

Six-body calculation for electric-dipole response of ${}^6\text{Li}$

Hokkaido University, Japan

Shuji Satsuka

Wataru Horiuchi

Introduction

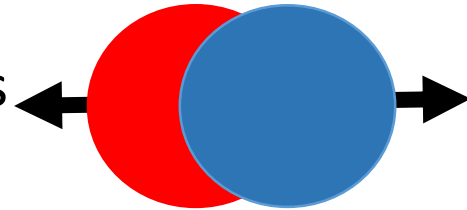
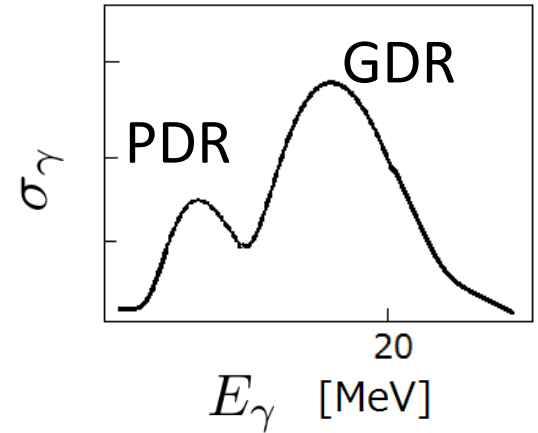
Electric-dipole (E1) response reflects the nuclear structure

- ✓ The peak energy region
- ✓ The shape of peak

⋮

Giant-dipole-resonance (GDR)

- large and broad peak
- occurring at high energy region
- out-of-phase oscillation of all protons and neutrons



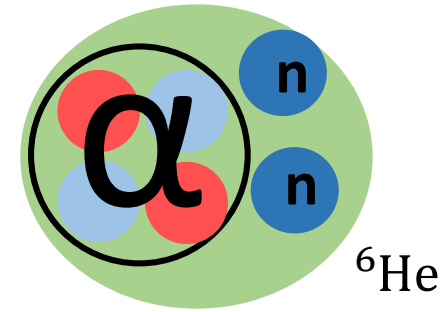
Pygmy-dipole-resonance (PDR)

- Occurring at low energy region in neutron-proton unbalanced nuclei
- Mechanism is still controversial

The mode is collective, one-particle excitation or ...

Introduction

$\alpha(^4\text{He})$ cluster structure appears in light nuclei (e.g. ^6He , ^6Li , ...)



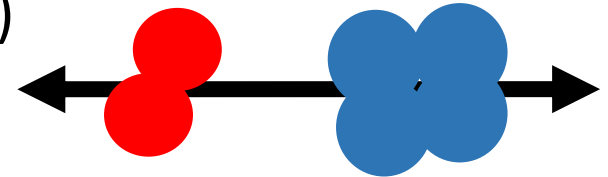
In the case of ^6He , there are two modes of GDR

D. Mikami, W. Horiuchi, and Y. Suzuki, Phys. Rev. C89, 064303 (2014)

Two valence neutrons is bound weakly

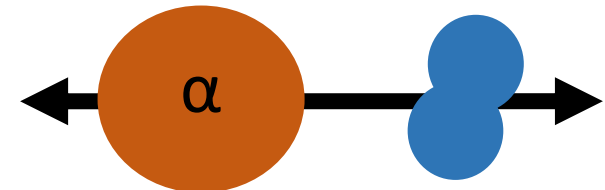
GDR

- occurring at high energy region ($\sim 30\text{MeV}$)



Soft-dipole mode (SDM)

- out-of-phase oscillation of α and two valence neutron
- occurring at low energy region ($\sim 3\text{MeV}$)

