

BEAM ENERGY MEASUREMENT (BEM)

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CEPC workshop @IHEP
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OUTLINE

- Introduction
- Compton scattering method
- Summary

To show the feasibility of Compton scattering method.

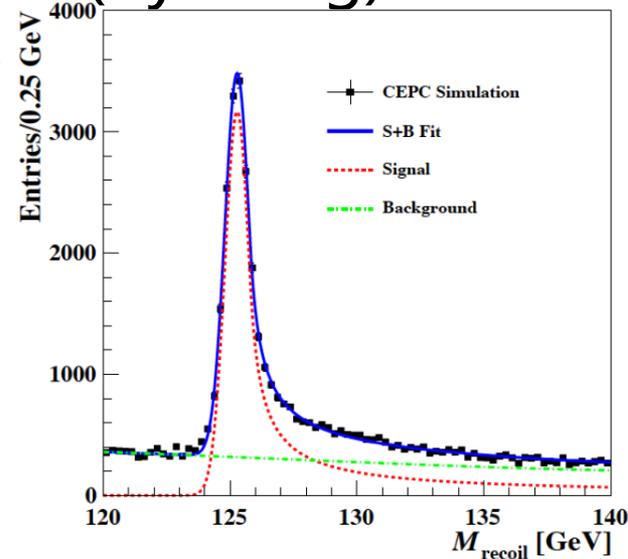
INTRODUCTION

- Higgs Mass from Recoil Mass method (by Gang)

$$\delta m_{\mu\mu}^{rec} = \begin{cases} (0.31 \sim 0.81)\epsilon = (0.44 \sim 1.14)\delta E_B & \text{uncorrelated} \\ 2\epsilon = 4\delta E_B & \text{correlated} \end{cases}$$

- If we require $\delta M_{recoil} \begin{cases} < 5.4\text{MeV} \\ < 1\text{MeV} \end{cases}$,

$$\text{than, } \delta E_B \begin{cases} < 1.35 \sim 12\text{MeV} \\ < 0.25 \sim 2.3\text{MeV} \end{cases}$$



- $\sigma(ZH)$ measurement

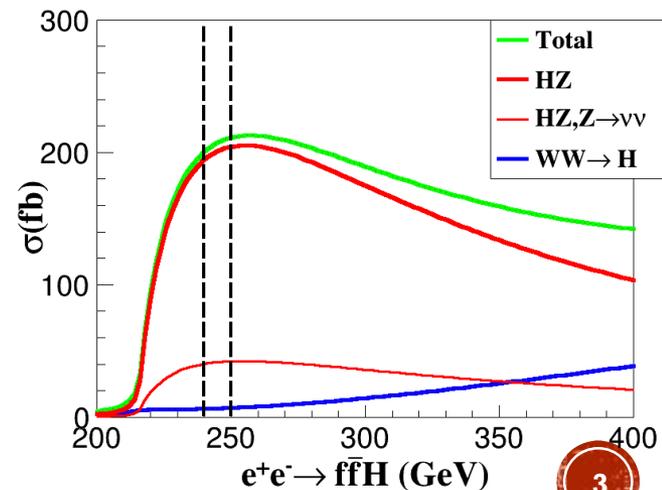
- Find Left/Right Shift with 0.5%

$$\sigma(ZH) = 200.5\text{fb}@240\text{GeV}$$

$$200.5\text{fb} \cdot (1.005) \sim @240.6\text{GeV}$$

$$200.5\text{fb} \cdot (0.995) \sim @239.5\text{GeV}$$

$$\text{than, } \delta E_{cm} < 500\text{MeV}.$$



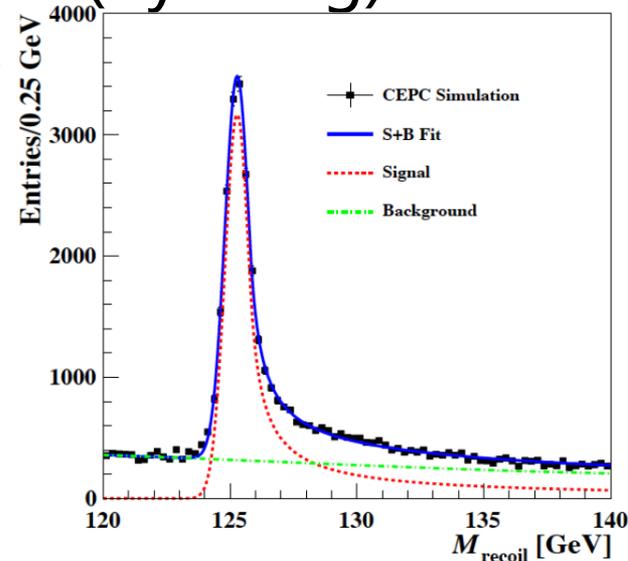
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- No significant impact on other Higgs program
 - Event/Background selection efficiency.
 - $\sigma(ZH)$ measurement requires $\delta E_{cm} < 500\text{MeV}$.
 - Branching ratio ($\text{Br}(H \rightarrow b\bar{b})$) requires $\delta m_H < 130\text{MeV}$.

