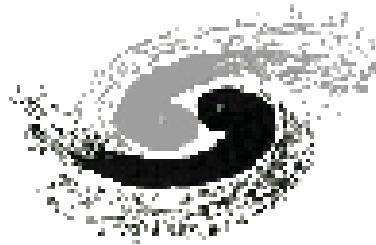
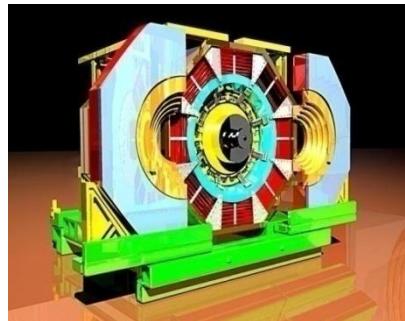


Form Factor Measurements at BESIII for an Improved Standard Model Prediction of the muon $g-2$

Marco Destefanis

Università degli Studi di Torino e INFN

on behalf of the BESIII Collaboration



PANIC 2017

21st Particles & Nuclei International Conference

Beijing, China

September 1-5, 2017

Overview

➤ Introduction

Muon magnetic moment

BEPCII and the BESIII experiment

BESIII dataset

➤ Physics results

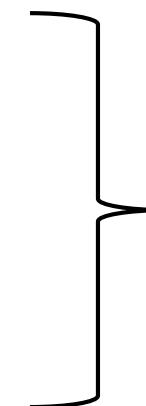
$\pi^+\pi^-$

$\pi^+\pi^-\pi^0$

$\pi^+\pi^-2\pi^0$

$\pi^+\pi^-3\pi^0$

Two-photon physics



BESIII
Preliminary

➤ Summary

Muon Magnetic Moment

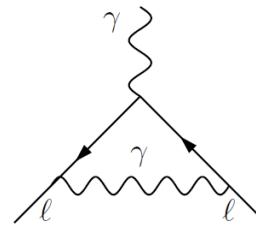
Lepton magnetic moment: $\bar{\mu} = g \frac{qe}{2m} \bar{s}$

Dirac theory prediction: $g = 2(1 + a)$

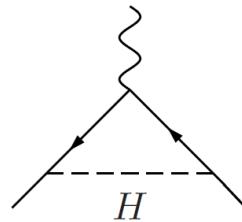
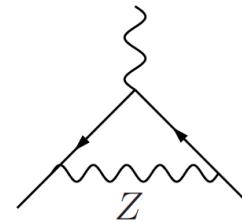
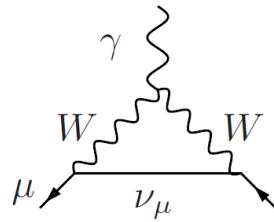
$$a_\mu = \frac{g_\mu - 2}{2}$$

Muon **anomaly** arises from quantum fluctuations

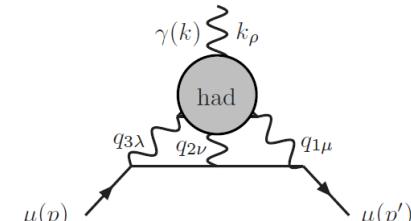
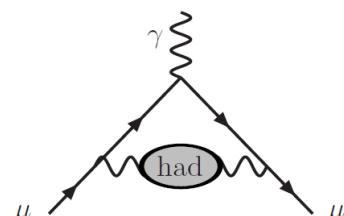
QED contribution (largest):



Weak contribution:



Hadronic contribution:



Muon Magnetic Moment

$$a_\mu = \frac{g_\mu - 2}{2} = \frac{\alpha}{2\pi} + \dots = 0.001161$$

$$a_\mu^{theo} = a_\mu^{QED} + a_\mu^{weak} + a_\mu^{hadr}$$

Contribution	Results in 10^{-10} units		
QED (leptons)	11658471.885	± 0.004	Kinoshita et al. (2012)
Weak	15.4	± 0.2	Czamecki et al. (2003)
HVP (LO)	692.3	± 4.2	Davier et al. (2001)
HVP (HO)	-9.84	± 0.07	Hagiwara et al. (2009)
HLBL	11.6	± 4.0	Jegerlehner, Nyffler (2009)
Total	11659181.3	± 5.8	
Experiment	11659208.9	± 6.3	Discrepancy: 27.6

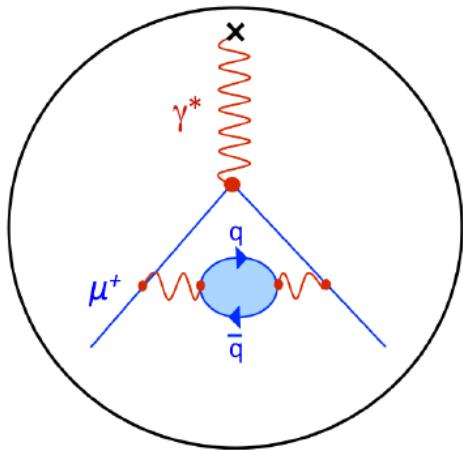
Prediction limited by hadronic contributions

Perturbative method cannot be applied in the relevant energy regime

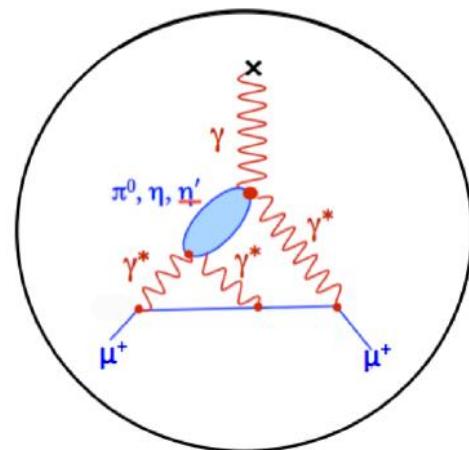
Muon Magnetic Moment

Hadronic Contributions

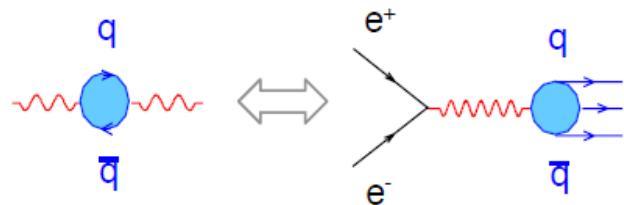
Hadronic Vacuum Polarization



Hadronic Light-by-Light



Optical theorem



Two-photons collisions

$$\text{Dispersion integral: } a_{\mu,LO}^{HVP} = \frac{1}{4\pi^3} \int_{m_{\pi^0}}^{\infty} ds K(s) \sigma_{had}(s)$$

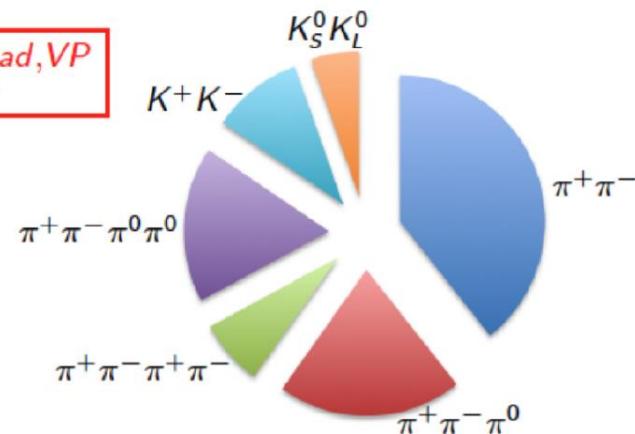
Muon Magnetic Moment

Hadronic Contributions

$a_\mu^{had, VP}$



$\delta a_\mu^{had, VP}$



M. Ripka, *Initial State Radiation Measurement at BESIII, PhiToPsi2017 proceedings, in press*

KLOE^[1] and BABAR^[2] measurement discrepancy 3-5%

Another **high precision** measurement needed -> BESIII

Wider mass range than KLOE

Closer to $\sqrt{s} \lesssim 2$ GeV than BABAR -> lower suppression of ISR events

Untagged ISR mode can be used above $\sqrt{s} \gtrsim 1$ GeV
-> no problem for $\geq 4\pi$

ISR measurement of baryon Form Factors:
see presentation of **Zhaoxia Meng**

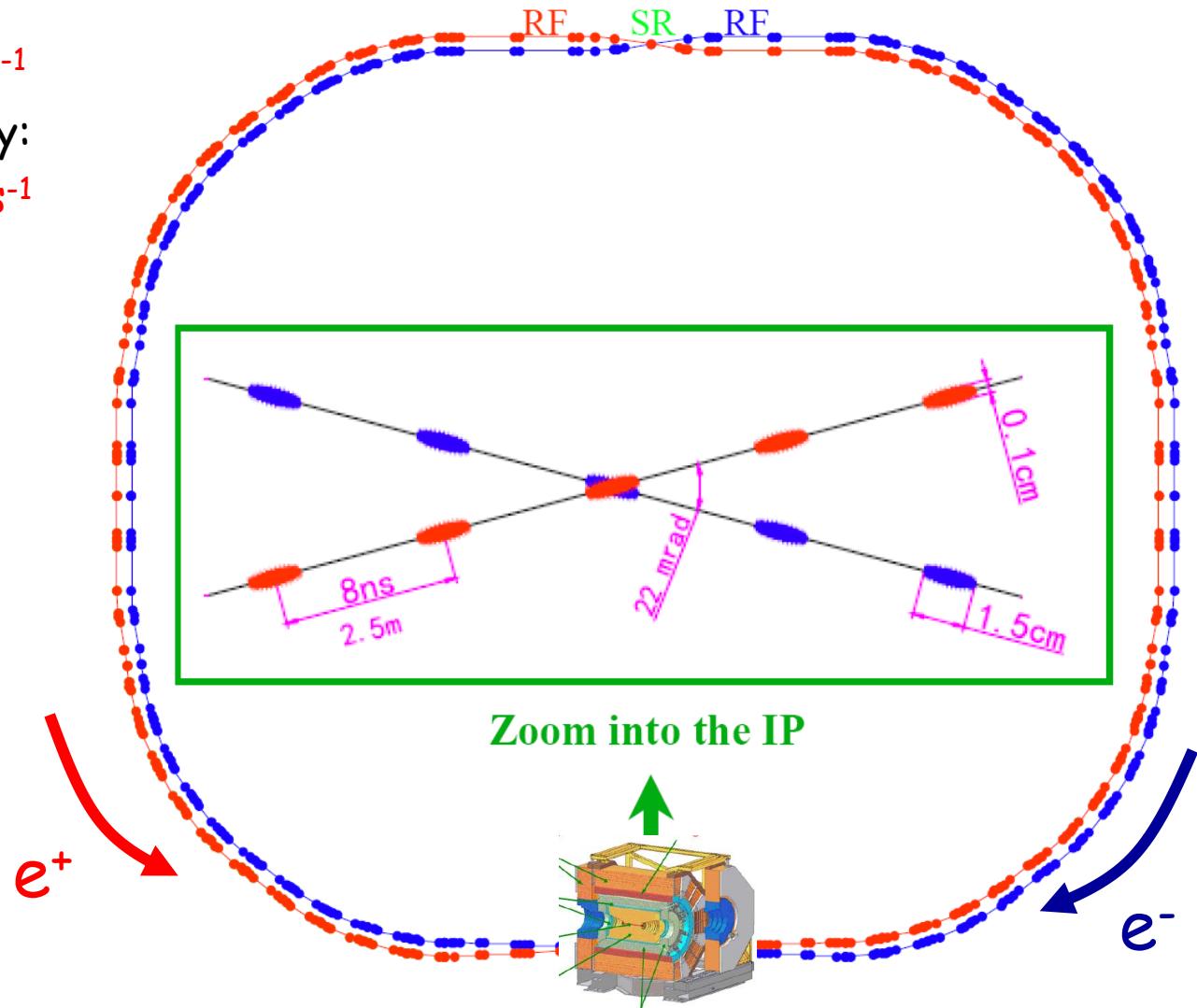
[1] B. Aubert et al., Phys. Rev. Lett. 103, 231801 (2009). J.P. Lees et al., Phys. Rev. D86, 032013 (2012)

[2] F. Ambrosino et al. Phys. Lett. B 670, 285 (2009). F. Ambrosino et al. Phys. Lett. B 700, 102-110 (2011).
D. Babusci et al. Phys. Lett. B 720, 336-343 (2013).