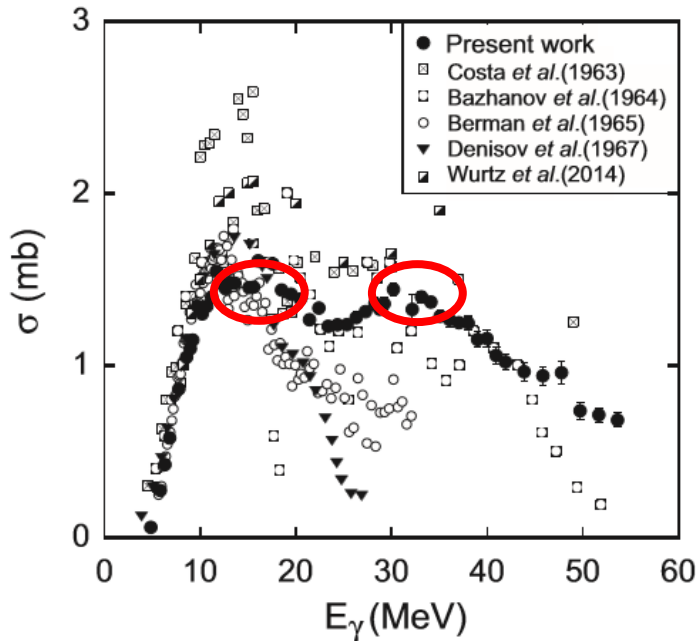


Introduction

The photoabsorption reaction cross section was measured for ${}^6\text{Li}$ recently

Two peak structure was shown

They conjectured ...



$E_\gamma \sim 12 \text{ MeV}$ GDR of ${}^6\text{Li}$

$E_\gamma \sim 33 \text{ MeV}$ GDR of ${}^4\text{He}$ in ${}^6\text{Li}$

However the GDR of free ${}^4\text{He}$ was shown to occur at 26 MeV

W. Horiuchi, Y. Suzuki, K. Arai, Phys. Rev. C 85 (2012) 054002

${}^4\text{He}$ is distorted

by interaction with other particles



FIG. 9. Comparison of the present data with the ${}^6\text{Li}(\gamma, n)$ reaction data reported by Costa *et al.* [1], Bazhanov *et al.* [2], Denisov *et al.* [3], Berman *et al.* [4], and Wurtz *et al.* [5]. For simplicity, error bars in the previous data are not shown.

T. Yamagata *et al.* Phys. Rev. C 95, 044307, (2017)

Introduction

Its conjecture are not confirmed by
fully microscopic (six-body) calculation



The distortion of α cluster is taken into account naturally

Purpose

- Perform fully microscopic calculation for ground and E1 excited states of ${}^6\text{Li}$
- Understand the E1 excitation mechanism of ${}^6\text{Li}$

Problem

□ Difficulty to calculate many-body system

- ✓ describe the full variety of correlations between particles
 - ➔ Correlated Gaussian (CG) basis expansion
 - Correlations are described explicitly
- ✓ High calculation cost : the number of bases increases ,
the cost becomes higher
 - ➔ Stochastic variational method (SVM)
 - More important bases are selected

K.Varga and Y.Suzuki Phys. Rev .C52 (1995), 6

Method: Wave function

Schrödinger equation

$$\hat{H}\Psi = E\Psi$$

Hamiltonian

$$H = \sum_{i=1}^N T_i - T_{c.m.} + \sum_{j>i=1}^N (V_{ij}^{NN} + V_{ij}^{coul})$$

Wave function $\rightarrow$ Basis expansion

$$\Psi = \sum_i c_i \varphi_i$$

Variational method + Basis expansion

Generalized eigenvalue problem



$$H\mathbf{c} = E\mathbf{B}\mathbf{c}$$

$$B_{jk} = \langle \varphi_j | \varphi_k \rangle$$

$$H_{jk} = \langle \varphi_j | \hat{H} | \varphi_k \rangle$$

Method: Basis function

$$\varphi_i = \mathcal{A}[\exp(-\frac{1}{2}\tilde{\mathbf{x}}A_i\mathbf{x})\chi_S^{(i)}\eta] \text{ :basis function}$$

Correlated Gaussian

$$\chi_S^{(i)} = [[\chi^1\chi^2]_{S_{12}^{(i)}}\chi^3]_{S_{123}^{(i)}}\cdots\chi^6]_{S=1}$$

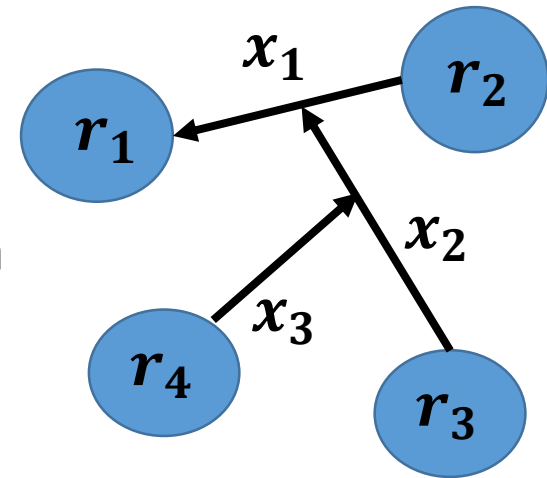
$$\eta = |\text{pppnnn}\rangle$$

A_i :positive-definite matrix

$$\tilde{\mathbf{x}}A\mathbf{x} = \sum_{j,k=1}^N A_{jk}\mathbf{x}_j \cdot \mathbf{x}_k$$

