

# Nucleon resonances in $\gamma p \rightarrow K^{*+} \Lambda$

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# Outline

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- Why  $\gamma p \rightarrow K^{*+} \Lambda$ ?
- Current experimental & theoretical status
- Our approach
- Results & discussions
- Summary

# Why $\gamma p \rightarrow K^{*+} \Lambda$ ?

- Extraction N\*'s from data & understanding their nature are essential to our understanding of NPQCD
- Our current knowledge of most of the N\*'s is coming from  $\pi N \rightarrow \pi N$  &  $\gamma N \rightarrow \pi N$ 

“missing N\*'s problem”
- Quark models predict more N\*'s than found
- N\*'s may couple weakly to  $\pi N$  but strongly to other channels
- $K^{*+}\Lambda$  threshold higher than that of  $\pi N$ : more suited to study N\*'s with higher masses
- $K^{*+}\Lambda$  has isospin 1/2: “isospin filter”

# Experimental status

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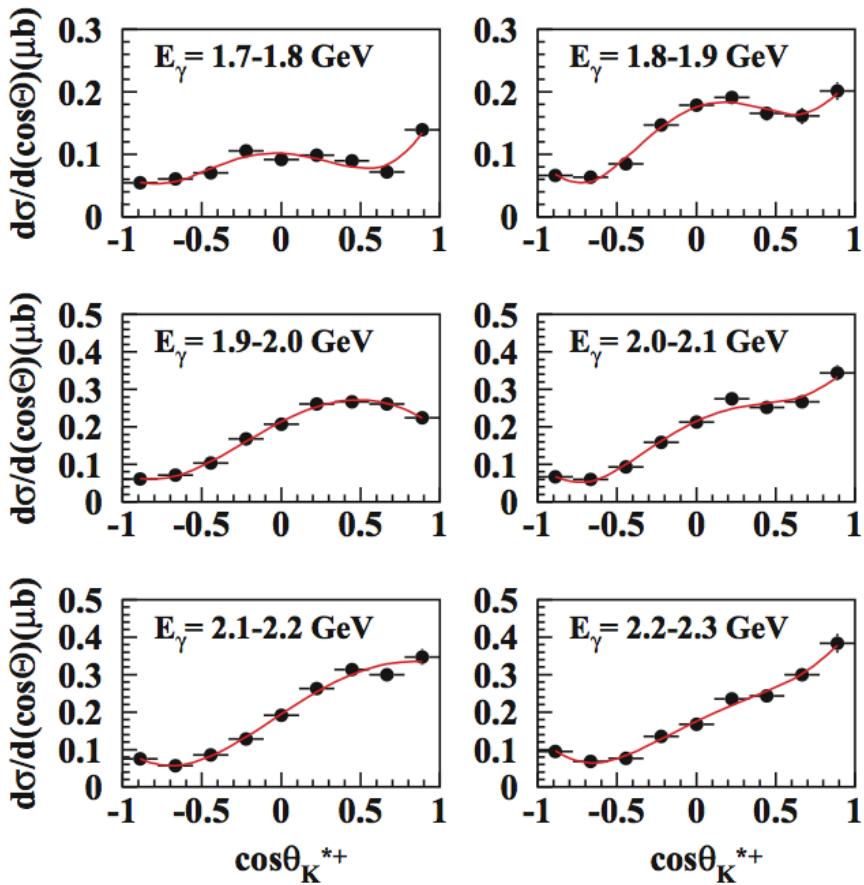
Available data for  $\gamma p \rightarrow K^{*+} \Lambda$  all reported by CLAS@JLab:

- ① Preliminary  $\sigma$  from threshold up to 2.85 GeV:  
L. Guo et al. [CLAS Collaboration], NSTAR 2005 proceedings
- ② Preliminary  $d\sigma/d\Omega$ ,  $W = 2.22 \sim 2.42$  GeV:  
K. Hicks et al. [CLAS Collaboration], MENU 2010 proceedings
- ③ High statistics  $d\sigma/d\Omega$  &  $\sigma$ , from threshold up to  $W \sim 2.85$  GeV:  
W. Tang et al. [CLAS Collaboration], PRC 87, 065204 (2013)

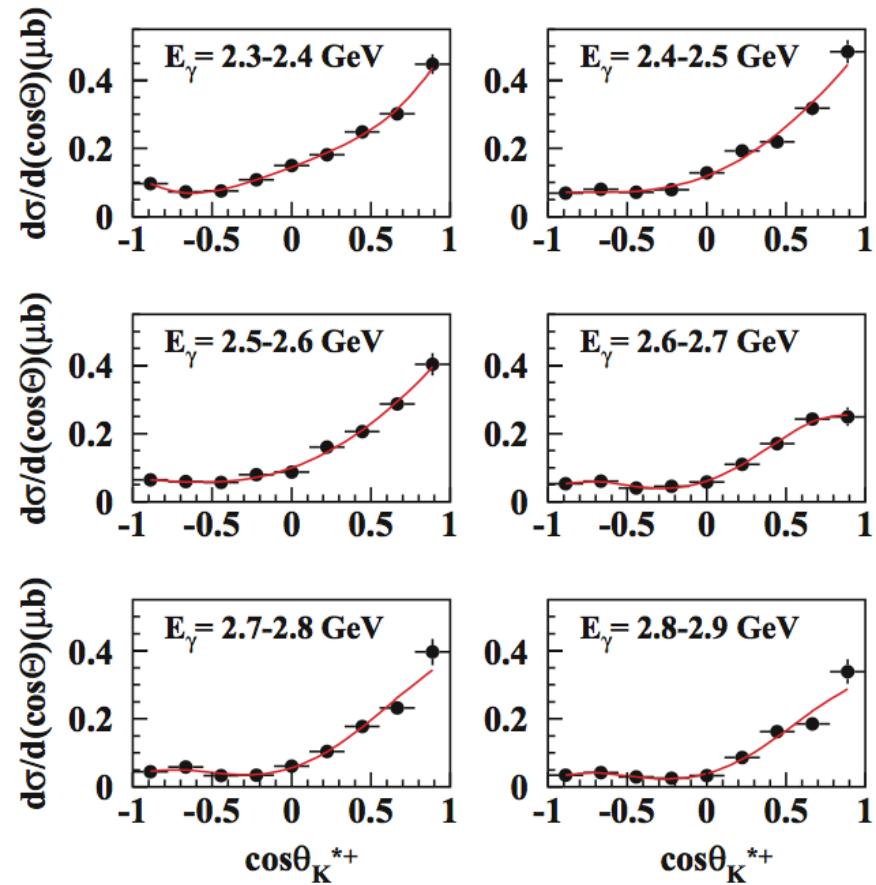
# High statistics data from CLAS

W. Tang et al. [CLAS Collaboration], Phys. Rev. C 87 (2013) 065204.

W: 2.04~2.26 GeV



W: 2.30~2.50 GeV



# **N<sup>\*</sup>'s near K<sup>\*</sup>Λ threshold**

C. Patrignani et al. (Particle Data Group), Chin. Phys. C 40 (2016) 100001.

N <sup>*</sup>	Status	Mass	Width
N(2000)5/2 <sup>+</sup>	**		
N(2040)3/2 <sup>+</sup>	*		
N(2060)5/2 <sup>-</sup>	**		
N(2100)1/2 <sup>+</sup>	*	~2100	
N(2120)3/2 <sup>-</sup>	**	~2120	
N(2190)7/2 <sup>-</sup>	****	2100~2200	300~700

Four-star N<sup>\*</sup> needs further investigation to improve the accuracy of its parameters;  
One- or two-star N<sup>\*</sup>'s need more information to improve the evidences of their existences and to extract their parameters.

