

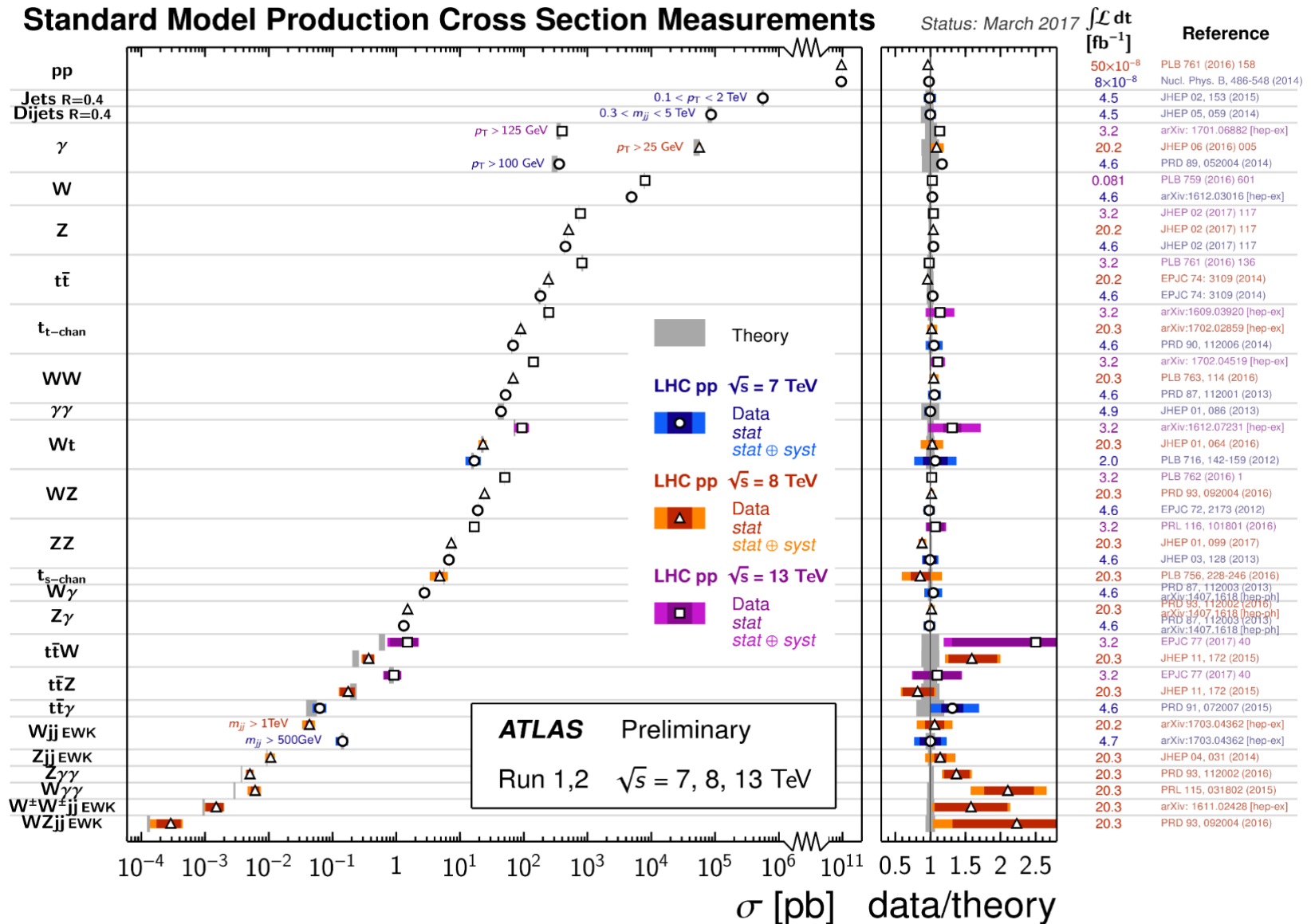


# Heavy Quarkonium Physics at CEPC

- ✧ QCD – Final frontier of the SM physics
- ✧ Heavy quarkonium production in QCD
- ✧ Heavy quarkonium at CEPC – go beyond the SM
- ✧ Summary and outlook

*Jianwei Qiu*  
*Theory Center, Jefferson Lab*

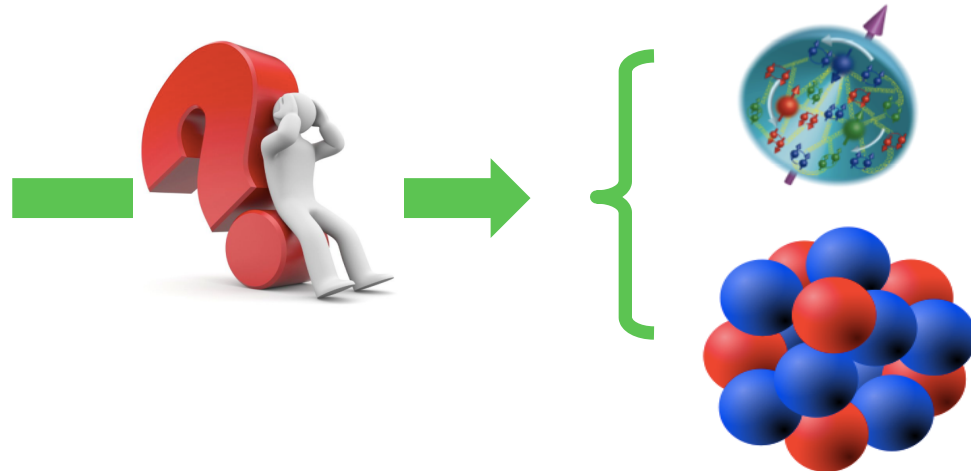
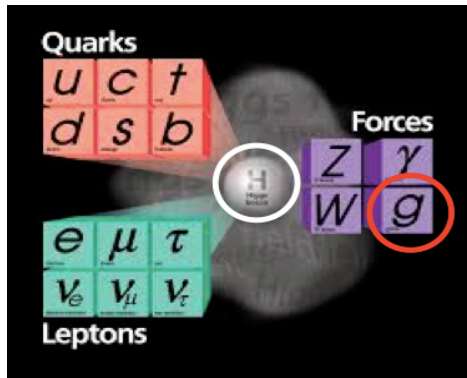
# The great success of the SM physics



**SM: Electroweak processes + QCD perturbation theory works!**

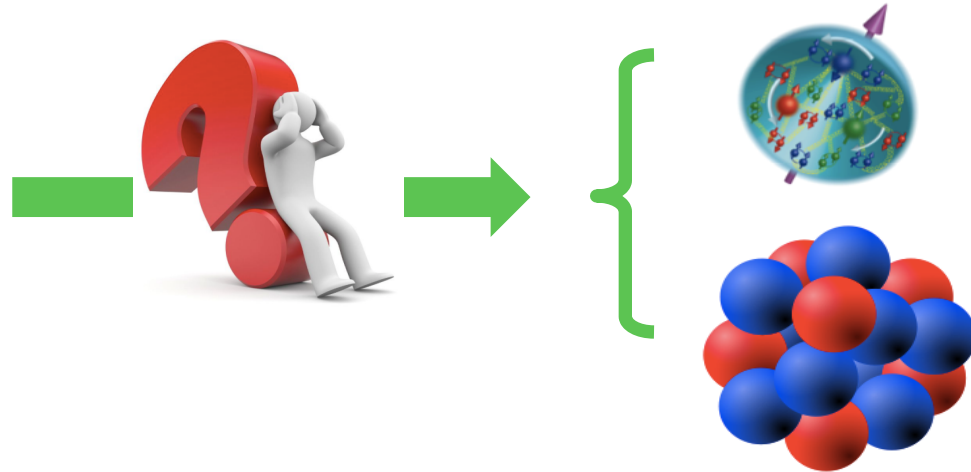
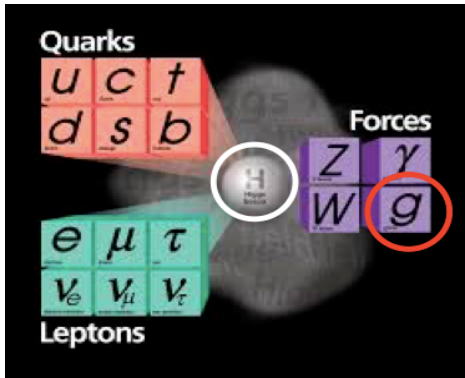
# QCD – Final frontier of the SM physics

□ How QCD works to get all of us – the visible world?



# QCD – Final frontier of the SM physics

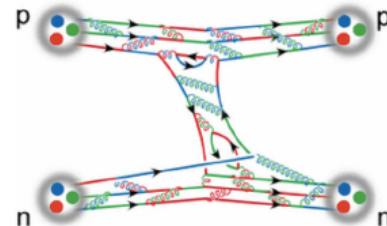
- How QCD works to get all of us – **the visible world?**



- How hadrons are **emerged** from quarks and gluons?
- What is the quark/gluon **structure** of nucleon and nuclei?
- How does QCD make up the **properties** of hadrons?

Their mass, spin, magnetic moment, ...

- How does the **nuclear force** arise from QCD?
- ...



# Why QCD is so hard to deal with?

- ❑ It is strongly coupled – nonlinear + nonperturbative!
- ❑ It is relativistic – nontrivial QCD vacuum, no still picture!
- ❑ No localized mass/charge center – unlike nucleus in an atom!
- ❑ Gluons are “dark” and carry “color” – intellectual challenge!

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## Heavy quarkonium:

- ✧ Heavy quark as relatively localized heavy mass/charge center
- ✧ Heavy quark in the pair's rest frame is almost non-relativistic
- ✧ Production of heavy quark pair could be perturbative
- ✧ Top decays too quickly, strange is too light, ...

