

# 2<sup>nd</sup> ISIS-CSNS Workshop

## Neutron Total Scattering: Methods, Instrumentation and Data Modelling



Prof Robert McGreevy  
Director of the ISIS Neutron and Muon Source



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# Reverse Monte Carlo Simulation: a new technique for the determination of disordered structures

McGreevy R L and Pusztai L, *Molecular Simulation* 1(1988) 35

We have developed a new technique, based on the standard Monte Carlo simulation method with Markov chain sampling, where a set of three dimensional particle configurations are generated that are consistent with the experimentally measured structure factor,  $A(Q)$ , and radial distribution function,  $g(r)$ , of a liquid or other disordered system. Consistency is determined by a standard  $\chi^2$  test using the experimental errors. No input potential is required. We present initial results for liquid argon. Since the technique can work directly from the structure factor it promises to be extremely powerful for modelling the structures of glasses or amorphous materials. It also has many other advantages in multicomponent systems and as a tool for experimental data analysis.

Key words: Monte Carlo, structure factor, radial distribution function, liquid, glass.





**Total scattering methods  
can be applied to many  
problems**

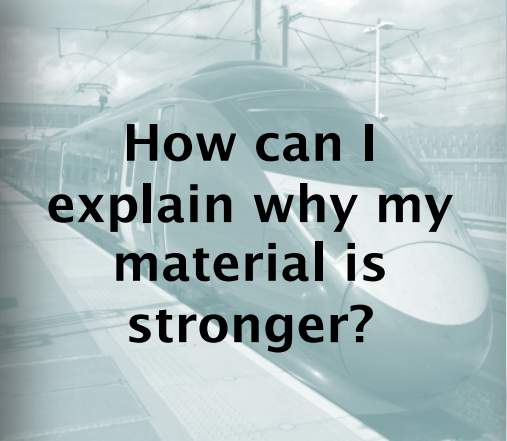


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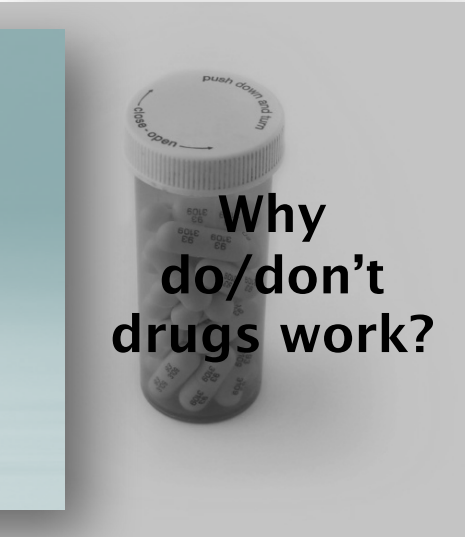
How does water solvate ions?




How can I explain why my material is stronger?



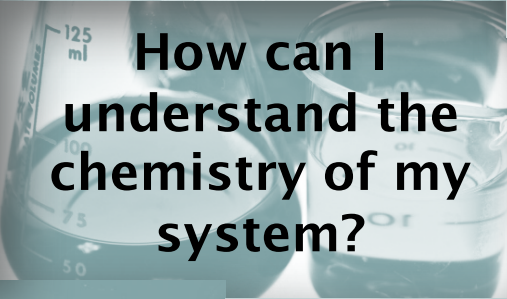
How do stars form?



Why do/don't drugs work?



Why does window glass break into shards?




How can I understand the chemistry of my system?



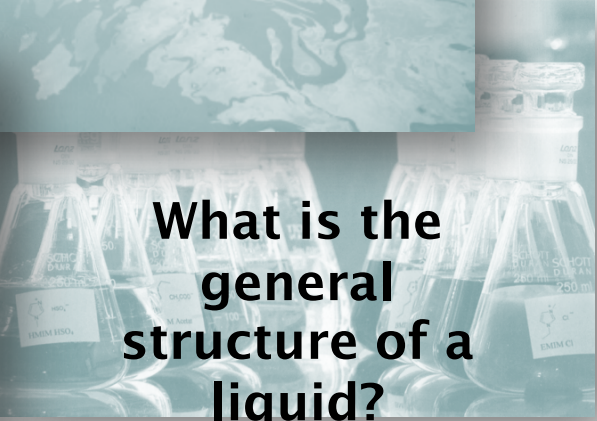
Why don't two liquids mix?



What makes an effective surfactant?



Why do pipelines get blocked?



What is the general structure of a liquid?

**And can answer many questions**



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# ISIS team for the PDF and Total Scattering Workshop



Daniel Bowron



Sam Callear



Alex Hannon



Dave Keen



Helen Playford



Alan Soper

7<sup>th</sup>-9<sup>th</sup> November 2016



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# Calls for proposals to use ISIS are made twice a year

## Submission deadlines are 16<sup>th</sup> April and 16<sup>th</sup> October

<http://www.isis.stfc.ac.uk/apply-for-beamtime/apply-for-beamtime2117.html>

### Newton Funding for Indian, Chinese and South African researchers

ISIS has been awarded funds as part of the UK Government's Newton Fund to support researchers from China, India and South Africa to use ISIS.

ISIS is able to support a limited number of experiments each round from users from these three countries. For supported experiments we can fund up to two researchers to come to ISIS for the experiment, and will pay for economy flights, accommodation and food costs for those researchers. Accommodation arrangements should be made through the ISIS user office, who will also provide a per diem amount for food; claims for flights should also be made through the user office and require supporting receipts.

To apply for Newton Funding for an ISIS experiment, please tick the box on page 3 of the ISIS online proposal system saying that you would like funding when you are creating your beamtime application (this mechanism will be available from ISIS round 16/2 onwards – for experiments approved before then, please contact [Philip King](#) to ask about the possibility of funding).

Details of the UK Government's Newton Fund can be found [online](#).



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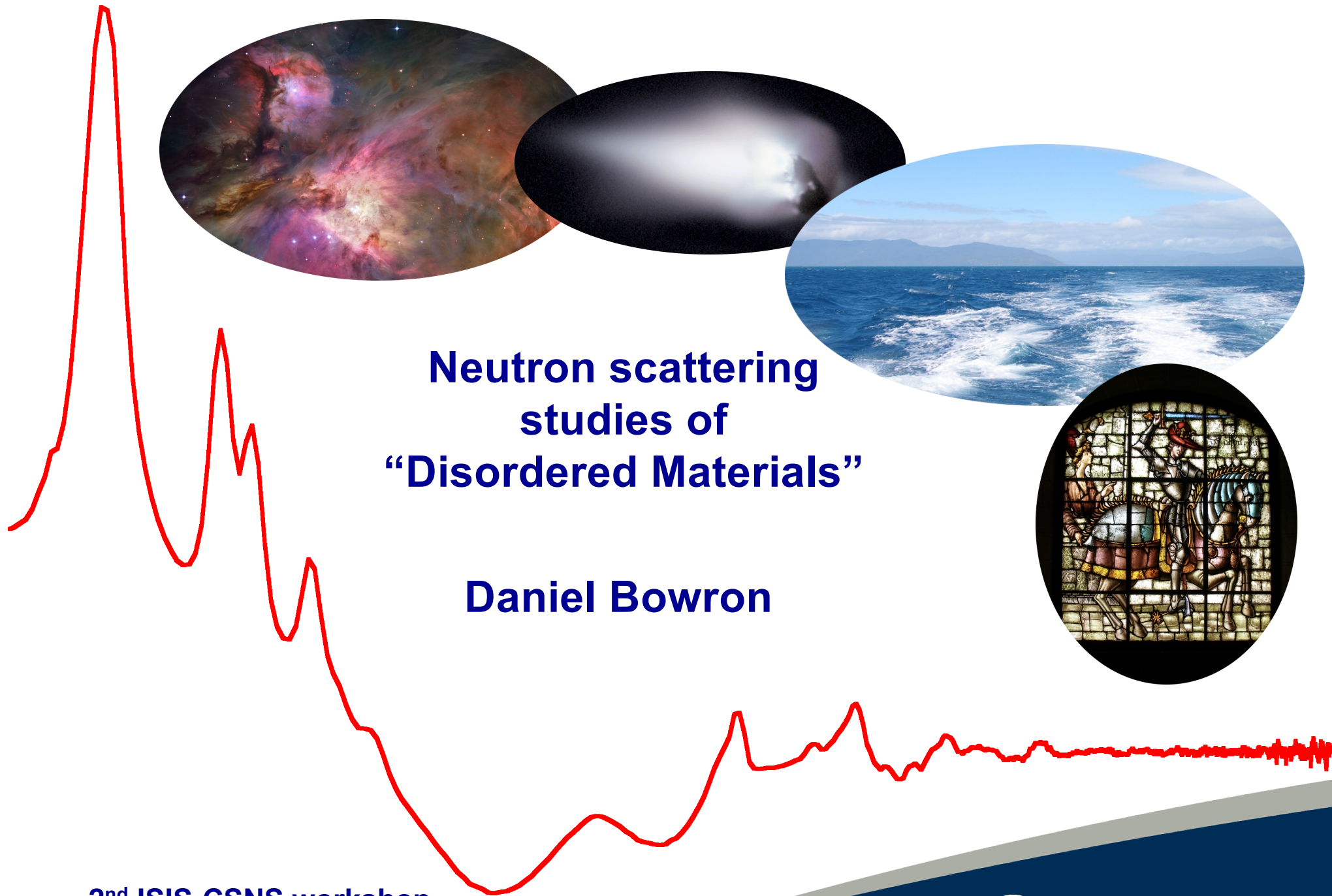
Wishing you all a successful and  
informative workshop and hoping  
to see you at ISIS one day

Prof Robert McGreevy  
Director of the ISIS Neutron and Muon Source



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**Neutron scattering  
studies of  
“Disordered Materials”**

**Daniel Bowron**

**2<sup>nd</sup> ISIS-CSNS workshop  
PDF and Total Scattering Methods  
7<sup>th</sup> – 9<sup>th</sup> November 2016**



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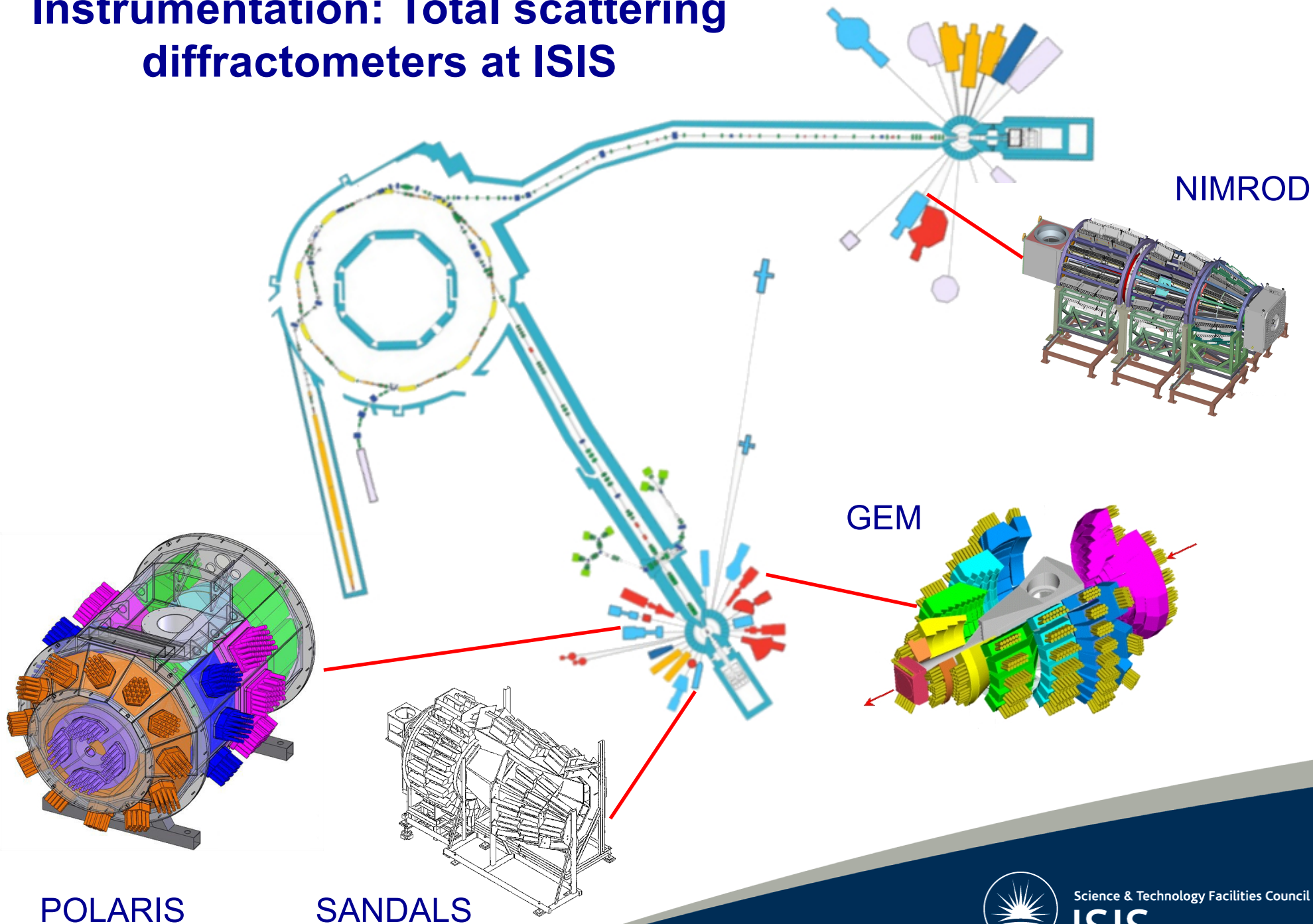
**2<sup>nd</sup> ISIS-CSNS workshop**  
***PDF and Total Scattering Methods***  
**7<sup>th</sup> – 9<sup>th</sup> November 2016**

Aims of workshop

- (1) Give some examples of the scientific applications of neutron total scattering
- (2) Outline instrumentation requirements
- (3) Give an overview of underlying scattering theory
- (4) Explain the corrections that need to be applied to measured data
- (5) Introduce methods that can be used to bring understanding of scattering data using atomistic models: Empirical Potential Structure Refinement (EPSR) and Reverse Monte Carlo (RMC) modelling



# Instrumentation: Total scattering diffractometers at ISIS



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# Theory: Differential Scattering Cross Section

$$\frac{d\sigma_s^{scat}}{d\Omega} = \sum_{i=1}^n c_i \bar{b}_i^2 + \sum_{i,j=1}^n c_i c_j \bar{b}_i \bar{b}_j [A_{ij}(Q) - 1]$$