Off diagonal elements describe correlations among particles

Variational parameters $A_i, \chi_S^{(i)}$



$\mathbf{x} = (x_1, \cdots x_{A-1})$
:Jacobi coordinates

Method: Selection of bases

Stochastic variational method (SVM)

K.Varga and Y.Suzuki Phys. Rev .C52 (1995), 6

- ① Candidates of variational parameter set $\{A^1, A^2, \dots, A^K\}$ are generated randomly
- ② Energies $\{E^1, E^2, \dots, E^K\}$ for each set are calculated
- ③ Set A^i giving lowest energy is selected and added in bases
- ④ ①~③ are repeated until the energy reaches convergence

Results: ground state

$V_{ij}^{NN} = (V_1 + \frac{1}{2}(1 + P_{ij}^\sigma)V_2 + \frac{1}{2}(1 - P_{ij}^\sigma)V_3)(\frac{1}{2}u + \frac{1}{2}(2 - u)P_{ij}^r)$:Minnesota potential

$V_l = V_{0l} \exp(-\mu_l |\mathbf{r}_i - \mathbf{r}_j|^2)$ D. R. Thompson *et al.* Nucl. Phys. A286 (1977) ,53

	r_m [fm]	r_p [fm]	r_n [fm]	$E_{g.s.}$ [MeV]
${}^6\text{He}$	2.40	1.83	2.64	-30.95
${}^6\text{He}(*)$	2.41	1.83	2.65	-30.98

Experimental S_{2N} is reproduced by adjusting the u value

(*)D. Mikami, W. Horiuchi, and Y. Suzuki, Phys. Rev. C89, 064303 (2014)

	r_m [fm]	r_p [fm]	r_n [fm]	$E_{g.s.}$ [MeV]	S_{2N} [MeV]
${}^6\text{Li}$	2.29	2.29	2.29	-33.90	4.0
${}^6\text{Li}(\text{Exp.})$		2.45		-31.99	3.7

F. Ajzenberg-Selove, Nucl. Phys. A413, 1 (1984)

Different u values to reproduce the experimental data of rms radius can be considered

E1 excited state

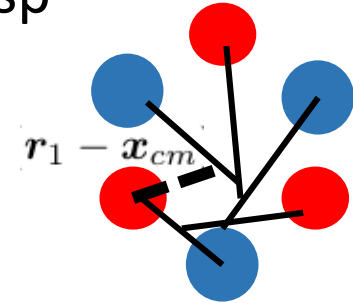
E1 strength

$$B(E1, E_\nu) = \frac{1}{2J_{g.s.} + 1} \sum_{M, m} | \langle \Phi_M^{(ex)}(E_\nu) | M(E1, \mu) | \Phi_m^{(g.s.)} \rangle |^2$$

E1 operator

$$M(E1, \mu) = \sqrt{\frac{4\pi}{3}} e \sum_{i \in \text{proton}} \mathcal{Y}_{1\mu}(\mathbf{r}_i - \mathbf{x}_{cm})$$

sp



Model space

W. Horiuchi, Y. Suzuki, K. Arai, Phys. Rev. C 85 (2012) 054002

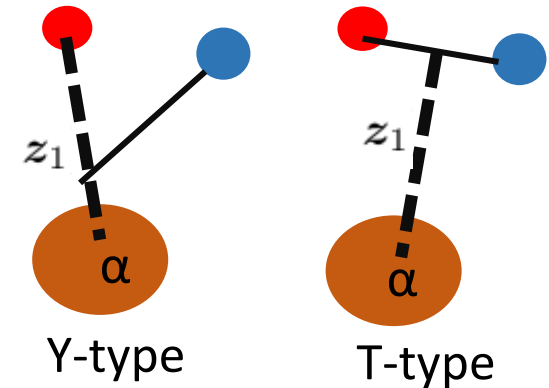
single-particle (sp) excitation

$$\phi_i^{(sp)} = \mathcal{A}[\phi_i^{(6\text{Li})} \mathcal{Y}_{1\mu}(\mathbf{r}_1 - \mathbf{x}_{cm})]_J$$

