

An aerial photograph of a rural landscape with green fields and some buildings. A white crosshair is centered on the image. A red triangle is drawn with its base on the horizontal line of the crosshair and its top vertex pointing upwards. The letters 'CKM' are written in large, bold, yellow font in the upper right quadrant.

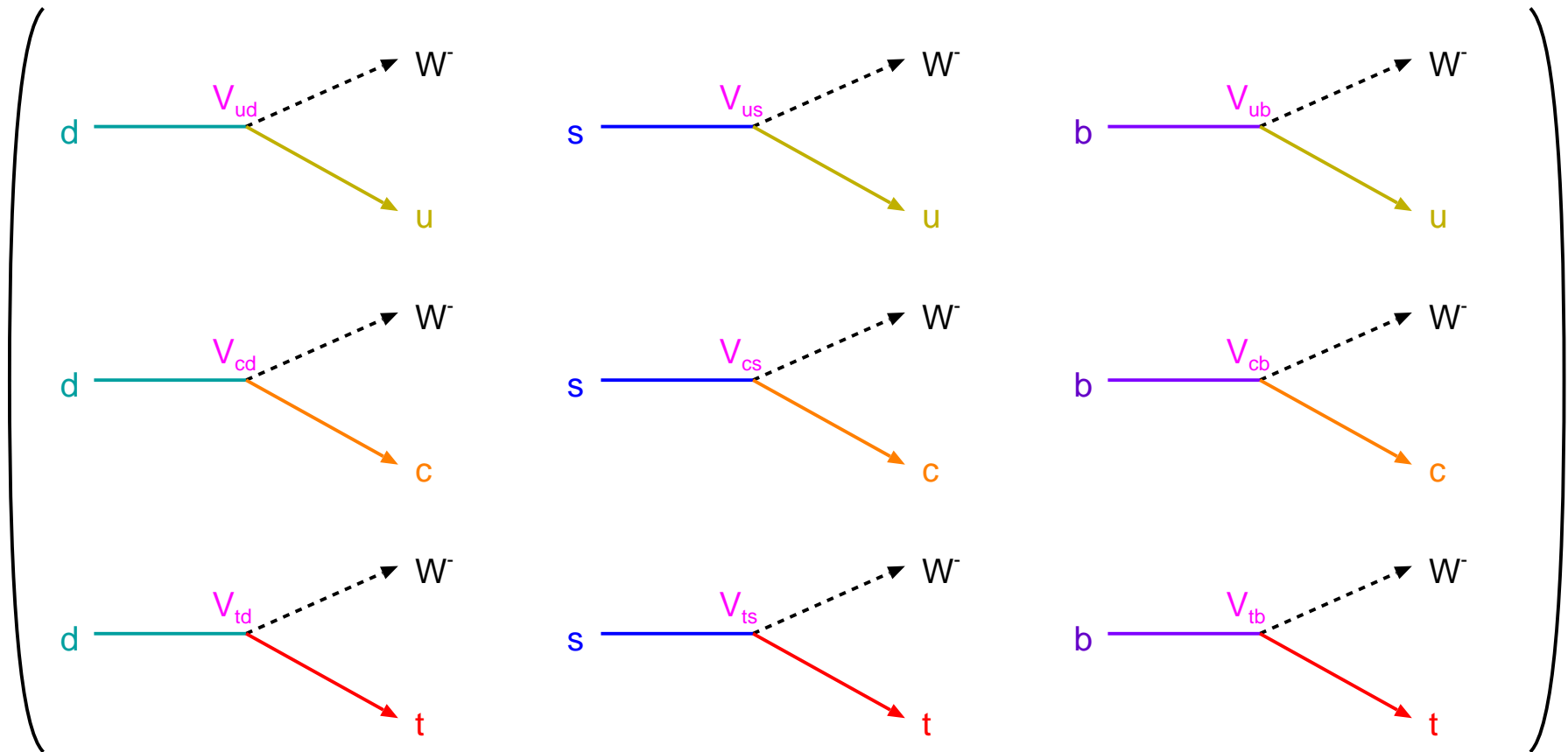
CKM

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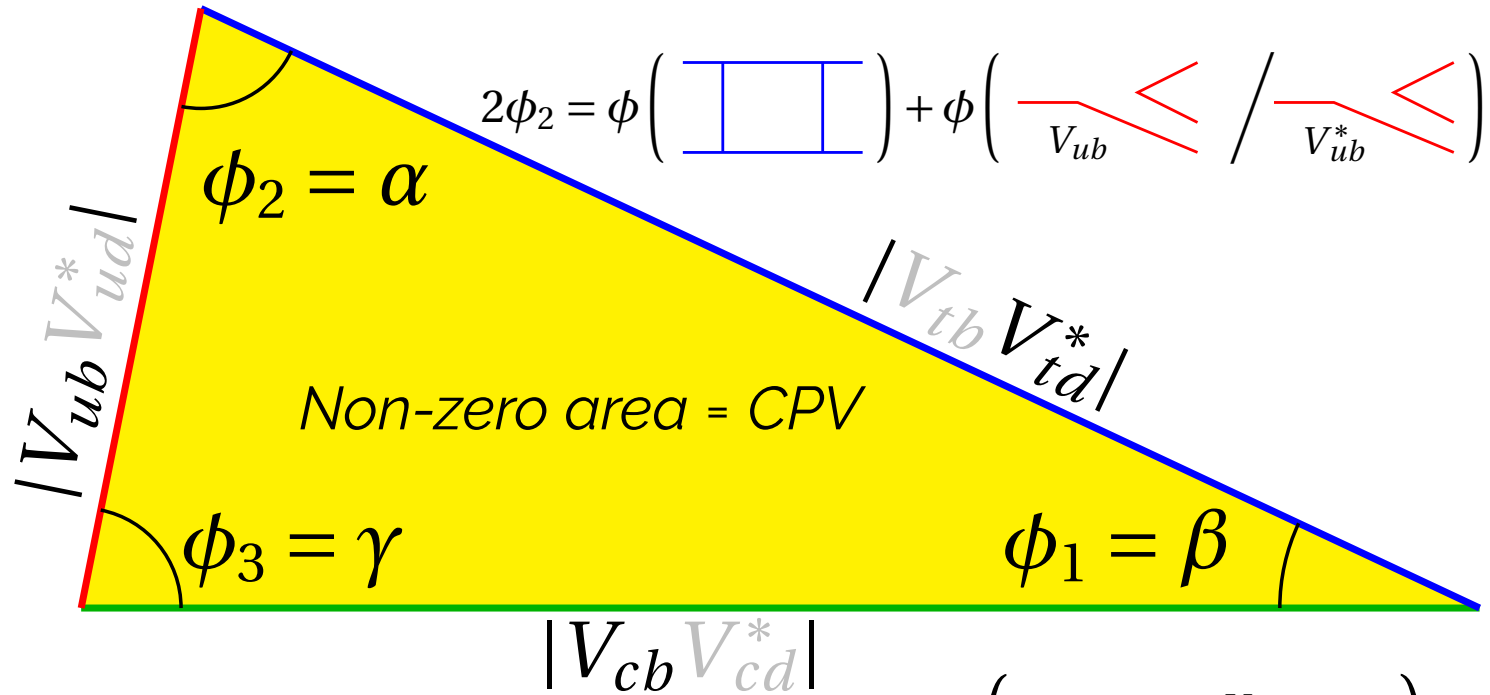
21st International Conference on Particles and Nuclei
1–5 September, 2017, Beijing

$V_{\text{Cabibbo-Kobayashi-Maskawa}} =$



Simple 3×3 complex matrix of tree-level quark transitions, loop and box diagrams give a rich structure, including CPV

Unitarity Triangle



$$2\phi_2 = \phi \left(\begin{array}{c} \text{---} \\ | \\ \text{---} \\ | \\ \text{---} \end{array} \right) + \phi \left(\frac{\text{---} \text{---} \text{---}}{V_{ub}} \text{---} / \frac{\text{---} \text{---} \text{---}}{V_{ub}^*} \text{---} \right)$$

$$\phi_3 = \phi \left(\text{---} \text{---} \text{---} \right)$$

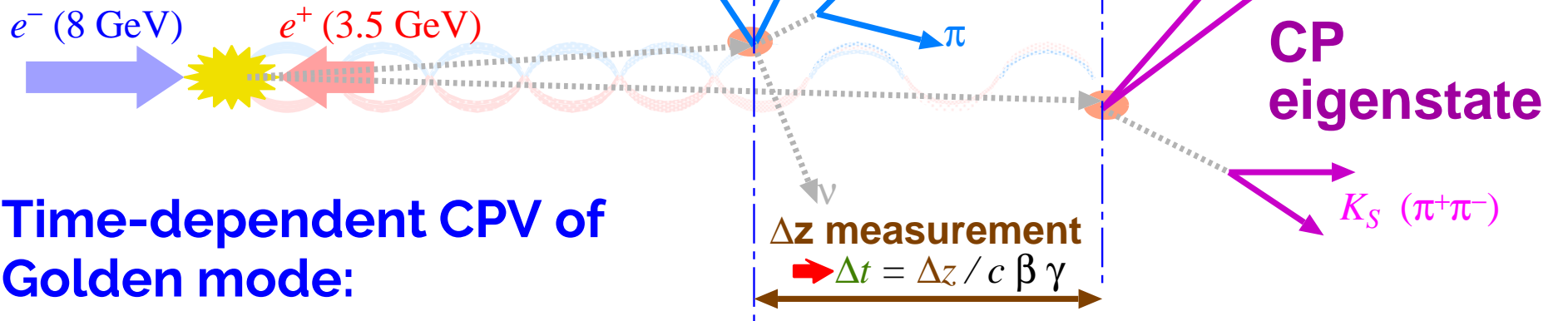
$$2\phi_1 = \phi \left(\begin{array}{c} \text{---} \\ | \\ \text{---} \\ | \\ \text{---} \end{array} \right)$$

$$|V_{ub}|^2 \propto \left| \text{---} \text{---} \text{---} \right|^2 \text{ or } \left| \text{---} \text{---} \text{---} \right|^2 \quad |V_{cb}|^2 \propto \left| \text{---} \text{---} \text{---} \right|^2$$

+ Hadronic uncertainties...

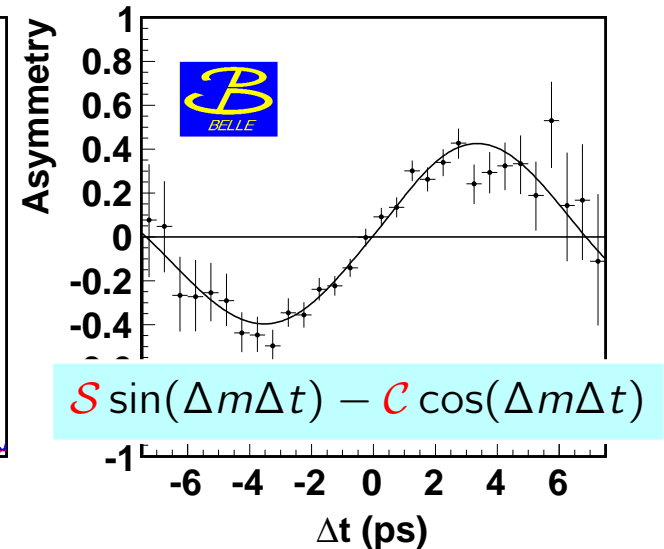
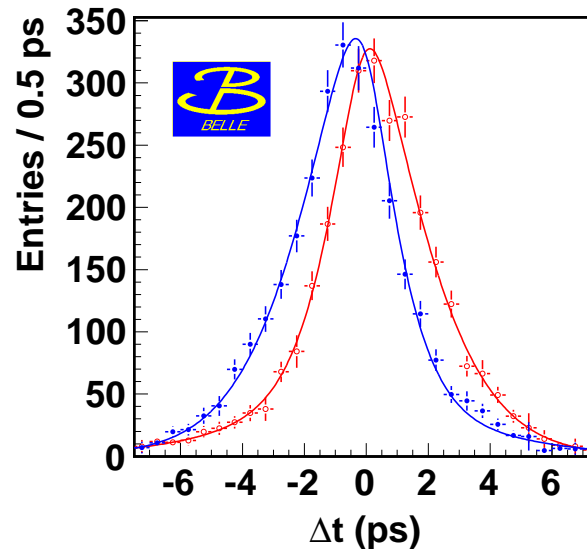
B-factory


