



北京航空航天大學
BEIHANG UNIVERSITY

Review on tetraquark states from experimental results

Chengping Shen

9th Workshop on Hadron physics in China and
Opportunities Worldwide

2017年7月26日



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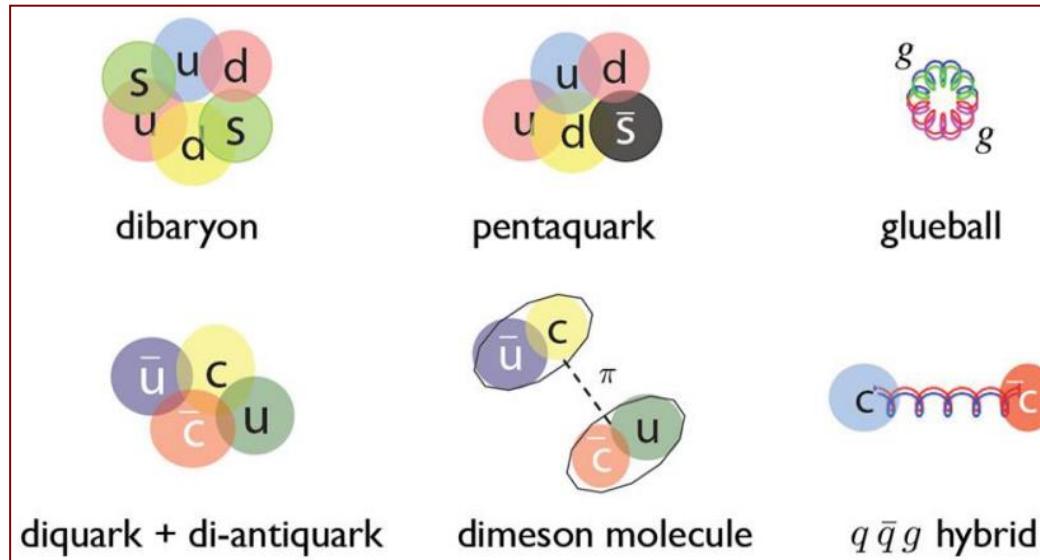


Outline

- Introduction
- Recent experimental results on X states
- Recent experimental results on Y states
- Recent experimental results on Z states
- The future plan
- Summary

Hadrons: normal & exotic

- Quark model: hadrons are composed from 2 (meson) quarks or 3 (baryon) quarks



- QCD does not forbid hadrons with $N_{\text{quarks}} \neq 2, 3$
 - Glueball : $N_{\text{quarks}} = 0$ (gg, ggg, ...)
 - Hybrid : $N_{\text{quarks}} = 2$ (or more) + excited gluon
 - Multiquark state : $N_{\text{quarks}} > 3$
 - Molecule : bound state of more than 2 hadrons
 - ...

Multiquark states have been discussed since the 1st page of the quark model

A SCHEMATIC MODEL OF BARYONS AND MESONS *

M. GELL-MANN

California Institute of Technology, Pasadena, California

Received 4 January 1964

M. Gell-Mann, Phys. Lett. 8, 214 (1964)

If we assume that the strong interactions of baryons and mesons are correctly described in terms of the broken "eightfold way" 1-3), we are tempted to look for some fundamental explanation of the situation. A highly promised approach is the purely dynamical "bootstrap" model for all the strongly interacting particles within which one may try to derive isotopic spin and strangeness conservation and broken eightfold symmetry from self-consistency alone 4). Of course, with only strong interactions, the orientation of the asymmetry in the unitary space cannot be specified; one hopes that in some way the selection of specific components of the F-spin by electromagnetism and the weak interactions determines the choice of isotopic spin and hypercharge directions.

Even if we consider the scattering amplitudes of strongly interacting particles on the mass shell only and treat the matrix elements of the weak, electromagnetic, and gravitational interactions by means

ber $n_t - n_{\bar{t}}$ would be zero for all known baryons and mesons. The most interesting example of such a model is one in which the triplet has spin $\frac{1}{2}$ and $z = -\frac{1}{3}$, so that the four particles d^- , s^- , u^0 and b^0 exhibit a parallel with the leptons.

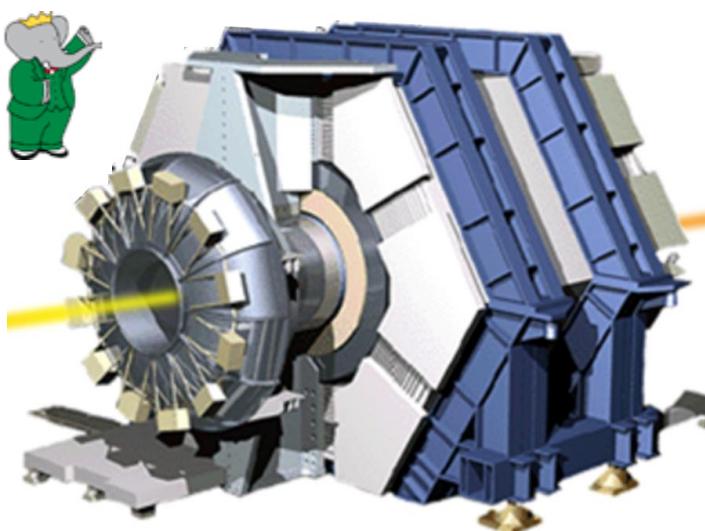
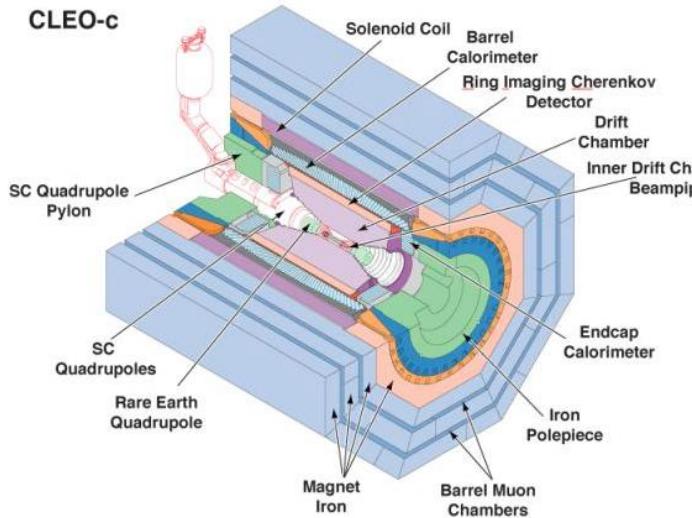
A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon b if we assign to the triplet t the following properties: spin $\frac{1}{2}$, $z = -\frac{1}{3}$, and baryon number $\frac{1}{3}$. We then refer to the members $u^{\frac{2}{3}}$, $d^{-\frac{1}{3}}$, and $s^{-\frac{1}{3}}$ of the triplet as "quarks" 6) q and the members of the anti-triplet as anti-quarks \bar{q} . Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqq\bar{q})$, etc., while mesons are made out of $(q\bar{q})$, $(q\bar{q}\bar{q}\bar{q})$, etc. It is assuming that the lowest baryon configuration (qqq) gives just the representations **1**, **8**, and **10** that have been observed, while the lowest meson configuration $(q\bar{q})$ similarly gives just **1** and **8**.



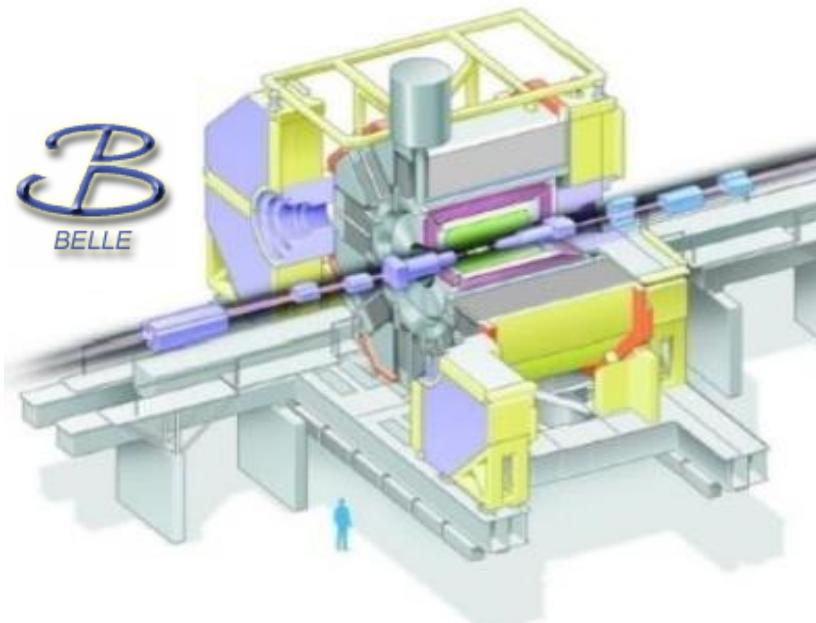
Where are they?

Main Suppliers of Exotics

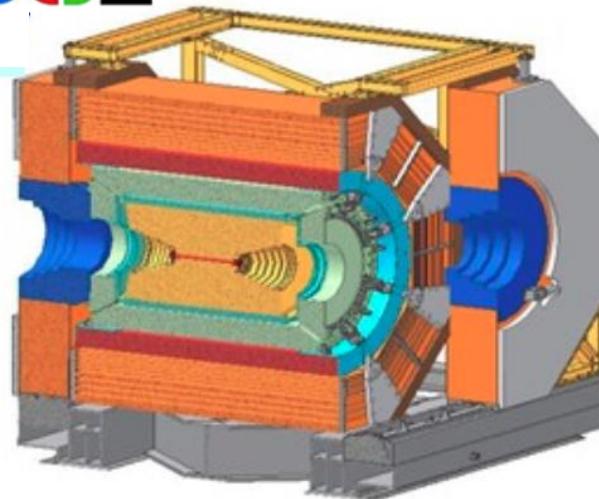
CLEO-c



B
BELLE



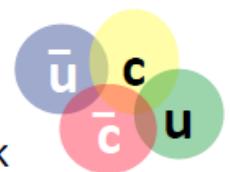
BES III



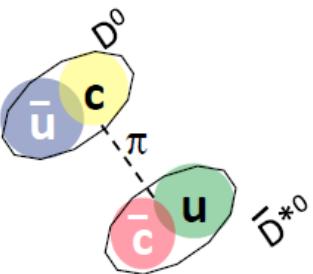
State	M , MeV	Γ , MeV	J^{PC}	Process (mode)	Experiment (# σ)	Year	Status	
Y(3915)	3918.4 ± 1.9	20 ± 5	$0/2^{?+}$	$B \rightarrow K(\omega J/\psi)$	Belle [753] (8), BaBar [? ?] (19)	2004	Ok	
				$e^+e^- \rightarrow e^+e^-(\omega J/\psi)$	Belle [754] (7.7), BaBar [755] (7.6)	2009	Ok	
					756] (5.3), BaBar [757] (5.8)	2005	Ok	
					Belle [758?] (6)	2005	NC!	
					PDG [61]	1978	Ok	
Y(4140)	$4146.5^{+6.4}_{-5.3}$	83^{+30}_{-25}	1^{++}	$B^+ \rightarrow K^+(\phi J/\psi)$	I [?] (>10), Belle [?] (6.0)	2012	NC!	
					: [?] (5.0), BaBar [?] (1.1)	2008	NC!	
					CDF [759, 760] (5.0), Belle [761] (1.9)	2009	Ok	
ψ(4160)	4153 ± 3	103 ± 8	1^{--}	$e^+e^- \rightarrow (\text{hadrons})$	LHCb [762] (1.4), CMS [763] (>5)			
				$e^+e^- \rightarrow (\eta J/\psi)$	D0 [764] (3.1), BaBar [765] (1.6)			
					LHCb [766, 767] (8.4)			
X(4160)	4156^{+29}_{-25}	139^{+113}_{-65}	$?^{?+}$	$e^+e^- \rightarrow J/\psi(D^*\bar{D}^*)$	PDG [61]	1978	Ok	
					Belle [?] (6.5), BESIII [?] (>5)	2013	NC!	
					Belle [?] (5.5)	2007	NC!	
Z(4200) ⁺	4196^{+35}_{-32}	370^{+99}_{-149}	1^{+-}	$\bar{B}^0 \rightarrow K^-(\pi^+ J/\psi)$	Belle [?] (6.2)	2014	NC!	
Z(4250) ⁺	4248^{+185}_{-45}	177^{+321}_{-72}	$?^{?+}$	$\bar{B}^0 \rightarrow K^-(\pi^+ \chi_{c1})$	Belle [?] (5.0), BaBar [?] (2.0)	2008	NC!	
Y(4260)	4221.1 ± 2.5	47.7 ± 4.0	1^{--}	$e^+e^- \rightarrow (\pi^+\pi^- J/\psi)$	BaBar [768, 769] (8), CLEO [770?] (11)	2005	Ok	
				$e^+e^- \rightarrow (\pi^0\pi^0 J/\psi)$	Belle [741, 771] (15), BESIII [740?] (np)			
				$e^+e^- \rightarrow (K^+K^- J/\psi)$	CLEO [?] (5.1), BESIII [?] (np)	2006	Ok	
				$e^+e^- \rightarrow (f_0(980) J/\psi)$	CLEO [?] (3.7)	2006	NC!	
				$e^+e^- \rightarrow (\pi^+\pi^- h_c)$	BaBar [769] (np), Belle [741] (np)	2012	Ok	
				$e^+e^- \rightarrow (\pi^0\pi^0 h_c)$	BESIII [742, 772] (10)	2013	NC!	
				$e^+e^- \rightarrow (\omega \chi_{c0})$	BESIII [744] (np)	2014	NC!	
				$e^+e^- \rightarrow (\gamma X(3872))$	BESIII [773] (>9)	2014	NC!	
				$e^+e^- \rightarrow (\pi^- Z_c(3900)^+)$	BESIII [740?] (>8), Belle [741] (5.2)	2013	Ok	
				$e^+e^- \rightarrow (\pi^0 Z_c(3900)^0)$	BESIII [? ?] (10.4)	2015	Ok	
Y(4274)	$4273.3^{+19.1}_{-9.0}$	$56.2^{+13.8}_{-15.6}$	1^{++}	$e^+e^- \rightarrow (\pi^\mp\pi^0 Z_c(4020)^{\pm,0})$	$B^+ \rightarrow K^+(\phi J/\psi)$	CDF [760] (3.1), LHCb [762] (1.0), CMS [763] (>3), D0 [764] (np)	2011	NC!
						LHCb [766, 767] (6.0)		
X(4350)	$4350.6^{+4.6}_{-5.1}$	13^{+18}_{-10}	$0/2^{?+}$	$e^+e^- \rightarrow e^+e^-(\phi J/\psi)$	Belle [775] (3.2)	2009	NC!	
Y(4360)	4341.2 ± 5.4	101.9 ± 9.3	1^{--}	$e^+e^- \rightarrow (\pi^+\pi^-\psi(2S))$	Belle [746, 776] (8), BaBar [777] (np)	2007	Ok	
				$e^+e^- \rightarrow (\pi^+\pi^- J/\psi)$	BESIII [?] (7.6)	2016	NC!	
				$e^+e^- \rightarrow (\pi^+\pi^-\psi_2(3823))$	BESIII [778] (np)	2015	NC!	
				$e^+e^- \rightarrow (\pi^0 Z_c(3900)^0)$	BESIII [?] (np)	2015	NC!	
				$e^+e^- \rightarrow (\pi^- Z_c(4055)^+)$	Belle [746] (3.5)	2014	NC!	
Y(4390)	4391.6 ± 6.4	139.5 ± 16.1	1^{--}	$e^+e^- \rightarrow (\pi^+\pi^- h_c)$	BESIII [772] (10)	2016	NC!	
				$e^+e^- \rightarrow (\pi^\mp\pi^0 Z_c(4020)^{\pm,0})$	BESIII [742, 744] (np)	2013	NC!	
ψ(4415)	4421 ± 4	62 ± 20	1^{--}	$e^+e^- \rightarrow (\text{hadrons})$	PDG [61]	1976	Ok	
				$e^+e^- \rightarrow (\eta J/\psi)$	Belle [?] (np), BESIII [?] (>5)	2013	NC!	
				$e^+e^- \rightarrow (\omega \chi_{c2})$	BESIII [?] (10.4)	2015	NC!	
				$e^+e^- \rightarrow (D\bar{D}_2^*(2460))$	Belle [?] (10)	2007	NC!	
Z(4430) ⁺	4478^{+15}_{-18}	181 ± 31	1^{+-}	$\bar{B}^0 \rightarrow K^-(\pi^+\psi(2S))$	Belle [779? , 780] (6.4), BaBar [?] (2.4), LHCb [781?] (13.9)	2007	Ok	
				$\bar{B}^0 \rightarrow K^-(\pi^+ J/\psi)$	Belle [?] (4.0)	2014	NC!	
Y(4500)	4506^{+16}_{-19}	92^{+30}_{-29}	0^{++}	$B^+ \rightarrow K^+(\phi J/\psi)$	LHCb [766, 767] (6.1)	2016	NC!	
Y(4660)	4643 ± 9	72 ± 11	1^{--}	$e^+e^- \rightarrow (\pi^+\pi^-\psi(2S))$	Belle [746, 776] (5.8), BaBar [777] (5)	2007	Ok	
				$e^+e^- \rightarrow (A_c^+ \bar{A}_c^-)$	Belle [782] (8.2)	2007	NC!	
Y(4700)	4704^{+17}_{-26}	120^{+52}_{-45}	0^{++}	$B^+ \rightarrow K^+(\phi J/\psi)$	LHCb [766, 767] (5.6)	2016	NC!	

Possible non $q\bar{q}$ “white” combinations of quarks:

Tetraquark mesons



tightly bound
diquark-dantiquark



loosely bound
meson-antimeson
“molecule”



Particle “Zoo” again !

XYZ particles

- Charmonium-like (XYZ) particles
- New type of hadron (multi-quark ...)?
- Too many vector states! Exotics?

X(3823) GeV

X(3872)

X(3915)

X(4350)

Y(4008)

Y(4260)

Y(4140)

Y(4360)

Y(4660)

Y(4630)

... XYZ(3940)

Z_c(3900)

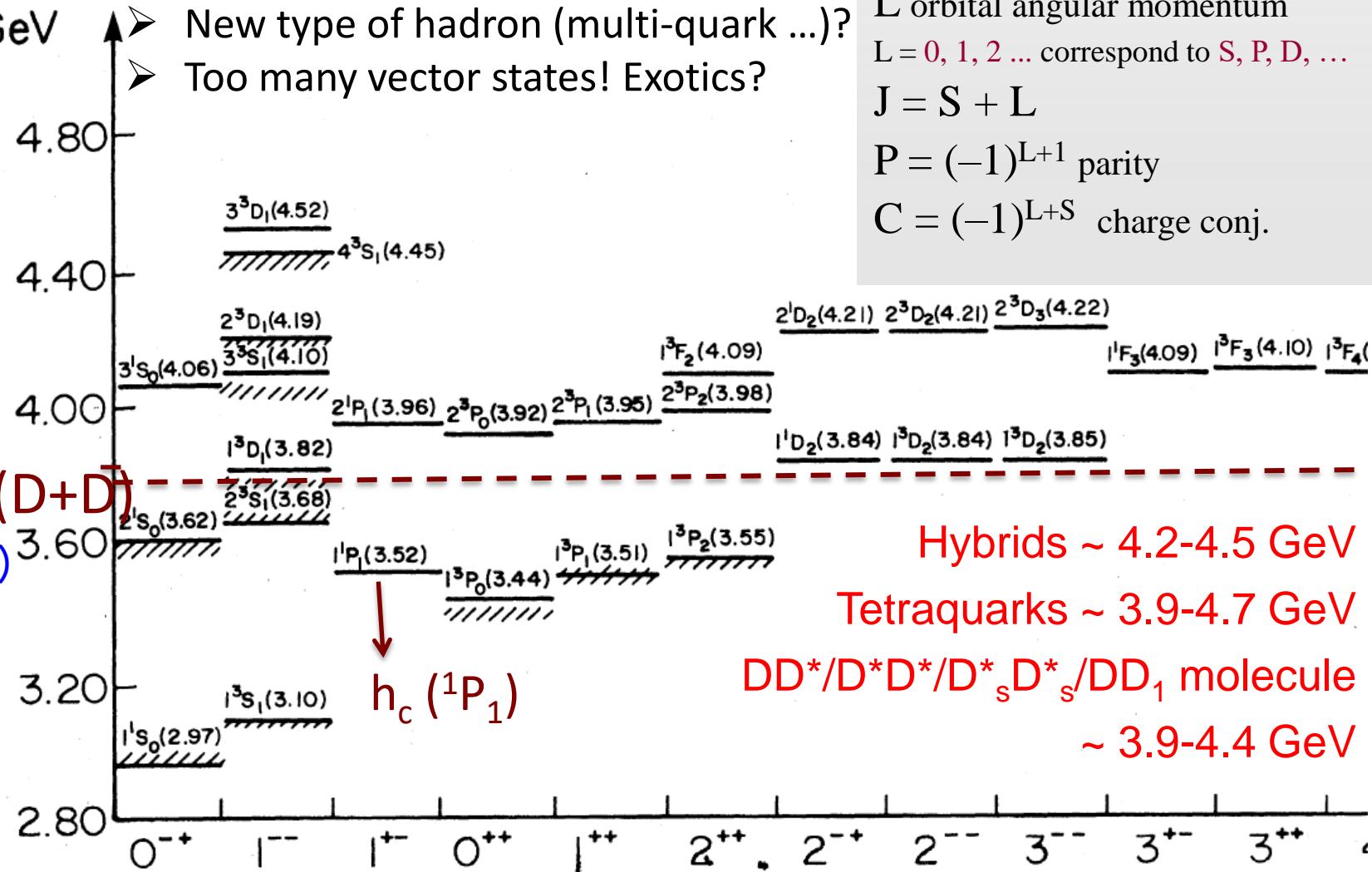
Z_c(4020)

Z(4430)

Z(4250)

Z(4050)

...



n radial quantum number

S total spin of c & cbar

L orbital angular momentum

L = 0, 1, 2 ... correspond to S, P, D, ...

J = S + L

P = $(-1)^{L+1}$ parityC = $(-1)^{L+S}$ charge conj.

Hybrids ~ 4.2-4.5 GeV

Tetraquarks ~ 3.9-4.7 GeV

DD*/D*D*/D*sD*/DD₁ molecule
~ 3.9-4.4 GeV

Too many models !

- Theory 1: screened potential
- Theory 2: hybrids with excited gluons
- Theory 3: tetraquark states
- Theory 4: meson molecules
- Theory 5: cusps effect
- Theory 6: final state interaction
- Theory 7: coupled-channel effect
- Theory 8: mixing of normal quarkonium and exotics
- Theory 9: mixture of all these effects
- Theories ...

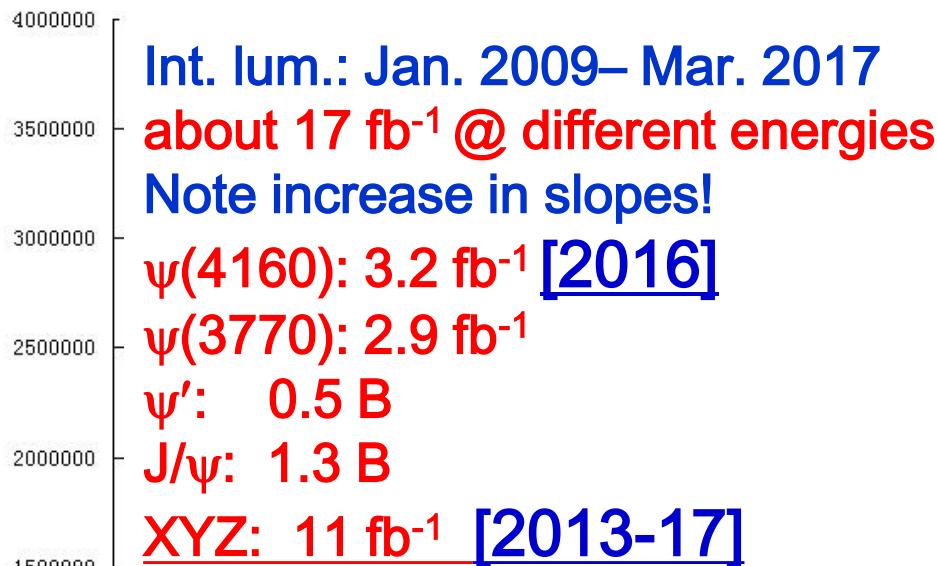
QCD is another least understood part of the SM.

“The absence of exotics is one of the most obvious features of QCD” – R. L. Jaffe, 2005

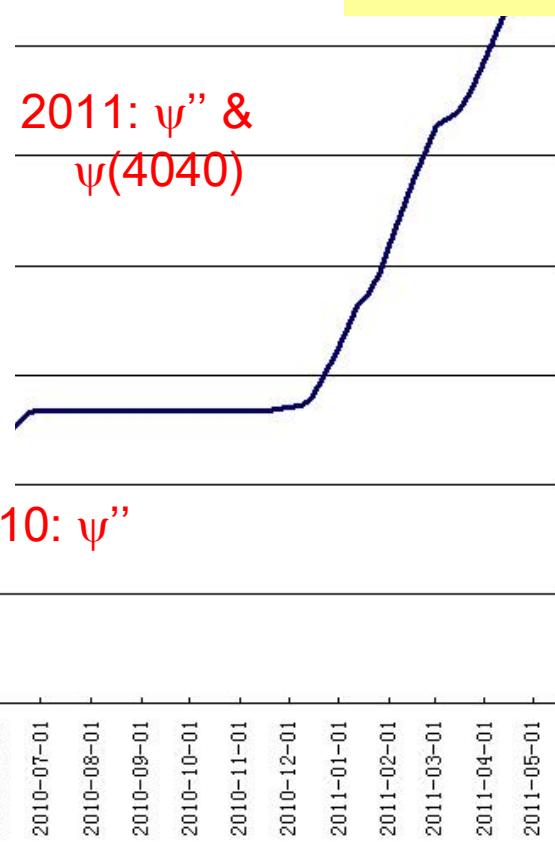
“The story of pentaquark shows how poorly we understand QCD” – F. Wilczek, 2005

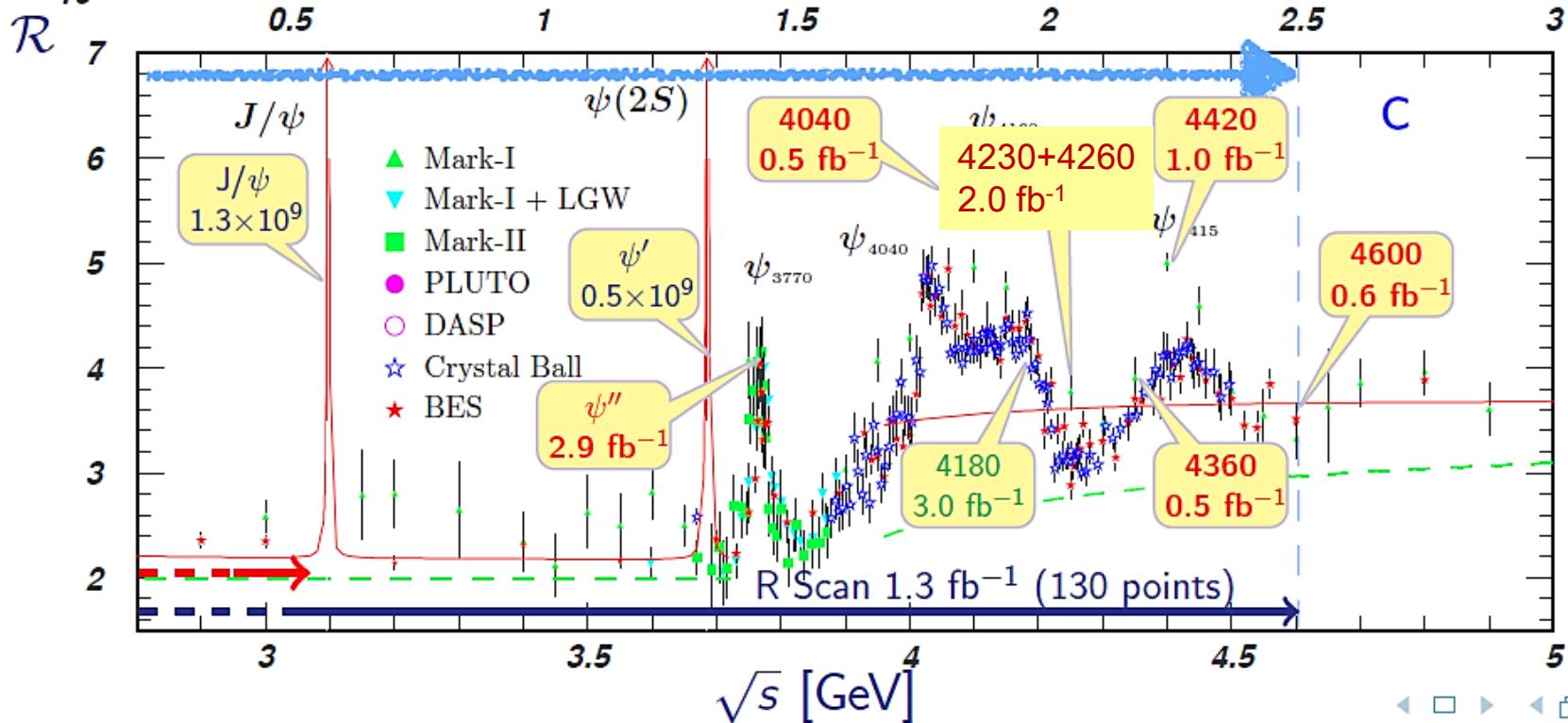
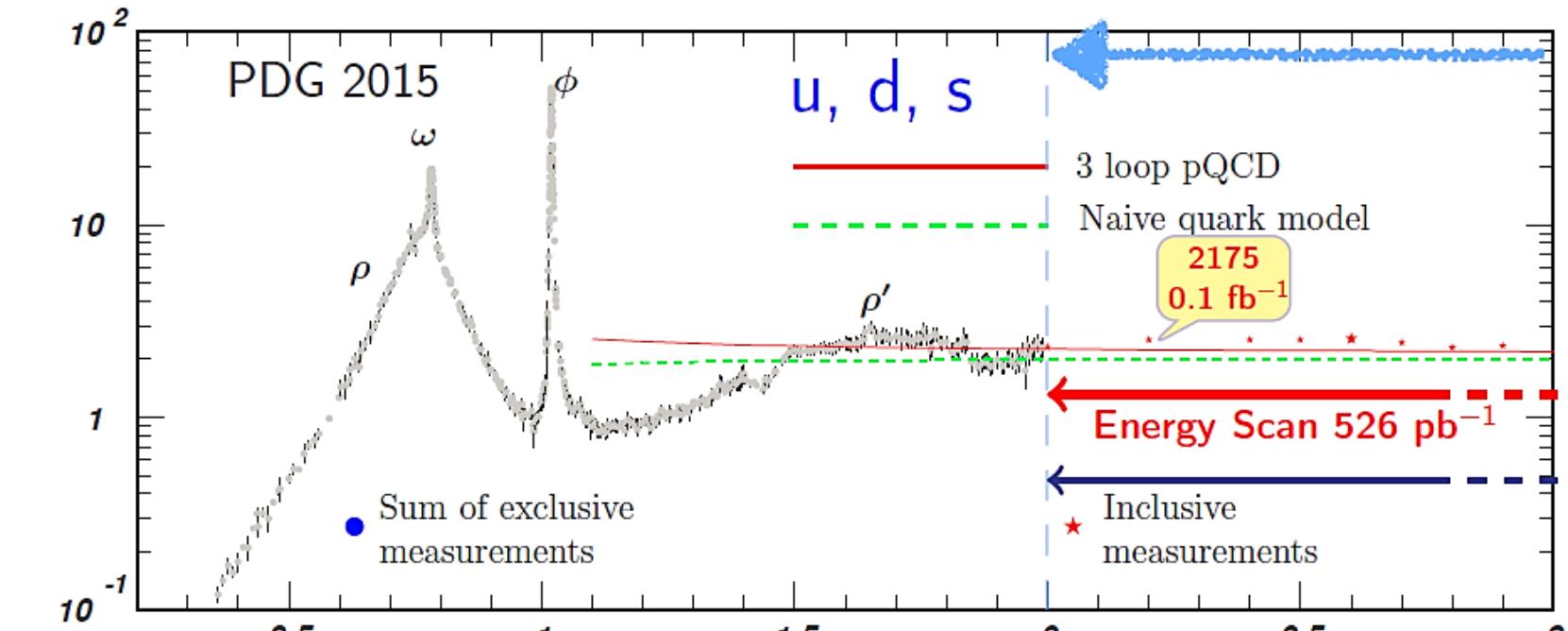
BESIII data samples

Note that luminosity is lower at J/ψ ,
and machine is optimal near ψ'' peak

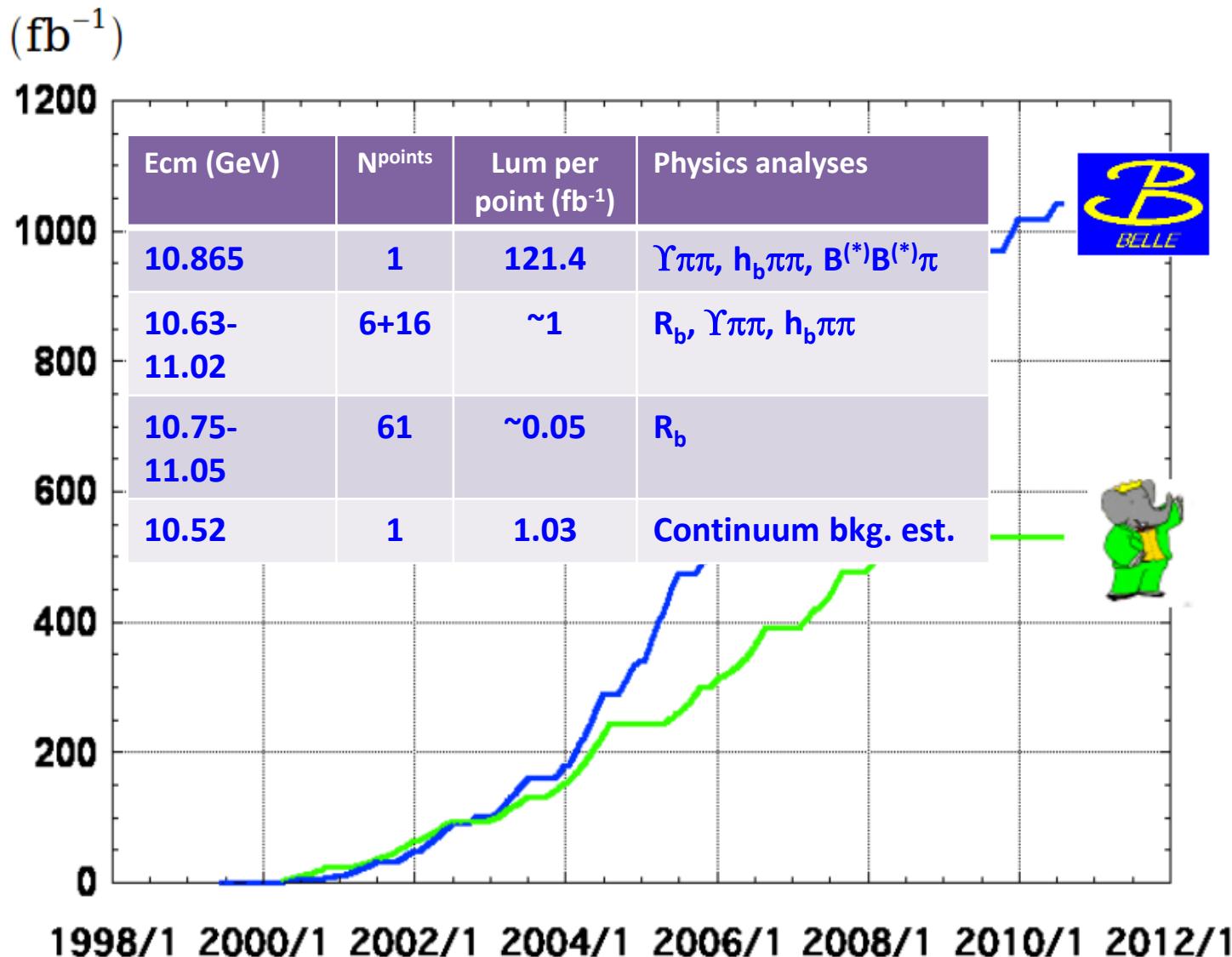


2012:
 ψ' & J/ψ
[0.35B & 1.1B]





Integrated luminosity of B factories



> 1 ab^{-1}

On resonance:

$\Upsilon(5S): 121 \text{ fb}^{-1}$

$\Upsilon(4S): 711 \text{ fb}^{-1}$

$\Upsilon(3S): 3 \text{ fb}^{-1}$

$\Upsilon(2S): 25 \text{ fb}^{-1}$

$\Upsilon(1S): 6 \text{ fb}^{-1}$

Off reson./scan:

~ 100 fb^{-1}

~ 550 fb^{-1}

On resonance:

