



# Rare B-decays

Lars Eklund on behalf of the LHCb Collaboration

## Experimental overview

Results from Babar, Belle, LHCb, ATLAS and CMS

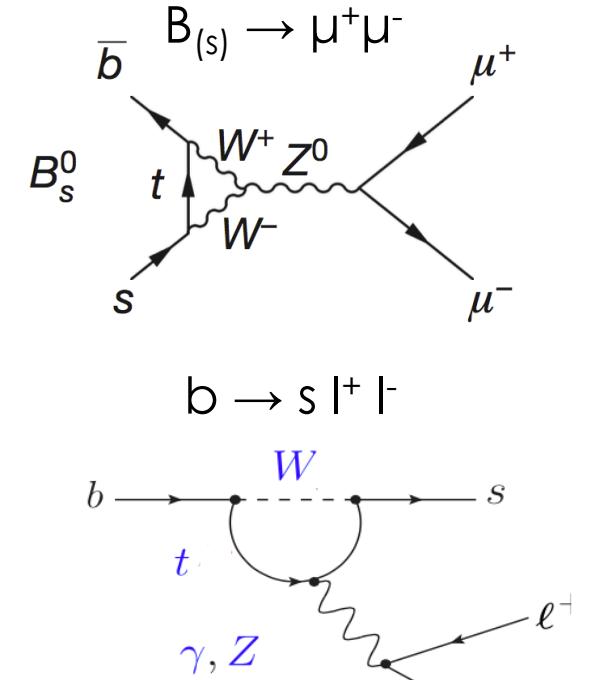
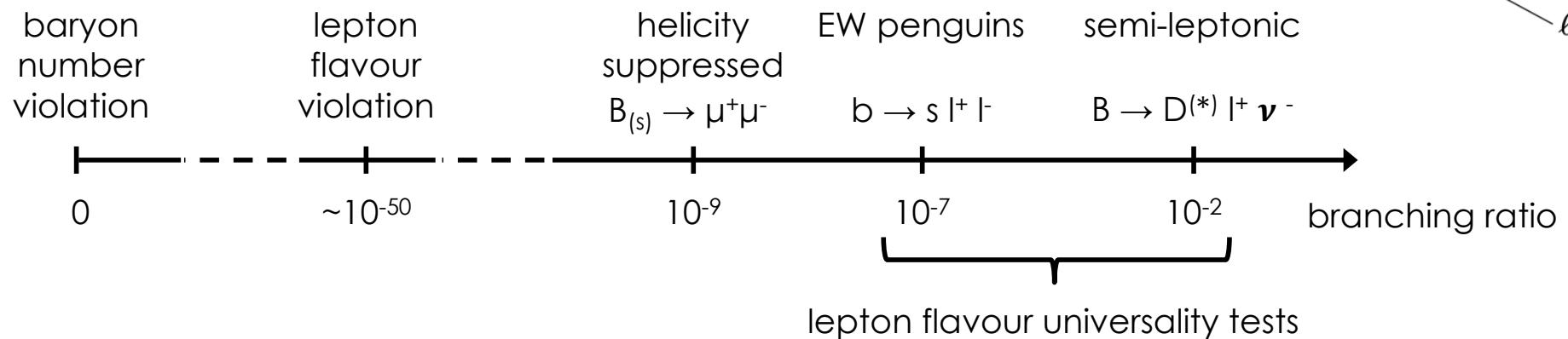


University  
of Glasgow



# Why study rare processes?

- Rare decays: SM is suppressed
  - Sensitive to BSM contributions
- Flavour Changing Neutral Currents (FCNC)
  - Forbidden at tree-level in the SM
  - Further suppression, e.g. helicity
- Probes mass scales beyond direct searches
  - Up to  $\sim 100$  TeV





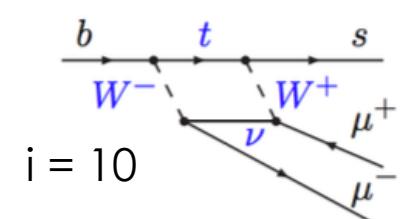
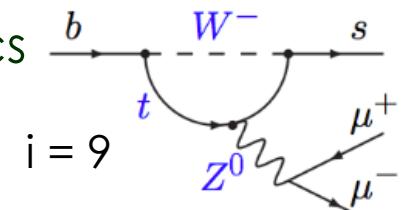
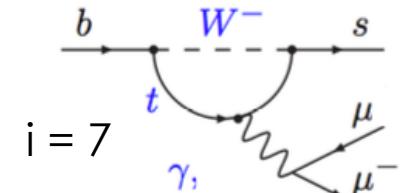
# FCNC: theoretical description

- Processes at many different energy scales

0.2 GeV ... 4 GeV ... 80 GeV ... 10-100 TeV

$\Lambda_{\text{QCD}}$        $\Lambda_b$        $\Lambda_{\text{EW}}$        $\Lambda_{\text{BSM}}$   
(non-perturbative)    b mass    W mass    BSM scale

Example of SM terms



- Described by an effective Hamiltonian

- $O_i$  (Operators): long-distance, non-perturbative physics
- $C_i$  (Wilson coefficients): short distance, high energy physics
  - BSM processes may modify these coefficients

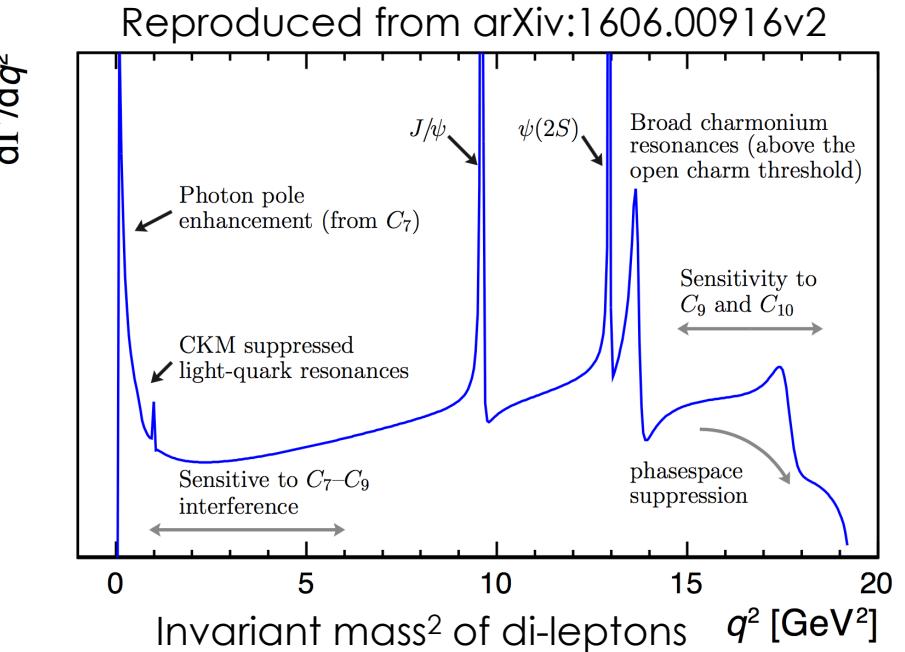
$$H_{eff} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i [\underbrace{C_i(\mu) O_i(\mu)}_{\text{left handed}} + \underbrace{C'_i(\mu) O'_i(\mu)}_{\text{right handed}}]$$

(suppressed in the SM)



# Rare decay observables

- (Differential) branching ratios
  - $q^2$  dependence for  $b \rightarrow s l^+ l^-$ 
    - E.g.  $B^0 \rightarrow K^* \mu^+ \mu^-$
- Angular distributions
  - $b \rightarrow s l^+ l^-$  decays
- Effective lifetime
  - $B_s$  decays where  $\Delta\Gamma_s \neq 0$ 
    - Measure of CP violation
- BSM processes can modify the effective Hamiltonian by
  - Modifying Wilson coefficients of operators present in SM
  - Making Wilson coefficients dependent on lepton flavour
  - Introducing new operators





# Overview of results

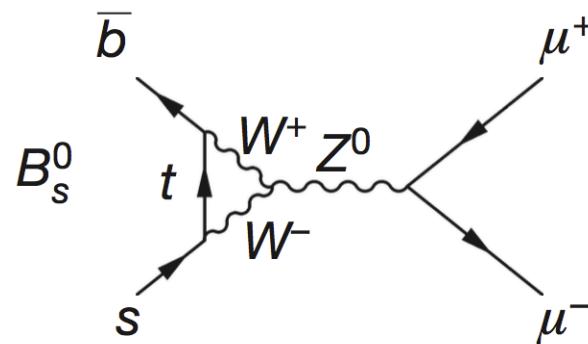
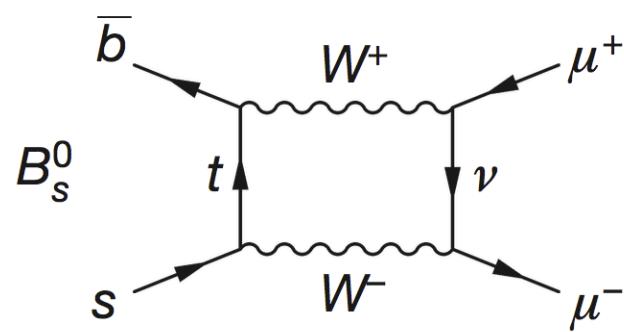
---