asymmetric energy




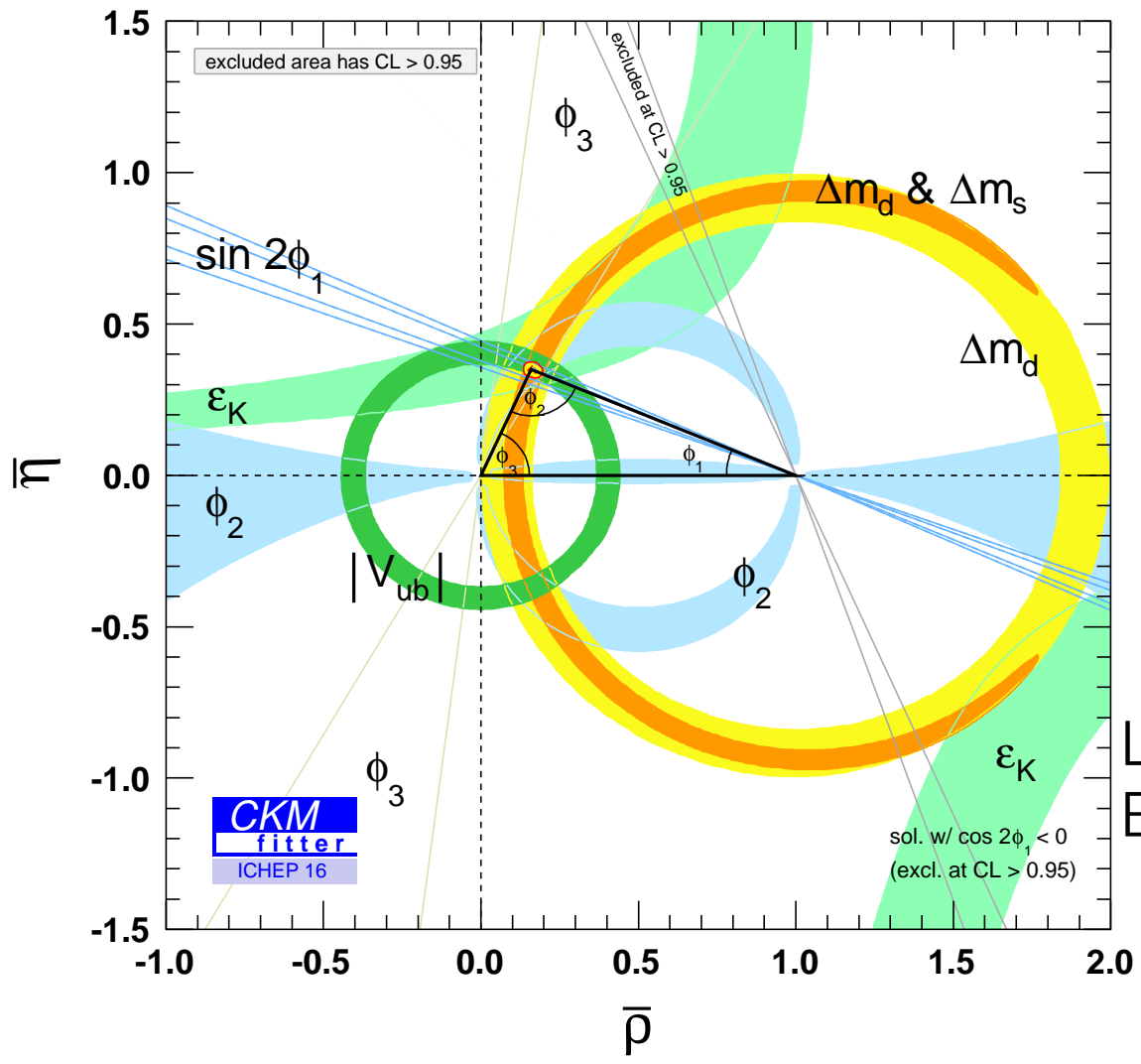
Time-dependent CPV of Golden mode:

- ✓ $B^0 \rightarrow J/\psi K_S$
- ✓ flavor tag
 $\epsilon_{\text{effective}} \sim 30\%$
- ✓ $\sigma(\Delta z) \sim 100 \mu\text{m}$
 $\Leftrightarrow \langle \Delta z \rangle \sim 200 \mu\text{m}$



$S_{C\bar{C}S} = \sin 2\phi_1 = +0.667 \pm 0.023 \pm 0.013$ PRL 108, 171802 (2012) 

$S_{C\bar{C}S} = \sin 2\beta = +0.687 \pm 0.028 \pm 0.012$ PRD 79, 072009 (2009) 

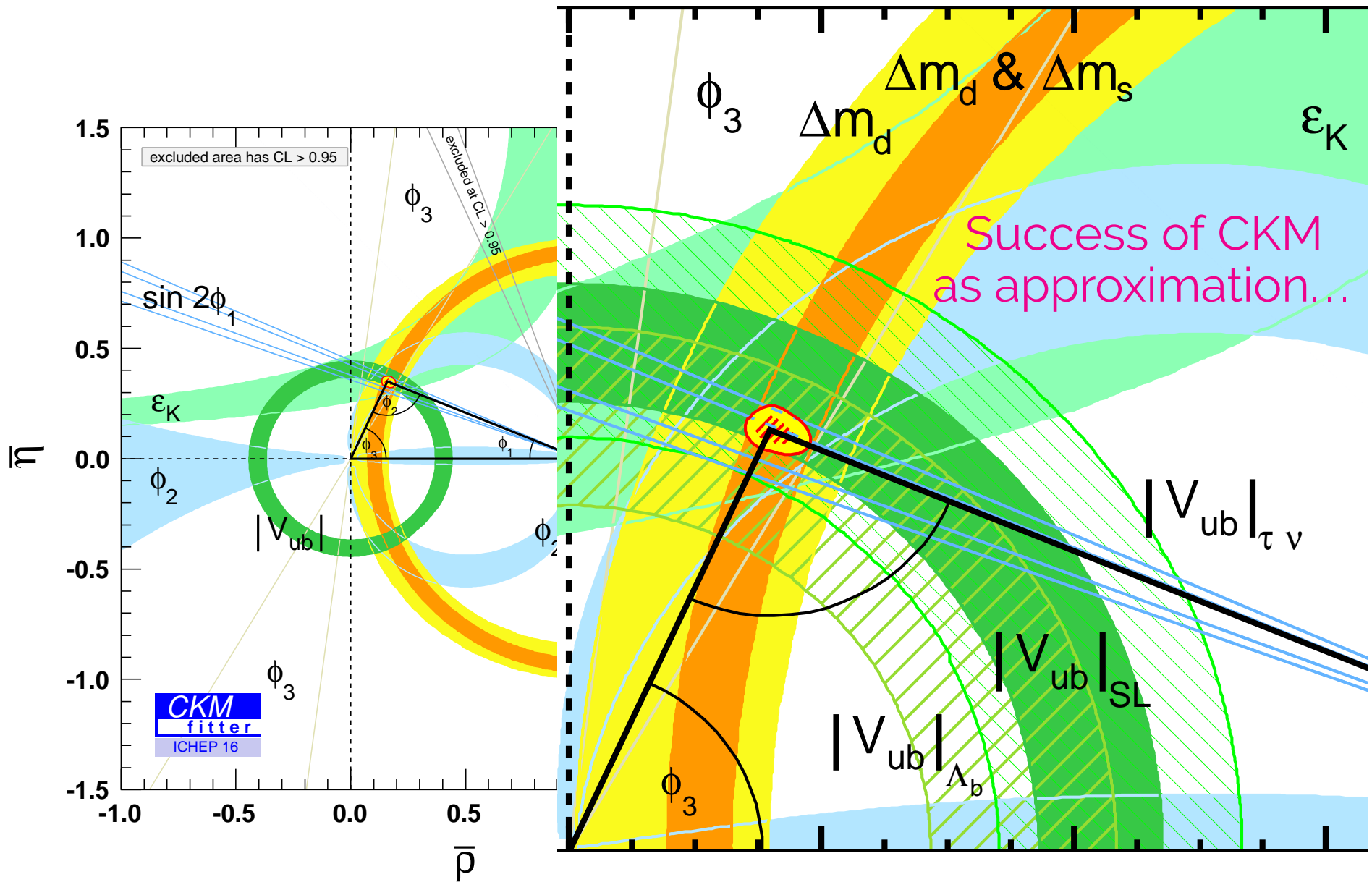


- All sides and angles
- Trees and loops
- Overconstraints

Success of CKM

Legacy of first generation B-factories (+LHCb)

2008 Nobel Prize to Kobayashi and Maskawa



- ⚠ Problems in $|V_{ub}|$, most likely in measurements + SM theory
- ⚠ **No constraint for O(10%) new physics contributions!**

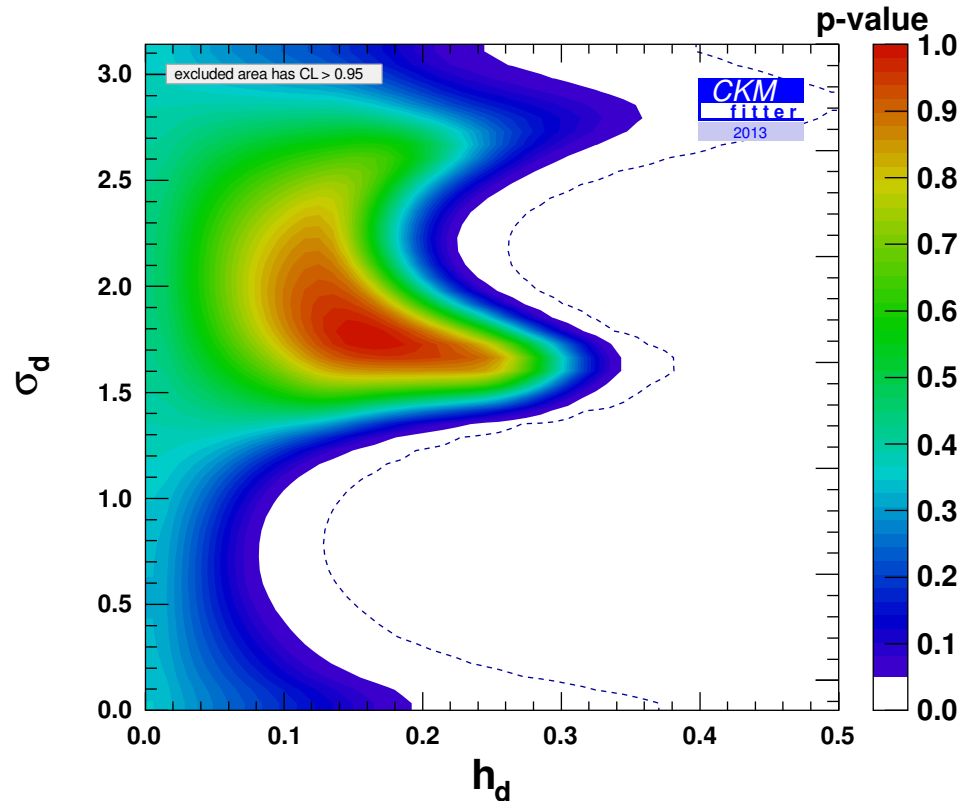


Quark transitions in NP modify the Unitarity Triangle



Deviation of **loop** (ϕ_1 and V_{td}) from **tree** (ϕ_3 and V_{ub}) as a clear sign of NP, parametrized in a model independent way

$$M_{12} = M_{12}^{\text{SM}} (1 + h_d e^{2i\sigma_d})$$



✓ **Scale of new physics**

$$h_d \simeq \frac{|C_d^{\text{NP}}|^2}{|V_{tb}^* V_{td}|^2} \left(\frac{4.5 \text{ TeV}}{\Lambda_{\text{NP}}} \right)^2$$



If NP coupling is similar to CKM (=MFV), Λ_{NP} is already larger than 8 TeV

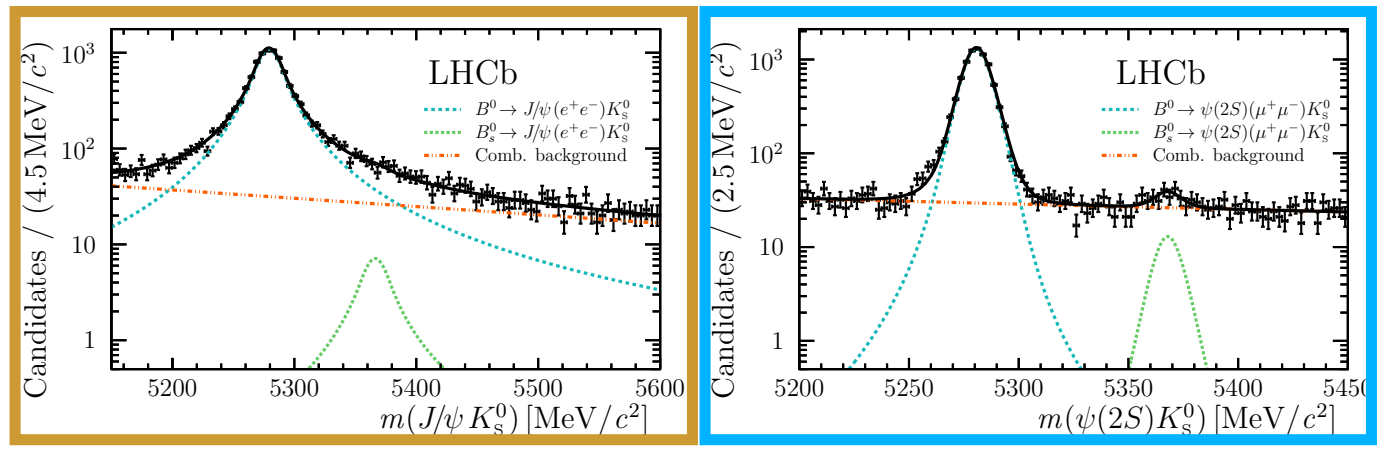
Recent progress — outline of this talk

- ϕ_1/β — addition of $\psi(2S)$ and electron modes (LHCb)
— from time-dependent Dalitz analysis (Belle)
- ϕ_2 — new results on $B^0 \rightarrow \pi^0\pi^0$ (Belle)
- γ — new results (LHCb)
- V_{cb} — recent progress on form factor (Belle)
- V_{ub} — inclusive electron spectrum of $B \rightarrow X_u e \nu$ (BaBar)
— measurement of $B \rightarrow \mu\nu$ (Belle)

Disclaimer: some of the recent topics are not included: such as ϕ_s measurement (LHCb), $B \rightarrow \eta' l \nu$ (Belle), CPV in b -baryons (LHCb), CPV in $B \rightarrow KK\pi$ (Belle), ...