# Theoretical status

Based on  $\sigma$  &  $d\sigma/d\Omega$  reported at NSTAR 2005 & MENU 2010

- ① Y. Oh & H. Kim, PRC 73 (2006) 065202.
- ② Y. Oh & H. Kim, PRC 74 (2006) 015208.
- ③ S. Ozaki, H. Nagahiro, & A. Hosaka, PRC 81 (2010) 035206.
- ④ S. H. Kim, S. Nam, Y. Oh, & H. C. Kim, PRD 84 (2011) 114023.

Based on high statistics  $d\sigma/d\Omega$  &  $\sigma$  from PRC 87 (2013) 065204

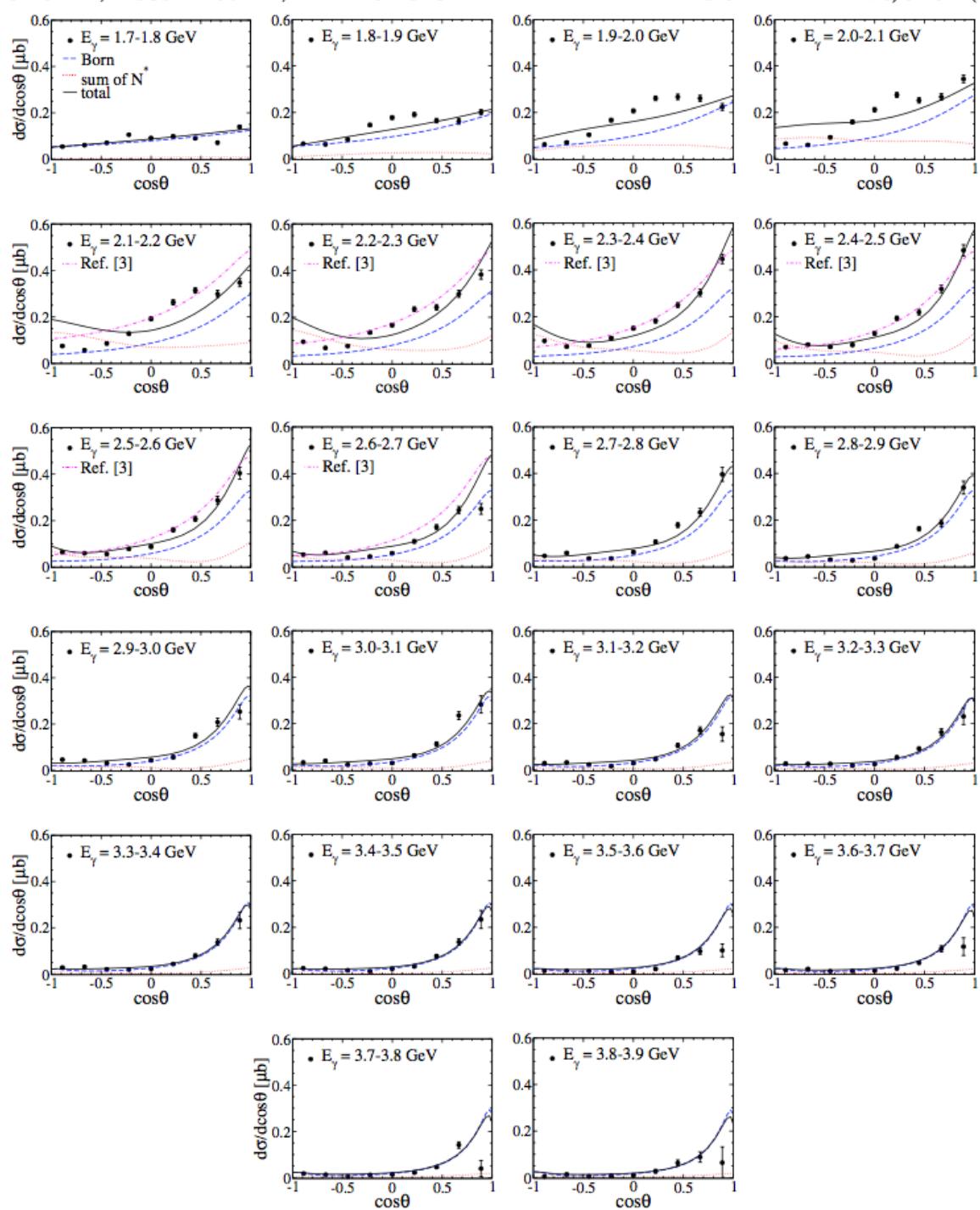
- ⑤ S. H. Kim, A. Hosaka, & H. C. Kim, PRD 90 (2014) 014021.  
N(2000)5/2<sup>+</sup>, N(2060)5/2<sup>-</sup>, N(2120)3/2<sup>-</sup>, N(2190)7/2<sup>-</sup>
- ⑥ B.-G. Yu, Y. Oh, and K.-J. Kong, PRD 95 (2017) 074034.  
Regge approach, no resonance, focus on t-channel K\*