 **Charmonium ( $c\bar{c}$ ) + Bottomonium ( $b\bar{b}$ )**

$c$	1.0 – 1.4 GeV
$b$	4.0 – 4.5 GeV

# Heavy quarkonium

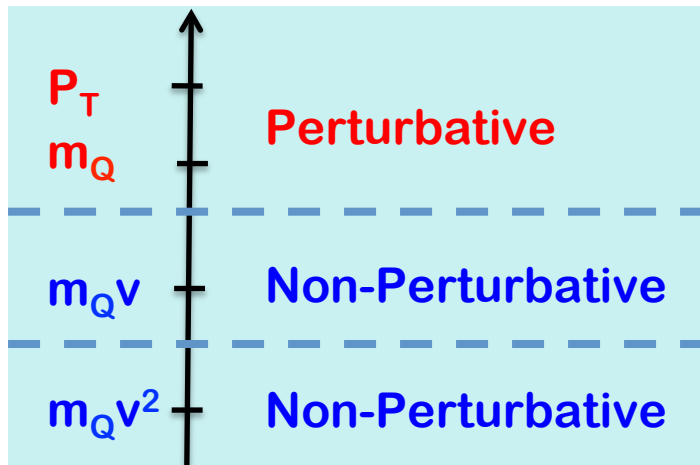
## □ One of the simplest QCD bound states:

Localized color charges (heavy mass), non-relativistic relative motion

Charmonium:  $v^2 \approx 0.3$

Bottomonium:  $v^2 \approx 0.1$

## □ Well-separated momentum scales – effective theory:



Hard — Production of  $Q\bar{Q}$  [pQCD]

Soft — Relative Momentum [NRQCD]

←  $\Lambda_{\text{QCD}}$

Ultrasoft — Binding Energy [pNRQCD]



# Heavy quarkonium

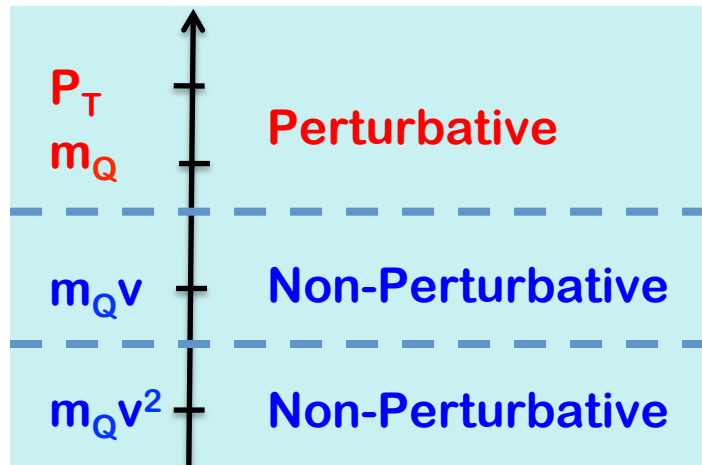
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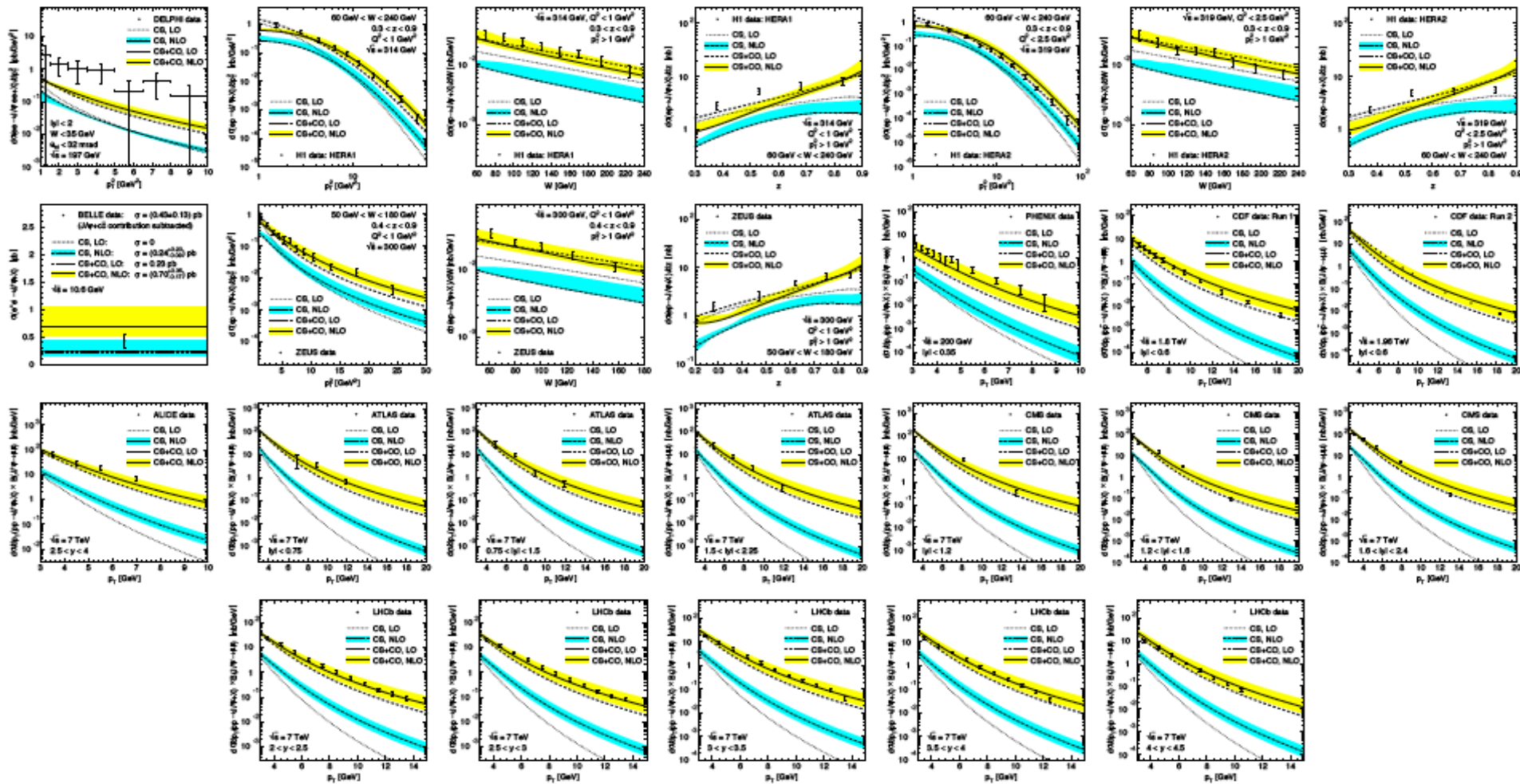
## □ Cross sections and observed mass scales:

$$\frac{d\sigma_{AB \rightarrow H(P)X}}{dy dP_T^2} \quad \sqrt{S}, \quad P_T, \quad M_H,$$

PQCD is “expected” to work for the production of heavy quarks

*Ideal probe: Emergence of a quarkonium from a heavy quark pair?*

# NRQCD – global analysis



194 data points from 10 experiments, fix singlet  $\langle O[{}^3S_1^{[1]}] \rangle = 1.32 \text{ GeV}^3$

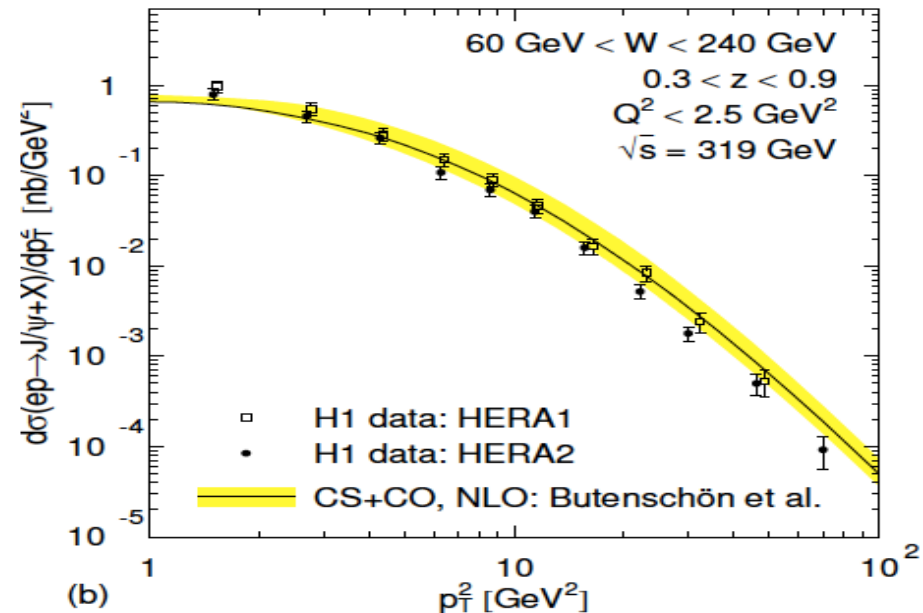
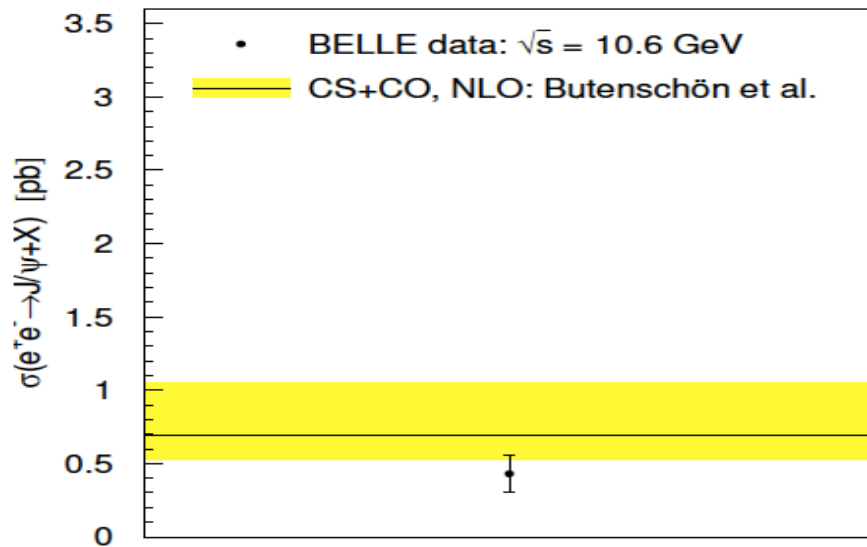
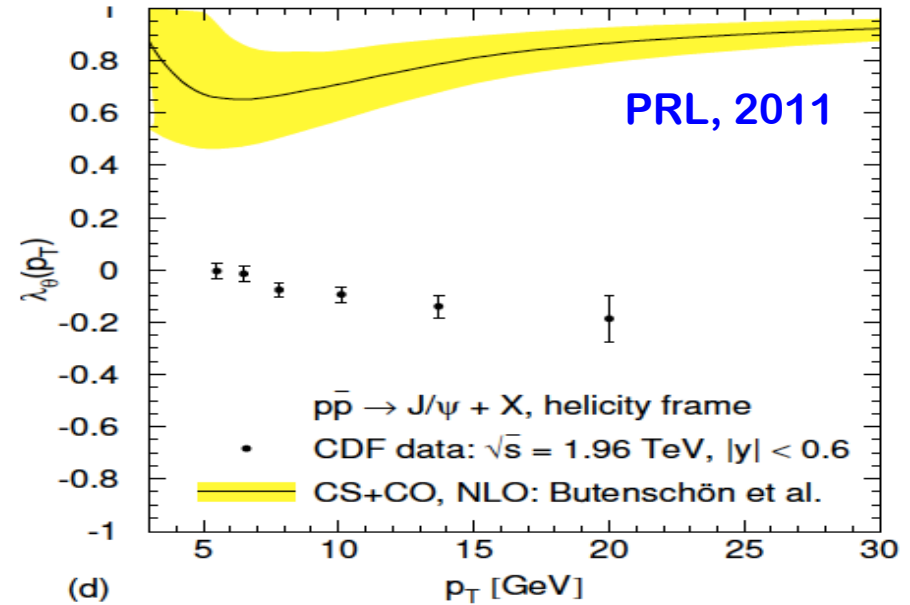
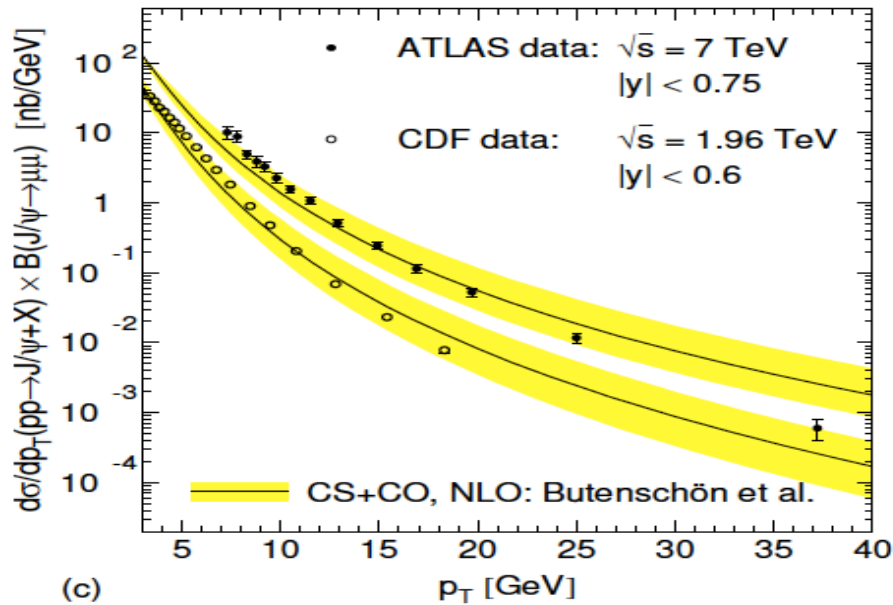
$$\langle O[{}^1S_0^{[8]}] \rangle = (4.97 \pm 0.44) \cdot 10^{-2} \text{ GeV}^3$$