- Fully leptonic decays
  - $B_{(s)} \rightarrow \mu^+ \mu^-$  &  $B_{(s)} \rightarrow \tau^+ \tau^-$
- Electroweak  $b \rightarrow s l^+ l^-$  transitions
  - $B^0 \rightarrow K^* \mu^+ \mu^-$  and friends
  - Differential branching ratios & angular analysis
  - Global fits to Wilson coefficients
- Lepton flavour universality test ( $l^+ = e^+, \mu^+$  or  $\tau^+$ )
  - $B \rightarrow K^{(*)} l^+ l^-$  decay rates
  - $B \rightarrow D^{(*)} l^+ \nu$  decay rates
- Outlook



# Fully leptonic final states

$B_{(s)} \rightarrow \mu^+ \mu^-$  and friends





# $B_{(s)} \rightarrow \mu^+ \mu^-$ branching ratio

- Very precise predictions available

- Only  $C_{10}$  contribute in the SM:  $BR(B_q \rightarrow l^+ l^-) \propto m_l^2 \sqrt{1 - \frac{4m_l^2}{m_{B_q}^2}} |C_{10}|^2$

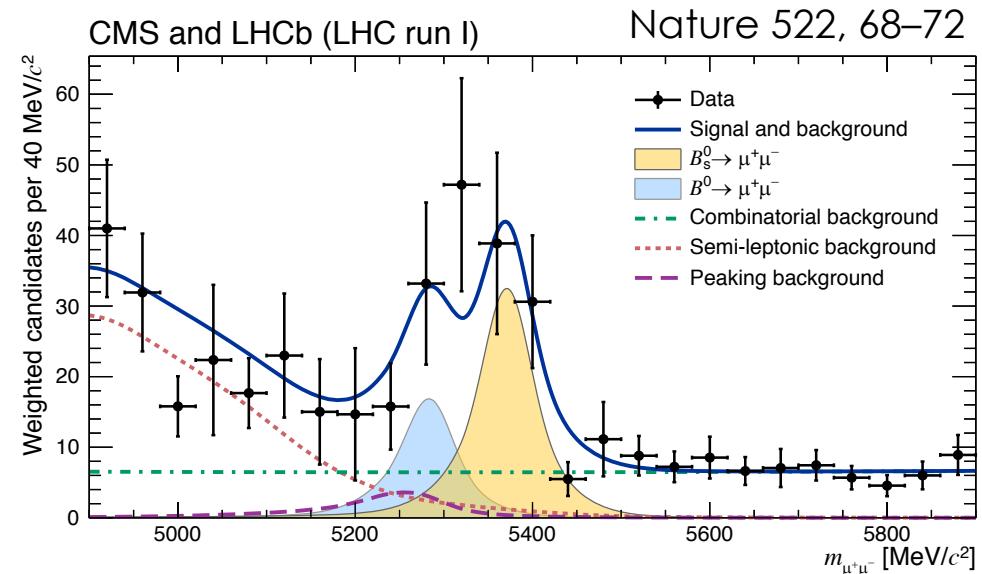
$$\overline{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} = (3.52 \pm 0.15) \times 10^{-9}, \quad BR(B^0 \rightarrow \mu^+ \mu^-)_{\text{SM}} = (1.12 \pm 0.12) \times 10^{-10}$$

- BSM scalar & pseudo-scalar operators may contribute
    - Change in decay rate
    - Mixing induced CP violation

- LHCb & CMS: Run 1 dataset
  - Observation of  $B_s \rightarrow \mu^+ \mu^-$  ( $6.2 \sigma$ )
  - Evidence for  $B^0 \rightarrow \mu^+ \mu^-$  ( $3.0 \sigma$ )

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (2.8^{+0.7}_{-0.6}) \times 10^{-9}$$

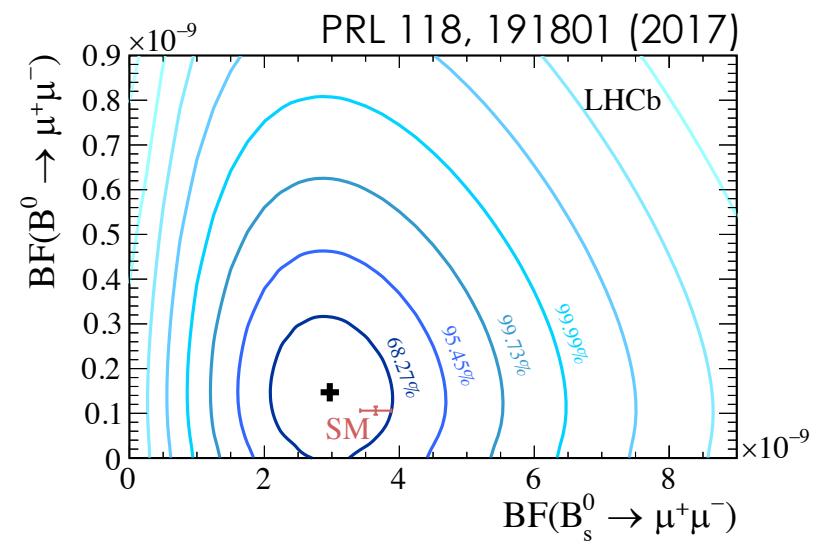
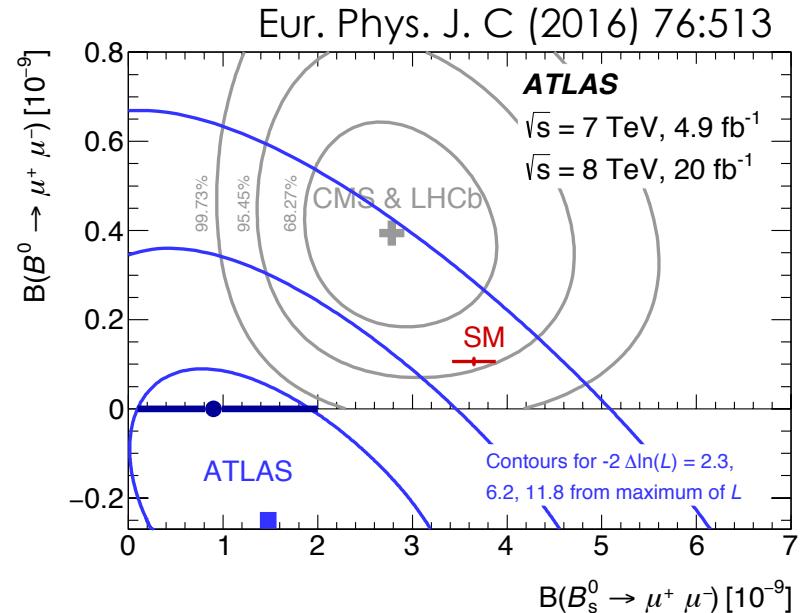
$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) = (3.0^{+1.6}_{-1.4}) \times 10^{-10}$$





# $B_{(s)} \rightarrow \mu^+ \mu^-$ branching ratio

- ATLAS:  $25 \text{ fb}^{-1}$  run I
  - First ATLAS result on  $B_{(s)} \rightarrow \mu^+ \mu^-$ 
 $\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (0.9^{+1.1}_{-0.8}) \times 10^{-9}$ 
Significance:  $1.4\sigma$  (3.0 expected from SM)
  $\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) < 4.2 \times 10^{-10}$  (95 % CL)
- LHCb  $3+1.4 \text{ fb}^{-1}$  run I+II
  - First single experiment observation
    - $7.9\sigma$  significance  $B_s \rightarrow \mu^+ \mu^-$ 
 $\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.0 \pm 0.6^{+0.3}_{-0.2}) \times 10^{-9}$ 
 $\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) < 3.4 \times 10^{-10}$
    - Effective lifetime of  $B_s \rightarrow \mu^+ \mu^-$ 
 $\tau(B_s^0 \rightarrow \mu^+ \mu^-) = 2.04 \pm 0.44 \pm 0.05 \text{ ps}$





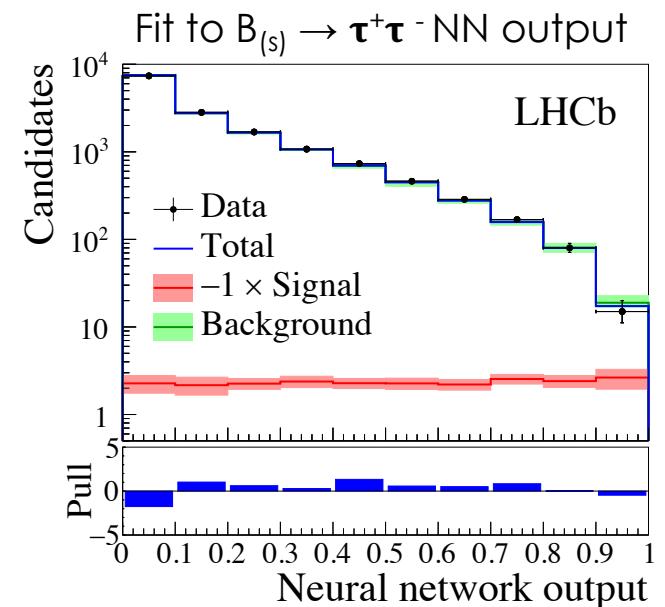
# The heavier cousin: $B_{(s)} \rightarrow \tau^+ \tau^-$