BEPCII Storage Rings

- Beam energy:
1.0-2.3 GeV
- Design Luminosity:
 $1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
- Achieved Luminosity:
 $\sim 1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
- Optimum energy:
1.89 GeV
- Energy spread:
 5.16×10^{-4}
- No. of bunches:
93
- Bunch length:
1.5 cm
- Total current:
0.91 A
- Circumference:
237m

Beijing Electron-Positron Collider II

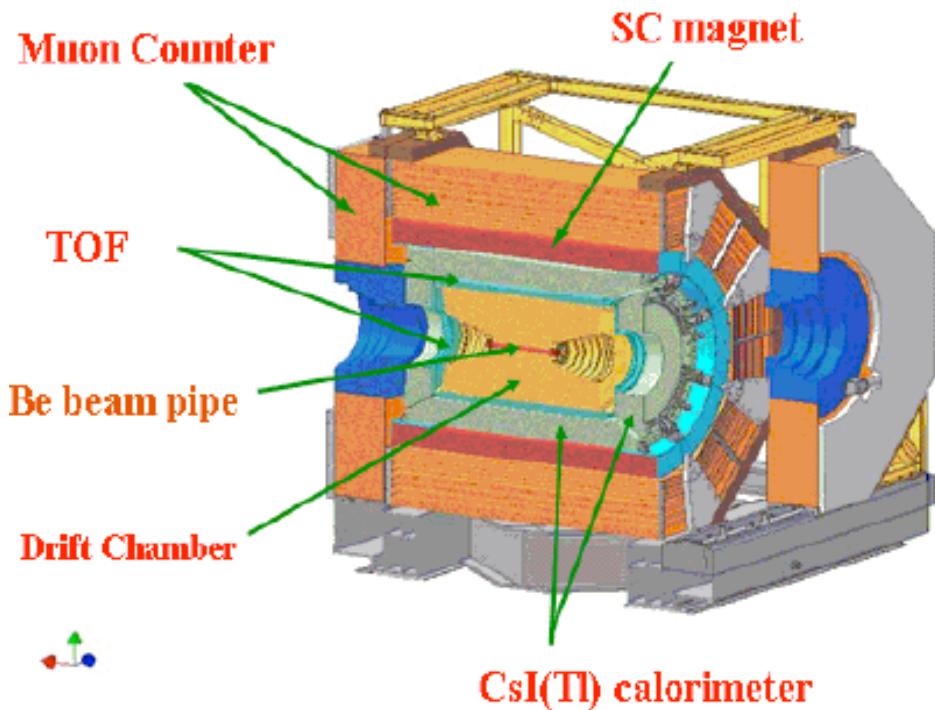


The BESIII Spectrometer @ IHEP

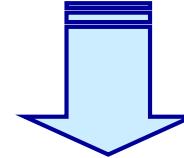
BEijing Spectrometer III

e^+e^- collisions

\sqrt{S} tuned depending on energy



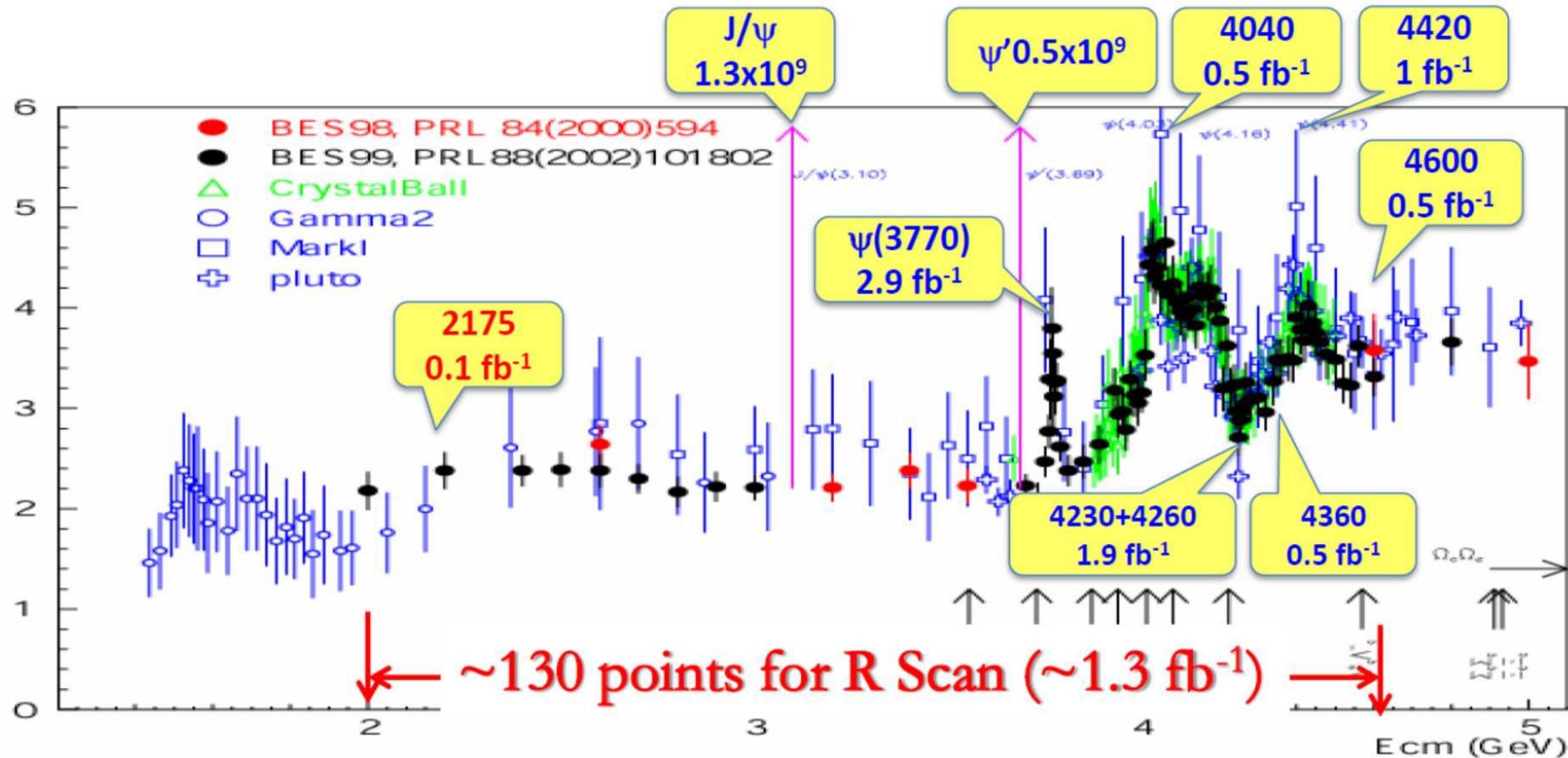
Physics program



- Charmonium Physics
- D-Physics
- Light Hadron Spectroscopy
- τ -Physics
- ...

BESIII Dataset

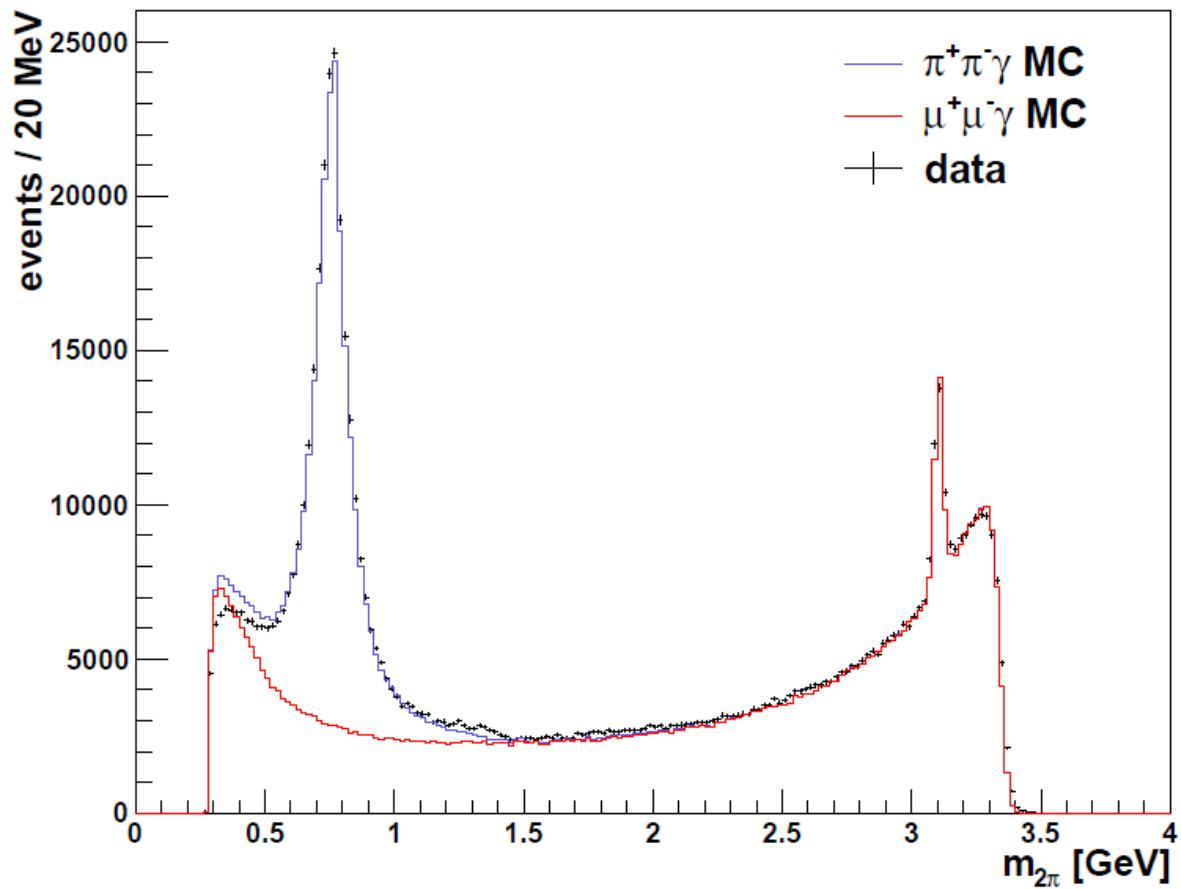
R Value



- World largest data sample on J/ψ , $\psi(2S)$, $\psi(3770)$, $\Upsilon(4260)$... in e^+e^- collisions
- From light meson spectroscopy to $\Lambda_c\bar{\Lambda}_c$
- Fine and coarse scan of the accessible energy region