$\Upsilon(4S): 433 \text{ fb}^{-1}$

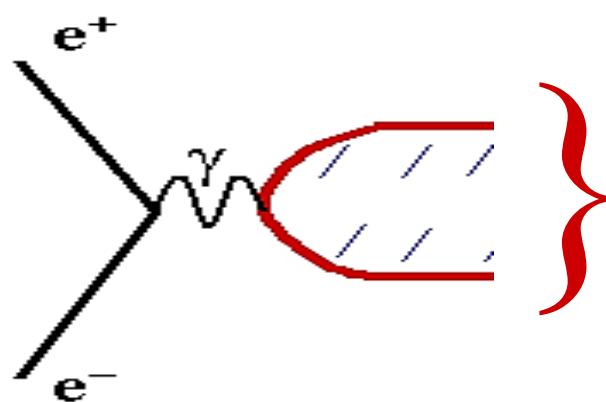
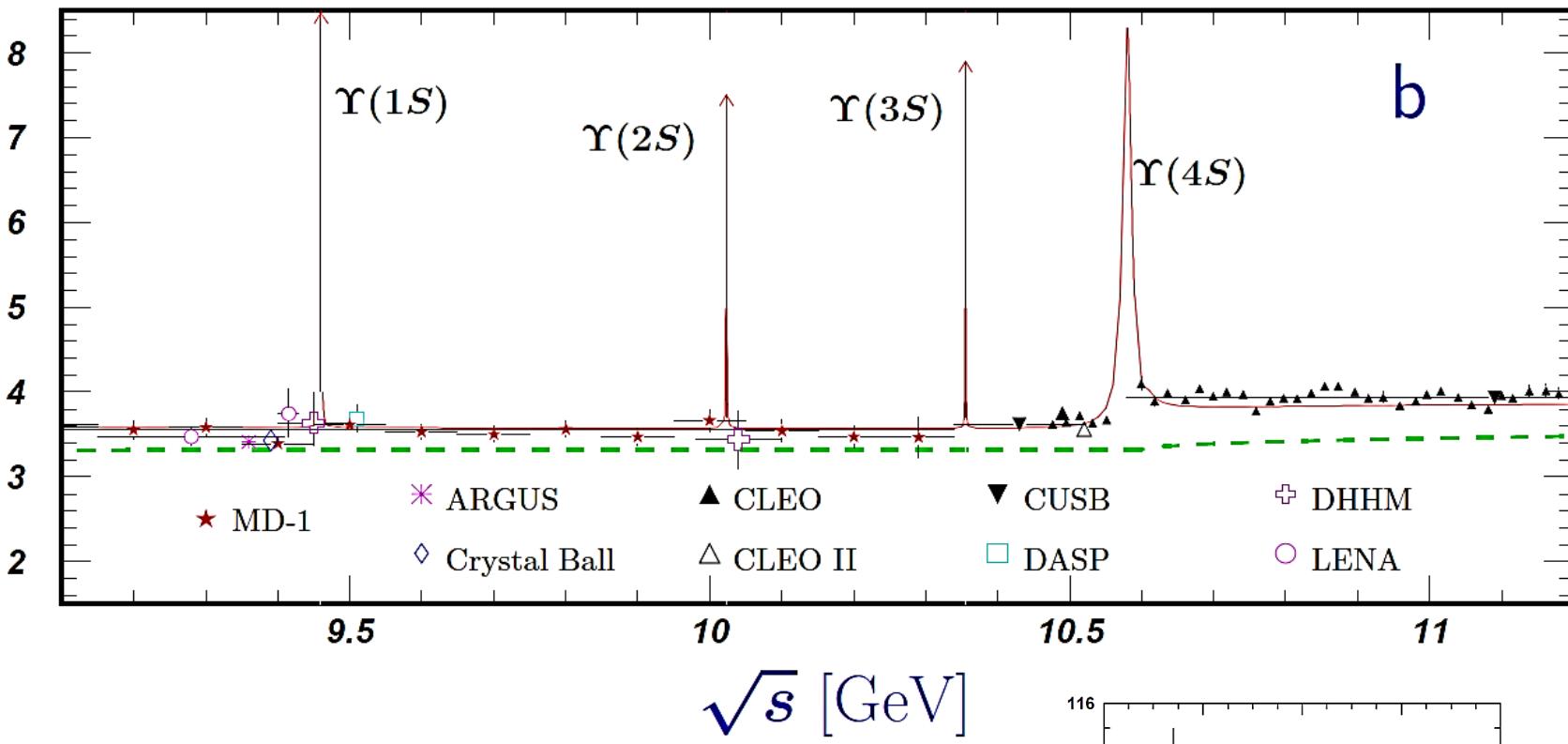
$\Upsilon(3S): 30 \text{ fb}^{-1}$

$\Upsilon(2S): 14 \text{ fb}^{-1}$

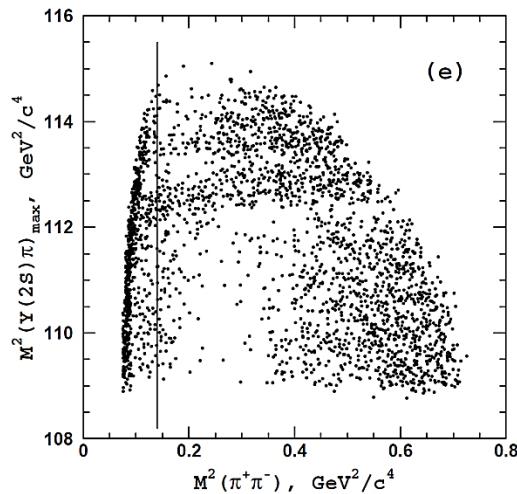
Off resonance:

~ 54 fb^{-1}

e^+e^- annihilation to vector bottomonia

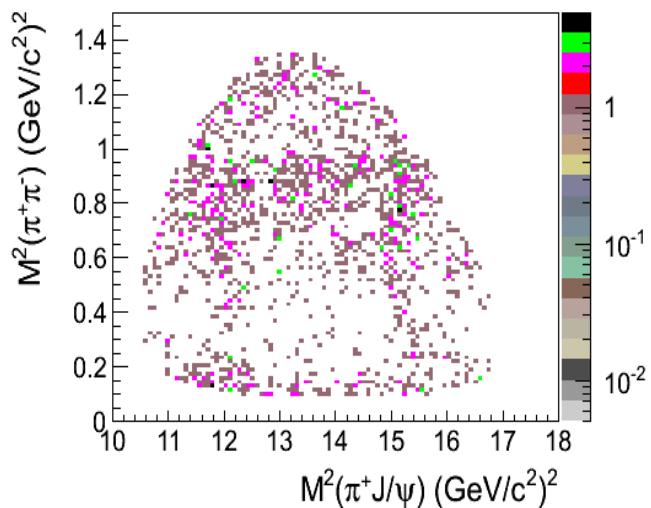
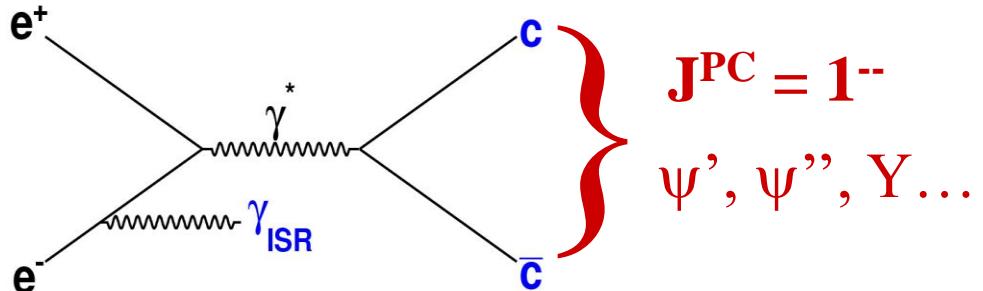
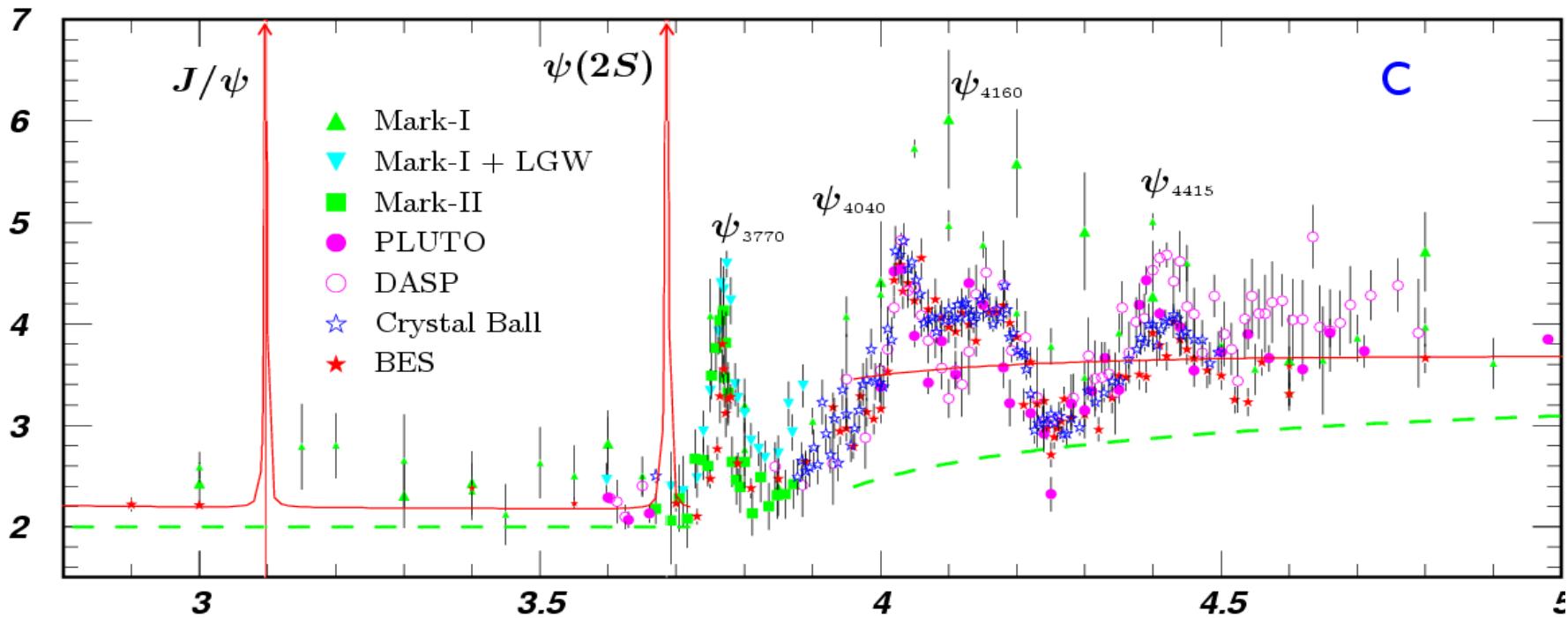


$J^{PC} = 1^{--}$
 $\Upsilon(nS), Y_b \dots$



ISR production of vector charmonia

R



X States

X(3872), X(5568), X_b ...

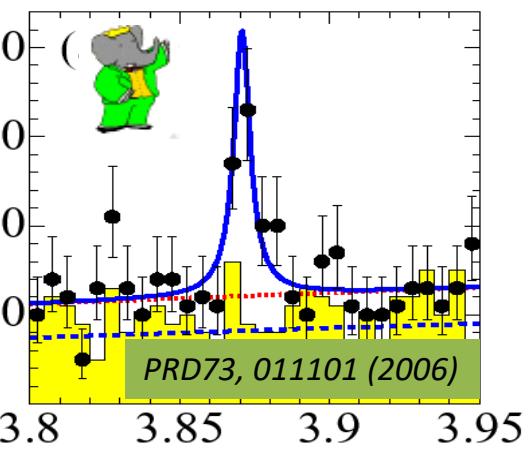
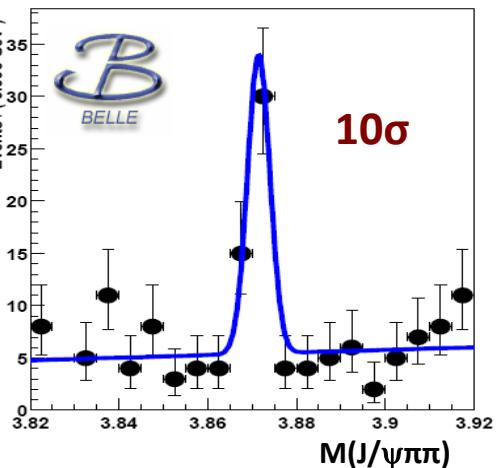
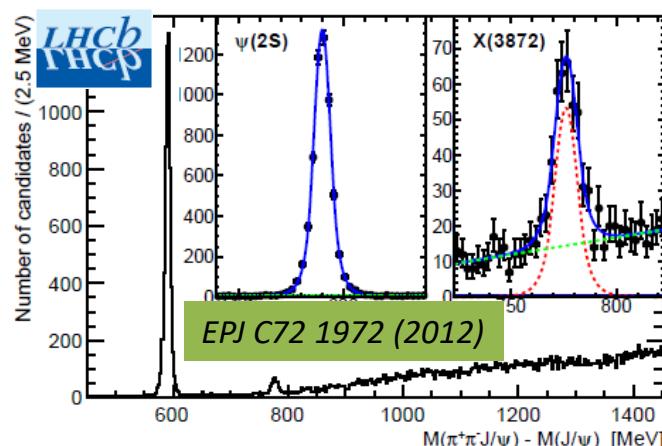
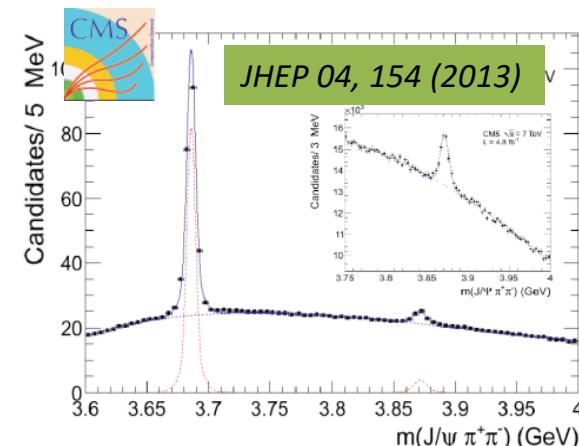
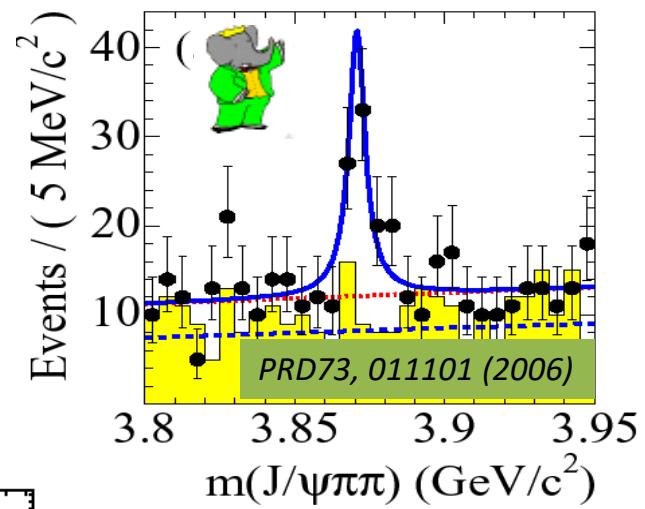
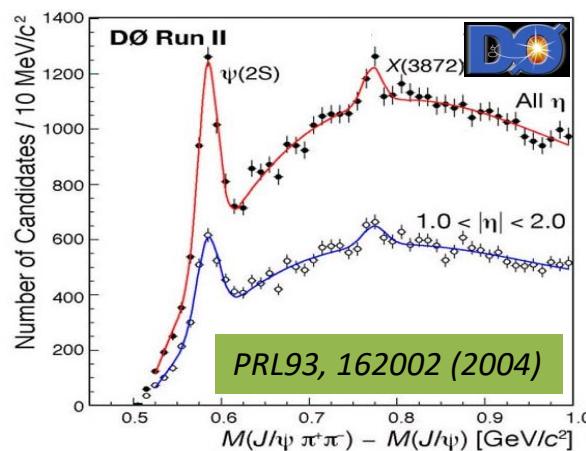
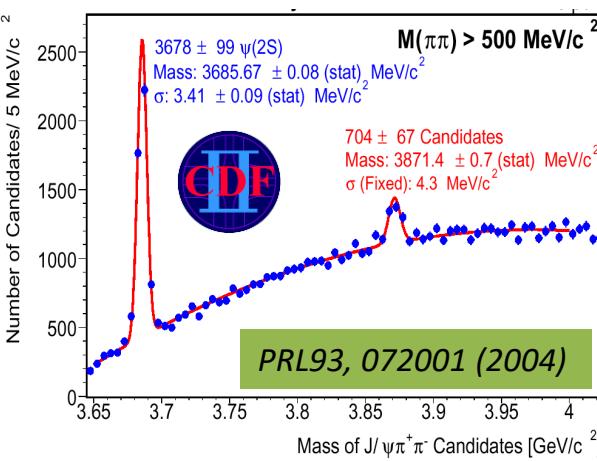
Observed in B decays and (suggestively) in decays of Y type states

$X(3872) \rightarrow J/\psi \pi^+ \pi^-$

Belle's most cited paper: 1200+

first observed by Belle in $B \rightarrow K J/\psi \pi^+ \pi^-$ PRL91, 262001 (2003)

- ◆ M_X close to $D^0 D^{*0}$ threshold $M = 3871.68 \pm 0.17$ MeV
(not clear below or above: $\Delta m = -0.16 \pm 0.32$ MeV)
- ◆ surprisingly narrow: $\Gamma_{\text{tot}} < 1.2$ MeV at 90% CL



$X(3872) \rightarrow J/\psi \gamma$: C-even

Angular analysis:

Belle 2006: $J^{PC} = 1^{++}$ or ≥ 2

CDF 2008: $J^{PC} = 1^{++}$ or 2^{-+}

Belle 2011: $J^{PC} = 1^{++}$ or 2^{-+}

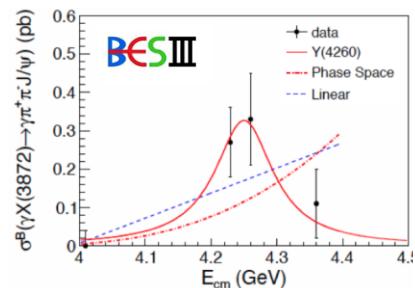
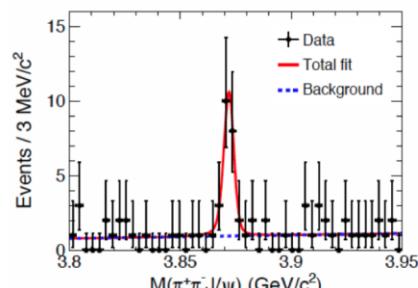
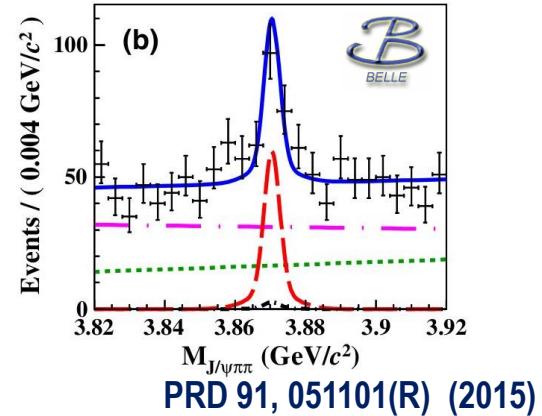
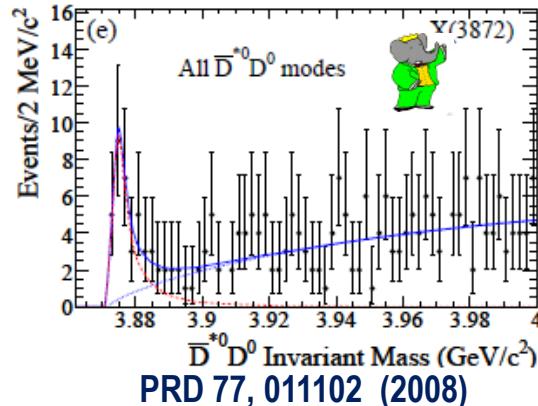
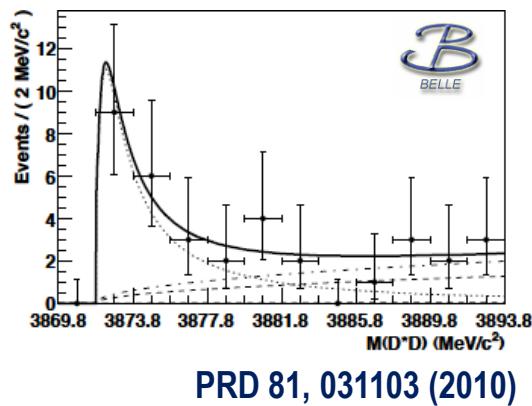
LHCb 2013: $J^{PC} = 1^{++}$

X(3872): Other Decay Modes

- ◆ $\pi\pi = \rho$ means Isospin violation!
- ◆ $X(3872) \rightarrow J/\psi\omega$ is seen: confirms isospin violation

$$B(X(3872) \rightarrow J/\psi\omega)/B(X(3872) \rightarrow J/\psi\pi\pi) = 0.8 \pm 0.3$$

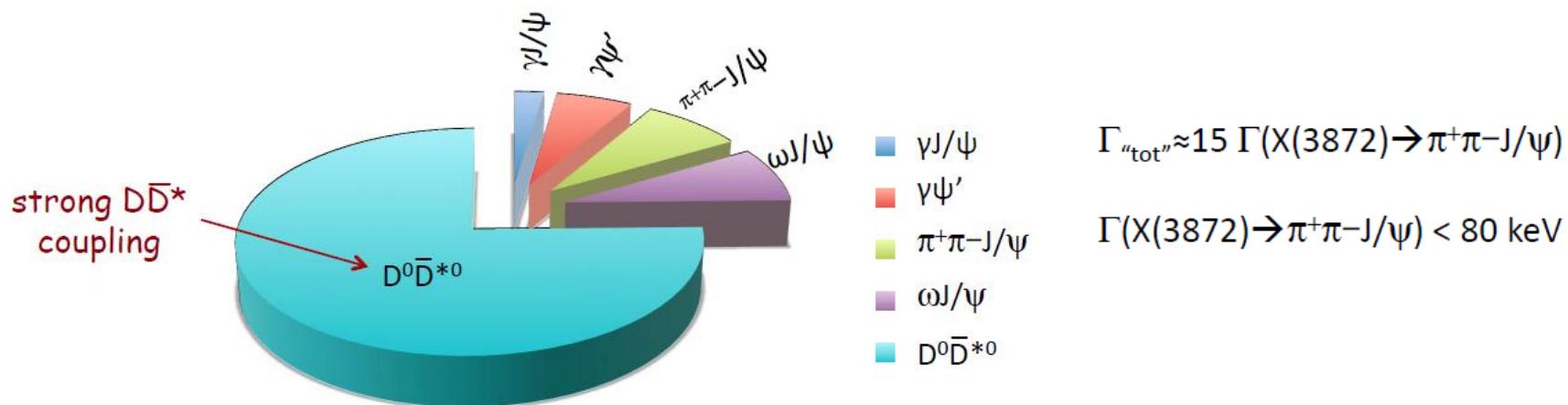
- ◆ Radiative decays: Belle&Babar good agreement for $X \rightarrow J/\psi\gamma$; **not consistent for $X \rightarrow \psi(2S)\gamma$** . LHCb confirms BaBar's not vanishing $X \rightarrow \psi(2S)\gamma$.
- ◆ $X(3872) \rightarrow D\bar{D}^*$ - dominant mode
- ◆ $B \rightarrow X(3872)K\pi$ non-resonant $K\pi$ dominates!



PRL 112, 092001 (2014)

- The first observation of $e^+e^- \rightarrow \gamma X(3872) \rightarrow \gamma\pi^+\pi^- J/\psi$
- $M = 3871.9 \pm 0.7 \pm 0.2$ MeV/c², $\Gamma < 2.4$ MeV, consistent with Belle's result
- Suggestive of $Y(4260) \rightarrow \gamma X(3872)$
- If $B(X(3872) \rightarrow \pi^+\pi^- J/\psi) = 5\%$, $\mathcal{R} = \frac{Br(e^+e^- \rightarrow \gamma X(3872))}{Br(e^+e^- \rightarrow \pi^+\pi^- J/\psi)} = 0.1$

X(3872) decay channels



$D^0\bar{D}^{*0}$ molecule?

Lots of literature about this

Impossible to produce such an fragile extended object in prompt high energy hadron colliders at the rates reported by CDF & CMS

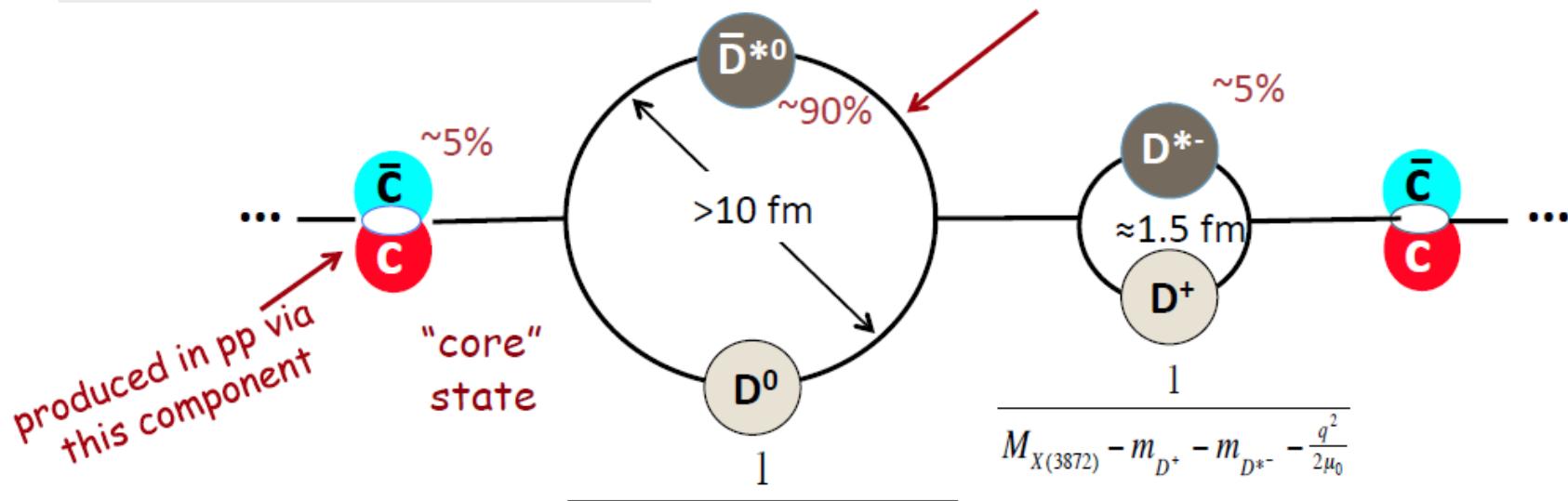
QCD diquark-dantiquark?

Maiani et al. PRD 71, 014028 (2005)

Predicts partner states (e.g., a nearby state with $u \rightarrow d$) that have yet be seen.
no charged partners of the X(3872)
no nearby neutral X(3872) partners

Probably a mixture of $D\bar{D}^*$ & a $c\bar{c}$ “core”

Specific model by
Takizawa & Takeuchi, PTEP 9, 093D01



$$d_{\text{rms}} \approx \frac{1}{\sqrt{2\mu_D |BE|}};$$

reduced mass $|m_D + m_{D^*} - m_{X3872}|$

$$\frac{M_{X(3872)} - m_{D^0} - m_{D^{*0}} - \frac{q^2}{2\mu_0}}{M_{X(3872)} - m_{D^+} - m_{D^{*-}} - \frac{q^2}{2\mu_0}}$$

$$|BE| < 0.2 \text{ MeV}$$

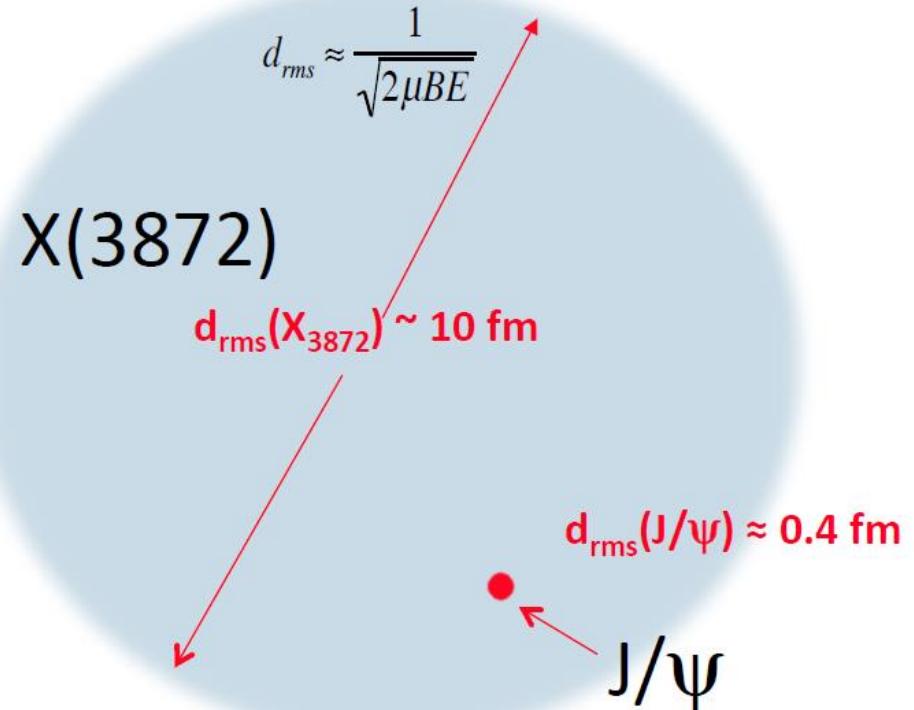
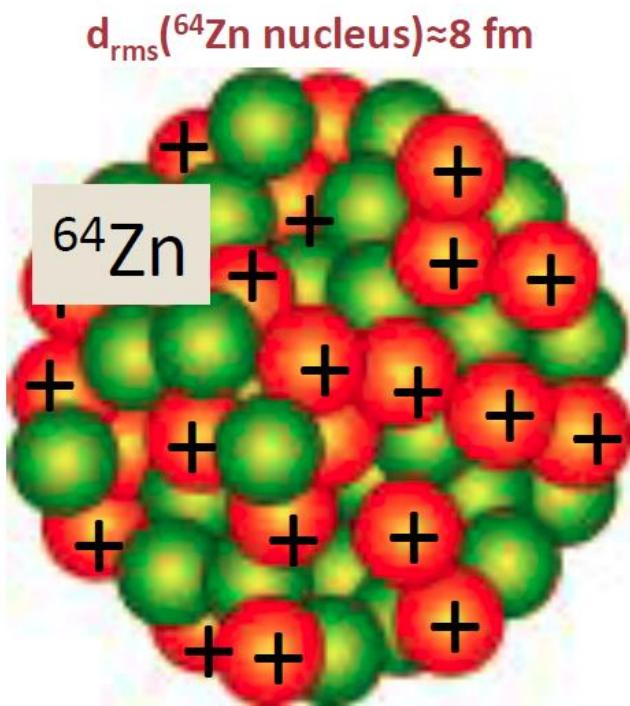
$$d_{\text{rms}}^{D^0\bar{D}^{*0}} > 10 \text{ fm}$$

$$|BE| \approx 8 \text{ MeV}$$

$$d_{\text{rms}}^{D^+D^{*-}} \approx 1.5 \text{ fm}$$

X(3872)-J/ ψ relative sizes

E. Braaten, J. Stapleton PRD81, 0140189



$$\text{Volume}(J/\psi) / \text{Volume}(X_{3872}) \approx 10^{-4}$$

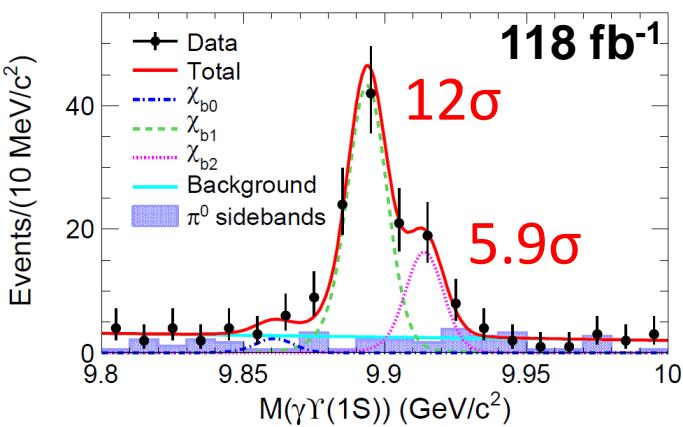
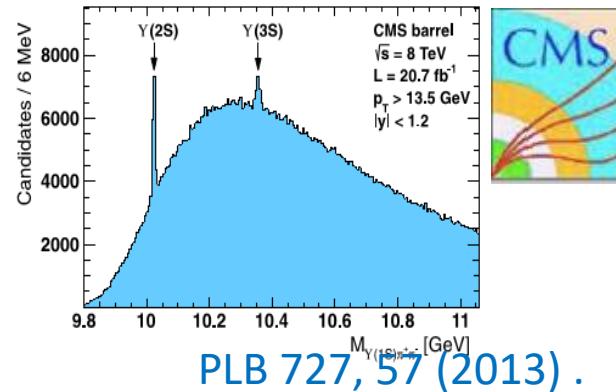
- How can such a fragile object be produced in H.E. pp collisions?

C. Bignamini *et al*, PRL 103, 162001: $\sigma_{CDF}(\text{meas}) > 3.1 \pm 0.7 \text{ nb}$ vs $\sigma_{\text{theory}}(\text{molecule}) < 0.11 \text{ nb}$

after 14 years, we still don't know

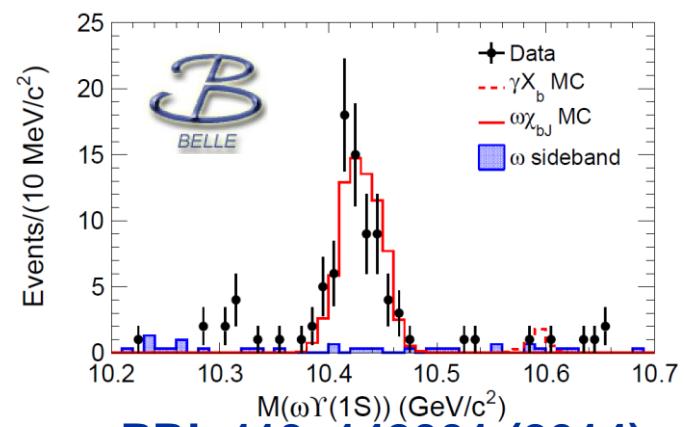
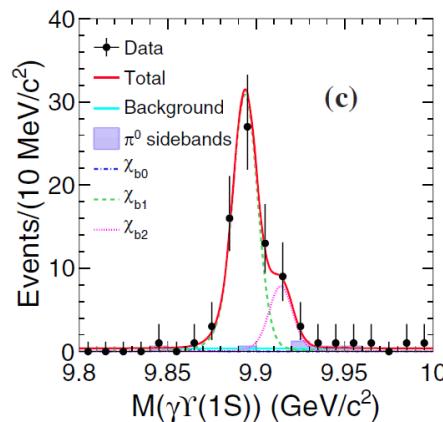
Search for X_b in $e^+e^- \rightarrow \gamma\pi^+\pi^-\pi^0Y(1S)$ at 10.867 GeV

- The $X(3872)$ counterpart in the bottomonium sector X_b , NOT observed decay channel $\pi^+\pi^-\gamma Y(1S)$.
- As X_b is above $\omega Y(1S)$ threshold, this Isospin-conserving process should be a more promising decay mode. [PRD88, 054007].

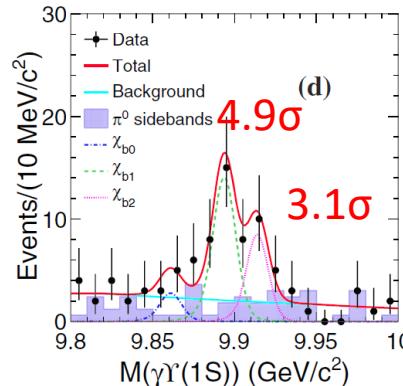


- Large Brs of $Y(5S)$ to $\pi^+\pi^-\pi^0\chi_{b1/b2}$, $\omega\chi_{b1/b2}$ are observed for the first time and their ratios are measured: hadronic loop effect ?

arXiv:1406.6763

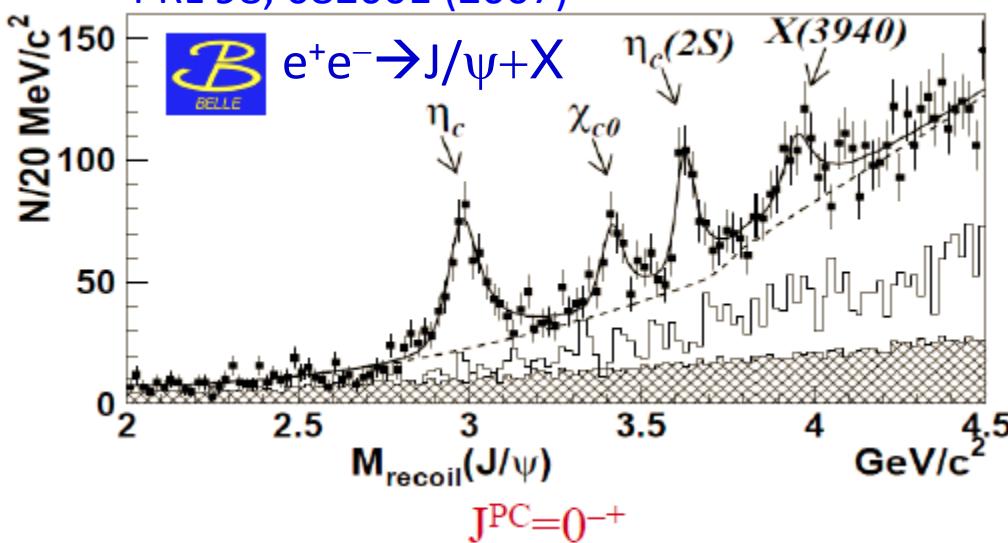


Assuming X_b is narrow, the upper limit on the product branching fraction was given.