$$\langle O[{}^3S_1^{[8]}] \rangle = (2.24 \pm 0.59) \cdot 10^{-3} \text{ GeV}^3$$

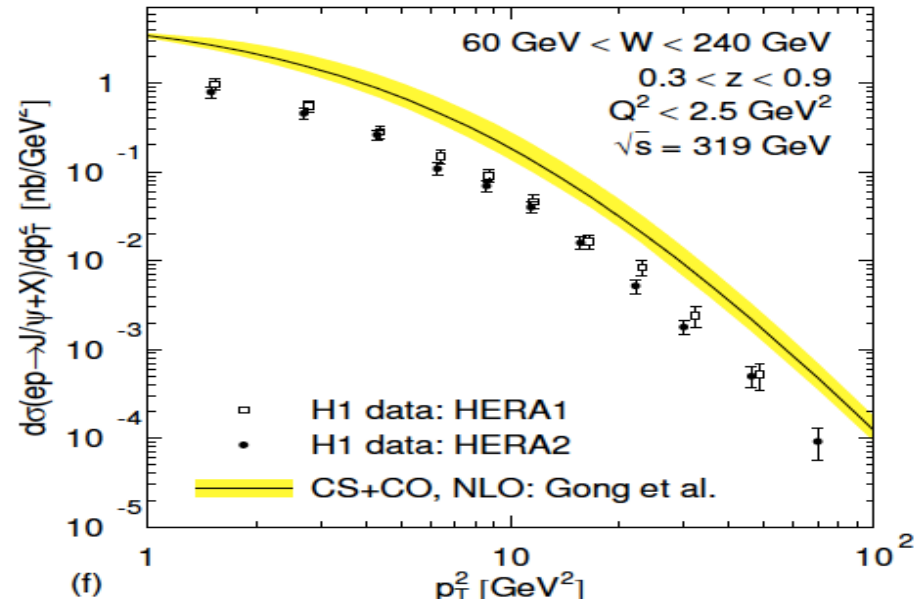
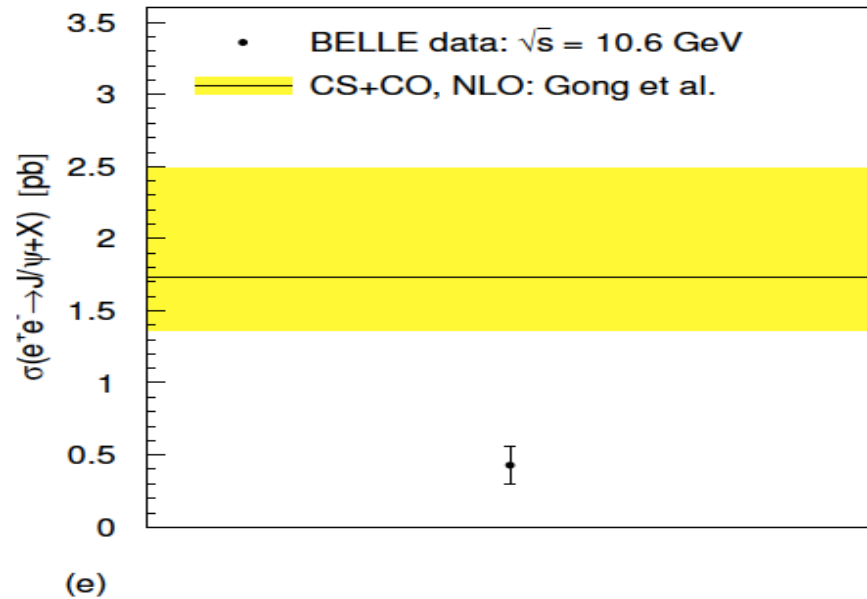
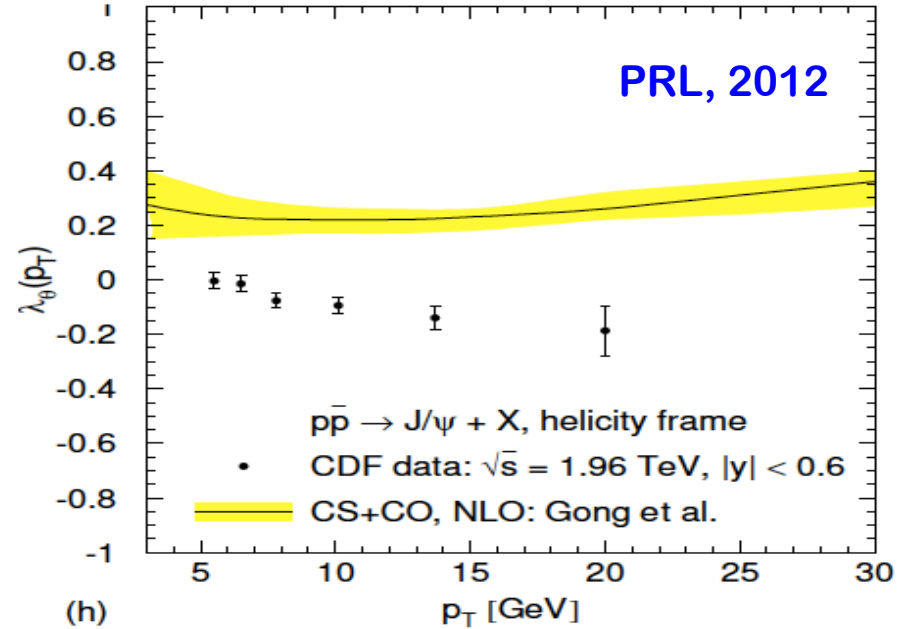
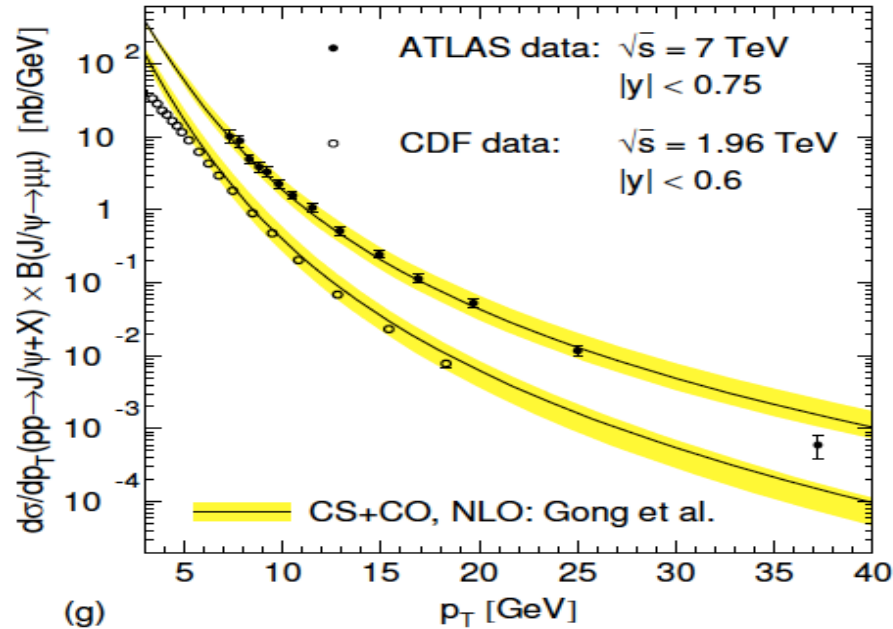
$$\langle O[{}^3P_0^{[8]}] \rangle = (-1.61 \pm 0.20) \cdot 10^{-2} \text{ GeV}^5$$