- LHCb 3 fb<sup>-1</sup> run 1 PRL 118, 251802 (2017)
  - Larger branching ratio due to the larger mass
    - Additional enhancement possible in BSM scenarios that violate LFU

$$\overline{\text{BR}}(B_s \rightarrow \tau^+ \tau^-)_{\text{SM}} = (7.46 \pm 0.30) \times 10^{-7}, \quad \text{BR}(B^0 \rightarrow \tau^+ \tau^-)_{\text{SM}} = (2.35 \pm 0.24) \times 10^{-8}$$

- Experimentally challenging: multiple neutrinos in the final state
  - Reconstructed in the mode  $\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu_\tau$
  - Normalisation  $B_s \rightarrow D^- (\rightarrow K^+ \pi^- \pi^-) D_s (\rightarrow K^- K^+ \pi^+)$

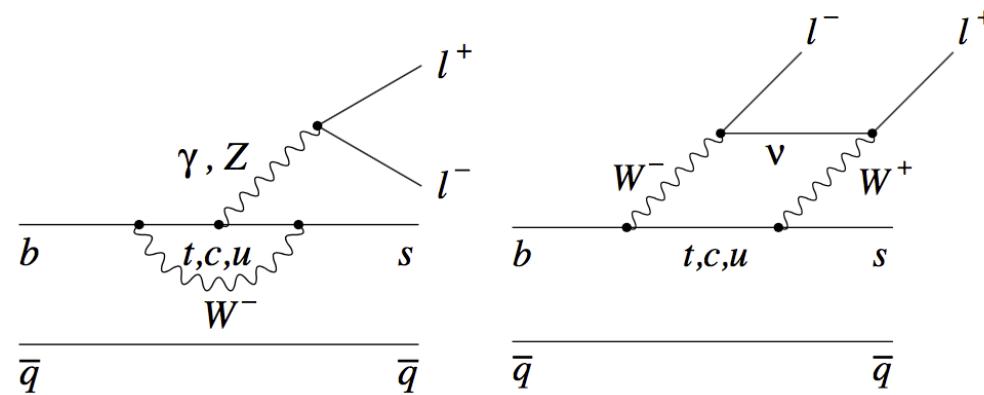
$$\mathcal{B}(B_s^0 \rightarrow \tau^+ \tau^-) < 6.8 \times 10^{-3} \text{ at 95% CL}$$
$$\mathcal{B}(B^0 \rightarrow \tau^+ \tau^-) < 2.1 \times 10^{-3} \text{ at 95% CL}$$





# Electroweak $b \rightarrow s l^+ l^-$ transitions

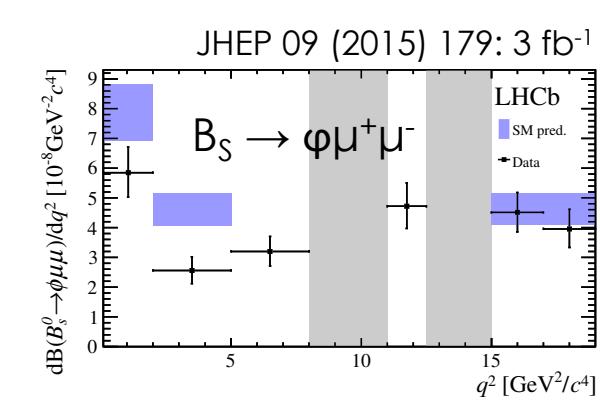
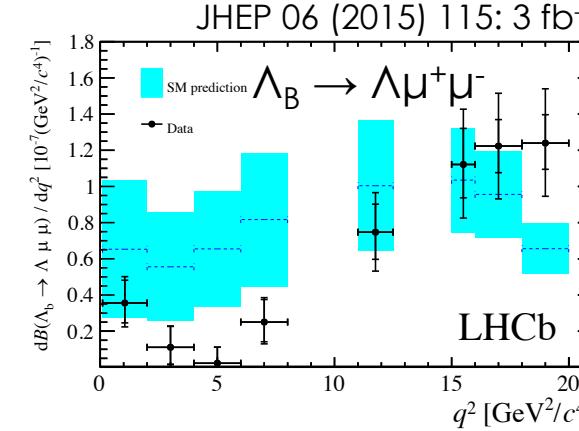
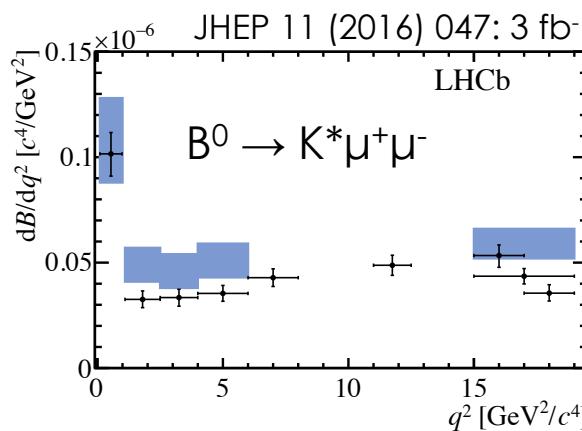
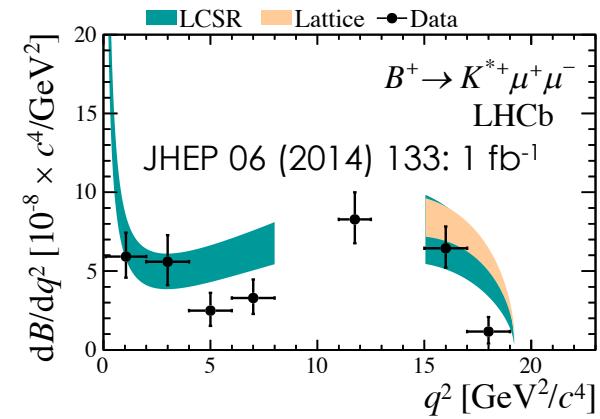
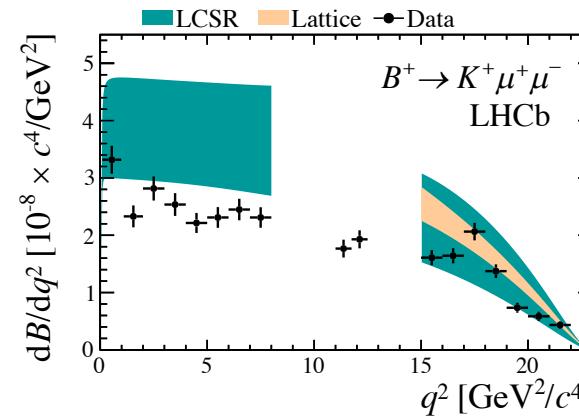
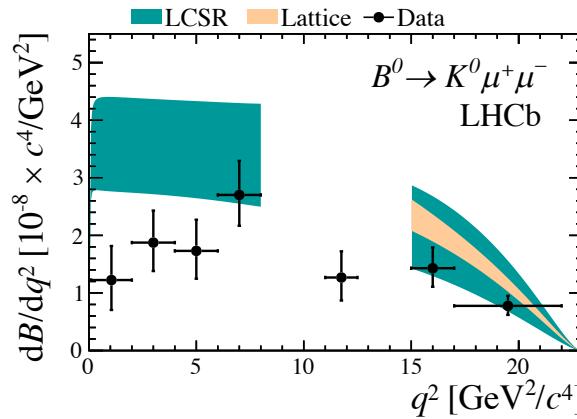
$B^0 \rightarrow K^* \mu^+ \mu^-$  and friends





# $b \rightarrow s l^+ l^-$ differential branching ratios

- LHCb: differential branching fractions in several  $b \rightarrow s l^+ l^-$  modes
  - Versus di-muon invariant mass squared:  $q^2$

