

# Masses of singly and doubly heavy baryons within the $SU(3)$ chiral quark-soliton model

June-Young Kim

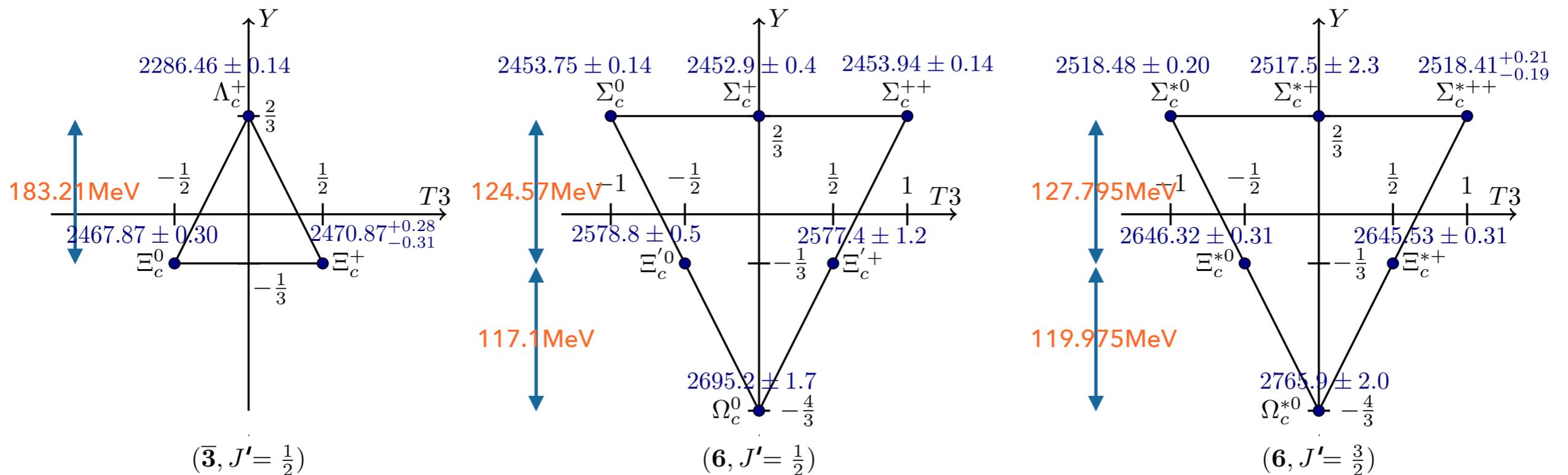
Department of Physics

Inha University



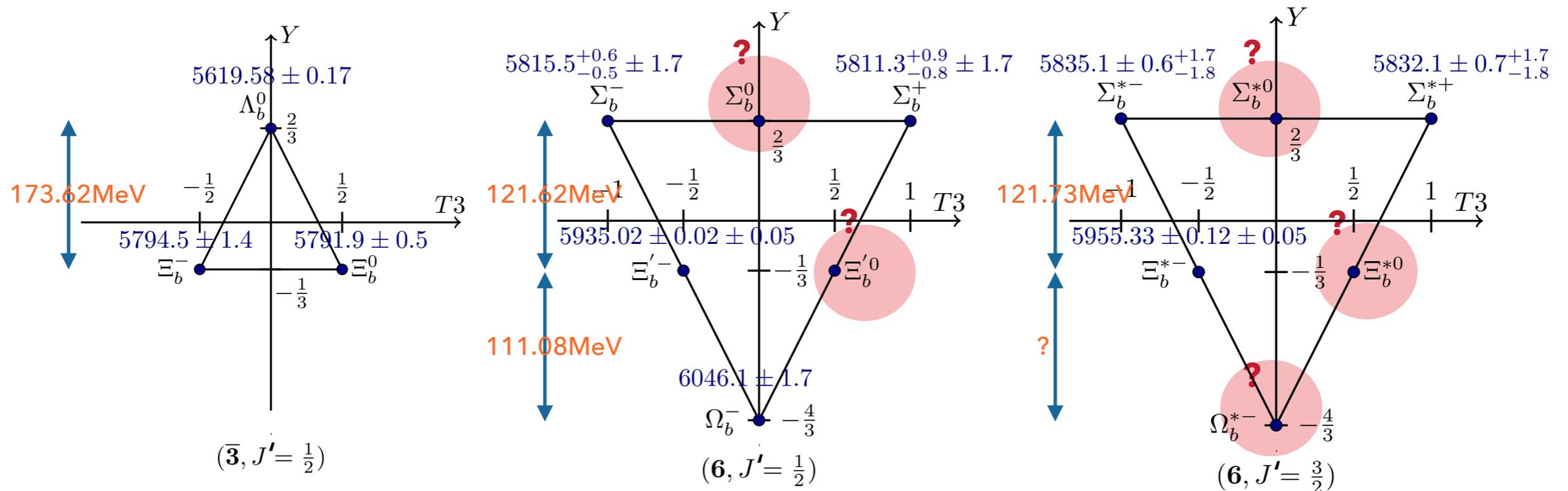
- ▶ Motivation
- ▶ Chiral quark-soliton model
- ▶ Mass splittings of the singly heavy baryons
- ▶ Masses of the singly heavy baryons
- ▶ Masses of the doubly heavy baryons

- ▶ The masses of light baryons are well known in the ground state and were described very well in the chiral quark-soliton model.
- ▶ We want to extend the model to explain the mass spectra of heavy baryons.

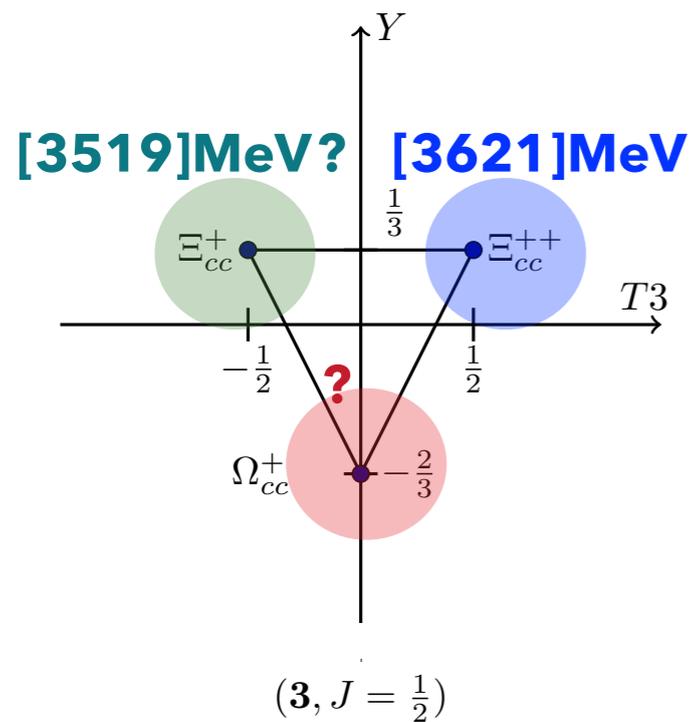


- ▶ As  $m_Q \rightarrow \infty$ , heavy quark spin is conserved, which leads to the fact that the light-quark spin is also conserved.
- ▶ The soliton and a heavy quark are decoupled and the heavy quark plays a role of the static color source.

- ▶ The masses of charmed baryons are well known. Thus we will first check the validity of the present approach in the charmed sector.



- ▶ On the other hand, some of bottom baryon masses are unknown.
- ▶ In this talk, we will show how **the mass of  $\Omega_b^{*-}$  is predicted.**