X(3940) and X(4160) (Exotic ? Standard ?)

PRL 98, 082001 (2007)



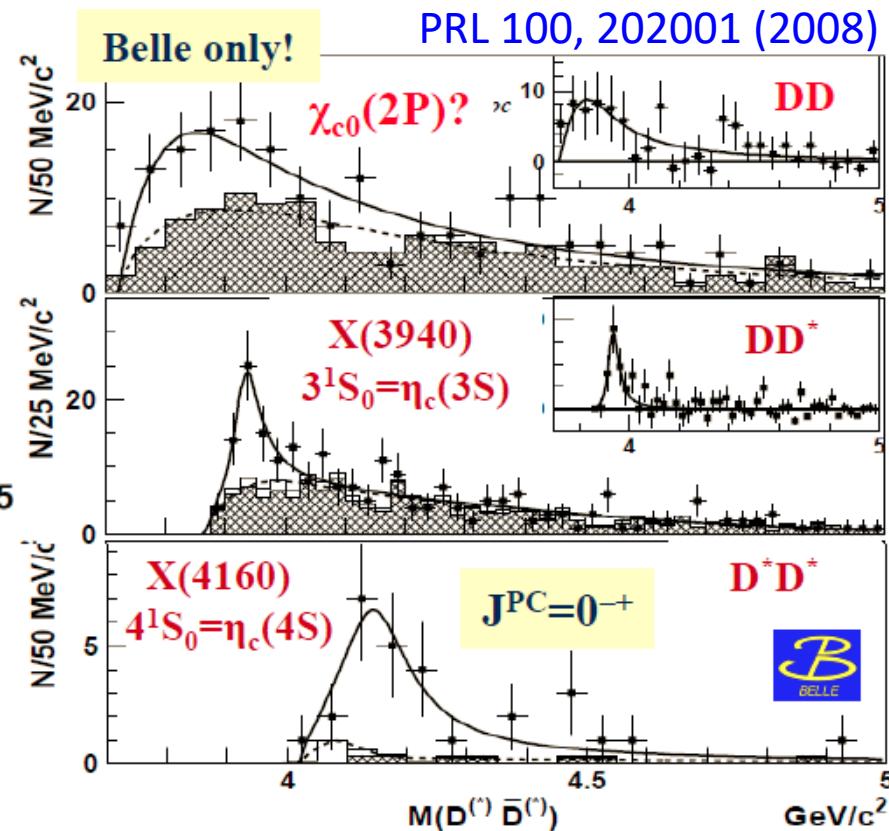
$$X(4160) = 4^1S_0 = \eta_c(4S)$$

Decays to open charm like standard charmonium

Mass of X(3940) & X(4160) are $\sim 100\text{-}150$ (250-300) MeV lower than the masses predicted by the potential models for $\eta_c(3S)$ and $\eta_c(4S)$

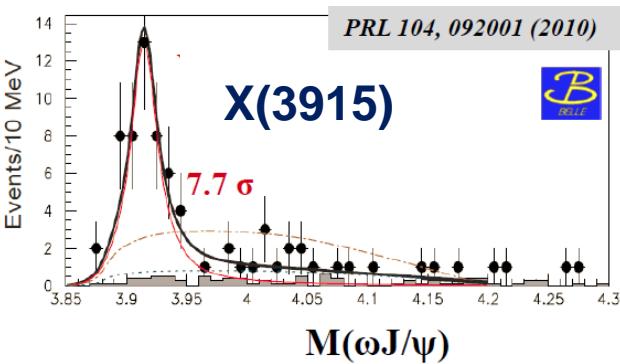
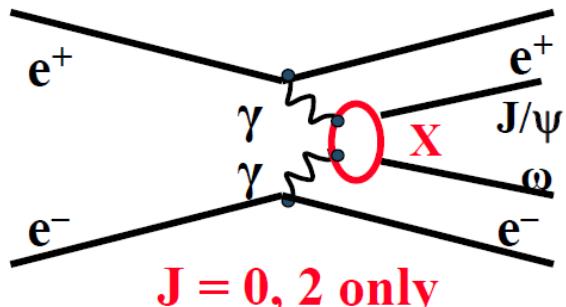
Theory probably needs more elaborate models to take into account charmonia couplings to meson pairs

PRL 100, 202001 (2008)



- Search for new states in $e^+e^- \rightarrow J/\psi D^{(*)}D^{(*)}\pi$ and in $e^+e^- \rightarrow \chi_{c1} D^{(*)}D^{(*)}$
- Production: reconstruction of the exclusive final states
- Production studies with other charmonium states (e.g. $\psi(2S)$, χ_{c1})

$X^*(3860)$ ($\chi_{c0}(2P)$)



Confirmed by BaBar, prefer $J^P=0^+$

PDG: $Y(3940)=X(3915)=\chi_{c0}(2P)$

Theory ☹

- $\chi_{c0}(2P)$ production in two body B decays is suppressed
- $\chi_{c0}(2P) \rightarrow DD$ should be dominant, but not seen
- a better candidate for $\chi_{c0}(2P)$ seen in $e^+e^- \rightarrow J/\psi DD$

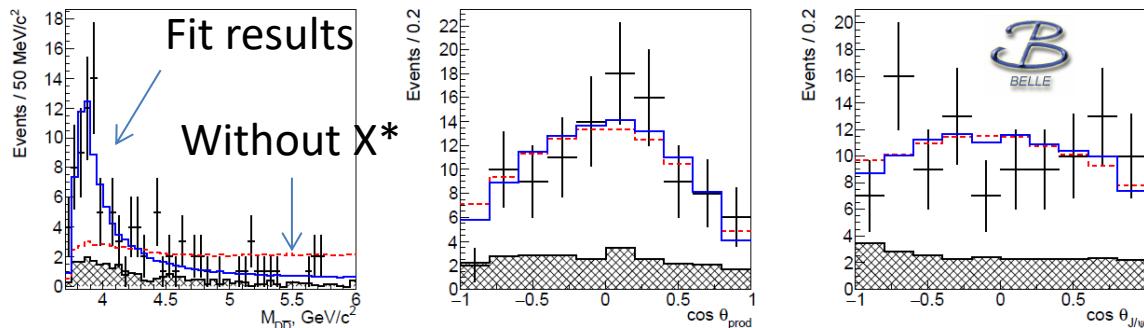
PDG 2016: $X(3915) \neq \chi_{c0}(2P)$

PRD 95, 112003 (2017)

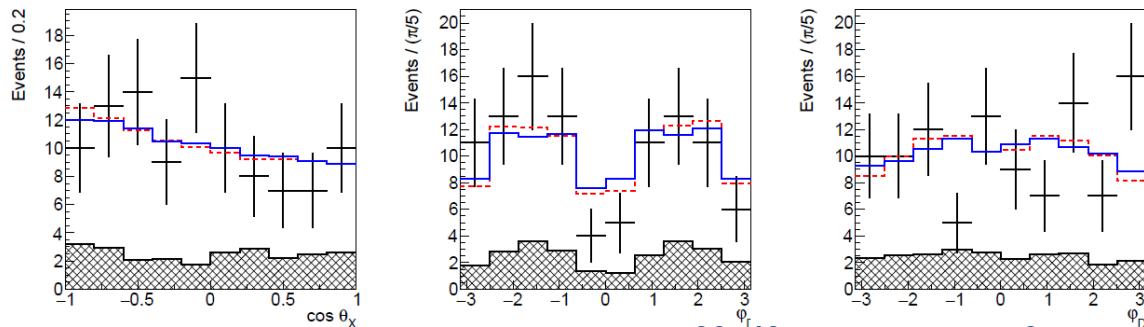
A 6D amplitude analysis was done to $e^+e^- \rightarrow J/\psi DD$

$$\Phi = (M_{D\bar{D}}, \theta_{\text{prod}}, \theta_{J/\psi}, \theta_{X^*}, \varphi_{\ell^-}, \varphi_D),$$

where θ_{prod} is the production angle, $\theta_{J/\psi}$ and θ_{X^*} are the J/ψ and X^* helicity angles, respectively, and φ_{ℓ^-} and φ_D are the ℓ^- and D azimuthal angles, respectively.



0^{++} is favored over the 2^{++} at 2.5σ



$X^*(3915): 8.5\sigma, 0^{++}, M=3862^{+26+40}_{-32-13} \text{ MeV}/c^2$

$\Gamma=201^{+154+88}_{-67-82} \text{ MeV}$

The parameters of $X^*(3915)$ are $<2.7\sigma$ difference from the predicted $\chi_{c0}(2P)$

If $X(3915) \neq \chi_{c0}'$, what is it?

It remains an intriguing puzzle

$X(3915) \rightarrow \omega J/\psi$ violates OZI-rule unless it's a 4-quark state

Mass is near $2m_{D_s}$ threshold: $M(X(3915)) = 2m_{D_s} - 18$ MeV

$X(3915) \rightarrow D\bar{D}$ decays are suppressed: $\Gamma(X(3915) \rightarrow D\bar{D}) < 1$ MeV

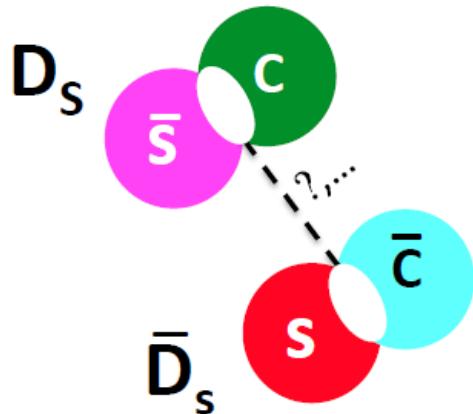
$D_s - \bar{D}_s$ molecule?

Li & Voloshin, PRD 91, 114014

$[\bar{c}\bar{s}][cs]$ tetraquark?

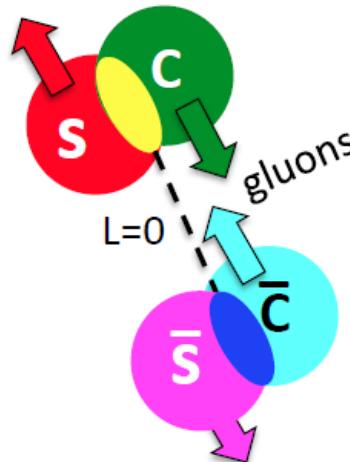
Lebed & Polosa, PRD 93, 094024

$c\bar{c}$ -gluon hybrid?

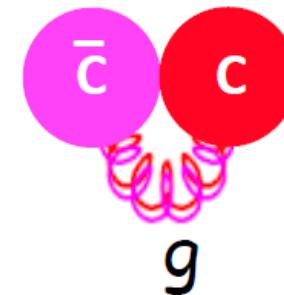


what binds it?

no plausible nuclear-physics-type
force can bind $D_s\bar{D}_s$ into a "molecule"



why not $X \rightarrow \eta\eta_c$?



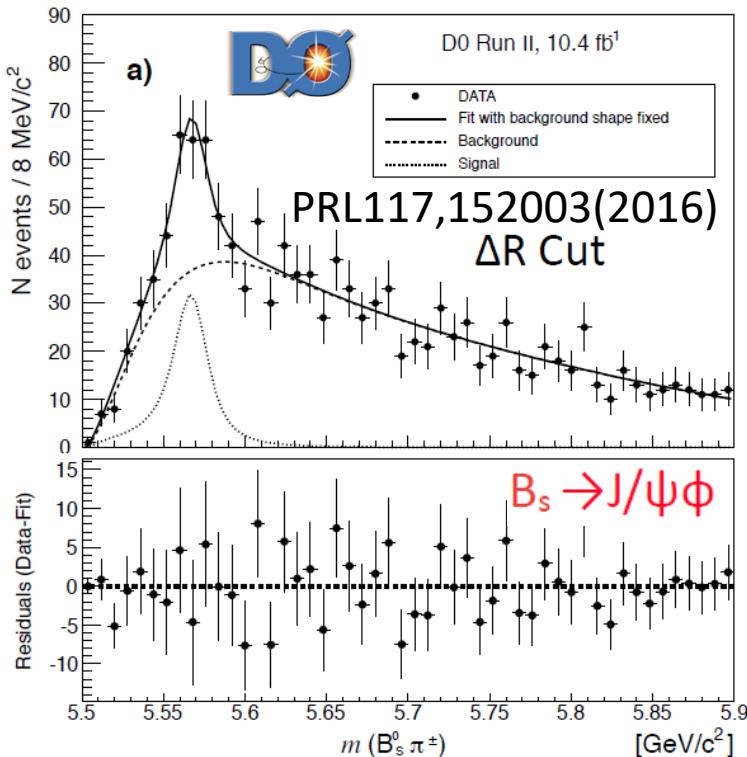
too light for 0^{++} cc-hybrid

X(5568)

Structure in $B_s\pi$ spectrum?

- D0 collaboration claimed state decaying to $B_s\pi^+$
- LHCb has large data sample to check it
 - 112600 B_s events (LHCb) vs. 5582 (D0)
- No state seen in place of D0 state

PRL117, 152003 (2016)



Statistical significance of signal
(including systematics and LEE)

$$\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2} < 0.3$$

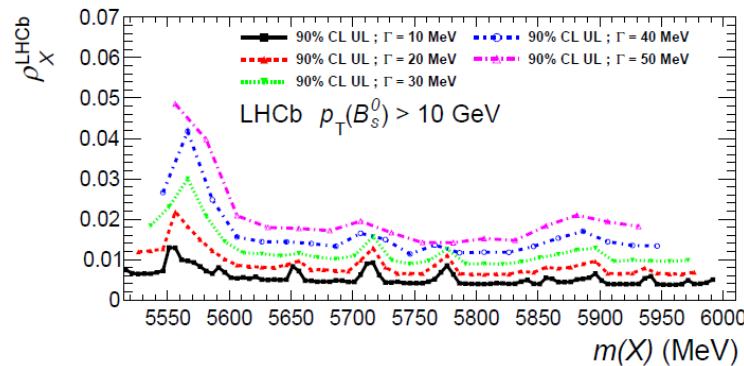
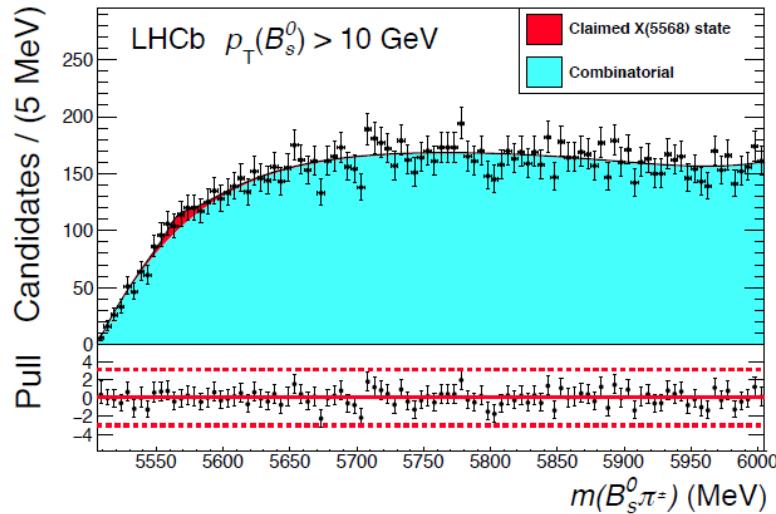
With ΔR Cut: 5.1 σ, Without ΔR Cut: 3.9 σ
Not seen at LHCb and CMS

X(5568)

$$M_X = 5567.8 \pm 2.9 \text{ (stat)}^{+0.9}_{-1.9} \text{ (syst)} \text{ MeV}/c^2$$

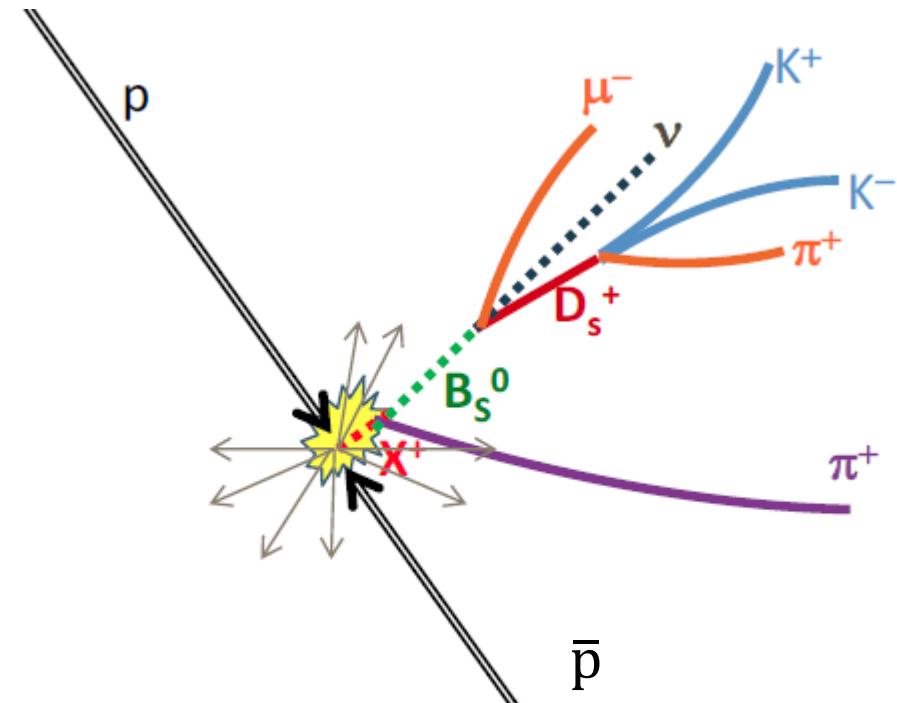
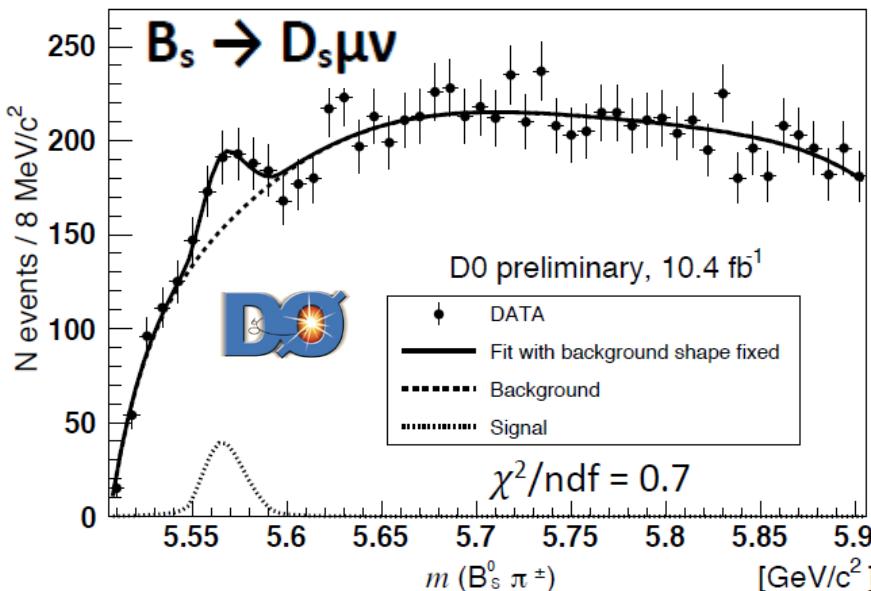
$$\Gamma_X = 21.9 \pm 6.4 \text{ (stat)}^{+5.0}_{-2.5} \text{ (syst)} \text{ MeV}/c^2$$

$$\rho = [8.6 \pm 1.9 \text{ (stat)} \pm 1.4 \text{ (syst)}] \%$$



X(5568)

D0 Conference Note 6494



X(5568)

$$N_X = 139^{+51}_{-63}$$

$$M_X = 5566.7^{+3.6}_{-3.4} \text{ MeV}/c^2$$

$$\Gamma_X = 6.0^{+9.5}_{-6.0} \text{ MeV}/c^2$$

Local Significance

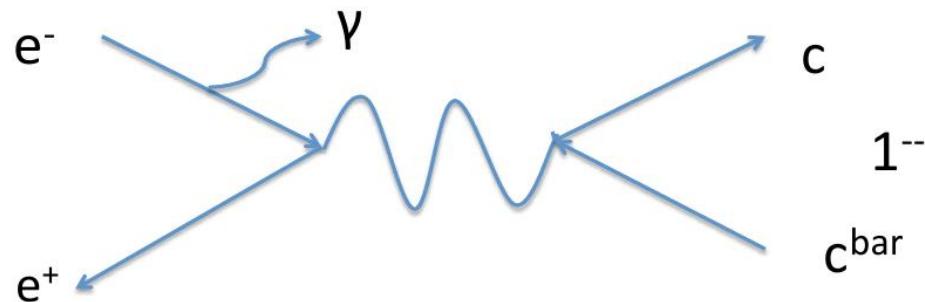
$$\sqrt{-2 \ln \frac{\mathcal{L}_0}{\mathcal{L}_{\max}}}$$

Statistical Significance 4.5σ .
Including Systematics 3.2σ .

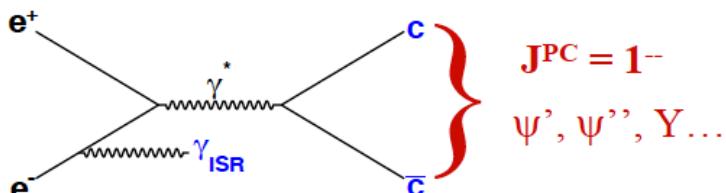
Y States

$\Upsilon(4260)$, $\Upsilon(4360)$, $\Upsilon(4660)...$

Observed in the e^+e^- annihilation (with ISR)



$e^+e^- \rightarrow \pi^+\pi^- J/\psi$ cross section

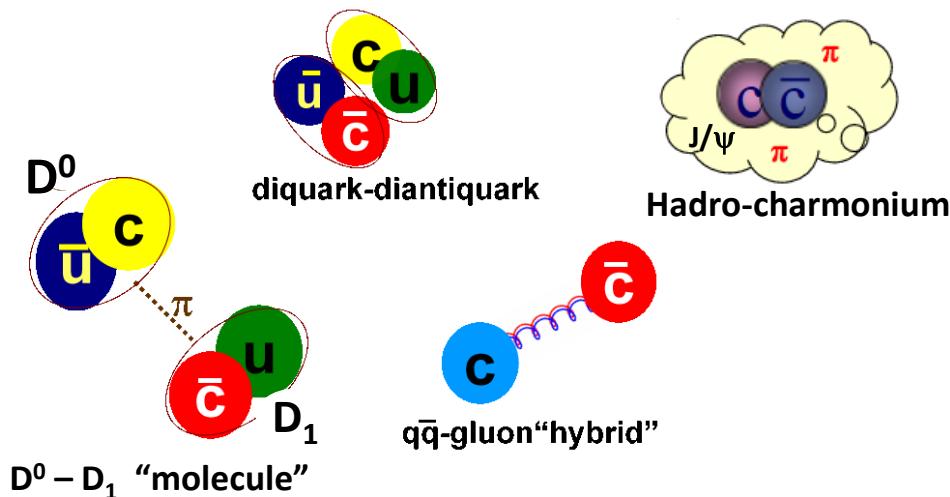
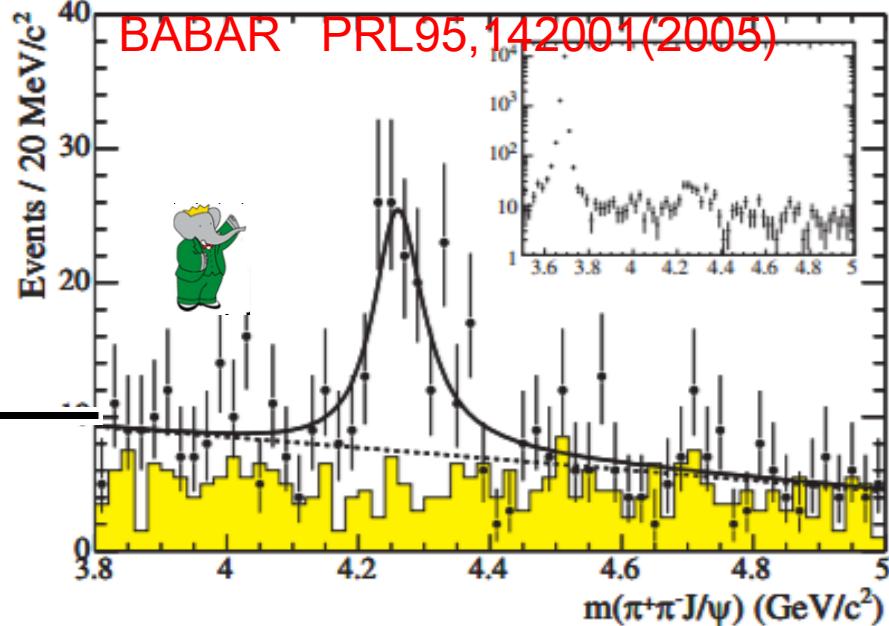


X(4260)

$I^G(J^{PC}) = ??(1^{--})$

X(4260) MASS **4251 \pm 9** PDG AVERAGE

X(4260) WIDTH **120 \pm 12** PDG AVERAGE



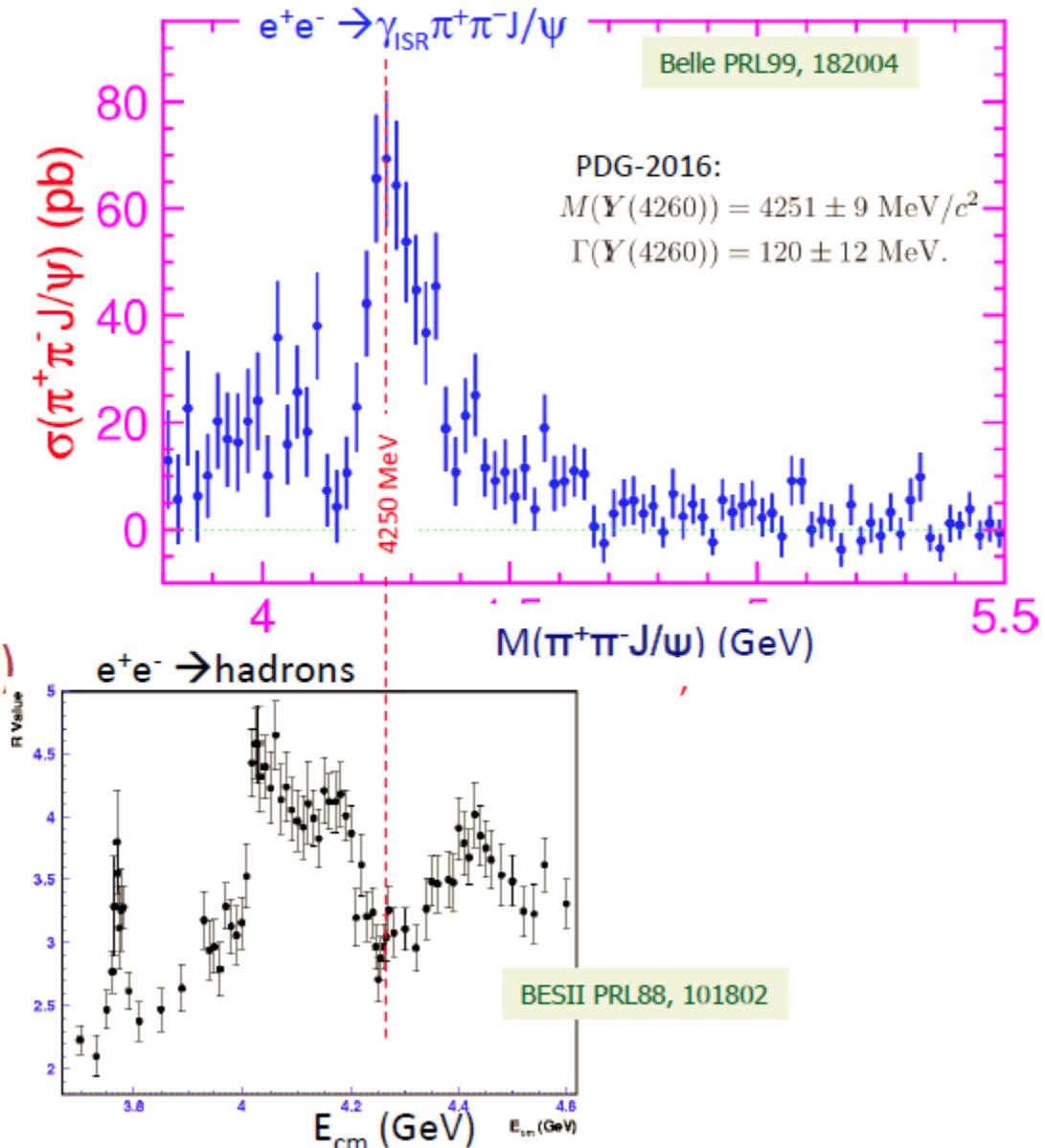
$\Upsilon(4260) \rightarrow \pi^+\pi^-J/\psi$ confirmed by Belle



no sign of $\Upsilon(4260) \rightarrow D^{(*)}\bar{D}^{(*)}$

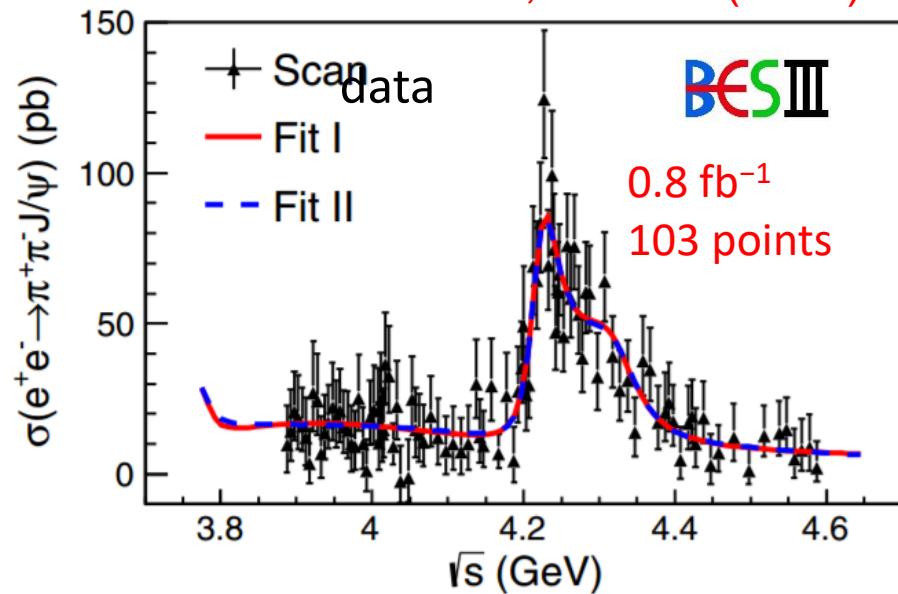
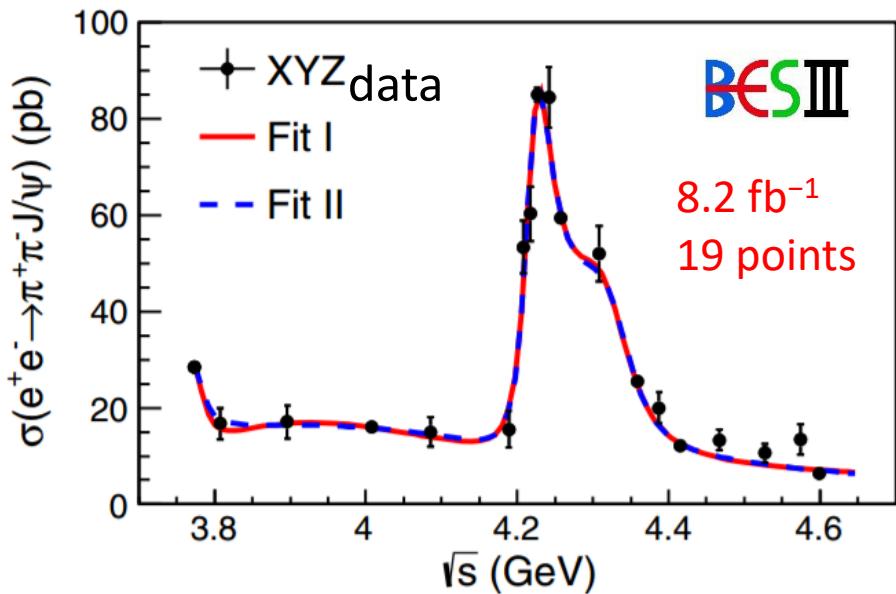
$\Upsilon(4260)$ peak in $\sigma(\pi^+\pi^-J/\psi)$
occurs at a dip in $\sigma(D^{(*)}\bar{D}^{(*)})$

$\Gamma(\pi^+\pi^-J/\psi)$ is large, but
should be OZI suppressed if $c\bar{c}$



$e^+e^- \rightarrow \pi^+\pi^- J/\psi$ cross section at BESIII

PRL118, 092001 (2017)



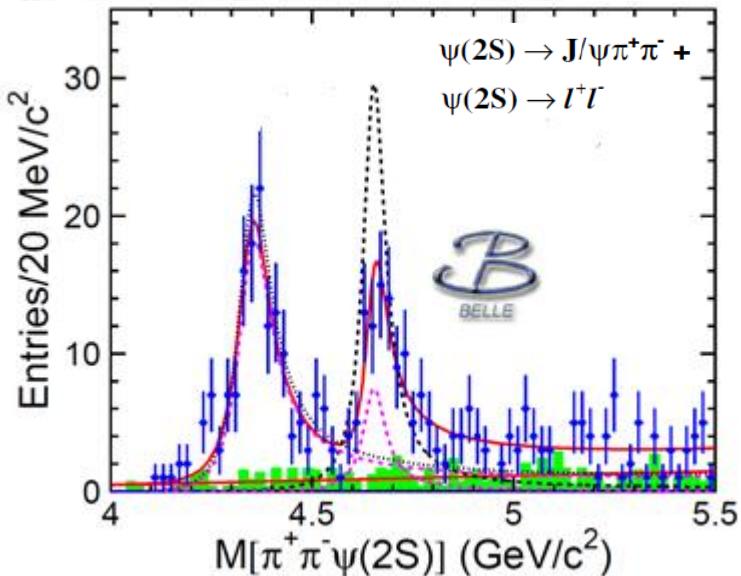
- Most precise cross section measurement to date from BESIII
- $\text{Fit I} = |\text{BW}_1 + \text{BW}_2 * e^{i\phi_2} + \text{BW}_3 * e^{i\phi_3}|^2$ or $\text{Fit II} = |\exp + \text{BW}_2 * e^{i\phi_2} + \text{BW}_3 * e^{i\phi_3}|^2$ (other fits ruled out)
- $M = 4222.0 \pm 3.1 \pm 1.4 \text{ MeV}$ (**lower**)
- $\Gamma = 44.1 \pm 4.3 \pm 2.0 \text{ MeV}$ (**narrower**)
- A 2nd resonance Y_2 with $M = 4320.0 \pm 10.4 \pm 7.0 \text{ MeV}/c^2$
 $\Gamma = 101.4^{+25.3}_{-19.7} \pm 10.2 \text{ MeV}$
- Observed for the **first time**, significance $> 7.6\sigma$

Updated $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$

PRD 91, 112007 (2015)

Unbinned simultaneous maximum likelihood fit for $\psi(4360)$ and $\psi(4660)$.

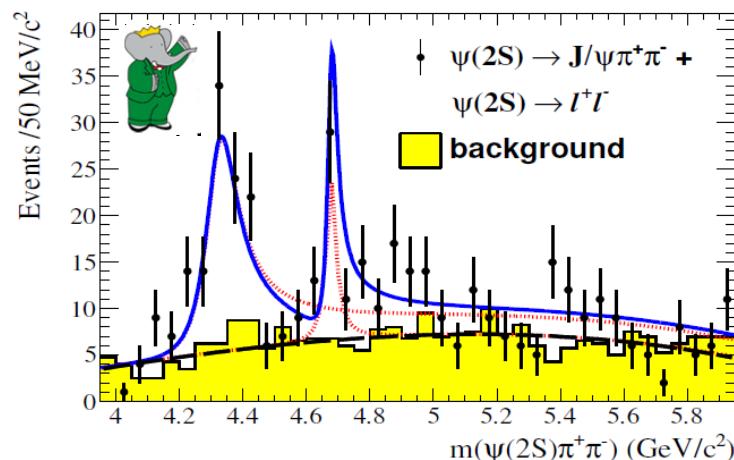
$$Amp = BW_1 + e^{i\phi} \cdot BW_2$$



Parameters	Solution I	Solution II
$M_{\psi(4360)} (\text{MeV}/c^2)$	$4347 \pm 6 \pm 3$	
$\Gamma_{\psi(4360)} (\text{MeV})$	$103 \pm 9 \pm 5$	
$\mathcal{B} \cdot \Gamma_{\psi(4360)}^{e^+e^-} (\text{eV})$	$9.2 \pm 0.6 \pm 0.6$	$10.9 \pm 0.6 \pm 0.7$
$M_{\psi(4660)} (\text{MeV}/c^2)$	$4652 \pm 10 \pm 11$	
$\Gamma_{\psi(4660)} (\text{MeV})$	$68 \pm 11 \pm 5$	
$\mathcal{B} \cdot \Gamma_{\psi(4660)}^{e^+e^-} (\text{eV})$	$2.0 \pm 0.3 \pm 0.2$	$8.1 \pm 1.1 \pm 1.0$
$\phi (\text{°})$	$32 \pm 18 \pm 20$	$272 \pm 8 \pm 7$

$$\chi^2/ndf = 18.7/21.$$

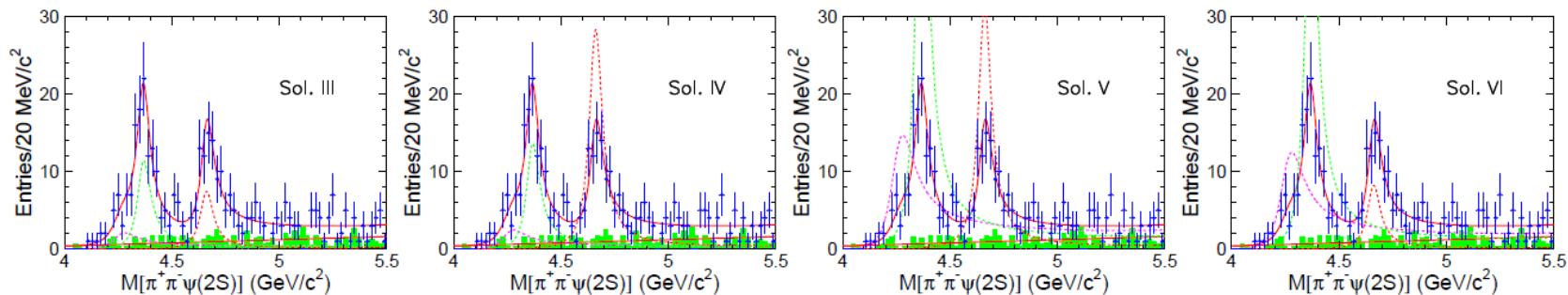
- Consistent with previous measurement
- No obvious signal above $\psi(4660)$.
- Some events accumulate at $\psi(4260)$, especially the $\pi^+\pi^-J/\psi$ mode.
- If $\psi(4260)$ is included in the fit, ...