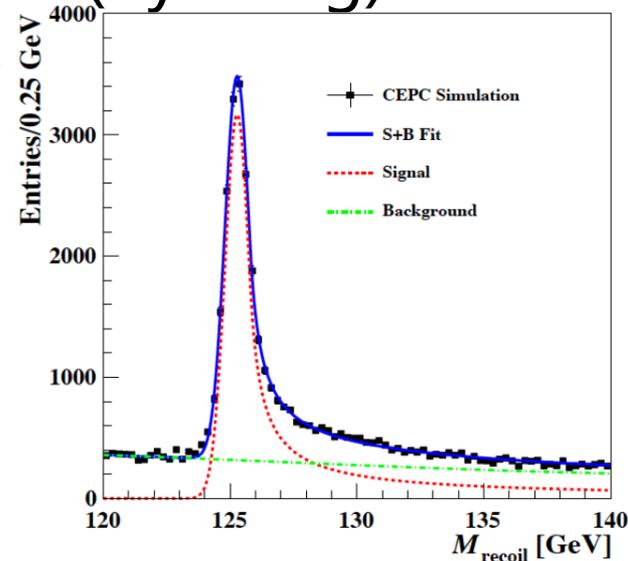
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- WW threshold & Z pole:

at least $\delta E_B < 1\text{MeV} \sim \text{LEP precision } 2 \times 10^{-5}$

- Try to do it better, $\delta E_B < 100\text{keV}$

BEAM ENERGY MEASUREMENT

- $\mu\mu\gamma$ events (by Qinglei)
 - Uncertainty $\sim 40\text{-}50\text{MeV}$ (CM energy)
- Resonant depolarization technique (@Z-pole, LEP)
 - Uncertainty $\sim 2 \times 10^{-5}$ (relative, beam energy)
- Compton scattering method. (beam energy)
- J/ψ production with other beams. (beam energy)
- ...

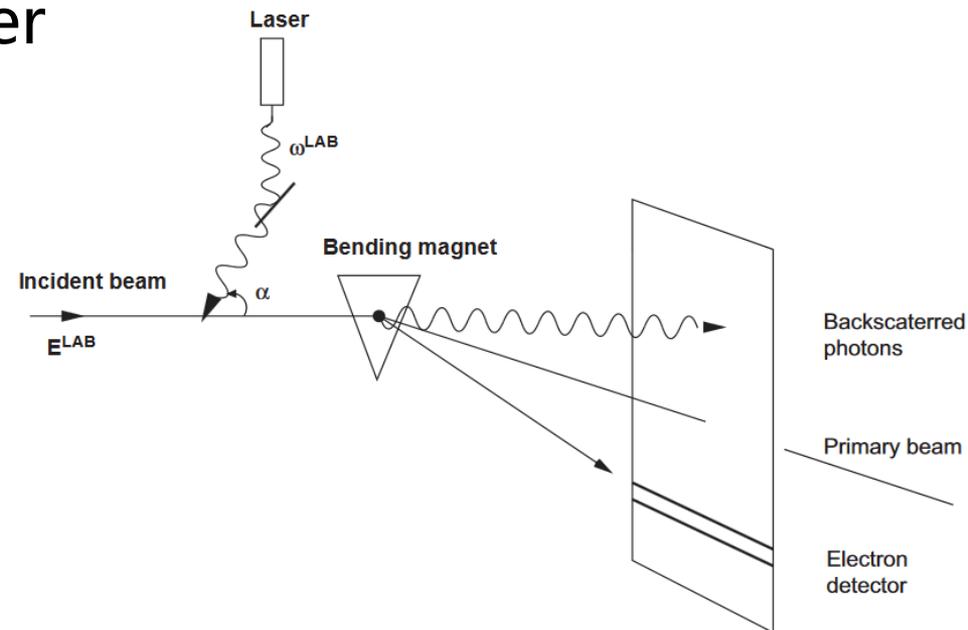
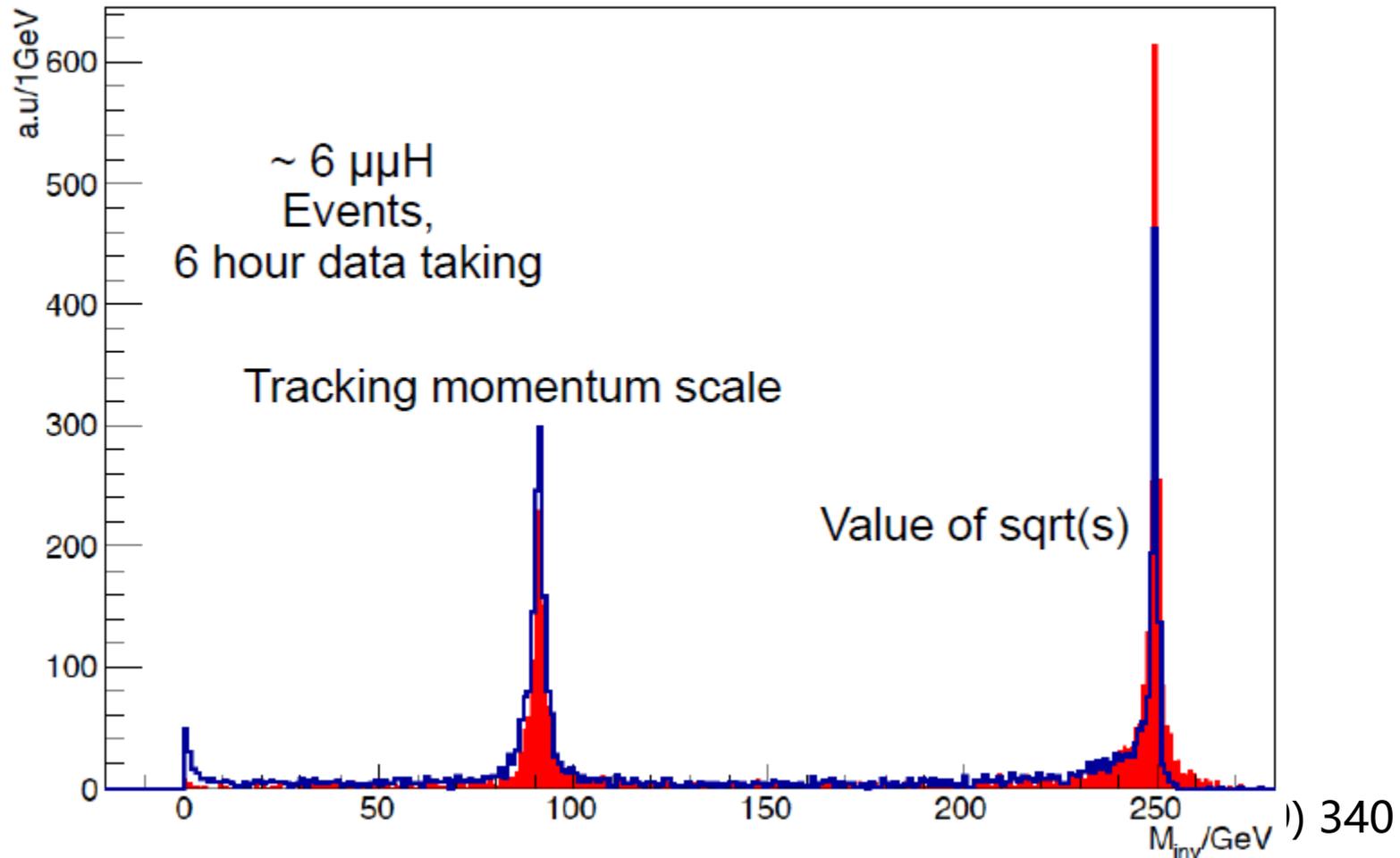