Particle Identification

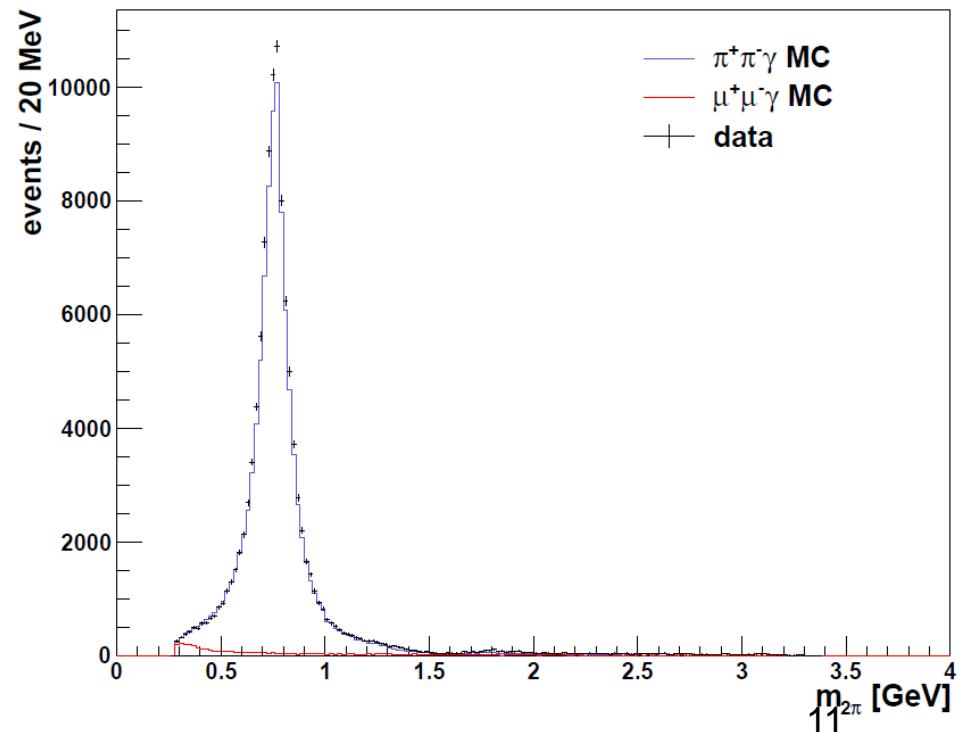
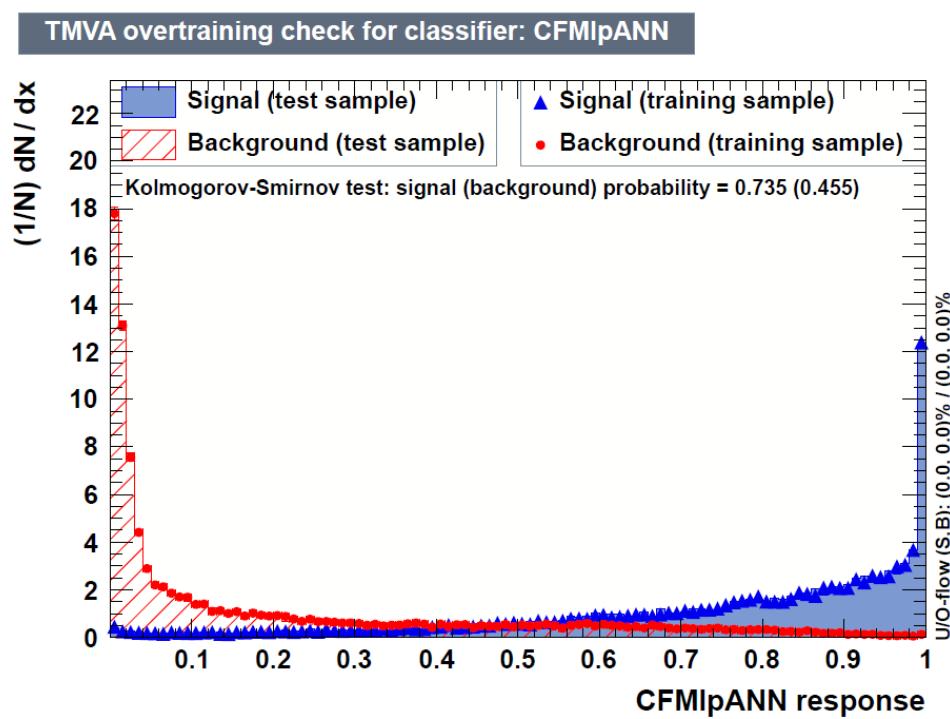
- Tagged ISR mode only
- Kinematic fit for $\pi^+\pi^-\gamma_{\text{ISR}}$ final state
- Standard BESIII PID system for electron rejection
- Muon-pion separation needed



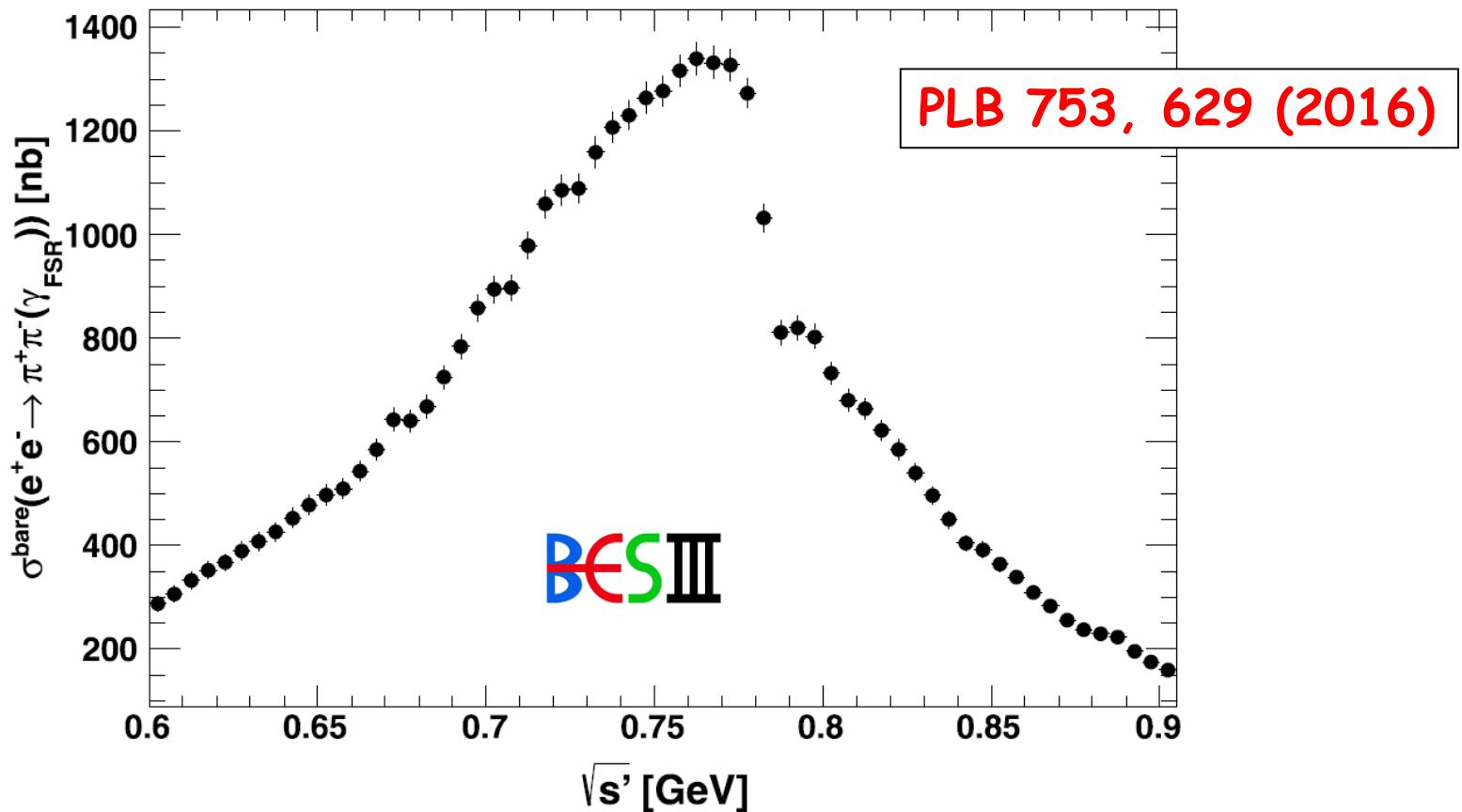
$e^+e^- \rightarrow \gamma\pi^+\pi^-$ Selection

PLB 753, 629 (2016)

- Muons and pions have different shower shape in EMC
- Artificial Neural Network (ANN) for μ - π separation
- Very clean sample after ANN
- ρ - ω interference clearly visible



$\pi^+\pi^-$ Cross Section



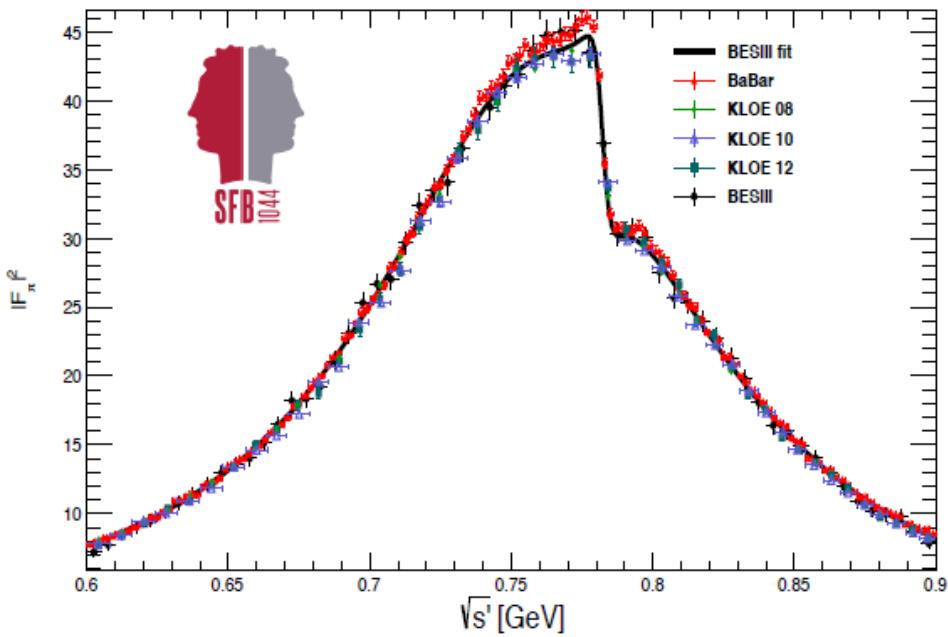
$$\sigma^{bare}(\sqrt{s'}) = \frac{1}{\frac{2\sqrt{s'}}{s} W(s, x) \epsilon(\sqrt{s'}) \mathcal{L} \delta_{vac} \delta_{FSR}} \frac{dN}{d\sqrt{s'}}$$

p-w interference clearly visible

Comparison of $\pi^+\pi^-$ Form Factor

PLB 753, 629 (2016)

