

Diffractionometers GEM and Polaris: Instruments for Total Scattering from Crystalline Materials

David Keen

ISIS Facility

Rutherford Appleton Laboratory

Total scattering from crystalline powders

$$g_{ij}(r) - 1 = \frac{1}{(2\pi)^3 \rho_0} \int_0^\infty 4\pi Q^2 [A_{ij}(Q) - 1] \frac{\sin Qr}{Qr} dQ$$

Total scattering from crystalline powders

$$g_{ij}(r) - 1 = \frac{1}{(2\pi)^3 \rho_0} \int_0^\infty 4\pi Q^2 [A_{ij}(Q) - 1] \frac{\sin Qr}{Qr} dQ$$

- As high a maximum Q as possible; correlations (bonds) can be sharp so high- Q data contains real information.

$$Q = 4\pi \sin\theta / \lambda$$

- As good a Q -resolution as possible; Bragg peaks are sharp!

$$dQ / Q \approx d\theta / \tan\theta (+ d\lambda / \lambda +)$$

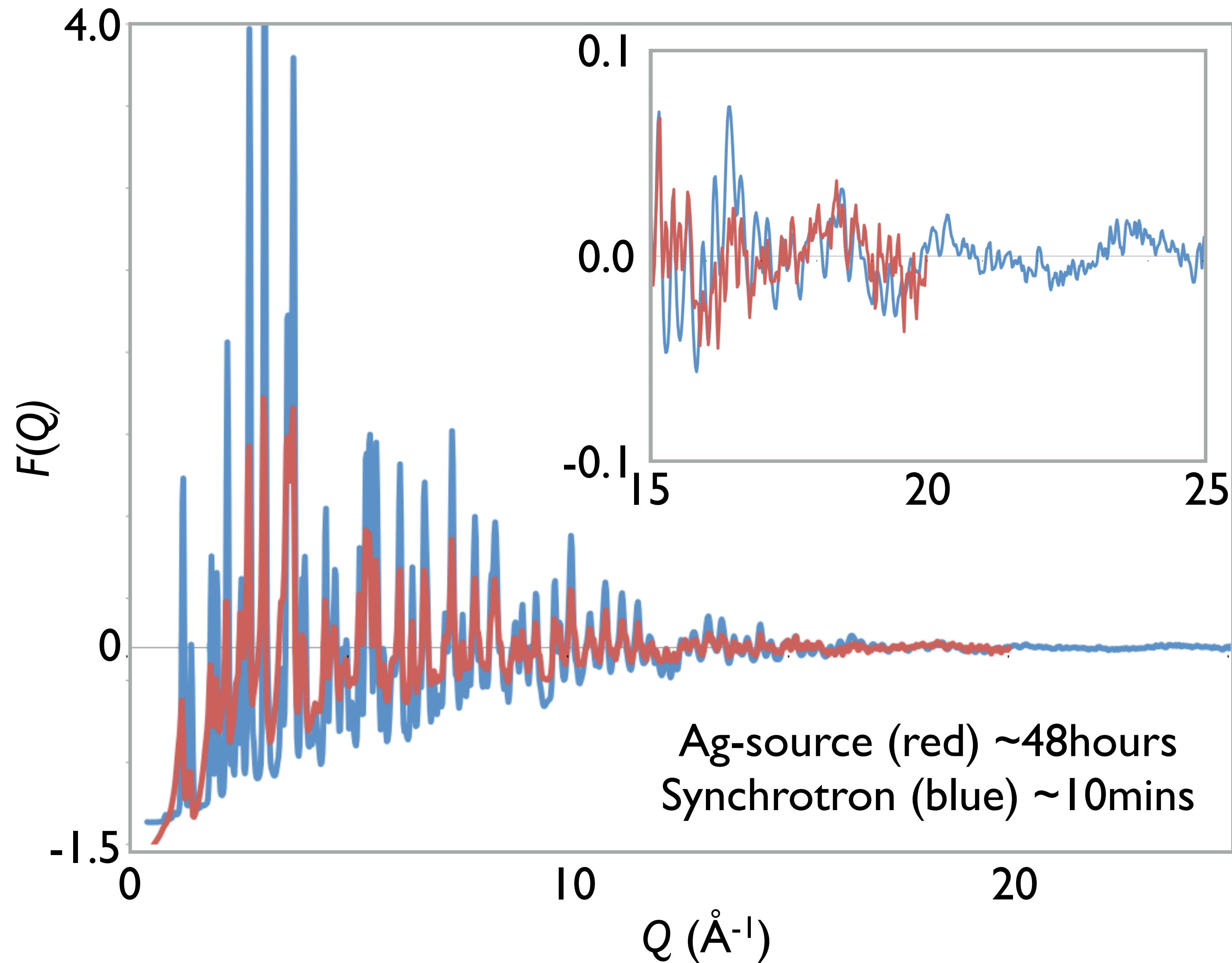
- Hence high scattering angles, 2θ , and short wavelengths, λ , are good.
- High count-rates; especially at high- Q

Total scattering from crystalline powders

Lab-source X-ray vs. Synchrotron X-ray

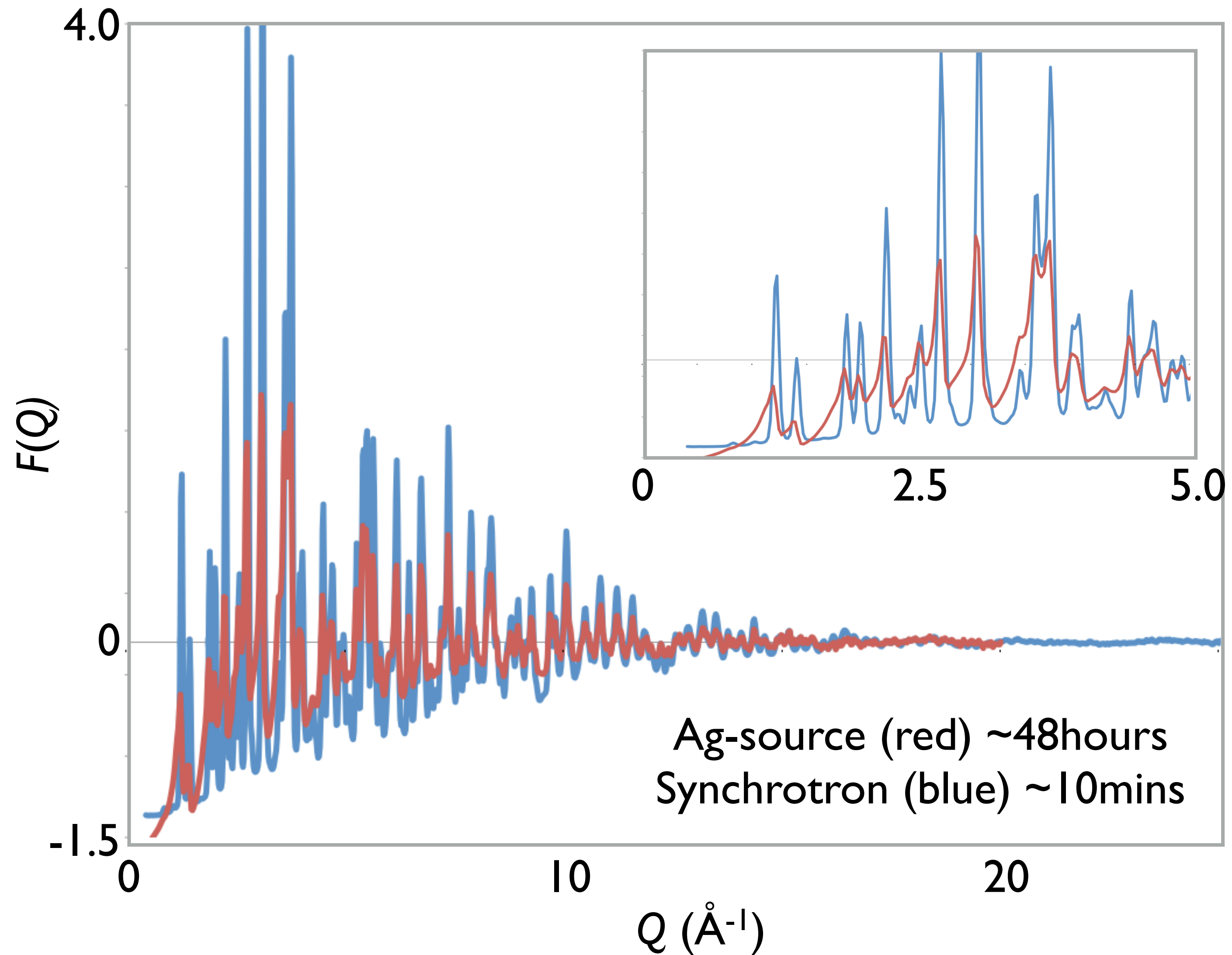
Total scattering from crystalline powders

Lab-source X-ray vs. Synchrotron X-ray



Total scattering from crystalline powders

Lab-source X-ray vs. Synchrotron X-ray



Total scattering from crystalline powders

Reactor neutron vs. Spallation neutron

Total scattering from crystalline powders

Reactor neutron vs. Spallation neutron

Reactor

- Single wavelength
- Low Q -resolution
- Limited $Q_{\max} \sim 24 \text{ \AA}^{-1}$
- Higher neutron flux
- More restricted scattering geometry
- Simpler data analysis

Spallation source

- Polychromatic
- High Q -resolution
- High $Q_{\max} \sim 50 \text{ \AA}^{-1}$
- Lower neutron flux
- Less restricted scattering geometry
- More complex data analysis

Total scattering from crystalline powders

Synchrotron X-ray vs. Spallation neutron

Total scattering from crystalline powders

Synchrotron X-ray vs. Spallation neutron

X-ray

- High Q -resolution
- Lower $Q_{\max} \sim 35 \text{ \AA}^{-1}$
- High flux, rapid measurements
- Approximately normalised data

Neutron

- High Q -resolution
- High $Q_{\max} \sim 50 \text{ \AA}^{-1}$
- Lower flux, longer measurements
- Absolutely normalised structure factors

...or combine X-ray and neutron measurements

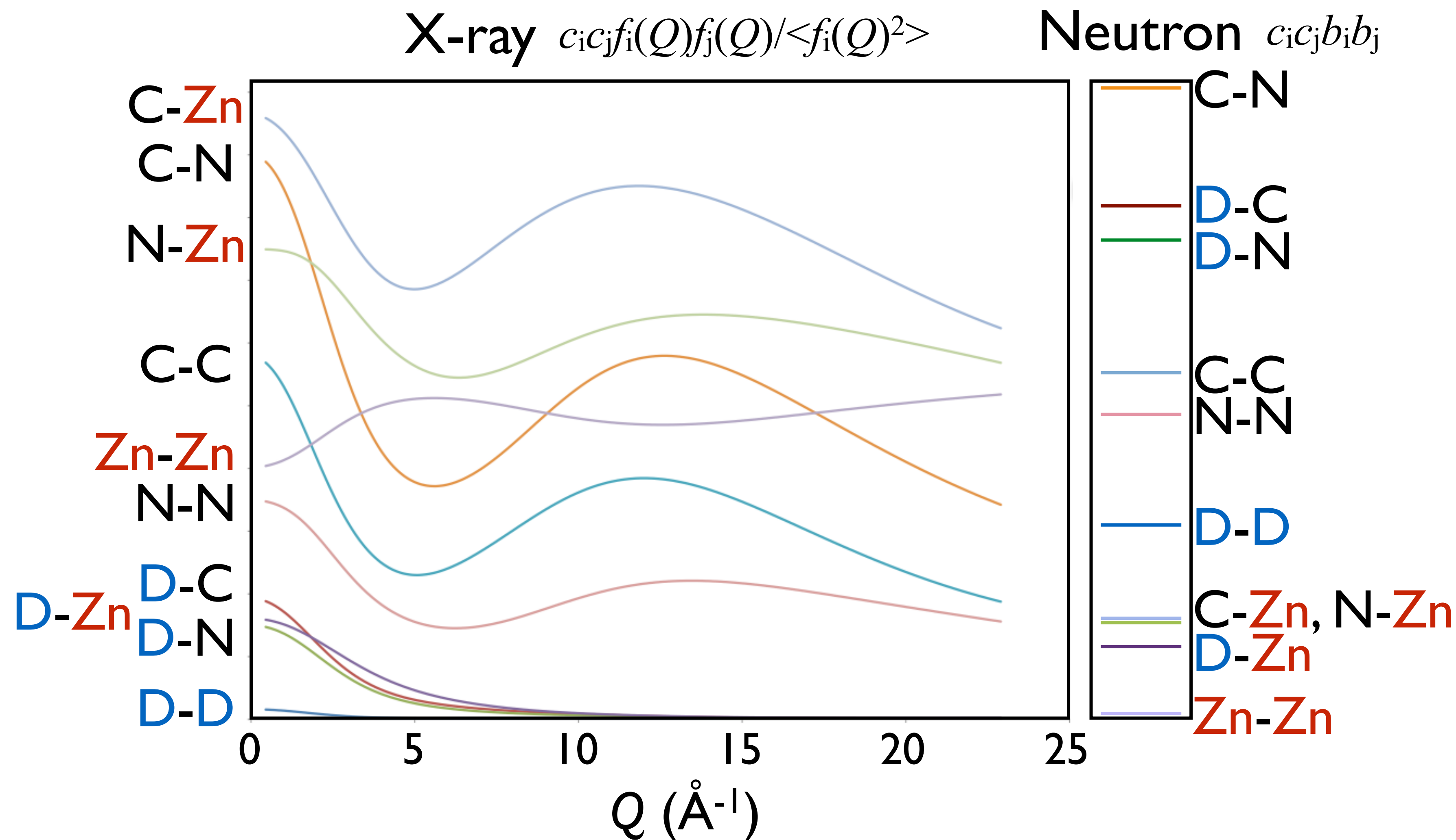
$$F(Q) = \sum_{i,j=1}^n c_i c_j \bar{b}_i \bar{b}_j [A_{ij}(Q) - 1]$$

e.g. MOF $\text{Zn}(\text{C}_3\text{N}_2\text{H}_3)_2$

...or combine X-ray and neutron measurements

$$F(Q) = \sum_{i,j=1}^n c_i c_j \bar{b}_i \bar{b}_j [A_{ij}(Q) - 1]$$

e.g. MOF $\text{Zn}(\text{C}_3\text{N}_2\text{H}_3)_2$



Summary: Use Central Facilities!