Fig. 8. Scheme of the proposed energy spectrometer based on Compton backscattering.

BEAM ENERGY MEASUREMENT

- $\mu\mu\gamma$ events (by Qinglei)
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Invariant Mass of dimuon (+ photon) for $\mu\mu\gamma$ events



BEAM ENERGY MEASUREMENT

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- @CEPC: pre-CDR
 - Typical time to form polarized beam: 21 min
 - Beam lift time: 25 min
 - Feasible or not in this case?

BEAM ENERGY MEASUREMENT

- $\mu\mu\gamma$ events (by Qinglei)
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- Compton scattering method. (beam energy)
 - $E_{beam} \sim f(\alpha, \omega, \omega')$;
 - α : crossing angle;
 - ω : laser photon energy;
 - ω' : maximum energy of outgoing photon.

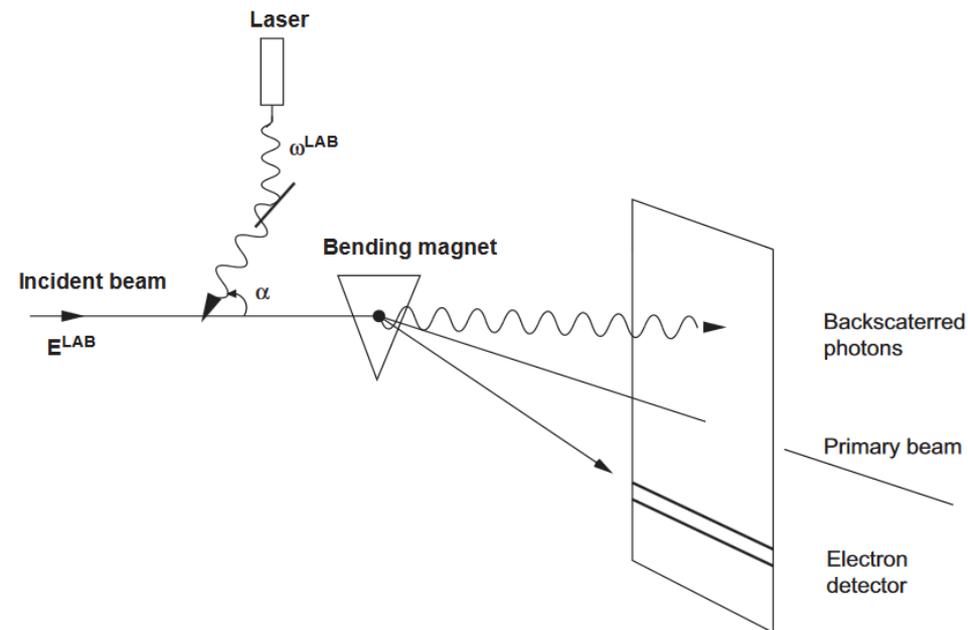
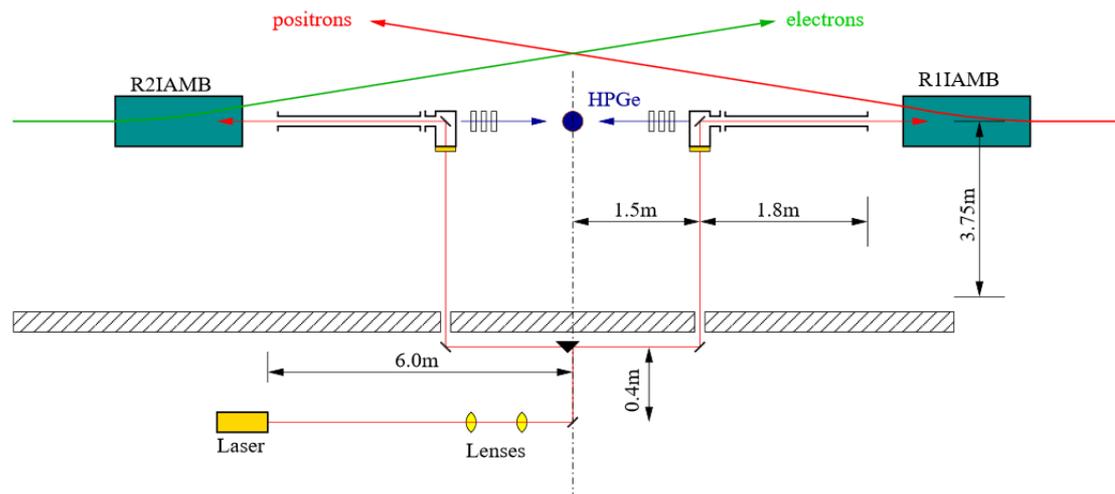