PRD89, 111103 (2014)

$M(\pi^+\pi^-\psi(2S))$ with $\Upsilon(4260,4360,4660)$

Unbinned simultaneous maximum likelihood fit for $\Upsilon(4260)$, $\Upsilon(4360)$ and $\Upsilon(4660)$. $Amp = BW_1 + e^{i\phi_1} \cdot BW_2 + e^{i\phi_2} \cdot BW_3$.



Parameters	Solution I	Solution II	Solution III	Solution IV
$\mathcal{B} \cdot \Gamma_{\Upsilon(4260)}^{e^+e^-}$ (eV)	$1.5 \pm 0.6 \pm 0.4$	$1.7 \pm 0.7 \pm 0.5$	$10.4 \pm 1.3 \pm 0.8$	$8.9 \pm 1.2 \pm 0.8$
$M_{\Upsilon(4360)}$ (MeV/ c^2)			$4365 \pm 7 \pm 4$	
$\Gamma_{\Upsilon(4360)}$ (MeV)			$74 \pm 14 \pm 4$	
$\mathcal{B} \cdot \Gamma_{\Upsilon(4360)}^{e^+e^-}$ (eV)	$4.1 \pm 1.0 \pm 0.6$	$4.9 \pm 1.3 \pm 0.6$	$21.1 \pm 3.5 \pm 1.4$	$17.7 \pm 2.6 \pm 1.5$
$M_{\Upsilon(4660)}$ (MeV/ c^2)			$4660 \pm 9 \pm 12$	
$\Gamma_{\Upsilon(4660)}$ (MeV)			$74 \pm 12 \pm 4$	
$\mathcal{B} \cdot \Gamma_{\Upsilon(4660)}^{e^+e^-}$ (eV)	$2.2 \pm 0.4 \pm 0.2$	$8.4 \pm 0.9 \pm 0.9$	$9.3 \pm 1.2 \pm 1.0$	$2.4 \pm 0.5 \pm 0.3$
ϕ_1 ($^\circ$)	$304 \pm 24 \pm 21$	$294 \pm 25 \pm 23$	$130 \pm 4 \pm 2$	$141 \pm 5 \pm 4$
ϕ_2 ($^\circ$)	$26 \pm 19 \pm 10$	$238 \pm 14 \pm 21$	$329 \pm 8 \pm 5$	$117 \pm 23 \pm 25$

Significance of $\Upsilon(4260)$ is 2.4σ —low, but affects $\Upsilon(4360)$ and $\Upsilon(4660)$ masses and widths.

FOUR solutions with equally good fit quality, which is $\chi^2/ndf = 14.8/19$.

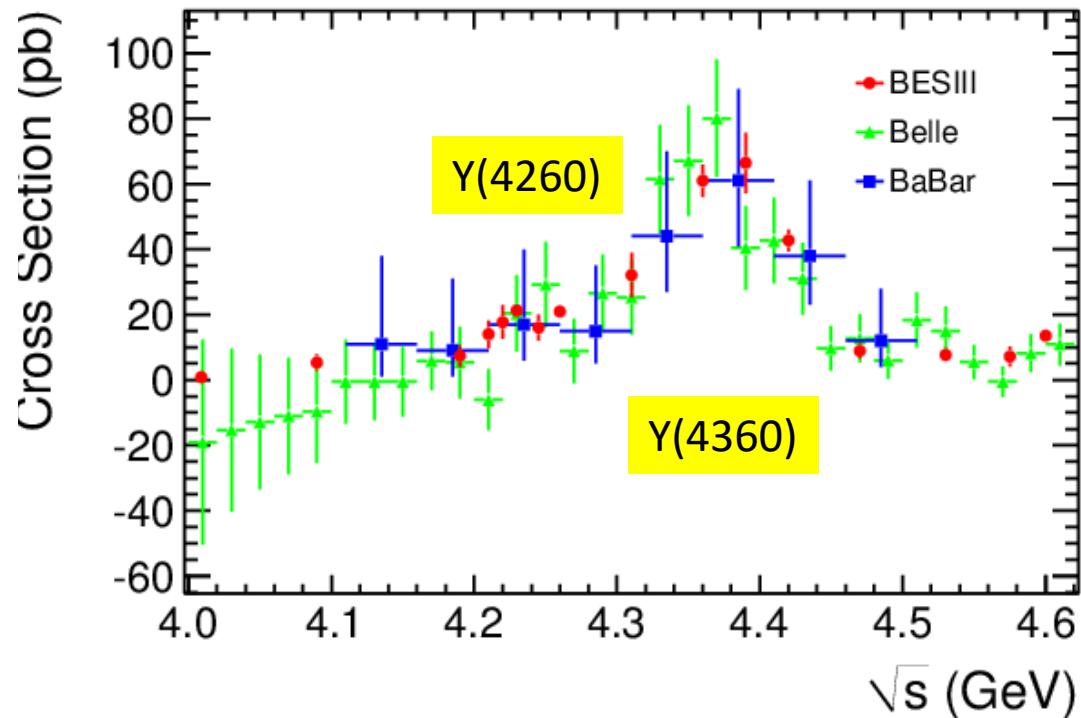
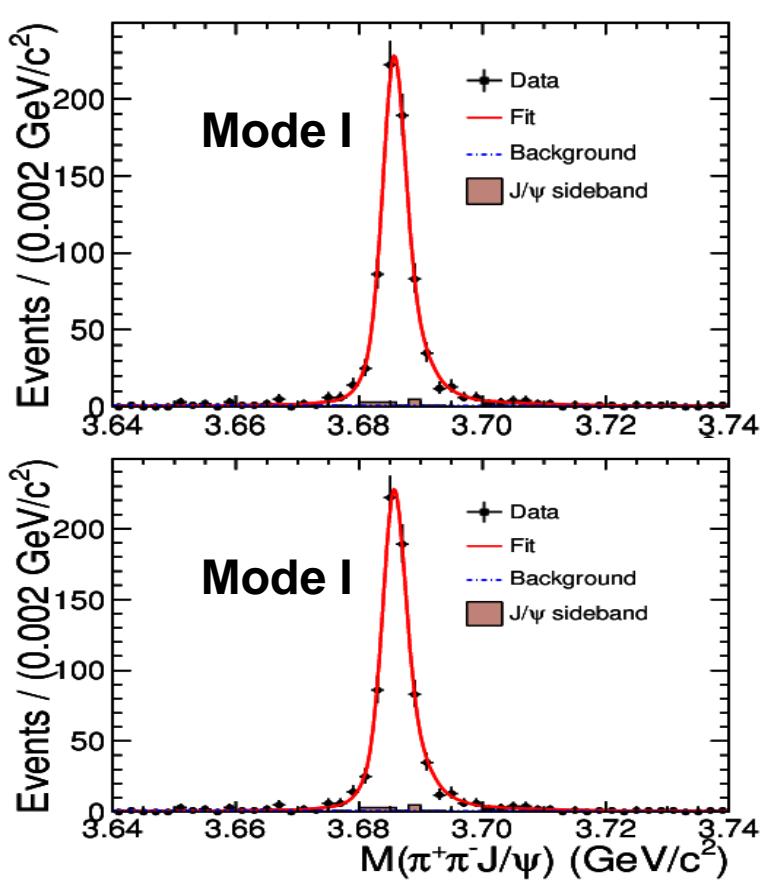
Comparsion of $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$ cross section

BESIII (16 energy points; $L_{\text{tot}}=5.1\text{fb}^{-1}$)

$\psi(2S)$ Reconstructed modes:

Mode I: $\Psi(3686) \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow l^+l^- (l=e/\mu)$

Mode II: $\Psi(3686) \rightarrow \text{neutrals} + J/\psi, \text{neutrals} = (\pi^0\pi^0, \pi^0, \eta \text{ and } \gamma\gamma) J/\psi \rightarrow l^+l^- (l=e/\mu)$



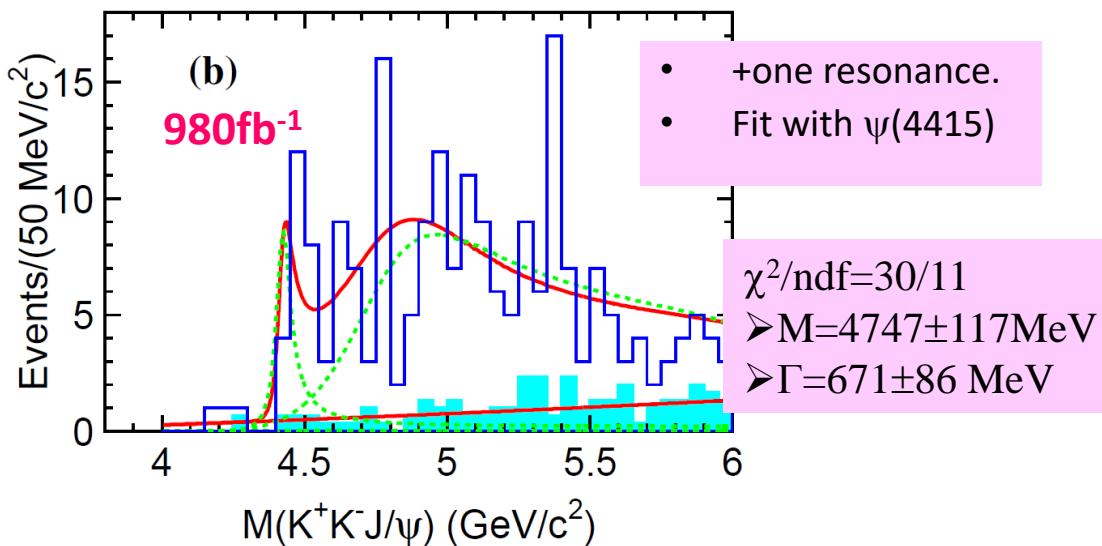
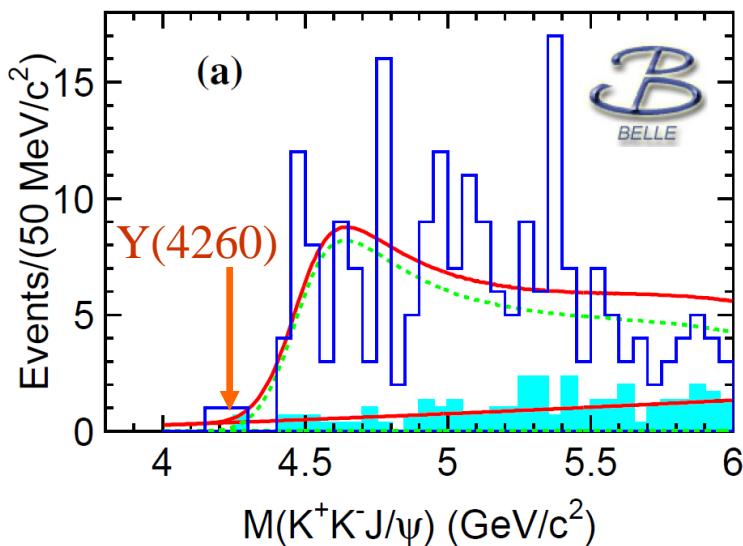
The measured Born cross sections of two modes are combined by considering the correlated and uncorrelated uncertainties.

Updated $e^+e^- \rightarrow K^+K^-J/\psi$

PRD 89,072015(2014)

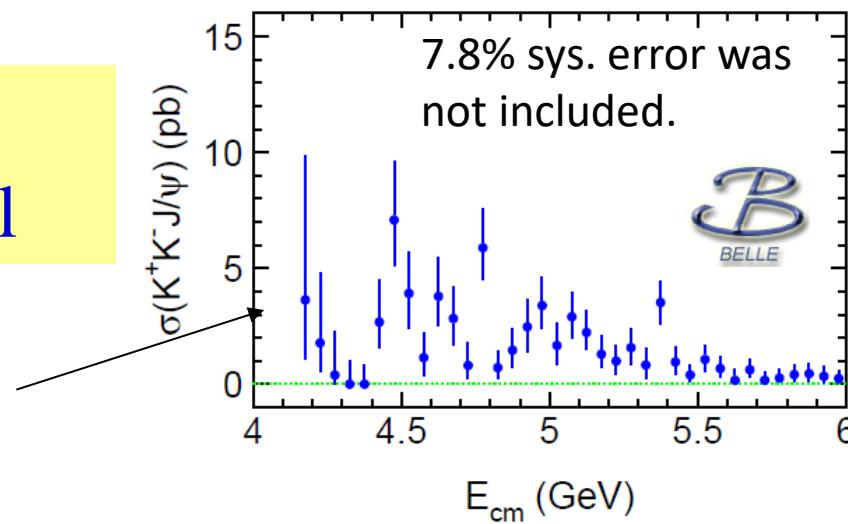
Event selections are almost the same as in Phys. Rev. D 77,
011105(R) (2008)

Shaded hist.: J/ψ mass sidebands



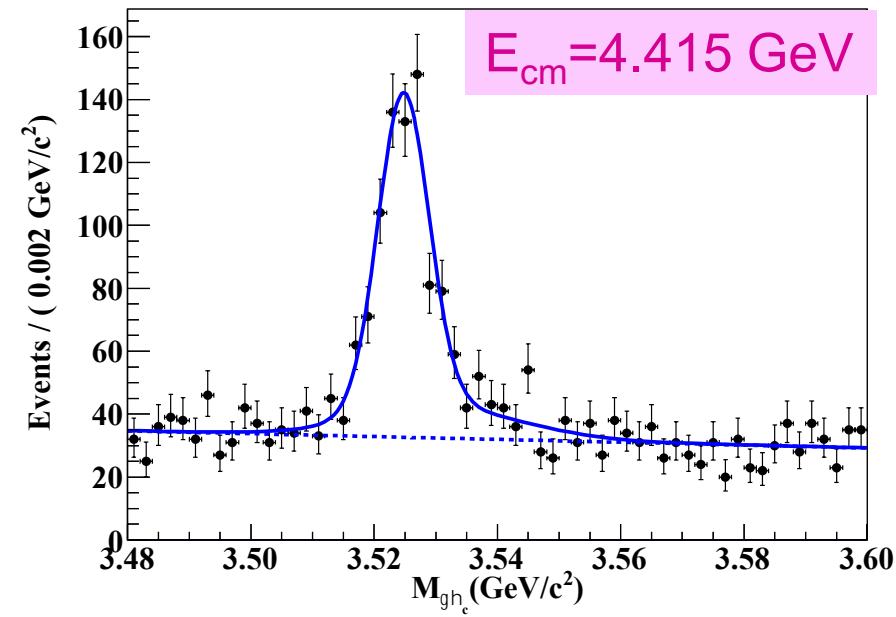
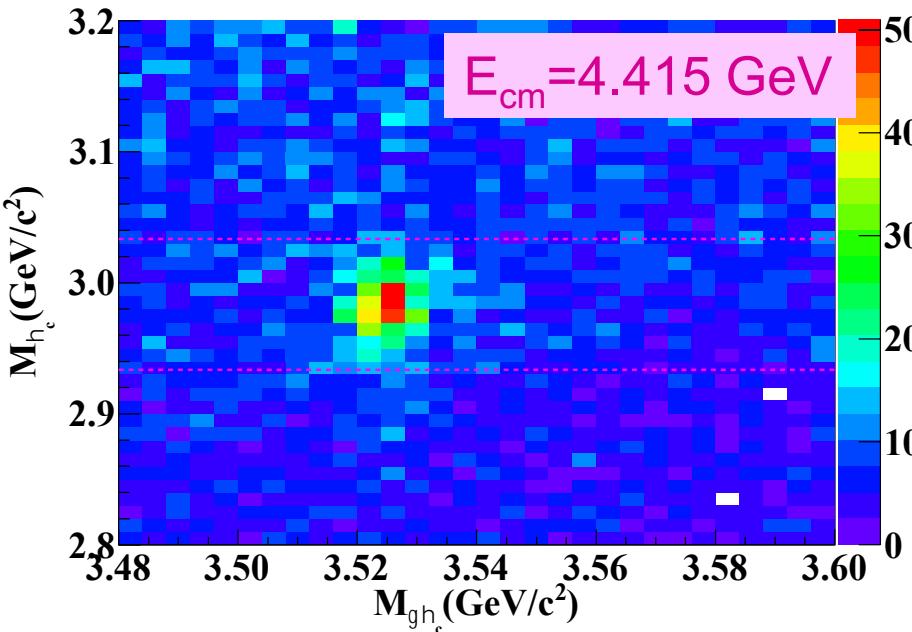
4-6 GeV: 213 events
35 bkg, 178 ± 16 signal

$$\sigma_i = \frac{n_i^{\text{obs}} - f \times n_i^{\text{bkg}}}{\mathcal{L}_i \cdot \epsilon_i \cdot \mathcal{B}(J/\psi \rightarrow \ell^+\ell^-)}$$



$e^+e^- \rightarrow \pi^+\pi^- h_c(1P)$ at BESIII

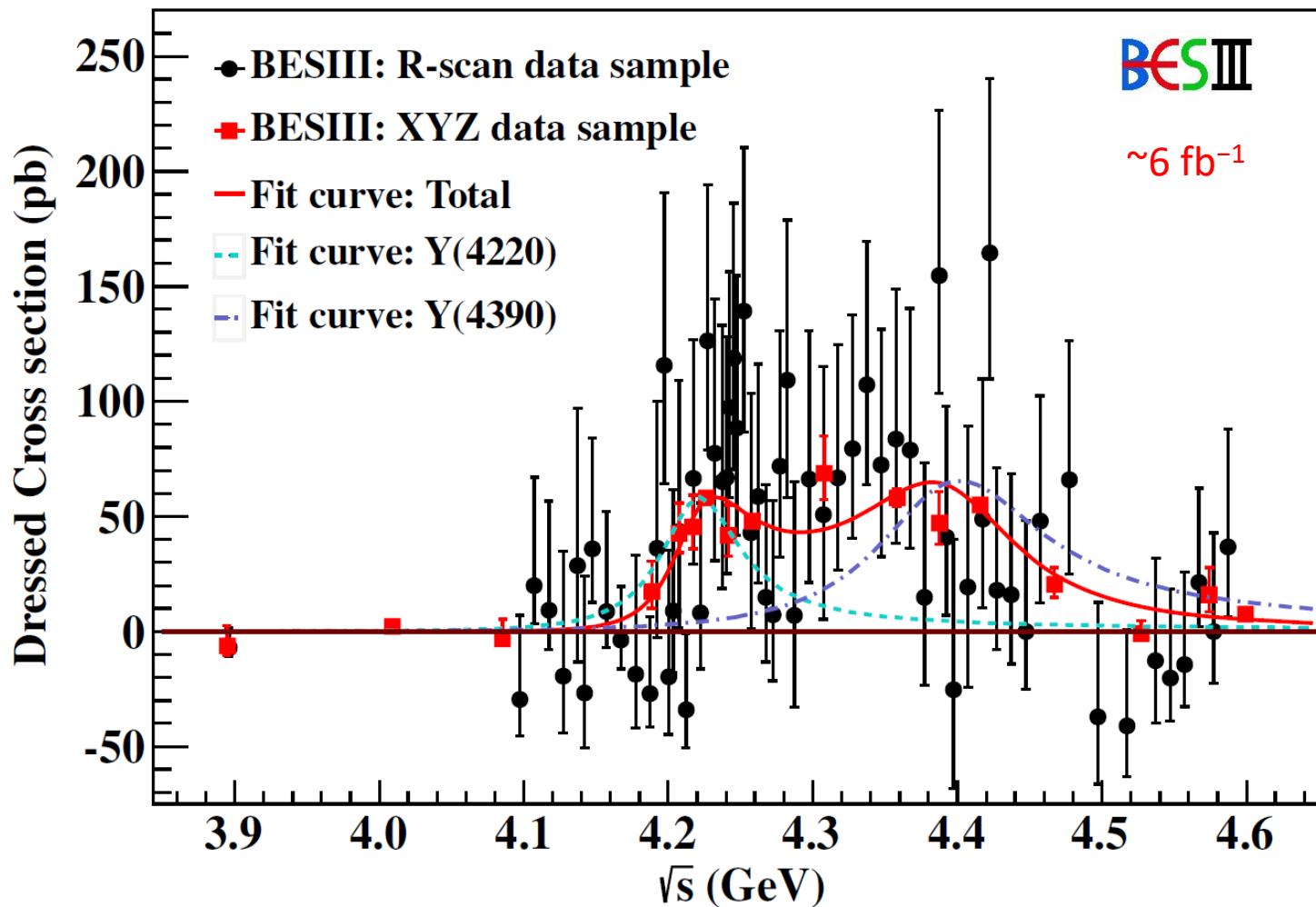
- $h_c \rightarrow \gamma\eta_c, \eta_c \rightarrow \text{hadrons}$ [16 exclusive decay modes]
 - $pp, \pi^+\pi^-K^+K^-, \pi^+\pi^-pp, 2(K^+K^-), 2(\pi^+\pi^-), 3(\pi^+\pi^-)$
 - $2(\pi^+\pi^-)K^+K^-, K_S^0K^+\pi^- + \text{c.c.}, K_S^0K^+\pi^-\pi^+\pi^- + \text{c.c.}, K^+K^-\pi^0$
 - $pp\pi^0, K^+K^-\eta, \pi^+\pi^-\eta, \pi^+\pi^-\pi^0\pi^0, 2(\pi^+\pi^-)\eta, 2(\pi^+\pi^-\pi^0)$



Method same as in PRL111, 242001 (2013)

$e^+e^- \rightarrow \pi^+\pi^- h_c$ cross section at BESIII

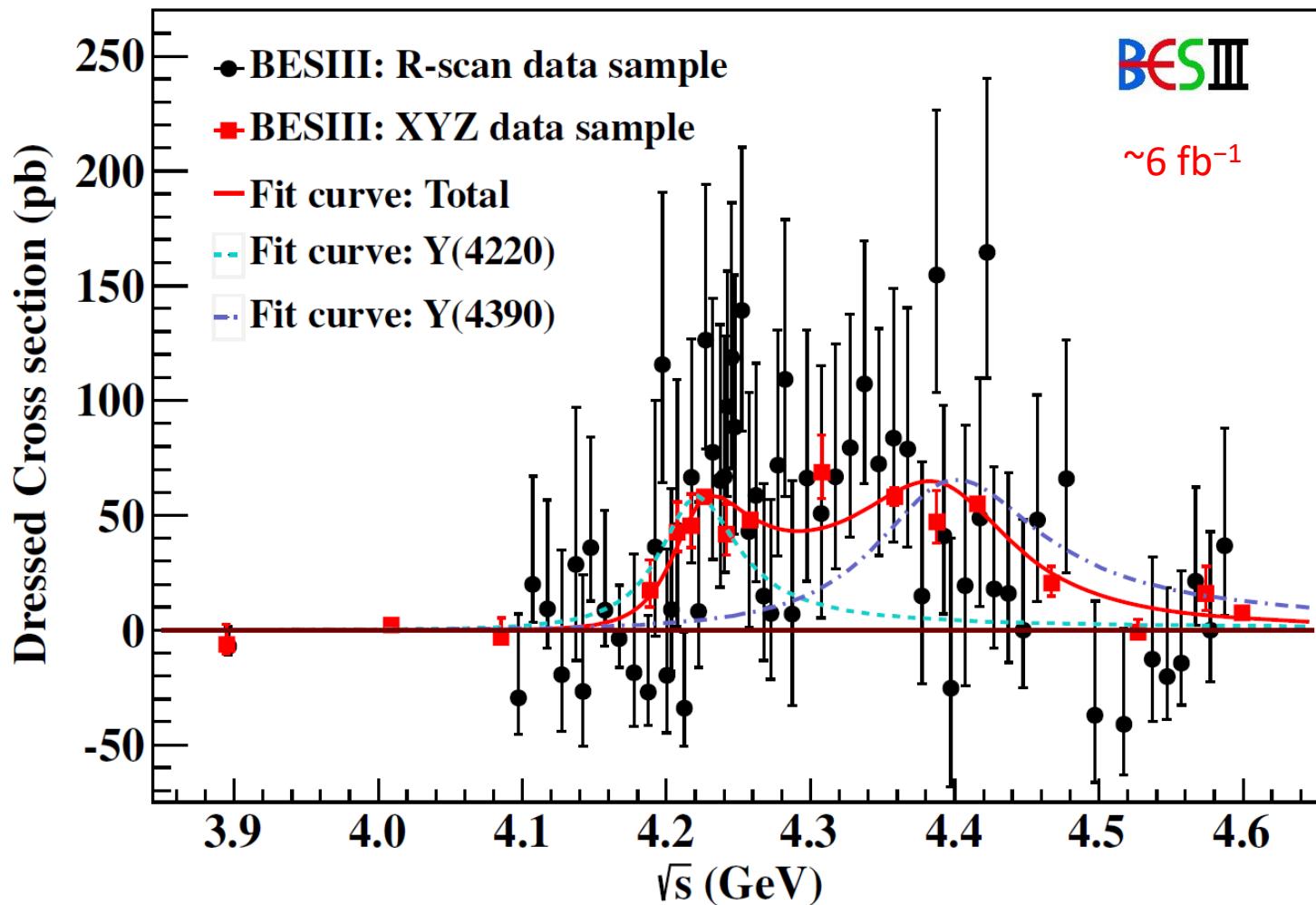
PRL118, 092002 (2017)



- First precise cross section measurement from threshold to 4.6 GeV
- Fit with $|BW_1 + BW_2 * e^{i\phi_2}|^2$, two resonant structures are evident

$e^+e^- \rightarrow \pi^+\pi^- h_c$ cross section at BESIII

PRL118, 092002 (2017)

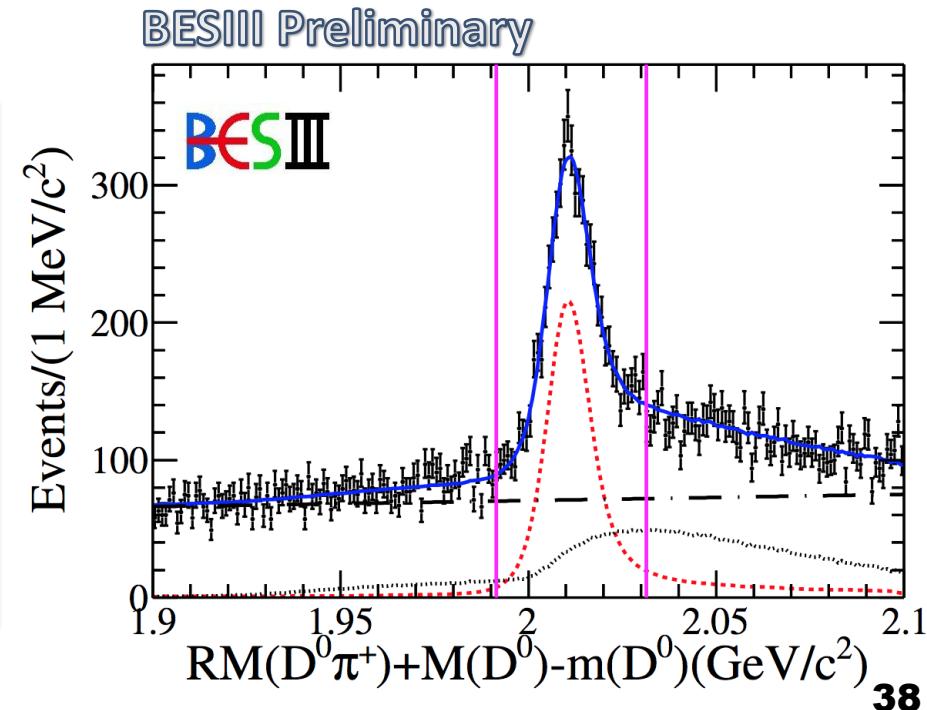


- $M_1 = 4218.4^{+5.5}_{-4.5} \pm 0.9 \text{ MeV}/c^2, \Gamma_1 = 66.0^{+12.3}_{-8.3} \pm 0.4 \text{ MeV} \rightarrow Y(4220)$
- $M_2 = 4391.5^{+6.3}_{-6.8} \pm 1.0 \text{ MeV}/c^2, \Gamma_2 = 139.5^{+16.2}_{-20.6} \pm 0.6 \text{ MeV} \rightarrow Y(4390)$

$$e^+ e^- \rightarrow \pi^+ D^0 D^{*-} + c.c.$$

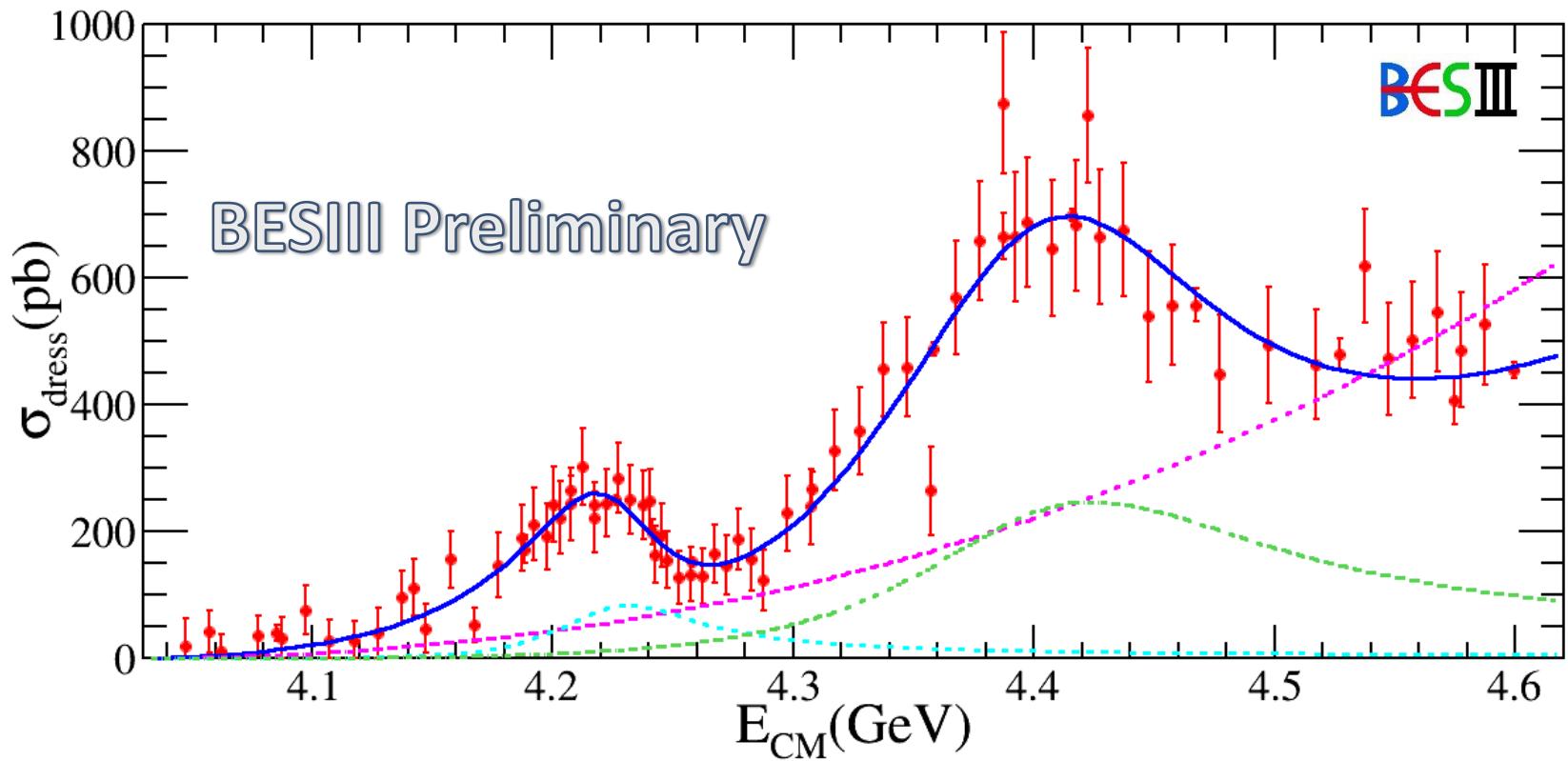
- Reconstruct $D^0 \rightarrow K^- \pi^+$
- Select the combination closest to D^0 mass ($m(D^0)$)
- Find an additional π^+ ;
- $1.9 < M(D^{*-}) (RM(D^0\pi^+) + M(D^0) - m(D^0)) < 2.1 \text{ GeV}/c^2$
- select the candidate closest to D^{*-} mass

- An un-binned maximum likelihood fit
- Signal shape: MC convoluted with a Gaussian;
- The isospin partner background (dotted line) is parameterized with MC;
- A linear function for other bkg



Fit to the dressed cross section of $e^+e^- \rightarrow \pi^+ D^0 D^{*-} + c.c.$

$$\sigma_{dress} = \frac{N^{obs}}{\mathcal{L}(1 + \delta r)B(D^0 \rightarrow K^-\pi^+)\varepsilon} \quad \sigma_{dress}(m) = |c \cdot \sqrt{P(m)} + e^{i\phi_1} B_1(m) \sqrt{\frac{P(m)}{P(M_1)}} + e^{i\phi_2} B_2(m) \sqrt{\frac{P(m)}{P(M_2)}}|^2$$



Fit with a constant (pink dashed triple-dot line) and two constant width relativistic BW functions (green dashed double-dot line and aqua dashed line).

Resonant parameters

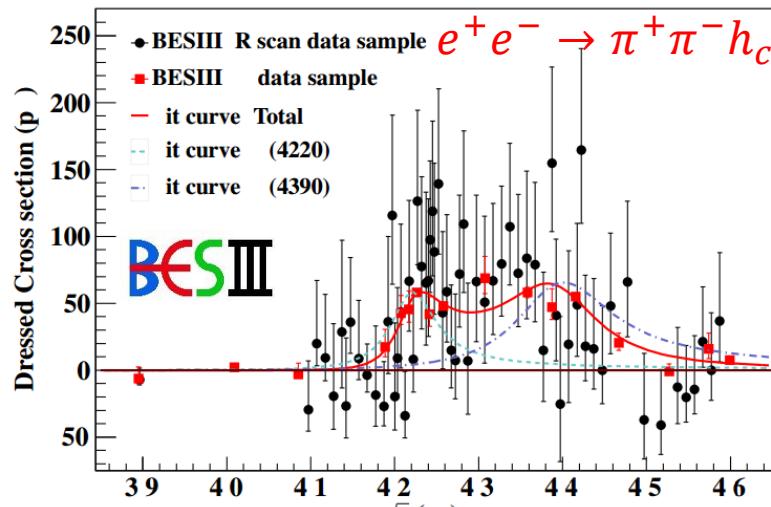
Parameters	SolutionI	SolutionII	SolutionIII	SolutionIV
c (10^{-4})		5.5 ± 0.6		
M_1 (MeV/c^2)		4224.8 ± 5.6		The error are statistical only.
Γ_1 (MeV)		72.3 ± 9.1		BESIII Preliminary
M_2 (MeV/c^2)		4400.1 ± 9.3		BESIII
Γ_2 (MeV)		181.7 ± 16.9		
Γ_1^{el} (eV)	62.9 ± 11.5	7.2 ± 1.8	81.6 ± 15.9	9.3 ± 2.7
Γ_2^{el} (eV)	88.5 ± 15.8	55.3 ± 8.7	551.9 ± 85.3	344.9 ± 70.6
ϕ_1	-2.1 ± 0.1	2.8 ± 0.3	-0.9 ± 0.1	-2.3 ± 0.2
ϕ_2	1.9 ± 0.3	2.3 ± 0.2	2.3 ± 0.1	-1.9 ± 0.1

- Statistical significance is greater than 10σ .
- Consistent with those of Y(4220) and Y(4390) in $e^+e^- \rightarrow \pi^+\pi^- h_c$.

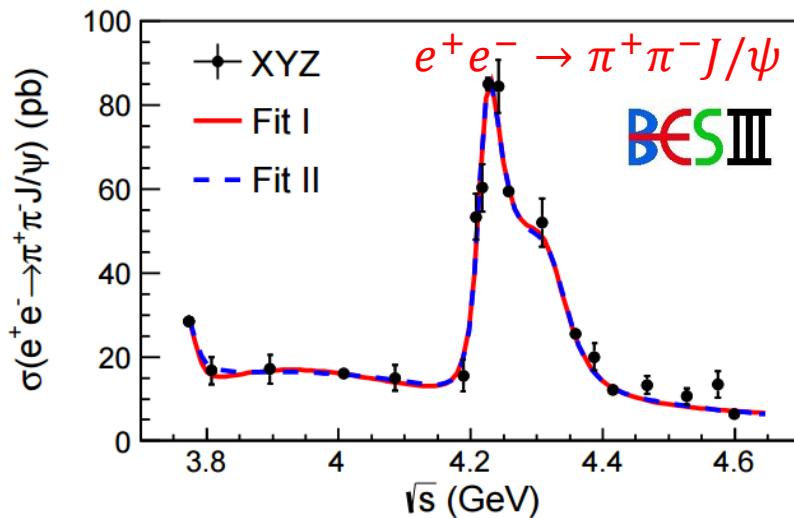
More precise measurements are helpful !

