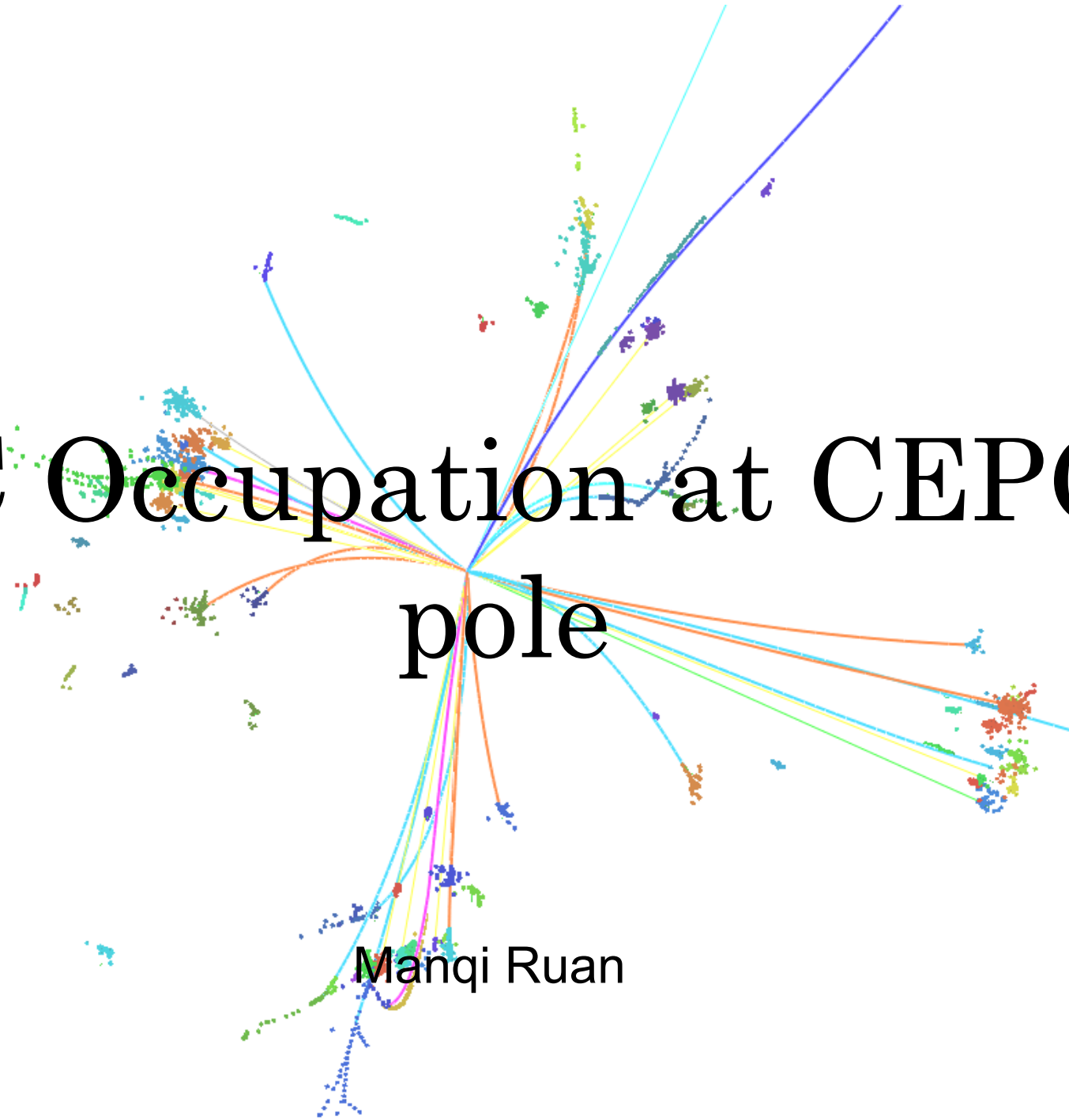


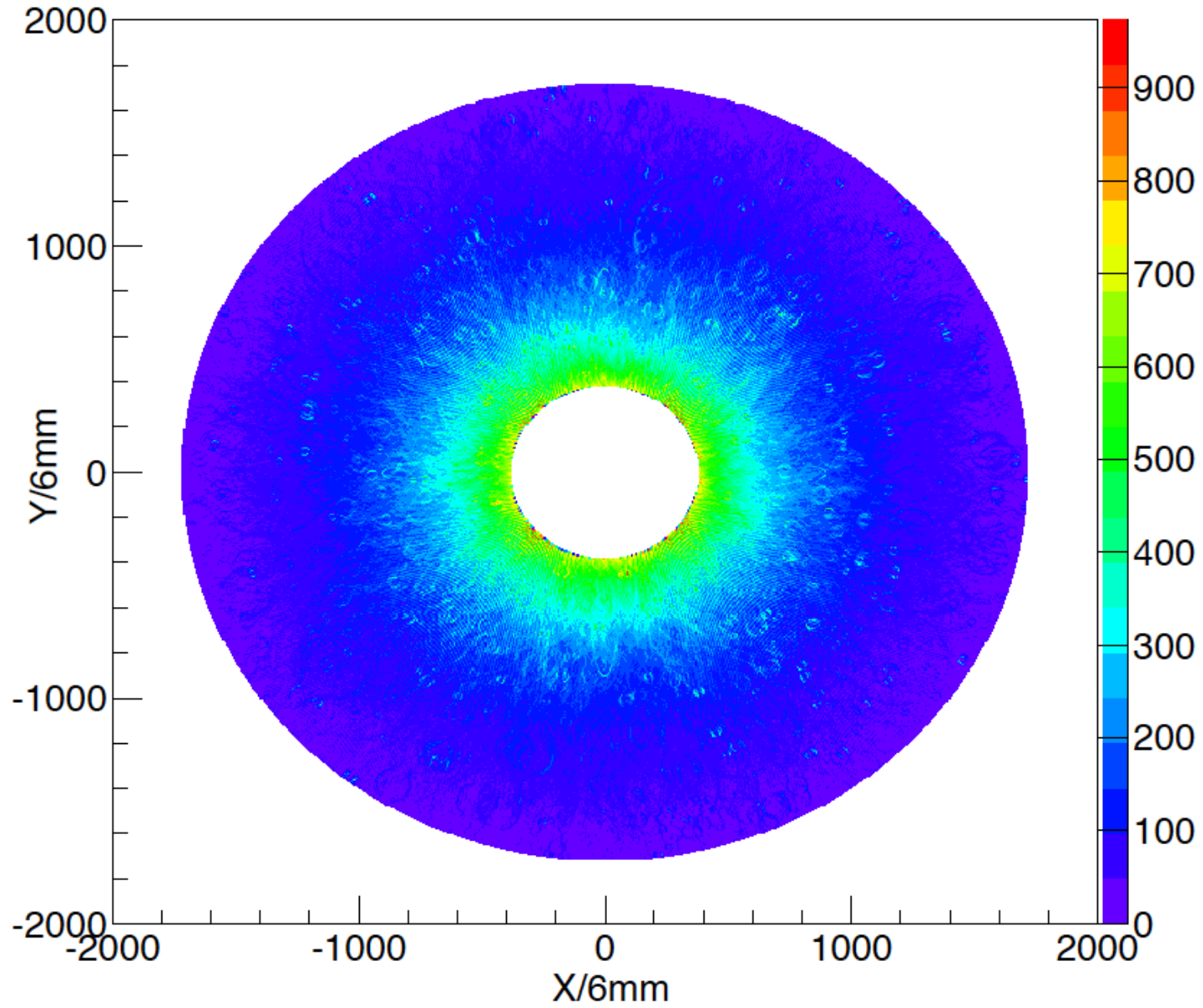