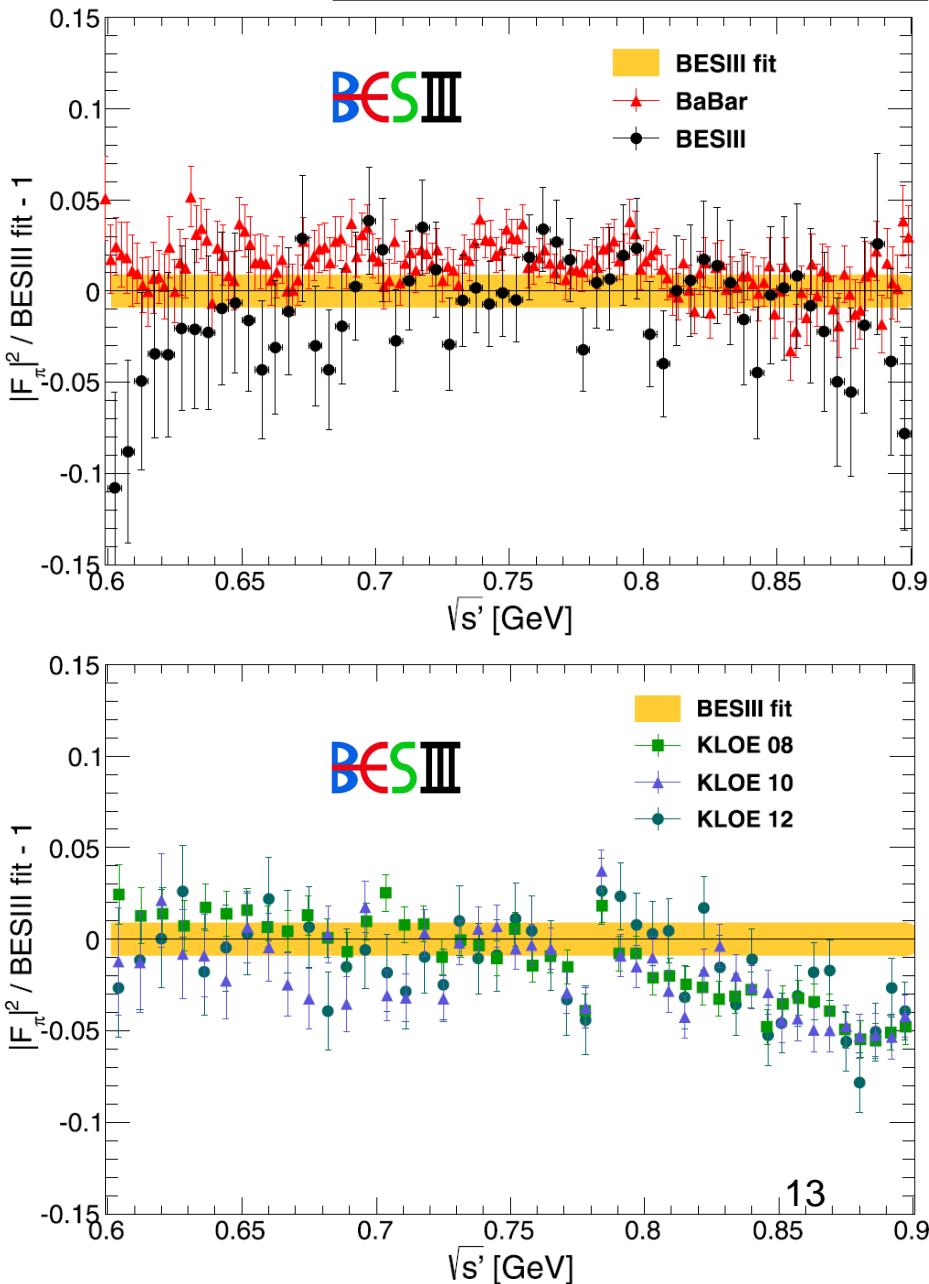
Pion Form Factor F_π



- New BESIII measurement **agrees** with KLOE^[1] and BABAR^[2]
- Small **shift** wrt BABAR above p-w interference

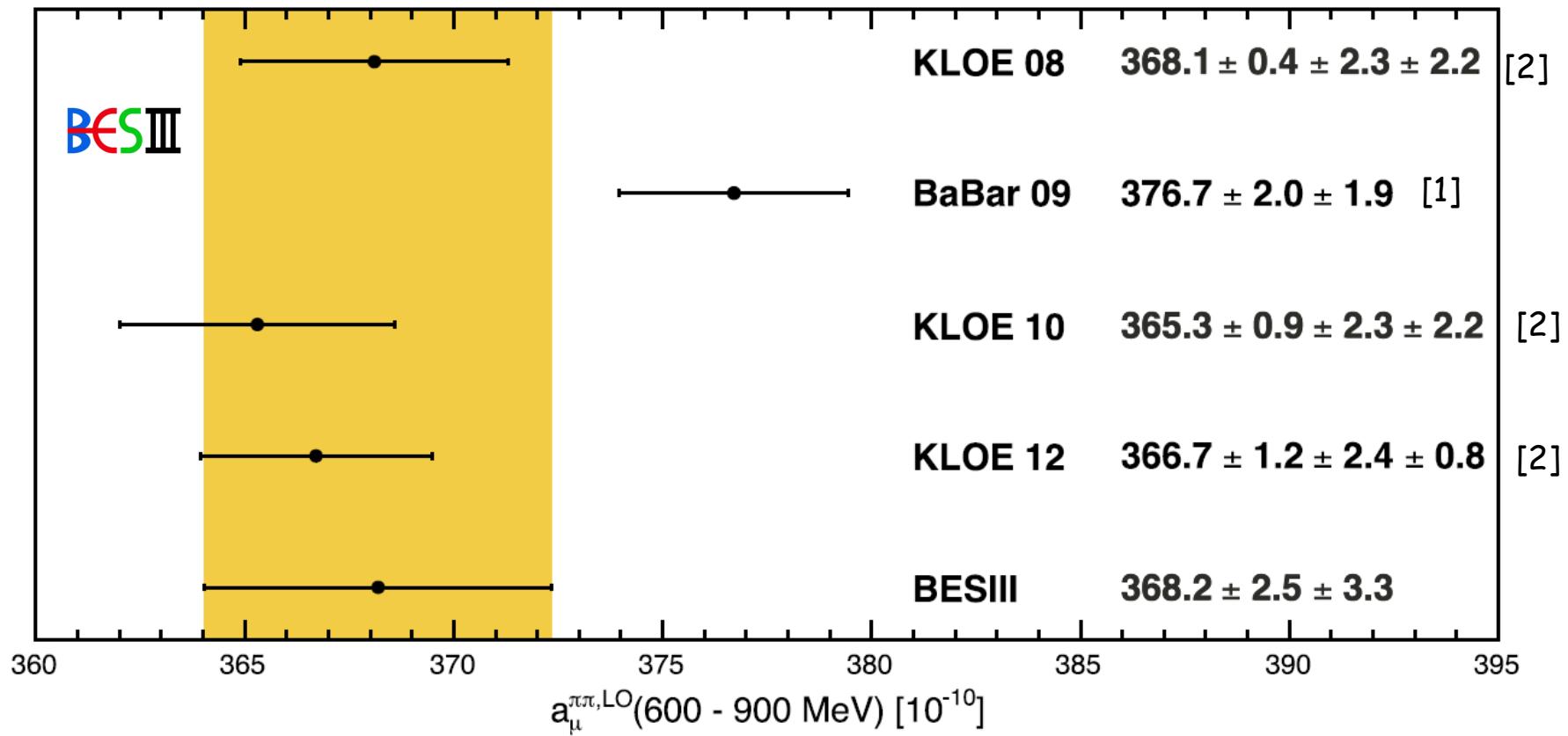
^[1] B. Aubert et al., Phys. Rev. Lett. 103, 231801 (2009).
J.P. Lees et al., Phys. Rev. D86, 032013 (2012)

^[2] F. Ambrosino et al. Phys. Lett. B 670, 285 (2009).
F. Ambrosino et al. Phys. Lett. B 700, 102-110 (2011).
D. Babusci et al. Phys. Lett. B 720, 336-343 (2013).



Contribution of $\pi^+\pi^-$ to $a_\mu^{VP,LO}$

PLB 753, 629 (2016)



- Precision compatible with previous measurements
- $a_\mu^{\pi\pi,LO}(600 - 900 \text{ MeV}) = (368.2 \pm 2.5_{\text{stat}} \pm 3.3_{\text{syst}}) \cdot 10^{-10}$
- Confirmation of deviation of $> 3\sigma$ between experiment and theory

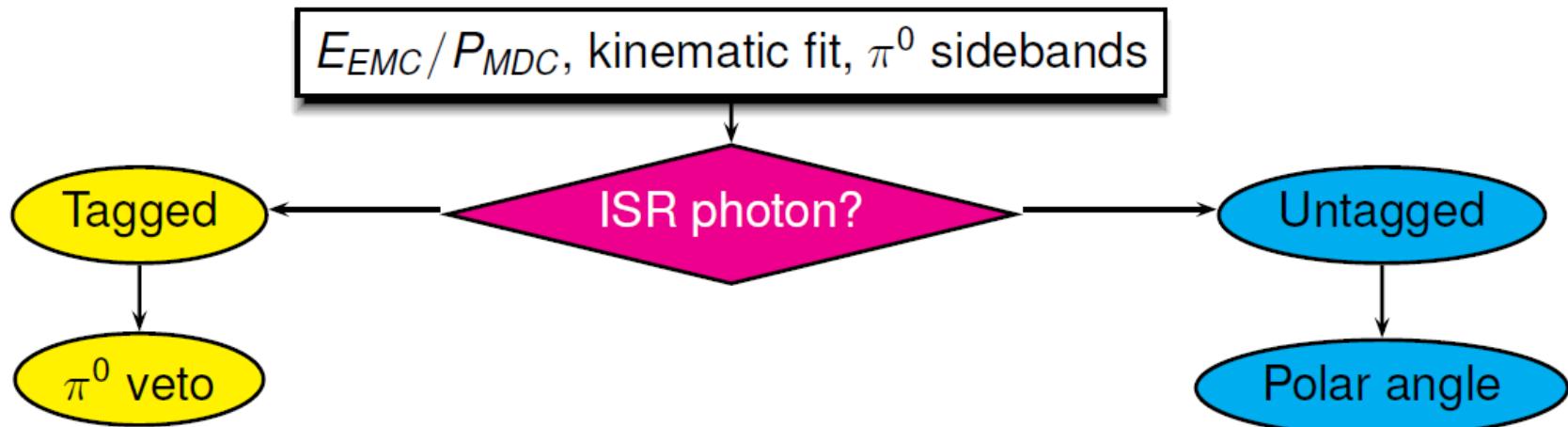
^[1] B. Aubert et al., Phys. Rev. Lett. 103, 231801 (2009). J.P. Lees et al., Phys. Rev. D86, 032013 (2012)

^[2] F. Ambrosino et al. Phys. Lett. B 670, 285 (2009). F. Ambrosino et al. Phys. Lett. B 700, 102-110 (2011).
D. Babusci et al. Phys. Lett. B 720, 336-343 (2013).

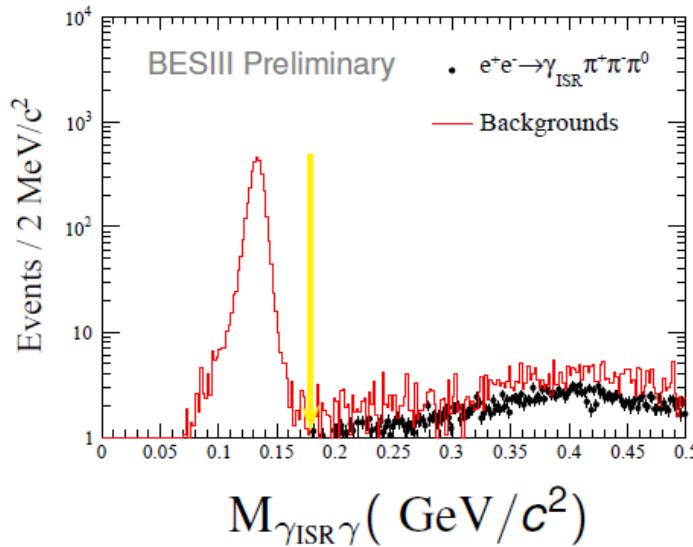
$$e^+e^- \rightarrow \gamma\pi^+\pi^-\pi^0$$