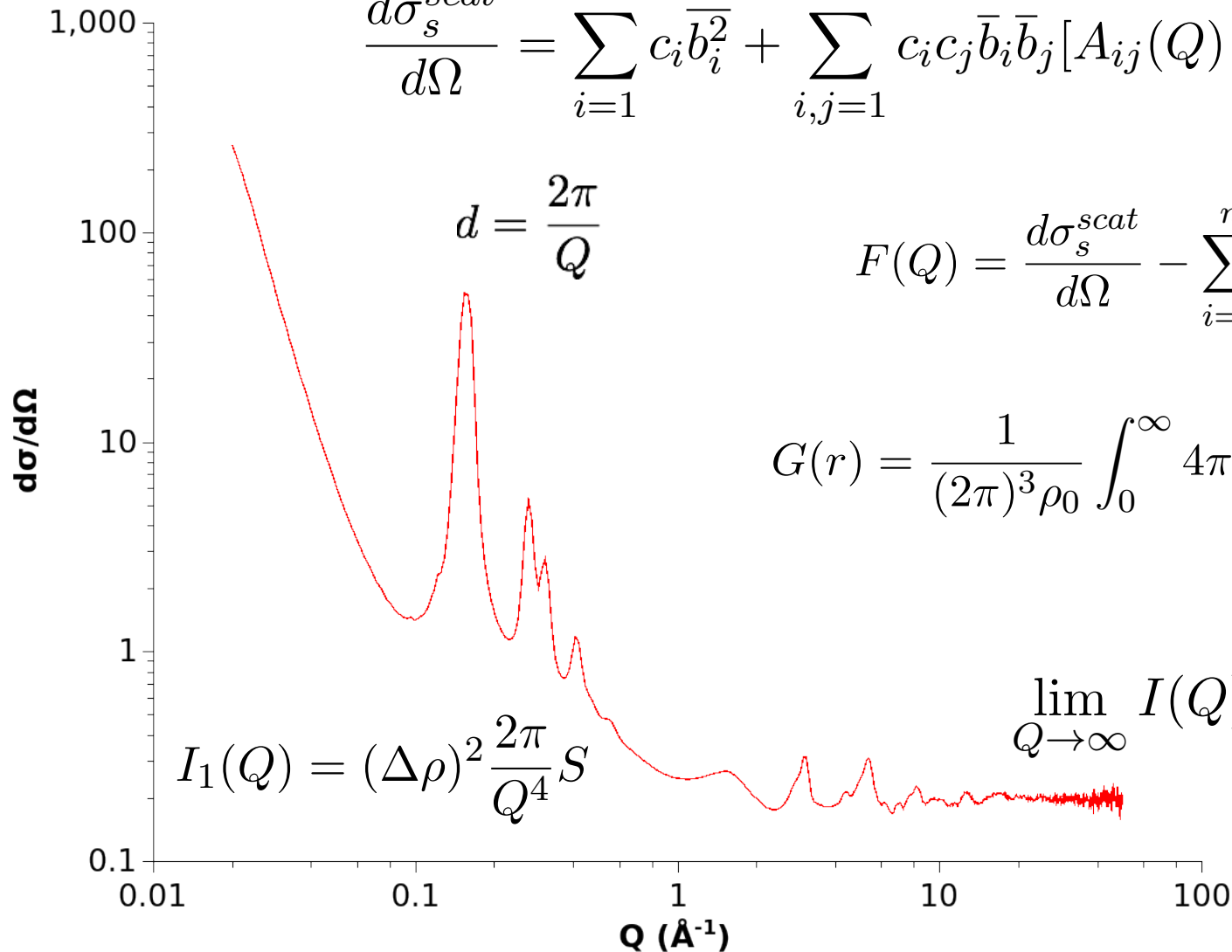
$$d = \frac{2\pi}{Q}$$

$$F(Q) = \frac{d\sigma_s^{scat}}{d\Omega} - \sum_{i=1}^n c_i \bar{b}_i^2$$

$$G(r) = \frac{1}{(2\pi)^3 \rho_0} \int_0^\infty 4\pi Q^2 F(Q) \frac{\sin(Qr)}{Qr} dQ$$

$$\lim_{Q \rightarrow \infty} I(Q) = \frac{\rho t f \sum_i c_i \sigma_i^{scat}}{4\pi}$$

$$I_1(Q) = (\Delta\rho)^2 \frac{2\pi}{Q^4} S$$



$$Q = \frac{4\pi}{\lambda} \sin \theta$$



# Modelling: Turning total scattering data into scientific impact requires more than just a good diffractometer

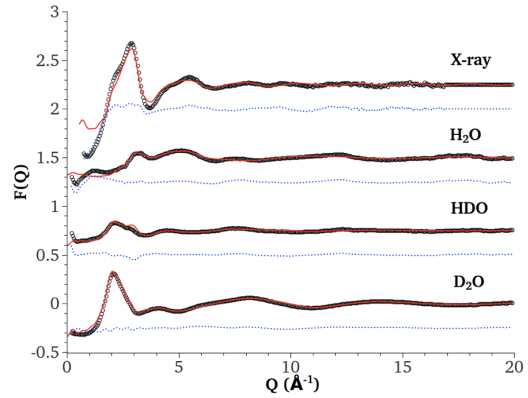
```

program wtsfracs
c
c This program reads in an EPSR total wts file and writes out the percentage wts
c contribution of each term to the total structure factor
c
real firstnumber
character*3 atom(C200),atom(C200)
real weight(C200),weight(C200),weight(C200)
real totalweight1,totalweight2,totalweight3
real fracwt(C200),fracwt(C200),fracwt(C200)
integer ipartial
character*99 filename,filenameout
c
101 format(iX,'Enter the name of the EPSR weights file:')
write(*,101)
read(*,*) filename
102 format(iX,'Enter the name of the output percentage file:')
write(*,102)
read(*,*) filenameout
c
ipartial=0
totalweight1=0.0
totalweight2=0.0
totalweight3=0.0
open(unit=10,file=filename,status='old')
read(10,*) firstnumber
do 1=1,1000
read(10,*,end=201) atom1(),atom2()
read(10,*) weight1(),weight2(),weight3()
ipartial=ipartial+1
totalweight1=totalweight1+weight1()
totalweight2=totalweight2+weight2()
totalweight3=totalweight3+weight3()
enddo
close(unit=10)
c
201 format(iX,'Number of partial structure weights read = ',20)
202 format(iX,'Sum of weight column 1 = ',F16.8)
203 format(iX,'Sum of weight column 2 = ',F16.8)
204 format(iX,'Sum of weight column 3 = ',F16.8)
write(*,103) ipartial
write(*,104) firstnumber
write(*,105) totalweight1
write(*,106) totalweight2
write(*,107) totalweight3
write(*,108) fracwt(C200)
write(*,109) fracwt(C200)
write(*,110) fracwt(C200)
end

```

Code

Data



Mathematics

$$U_{\alpha\beta}^{LJ} = 4\epsilon_{\alpha\beta} \left[ \left( \frac{\sigma_{\alpha\beta}}{r} \right)^{12} - \left( \frac{\sigma_{\alpha\beta}}{r} \right)^6 \right]$$



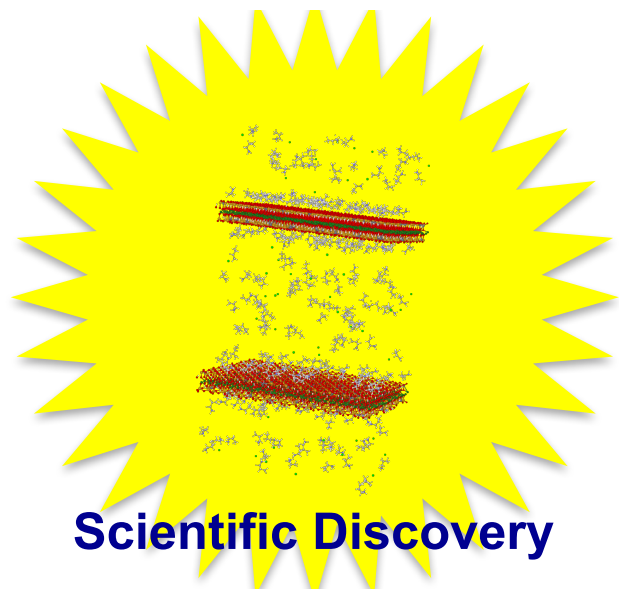
Model



Constraints

1 H Hydrogen 1.008	-252.762	6 C Carbon 12.011	graphite 3825 SP
7 N Nitrogen 14.007	-195.798	8 O Oxygen 15.999	

$\rho$   
 $\sigma$   
 $\epsilon$



Scientific Discovery

# Part 1

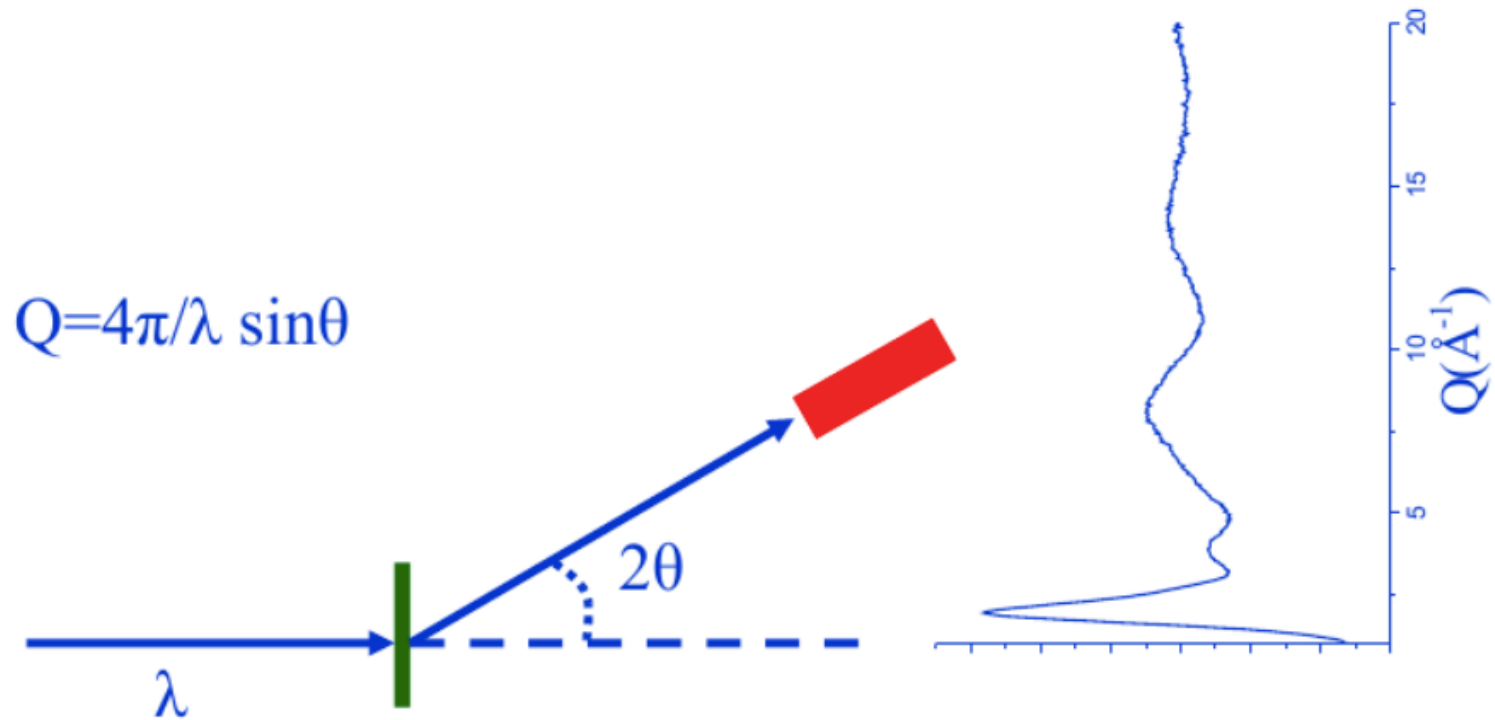
## The scattering experiment



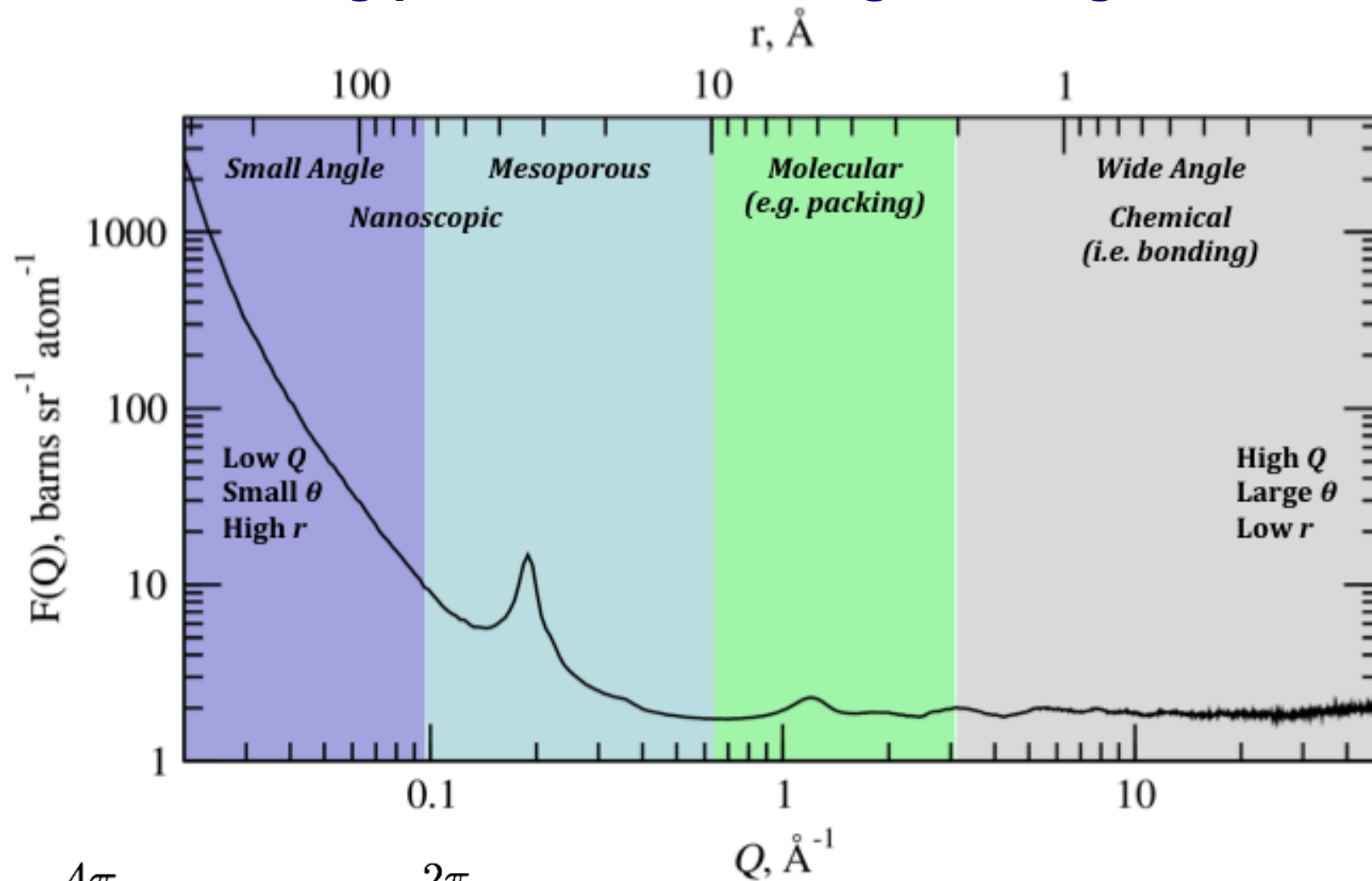
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# Schematic of a neutron scattering measurement



# Scattering probes a wide range of length scales



$$Q = \frac{4\pi}{\lambda} \sin \theta$$

$$d = \frac{2\pi}{Q}$$

$$r = \frac{\pi}{Q}$$

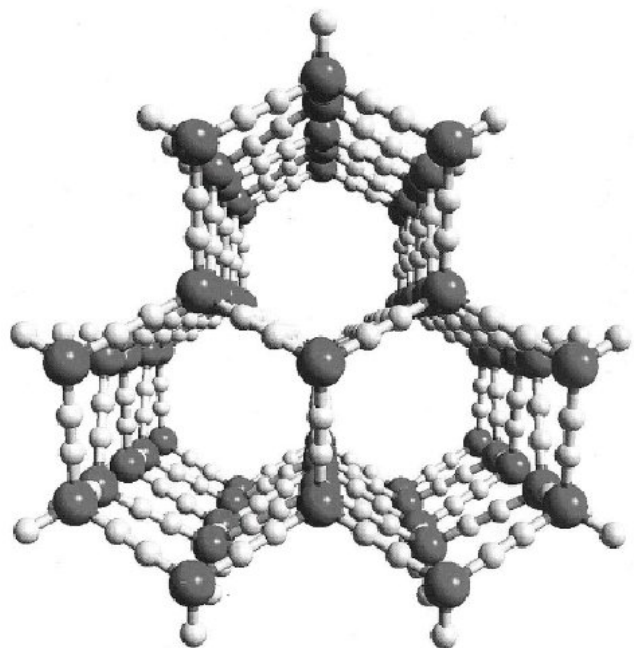


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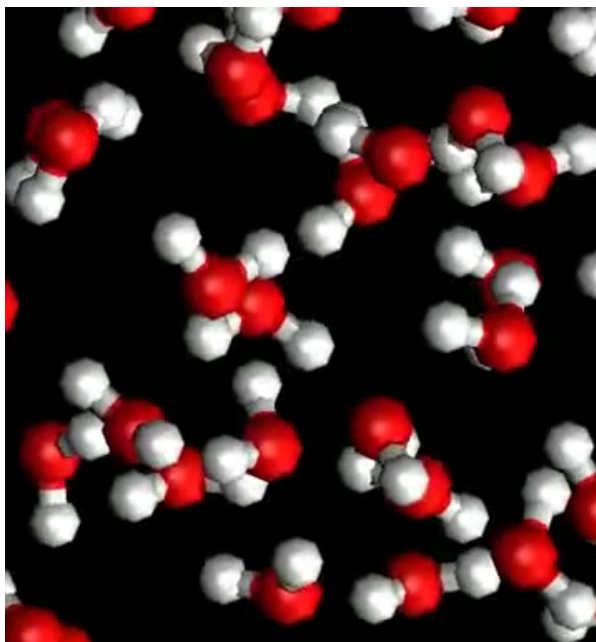
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# Total scattering methods are widely applicable