$$\chi^2/d.o.f. = 857/194 = 4.42$$

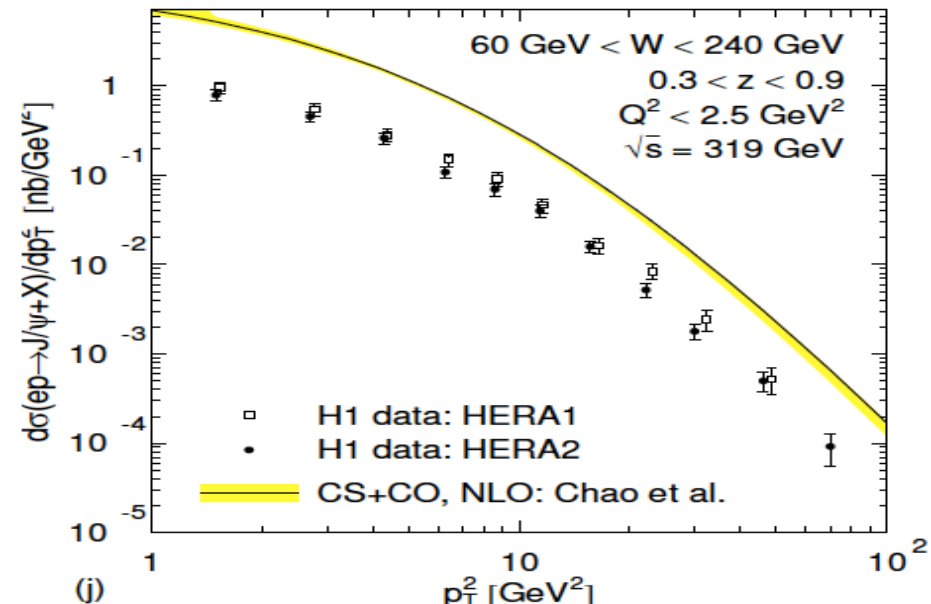
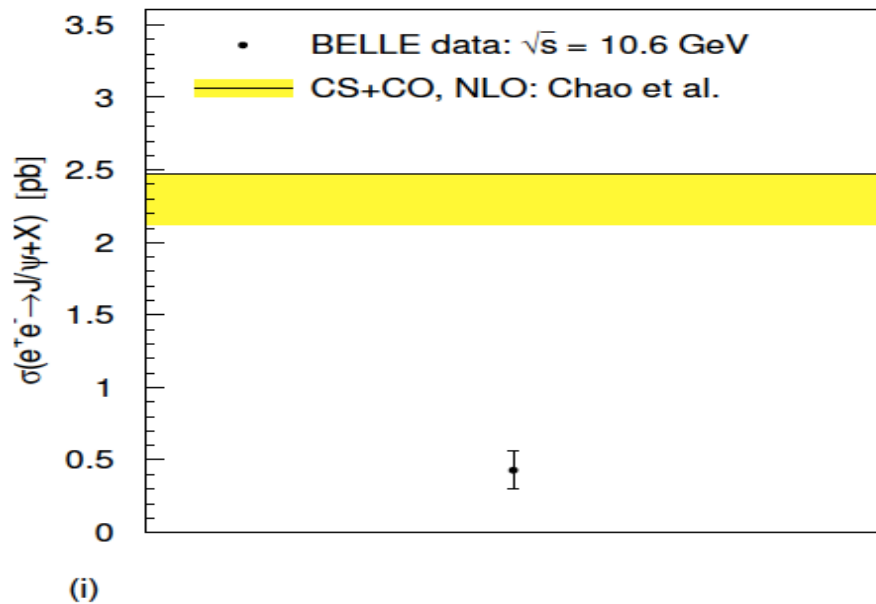
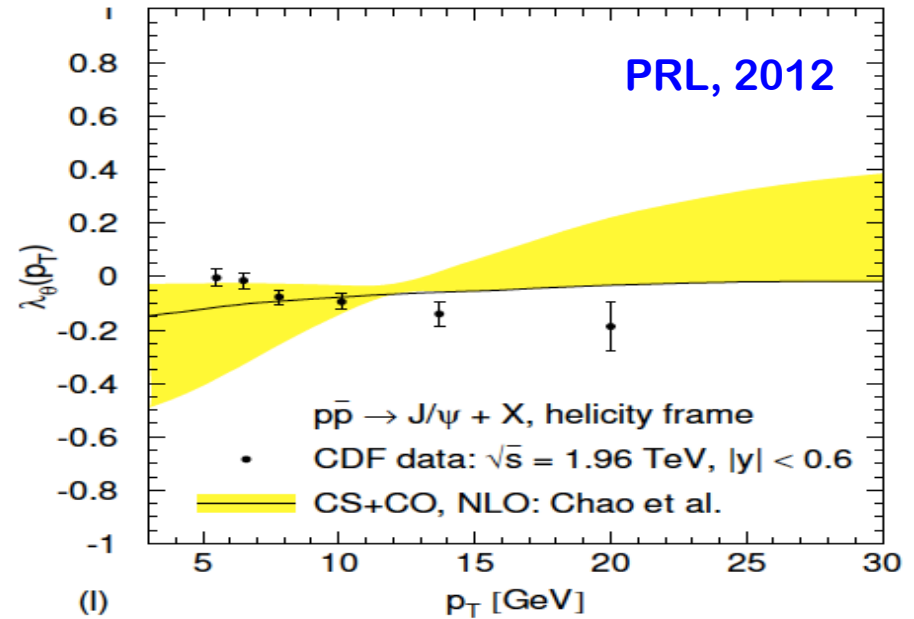
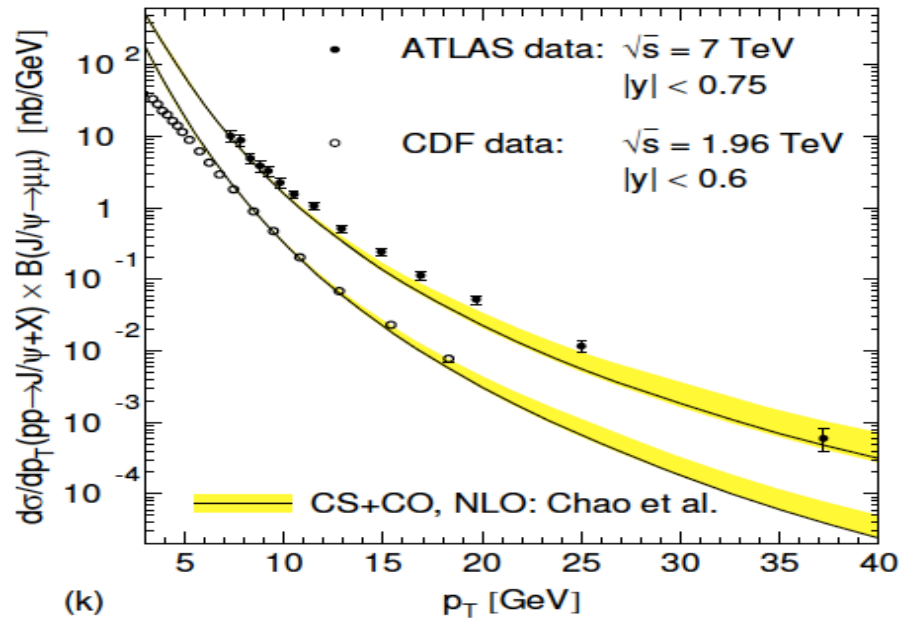
# NLO theory fits – Butenschön et al.



# NLO theory fits – Gong et al.



# NLO theory fits – Chao et al.

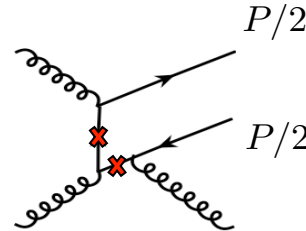


# Why high order corrections are so large?

Kang, Qiu and Sterman, 2011

- LO in  $\alpha_s$  but higher power in  $1/p_T$ :

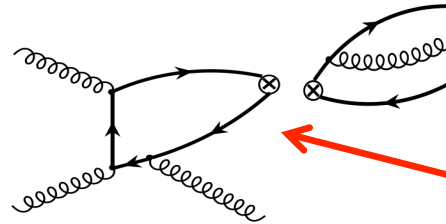
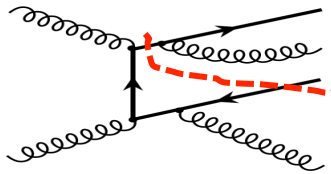
LO in  $\alpha_s$ :



$$\hat{\sigma}^{\text{LO}} \propto \frac{\alpha_s^3(p_T)}{p_T^8}$$

CSM and NRQCD  
spin-1 projection  
NNLP in  $1/p_T$ !

- NLO in  $\alpha_s$  but lower power in  $1/p_T$ :

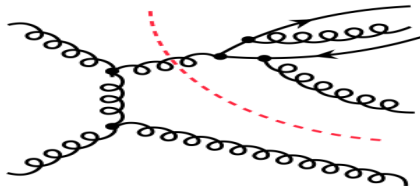


Relativistic  
projection to  
all  
“spin states”

$$\hat{\sigma}^{\text{NLO}} \rightarrow \frac{\alpha_s^3(p_T)}{p_T^6} \otimes \alpha_s(\mu) \log(\mu^2/\mu_0^2)$$

$$\mu_0 \gtrsim 2m_Q$$

- NNLO in  $\alpha_s$  but leading power in  $1/p_T$ :



$$\hat{\sigma}^{\text{NNLP}} \rightarrow \frac{\alpha_s^2(p_T)}{p_T^4} \otimes \alpha_s^3(\mu) \log^m(\mu^2/\mu_0^2)$$

Leading order in  $\alpha_s$ -expansion  $\neq$  leading power in  $1/p_T$ -expansion!



# New factorization formalism

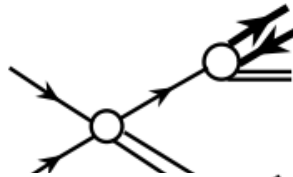
## Factorization formalism:

Kang, Qiu and Sterman, 2010

$$\begin{aligned}
 d\sigma_{A+B \rightarrow H+X}(p_T) = & \sum_i d\hat{\sigma}_{A+B \rightarrow i+X}(p_T/z, \mu) \otimes D_{i \rightarrow H}(z, m_Q, \mu) \\
 & + \sum_{[Q\bar{Q}(\kappa)]} d\hat{\sigma}_{A+B \rightarrow [Q\bar{Q}(\kappa)]+X}(P_{[Q\bar{Q}(\kappa)]} = p_T/z, \mu) \\
 & + \mathcal{O}(m_Q^4/p_T^4) \otimes D_{[Q\bar{Q}(\kappa)] \rightarrow H}(z, m_Q, \mu)
 \end{aligned}$$

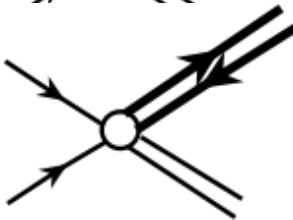
## Production of the pairs:

✧ at  $1/m_Q$ :



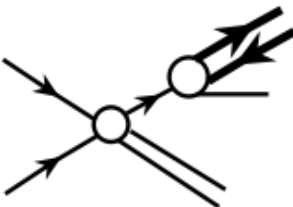
$D_{i \rightarrow H}(z, m_Q, \mu_0)$   
Transversely polarized pair

✧ at  $1/P_T$ :



$d\hat{\sigma}_{A+B \rightarrow [Q\bar{Q}(\kappa)]+X}(P_{[Q\bar{Q}]}(\kappa), \mu)$   
Longitudinally polarized pair