N(2000) $5/2^+$

N(2060) $5/2^-$

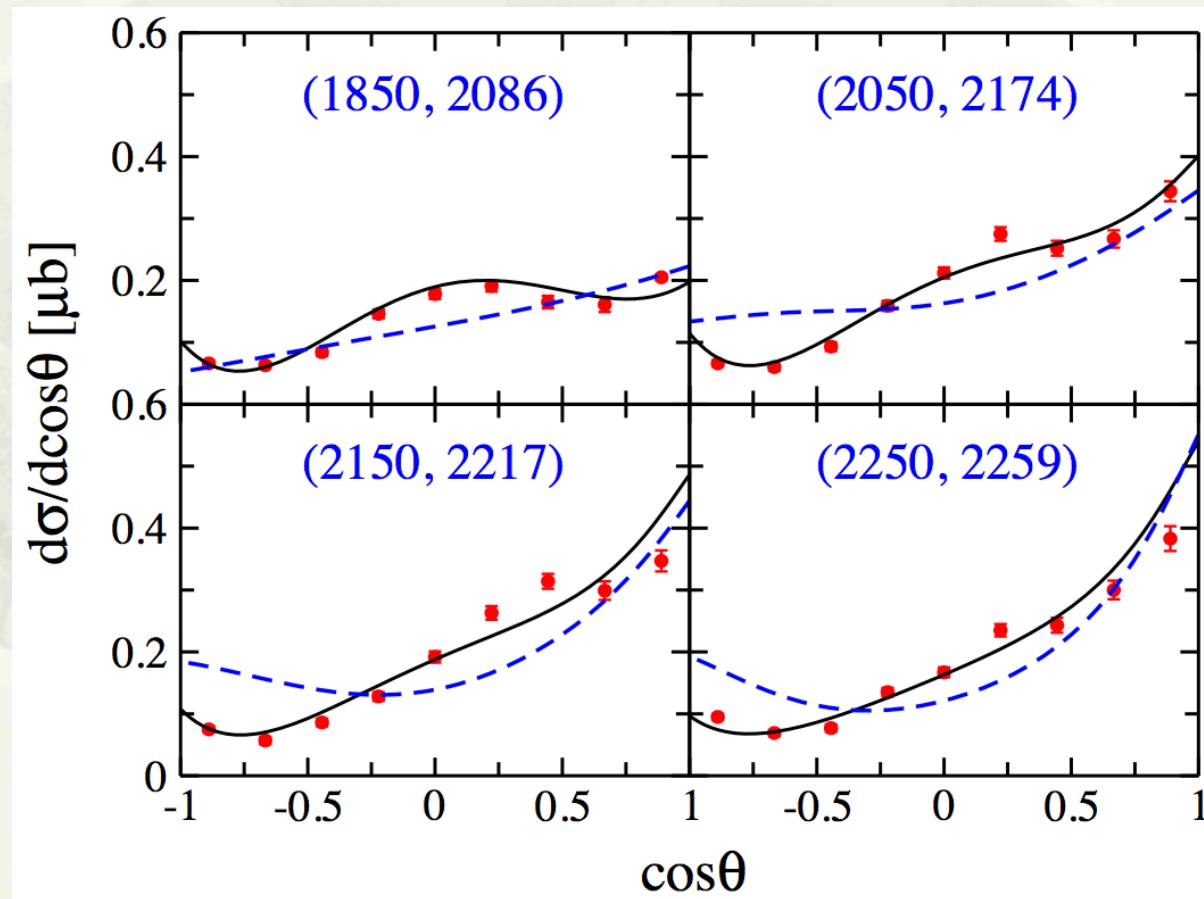
N(2120) $3/2^-$

N(2190) $7/2^-$



# Rooms to be improved

- - - S. H. Kim, A. Hosaka, & H. C. Kim, PRD 90 (2014) 014021
- Our results (will be discussed later)



# Aims of our work

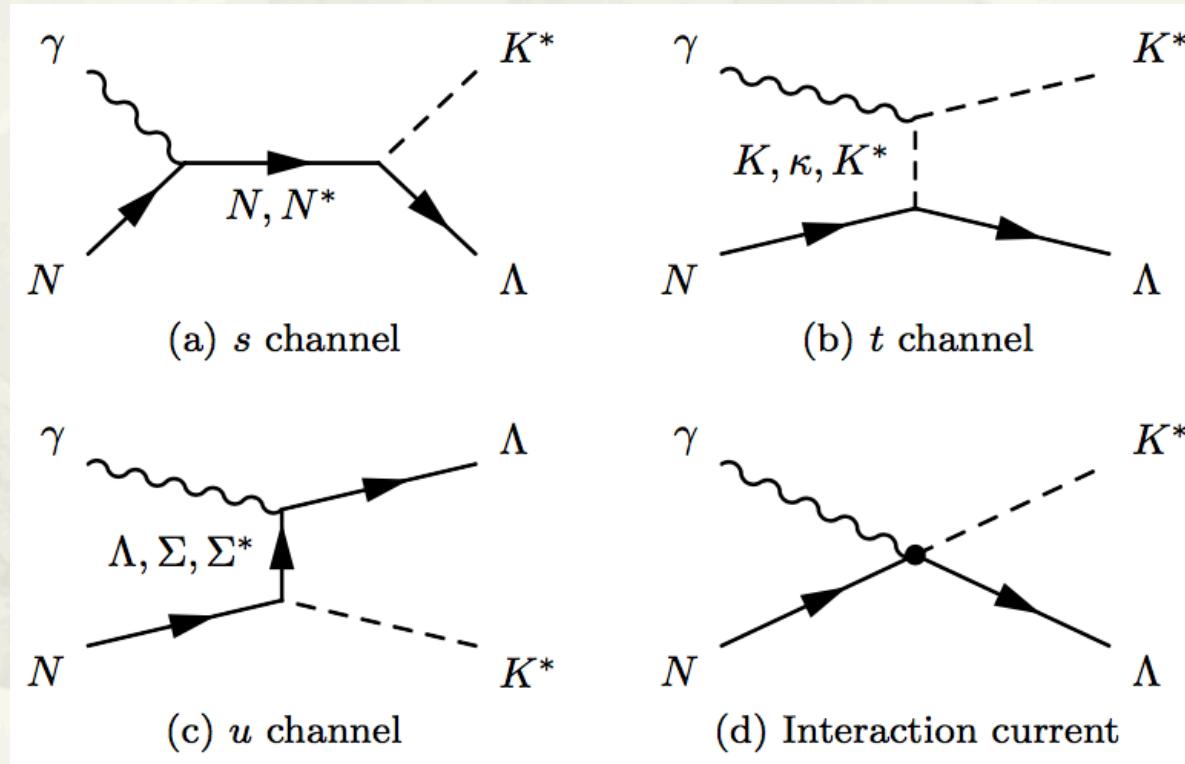
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Perform a better description of the data, and then answer the following questions:

- What's the reaction mechanism of  $\gamma p \rightarrow K^{*+} \Lambda$ ?
- How many  $N^*$ 's are really needed to describe the data?
- What are the associated resonances parameters?