$\alpha + p + n$ decay channel

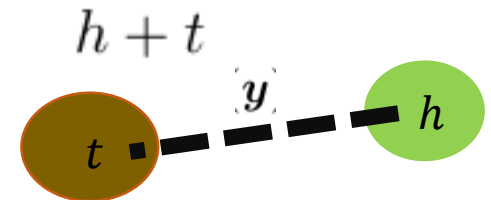
$$\phi_i^{(\alpha pn)} = \mathcal{A}[\phi_i^{(\alpha)} \exp(-\frac{1}{2} \tilde{z} B_i \mathbf{z}) [[\chi^{(5)} \chi^{(6)}]_{s_1}] \mathcal{Y}_{1\mu}(\mathbf{z}_1)]_{J_1} J$$

$\alpha + p + n$



$h(^3\text{He}) + t(^3\text{H})$ decay channel (Not included in this work)

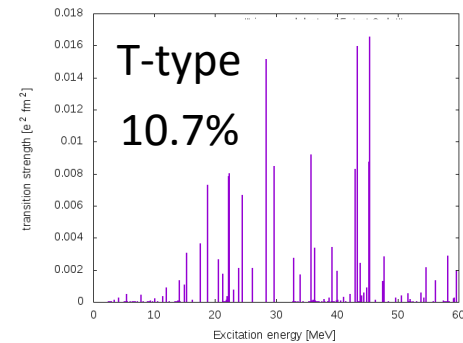
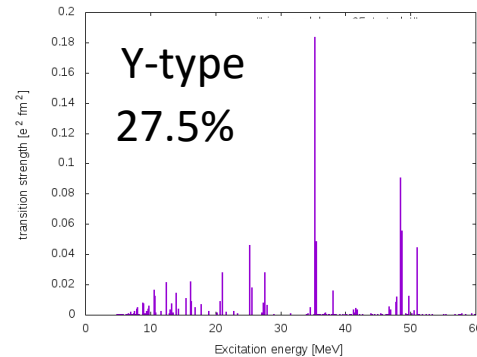
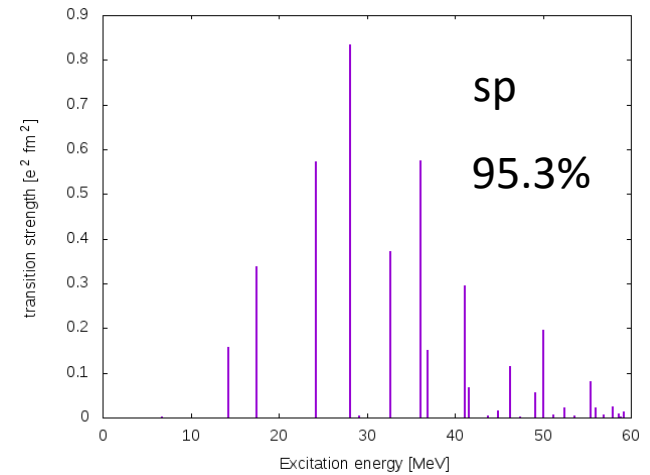
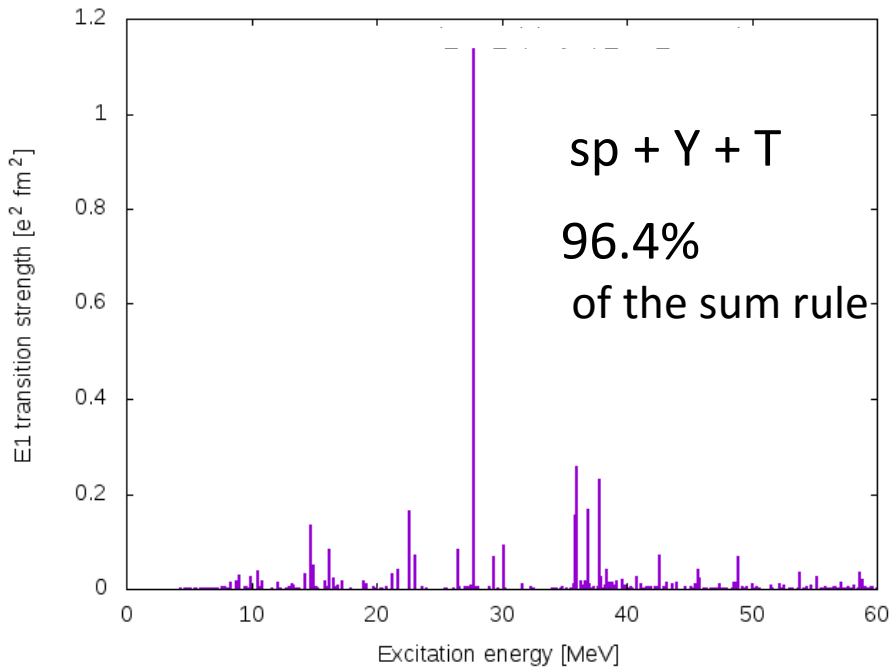
$$\phi_i^{(ht)} = \mathcal{A}[[\phi_i^{(h)} \phi_i^{(t)}]_{J_1} \exp(-\frac{1}{2} a \mathbf{y}^2) \mathcal{Y}_{1\mu}(\mathbf{y})]_{J_2} J$$