TPC Occupation at CEPC Z pole



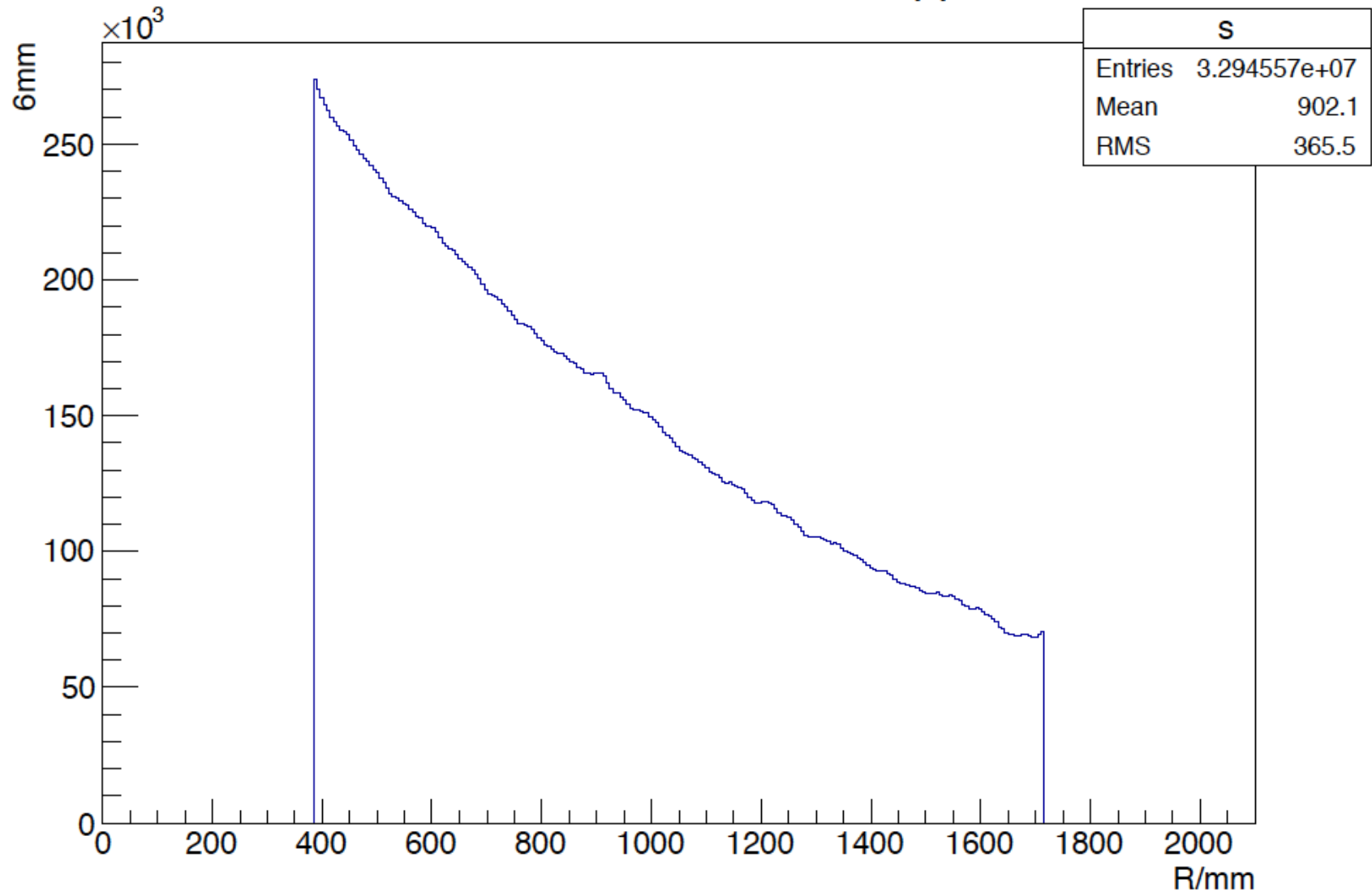