LHCb: $B \rightarrow (c\bar{c})K_S$

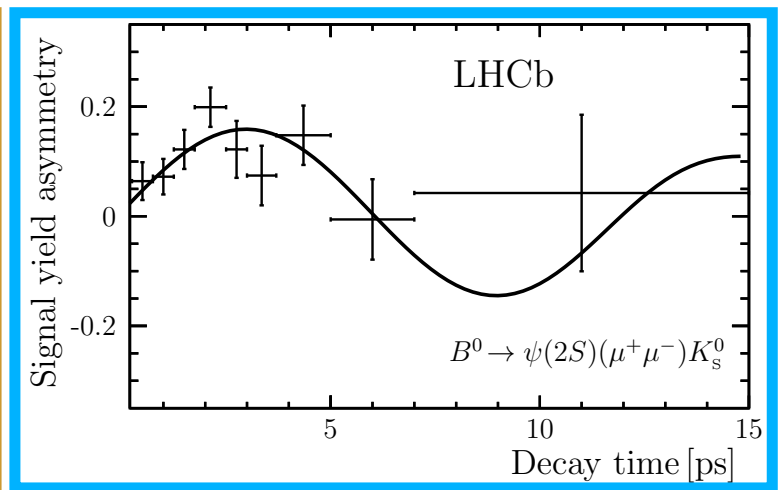
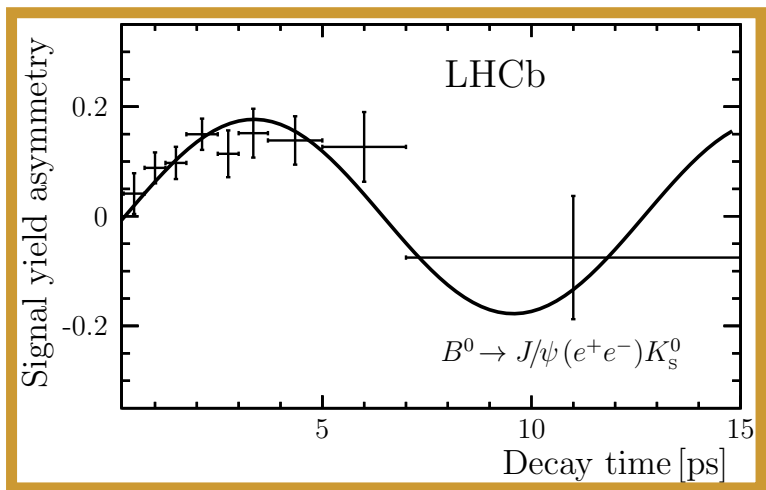
[G.Cowan LP'17, LHCb-PAPER-2017-029 in preparation]



preliminary

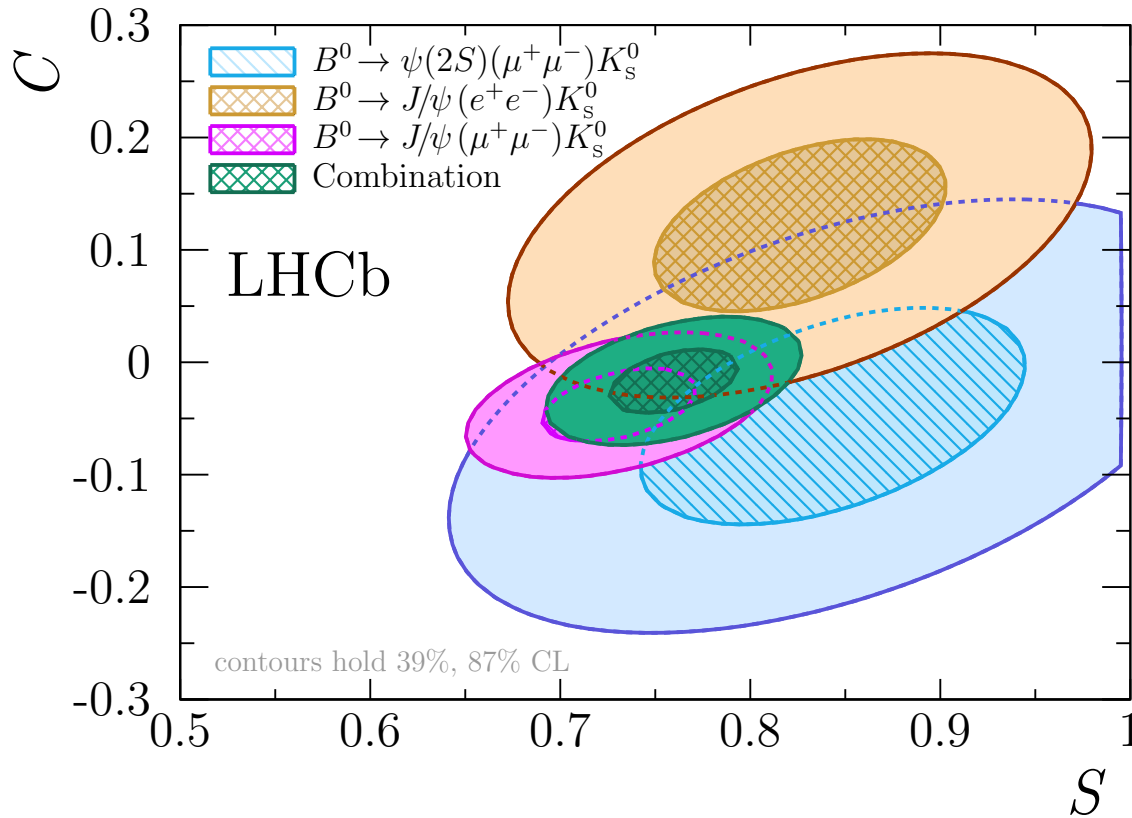
- Huge signal samples, penalty in small flavor tag efficiency
- **New:** $B \rightarrow J/\psi(\rightarrow e^+e^-)K_S$ and $B \rightarrow \psi(2S)(\rightarrow \mu^+\mu^-)K_S$
 [dominant mode: $B \rightarrow J/\psi(\rightarrow \mu^+\mu^-)K_S$, PRL115,031601(2015)]

time dependent fit: $A_{CP}(t) = \mathcal{S} \sin(\Delta mt) - \mathcal{C} \cos(\Delta mt)$, $\mathcal{S} = \sin 2\beta$



LHCb: $\sin 2\beta$

[G.Cowan LP'17, LHCb-PAPER-2017-029 in preparation]



preliminary

All combined:

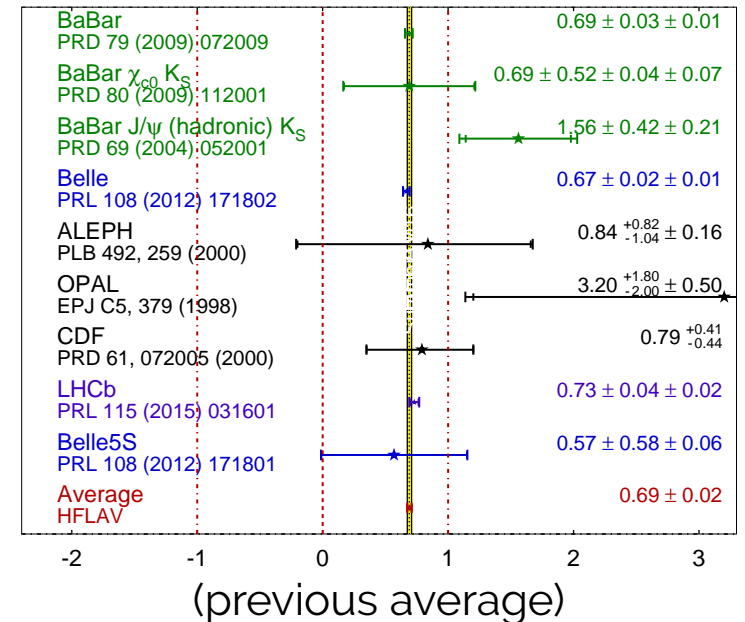
$$\mathcal{S} = +0.760 \pm 0.034$$

$$\mathcal{C} = -0.017 \pm 0.029$$

(Belle $\delta\mathcal{S} = 0.026$, BaBar $\delta\mathcal{S} = 0.030$)

- ✓ New modes help to reduce error
- ✓ Only a little behind the B-factories
- ✓ Contribution to the world average

$\sin(2\beta) \equiv \sin(2\phi_1)$ **HFLAV** Summer 2016



time-dependent Dalitz: $B \rightarrow D^{(*)} h^0$ ($h^0 = \pi^0, \eta, \eta', \omega$)

$$N_i(\Delta t, \phi_1) = h_2 e^{-\frac{|\Delta t|}{\tau_B}} \left[1 + Q_B \frac{K_i - K_{-i}}{K_i + K_{-i}} \cos(\Delta m_B \Delta t) + 2Q_B \xi_{h^0} (-1)^i \frac{\sqrt{K_i K_{-i}}}{K_i + K_{-i}} \sin(\Delta m_B \Delta t) (S_i \cos 2\phi_1 + C_i \sin 2\phi_1) \right]$$

Integrated |amplitude|²

$$K_i = \int |\mathcal{A}_D(m_-^2, m_+^2)|^2 d\mathcal{D}$$

from $B^- \rightarrow D^0 \pi^-$ (flavor specific)

Integrated strong phase

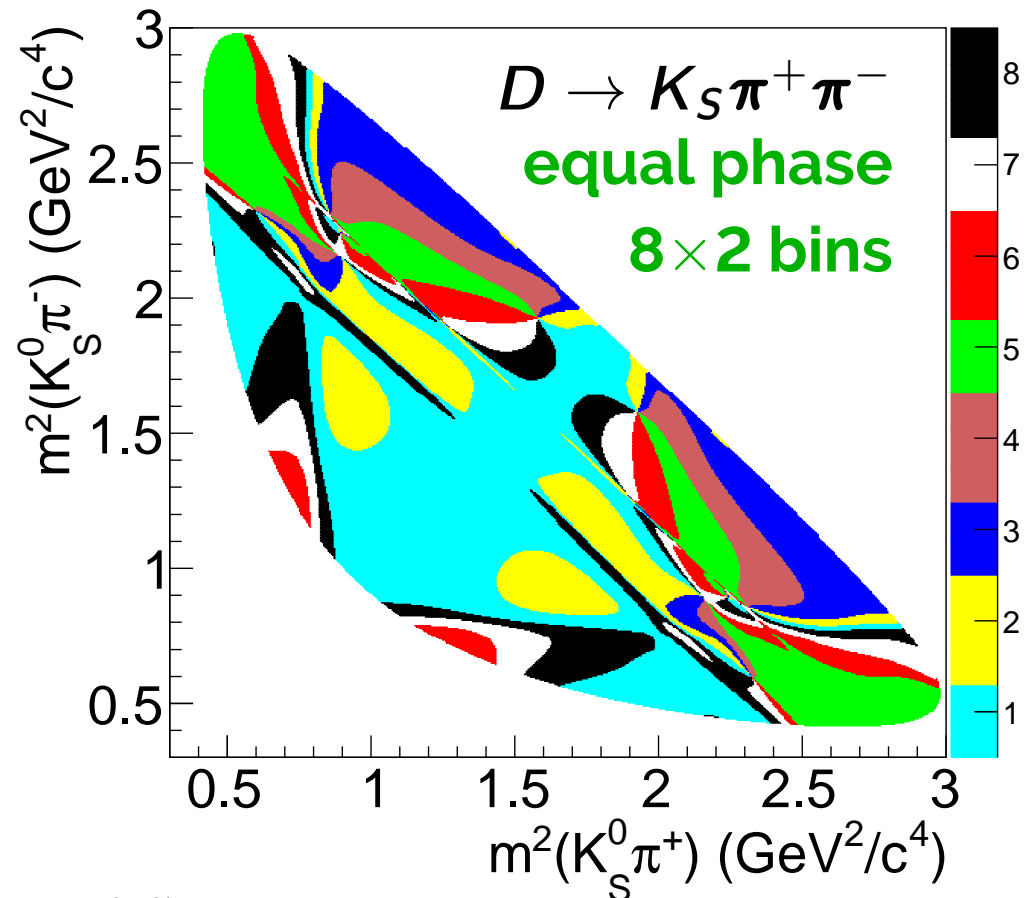
$$S_i = \frac{\int |\mathcal{A}_D| |\bar{\mathcal{A}}_D| \sin \Delta\delta_D d\mathcal{D}}{\sqrt{K_i K_{-i}}}$$

$$C_i = \frac{\int |\mathcal{A}_D| |\bar{\mathcal{A}}_D| \cos \Delta\delta_D d\mathcal{D}}{\sqrt{K_i K_{-i}}}$$