Results: E1 strength

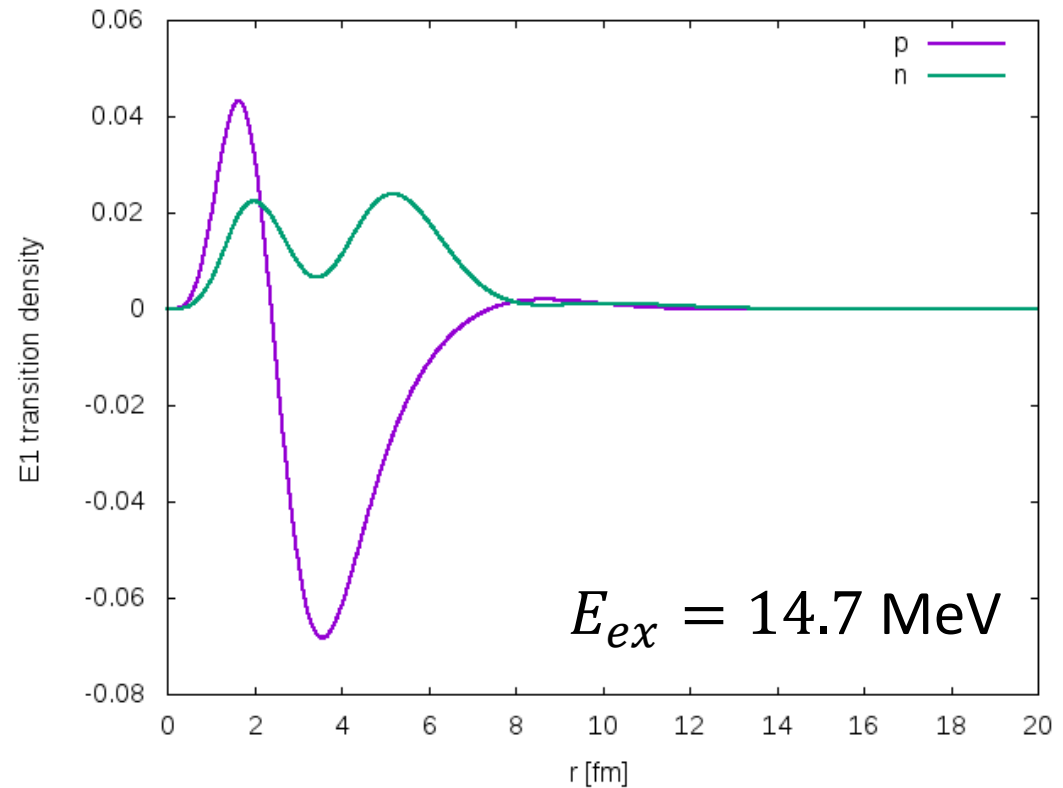
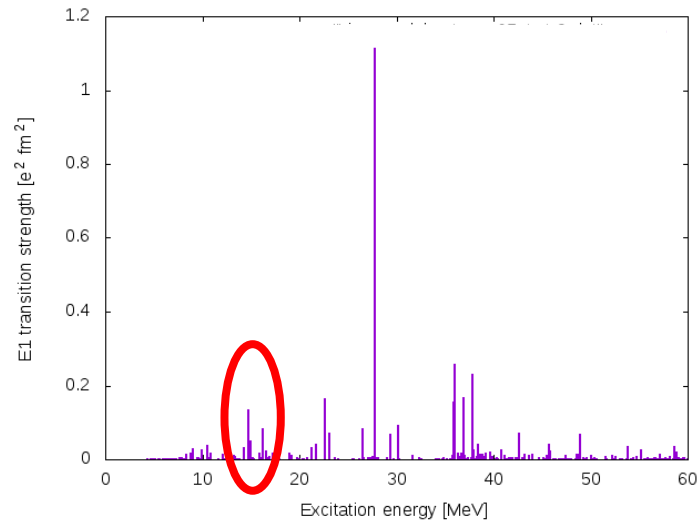
E1 sum rule