“Y(4260)” in different channels?

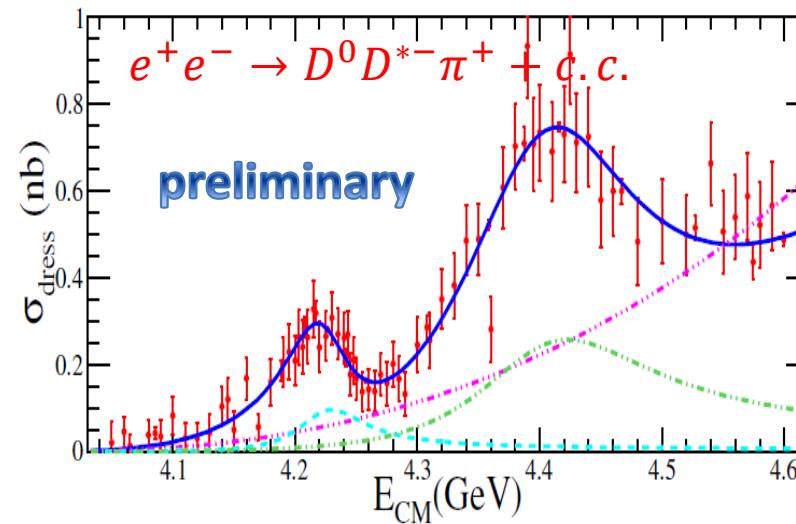
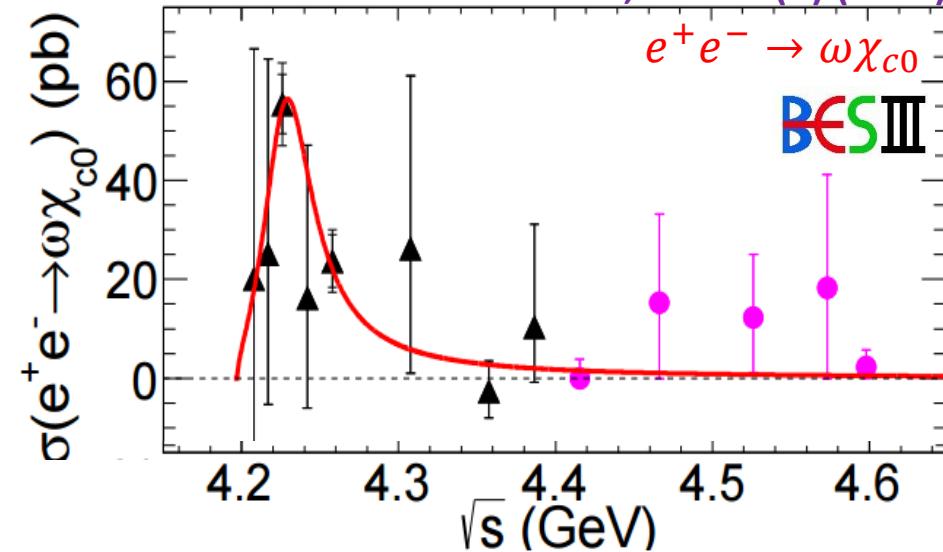
PRL 118, 092002 (2017)



PRL118, 092001 (2017)

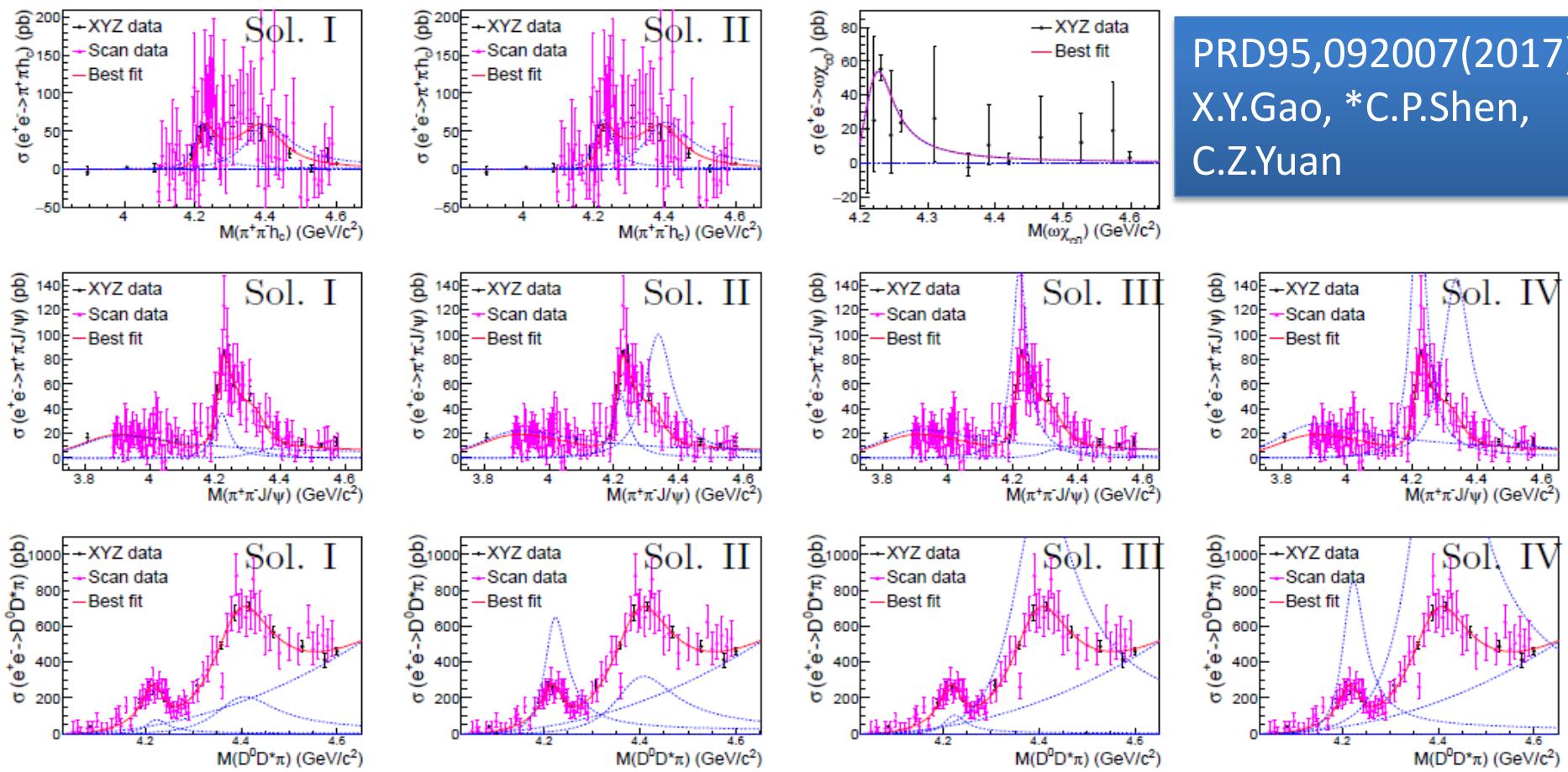


PRD 93, 011102(R) (2016)



All above four channels show a structure at around $4.22 \text{ GeV}/c^2$.

Combined fit to understand the Y(4220) better



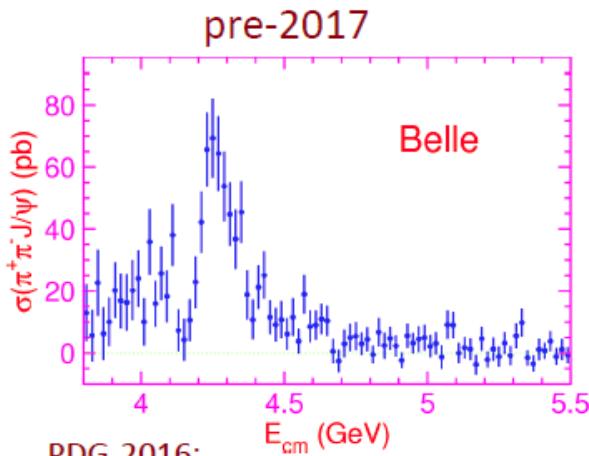
PRD95,092007(2017)
X.Y.Gao, *C.P.Shen,
C.Z.Yuan

$$M = 4219.6 \pm 3.3(\text{stat}) \pm 5.1(\text{sys}) \text{ MeV}/c^2$$

$$\Gamma = 56.0 \pm 3.6(\text{stat}) \pm 6.9(\text{sys}) \text{ MeV}$$

A **combined fit** is performed to extract the resonant parameters of the Y(4220) assuming it decays dominantly to the above four modes and their isospin symmetric modes

$\Upsilon(4260)$: mass \rightarrow lower & width \rightarrow narrower

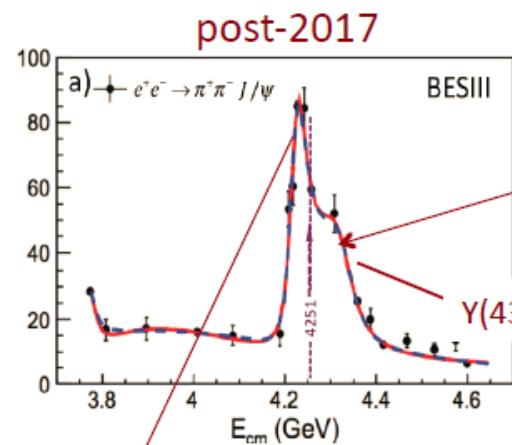


PDG-2016:

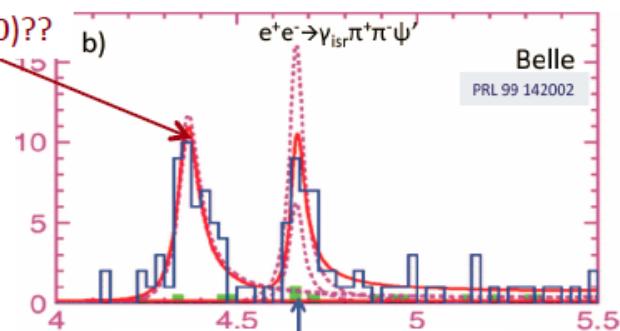
$$M(Y(4260)) = 4251 \pm 9 \text{ MeV}/c^2 \xrightarrow{-31 \text{ MeV}} M_1 = 4220 \pm 4 \text{ MeV}/c^2$$

$$\Gamma(Y(4260)) = 120 \pm 12 \text{ MeV.} \xrightarrow{\times 1/3} \Gamma_1 = 44 \pm 5 \text{ MeV}$$

- $\Upsilon(4220)$ decay modes:
- $\pi^+\pi^-J/\psi$
 - $\pi Z_c(3900)$
 - $f_0(980) J/\psi$
 - $\pi^+\pi^-h_c$
 - $\omega\chi_{c0}$
 - $\eta J/\psi$
 - $\gamma X(3872)$
 - $\pi D\bar{D}^*$



what is the 2nd peak?



$$M_2 = 4320 \pm 13 \text{ MeV}/c^2 \xrightarrow{\delta M \approx -1.8 \text{ GeV}} M(Y(4360)) = 4346 \pm 6 \text{ MeV}/c^2$$

$$\Gamma_2 = 101^{+27}_{-22} \text{ MeV} \xrightarrow{\text{spot on}} \Gamma(Y(4360)) = 102 \pm 12 \text{ MeV.}$$

- $\Upsilon(4320)$ decay modes:
- $\pi^+\pi^-J/\psi$
 - $\pi^+\pi^-\psi'$

What is the Y(4260)?

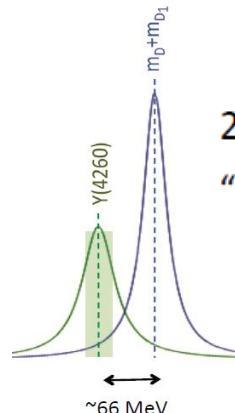
The Y(4260) mass is lower and width narrower than previously thought

"Y(4260)" \rightarrow Y(4220)?

If it is a $D\bar{D}_1(2420)$ molecule:

B.E. ≈ 66 MeV \leftarrow too large??

"affinity" to $D\bar{D}_1(2420)$ should be high



2012 LQCD calc. ($m_\pi \approx 400$ MeV):

"Lowest 1^{--} $c\bar{c}$ -gluon hybrid: $M=4285 \pm 14$ MeV"

pre-2017: too high by ~ 35 MeV
post-2017: too high by ~ 65 MeV

Had. Spectr. Collab. JHEP07, 126

If it is a $c\bar{c}$ -gluon hybrid:

its mass is ~ 65 MeV below current ($m_\pi \approx 400$ MeV) LQCD predictions \leftarrow not so bad?

"affinity" to $D\bar{D}_0(2400)$ should be high

If it is a QCD diquark-dantiquark tetraquark: Maiani et al. PRD89,114010

it should have Isospin- & $SU_c(3)$ -multiplet partner states \leftarrow not seen

Dubynskiy & Voloshin, PLB 666, 344

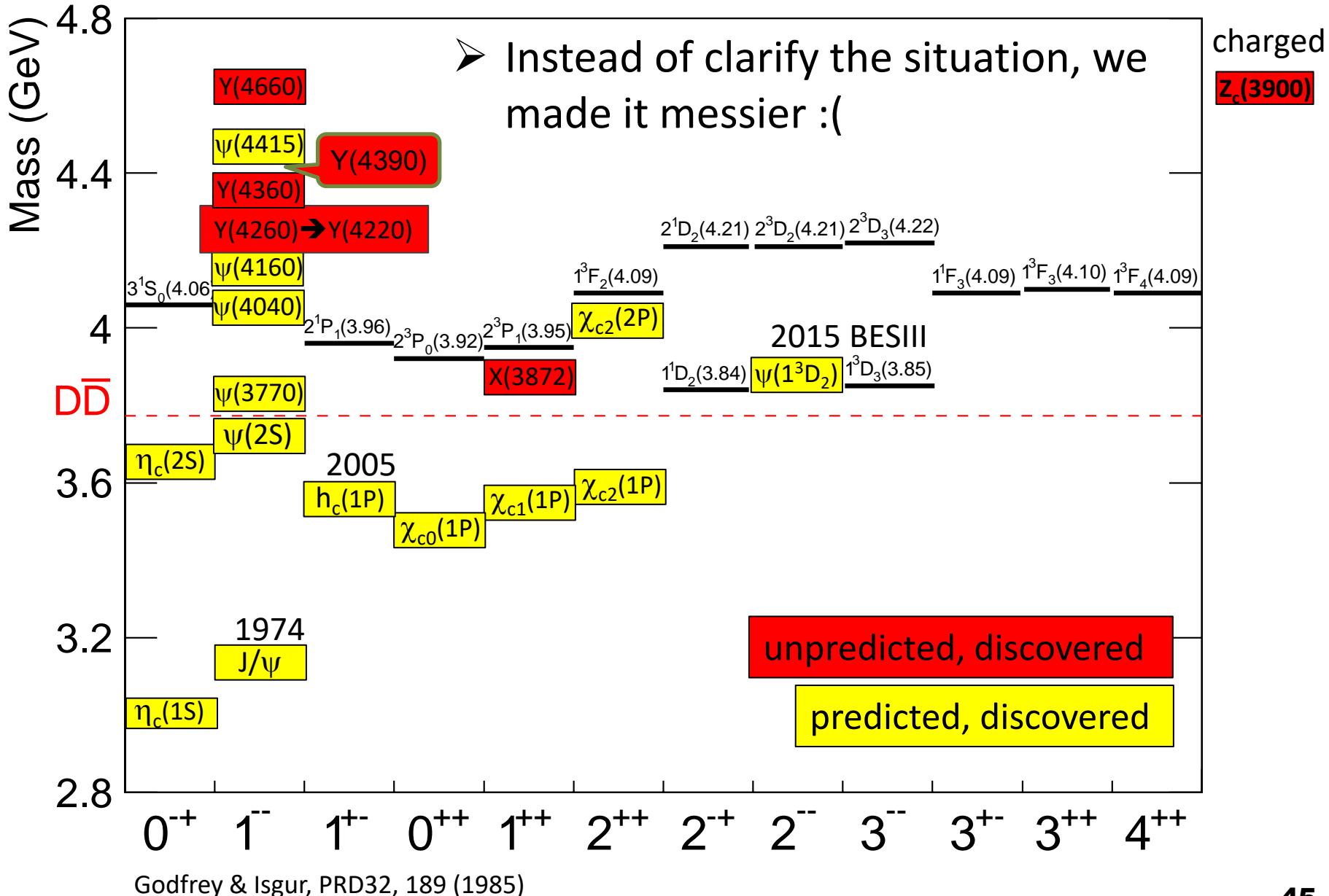
If it is hadrocharmonium:

Li & Voloshin, Mod. Phys. Lett. A29, 1450060

decays to non-J/ $\psi(h_c)$ charmonium states should be suppressed \leftarrow they aren't

BESIII is well suited to further investigate this intriguing puzzle \leftarrow a "Y(4260)" factory

Charmonium(like) spectroscopy



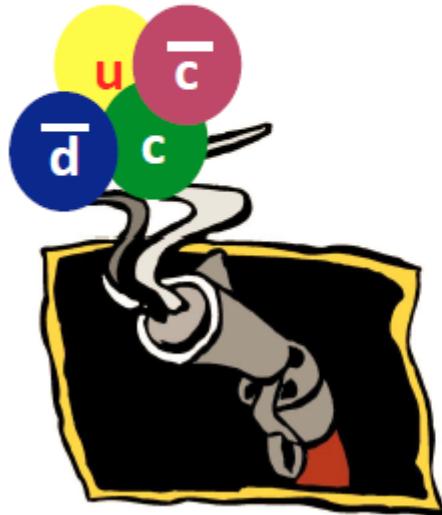
Z States

Zc(3900), Zc(4020), Zb(10610), Zb(10650), ...

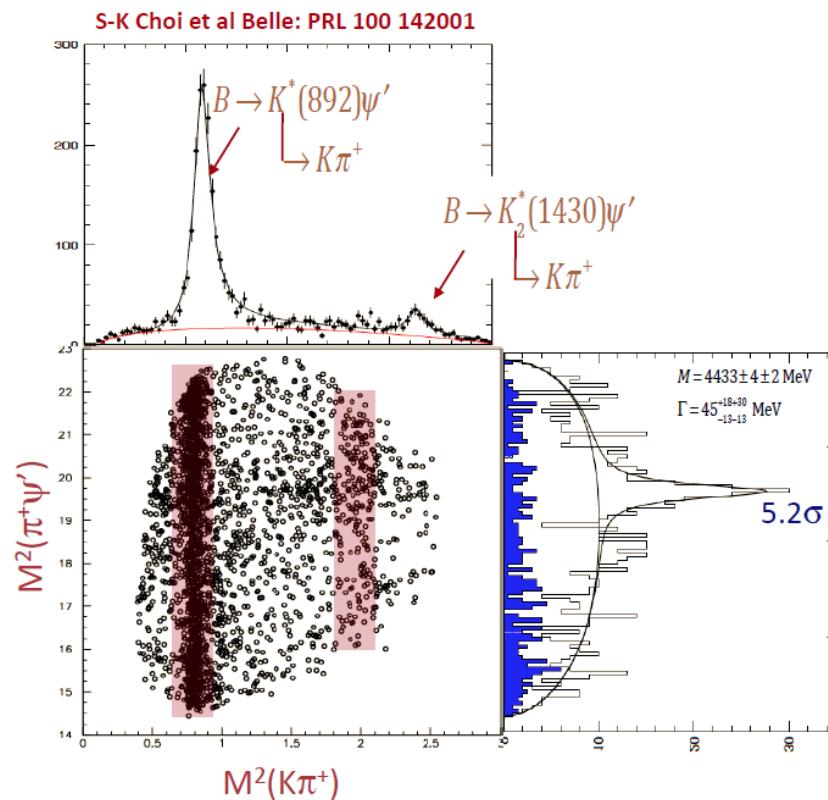
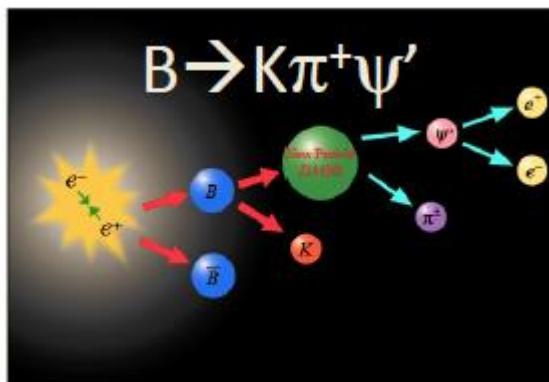
Observed in B decays and in decays of Y states

The $Z(4430)^+ \rightarrow \pi^+ \psi'$

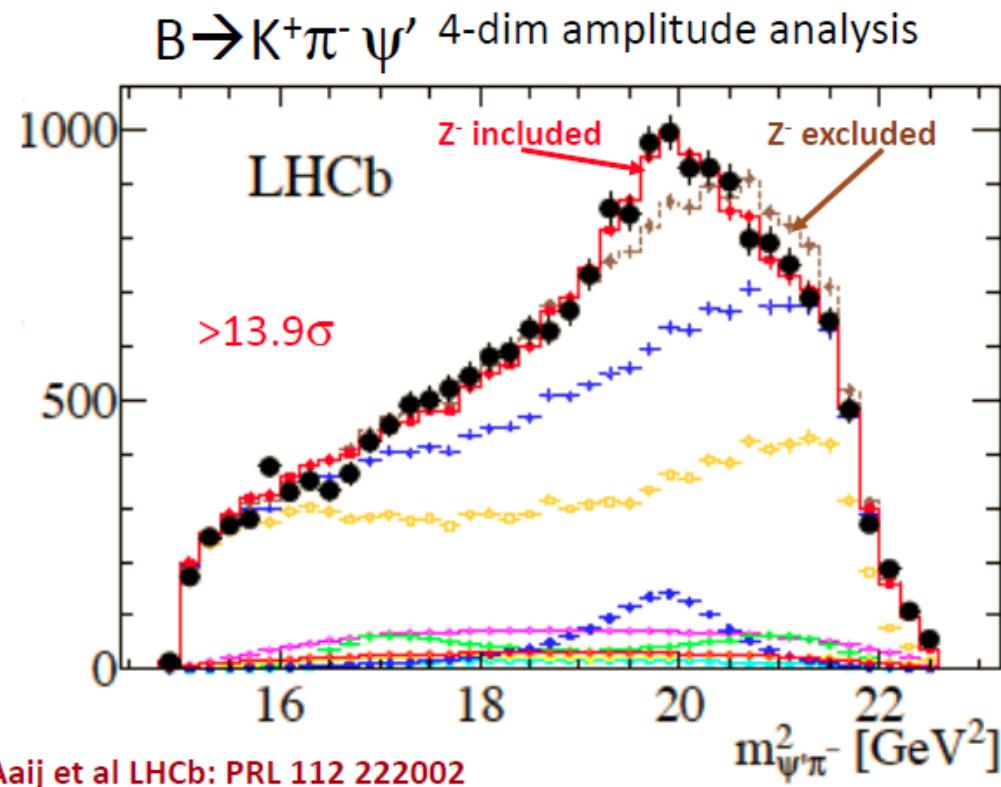
"smoking gun" evidence for a 4-quark meson



- decays to ψ' → must contain $c\bar{c}$ pair
- electrically charged → must contain $u\bar{d}$ pair



LHCb 4-dim analysis of $B \rightarrow K^+ \pi^- \psi'$



$$J^P = 1^+$$

$$M = 4475 \pm 7^{+15}_{-25} \text{ MeV}$$

$$\Gamma = 172 \pm 13^{+37}_{-34} \text{ MeV}$$

Good agreement with Belle,
(with smaller errors)

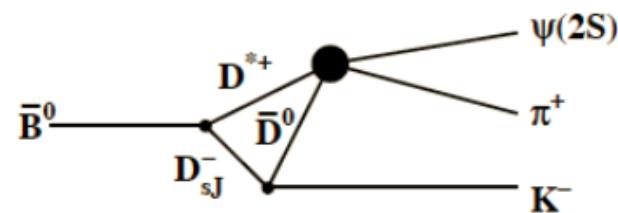
$$Bf(B^0 \rightarrow Z(4430)^- K^+) \times Bf(Z(4430)^- \rightarrow \pi^- \psi') \approx (3.4^{-1.1}_{-2.3}) \times 10^{-5}$$

What is the Z(4430)?

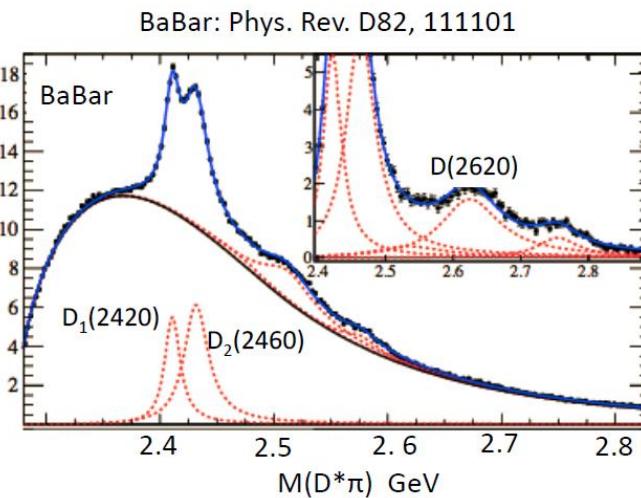
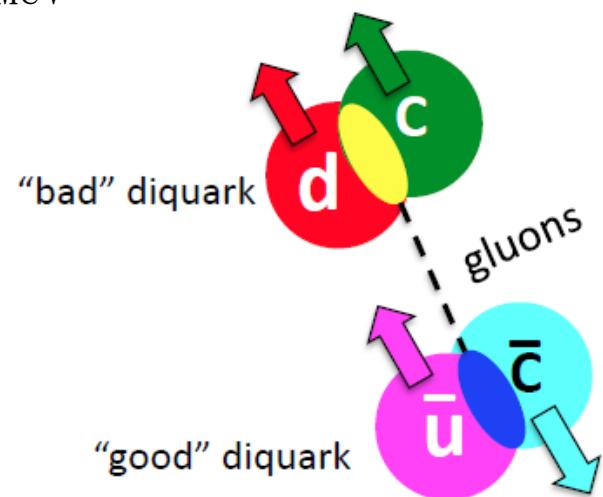
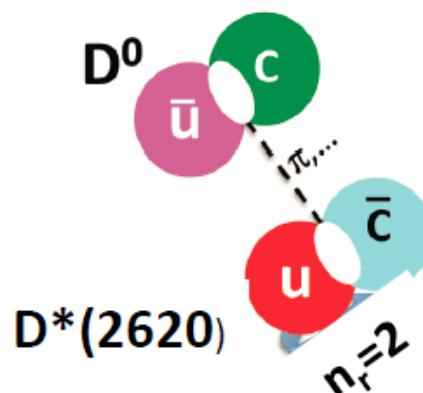
Kinematic effect due
to $D^*\bar{D}$ rescattering?

$D^*(2S)\bar{D}$ molecule?
Binding energy = 20 ± 30 MeV

tetraquark formed with a
radially excited diquark



Pakhlov & Uglov, PLB 183 (2015)

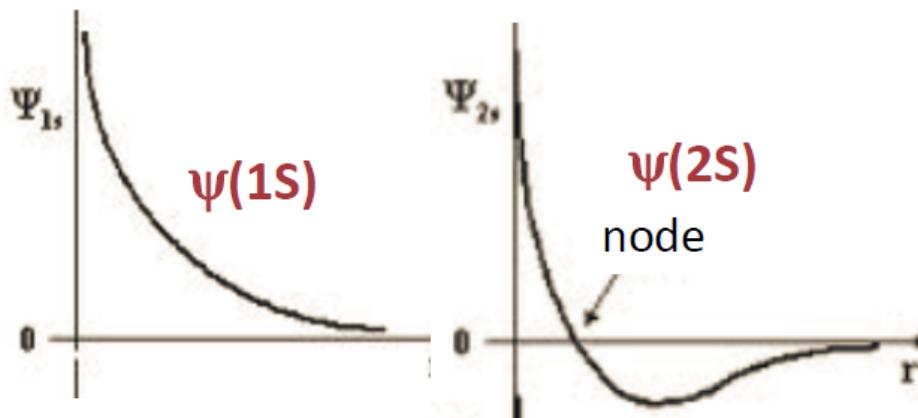


one of the diquarks is
is in an $n_r=2$, radially
excited state.

$Z(4430) = \text{radial excitation of } Z_c(3900)?$

$$\frac{\mathcal{B}(Z_c(4430)^+ \rightarrow \psi(2S)\pi^+)}{\mathcal{B}(Z_c(4430)^+ \rightarrow J/\psi\pi^+)} \sim 10$$

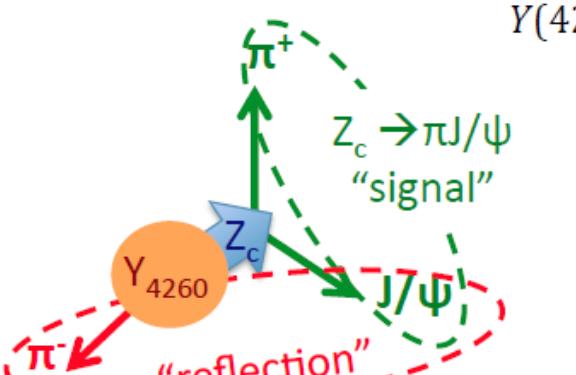
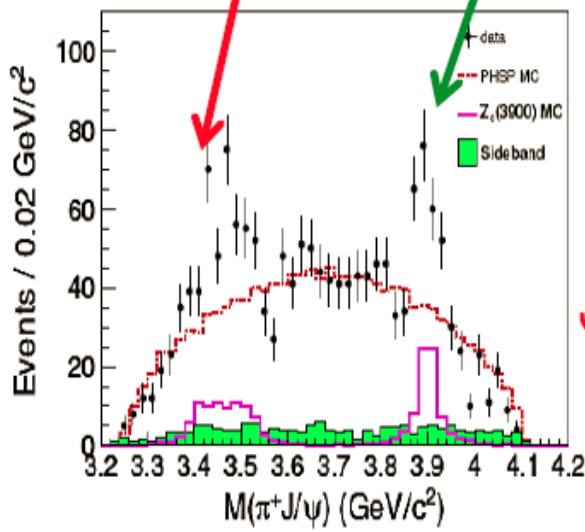
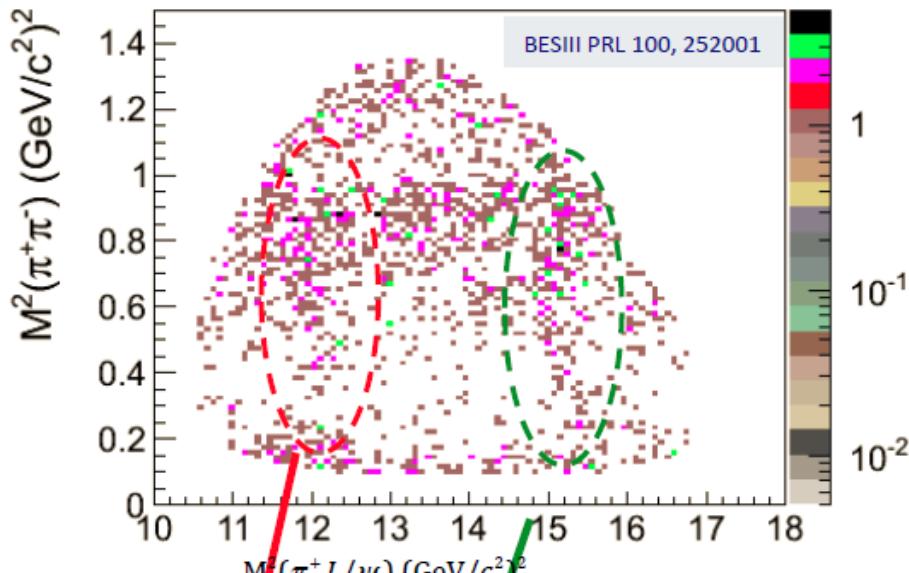
Radial Wave Functions



The $c\bar{c}$ part of the wave function of the $Z(4430)$ likely has a node \rightarrow a radial excitation of the ground state: the $Z_c(3900)$?

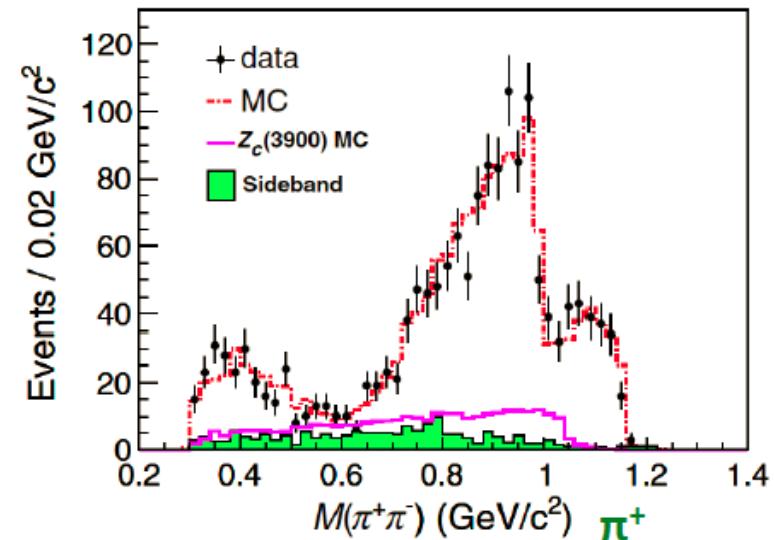
$$\begin{aligned} M(Z_c(4430)) - M(Z_c(3900)) &= 589 \pm 30 \text{ MeV} \\ M(\psi') - M(J/\psi) &= 589 \text{ MeV} \end{aligned}$$

$e^+e^- \rightarrow \pi^+\pi^- J/\psi$ “Dalitz plot”



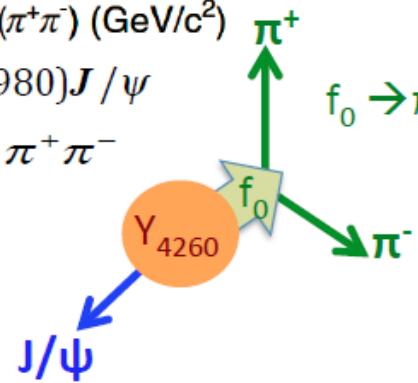
$$Y(4260) \rightarrow \pi^\pm Z_c^\mp(3900)$$

$\downarrow \pi^\pm J/\psi$



$$Y(4260) \rightarrow f_0(980)J/\psi$$

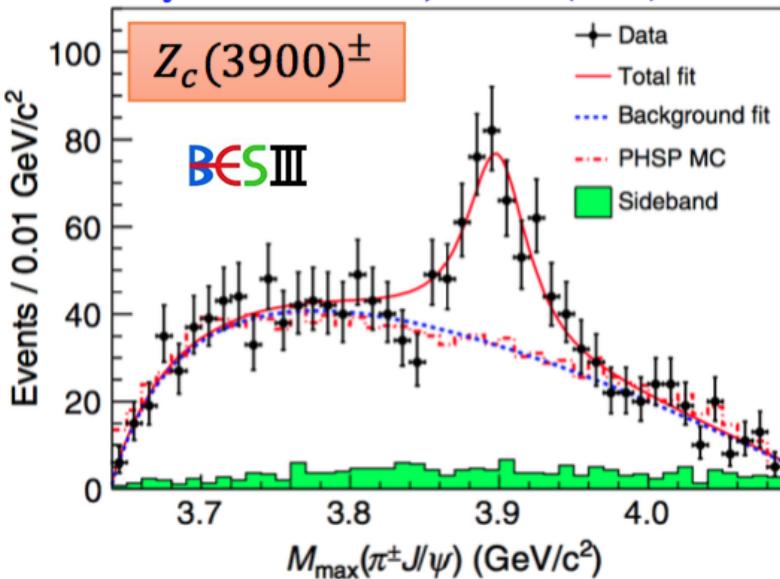
$\downarrow \pi^+\pi^-$



$Z_c(3900)$ State

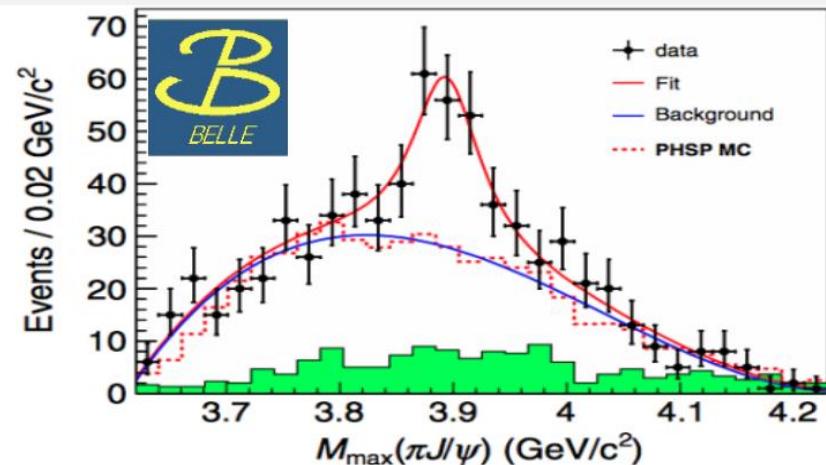
Observed in $e^+e^- \rightarrow (\gamma)\Upsilon(4260) \rightarrow J/\psi\pi^+\pi^-$

Phys. Rev. Lett 110, 252001 (2013)

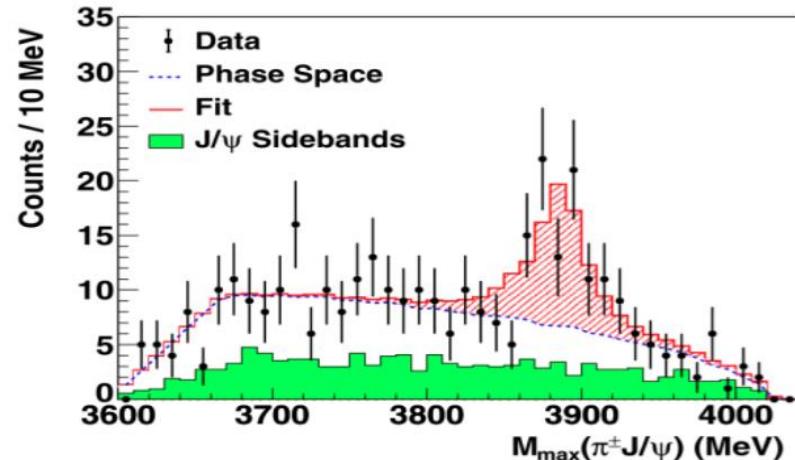


- Charged charmonium-like structure ($>10\sigma$)
- Decay to J/ψ ($c\bar{c}$) and electric charge ($u\bar{d}$ or $d\bar{u}$)
- $M = 3899.0 \pm 3.6 \pm 4.9 \text{ MeV}/c^2$, $\Gamma = 46 \pm 10 \pm 20 \text{ MeV}$
- $\sigma(e^+e^- \rightarrow \pi^+\pi^- J/\psi) = 62.9 \pm 1.9 \pm 3.7 \text{ pb}$ at 4.26 GeV
- $\frac{\sigma(e^+e^- \rightarrow \pi^\mp Z_c(3900)^\pm \rightarrow \pi^+\pi^- J/\psi)}{\sigma(e^+e^- \rightarrow \pi^+\pi^- J/\psi)} = 21.5 \pm 3.3 \pm 7.5 \%$
- The first Z_c state observed by more than one experiment (Belle and CLEO-c)!