Manqi Ruan

Input: TPC Hit Profile of Fully
Simulated $Z \rightarrow qq$ events

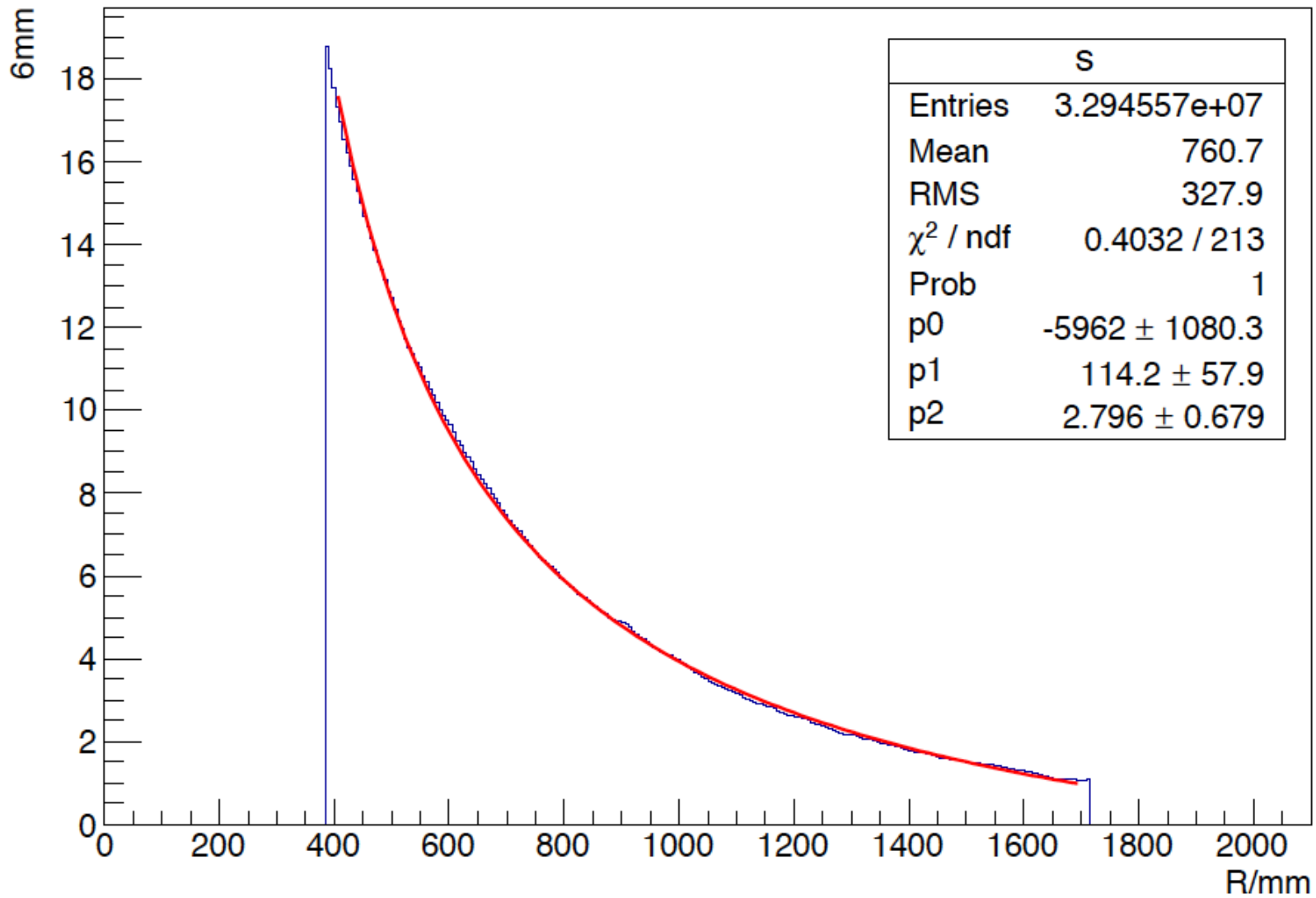
TPC Hit Map of 7500 Z->qq events at Z pole