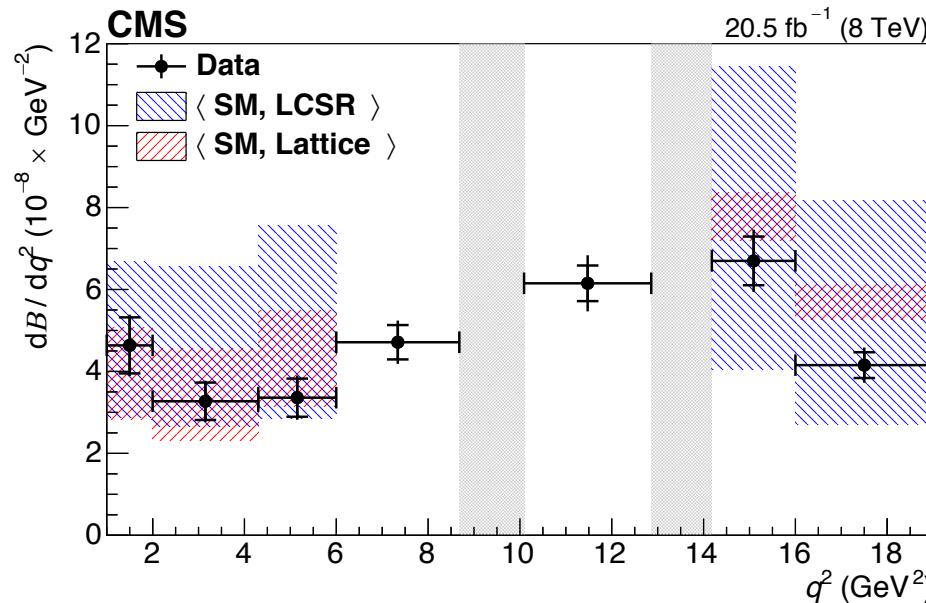


- Discrepancy in the low di-muon invariant mass region



# $b \rightarrow s l^+ l^-$ differential branching ratios

- CMS:  $20.5 \text{ fb}^{-1}$  run I Phys. Lett. B 753 (2016) 424
  - $B^0 \rightarrow K^* \mu^+ \mu^-$  differential branching ratio
  - Compatible with SM & LHCb results



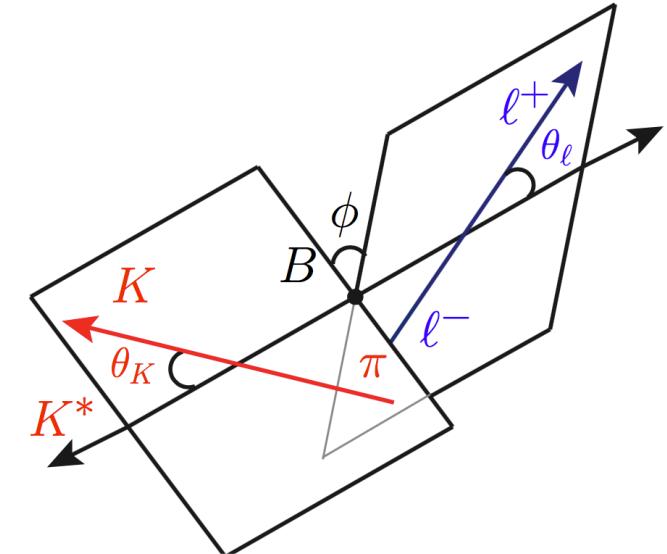


# $b \rightarrow s l^+ l^-$ angular observables

- Angles defined in  $B$  meson rest frame

- Angular variables:  $\theta_l$ ,  $\theta_K$  &  $\phi$
- Di-lepton invariant mass<sup>2</sup>:  $q^2$
- Fit PDF for  $B^0 \rightarrow K^*\mu^+\mu^-$

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2 \theta_K + \boxed{F_L} \cos^2 \theta_K \right. \\ + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_l \\ - F_L \cos^2 \theta_K \cos 2\theta_l + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi \\ + S_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + \boxed{S_5} \sin 2\theta_K \sin \theta_l \cos \phi \\ + \frac{4}{3} \boxed{A_{FB}} \sin^2 \theta_K \cos \theta_l + S_7 \sin 2\theta_K \sin \theta_l \sin \phi \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \right]$$



- Form-factor uncertainties in the predictions of observables
  - Alternative set of 7 observables with reduced uncertainties:  $P_i^{(')}$

For instance:

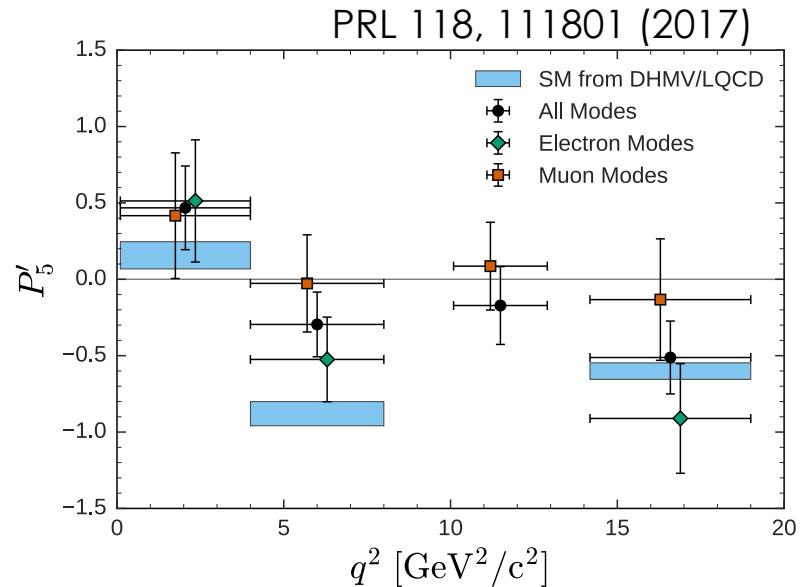
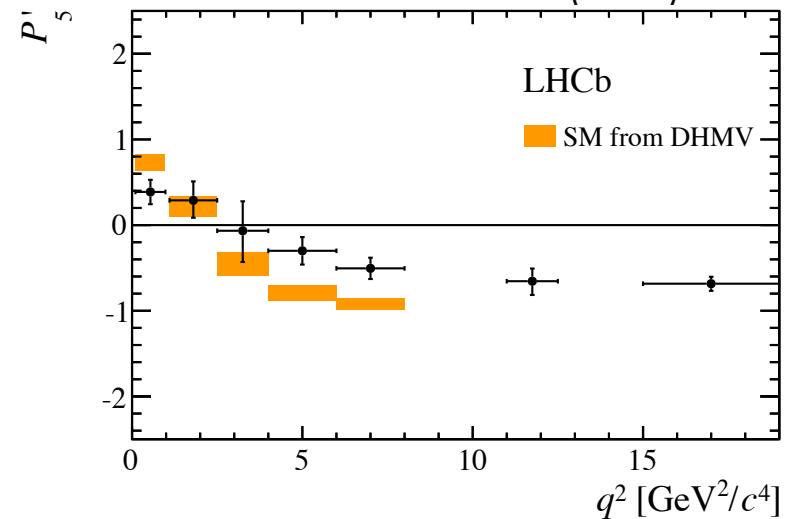
$$P'_5 = \frac{S_5}{\sqrt{F_L(1 - F_L)}}$$



# $B \rightarrow K^* \mu^+ \mu^-$ angular analysis

JHEP02 (2016) 104

- LHCb:  $3 \text{ fb}^{-1}$  run I data set
  - Full angular analysis  $B \rightarrow K^* \mu^+ \mu^-$
  - Local SM deviation  $P_5'$ 
    - $2.8\sigma$  in  $4 < q^2 < 6 \text{ GeV}^2/c^4$
    - $3.0\sigma$  in  $6 < q^2 < 8 \text{ GeV}^2/c^4$
  - Fit to  $C_9$ ,  $3.4\sigma$  from SM
- Belle:  $711 \text{ fb}^{-1}$  full data set
  - Both  $e^\pm$  and  $\mu^\pm$  modes
  - Local SM deviation  $P_5'$ 
    - $2.6\sigma$  in  $4 < q^2 < 8 \text{ GeV}^2/c^4$  in the muon mode
    - $e^\pm$  mode consistent with SM