Belle with ISR data (PRL 110, 252002)

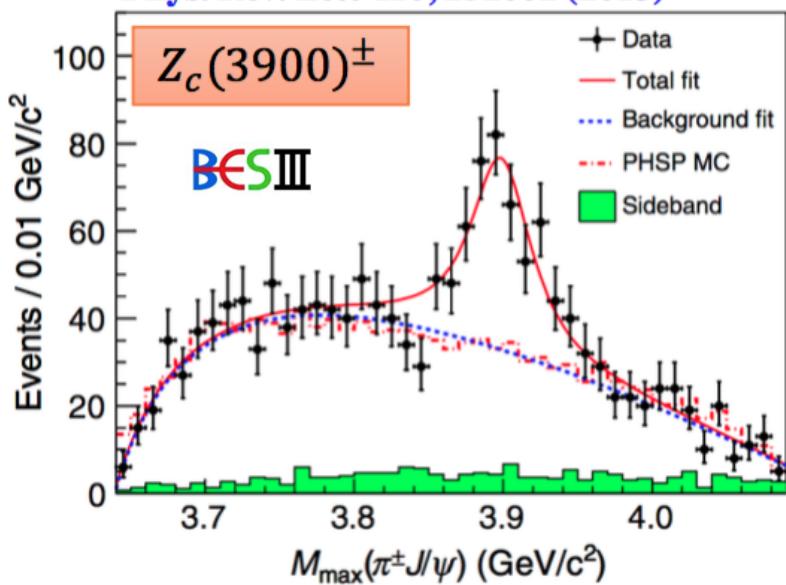


CLEOc data at 4.17 GeV (PLB 727, 366)



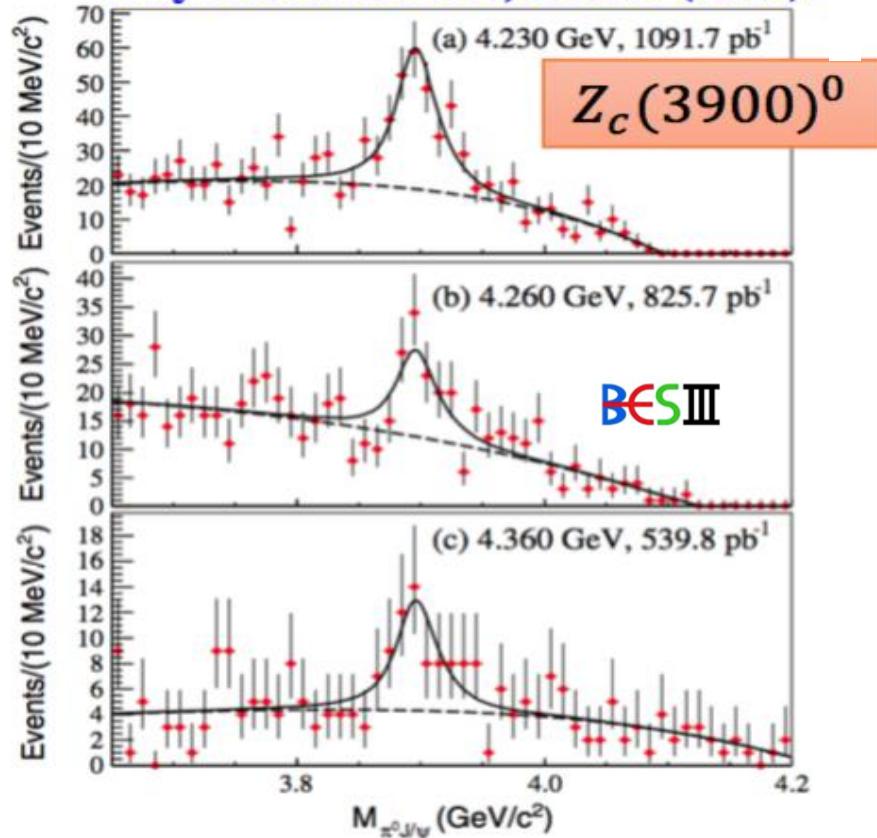
Z_c(3900) State

Phys. Rev. Lett 110, 252001 (2013)



- Charged charmonium-like structure (>10 σ)
- Decay to J/ψ (c̄c) and electric charge (ūd or d̄u)
- M = 3899.0 ± 3.6 ± 4.9 MeV/c², Γ = 46 ± 10 ± 20 MeV
- σ(e⁺e⁻ → π⁺π⁻J/ψ) = 62.9 ± 1.9 ± 3.7 pb at 4.26 GeV
- $\frac{\sigma(e^+e^- \rightarrow \pi^\mp Z_c(3900)^\pm \rightarrow \pi^+\pi^-J/\psi)}{\sigma(e^+e^- \rightarrow \pi^+\pi^-J/\psi)} = 21.5 \pm 3.3 \pm 7.5 \%$
- The first Z_c state observed by more than one experiment (Belle and CLEO-c)!

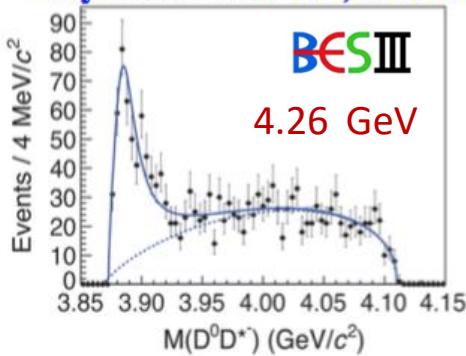
Phys. Rev. Lett 115, 112003 (2015)



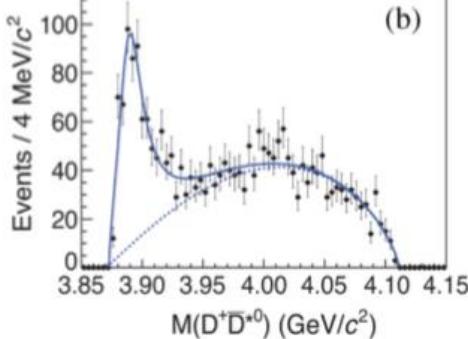
- Neutral charmonium-like structure (10.4 σ)
- Using 3 data samples (~2.5 fb⁻¹)
- Evidence with 3.7σ by using CLEO-c data
- M = 3894.8 ± 2.3 ± 3.2 MeV/c², Γ = 29.6 ± 8.2 ± 8.2 MeV
- An iso-spin triplet is established!

$Z_c(3900)$ State

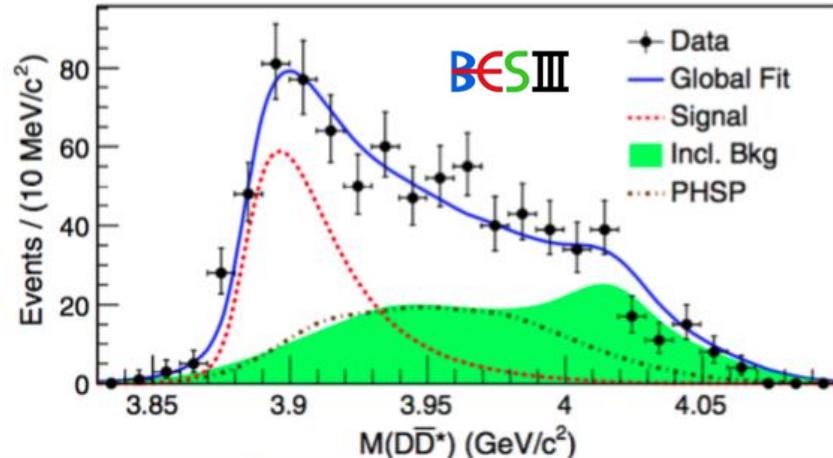
Phys. Rev. Lett 112, 022001 (2014)



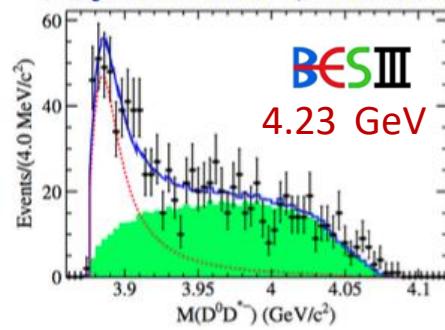
Single D tag (ST)



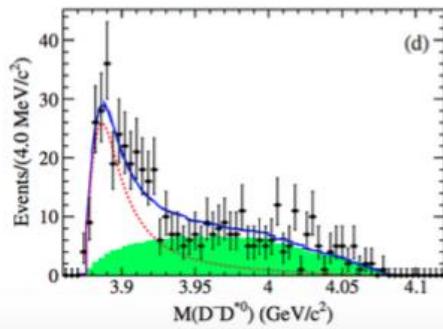
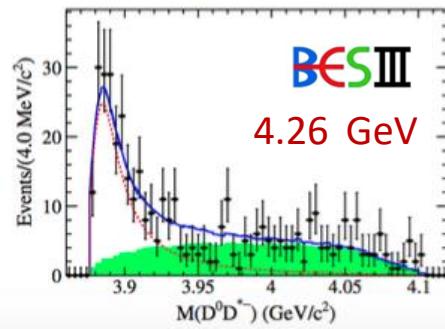
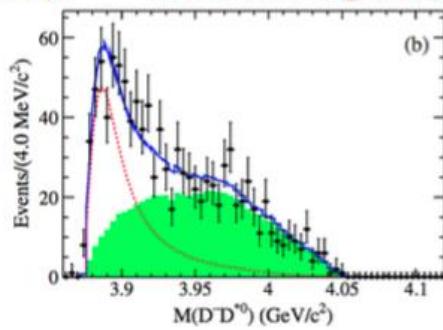
Double D tag (DT)



Phys. Rev. D 92, 092006 (2015)



Double D tag (DT)

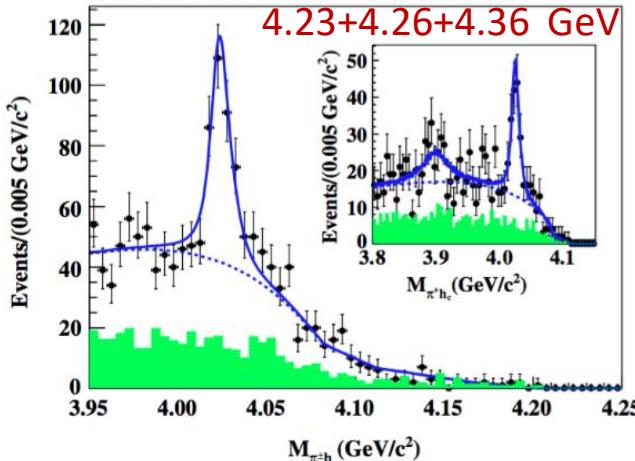


State	Mass (MeV/c ²)	Width (MeV)
$Z_c(3885)^\pm$ (ST)	$3883.9 \pm 1.5 \pm 4.2$	$24.8 \pm 3.3 \pm 11.0$
$Z_c(3885)^\pm$ (DT)	$3881.7 \pm 1.6 \pm 1.6$	$26.6 \pm 2.0 \pm 2.1$
Weighted average	$3882.2 \pm 1.1 \pm 1.5$	$26.5 \pm 1.7 \pm 2.1$
$Z_c(3885)^0$ (DT)	$3885.7^{+4.3}_{-5.7} \pm 8.4$	$35^{+11}_{-12} \pm 15$

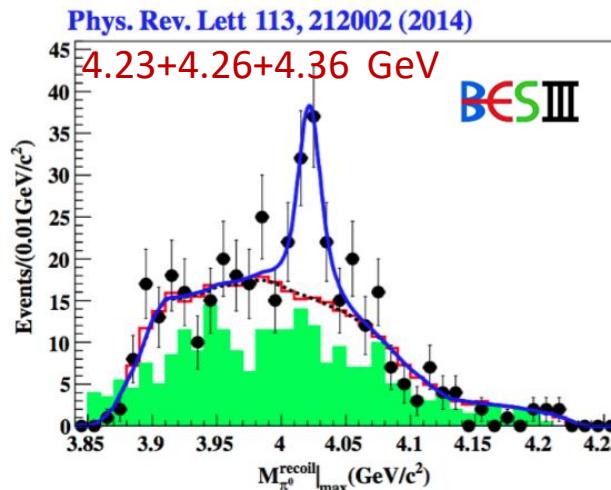
- Good agreement between ST and DT method
- Good agreement between charged state and neutral state
- Another iso-spin triplet is established!
- $Z_c(3885) = Z_c(3900)$?
- Tetraquark? Molecule state?

$Z_c(4020)$ & $Z_c(4025)$ States

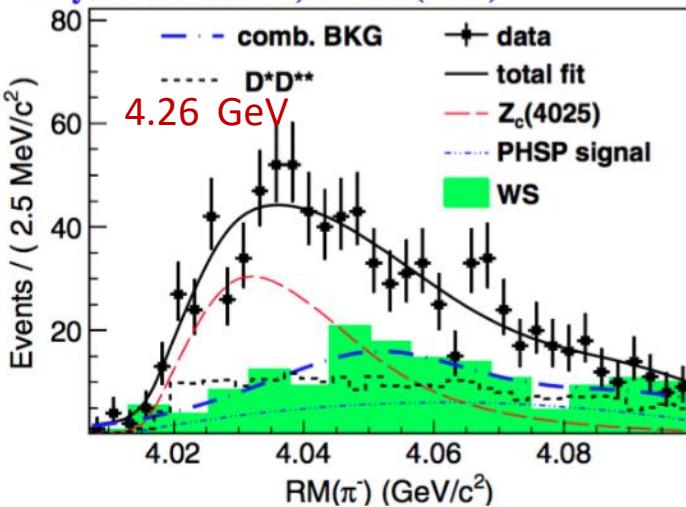
Phys. Rev. Lett 111, 242001 (2013)



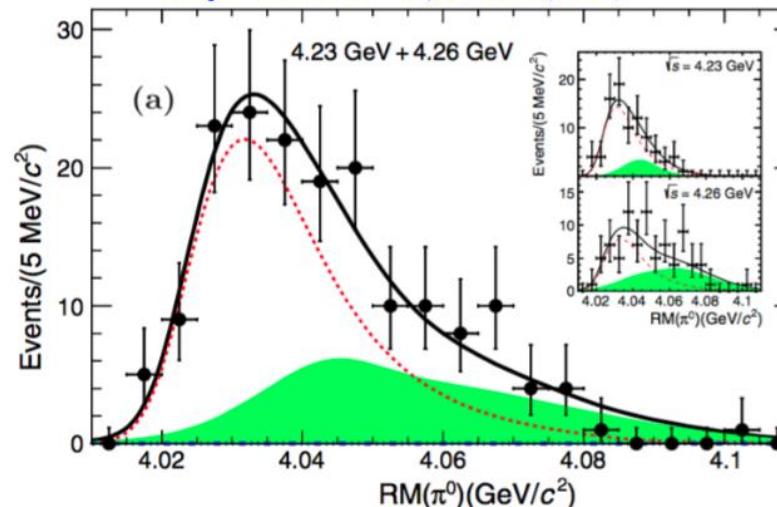
Phys. Rev. Lett 113, 212002 (2014)



Phys. Rev. Lett 112, 132001 (2014)



Phys. Rev. Lett 115, 182002 (2015)



➤ $Z_c(4020)^{\pm/0}$ observed

➤ Another iso-spin triplet is established!

➤ $Z_c(4020)^{\pm/0}$ observed

➤ Another iso-spin triplet is established!

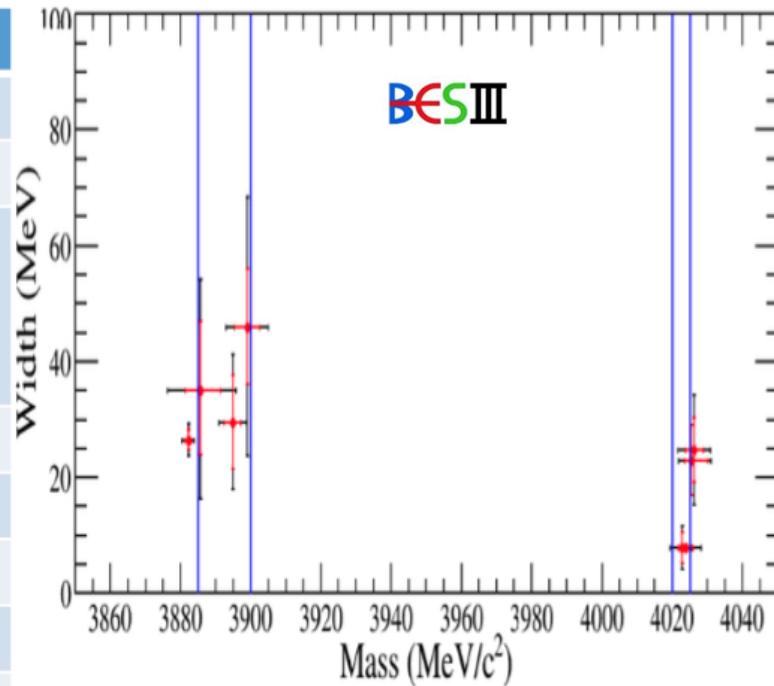
➤ No significant $Z_c(3900)^{\pm} \rightarrow \pi^{\pm} h_c$ is observed

State	Mass (MeV/c ²)	Width (MeV)
$Z_c(4020)^{\pm}$	$4022.9 \pm 0.8 \pm 2.7$	$7.9 \pm 2.7 \pm 2.6$
$Z_c(4020)^0$	$4023.9 \pm 2.2 \pm 3.8$	7.9 (fixed)

State	Mass (MeV/c ²)	Width (MeV)
$Z_c(4025)^{\pm}$	$4026.3 \pm 2.6 \pm 3.7$	$24.8 \pm 5.6 \pm 7.7$
$Z_c(4025)^0$	$4025.5^{+2.0}_{-4.7} \pm 3.1$	$23.0 \pm 6.0 \pm 1.0$

Summary on Z_c States by BESIII

State	Mass (MeV/c ²)	Width (MeV)	Process
$Z_c(3900)^{\pm}$	$3899.0 \pm 3.6 \pm 4.9$	$46 \pm 10 \pm 20$	$e^+ e^- \rightarrow \pi^+ \pi^- J/\psi$
$Z_c(3900)^0$	$3894.8 \pm 2.3 \pm 3.2$	$29.6 \pm 8.2 \pm 8.2$	$e^+ e^- \rightarrow \pi^0 \pi^0 J/\psi$
$Z_c(3885)^{\pm}$ (ST)	$3883.9 \pm 1.5 \pm 4.2$	$24.8 \pm 3.3 \pm 11.0$	
$Z_c(3885)^{\pm}$ (DT)	$3881.7 \pm 1.6 \pm 1.6$	$26.6 \pm 2.0 \pm 2.1$	$e^+ e^- \rightarrow \pi^\mp (D\bar{D}^*)^\pm$
Weighted average	$3882.2 \pm 1.1 \pm 1.5$	$26.5 \pm 1.7 \pm 2.1$	
$Z_c(3885)^0$ (DT)	$3885.7^{+4.3}_{-5.7} \pm 8.4$	$35^{+11}_{-12} \pm 15$	$e^+ e^- \rightarrow \pi^0 (D\bar{D}^*)^0$
$Z_c(4020)^{\pm}$	$4022.9 \pm 0.8 \pm 2.7$	$7.9 \pm 2.7 \pm 2.6$	$e^+ e^- \rightarrow \pi^+ \pi^- h_c$
$Z_c(4020)^0$	$4023.9 \pm 2.2 \pm 3.8$	7.9 (fixed)	$e^+ e^- \rightarrow \pi^0 \pi^0 h_c$
$Z_c(4025)^{\pm}$	$4026.3 \pm 2.6 \pm 3.7$	$24.8 \pm 5.6 \pm 7.7$	$e^+ e^- \rightarrow \pi^\mp (D^* \bar{D}^*)^\pm$
$Z_c(4025)^0$	$4025.5^{+2.0}_{-4.7} \pm 3.1$	$23.0 \pm 6.0 \pm 1.0$	$e^+ e^- \rightarrow \pi^0 (D^* \bar{D}^*)^0$

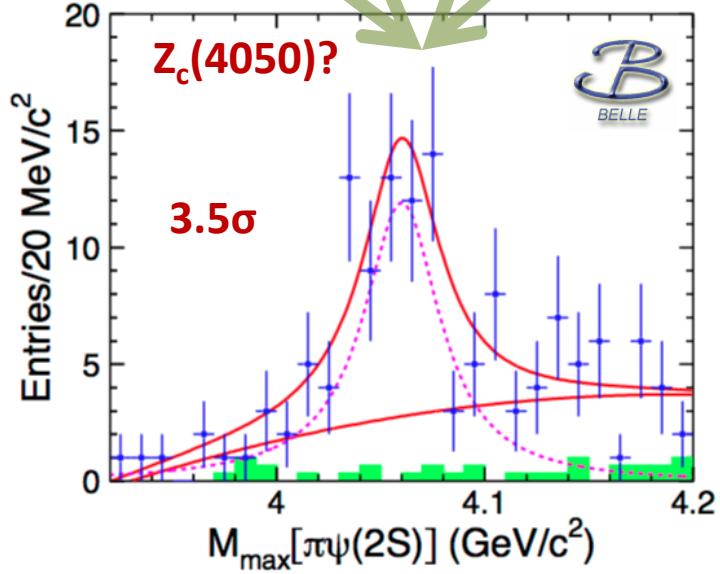
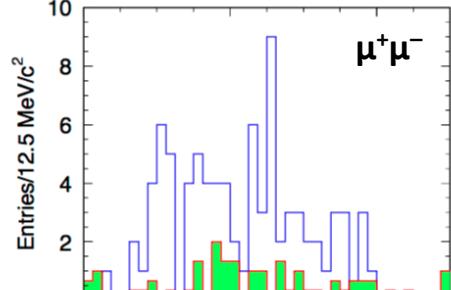
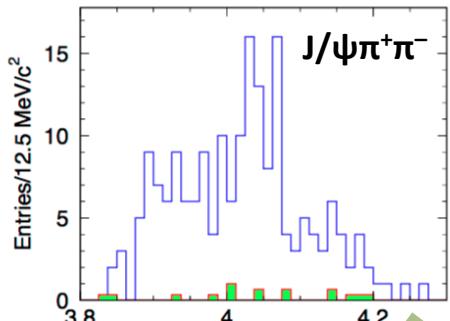


- $Z_c(3885)^{\pm}$ mass is about 2.6σ lower and the width 1.5σ lower than $Z_c(3900)^{\pm}$ value. If $Z_c(3885) = Z_c(3900)$, $\frac{\Gamma(Z_c(3885)^{\pm} \rightarrow (D\bar{D}^*)^{\pm})}{\Gamma(Z_c(3900)^{\pm} \rightarrow \pi^{\pm} J/\psi)} = 6.2 \pm 1.1 \pm 2.7$, coupling to $D\bar{D}^*$ is larger than to $\pi J/\psi$;
- $Z_c(4020)^{\pm}$ and $Z_c(4025)^{\pm}$ mass and width are consistent within 1.5σ . If $Z_c(4020) = Z_c(4025)$, $\frac{\Gamma(Z_c(4025)^{\pm} \rightarrow (D^* \bar{D}^*)^{\pm})}{\Gamma(Z_c(4020)^{\pm} \rightarrow \pi^{\pm} h_c)} = 12 \pm 5$, coupling to $D^* \bar{D}^*$ is larger than to πh_c .

$Z_c(4050)$

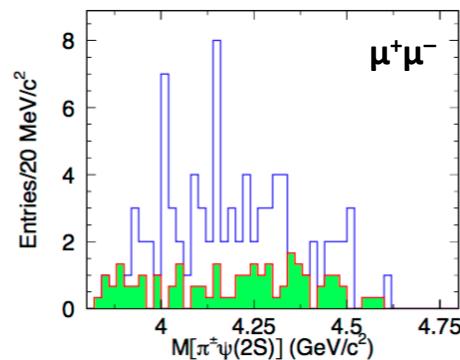
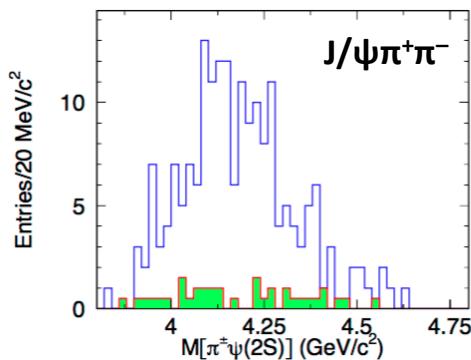
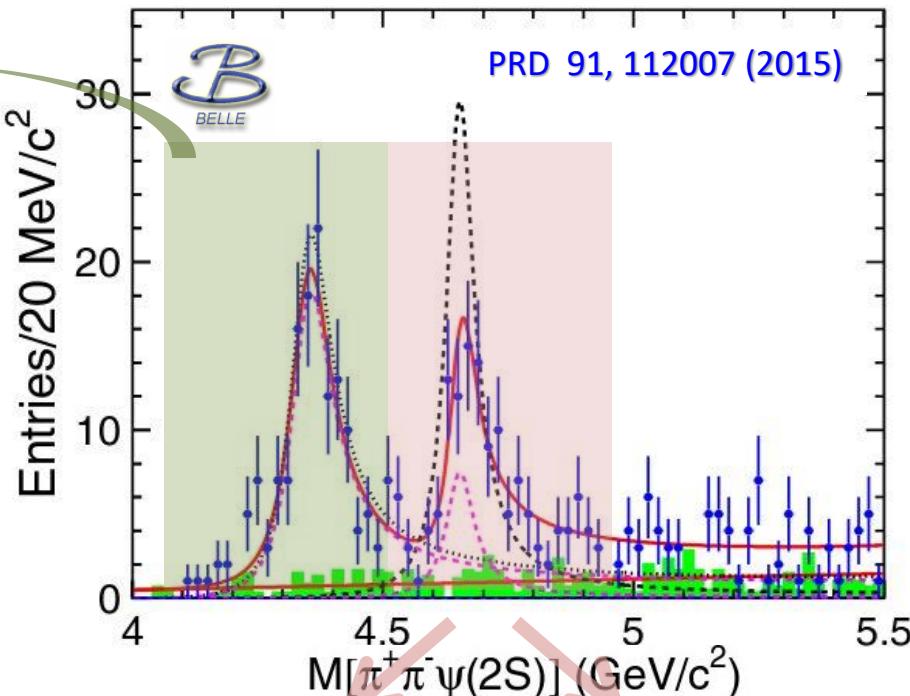
Observed by Belle in ISR

$$e^+e^- \rightarrow Y(4360) \rightarrow \Psi(2S)\pi^+\pi^-$$



$$M = 4054 \pm 3 \pm 1 \text{ MeV}/c^2$$

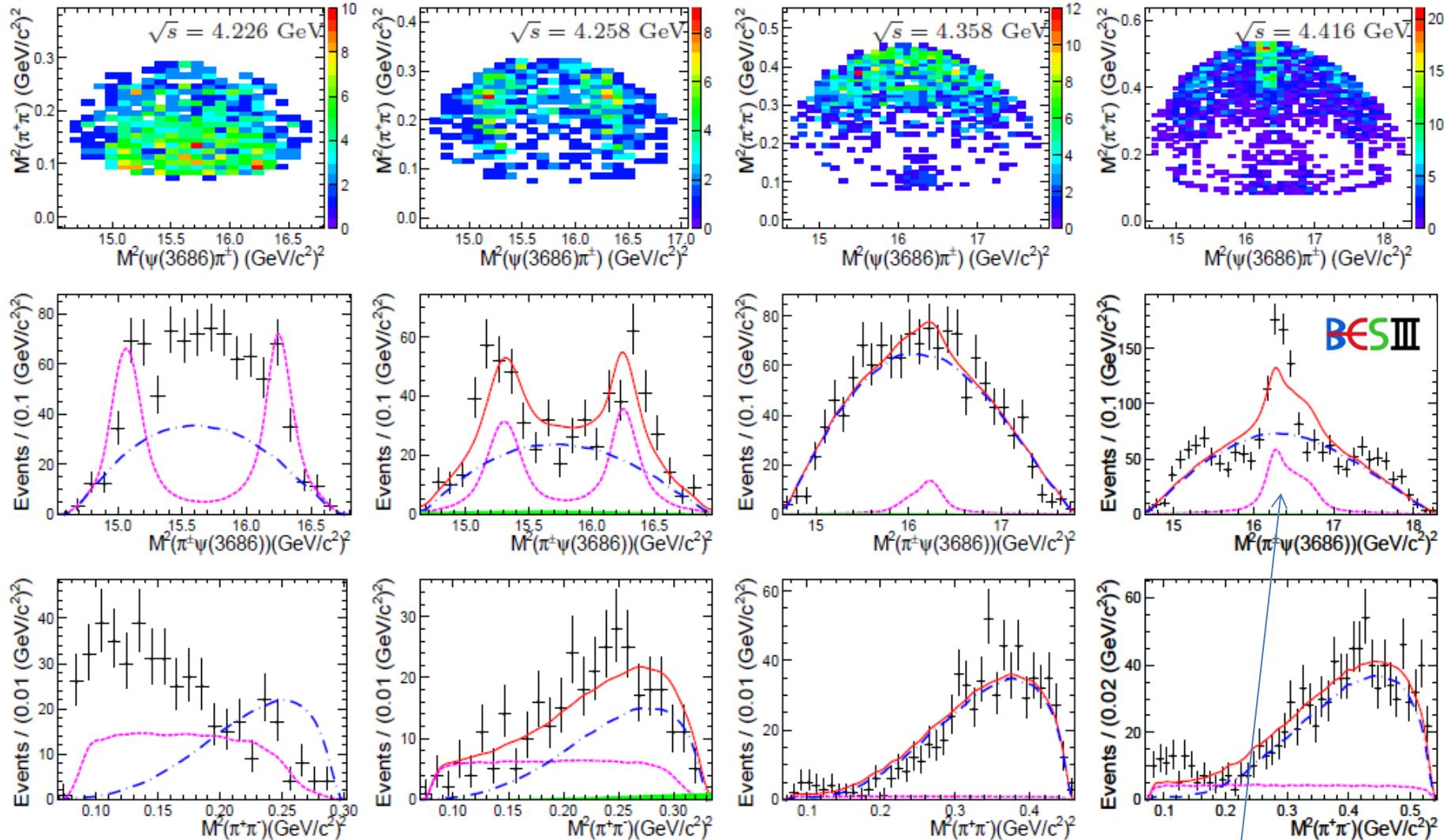
$$\Gamma = 45 \pm 11 \pm 6 \text{ MeV}$$



No clear signal found in the $Y(4660)$ region

Another Z_c state? Need confirmation

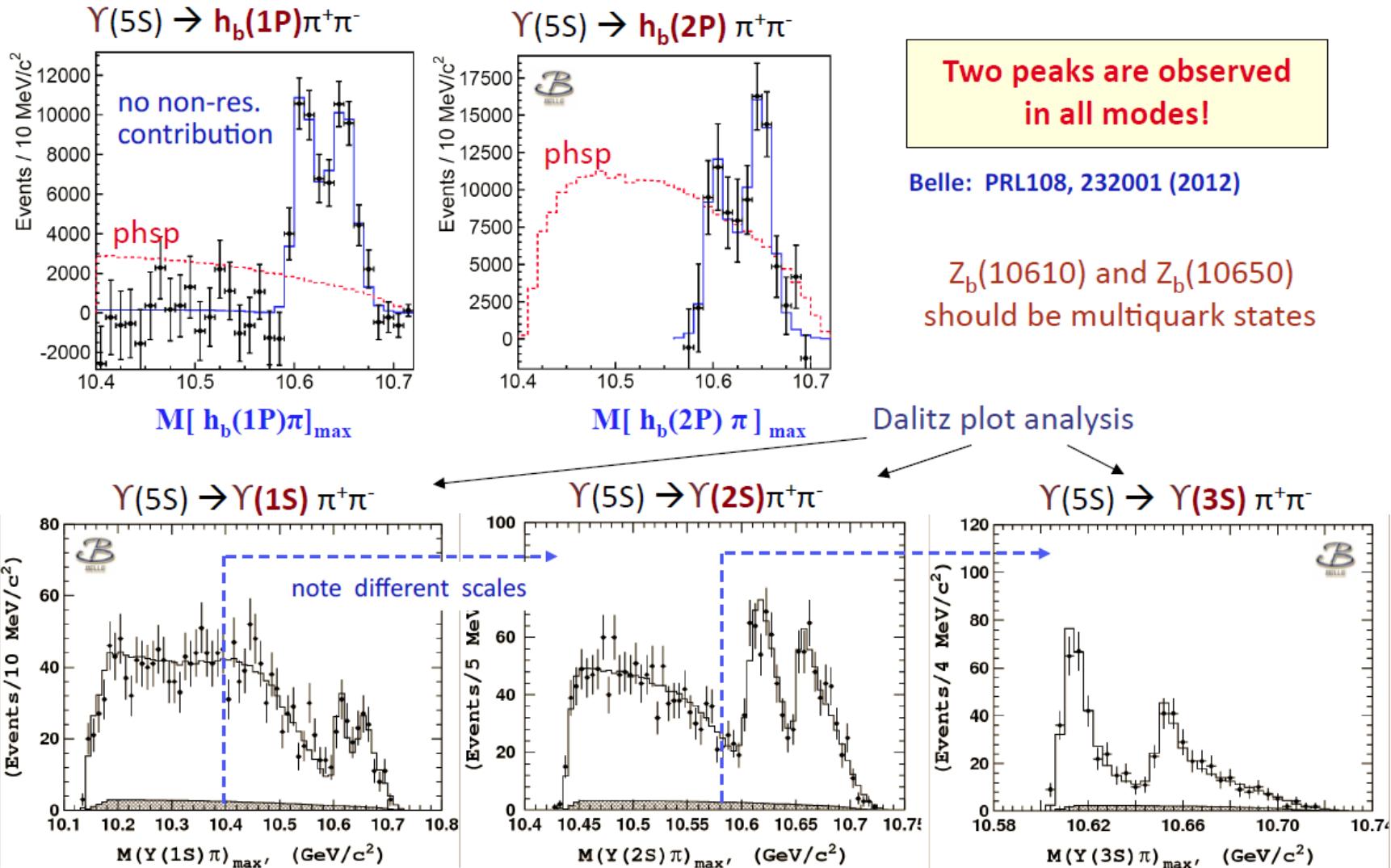
Search for $Z_c \rightarrow \pi\psi(2S)$ at BESIII