Radius Profile for 7500 qq events



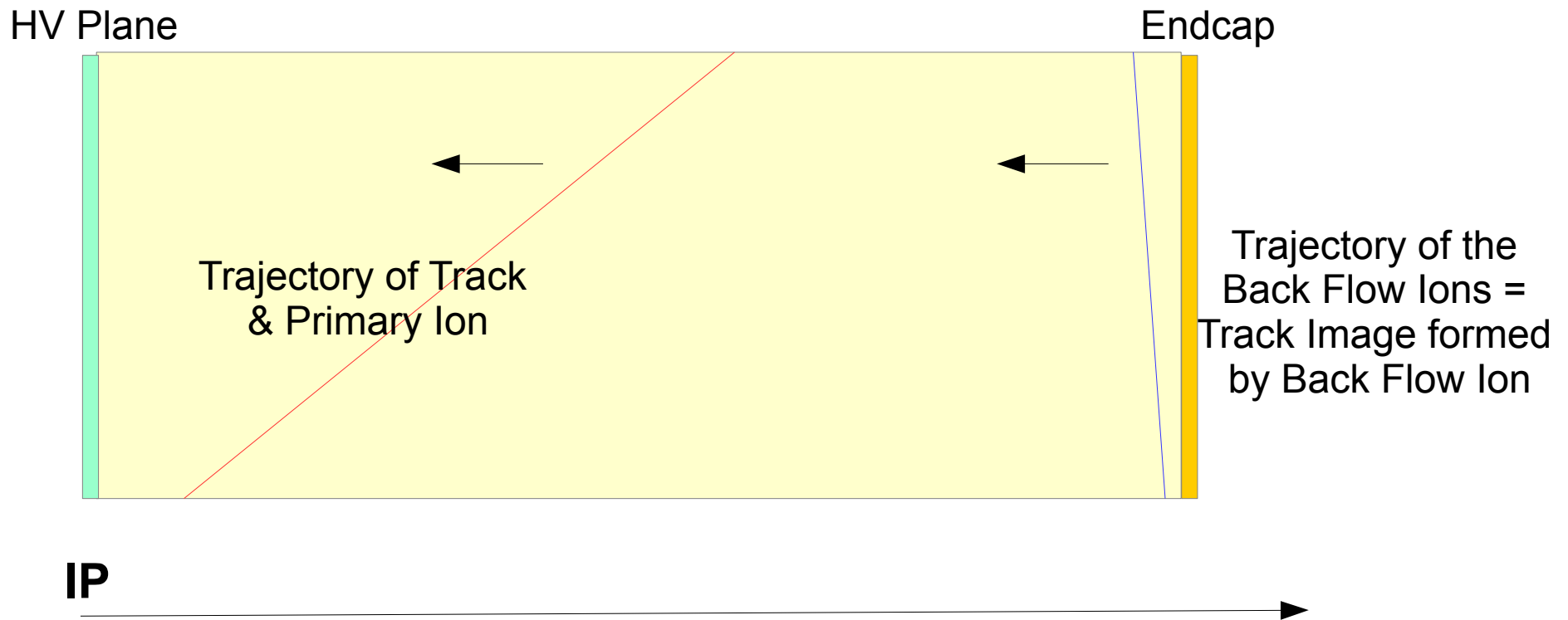
Hits/mm² for 7500 Z to qq at Z pole



Fit results

- Per 7500 events:
 - Hit Rate = $6000/(x - 114) - 2.8$; (per mm^2)
- At Instant Luminosity = $2\text{E}34/\text{IP}$;
 - Event Rate = 600 Hz. ($30 \text{ nb} * 2\text{E}-5 \text{ fb}^{-1}\text{s}^{-1}$)
 - Hit Rate = $480/(x - 114) - 0.224$ (Hz/ mm^2)
- At Instant Luminosity = $2\text{E}36$
 - Event Rate = 60000 Hz
 - Hit Rate = $48000/(x-114) - 22.4$ (Hz/ mm^2);