PRELIMINARY

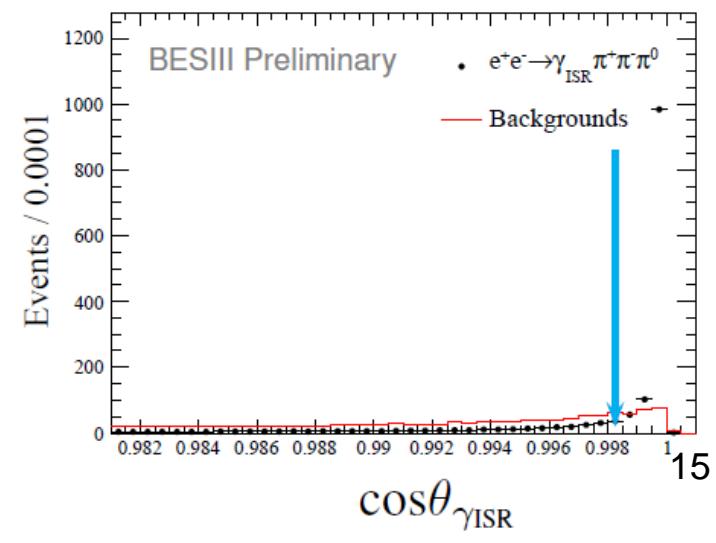
Event Selection



Combination of the ISR photon and any other photon



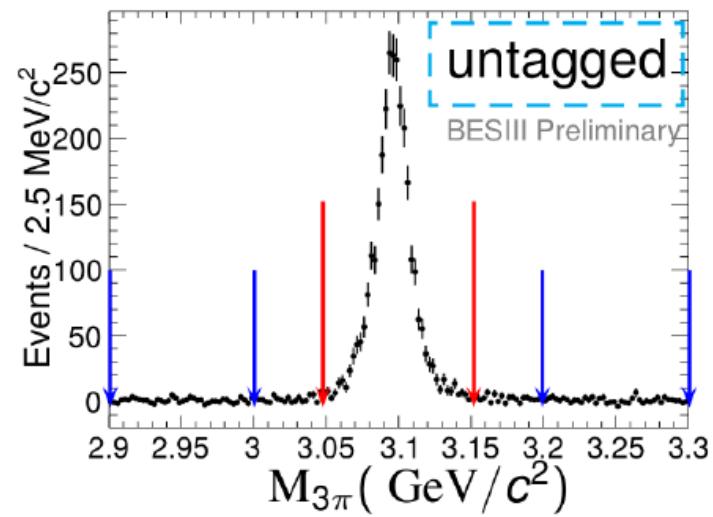
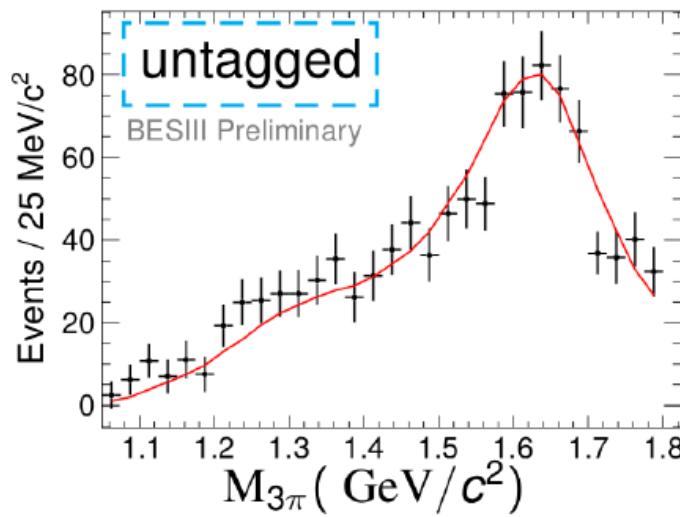
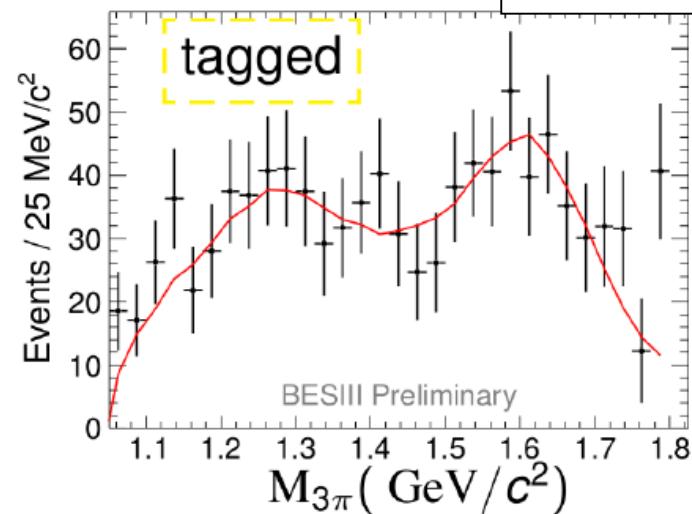
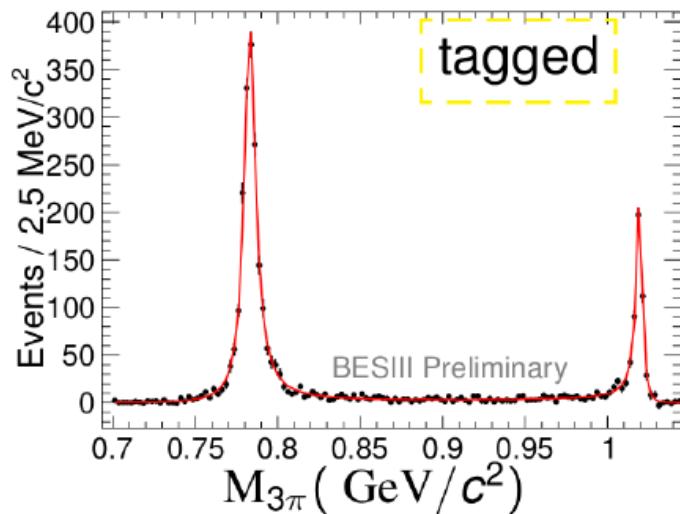
Polar angle of the ISR photon



15

Fit to $\pi^+\pi^-\pi^0$ Mass Spectrum

PRELIMINARY



$$\sigma(m) = \frac{12\pi}{m^3} F_{\rho\pi}(m) \left| \sum_{V=\omega, \phi, \omega', \omega''} \right.$$

$$\left. \frac{\Gamma_V m^{\frac{3}{2}} V \sqrt{\Gamma_V^{ee} \mathcal{B}(V \rightarrow 3\pi)}}{D_V(m)} \frac{e^{i\varphi_V}}{\sqrt{F_{\rho\pi}(m_V)}} \right|^2 \Bigg|^{16}$$

Fit Results of $\gamma\pi^+\pi^-\pi^0$

PRELIMINARY

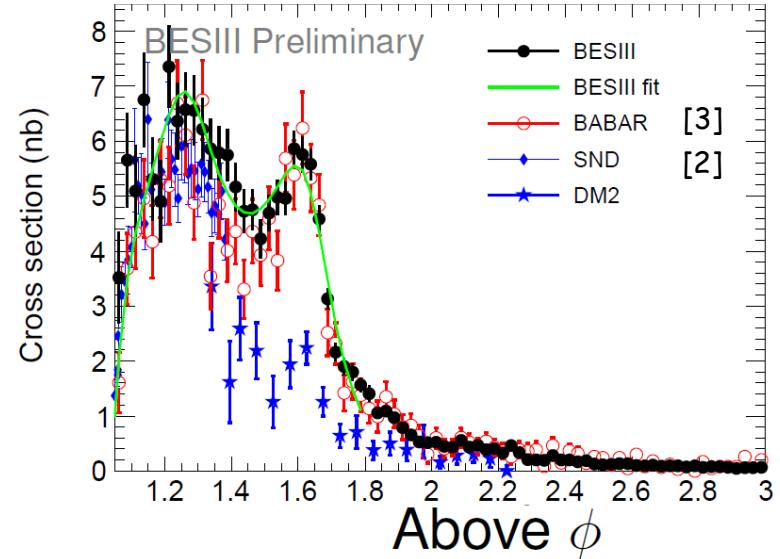
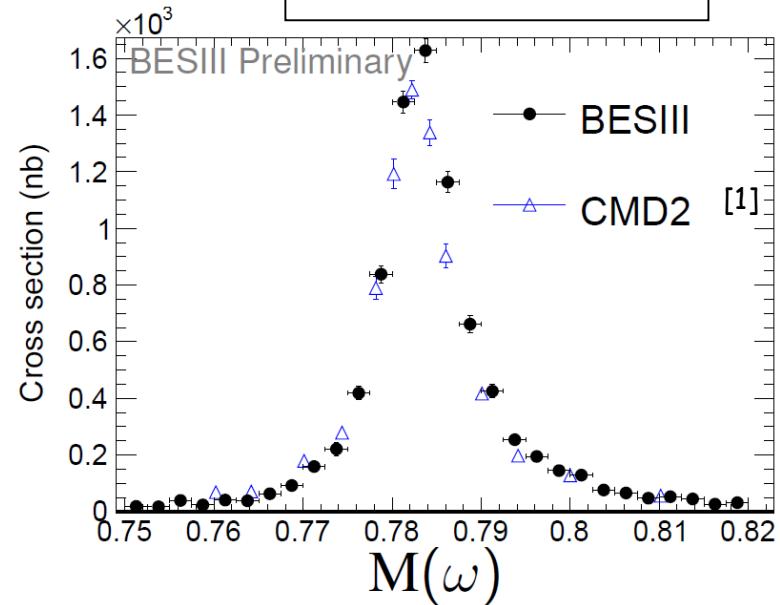
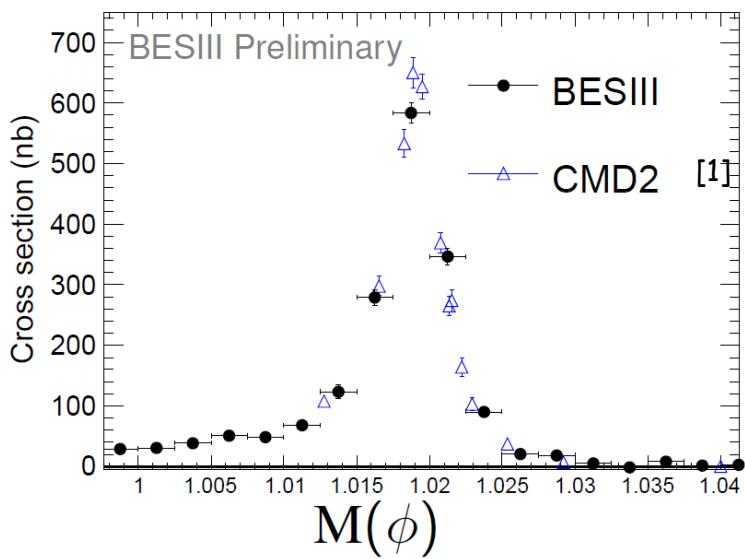
BESIII Preliminary

Parameters	PDG	This result
χ^2/NDF	-	443/390
m_ω (MeV/ c^2)	782.65 ± 0.12	$783.20 \pm 0.07 \pm 0.23$
m_ϕ (MeV/ c^2)	1019.46 ± 0.02	$1020.00 \pm 0.06 \pm 0.30$
$m_{\omega'}$ (MeV/ c^2)	$1400 \sim 1450$	$1388 \pm 39 \pm 52$
$m_{\omega''}$ (MeV/ c^2)	1670 ± 30	$1699 \pm 9 \pm 6$
Γ_ω (MeV/ c^2)	8.49 ± 0.08	PDG
Γ_ϕ (MeV)	4.26 ± 0.04	PDG
$\Gamma_{\omega'}$ (MeV)	$180 \sim 250$	$629 \pm 155 \pm 212$
$\Gamma_{\omega''}$ (MeV)	315 ± 35	$331 \pm 40 \pm 28$
$(\mathcal{B}_{\omega \rightarrow e^+e^-} \times \mathcal{B}_{\omega \rightarrow 3\pi}) (10^{-5})$	6.49 ± 0.11	$6.94 \pm 0.08 \pm 0.17$
$(\mathcal{B}_{\phi \rightarrow e^+e^-} \times \mathcal{B}_{\phi \rightarrow 3\pi}) (10^{-5})$	4.53 ± 0.10	$4.20 \pm 0.08 \pm 0.17$
$(\mathcal{B}_{\omega' \rightarrow e^+e^-} \times \mathcal{B}_{\omega' \rightarrow 3\pi}) (10^{-6})$	0.82 ± 0.08	$0.84 \pm 0.09 \pm 0.09$
$(\mathcal{B}_{\omega'' \rightarrow e^+e^-} \times \mathcal{B}_{\omega'' \rightarrow 3\pi}) (10^{-6})$	1.30 ± 0.20	$1.14 \pm 0.15 \pm 0.15$
$\mathcal{B}_{J/\psi \rightarrow 3\pi} (\%)$	2.11 ± 0.07	$2.18 \pm 0.03 \pm 0.06$

$\pi^+\pi^-\pi^0$ Cross Section

PRELIMINARY

- BESIII results clearly support BABAR measurement
- Improved precision
- Can be used as input for $a_\mu^{3\pi,LO}$



[1] R. R. Akhmetshin et al., Phys. Lett. B 476, 33 (2000). R. R. Akhmetshin et al., Phys. Lett. B 642, 203 (2006).

