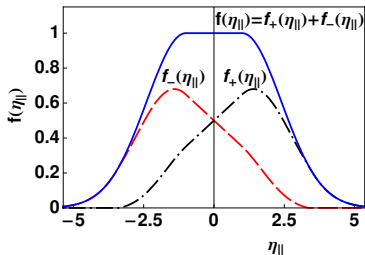


resonance decays spoil mass ordering

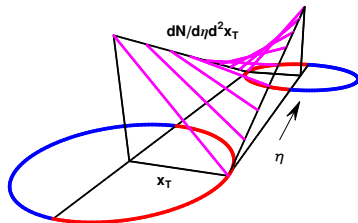


Asymmetric emission

(Białas, Czyż, Acta Phys.Polon.B36, 905 (2005))



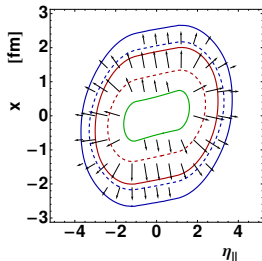
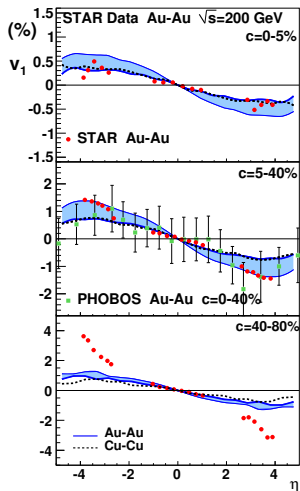
$$\rho(\eta, x, y) \propto f_{+}(\eta)N_{+}(x, y) + f_{-}(\eta)N_{-}(x, y)$$



bremsstrahlung (Adil Gyulassy, Phys. Rev.

C72, 034907 (2005))

Directed flow- tilted source



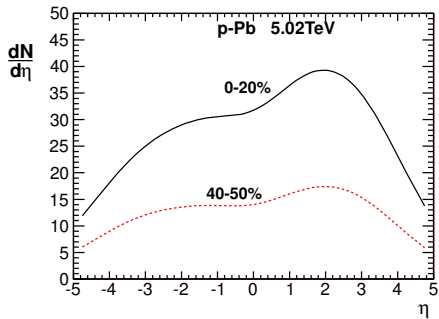
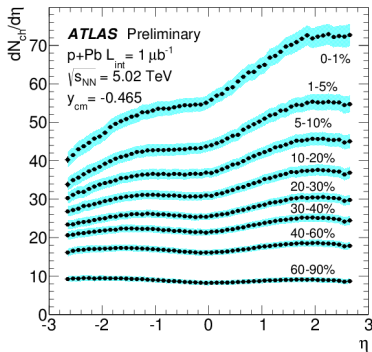
Bozek, Wyslciel, Phys. Rev. C81, 054902 (2010)

$$\partial_\tau u_x = -\frac{\partial_x p_\perp}{p + \epsilon}$$

$$\partial_\tau Y = -\frac{\partial_\eta p_\parallel}{\tau(p + \epsilon)}$$

tilted source \rightarrow transverse pressure + longitudinal pressure
Glauber model