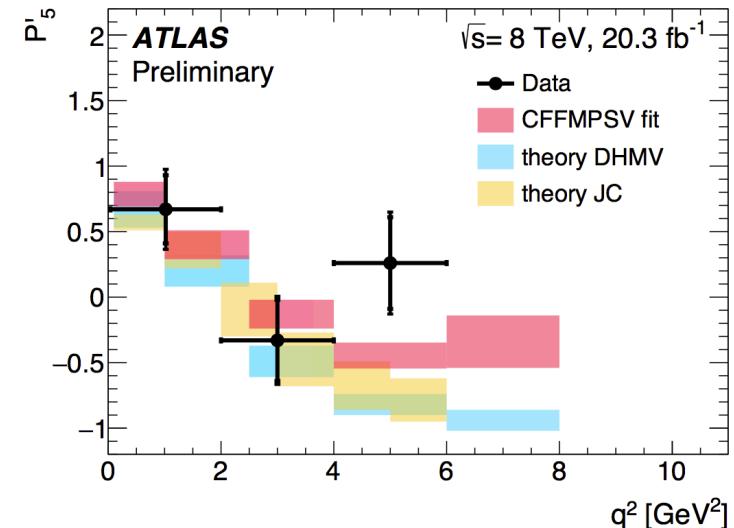




# $B \rightarrow K^* \mu^+ \mu^-$ angular analysis

- ATLAS:  $20.3 \text{ fb}^{-1}$  run I data

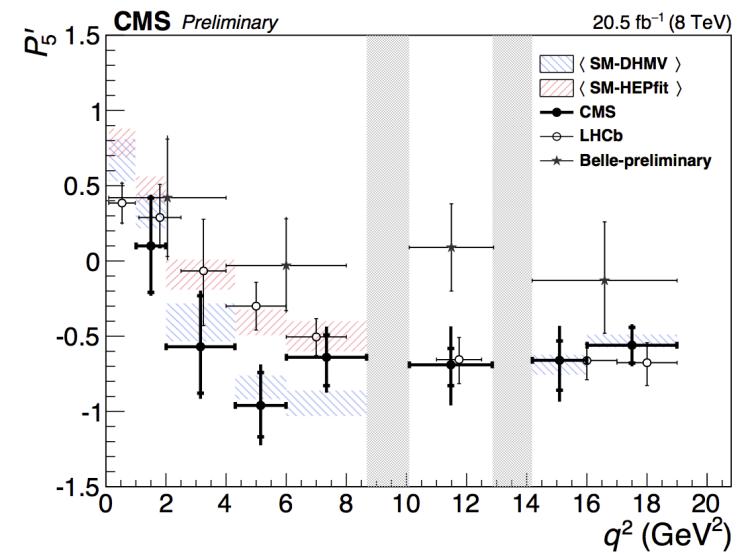
ATLAS-CONF-2017-023



- CMS:  $20.5 \text{ fb}^{-1}$  run 1 data

CMS PAS BPH-15-008

- Recent, preliminary result
- Compatible with SM
- Compatible with LHCb & Belle

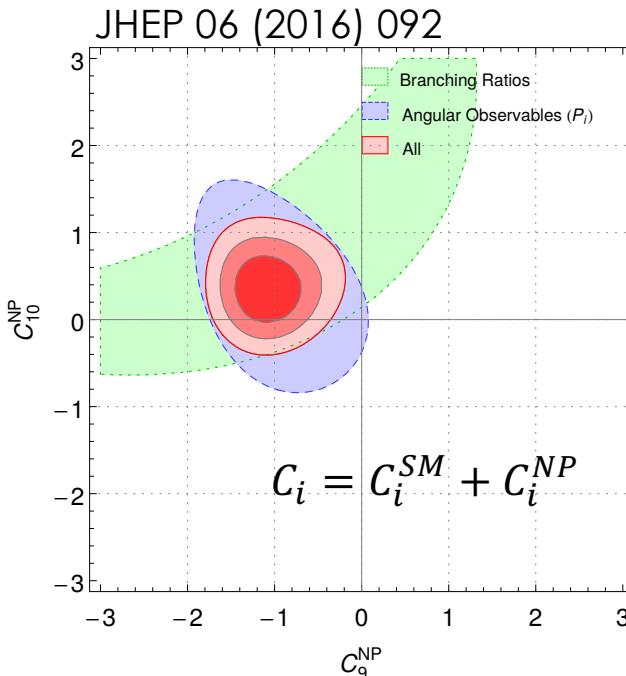
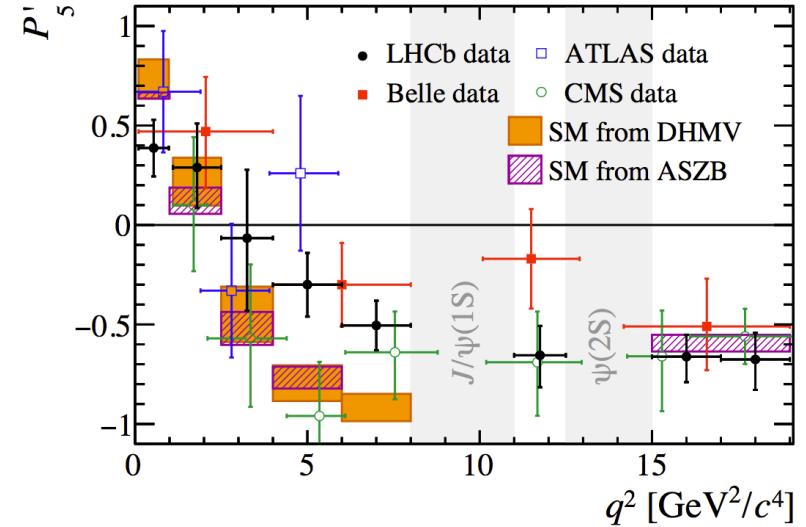




# Global fits to Wilson coefficients

- Is there a pattern in these deviations?
- Global fits of Wilson coefficients
  - Approximately 100 observables
    - $B_{(s)} \rightarrow \mu^+\mu^-$  and  $b \rightarrow s \gamma$  BR
    - $b \rightarrow s l^+ l^-$  BR & angular observables
  - Several global fits in literature
    - Fits prefer BSM contribution to  $C_9$
    - $3-5\sigma$  from SM depending on constraints
- Possible interpretations
  - BSM physics contributions
    - e.g.  $Z'$  of a few TeV
  - Limits in our understanding of QCD
    - E.g. contributions from charm loops

$B \rightarrow K^* \tau^+ \tau^-$  not yet observed  
Babar limit  $\text{BR} < 2.3 \times 10^{-3}$   
PRL 118, 031802 (2017)





# Lepton flavour universality

Ratios of branching ratios – comparing lepton flavour

$$\mathcal{R}_{K^{(*)}} \equiv \frac{\mathcal{B}(B \rightarrow K^{(*)}\mu^+\mu^-)}{\mathcal{B}(B \rightarrow K^{(*)}e^+e^-)} \quad \mathcal{R}_{D^*}^{\text{SM}} = \frac{\mathcal{B}(\bar{B} \rightarrow D^*\tau^-\bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^*e^-\bar{\nu}_e)}$$

See talk by **Anna Lupato**:

“Lepton flavour universality tests at LHCb”

Sunday 15:40 in ‘Test of symmetries and conservation laws’

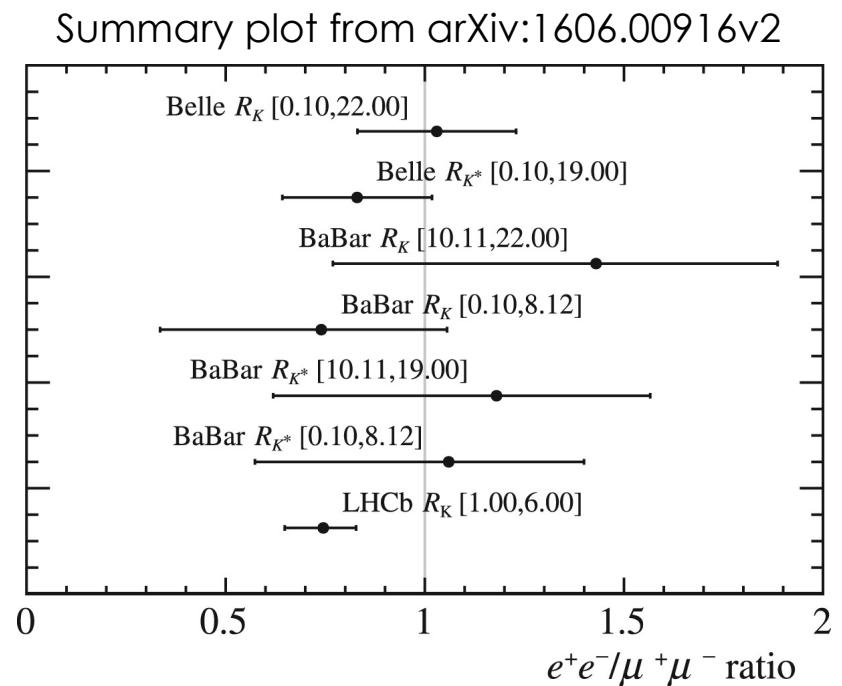


# LFU: $B \rightarrow K^{(*)} \mu^+ \mu^-$ vs. $B \rightarrow K^{(*)} e^+ e^-$

- Lepton flavour universality test
  - Close to unity in SM
- Measurements by Belle & Babar
  - Combines  $B^0$  &  $B^+$  ratios
  - $R(K)$  and  $R(K^*)$  for different  $q^2$  ranges
    - Consistent with SM prediction
- LHCb 3  $\text{fb}^{-1}$  run I:  $R_K$  PRL 113 (2014) 151601
  - Measured as a double ratio
$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ J/\psi (\rightarrow \mu^+ \mu^-))} / \frac{\mathcal{B}(B^+ \rightarrow K^+ J/\psi (\rightarrow e^+ e^-))}{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}$$

$$R_K = 0.745^{+0.090}_{-0.074} \text{ (stat)} \pm 0.036 \text{ (syst)}$$
  - $2.6\sigma$  deviation from SM

$$R_{K^{(*)}} = \frac{\mathcal{B}(B^{0/+} \rightarrow K^{0/+(*)} \mu^+ \mu^-)}{\mathcal{B}(B^{0/+} \rightarrow K^{0/+(*)} e^+ e^-)}$$