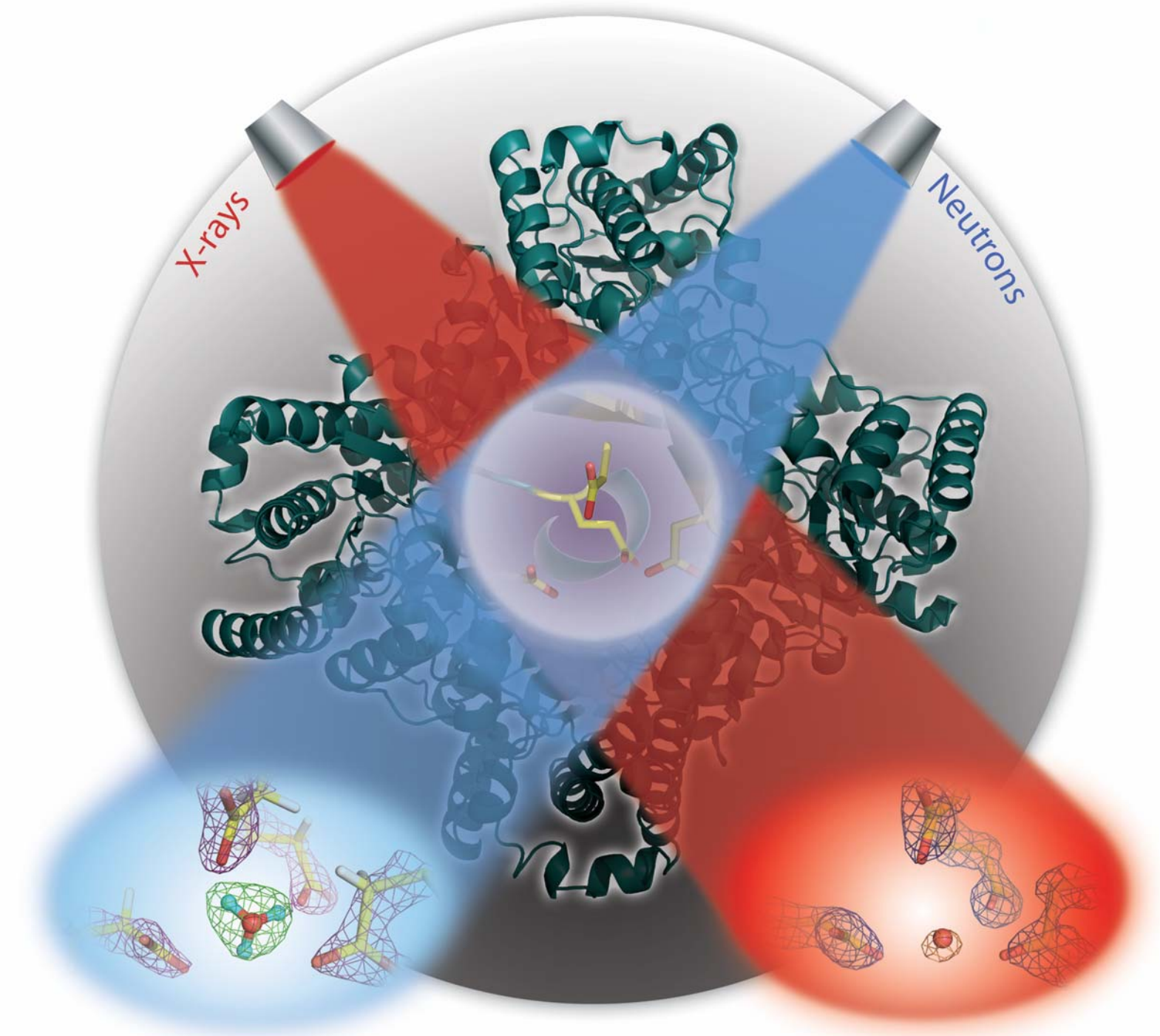
- Neutrons and x-rays 'see' things differently

$$F(Q) = \sum_{i,j=1}^n c_i c_j \bar{b}_i \bar{b}_j [A_{ij}(Q) - 1]$$

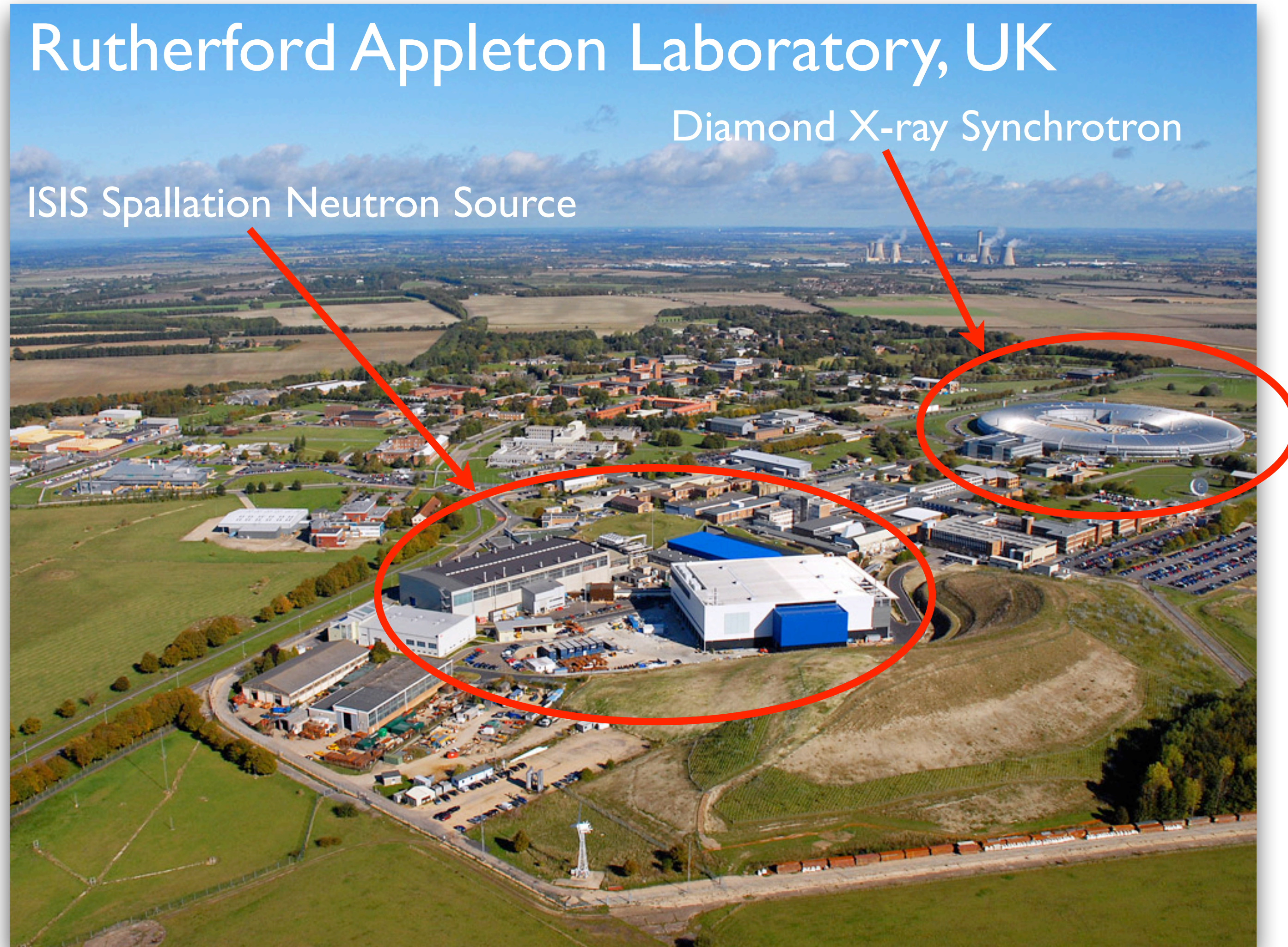
- Data may be measured faster, to higher resolution and with greater precision

$$g_{ij}(r) - 1 = \frac{1}{(2\pi)^3 \rho_0} \int_0^\infty 4\pi Q^2 [A_{ij}(Q) - 1] \frac{\sin Qr}{Qr} dQ$$

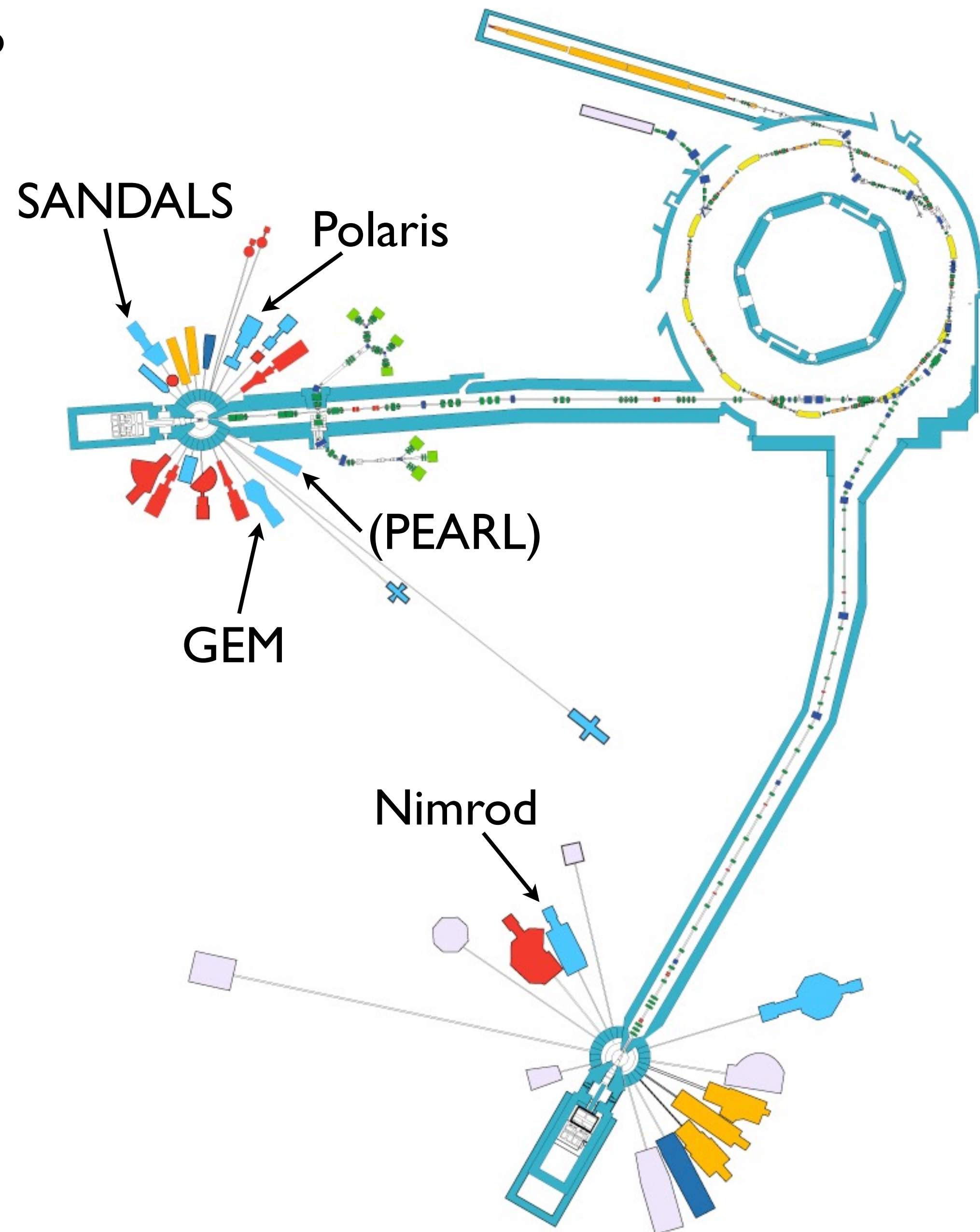
- (Spallation) neutron PDF is still the 'gold standard'!
- The resources are there...with more being built