[2] M. N. Achasov et al., Phys. Rev. D 68, 052006 (2003). M. N. Achasov et al., Phys. Rev. D 66, 032001 (2002).

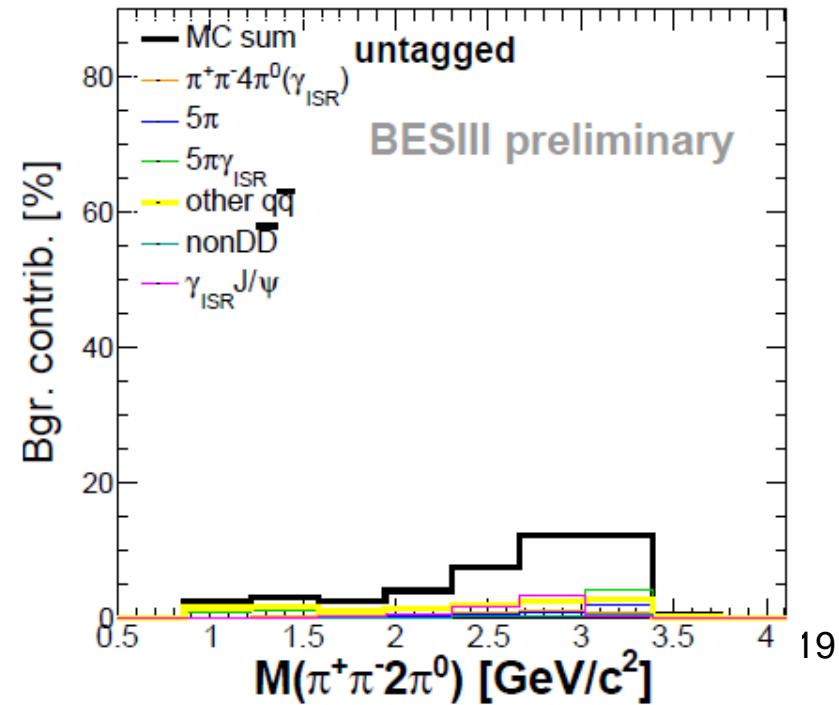
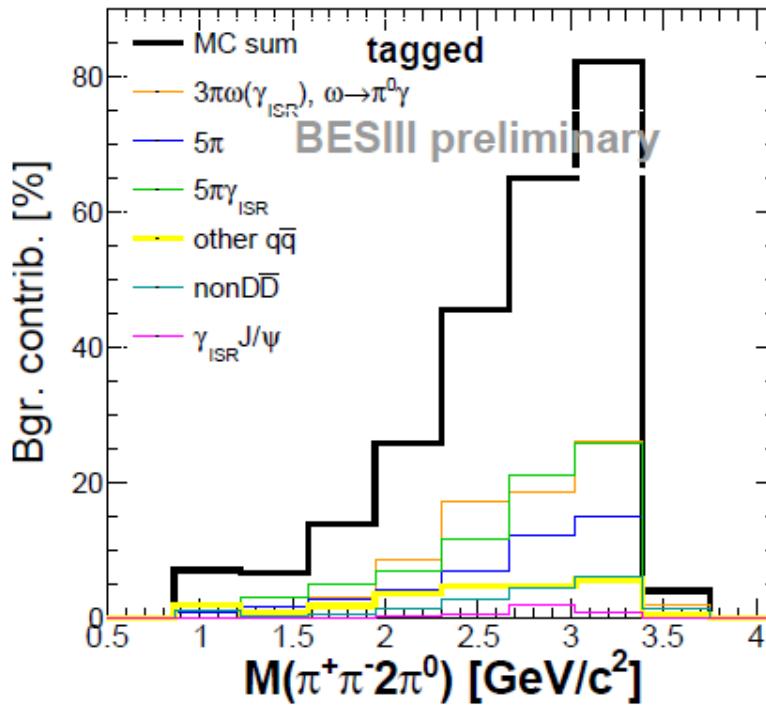
[3] B. Aubert et al., Phys. Rev. D 70, 072004 (2004).

$$e^+e^- \rightarrow \gamma\pi^+\pi^-2\pi^0$$

PRELIMINARY

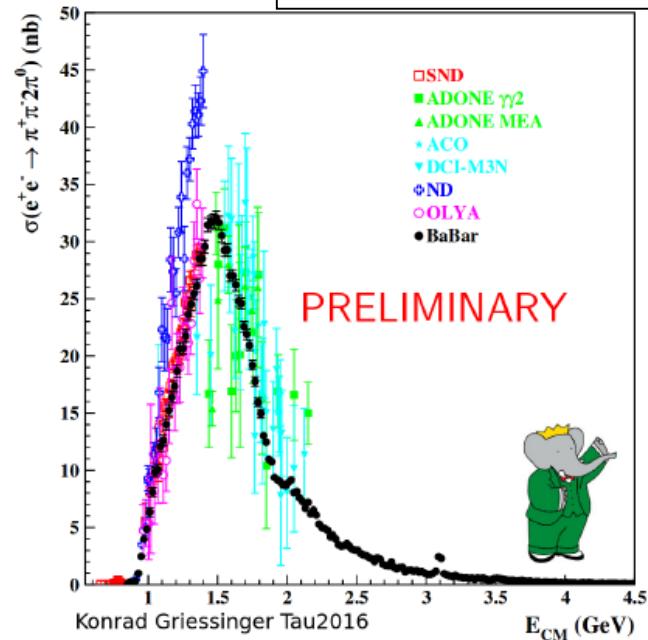
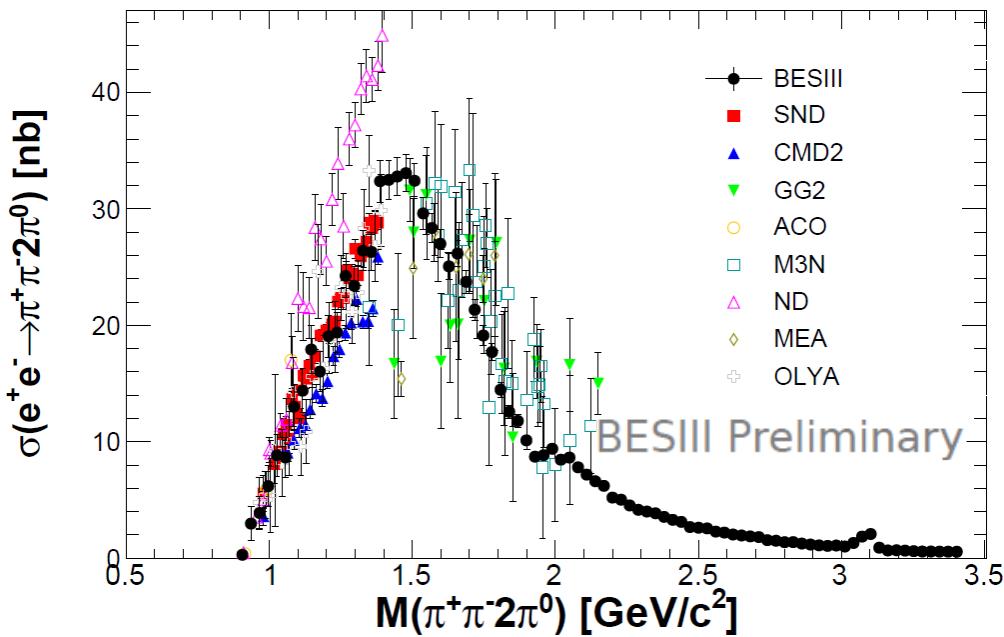
Event Selection

- Tagged and untagged analysis performed separately
- Tagged: kinematic fit, π^0 veto for ISR photon
- Untagged: $|\cos\theta_{\text{ISR}}| > 0.995$
- Main background from $\pi^+\pi^-3\pi^0(\gamma_{\text{ISR}})$
- Partial wave analysis with **HeLPWA** for $\pi^+\pi^-3\pi^0$
- Correct MC background according to data



$\pi^+\pi^-2\pi^0$ Combined Cross Section

PRELIMINARY



- Error: weighted mean of tagged and untagged events
- $\approx 3\%$ precision like BABAR

	$a_\mu^{\pi^+\pi^-2\pi^0[0.92-1.8 \text{ GeV}], LO} / 10^{-10}$
BESIII (preliminary)	$18.63 \pm 0.27 \pm 0.57$
BABAR (preliminary)	$17.9 \pm 0.1 \pm 0.6$

[1] R. R. Akhmetshin et al., Phys. Lett. B 466, 392 (1999).

[2] S. I. Dolinsky et al., Phys. Rept. 202, 99 (1991).

[3] C. Bacci et al., Nucl. Phys. B 184, 31 (1981).

[4] L. M. Kurdadze et al., J. Exp. Theor. Phys. Lett. 43 643 (1986).

[5] M. N. Achasov et al., Preprint BUDKER-INP-2001-34 (Novosibirsk, 2001).

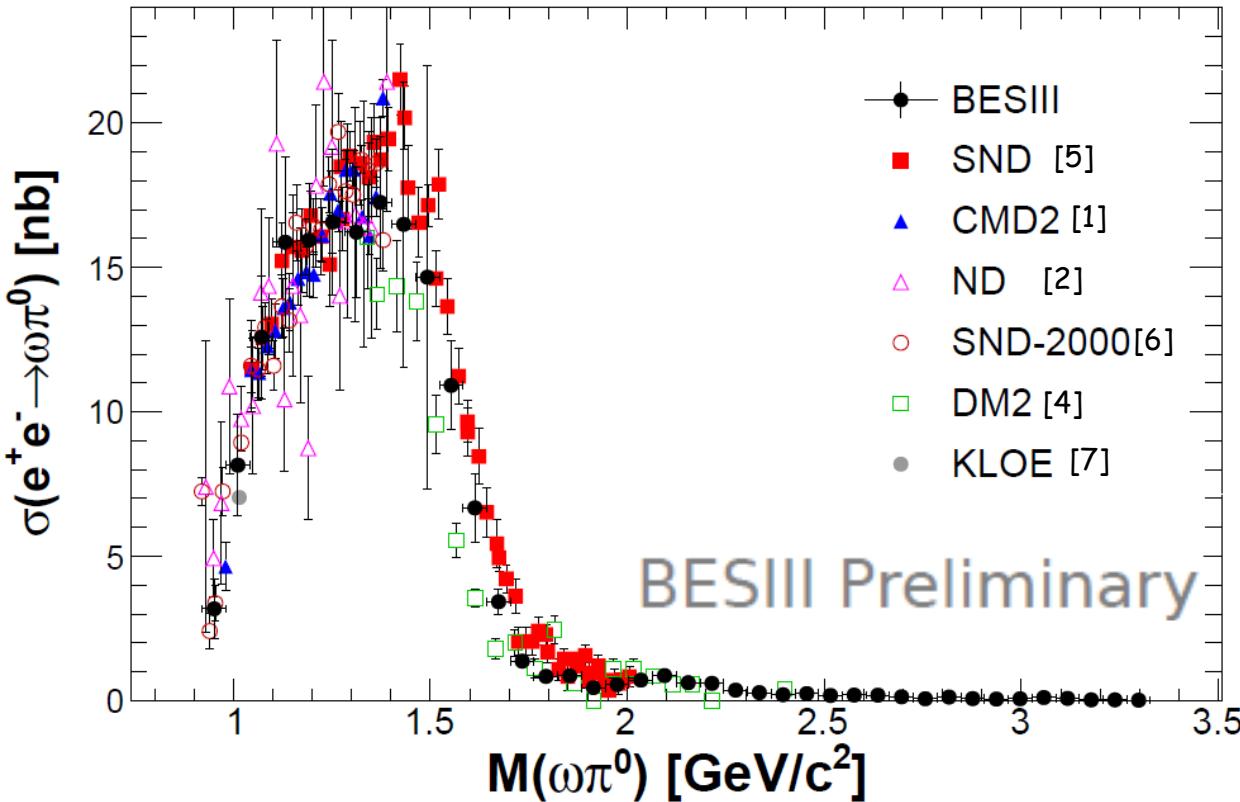
[6] G. Cosme et al., Phys. Lett. B 63, 349 (1976).