✧ between:  
[  $1/m_Q$  ,  $1/P_T$  ]



$$\begin{aligned}
 \frac{d}{d \ln(\mu)} D_{i \rightarrow H}(z, m_Q, \mu) = & \dots \\
 & + \frac{m_Q^2}{\mu^2} \Gamma(z) \otimes D_{[Q\bar{Q}(\kappa) \rightarrow H}(\{z_i\}, m_Q, \mu)
 \end{aligned}$$

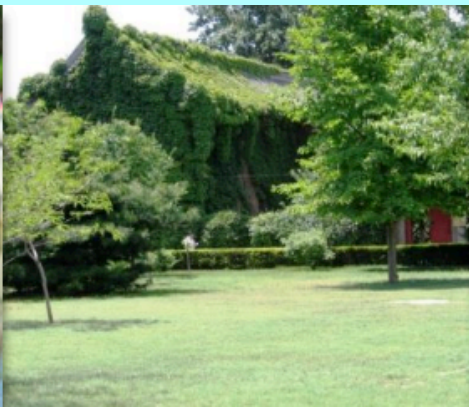
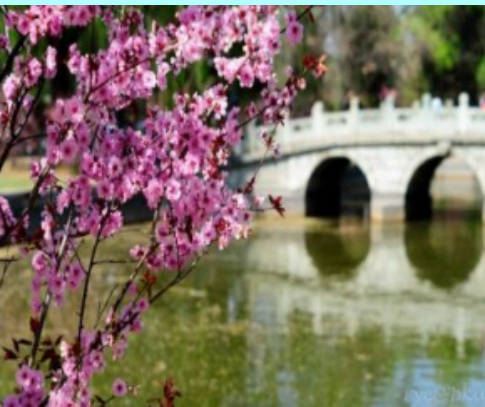
# Quarkonium 2017

The 12th International Workshop on Heavy Quarkonium



November 6-10, 2017, PKU, Beijing, China  
Organized by the Quarkonium Working Group

<http://itp.phy.pku.edu.cn/conference/qwg2017/>





# Electron-positron collider – CEPC

□ Ideal for studying the emergence of hadrons:

$$e^{+} + e^{-} \rightarrow \text{“Energy”} \rightarrow \text{Hadrons} + \text{Leptons...}$$

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$$\sigma(e^+ e^- \rightarrow J/\psi c \bar{c})$$

**Belle:**  $(0.87_{-0.19}^{+0.21} \pm 0.17) \text{ pb}$

**NRQCD:** 0.07 pb

Kiselev, et al 1994,  
Cho, Leibovich, 1996  
Yuan, Qiao, Chao, 1997

$$\sigma(e^+ e^- \rightarrow J/\psi c \bar{c}) / \sigma(e^+ e^- \rightarrow J/\psi X)$$

**Belle:**  $0.59_{-0.13}^{+0.15} \pm 0.12$

“Production rate of  $J/\psi c \bar{c}$   
larger than all these  
 $J/\psi gg, J/\psi q \bar{q}, \dots$   
channels combined!?”

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## □ At higher energy – CEPC:

$$e^+ + e^- \rightarrow \text{“Energy”} \rightarrow \text{Jets}(J/\psi, \dots) + \dots$$

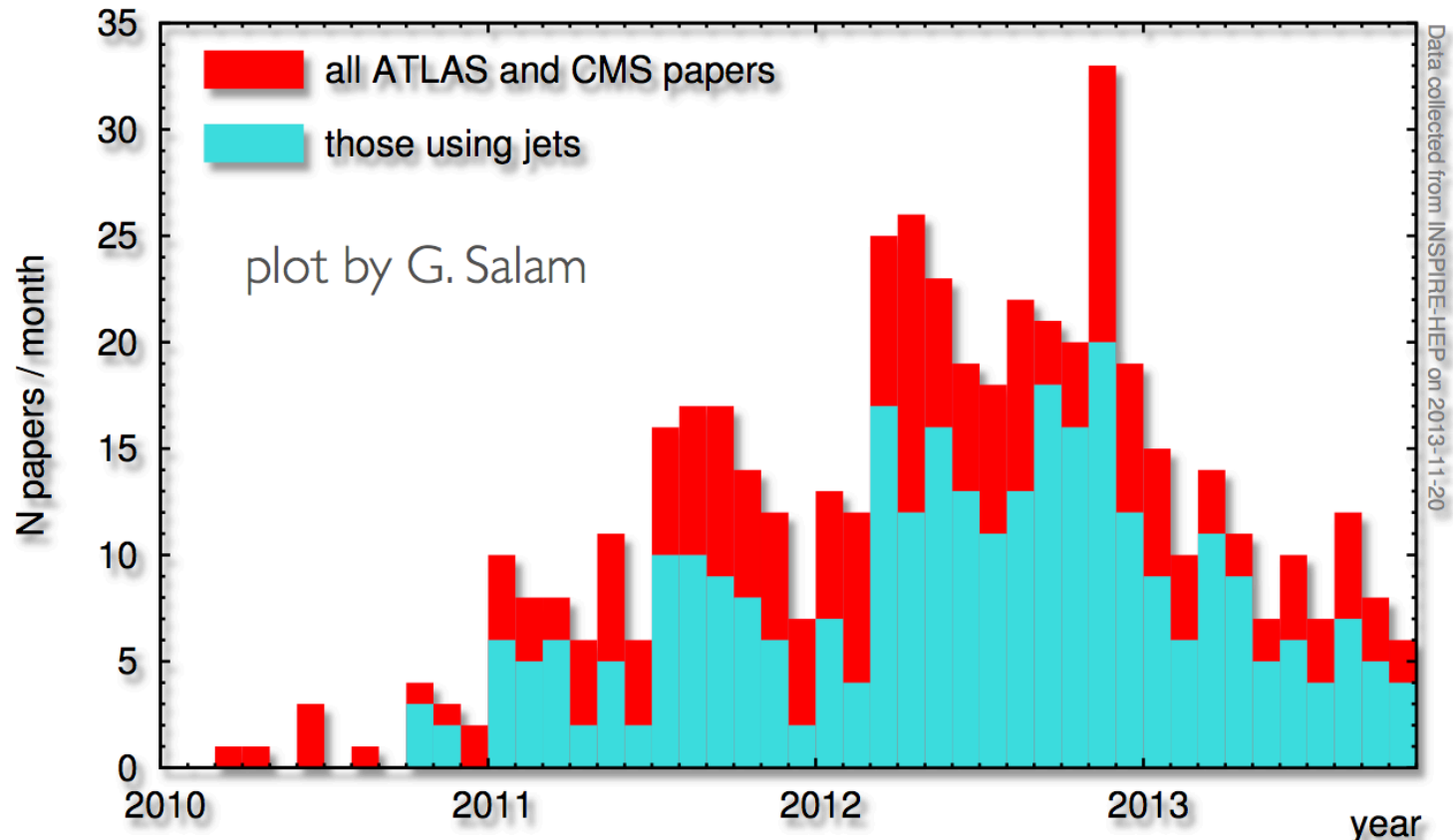
*Complementary or better way to test QCD and the SM*

$$e^+ + e^- \rightarrow \text{“Energy”} \rightarrow H^0(\rightarrow J/\psi(\Upsilon) + \gamma, \dots) + \dots$$

*Potential for testing Higgs couplings, and beyond the SM*

# Jets are everywhere at the LHC

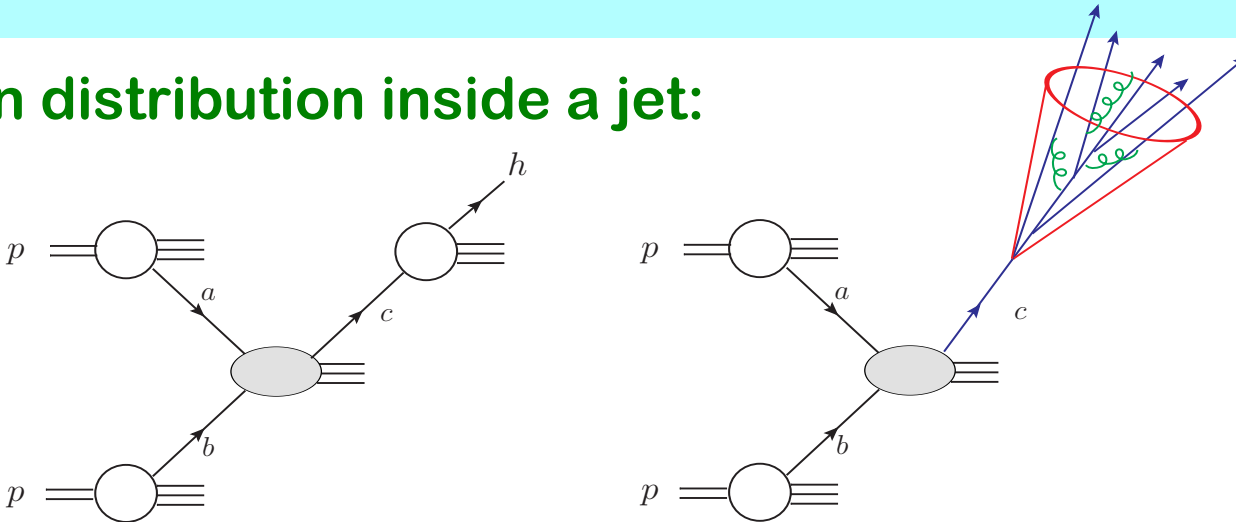
□ 60–70% of ATLAS & CMS papers using jets in their analysis!



- ✧ Jets as a precision probe of QCD: precision  $\alpha_s$ ,  $g(x)$ , ...
- ✧ Jets as a tool for BSM physics: jet correlation, jet sub-structure, ...
- ✧ Jet sub-structure: longitudinal vs transverse, ...