# Our Model

A.C. Wang, W.L. Wang, F. Huang, H. Haberzettl, K. Nakayama, arXiv: 1704.04562



**s-, t-, u-channel diagrams can be calculated straightforwardly;  
The exact calculation of the interaction current is impractical**

# Prescription for gauge invariance

Full amplitude:

$$M^{\nu\mu} = M_s^{\nu\mu} + M_t^{\nu\mu} + M_u^{\nu\mu} + M_{\text{int}}^{\nu\mu}$$

Interaction current:

$$M_{\text{int}}^{\nu\mu} = \Gamma_{\Lambda N K^*}^\nu(q) C^\mu + M_{\text{KR}}^{\nu\mu} f_t.$$

Kroll-Ruderman term:

$$M_{\text{KR}}^{\nu\mu} = g_{\Lambda N K^*} \frac{\kappa_{\Lambda N K^*}}{2M_N} \sigma^{\nu\mu} Q_{K^*}$$

Auxiliary current:

$$C^\mu = -Q_{K^*} \frac{f_t - \hat{F}}{t - q^2} (2q - k)^\mu - Q_N \frac{f_s - \hat{F}}{s - p^2} (2p + k)^\mu$$

$$\hat{F} = 1 - \hat{h} (1 - f_s) (1 - f_t)$$

# Strategy of choosing resonances

**Strategy:** Introduce  $N^*$ 's as few as possible to fit the data

$N^*$ 's near  $K^{*+}\Lambda$  threshold in PDG 2016:

$N^*$	Status	Mass	Width
$N(2000)5/2^+$	**		
$N(2040)3/2^+$	*		
$N(2060)5/2^-$	**		
$N(2100)1/2^+$	*	$\sim 2100$	
$N(2120)3/2^-$	**	$\sim 2120$	
$N(2190)7/2^-$	****	$2100\sim 2200$	$300\sim 700$

We allow all of them and perform numerous trials with different number of  $N^*$ 's and different combination of them.

# How many N\*'s are really needed?

**Strategy:** Introduce N\*'s as few as possible

- **1 N\*:** Data cannot be described. Particularly, the shape of angular distribution near threshold cannot be reproduced
- **2 N\*'s:** 5 among 15 sets can well describe the data

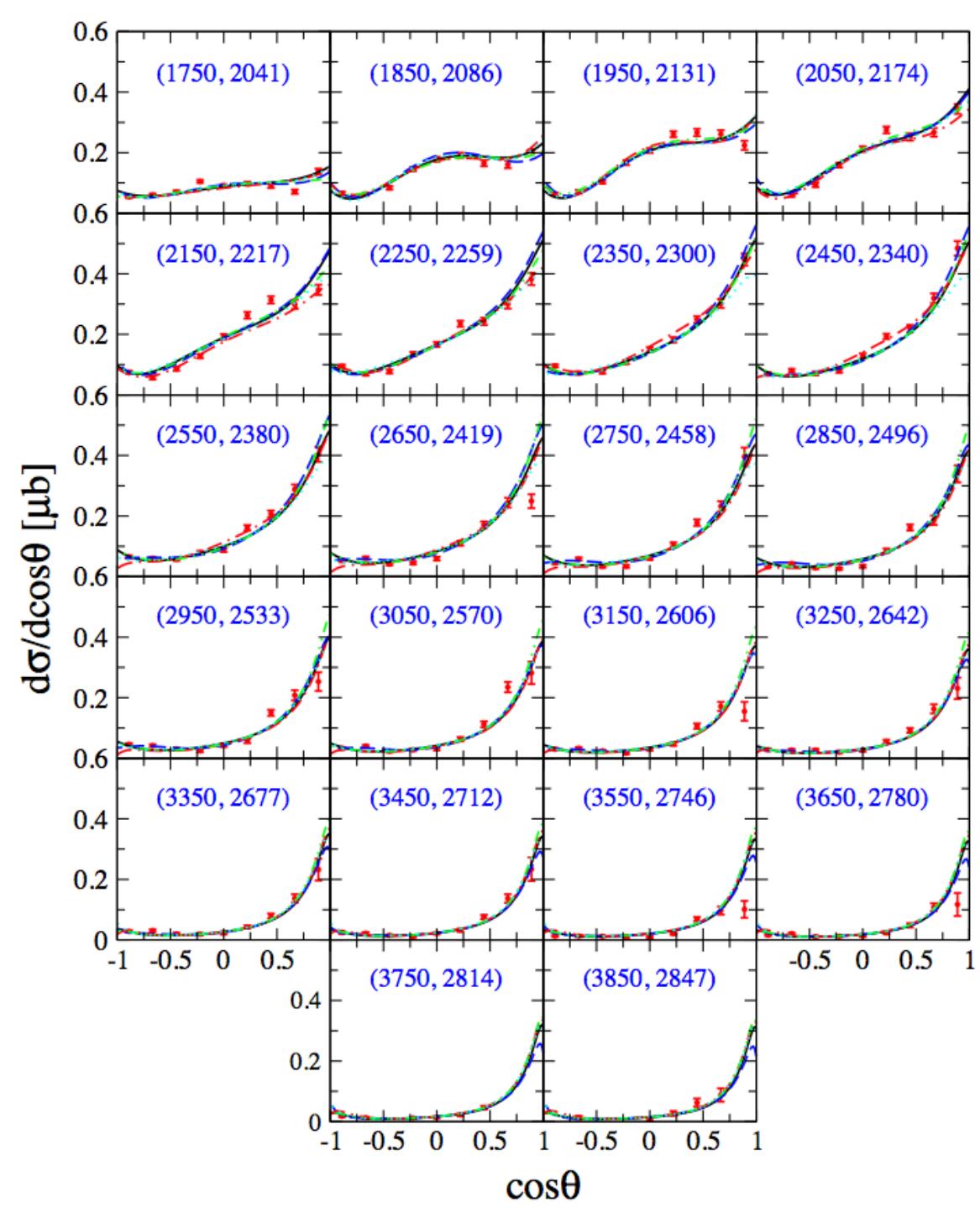
$N(2060)5/2^- + \text{one of}$

$N(2000)5/2^+$ ,  $N(2040) 3/2^+$ ,  $N(2100)1/2^+$ ,  $N(2120)3/2^-$ ,  $N(2190)7/2^-$

- **3 N\*'s:**  $\chi^2$  improves less than 12%

Analysis with 3 or more N\*'s postponed until  
data for spin observables become available