[7] G. Cosme et al., Nucl. Phys. B 152 215 (1979).

[8] B. Esposito et al., Lett. Nuovo Cim. 31, 445 (1981).

$\omega\pi^0$ Cross Section

PRELIMINARY



Fit of $M(3\pi)$ distribution with double Gaussian for ω plus third order polynomial for non- ω in each $M(\pi^+\pi^-2\pi^0)$ bin

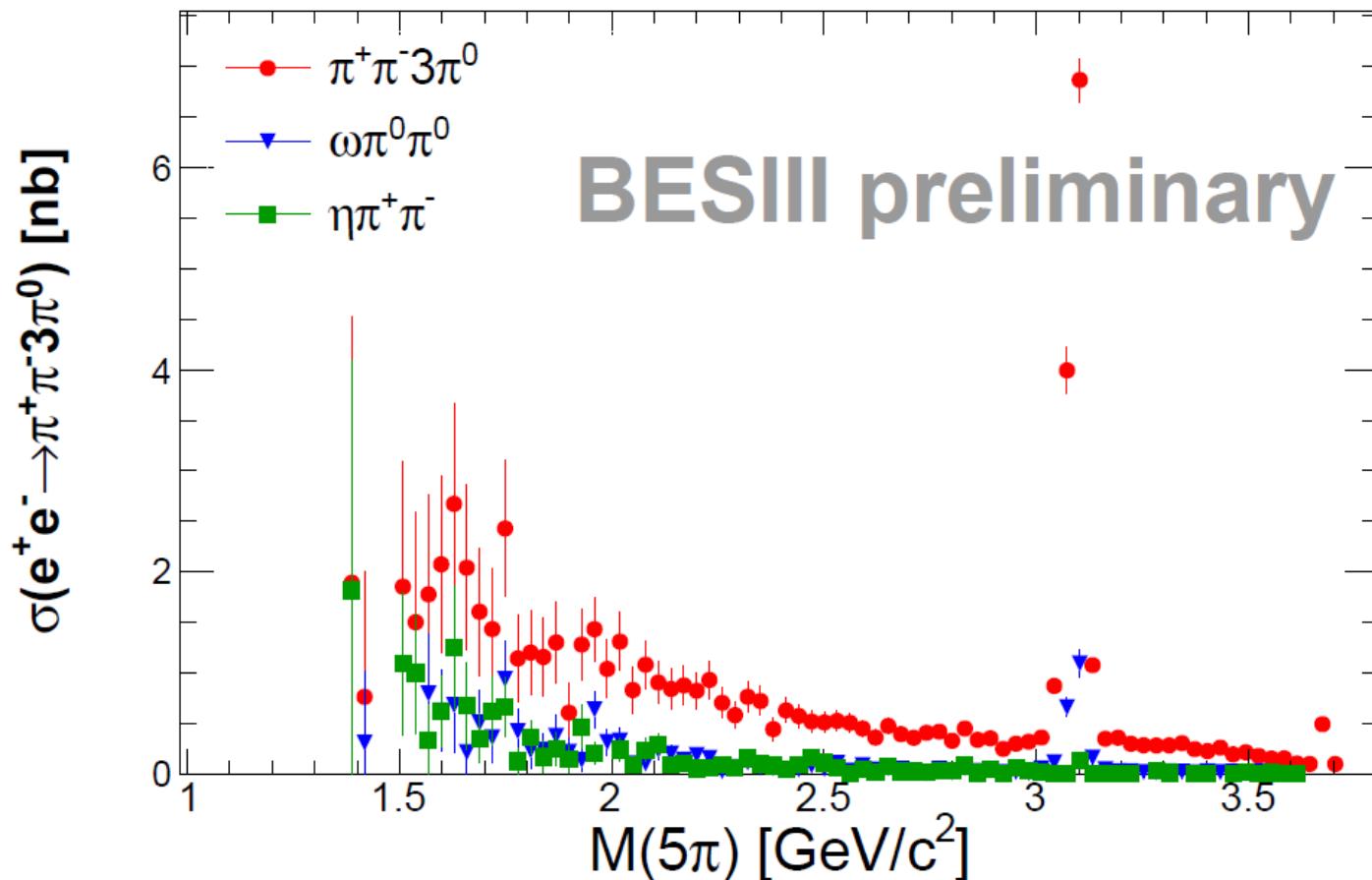
- [1] R. R. Akhmetshin et al., Phys. Lett. B 466, 392 (1999).
- [2] S. I. Dolinsky et al., Phys. Rept. 202, 99 (1991).
- [3] C. Bacci et al., Nucl. Phys. B 184, 31 (1981).
- [4] D. Bisello et al., Preprint LAL-90-35 (Orsay, 1990).

- [5] M. N. Achasov et al., Phys. Lett. B 486, 29 (2000).
- [6] M. N. Achasov et al., arXiv:1610.00235 [hep-ex].
- [7] F. Ambrosino et al., Phys. Lett. B 669, 223 (2008).

$\pi^+\pi^-3\pi^0$ Cross Section

PRELIMINARY

- From $\pi^+\pi^-2\pi^0\gamma_{\text{ISR}}$ background study
- Systematic uncertainty: 13.8%



Hadronic Light-by-Light Contribution

Interaction of virtual mesons with real/virtual photons

a_μ^{hLBL} not directly related to measurable quantities

- Hadronic models

- ChPT at lowest energies
- pQCD at high energies
- Intermediate region?

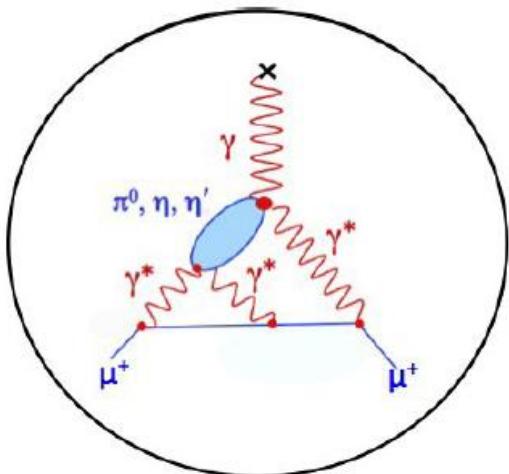
Glasgow Consensus, arXiv:0901.0306
Jegerlehner/Nyffeler, Phys. Rept. 477, 1

- Data driven approaches

- Based on dispersion relations
- Reduce model dependency
- Reliable error estimates

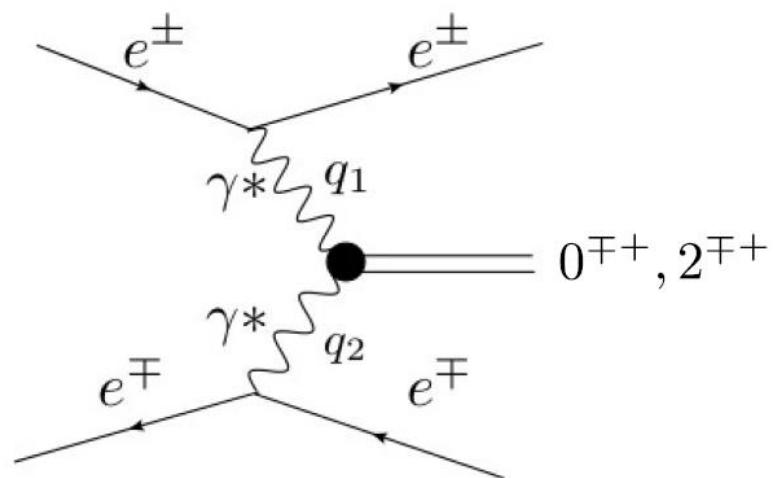
Colangelo, Hoferichter et al. (Bern)
Vanderhaeghen, Pauk et al. (Mainz)

- Transition FF as experimental input



Two-Photon Collisions

- Exchange of 2 photons in e^+e^- collisions
- Pseudoscalar, axial, and tensor states accessible
- $M_x \ll \sqrt{s}$
- $\sigma \propto \alpha^2 \ln^2 E$
- $\sigma \propto F^2(Q_1^2, Q_2^2)$, with $Q_1^2 = -q_i^2$
- Forward peaked kinematic
 - Experimentally challenging
 - Special tagging detectors



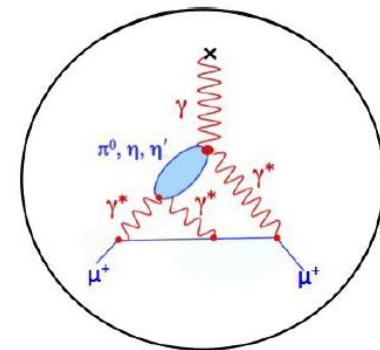
Contributions to a_μ

- Current accuracy of a_μ : $\sim 6.3 \cdot 10^{-10}$
- Contribution of π^0 : $\sim 7 \cdot 10^{-10}$ Knecht, Nyffeler
Phys. Rev. D65, 073034 (2002)
- Expected accuracy of new experiments at FNAL and J-PARC: $\sim 1.6 \cdot 10^{-10}$
- Contribution of η and η' relevant!

$$\eta \sim 1.5 \cdot 10^{-10}$$

Knecht, Nyffeler
Phys. Rev. D65, 073034 (2002)

$$\eta' \sim 1.5 \cdot 10^{-10}$$



Two-photons physics program established at BESIII

Untagged, single-tagged, and double-tagged measurements are ongoing

Summary

- High precision measurements of $\pi^+\pi^-$, $\pi^+\pi^-\pi^0$, $\pi^+\pi^-2\pi^0$ cross sections
Results compatible with previous experiments
Improved BR measurements
Further measurements will reduce the a_μ^{VP} uncertainty
- Near future
Two-photon physics program
Include all BESIII data sets
Investigate more final states ($2\pi^+2\pi^-$, etc...)
- Stay tuned for new results!!