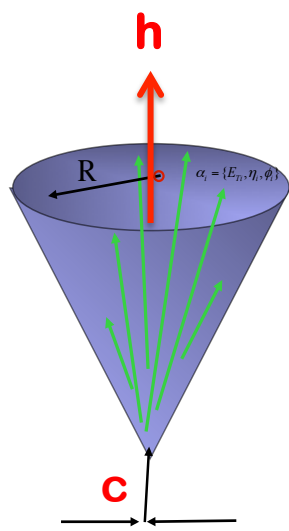
# Jet & jet fragmentation function

## Hadron distribution inside a jet:



$$\frac{d\sigma^{pp \rightarrow hX}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab \rightarrow c} \otimes D_c^h$$

$$\frac{d\sigma^{pp \rightarrow \text{jet} X}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab \rightarrow c} \otimes J_c(\mu \sim p_T R)$$

$$\frac{d\sigma^h}{dy dp_T dz_h} \propto \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab \rightarrow c} \otimes \mathcal{G}_c^h(z, z_h, R, \mu)$$


## Jet fragmentation:

$$F(z_h, p_T) = \frac{d\sigma^h}{dy dp_T dz_h} \bigg/ \frac{d\sigma}{dy dp_T}$$

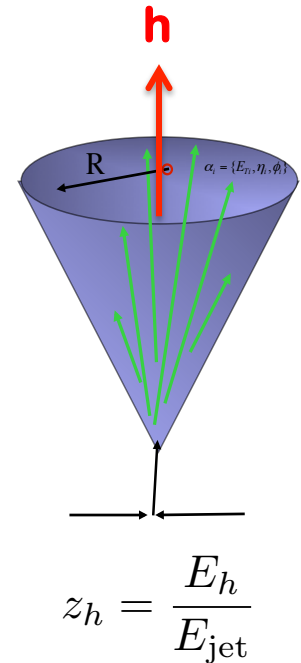
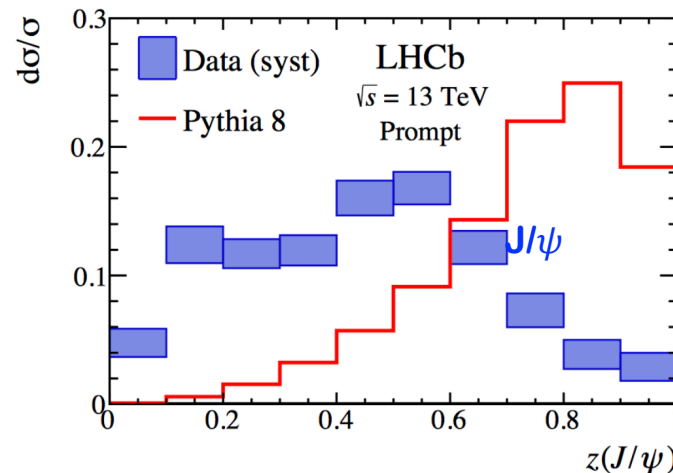
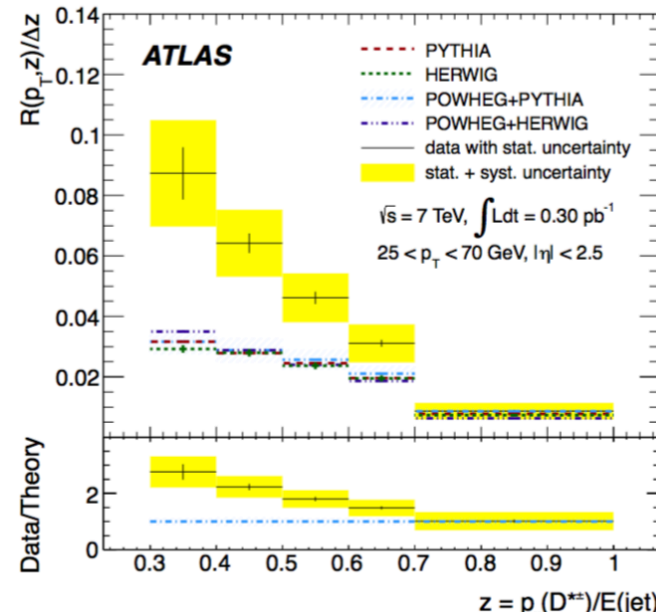
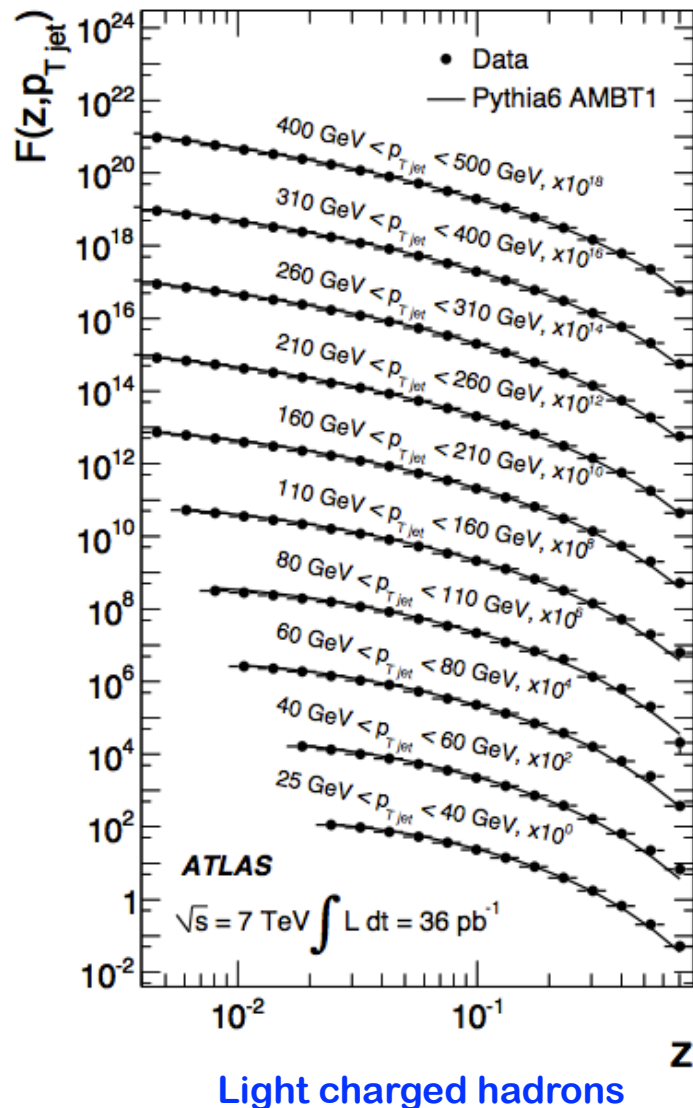
$$z_h = p_T^h / p_T$$

$$z = p_T / p_T^c$$

*First produce a jet, and then look further for a hadron inside the jet!*

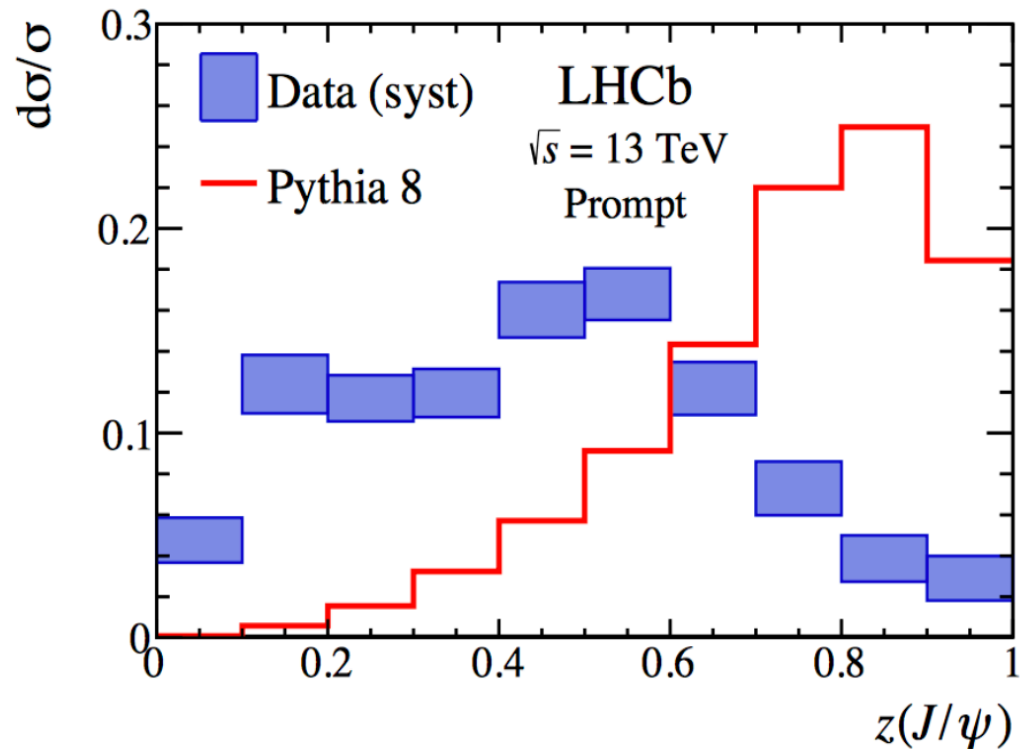
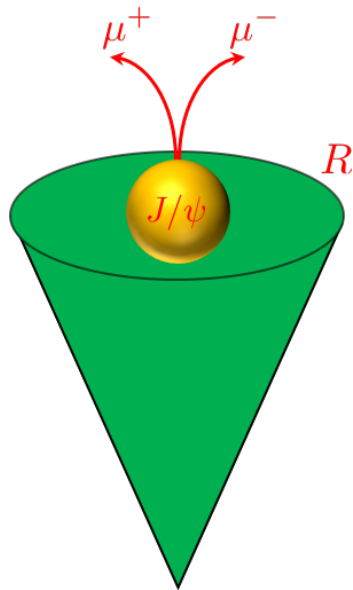
# Lots of data at the LHC

## Hadron distribution inside a jet – puzzle for heavy flavor?



# Quarkonium production inside a jet

## □ $J/\psi$ -in-jet measurement from LHCb:



**Production:** Baumgart, et al., JHEP 14, Bain, et al., PRL17

**Polarization:** Kang, Ringer, Xing, et.al., PRL17

$$\frac{d\sigma^{J/\psi(\rightarrow \ell^+ \ell^-)}}{d\cos\theta} \propto 1 + \lambda_F \cos^2\theta$$

$$\lambda_F = \begin{cases} +1, & \text{transversely polarized} \\ -1, & \text{longitudinally polarized} \end{cases}$$