1st limit factor: Charge Density

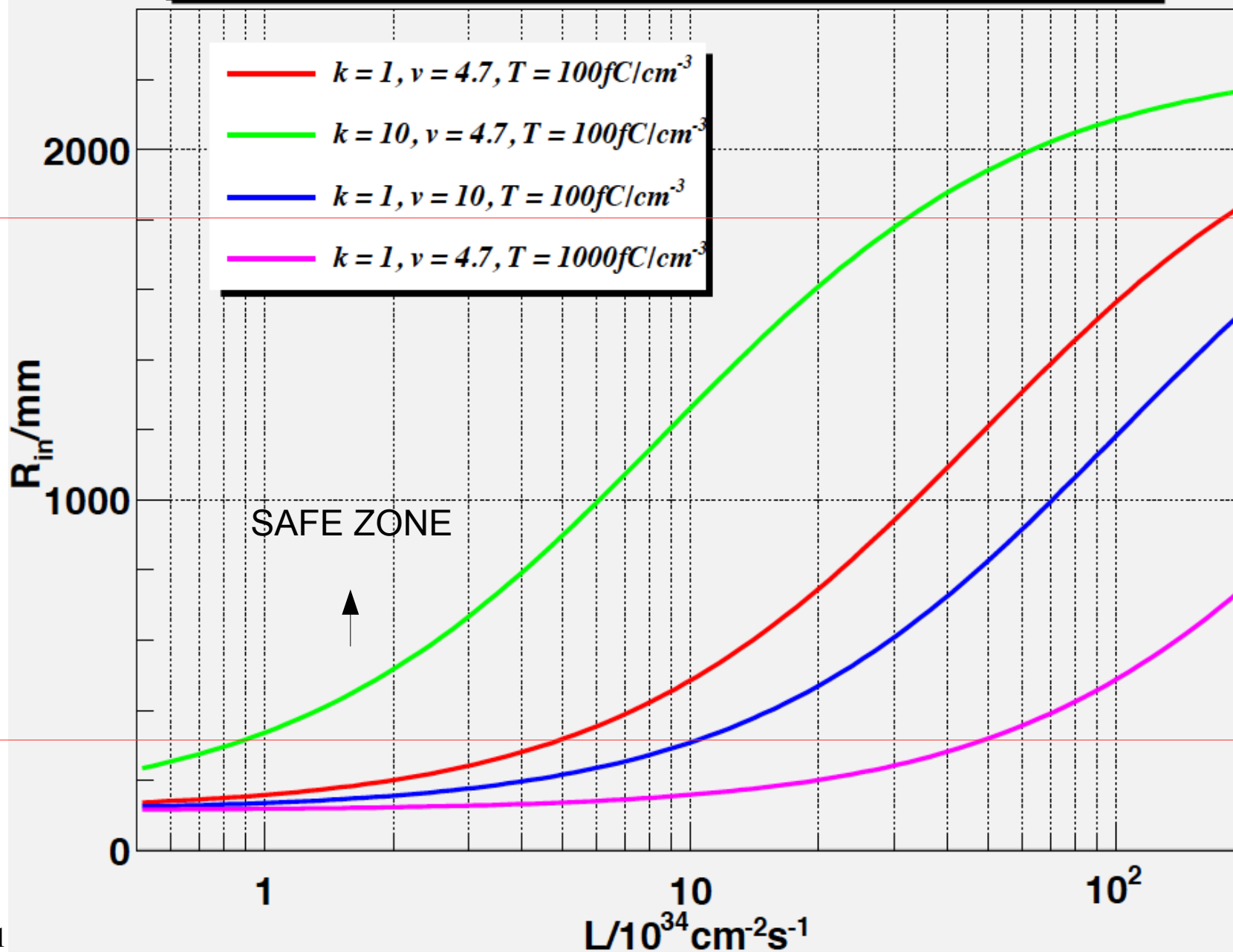


Quarter view of the TPC

Charge Density

- Charge Density: $\rho(r) = 22 \cdot (1+k) \cdot L/v \cdot (480/(r-114) - 0.224)$
 - Follows the same distribution to the Hit Density
 - Assume evenly distributed along Z direction
 - Quantity & Units:
 - ρ : charge density, unit in fQ/cm³
 - k : ratio between back flow ion to the primary ionization;
 - L : Luminosity Unit in 10³⁴cm⁻²s⁻¹;
 - v : Drift velocity of ion, unit in m*s⁻¹;
 - r : radius of the TPC test point, for instance TPC inner radius, unit in mm
- Define a tolerance level of Charge Density: T (fQ/cm³)
 - From Fujii San, 100 fQ/cm³ = 5 micrometer distortion (in X-Y plane?...)
 - TPC spatial resolution is 0.1 mm, maybe this limit can be limited to 1000 fQ/cm³
- Then the dependence of T and R (TPC inner radius) can be resolved as:
 - $R = 114 + 480 / (0.224 + T \cdot v / (22 \cdot (1+k) \cdot L))$