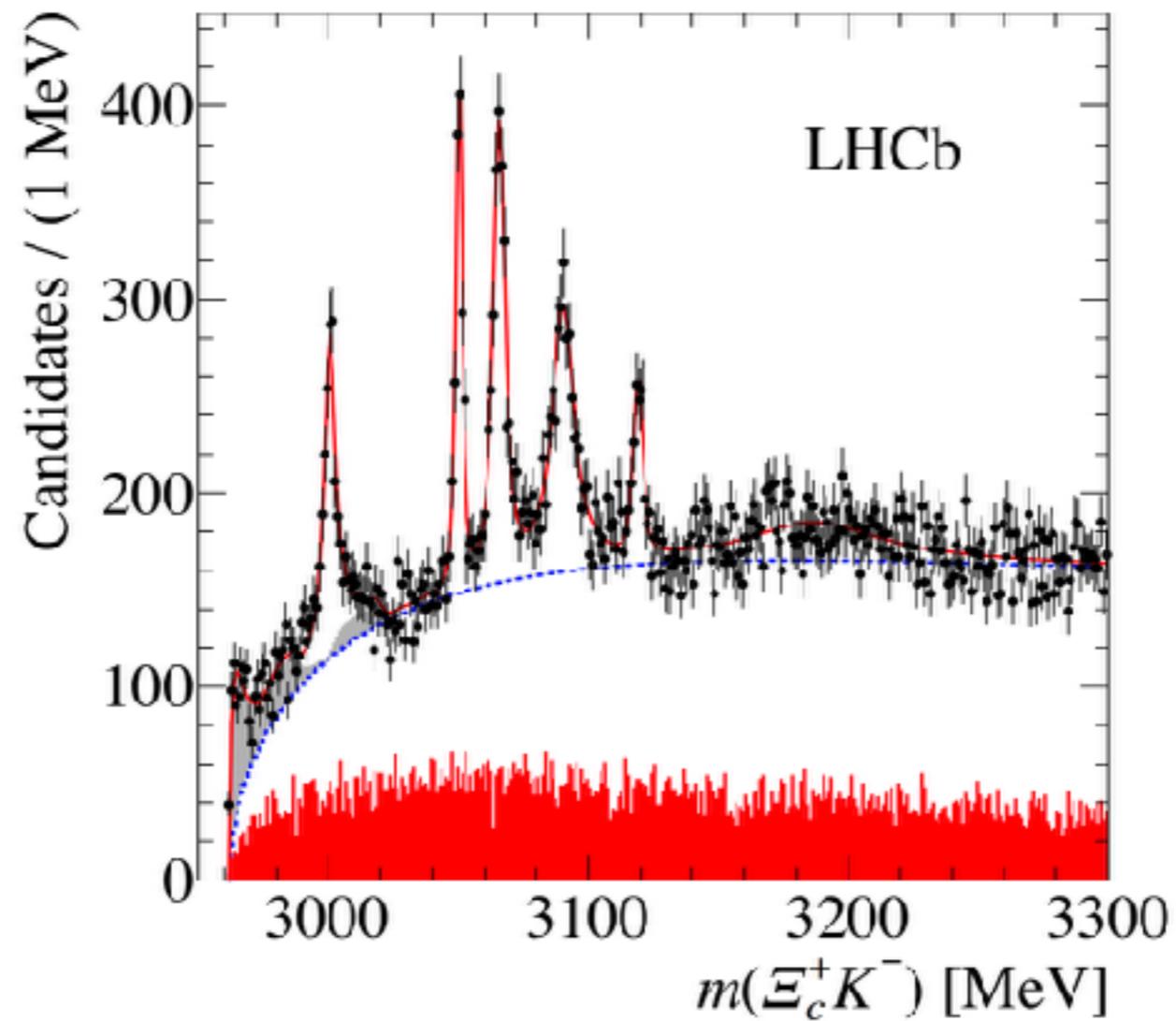
M. Mattson *et al* [SELEX Collaboration], Phys. Rev. Lett. **89**, 112001 (2002) :

$$M_{\Xi_{cc}^+} = (3519 \pm 1) \text{ MeV}$$

R. Aaij *et al.* [LHCb Collaboration], arXiv:1707.01621 [hep-ex] :

$$M_{\Xi_{cc}^{++}} = (3621.4 \pm 0.72 \pm 0.27 \pm 0.14) \text{ MeV}$$

- ▶ The mass of the  $\Omega_{cc}^+$  is unknown. Recently, the mass of the  $\Xi_{cc}^{++}$  was found. Using this data, we can predict that of  $\Omega_{cc}^+$



Five  $\Omega_c^0$ s were  
announced by  
LHCb Coll.

R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. Lett. **118**, no. 18, 182001 (2017)

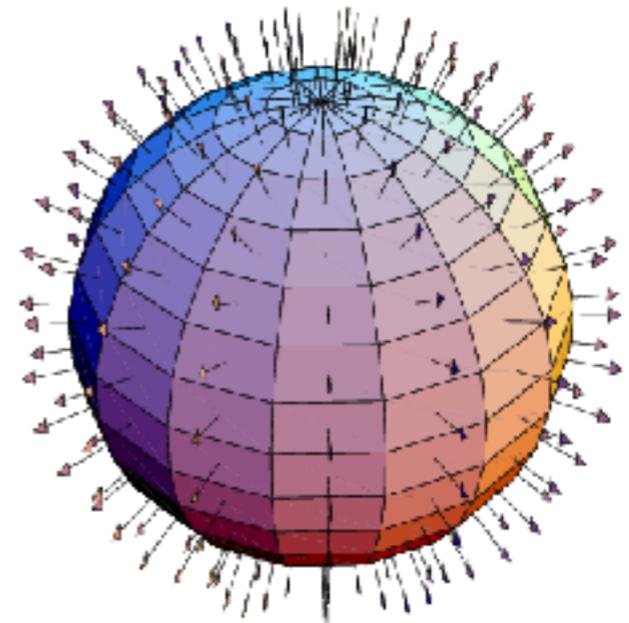
▶ Effective chiral action

$$S_{\text{eff}} = -N_c \text{Tr} \text{Ln}(i\gamma_\mu \partial^\mu + i\hat{m} + iMU\gamma^5)$$

$$\hat{m} = \text{diag}(m_u, m_d, m_s)$$

▶ Hedgehog Ansatz

$$U_c = e^{i\gamma_5 n^a \tau^a \pi(r)}$$



hedgehog

▶ Self-Consistent soliton solution

$$\left. \frac{\delta}{\delta U} [N_c E_{\text{val}} + E_{\text{sea}}] \right|_{U_c} = 0, \quad \underline{M_{\text{cl}} \approx 1300 \text{ MeV}}$$

## ▶ Zero-mode quantization

$$U(\mathbf{r}) = \begin{pmatrix} U_c(\mathbf{r}) & 0 \\ 0 & 1 \end{pmatrix}.$$

Witten's embedding

$$\vec{J} + \vec{T} = 0$$

$$U(\mathbf{r}, t) = A(t)U(\mathbf{r})A^\dagger(t),$$

Slowly rotating soliton

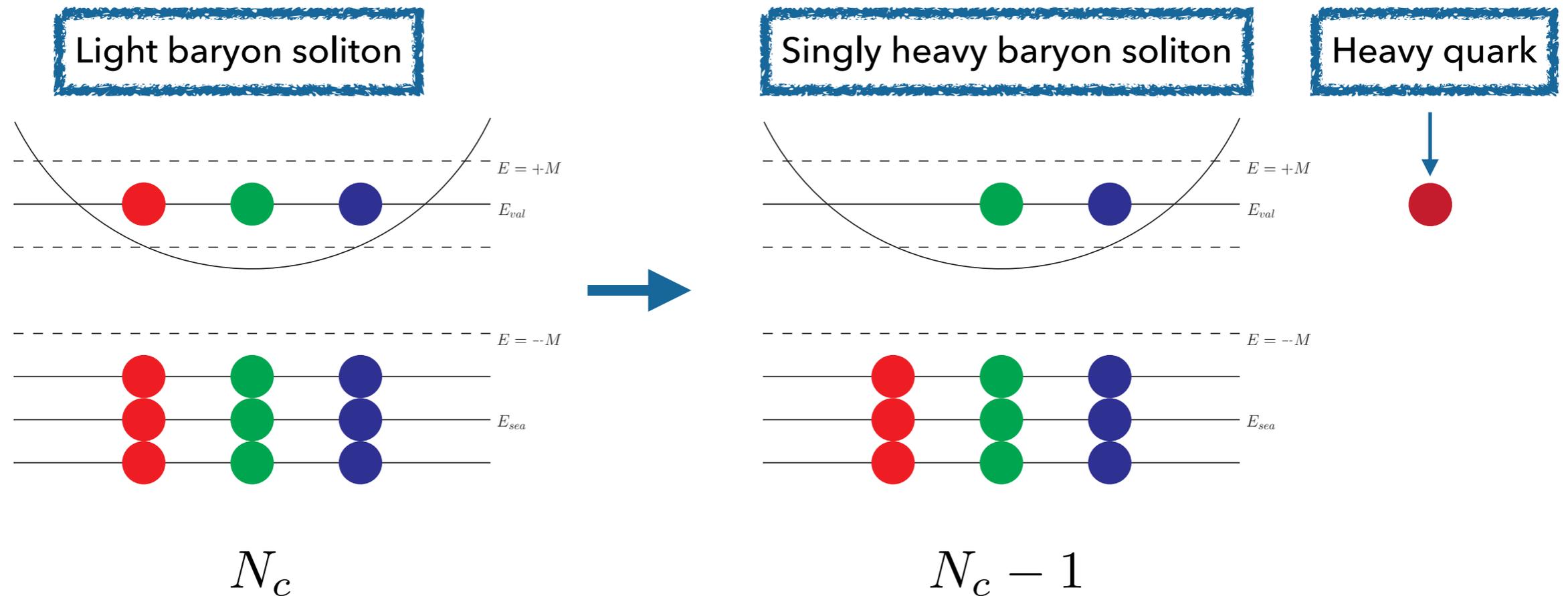
## ▶ Collective Hamiltonian

$$H = H_{\text{sym}} + H_{\text{sb}}^{(1)}$$

$$H_{\text{sym}} = M_{\text{cl}} + \frac{1}{2I_1} \sum_{i=1}^3 \hat{J}_i^2 + \frac{1}{2I_2} \sum_{a=4}^7 \hat{J}_a^2,$$

$$H_{\text{sb}}^{(1)} = \alpha D_{88}^{(8)} + \beta \hat{Y} + \frac{\gamma}{\sqrt{3}} \sum_{i=1}^3 D_{8i}^{(8)} \hat{J}_i,$$

