

BEAM ENERGY MEASUREMENT (BEM)

M-Q. Ruan, G-Y. Tang, J-Y. Zhang

The 3rd CEPC P&S Meeting

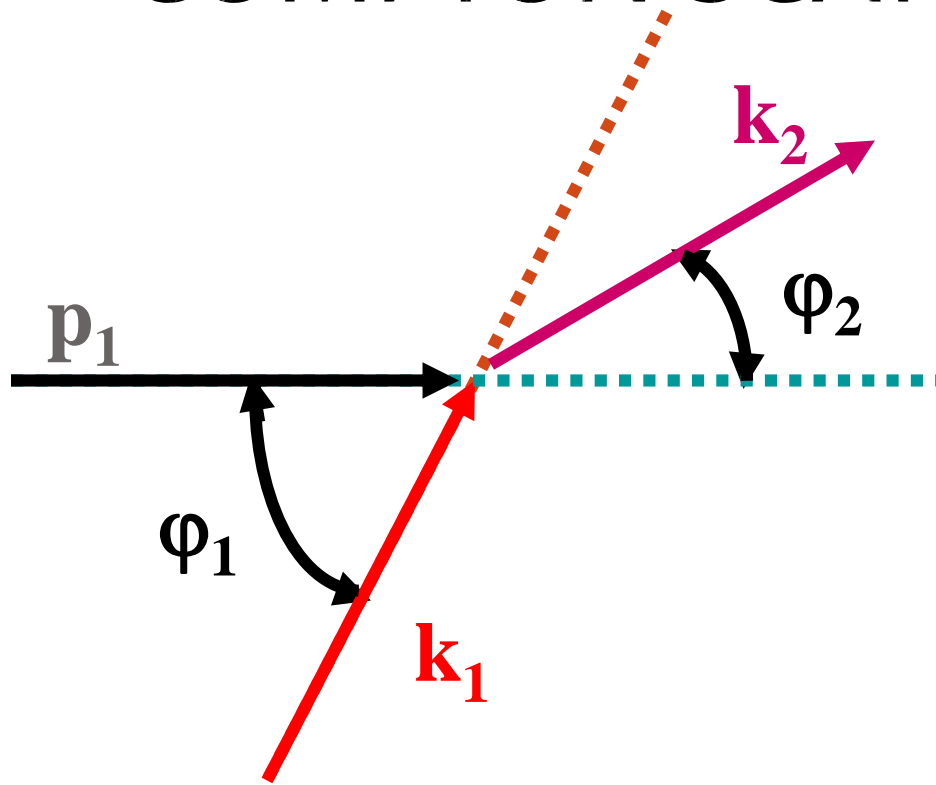


OUTLINE

Focus on Compton scattering method.

- ~~Motivation~~
- BEM@BEPC-II
- Pre...pre CDR of BEM@CEPC

COMPTON SCATTERING



In terms of relativistic invariant

$$s = -(\mathbf{p}_1 + \mathbf{k}_1)^2 = -(\mathbf{p}_2 + \mathbf{k}_2)^2$$

$$t = -(\mathbf{p}_1 - \mathbf{p}_2)^2 = -(\mathbf{k}_1 - \mathbf{k}_2)^2$$

$$u = -(\mathbf{p}_1 - \mathbf{k}_2)^2 = -(\mathbf{p}_1 - \mathbf{k}_1)^2$$

In laboratory system

$$s = m^2 + 2 \gamma m \omega_1 (1 - \beta \cos \varphi_1)$$

$$t = -2 \omega_1 \omega_2 (1 - \cos [\varphi_1 - \varphi_2])$$

$$u = m^2 - 2 \gamma m \omega_2 (1 - \beta \cos \varphi_2)$$

$$\omega_2 = \frac{\omega_1 (1 - \beta \cos \varphi_1)}{1 - \beta \cos \varphi_2 + \frac{\omega_1}{\gamma m} (1 - \cos [\varphi_1 - \varphi_2])} \quad \begin{array}{l} \beta = p_1 / E_1 \\ \gamma = E_1 / m_e \end{array}$$

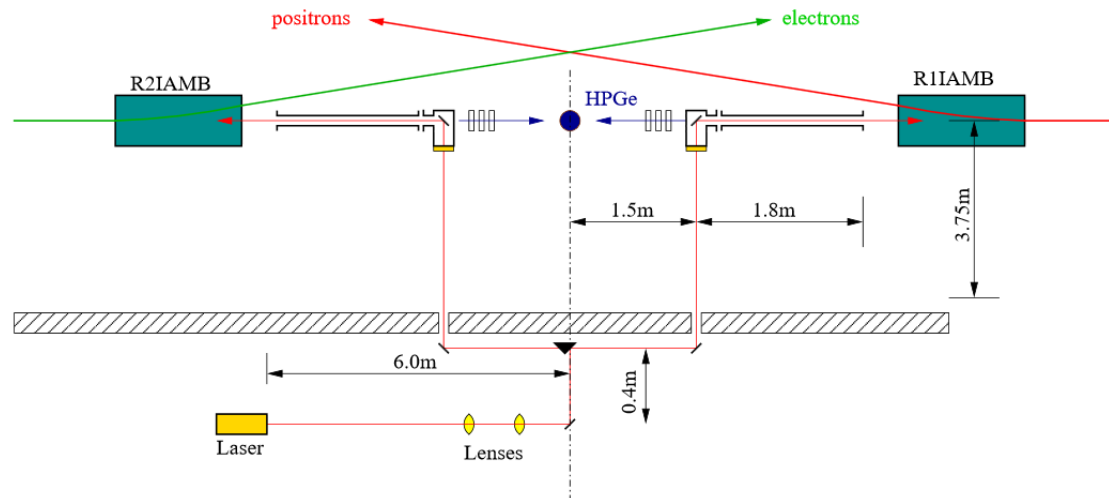
Novel Radiation Sources Using Relativistic Electrons (by P.Rullhusen, X.Artru, P.Dhez)



- Compton Back-scattering: (head-to-head collision)

- $$E_{beam} = \frac{\omega_{max}}{2} \sqrt{1 + \frac{m_e^2}{\omega_0 \omega_{max}}}$$