Safety Boundary of TPC inner Radius at different Luminosity



2nd limit factor: Voxel Occupancy

Beam Parameter at CEPC Z pole

- CEPC Z pole Bunch Structure
 - 40 MHz in phase with TPC readout;
 - 40 M bunches per second; 25 ns separation = 7.5 m separation
 - Luminosity:
 - $2.0 * 10^{34} \text{ cm}^{-2}\text{s}^{-1} = 2 * 10^{-5} \text{ fb}^{-1} * \text{s}^{-1}$
 - Per bunch
 - Integrated Luminosity $5 * 10^{-13} \text{ fb}^{-1} = 0.5 \text{ mb}^{-1}$
 - Z->qq events: $30 \text{ nb} * 0.5 \text{ mb}^{-1} = 1.5 * 10^{-5}$
 - Even if 2E36: $1.5\text{E-}3$ Z->qq Events per Bunch Xing

Voxel occupancy

- Giving 40 Mhz DAQ rate (25 ns interval) & 80 $\mu\text{m}/\text{ns}$ drift velocity, the Distance difference between 2 DAQ rate is:
 - 2 mm \sim (80km/s)
 - 7.5m \sim (300000km/s)
- Therefore the Voxel Volume = 2mm * 1mm * 6mm (in the default design)
- Total N Pixel = $\pi \cdot (1800^2 - 330^2) / 6 = 3.3\text{E}6$
- Number of Voxel in one snapshot = $3.3\text{E}6 * 1175 = 3.9\text{E}9$ Voxels;
- Number of Voxel in one second = $3.3\text{E}6 * 40 \text{ M} = 1.32\text{E}14$ Voxels;
- Number of Hits in one second: Depends on the luminosity:
 - $2\text{E}34$, 600 qq events, $2.64\text{E}6$ Hits;
 - $2\text{E}35$, 6000 qq events, $2.6\text{E}7$ Hits;
 - $2\text{E}36$, 60000 qq events, $2.6\text{E}8$ Hits;
- Voxel Occupancy: of the order of $1\text{E}-8$ to $1\text{E}-6$...

VERY SAFE...

Beam Parameter at CLIC

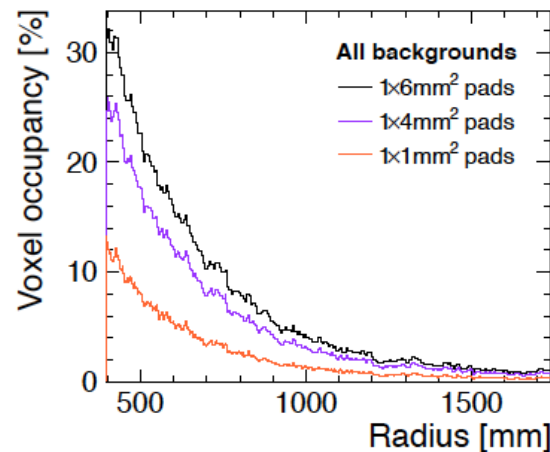
- CLIC Bunch Structure

- 0.5ns separation, 312-354 (3/0.5 TeV) bunches/train, 50 Hz (50 trains per second)
- 1 train = 156 – 177 ns;
- All trains = 7800 – 8850 ns
- **Occupancy = $1.13 - 1.28 \cdot 10^{-5}$**
- Luminosity: $2.3 - 5.9 \cdot 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- Luminosity per sec: $2.3 - 5.9 \cdot 10^{-5} \text{ fb}^{-1}$
- Luminosity per bunch
 - Assume at Z pole: $10 \mu\text{b}^{-1}$ per bunch $\sim 0.3 \text{ Z} \rightarrow \text{qq}$ per bunch
 - 0.5 TeV: $6.5 \cdot 10^{-8} \text{ fb}^{-1} = 65 \mu\text{b}^{-1}$
 - 3 TeV: $1.89 \cdot 10^{-7} \text{ fb}^{-1} = 189 \mu\text{b}^{-1}$