from coherent $D^0 \bar{D}^0$ by CLEO

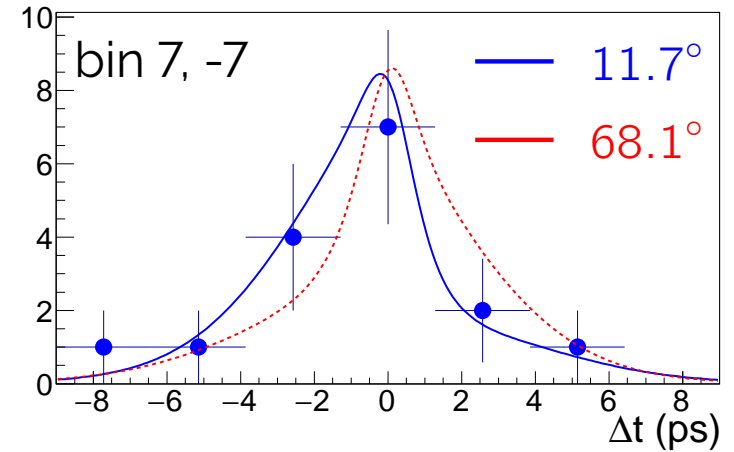
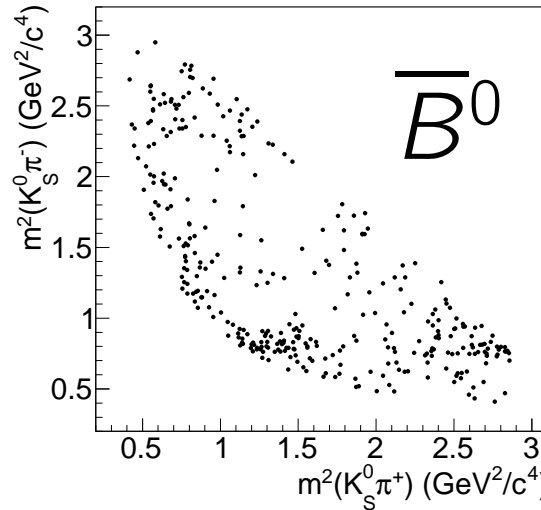
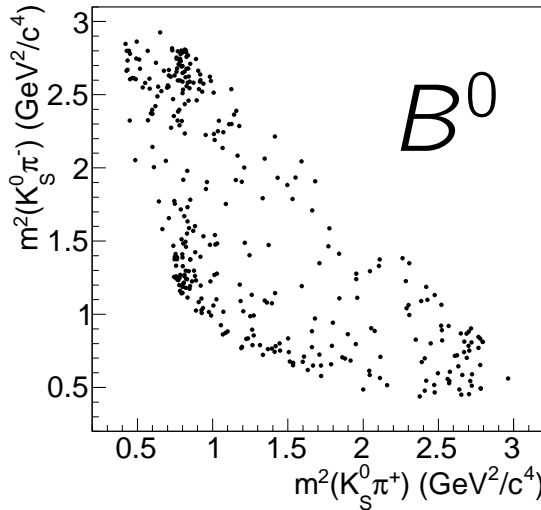
Measured in 8×2 bins

(binning based on a realistic resonant model)



Belle: ϕ_1 from Dalitz

[Belle PRD94,052004(2016)]



time-dependent Dalitz
fit of $B \rightarrow D^{(*)} h^0$

$$\phi_1 = 11.7^\circ \pm 7.8^\circ \pm 2.1^\circ$$

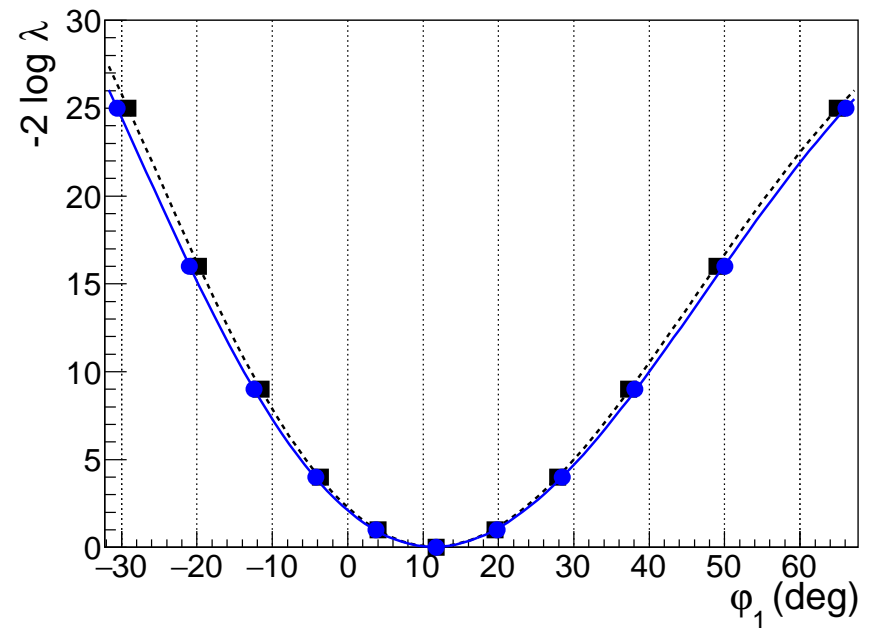
\Leftrightarrow two solutions
from $B \rightarrow [c\bar{c}]K^0$

$$\phi_1 = 21.9^\circ \text{ (1.3}\sigma \text{ away)}$$

$$\phi_1 = 68.1^\circ \text{ (5.1}\sigma \text{ away)}$$

second ϕ_1 solution

is definitely excluded (and no more needed in the CKMfitter UT plot)



ϕ_2/β : isospin analysis

- $\sin 2\phi_2$ from $B \rightarrow \pi^+\pi^-$ need to resolve “penguin pollution”
- $\mathcal{S} = \sqrt{1 - \mathcal{A}^2} \sin 2(\phi_2 + \Delta\phi_2)$,
where $\Delta\phi_2$ from 3 branching fractions and 2 direct CPV

$$A_{+-}: B^0 \rightarrow h^+ h^-$$

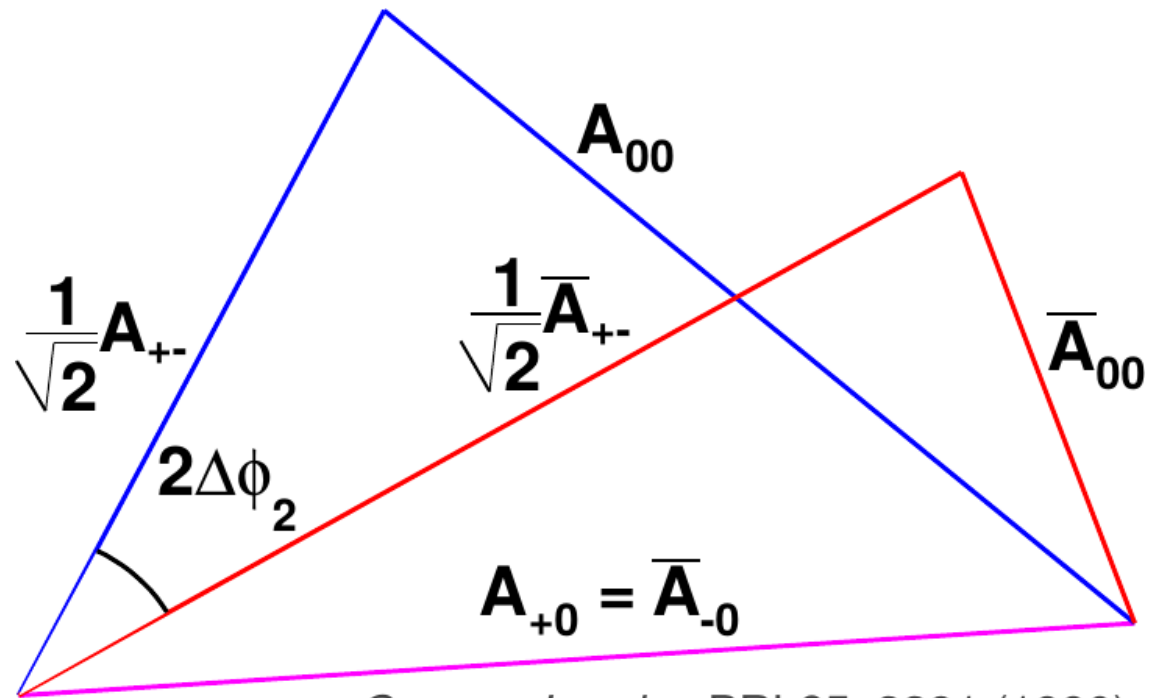
$$\bar{A}_{+-}: \bar{B}^0 \rightarrow h^+ h^-$$

$$A_{00}: B^0 \rightarrow h^0 h^0$$

$$\bar{A}_{00}: \bar{B}^0 \rightarrow h^0 h^0$$

$$A_{+0}: B^+ \rightarrow h^+ h^0$$

$$(h = \pi, \rho)$$

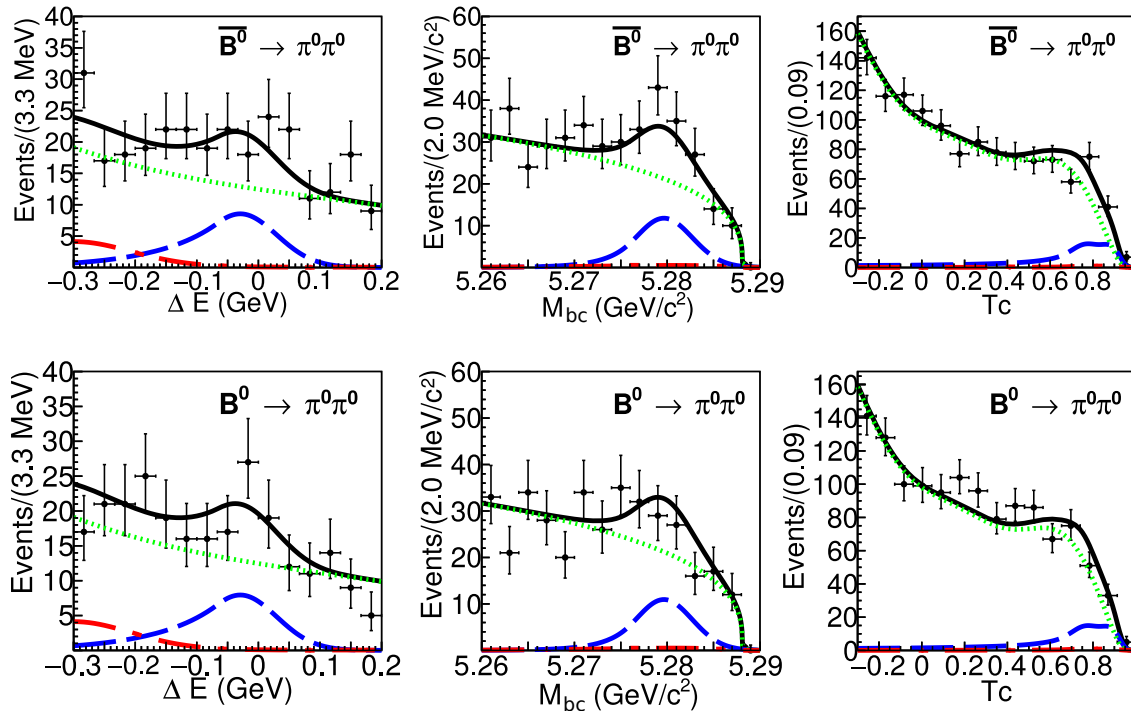


Gronau, London PRL65, 3381 (1990)

- $B \rightarrow \pi^+\pi^-$ and $B \rightarrow \pi^+\pi^0$ have been precisely measured, but it took long time for Belle to finalize $B \rightarrow \pi^0\pi^0$
[No charged track, need precise timing info for photon clusters]

Belle: $B \rightarrow \pi^0 \pi^0$ and ϕ_2

[arXiv:1705.02083 to appear in PRD]



(previous results)

$$\mathcal{B}(B \rightarrow \pi^0 \pi^0) (10^{-6})$$

PDG: 1.91 ± 0.22

BaBar(2013): 1.83 ± 0.25

Belle(2005): 2.3 ± 0.5

SM: < 1.0 ???