Fig. 8. Scheme of the proposed energy spectrometer based on Compton backscattering.

- Compton Back-scattering: (crossing angle $\alpha = 0$)

- $$E_{beam} = \frac{\omega'}{2} \sqrt{1 + \frac{m_e^2}{\omega \omega'}}$$

- Hardware: locate at north IP of BEPCII
 - CO_2 Laser ($\omega=0.117\text{eV}$, 50W) and optical system.
 - High purity germanium detector: 16384 channels.
 - Pulse generator and isotopes (Cs, Co, ...).
 - Data acquisition system.
- Side by side measurement.



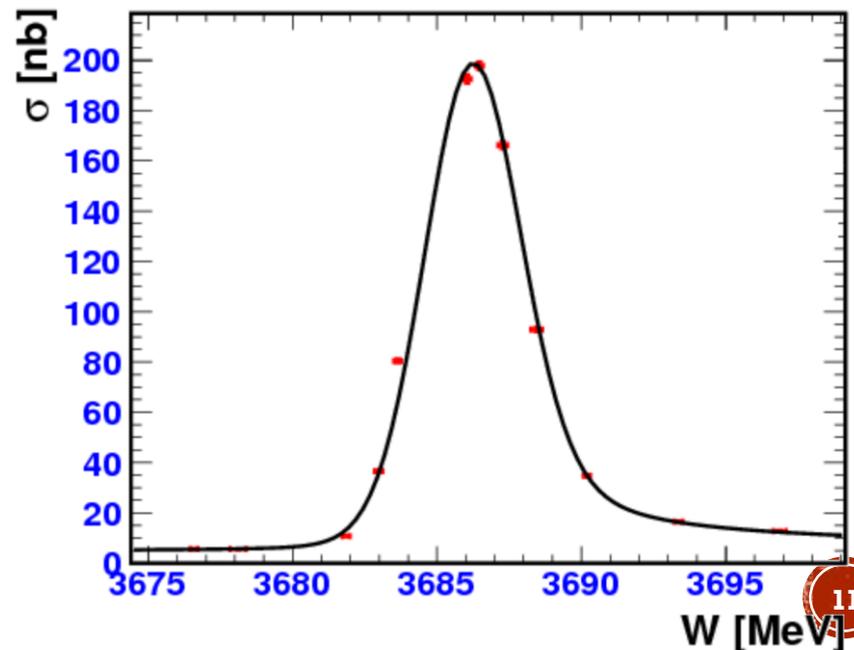
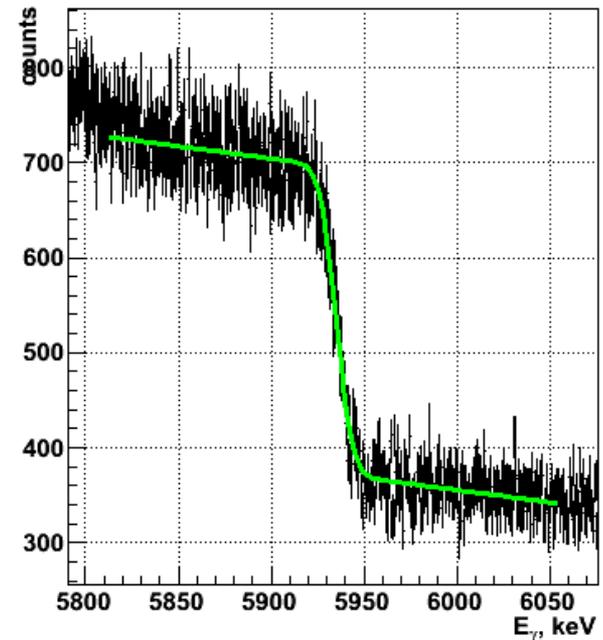
BEM@BEPCII

- Compton Back-scattering: (crossi

- $E_{beam} = \frac{\omega'}{2} \sqrt{1 + \frac{m_e^2}{\omega \omega'}}$

- Calibration** with isotopes and pulse generator.
- Fit** of maximum photon energy (Compton edge).
- Performance studied by comparison of $\psi(2S)$
 - relative uncertainty $\sim 2 \times 10^{-5}$

Positrons: 2010.11.23 | 06:32:58 -- 11:34:01 | 2010.11.23



BEAM ENERGY MEASUREMENT

- If we do the same work @CEPC
 - **120GeV**(beam) + **0.11eV**(CO2 laser) → **20GeV** (maximum scattering photon energy). Too large to be measured precisely.
 - Change crossing angle, $\alpha \in (3.06, 3.13)$.
The maximum energy of outgoing photon $\omega' \in (1,40)$ MeV.