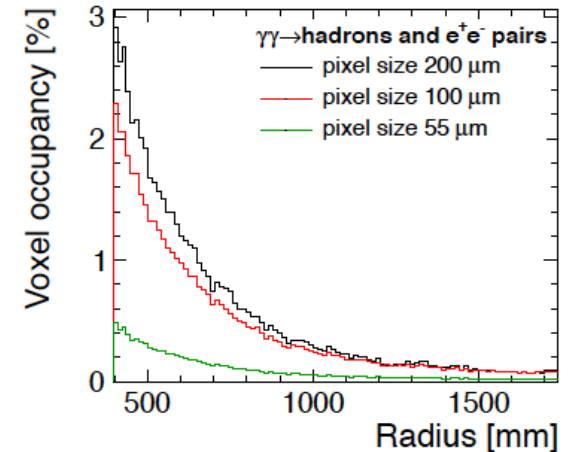
Parameter	Units	$\sqrt{s} = 500 \text{ GeV}$	$\sqrt{s} = 3 \text{ TeV}$
f_{rep}	Hz	50	50
n_b		354	312
Δt	ns	0.5	0.5
N		$6.8 \cdot 10^9$	$3.7 \cdot 10^9$
σ_x	nm	202	≈ 40
σ_y	nm	2.26	≈ 1
σ_z	μm	72	44
\mathcal{L}	$\text{cm}^{-2}\text{s}^{-1}$	$2.3 \cdot 10^{34}$	$5.9 \cdot 10^{34}$
$\mathcal{L}_{0.01}$	$\text{cm}^{-2}\text{s}^{-1}$	$1.4 \cdot 10^{34}$	$2.0 \cdot 10^{34}$
n_γ		1.3	2.1
$\Delta E/E$		0.07	0.28
N_{coh}		$2 \cdot 10^2$	$6.8 \cdot 10^8$
E_{coh}	TeV	$1.5 \cdot 10^1$	$2.1 \cdot 10^8$
N_{incoh}		$8 \cdot 10^4$	$3 \cdot 10^5$
E_{incoh}	TeV	$3.6 \cdot 10^2$	$2.3 \cdot 10^4$
n_{Had}		0.19	3.2

Voxel occupancy for CLIC: Validation

- CLIC: 3 gammagamma->Hadrons events per bunch Xing;
- For each bunch train: 1000 events;
- 1000 events -> 4000 tracks -> 800000 hits (Big Assumption), in 150 ns;
- $150 \text{ ns} * 80 \text{ micrometer/ns} = 12000 \text{ micrometer} = 12 \text{ mm} = 6 \text{ separation}$
- Voxel number in 150 ns:
 - $1.66\text{E}6 * 6 = 1\text{E}7$
- Occupancy = 0.08;
- Inner Vs Outer:
 - Scale = 3 -> 24%.



(a) The voxel occupancy for different pad sizes [4].



(b) The voxel occupancy for different pixel sizes.

Conclusion

- Considering Z→qq sample only
 - Need to considering gammagamma background, etc.
- TPC Usage limited by
 - Local Charge Density that perturbate the Hit position, Tolerance level ~ 100fC/cm³, result in a deviation of 5 micrometer in position resolution
 - Leads to a constrain of TPC inner radius & Integrated luminosity
 - Optimized scenario: Inner Radius > 500 mm at L = 2E36
 - Tolerance = 1000 fC/cm³,
 - Ion Shift velocity: $v = 4.7$ m/s,
 - Ratio between back flow Ion yield to Primary ionization $k = 1$;
- Voxel Occupancy (NOT A Limiting Factor)
 - Orders of magnitude lower than the CLIC Case as the beam bunch time structure is much evenly distributed
 - Of the order of 1E-8 to 1E-6 at 2E34 to 2E36 Luminosity, which 40 Mhz bunch separation (25ns = 7.5 m bunch separation)