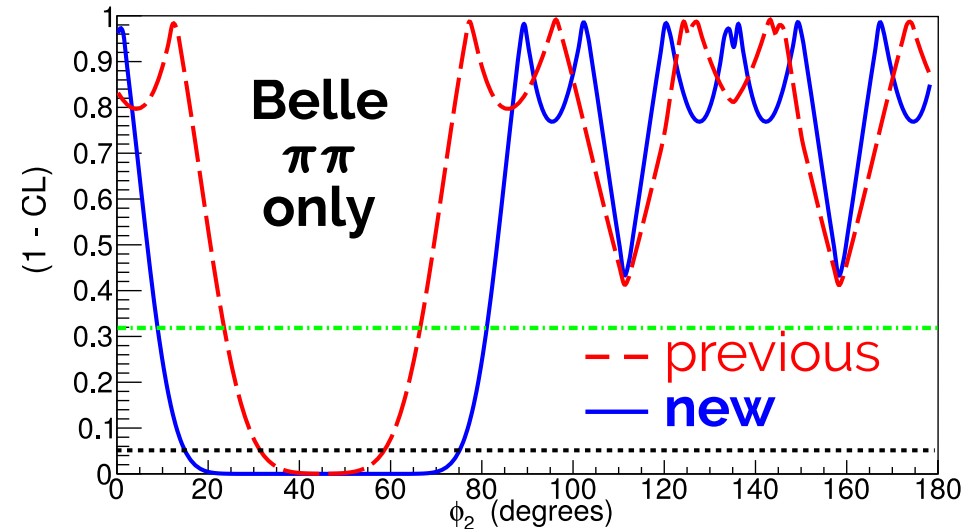
3D-fit: $M_{bc}, \Delta E, T_c$
(T_c : continuum suppression variable)

$$\mathcal{B} = (1.31 \pm 0.19 \pm 0.19) \times 10^{-6}$$

$$A_{CP} = 0.14 \pm 0.36 \pm 0.10$$

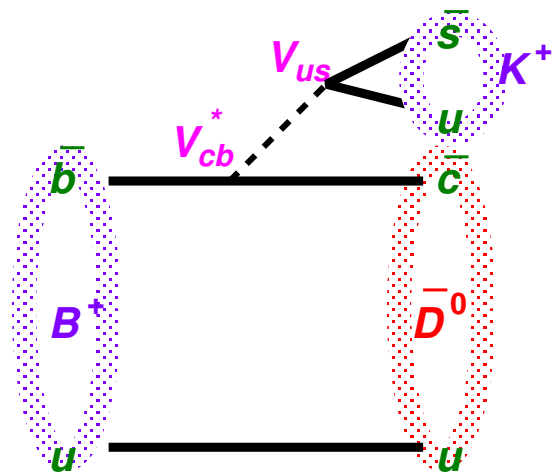
ϕ_2 excluded from the range:
 $15.5^\circ < \phi_2 < 75.0^\circ$ at 2σ

Confidence limit on ϕ_2

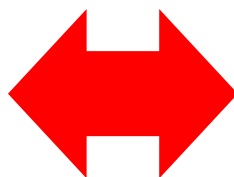
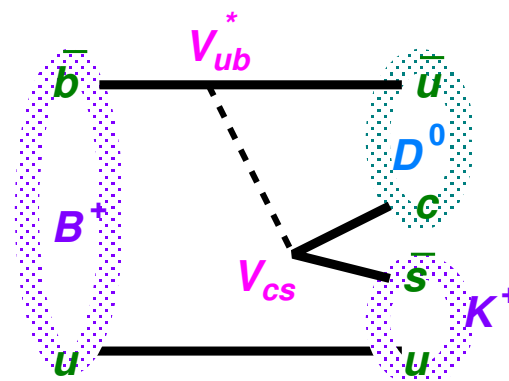


ϕ_3/γ measurement

$$A(B^- \rightarrow D^0 K^-) \propto \lambda^3$$



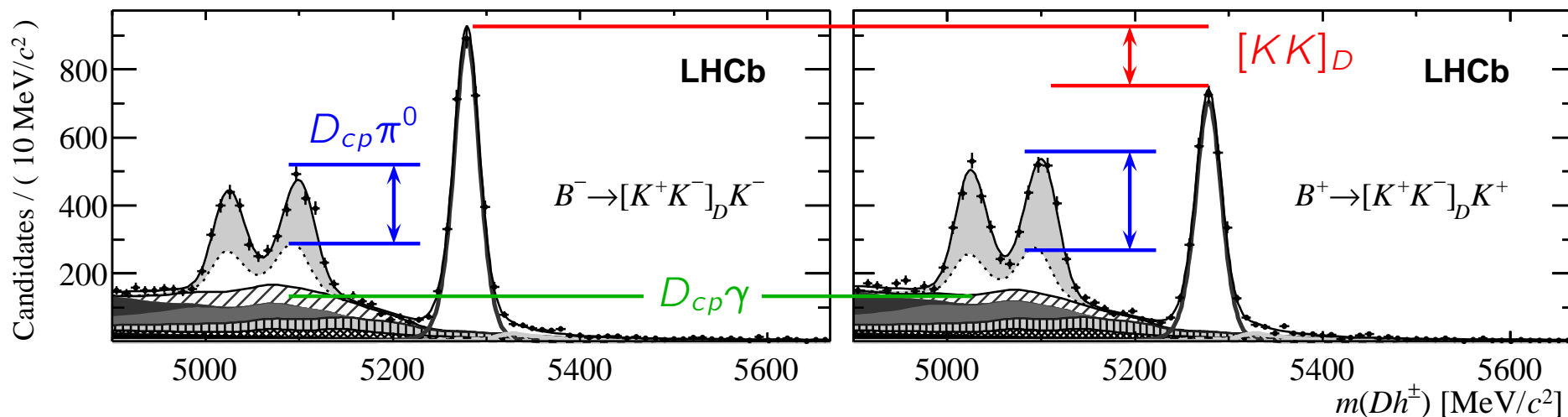
$$A(B^- \rightarrow \bar{D}^0 K^-) \propto \lambda^3(\rho + i\eta)$$



- Two interfering diagrams have the same order in λ and weak phase difference ϕ_3/γ (and unknown strong phase difference δ)
- $r = |A(\bar{D}^0 K^-)/A(D^0 K^-)| \sim 0.2$ for color suppression ($r^2 \sim 0.04$)
- ϕ_3/γ extraction methods
 - **GLW** — $D^0 \rightarrow f_{CP}$, e.g., $K^+ K^-$, $\pi^+ \pi^-$, $K_S \pi^0$
 - **ADS** — $D^0 \rightarrow$ doubly-cabibbo-suppressed, e.g., $K^+ \pi^-$
 - **GGSZ** — $D^0 \rightarrow K_S \pi^+ \pi^-$, using Dalitz plot

LHCb: γ from $B \rightarrow D^{(*)0} K$

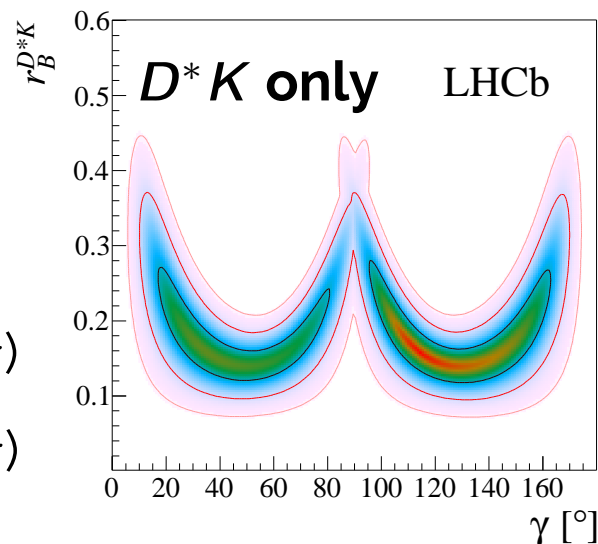
[arXiv:1708.06370 submitted to PLB]



- GLW method using $D_{CP} = K^+ K^-$ and $\pi^+ \pi^-$
- Partial reco of $D^* \rightarrow D^0 \pi^0$ and $D^0 \gamma$ (soft π^0 / γ not reconstructed)

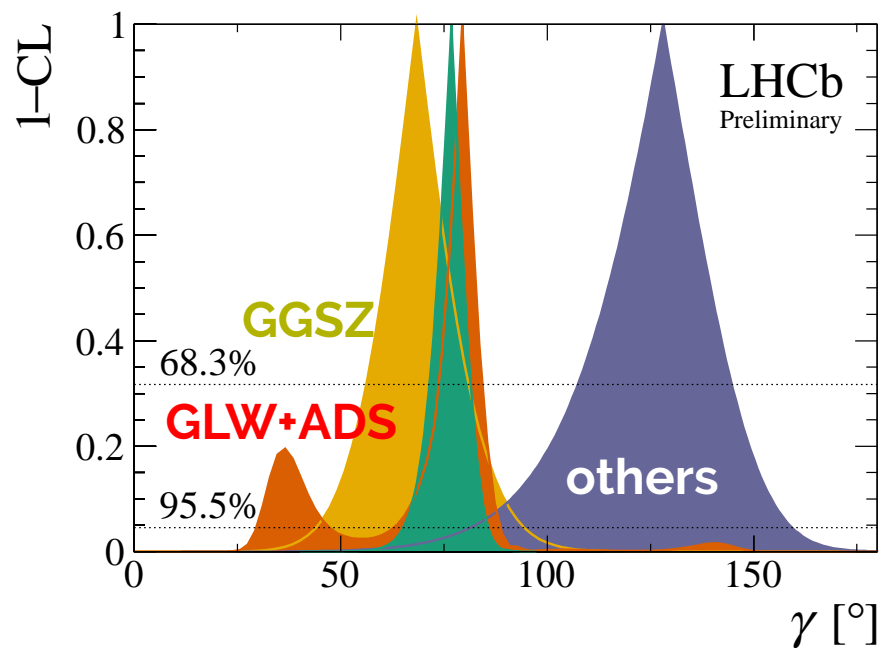
Results

$[KK]_D K$	$A_{CP} = +0.126 \pm 0.014 \pm 0.002$
$[\pi\pi]_D K$	$A_{CP} = +0.115 \pm 0.025 \pm 0.007$
$[D_{CP}\pi^0]_{D^*} K$	$-A_{CP} = +0.151 \pm 0.033 \pm 0.011 (4.3\sigma)$
$[D_{CP}\gamma]_{D^*} K$	$A_{CP} = +0.276 \pm 0.094 \pm 0.047 (2.4\sigma)$



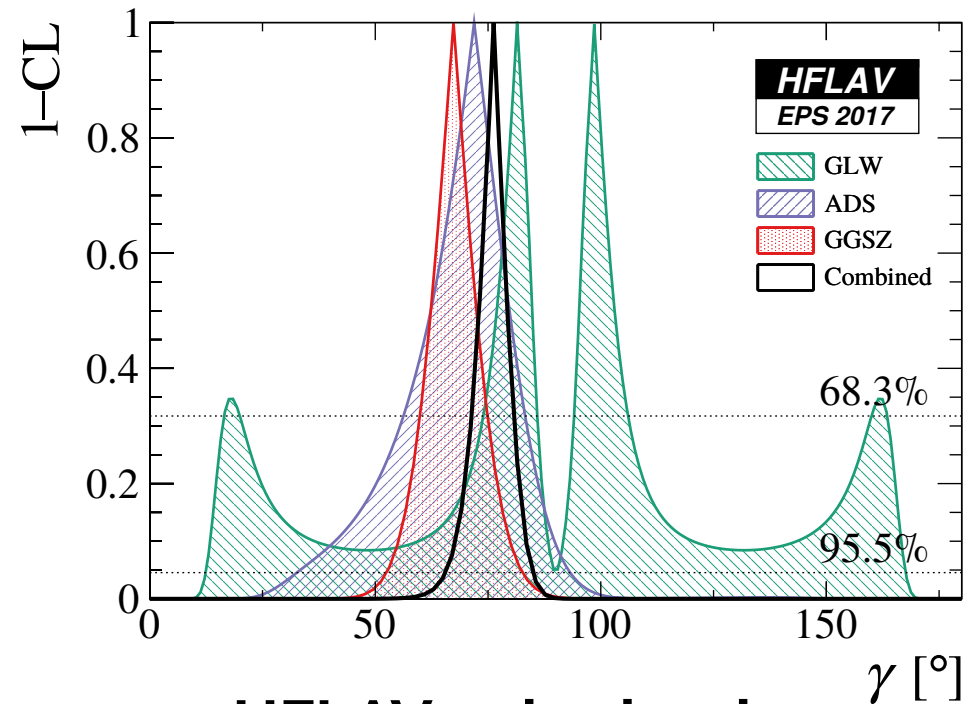
γ/ϕ_3 : average

[LHCb-CONF-2017-004, HFLAV]



LHCb combined

$$\gamma = (76.8^{+5.1}_{-5.7})^\circ$$



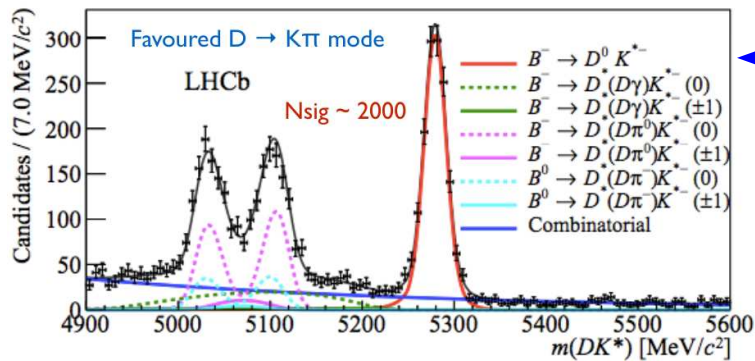
HFLAV combined

$$\gamma = (76.2^{+4.7}_{-5.0})^\circ$$

- γ measurement is dominated by LHCb, who provides 85 observables and 37 parameters
- World average is better than 5°
- More to come from LHCb...