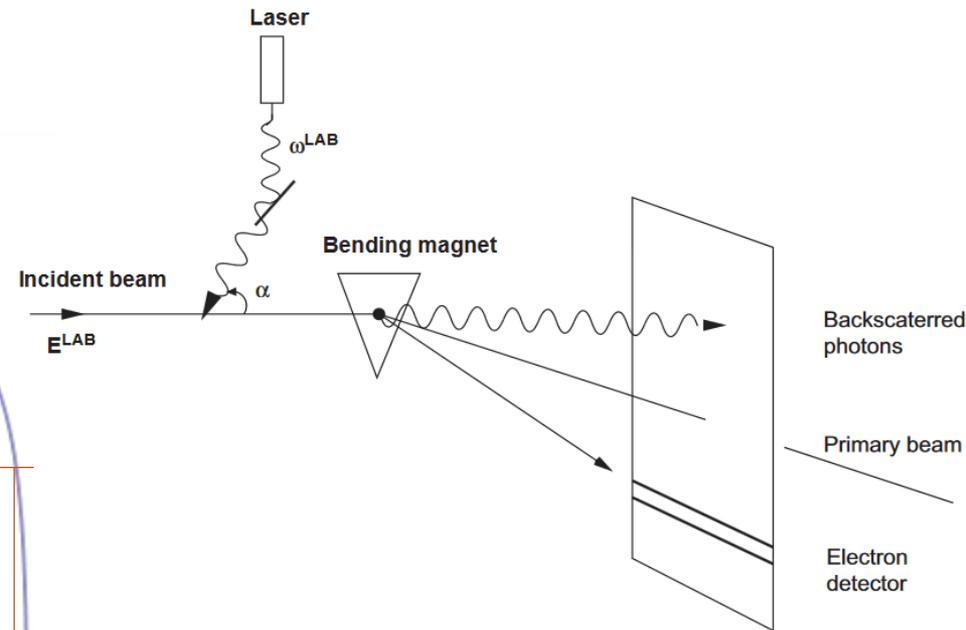
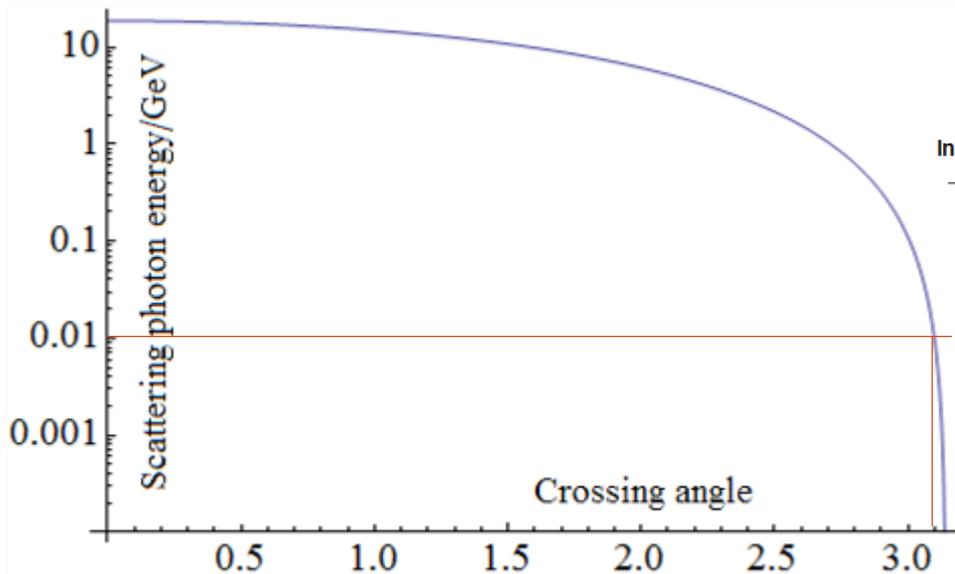


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The maximum energy of outgoing photon $\omega' \in (1, 40)\text{MeV}$.



- Easy to calibrate and detect
 - High SR background
 - Difficult to calibrate and detect
 - Low SR background
- Optimize the choice of crossing angle by a full simulation.

ERROR PROPAGATION

- Example: crossing angle $\alpha = 3.086$, (scatter maximum 20MeV photon)

- $\delta E_{beam} \sim \sqrt{(2.2 \times 10^6 \times \delta\alpha)^2 + (3.0 \times 10^3 \times \delta\omega')^2}$

- If $\delta E_{beam} < 1\text{MeV}$, $\delta\alpha < 4.2 \times 10^{-7}$ and $\delta\omega' < 3 \times 10^{-4}\text{MeV}$.

- Impact on $\delta\alpha$:

- Beam orbit, variance of beam momentum $\delta\vec{p}$;
 - Laser alignment.

- Impact on $\delta\omega'$:

- Detector calibration;
 - Statistic error.