# Change of the pion mean fields for Singly heavy baryon



- ▶ The soliton mass formula is changed **only for the valence part** in the singly heavy baryon sector.

$$M_{sol} = (N_c - 1)E_{val} + E_{sea} \approx 1100 \text{ MeV.}$$

## Change of the pion mean fields for Singly heavy baryon

- ▶ The moment of inertias and dynamical parameters are also changed

Light baryon	This work	Ref [14]	Singly heavy baryon	This work
$\tilde{I}_1$ [fm]	1.108	$1.230 \pm 0.002$	$I_1$ [fm]	0.844
$\tilde{I}_2$ [fm]	0.529	$0.420 \pm 0.006$	$I_2$ [fm]	0.404
$\tilde{K}_1$ [fm]	0.428	-	$K_1$ [fm]	0.286
$\tilde{K}_2$ [fm]	0.272	-	$K_2$ [fm]	0.181
$\tilde{N}_0$ [fm]	0.457	-	$N_0$ [fm]	0.499
$\tilde{N}_1$ [fm]	0.410	-	$N_1$ [fm]	0.380
$\tilde{N}_2$ [fm]	0.323	-	$N_2$ [fm]	0.286
$\tilde{\Sigma}_{\pi N}$ [MeV]	43.7	$36.4 \pm 3.9$	$\Sigma_{\pi N}$ [MeV]	40.0
$\tilde{\alpha}$ [MeV]	-392.0	$-262.9 \pm 5.9$	$\alpha$ [MeV]	-326.3
$\tilde{\beta}$ [MeV]	-99.3	$-144.3 \pm 3.2$	$\beta$ [MeV]	-77.8
$\tilde{\gamma}$ [MeV]	-49.4	$-104.2 \pm 2.4$	$\gamma$ [MeV]	-37.8
$\tilde{M}_{\text{sol}}$ [MeV]	1296.1	-	$M_{\text{sol}}$ [MeV]	1099.9

[14] Gh. S. Yang, H.-Ch. Kim, M. V. Polyakov and M. Praszalowicz, Phys. Rev. **D94**, 071502 (2016)

[32] T. Ledwig, A. Silva and H.-Ch. Kim, Phys. Rev. **D82**, 034022 (2010)

# ROTATIONAL ENERGY

$$\overline{M}_{\mathcal{R},Q} = M_{\text{cl}} + \frac{1}{2I_1} J(J+1) + \frac{1}{2I_2} [C_2(p, q) - J(J+1)] - \frac{3}{8I_2} \overline{Y}^2.$$

$$\begin{cases} M_{\text{cl}} = M_{\text{sol}} & \text{Light baryon} \\ M_{\text{cl}} = M_{\text{sol}} + m_Q & \text{Singly heavy baryon} \end{cases}$$

$$\begin{cases} \overline{Y} = N_c/3 & \text{Light baryon} \\ \overline{Y} = (N_c - 1)/3 & \text{Singly heavy baryon} \end{cases}$$

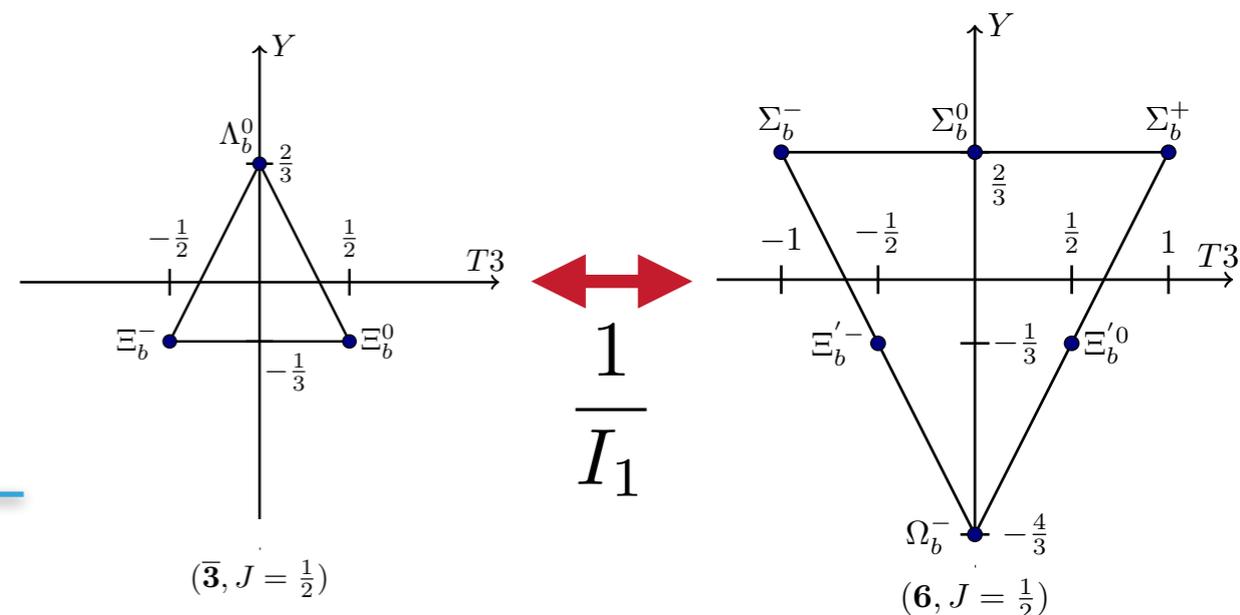
$$\psi_B^{(\mathcal{R})}(J' J'_3, J; A) = \sum_{m_3=-1/2}^{1/2} \sqrt{\dim(p, q)} (-1)^{-\overline{Y}/2 + J_3} C_{J_Q m_3 J - J_3}^{J' J'_3} \left[ \langle Y, T, T_3 | D^{(8)}(A) | \overline{Y}, J, -J_3 \rangle \right]^* \chi_{m_3},$$

- ▶ The rotational energy yields the energy difference between the  $\overline{\mathbf{3}}$  and the  $\mathbf{6}$ .

$\overline{\mathbf{3}} \rightarrow (p, q) = (0, 1) \rightarrow J = 0$  antitriplet

$\mathbf{6} \rightarrow (p, q) = (2, 0) \rightarrow J = 1$  sextet.

$$\overline{M}_{\mathbf{6},c} - \overline{M}_{\overline{\mathbf{3}},c} = \frac{1}{I_1}.$$



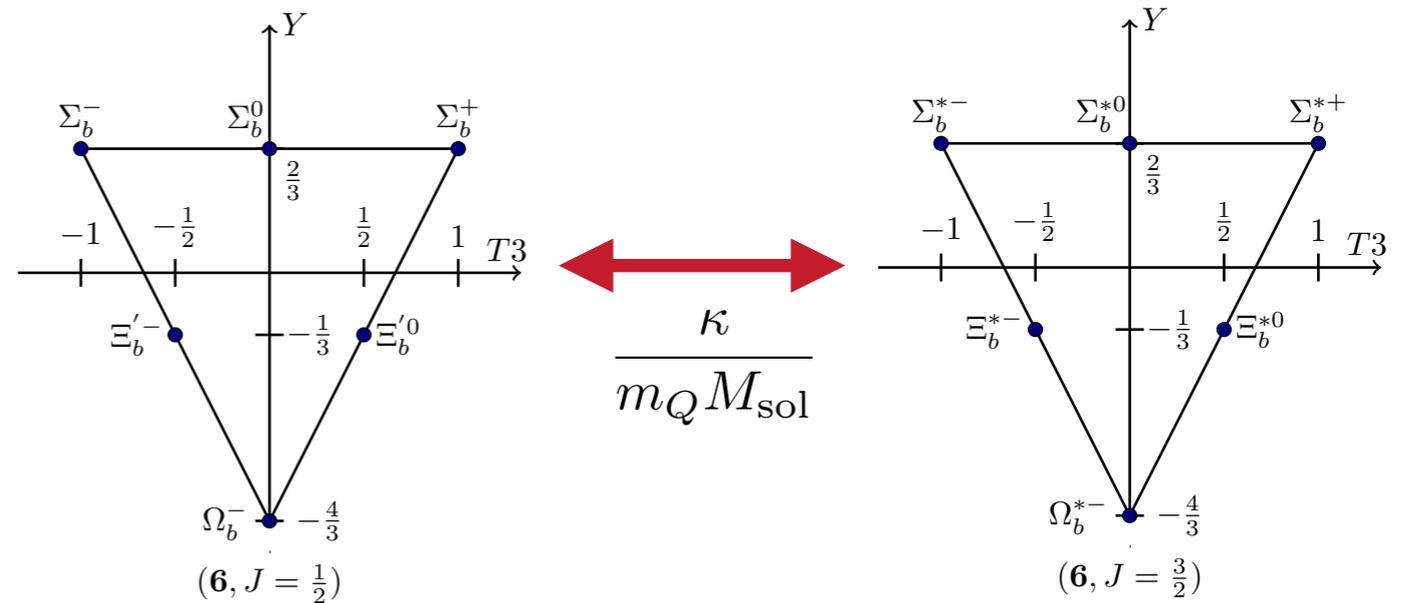
# HYPERFINE MASS SPLITTING

- ▶ We have to introduce the hyperfine interaction to lift the degeneracy in the sextet representations.