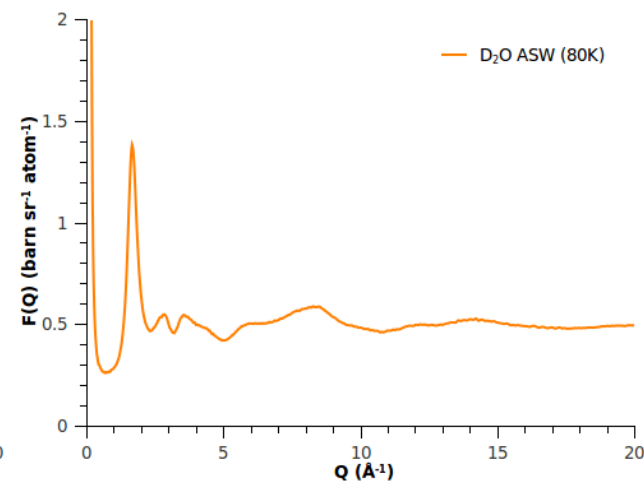
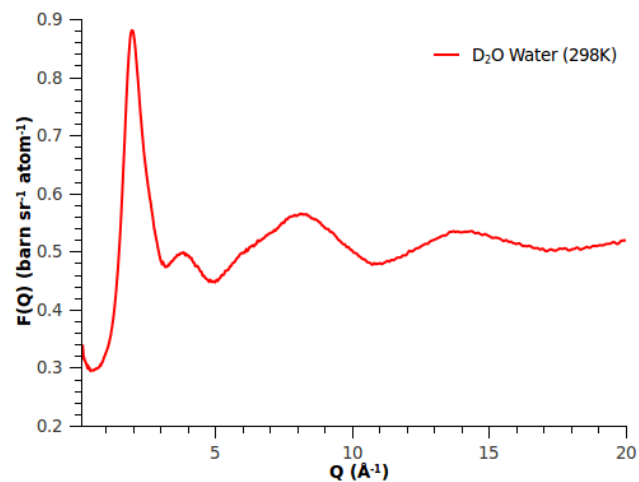
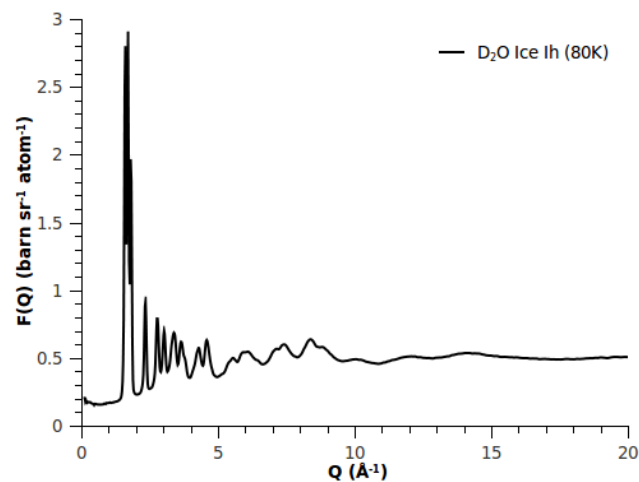
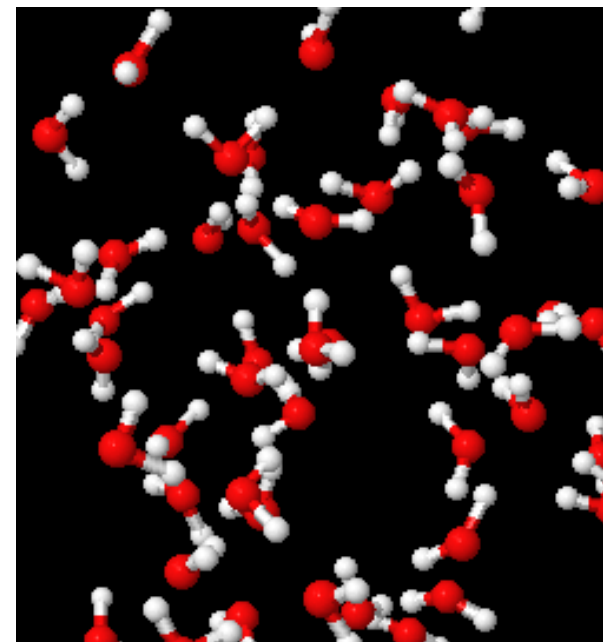
## Crystalline solid



## Liquid

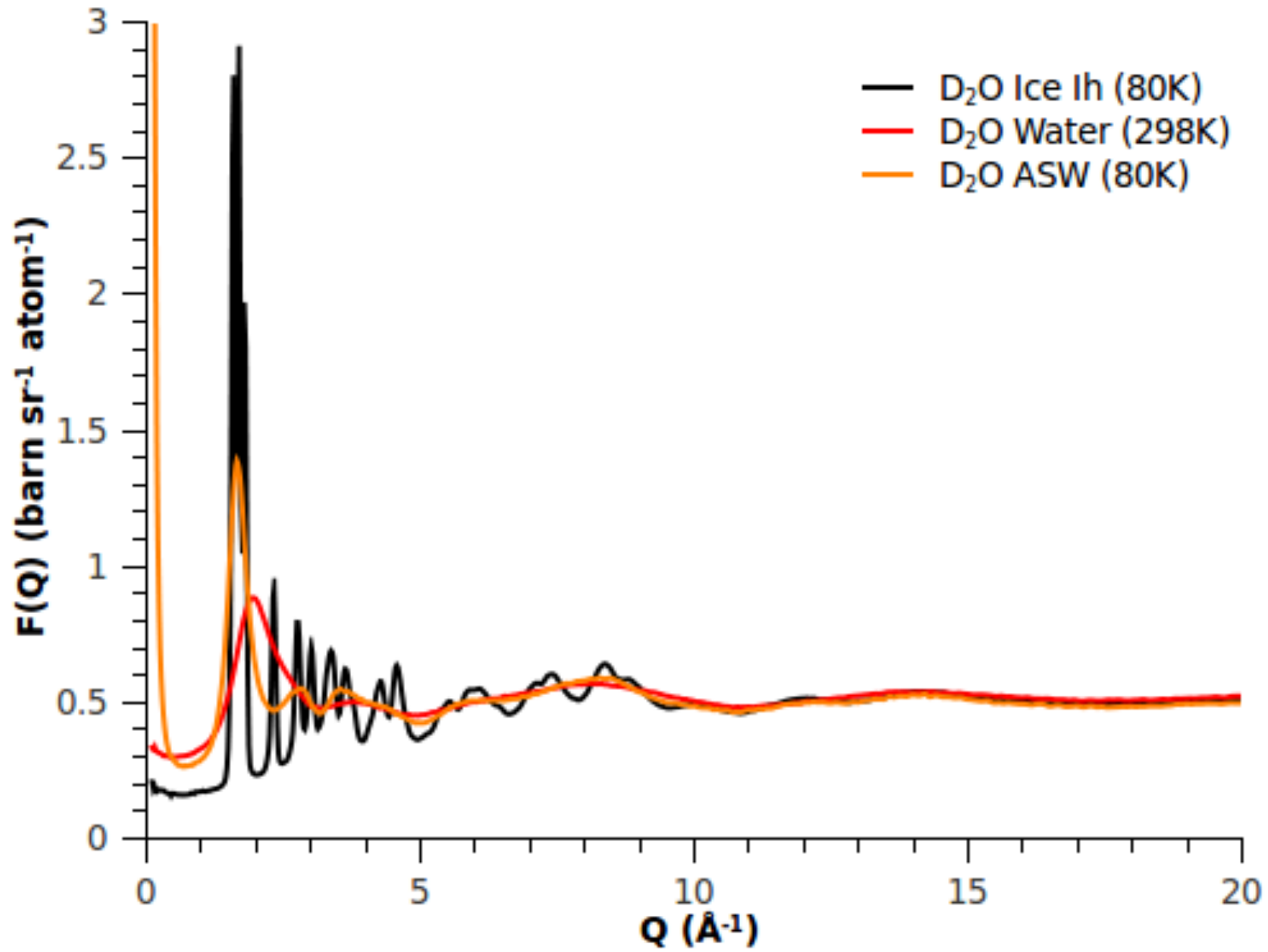


## Glass



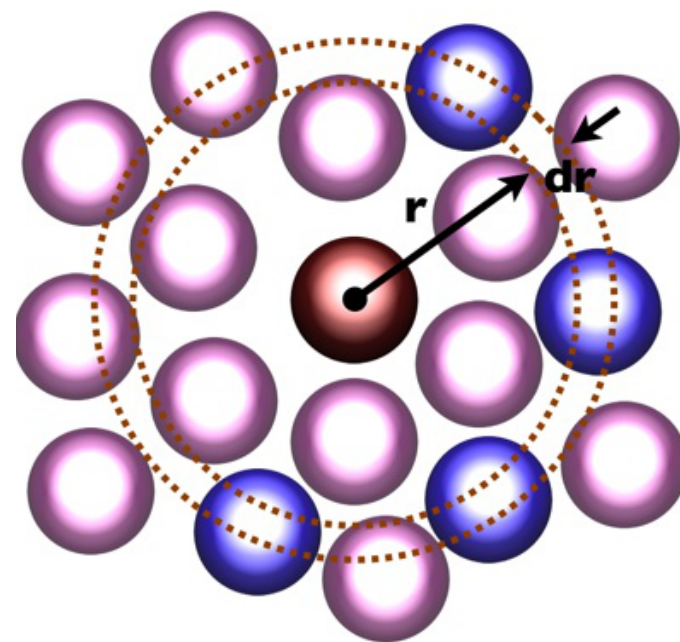
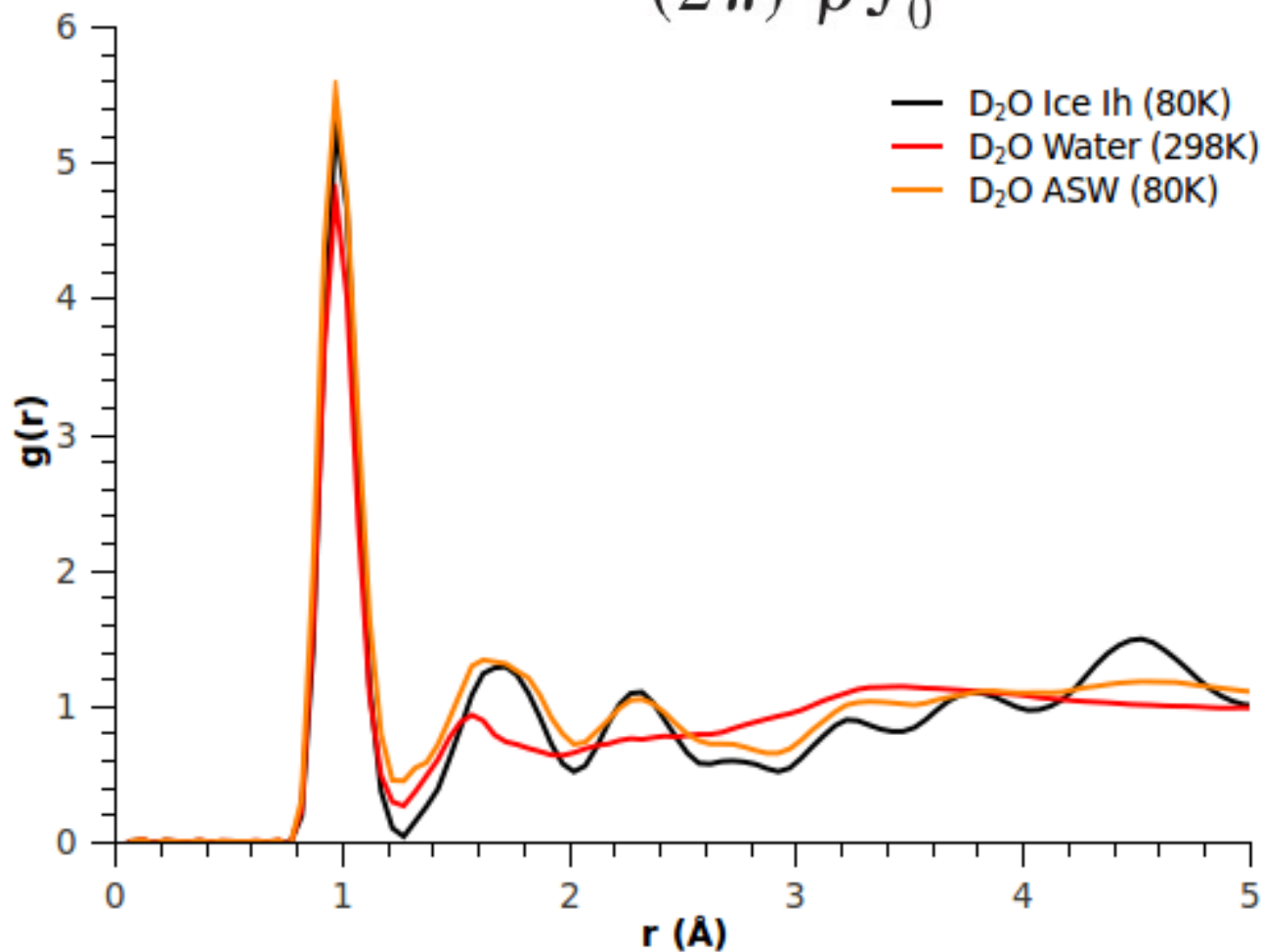


Solid → Liquid → Glass



# The radial distribution function

$$g(r) - 1 = \frac{1}{(2\pi)^3 \rho} \int_0^\infty 4\pi Q^2 F(Q) \frac{\sin Qr}{Qr} dQ.$$



# Part 2

## Examples of application



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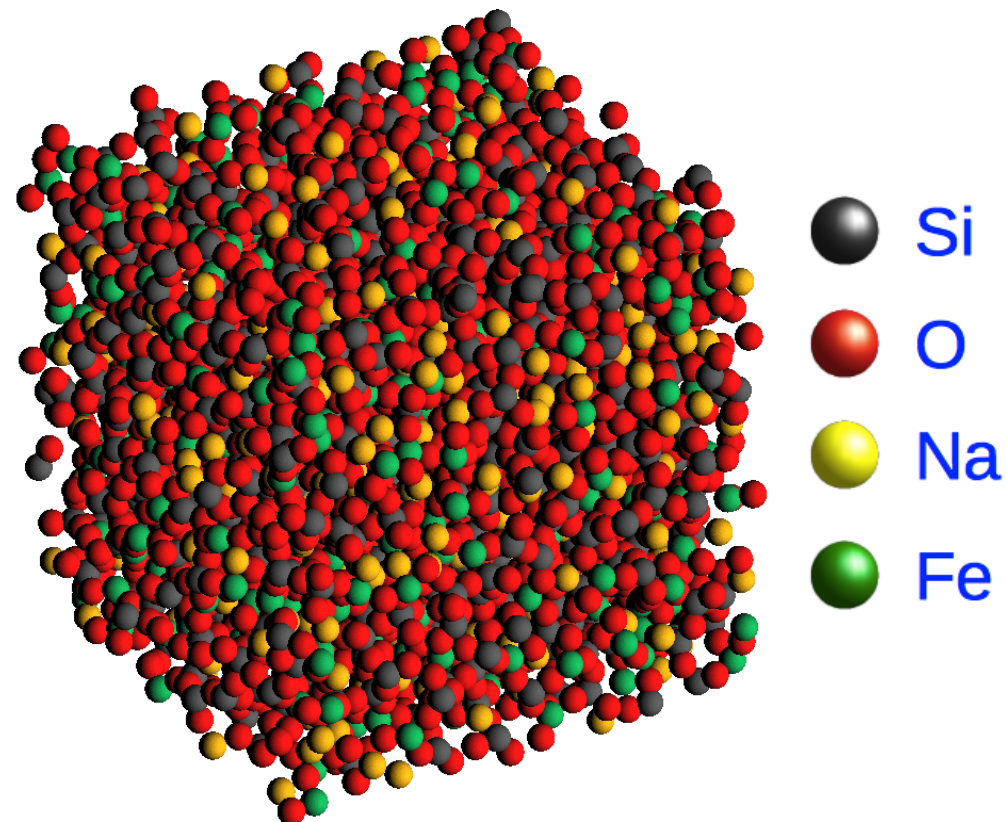
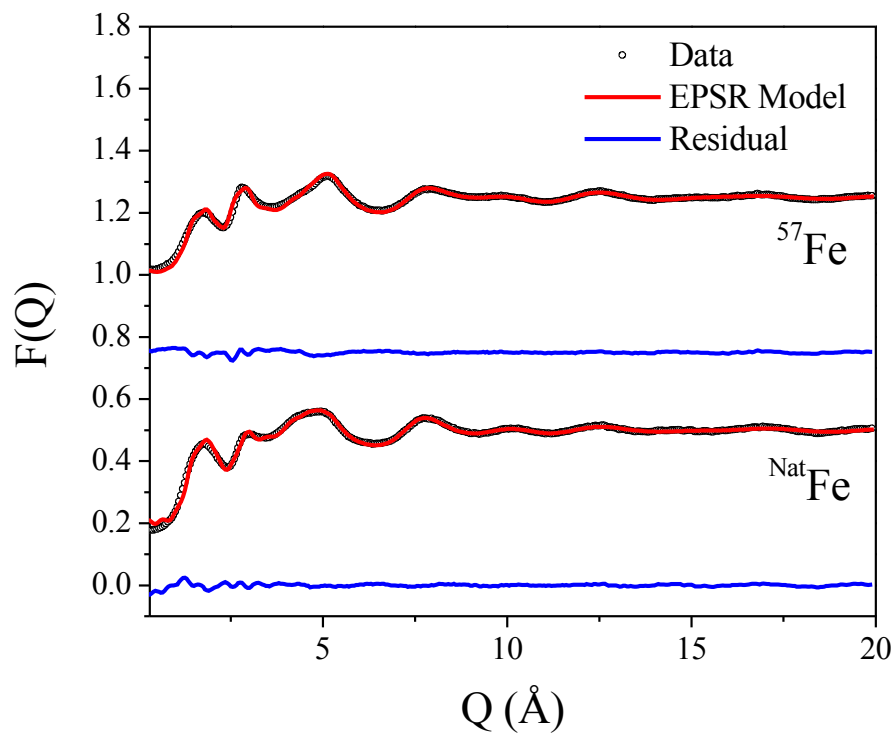
# The structure of glass and ceramic glazes