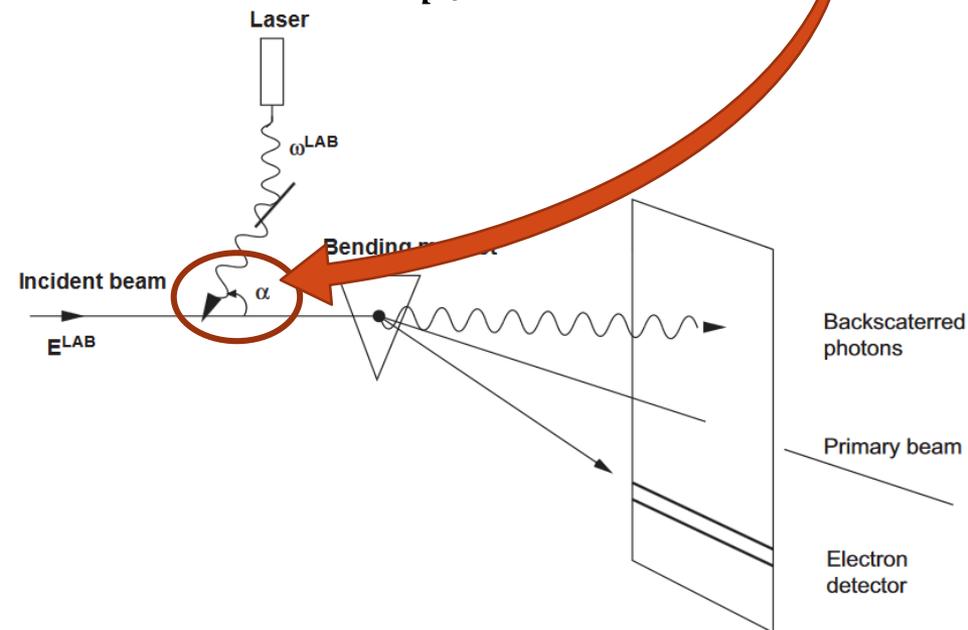


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- Impact on $\delta\omega'$:

- Detector calibration;
 - Statistic error.

- Beam position monitor + long linear orbit

- Long laser path

ERROR PROPAGATION

- Beam position monitor + long linear orbit.

To measure the mean value of α .

- if BPM precision **0.1mm**, **2km** linear orbit is needed.
- variance of beam momentum δp_{\perp} , δp_{\parallel}
 - If $\frac{\delta p_{\perp}}{p} < 4.2 \times 10^{-7}$, acceptable systematic error.
 - If $\frac{\delta p_{\perp}}{p} \geq 4.2 \times 10^{-7}$, the ω' will be **smearred**. The distribution should be known or estimated to extract ω' .
 - Beam energy spread $(\delta p_{\parallel}, \delta p_{\perp}) \sim 0.1\%$. Need to know the beam energy distribution. (Maybe Gaussian is a reasonable assumption.)
- It is crucial to input beam parameters to BEM.

ERROR PROPAGATION

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- Impact on $\delta\alpha$:

- Beam orbit, variance of beam momentum $\delta\vec{p}$;
 - Laser alignment.

- Impact on $\delta\omega'$:

- Detector calibration;
 - Statistical error.

- Isotopes to calibrate detector.

- Co, Cs, plutonium-carbon... Still need more.

- Signal-noise ratio? Statistical error?