$$H_{\text{hf}} = \frac{2}{3} \frac{\kappa}{m_Q M_{\text{sol}}} \vec{J} \cdot \vec{J}_Q,$$

$$M_{\mathbf{6}_{1/2}, Q}^{(\text{hf})} = -\frac{2\kappa}{3m_Q M_{\text{sol}}},$$

$$M_{\mathbf{6}_{3/2}, Q}^{(\text{hf})} = \frac{\kappa}{3m_Q M_{\text{sol}}},$$



- ▶ The hyperfine mass splittings are determined by using center values of the sextet masses [1]

$$\frac{\kappa}{m_c M_{\text{sol}}} = (68.1 \pm 1.1) \text{ MeV}$$

$$\frac{\kappa}{m_b M_{\text{sol}}} = (20.3 \pm 1.0) \text{ MeV}$$

## SU(3) SYMMETRY BREAKING

$m_s$  is considered as a perturbation.

$$H_{\text{sb}}^{(1)} = +\alpha D_{88}^{(8)} + \beta \hat{Y} + \frac{\gamma}{\sqrt{3}} \sum_{i=1}^3 D_{8i}^{(8)} \hat{J}_i,$$

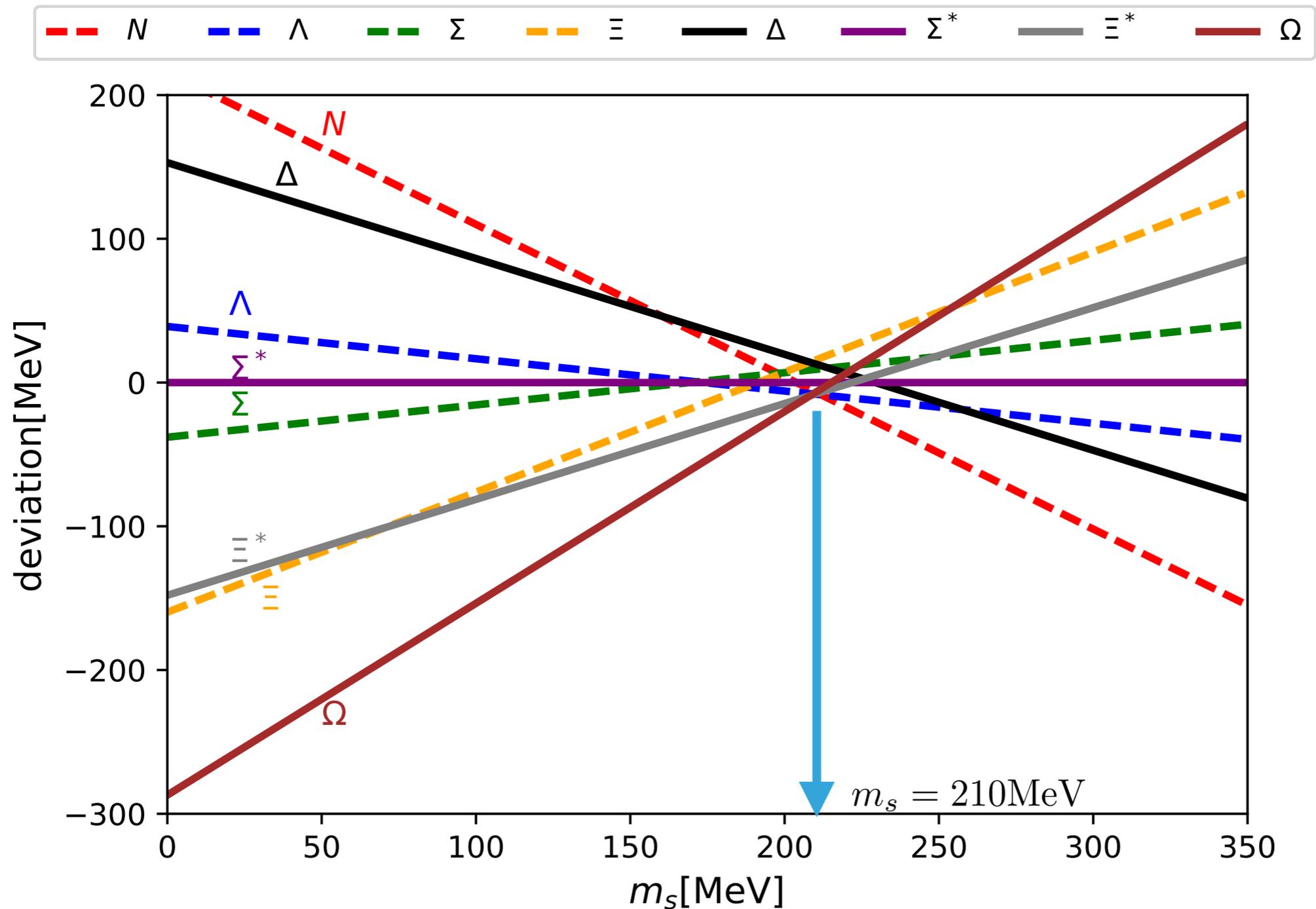
$$\alpha = \left( -\frac{\Sigma_{\pi N}}{3m_0} + \frac{K_2}{I_2} \bar{Y} \right) m_s, \quad \beta = -\frac{K_2}{I_2} m_s, \quad \gamma = 2 \left( \frac{K_1}{I_1} - \frac{K_2}{I_2} \right) m_s.$$

### ► Mass correction

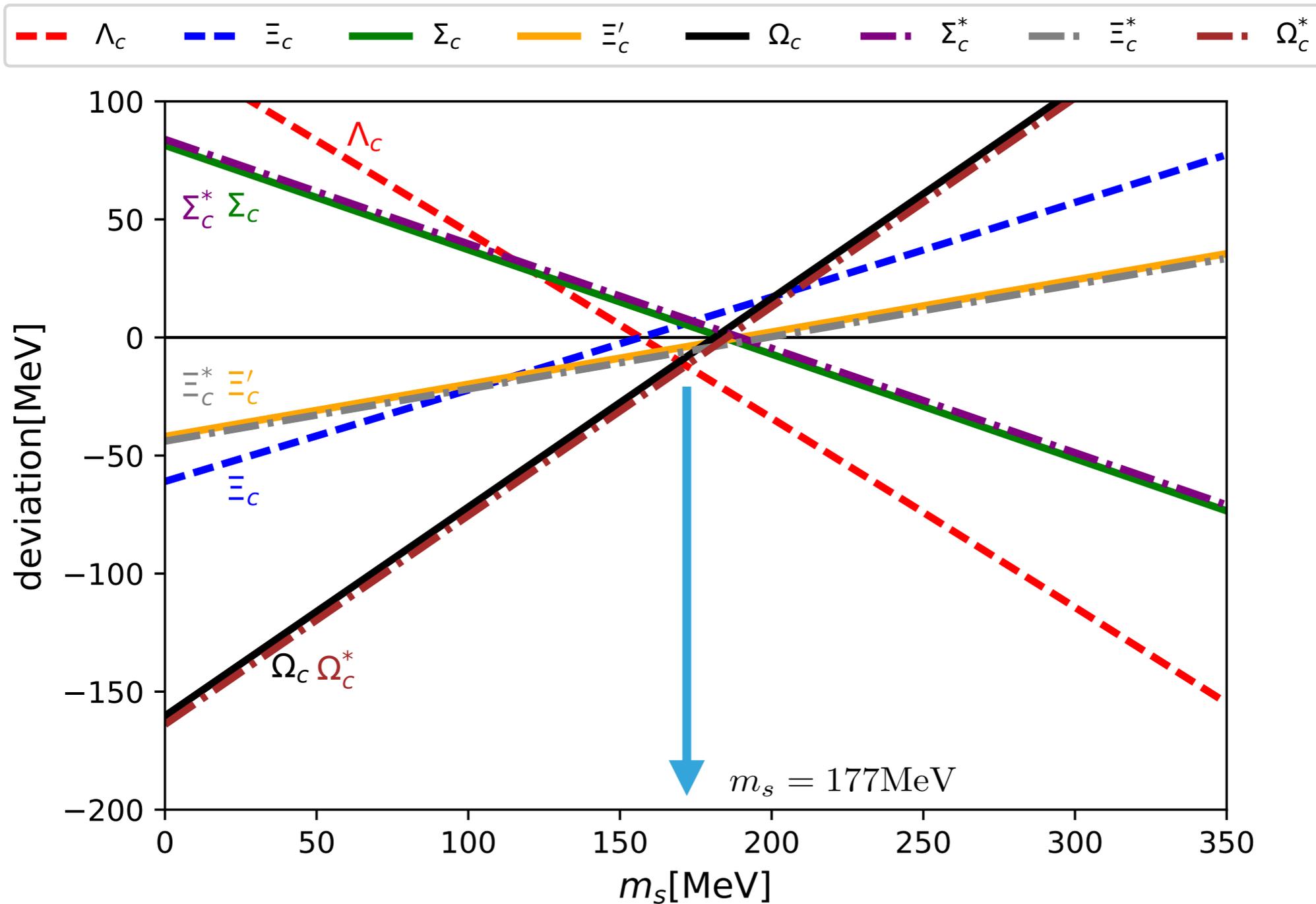
$$M_{B,\mathcal{R}}^{(1)} = \langle B, \mathcal{R} | H_{\text{sb}}^{(1)} | B, \mathcal{R} \rangle = Y \delta_{\mathcal{R}}$$