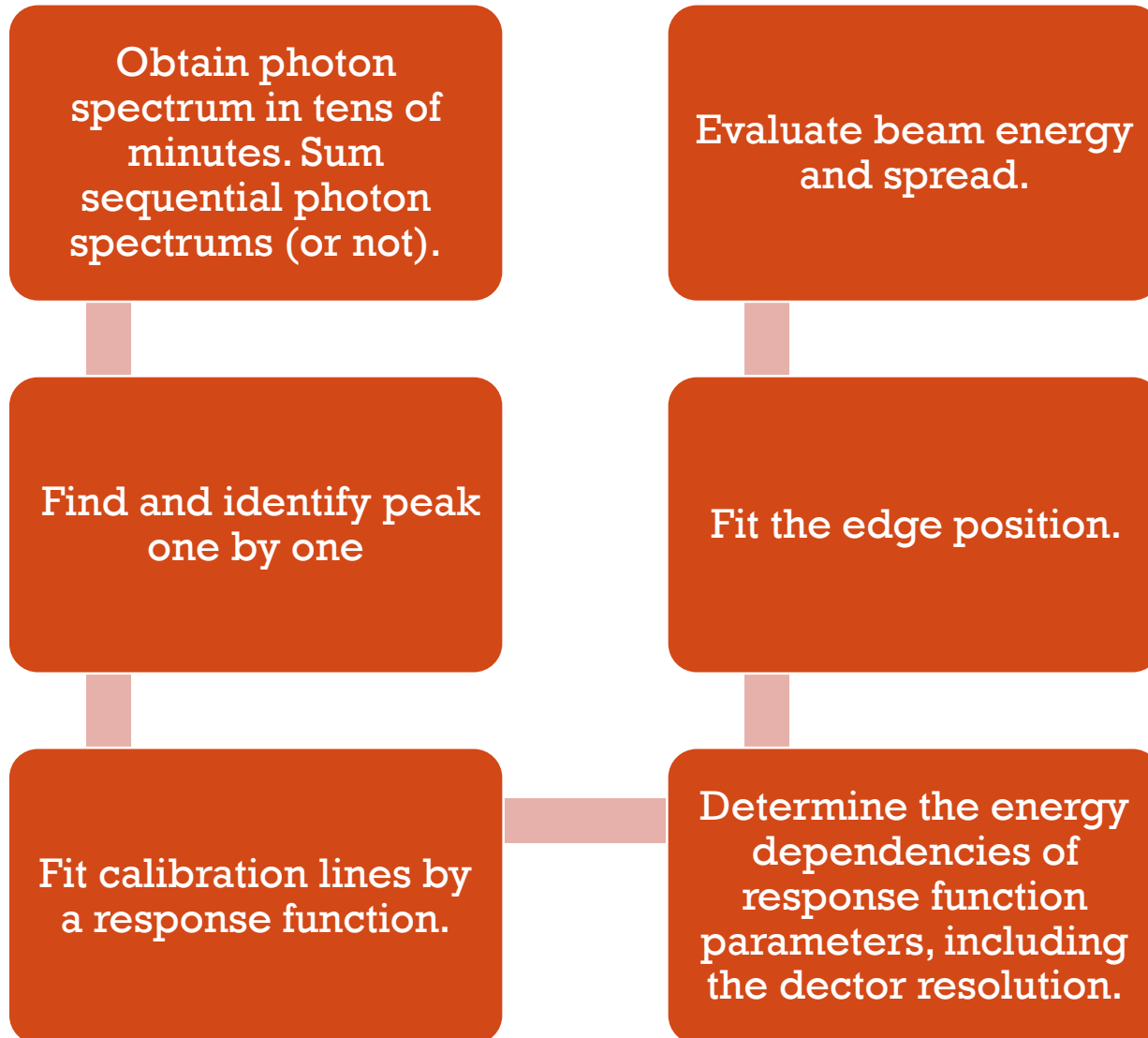
- Hardware: locate at north IP of BEPC-II
 - Laser and optical system.
 - High purity germanium detector: 16384 channels.
 - Pulse generator and isotopes.
 - Data acquisition system.



BEM@BEPC-II

Nuclear Inst. and Methods in Physics
Research, A 659 (2011)

- Online procedure:



BEM@BEPC-II

$$f(x) = A \cdot \left\{ \begin{array}{l} \exp\left[-\frac{(x-x_0)^2}{2\sigma^2}\right], \\ C + (1-C)\exp\left[-\frac{(x-x_0)^2}{2(K_0\sigma)^2}\right], \\ C + (1-C)\exp\left[K_1\left(\frac{(x-x_0)}{(K_0\sigma)} + \frac{K_1}{2}\right)\right], \end{array} \right.$$

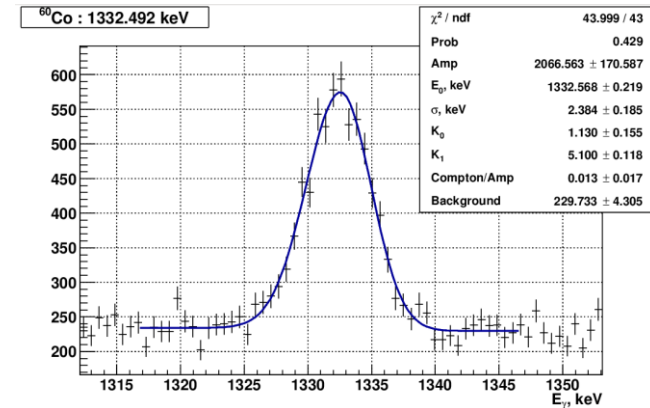
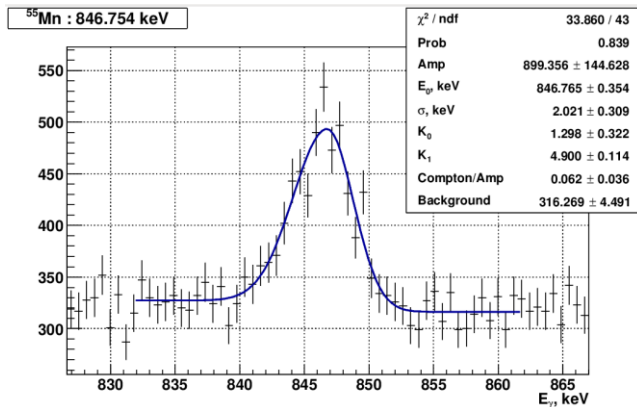
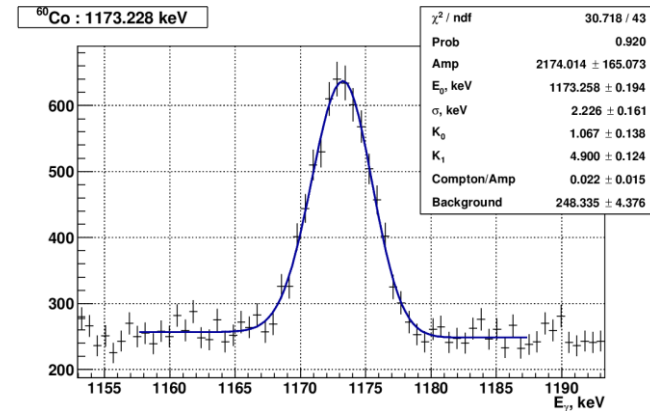
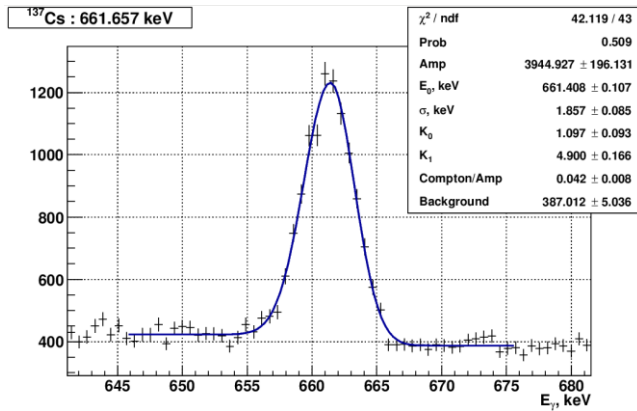
$$0 < x - x_0 < +\infty,$$

$$-K_0K_1\sigma < x - x_0 \leq 0,$$

$$-\infty < x - x_0 \leq -K_0K_1\sigma,$$

- Isotopes:

- Cs137: 661.657keV; Co60: 1173.228keV and 1332.492keV; Mn55: 846.754keV.