**Not like $\pi J/\psi$, the structures in $\pi\psi(2S)$ vs.
Ecm are much more complicated !**

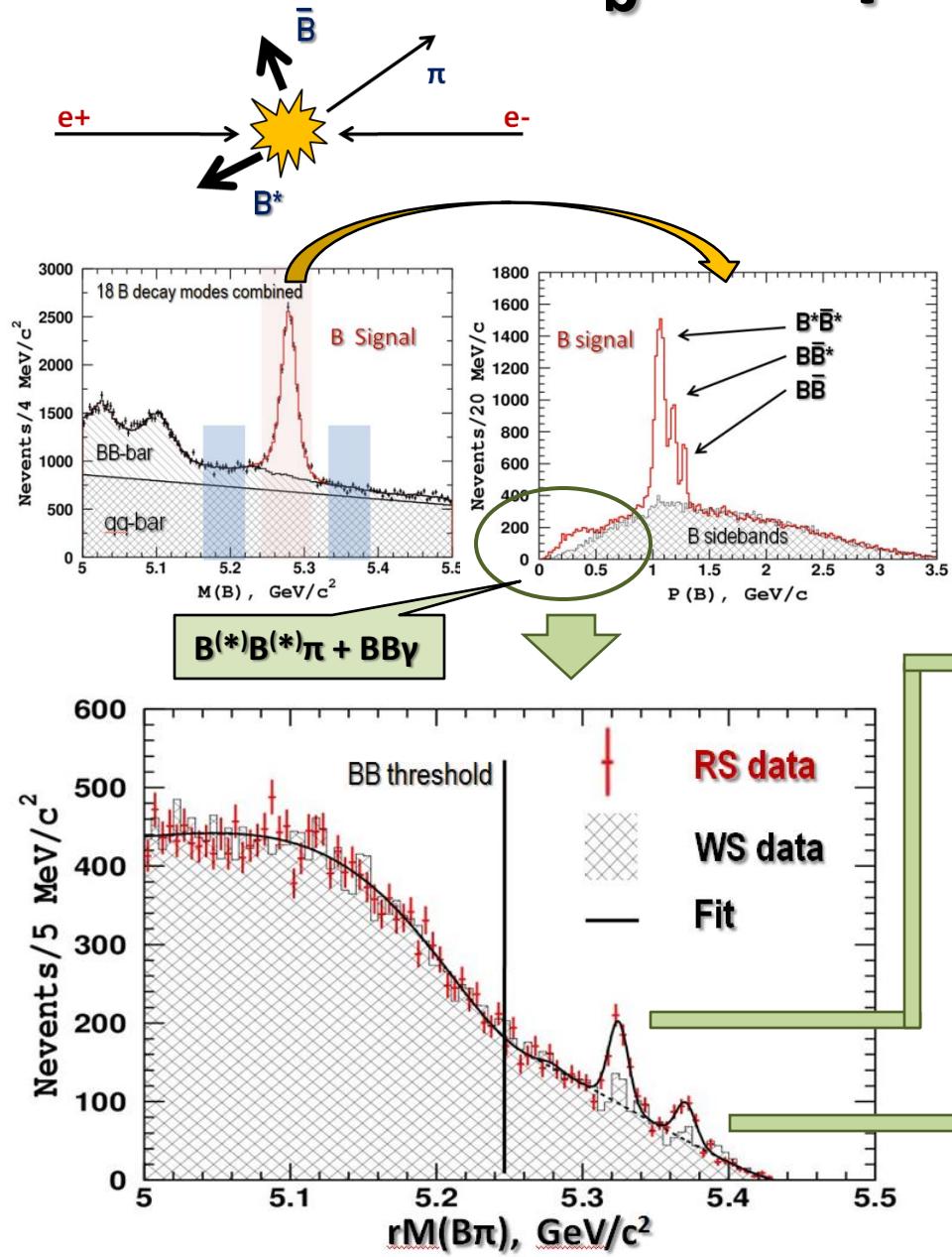
- $M = (4032.1 \pm 2.4) \text{ MeV}/c^2$
- $\Gamma = (26.1 \pm 5.3) \text{ MeV}$

Resonant structure of $\Upsilon(5S) \rightarrow (b\bar{b})\pi^+\pi^-$

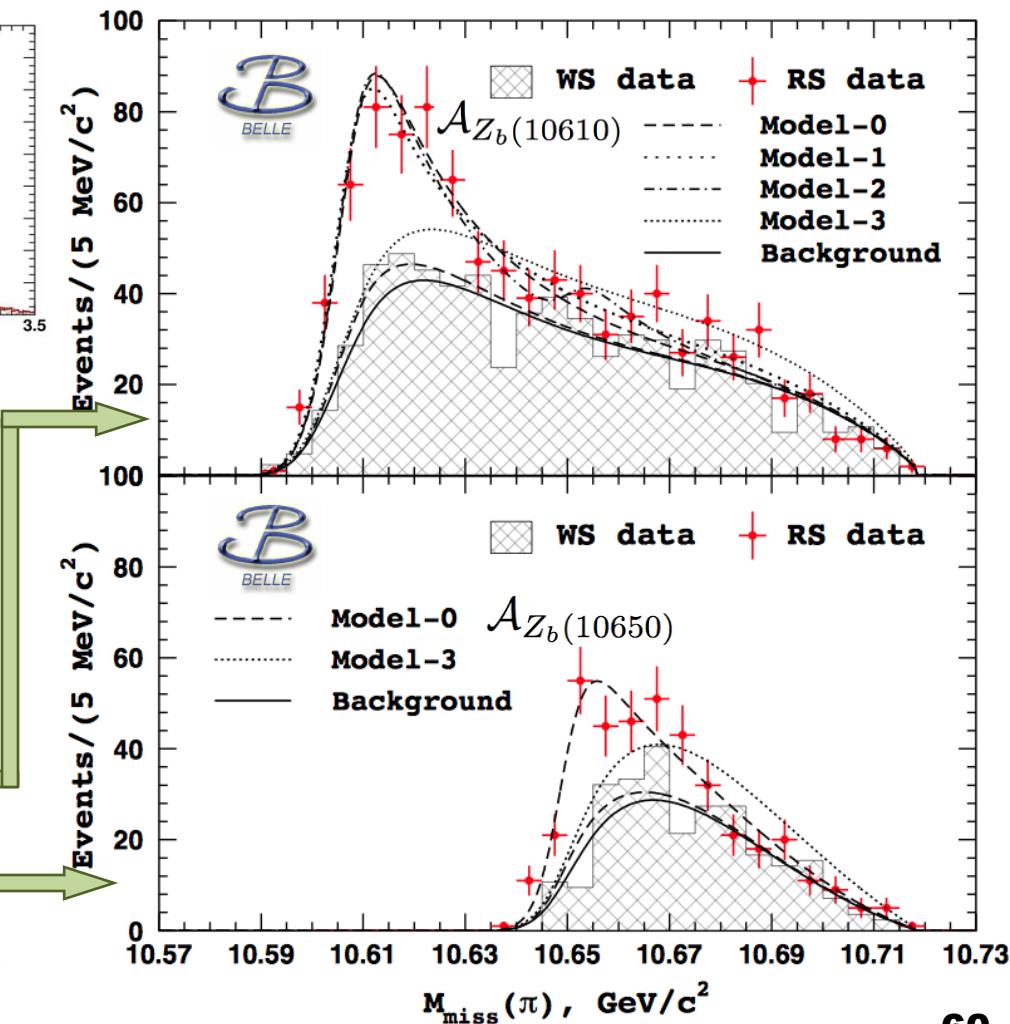


$Z_b^\pm \rightarrow \text{Open Beauty}$

PRL116,212001(2016)



$$S(m) = |\mathcal{A}_{Z_b(10610)} + \mathcal{A}_{Z_b(10650)} + \mathcal{A}_{\text{nr}}|^2$$



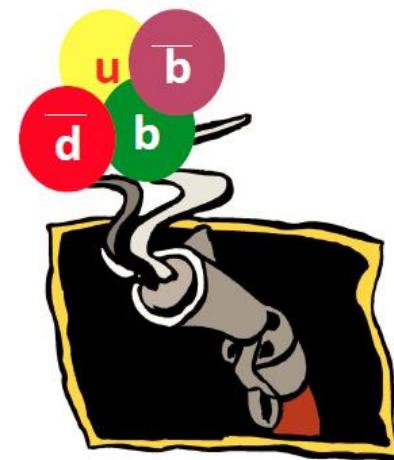
Summary on Z_b Decays by Belle

➤ decays to $\Upsilon(nS)$ & $h_b(nP)$ → must contain $b\bar{b}$ pair

➤ electrically charged → must contain $u\bar{d}$ pair

Assuming that Z_b decays are saturated by the $\Upsilon(nS)\pi$, $h_b(mP)\pi$ and $B^{(*)}B^*$ channels, one can calculate a table of relative branching fractions:

Channel	Fraction, %	
	$Z_b(10610)$	$Z_b(10650)$
$\Upsilon(1S)\pi^+$	$0.60 \pm 0.17 \pm 0.07$	$0.17 \pm 0.06 \pm 0.02$
$\Upsilon(2S)\pi^+$	$4.05 \pm 0.81 \pm 0.58$	$1.38 \pm 0.45 \pm 0.21$
$\Upsilon(3S)\pi^+$	$2.40 \pm 0.58 \pm 0.36$	$1.62 \pm 0.50 \pm 0.24$
$h_b(1P)\pi^+$	$4.26 \pm 1.28 \pm 1.10$	$9.23 \pm 2.88 \pm 2.28$
$h_b(2P)\pi^+$	$6.08 \pm 2.15 \pm 1.63$	$17.0 \pm 3.74 \pm 4.1$
$B^+\bar{B}^{*0} + \bar{B}^0B^{*+}$	$82.6 \pm 2.9 \pm 2.3$	—
$B^{*+}\bar{B}^{*0}$	—	$70.6 \pm 4.9 \pm 4.4$



$$\frac{\text{Br}(Z_b(10610)^+ \rightarrow B\bar{B}^*)}{\text{Br}(Z_b(10610)^+ \rightarrow b\bar{b})} = 5.93 + 0.99 / -0.59 + 1.01 / -0.73$$

$$\frac{\text{Br}(Z_b(10650)^+ \rightarrow B^*\bar{B}^*)}{\text{Br}(Z_b(10650)^+ \rightarrow b\bar{b})} = 2.80 + 0.69 / -0.40 + 0.54 / -0.36$$

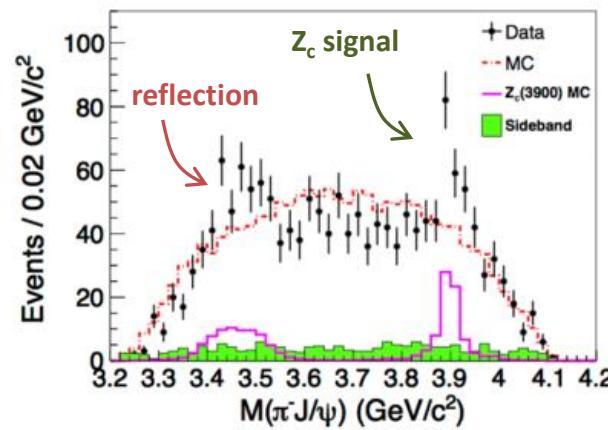
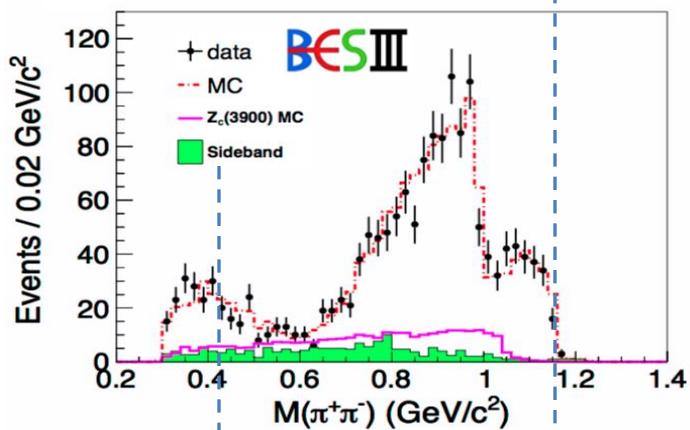
$B^{(*)}B^*$ channels dominate the Z_b decays

Charm vs. Beauty: I

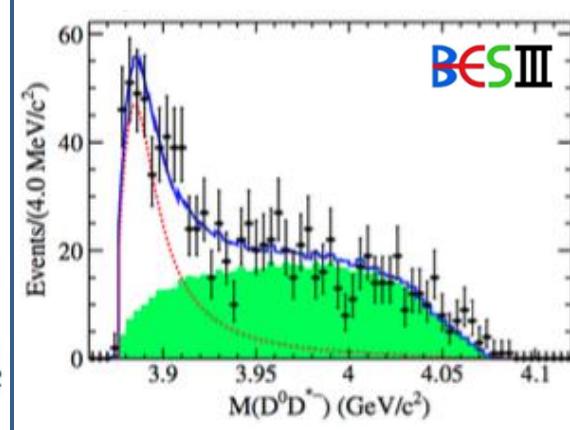
What is in common?

- $\Upsilon(10860)/\Upsilon(4260)$ demonstrates anomalously large coupling to $\Upsilon\pi^+\pi^-/\Psi\pi^+\pi^-$ and $h_b\pi^+\pi^-/h_c\pi^+\pi^-$ final states.

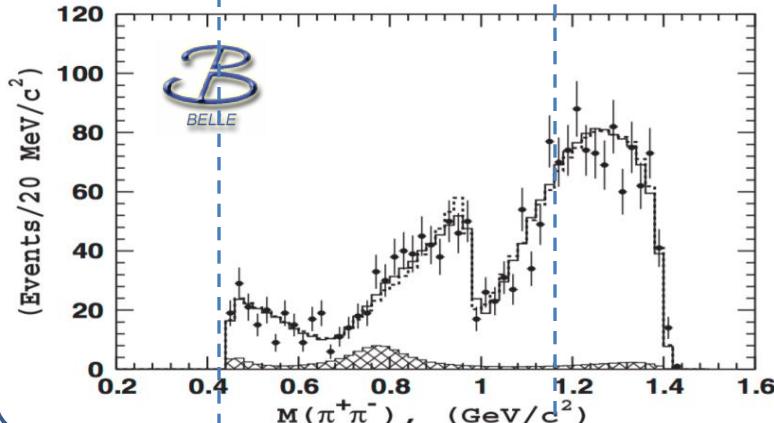
$Z_c(3900)$ is produced in $\Upsilon(4260) \rightarrow Z_c\pi \rightarrow \Psi\pi^+\pi^-$



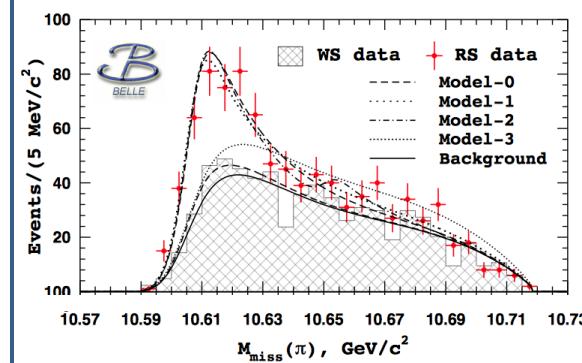
$\rightarrow Z_c\pi \rightarrow DD^*$



$Z_b(10610)$ is produced in $\Upsilon(10860) \rightarrow Z_b\pi \rightarrow \Upsilon(nS)\pi^+\pi^-$



MISSING PLOT



Charm vs. Beauty: II

What is difference?

- Both $Z_b(10610)$ and $Z_b(10650)$ isotriplets are observed in the $\Upsilon(nS)\pi$, ($n=1,2,3$) and $h_b\pi$ final states.
- Only $Z_c(3900)$ is observed in the $J/\psi\pi$ while both $Z_c(3900)$ and $Z_c(4020)$ are observed in the $h_c\pi$ final state. None of them is observed in the $\Psi(2S)\pi$ final state (instead, another $Z_c(4430)$ is found).
- $\Upsilon(10860) \rightarrow h_b\pi^+\pi^-$ is saturated by the intermediate two-body $Z_b\pi$ production.
- Large non $Z_c\pi$ component is observed in the $\Upsilon(4260) \rightarrow h_c\pi^+\pi^-$ amplitude.

The plan for BESIII

— a fine scan with large statistics —

- $E_{cm}=4.0$ up to $4.6+$ GeV
 - 10 MeV step (slight adjust \sim thresholds, skip those points we have already collected large samples)
 - $500 \text{ pb}^{-1}/\text{point}$
- total luminosity $\sim 25 \text{ fb}^{-1}$

- With peak luminosity of $10^{33}/\text{cm}^2/\text{s}$
- Top-up injection at BEPCII !
- This plan can be finished in about 5 years!

2016-17 running year: $E_{cm}=4.19, 4.20, 4.21, \dots, 4.30 \text{ GeV}$

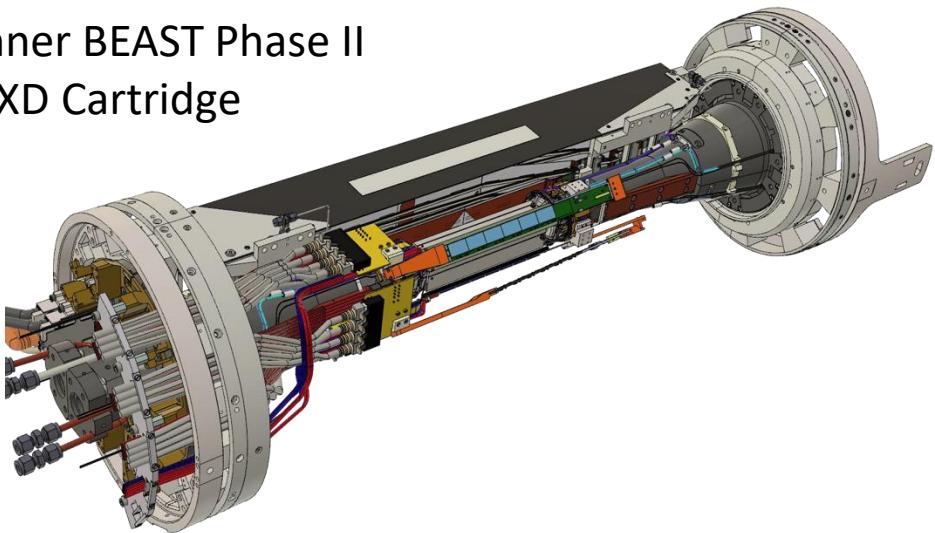
2017-18 running year: $E_{cm}=4.31, 4.32, 4.33, \dots, 4.40 \text{ GeV?}$

BelleII Status

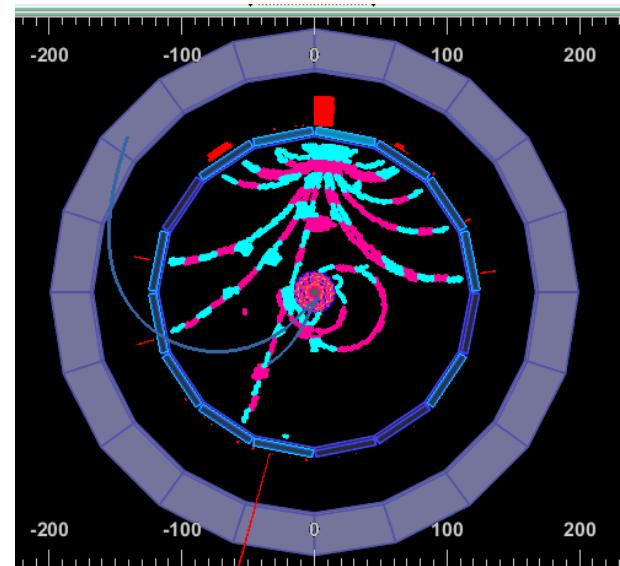


BelleII Roll-In
completed April 11,
2017

Inner BEAST Phase II
VXD Cartridge

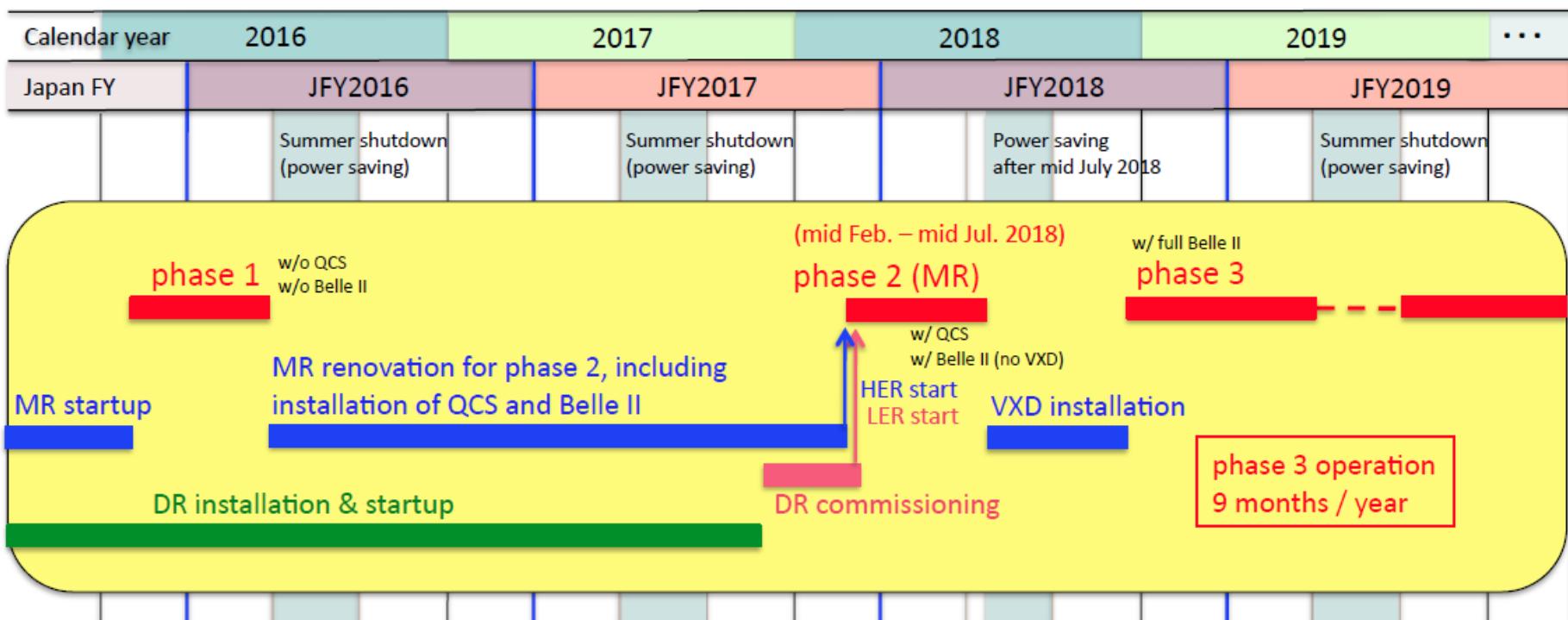


First Cosmics in a B field:



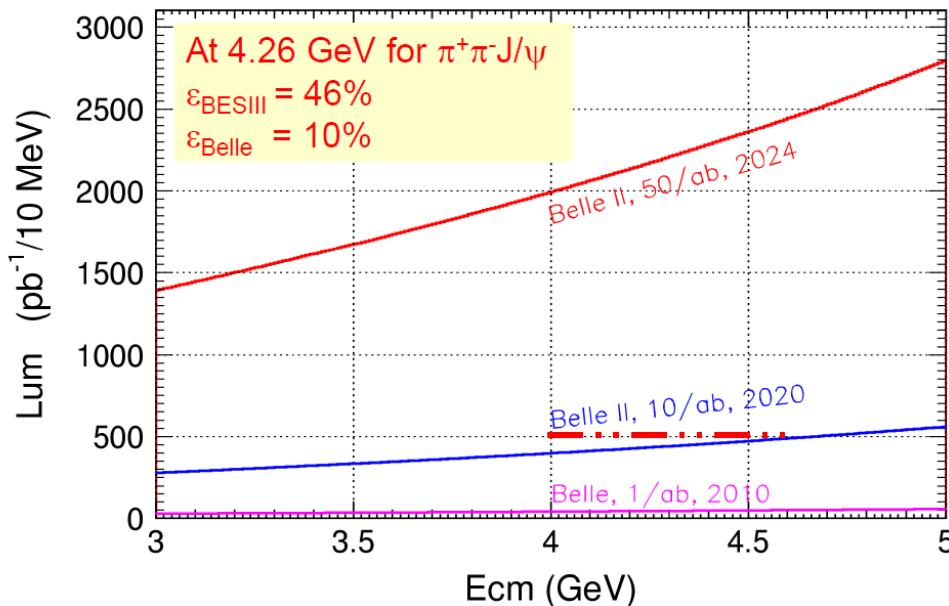


SuperKEKB / Belle II schedule



ISR at Belle II vs. BESIII

ISR produces events at all CM energies BESIII can reach



Direct scan

- (very) high luminosity at a few selected \sqrt{s}
- better resolution in \sqrt{s} — relevant for direct production of 1^{--} states

ISR

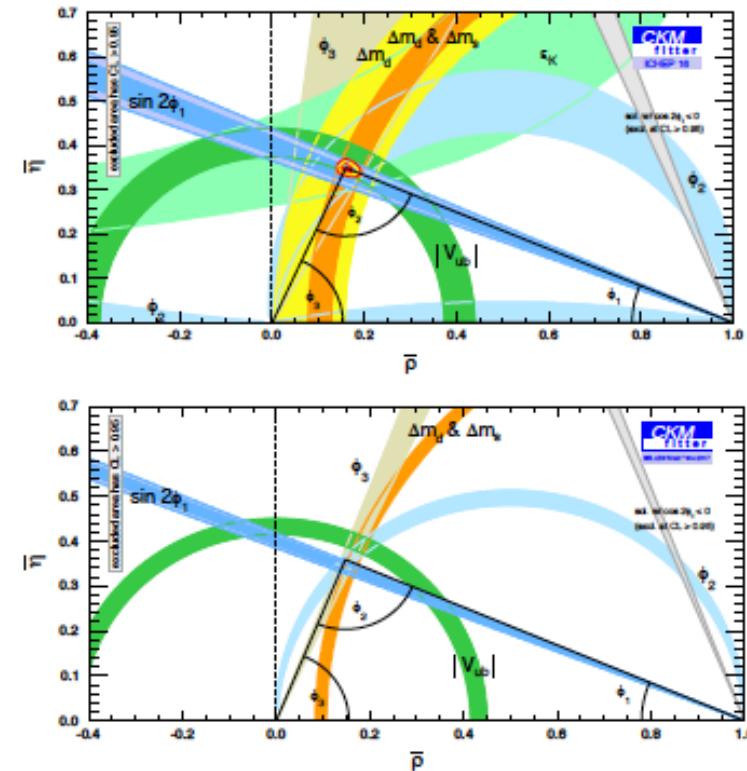
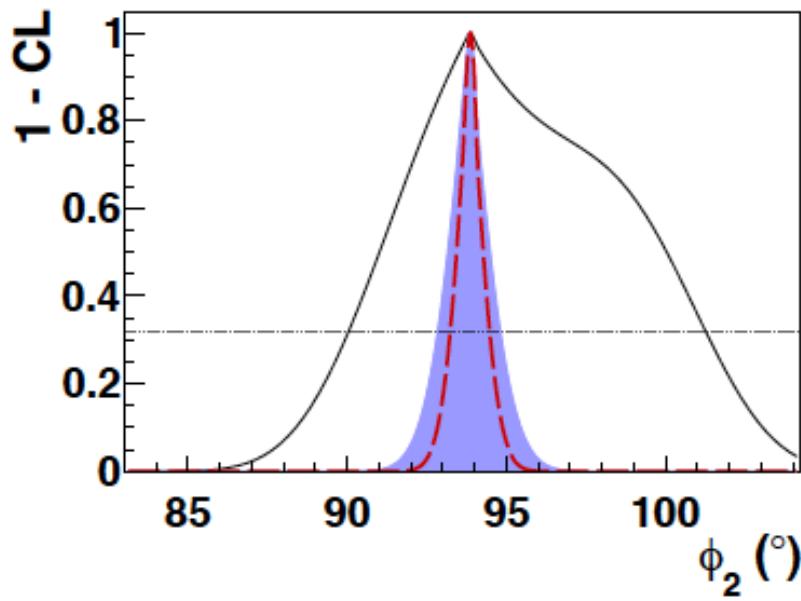
- ISR: many \sqrt{s} simultaneously
- reduced point-to-point systematics
- mass resolution limited by detector res.
- boost of hadronic system vs. γ_{ISR} may actually help efficiency

With $> 5(10) \text{ ab}^{-1}$ data sample, ISR $e^+e^- \rightarrow$ a charmonium+light hadrons [$\pi^+\pi^-J/\psi$, $\pi^+\pi^-\psi(2S)$, K^+K^-J/ψ , $K^+K^-\psi(2S)$, $\gamma X(3872)$, $\pi^+\pi^-X(3872)$, $\pi^+\pi^-hc$, $\pi^+\pi^-hc(2P)$, ωX_{cJ} , ϕX_{cJ} , $\eta J/\psi$, $\eta' J/\psi$, $\eta \psi(2S)$, ηhc]; and charm meson pair+light hadrons [DD, DD*, DD* π , ...]

Status of BelleII Physics Book

- Belle II physics book (630p), to be printed by PTEP / Oxford University Press
<https://confluence.desy.de/display/BI/B2TiP+ReportStatus>
- A few small unfinished areas, but otherwise close to complete and ready for review to commence.
- Await formation of Belle II publication committee to conduct collaboration wide review and form full collaboration author list ASAP.

Recent highlight $S_{CP}(B \rightarrow \pi^0\pi^0)$ & Φ_2 : F. Abudinen



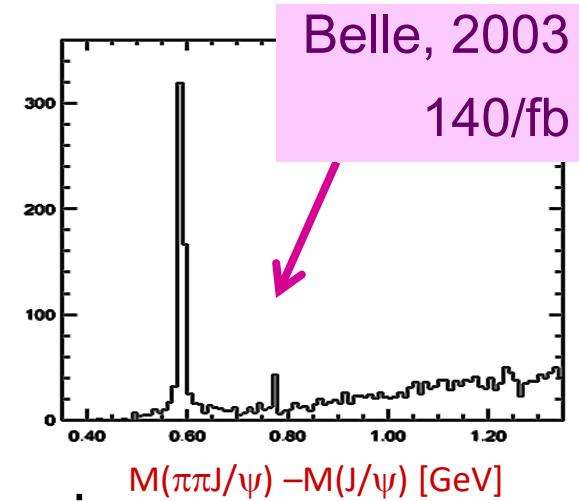
Summary

- A hole new field of exotic physics discovered in last decade; new information is still coming from both completed (Belle & BaBar) and currently ongoing (BESIII, D0, LHCb, CMS, ...) experiments
- However (much) more data required for a better understanding (BelleII, BESIII, LHCb, ...)
- BESIII is getting more data; start of the Belle II is approaching
- Input from Belle II is crucial to push exotic studies into bottomonium sector. Energy scan up to 11.24 GeV is accessible by the SuperKEKB.
- Common features between charmonium and bottomonium sectors is gradually emerging. No direct identity however.
- No clear understanding of the nature of new states yet. Theory needs to catch up with a flow of new data/puzzles from experiments.

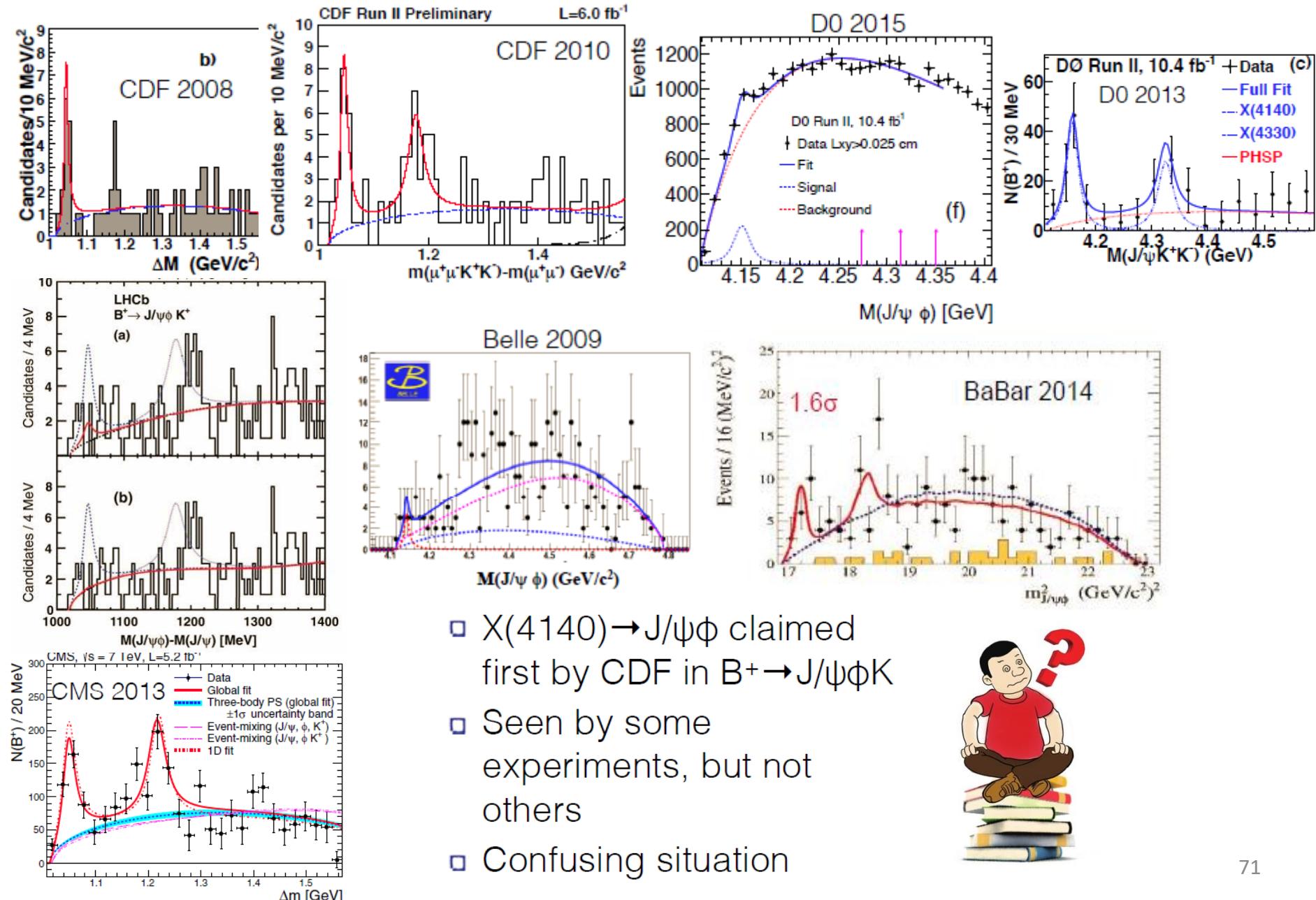


What is the X(3872)?

- Mass: Very close to $\bar{D}^0 D^{*0}$ threshold
- Width: Very narrow, < 1.2 MeV
- $J^{PC}=1^{++}$
- Production
 - in $\bar{p}p/p\bar{p}$ collision – rate similar to charmonia
 - In B decays – KX similar to $c\bar{c}$, K^*X smaller than $c\bar{c}$
 - $Y(4260) \rightarrow \gamma + X(3872)$ (?)
- Decay BR: open charm $\sim 50\%$, charmonium $\sim O(\%)$
- Nature (very likely exotic)
 - Loosely $\bar{D}^0 D^{*0}$ bound state (like deuteron?)?
 - Mixture of excited χ_{c1} and $\bar{D}^0 D^{*0}$ bound state?
 - Many other possibilities (if it is not χ'_{c1} , where is χ'_{c1} ?)



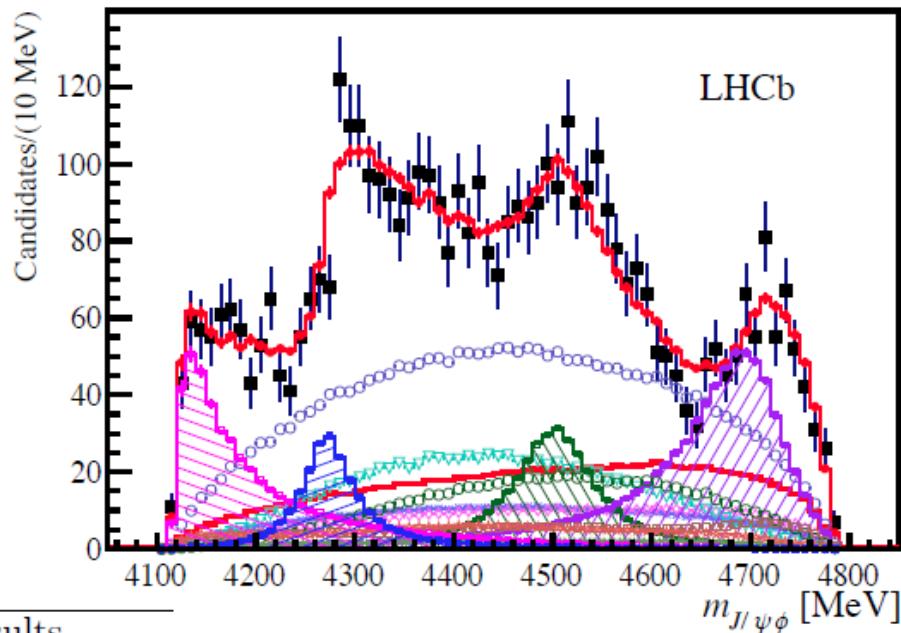
X(4140) and X(4270)



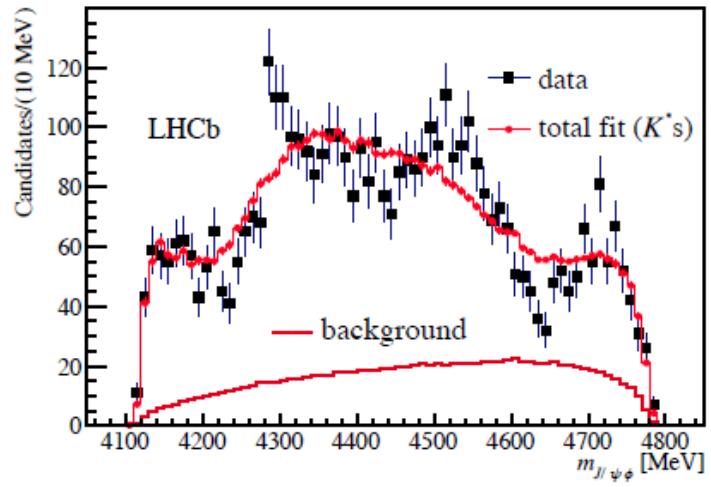
X(4140) at LHCb

PRD95, 012002(2017)

- ❑ Need 4 exotic contributions to describe data
- ❑ X(4140) possibly $D_s D_s^*$ cusp
- ❑ Some disagreement in parameters compared to previous experiments
 - ❑ Possibly due to missing interference effects in 1D fits



Contri- bution	sign. or Ref.	Fit results		
		M_0 [MeV]	Γ_0 [MeV]	FF %
All $X(1^+)$				
$X(4140)$	8.4σ	$4146.5 \pm 4.5^{+4.6}_{-2.8}$	$83 \pm 21^{+21}_{-14}$	$16 \pm 3^{+6}_{-2}$
ave.	Table 1	4147.1 ± 2.4	15.7 ± 6.3	$13.0 \pm 3.2^{+4.8}_{-2.0}$
$X(4274)$	6.0σ	$4273.3 \pm 8.3^{+17.2}_{-3.6}$	$56 \pm 11^{+8}_{-11}$	$7.1 \pm 2.5^{+3.5}_{-2.4}$
CDF	[29]	$4274.4^{+8.4}_{-6.7} \pm 1.9$	$32^{+22}_{-15} \pm 8$	
CMS	[25]	$4313.8 \pm 5.3 \pm 7.3$	$38^{+30}_{-15} \pm 16$	
All $X(0^+)$				
$NR_{J/\psi \phi}$	6.4σ			$28 \pm 5 \pm 7$
$X(4500)$	6.1σ	$4506 \pm 11^{+12}_{-15}$	$92 \pm 21^{+21}_{-20}$	$46 \pm 11^{+11}_{-21}$
$X(4700)$	5.6σ	$4704 \pm 10^{+14}_{-24}$	$120 \pm 31^{+42}_{-33}$	$6.6 \pm 2.4^{+3.5}_{-2.3}$
				$12 \pm 5^{+9}_{-5}$

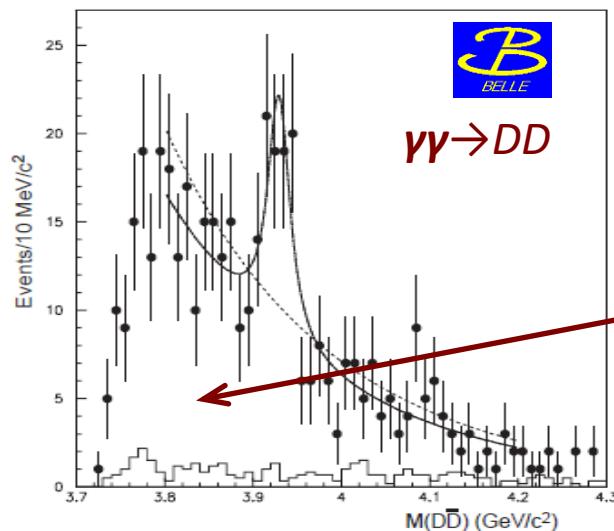


Is $X(3915) = \chi_{c0}'$?