$$\delta_{\mathbf{3}} = \frac{3}{8} \alpha + \beta, \quad \delta_{\mathbf{6}} = \frac{3}{20} \alpha + \beta - \frac{3}{10} \gamma.$$

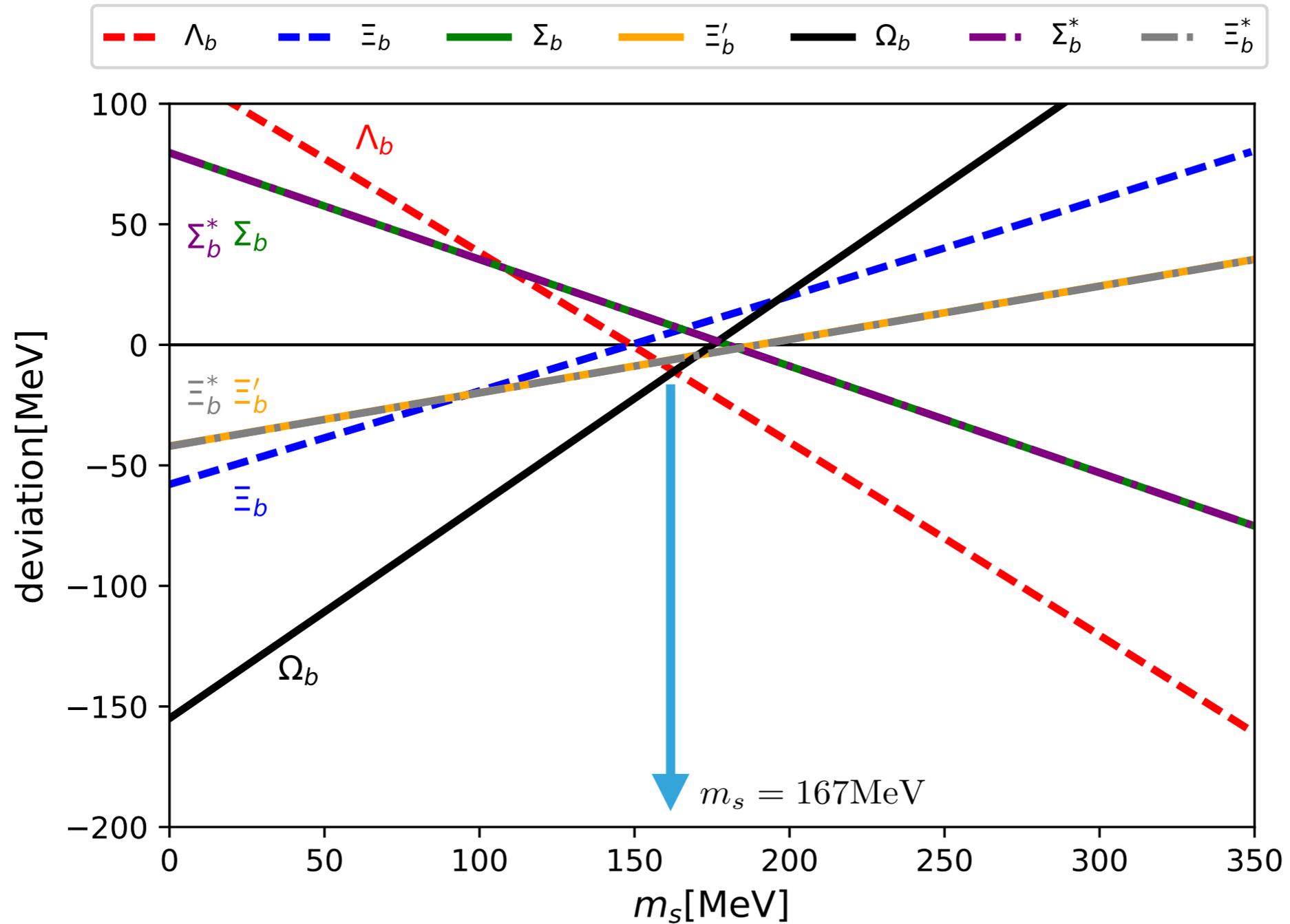
# LIGHT BARYON (1st order mass correction)



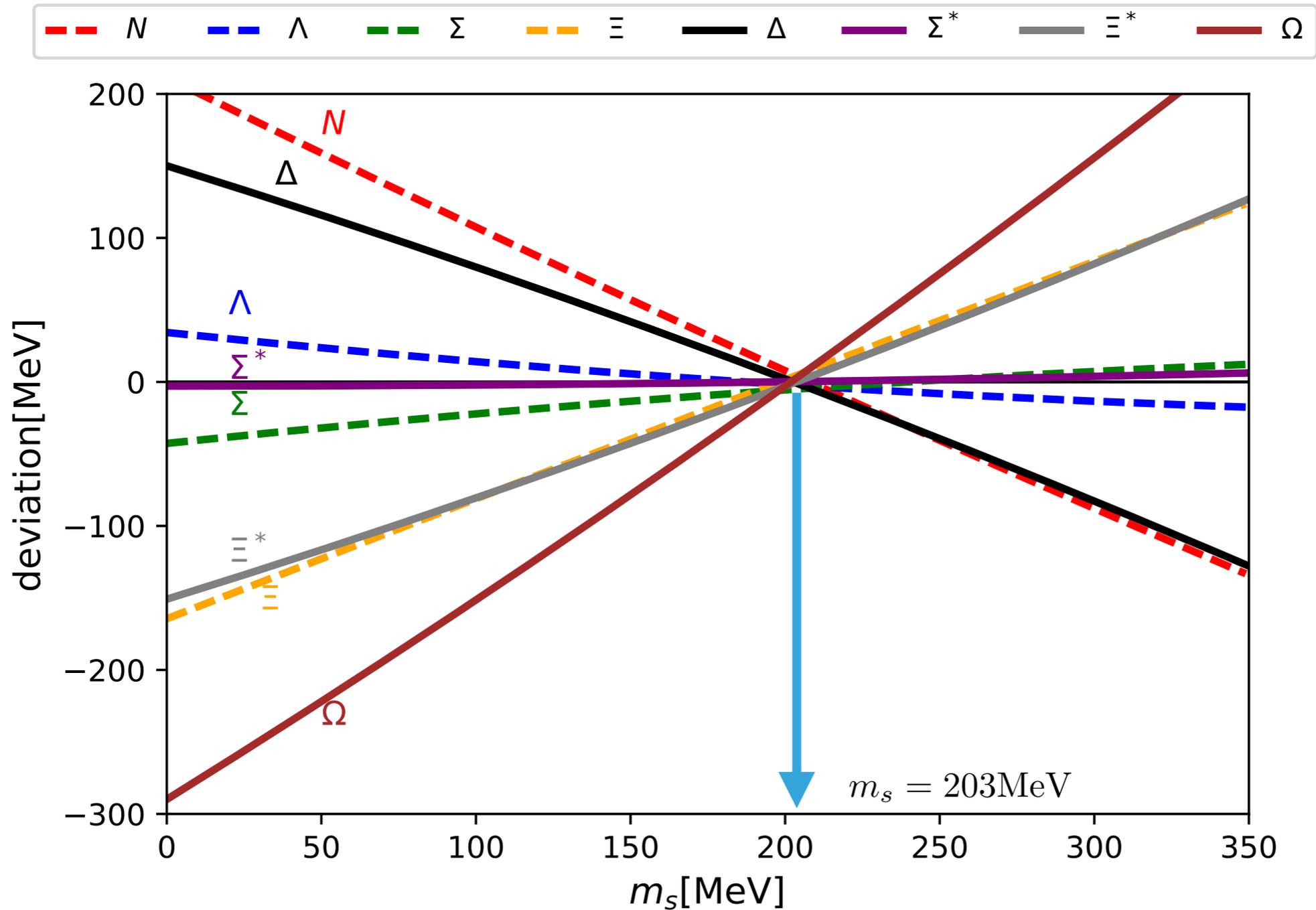
# CHARMED BARYON (1st order mass correction)