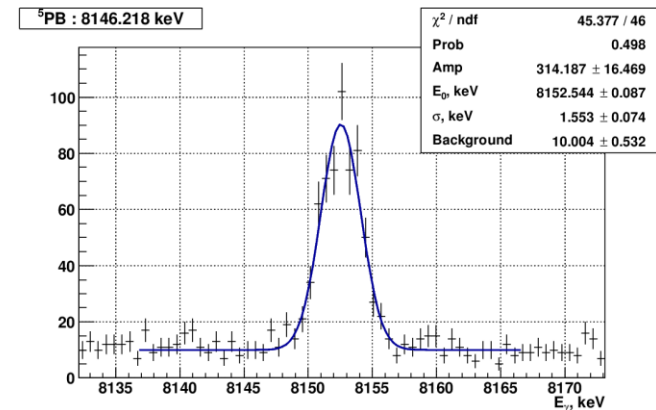
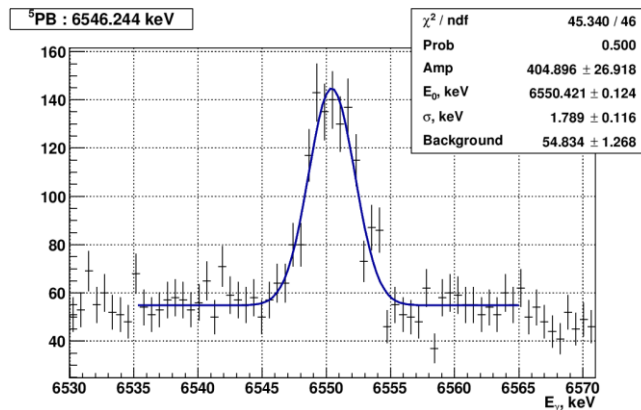
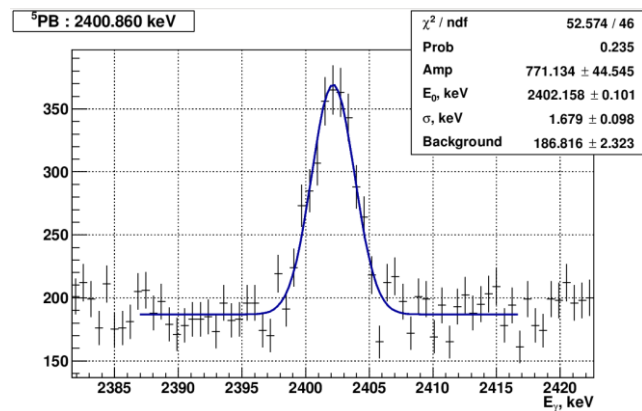
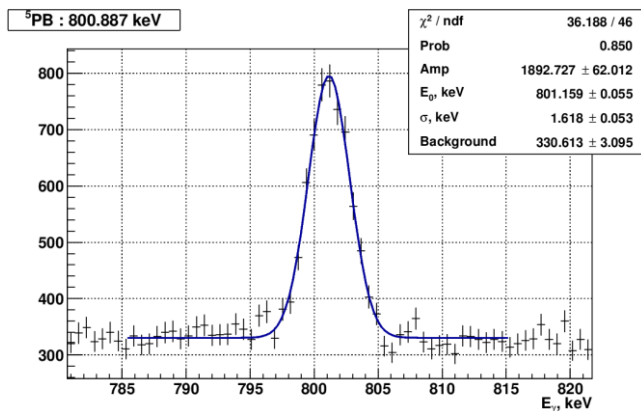


BEM@BEPC-II

- Pulsers:

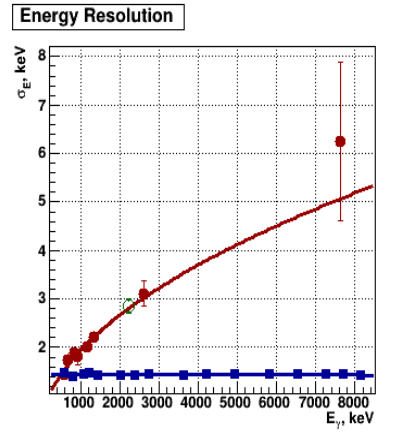
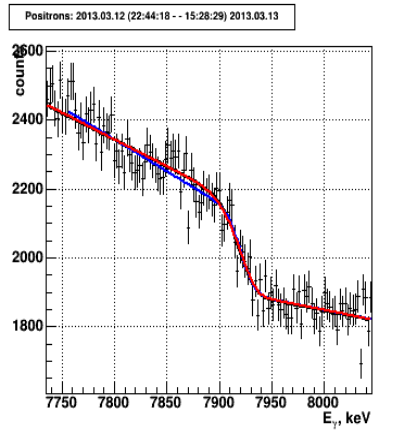
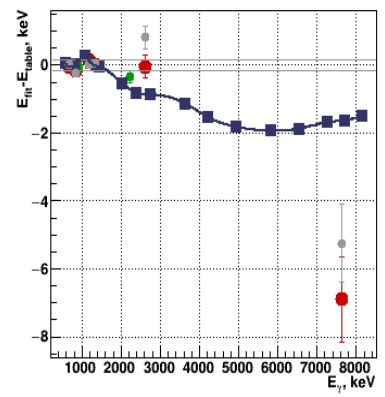
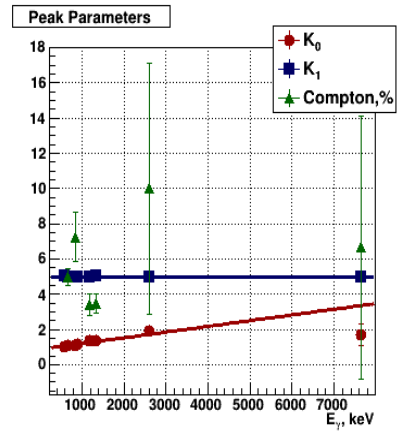
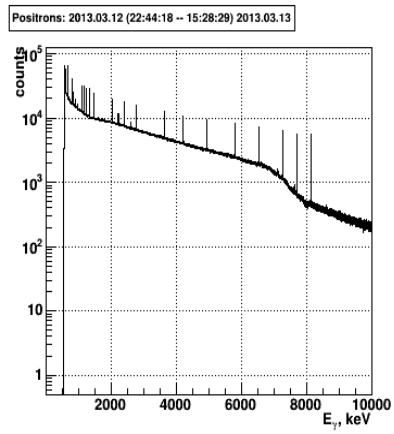
- linear response: *peak position = zero point + gain × voltage*

$$f(x) = A \cdot \begin{cases} \exp\left[-\frac{(x-x_0)^2}{2\sigma^2}\right], & 0 < x-x_0 < +\infty, \\ C + (1-C)\exp\left[-\frac{(x-x_0)^2}{2(K_0\sigma)^2}\right], & -K_0K_1\sigma < x-x_0 \leq 0, \\ C + (1-C)\exp\left[K_1\left(\frac{(x-x_0)}{(K_0\sigma)} + \frac{K_1}{2}\right)\right], & -\infty < x-x_0 \leq -K_0K_1\sigma, \end{cases}$$