LHCb: γ from $B \rightarrow D^0 K^*$

[G.Cowan LP'17, LHCb-PAPER-2017-030
in preparation]



← Large signal for **favoured** $D^0 \rightarrow K^- \pi^+$

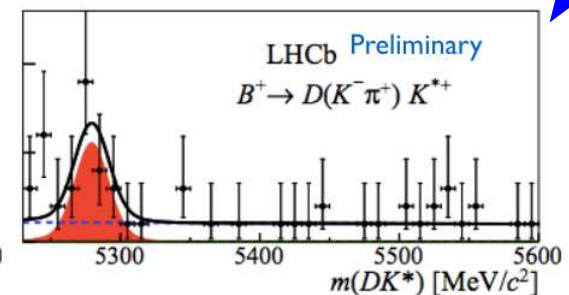
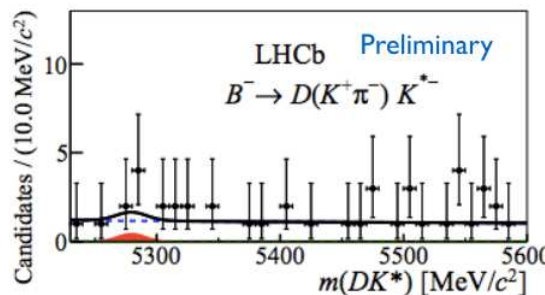
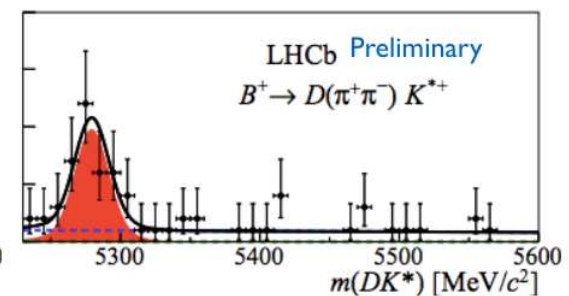
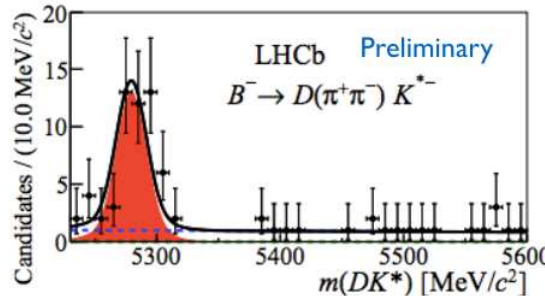
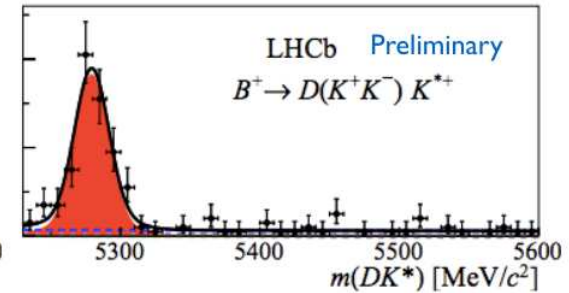
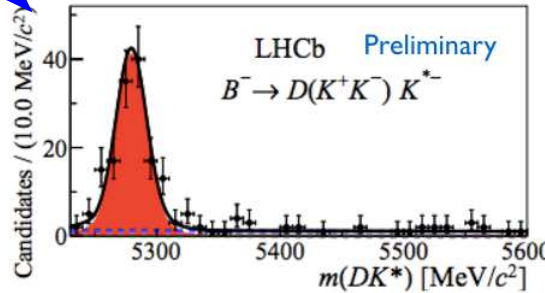
GLW: clean CP modes $D^0 \rightarrow K^+ K^- / \pi^+ \pi^-$

4.2 σ evidence for wrong sign $K^- \pi^+$: **ADS**

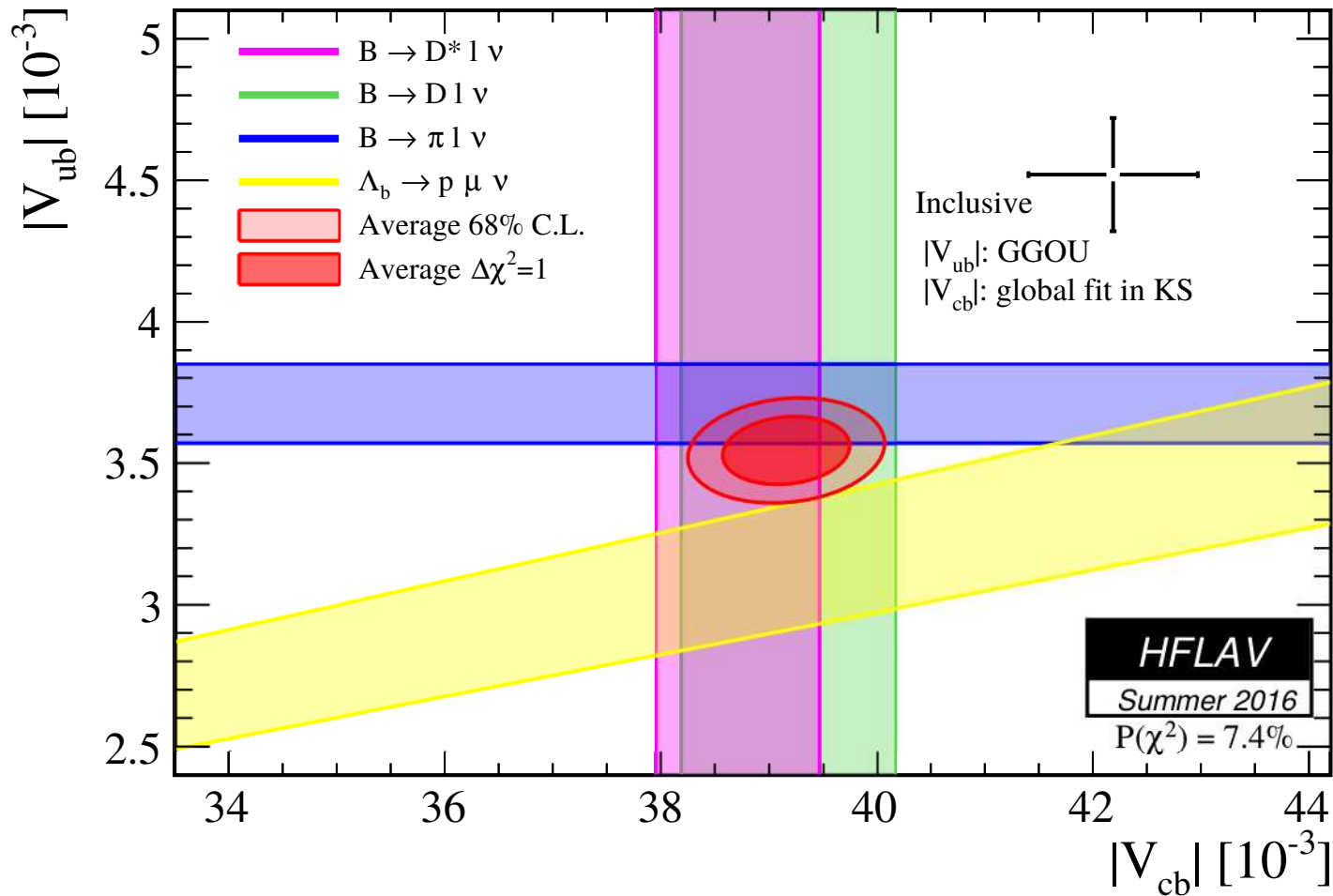
Rates and asymmetries
provide constraints on
 r , δ and γ

Not in average yet

preliminary



V_{ub} and V_{cb} , inclusive and exclusive



⚠ **Both** V_{ub} and V_{cb} suffer from discrepancy between **inclusive** and **exclusive** analyses by $2-3\sigma$

$$\begin{aligned}
 |V_{cb}|(D^* l \nu) &= (39.05 \pm 0.47 \pm 0.58) \times 10^{-3} & |V_{ub}|(\pi l \nu) &= (3.67 \pm 0.15) \times 10^{-3} \\
 |V_{cb}|(\text{incl}) &= (42.19 \pm 0.78) \times 10^{-3} & |V_{ub}|(\text{incl}) &= (4.52 \pm 0.15 \pm 0.13) \times 10^{-3}
 \end{aligned}$$

Belle: $B \rightarrow D^* \ell \nu$ hadronic tag

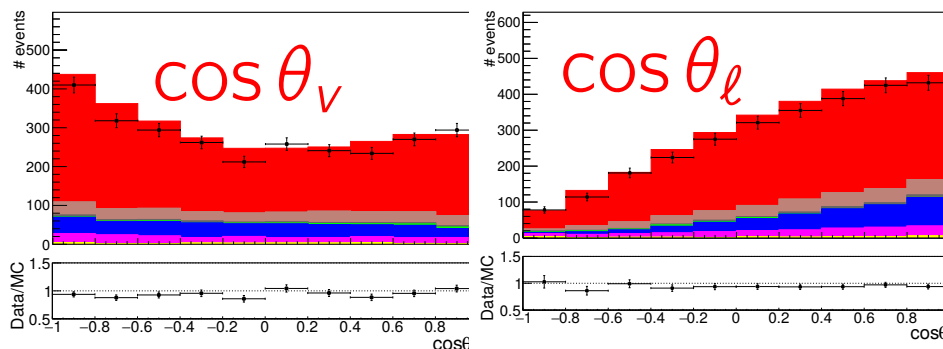
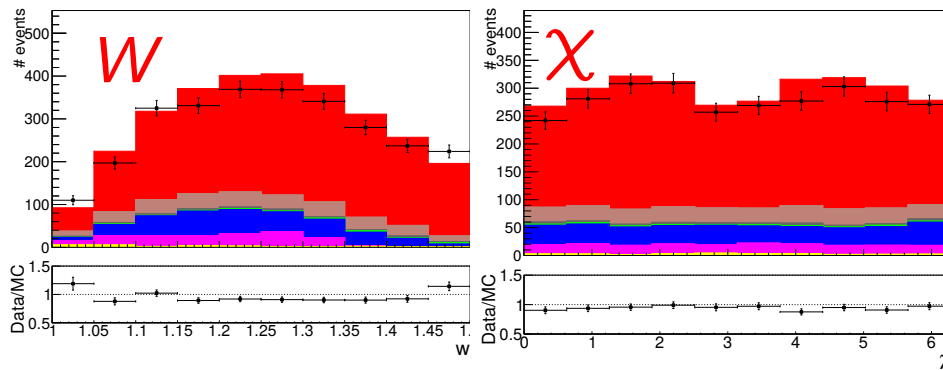
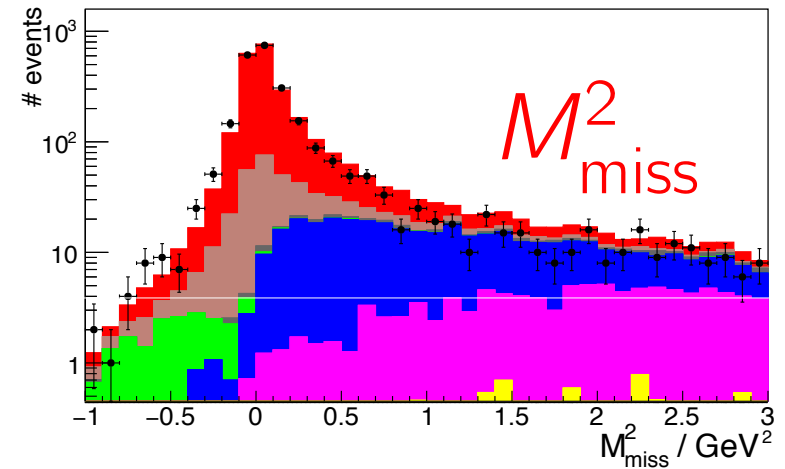
[arXiv:1702.01521 preliminary]

Standard method: CLN form factor

3-angles (θ_ν , θ_ℓ , χ) and $w (= \frac{m_B^2 - m_{D^*}^2 - q^2}{m_B m_{D^*}})$

$$\frac{d^4 \Gamma(B \rightarrow D^* \ell \nu)}{dw d \cos \theta_\nu d \cos \theta_\ell d \chi} = f(|V_{cb}|^2, \rho_D^2, R_1, R_2)$$

FF parameters determined from fit



preliminary

$$|V_{cb}| = (37.4 \pm 1.2) \times 10^{-3}$$

$$\Leftrightarrow |V_{cb}|_{WA} = (39.2 \pm 0.7) \times 10^{-3}$$

not filling the gap between
inclusive / exclusive

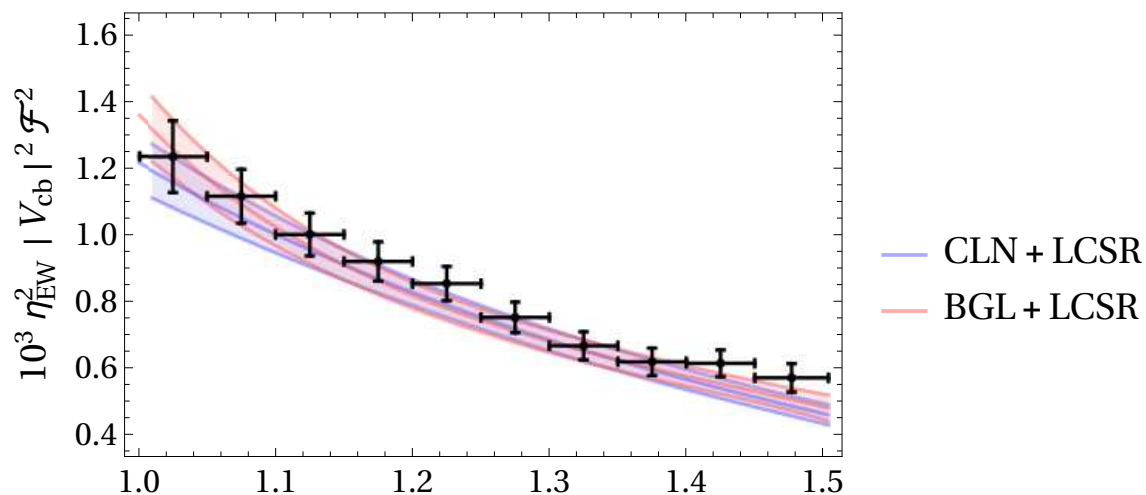
FF refit: BGL vs CLN

Alternative FF: BGL instead of CLN

Boyd-Grinstein-Lebed PRD56,6895(1997), Caprini-Lellouch-Neubert NPB530,153(1998)