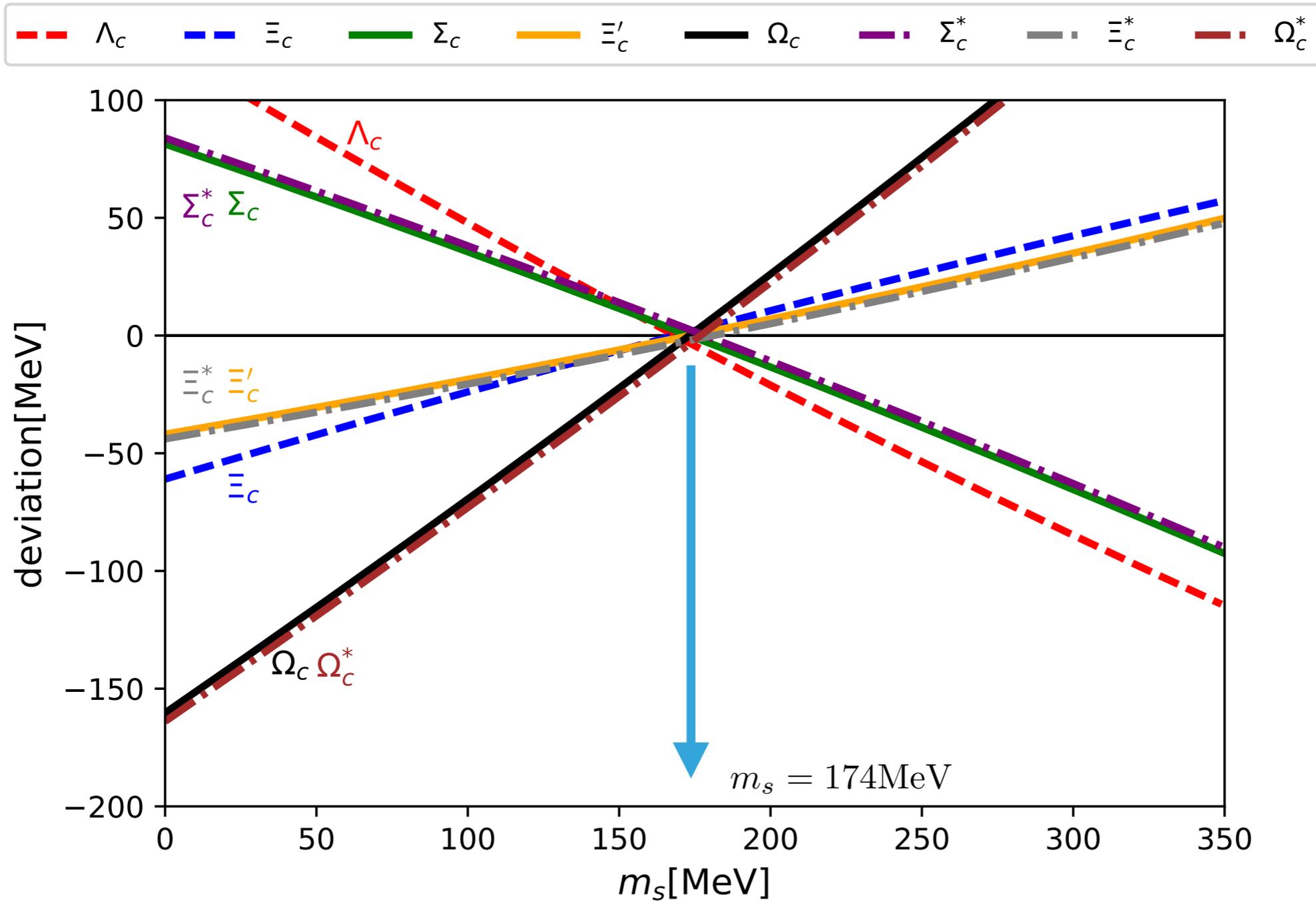
# BOTTOM BARYON (1st order mass correction)



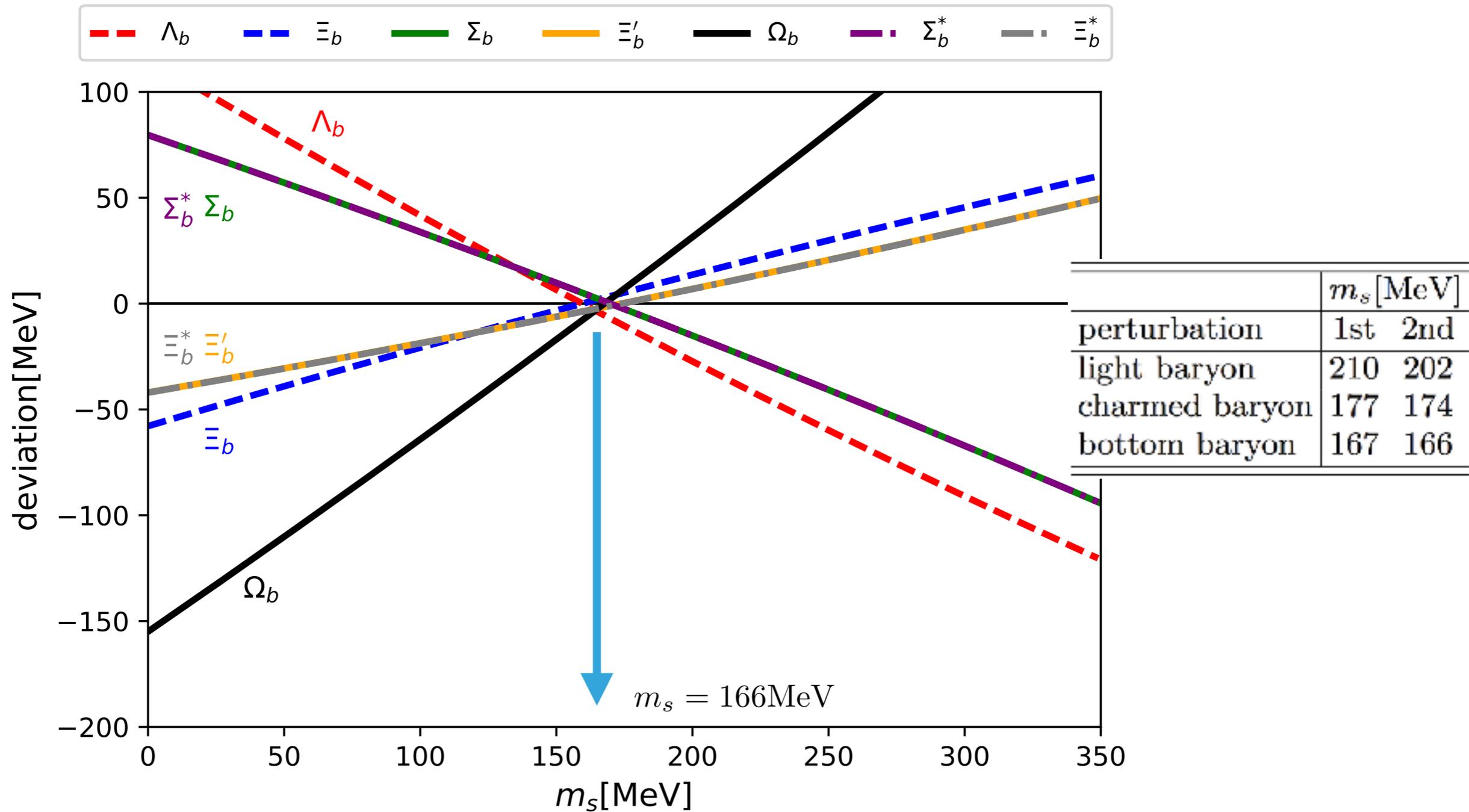
# LIGHT BARYON (2nd order mass correction)



# CHARMED BARYON (2nd order mass correction)



# BOTTOM BARYON (2nd order mass correction)



## CHARMED BARYON

- ▶ The heavy baryon masses are calculated by using the determined strange current quark mass.
- ▶ The soliton mass is overestimated. Thus, instead of using it, we employ the experimental center mass, so we predict the all masses of  $\bar{3}$  and 6.