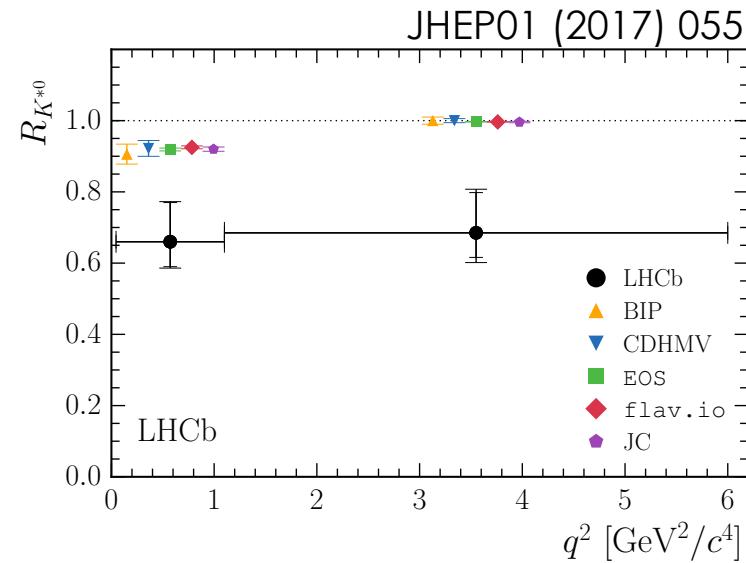
Babar: PRD 86 (2012) 032012  
 Belle: PRL 103 (2009) 171801



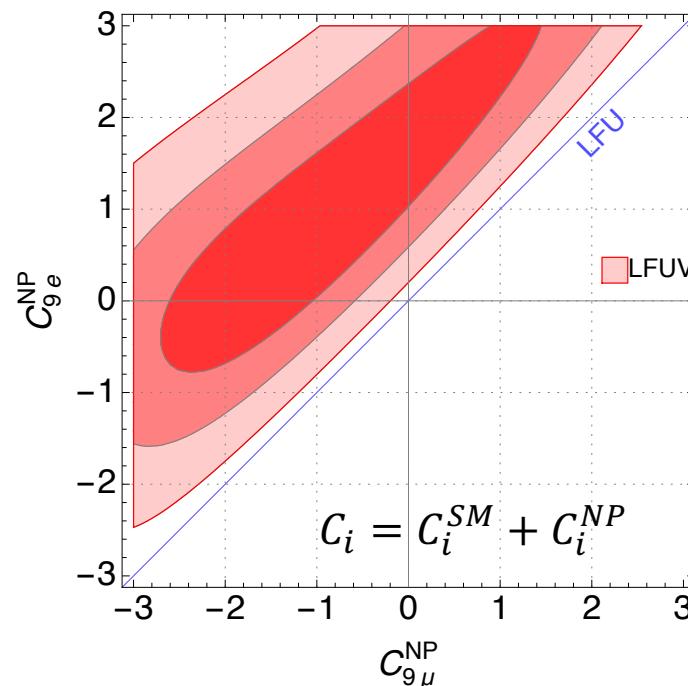
# LFU: $B \rightarrow K^{(*)} \mu^+ \mu^-$ vs. $B \rightarrow K^{(*)} e^+ e^-$

- LHCb:  $3 \text{ fb}^{-1}$  run I:  $R_{K^*}$ 
  - Tension with SM
    - $2.1\text{-}2.3\sigma$  in  $0.045 < q^2 < 1.1 \text{ GeV}^2/c^4$
    - $2.2\text{-}2.4\sigma$  in  $1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$

$$R_{K^*} = \frac{\mathcal{B}(B^0 \rightarrow K^{0*} \mu^+ \mu^-)}{\mathcal{B}(B^0 \rightarrow K^{0*} e^+ e^-)}$$



- Fit to Wilson coefficients
  - Allowing for  $C_{ie}^{NP} \neq C_{i\mu}^{NP}$ 
    - $3.5\sigma$  from SM
    - Preference for  $C_{9\mu}^{NP} \neq 0$

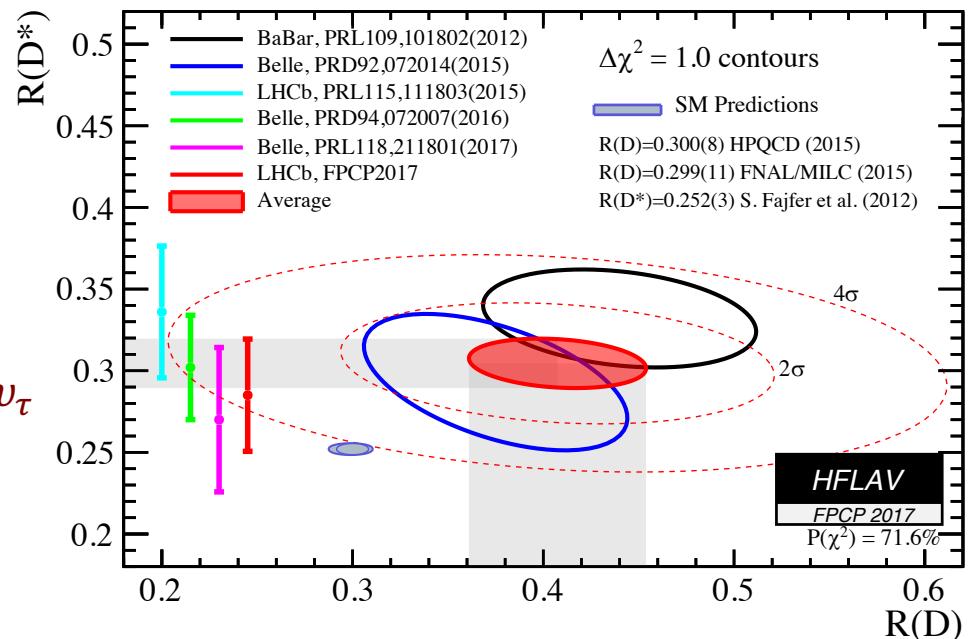




# LFU: $B \rightarrow D^{(*)} \tau^+ \nu$ vs. $B \rightarrow D^{(*)} l^+ \nu^-$ ( $l = e$ or $\mu$ )

- LFU ratios for semi-leptonic  $D^{(*)}$  decays
- $R_D$  measurements
  - Belle & Babar
    - Hadronic tag,  $\tau^- \rightarrow l^- \bar{\nu}_l \nu_\tau$
- $R_{D^*}$  measurements
  - Belle & Babar
    - Hadronic tag,  $\tau^- \rightarrow l^- \bar{\nu}_l \nu_\tau$
  - Belle
    - Hadronic tag,  $\tau^- \rightarrow \pi^- \nu_\tau, \tau^- \rightarrow \rho^- \nu_\tau$
    - Semi-leptonic tag,  $\tau^- \rightarrow l^- \bar{\nu}_l \nu_\tau$
  - LHCb 3 fb<sup>-1</sup> (run I)
    - $\tau^- \rightarrow l^- \bar{\nu}_l \nu_\tau$
    - $\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu_\tau$

$$R_{D^{(*)}} = \frac{\mathcal{B}(B^{0/-} \rightarrow D^{0/-(*)} \tau^+ \nu_\tau)}{\mathcal{B}(B^{0/-} \rightarrow D^{0/-(*)} l^+ \nu_l)}$$



Tension with SM prediction

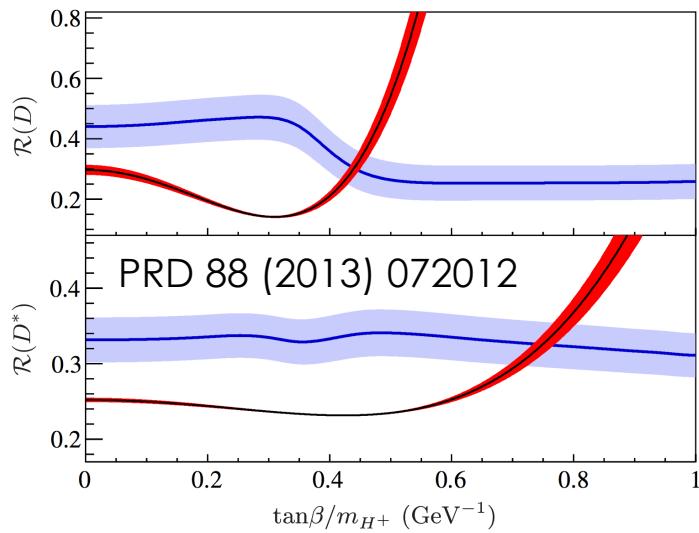
- $2.3\sigma$  in  $R_D$
- $3.4\sigma$  in  $R_{D^*}$
- $4.1\sigma$  combined