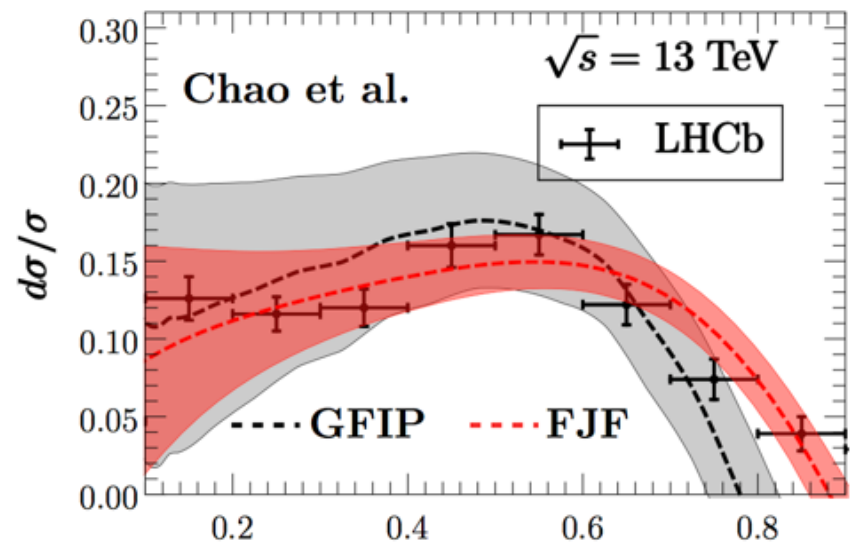
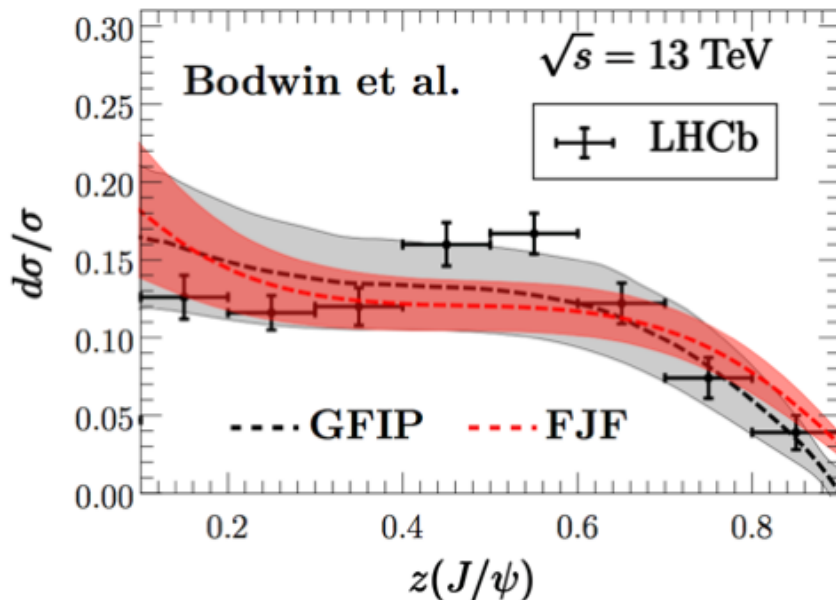
# $J/\psi$ production in jets

## □ Fitted NRQCD matrix elements:

Baumgart et al., JHEP14

Bain et al. PRL17

	$\langle \mathcal{O}^{J/\psi}(^3S_1^{[1]}) \rangle$ $\times \text{GeV}^3$	$\langle \mathcal{O}^{J/\psi}(^3S_1^{[8]}) \rangle$ $\times 10^{-2} \text{GeV}^3$	$\langle \mathcal{O}^{J/\psi}(^1S_0^{[8]}) \rangle$ $\times 10^{-2} \text{GeV}^3$	$\langle \mathcal{O}^{J/\psi}(^3P_0^{[8]}) \rangle / m_c^2$ $\times 10^{-2} \text{GeV}^3$
B & K [5, 6]	$1.32 \pm 0.20$	$0.224 \pm 0.59$	$4.97 \pm 0.44$	$-0.72 \pm 0.88$
Chao, et al. [12]	$1.16 \pm 0.20$	$0.30 \pm 0.12$	$8.9 \pm 0.98$	$0.56 \pm 0.21$
Bodwin et al. [13]	$1.32 \pm 0.20$	$1.1 \pm 1.0$	$9.9 \pm 2.2$	$0.49 \pm 0.44$



FJFs: fragmentation jet functions

GFIP: gluon fragmentation improved PYTHIA

Two are consistent



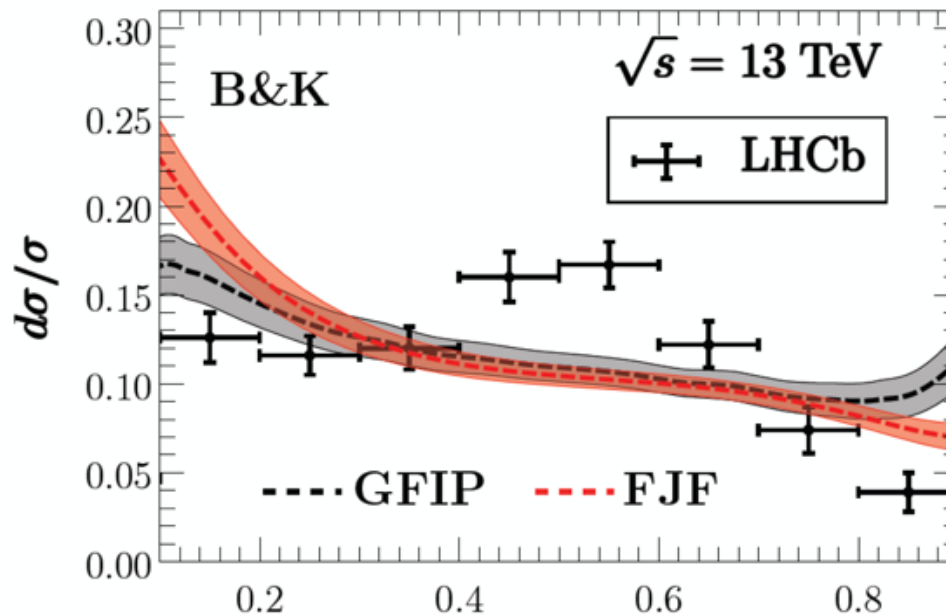
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FJFs: fragmentation jet functions

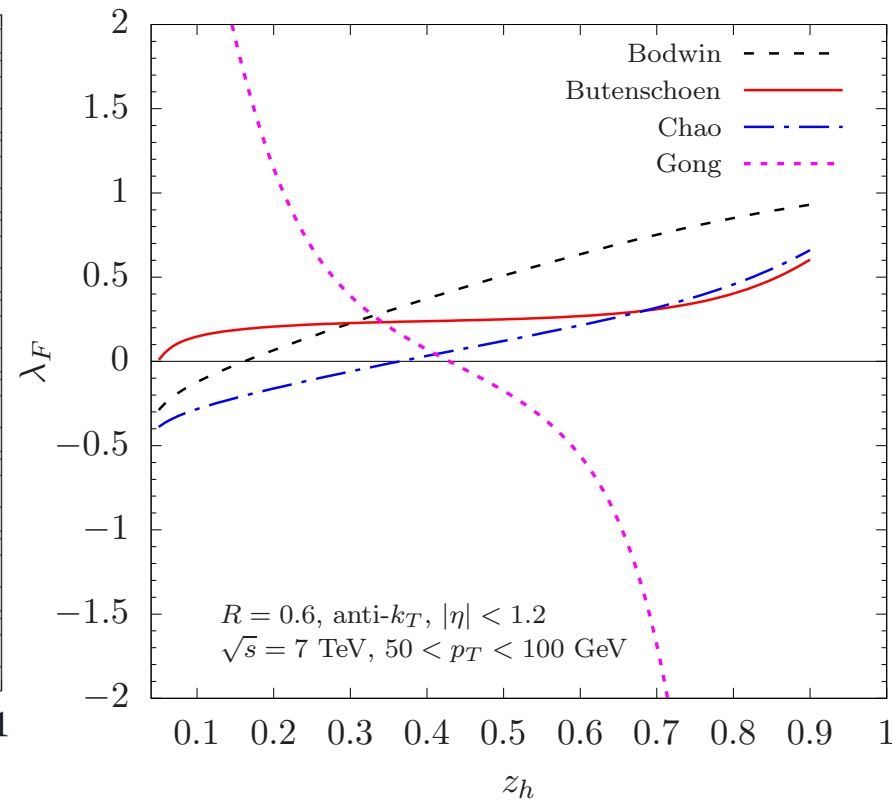
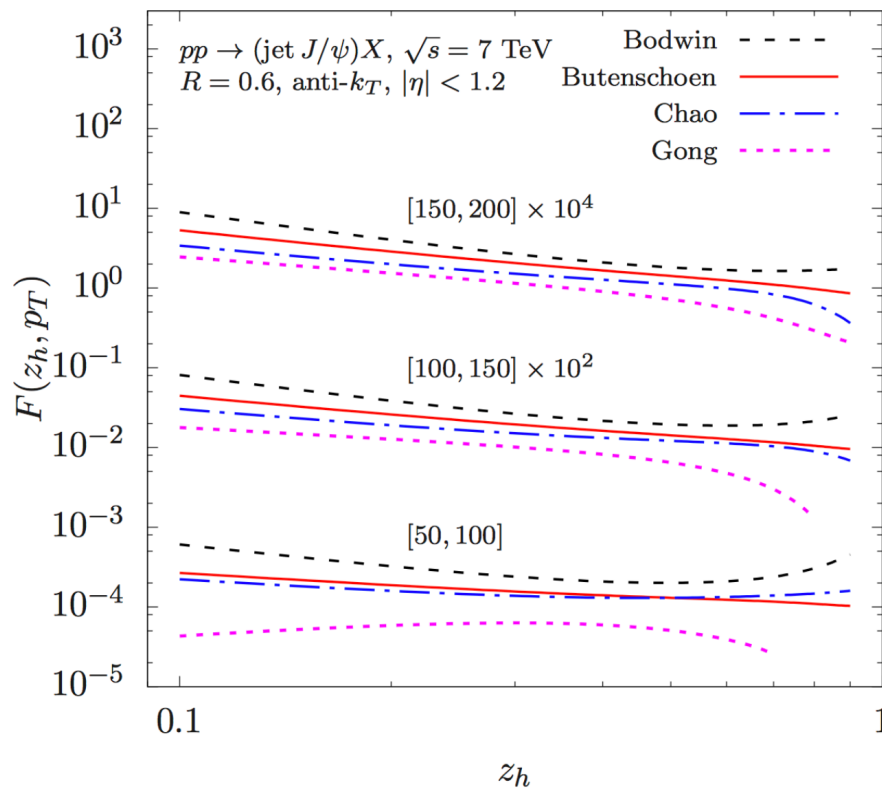
GFIP: gluon fragmentation improved PYTHIA