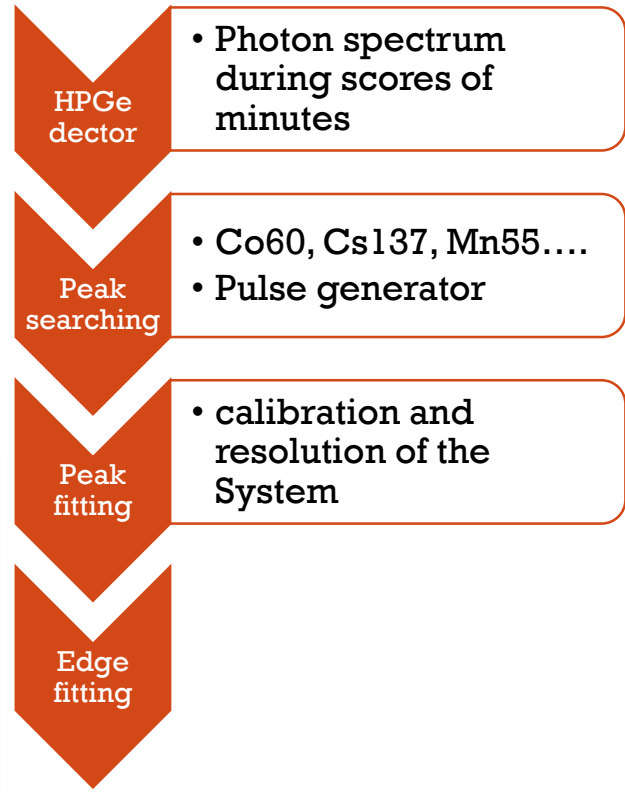


BEM@BEPC-II

- Online procedure:
 - Nucl.Instrum.Meth. A659 (2011) 21-29



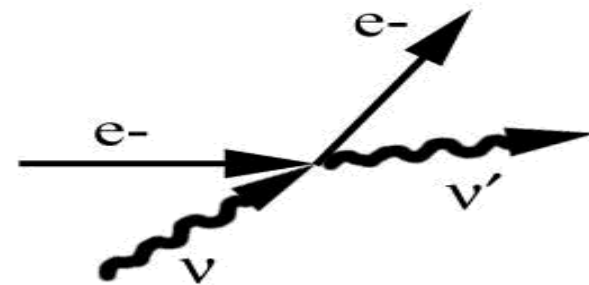
Zero = 1.44316 keV
 Gain = 0.61183 keV/Ch
 "Fano" = 1.117 ± 0.079
 "Noise" = 0.670 ± 0.007 keV
 $W_{max} = 7928.358 \pm 1.969$ keV
 $\sigma_{W_{max}} = 7.35 \pm 2.49$ keV
 $E_{beam} = 2130.821 \pm 0.265$ MeV
 $\sigma_{E_{beam}} = 987.3 \pm 334.0$ keV
 time from: 22:44:18 / 2013.03.12
 time upto: 15:28:29 / 2013.03.13



PRE...PRE CDR OF BEM@CEPC

- If we do the same thing as @BEPC-II
 - 120GeV (beam) + 0.11eV (CO₂ laser) → 20GeV (scattering photon). Too large to be measured precisely.
- Measure lepton position after scattering;
 - Head to head collision.
- Measure photon energy after scattering;
 - Change Xangle.

Inverse Compton scattering



$$\nu' > \nu$$

High energy e- initially
e- loses energy

MEASURE LEPTON

- Simple simulation is ongoing.
 - Beam energy spread: 0.16%.
 - Bunch size: $x \sim 70 \mu m$,
 $y \sim 0.16 \mu m$.
 - Distance: 100m.
- Suitable fitting function should be determined from simulation.
- New simulation based on MadX will be done if necessary.
 - Uncertainty of B field.

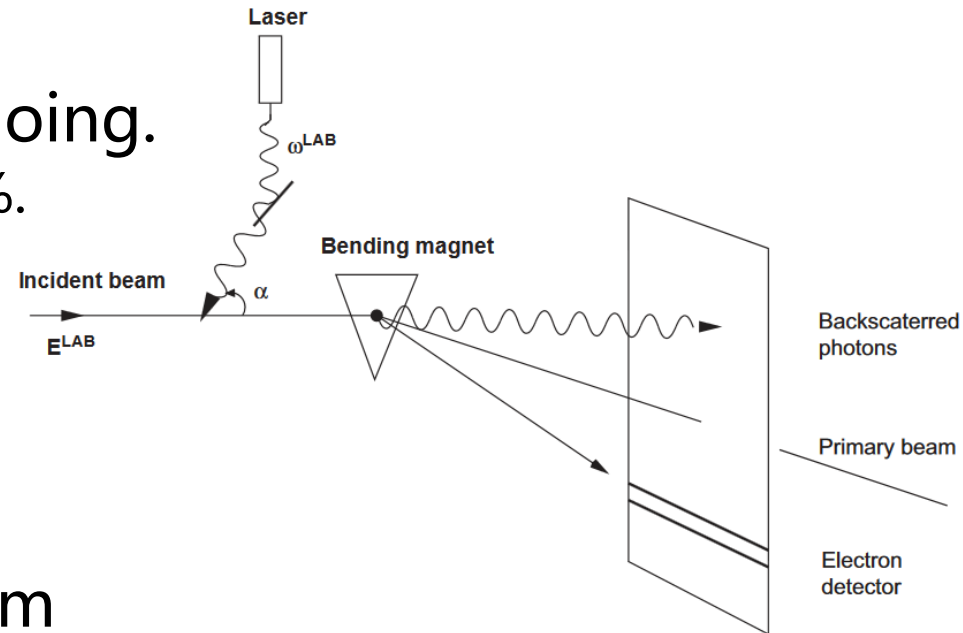
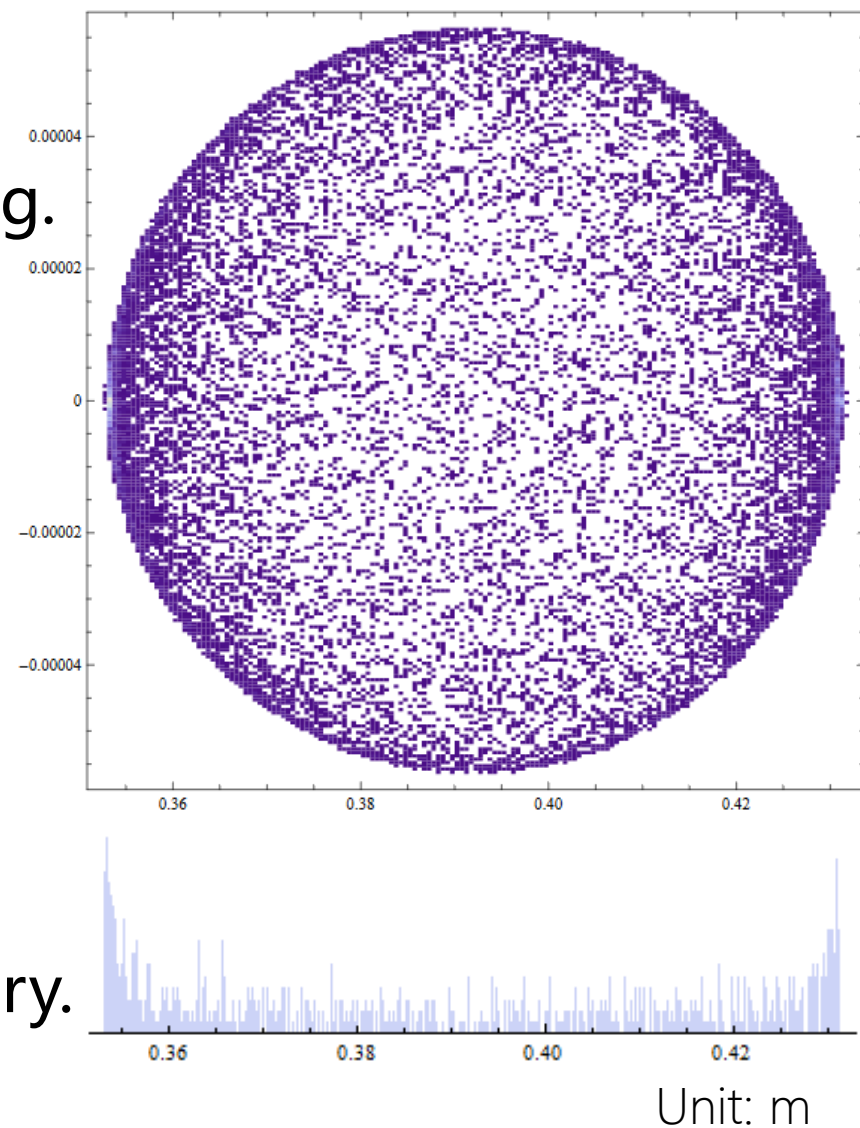