	$m_s$ [MeV]	
	1st	2nd
perturbation	210	202
light baryon	210	202
charmed baryon	177	174
bottom baryon	167	166

$\mathcal{R}_j^Q$	$B_c$	Experiment [MeV]	ref[14] [MeV]	Perturbative	
				1st order	2nd order
$\bar{3}_{1/2}^c$	$\Lambda_c$	$2286.5 \pm 0.1$	$2272.5 \pm 2.3$	$m_s = 177$ [MeV]	$m_s = 174$ [MeV]
$\bar{3}_{1/2}^c$	$\Xi_c$	$2469.4 \pm 0.3$	$2476.3 \pm 1.2$	2476.3	2471.2
$6_{1/2}^c$	$\Sigma_c$	$2453.5 \pm 0.1$	$2445.3 \pm 2.5$	2456.1	2453.2
$6_{1/2}^c$	$\Xi'_c$	$2576.8 \pm 2.1$	$2580.5 \pm 1.6$	2573.6	2576.9
$6_{1/2}^c$	$\Omega_c$	$2695.2 \pm 1.7$	$2715.7 \pm 4.5$	2691.0	2695.9
$6_{3/2}^c$	$\Sigma_c^*$	$2518.1 \pm 0.8$	$2513.4 \pm 2.3$	2525.0	2520.3
$6_{3/2}^c$	$\Xi_c^*$	$2645.9 \pm 0.4$	$2648.6 \pm 1.3$	2642.4	2644.0
$6_{3/2}^c$	$\Omega_c^*$	$2765.9 \pm 2.0$	$2783.8 \pm 4.5$	2759.9	2763.1

**The results obtained are in good agreement with the experiment result !**

## BOTTOM BARYON

- Especially, the mass of  $\Omega_b^*$  is predicted in the chiral quark-soliton model.

	$m_s$ [MeV]	
perturbation	1st	2nd
light baryon	210	202
charmed baryon	177	174
bottom baryon	167	166

				Perturbative	
				1st order	2nd order
$\mathcal{R}_J^Q$	$B_c$	Experiment [MeV]	ref[14] [MeV]	$m_s = 167$ [MeV]	$m_s = 166$ [MeV]
$\bar{\mathbf{3}}_{1/2}^b$	$\Lambda_b$	$5619.5 \pm 0.2$	$5599.3 \pm 2.4$	5607.1	5615.1
$\bar{\mathbf{3}}_{1/2}^b$	$\Xi_b$	$5793.1 \pm 0.7$	$5803.1 \pm 1.2$	5799.3	5795.3
$\mathbf{6}_{1/2}^b$	$\Sigma_b$	$5813.4 \pm 1.3$	$5804.3 \pm 2.4$	5821.0	5815.3
$\mathbf{6}_{1/2}^b$	$\Xi'_b$	$5935.0 \pm 0.05$	$5939.5 \pm 1.5$	5931.8	5933.0
$\mathbf{6}_{1/2}^b$	$\Omega_b$	$6048.0 \pm 1.9$	$6074.7 \pm 4.5$	6042.6	6046.4
$\mathbf{6}_{3/2}^b$	$\Sigma_b^*$	$5833.6 \pm 1.3$	$5824.6 \pm 2.3$	5840.9	5835.5
$\mathbf{6}_{3/2}^b$	$\Xi_b^*$	$5955.3 \pm 0.1$	$5959.8 \pm 1.2$	5951.7	5953.2
$\mathbf{6}_{3/2}^b$	$\Omega_b^*$	-	$6095.0 \pm 4.4$	6062.5	6066.6

**Our prediction :  $M_{\Omega_b^*} = 6066.6$  MeV**

# HEAVY PENTAQUARK

D. Diakonov, arXiv:1003.2157 [hep-ph].

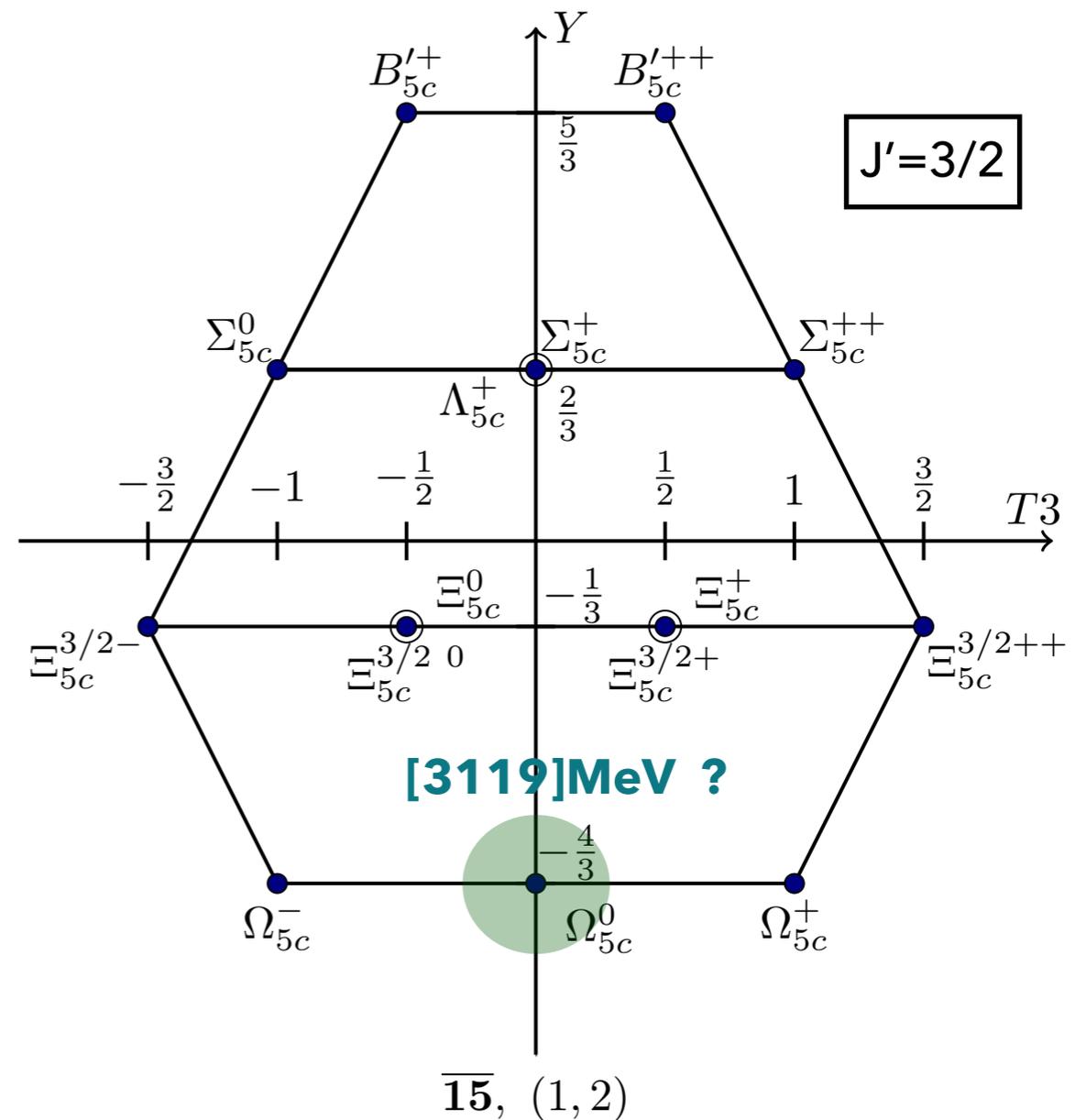
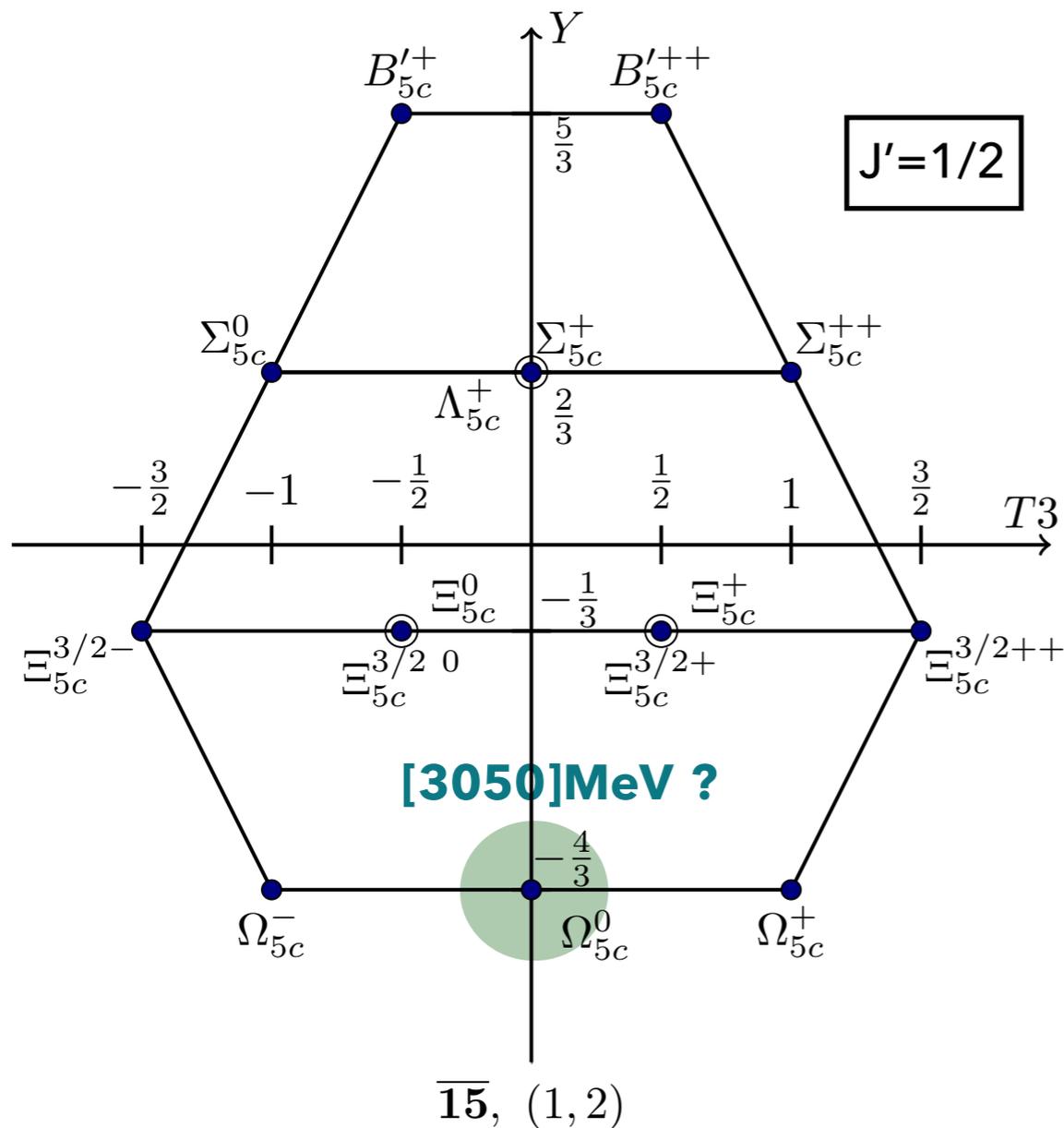
Resonance	Mass ( MeV)	$\Gamma$ ( MeV)	Yield	$N_\sigma$
$\Omega_c(3000)^0$	$3000.4 \pm 0.2 \pm 0.1^{+0.3}_{-0.5}$	$4.5 \pm 0.6 \pm 0.3$	$1300 \pm 100 \pm 80$	20.4
$\Omega_c(3050)^0$	$3050.2 \pm 0.1 \pm 0.1^{+0.3}_{-0.5}$	$0.8 \pm 0.2 \pm 0.1$	$970 \pm 60 \pm 20$	20.4
		$< 1.2 \text{ MeV, 95\% CL}$		
$\Omega_c(3066)^0$	$3065.6 \pm 0.1 \pm 0.3^{+0.3}_{-0.5}$	$3.5 \pm 0.4 \pm 0.2$	$1740 \pm 100 \pm 50$	23.9
$\Omega_c(3090)^0$	$3090.2 \pm 0.3 \pm 0.5^{+0.3}_{-0.5}$	$8.7 \pm 1.0 \pm 0.8$	$2000 \pm 140 \pm 130$	21.1
$\Omega_c(3119)^0$	$3119.1 \pm 0.3 \pm 0.9^{+0.3}_{-0.5}$	$1.1 \pm 0.8 \pm 0.4$	$480 \pm 70 \pm 30$	10.4
		$< 2.6 \text{ MeV, 95\% CL}$		
$\Omega_c(3188)^0$	$3188 \pm 5 \pm 13$	$60 \pm 15 \pm 11$	$1670 \pm 450 \pm 360$	
$\Omega_c(3066)_{fd}^0$			$700 \pm 40 \pm 140$	
$\Omega_c(3090)_{fd}^0$			$220 \pm 60 \pm 90$	
$\Omega_c(3119)_{fd}^0$			$190 \pm 70 \pm 20$	