Central facilities for total scattering



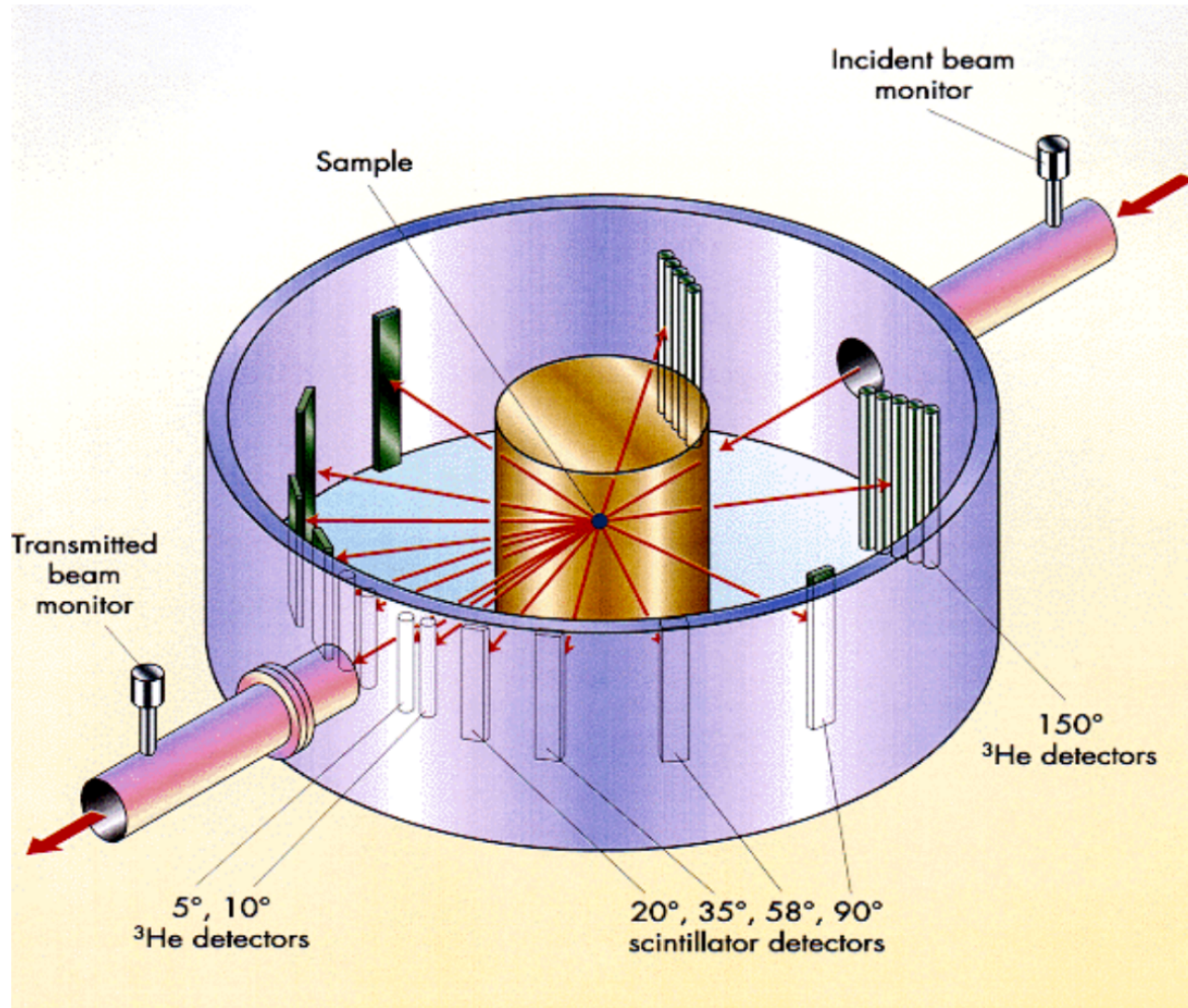
Total scattering instruments at ISIS



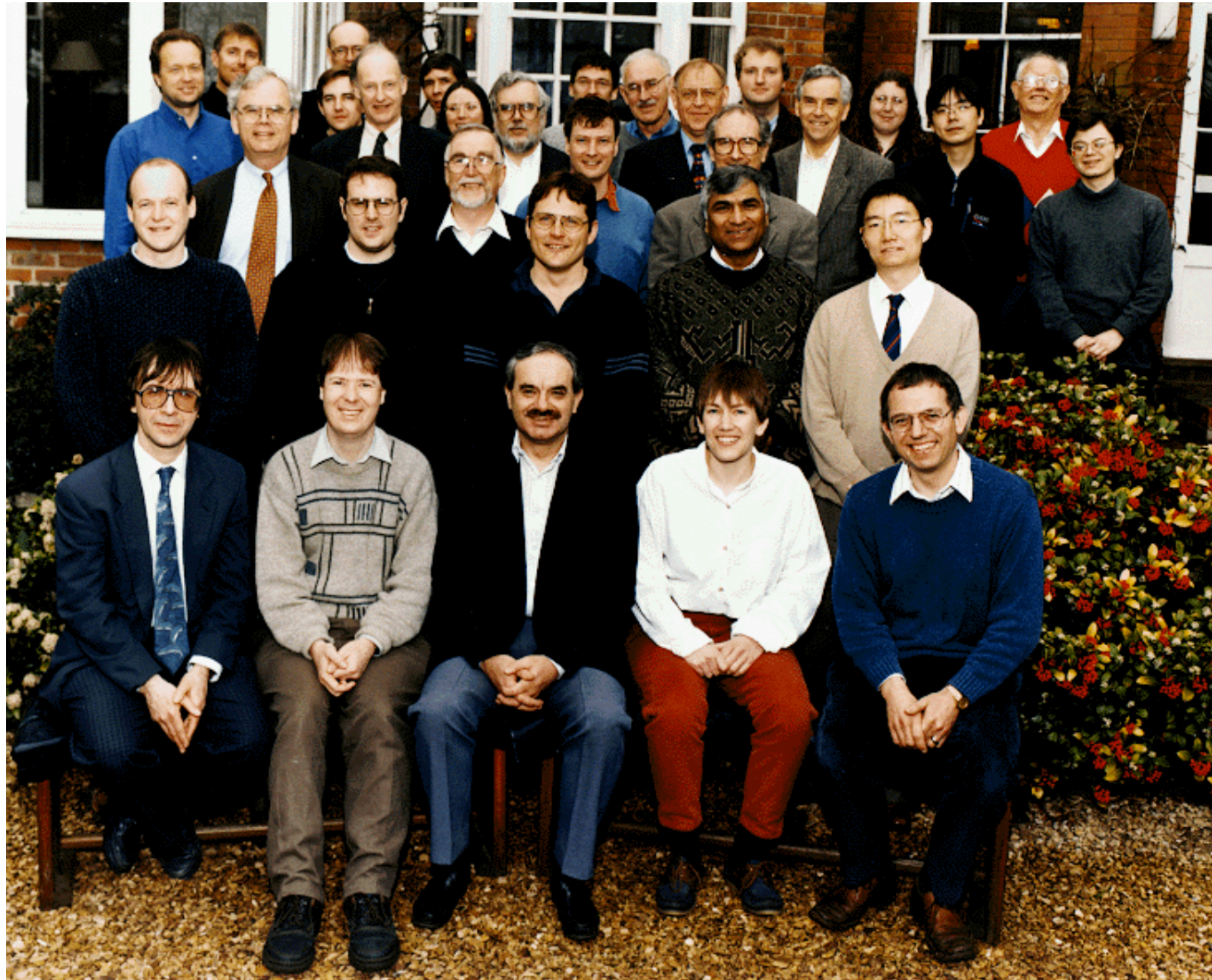
The Liquids and Amorphous Diffractometer (1982-1998)



The LAD diffractometer at ISIS (1984 - 1998)



LAD farewell meeting March 1999



LAD farewell meeting March 1999



LAD instrument parameters

LAD (1984–1998)

- Moderator Methane @ 110K
- Primary flight path 10 m
- Wavelength range $\sim 0.1 - 10 \text{ \AA}$
- Detector banks 7
- Detector coverage 0.016 steradians
- Resolution DQ/Q 14 – 0.6%

Lessons learnt:

Stability

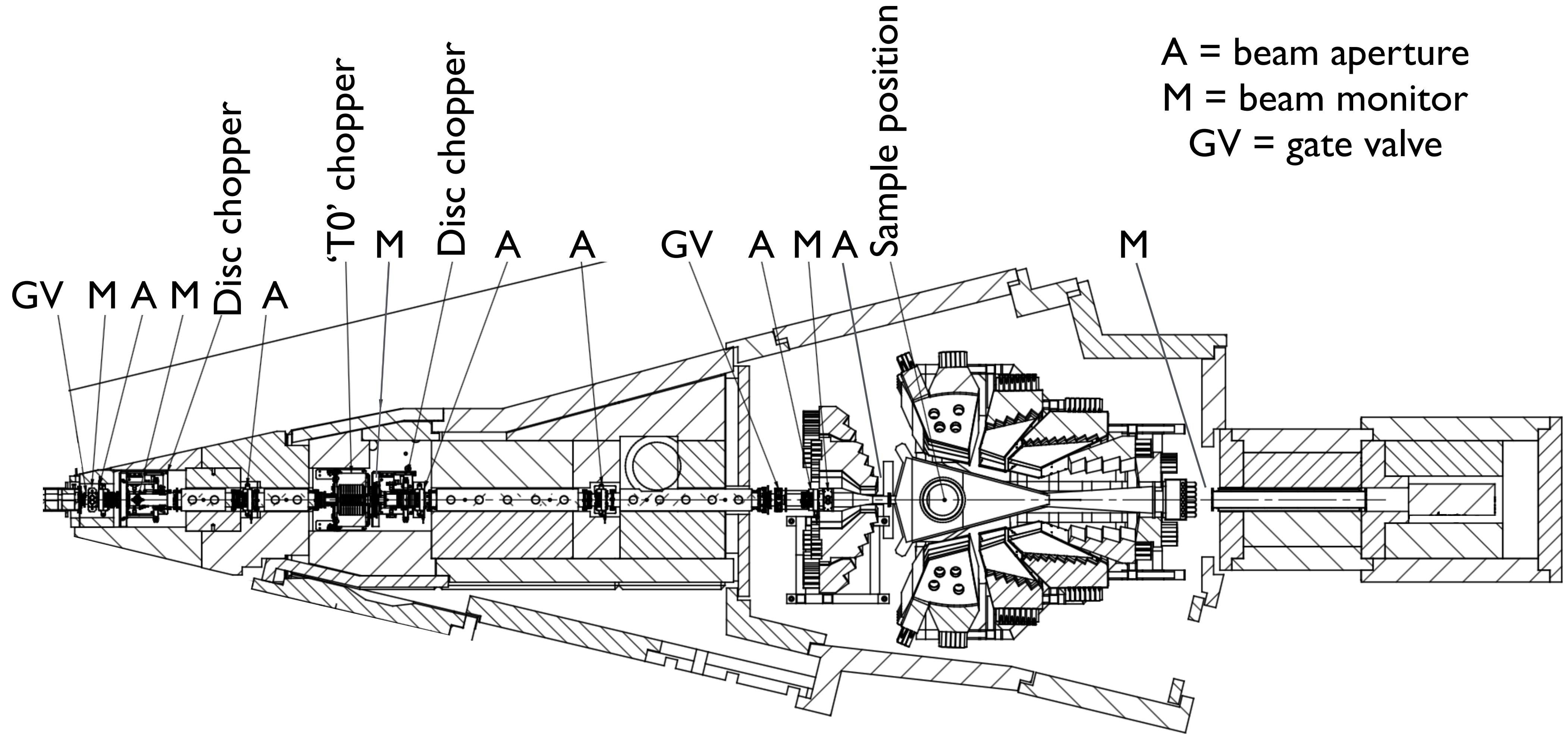
Low backgrounds

High count-rate

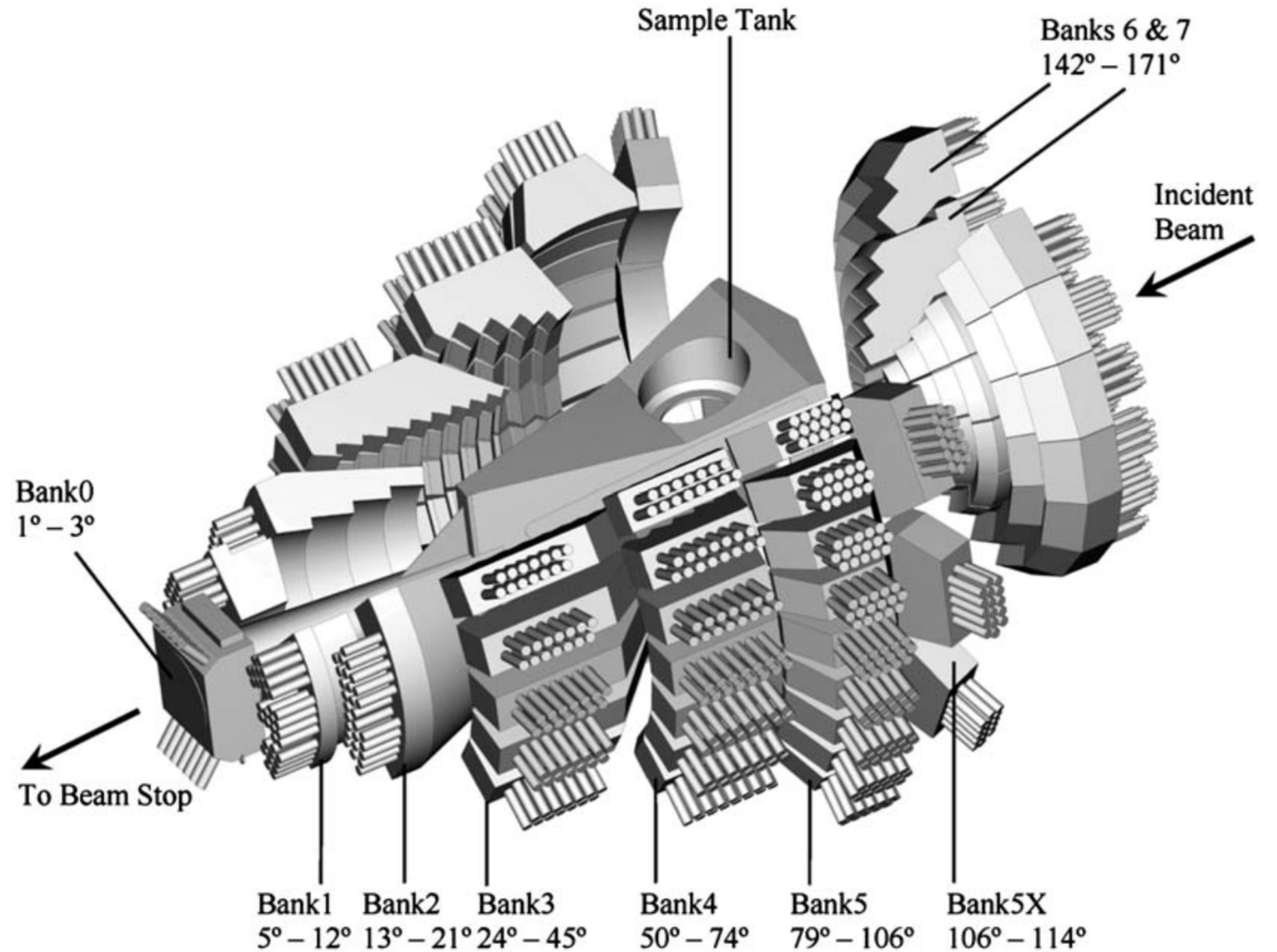
Good angle coverage

Short(er) wavelengths

The GEM total scattering diffractometer at ISIS



The GEM total scattering diffractometer at ISIS



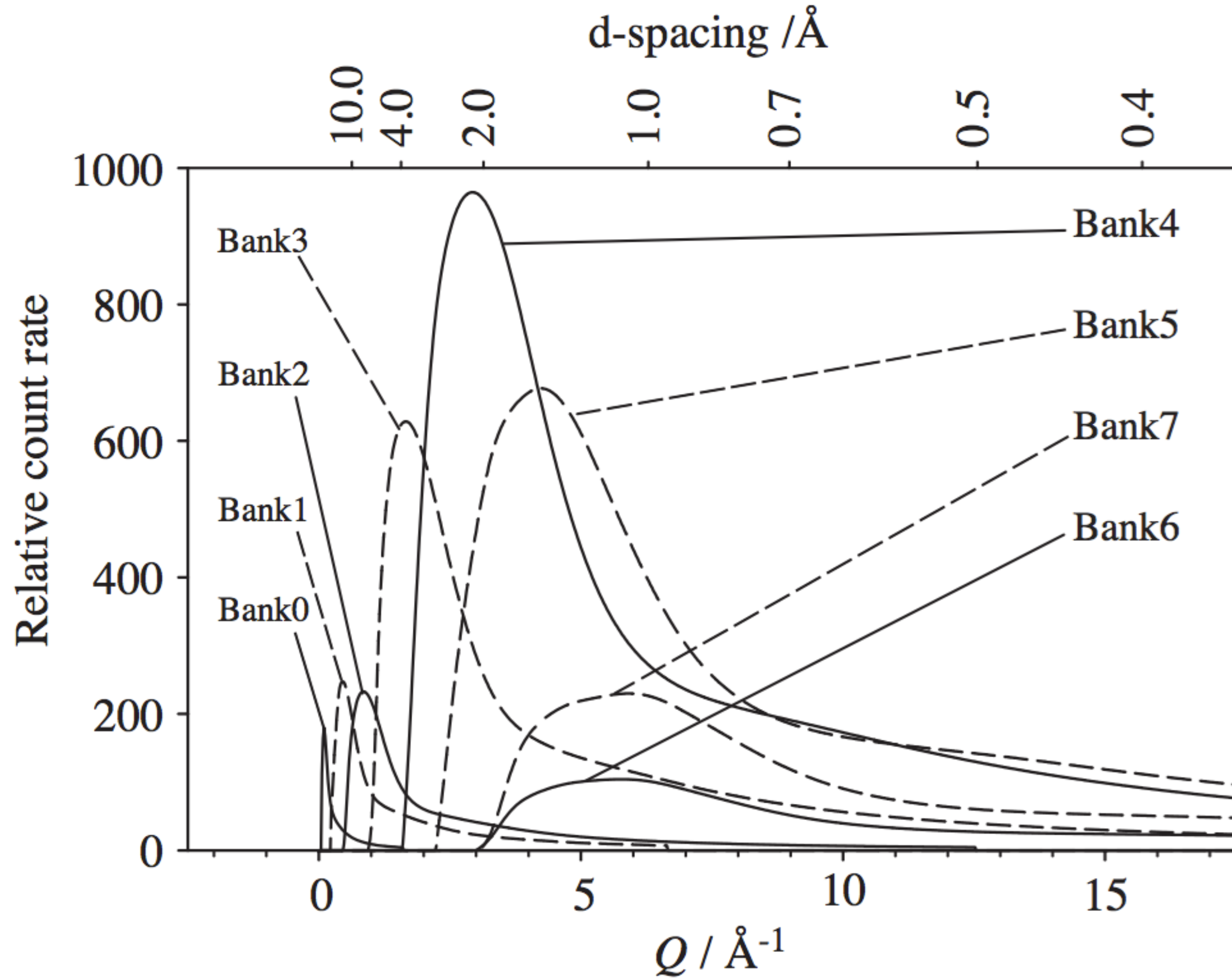
GEM and LAD instrument parameters

	<i>LAD (1984–1998)</i>	<i>GEM (~1999–)</i>
● Moderator	Methane @110K	Methane @110K
● Primary flight path	10 m	17m
● Wavelength range	~0.1 – 10Å	~0.1 – 3.4Å
● Detector banks	7	7 (8)
● Detector coverage	0.016 steradians	3.86st
● Resolution DQ/Q	14 – 0.6%	~10 – 0.34%

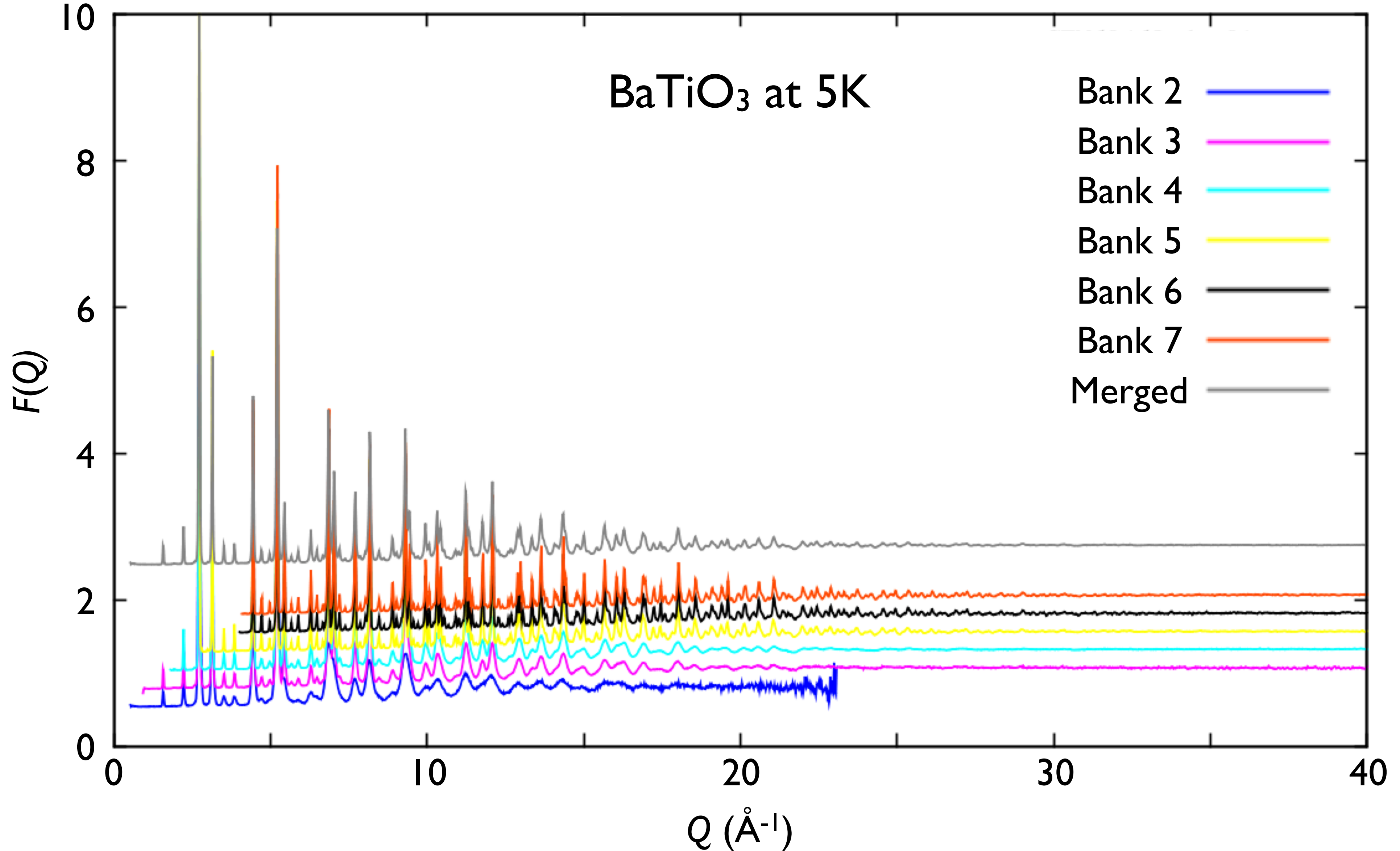
GEM detector coverage

Detector Bank	Scattering angle, 2θ (°)	Azimuthal angle, ϕ (°)	$L2$ (m)	Solid angle (st)	$\Delta Q/Q$ (%)	Q_{\min} (Å ⁻¹)
0	1.2-3.2	±90	~2.76	0.008	5-10	0.04
1	5.3-12.7	±45	~2.37	0.056	4.7	0.17
2	13.4-21.6	±43.4	1.48-2.10	0.093	2.4	0.43
3	24.7-45.6	±42.5	1.08-1.89	0.478	1.7	0.79
4	50.1-74.7	±44.4	1.03-1.44	0.988	0.79	1.56
5	79.1-114.2	±44.5	~1.38	1.513	0.51	2.95
6	142.5-149.7	±69.3	1.54-1.74	0.280	0.34	3.50
7	150.0-171.4	±66.6	1.04-1.39	0.443	0.35	3.57

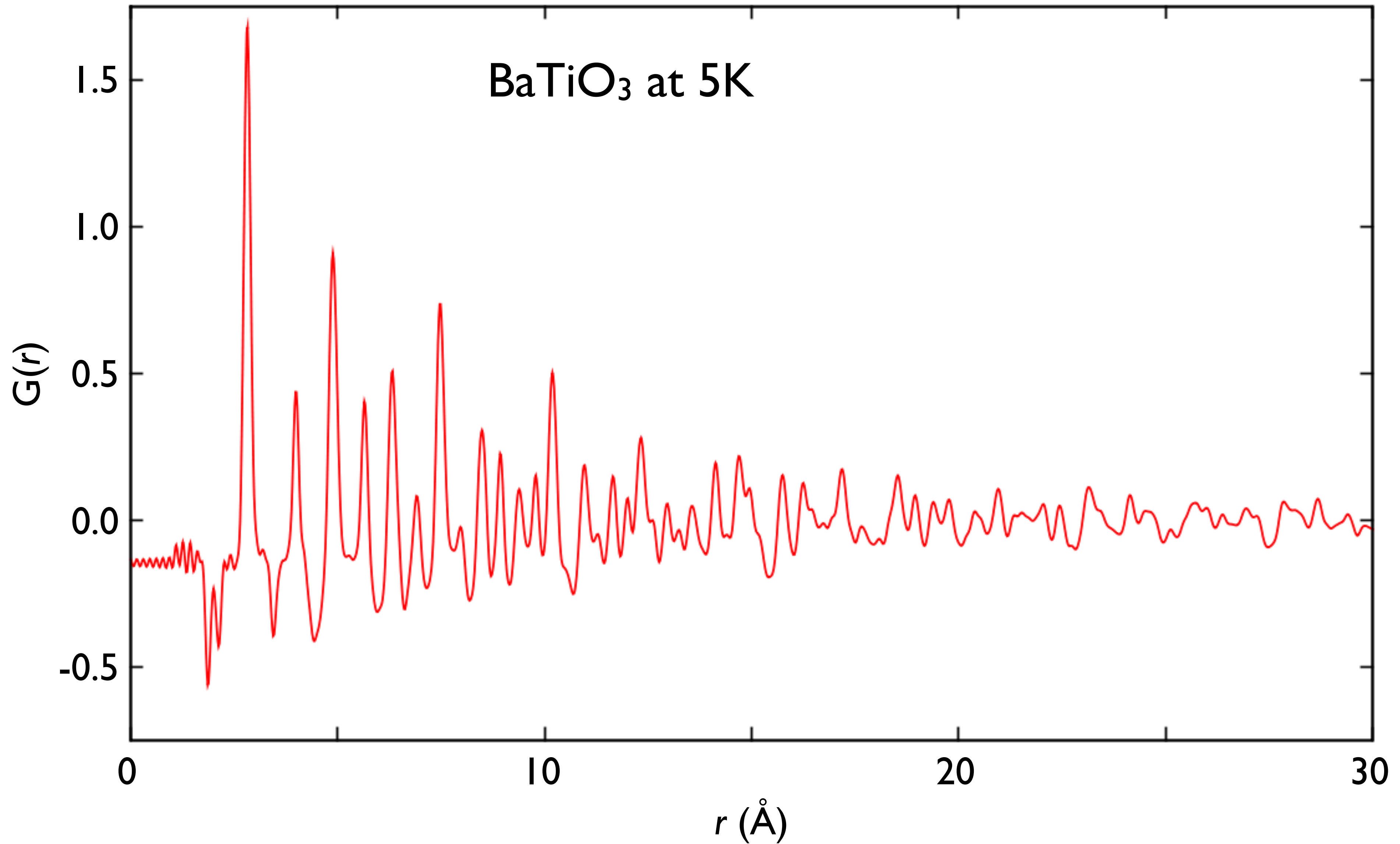
Relative count-rate of GEM detector banks