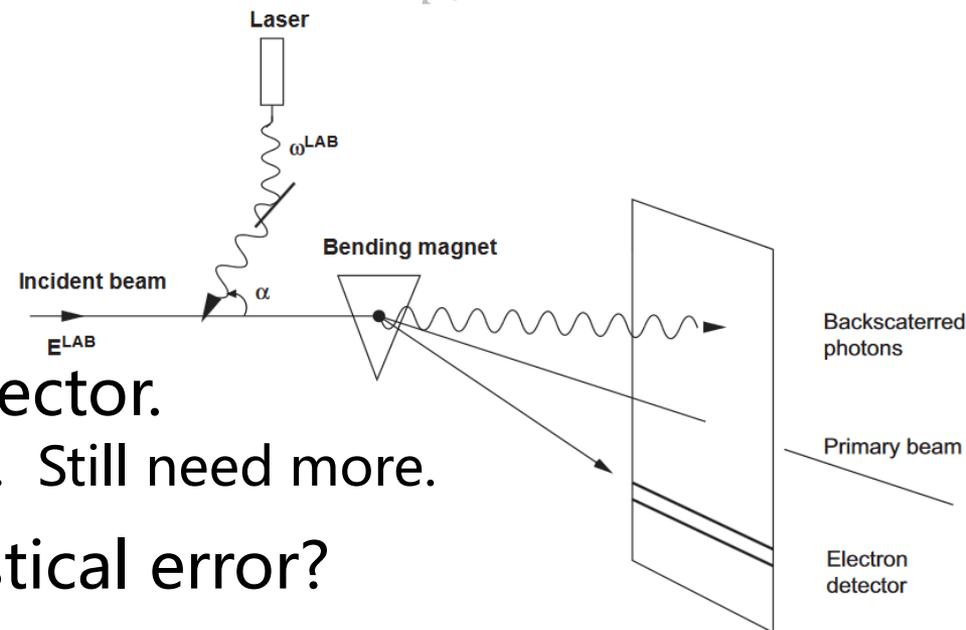


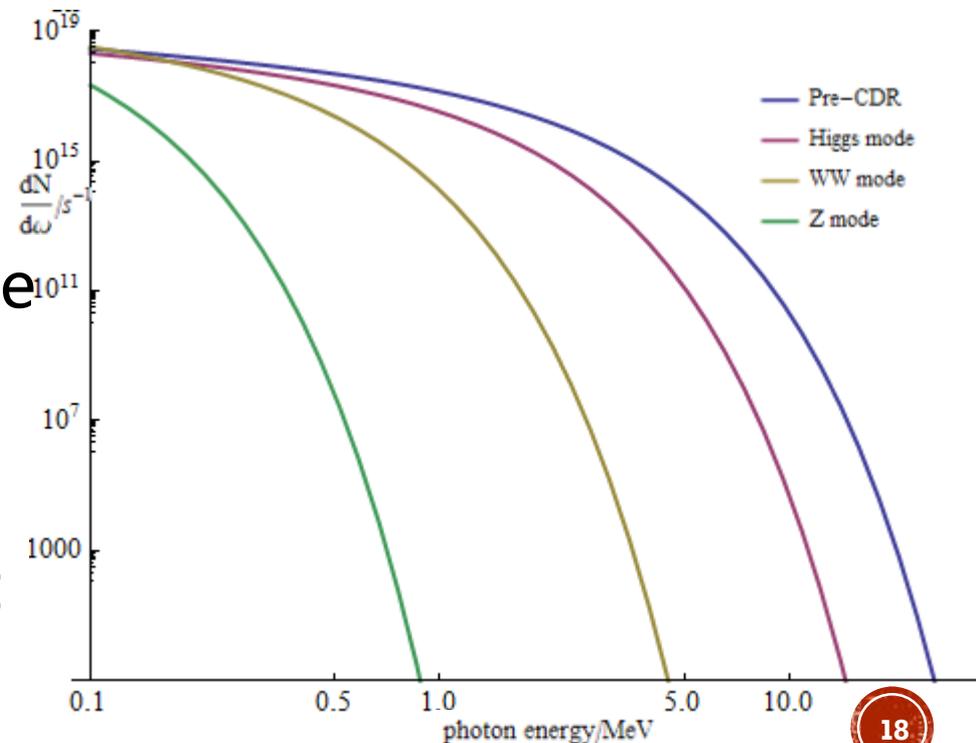
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SIGNAL-NOISE RATIO

- Compare between different energy region:

$\frac{dN}{d\omega}/s$		@3MeV	@10MeV	@20MeV	@40MeV
SR	Pre-CDR	10^{15}	10^{10}	2000	10^{-11}
	Double ring	10^{13}	10^4	10^{-7}	10^{-32}
CS		$10^6 \sim 10^7$ (integrated)			

- SR background of double ring is smaller than that of pre-CDR.
- Balance SN ratio against calibration.



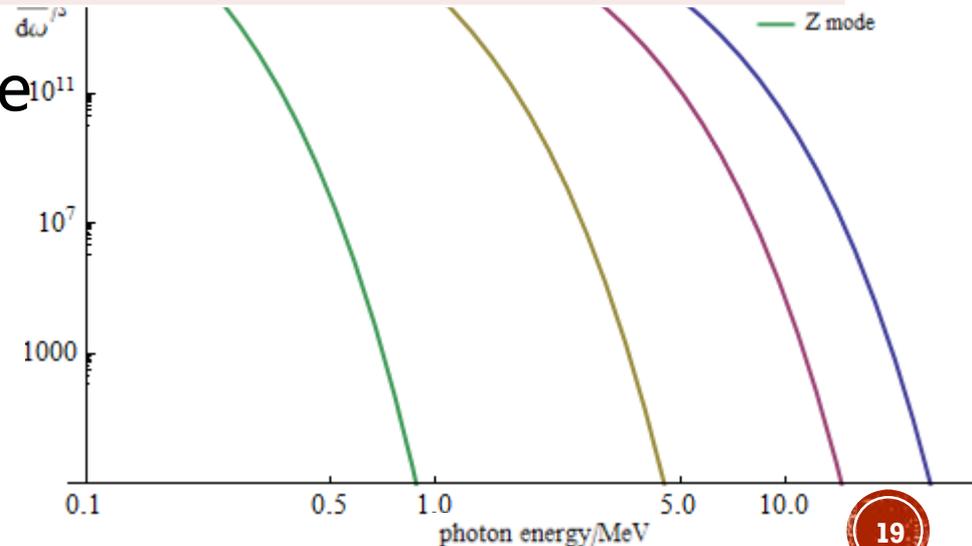
SIGNAL-NOISE RATIO

- Compare between different energy region:

$\frac{dN}{d\omega}/s$		@1MeV	@4MeV	@9MeV	@20MeV
SR	WW mode	10^{12}	10^{-2}	10^{-20}	10^{-54}
CS		$10^6 \sim 10^7$ (integrated)			

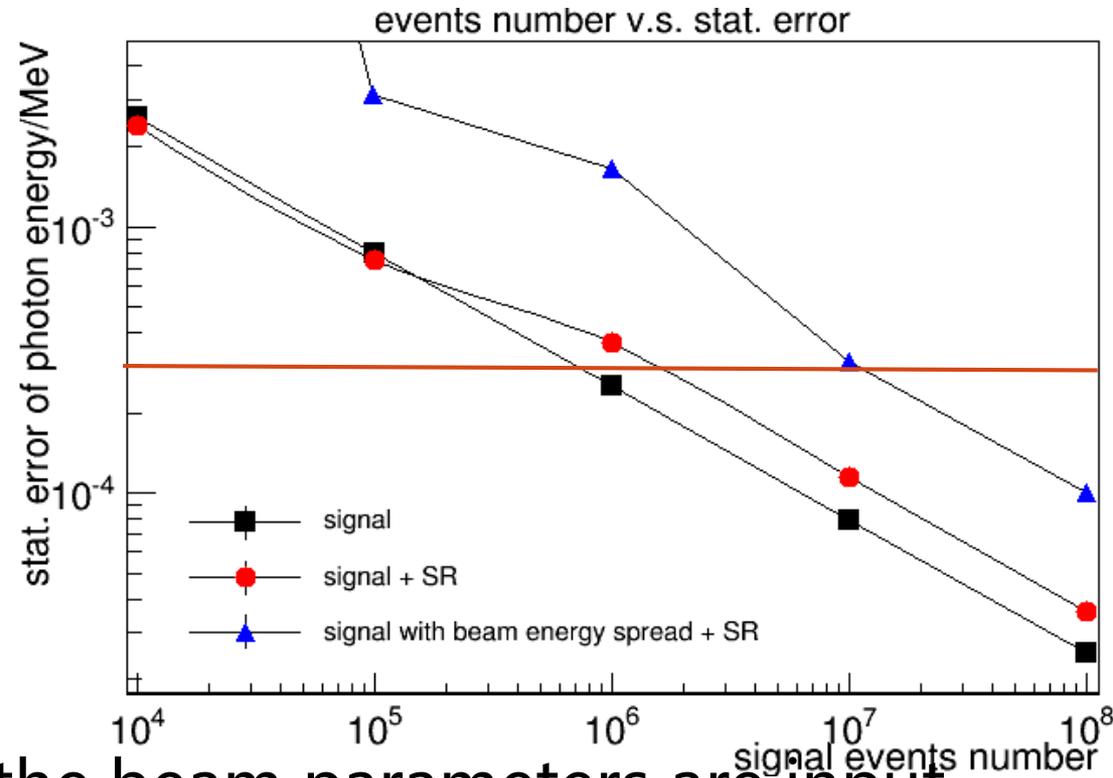
$\frac{dN}{d\omega}/s$		@0.4MeV	@1.4MeV	@2.8MeV	@5.7MeV
SR	Z mode	10^{10}	10^{-14}	10^{-46}	10^{-113}
CS		$10^6 \sim 10^7$ (integrated)			