**Conclusion:** One needs at least 2 N\*'s to describe the high statistics differential cross section data from CLAS

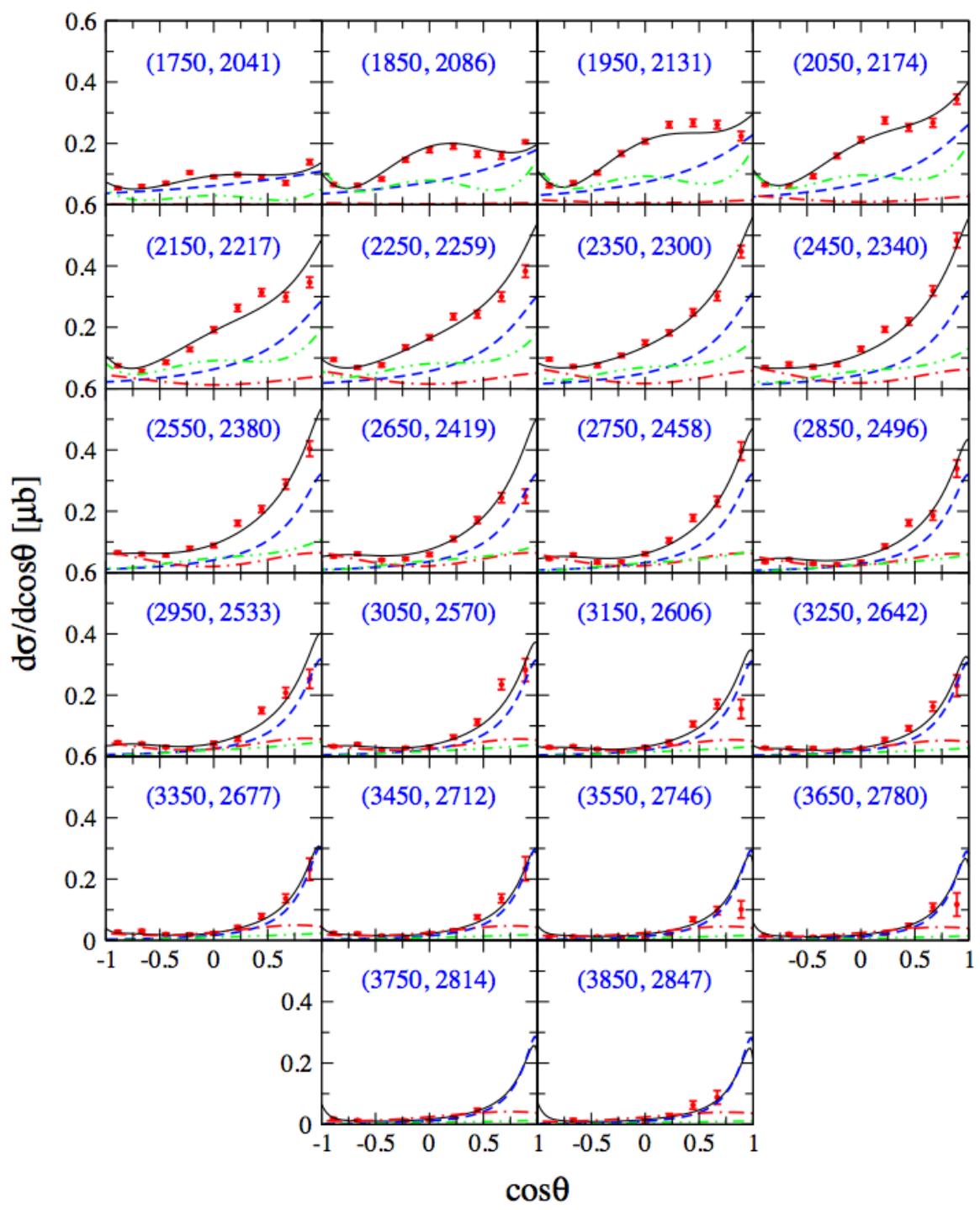


A.C. Wang, W.L. Wang, F. Huang,  
H. Haberzettl, K. Nakayama,  
arXiv: 1704.04562

- Data can be described by 2  $N^*$ 's
- 5 acceptable fits
- Differences are seen at forward & backward angles where data are sparse

# Extracted N\*'s parameters

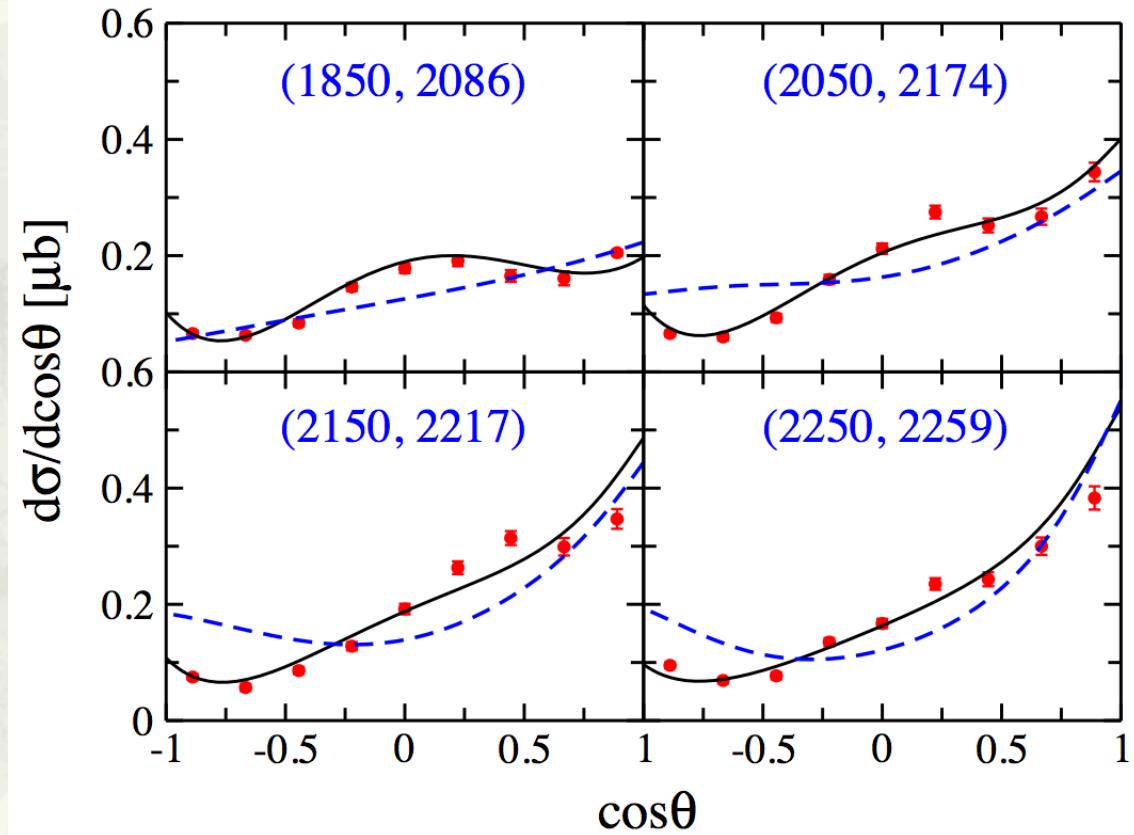
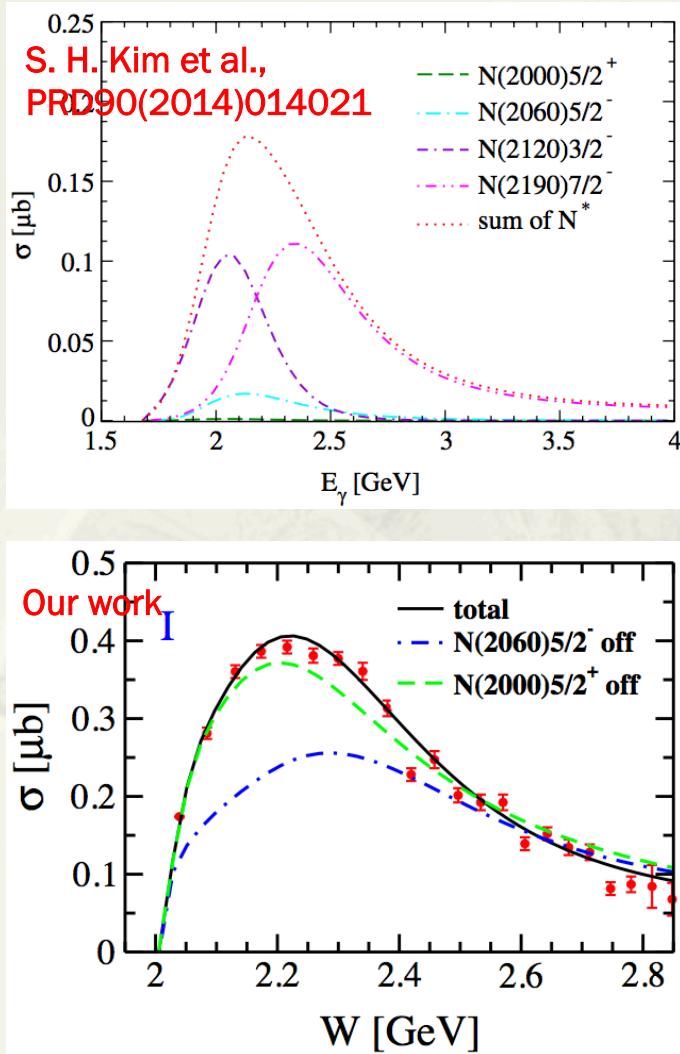
PDG	ratings	I	II	III	IV	V
$N(2060)5/2^-$	**	$2033 \pm 2$ $65 \pm 4$	$2009 \pm 5$ $213 \pm 20$	$2032 \pm 3$ $81 \pm 8$	$2043 \pm 4$ $202 \pm 16$	$2038 \pm 3$ $77 \pm 8$
$N(2000)5/2^+$	**	$2115 \pm 22$ $450 \pm 10$				
$N(2040)3/2^+$	*		$2200 \pm 62$ $540 \pm 7$			
$N(2120)3/2^-$ [~2120]	**			$2203 \pm 9$ $433 \pm 33$		
$N(2190)7/2^-$ [2100~2200] [300~700]	****				$2243 \pm 6$ $450 \pm 33$	
$N(2100)1/2^+$ [~2100]	*					$2100 \pm 15$ $450 \pm 9$