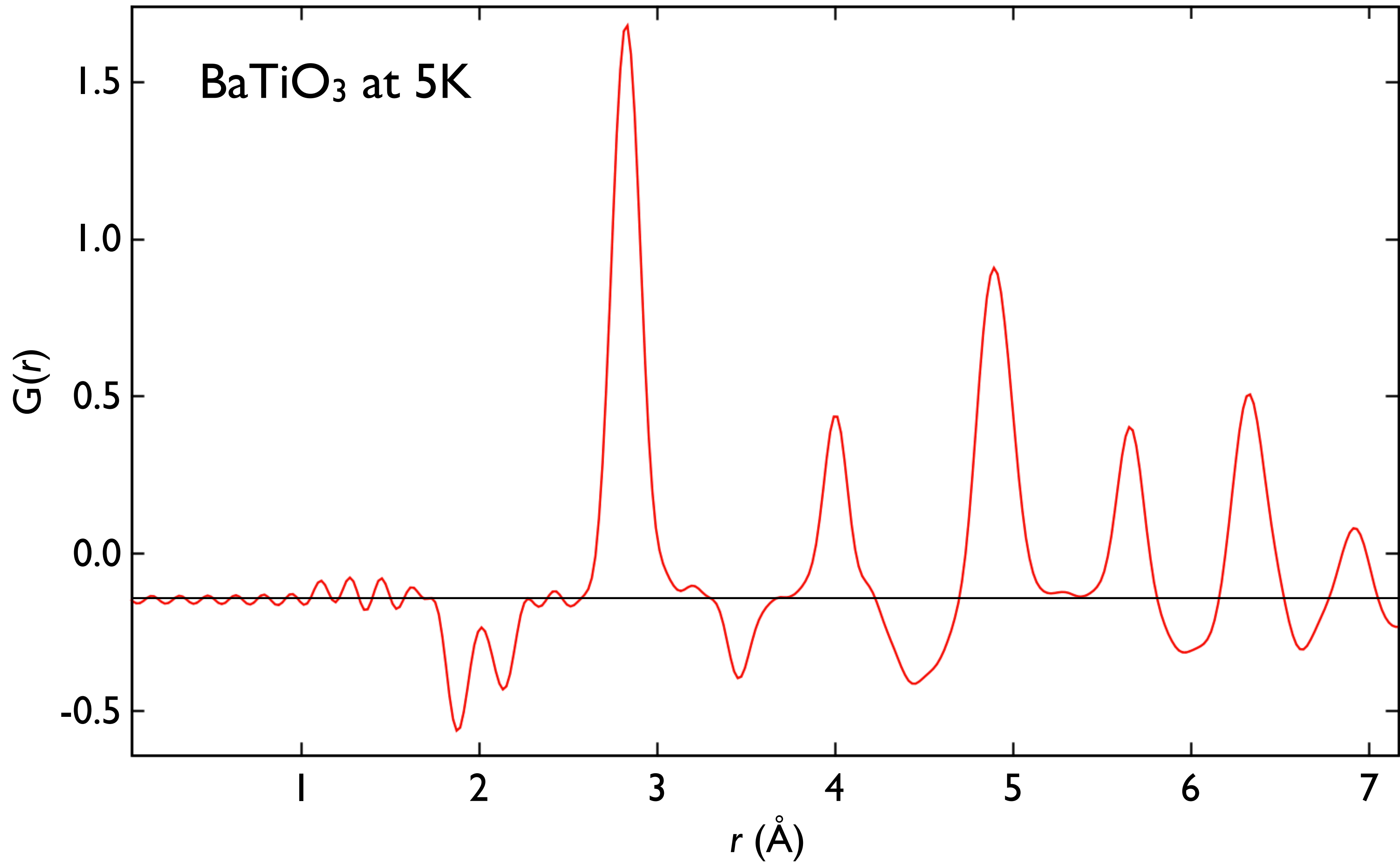
Corrected total scattering data from GEM