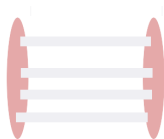
Asymmetric distributions



FSI scenarios

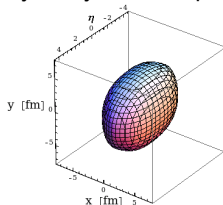
fields+thermalization

color fields

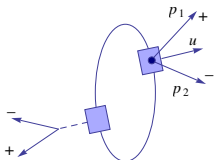


hydrodynamics

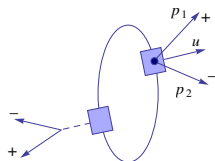
hydrodynamic expansion



local thermalization \rightarrow hadronization



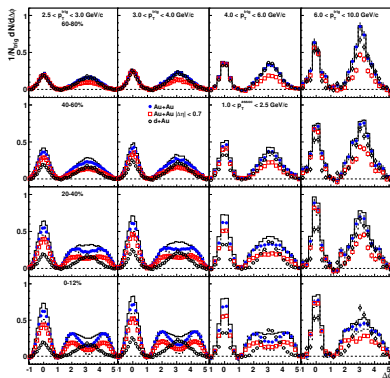
hadronization, statistical emission



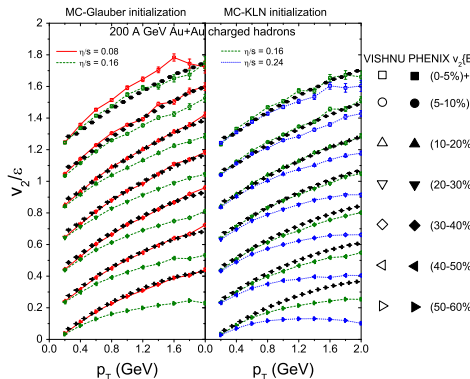
Give similar flow



Can we reduce uncertainties? go back to very peripheral A-A



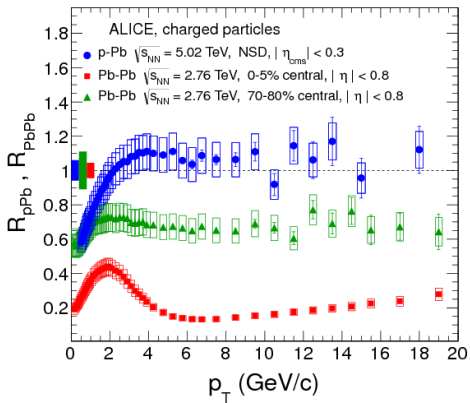
STAR-arXiv:1004.2377



Song, Bass, Heinz, Hirano, Shen-arXiv:1101.4638

also jet modification, dijet asymmetry, PID flow, HBT

Flow without jet quenching?



energy-momentum tensor

$$T^{\mu\nu} = \begin{pmatrix} \epsilon & 0 & 0 & 0 \\ 0 & p + \Pi & 0 & 0 \\ 0 & 0 & p + \Pi & 0 \\ 0 & 0 & 0 & p + \Pi \end{pmatrix} + \pi^{\mu\nu}$$

- ▶ shear viscosity

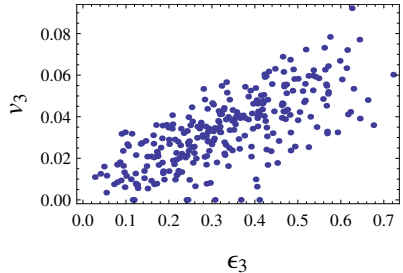
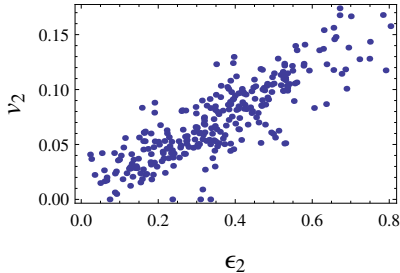
$$\Delta^{\mu\alpha} \Delta^{\nu\beta} u^\gamma \partial_\gamma \pi_{\alpha\beta} = \frac{2\eta\sigma^{\mu\nu} - \pi^{\mu\nu}}{\tau_\pi} - \frac{1}{2}\pi^{\mu\nu} \frac{\eta T}{\tau_\pi} \partial_\alpha \left(\frac{\tau_\pi u^\alpha}{\eta T} \right)$$

- ▶ bulk viscosity

$$u^\gamma \partial_\gamma \Pi = \frac{-\zeta \partial_\gamma u^\gamma - \Pi}{\tau_\Pi} - \frac{1}{2}\Pi \frac{\zeta T}{\tau_\Pi} \partial_\alpha \left(\frac{\tau_\Pi u^\alpha}{\zeta T} \right)$$

- ▶ viscosity corrections from velocity gradients
- ▶ **initial** stress tensor - pressure anisotropy
- ▶ equation of state

fireball asymmetry - flow asymmetry



- Ev-by-Ev hydro response to geometry valid
- response strength depends on details