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# Investigating the incorporation of iron in FeNaSi<sub>2</sub>O<sub>6</sub> glass



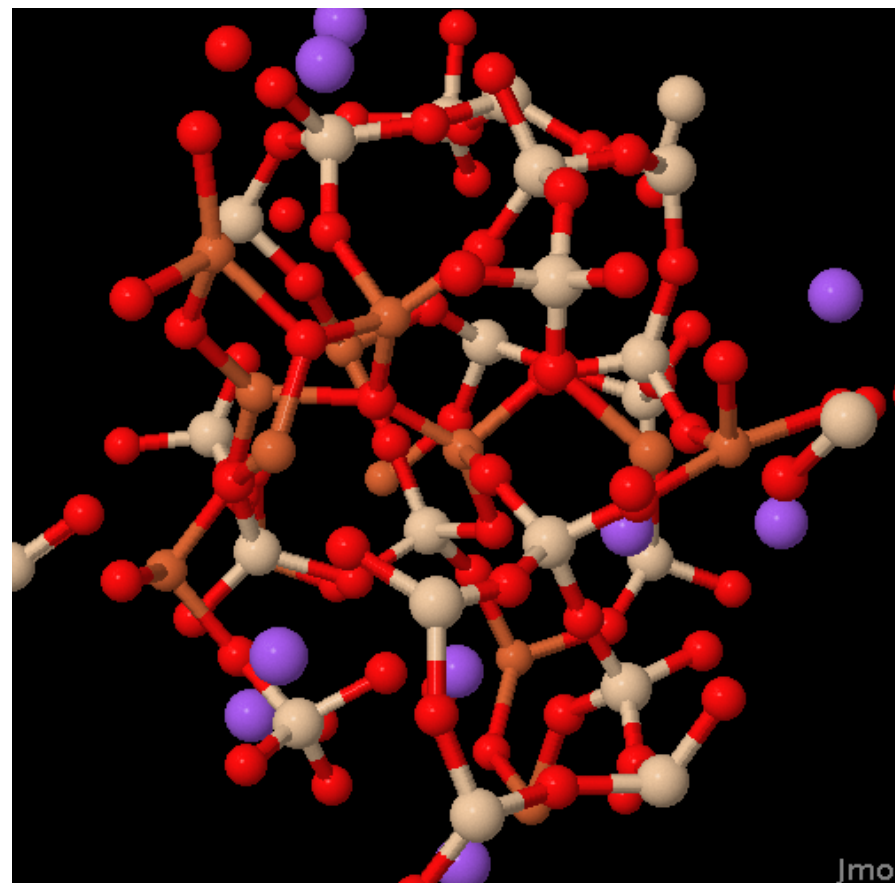
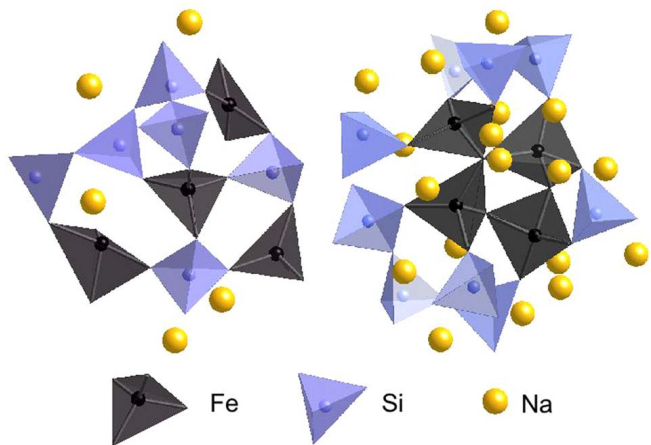
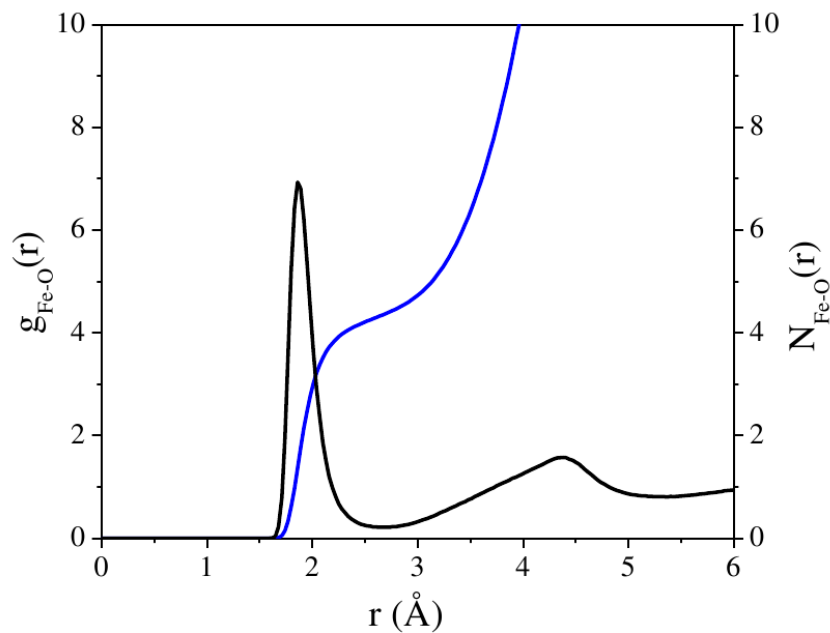
C. Weigel, L. Cormier, L. Galoisy, G. Calas, D.  
Bowron and B. Beuneu  
App. Phys. Lett. 89 (2006) 141911



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# Investigating the incorporation of iron in FeNaSi<sub>2</sub>O<sub>6</sub> glass



76% of total iron found as Fe<sup>3+</sup> in tetrahedral sites  
Remaining iron found in five-coordinate sites, 4%  
and 20% respectively for Fe<sup>3+</sup> and Fe<sup>2+</sup>

C. Weigel, L. Cormier, L. Galois, G. Calas, D.  
Bowron and B. Beuneu  
App. Phys. Lett. 89 (2006) 141911



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# The structure of complex solvent media



# SOLVENTS

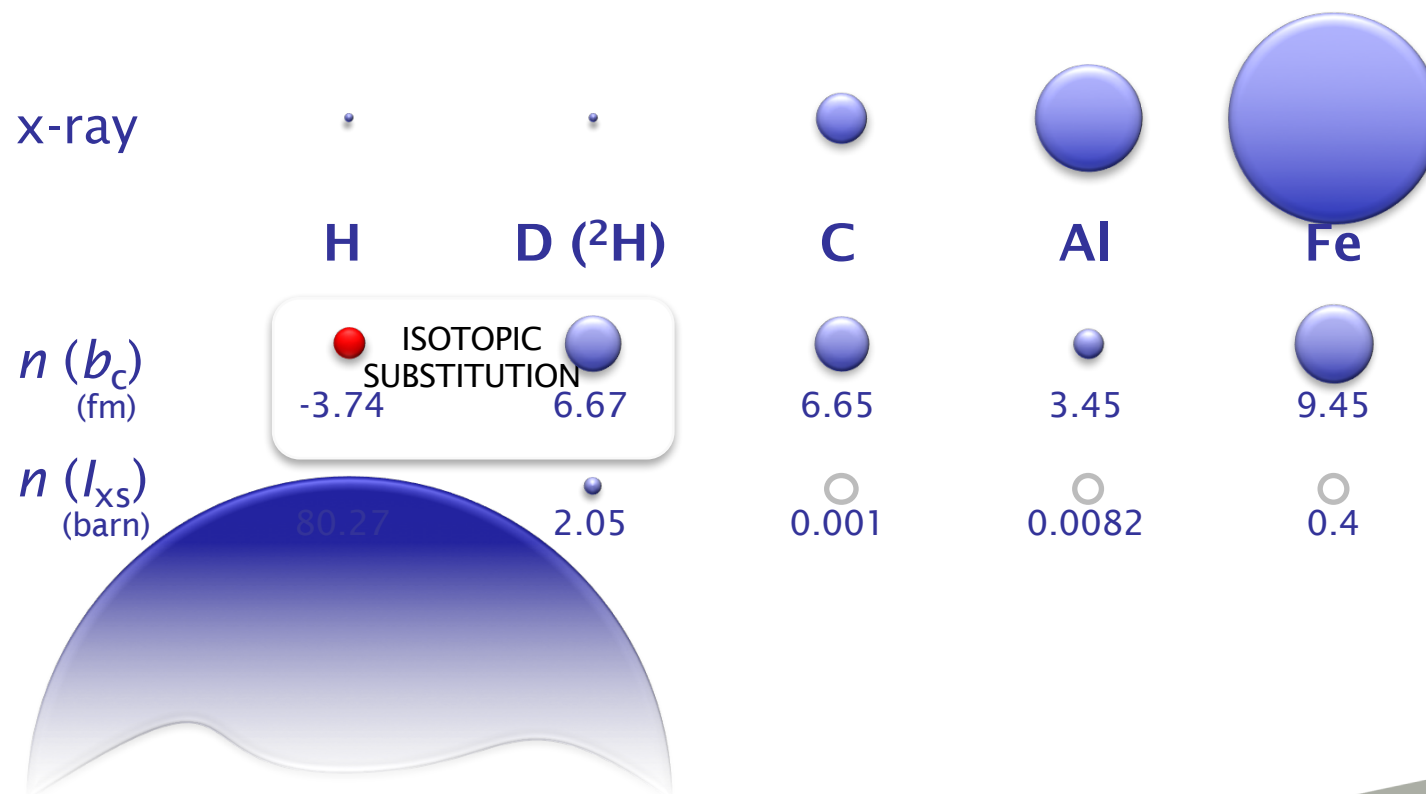


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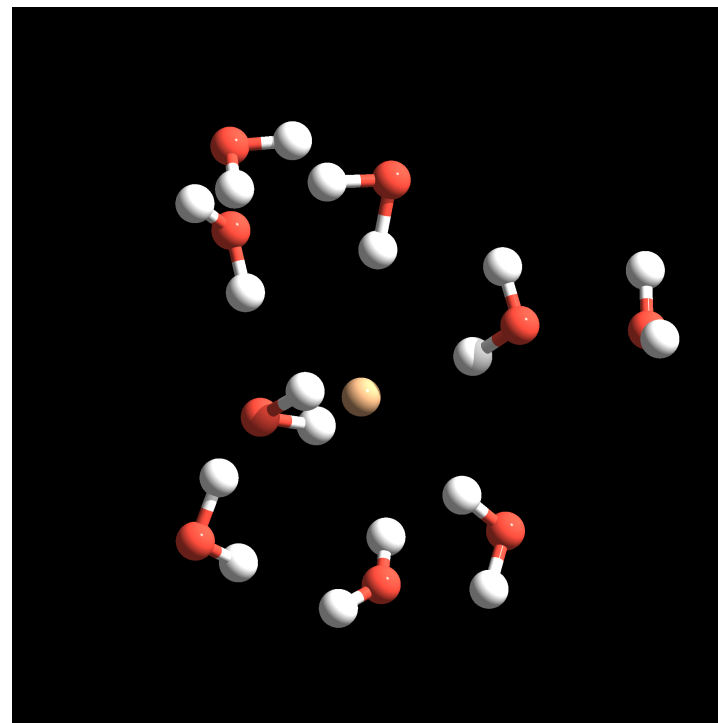
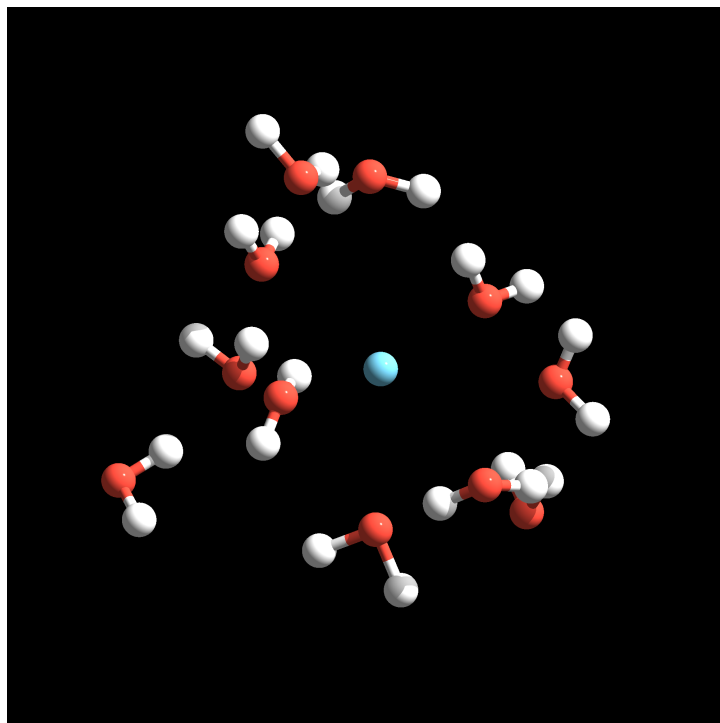
# H/D isotopic substitution – a route to enhanced insight

- Neutrons interact weakly with matter, interacting with only the nucleus
- Neutrons are sensitive to **element and isotope**
  - X-ray scattering of elements depends on number of electrons
  - Neutron scattering of elements varies across periodic table





# The neutron's view of hydrogen lets us....

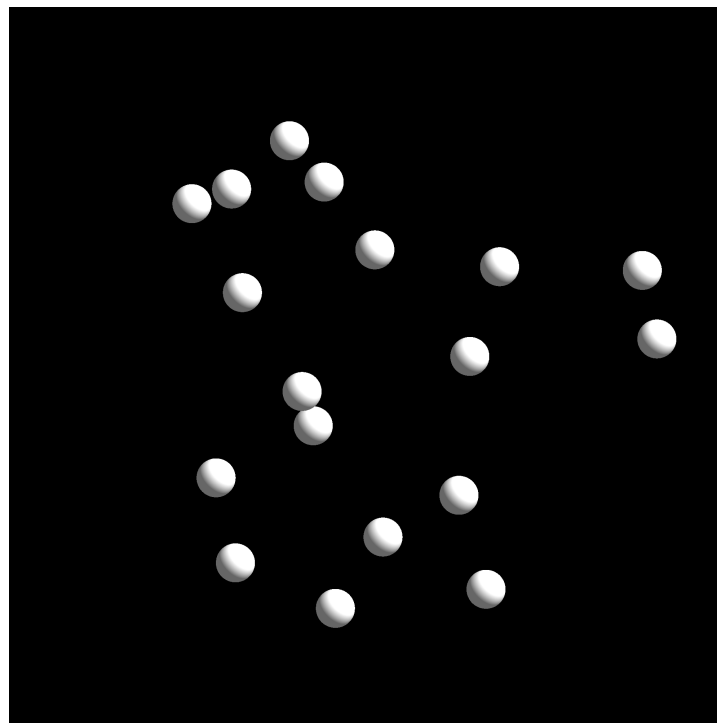
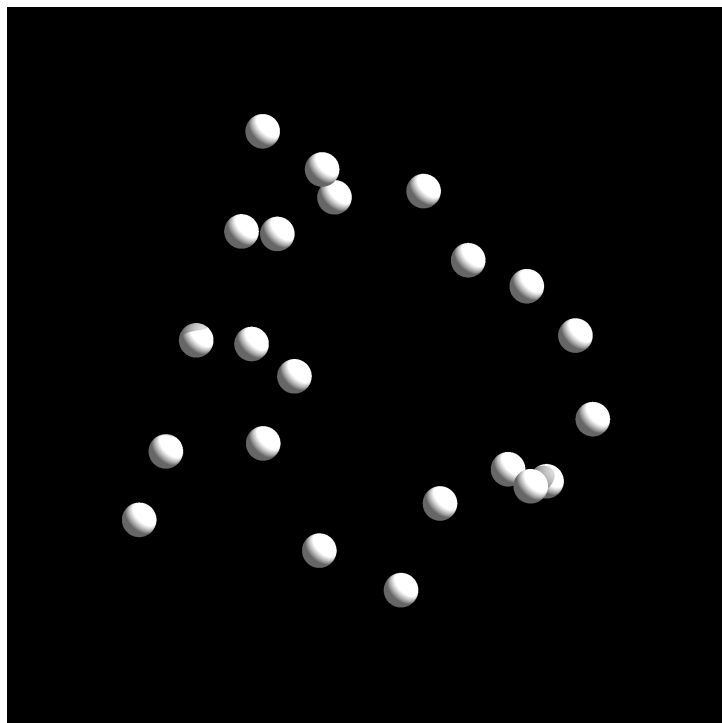