Refit of Belle data

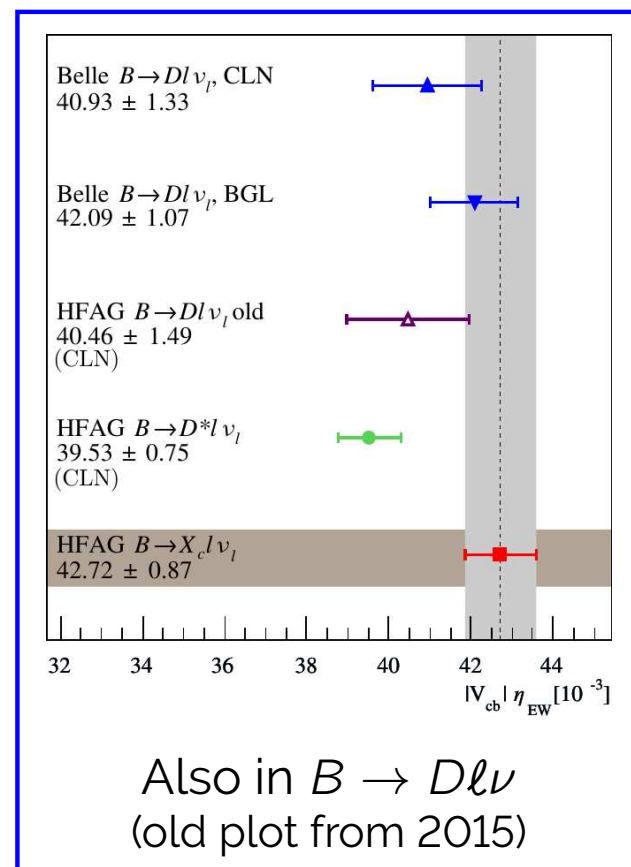
by Bigi-Gambino-Schacht PLB769,441(2017), also by Grinstein Kobach PLB771,359(2017)



$$|V_{cb}|(\text{BGL}) = (40.4^{+1.6}_{-1.7}) \times 10^{-3}$$

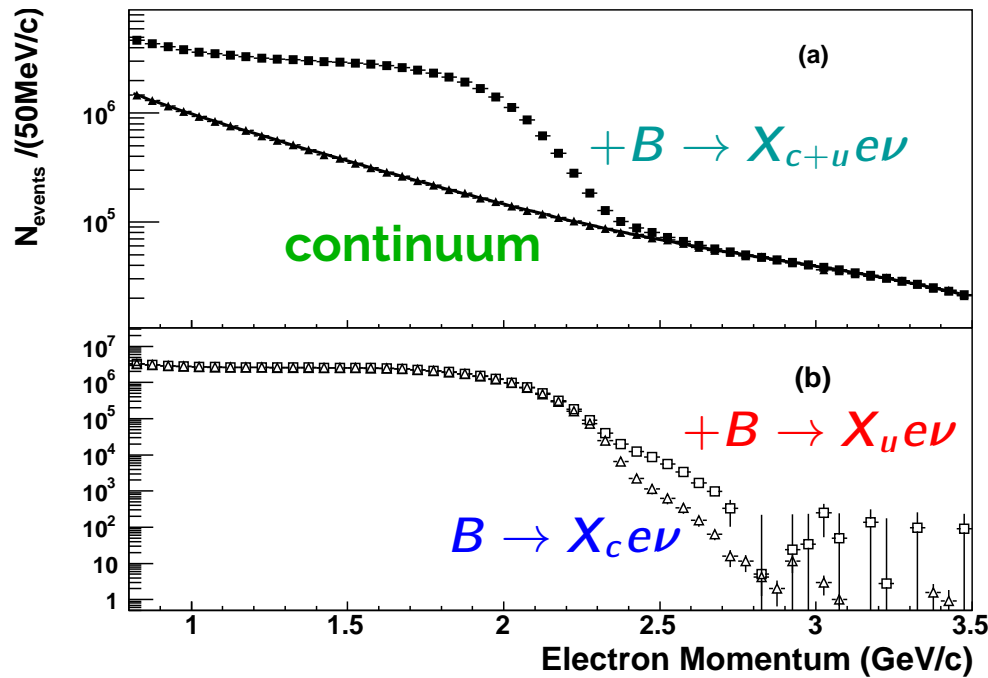
$$|V_{cb}|(\text{CLN}) = (38.2 \pm 1.4) \times 10^{-3}$$

Reconciliation of inclusive-exclusive?



BaBar: $B \rightarrow X_u e \nu$ inclusive

[PRD95,072001 (2017)]

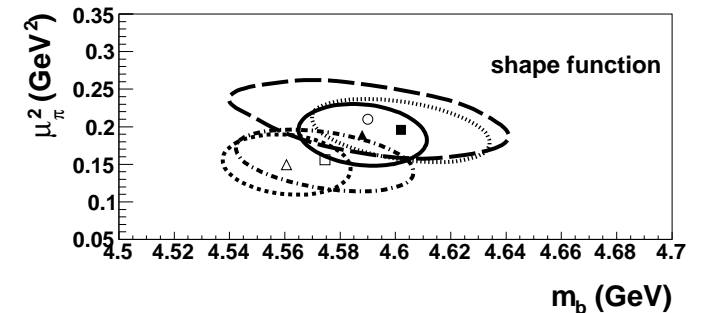
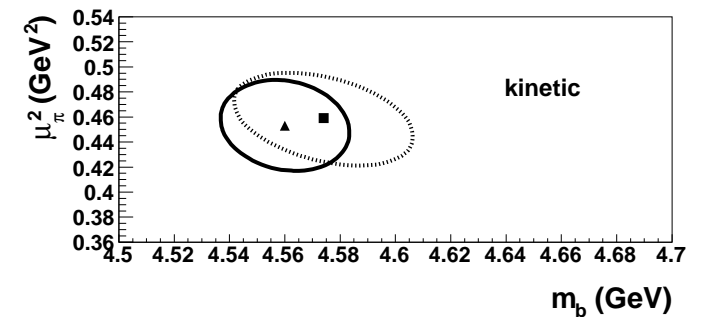


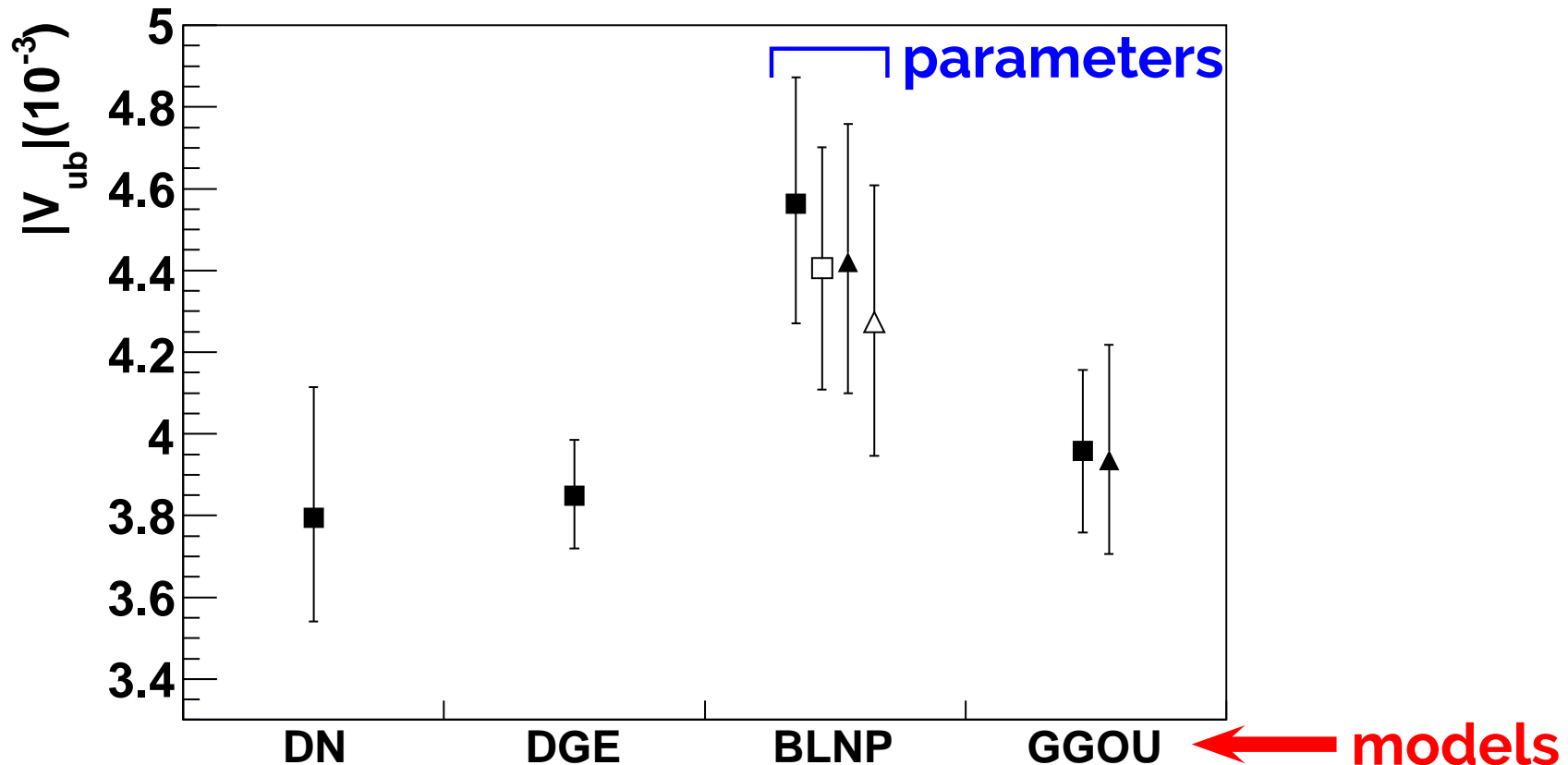
Endpoint analysis
single bin: 2.1–2.7 GeV

HQE parameters from
latest HFLAV fit

4 different models to extrapolate
the spectrum (shape function)

- DN (1999)
- BLNP (2004)
- GGOU (2007)
- DGE (2006)

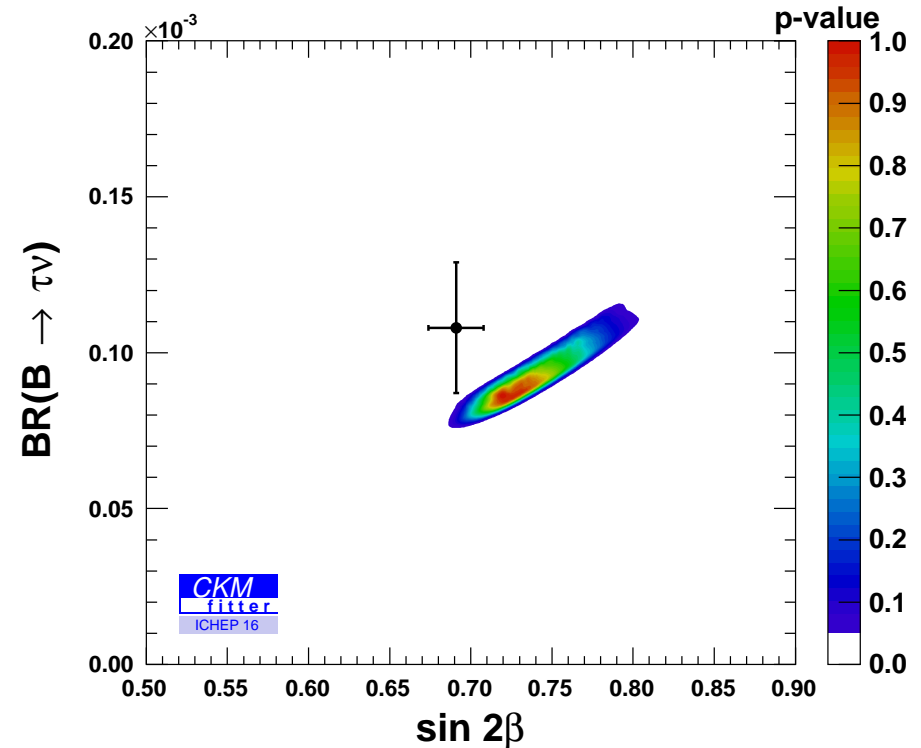
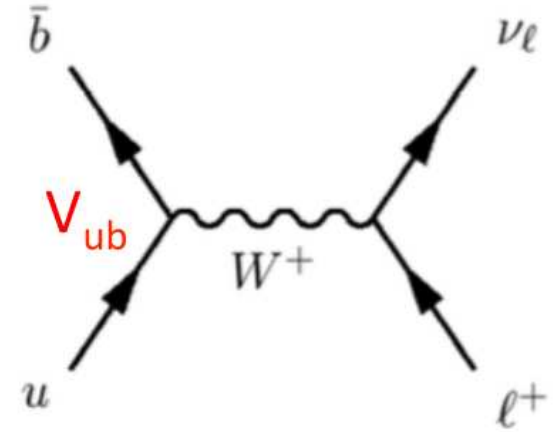