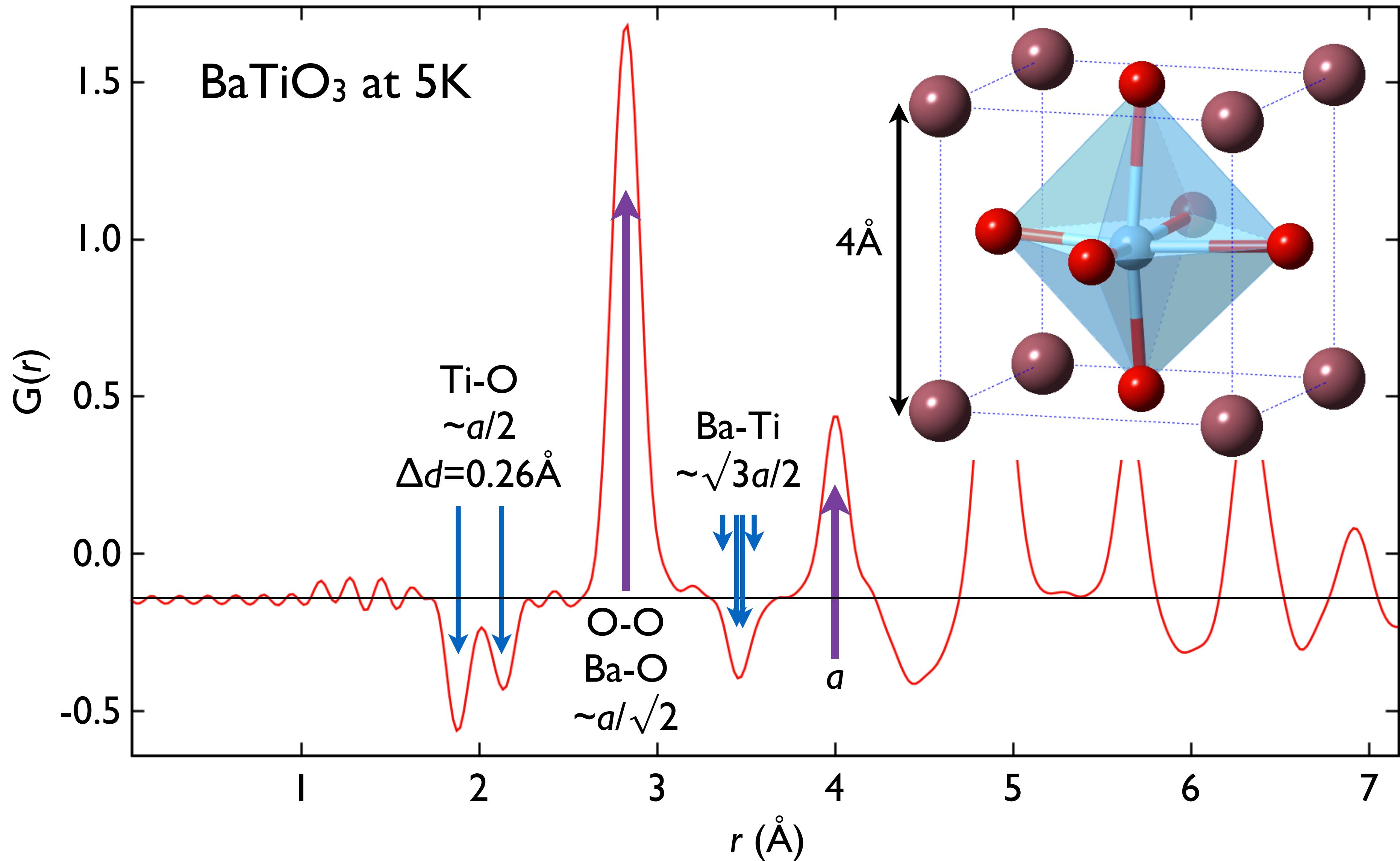
Corrected PDF data from GEM



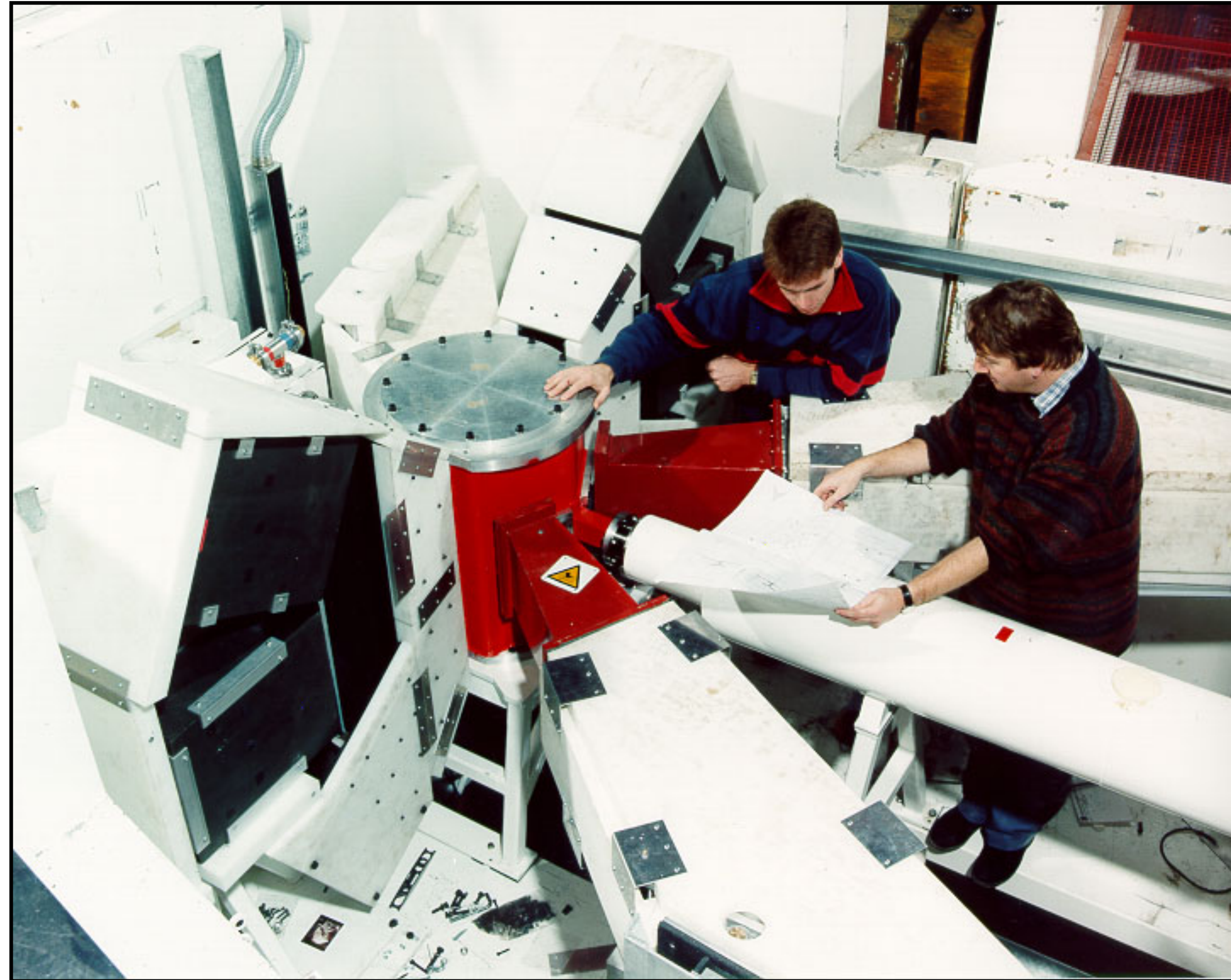
Corrected PDF data from GEM



Corrected PDF data from GEM

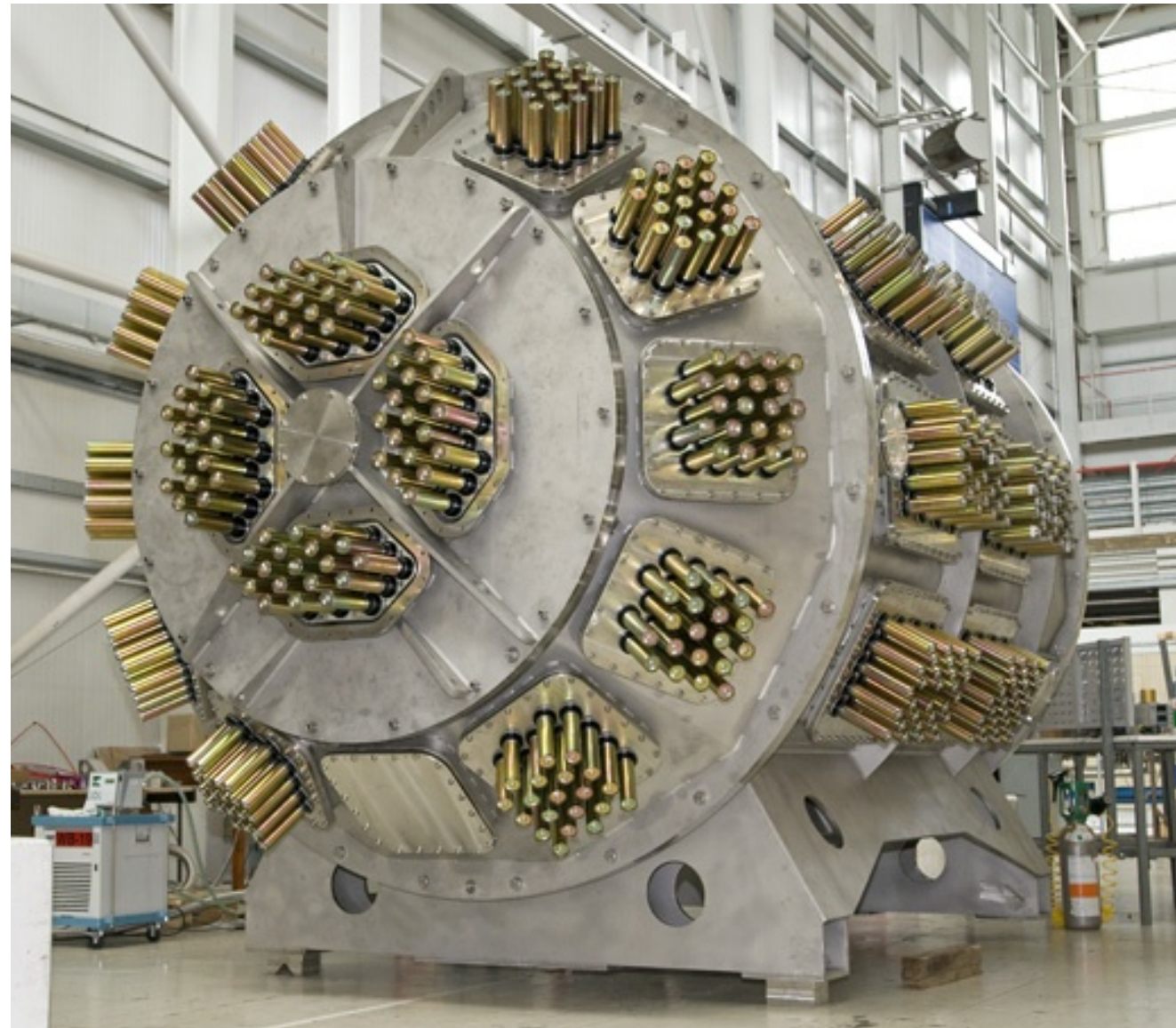
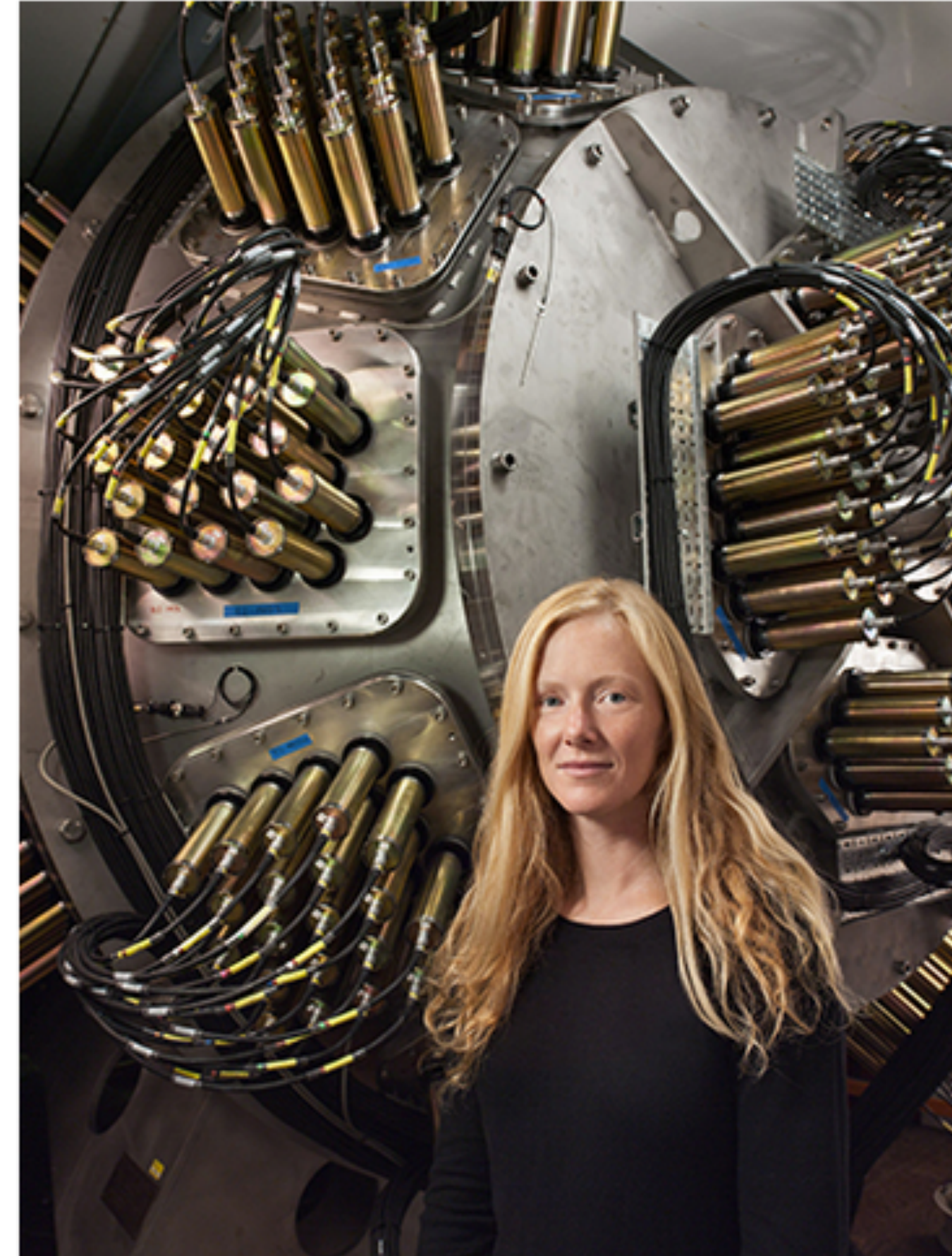
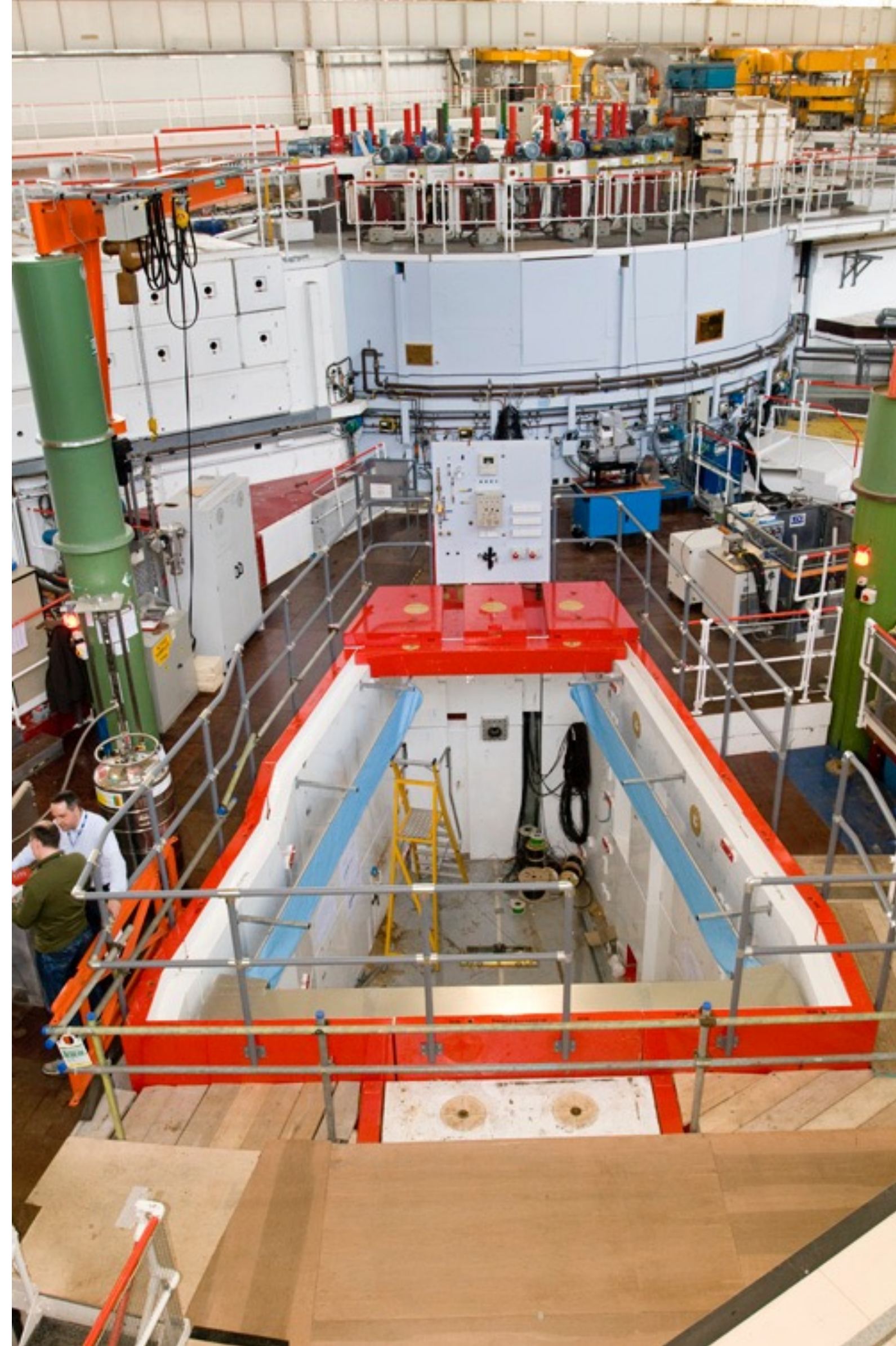
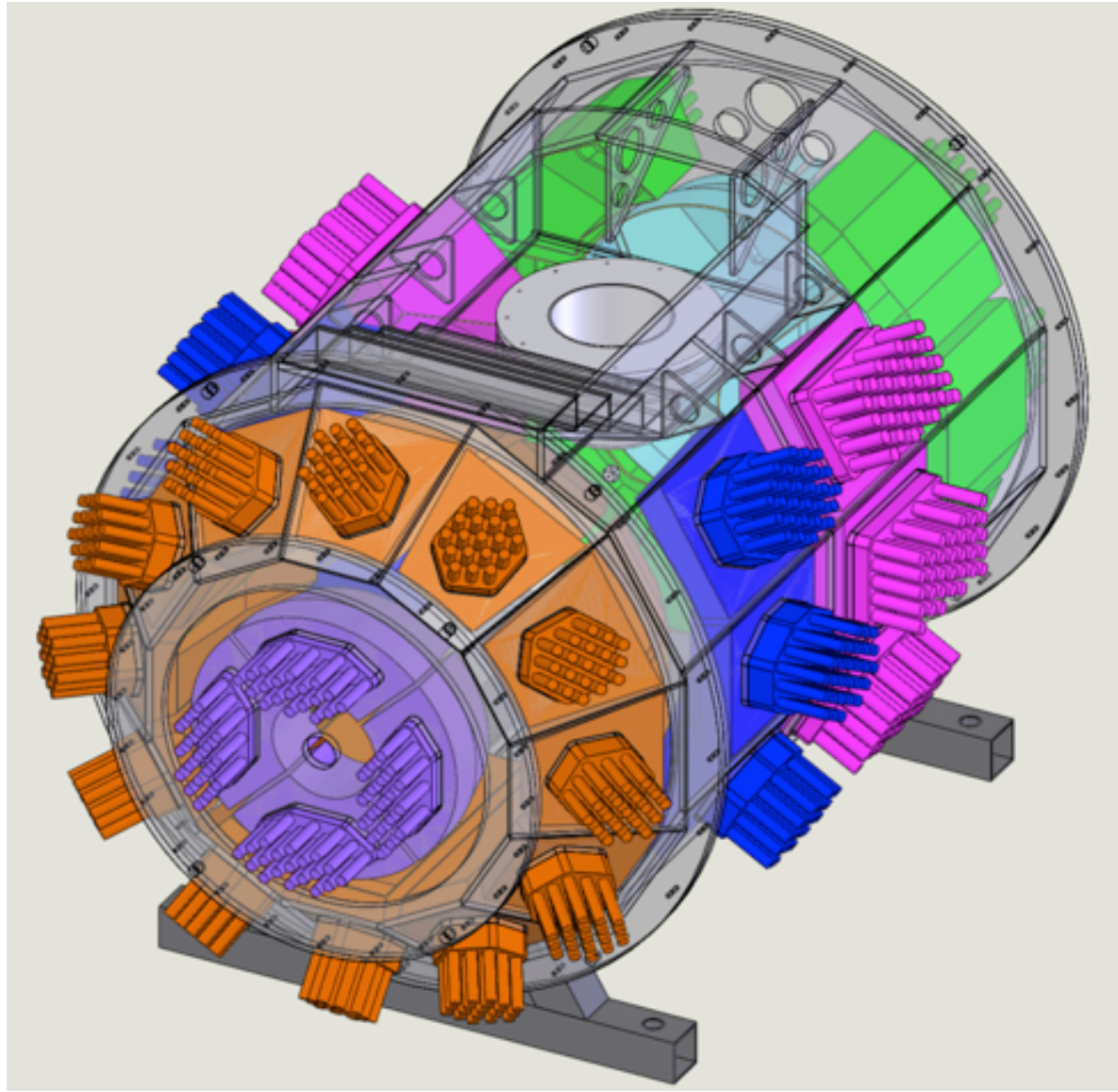


The “old” Polaris (1996-2006)