+  
v  
e

See all the atoms

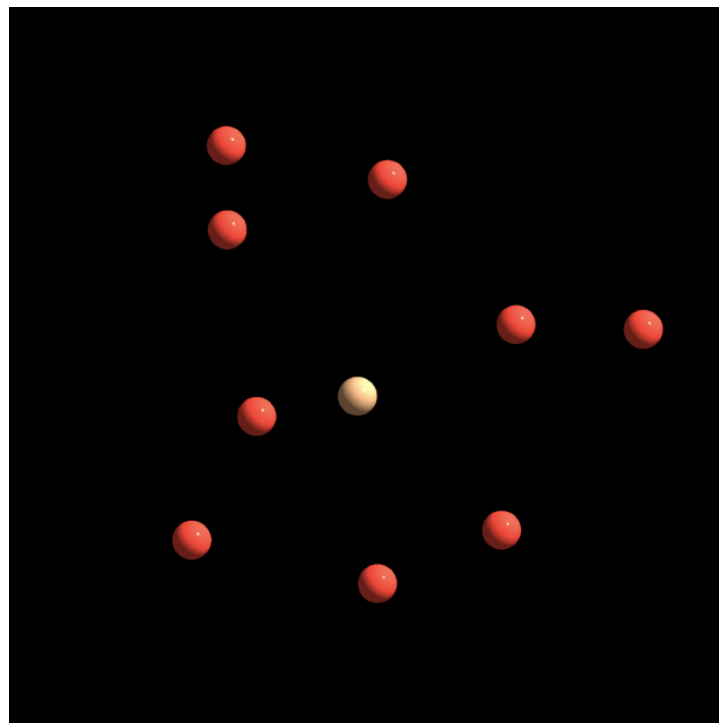
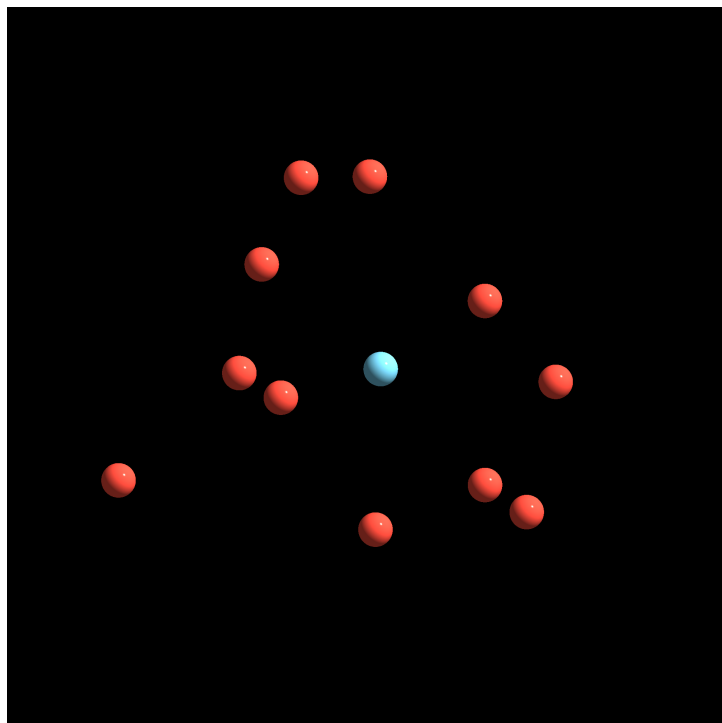
-ve

## The neutron's view of hydrogen lets us....



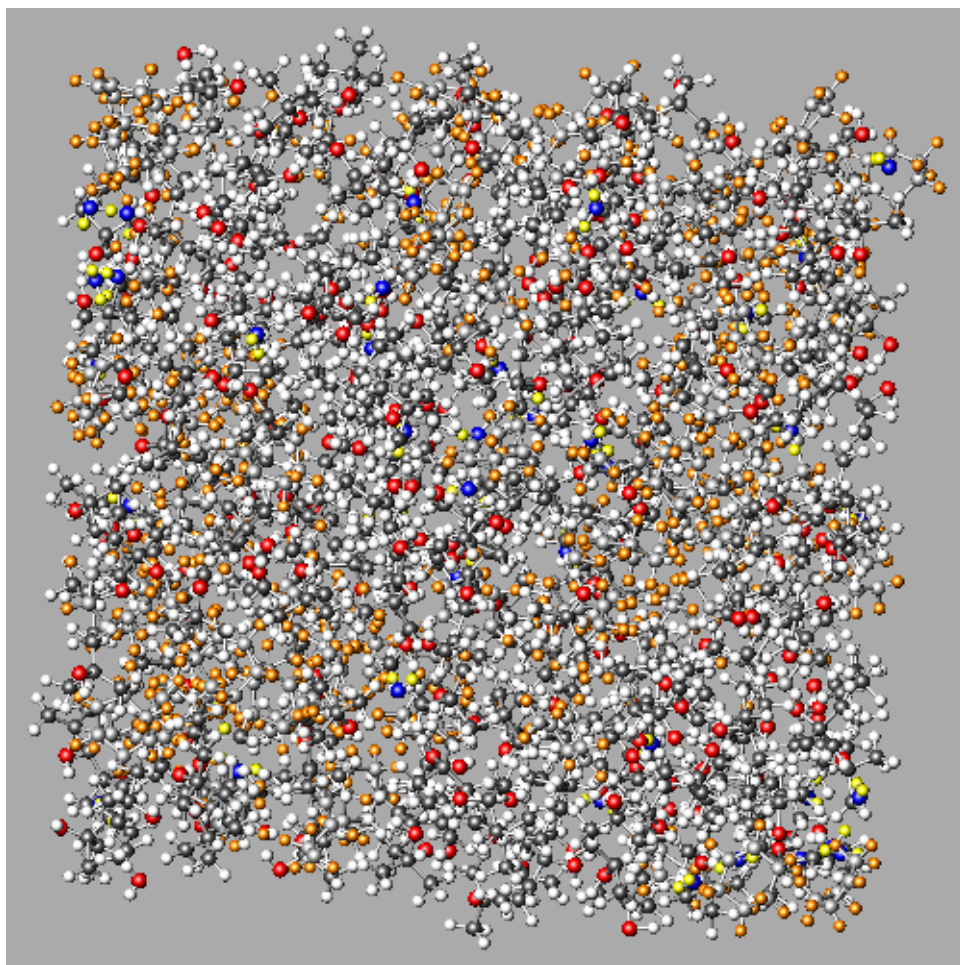
Only see the hydrogen atoms

## The neutron's view of hydrogen lets us....

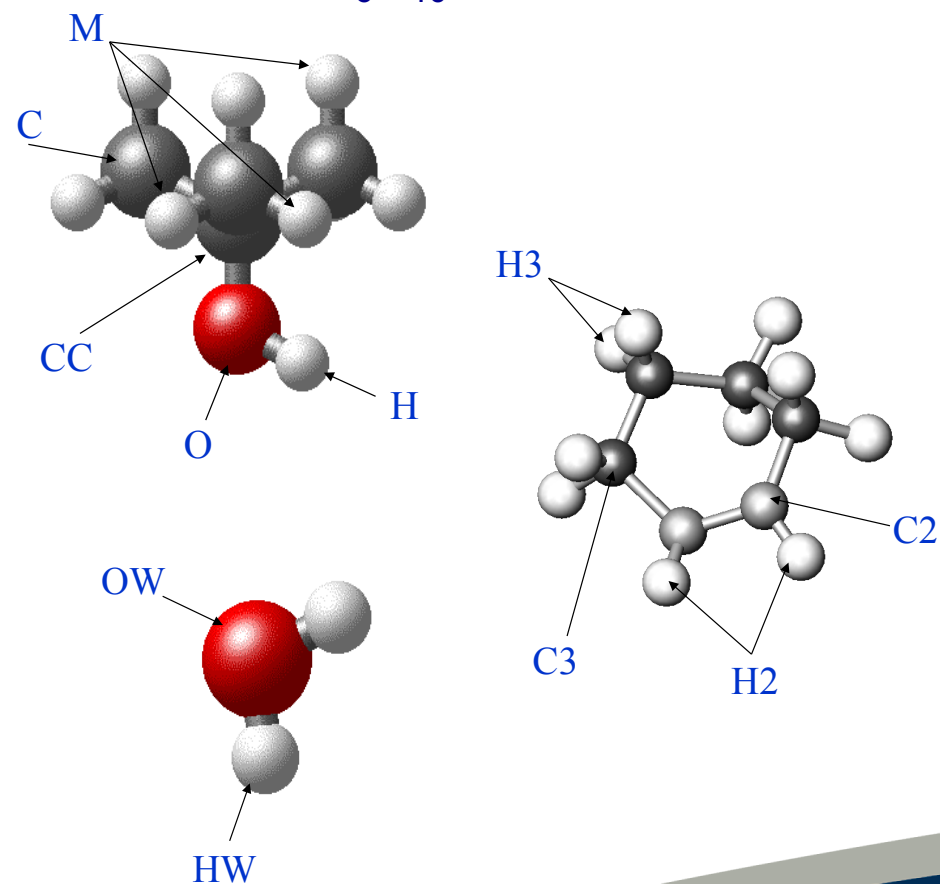


Make the hydrogen invisible

## 6:1:2 tertiary butanol:water:cyclohexene



240  $(\text{CH}_3)_3\text{COH}$  molecules  
40  $\text{H}_2\text{O}$  molecules  
80  $\text{C}_6\text{H}_{10}$  molecules



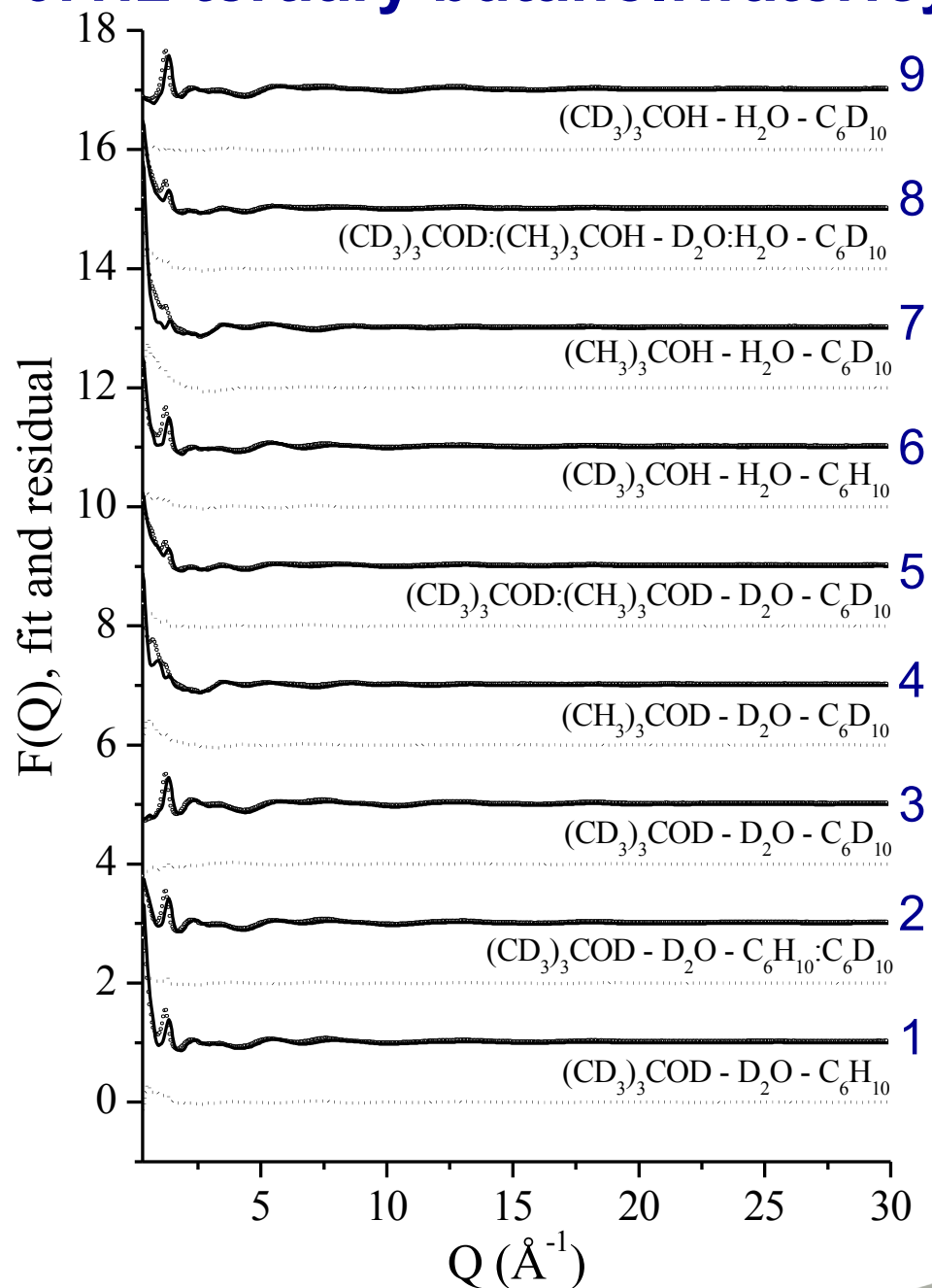
D.T.Bowron and S. Diaz Moreno  
JPC-B **109** 16210-16218 (2005)



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# 6:1:2 tertiary butanol:water:cyclohexene



Complex systems require comprehensive experiments

1,2 & 3 give cyclohexene-cyclohexene correlations

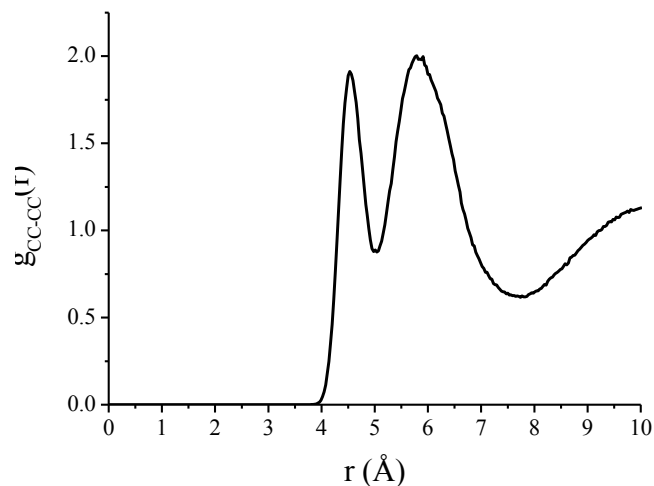
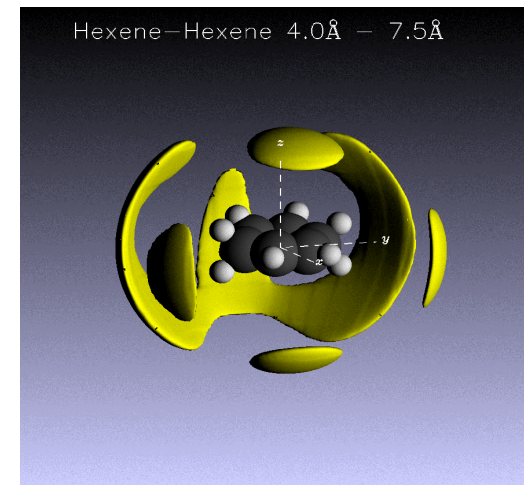
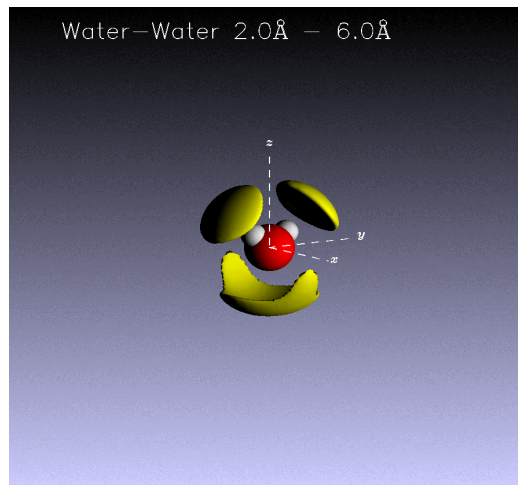
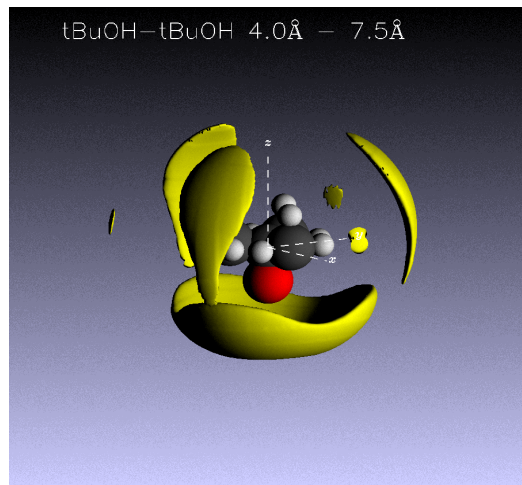
3,4 & 5 give tertiary butanol – tertiary butanol correlations