Backup Slides

$\pi^+\pi^-$ Systematic Uncertainties

Source	Uncertainty (%)
Photon efficiency correction	0.2
Pion tracking efficiency correction	0.3
Pion ANN efficiency correction	0.2
Pion e-PID efficiency correction	0.2
ANN	negl.
Angular acceptance	0.1
Background subtraction	0.1
Unfolding	0.2
FSR correction δ_{FSR}	0.2
Vacuum polarisation correction δ_{vac}	0.2
Radiator function	0.5
Luminosity \mathcal{L}	0.5
Sum	0.9

$\pi^+\pi^-\pi^0$ Systematic Uncertainties

BESIII Preliminary

Data samples	Data I		Data II	
Source	Tagged	Untagged	Tagged	Untagged
Tracking	0.4-1.0	0.4-0.9	0.4-0.7	0.4-0.7
Photon reconstruction	0.9	0.6	0.9	0.6
E/P	0.7-0.9	0.4	0.4	0.4
π^0 side band	0.6-0.9	0.4	0.4	0.4
Kinematic fit (χ^2 cut)	1.0-1.4	0.4	0.6	0.4
Veto π^0 for γ_{ISR}	0.6	-	0.5-1.0	-
$\cos \theta_{\gamma_{\text{ISR}}}^{2C}$	-	1.5	-	1.5
Vertex	-	0.2	-	0.2
BG subtraction	0.0-19	0-12	0.04-26	0-6.1
Vacuum polarization	0.02-0.23	0.02-0.07	0.02-0.23	0.02-0.07
Unfolding	0.91-1.7	1.3	0.61-0.93	0.77
Radiative function	0.5	0.5	0.5	0.5
Luminosity	1.1	1.1	1.1	1.1
Total	> 2.4	> 2.6	> 2.0	> 2.4

in unit [%]

- Systematic error < 2% in the resonance regions

$\pi^+\pi^-2\pi^0$ Systematic Uncertainties

- Background uncertainties are mass dependent

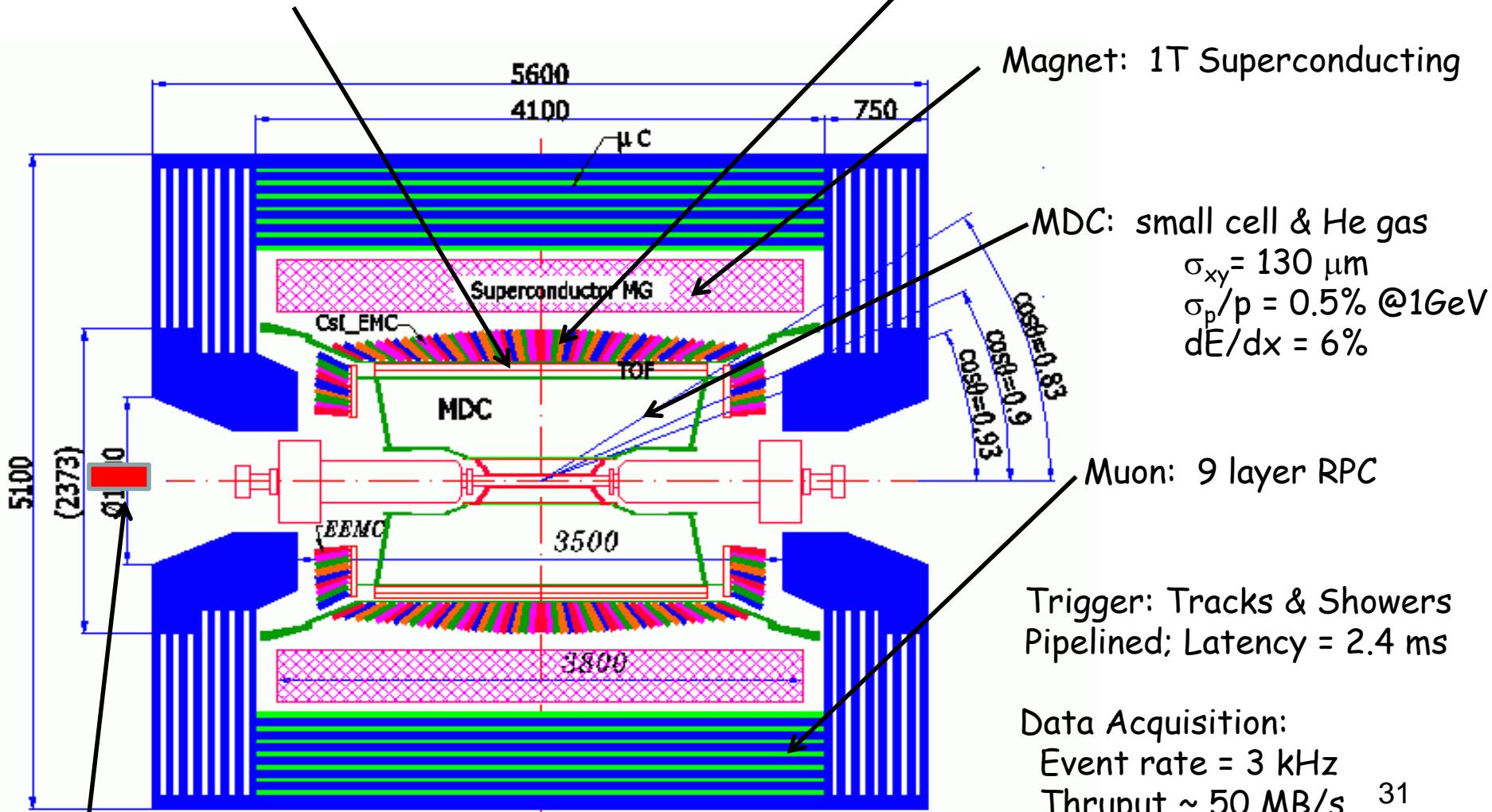
Region	Mass range [GeV]
R1	$0.5 < M(4\pi) < 1.5$
R2	$1.5 < M(4\pi) < 2.0$
R3	$2.0 < M(4\pi) < 3.0$
R4	$3.0 < M(4\pi) < 3.8$

Source	Tagged [%]				Untagged [%]			
	R1	R2	R3	R4	R1	R2	R3	R4
Luminosity		0.50				0.50		
Tracking		0.60				0.60		
VP correction		0.05				0.05		
FSR correction		0.20				0.20		
Radiator Function		0.50				0.50		
ISR Photon Eff.		0.30				-		
π^0 Eff.		2.57				2.52		
Signal Eff.		0.58				0.61		
Kin. fit		0.42				0.45		
Event selection	0.60		1.46			0.64		
Bgr. Subrt. 5π	0.01	0.13	2.47	3.23	0.00	0.01	0.08	0.15
Bgr. Subrt. $5\pi\gamma_{ISR}$	0.48	0.47	7.77	10.27	0.59	0.25	0.65	0.71
Bgr. Subrt. $q\bar{q}$	0.50	0.98	12.68	21.05	0.58	0.22	0.82	0.76
Bgr. Subrt. other	0.05	0.14	2.31	5.34	0.01	0.02	0.30	0.32
ω fits (only for $\omega\pi^0$)		2.26				2.26		
$\pi^+\pi^-2\pi^0$ Total	2.97	3.09	15.58	24.45	2.95	2.85	3.04	3.04
$\omega\pi^0$ Total	3.80	4.84	7.71	3.73	3.91	3.70	4.48	3.68

BESIII Detector

TOF:
 $\sigma_T = 80 \text{ ps}$ Barrel
 110 ps Endcap

EMC: CsI crystals, 28 cm
 $\Delta E/E = 2.5\% @ 1 \text{ GeV}$
 $\sigma_z = 0.6 \text{ cm}/\sqrt{E}$



Magnet: 1T Superconducting

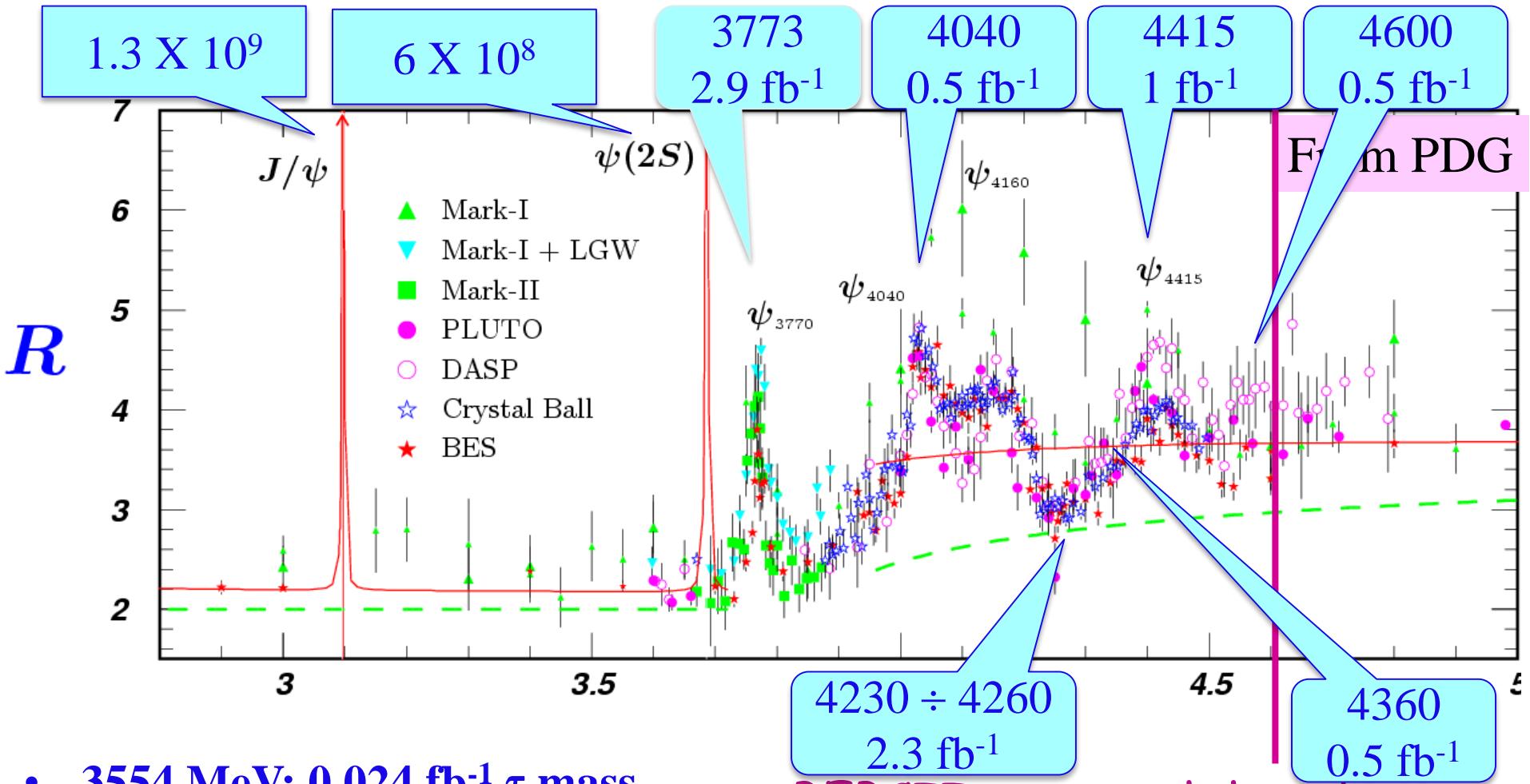
MDC: small cell & He gas
 $\sigma_{xy} = 130 \mu\text{m}$
 $\sigma_p/p = 0.5\% @ 1 \text{ GeV}$
 $dE/dx = 6\%$

Muon: 9 layer RPC

Trigger: Tracks & Showers
Pipelined; Latency = 2.4 ms

Data Acquisition:
Event rate = 3 kHz
Thruput $\sim 50 \text{ MB/s}$

BESIII Production of Charmonium(like) states



- 3554 MeV: 0.024 fb⁻¹ τ mass
- 4100 ÷ 4400 MeV: 0.5 fb⁻¹ coarse scan
- 3850 ÷ 4590 MeV: 0.5 fb⁻¹ fine scan

BEPCII can reach here!

BESIII: Baryon Production

- Charmonium decays offer complementary information to existing data
 - Coupling of unobserved states through conventional production channels could be small, but coupling may be large to $gggN$:
- $\psi \rightarrow N\bar{N} (\pi/\eta/\eta'/\omega/\varphi), \bar{p}\Sigma\pi, \bar{p}\Lambda K$
- High statistics available at BESIII