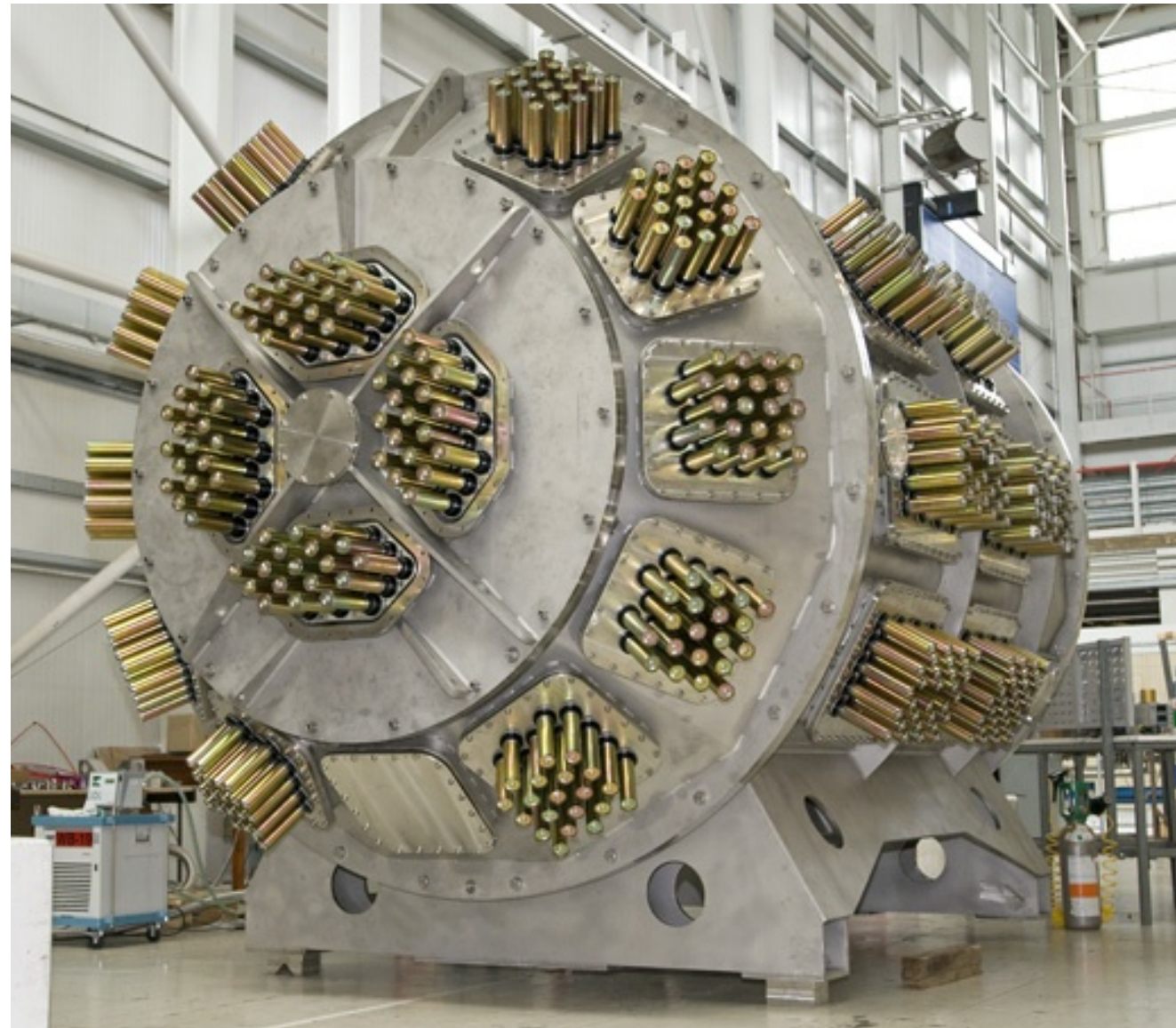
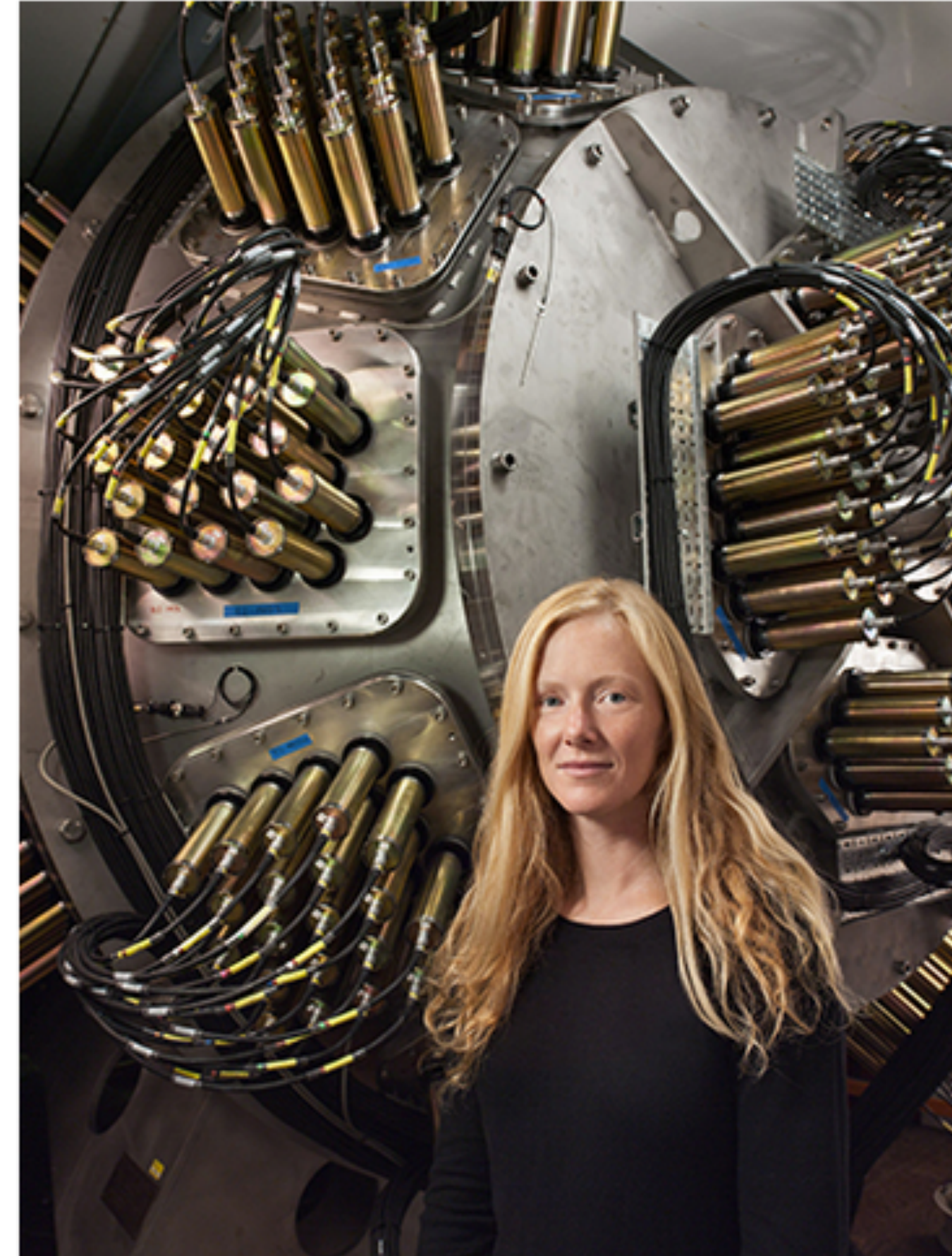
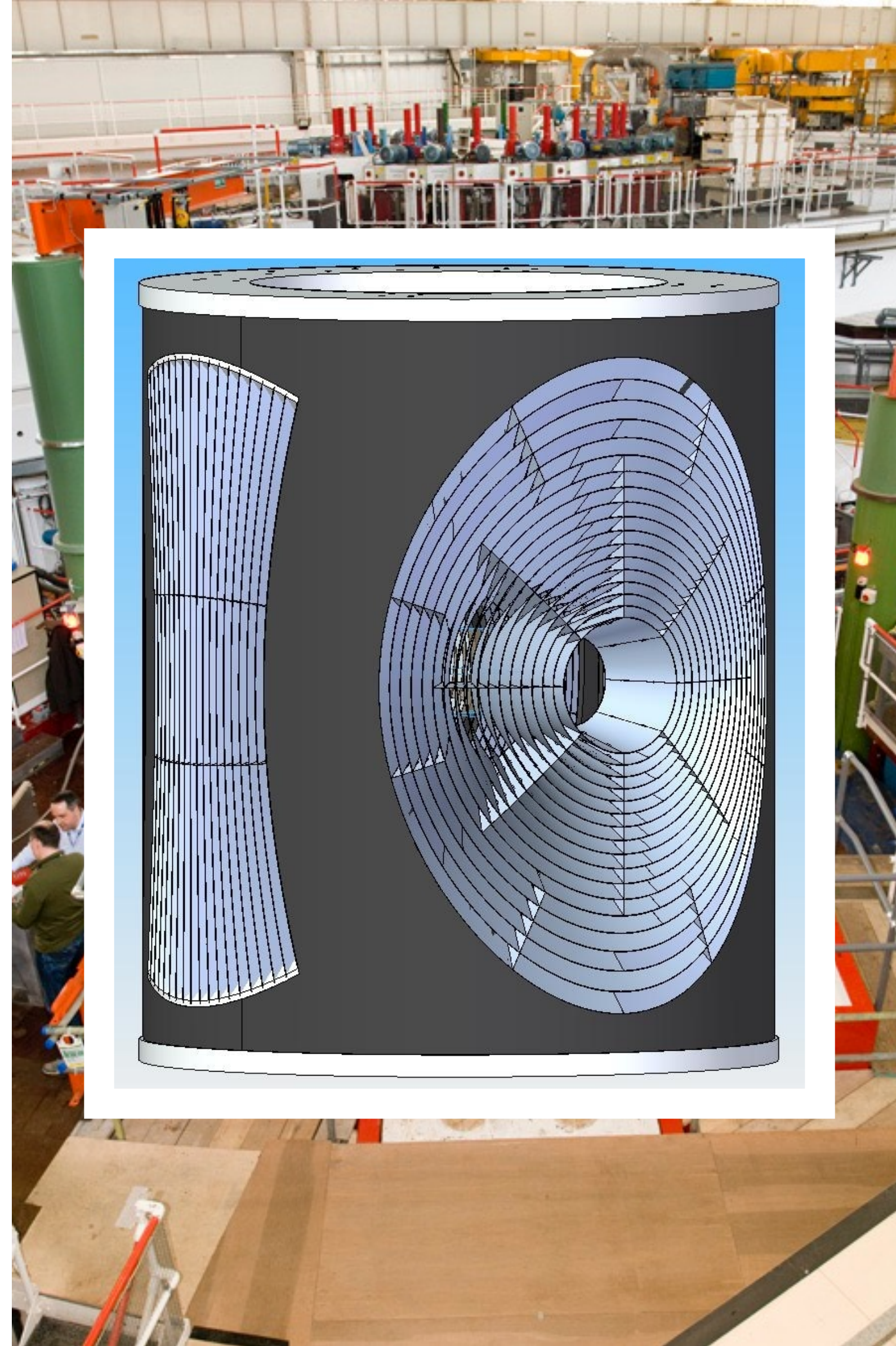
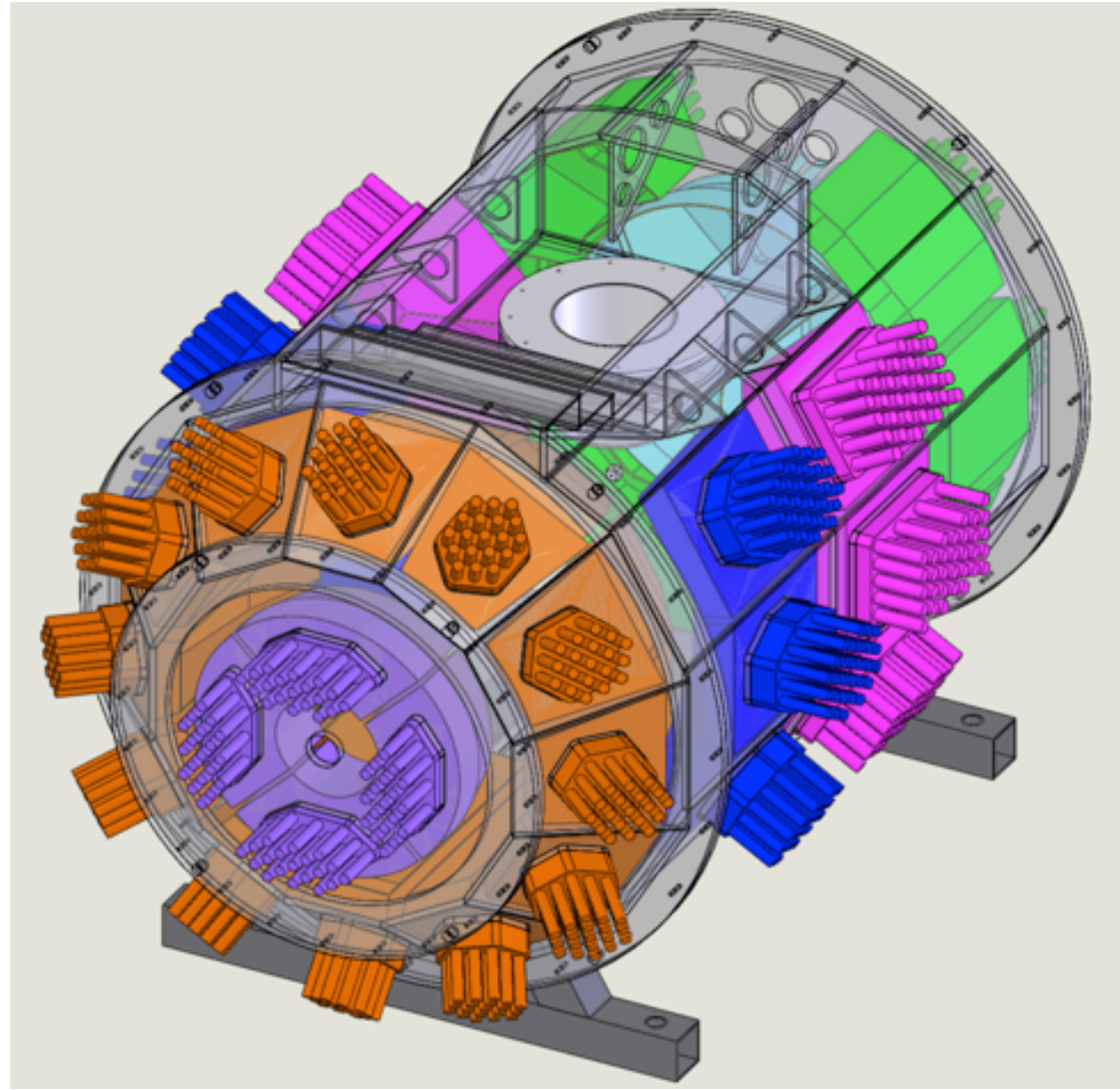
The Polaris total scattering diffractometer at ISIS