$$\sum_{\nu} B(E1, E_{\nu}) = e^2 (Z^2 \langle r_p^2 \rangle - \frac{Z(Z-1)}{2} \langle r_{pp}^2 \rangle)$$



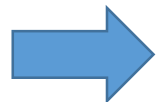
Results: Transition density

$$\rho_{p/n}^{tr}(E_\nu, r) = \langle \Phi^{(ex)}(E_\nu) | \sum_{i \in p/n} \mathcal{Y}_1(\mathbf{r}_i - \mathbf{x}_{cm}) \delta(|\mathbf{r}_i - \mathbf{x}_{cm}| - r) | \Phi^{(g.s.)} \rangle$$

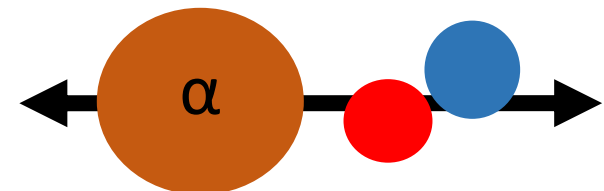


interior region $r < 2.5 \text{ fm}$
: in-phase

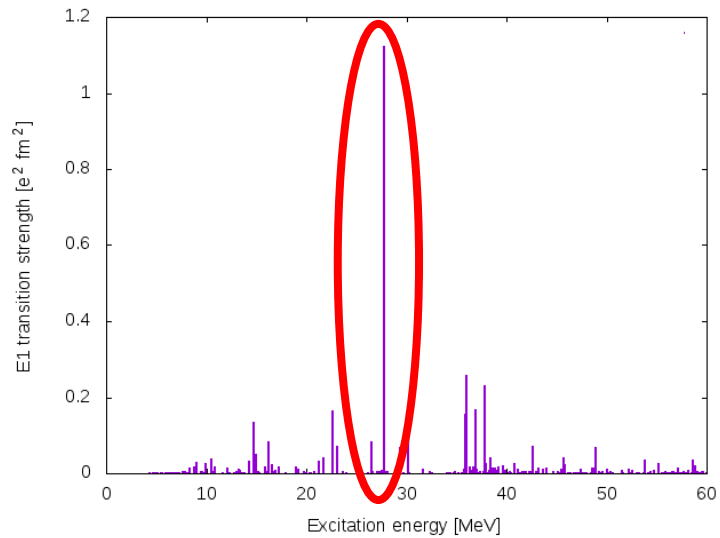
external region $r > 2.5 \text{ fm}$
: out-of-phase