— total  
 - - - K  
 - · - N(2060) $5/2^-$

- K dominates the cross sections at high energy
- N(2060) $5/2^-$ : significant contributions
- Near threshold shape: Interference of K & N(2060) $5/2^-$

# Contribution of N(2060) $5/2^-$



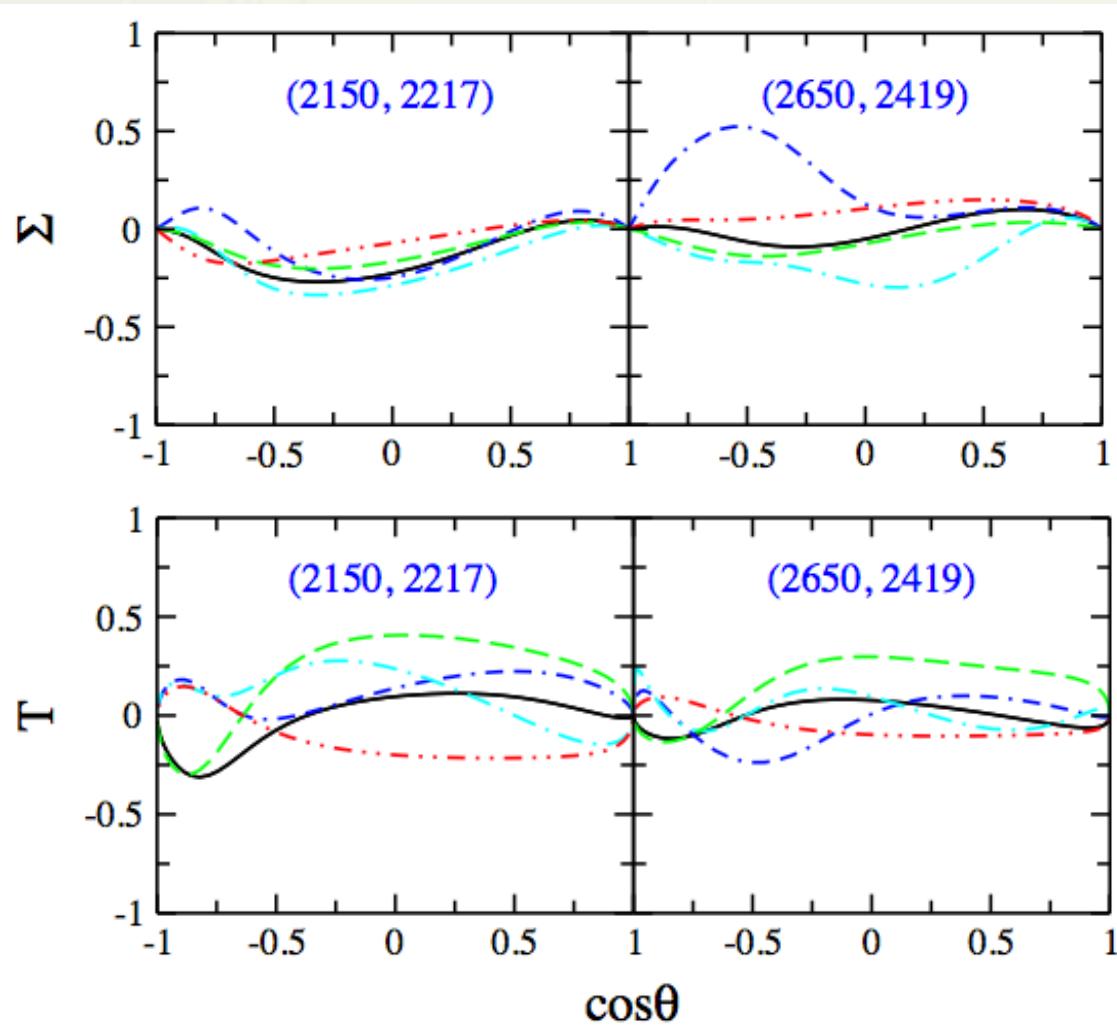
— S. H. Kim et al., PRD90(2014)014021, small N(2060) $5/2^-$   
— Our results with significant N(2060) $5/2^-$