This fit has a poor agreement with jet data

# $J/\psi$ production and polarization in jets

## □ Polarization is even more sensitive:

Kang, Qiu, Ringer, Xing, Zhang, PRL 2017  
See also Bain, et al, PRL 2017

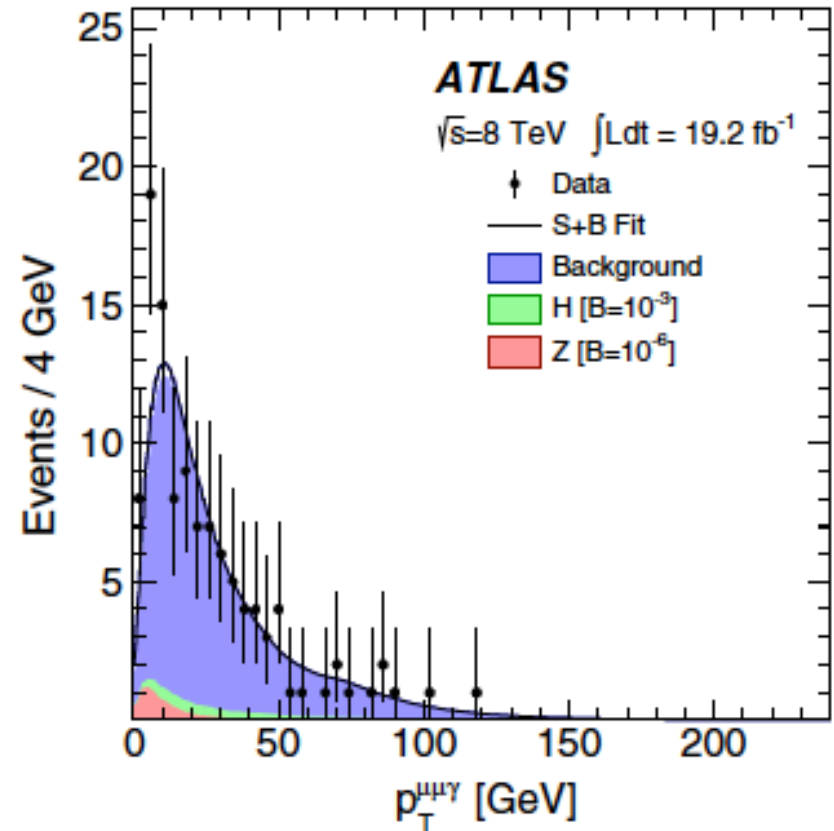
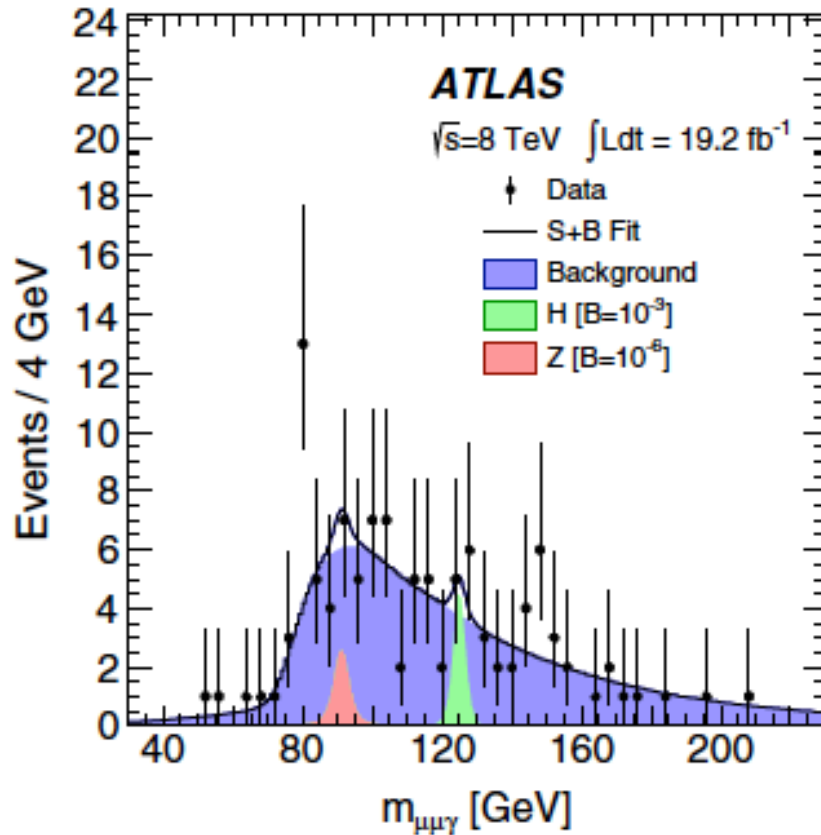


**More differential than inclusive  $J/\psi$   $p_T$  spectrum, and can better discriminate different NRQCD parameterizations**

# Higgs decays to quarkonium + $\gamma$ at the LHC

## □ $J/\psi$ + isolated $\gamma$ :

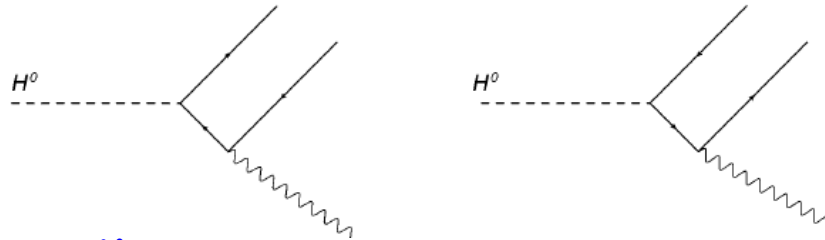
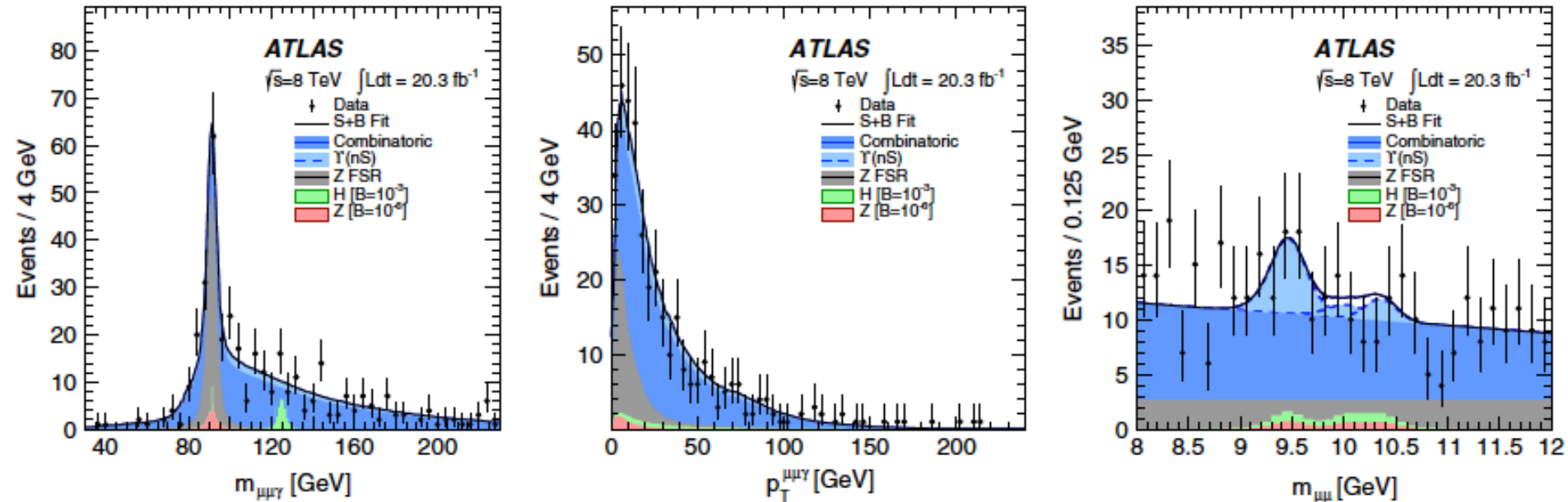
G. Aad et al. PRL114, 121801 (2015)



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□  $Y(n) + \text{isolated } \gamma$ :



- ✧ Branching ratio
- ✧ Flavor dependence of Higgs couplings
- ✧ NLO calculation for CEPC
- ✧ ...

# Summary and outlook

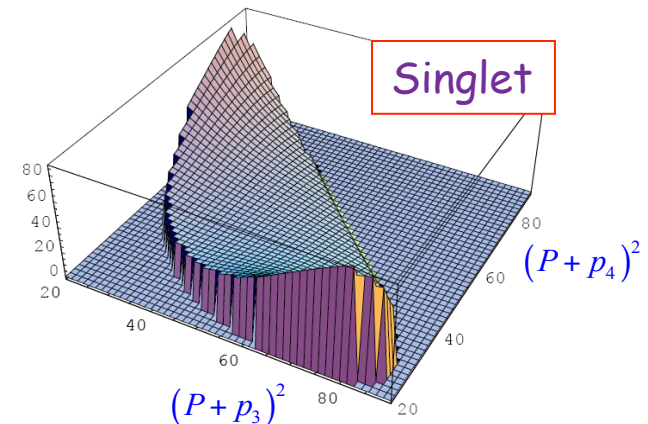
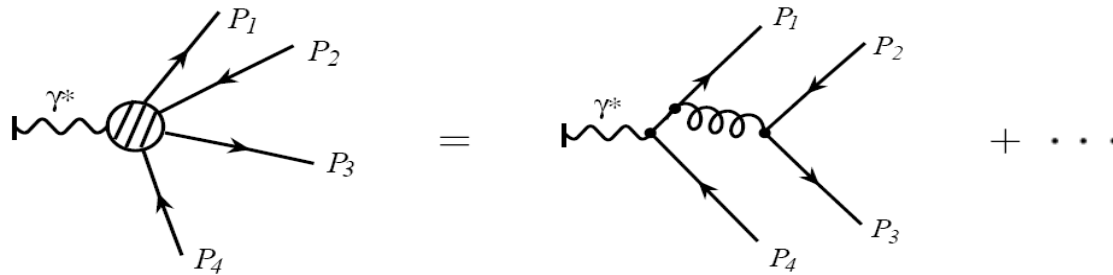
- ❑ It has been over 40 years since the discovery of  $J/\psi$
- ❑ When  $p_T(E) \gg m_Q$  at collider energies, earlier model calculations for the production of heavy quarkonia are not perturbatively stable  
LO in  $\alpha_s$ -expansion may not be the LP term in  $m_Q/p_T(E)$ -expansion
- ❑ QCD factorization works for both LP and NLP ( $\alpha_s$  for each power)  
Sub-leading power is very important for the  $p_T$ -shape and polarization  
*There are still a lot of unanswered questions related to quarkonium!*
- ❑ Quarkonium production and polarization in the jet could be very good observables to help pin down the production mechanism
- ❑ CEPC provides a clean and good environment for studying the emergence of heavy quarkonia/hadrons, and the potential for testing the SM and exploring the BSM physics

**Thank you!**

**Backup slides**

# Associated production at B-factory

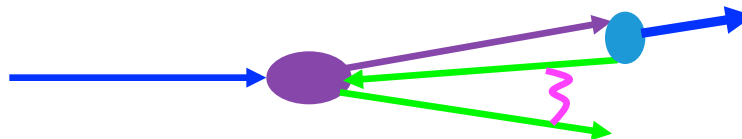
## □ Kinematically preferred configuration:



Production rate of a singlet charm quark pair is dominated by the phase space where  $s_3=(P_1+P_2+P_3)^2$  or  $s_4=(P_1+P_2+P_4)^2$  near its minimum

## □ NRQCD formalism does not apply when there are more than one heavy quark velocity involved

## □ Color transfer enhances associated heavy quarkonium production



A heavy quark as a color source to enhance the transition rate for an octet pair to become a singlet pair