# HEAVY PENTAQUARK

Prof. Hyun-Chul Kim - Possible existence of charmed exotics

The hyperfine mass splitting is determined in the charmed baryon sector.

$$\rightarrow \frac{\kappa}{m_c M_{\text{sol}}} = (68.1 \pm 1.1) \text{ MeV}$$



	Perturbative	
	1st order	2nd order
$m_s$	177	174
$M_{B_{5c}}$	2738.1	2751.7
$M_{\Sigma_{5c}}$	2827.9	2861.0
$M_{\Lambda_{5c}}$	2849.1	2859.9
$M_{\Xi_{5c}^{3/2}}$	2917.7	2923.3
$M_{\Xi_{5c}}$	2949.6	2964.3
$M_{\Omega_c}$	[Input]	
$M_{B_{5c}}$	2808.1	2820.7
$M_{\Sigma_{5c}}$	2897.9	2930.0
$M_{\Lambda_{5c}}$	2919.1	2928.9
$M_{\Xi_{5c}^{3/2}}$	2987.7	2992.3
$M_{\Xi_{5c}}$	3019.6	3033.7
$M_{\Omega_c}$	[Input]	

# DOUBLY CHARMED BARYON

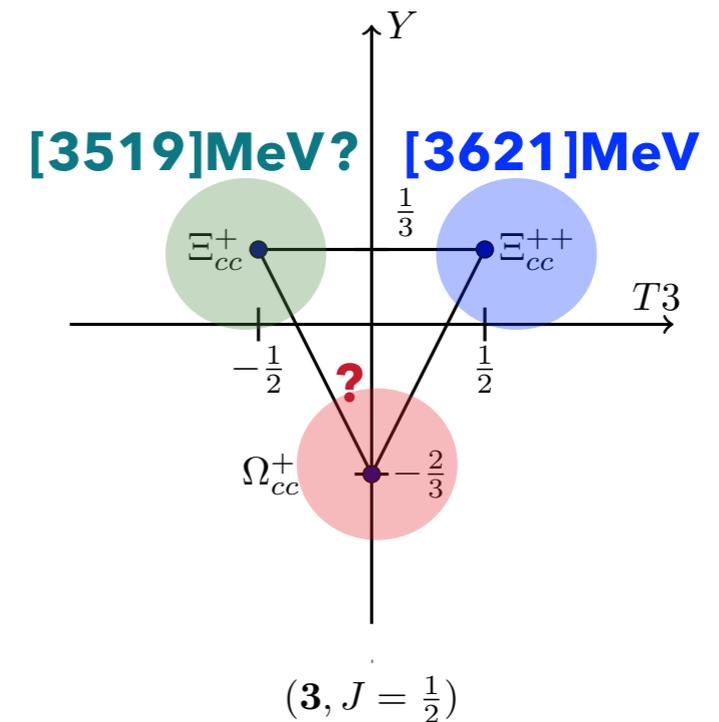
- ▶ The pion mean fields of the doubly heavy baryon is modified  $N_c$  to the  $N_c - 2$

$$M_{B_{Q_1 Q_2}}^{(1)} = Y \delta_{\mathcal{R}}.$$

$$\delta_{\mathbf{3}} = \frac{3}{16} \alpha' + \beta' - \frac{9}{32} \gamma'.$$

**Our prediction**

$$M_{\Omega_{cc}} = 3732.5 \text{ MeV}$$



Doubly heavy baryon	This work
$I'_1$ [fm]	0.579
$I'_2$ [fm]	0.280
$K'_1$ [fm]	0.143
$K'_2$ [fm]	0.090
$N'_0$ [fm]	0.540
$N'_1$ [fm]	0.348
$N'_2$ [fm]	0.248
$\Sigma'_{\pi N}$ [MeV]	36.3
$\alpha'$ [MeV]	-336.0
$\beta'$ [MeV]	-57.6
$\gamma'$ [MeV]	-26.1
$M'_{\text{sol}}$ [MeV]	903.7

- ▶ We investigated the mass splitting of the lowest-lying heavy baryons in a pion mean-field approach.
- ▶ We examined the dependence of the strange current quark mass on systems of heavy-quark baryons.
- ▶ We predicted the masses of particles  $\Omega_b^{*-}$  and  $\Omega_{cc}^+$  by using determined strange current quark masses and also the whole heavy pentaquark members.
- ▶ We also discussed the masses of the  $\Omega_c^0$  recently found by the LHCb Collaboration.
- ▶ Decay widths of the heavy baryons are under investigation in the chiral quark-soliton model.

**THANK YOU VERY MUCH!**