# Reaction mechanism of $\gamma p \rightarrow K^{*+} \Lambda^?$

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- K-exchange dominates the high energy cross sections
- 2 N\*'s are needed, one is  $N(2060)5/2^-$ , the other could be one of  $N(2000)5/2^+$ ,  $N(2040) 3/2^+$ ,  $N(2100)1/2^+$ ,  $N(2120)3/2^-$ ,  $N(2190)7/2^-$
- Interference of  $N(2060)5/2^-$  & K is responsible for the near threshold shape of the cross sections

# Predictions on spin observables

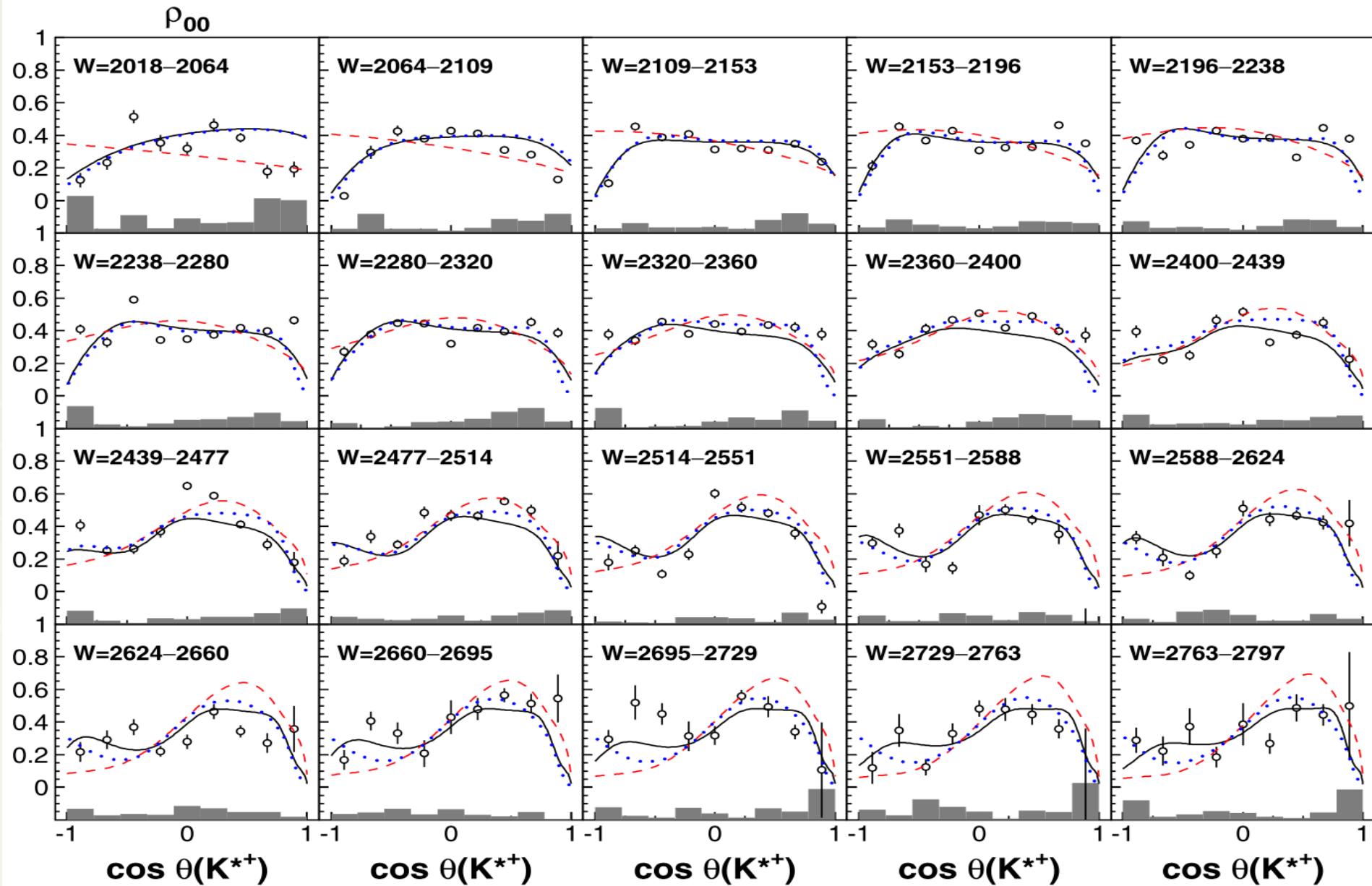


# Summary

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- Cross section data for  $\gamma p \rightarrow K^{*+} \Lambda$  from CLAS have been well described in an effective Lagrangian approach
- K-exchange dominates the high energy behavior
- At least 2 N\*'s are needed, one is  $N(2060)5/2^-$ , the other could be one of  $N(2000)5/2^+$ ,  $N(2040) 3/2^+$ ,  $N(2100)1/2^+$ ,  $N(2120)3/2^-$ ,  $N(2190)7/2^-$
- Interference of  $N(2060)5/2^-$  & K is responsible for the near threshold shape of the cross sections
- Further data on spin observables are needed to further pin down the resonance contents & parameters