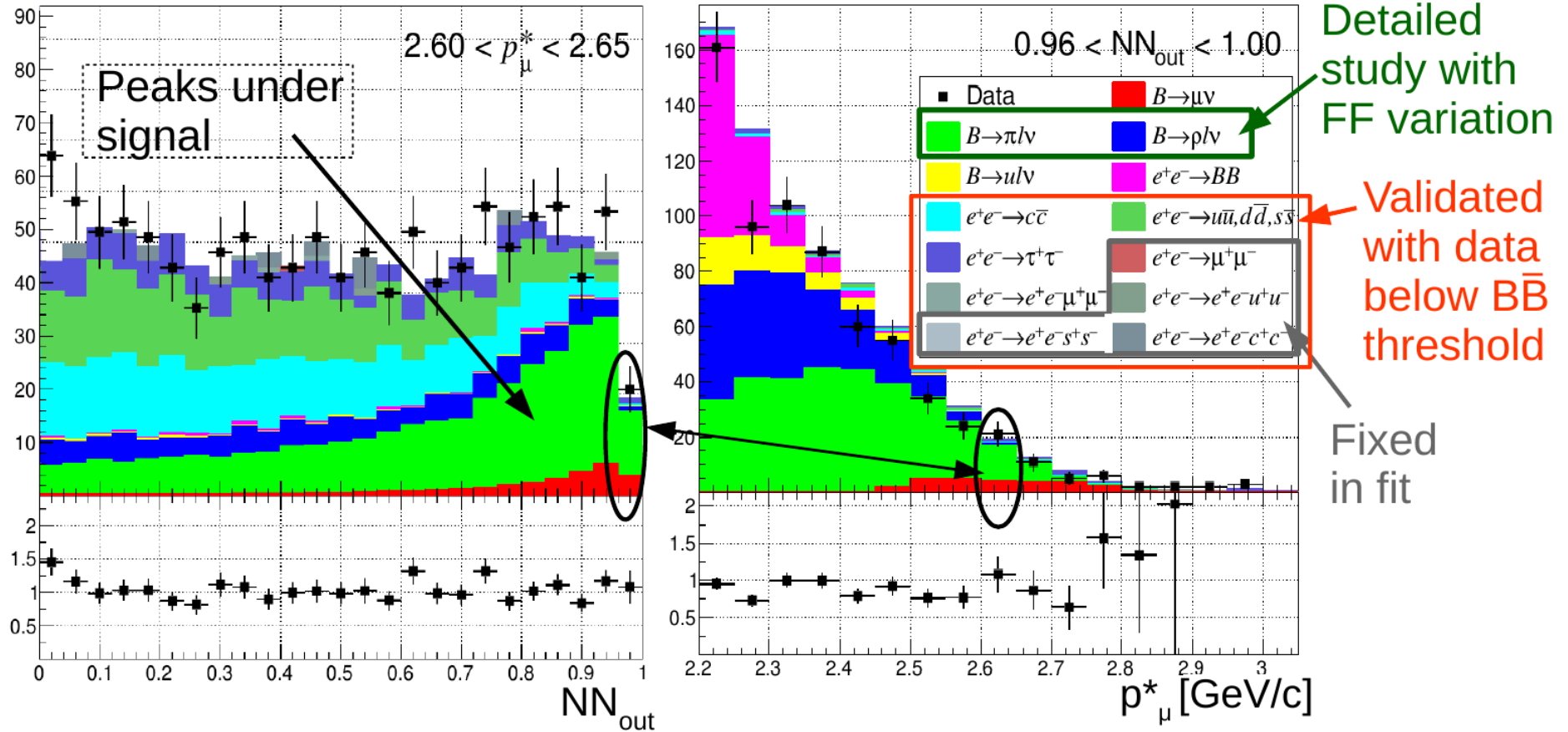
- Lower (= closer to the exclusive) in 3 models
- Variation of shape function parameters do not affect much
- Model dependence = limitation of single bin extrapolation

$B^+ \rightarrow \ell^+ \nu$ and CKM

- **Purely leptonic decay** is proportional to $f_B^2 |V_{ub}|^2$ (in SM), (also sensitive to type-II 2HDM charged Higgs)
- However, f_B is not precisely known (only from Lattice)
- Instead, **more reliable constraint** using Δm_d and other CKM (then no direct constraint to $|V_{ub}|$)
- $B \rightarrow \tau \nu$ has been measured, but no single 5σ signal yet (and previous tension is no more significant)
- $B \rightarrow \mu \nu$ **result is wanted** (lepton universality test is of great interest now)



Belle: $B^+ \rightarrow \mu^+ \nu$



Untagged analysis, neural network output, efficiency = 38%

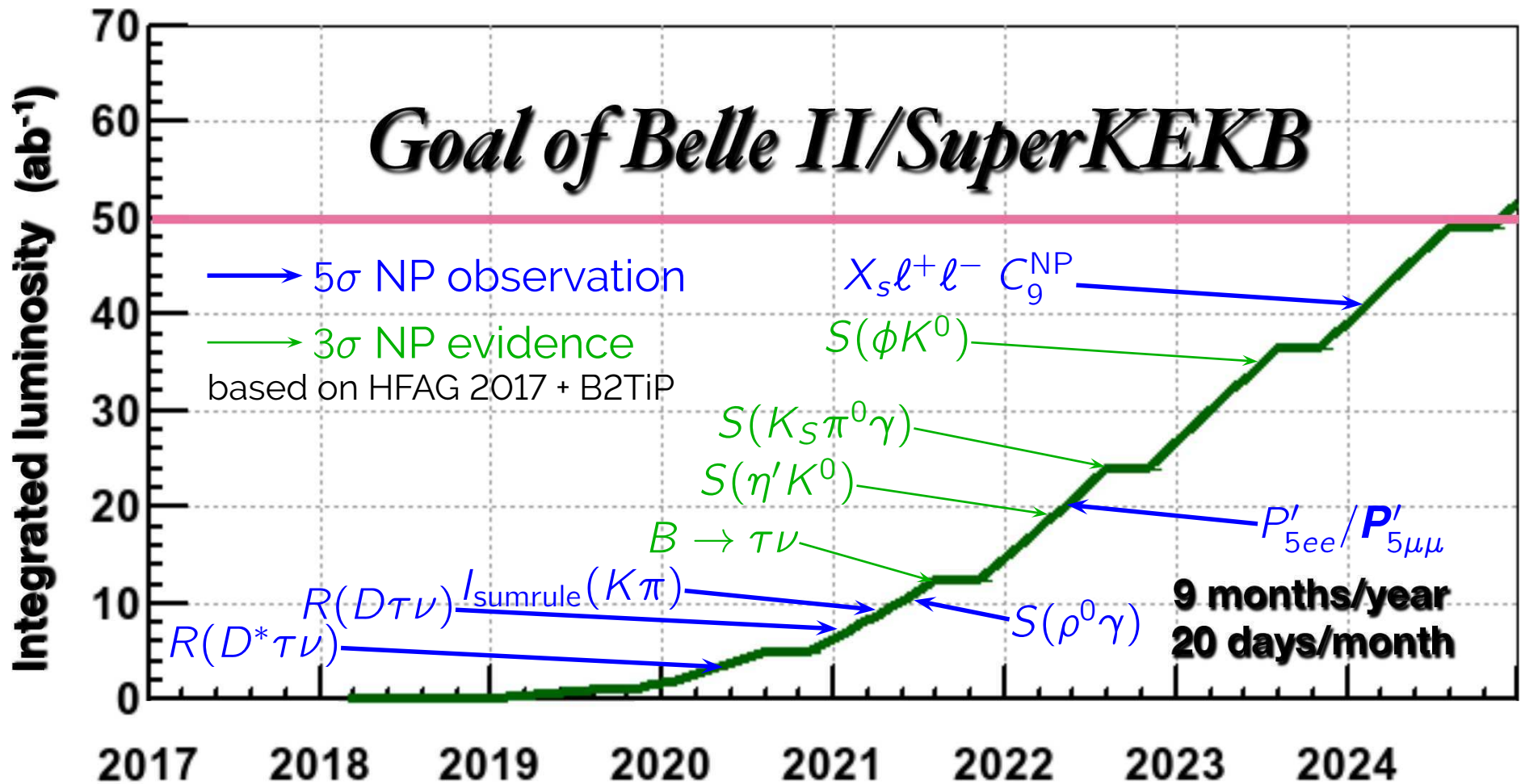
$$\mathcal{B}(B \rightarrow \mu \nu) = (6.5 \pm 2.2 \pm 1.6) \times 10^{-7} \in [2.9, 10.7] \times 10^{-7} \text{ (90\%CL)}$$

- 2.4σ from null, consistent with $\mathcal{B}_{\text{SM}} = (3.8 \pm 0.3) \times 10^{-7}$
- One of anticipated early Belle II hot topics (!)

Belle II at SuperKEKB coming soon



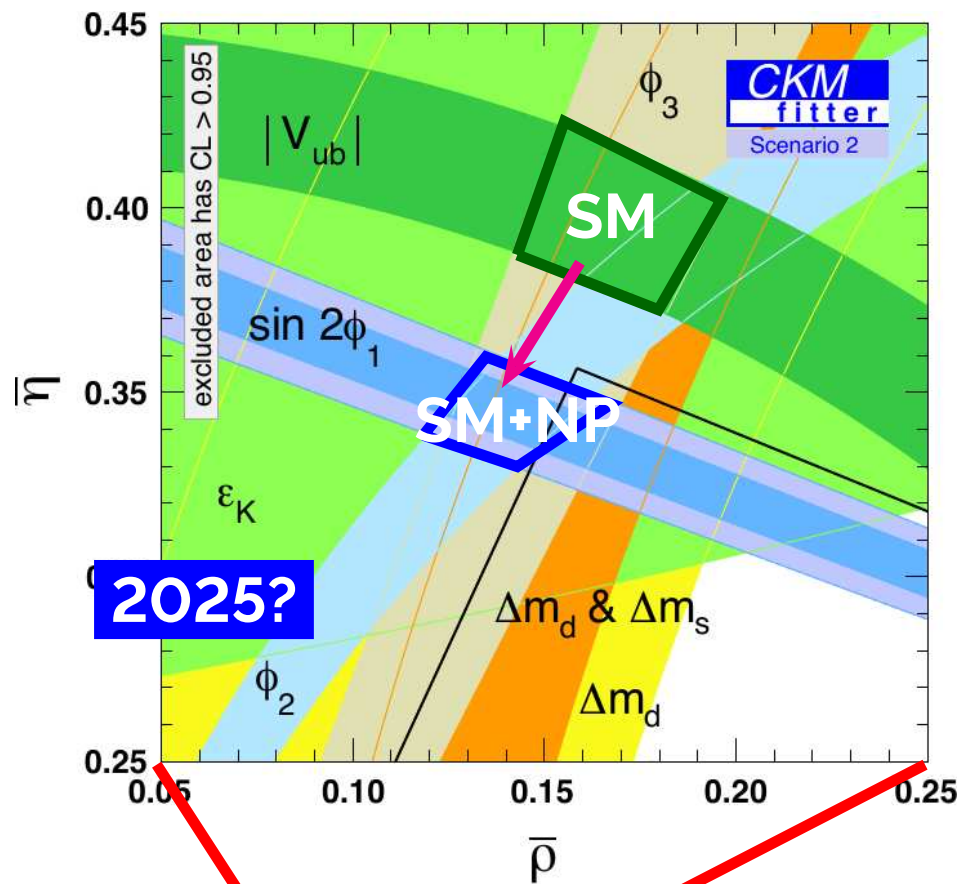
- Forward endcap installation — very soon
- **Phase II** operation (no VXD, limited physics) — 2018.2.–
- **Phase III** full physics run — (late 2018 or) 2019–



⚠ Rich physics ahead!

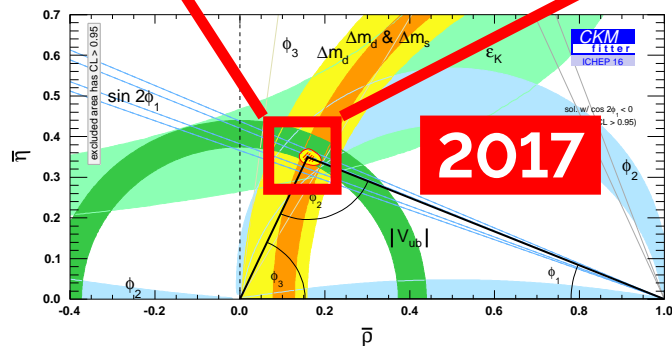
- ✓ Current inconclusive NP "hints" → "5 σ -observed" (?)
- ✓ Topics involving neutrals and inclusive: $\tau\nu$, $\rho\gamma$, $K\nu\bar{\nu}$, $X_S\gamma$, ...
- ✓ LHCb upgrade plan covered in the next talk

CKM prospects



- All angles are measured with $\sim 1\%$ precision
- V_{ub} inconsistency has to be resolved
- Chance to find the clear NP signal (!)

New paradigm of quark transition is coming (!?)



Summary

- Belle and BaBar are finalizing the analysis of CKM
- LHCb pushing down γ , now WA with 5° precision
- V_{ub} internal inconsistency has to be resolved
- Major progress by startup of Belle II and LHCb upgrade