3,7 & 8 give tertiary butanol and water correlations

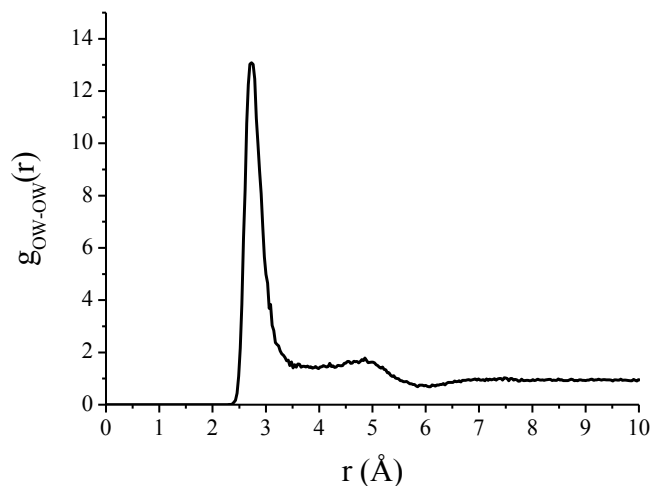
3 & 9 or 1 & 6 give hydroxyl hydrogen and water hydrogen information



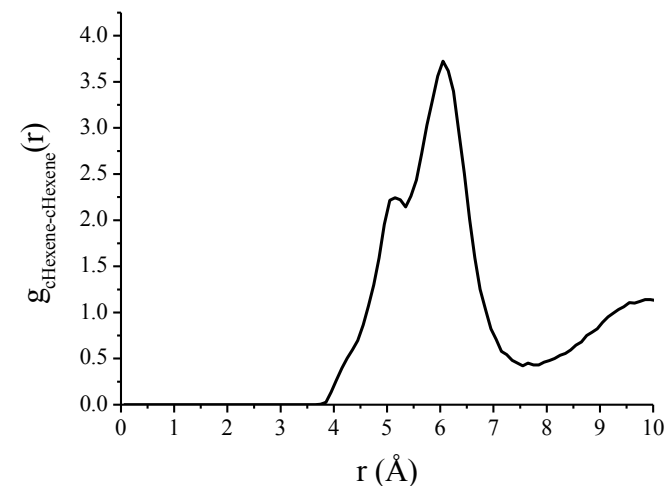
# 6:1:2 tertiary butanol:water:cyclohexene



$1.4 \pm 0.1$  between 4.0Å and 5.0Å  
 $7.5 \pm 0.3$  between 5.0Å and 7.5Å



$0.5 \pm 0.1$  between 2.3Å and 3.8Å



$\approx 4.2$  between 3.6Å and 7.5Å

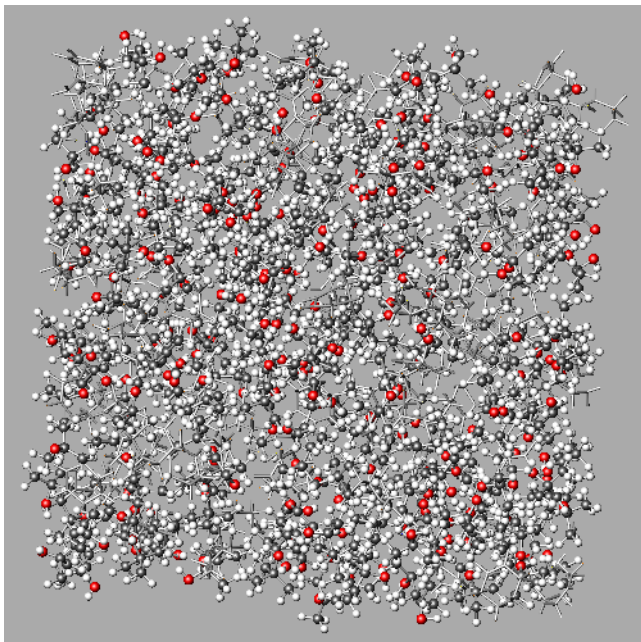
**Like - like interactions in the tri-molecular mixture**



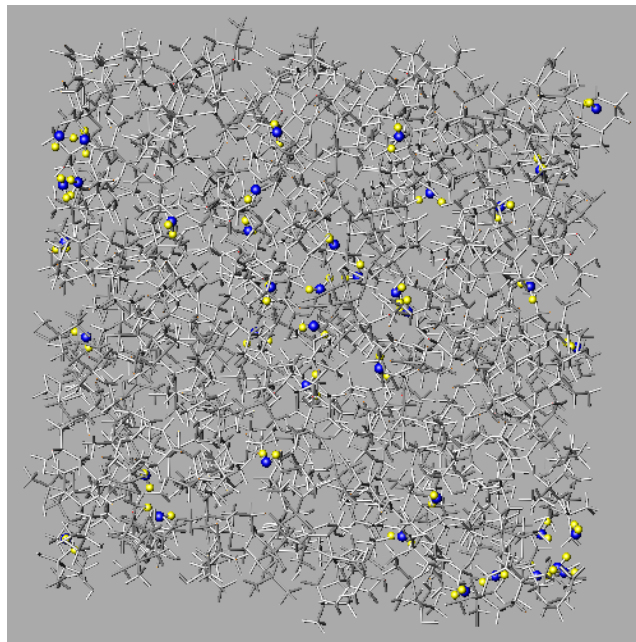
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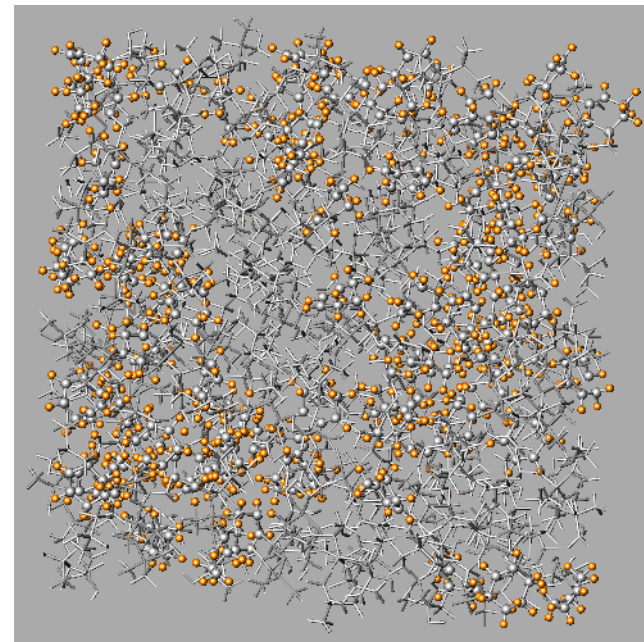
# 6:1:2 tertiary butanol:water:cyclohexene



Tertiary Butanol



Water



Cyclohexene

Mixing state of a 6:1:2 tertiary butanol-  
water-cyclohexene solution



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# The structure correlations in polymers



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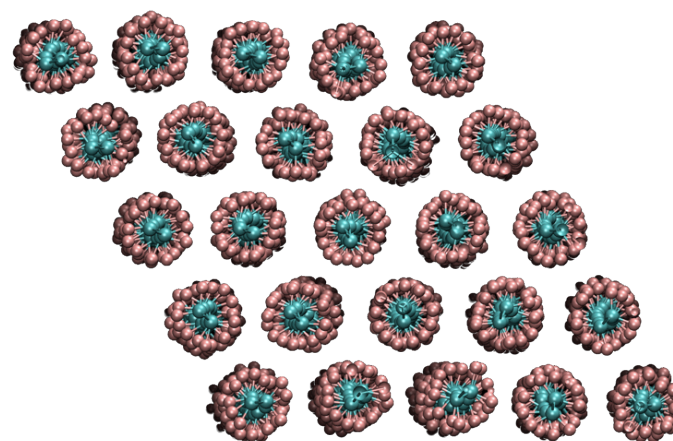
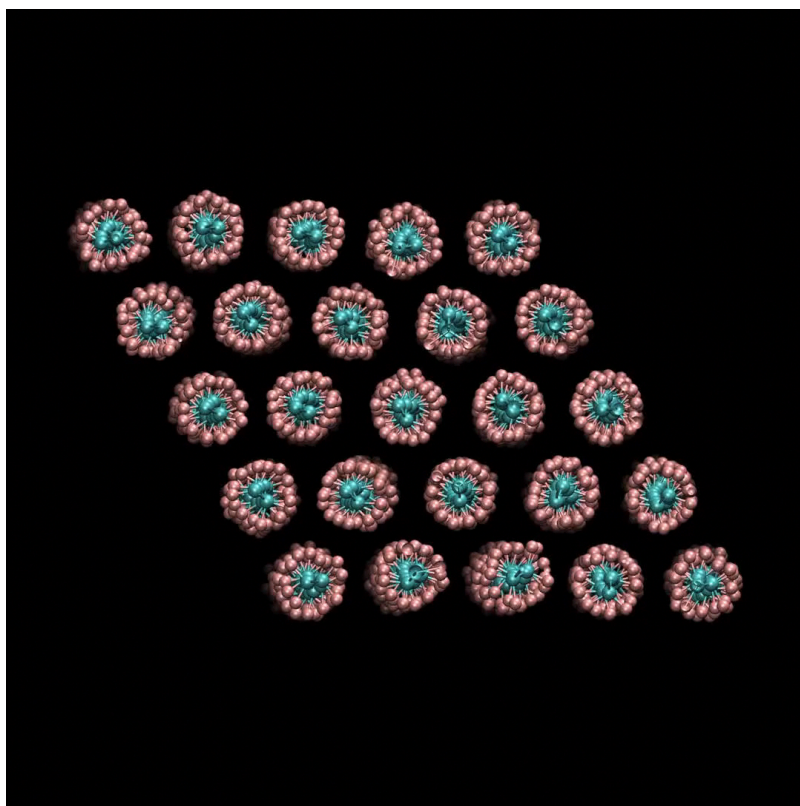
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# ***Total scattering – diffuse plus Bragg***

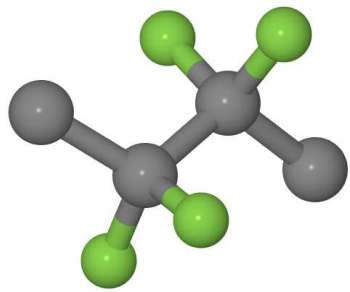
Structural disordered in crystalline and partially crystalline systems is a growing area of interest. Examples include the correlations between polymer chains in materials such as PTFE (crystalline) and Kelf (PCTFE) (disordered crystalline).

A.K.Soper, K.Page and A.Llobet, J. Phys.: Condens. Matter **25** 454219 (2013)



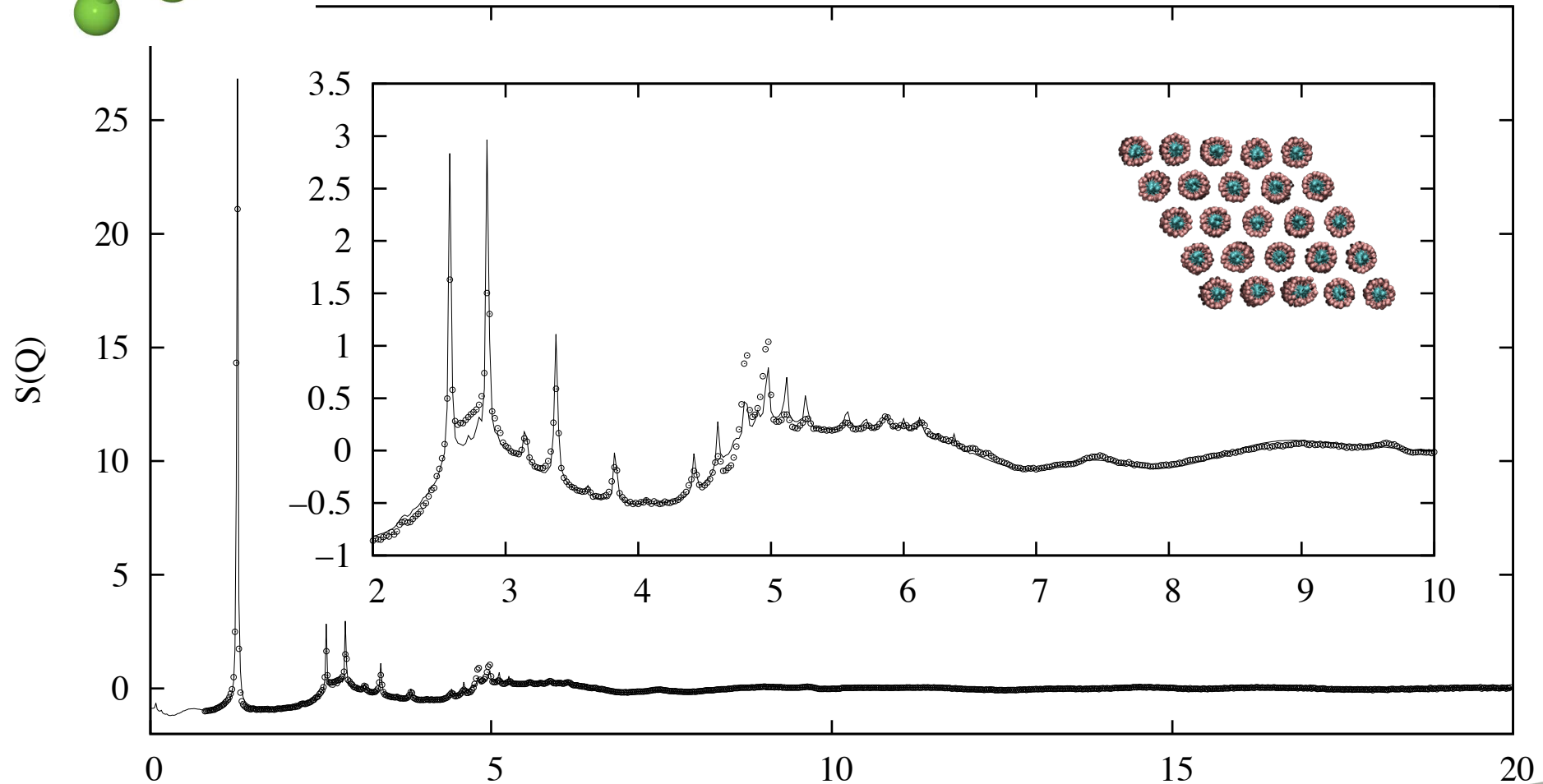
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# PTFE

Data from LANSCE: HIPD & NPDF



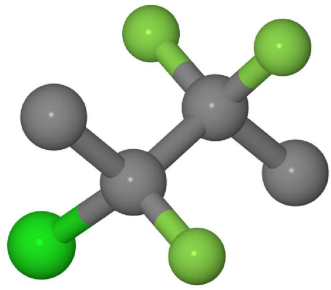
Refined model (EPSR) of crystalline PTFE  $Q$  [1/Å]  
with both diffuse and Bragg scattering  
features

A.K.Soper, K.Page and A.Llobet,  
*J. Phys.: Condens. Matter* **25** 454219 (2013)