Fig. 8. Scheme of the proposed energy spectrometer based on Compton backscattering.

MEASURE LEPTON

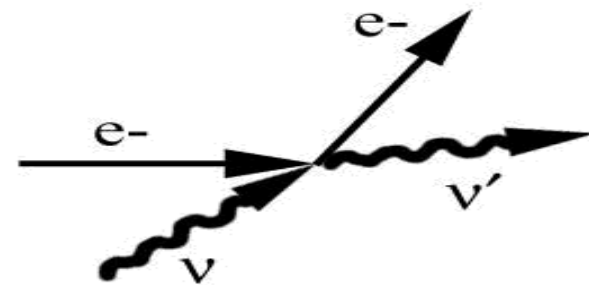
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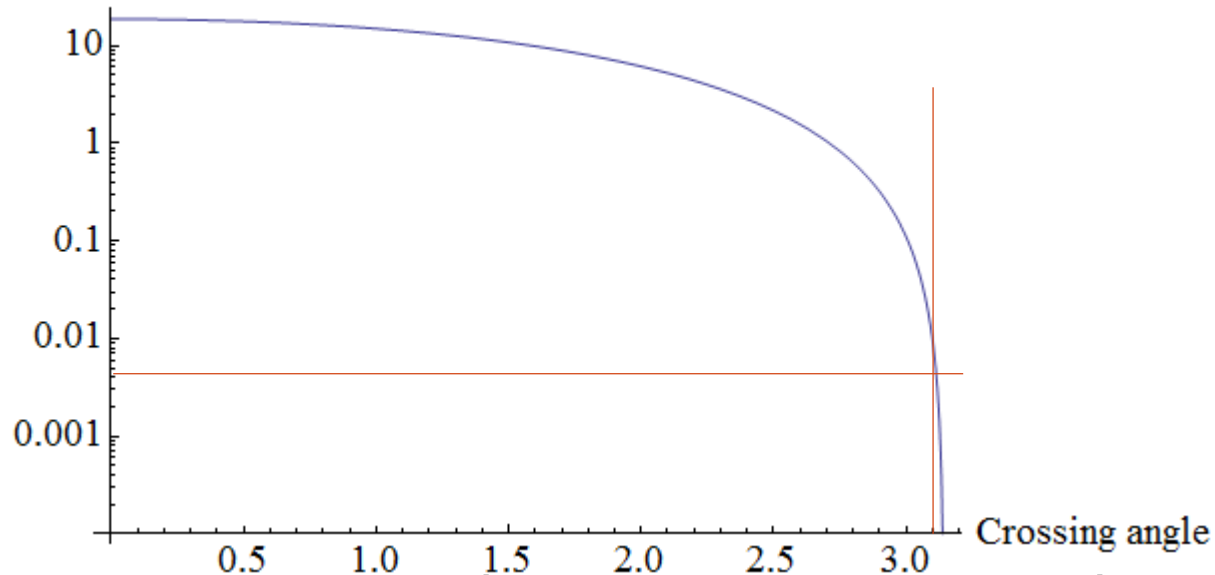
$$\nu' > \nu$$

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CHANGE CROSSING ANGLE

- Crossing angle $[0, \pi]$
- Scattering photon energy v.s. Xangle

Scattering photon energy/GeV

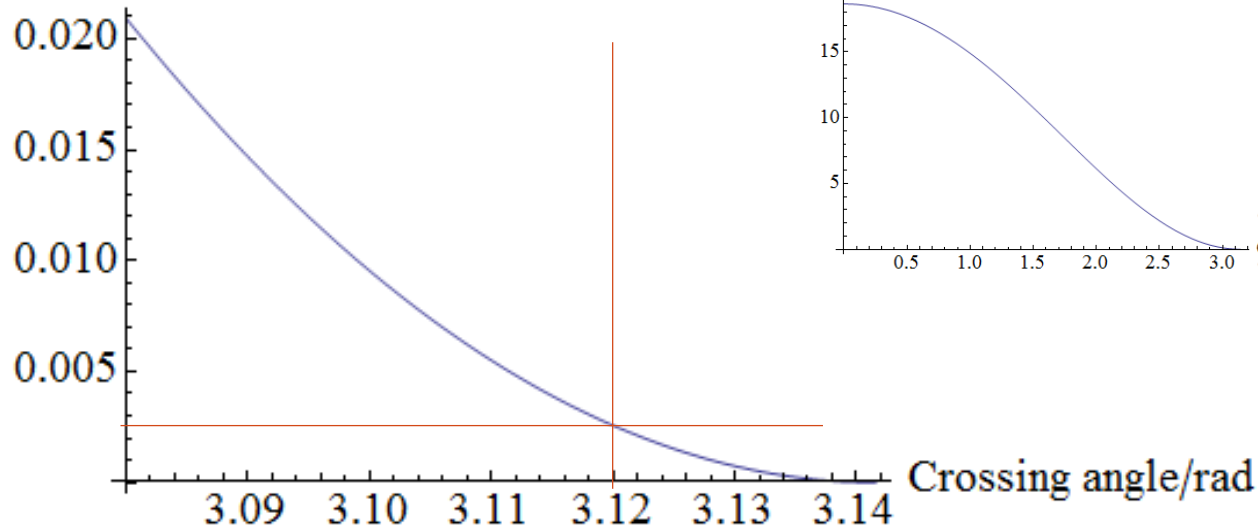


- When Xangle is 3.12 rad, maximum scattering photon energy is 2.815 MeV.
- TI208: 2.614MeV.