# Interpretations of the $R_{D^{(*)}}$ results

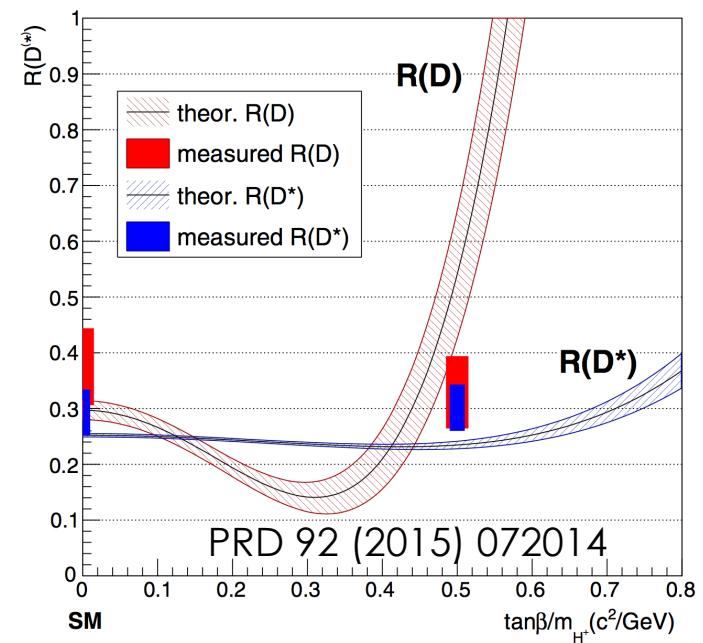
- Example of BSM model that would influence  $R_{D^{(*)}}$ 
  - 2-Higgs-dublet model Type II
    - Parametrised by  $\tan(\beta)/m_{H^+}$
  - Affects both measured and predicted  $R_{D^{(*)}}$

Comparison with Babar hadronic result



Not consistent with 2HDM type II

Comparison with Belle hadronic result



Consistent with 2HDM type II  
with  $\tan(\beta)/m_{H^+} \sim 0.45$



---

# Outlook

Many exciting results in the years to come

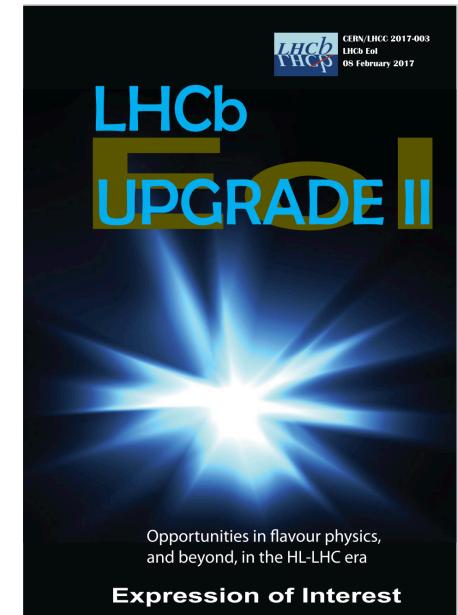


# LHCb datasets

- LHCb results almost exclusively from  $3 \text{ fb}^{-1}$  Run I data
  - Run II doubles signal yield/ $\text{fb}^{-1}$ 
    - Increased  $b\bar{b}$  cross section

CERN-LHCC-2017-003				
	LHC Run	Period of data taking	Maximum $\mathcal{L}$ [ $\text{cm}^{-2}\text{s}^{-1}$ ]	Cumulative $\int \mathcal{L} dt$ [ $\text{fb}^{-1}$ ]
Current detector	1 & 2	2010–2012, 2015–2018	$4 \times 10^{32}$	8
Phase-I Upgrade	3 & 4	2021–2023, 2026–2029	$2 \times 10^{33}$	50
Phase-II Upgrade	5 →	2031–2033, 2035 →	$2 \times 10^{34}$	300

- LHCb Phase-I upgrade
  - Remove H/W trigger – 40 Mhz readout
    - Doubles signal yield/ $\text{fb}^{-1}$  for hadronic channels
    - Construction progressing at full speed
- LHCb Phase-II upgrade
  - Preliminary studies ongoing
    - Major detector upgrade
    - EoI submitted

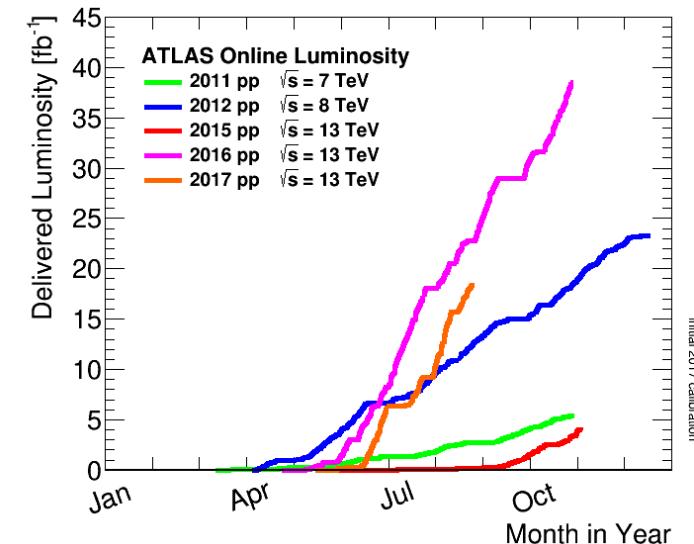
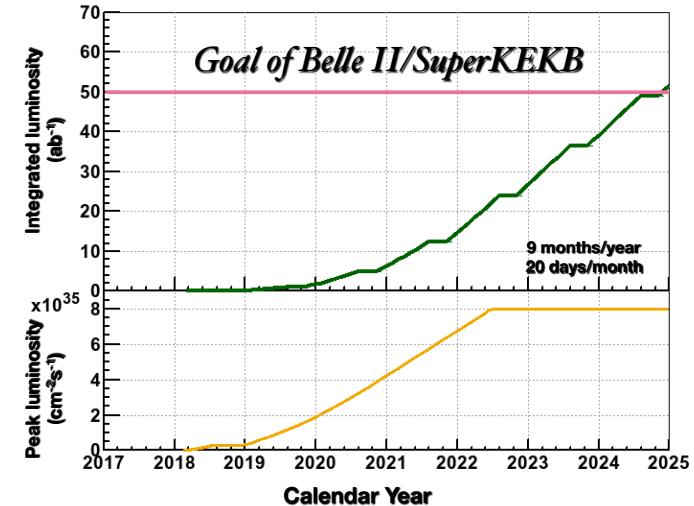




# Belle II, ATLAS & CMS

- Babar & Belle datasets
  - $550 + 1000 \text{ fb}^{-1}$
- Belle II:  $50 \text{ ab}^{-1}$ 
  - Physics data taking from 2018
    - See previous speaker (Mikihiko Nakao)
  - Dedicated talk by Jake Bennet
    - Sunday, 14:50 (accelerators & detectors)
- ATLAS & CMS: results from  $20-25 \text{ fb}^{-1}$ 
  - $\sim 80 \text{ fb}^{-1}$  on tape
    - Expect  $\sim 300 \text{ fb}^{-1}$  by 2023
  - $3 \text{ ab}^{-1}$  for sLHC upgrade era
  - Many important results are expected

## SuperKEKB luminosity projection





# Physics prospects

arXiv:1002.5012 and  
EPS-HEP 2017 talk by S. Falke

- Belle II:  $R_D$  &  $R_{D^*}$

$$\sigma_{BelleII} = \sqrt{(\sigma_{stat}^2 + \sigma_{sys}^2) \frac{\mathcal{L}_{Belle}}{50 \text{ ab}^{-1}} + \sigma_{irred}^2}$$

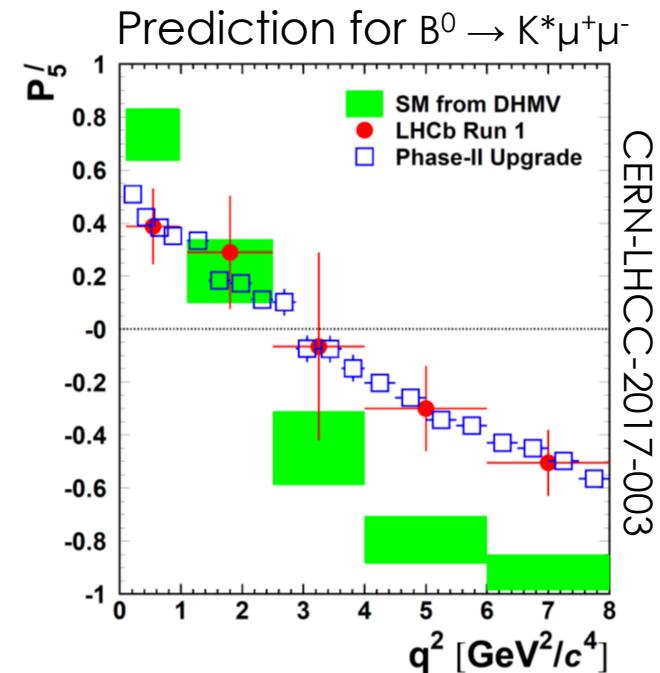
	Current precision	Belle II 5 ab <sup>-1</sup>	Belle II 50 ab <sup>-1</sup>
$R_D$	12%	5.6%	3.2%
$R_{D^*}$	5.4%	3.9%	2.2%
$R_K$	12%	7%	2%

- LHCb Phase I & II

CERN-LHCC-2017-003  
CERN-LHCC-2012-007

$B_{(s)} \rightarrow \mu^+ \mu^-$	Current precision	Phase-I 50 fb <sup>-1</sup>	Phase-II 300 fb <sup>-1</sup>
$\sigma_{BR} \times 10^{-9}$	0.7	0.15	0.07
Effective lifetime $\sigma_T$	25%	5%	2%