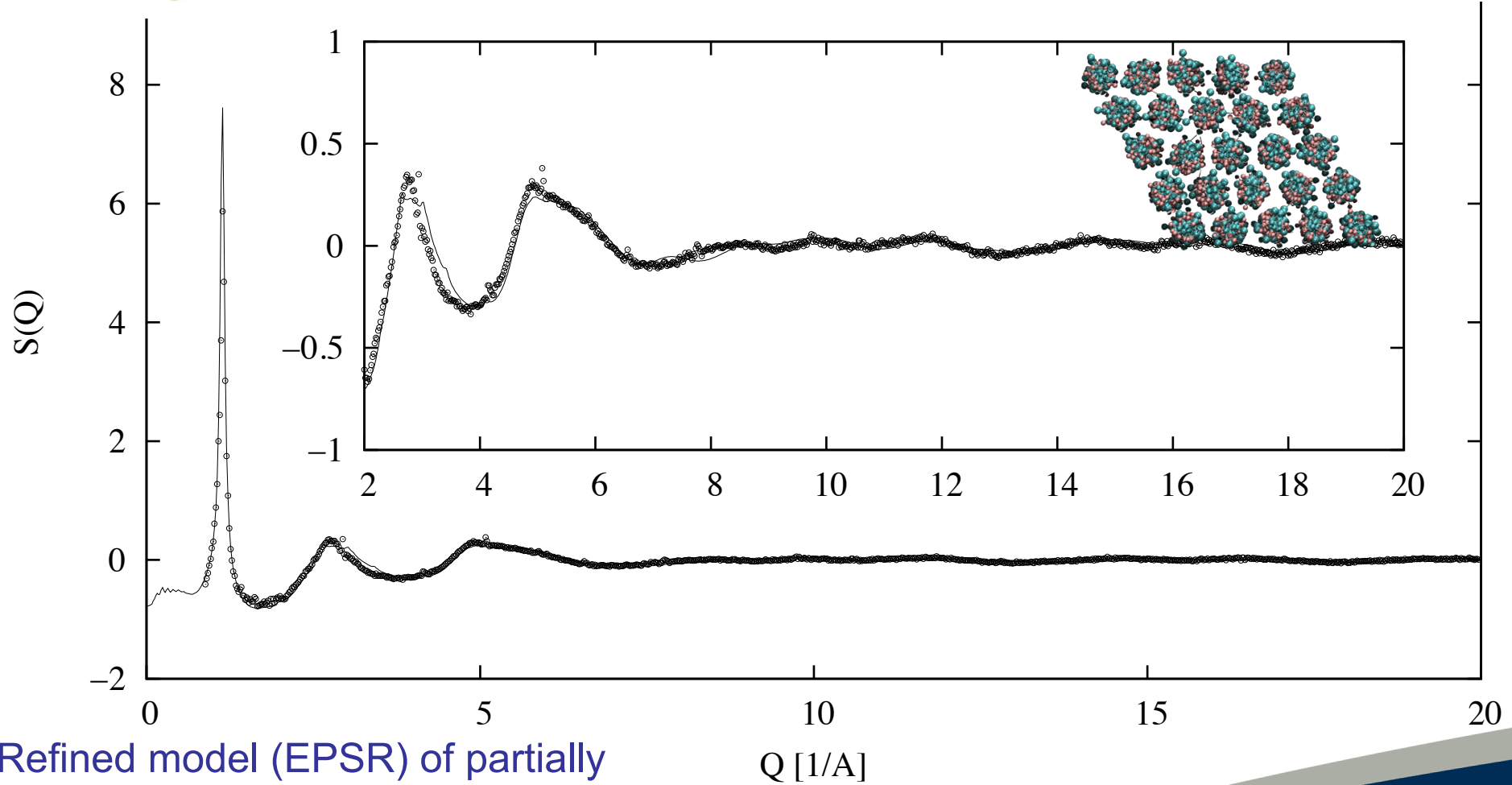
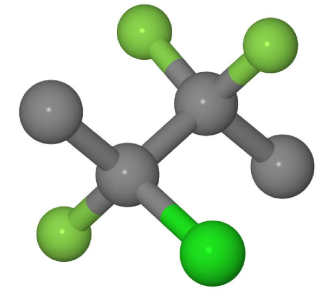
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# *KeIF (PCTFE)*

Data from LANSCE: HIPD & NPDF



Refined model (EPSR) of partially crystalline PCTFE with both diffuse and Bragg scattering features

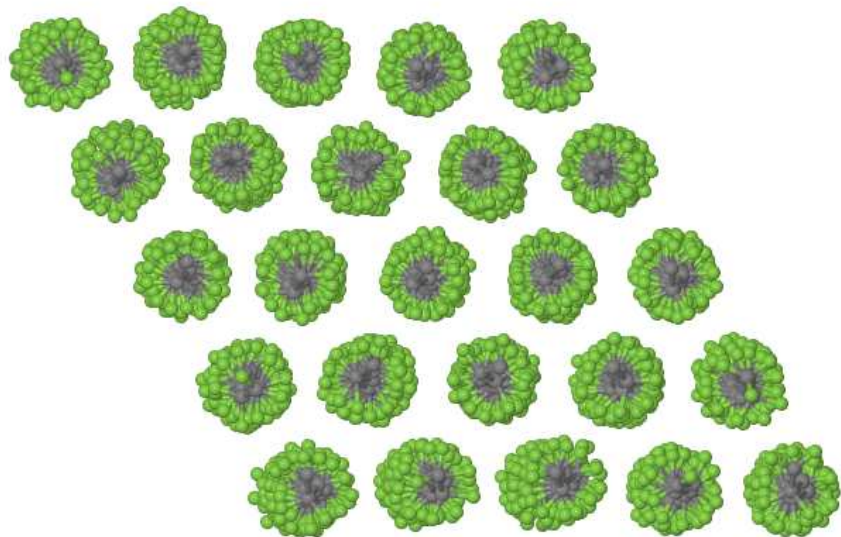
A.K.Soper, K.Page and A.Llobet,  
J. Phys.: Condens. Matter **25** 454219 (2013)



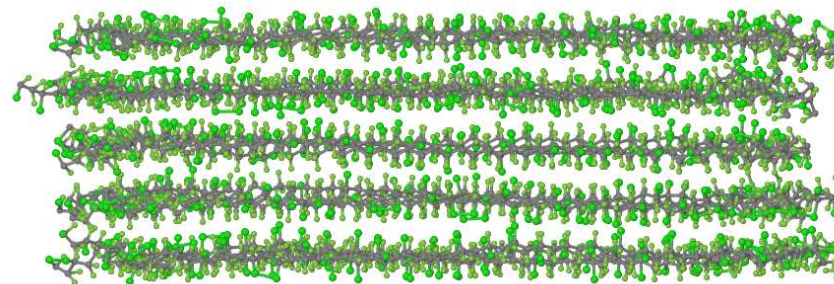
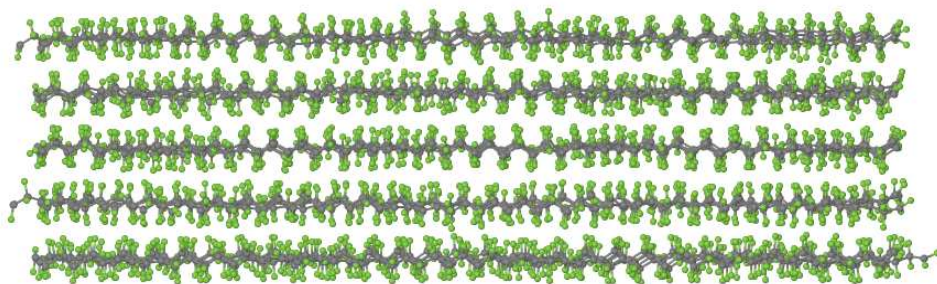
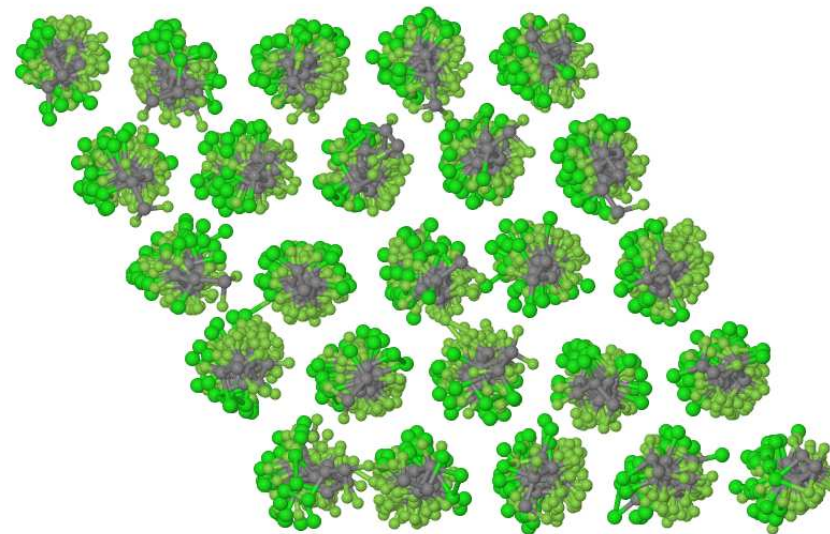
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# PTFE



# PCTFE



A.K.Soper, K.Page and A.Llobet,  
J. Phys.: Condens. Matter **25** 454219 (2013)



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# Interstellar Ice

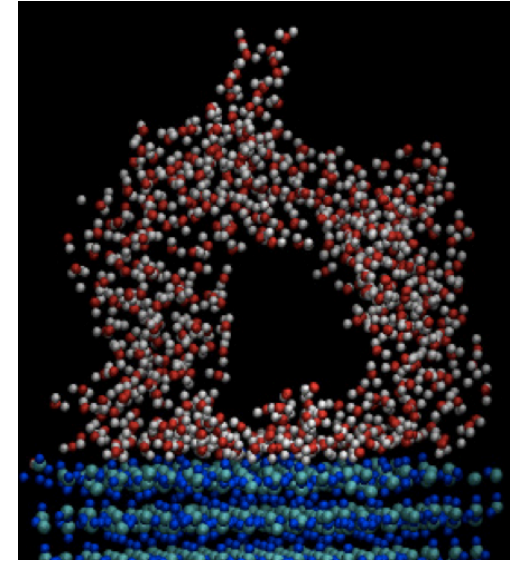


# Ice is thought to play an major role in astrophysical processes such as star formation



Credit: NASA

Ice in space forms as a porous amorphous solid and plays a role in promoting chemical reactions whilst also acting as a reservoir for trapping volatile gases



Credit: Helen Fraser

The collapse of interstellar gas clouds to form stars is governed by a balance between gravity and heat. Coolant gases moderate the kinetic effects of heat, via radiation, and act to promote cloud collapse. Porous ice is believed to help keep these gases present for longer periods of time.

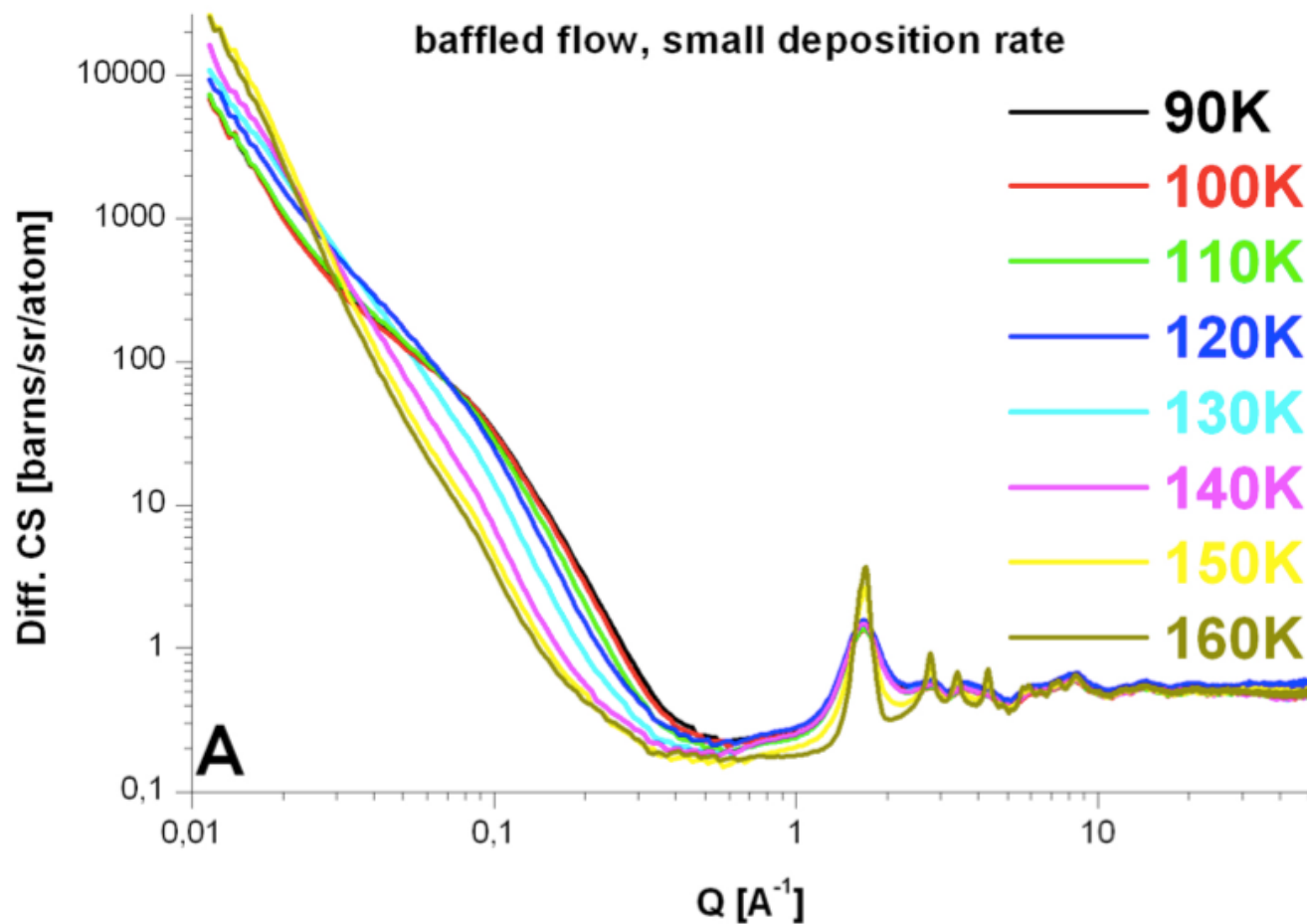
It is important to know how pores in amorphous ice behave as a function of temperature.



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# Neutron scattering from amorphous ice as it is warmed to 160K



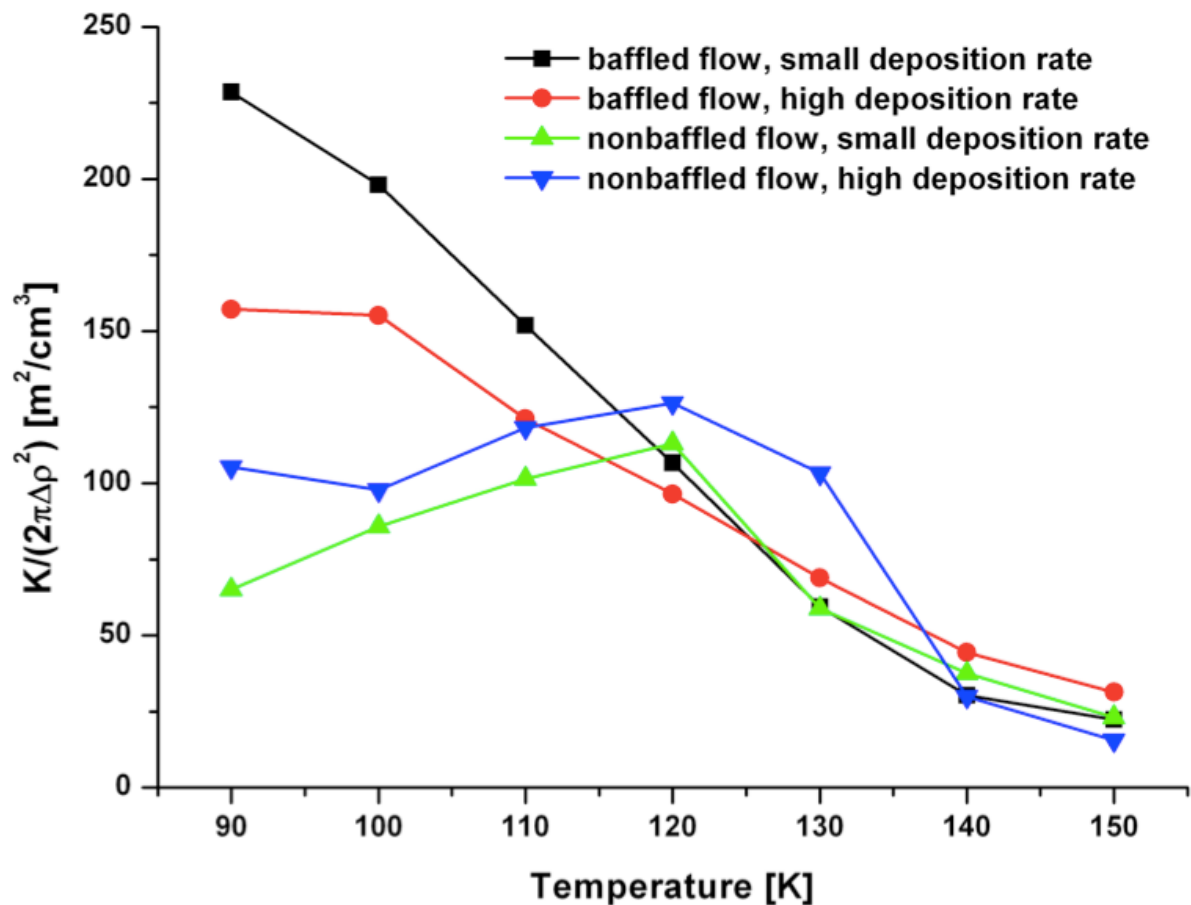
C.Mitterdorfer, M.Bauer, T.G.A.Youngs,  
D.T. Bowron, H.J.Fraser, J.L.Finney and  
T.Loerting PCCP **16** 16013 (2014)