CHANGE CROSSING ANGLE

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- Scattering photon energy v.s. Xangle

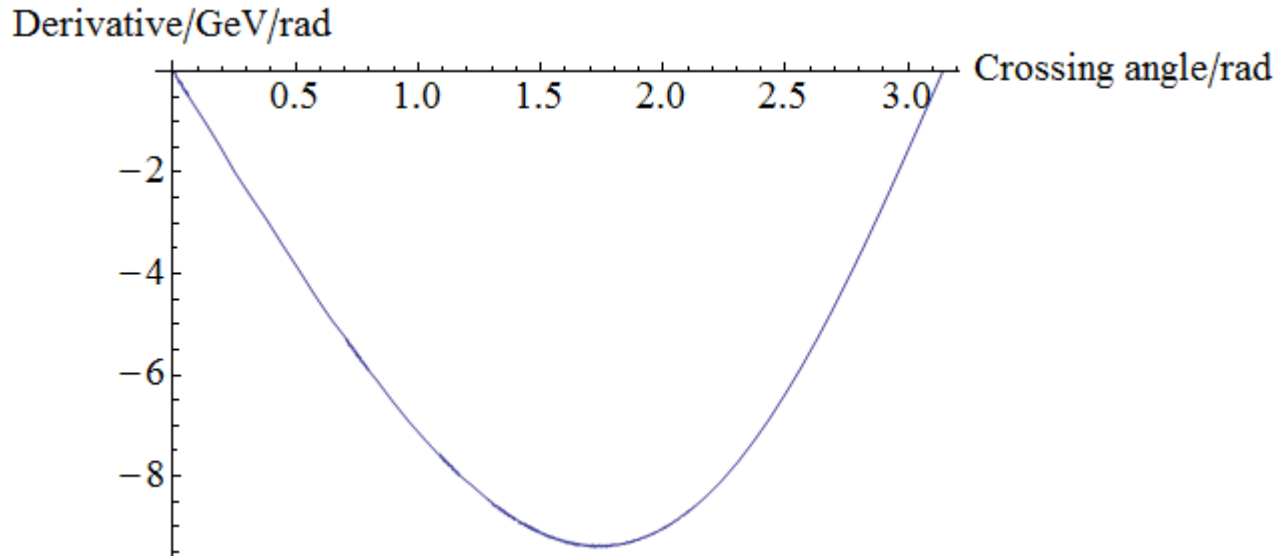
Scattering photon energy/GeV



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CHANGE CROSSING ANGLE

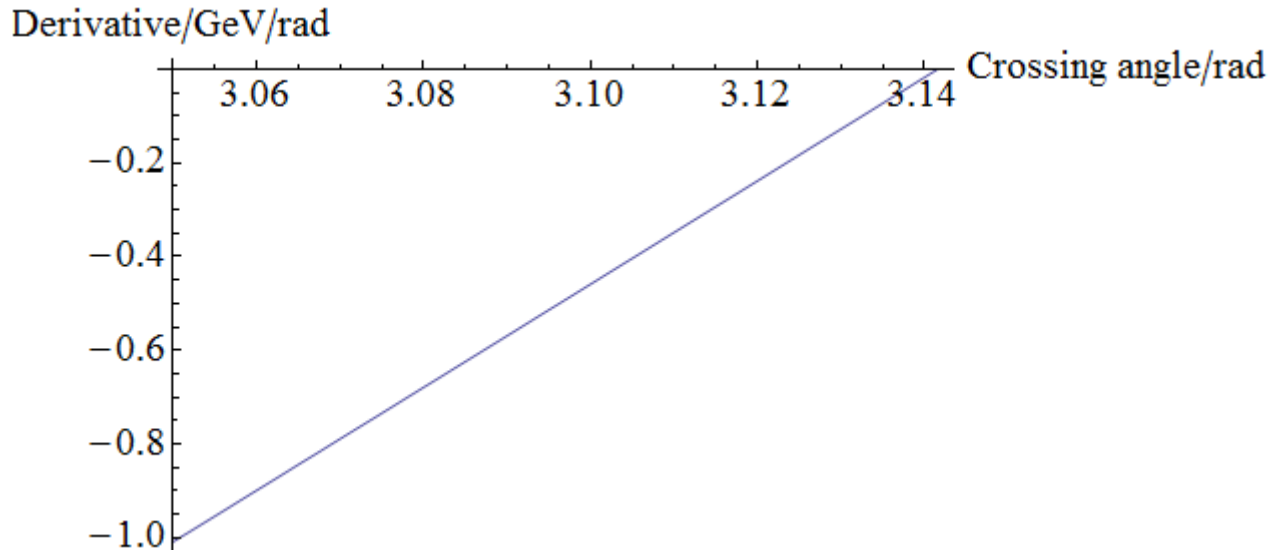
- Uncertainty estimation:
 - Derivative v.s. Xangle



- If 10^{-5} relative uncertainty of beam energy is required, the uncertainty of Xangle should be $10^{-4} \sim 10^{-5}$ radian.

CHANGE CROSSING ANGLE

- Uncertainty estimation:
 - Derivative v.s. Xangle



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CHANGE CROSSING ANGLE

- Minimum: $\sigma_{py} \sim 3 \times 10^{-8} \text{ rad}$,
 $\sigma_{px} \sim 2.4 \times 10^{-6} \text{ rad}$.

σ_{py} , σ_{px} mean the p_y , p_x momentum emittance.

- Meet the requirement (10^{-5} rad).
- More details (including MC simulation) will be given after discussing with accelerator people.

Handwritten notes showing calculations for beam emittance. The main derivation is as follows:

$$\beta_y^* = 1 \text{ mm}$$

$$\sigma_y = \sqrt{\beta_y \epsilon_y}$$

$$\sigma_{y'} = \sqrt{\epsilon_y / \beta_y^*}$$

$$\beta_y \approx \frac{s^2}{\beta_y^*}$$

$$\epsilon_y = \epsilon_x \cdot K$$

$$\sigma_{y'} = \sqrt{\frac{\epsilon_x \cdot K}{(L^* + \frac{1}{2} L_{d1})^2}}$$

$$= \frac{\sqrt{\epsilon_x \cdot K \cdot \beta_y^*}}{L^* + \frac{1}{2} L_{d1}}$$

$$= \frac{\sqrt{2 \times 10^{-9} \times 0.003 \times 0.001}}{1.5 + \frac{1}{2} \times 1.7}$$

$$\sim \frac{8 \times 10^{-8}}{2.35}$$

$$\sim 3 \times 10^{-8} \text{ rad}$$

Other calculations shown include:

$$\sigma_{x'} = \sqrt{\frac{\epsilon_x}{\beta_x}}$$

$$\sqrt{\frac{\epsilon_y \cdot 500}{\beta_y / 20}}$$

$$\sqrt{6000} \sim 80$$

$$\sqrt{60 \times 10^{-6}}$$

$$\sim 2.4 \times 10^{-6}$$

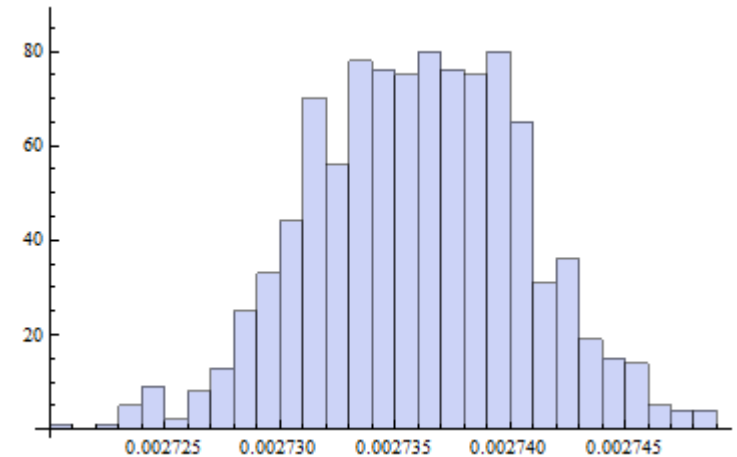
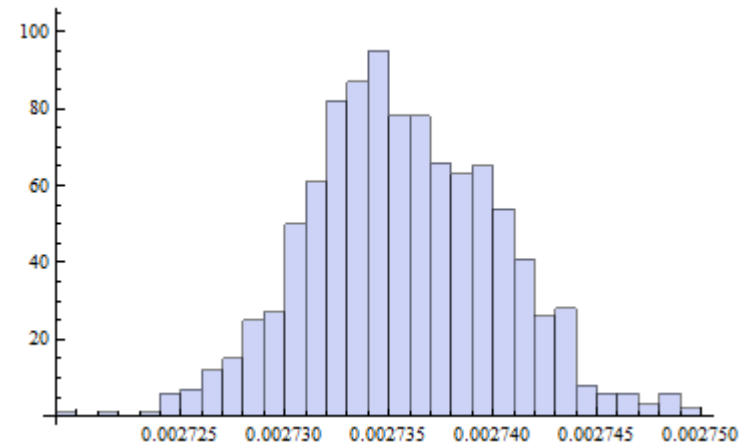
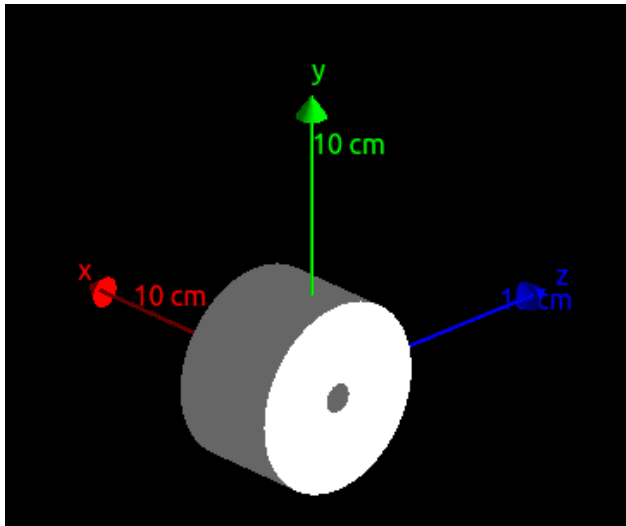
$$2.4^2 \sim$$

Additional notes: 0.4μ , $< 10\%$, and a diagram of a coordinate system with y and y' axes.

Thanks to Jianwei's discussion.

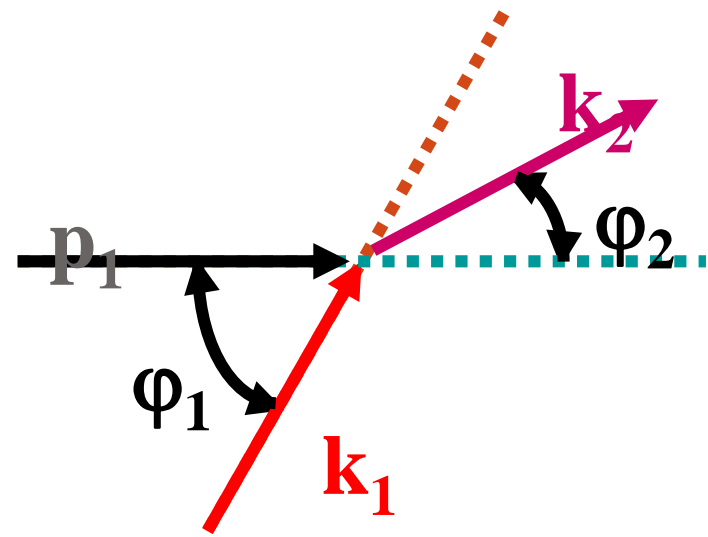
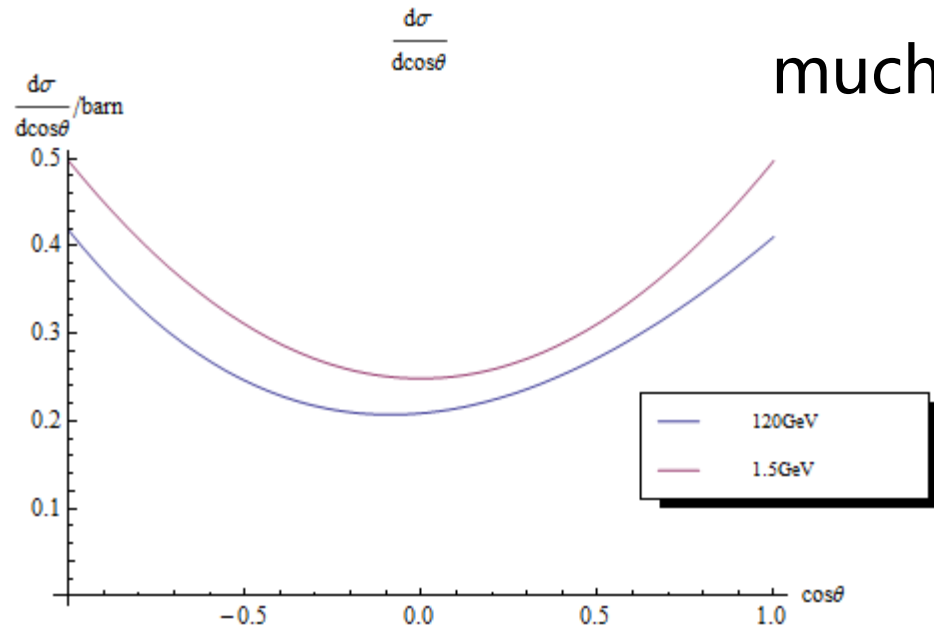
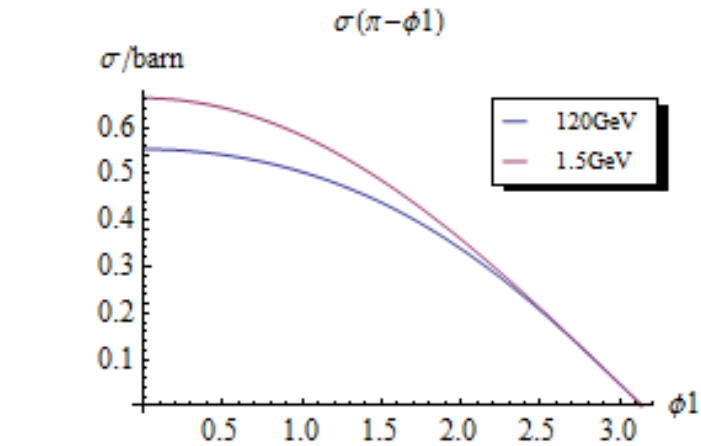
CHANGE CROSSING ANGLE

- Toy MC is done. (1000 events with different acceptance)
- Momentum emittance, energy spread and acceptance of HPGe detector are considered.
- Geant4 Model of Ge.