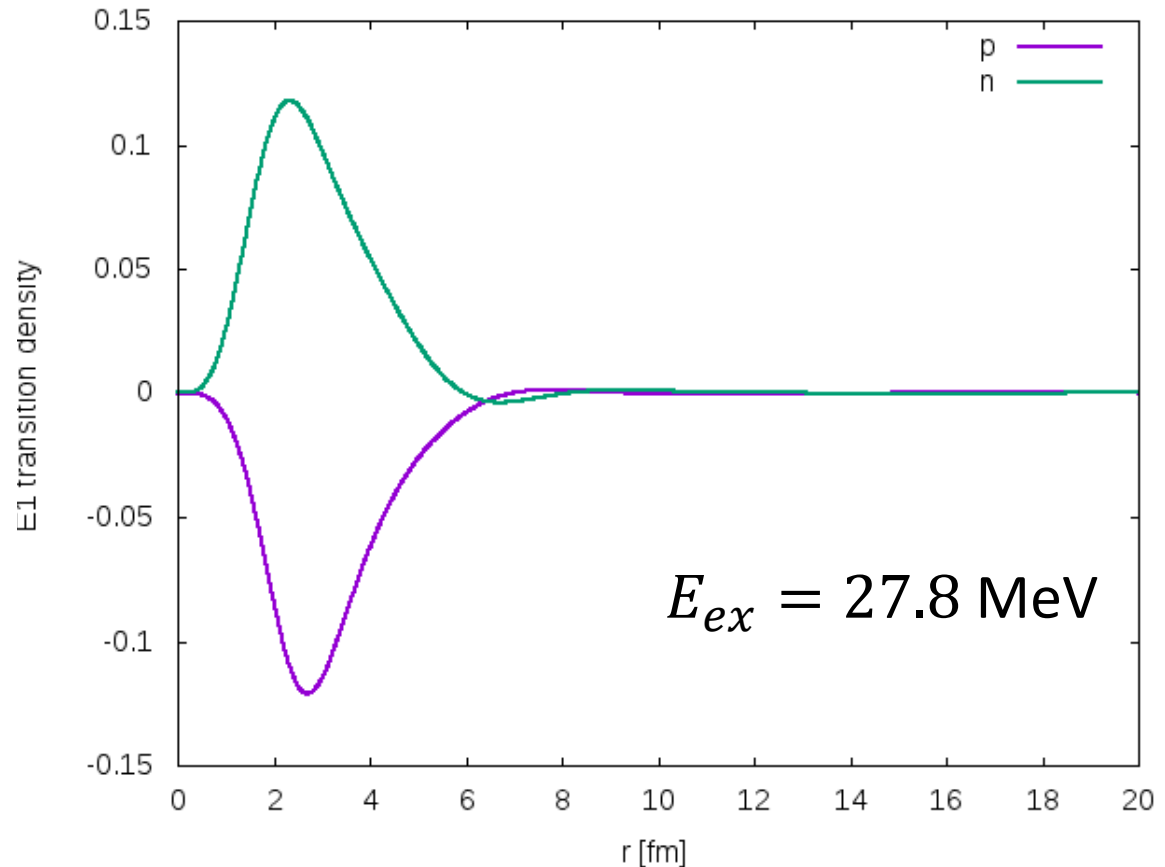
Like soft-dipole mode



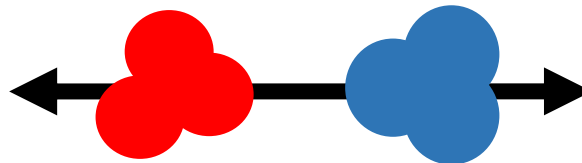
Results: Transition density



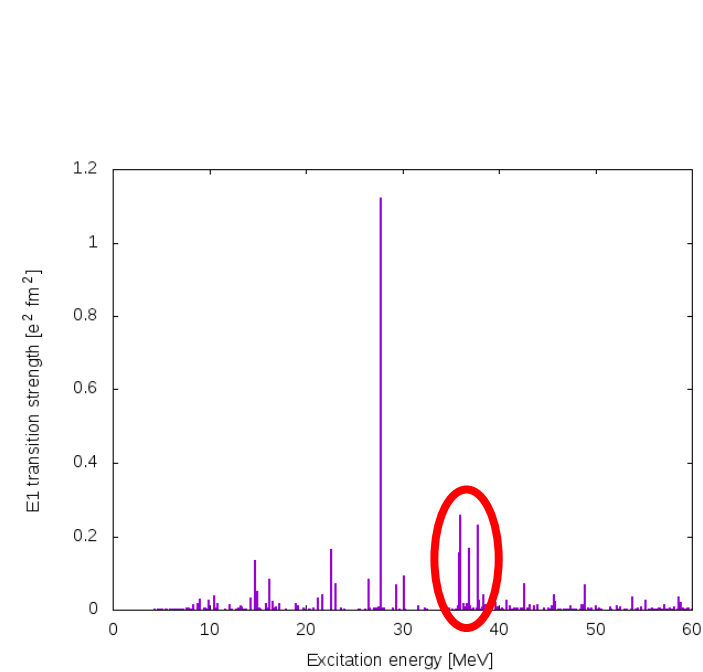
whole region
: out-of-phase



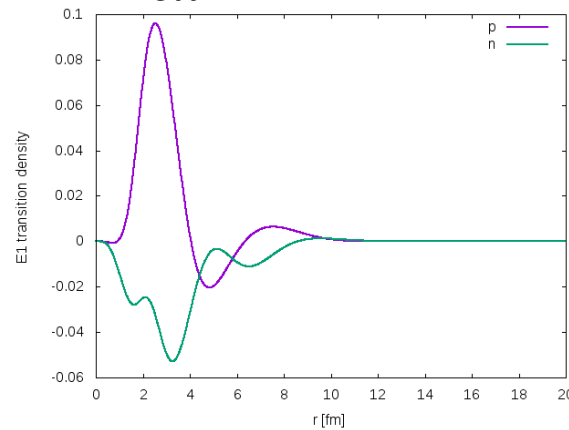
➡ GDR of ${}^6\text{Li}$



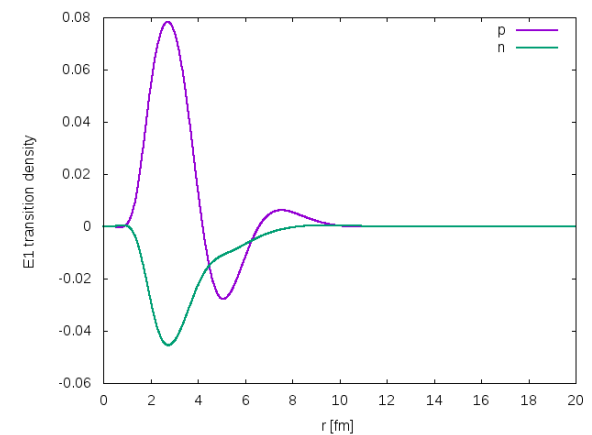
Results: Transition density



$E_{ex} = 36.0 \text{ MeV}$

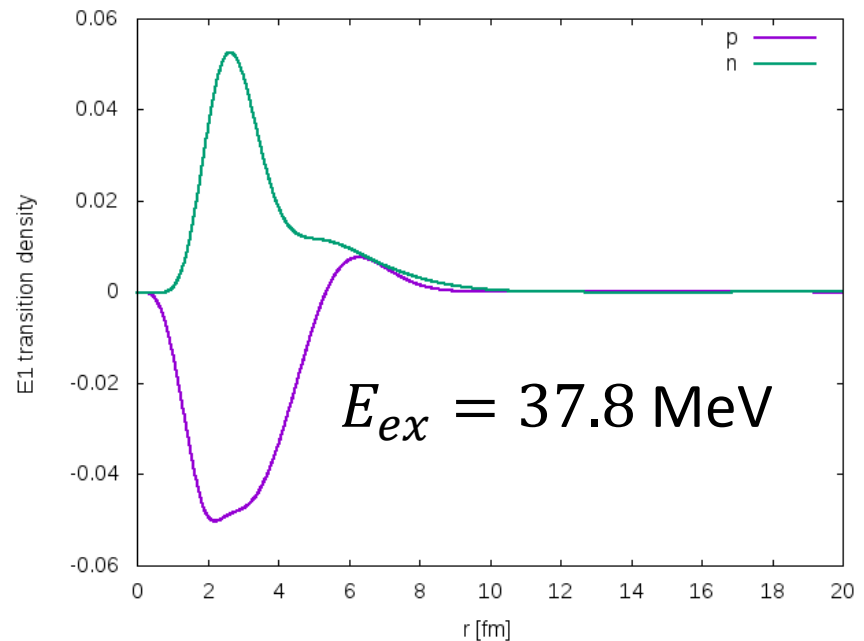
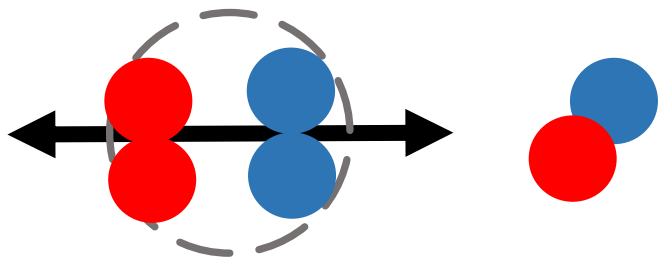


$E_{ex} = 36.9 \text{ MeV}$



interior region $r < 4 \text{ fm}$
: out-of-phase

➡ GDR of ^4He (α) in ^6Li ?



Summary

- ✓ Six-body calculation for ground and E1 excited state of ${}^6\text{Li}$ is performed
- ✓ The u parameter of Minnesota potential is adjusted to reproduce the experimental data of two nucleon separation energy for the ground state
- ✓ The E1 strength and transition density show the possibility of three modes of GDR, SDM, GDR of ${}^6\text{Li}$ and GDR of ${}^4\text{He}$ in ${}^6\text{Li}$

Future work

- Add $h + t$ decay channel to the model space
- Detail analyses of the modes of GDR