- SR background of double ring is smaller than that of pre-CDR.
- Balance SN ratio against calibration.



STATISTICAL ERROR

- The **more** statistics are, the **smaller** the statistical error is.
 - Efficiency
 - Laser power
 - Time
- Depends on the **details** of fits.
- The **more precisely** the beam parameters are input, the **better fit** we obtain.
 - Energy spread, orbit, emittance...



SUMMARY & OUTLOOK

- We **can measure** beam energy precisely (error~1MeV, or even smaller),

if uncertainty of crossing angle α can be handled.

- beam orbit is under control?
- variance of beam momentum is clearly known?
- laser alignment is well?

if we can calibrate germanium detector.

- suitable isotopes? (10 ~ 40MeV)
- detector damage by (SR) radiation?

if statistical error is small enough.

- detector efficiency?
- fit scheme?
- laser power?

SUMMARY & OUTLOOK

- We **can measure** beam energy precisely (error~1 MeV, or even smaller),

if uncertainty of crossing angle α can be handled.

- beam orbit 
- beam momentum  discuss with accelerator experts to **understand beam property**.
- laser alignment  optics system with long light path.

if we can calibrate detector.

- isotopes  neutron capture or proton resonance reactions
- detector damage by (SR) radiation? 

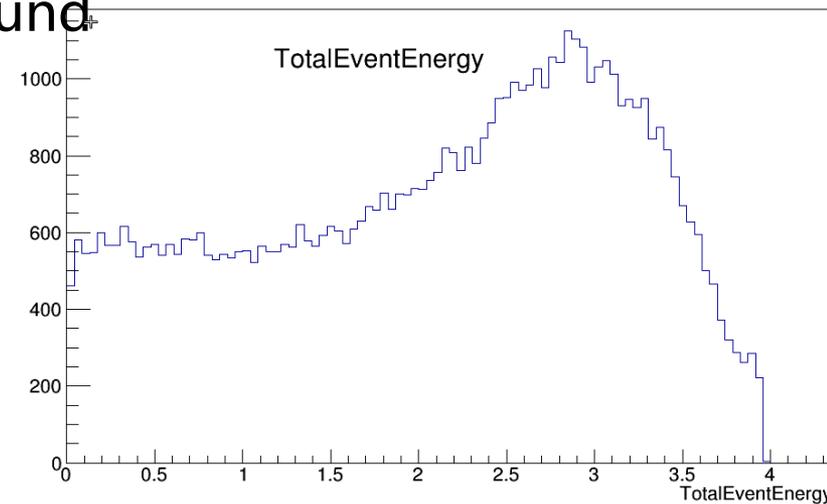
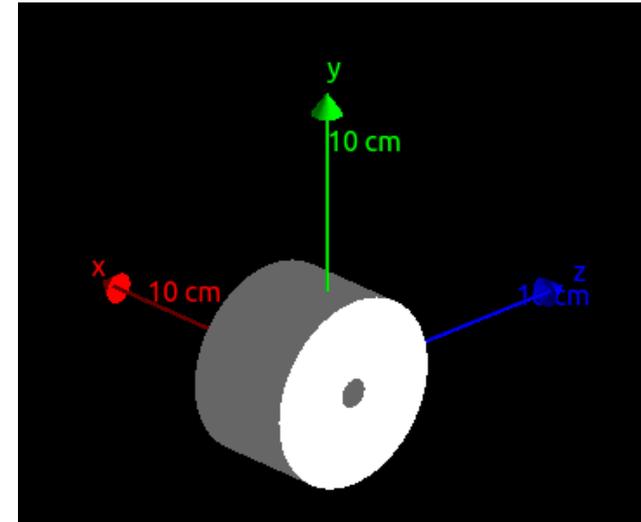
if statistical error is small enough.

- detector efficiency? 
- fit scheme?
- laser power  pulse laser or multiple reflection

study on detector and simulation.

SUMMARY & OUTLOOK

- We have been working on **full simulation** of BEM system based on Geant4: (by Guangyi Tang, Prof. Wang, Prof. Lou, ...)
 - Beam effects;
 - Detector performance and optimization;
 - SR (and other radiative background if exists);
 - Calibration;
 - Fit scheme.
 - ...



Thank you!