Available since late 2011



The Polaris total scattering diffractometer at ISIS

Available since late 2011



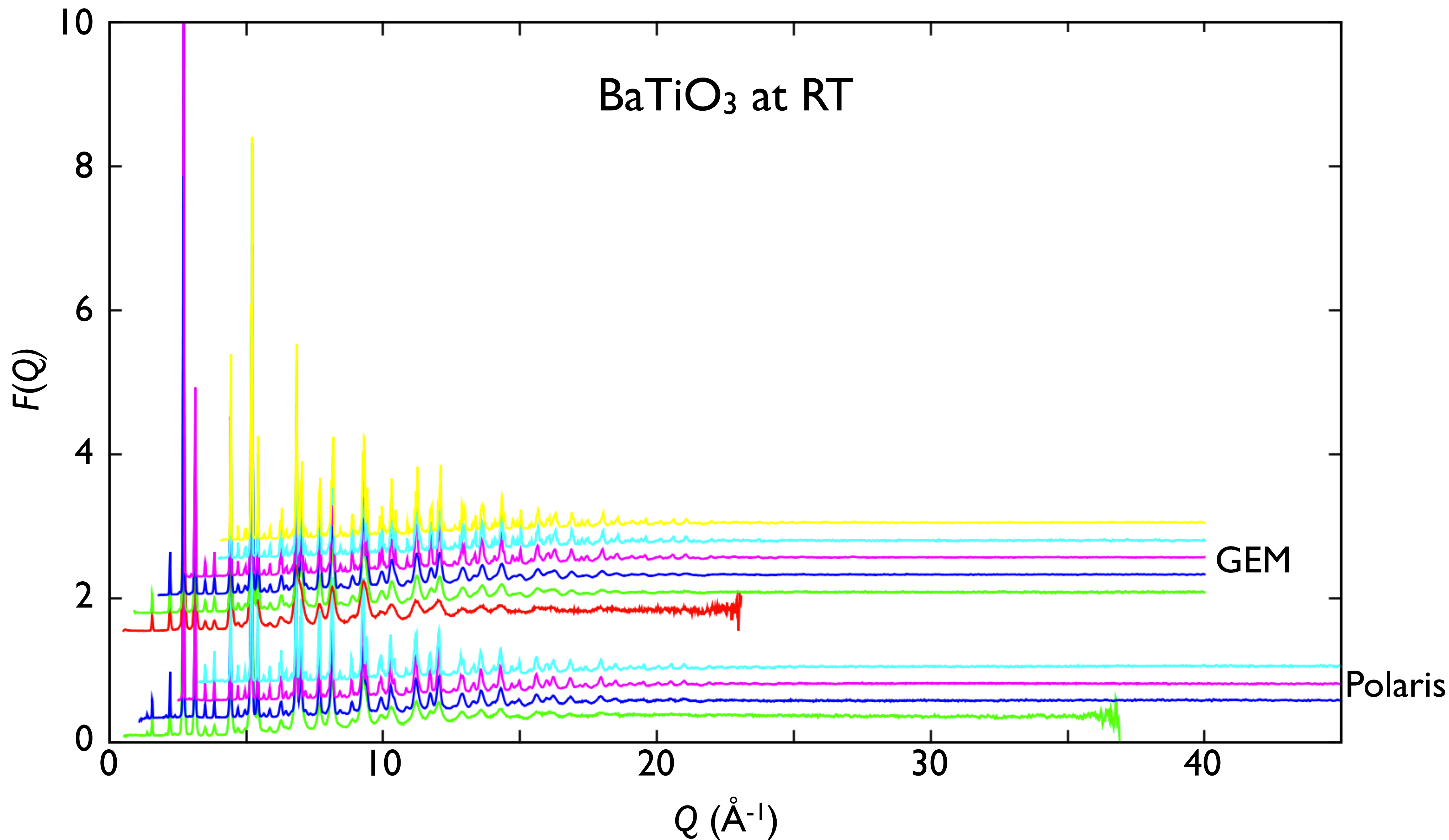
Polaris, GEM and LAD instrument parameters

	<i>LAD (1984–1998)</i>	<i>GEM (~1999–)</i>	<i>Polaris (2012–)</i>
● Moderator	Methane @110K	Methane @110K	Water @316K
● Primary flight path	10 m	17m	14m
● Wavelength range	~0.1 – 10Å	~0.1 – 3.4Å	~0.05 – 6.0Å
● Detector banks	7	7 (8)	5
● Detector coverage	0.016steradians	3.86st	5.67st
● Resolution DQ/Q	14 – 0.6%	~10 – 0.34%	~2.7 – 0.3%

Polaris detector coverage

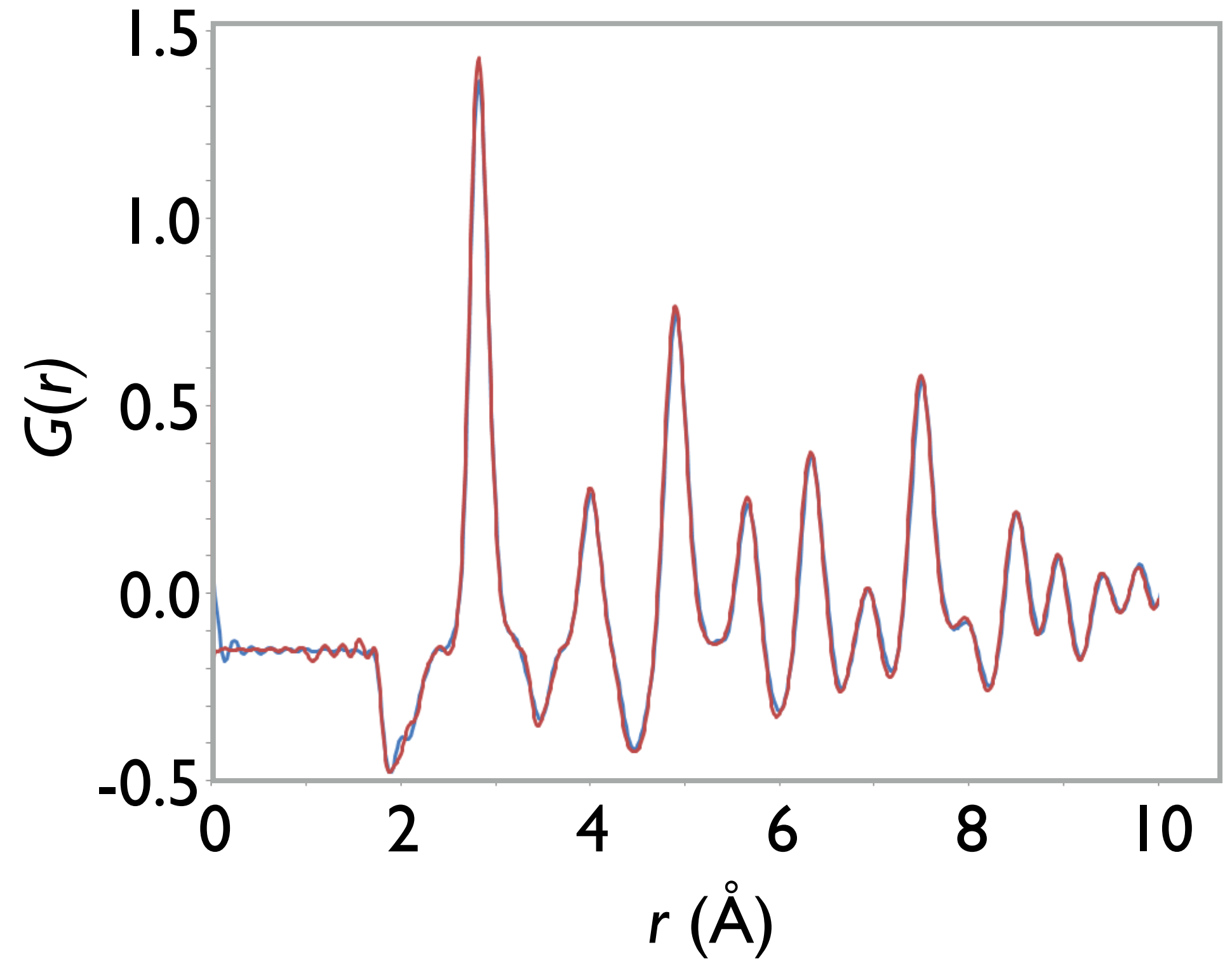
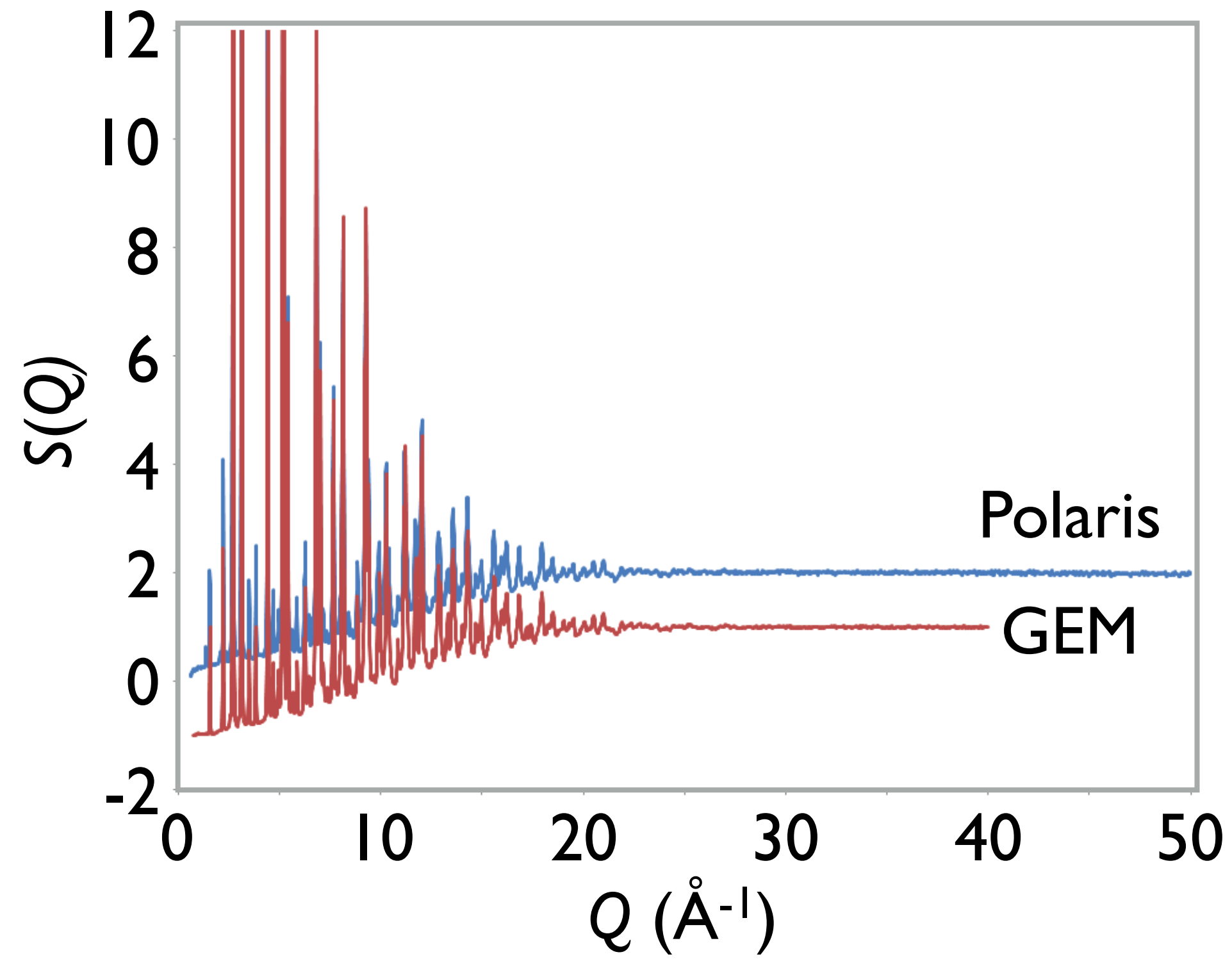
Detector Bank	Scattering angle, 2θ ($^\circ$)	$L2$ (m)	Solid angle (st)	$\Delta Q/Q$ (%)	Q_{\min} (\AA^{-1})
1	6-14	2.25	0.26	2.7	~ 0.15
2	19-34	1.30-2.36	1.04	1.5	0.47
3	40-66	0.92-1.56	0.92	0.85	0.90
4 (5 - GEM)	75-113 (79-114)	0.71-1.08 (~ 1.38)	1.33 (1.51)	0.51 (0.51)	1.53 (2.95)
5	135-167	0.8-1.54	2.12	0.3	2.37

Corrected total scattering data from Polaris and GEM



Corrected $S(Q)$ and PDF from Polaris and GEM

BaTiO₃ at RT



Possible future developments...

- Improved collimation and shielding and hence background
- Faster spinning Nimonic chopper to gain access to shorter wavelengths whilst keeping the beam completely blocked at T0
- Remodelling the GEM detector array following the experience gained from Polaris

Acknowledgements

Alex Hannon (GEM)

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Helen Playford (Polaris)

Ron Smith (Polaris)

Steve Hull (Crystallography Group Leader)



Total Scattering Formalism – In more detail...!

$$F(Q) = \rho_0 \int_0^\infty 4\pi r^2 G(r) \frac{\sin Qr}{Qr} dr$$

Reciprocal Space

$$F(Q) = \sum_{i,j=1}^n c_i c_j \bar{b}_i \bar{b}_j [A_{ij}(Q) - 1]$$

$$A_{ij}(Q) - 1 = \rho_0 \int_0^\infty 4\pi r^2 [g_{ij}(r) - 1] \frac{\sin Qr}{Qr} dr$$

F.T.
(n. only)

F.T.

$$g_{ij}(r) - 1 = \frac{1}{(2\pi)^3 \rho_0} \int_0^\infty 4\pi Q^2 [A_{ij}(Q) - 1] \frac{\sin Qr}{Qr} dQ$$

Real Space

$$G(r) = \frac{1}{(2\pi)^3 \rho_0} \int_0^\infty 4\pi Q^2 F(Q) \frac{\sin Qr}{Qr} dQ$$

$$G(r) = \sum_{i,j=1}^n c_i c_j \bar{b}_i \bar{b}_j [g_{ij}(r) - 1]$$

$$g_{ij}(r) = \frac{n_{ij}(r)}{4\pi r^2 dr \rho_j}$$