ESTIMATION OF EVENT RATE

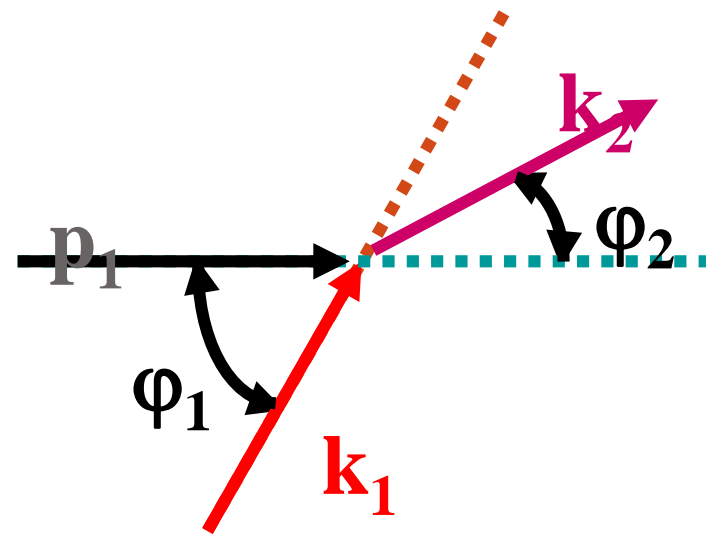
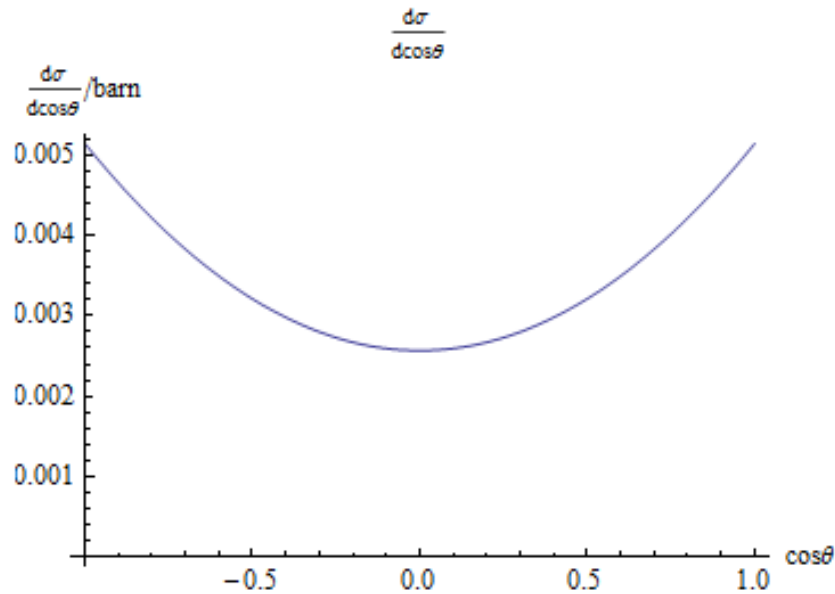
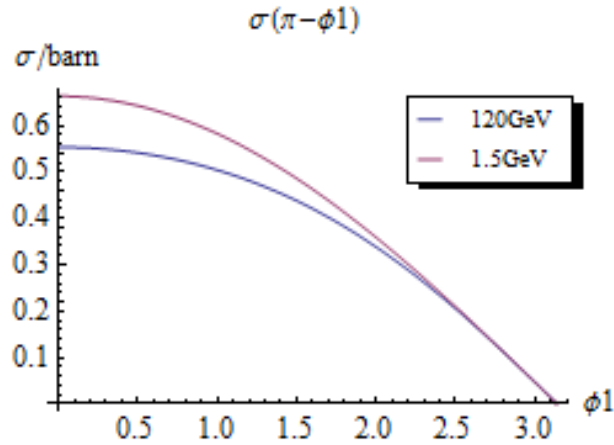
- Head-to-head collision:



Event rate should be as much as @BEPC-II.

ESTIMATION OF EVENT RATE

- Xangle~3.12 collision:



$$\frac{\left. \frac{d\sigma}{d\cos\theta} \right|_{120\text{GeV}}}{\left. \frac{d\sigma}{d\cos\theta} \right|_{1.5\text{GeV}}} \sim \frac{1}{100}$$

120GeV

ESTIMATION OF EVENT RATE

- Xangle ~ 3.12 collision:

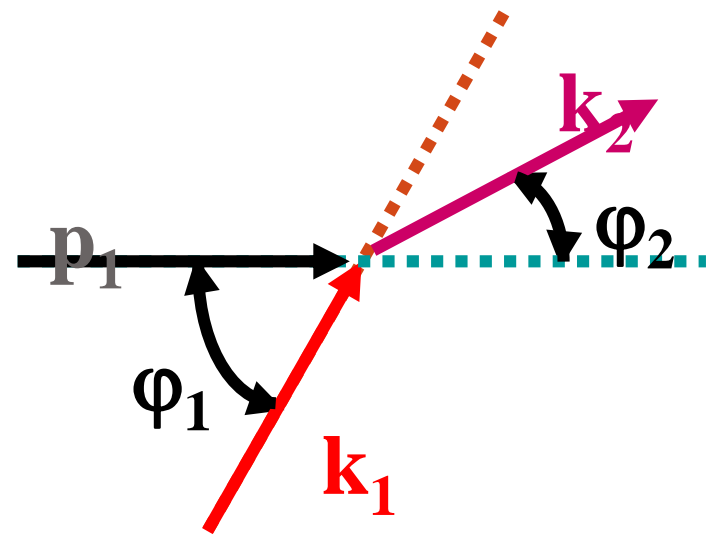
- Event number:

$$N = \sigma_T \cdot \iiint \rho_i \cdot \rho_e dx dy dz$$

- BEPC-II $\sim 5 \times 10^{32}$; CEPC $\sim 200 \times 10^{32}$

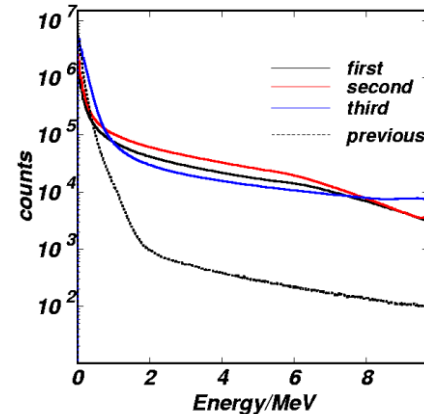
- $\frac{\rho_{e_{cepc}}}{\rho_{e_{bepcII}}} \sim 6$

- $\frac{\text{Event rate @CEPC}}{\text{Event rate @BEPC-II}} = \frac{1}{17}$. (How to Increase laser power?)



SUMMARY: BEM @ CEPC

- Measure lepton position after scattering;
 - New Simulation with MadX to take B field fluctuation into account.
- Measure photon energy after scattering.
 - Check all calculation.
 - MC simulation.
 - Background (synchrotron radiation, etc.)? Signal-to-noise ratio?



Thank you!