# CLAS Collaboration, Phys. Lett. B 771 (2017) 142



**Thank you for your patience!**

## Model Parameters

Model	I	II	III	IV	V
$\chi^2/N$	1.35	1.79	1.85	2.09	2.18
$g_{\Sigma^* \Lambda \gamma}^{(1)}$	$0.74 \pm 0.16$	$-0.90 \pm 0.17$	$-0.87 \pm 0.14$	$-0.60 \pm 0.18$	$-0.22 \pm 0.16$
$\Lambda_K$ [MeV]	$1000 \pm 6$	$1019 \pm 4$	$993 \pm 7$	$1030 \pm 3$	$1018 \pm 4$
$N^*$ Name	$N(2060)5/2^-$ **	$N(2060)5/2^-$ **	$N(2060)5/2^-$ **	$N(2060)5/2^-$ **	$N(2060)5/2^-$ **
$M_R$ [MeV]	$2033 \pm 2$	$2009 \pm 5$	$2032 \pm 3$	$2043 \pm 4$	$2038 \pm 3$
$\Gamma_R$ [MeV]	$65 \pm 4$	$213 \pm 20$	$81 \pm 8$	$202 \pm 16$	$77 \pm 8$
$\Lambda_R$ [MeV]	$1188 \pm 20$	$965 \pm 16$	$1126 \pm 12$	$889 \pm 13$	$981 \pm 22$
$\sqrt{\beta_{\Lambda K^*}} A_{1/2}$ [ $10^{-3}$ GeV $^{-1/2}$ ]	$0.69 \pm 0.06$	$0.03 \pm 0.01$	$0.33 \pm 0.03$	$0.60 \pm 0.06$	$-0.21 \pm 0.02$
$\sqrt{\beta_{\Lambda K^*}} A_{3/2}$ [ $10^{-3}$ GeV $^{-1/2}$ ]	$-1.39 \pm 0.13$	$-0.10 \pm 0.01$	$-1.10 \pm 0.10$	$-1.94 \pm 0.19$	$-1.56 \pm 0.15$
$N^*$ Name	$N(2000)5/2^+$ **	$N(2040)3/2^+$ *	$N(2120)3/2^-$ **	$N(2190)7/2^-$ ****	$N(2100)1/2^+$ *
$M_R$ [MeV]	$2115 \pm 22$	$2200 \pm 62$	$2203 \pm 9$ [ $\approx 2120$ ]	$2243 \pm 6$ [ $2100 \sim 2200$ ]	$2100 \pm 15$ [ $\approx 2100$ ]
$\Gamma_R$ [MeV]	$450 \pm 10$	$540 \pm 7$	$433 \pm 33$ [ $300 \sim 700$ ]	$450 \pm 33$	$450 \pm 9$
$\Lambda_R$ [MeV]	$1644 \pm 21$	$1564 \pm 36$	$1726 \pm 58$	$936 \pm 13$	$1431 \pm 31$
$\sqrt{\beta_{\Lambda K^*}} A_{1/2}$ [ $10^{-3}$ GeV $^{-1/2}$ ]	$-2.87 \pm 0.81$	$3.12 \pm 0.85$	$4.53 \pm 0.38$	$5.21 \pm 0.33$	$-7.22 \pm 1.40$
$\sqrt{\beta_{\Lambda K^*}} A_{3/2}$ [ $10^{-3}$ GeV $^{-1/2}$ ]	$-1.04 \pm 0.29$	$7.87 \pm 2.13$	$7.84 \pm 0.65$	$3.71 \pm 0.24$	

$$\mathcal{L}_{RN\gamma}^{1/2\pm} = e \frac{g_{RN\gamma}^{(1)}}{2M_N} \bar{R} \Gamma^{(\mp)} \sigma_{\mu\nu} (\partial^\nu A^\mu) N + \text{H. c.},$$

## Effective Lagrangians

$$\mathcal{L}_{RN\gamma}^{3/2\pm} = -ie \frac{g_{RN\gamma}^{(1)}}{2M_N} \bar{R}_\mu \gamma_\nu \Gamma^{(\pm)} F^{\mu\nu} N + e \frac{g_{RN\gamma}^{(2)}}{(2M_N)^2} \bar{R}_\mu \Gamma^{(\pm)} F^{\mu\nu} \partial_\nu N + \text{H. c.},$$

$$\mathcal{L}_{RN\gamma}^{5/2\pm} = e \frac{g_{RN\gamma}^{(1)}}{(2M_N)^2} \bar{R}_{\mu\alpha} \gamma_\nu \Gamma^{(\mp)} (\partial^\alpha F^{\mu\nu}) N \pm ie \frac{g_{RN\gamma}^{(2)}}{(2M_N)^3} \bar{R}_{\mu\alpha} \Gamma^{(\mp)} (\partial^\alpha F^{\mu\nu}) \partial_\nu N + \text{H. c.},$$

$$\mathcal{L}_{RN\gamma}^{7/2\pm} = ie \frac{g_{RN\gamma}^{(1)}}{(2M_N)^3} \bar{R}_{\mu\alpha\beta} \gamma_\nu \Gamma^{(\pm)} (\partial^\alpha \partial^\beta F^{\mu\nu}) N - e \frac{g_{RN\gamma}^{(2)}}{(2M_N)^4} \bar{R}_{\mu\alpha\beta} \Gamma^{(\pm)} (\partial^\alpha \partial^\beta F^{\mu\nu}) \partial_\nu N + \text{H. c.},$$

$$\mathcal{L}_{R\Lambda K^*}^{1/2\pm} = -\frac{g_{R\Lambda K^*}}{2M_N} \bar{R} \Gamma^{(\mp)} \left\{ \left[ \left( \frac{\gamma_\mu \partial^2}{M_R \mp M_N} \pm i \partial_\mu \right) - \frac{f_{R\Lambda K^*}}{g_{R\Lambda K^*}} \sigma_{\mu\nu} \partial^\nu \right] K^{*\mu} \right\} \Lambda + \text{H. c.},$$

$$\mathcal{L}_{R\Lambda K^*}^{3/2\pm} = -i \frac{g_{R\Lambda K^*}^{(1)}}{2M_N} \bar{R}_\mu \gamma_\nu \Gamma^{(\pm)} K^{*\mu\nu} \Lambda + \frac{g_{R\Lambda K^*}^{(2)}}{(2M_N)^2} \bar{R}_\mu \Gamma^{(\pm)} K^{*\mu\nu} \partial_\nu \Lambda \mp \frac{g_{R\Lambda K^*}^{(3)}}{(2M_N)^2} \bar{R}_\mu \Gamma^{(\pm)} (\partial_\nu K^{*\mu\nu}) \Lambda + \text{H. c.},$$

$$\begin{aligned} \mathcal{L}_{R\Lambda K^*}^{5/2\pm} &= \frac{g_{R\Lambda K^*}^{(1)}}{(2M_N)^2} \bar{R}_{\mu\alpha} \gamma_\nu \Gamma^{(\mp)} (\partial^\alpha K^{*\mu\nu}) \Lambda \pm i \frac{g_{R\Lambda K^*}^{(2)}}{(2M_N)^3} \bar{R}_{\mu\alpha} \Gamma^{(\mp)} (\partial^\alpha K^{*\mu\nu}) \partial_\nu \Lambda \\ &\quad \mp i \frac{g_{R\Lambda K^*}^{(3)}}{(2M_N)^3} \bar{R}_{\mu\alpha} \Gamma^{(\mp)} (\partial^\alpha \partial_\nu K^{*\mu\nu}) \Lambda + \text{H. c.}, \end{aligned}$$

$$\begin{aligned} \mathcal{L}_{R\Lambda K^*}^{7/2\pm} &= i \frac{g_{R\Lambda K^*}^{(1)}}{(2M_N)^3} \bar{R}_{\mu\alpha\beta} \gamma_\nu \Gamma^{(\pm)} (\partial^\alpha \partial^\beta K^{*\mu\nu}) \Lambda - \frac{g_{R\Lambda K^*}^{(2)}}{(2M_N)^4} \bar{R}_{\mu\alpha\beta} \Gamma^{(\pm)} (\partial^\alpha \partial^\beta K^{*\mu\nu}) \partial_\nu \Lambda \\ &\quad \pm \frac{g_{R\Lambda K^*}^{(3)}}{(2M_N)^4} \bar{R}_{\mu\alpha\beta} \Gamma^{(\pm)} (\partial^\alpha \partial^\beta \partial_\nu K^{*\mu\nu}) \Lambda + \text{H. c..} \end{aligned}$$