ATLAS & CMS are competitive in  $B_{(s)} \rightarrow \mu^+ \mu^-$





# Summary

---

- Rare B-decays are an excellent probe for BSM physics
- $B_{(s)} \rightarrow \mu^+ \mu^-$  branching ratios consistent with SM
  - Within experimental precision
- Intriguing deviations from SM predictions
  - $b \rightarrow s l^+ l^-$  branching ratios & angular observables
  - Lepton flavour universality test:  $R_{K^{(*)}}$  and  $R_{D^{(*)}}$
- Exciting results expected from
  - Data already recorded
  - Upgraded detectors



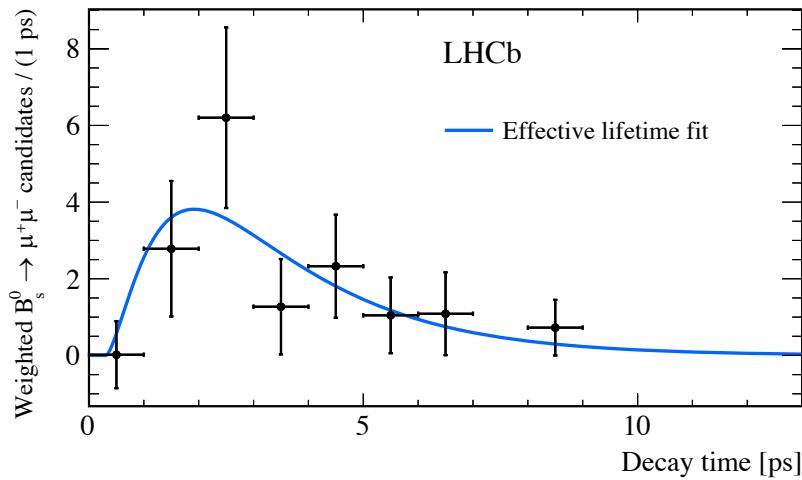
---

# Backup slides



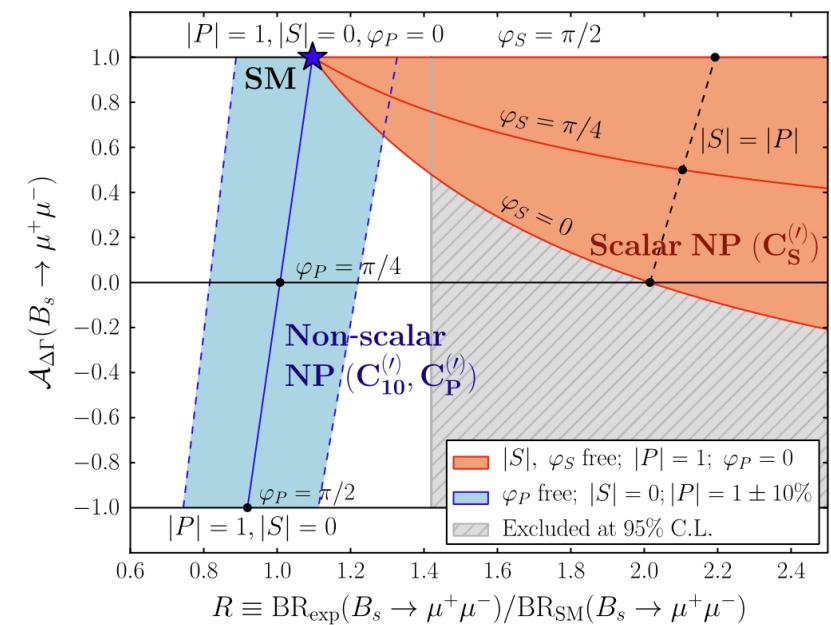
# $B_s \rightarrow \mu^+ \mu^-$ effective lifetime

- LHCb update:  $3 \text{ fb}^{-1}$  (run I) +  $1.4 \text{ fb}^{-1}$  (run 2)
- New observable sensitive to CP violation
  - $A_{\Delta\Gamma} = 1$  in SM (i.e. no CPV)  $\tau_{eff} = \tau_{B_H} = 1.619 \pm 0.009$



$$\tau(B_s^0 \rightarrow \mu^+ \mu^-) = 2.04 \pm 0.44 \pm 0.05 \text{ ps}$$

Measurement for the sLHC era



De Bruyn et al., PRL 109, 041801 (2012)

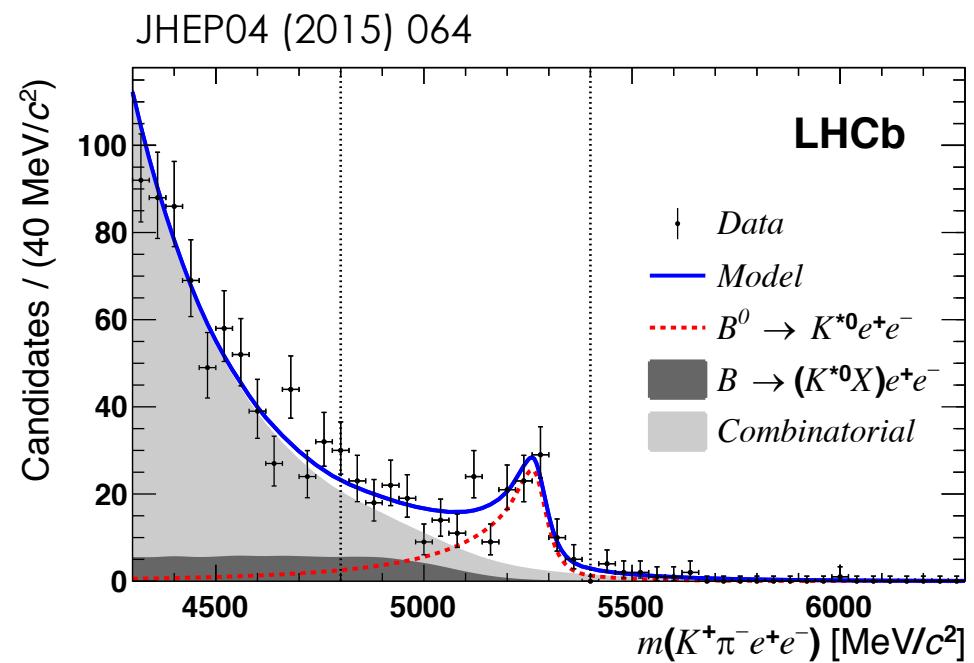


# $B^0 \rightarrow K^* e^+ e^-$ angular analysis

- LHCb: 3 fb<sup>-1</sup> run I
  - Particular interest in the low  $q^2$  region
    - Sensitivity to photon polarisation
    - Wilson coefficients  $C_7$  &  $C_7'$
  - Folded angular distributions
    - Increase sensitivity for low yields
    - 4 observables

$0.002 < q^2 < 1.12 \text{ GeV}^2/c^4$

$$\begin{aligned} F_L &= 0.16 \pm 0.06 \pm 0.03 \\ A_T^{(2)} &= -0.23 \pm 0.23 \pm 0.05 \\ A_T^{\text{Im}} &= +0.14 \pm 0.22 \pm 0.05 \\ A_T^{\text{Re}} &= +0.10 \pm 0.18 \pm 0.05 \end{aligned}$$





# Belle: $\tau$ polarisation in $B \rightarrow D^* \tau^+ \nu$

- Belle full dataset
  - Complementary observable
  - Hadronic tag,  $\tau^- \rightarrow \pi^- \nu_\tau$ ,  $\tau^- \rightarrow \rho^- \nu_\tau$

- Polarisation of  $\tau^-$

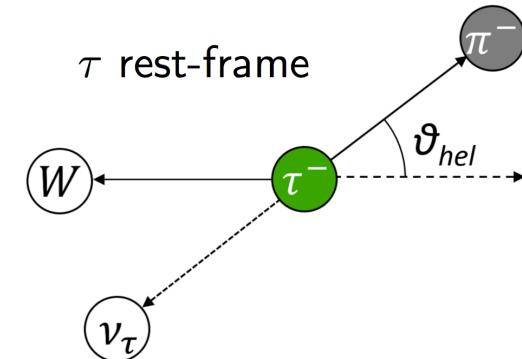
$$P_\tau(D^*) = \frac{\Gamma^+(D^*) - \Gamma^-(D^*)}{\Gamma^+(D^*) + \Gamma^-(D^*)}$$

- $\Gamma^\pm(D^*)$ : decay rate with  $\tau$  helicity  $\pm \frac{1}{2}$
- Differential BR

$$\frac{d\Gamma(D^*)}{d \cos \vartheta_{hel}} = \frac{\Gamma(D^*)}{2} [1 + \alpha P_\tau(D^*) \cos \vartheta_{hel}]$$

$$\tau \rightarrow \pi \nu_\tau \ (\alpha = 1)$$

$$\tau \rightarrow \rho \nu_\tau \ (\alpha = 0.45)$$



Result:

$$P_\tau^{SM} = -0.497 \pm 0.013$$

$$P_\tau = -0.38 \pm 0.51^{+0.21}_{-0.16}$$

Compatible with SM