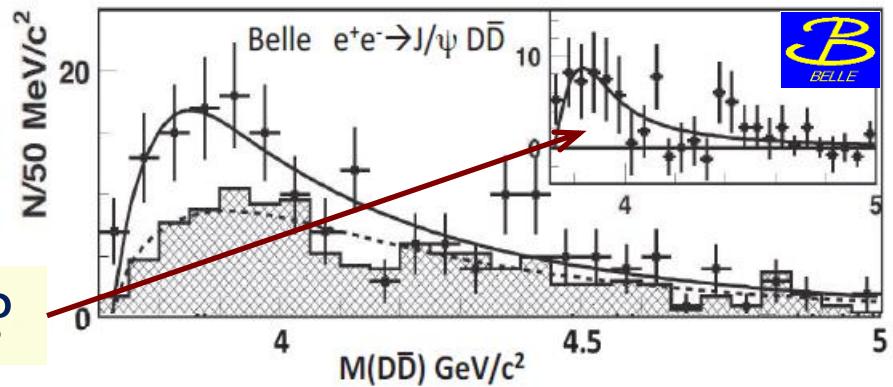
PDG ascribe $\Upsilon(3915)$ to vacant χ_{c0}' state, based on BaBar's measurement of $J=0$ in $\gamma\gamma \rightarrow \Upsilon(3940) \rightarrow \omega J/\psi$

strongly criticized by theoreticians

- ◆ χ_{c0}' production in two body B decays suppressed
- ◆ $\chi_{c0}' \rightarrow DD$ should be dominant, but not seen in B decays and $\gamma\gamma$
- ◆ there is a better candidate for χ_{c0}' !



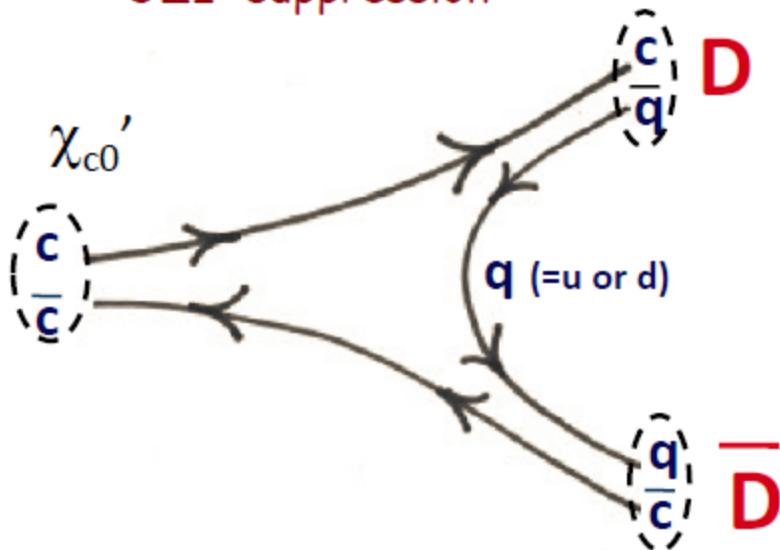
χ_{c0}' ?



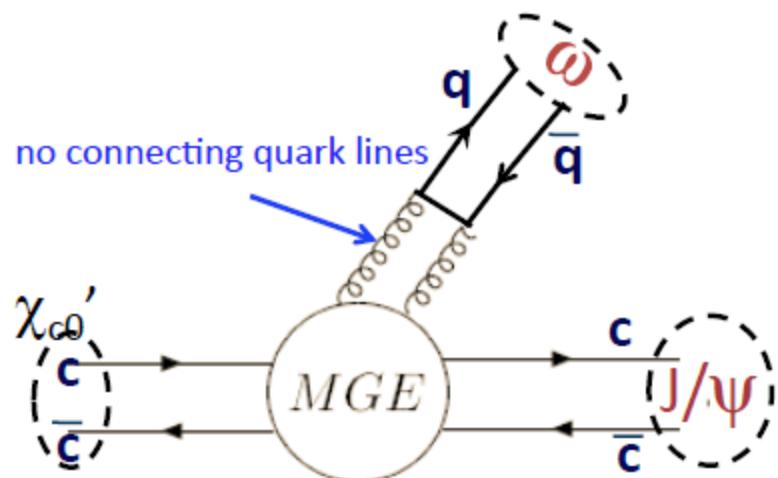
Theory does not like conventional interpretation, but suggests no good explanation for $X(3915)\dots$

$\chi_{c0}' \rightarrow D\bar{D}$ should be huge & $\chi_{c0}' \rightarrow \omega J/\psi$ tiny

Fall-apart mode, no
"OZI" suppression



"OZI" suppressed



But: $Bf(X_{3915} \rightarrow D^0\bar{D}^0) < 1.2 \times Bf(X_{3915} \rightarrow \omega J/\psi)$

J. Brodzicka et al. (Belle) PRD 100, 092001

This strongly suggests that the $X(3915)$ is a 4-quark state

$\Upsilon(4220)$ leptonic width

Considering the isospin symmetry, we estimate the lower limit on the $\Gamma_{e^+e^-}(\Upsilon(4220))$. For an isospin-zero charmoniumlike state, we expect

Taking Solutions with the smallest $B \times \Gamma_{e^+e^-}$,

$$\Gamma_{e^+e^-} > (29.1 \pm 2.5(stat) \pm 7.0(sys)) + \dots \text{ eV}$$

Taking Solutions with the largest $B \times \Gamma_{e^+e^-}$,

$$\Gamma_{e^+e^-} > (202.2 \pm 12.9(stat) \pm 23.4(sys)) + \dots \text{ eV}$$

For the most interesting mode $\Upsilon(4220) \rightarrow \pi\pi J/\psi$

For the case of highest $B \times \Gamma_{e^+e^-}$

$$B_{\pi\pi J/\psi} = (12.9 \pm 1.3 \pm 3.9)\%$$

For the case of smallest $B \times \Gamma_{e^+e^-}$

$$B_{\pi\pi J/\psi} = (11.2 \pm 1.1 \pm 1.9)\%$$

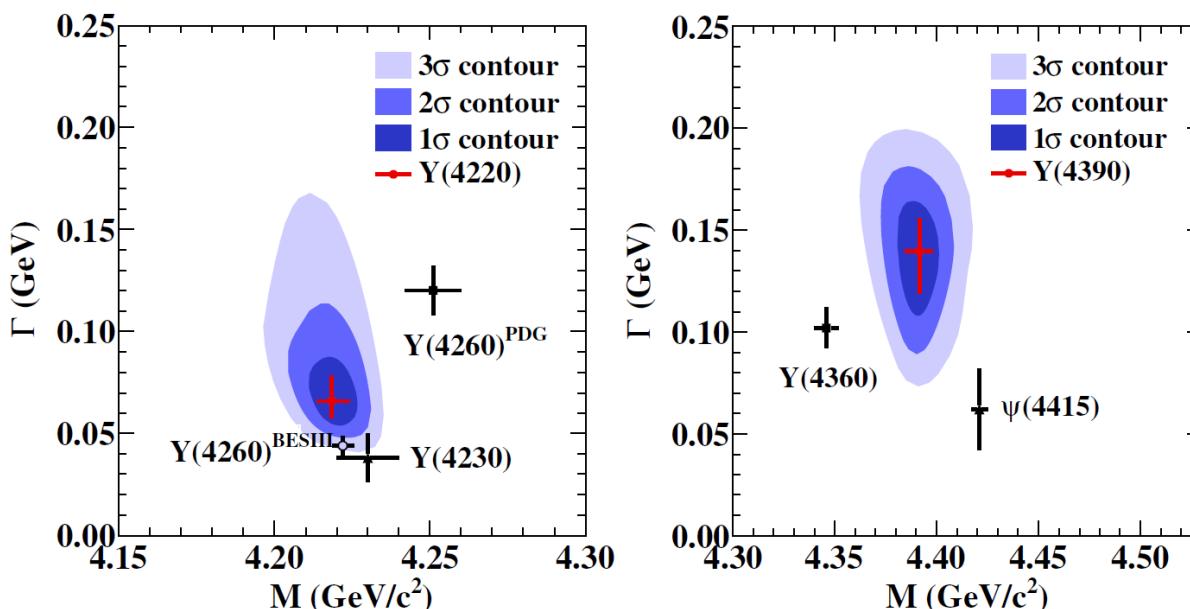
For the most extreme case, taking smallest $B \times \Gamma_{e^+e^-}$ for $\pi\pi J/\psi$ while largest $B \times \Gamma_{e^+e^-}$ for other mode

$$B_{\pi\pi J/\psi} = (2.1 \pm 0.3 \pm 0.7)\%$$

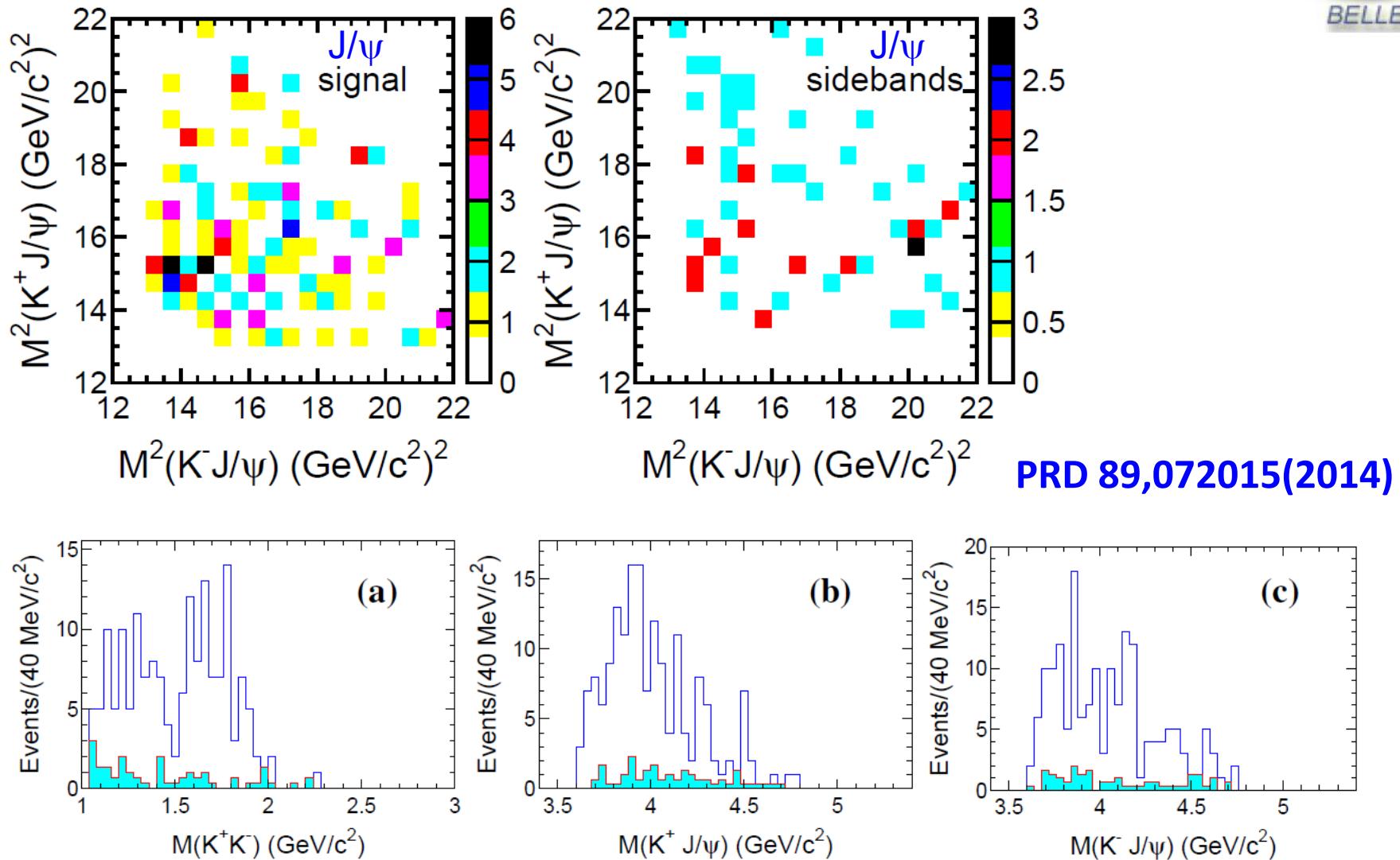
$$\left. \begin{array}{l} \Gamma_{e^+e^-} = \sum_i \mathcal{B}_i \times \Gamma_{e^+e^-} \\ \mathcal{B}_{\pi\pi h_c} = \frac{3}{2} \times \mathcal{B}_{\pi^+\pi^- h_c}, \\ \mathcal{B}_{\pi\pi J/\psi} = \frac{3}{2} \times \mathcal{B}_{\pi^+\pi^- J/\psi}, \\ \mathcal{B}_{D\bar{D}^*\pi} = 3 \times \mathcal{B}_{D^0 D^{*-} \pi^+ + c.c.} \end{array} \right\}$$

Υ or ψ structures

Parameters	$\Upsilon(4220)$ in $\pi^+\pi^-h_c$	$\Upsilon(4260)$	$\psi(4160)$	Structure in $\omega\chi_{c0}$
M (MeV)	$4218.4 \pm 4.0 \pm 0.9$	4251 ± 9	4191 ± 5	$4226 \pm 8 \pm 6$
Γ_{tot} (MeV)	$66.0 \pm 9.0 \pm 0.4$	120 ± 12	70 ± 10	$39 \pm 12 \pm 2$
Parameters	$\Upsilon(4390)$ in $\pi^+\pi^-h_c$	$\Upsilon(4360)$	$\psi(4415)$	
M (MeV)	$4391.6 \pm 6.3 \pm 1.0$	4362 ± 13	4421 ± 4	
Γ_{tot} (MeV)	$139.5 \pm 16.1 \pm 0.6$	74 ± 18	62 ± 20	



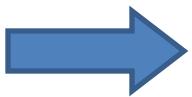
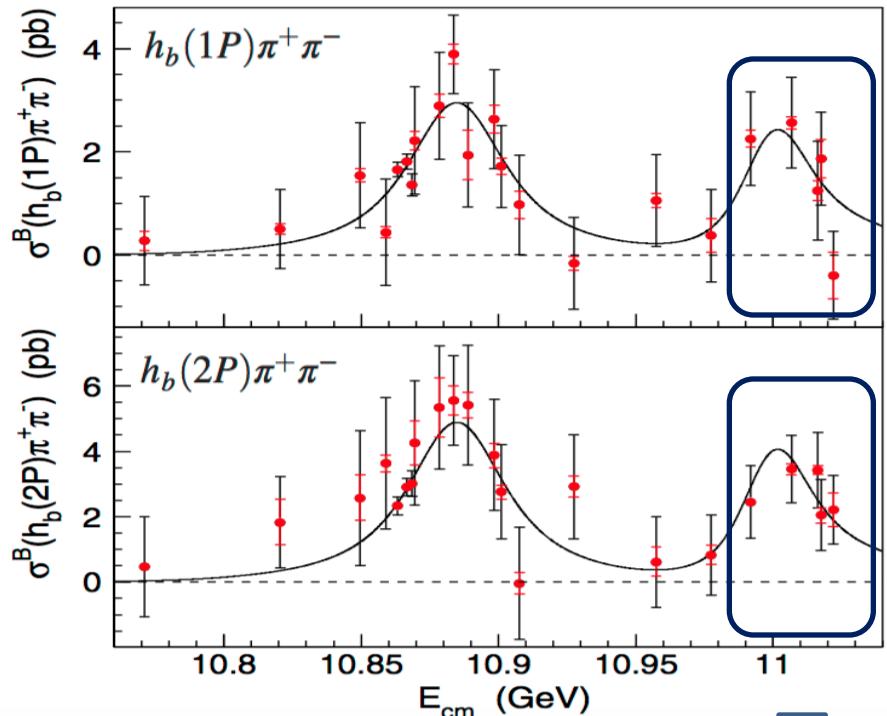
Search for $Z_{cs} \rightarrow K J/\psi$ states



No evident structure in $K^+ J/\psi$ mass distribution under current statistics

Z_b^\pm Production at $\Upsilon(6S)$

PRL117.142001(2016)



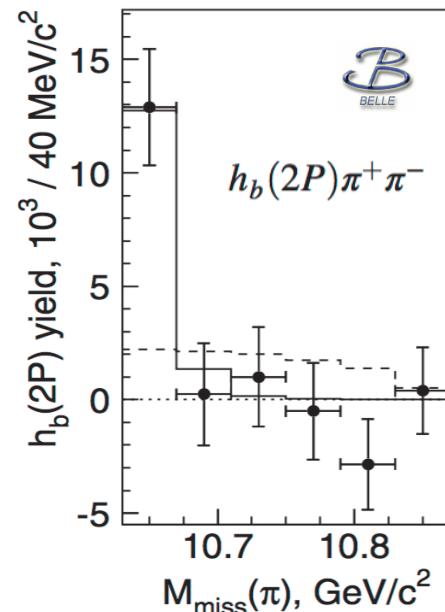
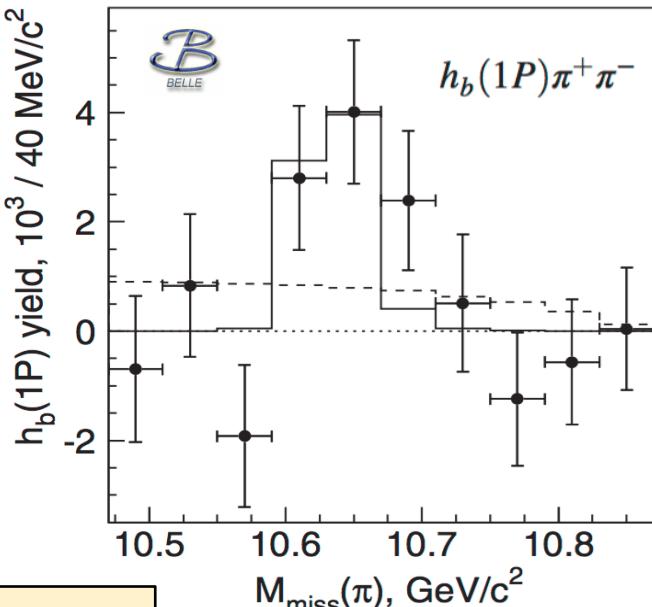
**$\Upsilon(6S)$ Data:
5 fb^{-1}**

- ◆ 1st obs. of $\Upsilon(6S) \rightarrow \pi^+\pi^- h_b(nP)$
3.5 σ for 1P, 5.3 σ for 2P.



The two Z_b states can not be separated with current statistics

**$\Upsilon(6S) \rightarrow h_b(mP)\pi^+\pi^-$ transition is dominated
(saturated) by the intermediate Z_b^\pm production.
Two Z_b can be separated at Belle II !**

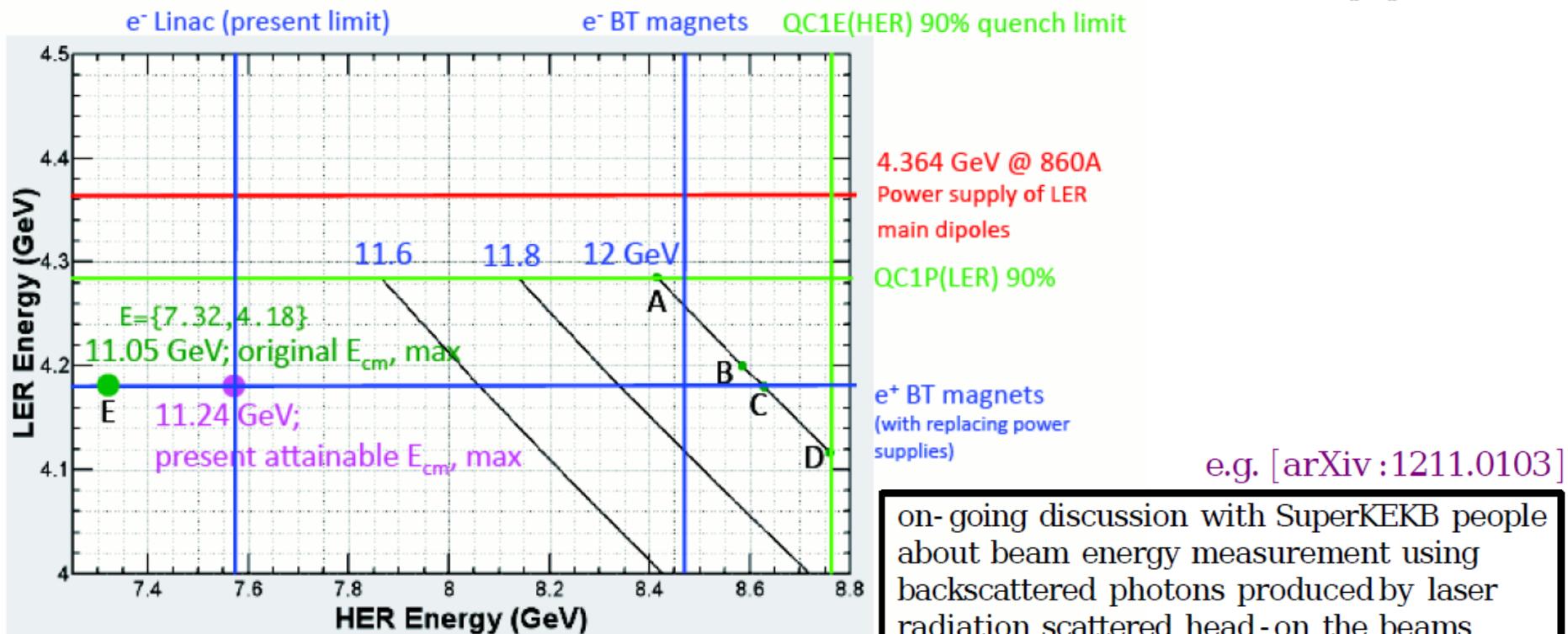


Higher energy run

from K. Akai,
BPAC Feb 2012

- Design: original design maximum energy is 11.05 GeV at Y(6S)
- Possible higher energy run (11.5 GeV – 12 GeV) ?
 - If any, higher energy run will be after several years running at Y(4S)~Y(6S)
 - **present max E_{cm} is 11.24 GeV**, limited by e^- Linac and e^+ BT magnets
 - In order to inject the electron beam to HER at the required energy for 12 GeV operation, there must be huge reinforcement of Linac (replacement of S-band with C-band, 7.571 → 8.6 GeV)

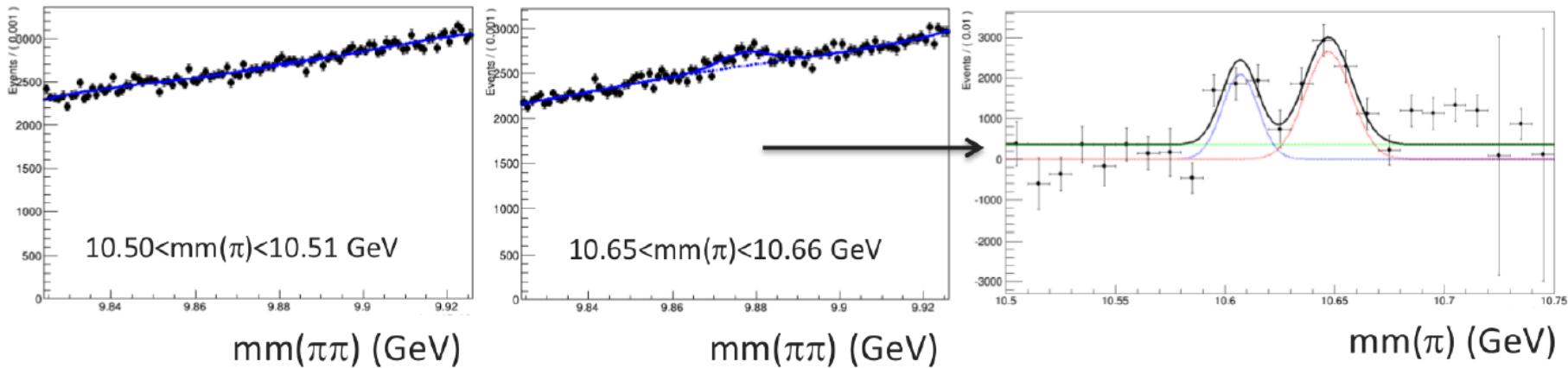
11.24 GeV region : $\Lambda_b \bar{\Lambda}_b$ threshold



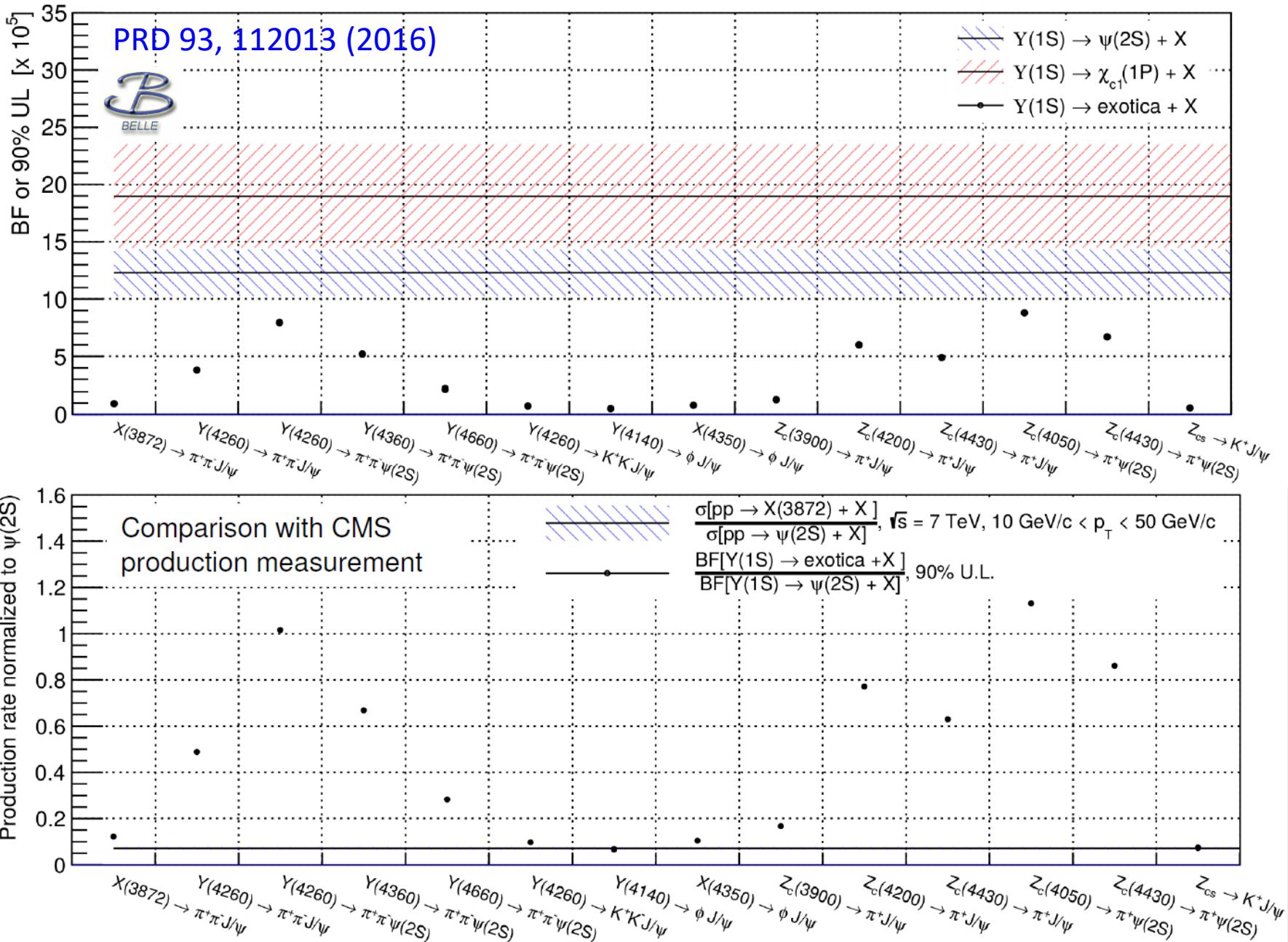
Belle II's $\Upsilon(6S)$ measurements in Phase II



- May take $\sim 20 - 40 \text{ fb}^{-1}$ during the Phase II data taking and $\sim 10 \text{ fb}^{-1}$ at $\Upsilon(6S)$ resonance energy
- Using the Golden Modes:
 - $\Upsilon(6S) \rightarrow \pi Z_b(\pi h_b(nP))$
 - $\Upsilon(6S) \rightarrow \pi Z_b(\pi \Upsilon(pS)(I^+ I^-))$
- Monte-Carlo studies show that a good separation is possible with 10 fb^{-1} of data



Y(1S) to inclusive XYZ



PWA on Zc(3900) state

BESIII

In the process $e^+e^- \rightarrow \gamma^* \rightarrow \pi^+\pi^- J/\psi$

preliminary

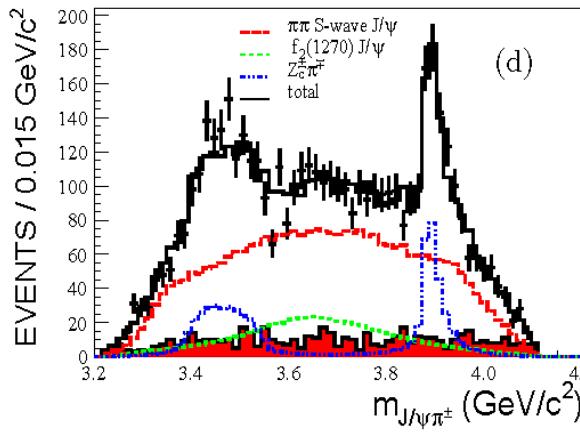
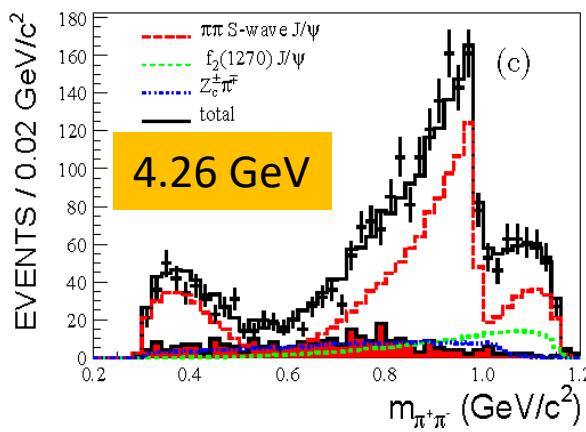
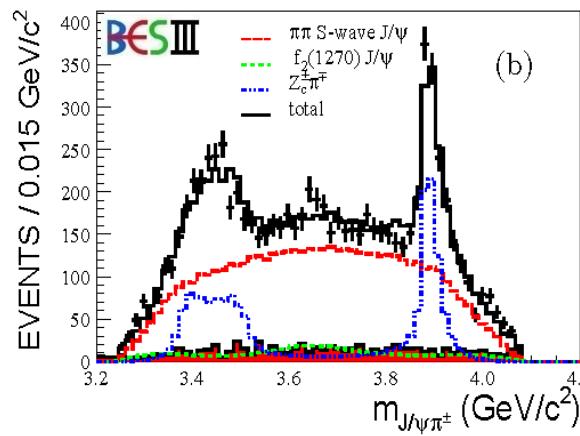
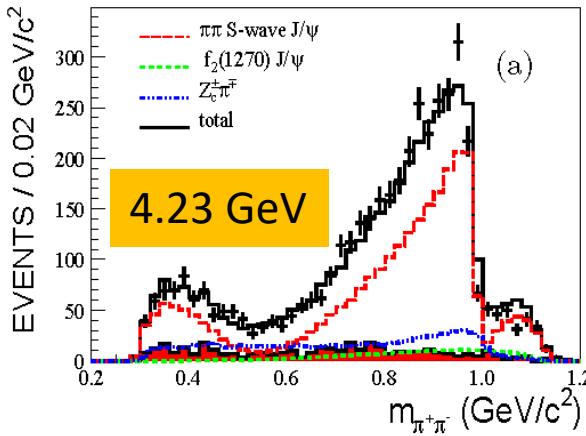
- The helicity value of γ^* is taken as $\lambda_0 = \pm 1$ due to from e+e- annihilation
- $\gamma^* \rightarrow Z_c^\pm\pi^\mp$, $Z_c^\pm \rightarrow J/\psi\pi^\pm$, we try J^P for X:
 0^- , 1^- , 1^+ , 2^- , 2^+ , and 0^+ is not allowed
- Z_c^+ and Z_c^- states are assumed as isospin partner, share the same mass and coupling constants
- Six resonances are included in fitting to data:

$\sigma_0, f_0(980), f_2(1270), f_0(1370), Z_c^\pm$, and $\pi^+\pi^- J/\psi$

Z_c is taken as 1^+ .

Resonance	σ	$f_0(980)$	$f_2(1270)$	$f_0(1370)$	Z_c^+	Z_c^-
Significance	13	25	5	11	22	22

PWA on Zc(3900) state



The signal yields corresponding for each mode with the Z_c^\pm assignment $J^P = 1^+$ **preliminary**

\sqrt{s}	σ	$f_0(980)$	$f_2(1270)$	$f_0(1370)$	$Z_c^+ + Z_c^-$	$\pi^+\pi^- J/\psi$
4.23 GeV	1576.9 ± 431.2	1050.2 ± 157.8	4356.2 ± 549.4	273.2 ± 85.1	875.2 ± 84.8	6.2 ± 7.6
4.26 GeV	1121.5 ± 112.0	465.1 ± 53.2	2236.8 ± 157.6	308.8 ± 108.2	314.2 ± 21.2	15.9 ± 39.3

- Zc line shape parameterized with Flatte-like formula

$$g'_2/g'_1 = 27.1 \pm 13.1$$

$$\begin{aligned} & \Gamma(Z_c^\pm \rightarrow (D\bar{D}^*)^\pm) / \\ & \Gamma(Z_c^\pm \rightarrow J/\psi \pi^\pm) \\ & = 6.2 \pm 2.9 \end{aligned}$$

Comparison of fit results

- Mass, g_1' and Log-likelihood

preliminary

$Z_c : J^P$	M (MeV)	$g'_1(\text{GeV}^2)$	g'_2/g'_1	$-\ln L$
0^-	3906.3 ± 2.3	0.079 ± 0.007	25.8 ± 2.9	-1528.8
1^-	3903.1 ± 1.9	0.063 ± 0.005	26.5 ± 2.6	-1457.7
1^+	3900.2 ± 1.5	0.075 ± 0.006	21.8 ± 1.7	-1569.8
2^-	3905.2 ± 2.1	0.060 ± 0.004	28.7 ± 2.7	-1516.5
2^+	3894.3 ± 1.9	0.051 ± 0.005	23.4 ± 3.3	-1316.2

- Z_c favors the quantum number $J^P=1^+$

Significance to distinguish the quantum number 1^+ over other quantum numbers.

Hypothesis	$\Delta(-\ln L)$	$\Delta(ndf)$	significance
1^+ over 0^-	44.5	$4 \times 2 + 5$	7.3σ
1^+ over 1^-	107.0	$4 \times 2 + 5$	$> 8.0\sigma$
1^+ over 2^-	51.8	$4 \times 2 + 5$	$> 8.0\sigma$
1^+ over 2^+	193.5	$4 \times 2 + 5$	$> 8.0\sigma$