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# Pore collapse is characterized by a continuous decrease in surface area



C.Mitterdorfer, M.Bauer, T.G.A.Youngs,  
D.T. Bowron, H.J.Fraser, J.L.Finney and  
T.Loerting PCCP **16** 16013 (2014)

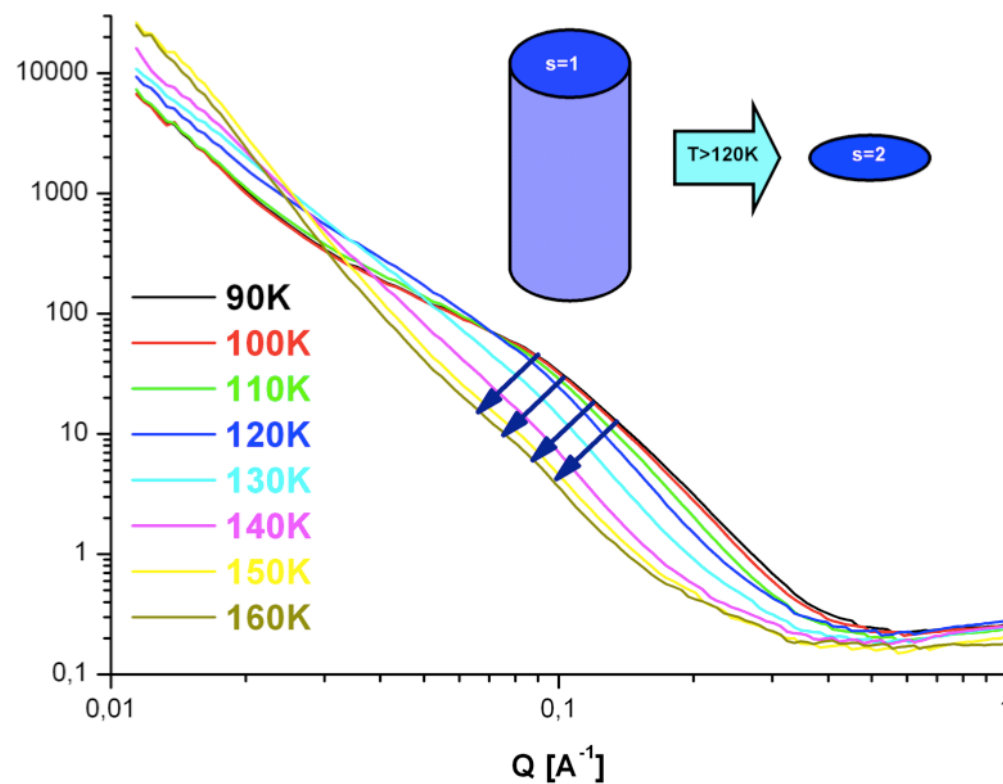
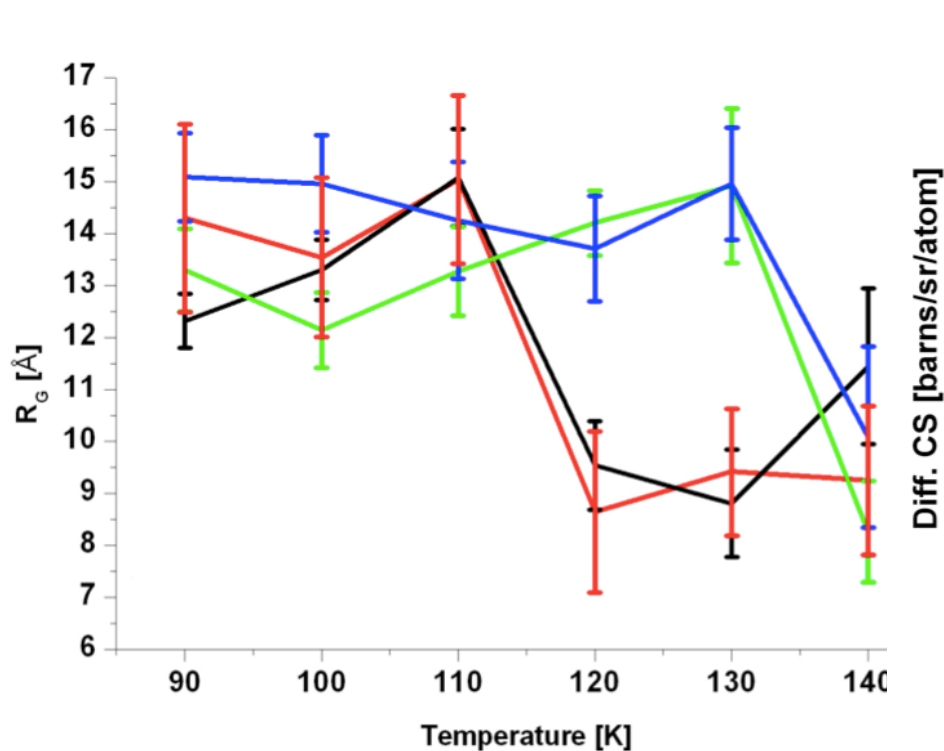


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# Pore collapse rapidly transitions from a three dimensional pore to a two dimensional pore of smaller radius of gyration



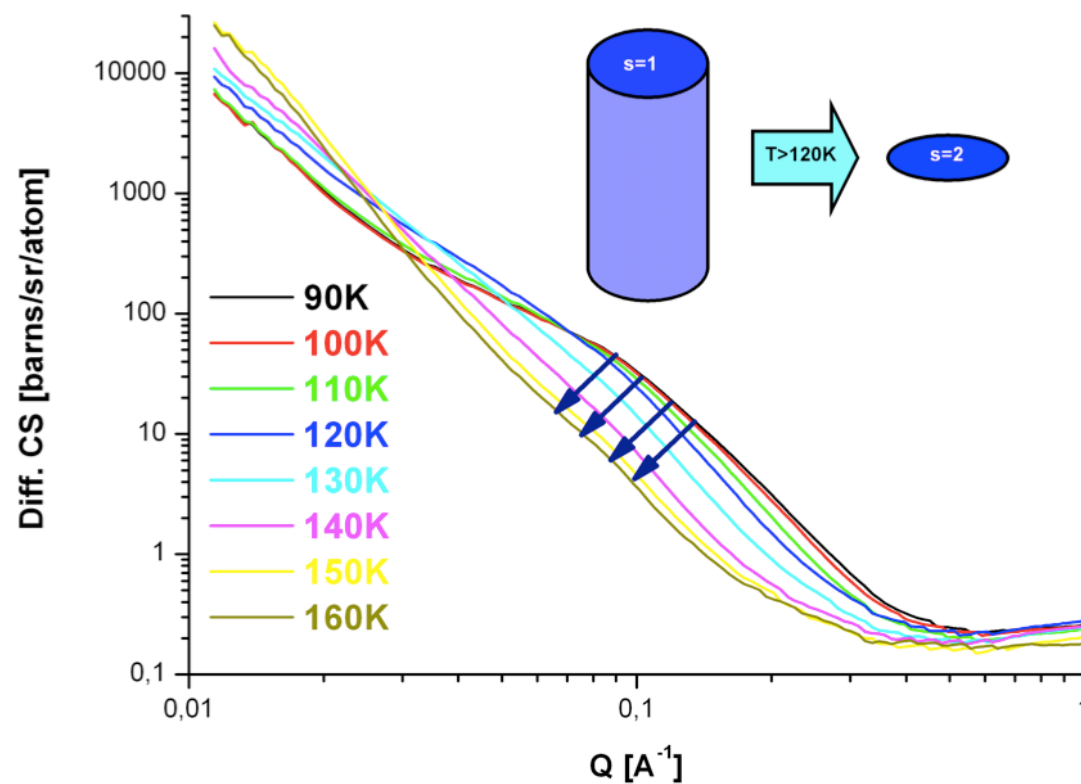
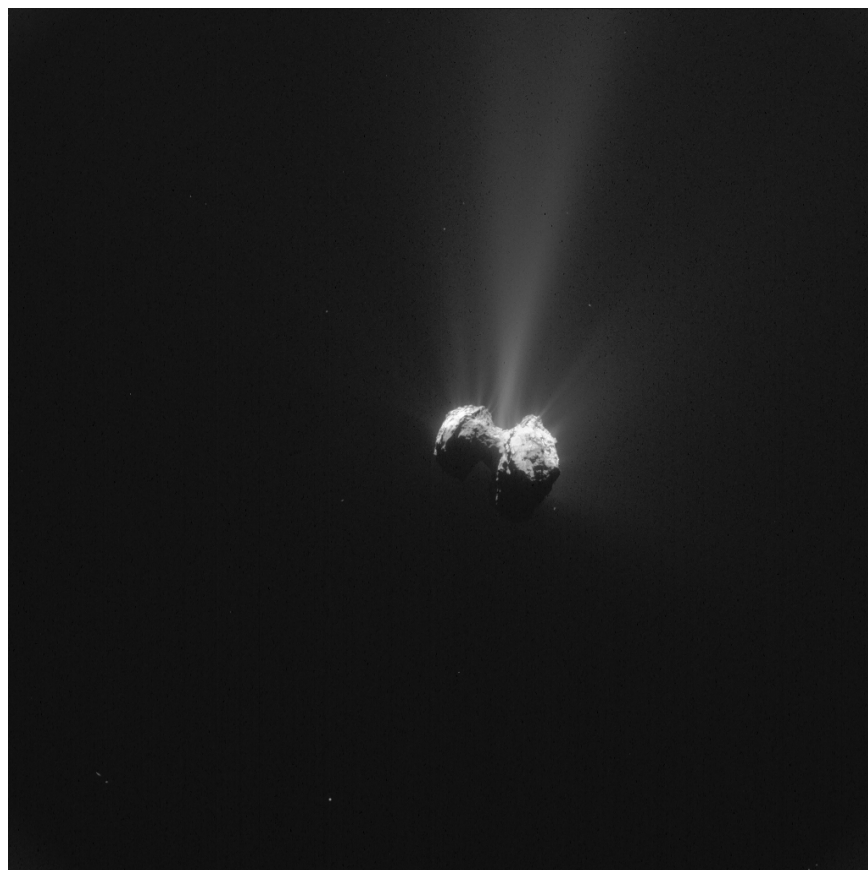
C.Mitterdorfer, M.Bauer, T.G.A.Youngs,  
D.T. Bowron, H.J.Fraser, J.L.Finney and  
T.Loerting PCCP **16** 16013 (2014)



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# Pore collapse rapidly transitions from a three dimensional pore to a two dimensional pore of smaller radius of gyration



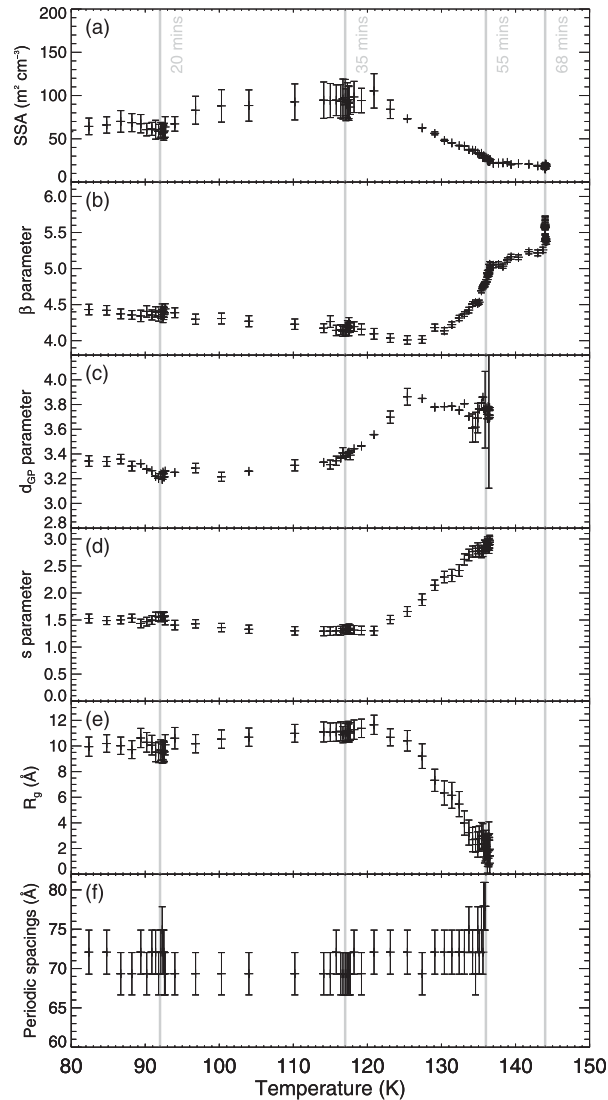
Rosetta: Comet 67P/Churyumov-Gerasimenko  
European Space Agency



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# Kinetic studies show that diffusive motion in porous ASW starts at 121K



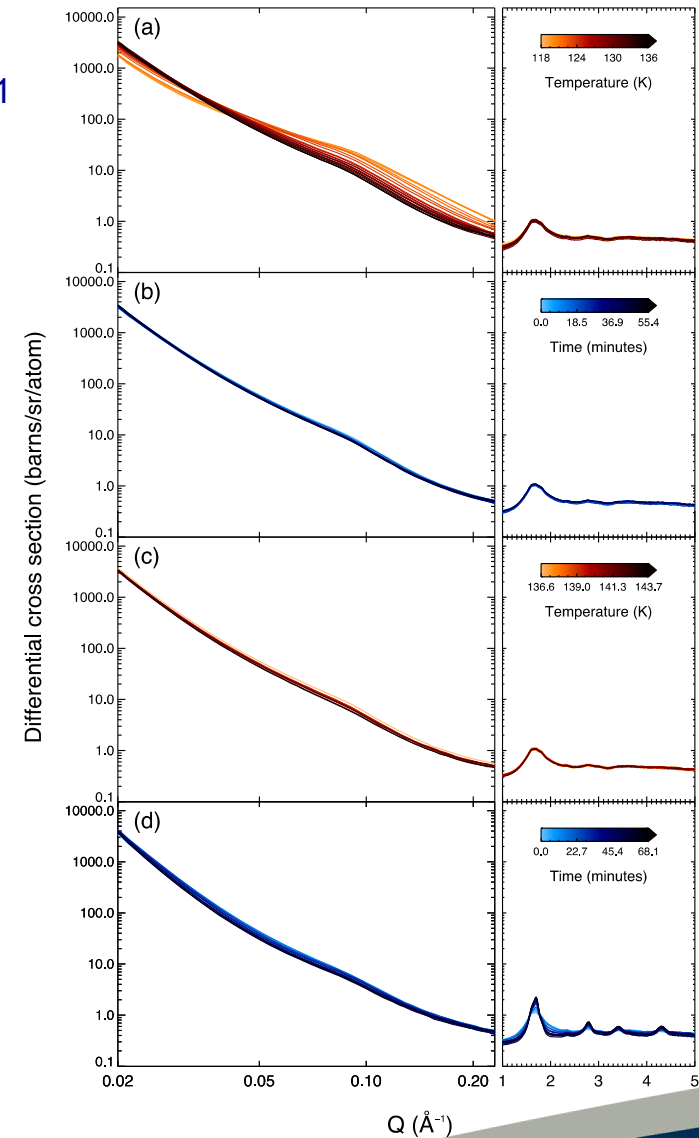
Heating @  $0.4 \text{ Kmin}^{-1}$

$T_{\text{non-trans start}} = 115\text{K}$

$T_{g,\text{start}} = 121\text{K}$

$T_{g,\text{end}} = 136\text{K}$

$T_x = 141\text{K}$



C.R.Hill, C.Mitterdorfer, T.G.A.Youngs,  
D.T.Bowron, H.J.Fraser and T.Loerting  
Phys. Rev. Lett. **116** 215501 (2016)



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# Summary: Issues we will aim to highlight in this workshop

**Issue 1:** The diversity of science that can be probed using neutron total scattering and PDF methods

**Issue 2:** Key aspects of the instrumentation that is required to make the measurements

**Issue 3:** The analysis methodologies that are required to extract the scientific information in the measured data.

**Issue 4:** Structure refinement of liquid and disordered materials data using atomistic models



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# Empirical Potential Structure Refinement Workshop 2017

Thursday 16<sup>th</sup> February – Friday 17<sup>th</sup> February 2017

The Cosener's House, Abingdon, Oxfordshire, UK

A two-day course providing

An introduction to liquids and disordered materials structure refinement

Basic training in EPSR25 and EPSRgui

Examples of application to glasses, liquids and complex systems

Training in a range structure characterization tools:

Radial Distribution Functions

Coordination Numbers

Bond Angle Distributions

Spatial Density Functions

Orientalional Correlation Functions

## Course tutors

Alan Soper

Daniel Bowron

Sam Callear

Tom Headen

Tristan Youngs